Mixed-Precision Computing in the GRIST Dynamical Core for Weather and Climate Modelling

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- 10 Abstract. Atmosphere modelling applications become increasingly memory-bound due to the inconsistent development rates between processor speeds and memory bandwidth. In this study, we mitigate memory bottlenecks and reduce the computational load of the GRIST dynamical core by adopting the mixed-precision computing strategy. Guided by a limiteddegree of iterative development principle, we identify the equation terms that are precision insensitive and modify them from double- to single-precision. The results show that most precision-sensitive terms are predominantly linked to pressure-
- 15 gradient and gravity terms, while most precision-insensitive terms are advective terms. The computational cost is reduced without compromising the solver accuracy. The runtime of the model's hydrostatic solver, non-hydrostatic solver, and tracer transport solver is reduced by 24%, 27%, and 44%, respectively. A series of idealized tests, real-world weather and climate modelling tests, has been performed to assess the optimized model performance qualitatively and quantitatively. In particular, in the high-resolution weather forecast simulation, the model sensitivity to the precision level is mainly dominated by the
- 20 small-scale features. While in long-term climate simulation, the precision-induced sensitivity can form at the large scale.

1 Introduction

Increasing model resolution is an effective approach of enhancing the atmosphere model forecast accuracy (Bauer et al. 2021; Benjamin et al.2019; Yu et al. 2019). Highly accurate, efficient, stable and scalable global dynamical cores have been widely pursued over the past two decades (e.g., Tomita and Satoh 2004; Harris and Lin 2012; Skamarock et al. 2012; Zängl et al. 2015; Wedi et al. 2020; Sergeev et al. 2023; Zhang et al. 2023). Doubling the horizontal resolution with a fixed vertical resolution leads to an increase of computational amount by a factor of ~2³, a significant challenge in terms of computational cost and energy consumption.

Operational weather and climate forecasting is a field where the dual demands of accuracy and computational efficiency converge, necessitating both quality and speed. In the context of high-resolution meso-scale forecasting, which operates on

- 30 scales of a few kilometers, computational efficiency itself implies forecast accuracy. Faster models enable more frequent forecast-assimilation cycles and the use of larger ensemble sizes within the constraints of finite computational resources. To tackle these computational hurdles, efforts have concentrated on enhancing the efficiency of numerical models. Progress such as Field Programmable Gate Arrays (FPGAs) and heterogeneous computing (e.g., Gan et al. 2013; Yang et al. 2016; Fu et al. 2017; Gu et al. 2022; Taylor et al. 2023), alongside compiler optimizations (e.g., Santos et al. 2024), have
- 35 demonstrated significant potential in accelerating earth system model.

Conventional weather/climate model development has typically relied on double-precision (64-bit) floating-point. The transition from double- to single-precision (32-bit) or even half-precision floating-point arithmetic presents an intriguing avenue for enhancing the computational efficiency (Düben et al. 2014). Single-precision computation unveils several compelling advantages, especially when confronted with the memory wall (Abdelfattah et al. 2021; Fornaciari et al. 2023;

- 40 Brogi et al. 2024). Beyond the alleviation of memory constraints, single-precision arithmetic promises three distinct benefits: accelerated arithmetic operations, improved cache hit rates, and reduced inter-node data communication (Baboulin et al. 2009; Düben and Palmer 2014; Düben et al. 2015; Váňa et al. 2016; Nakano et al. 2018). The benefits highlighted illustrate the capability of single-precision computation to boost computational efficiency in high-performance computing tasks, especially within the realm of large-scale weather and climate simulations where computational expenses are significant.
- 45 However, a wholesale migration from double- to single-precision computing may not always yield beneficial outcomes. This has led to the exploration of precision sensitive model component and/or physical scale in earth system modeling (e.g., Thornes et al. 2017; Nakano et al. 2018; Chantry et al. 2019; Maynard and Walters 2019; Cotronei and Slawig 2020). Singleprecision algorithms may struggle to converge or achieve the required precision when tackling intricate fluid dynamics simulations. In certain scenarios, single-precision computations can also result in floating-point under/overflow (Váňa et al.
- 50 2016; Cotronei et al. 2020). Additionally, physical parameterization schemes in the atmospheric models may amplify the grid-scale oscillations when executed in a pure single-precision mode (Váňa et al. 2016). Therefore, it becomes imperative to identify the specific algorithms within the modeling framework that are sensitive to the precision level.

Previous studies have made a notable progress. A pivotal study (Váňa et al. 2016) explored the reduction of almost all real-number variables in the Integrated Forecast System (IFS) of the European Center for Medium-Range Weather

- 55 Forecasting (ECMWF) from 64 bits to 32 bits. Results revealed that reducing precision did not significantly compromise the model accuracy, while it considerably reduced the computational burden by a factor of ~40%. Based on the dynamical core of the nonhydrostatic icosahedral model (NICAM), Nakano et al. (2018) witnessed an undesirable wavenumber-5 structure when completely using single-precision computing. This abnormal wave growth was traced back to the errors in the grid cell geometry calculations. By using double precision for only necessary parts in the dynamical core and single precision for all
- 60 other parts, the model successfully simulated the baroclinic wave growth, and achieved a ~46% reduction of runtime. Based on the Yin-He global spectral model, Yin et al. (2021) used a single-precision fast spherical harmonic transform (SHT) to conduct a 10-day global simulation and a 30-day retrospective forecasting experiment. Their simulations reproduced the

major precipitation events over southeastern China. The single-precision fast SHT may lead to a reduction of runtime by \sim 25.28% without significantly affecting the forecasting skill. Cotronei et al. (2020) converted the majority of the

- 65 computations within the radiation component of European Centre Hamburg Model (ECHAM) to single-precision, resulting in a 40% reduction in the runtime of the individual component. The obtained results were comparable to those achieved with double-precision. Banderier et al. (2023) indicated that employing single precision for regional climate simulations can significantly reduce computational costs (~30%) without significantly compromising the quality of model results.
- While these studies have demonstrated various ways for precision optimization, certain limitations remain. First, some studies focused on a complete transition to single-precision, potentially overlooking the precision-sensitive components and lacked a discussion of optimization strategies. Moreover, the applicability of mixed-precision in global climate simulations remains to be validated. Furthermore, because of the diversity of numerical models and algorithms, encompassing grid systems and solver techniques, these differences may lead to the model-specific precision sensitivity. Certain algorithms may remain amenable to single-precision computations, while others necessitate the use of double precision for stability and
- 75 accuracy. These gaps in the literature underscore the need for the present research to explore precision sensitivity, and to test the reduced-precision computing for both weather and climate simulations.

In this study, we explored the strategies of mixed-precision computing in the dynamical core of the Global-Regional Integrated Forecast System (GRIST; Zhang et al. 2019; Zhang et al. 2020). GRIST is a unified weather-climate model system designed for both research and operational modeling applications. Through a detailed implementation by modifying certain parts of the original (double-precision) dynamical core to support single-precision, a significant reduction of the computational burden has been achieved without sacrificing the solution accuracy, stability, and physical performance. This

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The remainder of this paper is organized as follows. Section 2 introduces the GRIST model, presents the mixedprecision optimization strategies, code modifications and highlighting the key equation terms sensitive to precision. Section 3 examines the computational performance of mixed-precision computing. Section 4 evaluates the physical performance of

has been validated based on a series numerical tests ranging from idealized to real-world flow.

mixed-precision computing in a series of test cases. <u>Discussion and conclusion are given in Sections 5 and 6, respectively.</u> 2.1. GRIST

The GRIST dynamical core employs layer-averaged governing equations based on the generalized hybrid sigma-mass vertical coordinate and a horizontal unstructured grid, allowing a switch between the hydrostatic and non-hydrostatic solvers (Zhang 2018; Zhang et al. 2019; Zhang et al. 2020). Prognostic variables are arranged in a hexagonal Arakawa-C grid approach. The hydrostatic solver is fully explicit, based on the Runge-Kutta integrator and the Mesinger forward-backward scheme. The nonhydrostatic solver employs a horizontally explicit vertically implicit approach. There is no time splitting in the integration of the dry dynamical core (dycore hereafter), while the tracer transport module is time-splitted from the dycore, and supports several transport schemes for various applications (Zhang et al. 2020). In this study, a third-order

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100 2.2 Mixed-precision optimization strategy

The purpose is to decrease the precision level (and thus computational cost) and maintain the accuracy and stability. Before implementing mixed-precision computing, we have checked that completely using single precision for the entire dynamical core leads to an unacceptable accuracy loss (see Section 4.1). However, considering the extensive codebase and its degree of complexity, comprehensively and randomly testing every component and variable is impractical. An iterative

105 development approach with a minimum degree of trial and error is used to identify the model components that are sensitive to the precision level. The dry baroclinic wave of Jablonowski and Williamson (2006) is used as a benchmark test during the iterative development cycle because this case has complex fluid dynamics characteristics and is very sensitive to numerical precision.

We established an acceptable error threshold, α , to assess whether the difference between outcomes from doubleprecision and mixed-precision simulations falls within a tolerable limit. Results from original double-precision computing serve as the true values. The iteration is: initially, a 10-day simulation was executed. We then embarked on a series of precision reduction tests for selected model variables, and we computed the error norm of <u>selected</u> diagnostic variables for each test. *E* is defined to represent the overall error level:

$$E = \max(L(\mathcal{H})) \tag{1}$$

$$L_{(x)} = \max(L_1(\mathcal{H}), L_2(\mathcal{H}), L_{\infty}(\mathcal{H}))$$
⁽²⁾

where L₁, L₂, and L_∞ represent the first, second and infinite norm of variable *H*. The definitions of L₁, L₂, and L_∞ can be found in the appendix. Should "error" *E* exceed α (0.05 for this study), the modification is deemed unacceptable and consequently abandoned; otherwise, the modification is accepted, allowing a further reduction in variable precision based on this new configuration. The precision optimization tests were conducted using the G8 grid. The grid names and their
120 corresponding resolutions can be found in Table 1. Initially, selected diagnostic variables (*H*) are ps (surface pressure) and vor_v(relative vorticity), because they can effectively quantify deviations in the mass field and velocity field. This criterion was set beforehand, while it has turned out that L(vor) overall has much larger error magnitude than L(ps). Thus, it is

L(vor) determines our optimization outcome,

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Technically, the switch between double-precision and single-precision code is defined through the FORTRAN KIND parameter, specified in a constant module. As single-precision results may not always replicate the double-precision results and can occasionally generate unacceptable errors (e.g., see Section 3.2), it is crucial to identify precision-sensitive variables and solver components. An additional parameter 'ns' has been introduced in this constant module for the precisioninsensitive variables. This modification facilitates the transition between double-precision, single-precision, and mixedprecision computations. Please note that only the subroutine of the solver is modified, indicating that the model initialization

130 section remains in double-precision operations. If the solver requires single-precision operands, double-precision variables

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Some important aspects are summarized as follows:

- 155 (i) Model variables insensitive to the precision level are set to the type parameter "ns". When "ns" is defined as single precision, the code executes mixed-precision computations; when defined as double precision, the code regresses double-precision computing and produces identical solutions as the original unmodified code;
 - (ii) Appropriately decompose computations involving implicit type conversions to reduce performance degradation due to precision conversion. For instance, 'a = b * c'. Here, 'a' is a single-precision floating point, 'b' a larger double-
- 160 precision float, and 'c' a single-precision float. The conversion of 'c' to double-precision can introduce extra rounding errors. These errors, amplified by 'b', may accumulate over time, adversely affecting model outcomes. Single-precision calculations provide a consistent error boundary, unlike mixed-precision which introduces uncertainty. In some cases, results might even be better if the computation of a function were entirely in single precision. Hence, optimization should proceed with caution, considering these error dynamics.
- 165 (iii) The Message Passing Interface (MPI) communication was modified for single-precision variables; The built-in functions such as 'HUGE' or 'TINY' are used to obtain very large or very small values respectively, to ensure the values fall within the precision range of the variables.

2.3 Mixed-precision optimization results

Following the strategy outlined in Section 2.2, the mixed-precision GRIST dynamical core is established. The optimization results, as depicted on the left side of Fig. 1, are summarized based on the continuous-form governing equations. The meaning of each variable in the equations exactly follows Zhang et al. (2020) so that we avoid repeating explanation. Model variables, with underlined text denote single-precision operands, variables in black represent double-precision operands. Black dashed boxes indicate that this part uses double-precision variables for computation, but the

tendency is saved as single precision, Gray shading indicates that this variable is diagnosed mostly from single-precision

175 variables. Specifically, $\zeta_p = \frac{\zeta_a}{\delta \pi}$ is highly sensitive to the precision of $\delta \pi$, requiring a double precision $\delta \pi$.

For the dycore, the precision sensitivity varies among different terms. The precision-sensitive terms are primarily related to pressure gradient and gravity terms. The precision-insensitive terms are mainly advective, which may tolerate lower numerical precision. Computationally, the advective parts of the equations are using higher-order operators which are responsible for the major computational burden. The passive tracer transport equation (Eq. 10) can be mostly computed

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using single precision. The only part needs a careful modification is the <u>black solid box</u>, which indicates that it uses singleprecision variables for computing, but the result is saved as double precision. $\delta \pi V$ (representing the mass flux) in Eq. (10) is accumulated and averaged from $\delta \pi V$ in Eq. (3), so computing it uses single precision. But when using it for tracer transport, this variable is converted to double precision so that the mass continuity equation of tracer transport uses a double-precision mass flux.

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The mass continuity equation Eq. (3) is solved using a flux form, ensuring global mass conservation of $\pi_s - \pi_t (\pi_t \text{ is a} \text{ constant})$ within the bounds of machine rounding errors, which is at the double-precision level. Using single precision $\delta \pi V$ implies that mass continuity is locally conserved at the single precision level. Recognizing the potential importance of local mass conservation (e.g., Thuburn 2008), a compilation switch is designed, so that approximating $\delta \pi V$ and the related mass continuity tendency can be achieved in either single-precision or double-precision. The time difference between

approximating the continuity equation using single-precision and double-precision accounts for ~1% -2% of the total

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computational time. We will examine the model sensitivity to this operation in Section 4.4.

2.4 Model code modification

Figure 1 illustrates the modification made to the original model code repository. Thanks to the modular structure of the-

- 210 model code, the mixed-precision version of the model dynamics can be seamlessly integrated as an add-on component, allowing for independent development. The switch between double-precision and mixed-precision dynamics is governed by the model's control unit, facilitating the transition between two code repositories via a compiler option ("MIXCODE"). Additional adjustments for each component include modifying parallel exchange functions to support reduced-precision variables, altering the precision level of allocated dynamics data, accommodating precision changes of specific variables in
- 215 physics-dynamics coupling, and introducing a precision control variable. All these supplementary modifications (excluding those in the infrastructure layer) are also designated by the compiler option "MIXCODE". The pure single-precision code is achieved by simply using single-precision for all variables, marked as "SPCODE" in the code,

3 Computational performance

Before showing the physical performance, we first examine the computational performance of the optimized dynamical core. All computing performance are carried out on a local supercomputing cluster. Each computing node is equipped with 128GB memory, and the Central Processing Unit (CPU) is a Hygon C86 7285 model at 2.0 GHz. Each CPU features a 32 KB L1 data cache, a 64 KB L1 instruction cache, a 512 KB L2 cache, and an 8192 KB L3 cache. We use "SGL" to denote pure single precision computing, "DBL" to denote pure double precision, and "MIX" to represent mixed precision computing. All experiments were conducted on a G8 grid, submitted with the same topology: 756 MPI tasks distributed across six nodes.

- 225 Compared to the double-precision model, the runtime of the mixed-precision model for the non-hydrostatic dry dynamical core (NDC), hydrostatic dry dynamical core (HDC) and tracer transport solver reduced by 27%, 24%, and 44% (Table 2). The runtime of the mixed-precision dycore solver is still larger compared to the single-precision dycore, indicating the time overhead incurred by the use of double-precision in precision-sensitive algorithms. The runtime of the mixed-precision tracer transport solver is comparable to that of the single-precision tracer transport solver, as most computations in
- 230 the tracer transport module now use single-precision computing. It should be noted that the time gains from mixed-precision computing may also depend on hardware and compiler options (e.g., Brogi et al. 2024). This is out of the scope of this study.

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4 Physical Performance

Due to the inherent complexity of atmosphere models, which have dycore, tracer transport, and model physics suites, directly assessing errors induced by precision in the real cases is not precise. To ensure robustness, a hierarchy of five test cases from simple to complex is adopted for model evaluation,

4.1 Moist baroclinic wave

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This case is from the DCMIP2016, as outlined by Ullrich et al. (2014), a modified approach to the dry baroclinic instability scenario (Jablonowski and Williamson 2006). This experimental setup triggers the emergence of an unstable baroclinic wave pattern, initiated by early perturbations, which exhibits exponential growth and attains its maximum intensity around the 11th day. The experiment incorporates a passive tracer representing water vapor, which is subject to passive advection. Although the mixing ratio marginally influences the pressure gradient force, as noted by Zhang et al.

(2020), the overall behaviour of wave growth is in substantial agreement with that in the dycore (Zhang et al. 2019). The primary objective is to assess the model's efficacy in replicating the typical dynamics of moist atmospheric conditions across various precision settings.

- 270 Figure 2 shows surface pressure and relative vorticity field at the model level near 850hPa (model layer 23) at day 11, as simulated by the G8 resolutions. The baroclinic waves shown the anticipated growth in the DBL simulation (Figs. 2a). In the SGL simulation, the primary growth fluctuations in the DBL simulation were reproduced (Figs. 2c). However, in the Northern Hemisphere, there were developments of incorrect spurious waves, whose intensity was comparable to the major fluctuations (Figs. 2c). The Southern Hemisphere exhibited a weaker structure of spurious waves (Figs. 2c). The results from the MIX simulation displayed patterns much closer to those in the DBL simulation (Figs. 2e).
 - The primary difference between MIX and DBL simulations lies in the vicinity of strong gradients along the cold front (Figs. <u>2c</u>). But the primary fluctuations in both MIX and DBL simulations exhibit a high degree of similarity in their patterns (Figs. <u>2a</u> and <u>2c</u>), indicating that precision levels have a tangible impact on the phase speed of wave propagation.
- The error introduced by SGL and MIX can be quantified by comparing solutions to a DBL solution. Following Jablonowski and Williamson (2006), l_2 error norms of the relativity vorticity field at model layer 23 are compared on the global grid as a function of time. Fig. 3 shows the l_2 norm for the SGL and MIX. In the initial stages of the model integration, the errors in the SGL simulations increased rapidly. By checking the original fields (figure not shown), it was found that numerous small-scale spurious fluctuations had emerged on both sides of the equator, the intensity of which was similar to the physically meaningful fluctuations.
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After day 6, the primary fluctuations of the baroclinic waves in the SGL simulations began to develop, resembling the behaviour of the DBL simulations, and the errors started to decrease (Fig. 3). By day 10, the fluctuations rapidly developed, the primary fluctuations grew robustly, and the spurious fluctuations produced in the early stages of the SGL simulations also rapidly developed, leading to an increase in errors (Fig. 3). On day 11, the intensity of the spurious fluctuations developed in SGL was close to that of the primary fluctuations, which is unacceptable. Due to the slow growth of the

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primary fluctuations in the early stages, the MIX simulation exhibited minimal errors before day 9 (Fig. 2). Subsequently, as the fluctuations matured rapidly, prominent differences in phase speed compared to the DBL emerged, leading to a rapid increase in errors.

4.2 Splitting supercell thunderstorms

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The splitting supercell test of DCMIP2016 (Klemp et al. 2015; Zarzycki et al. 2019) emphasizes the importance of scrutinizing non-hydrostatic model simulations of small-scale dynamics, especially as models approach spatial resolutions on the (sub) kilometre scale. This test utilized the small-planet testing framework (Wedi and Smolarkiewicz 2009), a cost-effective approach by scaling down Earth's radius by a factor of 120. The model employs the Kessler warm-rain microphysics scheme for simplified physics. This particular test case is characterized by unstable atmospheric conditions

- 315 conducive to moist convection, posing a challenge numerical accuracy and stability. Klemp et al. (2015) suggested that an increase in horizontal resolution should lead to convergent solutions. For GRIST, this behaviour has been verified by Zhang et al. (2020). Our investigation further examines the capability of the MIX configuration to accurately replicate the behaviours observed in the DBL simulations.
- Figure ∉ shows the q_r mixing ratio at 5 km elevation in both DBL and MIX simulations at four resolution choices (G4: <u>~4km</u>, G6: ~1km, G7: ~0.5km and G8: ~0.25km). The DBL and MIX solutions show bulk similarities across all the resolutions. At 7200s, a single updraft splits and evolves into a symmetric storm propagating towards the poles, with two supercells located ~30° from the equator. These supercells show subtle differences in their structure and intensity <u>At a low</u> resolution of 4 km, the differences between MIX and DBL simulations are minimal at all altitudes (Figs. 4b-c). As the resolution increases from 4 km to 1km and to 0.5 km, the structural differences in supercells gradually become more
- 325 pronounced (Figs. 4b-d, f-h, j-l). However, when the resolution further increases from 0.5 km to 0.25 km, the differences, diminish (Figs. 4n-p). For DBL simulation results, the differences between 0.5 km and 0.25 km are smaller than those between 1 km and 0.5 km, indicating that the solution converges almost at a resolution of 0.5km. At 0.25 km, the results of MIX simulation show greater similarity to those of DBL simulation at all altitudes (Figs. 4n-p). This indicates that, in mixed-precision simulation, supercells also achieve good convergence at this resolution, and thus the sensitivity to the precision

330 level diminishes from 0.5 km to 0.25 km

Figure 5 shows the maximum vertical speed and area-integrated rainfall rate over the global domain as a function of time for each resolution. The vertical speed in both MIX and DBL increases with resolution (Figs. 5a). From the start of the model integration until 5400s, the vertical speed curves of MIX and DBL simulations nearly overlap (Figs. 5a). After 5400s, a noticeable deviation appears, expect for the G4 grid. The difference in vertical speed between MIX and DBL is minimal at

335 <u>4</u> km resolution, followed by the 0.25 km resolution, while it is larger at 1 km and 0.5 km resolutions (Figs. 5a). The areaintegrated rainfall rate curves exhibit similar evolutionary features (Figs. 5b). At very low resolutions, such as 4 km, the differences between MIX and DBL simulations are not significant. At a higher resolution of 0.25 km, the overall behaviour of supercells in MIX simulations is closer to that of DBL compared to 0.5km and 1 km resolutions. Both MIX and DBL solutions demonstrate good convergence.

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(删除了: The differences in the structure of the supercells are larger at lower resolutions than at higher resolutions. In the MIX simulation at 1 km, an additional small-scale local maximum is present near the storm core on the north side of the Equator (Figs. 3d).
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	删除了: The MIX simulated rainfall intensity is slightly weaker than the DBL solutions in some configurations (Figs. 3b and 3e). As the resolution increases, the differences between MIX and DBL diminish (Figs. 3g, 3h and 3i)
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4.3 Idealized tropical cyclone

This idealized tropical cyclone scenario integrates a three-dimensional dynamical core with a simple physics suite (Reed and Jablonowski 2012), alongside an analytic vortex initialization technique (Reed and Jablonowski 2011). The experiment produces the evolution of a tropical cyclone from a nascent, idealized vortex, highlighting the model's sensitivity

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to various parameter adjustments. Notably, alterations in tracer transport schemes in GRIST can produce subtle sensitivities in the development of the tropical cyclone due to the pressure gradient terms (Zhang et al. 2020), thereby establishing this case useful for assessing model precision sensitivity.

Figure 6 displays the wind speed at day 10 for the DBL (Figs. 6a and 6b) and MIX (Figs. 6c and 6d) simulations at G8 resolution. Fig. 6 (left) shows the longitude-height cross sections of the magnitude of the wind through the centre latitude of the vortex. Fig. 6 (right) displays the horizontal cross sections of the magnitude of the wind at surface model layer. The centre of vortex is defined as the grid point with the minimum surface pressure. At the day 10, the developed storm resembled a tropical cyclone. The overall behaviour in the MIX simulation was similar to that in the DBL simulation, with maximum winds near the surface and a distinct eyewall structure (Fig. 6). However, there was some differences in the vertical structure and centre location of the cyclone (Figs. 6a and 6c). In the MIX simulation, the generated cyclone was stronger, with higher wind speeds near the surface (Fig. 6c). The eyewall of the cyclone in the MIX simulation appeared less pronounced compared to that in the DBL simulation, where the cyclone's eyewall is narrower and straighter (Fig. 6c). Overall the characteristics of the cyclone ware compareable between the MIX and DBL simulations.

Overall, the characteristics of the cyclone were comparable between the MIX and DBL simulations. In addition to two deterministic control simulations using both double-precision and mixed-precision with the nonhydrostatic solver, eight ensemble simulations with the double-precision non-hydrostatic solver are further performed. This assesses the MIX simulation within the uncertainty range of the DBL simulation. The uncertainty range is quantified by the ensemble simulations encompassing eight initial-value perturbation members. Random small-amplitude perturbations were applied to the initial wind speeds (e.g., Li et al. 2020), where perturbations to the normal velocity at cell edges were prescribed within a range of 2% of their values in the control experiment.

Figure 7 describes the tracks of tropical cyclones, along with the evolution of minimum surface pressure and maximum surface wind speed over time. The red and blue lines represent two deterministic simulations conducted using MIX and DBL solvers, respectively. The eight random perturbation simulations with DBL solver are represented by gray lines. Minimal spread is observed in the early stages of the simulations (Figs. 7). Cyclone track separation between MIX and DBL simulations occurs at the day 1 (Fig. 7a). Subsequently, spread in the simulations increases over time (Figs. 7). The evolution of minimum surface pressure and maximum surface wind speed over time exhibits similar trends (Figs. 7b and 7c). No discernible difference is found between the sensitivity introduced by the MIX and that introduced by perturbed initial values in the DBL simulations. The overall behaviour of the MIX simulation falls within the range of uncertainty of the DBL simulation.

4.4 Atmospheric Model Intercomparison Project (AMIP) simulation

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Following the establishment of the MIX dynamical core, a detailed examination of its integration with the model 420 physics suite (Li et al. 2023) becomes crucial. The nonlinear interactions between the model's dynamics and its physical processes can result in varied performances across weather and climate simulations. It's imperative to investigate these differences to ensure that MIX simulations can accurately mirror the outcomes of DBL simulations in practical applications.

In assessing a new formulation for real-world modelling, our guiding principle is to first run long-term AMIP simulations (Zhang et al. 2021). This ensures that the model can achieve statistical equilibrium, maintain a realistic model

425 climate, and has good integral properties such as conservation and balanced budgets (e.g., Fu et al. 2024). Subsequently, the same model, with minimal application-specific modifications, undergoes shorter-range but higher-resolution, kilometre-scale tests (Zhang et al. 2022).

The AMIP experiment is conducted in alignment with Zhang et al. (2021). This involved running both global hydrostatic and non-hydrostatic models with the weather physics suite at a G6 over a decade, spanning from 2001 to 2010. 430 The simulations were performed under conditions with prescribed climatological sea surface temperatures and sea ice concentrations. The focus was narrowed to precipitation, which is a comprehensive metric due to its sensitivity to both model dynamics and physics, effectively reflecting the non-linear interactions that are crucial for accurate weather and climate simulations (Zhang and Chen 2016).

Figure & shows the simulated climatological (2001-2010) precipitation field for June-July-August (JJA) and DecemberJanuary-February (DJF). Both the MIX hydrostatic and non-hydrostatic solvers are capable of replicating the JJA and DJF precipitation patterns in the DBL simulations. The discrepancies between MIX and DBL simulations are similar in both hydrostatic and non-hydrostatic simulations, with the primary differences occurring in the tropics. The precipitation differences shift from north to south along with the main rain bands as the season transition from summer to winter. The deviation in summer precipitation is greater than that in winter precipitation, because convective activities are most vigorous.
In the summer, the MIX simulation overestimates the precipitation in the tropical coastal regions of the Western Pacific, especially along the western coast (Figs. *§a* and *§b*). In winter, the main biases in the MIX simulation are concentrated in the

especially along the western coast (Figs. <u>8a</u> and <u>8b</u>). In winter, the main biases in the MIX simulation are concentrated Southern Ocean (Figs. <u>8c</u> and <u>8d</u>).

These results may have two implications. In MIX simulations, the cumulative effects of rounding errors might be progressively magnified over the course of long-term climate integrations. This phenomenon could lead to notable differences in the simulated large-scale atmospheric phenomena. This contrasts with high-resolution shorter-range weather modeling, where discrepancies primarily emerge at the small scales, as will be discussed in Section 4.5. This might imply that MIX may more diverge from their DBL counterparts over extended integration periods, necessitating a careful consideration of how rounding errors accumulate and their impact on the climate simulation performance.

Second, the differences induced by varying levels of precision can be further exacerbated by physical processes within 450 the climate system. A clear example is observed in the tropical regions during the boreal summer, where higher discrepancies are noted. This suggests that certain atmospheric conditions or regions, such as the tropics during periods of

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intense solar heating, may be more susceptible to the effects of precision-level differences. These conditions can amplify the inherent precision differences, leading to more pronounced variations.

In the MIX implementation, Eq. 3 implies that global mass is conserved at the double precision level. The local mass flux is only conserved at the single precision level, because the mass flux and its divergence are treated as single precision. As mentioned in Section 2.3, we have retained a capability to compute the terms related to the mass flux divergence equation also in the double precision. Local mass can be conserved at the double precision level as well. We then evaluated the longterm climate integration results based on the hydrostatic solver.

Figure <u>9</u> shows the differences of the climatological precipitation field between MIX with single- (MIX_SGL_mass)
and double-precision (MIX_DBL_mass) mass flux divergence against the pure DBL simulation. In the summer, the simulation differences between the MIX_SGL_mass and MIX_DBL_mass solver for the continuous equations is small (Figs. <u>9a</u> and <u>9b</u>). In the winter, the deviations in the MIX_SGL_mass is smaller than those in the MIX_DBL_mass solver (Figs. <u>9c</u> and <u>9d</u>). The deviations are most pronounced in the tropical convective precipitation over the Southern Ocean (Figs. <u>9c</u> and <u>9d</u>). The larger difference between MIX_DBL_mass and DBL is *likely* due to implicit type conversions, as discussed in
470 Section 2.2.

4.5 A global storm-resolving simulation

Under the constraints of today's computational resources, executing global storm-resolving nonhydrostatic simulations remains resource intensive (Satoh et al. 2017; Stevens et al. 2019). The use of MIX simulations presents a cost-effective solution to this challenge. However, it has been reported, for instance by Nakano et al. (2018), that as the resolution of the

475 model increases, the difference between MIX and DBL may increase, especially for the smaller-scale flow features. This observation prompts a closer investigation into the performance of nonhydrostatic models at high-resolution modelling.

A global storm-resolving experiment at 5 km (G9B3) is performed using the MIX nonhydrostatic model, following Zhang et al. (2022). The model was integrated from UTC00, 10th, to UTC00, 15th, July, 2015. We expect that the developed mixed-precision dynamical core can replicate the behaviour of DBL in kilometre-scale weather simulations.

- 480 Figure <u>10</u> show the period-accumulated precipitation (UTC00, 10th-UTC23, 15th, 2015) from the MIX and DBL model runs. All data have been interpolated to the 0.5° regular latitude-longitude grid. The precipitation pattern simulated by MIX are very close to those of DBL simulations. MIX obtains nearly the same general position, orientation, and intensification of the rain band (Figs. <u>10a</u>, <u>10b</u>). MIX and DBL also produced very comparable kinetic energy spectra (figure not shown).
- Like the AMIP simulations, the differences in precipitation are primarily located within the tropics, with the most pronounced differences in areas with vigorous convection. Close-ups of these locations reveal that it is small-scale (a few grid spacing) that is most sensitive to the precision level, because small scales are most sensitive to numerical discretization and dissipation (Jablonowski and Williamson 2011). Considering that global meso-scale forecast at a few kilometres would greately benefit from ensemble prediction (Palmer 2019), in practice, the MIX induced small-scale sensitivity may also fall within the uncertainty range of the ensemble, similar to that in Section 4.3.

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	As mentioned in Section 2.3, the advective parts of the equations are not sensitive to the precision level and they are	 删除
	using higher-order operators. To understand whether this optimization outcome is sensitive to the nominal order of numerics,	
	we utilized an isolated 3D tracer transport experiment (Kent et al. 2013, Hadley-like meridional circulation) and performed a	
	convergence test. This test case was also performed by Zhang et al. (2020) and Li and Zhang (2022), and thus their results	
505	can be used as reference. By adjusting the very small values introduced by the limiter to be within the single-precision range,	_
	this equation (Eq. 10 in Fig.1) is solved independently in single-precision ("SPCODE" compiler option in the model code),	 删除 teste
	We used various orders of horizontal flux operators, namely RK302, RK303, and RK304 (combinations of third	Inter (Ken
	order Runge-Kutta integration scheme, and nominal 2 nd - to 4 th order spatial flux operators). RK3O3 is used in other tests of	objec
	this paper. The vertical advection operator remains unchanged. The results are shown in Fig, 11. The tested resolutions and	intro
510	associated time step include G5L30 (600s), G6L60 (300s), G7L120 (150s), G8L240 (75s) and G9L480 (37.5s). The results	equa
	demonstrate that, using different orders of horizontal flux operators, the single-precision simulations are comparable to the	opera
	double-precision simulations across all resolutions, with nearly identical error norms and convergence rates	删除
	This outcome suggests that, within the current code implementation, the advective part of the model demonstrates	删除
	greater resilience when subjected to changes in precision, regardless of the nominal order of the operator. This supports the	删除
515	optimization results in the entire dynamical equations. As reported by Nakano et al. (2018) and Yin et al. (2020), the	(删除
	precision-sensitive components are related to the specific numerical algorithms. Meanwhile, badly conditioned code or poor	し 投置
	coding practice can also necessitate double-precision calculations (Váňa et al. 2016; Palmer 2020). For other components	双旦 删除
	(e.g., pressure gradient) that currently have higher sensitivity to the precision level, we believe that it may require more	2022
	careful code implementation to allow us to benefit more from reduced-precision computing	一删除

520 6,Summary and outlook

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In this study, we investigated mixed-precision computing within the GRIST dynamical core, identifying the equation terms particularly sensitive to numerical precision. We outlined an optimization procedure characterized by a limited extent of iterative development. Given the current development trajectory of high-performance computing, where advancements in memory bandwidth lag behind peak processor performance improvements, mixed-precision computation holds promise for enhancing weather and climate model development. The major conclusions are summarized as follows.

We discovered that terms sensitive to numerical precision primarily involve pressure gradient and gravity. In contrast, advective terms exhibit resilience to single precision and can be optimized. The advective terms are computationally more expensive than the pressure gradient and gravity terms. The viability of employing mixed-precision computing in the GRIST dynamical core has been validated across a spectrum of scenarios, from idealized flow to real-world AMIP and global storm-

530 resolving simulations. These MIX experiments yielded results remarkably similar to those from DBL simulations. For dycore, the runtime for hydrostatic and non-hydrostatic solvers was reduced by 24% and 27%, respectively. The tracer

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It is important to note that the current mixed-precision version, despite achieving significant computational efficiency gains, is not the final version. There are still some double-precision variables in the dynamical core that can be further reduced to single precision. This work serves as a starting point for exploring the application of low precision in the GRIST dynamical core, including future use of half precision and rewriting suboptimal code.⁴⁴

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transport solver witnessed a runtime reduction of 44%. The overall time savings depend on the proportion of dycore and tracer transport in the total computation time, varying by application.

We noted a higher sensitivity to precision in long-term climate simulations compared to short-term higher-resolution weather forecasts, particularly affecting the precipitation field over certain regions. In weather forecast, the difference between MIX and DBL are mainly for the small scales, while in AMIP simulations, the difference is found for the larger scales. These effects may primarily stem from the model sensitivity to the precision level or from biases introduced by mixed-precision computations themselves.

It also needs to recognize that while the mixed-precision GRIST dynamical core has been examined across multiple scenarios, more realistic tests and some fine tuning may still be needed to ensure robust operational forecasting. Some alternative advection schemes in the tracer transport module have not been implemented to single precision yet and this can be achieved in future. It is also possible that room remains for further optimization and time reduction, especially when considering modifying the original code implementation and using further reduced significant digits

Acknowledgments

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Code and Data availability

Model code and plotting data related to this manuscript is available at: https://zenodo.org/records/11229770.

Author contribution

SYC developed the mixed precision model code and prepared the initial draft. YZ designed and led this model development

595 research. YW contributed to experiments. All the authors discussed this work and contributed to the final manuscript version.

Competing interests

None.

Appendix

We define the three-dimensional global integral of \mathcal{H} as:

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$I(\mathcal{H}) = \int_{Z=Z_{aurface}}^{Z=Z_{top}} \mathcal{H} \, dAdz, \quad (A1)$

where A denotes cell area and z denotes height. The vertical integral is omitted if two-dimensional space is under consideration. The definitions of J_{uv} J_{vo} and J_{vor} are as follows:

$$L_1 = \frac{l_1(\mathcal{H} - \mathcal{H}_T)}{l_1(\mathcal{H} - \mathcal{H}_T)^2}, \qquad (A2)$$

$$L_2 = \int_{-\infty}^{1} \frac{l_1(\mathcal{H} - \mathcal{H}_T)^2}{l_1(\mathcal{H} - \mathcal{H}_T)^2}, \qquad (A3)$$

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 $L_{\infty} = \frac{\max\{|\mathcal{H} - \mathcal{H}_T|}{\max\{|\mathcal{H}_T|}, \qquad (A4)$

where $\mathcal{H}_{\mathbf{x}}$ and $\mathcal{H}_{\mathbf{x}}$ are the computational solution and true solution, respectively. Max \forall means selecting the maximum value from the field.

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	Table 1. Grid Name and Corresponding Horizon	ntal Resolutions.	
Grid <u>level of a</u>	Horizontal resolution (km) on a full-size	Number of Cells	删除了: Name
subdivided	Earth and on a small-radius Sphere (if		删除了:R
icosahedron	<u>used)</u>		格式化表格
<u>G4</u>	<u>480km (4km)</u>	<u>2,562</u>	
<u>G5</u>	<u>240km</u>	10,242	
<u>G6</u>	<u>120km (1km)</u>	40,962	
G7	60km <u>(0.5km)</u>	163,842	
G8	30km <u>(0.25km)</u>	655,362	
<u>G9</u>	<u>15km</u>	2,621,442	
G9B3	5km	23,592,962	

Table 2. Elapsed time using single-, mixed- and double precision (The runtime of each solver is

normalized to that of the corresponding solver in double-precision).

Grid Name	Precision	Dycore time (1440_steps)	Tracer time (1440_steps)
G8	DBL	1 (NDC) 1 (HDC)	1
	SGL	0.53 (NDC) 0.56 (HDC)	0.58
	MIX	0.73 (NDC) 0.76 (HDC)	0.56

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and (d) MIX simulation. (left) Colors show relative vorticity ($\times 10^{-5} s^{-1}$) and contours of the surface pressure and (right) the, relative error between SGL and DBL, as well as the difference between MIX and DBL.

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825 SGL and MIX experiments, respectively.







thunderstorms simulations. The first row displays double-precision simulations at 5 km altitude.
 The second, third, and fourth rows show the differences between mixed-precision and double-precision simulations at 5 km, 2.5 km, and 10 km altitudes, respectively. The four columns represent results at different resolutions: G4 (4 km), G6 (1 km), G7 (0.5 km), and G8 (0.25 km) from left to right,



Figure 5: The (a) domain maximum vertical speed and (b) area-integrated rainfall rate obtained from the supercell simulations.

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Figure 6: The simulated wind speed (m s⁻¹) at the G8 resolution with NDC solver, including MIX (a, b) and DBL (c, d) simulations. (left) Longitude-height cross section of the wind speed through the center latitude of the vortex as a function of the radius from the vortex center. (right) Horizontal cross section of the wind speed at surface model layer.



Figure 7: The results of deterministic and ensemble simulations. (a) The track of the tropical 865 cyclone center for MIX (blue lines) and DBL (read lines) deterministic simulations. Time evolution of the (b) minimum surface pressure and (c) maximum surface wind speed from the and deterministic and ensemble simulations. The red and blue lines represent the deterministic MIX and DBL simulations, respectively. The gray lines represent the eight runs with random perturbations to initial normal velocity at cell edges. 870



Figure <u>8</u>: The difference between the MIX and DBL simulations, including solutions from the hydrostatic (left column) and non-hydrostatic (right column) solver. The first and second rows respectively display the averaged (2001-2010) precipitation rate (mm/day) for JJA and DJF.



880 Figure 2: (a) Difference between the JJA-averaged (2001-2010) precipitation rate (mm/day) simulated by the SGL continuous equation solver in mixed-precision mode and the "true <u>DBL</u> value"; (b) same as (a) but for the DBL continuous equation solver. (c)-(d) same as (a)-(b) but for the DJF-averaged (2001-2010) results.





precipitation (units: mm) from the (a) DBL simulation, (b) MIX simulation and (c) the difference between MIX and DBL simulations.

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Figure 11: The L₂, norm error and convergence rate of 3D passive transport test (Hadlev-like meridional circulation) using single and double precision for three horizontal flux operators:
 RK3O2, RK3O3, and RK3O4. The upper and lower grev lines correspond to the slopes of first-and second-order convergence rates, respectively,

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