



# 1 Computation of Self-recruitment in Fish Larvae using Forward- and 2 Backward-in-Time Particle Tracking in a Lagrangian Model 3 (SWIM-v2.0) of the Simulated Circulation of Lake Erie (AEM3D- 4 v1.1.2)

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13 **Abstract.** Accurately estimating self-recruitment (SR), the fraction of recruits in a location that originated locally, is critical  
14 for understanding population connectivity. Biophysical models have been typically applied to compute SR by releasing a  
15 certain number of larval particles from each assumed source location and tracking them forward in time. However, various  
16 strategies have been employed for releasing these larval particles: including randomly, consistently, or a number  
17 proportional to the location's area or larval production, which causes ambiguous results. We demonstrate, using theoretical  
18 arguments and numerical simulations from Lake Whitefish (*Coregonus clupeaformis*) larvae in Lake Erie, that SR depends  
19 on larval production at each source location. This dependency suggests that SR may not be computed unambiguously in  
20 these models unless realistic larval production is released from all potential source locations. In contrast, parentage analysis  
21 studies typically computed SR by assessing the fraction of sampled juveniles that originate locally at a settlement location,  
22 instead of identifying larval production at all sources. Therefore, tracking larval particles backward from the settlement  
23 location is proposed as a straightforward approach for computing SR. Our findings demonstrate that SR is independent of the  
24 number of larval recruits at the settlement location, supporting the employment of backtracking models with randomly  
25 released larval particles. In this way, considerable effort and resources, that would otherwise be spent on identifying all  
26 potential sources and their larval output, in forward tracking can be saved. We believe this result will have important  
27 implications for studies on larval dispersal and recruitment in aquatic systems.

## 28 1 Introduction

29 Most marine species have a pelagic larval phase, during which larvae are transported by currents away from a source  
30 population and subsequently recruited into a receiving population, thereby regulating population connectivity (Cowen and



31 Sponaugle, 2009; Arevalo et al., 2023; Wood et al., 2014). Since Cowen et al. (2000) stated that marine populations may not  
32 be as open as previously thought, there has been accumulating evidence that the probability of dispersal declines rapidly with  
33 distance (Almany et al., 2013; Buston and D'aloia, 2013). Furthermore, high values of self-recruitment (SR) and local  
34 retention (LR) may be common in many fish populations (Cowen et al., 2000; James et al., 2002; Cowen et al., 2006;  
35 Almany et al., 2007; Hamilton et al., 2008; Hogan et al., 2012). This indicates that management decisions, based on open  
36 population models, might overestimate larval exchange, potentially leading to mismanagement of both local and downstream  
37 populations (Cowen et al., 2000; Nanninga et al., 2015). Therefore, measuring SR and LR is essential for quantifying  
38 localized recruitment, assessing the self-replenishment and persistence of populations, and designing effective fisheries  
39 management plans (D'aloia et al., 2013; Burgess et al., 2014; Lett et al., 2015).

40 SR is defined as the fraction of all recruits at a location that originated locally (Botsford et al., 2009); it reflects  
41 regional replenishment and the openness to recruitment from other locations (Burgess et al., 2014; Lett et al., 2015). LR  
42 indicates the self-persistence of a population, in the absence of external propagule inputs (Burgess et al., 2014). LR has been  
43 defined as the ratio of locally produced settlers to total local larval release (Botsford et al., 2009) or as the ratio of locally  
44 produced settlers to the total number of locally released larvae, that successfully settle in suitable nursery locations and  
45 survive (Hogan et al., 2012). Here, we define the latter, which includes only successfully settled larvae, as local retention,  
46 while the former, which encompasses both successful and unsuccessful settlers (those settling in unsuitable nursery  
47 locations), is termed “theoretical” local retention (TLR), as described by Shi et al. (2024). The three metrics (LR, TLR, and  
48 SR) share the same numerator, representing the number of local settlers, but differ in their denominators.

49 Parentage analysis and/or larval tagging have been widely used to estimate LR, TLR and SR (Jones et al., 1999;  
50 Pinsky et al., 2012; D'aloia et al., 2013; Lett et al., 2015; Planes et al., 2009). By assigning sampled juveniles to their parents  
51 according to DNA relationships, researchers can identify their source locations and quantify the number of settlers  
52 originating from each source location. However, the total number of eggs/larvae produced at a source location  $i$ ,  $N'_i$ , and their  
53 survival rates remain poorly understood, making it challenging to empirically assess LR and TLR (Lett et al., 2015).  
54 Consequently, biophysical models, typically coupled with forward-in-time Lagrangian particle tracking models (herein  
55 referred to as forward tracking models), have been widely applied to study larval dispersal and compute TLR and LR  
56 (Chaput et al., 2022; Saint-Amand et al., 2023; Sato et al., 2023; Gurdek-Bas et al., 2022). By assuming that  $N_i$  larvae are  
57 produced at location  $i$ , i.e., assuming  $N'_i = N_i$ , releasing  $N_i$  larval particles from  $i$  and tracking them forward in time, TLR  
58 can be computed as the ratio of the number of larvae that settle at location  $i$  to  $N_i$ . LR can also be computed by excluding the  
59 larvae that settle in unsuitable nursery locations from  $N_i$  (Gurdek-Bas et al., 2022). It is worth noting that both LR and TLR  
60 at location  $i$  are independent of  $N'_i$ , making it effective to release a random number of larval particles  $N_i$  from the location, as  
61 will be demonstrated in this research.

62 Typically, SR has also been computed using biophysical models (Paris et al., 2005; Hiddink et al., 2013; Dubois et  
63 al., 2016; Klein et al., 2016; Faillettaz et al., 2018; Lequeux et al., 2018; Meerhoff et al., 2018; Hidalgo et al., 2019;  
64 Wolanski et al., 2021; Saint-Amand et al., 2023; Michie et al., 2024; Nadal et al., 2024; Corrochano-Fraile et al., 2022; Sato



65 et al., 2023). In this case, a certain number of larval particles are released from each assumed source location and tracked  
66 forward in time. SR at the settlement location  $j$  is then computed as the number of larvae both released from and settled at  $j$ ,  
67 divided by the total number of larvae that settled at  $j$ . Notably, the denominator is related to the larval production from all  
68 source locations, which may transport larvae to  $j$ . In contrast, the numerator, representing the number of settlers originating  
69 from  $j$  itself, varies only with the larval production at  $j$ . Changes in larval production at any of the source locations can thus  
70 potentially alter the total number of settlers at  $j$ , resulting in variation in SR. However, simply identifying all potential source  
71 locations poses a challenge and it remains even less understood how many larval particles should be released from each  
72 source location.

73 At least four distinct strategies have been employed for releasing larval particles. For example, Hiddink et al. (2013),  
74 Dubois et al. (2016), and Faillettaz et al. (2018) assumed that larval production was consistent across all source locations,  
75 where each location was assumed to produce 500 larvae (Dubois et al., 2016), 1500 larvae (Faillettaz et al., 2018), or 10,000  
76 larvae (Hiddink et al., 2013), respectively. In this strategy, the SR at a location of interest was computed independently of  
77 the larval production at each source location. Sato et al. (2023) assumed that 900 larvae were produced from each of the 84  
78 source locations at Puerto Galera (PG) in the Verde Island Passage. The 84 source locations were randomly divided into  
79 three regions, with 5 locations at PG, 45 locations east of PG, and 34 locations west of PG. Therefore, 4500 larval particles  
80 were released from PG, 40500 from the east and 30600 from the west, resulting in 17.9, 4.4, and 71.9 particles settled at PG,  
81 respectively, giving a value of SR at region PG as  $17.9 / (17.9 + 4.4 + 71.9) = 0.19$ . However, if PG was divided into more  
82 locations, the number of local settlers at PG (i.e., 17.9) may be increased, altering the value of SR. D'agostini et al. (2015)  
83 assumed that larger locations produced proportionally more larvae than smaller ones, and Saint-Amand et al. (2023) assumed  
84 a constant density of 500 larvae/km<sup>2</sup> and a minimum release of 100 larvae for the smallest location. The resultant SR at each  
85 location, therefore, depended on the location area. Nolasco et al. (2022) assumed larval production at each location was  
86 proportional to the product of the adult abundance score by the spawning intensity score. From these examples, it remains  
87 uncertain whether larval production at each location is constant or proportional to the area of the location. Accurately  
88 releasing the number of larvae produced at each location may yield a more precise estimation of SR; however, the realistic  
89 number of larval productions at each location remains a challenge to observe. Additionally, there may be unknown source  
90 locations contributing to unexpected recruitment that is not accounted for in these simulations, causing potentially  
91 misleading estimates of SR.

92 Conversely, Shi et al. (2024) used backward-in-time Lagrangian particle tracking models (SWIM-V2.0, herein  
93 referred to as backtracking models) to estimate larval hatching locations of Lake Whitefish (*Coregonus clupeaformis*) and  
94 proposed that backtracking models may be more efficient in computing SR. Backtracking models, release larval particles  
95 from larval sampling locations and track them in reverse time, providing a straightforward approach to modeling recruitment  
96 that has been widely applied to study the spawning/hatching locations of fish larvae (Christensen et al., 2007; Thygesen,  
97 2011; Bauer et al., 2014; Gargano et al., 2022; Rowe et al., 2022; Chaput et al., 2023). In this case, the denominator of SR,  
98 the total number of settlers at location  $j$ ,  $M_j'$  (which is unknown as well), is assumed to be  $M_j$ , indicating that  $M_j$  larval



99 particles will be released from  $j$  and tracked backward in time. It is no longer necessary to identify all potential source  
100 locations and their corresponding larval production for estimating the denominator. The SR at  $j$  is independent of the real  
101 number of recruits at  $j$ , making it effective to release a random number ( $M_j$ ) of larval particles from  $j$ , as will be  
102 demonstrated.

103 In this research, we show theoretically that in forward tracking simulations, LR and TLR are independent of the  
104 larval production from the source location, while SR is not. Moreover, using forward tracking models to compute SR can  
105 yield ambiguous results. This assertion brings into question the numerous estimates of SR from studies that have employed  
106 different strategies for releasing larval particles from each source location within forward tracking models. Additionally, we  
107 compute SR using backtracking models and show that this SR remains independent of the number of recruits at the  
108 settlement location. We validate these assertions by applying both forward and backtracking models to compute LR and SR  
109 associated with observations of Lake Whitefish (*Coregonus clupeaformis*) larvae sampled in Lake Erie. Our findings are  
110 applicable to both freshwater and marine species that undergo a pelagic larval phase.

## 111 2 Theoretical Development

### 112 2.1 Self-recruitment from forward tracking models

113 Suppose that there are a set of  $n$  locations associated with larval hatching and larval settling or recruitment (locations 1, 2, ...,  
114  $i, j, \dots, n$ ). Here,  $N_i'$  represents the realistic number of eggs spawned or newly hatched larvae at location  $i$ . The larvae become  
115 pelagic upon hatching and undergo a dispersal process, being transported away from the source location by water currents.  
116 The dispersal rate from patch  $i$  to patch  $j$ , denoted as  $D_{ij}$ , is defined as the proportion of larvae released from location  $i$  that  
117 settle at location  $j$ . The theoretical local retention (TLR) at location  $i$ , commonly used in forward tracking simulations (Saint-  
118 Amand et al., 2023; Sato et al., 2023), is defined as follows, as per Shi et al. (2024):

$$119 \text{TLR}_i = \frac{D_{ii}N_i'}{N_i'} = D_{ii}, \quad (1)$$

120 At the end of larval dispersal, some larvae settle at suitable nursery locations, while some settle in unsuitable ones;  
121 the latter are referred to as 'unsuccessful' settlers (Almany et al., 2017). By excluding the unsuccessful settlers from the  
122 denominator of TLR, we obtain local retention (LR), which is also known as relative local retention (Hogan et al., 2012; Lett  
123 et al., 2015):

$$124 \text{LR}_i = \frac{D_{ii}N_i'}{\sum_{j=1}^n D_{ij}N_i'} = \frac{D_{ii}}{\sum_{j=1}^n D_{ij}}, \quad (2)$$

125 Self-recruitment (SR), the ratio of local larval recruitment to all the recruitment at the settlement location, at  
126 location  $i$  is (Botsford et al., 2009; Lett et al., 2015; Almany et al., 2017):



127 
$$SR_i = \frac{D_{ii}N'_i}{\sum_{j=1}^n D_{ji}N'_j}, \quad (3)$$

128 Assuming consistent larval production across all locations, i.e.,  $N'_1 = \dots = N'_i = N'_j = \dots = N'_n$ , the SR can be expressed as  
129 follows:

130 
$$SR_i = \frac{D_{ii}}{\sum_{j=1}^n D_{ji}}, \quad (4)$$

131 Here, both TLR and LR are theoretically independent of  $N'_i$ . When performing the forward tracking simulations,  
132 releasing a random number of larval particles,  $N_i$ , from the location  $i$ , is demonstrated as an effective approach to compute  
133 the unambiguous values of TLR and LR. In practice, a sufficiently large number of particles is needed for the dispersal rate  
134 ( $D$ ) to converge and accurately reflect the underlying processes. With more particles, the estimate of  $D$  stabilizes as it better  
135 captures the full distribution of trajectories. TLR provides a minimum value of LR as stated by Shi et al. (2024), as the  
136 denominator contains both successfully and unsuccessfully settlers. However, SR is shown to be dependent on larval  
137 production at each source location ( $N'_1, N'_2, \dots, N'_i, N'_j, \dots, N'_n$ ), demonstrating that any strategies for larval particle release  
138 other than releasing the realistic larval production from each source location in forward tracking may not unambiguously  
139 compute SR. Though assuming consistent larval production across all locations can make SR independent of larval  
140 production (Eq. 4), this assumption can lead to significant discrepancies in the estimated value of SR compared to using  
141 realistic value of larval production (Eq. 3), particularly when there are many source locations.

## 142 2.2 Self-recruitment from backward tracking models

143 An alternate approach is to release larval particles from the locations where larvae are recruited into the population  
144 (settlement locations) and track them backward-in-time. Suppose that there are a set of  $m$  locations associated with larval  
145 hatching and recruitment respectively (locations 1, 2, ...,  $i, j$ , ...,  $m$ ).  $M'_i$  larvae are recruited into settlement location  $i$ . The  
146 recruitment rate  $R'_{ij}$  is defined as the proportion of larvae recruited into the settlement location  $i$  that originated from the  
147 source location  $j$ . SR at location  $i$  can be written as:

148 
$$SR_i = \frac{R'_{ii}M'_i}{M'_i} = R'_{ii}, \quad (5)$$

149 SR at location  $i$  is theoretically equivalent to the recruitment rate at that location, independent of the number of  
150 recruits at  $i$ . This is reasonable; for instance, in parentage analysis studies, sampling all recruits at a location in the field is  
151 often challenging, SR is thus estimated as the number of sampled juveniles assigned to originate locally based on DNA  
152 relationships, divided by the total number of sampled juveniles at that location (D'aloia et al., 2013; Almany et al., 2017).  
153 This computation of SR, based on sampled recruits, can be used to reflect the overall recruitment dynamics, further  
154 supporting the notion that SR is independent of the number of recruits at the location of interest.



155 In backtracking simulations, a random number of larval particles  $M_i$  are typically released from location  $i$ . It is  
156 important to note that by the end of the simulation, some particles will have settled in suitable hatching or source locations,  
157 while some will have settled in unsuitable locations, leading to what is termed ‘unreal’ recruitment (Shi et al., 2024). The  
158 settlement rate  $R_{ij}$ , is the ratio of the number of larval particles that settle at location  $j$  and originate from location  $i$ , divided  
159 by the total number of larval particles released from location  $i$ . The difference between  $R_{ij}$  and  $R'_{ij}$  lies in the denominator,  
160 which corresponds to  $M_i$  and  $M'_i$ , respectively. Substituting  $R_{ij}$  and  $M_i$  for  $R'_{ij}$  and  $M'_i$  in Eq. 5 does not yield SR, but rather  
161 the theoretical self-recruitment (TSR), which is the minimum value of SR, as its denominator contains unreal recruits (Shi et  
162 al., 2024):

$$163 \text{TSR}_i = \frac{R_{ii}M_i}{M_i} = R_{ii}, \quad (6)$$

164 The SR at location  $i$ , in backtracking simulations, is obtained by excluding the unreal recruits from the denominator of TSR,  
165 expressed as:

$$166 \text{SR}_i = \frac{R_{ii}M_i}{\sum_{j=1}^n R_{ij}M_i} = \frac{R_{ii}}{\sum_{j=1}^n R_{ij}}, \quad (7)$$

167 Unlike Eq. (3), SR at location  $i$ , computed through backtracking models, is theoretically independent of the number  
168 of larval particles released from the location ( $M_i$ ). This independence arises because the settlement rate remains constant  
169 regardless of  $M_i$ , as will be demonstrated later with numerical data. Consequently, it is effective to release a random  
170 number of particles from the settlement location of interest.

171 The LR at location  $i$  in backtracking simulations is:

$$172 \text{LR}_i = \frac{R_{ii}M_i}{\sum_{j=1}^n R_{ji}M_j}, \quad (8)$$

173 The LR, estimated by backtracking, is dependent on  $M_i$ , unlike for forward tracking (Eq. 2). Moreover, backtracking cannot  
174 be used to compute TLR as there is no unsuccessful dispersal in the simulation, and similarly, forward tracking cannot  
175 compute TSR as there is no unreal recruitment.

### 176 2.3 Number of larvae produced and recruited at each location

177 The number of larvae produced at each location  $N'_i$  may be computed for use in forward tracking simulations to obtain  
178 unbiased estimates of SR, based on the number of recruits to location  $i$ ,  $M'_i$ .

179 If  $M_i$  particles are released from location  $i$  in backtracking simulations,  $M_i \cdot \sum_{j=1}^n R_{ij}$  particles are real recruits, as  
180 they settle in suitable hatching locations; correspondingly,  $M_i \cdot (1 - \sum_{j=1}^n R_{ij})$  are unreal recruits. Therefore, if  $M'_i$  recruits  
181 are sampled at a location  $i$ , the number of real recruits  $M_i \cdot \sum_{j=1}^n R_{ij}$  must equal  $M'_i$ , and  $M_i = M'_i / \sum_{j=1}^n R_{ij}$  particles should be



182 released at the location for backtracking. The number of recruits, at location  $i$ , that originates from location  $j$  can thus be  
183 obtained as:

$$184 \quad N'_{ji} = R_{ij} \cdot M'_i / \sum_{j=1}^n R_{ij}, \quad (9)$$

185 From the dispersal rate  $D_{ji}$ , the number of larvae produced at location  $j$ , is:

$$186 \quad N'_j = \frac{N'_{ji}}{D_{ji}} = M'_i \cdot \frac{R_{ij}}{D_{ji}} \cdot \frac{1}{\sum_{j=1}^n R_{ij}}, \quad (10)$$

187 Interestingly, if the number of recruits at another location  $a$  is  $M'_a$ , then the number of larvae produced at location  $j$  can also  
188 be written as:

$$189 \quad N'_j = M'_a \cdot \frac{R_{aj}}{D_{ja}} \cdot \frac{1}{\sum_{j=1}^n R_{aj}}, \quad (11)$$

190 Combining Eq. (10) and (11), we can obtain the number of recruits at location  $a$  as:

$$191 \quad M'_a = M'_i \cdot \frac{R_{ij}}{D_{ji}} \cdot \frac{D_{ja}}{R_{aj}} \cdot \sum_{j=1}^n \frac{R_{aj}}{R_{ij}}, \quad (12)$$

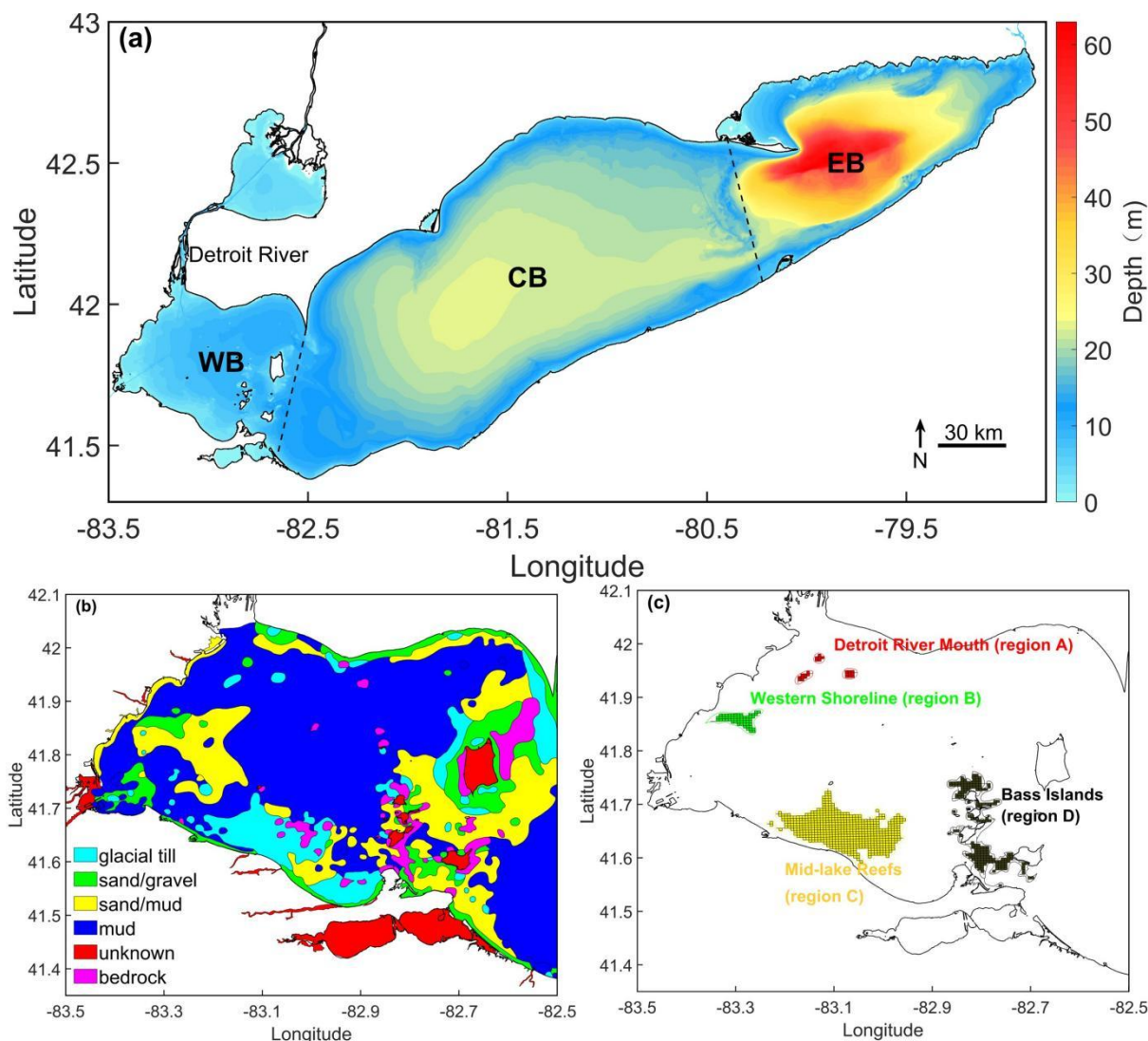
192 Both  $N'_j$  and  $M'_a$  are undefined when the dispersal, recruitment or settlement rates become zero.

### 193 3 Putting Theory into Practice: Application to Lake Erie

#### 194 3.1 Study area

195 Shi et al. (2024) identified the Lake Whitefish larval hatching locations in Lake Erie from backtracking simulations. The  
196 locations were primarily distributed along the western and southern flanks of the western basin. Considering that Lake  
197 Whitefish eggs incubate on hard substrates (Amidon et al., 2021), we selected four regions with hard substrates along the  
198 western and southern flanks of the western basin as potential hatching locations (Fig. 1). These were the release regions for  
199 larval particles in our forward tracking simulations. We refer to these locations as the Detroit River Mouth (region A),  
200 Western Shoreline (region B), Midlake Reefs (region C), and Bass Islands (region D). The Midlake Reef and Bass Island  
201 regions were also selected as settlement regions, where we released larval particles for backtracking simulations.





202

203 **Figure 1:** (a) Map showing the three basins of Lake Erie: western basin (WB), central basin (CB), and eastern basin (EB). The lake  
204 bathymetry was obtained from <https://www.ngdc.noaa.gov/mgg/greatlakes/erie.html>. (b) Substrate distributions in the western basin  
205 from side-scan sonar transects (Haltuch et al., 2000). (c) Color coded Lake Whitefish (*Coregonus clupeaformis*) hatching locations  
206 (Detroit River Mouth in red, region A; Western Shoreline in green, region B; Mid-Lake Reefs in yellow, region C; Bass Islands in  
207 black, region D), where larval particles were released at the centre of each 500 m × 500 m AEM3D grid (black cross-hatching).

### 208 3.2 The hydrodynamic model

209 Larval particles were transported using output from an application of the hydrostatic 3D Reynolds-averaged Navier-Stokes  
210 equation model, the Aquatic Ecosystem Model (AEM3D) ([www.hydronumerics.com.au](http://www.hydronumerics.com.au)). The model simulated the water  
211 temperature and currents in Lake Erie during a continuous 2017-2019 hindcast run, using a 500 m × 500 m horizontal grid  
212 with 45 vertical layers (Shi et al., 2024; Lin et al., 2022). There was fine resolution (0.5 m) through the surface layer,  
213 metalimnion and bottom of the central basin, and coarser resolution layers (5 m) through the hypolimnion of the deeper





214 eastern basin. The model was forced with surface meteorological data (wind speed and direction, air temperature, relative  
215 humidity and long- and short-wave solar radiation) from four weather stations, had five inflows (Detroit, Maumee, Sandusky,  
216 Cuyahoga and Grand rivers) and the Niagara River outflow. Model calibration and validation were described in the  
217 supplemental material (tables S2-S4) of Shi et al. (2024).

218 The AEM3D model, and its non-parallel predecessor the Estuary and Lake Computer Model (ELCOM), have been  
219 applied to Lake Erie to backtrack the present Lake Whitefish larval observations and determine hatching locations (Shi et al.,  
220 2024); to hindcast the thermal structure (León et al., 2005), internal wave dynamics (Valipour et al., 2015), surface wave /  
221 sediment transport (Lin et al., 2021), nutrient and chlorophyll-a distributions (Leon et al., 2011), seasonal succession of  
222 phytoplankton groups (Wang et al., 2024); and to forecast storm surge and upwelling/downwelling events (Lin et al., 2022).

### 223 3.3 The Lagrangian particle tracking model

224 We used a Matlab<sup>®</sup>-based Lagrangian particle tracking model (SWIM-v2.0) to study SR. An earlier version of this model  
225 was applied forward-in-time to track silver eel (*Anguilla rostrata* and *Anguilla anguilla*) migration (Béguer-Pon et al., 2016)  
226 and backward-in-time to determine the larval Lake Whitefish hatching locations used in this study (Shi et al., 2024). Diel  
227 vertical migration and active swimming behavior were not considered (Di Stefano et al., 2022; Rowe et al., 2022; Suca et al.,  
228 2022).

229 A horizontal turbulent diffusivity  $K_h = 0.1 \text{ m}^2\text{s}^{-1}$  and timestep  $dt_p = 600 \text{ s}$  were used in both forward and backward  
230 tracking simulations and larval particles were released at a 3-m water depth and were removed if they encountered the lake  
231 boundary (Shi et al., 2024). In the forward tracking simulations, particles were released daily at 12:00-noon between 21  
232 March and 8 May 2018 (in four regions; Table A1, regions A, B, C and D) and were tracked for 12 days. In the backtracking  
233 simulations, particles were released daily at 12:00-noon between 2 April and 20 May 2018 (in two regions for 12 days; Table  
234 A1, regions C and D). Each release region was divided into  $500 \text{ m} \times 500 \text{ m}$  AEM3D grid cells, and particles were released at  
235 the centres of these cells.

### 236 3.4 Nomenclature and data analysis

237 In forward tracking, the number of larval particles released from location  $i$  was  $N_i$  and the number of particles released from  
238 location  $i$  that settled at location  $j$  was  $F_{ij}$ . For example, if  $N_A$  particles were released from region A;  $F_{AC}$  represents the  
239 number of particles that settled in region C that were released from region A. In backtracking, the number of particles  
240 released from location  $i$  was  $M_i$  and the number of particles released from location  $i$  that settled at location  $j$  was  $B_{ij}$ . For  
241 example, if  $M_C$  particles were released from region C;  $B_{CA}$  represents the number of particles that settled in location A that  
242 were released from region C.

243 The dispersal rate  $D_{ij}$  and settlement rate  $R_{ij}$  are given by:

$$244 D_{ij} = F_{ij}/N_i, \quad (13)$$



245  $R_{ij}=B_{ij}/M_i$ , (14)

246 When computed from forward and backward simulations, local retention and self-recruitment are written as LR\_F, LR\_B,  
247 SR\_F and SR\_B, respectively. From Eqs. (11) and (14), the number of larvae produced at each location  $N'_i$  is:

248

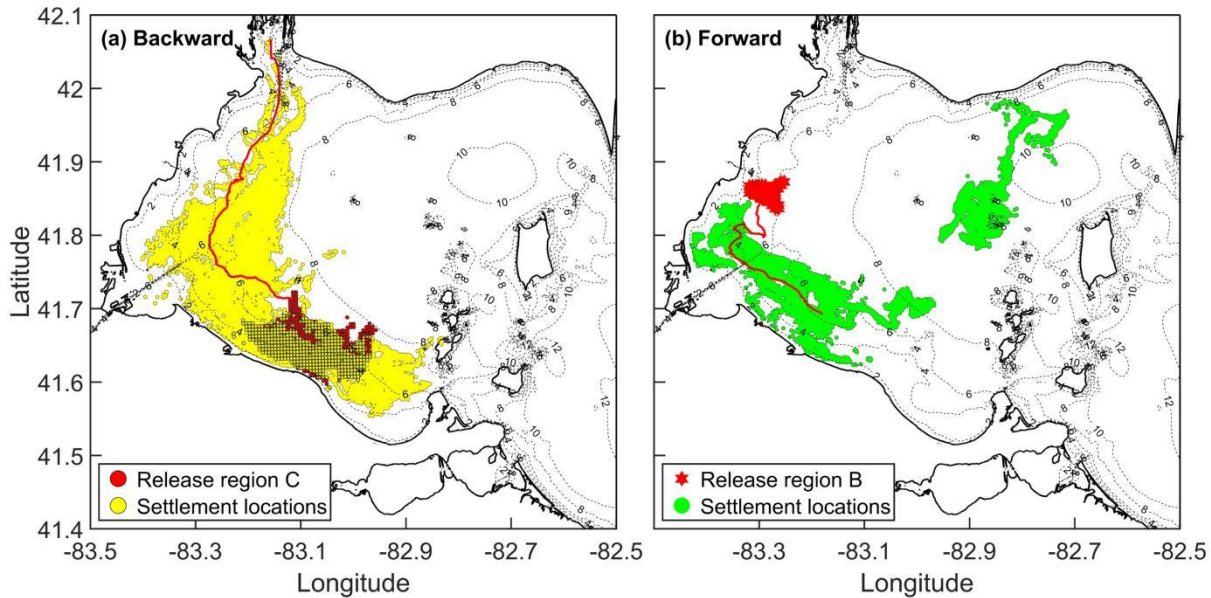
249  $N'_i = B_{ji}/D_{ij}$ , (15)

250 For example,  $N'_A$  is the number of larvae produced from region A. To estimate  $N'_i$ , from Eq. (11), requires both  
251 backward and forward tracking simulations, and the number of recruits to the location. Here, we only backtracked particles  
252 from region C and D; therefore,  $N'_i$  can be computed as  $B_{Ci}/D_{iC}$  or  $B_{Di}/D_{iD}$ , which are referred to as  $N'_{iC}$  and  $N'_{iD}$ ,  
253 respectively. Dividing  $N'_{A_C}$  by the number of AEM3D grid cells in region A (or the total area of the 500 m × 500 m grid  
254 cells) gives the density  $d'_{A_C}$ .

#### 255 4 Results

256 As examples of forward and backward trajectories, and to illustrate the validity of the tracking simulations, we show  
257 backtracked larval particles from the Midlake Reefs (region C, Fig. 2a) and forward tracked particles from the Western  
258 Shoreline (region B, Fig. 2b). When particles were released from region C and tracked backward for a period of 12 days,  
259 they mostly settled along the southern and western franks of the western basin (yellow dots in Fig. 2a), consistent with the  
260 settlement distributions in Shi et al. (2024). Most particles were backtracked to regions westward of the release locations  
261 with few travelling to regions eastward, following the predominant west-to-east flow patterns of water movement in the lake  
262 (Beletsky et al., 2013).

263 When particles were released from region B and tracked forward for a period of 12 days, they were mostly  
264 transported to the east of the release locations (green dots in Fig. 2b), also consistent with the flow patterns moving particles  
265 from west to east in the lake. However, some of the particles were transported southeast and northeast of the release  
266 locations, which seems to be counter-intuitive but is not unreasonable given the complex topography and variability in the  
267 wind direction in the region. Adding the northeast release region to the backtracking simulations would, therefore, lead to  
268 backward trajectories to region B.



269

270 **Figure 2: The settlement location distributions when (a) releasing particles from the red circles and tracking them backward, (b)**  
 271 **releasing particles from the red stars and tracking them forward. Yellow circles indicate the settlement locations in backtracking**  
 272 **and green circles indicate the settlement locations in forward tracking. Red lines show particle trajectories.**

273

In the forward tracking simulations, the number of settled larval particles ( $F_{ij}$ ) varied with the number of particles  
 274 released ( $N_i$ ) and the dispersal rate ( $D_{ij}$ ) was independent of  $N_i$  (Table 1). Both TLR and LR had negligible variation with  $N_i$ ,  
 275 for example TLR\_F at region C equaled to  $D_{CC}$  as  $\sim 0.13$  and TLR\_F at region D equaled to  $D_{DD}$  as  $\sim 0.024$ . Based on Eq. 3,  
 276 LR\_F equaled to 0 for region A and region B,  $\sim 0.755$  for region C, and  $\sim 0.99$  for region D.

277

The individual SR\_F values are not given in Table 1, because there were 81 different SRs obtained at region C  
 278 through changing  $N_i$ , consistent with Eq. (3), ranging from 0.22 to 0.95. For example, when 151200 particles were released  
 279 from A, 140000 particles from B, 19460 from C and 148400 from D, the SR\_F at region C was  
 280  $2537/(4668+4195+2537+37)=0.22$ ; whereas when 16800 particles, 17500 particles, 155680 particles, and 18550  
 281 particles were released from region A, B, C, and D respectively, SR\_F at region C was  
 282  $20758/(527+501+20758+2)=0.95$ . In other words, releasing more particles from region C and fewer particles from the  
 283 other regions increased the SR at region C, as  $D_{CC}$  was much larger than  $D_{AC}$ ,  $D_{BC}$  and  $D_{DC}$ . Indeed, SR can approach 1 or 0  
 284 through adjustment of  $N_i$ . The true value of SR can only be obtained if the actual number of larvae produced at each location  
 285 is released (i.e.,  $N_i = N'_i$ ); however,  $N'_i$  remains unknown.

286

If all four regions released the same number of particles, SR\_F would be only a function of  $D_{ij}$ , and would be  
 287 independent of  $N_i$ . For example, the SR\_F for region C was  $D_{CC}/D_{AC}+D_{BC}+D_{CC}+D_{DC}=0.68$  and the SR\_F for region D  
 288 was  $D_{DD}/D_{AD}+D_{BD}+D_{CD}+D_{DD}=0.32$ .



289 In the backtracking simulations, the number of settled larval particles  $B_{ij}$  varied with  $M_i$ . The settlement rate  $R_{ij}$  and  
 290 SR\_B had negligible variation with  $M_i$  (Table 2); showing the SR calculated from backtracking to be independent of  $M_i$ , as  
 291 indicated by Eq. (7). The correct SR values from backtracking may be compared to the erroneous ones from forward  
 292 tracking, which had assumed  $N_i$  to be the same for all sources. SR\_B at region C was larger than SR\_F (0.97 vs. 0.68) and  
 293 SR\_B at region D was smaller (0.18 vs. 0.32) because of the variation in the number of particles released from each location  
 294  $N_i$ . If the recruits to region C,  $M'_C$ , was equal to  $M_C \cdot (R_{CA} + R_{CB} + R_{CC} + R_{CD})$ , then the number of particles that should  
 295 have been released in forward tracking from region C should be  $\sim 2$  times greater than those from region D,  $\sim 10$  times  
 296 greater than those from region B, and  $\sim 50$  times greater than those from region A (see  $N'_{A,C}$ ,  $N'_{B,C}$ ,  $N'_{C,C}$ , and  $N'_{D,C}$  in Table  
 297 3); assuming the same  $N'_i$  increased the denominator of SR\_F at region C, and decreased the denominator of SR\_F at region  
 298 D. When scaled by the number of cells in each region, the larval density from region C was roughly half that from region D,  
 299  $\sim 4$  times that from region B, and  $\sim 10$  times that from region A (see  $d'_{A,C}$ ,  $d'_{B,C}$ ,  $d'_{C,C}$ , and  $d'_{D,C}$  in Table 3).

300

301 **Table 1.** Number of particles released from the four regions  $N_i$ , settled to four regions  $F_{ij}$ , and the dispersal rate  $D_{ij}$  in the  
 302 forward tracking simulations. The regions are the Detroit River Mouth (region A), Western Shoreline (region B), Midlake  
 303 Reefs (region C), and Bass Islands (region D).

$N_A$	$F_{AA}$	$F_{AB}$	$F_{AC}$	$F_{AD}$	$D_{AA}$	$D_{AB}$	$D_{AC}$	$D_{AD}$	LR_ $F_A$
16800	0	0	527	140	0	0	0.0313	0.0083	0
84000	0	0	2587	665	0	0	0.0308	0.0079	0
151200	0	0	4668	1189	0	0	0.0309	0.0079	0
$N_B$	$F_{BA}$	$F_{BB}$	$F_{BC}$	$F_{BD}$	$D_{BA}$	$D_{BB}$	$D_{BC}$	$D_{BD}$	LR_ $F_B$
17500	0	0	501	0	0	0	0.029	0	0
70000	0	0	2097	0	0	0	0.030	0	0
140000	0	0	4195	0	0	0	0.030	0	0
$N_C$	$F_{CA}$	$F_{CB}$	$F_{CC}$	$F_{CD}$	$D_{CA}$	$D_{CB}$	$D_{CC}$	$D_{CD}$	LR_ $F_C$
19460	0	0	2537	843	0	0	0.130	0.0433	0.751
77840	0	0	10440	3327	0	0	0.134	0.0427	0.758
155680	0	0	20758	6739	0	0	0.133	0.0433	0.755
$N_D$	$F_{DA}$	$F_{DB}$	$F_{DC}$	$F_{DD}$	$D_{DA}$	$D_{DB}$	$D_{DC}$	$D_{DD}$	LR_ $F_D$
18550	0	0	2	435	0	0	0.0001	0.0235	0.995
74200	0	0	19	1800	0	0	0.0002	0.0242	0.990
148400	0	0	37	3648	0	0	0.0002	0.0246	0.990



304 **Table 2.** Number of particles released from two regions  $M_i$  and settled in four regions  $B_{ij}$ , settlement rate  $R_{ij}$ , and self-  
 305 recruitment from the backtracking simulations. The regions are the Detroit River Mouth (region A), Western Shoreline  
 306 (region B), Midlake Reefs (region C), and Bass Islands (region D).

$M_C$	$B_{CA}$	$B_{CB}$	$B_{CC}$	$B_{CD}$	$R_{CA}$	$R_{CB}$	$R_{CC}$	$R_{CD}$	$SR_{B_C}$
19460	17	94	3778	2	$8.7 \times 10^{-4}$	0.0048	0.194	0.0001	0.971
77840	75	337	15300	8	$9.6 \times 10^{-4}$	0.0043	0.196	0.0001	0.973
155680	137	685	30659	22	$8.8 \times 10^{-4}$	0.0044	0.197	0.0001	0.973
$M_D$	$B_{DA}$	$B_{DB}$	$B_{DC}$	$B_{DD}$	$R_{DA}$	$R_{DB}$	$R_{DC}$	$R_{DD}$	$SR_{B_D}$
18550	0	0	1911	407	0	0	0.103	0.022	0.176
74200	0	0	7628	1718	0	0	0.102	0.023	0.184
148400	1	0	15302	3430	$6.7 \times 10^{-6}$	0	0.103	0.023	0.183

307 **Table 3.** The number of larvae and larval density (No. per cell) produced in the four regions. The regions are the Detroit  
 308 River Mouth (region A), Western Shoreline (region B), Midlake Reefs (region C), and Bass Islands (region D).

$M_C$	$N'_{A_C}$	$N'_{B_C}$	$N'_{C_C}$	$N'_{D_C}$	$d'_{A_C}$	$d'_{B_C}$	$d'_{C_C}$	$d'_{D_C}$
19460	550	3133	28406	10000	22.9	62.7	51.1	94.3
77840	2427	11233	115038	40000	101.1	224.7	206.9	377.4
155680	4434	22833	230519	110000	184.8	456.7	414.6	1037.7
$M_D$	$N'_{A_D}$	$N'_{B_D}$	$N'_{C_D}$	$N'_{D_D}$	$d'_{A_D}$	$d'_{B_D}$	$d'_{C_D}$	$d'_{D_D}$
18550	0	0	44134	16545	0	0	79.4	156.1
74200	0	0	176166	69837	0	0	316.8	658.8
148400	126	0	353395	139431	5.3	0	635.6	1315.4

## 309 5 Discussion

310 We have shown, using both theoretical arguments and numerical data, that self-recruitment (SR) cannot be unambiguously  
 311 computed using forward Lagrangian particle tracking models. In contrast, backward Lagrangian particle tracking models  
 312 have demonstrated to be straightforward and effective in calculating SR.

313 SR depends on the larval production at each source location (Eq. 3), as noted by Lett et al. (2015). This dependence  
 314 suggests that using forward tracking models to compute SR may be invalid if any strategy for larval particle release, such as  
 315 releasing a random number, an equal number, or a number proportional to the area of the location, is employed, rather than  
 316 releasing the realistic larval production from each source location. Our numerical data confirmed that variations in the  
 317 release of larval particles from any source location can lead to different values of SR. This is in addition to the likelihood  
 318 that there are unknown source locations contributing unexpected recruitment that are not accounted for in the simulation.



319 Similarly, researchers do not need to measure the larval production and dispersal rates of every potential source location to  
320 estimate the SR at a given location. Instead, they can easily obtain the SR by estimating the number of local juveniles from  
321 the total sampled juveniles at a given location, based on DNA relationships (D'aloia et al., 2013; Almany et al., 2017).

322 This shows that SR is independent of the number of larval recruits at the location of interest. This independence  
323 makes it effective to compute SR using backward tracking models by releasing a random number of larval particles from the  
324 location, as our numerical data demonstrated that SR had negligible variations with the number of larval particles released  
325 from the settlement location. Despite the increasing usage of backtracking models to estimate larval hatching/spawning  
326 locations and to study larval recruitment, few studies have used backtracking models to compute SR (Torrado et al., 2021).  
327 Considering the limitations of backtracking models, for example that they are diffusive backward-in-time rather than being  
328 convergent, comparisons with results from parentage analysis should be undertaken to further verify the validity of SR when  
329 computed using backtracking models.

330 Local retention (LR) is typically more challenging to evaluate empirically, compared to SR, as sampling the  
331 eggs/larvae that successfully grow into juveniles is more difficult than sampling recruits/juveniles (Lett et al., 2015). While  
332 parentage analysis can identify the source of sampled juveniles, accurately accounting for the total number of juveniles  
333 originating from a given source remains a challenge, as some juveniles are inevitably transported to unknown locations and  
334 may be missed. For example, Almany et al. (2017) sampled adult and juvenile *Amphiprion percula* and *Chaetodon*  
335 *vagabundus* from eight different locations in Papua New Guinea and assigned juveniles to their parents according to DNA  
336 relationships. The location of their parents served as the source location of the juveniles, allowing the researchers to  
337 determine the number of juveniles produced from each source location. However, the total number of larvae produced  
338 (including those lost to mortality) remained unknown. The difficulty in sampling newly hatched larvae, i.e., measuring  $N'_i$ , is  
339 likely why it is common to apply different larval particle release strategies from each source location in forward tracking  
340 simulations.

341 Knowing the number of recruits  $M'_i$ , or the larval production  $N'_i$  at one location, can allow us to estimate the number  
342 of recruits and larval production at all other locations from Eqs. (11) and (12) using forward and backward tracking  
343 simulations. An approach to estimate  $N'_i$  was proposed (Eq. 10), based on the number of recruits at a settlement location  $M'_j$ ,  
344 the settlement rate  $R_{ji}$  and the dispersal rate  $D_{ij}$ . From Eqs. (10) and (11), the  $N'_i$  values can be computed based on the  
345 recruits at different settlement locations and should be consistent. For example,  $N'_i$  computed from the recruits at regions C  
346 and D should be equal, such that  $N'_{i,C} = N'_{i,D}$ . However, large differences between  $N'_{i,C}$  and  $N'_{i,D}$  were modeled (Table 3).  
347 When  $D_{ij}$  or  $R_{ji}$  approaches zero, the computation of  $N'_i$  is undefined (section 2.3), which partly explains the difference.  
348 Moreover, random numbers of recruits  $M_j$  were released from regions C and D, which also caused differences between  $N'_{i,C}$   
349 and  $N'_{i,D}$ . These differences can be reconciled when  $D_{ij}$  and  $R_{ji}$  are non-zero by adjusting  $M_D$  based on  $M_C$ ;  $N'_{i,C}$  would then  
350 equal  $N'_{i,D}$ . For example, if  $M_C = 19460$  particles released and backtracked from region C, the realistic number of recruits at  
351 region C is  $M'_C = M_C \cdot (R_{CA} + R_{CB} + R_{CC} + R_{CD}) = 3887$ , the realistic recruits at region D,  $M'_D = 1514$  would then be





352 estimated based on Eq. (12). The particles released and backtracked from region D should, therefore, be  $M_D =$   
353  $M'_D/R_{DA}+R_{DB}+R_{DC}+R_{DD} = 12112$  instead of 18550 in Table 3. The  $N'_C$  value based on the recruits at region C,  $N'_{C,C}$ ,  
354 would be equal to 28820 (from Eq. 11) and  $N'_C$  estimated from the recruits to region D,  $N'_{C,D}$ , would equal to 28811. The  
355 negligible difference between 28820 and 28811 indicates the correctness of Eqs. (11) and (12).

## 356 6 Conclusions

357 Our findings show that self-recruitment (SR) is dependent on larval production at each potential source location that may  
358 transport larvae to the location of interest. From this, we show theoretically and confirm using Lake Whitefish simulations,  
359 that SR may not be computed unambiguously in forward tracking models without first identifying all the potential source  
360 locations and their respective larval production. The latter becomes particularly evident given that four different strategies  
361 for releasing larval particles from each source location have been employed. In contrast, in parentage analysis studies, it is  
362 typically not necessary to measure the larval production and dispersal rates of every potential source location to estimate SR  
363 at a given settlement location. Instead, by directly identifying the proportion of locally originating juveniles among the  
364 sampled juveniles at a given location based on DNA relationships, SR can be determined more efficiently and accurately.  
365 Similarly, releasing larval particles at the settlement location and tracking them backward in time offers a straightforward  
366 approach to computing SR. Our findings demonstrated that SR is independent of the number of larval recruits at the  
367 settlement location, making it viable to release a random number of larval particles. SR can thus be easily obtained as the  
368 fraction of larval particles that settle locally, saving considerable effort and resources that would otherwise be spent  
369 identifying all potential sources and their larval output. Furthermore, we proposed an approach to estimate larval production  
370 at each source location by leveraging the connectivity between source and settlement locations, computed through  
371 combining forward and backward tracking models. When run in isolation, backtracking models are only able to compute SR  
372 (or theoretical SR) and the settlement rate, and forward tracking models are only able to compute LR (or theoretical LR) and  
373 the dispersal rate. Whereas using a combination of both models allows for the calculation of not only SR and LR, but also  
374 the larval production at each source location and the number of recruits at settlement locations. The ability to accurately  
375 compute these metrics will significantly improve understanding of population connectivity. The findings were validated  
376 using numerical data for the Lake Whitefish freshwater species but are also applicable to marine species with a pelagic larval  
377 phase.  
378



379 **Appendix A**

380 **Table A1.** Release regions, times and durations for forward and backward tracking simulations.

	Release regions	Release times	Tracking periods (day)	Number of cells
Forward	Detroit River Mouth (Region A)	21 March to 8 May	12	24
	Western Shoreline (Region B)	21 March to 8 May	12	50
	Midlake Reefs (Region C)	21 March to 8 May	12	556
	Bass Islands (Region D)	21 March to 8 May	12	106
Backward	Midlake Reefs (Region C)	2 April to 20 May	12	556
	Bass Islands (Region D)	2 April to 20 May	12	106

381

382 **Table A2.** The description of the notations in this research.

Notation	Description
$B_{ij}$	Number of particles recruited to site $j$ that were released from site $i$ in backtracking
$d'_i$	Number of larvae per cell ( $500 \text{ m} \times 500 \text{ m}$ ) produced from site $i$
$d'_{i,j}$	Number of larvae per cell ( $500 \text{ m} \times 500 \text{ m}$ ) produced from site $i$ estimated based on the recruits to site $j$
$D_{ij}$	Proportion of larvae released from site $i$ that recruit into the juvenile population at site $j$
$F_{ij}$	Number of particles recruited to site $j$ that were released from site $i$ in forward tracking
$LR_i$	Ratio of local larval recruitment at site $i$ to the number of larvae released locally, that settled in suitable nursery sites
$M_i$	Number of particles released from site $i$ in the backtracking simulations
$M'_i$	Number of larval recruits to site $i$
$N_i$	Number of particles released from site $i$ in forward tracking simulations
$N'_i$	Number of larvae produced at site $i$
$N'_{i,j}$	Number of larvae produced from site $i$ estimated from the recruits to site $j$
$N'_{ji}$	Number of recruits at site $i$ that were released from site $j$
$R_{ij}$	Proportion of particles released from patch $i$ that settled in patch $j$ in the backtracking simulations
$SR_i$	Ratio of local larval recruitment at site $i$ to all recruitment at site $i$
$TLR_i$	Ratio of local larval recruitment to site $i$ to local larvae released



TSR <sub><i>i</i></sub>	Ratio of particles that settled at site <i>i</i> to all the particles released from site <i>i</i> in backtracking simulations
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383

384 *Code and data availability.* The AEM3D executable was used as a black-box hydrodynamic transport code. The AEM3D  
385 source code was not modified in this application but is available with permission from HydroNumerics. The model setup for  
386 AEM3D are available at <https://doi.org/10.5281/zenodo.14749408>. The forward and backward particle tracking models were  
387 performed in Matlab. Their code and simulated data are all available at <https://doi.org/10.5281/zenodo.14789098>. The  
388 velocity output from AEM3D is also presented at <https://doi.org/10.5281/zenodo.14789098>.

389

390 *Author contributions.* WS conceived the main study design, developed the theory, performed the simulations and analyses.  
391 WS wrote the first draft of manuscript and LB and JDA revised the draft significantly. LB and SLS co-supervised the  
392 research and provided resources. JDA, LB, SLS and YMZ acquired research funding. All authors contributed to the project  
393 conceptualization, and editing and revising the manuscript.

394

395 *Competing interests.* The contact author has declared that none of the authors has any competing interests.

396

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