



1	A Fortran-Python Interface for Integrating Machine Learning Parameterization into
2	Earth System Models
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16 Abstract

18	Parameterizations in Earth System Models (ESMs) are subject to biases and uncertainties arising from
19	subjective empirical assumptions and incomplete understanding of the underlying physical processes.
20	Recently, the growing representational capability of machine learning (ML) in solving complex problems
21	has spawned immense interests in climate science applications. Specifically, ML-based parameterizations
22	have been developed to represent convection, radiation and microphysics processes in ESMs by learning
23	from observations or high-resolution simulations, which have the potential to improve the accuracies and
24	alleviate the uncertainties. Previous works have developed some surrogate models for these processes
25	using ML. These surrogate models need to be coupled with the dynamical core of ESMs to investigate
26	the effectiveness and their performance in a coupled system. In this study, we present a novel Fortran-
27	Python interface designed to seamlessly integrate ML parameterizations into ESMs. This interface
28	showcases high versatility by supporting popular ML frameworks like PyTorch, TensorFlow, and Scikit-
29	learn. We demonstrate the interface's modularity and reusability through two cases: a ML trigger function
30	for convection parameterization and a ML wildfire model. We conduct a comprehensive evaluation of
31	memory usage and computational overhead resulting from the integration of Python codes into the





- 32 Fortran ESMs. By leveraging this flexible interface, ML parameterizations can be effectively developed,
- 33 tested, and integrated into ESMs.
- 34

35 Plain Language

- 36 Earth System Models (ESMs) are crucial for understanding and predicting climate change. However, they
- 37 struggle to accurately simulate the climate due to uncertainties associated with parameterizing sub-grid
- 38 physics. Although higher-resolution models can reduce some uncertainties, they require significant
- 39 computational resources. Machine learning (ML) algorithms offer a solution by learning the important
- 40 relationships and features from high-resolution models. These ML algorithms can then be used to develop
- 41 parameterizations for coarser-resolution models, reducing computational and memory costs. To
- 42 incorporate ML parameterizations into ESMs, we develop a Fortran-Python interface that allows for
- 43 calling Python functions within Fortran-based ESMs. Through two case studies, this interface
- 44 demonstrates its feasibility, modularity and effectiveness.

45 1. Introduction

- 46 Earth System Models (ESMs) play a crucial role in understanding the mechanism of the climate system
- 47 and projecting future changes. However, uncertainties arising from parameterizations of sub-grid
- 48 processes pose challenges to the reliability of model simulations (Hourdin et al., 2017). Kilometer-scale
- 49 high-resolution models (Schär et al., 2020) can potentially mitigate the uncertainties by directly resolving
- 50 some key subgrid-scale processes that need to be parameterized in conventional low-resolution ESMs.
- 51 Another promising method, superparameterization a type of multi-model framework (MMF) (D.
- 52 Randall et al., 2003; D. A. Randall, 2013), explicitly resolves sub-grid processes by embedding high-
- 53 resolution cloud-resolved models within the grid of low-resolution models. Consequently, both high-
- 54 resolution models and superparameterization approaches have shown promise in improving the
- 55 representation of cloud formation and precipitation. However, their implementation is challenged by
- 56 exceedingly high computational costs.
- 57
- 58 In recent years, machine learning (ML) techniques have emerged as a promising approach to
- 59 improve parameterizations in ESMs. They are capable of learning complex patterns and
- 60 relationships directly from observational data or high-resolution simulations, enabling the
- 61 capture of nonlinearities and intricate interactions that may be challenging to represent with





62	traditional parameterizations. For example, Zhang et al. (2021) proposed a ML trigger function
63	for a deep convection parameterization by learning from field observations, demonstrating its
64	superior accuracy compared to traditional CAPE-based trigger functions. Chen et al. (2023)
65	developed a neural network-based cloud fraction parameterization, better predicting both spatial
66	distribution and vertical structure of cloud fraction when compared to the traditional Xu-Randall
67	scheme (Xu & Randall, 1996). Krasnopolsky et al. (2013) prototyped a system using a neural
68	network to learn the convective temperature and moisture tendencies from cloud-resolving
69	model (CRM) simulations. These tendencies refer to the rates of change of various atmospheric
70	variables over one time step, diagnosed from particular parameterization schemes. These studies
71	lay the groundwork for integrating ML-based parameterization into ESMs.
72	
73	However, the aforementioned studies primarily focus on offline ML of parameterizations that do
74	not directly interact with ESMs. Recently, there have been efforts to implement ML
75	parameterizations that can be directly coupled with ESMs. Several studies have developed ML
76	parameterizations in ESMs by hard coding custom neural network modules, such as O'Gorman
77	& Dwyer (2018), Rasp et al. (2018), Han et al. (2020) and Gettelman et al. (2021). They
78	incorporated a Fortran-based ML inference module to allow the loading of the pre-trained ML
79	weights to reconstruct the ML algorithm in ESMs. The hard-coding has limitations. Kochkov et
80	al. (2023) presented an innovative ML parameterization that feeds back from the dynamics, in
81	order to improve stability and reduce bias. However, such hard-coding approach restricts the ML
82	algorithm's ability to adapt to changes in the model dynamics over time, as the 'online' updating
83	requires a two-way coupling between the dominantly Fortran-based ESMs and Python ML
84	libraries.
85	
86	Fortran-Keras Bridge (FKB; Ott et al. (2020)) and C Foreign Function Interface (CFFI;
87	https://cffi.readthedocs.io) are two packages that support two-way coupling between Fortran-based ESM
88	and Python based ML parameterizations. FKB enables tight integration of Keras deep learning models but
89	is specifically bound to the Keras library, limiting its compatibility with other frameworks like PyTorch
90	and Scikit-Learn. On the other hand, CFFI provides a more flexible solution that in principle supports

- 91 coupling various ML packages due to its language-agnostic design. Brenowitz & Bretherton (2018)
- 92 utilized it to enable the calling of Python ML algorithms within ESMs. However, the CFFI has several
- 93 limitations. When utilizing CFFI to interface Fortran and Python, it uses global data structures to pass





94	variables between the two languages. This approach results in additional memory overhead as variable
95	values need to be copied between languages, instead of being passed by reference. Additionally, CFFI
96	lacks automatic garbage collection for the unused memory within these data structures and copies.
97	Consequently, the memory usage of the program gradually increases over its lifetime. In addition, when
98	using CFFI to call Python functions from a Fortran program, the process involves several steps such as
99	registering variables into a global data structure, calling the Python function, and retrieving the calculated
100	result. These multiple steps can introduce computational overhead due to the additional operations
101	required.
102	
103	Additionally, Wang et al. (2022) developed a coupler to facilitate two-way communication between ML
104	parameterizations and host ESMs. The coupler gathers state variables from the ESM using the Message
105	Passing Interface (MPI) and transfers them to a Python-based ML module. It then receives the output
106	from the Python code and returns them to the ESM. While this approach effectively bridges Fortran and
107	Python, its use of file-based data passing to exchange information between modules carries some
108	performance overhead relative to tighter coupling techniques. Optimizing the data transfer, such as via
109	shared memory, remains an area for improvement to fully leverage this coupler's ability to integrate
110	online-adaptive ML parameterizations within large-scale ESM simulations, which is the main goal for this
111	study.
112	
113	In this study, we investigate the integration of ML parameterizations into Fortran-based ESM
114	models by establishing a flexible interface that enables the invocation of ML algorithms in
115	Python from Fortran. This integration offers access to a diverse range of ML frameworks,
116	including PyTorch, TensorFlow, and Scikit-learn, which can effectively be utilized for
117	parameterizing intricate atmospheric and other climate system processes. The coupling of the
118	Fortran model and the Python ML code needs to be performed for thousands of model columns
119	and over thousands of timesteps for a typical model simulation. Therefore, it is crucial for the
120	coupling interface to be both robust and efficient. We showcase the feasibility and benefits of
121	this approach through case studies that involve the parameterization of deep convection and
122	wildfire processes in ESMs. The two cases demonstrate the robustness and efficiency of the
123	coupling interface. The focus of this paper is on documenting the coupling between the Fortran
124	ESM and the ML algorithms and systematically evaluating the computational efficiency and
125	memory usage of different ML frameworks (such as Pytorch and TensorFlow), different ML
126	algorithms, and different configuration of a climate model. The assessment of the scientific





- 127 performance of the ML emulators will be addressed in follow-on papers. The showcase examples
- emphasize the potential for high modularity and reusability by separating the ML components
- 129 into Python modules. This modular design facilitates independent development and testing of
- 130 ML-based parameterizations by researchers. It enables easier code maintenance, updates, and the
- adoption of state-of-the-art ML techniques without disrupting the existing Fortran infrastructure.
- 132 Ultimately, this advancement will contribute to enhanced predictions and a deeper
- 133 comprehension of the evolving climate of our planet.
- 134
- 135 The rest of this manuscript is organized as follows: Section 2 presents the detailed interface that
- 136 integrates ML into Fortran-based ESM models. Section 3 discusses the performance of the
- 137 interface and presents its application in two case studies. Finally, Section 4 provides a summary
- 138 of the findings and a discussion of their implications.

139 2. General design of the ML interface

140 2.1 Architecture of the ML interface

- 141 We developed an interface using shared memory to enable two-way coupling between Fortran and Python
- 142 (Figure 1). The ESM used in the demonstration in Figure 1 is the U.S. Department of Energy (DOE)
- 143 Energy Exascale Earth System Model (E3SM; Golaz et al., 2019, 2022). Because Fortran cannot directly
- 144 call Python, we utilized C as an intermediary since Fortran can call C functions. This approach leverages
- 145 C as a data hub to exchange information without requiring a framework-specific binding like KFB. As a
- 146 result, our interface supports invoking any Python-based ML package such as PyTorch, TensorFlow, and
- 147 scikit-learn from Fortran. While C can access Python scalar values through the built-in
- 148 PyObject_CallObject function from the Python C API, we employed Cython for its ability to transfer
- 149 array data between the languages. Using Cython, multidimensional data structures can be efficiently
- 150 passed between Fortran and Python modules via C, allowing for flexible training of ML algorithms within
- 151 ESMs.









Figure 1. The interface of the ML bridge for two-way communication via memory between Fortran ESM

and Python ML module. The diagram for the ESMs uses E3SM as an illustration. Note that MALI and

155 GCAM are yet active components of officially released E3SM.

156 2.2 Code structure

157 Figure 2 illustrates the structure of the ML bridge interface as applied to E3SM. The interface consists of 158 four main components: the Fortran ESM, Fortran Interface, C Bridge, and Python ML. The ML functions 159 are invoked within the original Fortran ESM parameterization components, such as the atmospheric 160 convection and microphysics modules. This process involves transferring the required input variables to 161 Python and defining the expected output variables to be returned to the Fortran component. The Fortran 162 Interface and C Bridge play a crucial role in establishing the interface between Fortran and Python. They 163 facilitate the transfer of variables between Fortran and Python by utilizing memory references. The ML 164 function called within the Fortran ESM is defined in the Fortran interface, which is then bound to a 165 corresponding C function. This seamless integration enables efficient communication and data exchange 166 between the Fortran and Python components. The Python ML component is responsible for handling ML-167 related tasks, such as loading the trained ML algorithm and using it to make predictions. Cython is used 168 to simplify the usage and facilitate the transfer and return of arrays. It allows for efficient integration of 169 Python code with C libraries, enhancing performance and enabling seamless array operations within the 170 ML component. 171

- 172 The interface consists of two stages. The first stage involves initializing the ML environment, which
- 173 persists throughout the model simulations. On the Fortran ESM side, the init_ml() function is called in the
- 174 atm_init_mct module. Through the Fortran Interface and C Bridge, the corresponding function in the





- 175 Python ML component is invoked. This function loads the ML-related global data and the trained ML 176 algorithm. This initialization process is performed only once to enhance efficiency and avoid unnecessary 177 repetition during the simulations. The second stage involves the actual invocation of the ML process. The 178 example here is an ML-based closure for the deep convection parameterization. We aim to utilize ML to 179 calculate Convective Available Potential Energy (CAPE) by utilizing an ML emulator based on high-180 resolution cloud-resolving model simulations. We call the cape ml function in the Fortran module 181 zm conv, providing temperature, pressure, and humidity as input variables, and defining the returned 182 CAPE from the ML side. Through the Fortran Interface and C Bridge, these three variables are passed to 183 the Python ML component. In the Python ML component, the received variables, along with other pre-184 loaded global data and the trained ML algorithm, are used to calculate the ML-based CAPE. The 185 calculated result is then returned to the Fortran ESM. The Fortran ESM utilizes this ML-derived CAPE to 186 determine how convection will evolve. 187
- 188



- Figure 2. The code structure of the ML bridge interface using the ML closure in deep convection as anexample.
- 192
- 193 In traditional ESMs, sub-grid scale parameterization routines such as convection parameterizations are 194 often calculated separately for each vertical column of the model domain. Meanwhile, the domain is typically decomposed horizontally into 2D chunks that can be solved in parallel using MPI processes. 195 196 Each CPU core/MPI process is assigned a number of chunks of model columns to update asynchronously 197 (Figure 3). Our interface takes advantage of this existing parallel decomposition by designing the ML 198 calls to operate over all columns simultaneously within each chunk, rather than invoking the ML scheme 199 individually for each column. This allows the coupled model-ML system to leverage parallelism in the 200 neural network computations. If the ML were called separately for every column, parallel efficiencies





- 201 would not be realized. By aggregating inputs over the chunk-scale prior to interfacing with Python,
- 202 performance is improved through better utilization of multi-core and GPU-based ML capabilities during
- 203 parameterization calculations. The Python, C, Cython and Fortran code components are compiled
- 204 together into a unified executable file. Table 1 shows the detailed steps to enable the ML bridge interface
- 205 in E3SM.
- 206



207

Figure 3. Data and system structure. The model domain is decomposed into chunks of columns. pver
 refers to number of pressure vertical levels. A chunk contains multiple columns (up to pcol). Multiple

210 chunks can be assigned to each CPU core.

211

212

Table 1. The steps to enable the ML bridge framework in E3SM

Step	Description
1.	Create the Python environment using Conda
	• conda create ML4ESM
	conda activate ML4ESM
2.	Add the Python ML environment in the compile CMake file
3.	Incorporate the ML bridge framework codes (including the Fortran Interface and C
	Bridge) into the ESM codebase.





4.	Initialize of ML environment by loading necessary global data and the pre-trained ML algorithm.
5.	Implement the ML prediction and the transmission of the resulting values to the ESM parameterization module.
6.	Cythonize the Python code
7.	Build and compile the ESM
8.	Submit the job for model simulation

213

214 3. Results

215 The framework explained in the previous section provides seamless support for various ML 216 parameterizations and various ML frameworks, such as PyTorch, Tensorflow, and Scikit-learn. To 217 demonstrate the versatility of this framework, we applied it two distinct case applications. The first 218 application replaces the conventional CAPE-based trigger function in deep convection parameterization 219 with a machine-learnt trigger function. The second application involves a ML-based wildfire model that interacts bidirectionally with the ESM. We provide a brief introduction to these two cases. Detailed 220 221 descriptions and evaluations will be presented in separate papers. 222 223 The framework's performance is influenced by two primary factors: increasing memory usage and 224 increasing computational overhead. Firstly, maintaining the Python environment fully persistent in 225 memory throughout model simulations can impact memory usage, especially for large ML algorithms. 226 This elevated memory footprint increases the risk of leaks or crashes as simulations progress. Secondly, 227 executing ML components within the Python interpreter inevitably introduces some overhead compared 228 to the original ESMs. The increased memory requirements and decreased computational efficiency 229 associated with these considerations can impact the framework's usability, flexibility, and scalability for 230 different applications.





- 232 To comprehensively assess performance, we conducted a systematic evaluation of various ML
- frameworks, ML algorithms, and physical models. This evaluation is built upon the foundations
- established for evaluating the ML trigger function in the deep convection parameterization.
- 235 3.1 Application cases
- 236 3.1.1 ML trigger function in deep convection parameterization

237 Convection plays a vital role in atmospheric processes, such as precipitation formation, heat and moisture 238 transport, and energy redistribution (Arakawa, 2004; Arakawa & Schubert, 1974). However, the 239 deficiencies in convection parameterizations constitute one of the principal sources of uncertainties in 240 General Circulation Models (D. A. Randall, 2013). Some uncertainties in convection parameterizations 241 are recognized to be closely linked to the convection trigger function used in these schemes (Bechtold et 242 al., 2004; Xie et al., 2004, 2019; Xie & Zhang, 2000; Lee et al., 2007). The convective trigger in a 243 convective parameterization determines when and where model convection should be triggered as the 244 simulation advances. In many convection parameterizations, the trigger function consists of a simple, 245 arbitrary threshold for a physical quantity, such as convective available potential energy (CAPE). 246 Figure 4a illustrates how the CAPE-based trigger function works. Convection will be triggered if the 247 CAPE value exceeds a threshold value, such as 70 J/kg used in E3SM version 1. 248 249 In this work, we develop a ML trigger function and apply it to E3SM (Golaz et al., 2019, 2022). A brief 250 overview of this ML trigger function is given here, while further details will be elaborated upon in a 251 subsequent paper. The training data originates from simulations performed using the Met Office Unified 252 Model Regional Atmosphere 1.0 configuration (Bush et al., 2020). Each simulation consists of a limited 253 area model (LAM) nested within a global forecast model providing boundary conditions (Walters et al., 254 2017; Webster et al., 2008). In total 80 LAM simulations were run located so as to sample different 255 geographical regions worldwide. Each LAM was run for 1 month, with 2-hourly output, using a grid-256 length of 1.5 km, a 512 x 512 domain, and a model physics package used for operational weather 257 forecasting. This physics package does not include a convective parameterization scheme, but does 258 include a representation of fractional cloudiness (Bush et al., 2020). The 1.5 km data is coarse-grained to 259 several scales from 15 to 144 km, comparable to the scale a global model might be run at. At each scale, 260 we assess whether individual pixels can be considered to be buoyant cloudy updrafts (BCU, e.g. 261 Hartmann et al., 2019; Swann, 2001). Here, the threshold for buoyant is local virtual temperature more 262 than 0.1 K warmer than the average at that scale and height. Cloudy is defined whenever the fractional 263 cloud cover is greater than 0.0 and updraft is defined as vertical ascent larger than 0.2 m/s. In each





- averaging region, the number of grid points that meet all three criteria are counted and saved as a profileof BCU fraction.
- 266
- 267 A two-stream neural network architecture is used for the ML model. The first stream takes profiles of
- temperature, specific humidity and pressure as inputs and passes them through a 4-layer convolutional
- 269 neural network (CNN) with kernel sizes of 3, to extract large scale features. The second stream takes
- 270 mean orographic height, standard deviation of orographic height, land fraction and the size of the grid-
- box as inputs. The outputs of the two streams are then combined and fed into a 2-layer fully connected
- 272 network to allow the ML model to leverage both atmospheric and surface features when making its
- 273 predictions. The output pf the ML model is a profile of BCU.
- 274
- 275 Once trained, the CNN is coupled to E3SM and thermodynamic information from E3SM is passed to it to
- predict the profile of BCU. If there are 3 contiguous levels where the predicted BCU is larger than 0.05,
- the convection scheme is triggered.
- 278



- 279
- 280 Figure 4. Structure of traditional CAPE-based and the new ML BCU-based trigger function. The
- 281 rectangles in LAM represent the LAM domains.
- 282
- 283 The ML trigger function is implemented using this two-stream architecture and coupled with the E3SM
- 284 model using the framework described in Section 2. Figure 5 shows the comparison of annual mean
- 285 precipitation between the control run using the CAPE-based trigger function and the run using the ML
- 286 BCU trigger function. The ML BCU scheme demonstrates reasonable spatial patterns of precipitation,
- similar to the control run, with comparable root-mean-square error and spatial correlation. Additional





- 288 experiments exploring the definition of BCU and varying the thresholds along with an in-depth analysis
- 289 will be presented in a follow-up paper.

290



291

292 Figure 5. Comparison of annual mean precipitation between the control run using the CAPE-based 293 trigger function (a, c) and the run using the ML BCU trigger function (b, d). 294

295 3.1.2 ML learning fire model

296 Wildfires in the United States have significantly increased in frequency and intensity in recent decades, 297 resulting in substantial direct and indirect losses (Iglesias et al., 2022). Predicting wildfire burned area is 298 challenging due to the complex interrelationships between fires, climate, weather, vegetation, topography, 299 and human activities (Huang et al., 2020). Traditionally, statistical methods like multiple linear regression 300 have been applied, but are limited in the number and diversity of predictors considered (Yue et al., 2013). 301 Alternatively, ML algorithms that capture statistical relationships between the burned area and environmental factors have shown promising burned area prediction (Kondylatos et al., 2022; Li et al., 302 303 2023; Wang et al., 2022, 2023). However, improving long-term burned area projections and evaluating 304 fire impacts requires the coupling of the fire model to an earth system model, which allows simulations of 305 the interactions between the fire, atmosphere, land cover and vegetation (Huang et al., 2021). To achieve 306 this, we develop a coupled fire-land-atmosphere framework using ML. 307 308

- The ML algorithm is trained using a monthly dataset, which includes the target variable of burned area, as
- 309 well as various predictor variables. These predictors encompass local meteorological data (e.g., surface
- 310 temperature, precipitation), land surface properties (e.g., monthly mean evapotranspiration and surface





- soil moisture), and socioeconomic variables (e.g., gross domestic product, population density), as
- described by Wang et al. (2022). In the coupled fire-land-atmosphere framework, meteorology variables
- and land surface properties are provided by the E3SM, as illustrated in Figure 6. We use the eXtreme
- 314 Gradient Boosting algorithm implemented in Scikit-Learn to train the ML fire model. Figure 7
- 315 demonstrates that the ML4Fire model exhibits superior performance in terms of spatial distribution
- 316 compared to process-based fire models, particularly in the Southern US region. Detailed analysis will be
- 317 presented in a separate paper. The ML4Fire model has proven to be a valuable tool for studying
- 318 vegetation-fire interactions, enabling seamless exploration of climate-fire feedbacks.



319

320 321

Figure 6. Structure of ML fire model (ML4Fire) coupled into E3SM model.



Figure 7. Comparison between ML4Fire model and process-based fire model against the historical
burned area from Global Fire Emissions Database 5 from 2001-2020. R and BIAS are the spatial
pattern correlation and difference against the observation, respectively.





326 3.2 Performance of different ML frameworks

- 327 The Fortran-Python bridge ML interface supports various ML frameworks, including PyTorch,
- 328 TensorFlow, and scikit-learn. These ML frameworks can be trained offline using kilometer-scale high-
- resolution models (such as the ML trigger function) or observations (ML fire model). Once trained, they

can be plugged into the ML bridge interface through different API interfaces specific to each framework.

- 331 The coupled ML algorithms are persistently resident in memory, just like the other ESM components.
- 332 During each step of the process, the performance of the full system is significantly affected by memory
- 333 usage. If memory consumption increases substantially, it may lead to memory leaks as the number of time
- 334 step iteration increases. In addition, Python, being an interpreted language, is typically considered to have
- 335 slower performance compared to compiled languages like C/C++ and Fortran. Therefore, incorporating
- 336 Python may decrease computational performance. We examine the memory usage and computational
- 337 performance across various ML frameworks based on implementing the ML trigger function in E3SM.
- 338 The ML algorithm is implemented as a two-stream CNN model using Pytorch and TensorFlow
- 339 frameworks, as well as XGBoost using the Scikit-learn package.



340

Figure 8. Computational and memory overhead as the simulation progresses for coupling the ML trigger
function with the E3SM model. The x-axis represents the simulated time step. The y-axis of (a) represents
the simulation speed measured in seconds per day (indicating the number of seconds required to simulate
one day). The y-axis of (b) represents the relative increase in memory usage for Scikit-learn, TensorFlow,
and PyTorch compared with CNTL. CNTL represents the original simulation without using the ML
framework.

348 Figure 8 illustrates the computational and memory overhead associated with the ML parameterization

- 349 using different ML frameworks. It shows that XGBoost only exhibits a 20% increase in the simulation
- time required for simulating one day due to its simpler algorithm. For more complex neural networks,





351	PyTorch incurs a 52% overhead, while TensorFlow's overhead is almost 100% – about two times as much
352	as the overhead by PyTorch. In terms of memory usage, we use the highwater memory metric (Gerber &
353	Wasserman, 2013), which represents the total memory footprint of a process. Scikit-learn and PyTorch do
354	not show any significant increase in memory usage. However, TensorFlow shows a considerable increase
355	up to 50MB per simulation day per MPI process element. This is significant because for a node with 48
356	cores, it would equate to an increase of around 2GB per simulated day on that node. This rapid memory
357	growth could quickly lead to a simulation crash due to insufficient memory during continuous
358	integrations, preventing the use in practical simulations. Our findings show that the TensorFlow
359	prediction function does not release memory after each call. Therefore, we recommend using PyTorch for
360	complex deep learning algorithms and Scikit-learn for simpler ML algorithms to avoid these potential
361	memory-related issues when using TensorFlow.
362	
363	Previous work, such as Brenowitz & Bretherton (2018, 2019) has utilized the CFFI package to establish
364	communication between Fortran ESM and ML Python. As described in the Introduction, while CFFI
365	offers flexibility in supporting various ML packages, it does have certain limitations. To pass variables
366	from Fortran to Python, the approach relies on global data structures to store all variables, including both
367	the input from Fortran to Python and the output returning to Fortran. Consequently, this package results in
368	additional memory copy operations and increasing overall memory usage. In contrast, our interface takes
369	a different approach by utilizing memory references to transfer data between Fortran and Python,
370	avoiding the need for global data structures and the associated overhead. This allows for a more efficient
371	data transfer process.
372	
373	In Figure 9, we present a comparison between the two frameworks by testing the different number of
374	elements passed from Fortran to Python. The evaluation is based on a demo example that focuses solely
375	on declaring arrays and transferring them from Fortran to Python, rather than a real E3SM simulation.
376	Figure 9a illustrates the impact of the number of passing elements on the overhead of the two interfaces.
377	As the number of elements exceeds 10 ⁴ , the overhead of CFFI becomes significant. When the number
378	surpasses 10 ⁶ , the overhead of CFFI is nearly ten times greater than that of our interface. Regarding
379	memory usage, our interface maintains a stable memory footprint of approximately 60MB. Even as the
380	number of elements increases, the memory usage only shows minimal growth. However, for CFFI, the
381	memory usage starts at 80MB, which is 33% higher than our interface. As the number of elements

- 382 reaches 10^6 , the memory overhead for CFFI dramatically rises to 180MB, twice as much as our interface.
- 383







Figure 9. Comparison of our framework and the CFFI framework in terms of computational timeand memory usage. The x-axis represents the number of elements transferred from Fortran to

387 Python, while the y-axis displays the total time (a) and total memory usage (b) for a

388 demonstration example. The evaluations presented are based on the average results obtained

389 from 5 separate tests.

390

384

391 3.3 Performance of ML algorithms of different complexities

392 ML parameterizations can be implemented using various deep learning algorithms with different levels of 393 complexity. The computational performance and memory usage can be influenced by the complexity of 394 these algorithms. In the case of the ML trigger function, a two-stream four-layer CNN structure is 395 employed. We compare this structure with other ML algorithms such as Artificial Neural Network (ANN) 396 and Residual Network (ResNet), whose structures are detailed in Table 2. These algorithms are 397 implemented in PyTorch. The algorithm's complexity is measured by the number of parameters, with the 398 CNN having approximately 60 times more parameters than ANN, and ResNet having roughly 1.5 times 399 more parameters than CNN.

- 400
- 401 Table 2. The structure and number of parameters of each ML algorithms.

Algorithms	Structure	# of parameters
ANN	3 x Linear	121,601
CNN	4 x Conv2d + 2 x Linear	7,466,753
ResNet	17 x Conv2d + 1 x Linear	11,177,025





402

403	Figure 10 presents a comparison of the memory and computational costs between the CNTL run without
404	deep learning parameterization and various deep learning algorithms. A same specific process-element
405	layout (placement of ESM component models on distributed CPU cores) is used for all the simulations.
406	Deep learning algorithms incur a significant yet affordable increase in memory overhead, with at least a
407	20% increase compared to the CNTL run (Figure 10a). This is primarily due to the integration of ML
408	algorithms into the ESM, which persist throughout the simulations. Although there is a notable increase in
409	complexity among the deep learning algorithms, their memory usage only shows a slight rise. This is
410	because the memory increment resulting from the ML parameters is relatively small. Specifically, ANN
411	requires 1MB of memory, CNN requires 60MB, and the ResNet algorithms requires 85MB, which are
412	calculated based on the number of parameters in each algorithm. When comparing these values to the
413	memory consumption of the CNTL run, which is approximately 3000MB, the additional parameters'
414	incremental memory consumption is not substantial.
415	

- 416 However, there is a significant decrease in computational performance as the complexity of the deep
- 417 learning algorithms increases (Figure 10b). This is primarily due to the larger number of parameters in
- 418 neural networks, which require more forward computations. It is worth noting that in this study, the deep
- 419 learning algorithms are executed on CPUs. To enhance computational performance, future work could
- 420 consider utilizing GPUs for acceleration.





- 423 CNTL is the default run without ML parameterizations.
- 424







425 3.4 Performance for physical models of different complexities



430

431 ML parameterization can be applied to various ESM configurations, for example, with the E3SM

432 Atmosphere Model (EAM), we experiment with Single Column Model (SCM), the ultra low-resolution

433 model of EAM (ne4), and the nominal low resolution model of EAM (ne30) configurations. The SCM

434 consists of one single atmosphere column of a global EAM (Bogenschutz et al., 2020; Gettelman et al.,

435 2019). ne4 has 384 columns, with each column representing the horizontal resolution of 7.5°. ne30 is the

default resolution for EAM and comprises 21,600 columns, with each column representing the horizontal
resolution of 1°. In the case of the ML trigger function, the memory overhead is approximately 500MB

resolution of 1°. In the case of the ML trigger function, the memory overhead is approximately 500MB
for all configurations due to the loading of the ML algorithm, which does not vary with the configuration
of the ESM.

439

440

441 Regarding computational performance, SCM utilizes 1 process, ne4 employs 1 node with 64 processes,

442 and ne30 utilizes 10 nodes with each node using 128 processes. In the case of SCM, the overhead

443 attributed to the ML parameterization is approximately 9% due to the utilization of only 1 process.

444 However, for ne4 and ne30, the overhead is 23% and 28% respectively (Figure 11). The increasing

445 computational overhead is primarily due to resource competition when multiple processes are used within

a single node.





448 4. Discussion and Conclusion

449	In this study, we develop a novel Fortran-Python interface for developing ML parameterizations. ML
450	algorithm can learn detailed information about cloud processes and atmospheric dynamics from
451	kilometer-scale models and observations and serves as an approximate surrogate for the kilometer-scale
452	model. Instead of explicitly simulating kilometer-scale processes, the ML algorithms can be designed to
453	capture the essential features and relationships between atmospheric variables by training on available
454	kilometer-scale data. The trained algorithms can then be used to develop parameterizations for use in
455	models at coarser resolutions, reducing the computational and memory costs. By using ML
456	parameterizations, scientists can effectively incorporate the insights gained from kilometer-scale models
457	for coarser-resolution simulations. Through learning the complex relationships and patterns present in the
458	high-resolution data, the ML-based parameterizations have the potentials to more accurately represent
459	cloud processes and atmospheric dynamics in the ESMs. This approach strikes a balance between
460	computational efficiency and capturing critical processes, enabling more realistic simulations and
461	predictions while minimizing computational resources. All these potential benefits in turn promote
462	innovative developments to facilitate increasing and more efficient use of ML parameterizations.
463	
464	In this study, we develop a novel Fortran-Python interface for developing ML parameterizations. This
465	interface demonstrates feasibility in supporting various ML frameworks, such as PyTorch, TensorFlow,
466	and Scikit-learn and enables the effective development of new ML-based parameterizations to explore
467	ML-based applications in ESMs. Through two cases - a ML trigger function in convection
468	parameterization and a ML wildfire model - we highlight high modularity and reusability of the
469	framework. We conduct a systematic evaluation of memory usage and computational overhead from the
470	integrated Python codes.
471	
472	Based on our performance evaluation, we observe that coupling ML algorithms using TensorFlow into
473	ESMs can lead to memory leaks. As a recommendation, we suggest using PyTorch for complex deep
474	learning algorithms and Scikit-learn for simple ML algorithms for the Fortran-Python ML interface.
475	
476	The memory overhead primarily arises from loading ML algorithms into ESMs. If the ML algorithms are
477	implemented using PyTorch or Scikit-learn, the memory usage will not increase significantly. The
478	computational overhead is influenced by the complexity of the neural network and the number of
479	processes running on a single node. As the complexity of the neural network increases, more parameters





- in the neural network require gradient computation. Similarly, when there are more processes running on
- a single node, the integrated Python codes introduces more resource competition.
- 482

483 Although this interface provides a flexible tool for ML parameterizations, it does not currently utilize

- 484 GPUs for ML algorithms. In Figure 3, it is shown that each chunk is assigned to a CPU core. However, to
- effectively leverage GPUs, it is necessary to gather the variables from multiple chunks and pass them to
- the GPUs. Additionally, if an ESM calls the Python ML module multiple times in each time step, the
- 487 computational overhead becomes significant. It is crucial to gather the variables and minimize the number
- 488 of calls. In the future, we will enhance the framework to support this mechanism, enabling GPU
- 489 utilization and overall performance improvement.

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- 499

500 Author contribution

- 501 TZ developed the Fortran-Python Interface. CM and JR contributed the ML model for the trigger
- $\label{eq:solution} 502 \qquad \text{function. YL contributed the ML model for the wire fire model. TZ and MZ assessed the performance of \\$
- 503 the ML trigger function. TZ took the lead in preparing the manuscript, with valuable edits from CM, MZ,
- WL, SX, YL, KW, and JR. All the co-authors provided valuable insights and comments for themanuscript.

506 Conflict of Interest

507 The authors declare that they have no conflict of interest.





509 Data Availability Statement

- 510 The Fortran-Python interface for developing ML parameterizations can be archived at
- 511 https://doi.org/10.5281/zenodo.11005103 (Zhang et al., 2024). The E3SM model can be accessed at
- 512 <u>https://doi.org/10.11578/E3SM/dc.20240301.3</u> (E3SM Project, 2024).

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