"Pochva": a new hydro-thermal process model in soil, snow, vegetation for application in atmosphere numerical models

Oxana Drofa[1]

[1]Istitute of Atmospheric and Climate of National Research Council (CNR-ISAC), Bologna, 40129, Italy

5 *Correspondence to*: Oxana Drofa (o.drofa@isac.cnr.it)

Abstract. This work presents the land model "Pochva". "Pochva" is a model of hydro-thermal processes at the Earth surface and in the underlying medium. The model simulates the main hydro-thermal parameters of the surface, soil layer, vegetation and snow layer. Its soil process scheme allows to use physical parameters having vertical variations along the soil profile. Its snow processes scheme is a multiple layer scheme and has a numerical algorithm allowing to solve both cases of extremely
10 thin and extremely thick layer. The model is marked by a particular accuracy in simulating the water phase transitions in soil and snow, and by the autonomy in the determination of the lower boundary condition in the soil column. The model can be used as a stand-alone land-surface model driven by observed or analytical forcing data, or coupled to an atmospheric model, either global or limited-area, either in forecast regime or climatic (hindcast) regime. The results of coupling "Pochva" to the numerical weather prediction limited-area model "Bolam" are presented in this article.

1 Introduction

Water mass balance and energy balance at the Earth surface are key processes in a numerical model of the atmosphere. These processes determine the condition at the lower boundary for the main atmospheric parameters as well as air parameters in the surface layer. The surface hydro-thermal conditions are simulated by a scheme (or model) of hydro-thermal processes in the
20 surface and in the underlying media, composed by soil layer, possibly covered by vegetation, and by snow layer.

The simulation of hydro-thermal processes in the underlying media in the current model is significantly evolved from a simple soil scheme (e.g. Deardorff, 1978) through to complex vegetation structures with multiple layer soil hydrology and energy and multiple layer snow. Examples of currently used land surface schemes include the Interaction Soil-Biosphere-Atmosphere model (ISBA, Noilhan and Planton, 1989); the Canadian Land Surface Scheme (CLASS, Verseghy, 1991; Verseghy et al.,
25 1993); the Tiled ECMWF Scheme for Surface Exchanges over Land model (TESSEL, Viterbo and Beljaars, 1995), including multi-layer snow scheme (Arduini et al., 2019), the NOAH model (Ek et al., 2003); the Common Land Model of National Center of Atmospheric Research (USA) and Sun Yat-sen University (China) (Dai et al., 2003); the Community Land Model (CLM, Oleson et al., 2010), Joint UK Land Environment Simulator (JULES, Best et al., 2011), GEOtop (S. Endrizzi et al.,

2014). The important role of a correct simulation of the interaction between the atmosphere and the land surface for current

30   atmospheric and climatic research is discussed in a clear and complete manner in (Santanello et al., 2018).

The high number and variety of existing models is due to the fact that different models underline different processes in soil and vegetation. The differences are connected to the different purposes of their application: weather prediction, study of atmospheric processes, simulation of snow cover and avalanche prediction, climatic simulations coupled with biosphere models. Some models pay particular attention to hydro-thermal exchange processes in soil, take into account phase transition

35   processes in soil water, and processes in the snow layer, they accurately describe the fluxes at soil surface. These models are more suitable for application in modelling of atmospheric processes and weather forecast. Other models pay more attention to an accurate description of the processes connected to vegetation, distinguishing high and low vegetation, simulating in detail processes like evapotranspiration and giving an accurate simulation of carbon cycle. These models are more addressed to climate and Earth system modelling.

40   The model proposed in the present work is closer to the first class of models, i.e. is more suitable for models targeted at the study of atmospheric process and weather prediction models. In the proposed model, special attention was paid to the accuracy of description of heat and moisture exchange in soil, including water phase transitions, to the accuracy and reliability in the description of processes in the snow layer, including water melting and re-freezing, to the inhomogeneity in soil parameters along the vertical, to the definition of thermal and hydraulic conductivity in the different situations, to the problem of defining

45   the atmospheric humidity at the contact surface with the soil and vegetation leaves, to the problem of determining the albedo and density of snow cover depending on its history. In the proposed model an original method for defining bottom boundary conditions for temperature and humidity is applied, making the model autonomous in the frame of a known climatology or climatological drift. The model can also be useful for the simulation of snow cover for avalanche prediction purposes since the snow module is independent of the other modules and applied separately. The model can also be used with a forcing derived

50   from observational data for defining the fluxes between the surface and the atmosphere as well as for idealised column simulations.

The present paper is divided into eight sections, the second, third, fourth, fifth and sixth are devoted to the description of the schemes included in the model: surface processes, processes in the vegetation, heat exchange processes in the soil, moisture exchange processes in the soil, processes in the snow layer. The seventh section contains the description of the numerical

55   experiments and their results. The last section contains the conclusions and some discussion about the critical points of the model and of the verification results.

2 Surface processes scheme

The interaction between the atmosphere and the Earth surface from the point of view of atmospheric modelling, takes place mainly by means of fluxes of heat and moisture. The main parameter describing the thermal state of the soil environment in

60 the present model is the entropy. This variable has been chosen since it simplifies the description of the water phase changes following the idea proposed in (Pressman, 1994).

The state of the atmosphere interacting with the Earth surface is described by air temperature, specific humidity and pressure at the lowest atmospheric level, turbulent transfer coefficients between surface and lowest atmospheric level, total net radiation flux, fluxes of atmospheric precipitation in liquid and crystal phases. The state of the surface with regard to atmospheric

65 dynamics equations, is described by temperature and specific humidity of the air. The values of these two parameters depend on the whole state of the underlying surface.

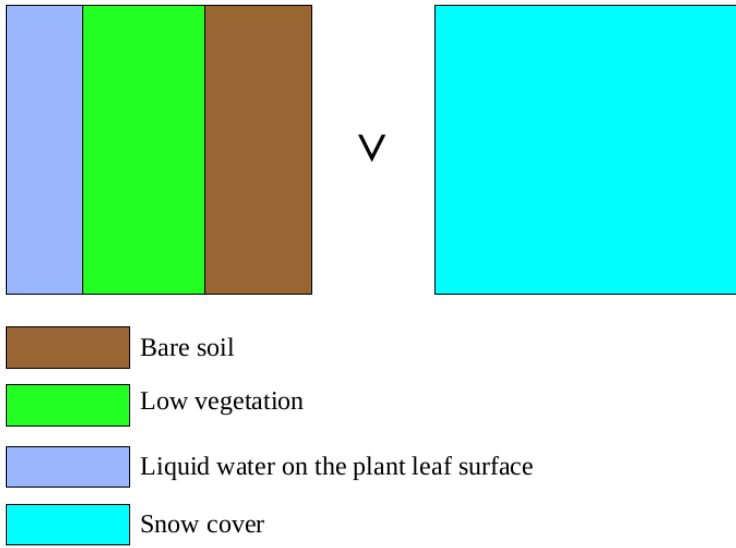
2.1 State of the soil surface

According to the principles adopted in this work, a unit size of underlying surface is composed of a set of fractions each having uniform characteristics from the point of view of the interaction with the atmosphere. The soil surface can be covered by

70 vegetation (grass, shrub), high vegetation (trees, woodland) and snow. Snow cover and high vegetation imply the presence of a particular layer with its own thermodynamic characteristics, thus with a distinct temperature. For this reason, it is not possible to consider them as a fraction of the surface of the soil itself, but it is necessary to consider them as independent "columns". As a consequence, if we introduce the concept of fraction of snow cover, it is necessary to divide the surface into three independent columns, each having its own temperature even in case of equal upper and lower boundary conditions. In the

75 present version of the model here described, however, the following simplifying assumptions have been made: the vegetation has not been divided into high and low and the two types, possibly mixed, are considered as a part of the soil surface with particular characteristics; the snow layer can either cover all the surface or not exist at all, a fractional snow cover is introduced only as a diagnostic field to allow computation of the radiative characteristics of the surface (albedo, emissivity). Under this assumption, the soil surface can either consist of bare soil possibly partly covered by low vegetation, which in turn may be

80 partly covered by water, or consist of snow cover. These two states of the surface can turn one into the other but cannot exist simultaneously.

■ Bare soil	
■ Low vegetation	
■ Liquid water on the plant leaf surface	
■ Snow cover	

95 **Figure 1: Scheme of the soil surface.**

In the area of a single model grid cell the vegetation fraction is determined using a useful vegetation parameter dataset. The fraction of vegetation leaves covered by water is determined be ration of water mass deposited on the leaf surface and maximum value of this mass, which is also determined using an dataset.

In this way, the surface interacting with atmosphere can be of the following types:

100 - without snow cover (F_{snow}=0):
  1) $F_{baresoil} = 1 - F_{veg}$ bare soil

  2) $F_{veg}^{dry} = F_{veg} \cdot \left(1 - F_{veg}^{leaf\ wet}\right)$ vegetation leaves not covered by water

  3) $F_{veg}^{wet} = F_{veg} \cdot F_{veg}^{leaf\ wet}$ vegetation leaves covered by water

- in case of snow cover, under the indicated assumptions the only type of interacting surface is:
105 4) F_{snow}=1.

More precisely, in presence of snow, we always assume F_{snow}=1 for the computation of moisture fluxes, while for the entropy fluxes, F_{snow}=1 holds only if the snow cover has a minimal thickness, otherwise, for a shallow snow layer, entropy fluxes are computed under the assumption of F_{snow}=0 (see the explanation of the snow scheme for more details).

For each of these four surface types, surface air temperature and humidity have to be defined. The overall surface air
110 temperature and humidity for the whole grid cell are then computed as an average of these values weighted with the fractional area of each surface type.

2.2 Air temperature and humidity on bare soil

For bare soil, the surface air temperature ($T_{surf\ soil}$) is equal to the temperature of the upper soil layer (T_{soil0}). The air specific humidity $q_{v\ surf\ soil}$ (kg kg-1) is defined according to the diagnostic expression

$$115 \quad q_{v\,surf\,soil} = q_{v\,atm\,1} \cdot (1 - \alpha_{soil}) + q_{v\,sat}(T_{soil\,0}) \cdot \alpha_{soil}, \tag{1}$$

where: $q_{v\,atm}$ is the air specific humidity at the lowest atmospheric level (kg kg-1), $q_{v\,sat}(T_{soil0})$ is the saturation air specific

humidity at temperature T_{soil0} computed as:

$$q_{v\,sat} = \begin{cases} q_{v\,sat}^{water}(T_{soil0}), & if\ T_{soil0} \geqslant T_0 \\ q_{v\,sat}^{ice}(T_{soil0}), & if\ T_{soil0} < T_0 \end{cases}, \tag{2}$$

where, in turn, $q_{v\,sat\,water}$ and $q_{v\,sat\,ice}$ are saturation air specific humidity over liquid water and ice respectively, αsoil is

120   an empirical coefficient, $To = 273.15$ (K) is the constant.

For the definition of the empirical coefficient αsoil an original method is proposed in this work. The approach proposed has

been formulated following the method proposed in (Kondo et. Al, 1990) using both concepts of turbulent exchange and of

influence of top soil moisture to surface air humidity. Various empirical parameters have been introduced by the author and

presented in formulae (3), (4), (5). These formulations and the values of parameters are the results of many numerical

125   experiments and statistical verification on a big number of observational meteorological stations (see section 7). The

definition is the following:

$$\alpha_{soil} = \frac{2 \cdot F_2^{soil}}{e^{F_1^{soil} K_v^{turb}} + e^{-F_1^{soil} K_v^{turb}}}, \tag{3}$$

where:

K_v^{turb} is the coefficient of water vapour turbulent exchange in the lowest 1 m of the surface layer (m^{2}s^{-1}),

130   F_1^{soil} and F_2^{soil} are empirical functions of the relative moisture contents of the upper soil layer:

$$F_1^{soil} = 7 \cdot [2 + 3 \cdot (1 - q_0^{rel})^{0.2 + 0.05 \cdot b}], \tag{4}$$

$$F_2^{soil} = 1 - 0.8 \cdot (1 - q_0^{rel})^{0.2 + 0.05 \cdot b}, \tag{5}$$

where b is the so-called «soil exponent» (Clapp and Hornberger, 1978), q_0^{rel} is soil relative water content at the top level (see

section 4). The choice of the values defining the empirical function is crucial since it strongly influences the magnitude of the

135   water vapour flux and its associated latent heat flux, which, in turn, influences the soil surface temperature and the air

temperature at 2 meters routinely used for the verification of numerical weather predictions. The methodology used for defining

these empirical coefficients and their influence on the numerical weather forecast will be treated in a separate publication

dedicated to the evaluation of the numerical model results.

2.3 Air temperature and humidity over vegetation with leaves not covered by water

140   The air temperature in this case (T_{veg}^{dry}) is equal to the temperature of the topmost soil layer (T_{soil0}). For the definition of air

humidity two cases are distinguished: the evapotranspiration is active or is not active. The conditions under which

evapotranspiration is or is not active are shown in section 3.

The method of numerical approximation of evapotraspiration presented here has been formulated using the approach presented

in (Pressman, 1994).

145   In the case of lack of evapotranspiration, the air humidity is equal to the air humidity at the lowest atmospheric layer while in the case of active evapotranspiration by leaves not covered by water it is defined analogously to the case of bare soil:

$$q_{v\,veg}^{dry} = \begin{cases} q_{v\,atm}, & if\ evapotraspiration\ not\ active \\ q_{v\,atm} \cdot (1 - \alpha_{veg} \cdot \beta_{veg}) + q_{v\,sat}(T_{soil\,0}) \cdot \alpha_{veg} \cdot \beta_{veg}, & if\ evapotraspiration\ active \end{cases}' \tag{6}$$

where:

$q_{v\,veg}^{dry}$ is the air specific humidity over respiring plant leaf,

150    $q_{v\,atm}$ is air specific humidity at the bottom atmospheric level (kg kg^{-1}),

$q_{v\,sat}(T_{soil0})$ is saturation air specific humidity (kg kg^{-1}) at soil surface temperature T_{soil0}, (see paragraph 2.2),

α_{veg} is an empirical parameter depending on the magnitude of the evapotranspiration activity,

β_{veg} is a parameter depending on the moisture content in the root layer of the soil.

A method similar to the one presented in the previous paragraph was used to formulate the parameter defining the
155   evapotranspiration activity it is given by:

$$\alpha_{veg} = \frac{2 \cdot F_2^{veg}}{e^{F_1^{veg} \cdot K_v^{turb}} + e^{-F_1^{veg} \cdot K_v^{turb}}}, \tag{7}$$

where F_1^{veg} and F_2^{veg} are empirical functions depending on the turbulent exchange coefficients for water vapour in the lowest 1 m of the atmospheric surface layer and on the intensity of the evapotranspiration process which in turn depends on the flux of incoming visible solar radiation and on LAI (Leaf Area Index) following the conception proposed in (Viterbo et. al, 1995)
160   according to:

$$F_1^{veg} = 30 \cdot \left[-1.9 \cdot \frac{LAI}{LAI_{max}} + 2 \right], \tag{8}$$

$$F_2^{veg} = min \left[\left[min \left(\frac{F_{rad\,vis}}{600}, 1 \right) \right]^{0.3}, \left(\frac{LAI}{LAI_{max}} \right)^{0.2} \right], \tag{9}$$

where

$F_{rad\,vis}$ is the flux of visible solar radiation at the surface (W m^{-2}),

165   LAI_{max} is the maximum value of LAI in the static global database used.

In this case, as in the case of air surface humidity over bare soil, the various empirical parameters in formulae (7), (8), (9) have been introduced by the author and their values have been obtained as result of many numerical experiments and statistical verification.

In order to evaluate the parameter $\beta_{,veg}$, a description of the finite-difference representation of the vertical space coordinate
170   used in the model is described here.

As a vertical coordinate, the geometrical length (depth) is used, with the origin at the surface and values growing with growing depth. The vertical computational domain is divided into full and half levels, with the upper full level having index zero, and with each half level having the same index as the full level located below it; the level indexes grow with growing depth (see fig. 2).

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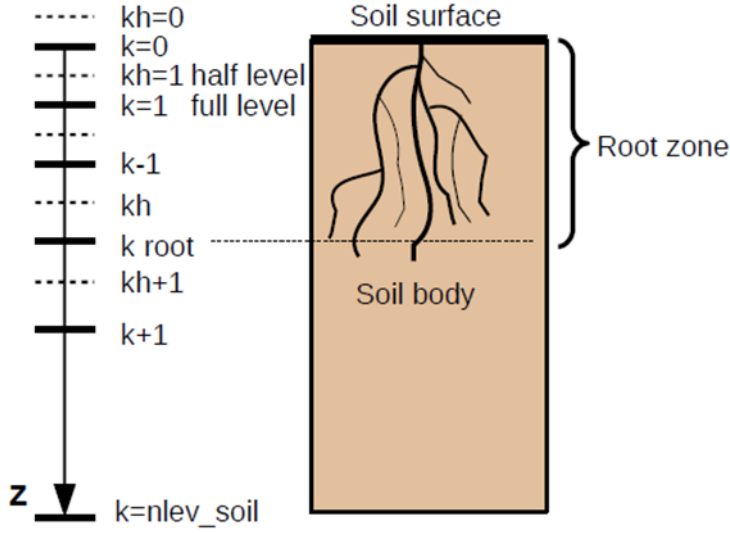
Figure 2: Finite-difference discretisation of the vertical coordinate in the soil.

The upper part of the soil column may contain plant roots. The depth of the root layer is defined as:

$$Z_{root} = \sum_{k=0}^{k_{root}}(z_{kh+1} - z_{kh}),$$ (10)

180 Where z (m) is the space coordinate in soil, k is the index of full level in the vertical discretization, k_{root} is the index of the deepest root zone level, root zone depth is defined using a suitable vegetation dataset, *nlev_soil* is the index of bottom soil level. In this work the distribution of vertical soil levels is not uniform, the thickness of soil layers increases with depth according to an exponential law, but it is possible to apply any other distribution. The depth of soil bottom in the present scheme may be different for the water exchange processes and for thermal exchange processes, depending on bottom boundary conditions, and they may change from a geographical location to another according to the local geographical characteristics.

185
$$\beta_{veg} = \frac{\sum_{k=0}^{k_{root}}(z_{kh+1}-z_{kh})\cdot F\left(q_k^{rel}\right)}{Z_{root}},$$ (11)

$$F\left(q_k^{rel}\right) = \begin{cases} 1, & if\ q_k^{rel} \geqslant q_k^{rel\,ref} \\ \frac{q_k^{rel}-q_k^{rel\,wilt}}{q_k^{rel\,ref}-q_k^{rel}}, & if\ q_k^{rel\,wilt} < q_k^{rel} < q_k^{rel\,ref}, \\ 0, & if\ q_k^{rel} \leqslant q_k^{rel\,wilt} \end{cases}$$ (12)

$$q_k^{rel} = \frac{q_k-q_k^{min}}{q_k^{max}-q_k^{min}}, q_k^{rel\,wilt} = \frac{q_k^{wilt}-q_k^{min}}{q_k^{max}-q_k^{min}}, q_k^{rel\,ref} = \frac{q_k^{ref}-q_k^{min}}{q_k^{max}-q_k^{min}},$$ (13)

where

190 q_k and $q_k{}^{rel}$ are the soil specific volumetric (m³ m⁻³) and relative (proportion) water content at level k,

$q_k{}^{max}$ and $q_k{}^{min}$ are the maximum and minimum soil specific volumetric contents at level k (m³ m⁻³),

q_k^{wilt} and $q_k^{rel\ wilt}$ are soil specific volumetric (m³ m⁻³) and relative (proportion) water contents at level k at wilting point, i.e. at the water content at which plant evapotranspiration stops because of too dry soil,

$q_k^{\ ref}$ and $q_k^{rel\ ref}$ are soil specific volumetric (m³ m⁻³) and relative (proportion) water contents at level k at «reference point», i.e. at the water content level at which plant evapotraspiration stops increasing because of highly wet soil.

2.4 Air temperature and humidity over vegetation with leaves covered by water

The air temperature in this case (T_{veg}^{wet}) is equal to the temperature of the topmost soil layer (T_{soil0}). The air humidity is equal to the saturation humidity at the given temperature:

$$q_{v\ veg}^{wet} = q_{v\ sat}(T_{soil\ 0}), \tag{14}$$

where $q_{v\ sat}(T_{soil0})$ is the saturation air specific humidity (kg kg-1) at soil surface temperature T_{soil0} (see paragraph 2.2).

2.5 Air temperature and humidity over snow cover

The air temperature in this case ($T_{surf\ snow}$) is equal to the temperature of the topmost snow layer (T_{snow0}). The air humidity is equal to the saturation humidity at the given temperature:

$$q_{v\ surf\ snow} = q_{v\ sat}(T_{snow\ 0}), \tag{15}$$

where $q_{v\ sat}(T_{snow0})$ is the saturation air specific humidity (kg kg⁻¹) at snow cover surface temperature T_{snow0}.

$$q_{v\ sat} = \begin{cases} q_{v\ sat}^{water}(T_{snow0}), & if\ T_{snow0} \geqslant T_0 \\ q_{v\ sat}^{ice}(T_{snow0}), & if\ T_{snow0} < T_0 \end{cases}, \tag{16}$$

where $q_{v\ sat}^{water}$ and $q_{v\ sat}^{ice}$ are saturation air specific humidity (kg kg⁻¹) at snow cover surface temperature T_{snow0} over liquid water and over ice respectively.

2.6 Air temperature and humidity over a composite soil surface

Having defined the values of air temperature and humidity over all the possible components of a composite soil surface, and knowing the fraction of each component of the surface, it is possible to define the overall surface air temperature (T_{surf}) and humidity ($q_{v\ surf}$).

In absence of snow cover, or in presence of a so-called shallow snow layer (see the description of snow scheme) the overall surface air temperature is equal to the weighted mean of the temperatures of the surface components:

$$T_{surf} = T_{surf\ soil} \cdot F_{baresoil} + T_{veg}^{dry} \cdot F_{veg}^{dry} + T_{veg}^{wet} \cdot F_{veg}^{wet}, \tag{17}$$

while in case of a thick snow layer we have:

$$T_{surf} = T_{surf\ snow}. \tag{18}$$

Similar formulas hold for the surface specific humidity, in case of absence of snow cover:

$$q_{v\ surf} = q_{v\ surf\ soil} \cdot F_{baresoil} + q_{v\ veg}^{dry} \cdot F_{veg}^{dry} + q_{v\ veg}^{wet} \cdot F_{veg}^{wet}, \tag{19}$$

and in presence of snow cover (either thick or shallow):

$$q_{v\,surf} = q_{v\,surf\,snow}. \tag{20}$$

2.7 Entropy flux between soil surface and atmosphere

The surface incoming entropy flux is composed by the turbulent flux of entropy for dry air, the turbulent flux of entropy due to water vapour and the entropy flux due to the global radiation:

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$$\Phi_{S\,surf} = \Phi_{S\,rad} + \Phi_{S_{da}}^{turb} + \Phi_{S_v}^{turb}, \tag{21}$$

where:

$\Phi_{S\,surf}$ is the surface entropy flux (J K^{-1} m^{-2} s^{-1}),

$\Phi_{S\,da}{}^{turb}$ and $\Phi_{S\,v}{}^{turb}$ are the entropy fluxes originating from turbulent entropy flux of dry air and of water vapour (J K^{-1} m^{-2} s^{-1}),

$\Phi_{S\,rad}$ is the entropy flux originating from global radiation (J K^{-1} m^{-2} s^{-1}).

230 The flux of entropy due to the flux of water (in liquid and solid phases) from atmospheric precipitation is neglected since in the soil entropy scheme the entropy flux originating from soil moisture flux is also neglected.

The entropy fluxes are computed according to the following relations:

$$\Phi_{S\,rad} = \frac{\Phi_{rad}}{T_{surf}}, \tag{22}$$

where Φ_{rad} is the flux of global radiation (W m^{-2}).

235

$$\Phi_{S_{da}\,surf}^{turb} = K_h^{turb} \cdot \rho_{a\,surf} \cdot \frac{S_{da\,surf} - S_{da\,atm}}{z_{atm}}, \tag{23}$$

where:

$K_h{}^{turb}$ is the coefficient of heat exchange in the surface layer (m^2 s^{-1}),

$\rho_{a\,surf}$ is the air density at the surface (kg m^{-3}),

z_{atm} is the height of the lowest atmospheric level (m).

240 $S_{da\,surf}$ and $S_{da\,atm}$ are specific entropy of dry air on the surface and at the lowest atmospheric level (J kg^{-1} K^{-1}).

The entropy of dry air is defined by the relation:

$$S_{da} = q_d \cdot \left[C_p^d ln\left(\frac{T}{T_0}\right) - R_d ln\left(\frac{P_d}{P_0}\right) \right]: \tag{24}$$

where:

S_{da} is the specific entropy of dry air (J kg^{-1} K^{-1}),

245 q_d is the specific mass of dry air (kg kg^{-1}),

T is the temperature (K),

P_d is the partial pressure of dry air (Pa),

T_0=273.15 K is the reference temperature,

P_0=10^5 Pa is the reference pressure,

250 C_p^d=1004.6 J kg^{-1} K^{-1} is the specific heat capacity of dry air at constant pressure,

R_d=287.05 J kg^{-1} K^{-1} is the gas constant of dry air.

In order to define the entropy of dry air at the surface and at the lowest atmospheric level, the known values of air temperature, humidity and pressure are used together with the relations:

$$q_{da\ surf} = 1 - q_{v\ surf}, \tag{25}$$

$$q_{da\ atm} = 1 - q_{v\ atm}, \tag{26}$$

$$P_{d\ surf} = P_{surf} - e_{surf}, \tag{27}$$

$$P_{d\ atm} = P_{atm} - e_{atm}, \tag{28}$$

$q_{da\ surf}$ and $q_{da\ atm}$ are dry air specific mass at the surface and at the lowest atmospheric level (kg kg^{-1}),

$P_{d\ surf}$ and $P_{d\ atm}$ are partial pressure of dry air at the surface and at the lowest atmospheric level (Pa),

e_{surf} and e_{atm} are partial pressure of water vapour at the surface and at the lowest atmospheric level (Pa).

The entropy flux of water vapour originating from turbulent exchange in the layer between soil surface and lowest atmospheric level is defined as:

$$\Phi_{S_v}^{turb} = K_v^{turb} \cdot \rho_a \cdot \frac{S_{v\ surf} - S_{v\ atm}}{z_{atm}}, \tag{29}$$

where $S_{v\ surf}$ and $S_{v\ atm}$ are specific entropy of water vapour at the surface and at the lowest atmospheric level respectively (J kg^{-1} K^{-1}), which, in turn, are defined by:

$$S_v = q_v \cdot \left[C_v^d ln\left(\frac{T}{T_0}\right) - R_v ln\left(\frac{e}{e_0}\right) + \frac{L_i^v}{T_0} \right] \tag{30}$$

where:

S_v is the specific entropy of water vapour (J kg^{-1} K^{-1}),

q_v is the air specific humidity (kg kg^{-1}),

e is the partial pressure of water vapour (Pa),

e_0=611 Pa is the reference partial pressure of water vapour,

C_p^v=1869.46 J kg^{-1} K^{-1} is the specific heat of water vapour at constant pressure,

R_v=461.51 J kg^{-1} K^{-1} is the gas constant for water vapour,

L_i^v=2834170.5 J kg^{-1} is the specific latent heat for ice-vapour phase transition.

The total entropy flux between atmosphere and soil surface ($\Phi_{S\ surf}$) determined in this way has to be assigned to each component of the complex soil surface in order to define the boundary condition for each type of surface. As introduced in section 2.1, the surface can either be composed of soil partially covered by low vegetation, or by snow, which, in turn, may be "thick" or "shallow". From the point of view of entropy (energy) exchange, low vegetation behaves as a "transparent" layer, i.e. it does not have an own temperature and it is part of the soil surface thus it does not have its own entropy flux. Thus, two cases may be realised.

The first case is realised when snow cover is absent or shallow. In this case all the components of the flux fully impinge on the soil surface with low vegetation and snow surface does not receive any flux:

$$\Phi_{S\ surf}^{soil} = \Phi_{S\ surf},$$

$$\Phi_{S\,surf}^{snow} = 0.$$

285 The second case is realised when snow layer is present and thick. In this case all the entropy flux impinges on the snow surface and the soil surface does not receive any direct flux:

$$\Phi_{S\,surf}^{soil} = 0,$$

$$\Phi_{S\,surf}^{snow} = \Phi_{S\,surf}.$$

2.8 Water vapour flux between soil and atmosphere

290 The flux of water vapour originating by means of turbulent exchange between surface and atmosphere is defined as:

$$\Phi_v^{turb} = K_v^{turb} \cdot \rho_{a\,surf} \cdot \frac{q_{v\,surf} - q_{v\,atm}}{z_{atm}}, \tag{31}$$

where $\Phi_v{}^{turb}$ is the flux of water vapour in the atmosphere surface layer (kg m^{-2} s^{-1}).

This summary flux has to be split between the components of the soil surface.

In the absence of snow cover, the water vapour exchange takes place between atmosphere and soil surface covered by (partly

295 wet) vegetation. Two cases can be distinguished: in the first case the flux is positive (i.e. downwards) thus condensation (deposition) of water vapour on the surface takes place; in the second case the flux is negative (i.e. upwards) thus evaporation (sublimation) from the surface takes place.

When the flux is directed downwards, it partly impinges on the bare soil surface and partly on the vegetation, where it contributes to the formation of dew over the leaves up to a maximum pre-specified value of water content as in the formulas:

300
$$\Phi_{v\,soil}^{turb} = \Phi_v^{turb} \cdot \left(1 - F_{veg}\right), \tag{32}$$

$$\Phi_{v\,veg\,dry}^{turb} = 0, \tag{33}$$

$$\Phi_{v\,veg\,wet}^{turb} = min\left\{\Phi_v^{turb} \cdot F_{veg}, \frac{q_{w\,veg}^{max} - q_{w\,veg}}{\Delta t}\right\}, \tag{34}$$

where:

$\Phi_v{}^{turb}{}_{soil}$ is the flux of water vapour in the atmospheric surface layer towards bare soil (kg m^{-2} s^{-1}),
$\Phi_v{}^{turb}{}_{veg\,dry}$ and $\Phi_v{}^{turb}{}_{veg\,wet}$ are the fluxes of water vapour in the atmospheric surface layer towards not moistened and moistened vegetation (kg m^{-2} s^{-1}),
$q_{w\,veg}$ and $q_{w\,veg}{}^{max}$ are the water contents of plant leaves and its maximum value (kg m^{-2}) respectively,
Δt is the model time step (s).

305 When the flux is directed upwards, it removes water partly from the bare soil surface, partly from the soil through plant evapotranspiration and partly through evaporation of water on the leaves. When conditions for evapotranspiration are not met the corresponding flux is zero (see description of vegetation scheme), while evaporation from leaves obviously takes place as long as there is water available on leaves surface, as in the following formulas:

$$\Phi_{v\,veg\,dry}^{turb} = \begin{cases} \Phi_{v\,surf}^{turb} \cdot F_{veg}^{dry}, \text{if evapotranspiration possible} \\ 0, \text{if evapotranspiration not possible} \end{cases}, \tag{35}$$

$$\Phi_{v\,veg\,wet}^{turb} = max\left\{\Phi_v^{turb} \cdot F_{veg}^{wet}, \frac{-q_{w\,veg}}{\Delta t}\right\}, \tag{36}$$

$$\Phi_{v\,soil}^{turb} = \Phi_v^{turb} - \Phi_{v\,veg\,dry}^{turb} - \Phi_{v\,veg\,wet}^{turb}. \tag{37}$$

In the presence of snow cover, the water vapour fluxes between atmosphere and bare soil/vegetation are null and the interaction takes place only between atmosphere and snow layer:

$$\Phi_{v\,snow}^{turb} = \Phi_v^{turb}, \tag{38}$$

where $\Phi_{v\,snow}^{turb}$ is the flux of water vapour in the atmosphere surface layer towards snow layer (kg m^{-2} s^{-1}).

2.9 Atmospheric precipitation flux at the surface

Atmospheric precipitation flux over surface, divided into liquid (Φ_w^{liq}) and solid (Φ_w^{ice}), is provided by the atmospheric model. The distribution of these fluxes over the soil surface depends on the presence of snow over it.

In absence of snow cover, liquid precipitation contributes to the surface components, including leaves, according to the fraction of each component; the amount of water on leaves exceeding the maximum allowable is immediately redistributed among the bare soil components:

$$\Phi_{w\,veg}^{liq} = min\left\{\Phi_w^{liq} \cdot F_{veg}, \frac{q_{w\,veg}^{max}-q_{w\,veg}}{\Delta t}\right\}, \tag{39}$$

$$\Phi_{w\,soil}^{liq} = \Phi_w^{liq} - \Phi_{w\,veg}^{liq}, \tag{40}$$

$$\Phi_{w\,snow}^{liq} = 0, \tag{41}$$

where Φ_w^{liq}, $\Phi_{w\,soil}^{liq}$, $\Phi_{w\,veg}^{liq}$, $\Phi_{w\,snow}^{liq}$ are the fluxes of atmospheric precipitation in liquid phase on the whole surface, on the soil surface, on vegetation and on the snow-covered surface respectively (kg m^{-2} s^{-1}).

In presence of snow cover, all the liquid precipitation flux is directed to the snow layer:

$$\Phi_{w\,soil}^{liq} = \Phi_{w\,veg}^{liq} = 0, \tag{42}$$

$$\Phi_{w\,snow}^{liq} = \Phi_w^{liq}. \tag{43}$$

Conversely, solid precipitation flux is always directed to snow layer, creating it if it does not exist:

$$\Phi_{w\,snow}^{ice} = \Phi_w^{ice}, \tag{44}$$

$$\Phi_{w\,soil}^{ice} = \Phi_{w\,veg}^{ice} = 0. \tag{45}$$

where Φ_w^{ice}, $\Phi_{w\,snow}^{ice}$, $\Phi_{w\,soil}^{ice}$, $\Phi_{w\,veg}^{ice}$ are the fluxes of atmospheric precipitation in solid phase on the whole surface, on the snow-covered surface, on the snow-free soil surface and on vegetation respectively (kg m^{-2} s^{-1}).

The surface processes scheme defines the conditions on the upper layer of the soil column in absence of snow cover or on the snow column in presence of snow. The boundary conditions are given by fluxes of entropy and water which can consist of water vapour and precipitation. The soil scheme can also define the air temperature and humidity over a composite surface.

3 Scheme of vegetation processes

In the vegetation scheme two processes are represented: evapotranspiration and interception of water by plant leaves.

Considering evapotranspiration process, we recall that in the previous section the water vapour flux between soil surface and the lowest atmospheric model was defined taking into account evapotranspiration of plants ($\Phi_{v\,veg\,dry}^{turb}$, 33, 35). In this section

the conditions under which evapotranspiration can take place are defined, as well as the change in soil wetness due to evapotranspiration.

Evapotranspiration is possible when the following conditions are fulfilled:

340
1. in each level of the plant root zone the temperature is above 0°C;
2. the air saturation specific humidity at surface temperature is higher than the actual air specific humidity at the lowest atmospheric layer, i.e. the water vapour flux can be directed upwards;
3. leaves are present, i.e. Leaf Area Index (LAI) is nonzero;
4. photosynthesis is possible, i.e. the incoming visible radiation flux is positive.

345 The water vapor flux due to evapotranspiration from leaf surface not covered by water ($\Phi_v{}^{turb}{}_{veg\,dry}$, see paragraph 2.7) removes water from the root zone of soil and each layer of this zone loses water proportionally to its contribution to evapotranspiration flux. In paragraph 2.3 it was shown how to determine air humidity over a vegetation surface not covered by water depending on the evapotranspiration rate (6) and the scheme of vertical space discretisation in soil was presented (fig. 2).

Consequently, the contribution of each root-zone level to the overall water flux due to evapotranspiration becomes:

350
$$F_k = \frac{(z_{kh+1} - z_{kh}) \cdot F\left(q_k^{rel}\right)}{z_{root}} \tag{46}$$

and the wetness variation in each soil level due to evapotranspiration is:

$$q_k^{\Delta t} = q_k^0 + \Phi_{v\,veg\,dry}^{turb} \cdot F_k \cdot \frac{\Delta t}{\rho_w \cdot (z_{kh+1} - z_{kh})}, \tag{47}$$

where ρ_w is the liquid water density (kg m^{-3}).

Considering, on the other hand, interception by vegetation leaves, the water content over low-vegetation leaves is determined

355 by the turbulent flux of water vapor between the leaves and the lowest atmospheric level ($\Phi_v{}^{turb}{}_{veg\,wet}$), thanks to which either evaporation (sublimation) or condensation (deposition) can take place, as well as by atmospheric liquid precipitation flux over vegetation surface ($\Phi_w{}^{liq}{}_{veg}$). Thus the prognostic equation for the water deposited over leaves looks like:

$$q_{w\,veg}^{\Delta t} = max\{min[q_{w\,veg}^0 + \left(\Phi_{v\,veg\,wet}^{turb} + \Phi_{w\,veg}^{liq}\right) \cdot \Delta t, q_{w\,veg}^{max}], 0\}, \tag{48}$$

where $q^{\Delta t}{}_{w\,veg}$ and $q^0{}_{w\,veg}$ are the water contents on plant leaves at the beginning and at the end of the time step (kg m^{-2}), while

360 the other variables were defined at paragraphs 2.7 and 2.8.

The water intercepted by vegetation leaves can cover the leaves either partially or completely, as mentioned in paragraph 2.1, where the concept of leaf fraction covered by water ($F_{veg}{}^{leaf\,wet}$) was introduced. This fraction is determined by the diagnostic relation:

$$F_{leaf\,wet}^{veg} = \left(\frac{q_{w\,veg}}{q_{w\,veg}^{max}}\right)^{2/3}, \tag{49}$$

365 where the exponent 2/3 is needed to evaluate the cross-section ratio from the volume ratio for a spherical drop.

The vegetation scheme thus defines the variation of water content in the root zone due to evapotranspiration and to water intercepted by leaves and provides a diagnostic relation for the leaf fraction covered by water.

4. Scheme of water exchange processes in the soil

370   The main equation describing dynamics of liquid water along the soil profile is the Darcy's law:

$$\Phi_f = \frac{-\Omega}{\mu}\nabla P, \tag{50}$$

where Φ_f is the fluid flux (m s^{-1}), ∇P is pressure gradient (Pa m^{-1}), μ is the fluid viscosity (Pa s), Ω is the section area (m^2).

When applied to the transport of water in soil, Darcy's law takes the form:

$$W_s\frac{\partial \Psi}{\partial t} = K\nabla^2\Psi - G, \tag{51}$$

375   where Ψ is the hydraulic head or hydraulic potential (m), W_s is the ratio of drained water volume at saturation to the total material volume (m^{3}m^{-3}) or maximum specific volumetric water content , K is the hydraulic conductivity (m s^{-1}), G represents the water source terms (m^{3}m^{-3}s^{-1}), t is time (s).

Assuming the absence of water sources, in the hypothesis of constant K and considering only the vertical coordinate, the equation can be written as:

380
$$W_s\frac{\partial \Psi}{\partial t} = K\frac{\partial^2\Psi}{\partial z^2}. \tag{52}$$

In the usual "soil notation" this equation is written as:

$$q_{max}\frac{\partial \Psi}{\partial t} = \frac{\partial\left(\frac{\Phi_w}{\rho_w}\right)}{\partial z}, \tag{53}$$

where $\frac{\Phi_w}{\rho_w} = K\frac{\partial \Psi}{\partial z}$, Φ_w is the soil water flux (kg m^{-2} s^{-1}), q_{max} is the maximum specific volumetric water content (m^{3}m^{-3}), i.e. in the case when all the soil pores are filled with water; this parameter depends on the soil texture and changes along the profile

385   depending on soil horizon.

The equation introduced here operates on soil hydraulic potential, while the main prognostic quantity for soil moisture is q, i.e. the specific volumetric moisture content (m^{3}m^{-3}), so it is necessary to express Ψ in terms of q.

Using the method of Clapp and Hornberger (1978) and introducing the concept of partially frozen soil moisture, the hydraulic potential can be represented as:

390
$$\Psi = \Psi_g\left(\frac{q_{max}}{q\left(1-f_{ice}^{soil}\right)}\right)^b, \tag{54}$$

where Ψ_g is the hydraulic potential of saturated soil (i.e. when $q=q_{max}$), b is an empirical parameter named "soil exponent", both these parameters depend on soil texture and can change along the soil profile depending on soil horizon, f_{ice}^{soil} is the fraction of frozen water with respect to total soil water. It can be noticed that formula (54) is valid only when $f_{ice}^{soil}<1$ since in case of total freezing of water in soil the hydraulic potential tends to infinity and no moisture motion can take place.

395   An important component of (53) is the hydraulic conductivity of soil which depends on its physical properties and on soil water content itself. Using again the Clapp and Hornberger (1978) method and extending it to the case of partly frozen soil moisture, the dependence of hydraulic conductivity on water content takes the form:

$$K = K_g \left(\frac{q - f_{ice}^{soil} q}{q_{max} - f_{ice}^{soil} q} \right)^{2b+3}, \tag{55}$$

where K_g is the hydraulic conductivity of saturated soil (when $q=q_{max}$), also depending on soil texture.

400   By substituting equation (54) into equation (53) under the assumption that the fraction of frozen water does not change during the process, i.e. $\partial f_{ice}^{soil} / \partial t = 0$, a prognostic equation for q is obtained, describing the motion of moisture along the soil profile:

$$\frac{\partial q}{\partial t} = \frac{\frac{\partial \left(\frac{\Phi_w}{\rho_w} \right)}{\partial z}}{-\frac{q_{max}}{q} \cdot \Psi_g \cdot b \cdot \left(\frac{q_{max}}{q \left(1 - f_{ice}^{soil} \right)} \right)^b}. \tag{56}$$

In a finite difference representation, (see fig. 2), applying an explicit approximation of the moisture flux terms and of the space derivatives, equation (56) takes the form:

405
$$\frac{q_k^{\Delta t} - q_k^0}{\Delta t} = \frac{\frac{\Phi_{w\,kh+1}^0}{\rho_w} - \frac{\Phi_{w\,kh}^0}{\rho_w}}{z_{kh+1} - z_{kh}} \cdot \frac{1}{-\left(\frac{q_{max}}{q_k^0} \right) \cdot \Psi_g \cdot b \cdot \left(\frac{q_{max}}{q_k^0 \left(1 - f_{ice\,k}^{soil\,0} \right)} \right)^b}, \tag{57}$$

$$\frac{\Phi_{w\,kh}^0}{\rho_w} = K_{kh} \cdot \frac{\Psi_k^0 - \Psi_{k-1}^0}{z_k - z_{k-1}}, \tag{58}$$

where the upper indexes 0 and Δt indicate the variables at the beginning and at the end of the time step respectively, while the lower indexes k and kh indicate the values of variables taken at full and half vertical levels respectively (fig. 2).

The values of the variables at half levels are computed as arithmetical means $x_{kh}=1/2(x_{k-1}+x_k)$.

410   In the case when a soil layer is completely frozen, $f_{ice}^{soil}=1$, the hydraulic potential tends to infinity, so the moisture flux is simply set to 0, i.e. if $f_{ice}^{soil}=1$ or $f_{ice\,k-1}=1$, then $\Phi_{wkh}^0=0$.

5 Scheme of thermal exchange processes in the soil

As stated in section 2, the quantity describing the thermal state of the environment in the present model has been chosen to be the entropy. The use of this quantity allows to describe phase changes of water in soil in a simple mathematical form, while it

415   does not significantly differ from other thermodynamical quantities in the description of thermal exchange. In the present model two main approximations are applied in the numerical solution scheme. The first is the application of the splitting method for solving the prognostic equation for entropy, i.e. the equation for the conductive transport of entropy is solved separately from the equation for entropy conservation in moist soil in case of phase change of soil water. The second approximation consists in neglecting the entropy due to water fluxes in the equation for the conductive transport of entropy.

420   These approximations are applied on the base of the experience in numerically solving the given problem. Due to the application of different space and time approximations, problems generated by small numerical inaccuracies (differences of big numbers) appeared, leading to an unacceptable instability and unphysical solution in particular situations. The aforementioned approximations mitigated these instabilities.

Starting from the first part of the problem, i.e. the conductive transport of entropy in humid soil. This process is described by the diffusion equation in the form:

$$\frac{\partial S_{soil}}{\partial t} = \frac{\partial \Phi_{S\,soil}}{\partial z}, \tag{59}$$

where S_{soi} is the soil entropy (J K^{-1} m^{-3}), $\Phi_{S\,soil}$ is the soil entropy flux (J K^{-1} m^{-2} s^{-1}).

The entropy of humid soil is a function of the specific entropy:

$$S_{soil} = \rho_{soil} S_{soil}^{spec}, \tag{60}$$

$$S_{soil}^{spec} = C_{soil} ln\left(\frac{T}{T_0}\right), \tag{61}$$

where S_{soil}^{spec} is the specific entropy of humid soil (J kg^{-1} K^{-1}), ρ_{soil} is the density of humid soil (kg m^{-3}), C_{soil} is the specific heat capacity of humid soil (J kg^{-1} K^{-1}) , T is the soil temperature (K).

The conductive flux of entropy is defined as:

$$\Phi_{S\,soil} = \frac{\lambda_{soil}}{C_{soil}} \frac{\partial S_{soil}^{spec}}{\partial z}, \tag{62}$$

where λ_{soil} is the heat conductivity of humid soil (J s^{-1} m^{-1} K^{-1}).

From the thermodynamical point of view, humid soil includes two components: dry soil, which does not undergo phase changes, and water, which undergoes phase changes and can be represented as a mixture of water and ice (the gaseous phase of water in soil is neglected). For this reason, the following assumptions are made in relation to the parameters of humid soil:

$$\rho_{soil} = \rho_{soil}^{dry} + q\left((1 - f_{ice}^{soil})\rho_w + f_{ice}^{soil}\rho_i\right), \tag{63}$$

$$C_{soil} = C_{soil}^{dry} + q\left((1 - f_{ice}^{soil})C_w + f_{ice}^{soil}C_i\right), \tag{64}$$

where ρ_{soil}^{dry} is the density of dry soil (kg m^{-3}), C_{soil}^{dry} is the specific heat capacity of dry soil (J kg^{-1} K^{-1}), both quantities depending on the soil characteristics (texture) and varying along the vertical, ρ_w and ρ_i are density of liquid water (1000 kg m^{-3}) and ice (900 kg m^{-3}), C_w and C_i are specific heat capacity of liquid water (4186.8 J kg^{-1} K^{-1}) and ice (2093.4 J kg^{-1} K^{-1}), q is the soil specific volumetric water content (m^3 m^{-3}) and f_{ice}^{soil} is the fraction of frozen water in total soil water, introduced in previous chapters.

Defining the value of the specific heat conductivity of moist soil is by itself a non-obvious problem. The main factor influencing this quantity is the moisture content of the soil. Different approaches for defining soil heat conductivity depending on its moisture content are known in literature, for example through hydraulic potential (Pielke, 2013) or through relative water content and heat conductivity of dry and saturated soil (Peters-Lidard et al., 1998, Best at al., 2011). In the present work a different approach is proposed. i.e. by means of relative water content and soil density:

$$\lambda_{soil} = min\left\{min\left[\frac{\rho_{soil}^{dry}}{1000} \cdot \sqrt{q^{rel}} + 0.3 \cdot \frac{\rho_{soil}^{dry}}{1000}, 3.0\right] + q \cdot f_{ice}^{soil} \cdot \lambda_i, 3.0\right\}, \tag{65}$$

where q^{rel} is the soil relative water content, as in (13) and λ_i is the heat conductivity of ice (2.0 J s^{-1} m^{-1} K^{-1}).

The proposed definition and the proposed values for the coefficients were formulated during the numerical experiments and verification of air temperature shown in section 9. The definition of this quantity significantly influences near-surface

temperatures, especially daily minimum and maximum values and amplitude of diurnal cycle, in the cases of stable boundary layer. The experiments showed that the given formula is suitable for different types of soil encountered in the territories of Europe and Western Asia.

Considering now the second part of the problem, i.e. the conservation of entropy of soil moisture in case of phase change, the quantity which has to be conserved is the sum of liquid water and ice entropy:

$$S_{soil}^{water} = \rho_w q \left(1 - f_{ice}^{soil}\right)\left(C_w ln\frac{T}{T_0} + \frac{L_i^w}{T_0}\right) + \rho_i q f_{ice}^{soil} C_i ln\frac{T}{T_0}, \tag{66}$$

where S_{soil}^{water} is the entropy of soil water (J K^{-1} m^{-3}), L_i^w is the specific latent heat of ice-water phase change (333560.5 J kg^{-1}).

In the equation for the conductive transport of entropy the phase changes of water are not considered, i.e. the fraction of ice in total soil water (f_{ice}^{soil}) is assumed to be known and the only unknown is the temperature. In the equation describing the phase changes of soil water (66) two unknowns are present, temperature and fraction of ice in soil water, so that, in order to solve this equation an additional equation relating the two quantities has to be added. This equation is introduced on the base of the hypotheses that at temperatures over 0 ºC the fraction of ice is equal to zero, while at temperatures below a certain threshold (here -30 ºC is assumed) the water in liquid phase cannot exist thus the fraction is equal to one. Between these two threshold values the fraction of ice grows monotonically with decreasing temperature and the shape of growth is assumed to be an hyperbolic tangent:

$$f_{ice}^{soil} = -tanh[(T - T_0) \cdot a \cdot f_b], \tag{67}$$

where the empirical coefficient $a = \frac{-4}{-30}$ defines the thermodynamic regime and does not depend on the soil characteristics, while the coefficient f_b depends on the soil characteristics and can assume values in the interval $1 \leq f_b \leq 2$:

$$f_b = 2 - \left\{\frac{min[max(b, 4), 12] - 4}{8}\right\}, \tag{68}$$

where b is the soil exponent already introduced in previous sections (about water exchange processes), the higher the value of b, the smoother the growth of the ice fraction with decreasing temperature.

The numerical solution of the split problem is now considered: the discretisation of the vertical coordinate is the one shown in section 2 (fig.2), while a time-explicit approximation of fluxes and of their derivatives, is used; the equation for conductive transport of entropy (59) thus becomes, in finite-difference form:

$$\frac{\rho_{soil}^k C_{soil}^k ln\frac{T_k^*}{T_0} - \rho_{soil}^k C_{soil}^k ln\frac{T_k^0}{T_0}}{\Delta t} = \frac{\frac{\lambda_{soil}^{kh+1} C_{soil}^{k+1} ln\frac{T_{k+1}^0}{T_0} - C_{soil}^k ln\frac{T_k^0}{T_0}}{C_{soil}^{kh+1}} \frac{\lambda_{soil}^{kh} C_{soil}^k ln\frac{T_k^0}{T_0} - C_{soil}^{k-1} ln\frac{T_{k-1}^0}{T_0}}{z_{k+1} - z_k} - \frac{\lambda_{soil}^{kh} C_{soil}^k ln\frac{T_k^0}{T_0} - C_{soil}^{k-1} ln\frac{T_{k-1}^0}{T_0}}{C_{soil}^{kh}} \frac{}{z_k - z_{k-1}}}{z_{kh+1} - z_{kh}}, \tag{69}$$

where indices k and kh indicate values on vertical full and half levels respectively, the upper indices ^{o} and * indicate values of temperature before and after the solution of the conductive transport equation respectively. The values of the physical parameters on half levels are computed as the arithmetical mean of the values on the full levels. In order to compute the density and the heat capacity of wet soil, the value of soil ice fraction computed at the beginning of the step is used.

485 The solution of (69) allows to compute the temperature T* taking into account the contribution of conductive heat flux but without taking into account any possible phase change.

After solving the first part of the split problem, the value of temperature T* obtained allows to compute the entropy of soil water, which is being considered its final value at the end of the time step:

$$S_{soil\ k}^{\Delta t} = \left\{ \rho_w q_k \left(1 - f_{ice\ k}^{soil\ 0}\right) \left(C_w ln \frac{T_k^*}{T_0} + \frac{L_i^w}{T_0} \right) + \rho_i q_k f_{ice\ k}^{soil\ 0} C_i ln \frac{T_k^*}{T_0} \right\} \cdot (z_{kh+1} - z_{kh}), \tag{70}$$

490 where q_k and $f_{ice\ k}^{soil\ 0}$ are the total moisture content and soil ice fraction on the level k, before taking into account the phase changes.

The value of soil water entropy obtained is then used for computing the temperature and ice fraction at the end of the time step, i.e. after considering the possible phase changes, by solving the equation system:

$$\begin{cases} \left[\rho_w q_k \left(1 - f_{ice\ k}^{soil\ \Delta t}(T_k^{\Delta t}) \right) \left(C_w ln \frac{T_k^{\Delta t}}{T_0} + \frac{L_i^w}{T_0} \right) + \rho_i q_k f_{ice\ k}^{soil\ \Delta t}(T_k^{\Delta t}) C_i ln \frac{T_k^{\Delta t}}{T_0} \right] \cdot (z_{kh+1} - z_{kh}) = S_{soil\ k}^{\Delta t}, \\ f_{ice}^{soil\ \Delta t} = -tanh[(T_k^{\Delta t} - T_0) \cdot a \cdot f_b] \end{cases} \tag{71}$$

495 where $T_k^{\Delta t}$ and $f_{ice\ k}^{soil\ \Delta t}$ are the values of temperature and ice fraction on level k at the end of the time step. The system (71) is solved by successive iterations, which is an effective method in this case since functions (66) and (68) are smooth and monotonous.

It has to be noted that, in the presence of a thin layer of snow over the soil surface, for which it is not convenient, from the point of view of numerical precision, to solve a separate equation for conductive transport and phase change, the entropy of 500 soil moisture on the upper soil layer is increased by the value of entropy of the thin snow layer (see next section for more details). The resulting temperature value is valid both for the soil surface and for the snow layer.

6 Snow scheme

The processes of formation, transformation and melting of snow over the soil surface are very important since they are connected with water phase changes, i.e. with a powerful energy source or sink, and with an important thermal insulating layer 505 between atmosphere and soil. In this work an original multi-layer scheme for the evolution of snow cover is proposed.

As it was shown in section 2, from the point of view of thermodynamic processes, the snow layer may either cover the entire surface or be completely absent. However, a concept of minimal snow thickness is introduced, above which the snow can be considered as a separate layer from the point of view of heat transport and phase changes. If the snow layer thickness is smaller than this minimum value, the snow is considered as an additional component of the soil surface (section 5). At the same time, 510 when considering water balance, i.e. processes related to atmospheric precipitation and water vapour condensation and sublimation, the snow layer thickness can be arbitrarily small, i.e. there is no minimum layer thickness.

The snow layer can be modeled as a porous ice mass which can contain water in the liquid phase, formed either by melting of the mass itself or because of liquid precipitation incoming. This liquid water, as soon as it appears, flows in the deepest layers of snow or in the soil. On the snow surface, sublimation from the solid ice phase takes place.

515   In the proposed model, as a vertical coordinate in the snow layer the snow mass per unit area (kg/m2) is used instead of the
       more common geometric length, thus the term "layer thickness" here refers to the amount of snow mass associated to a layer
       and not to its geometrical thickness. The vertical discretisation includes full and half levels, the topmost full level has index
       zero, index grows with growing depth and each half level is situated above the full level with the same index (fig. 3). With the
       use of this vertical coordinate each layer, except the topmost one, have the same, constant standard thickness. An increase or
520   decrease of total snow mass first changes the thickness of the top layer. If this thickness reaches or exceeds the standard
       thickness or becomes smaller than a minimum value, a layer is added or removed respectively. In these cases the values of
       snow temperature and melted water content are recomputed considering the newly appeared or disappeared level so that, in
       the whole snow column, the total snow entropy, the liquid water content and other diagnostic characteristics such as snow age
       and density are conserved. However, the amount of vertical snow levels cannot exceed a given value. When the snow cover
525   thickness is such that this amount of vertical levels is not enough, the standard layer thickness is increased (doubled) for that
       point and all the prognostic and diagnostic quantities are recomputed on the new set of levels with conservation of the vertical
       integral values. The opposite happens when, in case of snow mass reduction, the number of levels becomes too small, in that
       case the standard thickness is reduced (halved) up to the initial standard thickness. In this way the numerical scheme allows to
       represent a snow cover of arbitrary thickness, follow its thickening or thinning, while keeping the number of layers between
530   given limits.
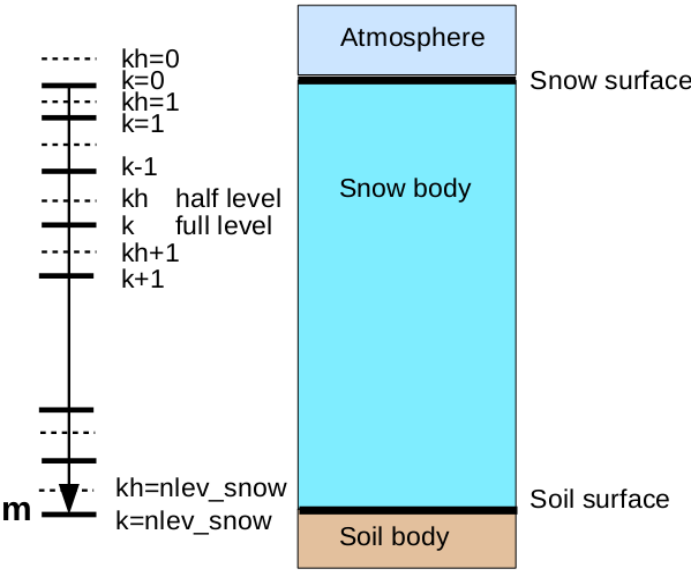
Figure 3. Scheme of the finite difference representation of the space coordinate in the snow layer.

6.1 Dynamics and balance of snow mass

The dynamics of the snow layer mass is determined by the variations of the two components of the snow layer: solid and liquid. The variations of the solid component take place in the top snow level in presence of solid precipitation or sublimation/deposition of water vapour, while the other levels do not contribute to this process. The variations of the liquid component take place in presence of liquid precipitation falling on the top snow level and in case of snow melting in any layer; in this case liquid water flows in the lower layers or in the soil. The general balance of snow mass is determined by the sum of the water fluxes (in all the phases) at the top and bottom layers.

The water mass flux at the top layer is described in section 2 (see equations 38 ($\Phi_v{}^{turb}{}_{snow}$), 41 and 43 ($\Phi_w{}^{liq}{}_{snow}$), 44 ($\Phi_w{}^{ice}{}_{snow}$)). At the bottom layer, the water mass flux is determined by the liquid water flux from the layer above. The process of water draining along the snow profile is described in the following way: all the liquid water that at the beginning of the time step is found at level k, at the end of the step is found at level k+1, this hypothesis is acceptable since empirical data show that even a very small liquid water draining speed is anyway higher than the values resulting from this hypothesis. The thickness of the snow layers is in the order of the centimeters and the time step is in the order of the minute, thus all the water can drain through a layer of any reasonable thickness in some seconds even with very low hydraulic conductivity valueof the order of 10^{-4} m/s. The liquid water flux at a half snow layer is thus:

$$\Phi_{m\ kh} = \frac{m_{k-1} \cdot (1 - f_{ice\ k-1}^{snow})}{\Delta t},$$
(72)

where Φ_m is the flux of liquid water at level kh (kg m-2 s-1), m_{k-1} is the specific (total) snow mass at level k-1 (kg m-2), $f_{ice}{}^{snow}_{k-1}$ is the fraction of ice phase in the total snow mass at level k-1.

The water flux at the lowest snow half level is the water flux at the soil surface (see section 3).

6.2 Processes of heat conduction and water phase transition in the snow

As in the soil scheme, the main equation describing the thermodynamic state of the snow is the equation of entropy transport and conservation (see section 5). In the case of snow, for solving the entropy prognostic equation the splitting method is applied: first, the conductive entropy transport term is solved, then the entropy conservation in case of phase transition in the snow layer is solved.

Let us now consider the conductive transport. In mass coordinates, the equation has the following aspect:

$$\frac{\partial S_{snow}^{spec}}{\partial t} = \frac{\partial \Phi_{S\ snow}}{\partial m},$$
(73)

where S_{snow}^{spec} is the specific entropy of snow (J K-1 kg-1) and $\Phi_{S\ snow}$ is the snow entropy flux (J K-1 m-2 s-1).

In analogy with soil entropy (see equations 60, 61) the total specific entropy of snow layer, including the solid and liquid phases of water, is defined as:

$$S_{snow}^{spec} = C_{snow}^{\Sigma} ln \frac{T}{T_0},$$
(74)

where $C_{snow}{}^{\Sigma}$ is the total specific heat capacity of snow including ice and liquid water (J kg-1 K-1), which can be rewritten, by making use of the concept of fraction of solid phase with respect to total mass, in the following way:

$$C_{snow}^{\Sigma} = f_{ice}^{snow} C_i + (1 - f_{ice}^{snow}) C_w. \tag{75}$$

The flux of conductive entropy transport is defined as:

$$\Phi_{S\,snow} = \frac{\lambda_{snow}}{C_{snow}^{\Sigma}} \cdot \rho_{snow}^{\Sigma} \cdot \frac{\partial S_{snow}^{spec}}{\partial m}, \tag{76}$$

where λ_{snow} is the specific heat conductivity of snow (J s-1 m-1 K-1) and $\rho_{snow}{}^{\Sigma}$ is the total density of snow including ice and liquid water (kg m-3).

In this equation the density is not the density of the porous medium but it is a virtual density of the thermodynamically active medium, excluding the pore volume, defined as:

$$\rho_{snow}^{\Sigma} = f_{ice}^{snow} \rho_i + (1 - f_{ice}^{snow}) \rho_w. \tag{77}$$

At the same time, for the snow a density from the point of view of the porous medium is introduced, in order to define the characteristics of heat conductivity. This density is indicated with the symbol ρ_{snow}. This quantity is a diagnostic parameter defined at each snow layer, depending on the thickness of the snow layer, on the snow age at each layer and on the total period during which snow at every layer was subject to melting/freezing processes. The following method for determining diagnostic snow density is proposed in the present model:

$$\begin{aligned}
\rho_{snow} &= min[f_2 \cdot f_3, \rho_{firn}] \\
f_2 &= max\left\{ min\left[\left(\frac{\tau_{snow}^{melt}+30}{395}\right)^{0.3}, 1 \right] \cdot \rho_{firn}, f_1 \right\} \\
f_1 &= max\left\{ min\left[\left(\frac{\tau_{snow}}{365}\right)^{0.3}, 1 \right] \cdot \rho_{snow}^{old}, \rho_{snow}^{fresh} \right\}, \\
f_3 &= min\left[1 + 0.5 \left(\frac{m}{100}\right)^{0.5}, 1.5 \right]
\end{aligned} \tag{78}$$

where τ_{snow} and $\tau_{snow}{}^{melt}$ are total snow age and total period during which snow was subject to melting (days), ρ_{firn}, $\rho_{sno}{}^{fresh}$ and $\rho_{sno}{}^{old}$ are density of firn, of fresh snow and of old snow (kg m-3), m is the snow mass in the current layer according to the vertical coordinate used (kg m-2). When density is determined, a limitation is applied, according to which the density variation cannot exceed 10% per day.

The heat conductivity of snow was defined following the study of (Jin et al., 1999):

$$\lambda_{snow} = 2.45 \cdot 10^{-6} \cdot \rho_{snow}^2. \tag{79}$$

When equation (73) is solved, the snow temperature including effect of heat conduction is determined, while the solid fraction does not change and is considered known.

We consider now the solution of the second part of the problem, i.e. the conservation of snow entropy in case of phase transition. The following quantity, equal to the entropy of a particular snow layer including liquid and solid phases, should be conserved:

$$S_{snow} = \Delta m \cdot \left\{ f_{ice}^{snow} C_i ln \frac{T}{T_0} + (1 - f_{ice}^{snow}) \left(C_w ln \frac{T}{T_0} + \frac{L_l^w}{T_0} \right) \right\}, \tag{80}$$

where S_{snow} is the entropy of snow (J K-1 m-2) and Δm is the specific mass of a snow layer (kg m-2).

In order to numerically solve equation (73) a discretisation of the vertical coordinate as shown in fig. 3 is used, together with a time-explicit method of approximation of fluxes and of their derivatives. The following finite-difference prognostic equation is thus obtained:

$$\frac{C^{\Sigma}_{snow\,k}\ln\frac{T^*_k}{T_0}-C^{\Sigma}_{snow\,k}\ln\frac{T^0_k}{T_0}}{\Delta t} = \rho^{\Sigma}_{snow\,k}\cdot\frac{\frac{\lambda^{kh+1}_{snow}}{C^{\Sigma}_{snow\,kh+1}}\frac{C^{\Sigma}_{snow\,k+1}\ln\frac{T^0_{k+1}}{T_0}-C^{\Sigma}_{snow\,k}\ln\frac{T^0_k}{T_0}}{m_{k+1}-m_k}-\frac{\lambda^{kh}_{snow}}{C^{\Sigma}_{snow\,kh}}\frac{C^{\Sigma}_{snow\,k}\ln\frac{T^0_k}{T_0}-C^{\Sigma}_{snow\,k-1}\ln\frac{T^0_{k-1}}{T_0}}{m_k-m_{k-1}}}{m_{kh+1}-m_{kh}}, \qquad (81)$$

where the indexes k and k_h indicate respectively the values on the full and half vertical levels respectively, the upper indexes 0 and * indicate the values of temperature variables before and after the solution of the conductive heat transport equation respectively. The values of the physical parameters at half levels is computed as the arithmetic mean of the values at the surrounding full levels. In order to compute the overall virtual density (density used in thermodynamic contest) and heat capacity of snow, the value of solid fraction of snow layer at the beginning of the time step is used.

Solution of (81) allows to compute temperature T^* after taking in account the conductive heat transfer but without considering the phase transition.

After having solved the first part of the split problem which provided the value of temperature T^*, it is possible to define the value of snow entropy, which is considered the definitive value at the end of the time step. For determining entropy, the finite different discretisation of (80) is used:

$$S^{\Delta t}_{snow\,k} = \left\{f^{snow\,0}_{ice\,k}C_i\ln\frac{T^*_k}{T_0} + \left(1-f^{soil\,0}_{ice\,k}\right)\left(C_w\ln\frac{T^*_k}{T_0}+\frac{L^w_i}{T_0}\right)\right\}\cdot(m_{kh+1}-m_{kh}), \qquad (82)$$

where $f_{ice\,k}^{snow\,0}$ is the fraction of solid phase at level ^{k} before taking into account phase transitions.

Equation (82) includes two unknowns: temperature and fraction of solid phase. Unlike the case for soil moisture, it is assumed that in the snow layer the presence of water in liquid phase ($f_{ice}^{snow}<1$) is possible only at 0°C ($T=T_0$). This assumption simplifies the solution: either the initial temperature is T_0, then equation (82) has a single unknown, i.e. fraction of solid phase, or the initial temperature is below zero, then the only unknown is temperature which has to be below or equal zero Celsius. The temperature and fraction of solid phase determined in this way are considered definitive at the end of the time step.

As remarked in section 5, the solution of the thermodynamic state of snow layer is performed only when the amount of snow exceeds a given threshold in order to avoid numerical problems. If the snow specific mass is below the given threshold, its thermodynamic state is described by the solution of the entropy equation for the top soil level, whose entropy is augmented by the value of entropy for snow.

Solution of equation (82) allows to diagnose the length of the time interval during which snow is exposed to melting. The value of this interval is required for computing snow density.

In conclusion, the scheme of snow-layer processes defines the overall specific snow mass, the distribution of this mass in the vertical levels, and, at each level, the temperature, the fraction of solid phase, the snow age, the length of melting time-interval and the snow density.

7 Verification of «Pochva» scheme in NWP model Bolam in hindcast regime

The scheme "Pochva", described above, is developed for use in numerical atmosphere models as a parameterisation of heat and water exchange processes at the surface. However, it can be applied in column variant using observational data on energy and water fluxes at the surface. Such application allows for studies of soil physical parameters, as well as for testing the scheme itself. The results of such testing using observations of Coordinated Energy and Water Cycle Observation ProjectBaltic Sea Experiment (BALTEX) are presented in the appendix A.

The scheme "Pochva" is available as free and open source software and it has been coded in a way that makes it easily adaptable to any atmospheric model and is freely available. As input data, atmospheric variables at the lowest level are required, together with fluxes of precipitation, visible and infrared radiation, heat and humidity (or variables allowing to compute these fluxes). Besides these variables, quantities defining the physical characteristics of soil and vegetation are required. Soil characteristics are allowed to vary along the vertical direction as well. In "Pochva" the bottom boundary condition for temperature and soil moisture can be specified through a "climatological level", with a horizontally-varying depth, depending on the local climatological and hydrological conditions, at which the values of temperature and moisture content are considered constant. The description of the methods used for defining the physical parameters of soil and vegetation and the method for defining the climatological level may be the subject of a future publication. Here we just note that the space variability of soil physical parameters has been defined on the basis of FAO dataset (FAO Unesco, 1997), the vegetation types and corresponding physical parameters have been defined using the GLC2000 dataset (Joint Research Centre, 2003), while, for defining the climatological levels, the analysis of air temperature at 2 m above surface for the period 1979-2014 from ECMWF ERA Interim dataset together with the FAO soil type dataset have been used.

In order to test the implementation, the "Pochva" scheme has been included in the NWP model "Bolam" (Buzzi et al., 1994, Buzzi et al., 1998) and in its global variant "Globo" (Malguzzi et al., 2011). Bolam is a hydrostatic NWP model on a limited area. A numerical experiment in hindcast regime has been set up with Bolam, the experiment consisted in a continuous integration of the model on a long period using objective analysis data as boundary conditions during all the period. As initial and boundary conditions, data from the ECMWF IFS model have been used from the ECMWF operational archive. The model domain included most of European territory. The time extent of the experiment covered the period June 2013-November 2015, where the first six months were used to let the soil layer reach the thermodynamical equilibrium with the climatological bottom boundary conditions, thus they have not been considered in the analysis of the results. In this way the effective period includes two full years, from beginning of December 2013 to the end of November 2015. The length of two years was chosen in order to exclude the presence of interannual oscillations and trends in the simulations.

In order to verify the results, data from standard meteorological observations from WMO GTS network have been used, retrieved from ECMWF archive. The main purpose of the numerical experiment was to evaluate the contribution of the "Pochva" scheme to the numerical modelling results, thus the variables used in the verification process were air temperature and dew-point temperature at 2 m above surface.

The experiment showed that the main scores, such as mean error (bias) and root mean square error (RMSE), of near-surface temperature and humidity, stratified on monthly and seasonal intervals do not vary significantly among the two simulated years. This suggests that there is no significant trend due to error accumulation in the simulation. In the figures below, scores averaged on seasonal intervals based on the two simulated years are shown.

660 Figures 4 and 5 show seasonal averages of temperature bias and RMSE over observation points. As it can be seen from fig. 4, the bias obtained is relatively low, mostly between -1ºC and +1ºC. A higher error is noticed in the cold seasons (winter, autumn), when Central Europe experiences a bias values between -1ºC and -3ºC (up to -5ºC in mountainous areas) while at the east of Ural range the bias sign is opposite (+1ºC +2ºC). In the warm seasons, mainly in summer, a bias up to +5ºC is noticed in the desert or semi-arid areas of Eastern Mediterranean.

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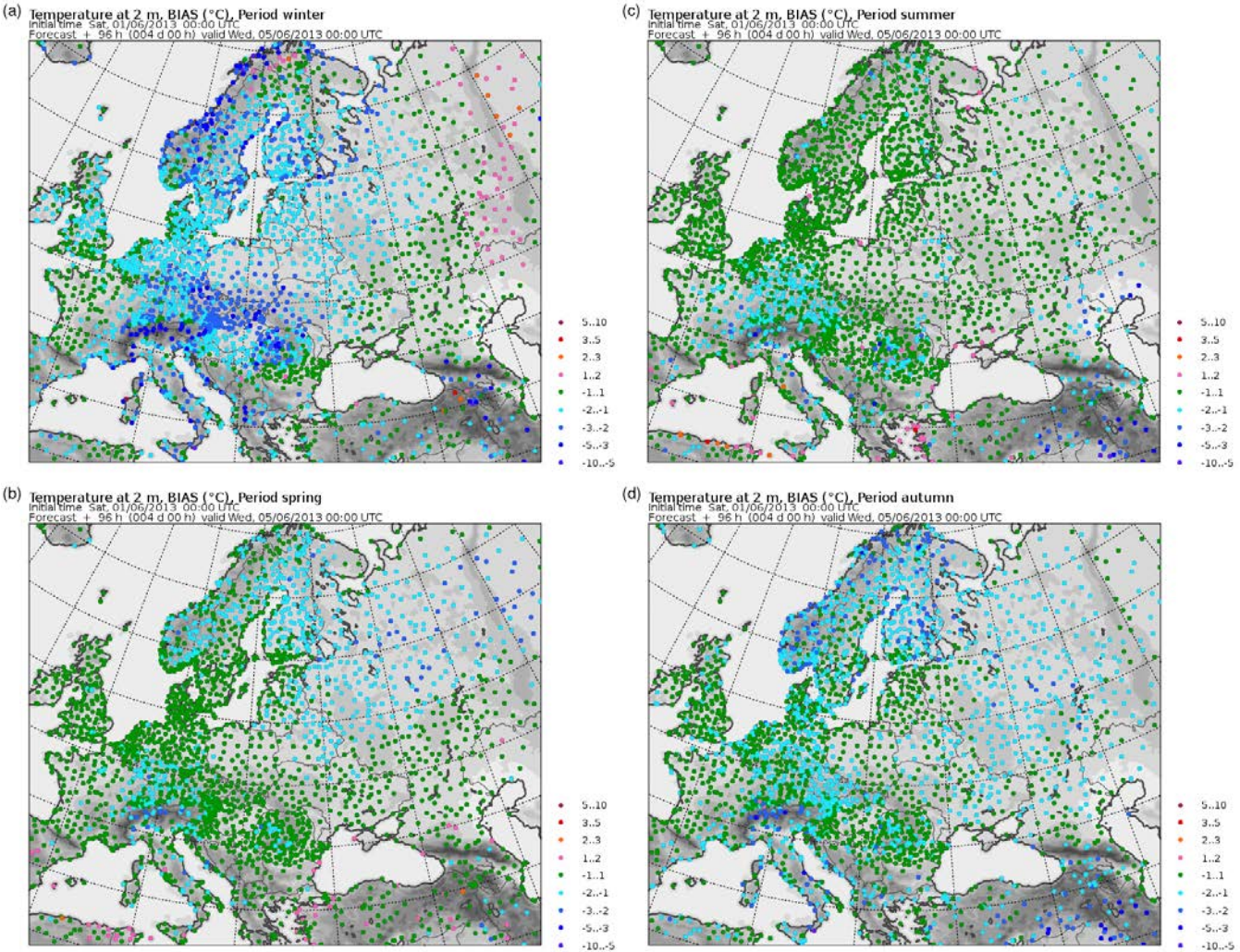
Figure 4. Seasonally averaged bias of temperature at 2 m above surface at observation points: (a) winter, (b) spring, (c) summer, (d) autumn.
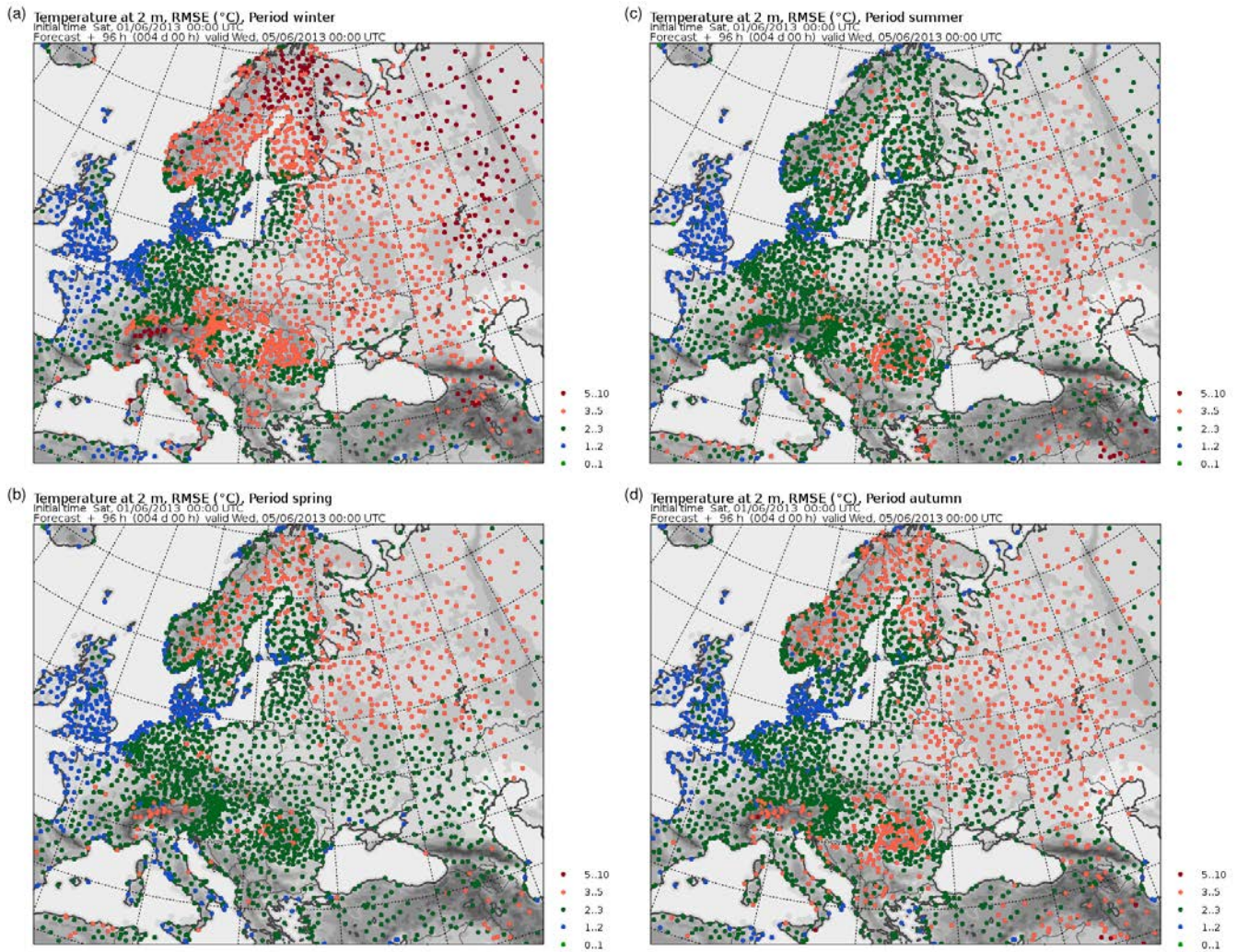
Figure. 5. Seasonally averaged RMSE of temperature at 2 m above surface at observation points: (a) winter, (b) spring, (c) summer, (d) autumn.

The RMSE shown in fig. 5 also shows that, on the background of an error with a magnitude of 2-3ºC, the error is higher in the colder seasons especially in mountain and continental areas, up to 5ºC. In general, coastal areas show lower RMSE, with values lower than 2ºC, growing up to 3-5ºC with growing distance from the sea.

It can be concluded that the overall near-surface atmospheric thermal regime is simulated with enough accuracy. The errors in the cold periods in continental and mountain areas can be explained by a poor simulation of the snow cover, which strongly influences the near-surface temperature, while high errors in desert areas during the warm periods can either be due to an error

in the soil surface temperature or in the inaccurate representation of surface turbulent exchange in cases of dry thermal instability.

Fig. 6 shows the seasonal dew-point temperature bias on observation points. In the cold seasons the systematic error is in the interval -1⁰C +2⁰C, while in the warm seasons the dew-point temperature (and thus air humidity) is overestimated in the continental areas, with a bias growing up to +3⁰C +5⁰C with increasing distance from the sea. Similar conclusions may be drawn from the analysis of seasonal RMSE, presented in fig. 7. In the coastal areas all year round and anywhere in the colder seasons, RMSE has low or moderate values, 1-3⁰C, while in the continental areas in the warm seasons it may grow up to 5⁰C and more. It can thus be noticed that most of the RMSE is explained by the bias. The overestimation of air humidity in the continental areas during warm seasons is difficult to explain. The absence of a corresponding systematic error for temperature suggests that it is not due to an overestimation of evaporation, since, if that was the case, temperature would have been underestimated. It can be proposed that this is due to inaccuracy in the definition of water vapor fluxes or of the humidity profile in the surface layer in the warm season, i.e. in cases of neutral or unstable stratification.
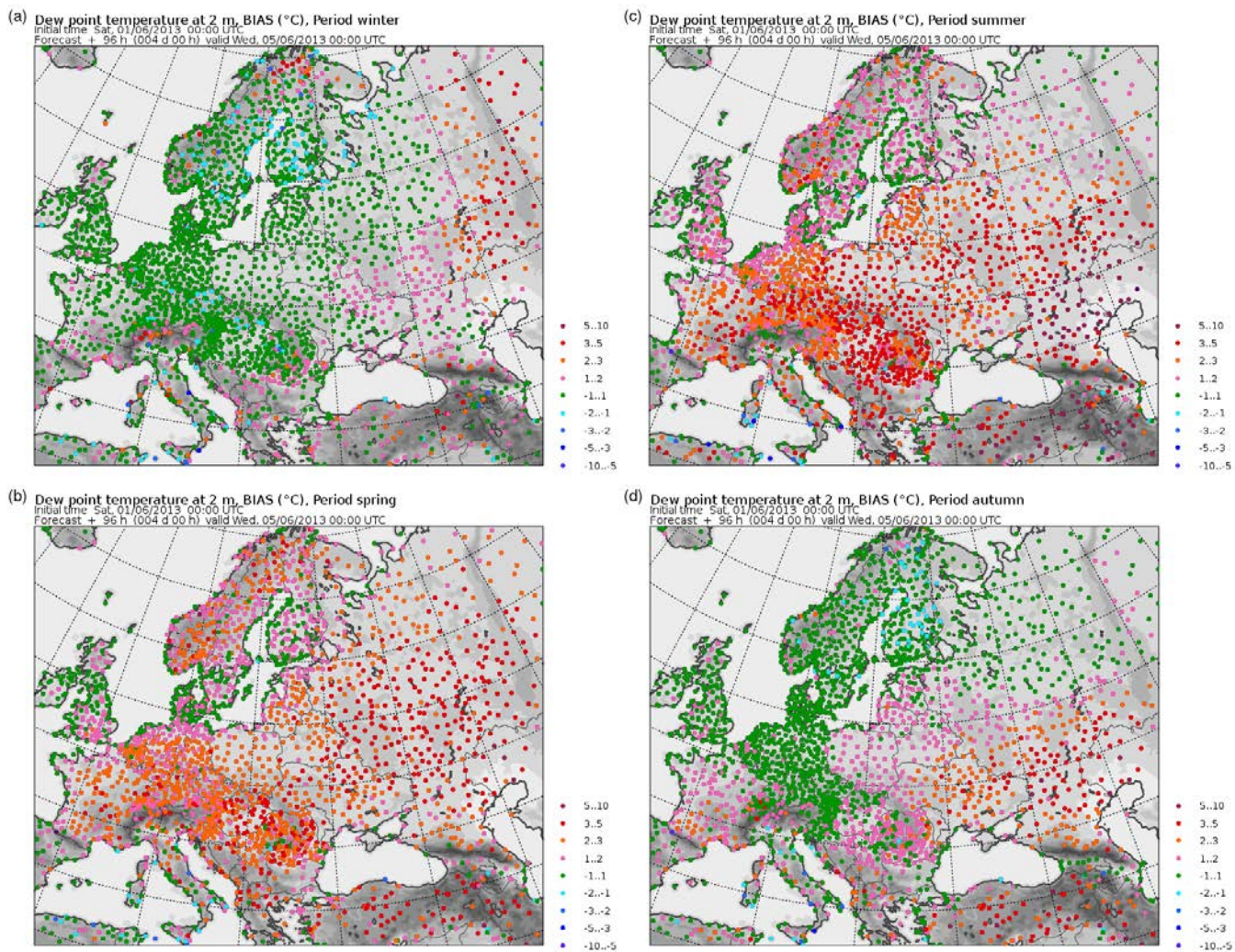
Figure 6. Seasonally averaged bias of dew-point temperature at 2 m above surface at observation points: (a) winter, (b) spring, (c) summer, (d) autumn
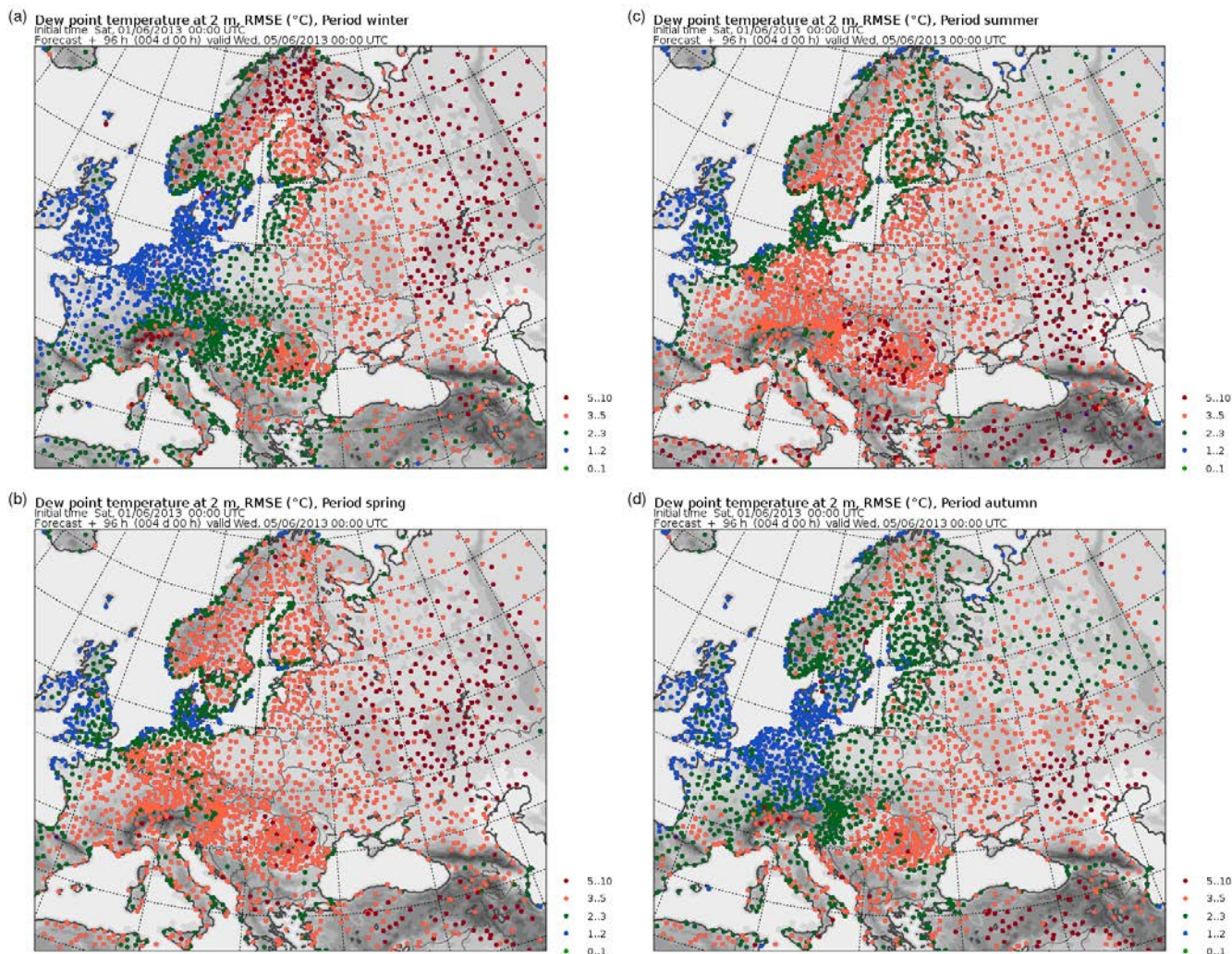
Figure 7. Seasonally averaged RMSE of dew-point temperature at 2 above surface at observation points: (a) winter, (b) spring, (c) summer, (d) autumn.

For a more detailed examination of the errors in near-surface air temperature and humidity from the point of view of the representation of daily cycle, the simulated and observed values for these variables at all the observation times, averaged on seasons and on specific geographical areas are here shown. Since the model domain covers areas with completely different meteorological and climatological characteristics, the geographical averaging has been carried out considering climatologically uniform areas. For this purpose, a dataset of the Köppen-Geiger climate classification has been used (Rubel and Kottek, 2010). Most of the observation points falls into six climatic areas according to the Köppen-Geiger classification, namely Bsk (cold steppe), Cfa (humid subtropical), Cfb (temperate oceanic), Csa (hot-summer Mediterranean), Dfb (warm-summer humid

705   continental), Dfc (subarctic), moreover the points on mountain areas (defined as having height >1000m above mean sea level) were treated separately. Fig. 8 shows the distribution of observation points by climatic zone.
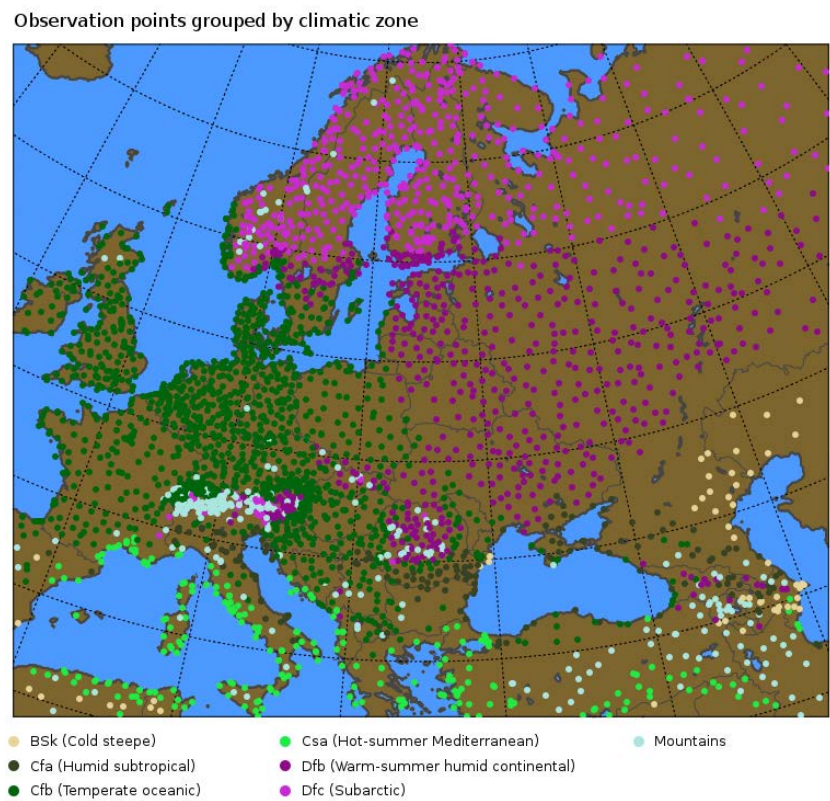
Figure 8. Distribution of observation points by climatic zone according to Köppen-Geiger classification.

710   For all the observation points falling in each of the seven main climatic zones, bias and RMSE of temperature and dew-point temperature at 2 m above surface have been computed at all the times of the day at which observations are available, namely 0, 3, 6, 9, 12, 15, 18, and 21 UTC. Below, the error obtained in the representation of daily cycle in each climatic zone will be examined.

     In winter period (fig. 9 and 10), the error does not depend on the time of the day in all the climatic zones except in the mountain

715   areas, where the error is higher during the day. In most of the climatic zones, the error is mostly due to bias, which is quite low, -1.3ºC -1ºC, while RMSE is in the range 1-4ºC, it is lower in the oceanic climate areas and it grows in areas with a continental climate. The zone with subarctic climate stands out from this picture, since it is characterised by low bias (-1.5ºC)and high RMSE (4.5-5ºC). At the same time, the mountains areas, characterised by a similar cols climate, show good scores. This suggests that there are some problems with surface albedo definition in subarctic area and further studies are

720   needed.
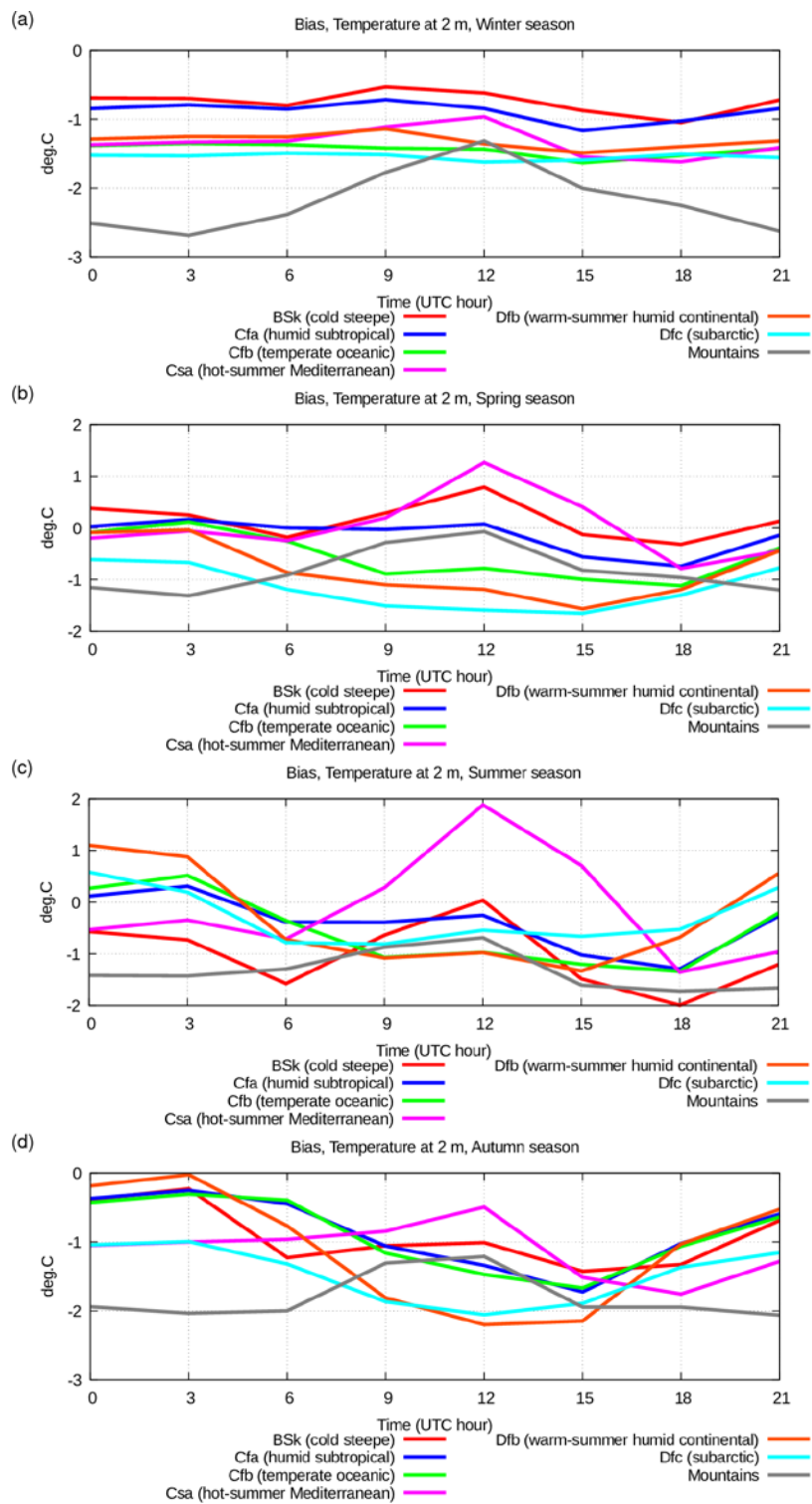
Figure 9. Diurnal cycle of bias of simulated temperature at 2 m above surface for various seasons: (a) winter, (b) spring, (c) summer, (d) autumn, in various climatic zones: cold steppe (Bsk) red line, humid subtropical (Cfa) blue line, temperate oceanic Cfb green line, hot-summer Mediterranean (Csa) violet line, warm-summer humid continental (Dfb) orange line, subarctic (Dfa) azure line, mountains grey line.

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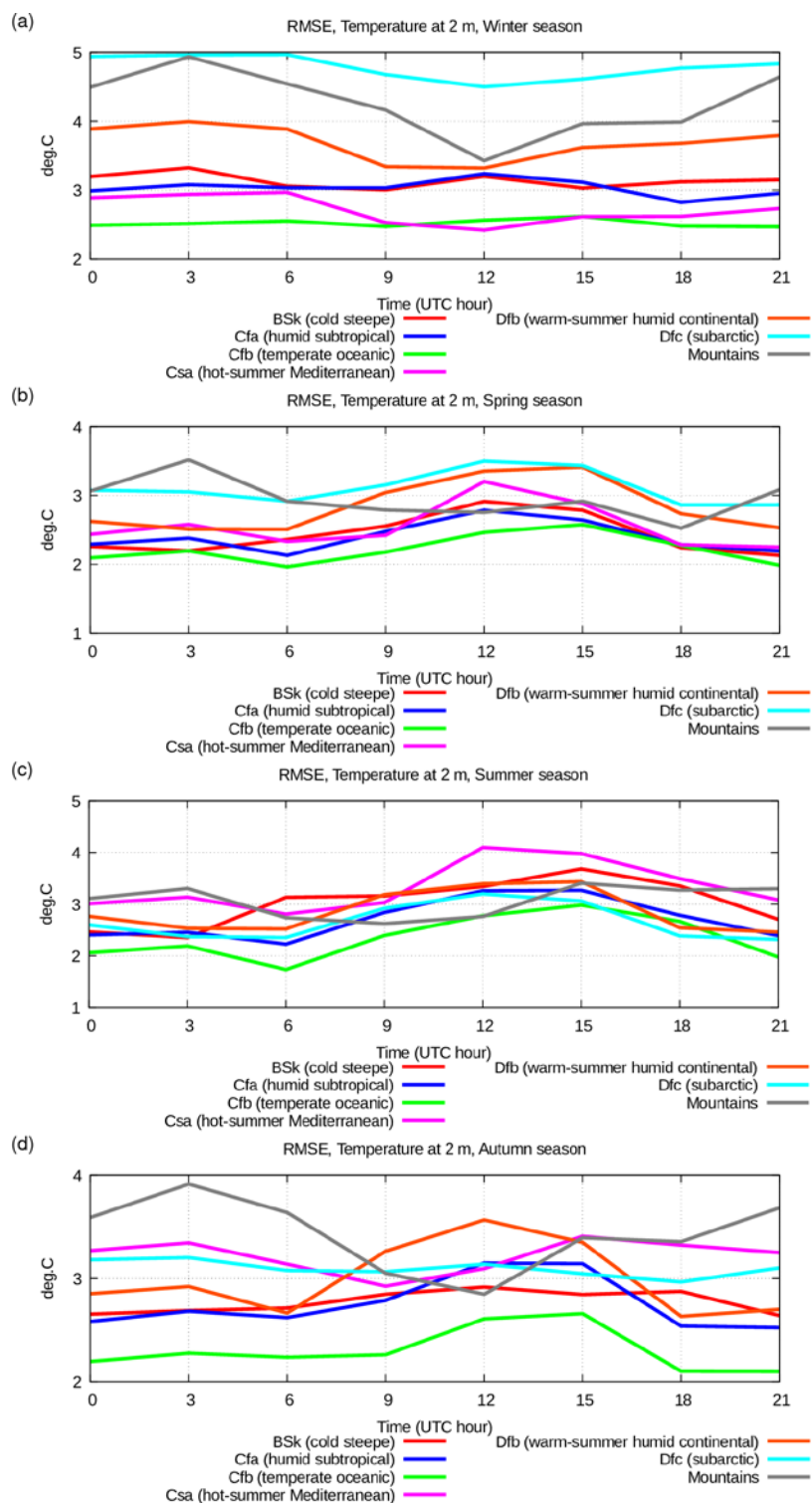
Figure 10. Same as figure 9 but for RMSE of simulated air temperature at 2 m above surface.

765   During the summer period (fig. 9 and 10), all the climatic zones are characterised by the fact that bias explains most of the RMSE (2-4ºC); bias is in the range -2ºC +2ºC and it is positive during daytime and negative in the evening and morning hours. This is particularly evident in the zones with dry climate, such as "hot summer Mediterranean" and "cold steppe". This could be possibly due to some problems in the representation of the surface sensible heat flux in the presence of an unstable surface layer, or in the surface latent heat flux, or due to the insufficient heat capacity of the higher soil layer which, in turn, could be

770   due to too low values of soil moisture. In areas with mountain and subarctic climate, the score is significantly better in summer than in winter. This is possibly due to deficiencies in the representation of snow cover or of the radiative characteristics of the snow cover itself.

In the spring and autumn periods, (fig. 9 and 10, panels b and d) the scores for 2m temperature have intermediate values between those for summer and winter. The overall errors are not high, the bias ranges between -1.5ºC and +1.5ºC, while RMSE

775   is around 2-4ºC. In spring the error characteristics are closer to the summer ones, while in autumn they are closer to the winter ones. It is probably the case that the processes of formation and melting of the snow layer in the areas with a stable winter snow cover (warm-summer humid continental, subarctic and mountains) are simulated more or less correctly, since no increase of the error is observed in these transitional seasons

Concerning the scores for humidity in terms of 2-m dew-point temperature figures 11 and 12 show the daily cycle of the bias

780   and RMSE for this variable.

In the winter period (fig. 11 and 12, panel a) all the climatic zones are characterised by a low systematic error (0ºC +2ºC) and a significant RMSE (2-5ºC) with a very weak daily cycle. In the same way as for temperature, the scores strongly depend on the climatic zone: better scores (RMSE up to 3ºC) are found in the area with oceanic climate (temperate oceanic, hot-summer Mediterranean, humid subtropical), while worst scores (RMSE higher than 4ºC) are found in zones with cold continental

785   climate (warm-summer humid continental, subarctic, mountains). This can be due to deficiencies in the definition of latent heat flux or air humidity profile over snow layer, i.e. in cases of stable surface layer.

In the summer period, on the other hand, most of the RMSE (2.5-8.5ºC) is explained by systematic error (0ºC +6ºC) which is always positive, i.e. the air humidity is systematically overestimated. In general, the minimum of daily error occurs ad daytime, while it is maximum in the evening and night. This may be due to a suboptimal tuning of the turbulent exchange

790   parameterisation in neutral and stable boundary layer conditions. In the areas characterised by oceanic climate or in cold climate areas (temperate oceanic, subarctic) the errors are lower, while in dry areas (cold steppe) they are higher. At the time of day when errors are higher, the overestimation of air humidity is accompanied by underestimation of air temperature. This may be an evidence of deficiencies in the computation of latent heat flux (evaporation).

In spring and autumn seasons (fig. 11 and 12, panels b, d) the dew point temperature scores, similarly to the case of

795   temperatures, have intermediate values between those found in winter and summer seasons. In general, the air humidity is almost always overestimated, in the warm season more than in the cold one

(a)

Bias, Dew point temperature at 2 m, Winter season

BSk (cold steepe)
Cfa (humid subtropical)
Cfb (temperate oceanic)
Csa (hot-summer Mediterranean)
Dfb (warm-summer humid continental)
Dfc (subarctic)
Mountains

(b)

Bias, Dew point temperature at 2 m, Spring season

BSk (cold steepe)
Cfa (humid subtropical)
Cfb (temperate oceanic)
Csa (hot-summer Mediterranean)
Dfb (warm-summer humid continental)
Dfc (subarctic)
Mountains

(c)

Bias, Dew point temperature at 2 m, Summer season

BSk (cold steepe)
Cfa (humid subtropical)
Cfb (temperate oceanic)
Csa (hot-summer Mediterranean)
Dfb (warm-summer humid continental)
Dfc (subarctic)
Mountains

(d)

Bias, Dew point temperature at 2 m, Autumn season

BSk (cold steepe)
Cfa (humid subtropical)
Cfb (temperate oceanic)
Csa (hot-summer Mediterranean)
Dfb (warm-summer humid continental)
Dfc (subarctic)
Mountains

Figure 11. Diurnal cycle of bias of simulated dew-point temperature at 2 m above surface for various seasons: (a) winter, (b) spring, (c) summer, (d) autumn, in various climatic zones: cold steppe (Bsk) red line, humid subtropical (Cfa) blue line, temperate oceanic Cfb green line, hot-summer Mediterranean (Csa) violet line, warm-summer humid continental (Dfb) orange line, subarctic (Dfa) azure line, mountains grey line.

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(a) RMSE, Dew point temperature at 2 m, Winter season

(b) RMSE, Dew point temperature at 2 m, Spring season

(c) RMSE, Dew point temperature at 2 m, Summer season

(d) RMSE, Dew point temperature at 2 m, Autumn season

BSk (cold steepe)
Cfa (humid subtropical)
Cfb (temperate oceanic)
Csa (hot-summer Mediterranean)
Dfb (warm-summer humid continental)
Dfc (subarctic)
Mountains
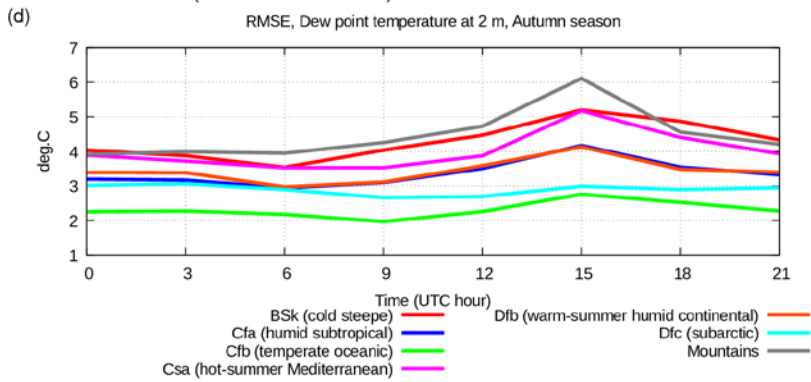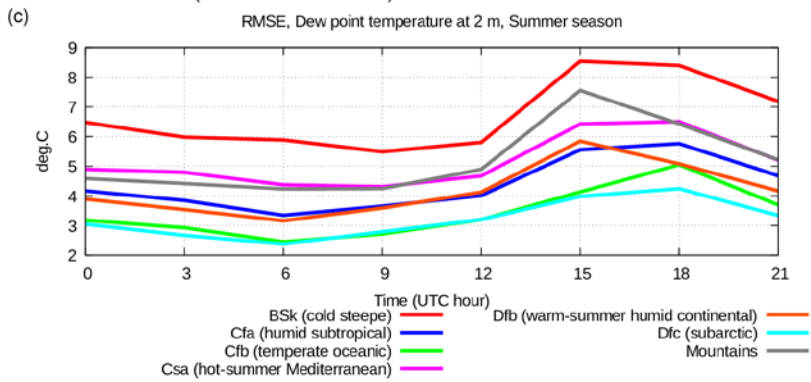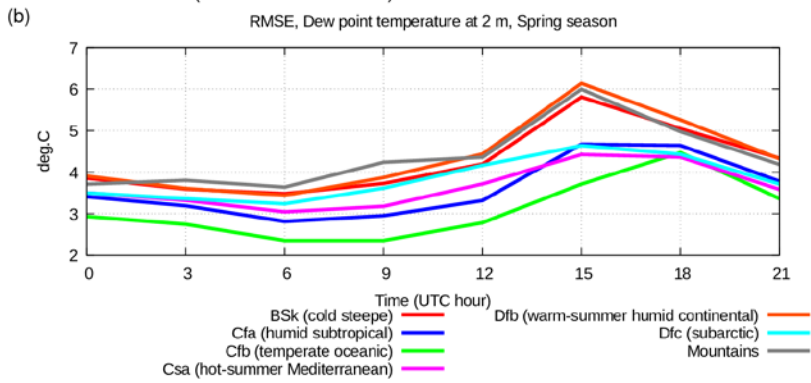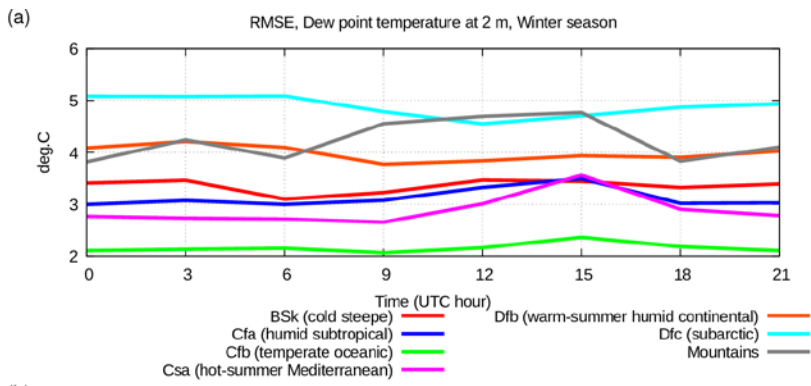
Figure 12. Same as figure 11 but for RMSE of simulated dew-point temperature at 2 m above surface.

The scores presented here show no evidence of systematic deficiencies in the near-surface temperature, with the exception of periods characterised by a stable snow cover, when temperature is systematically underestimated, or of summer periods in dry climatic zones when daytime temperature is overestimated. At the same time, near-surface air humidity is systematically overestimated, especially in summer time, and, in particular, in dry climatic areas at evening and night time.

As a general conclusion the results shown by the numerical experiments with the scheme "Pochva" are definitely convincing.

8 Summary

The model of hydro-thermal processes in vegetated soil and snow cover presented in this work is characterized by a special attention to soil-water phase transition, and by novel approaches to define some soil and snow physical parameters. The proposed model has been validated by a solid verification presented in this work consisting in a two year hindcast experiment. The presented model may be useful for modeling research over polar or cold climate zones, in permafrost evolution studies, in studies and forecast of snow cover, in studies of surface layer in stable conditions over cold surfaces. The model is realized using an effective and stable numerical algorithm with a clear, intuitive interface that allows a simple coupling to an atmospheric model or to observations of energy and water fluxes in the air surface layer and at the surface.

This land model has been included in the CNR-ISAC NWP models: Globo (hydrostatic approximation, global domain), Bolam, described above, and Moloch (non-hydrostatic, high space resolution at limited area). The indicated NWP models with "Pochva" are used from 2018 up to present day for the routine operational weather prediction in CNR-ISAC for Civil Protection Department of Italy. Forecast products are available at https://www.isac.cnr.it/dinamica/projects/forecasts/ and results of forecast verification are available at https://www.isac.cnr.it/dinamica/projects/forecast_verif.

Code availability

The model code in stand alone version for column test simulations is available from the project website https://gitlab.com/oxana-meteo/pochva-stand-alone under the GNU GPL licence. The version of the model used to produce the results used in this paper (v1.1) is archived on Zenodo (Drofa, 2024), this package includes the instructions for use and input/output data format description in readme.txt file.

The package of CNR-ISAC models, including "Pochva" scheme is open source code freely available at https://gitlab.com/isac-meteo/globo-bolam-moloch.

Competing interest

The authors declare that they have no conflict of interest.

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835 The author would like to thank Dmitriy Pressman (Hydrometeorological Research Center of the Russian Federation) for her knowledge gained in the field of physical process modelling in soil and for her background in NWP model development.

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The author would like to thank the Italian National Computing Centre "CINECA" for providing the computational resources with which the simulations, presented in this paper, were performed.

845 **Appendix A**

A test of "Pochva" scheme in column version has been performed using observational data of Coordinated Energy and Water Cycle Observation Project (CEOP) Baltic Sea Experiment (BALTEX). The observed data have been used as forcing parameters for "Pochva" simulation, for determining the physical parameters of soil profile and for defining the initial

850 condition. The observed data have also been used for the verification of simulation results. The observations have been performed in Falkenberg, a site at the Meteorological Observatory of the German Meteorological Service. This site is located in grassland fields, in a heterogeneous rural landscape typical for central Europe. The observational data are freely available upon individual request.

The forcing parameters, included in observation dataset, are: sensible and latent heat flux 2.4 m above the surface, downward

855 and upward short-wave and long-wave solar radiation at the surface, precipitation and pressure at the surface. These observational data are presented in (Beyrich, BALTEX: Lindenberg Flux Data, 2011), (Beyrich, BALTEX: Lindenberg Meteorological Tower Data Set., 2011). The parameters used for defining the initial condition are: surface temperature, soil temperature at 0.05, 0.10, 0.15, 0.20, 0.30, 0.45, 0.50, 0.60, 0.90, 1.00, 1.20, 1.50 m depth, specific volumetric soil water content at 0.08, 0.15, 0.30, 0.45, 0.60, 0.90 m depth. These data are presented in (Beyrich, BALTEX: Lindenberg Soil

860 Temperature and Soil Moisture Data Set., 2011), (Beyrich, BALTEX: Lindenberg Meteorological Tower Data Set., 2011). The soil temperature at the deepest observation level (-1.5 m) has been used as bottom condition for soil thermal exchange

processes in Pochva simulation, and the soil moisture at the deepest observation level (-0.90 m) has been used as bottom condition for soil water exchange processes.

865   The observation soil levels are used in Pochva simulations to avoid space interpolation of simulated results for their verification. The following depth levels are determined for simulation: 0.02, 0.05, 0.08, 0.10, 0.15, 0.20, 0.30, 0.45, 0.50, 0.60, 0.90, 1.00, 1.20, 1.50 m below the surface, for soil water exchange processes the bottom level is 0.90 m as indicated above. Values of physical parameters in Pochva simulation have been defined following the values measured at the observation point and presented in table A1 taken from dataset documentation (Beyrich, BALTEX: Lindenberg Soil Temperature and Soil Moisture Data Set., 2011).

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layer no.	horizon	upper boundary [cm]	lower boundary [cm]	clay / poor clay [M%]	sand [M%]	dry density [g/cm³]	pore volume [%]	field capacity [*] [V%]	wilting point [V%]	hydraulic conductivity [cm/d]	soil heat capacity [*10⁶ J/(K*m³)]
Lindenberg – Falkenberg station											
1	Ap	0	30	26	74	1.6	37	16	4	110	1.32
2	Al	30	60	26	74	1.7	36	18	3	80	
3	Bt	60	120	40	60	1.7	34	24	11	20	

Table A1. Physical parameters of the soil at the Lindenberg - Falkenberg observation station.

    The observation datasets contain the data for the period 01.01.2002-31.12.2009. All observed data have time resolution equal to 30 minutes. Unfortunately, the observation series is not continuous, there are many gaps in observations, mainly in heat

875 fluxes. A search for periods with gaps no longer than two hours for all the required forcing parameters resulted in 90 periods, the longest of which was four days long. Thus the author selected two periods for performing Pochva simulations, one in summer and one in winter. The observed data have a too coarse time resolution in comparison to the step required for a correct numerical simulation, so the data have been interpolated in time with a step of 1 minute, which is the length of a typical time step in meteorological numerical models. These time-interpolated observation values have been used as forcing variables for

880 Pochva simulations. The simulation results and their comparison with the observation data is presented below.

    The summer verification period is 01/07/2003 23:00 – 04/07/2003 04:30 (53.5 hours). Input data about energy fluxes at the surface and about water mass fluxes are shown in figure A1.
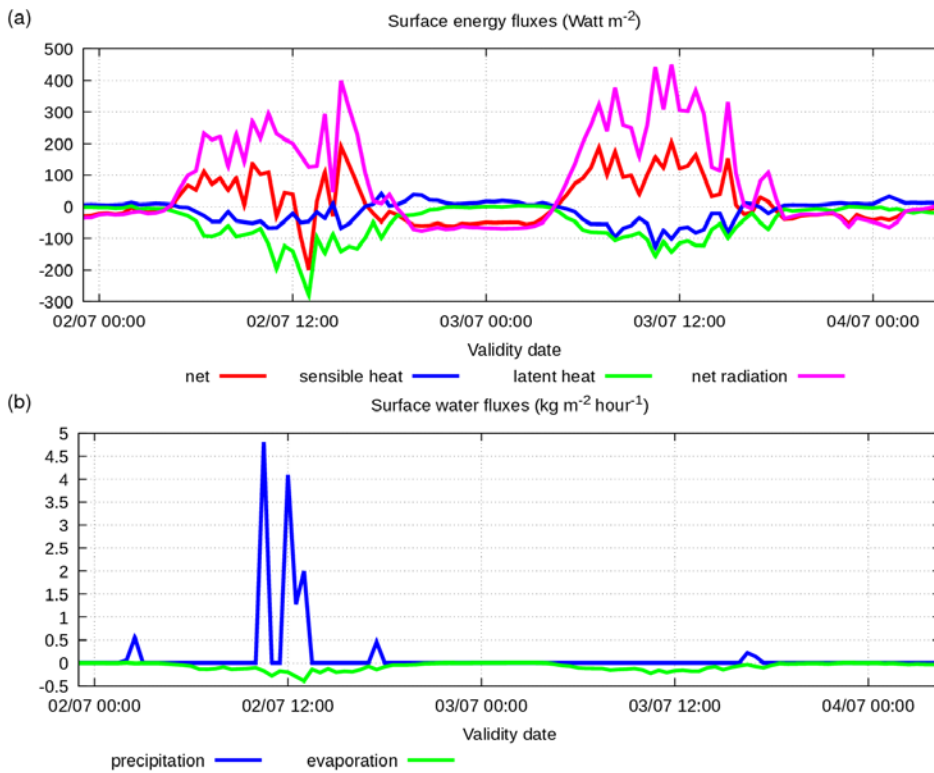
Figure A1. Observation data (BALTEX) in Falkenberg 2-3 July 2003, parameters at the surface: (a) solar radiation and heat fluxes (W m^{-2}); (b) precipitation and evaporation rate (kg m^{-2} hour^{-1}).

These July days are characterised by intensive net radiation flux accompanied by moderate sensible and latent heat fluxes, latent heat flux is significant only after light rain in the first day.

The simulated soil temperature and moisture data at same depth levels are shown in figures A2 and A3 together with observed data.
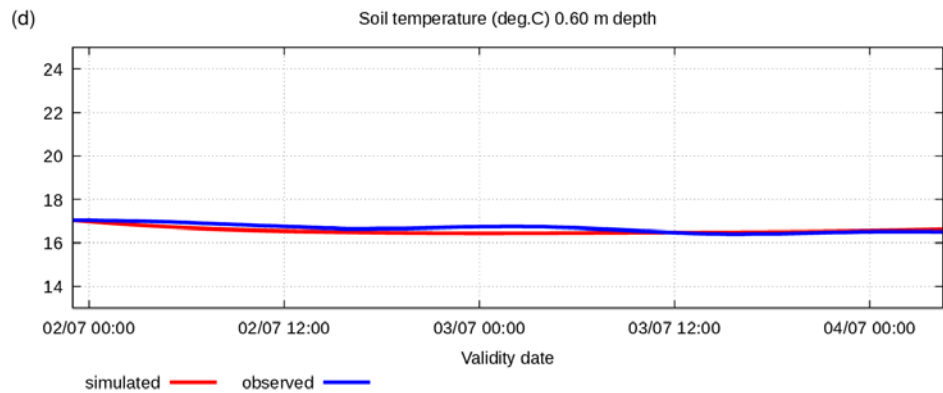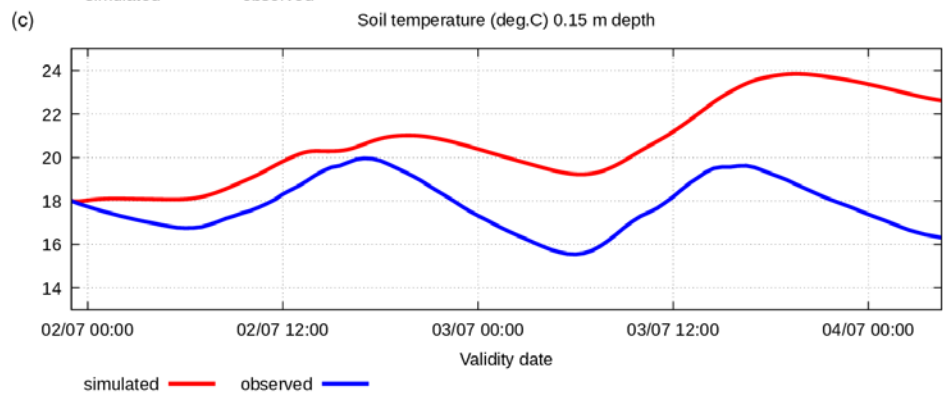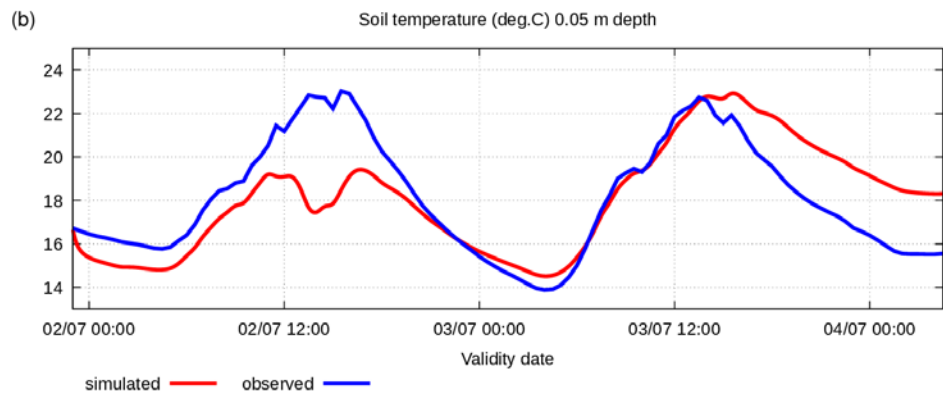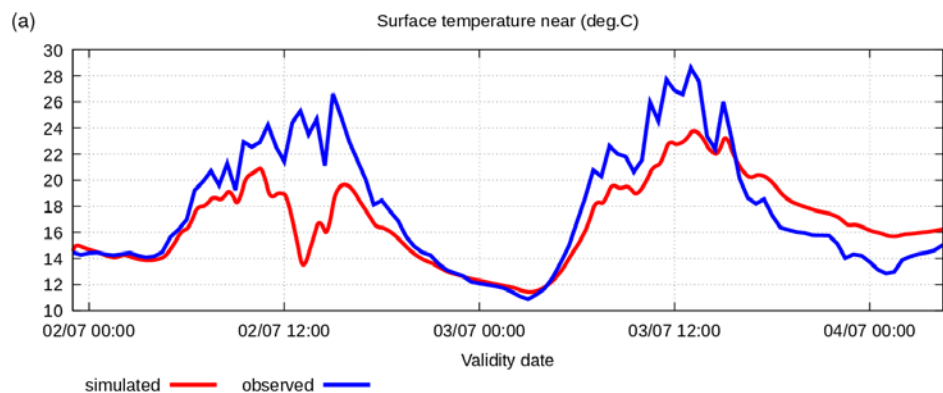
Figure A2. Simulated and observed 2-3 July 2003 soil temperature (degree C) at the surface and at various depths: (a) surface; (b) -0.05 m; (c) -0.15 m; (d) -0.60 m.
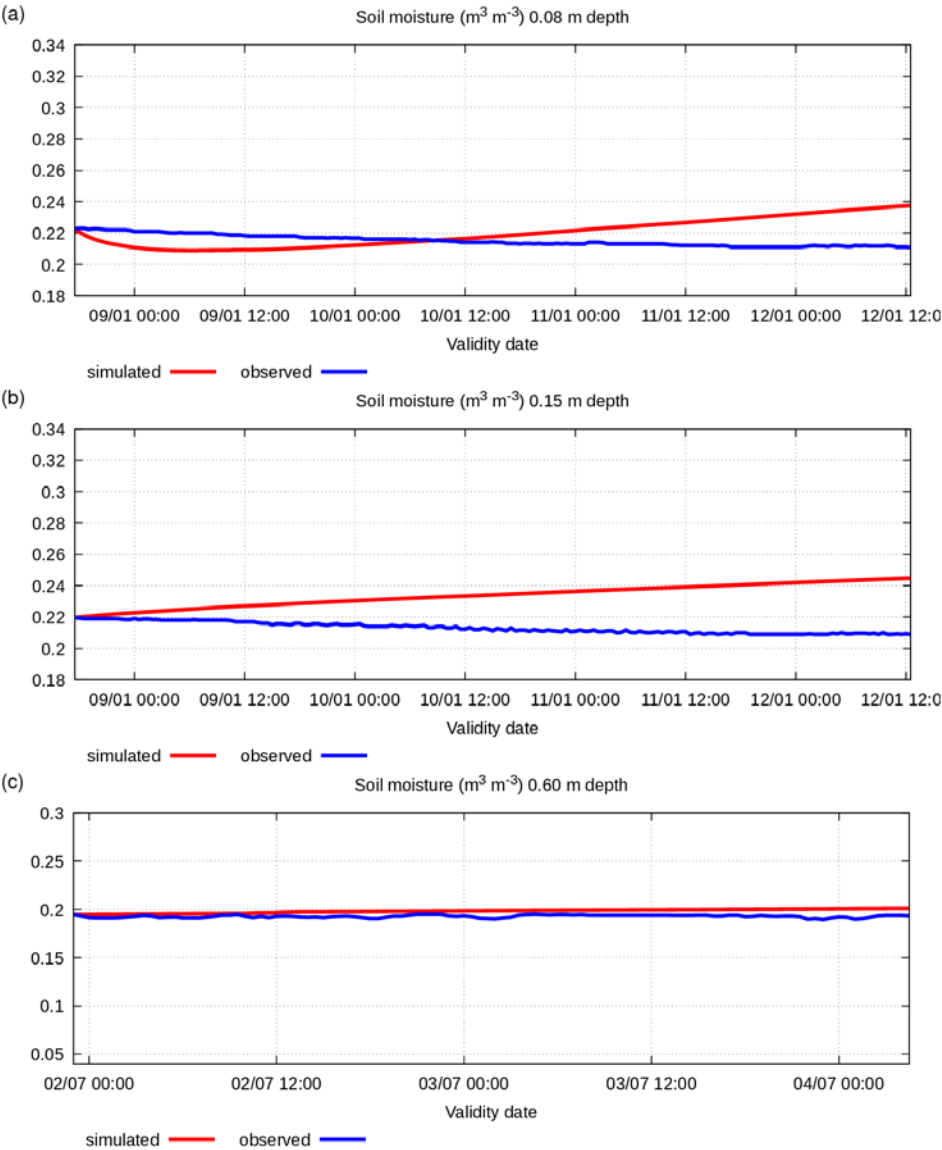
Figure A3. Simulated and observed 2-3 July 2003 soil specific volumetric water content (m3 m-3) at various depths: (a) -0.08 m; (b) -0.15 m; (c) -0.60 m.

Figures A2 and A3 show that the simulated soil parameters at the different levels are out of numerical equilibrium. This is an expected result. A numerical scheme needs a warm-up period in order to reach numerical equilibrium after initialisation. Unfortunately, it has not been possible to find a continuous observation period of sufficient length in order for the simulated

parameters to reach a balanced state. Despite this fact, the simulated parameter values are close to observed values. The soil

905   temperature simulated at various levels shows a correct daily cycle especially at the surface and at the top soil levels, which is

important for an atmospheric model parameterisation. Moreover, the observation data show some odd characteristics: A light

rain was observed on 02/07 at 12:30 (fig. A1(b)) accompanied by a sharp decrease in solar incoming radiation flux and an

increase in outgoing latent heat flux, thus determining a strongly negative energy budget at the surface. This phenomenon is

simulated by Pochva, simulated surface and soil top temperature evidently drop at this time, while, on the other hand, the

910   observed surface and soil top temperature do not reflect this phenomenon. Furthermore, the observed soil moisture at different

levels remains unchanged despite the presence of significant vertical gradient of soil moisture, rain and evaporation in the

observation data.

The winter verification period is 08/01/2005 17:30 – 12/01/2005 12:30 (91 hours). Input data about energy fluxes at the surface

and about water mass fluxes are presented in the figure A4.

915
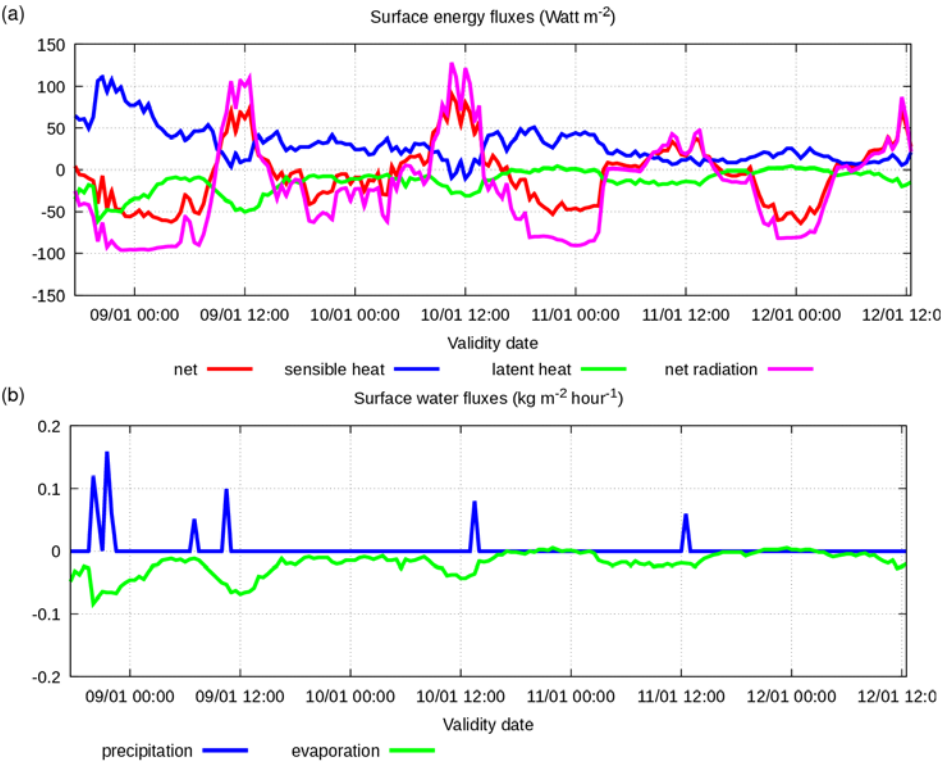
Figure A4. Observation data (BALTEX) in Falkenberg 8-12 January 2005, parameters at the surface: (a) solar radiation and heat fluxes (W m^{-2}); (b) precipitation and evaporation rate (kg m^{-2} hour^{-1}).

920   This January period is characterised by intensive radiation net flux in the first and second days with significant daytime heating

and nighttime cooling, accompanied by weak sensible and latent heat fluxes with the exception of the first night when

significant sensible heat flux is observed; latent heat flux is significant only after light rain in the first day. Some episodes of very light precipitation occur. The evaporation flux has small values.

The simulated soil and moisture data at same depth levels are presented in the figures A5 and A6 together with observed data.

925
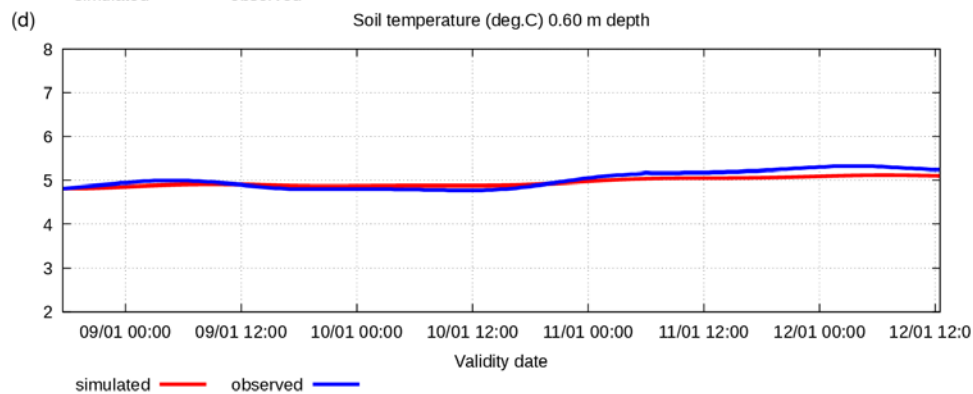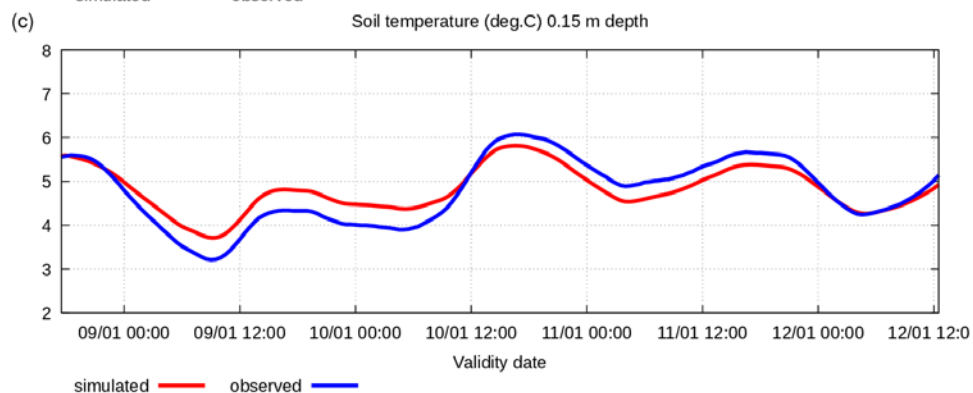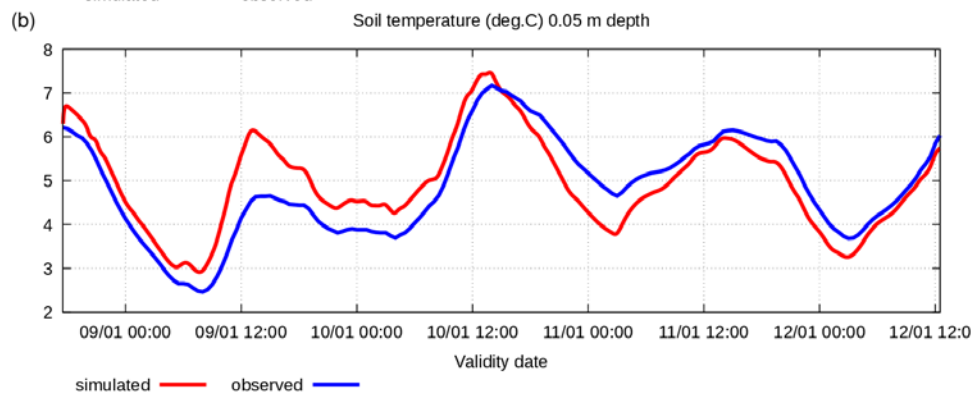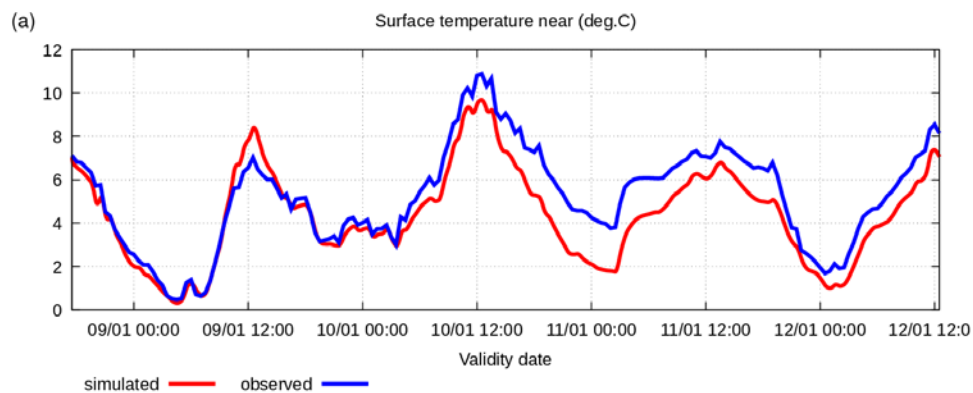
Figure A5. Simulated and observed 8-12 January 2005 soil temperature (C degree) at the surface and various depths: (a) surface; (b) -0.05 m; (c) -0.15 m; (d) -0.60 m.

930
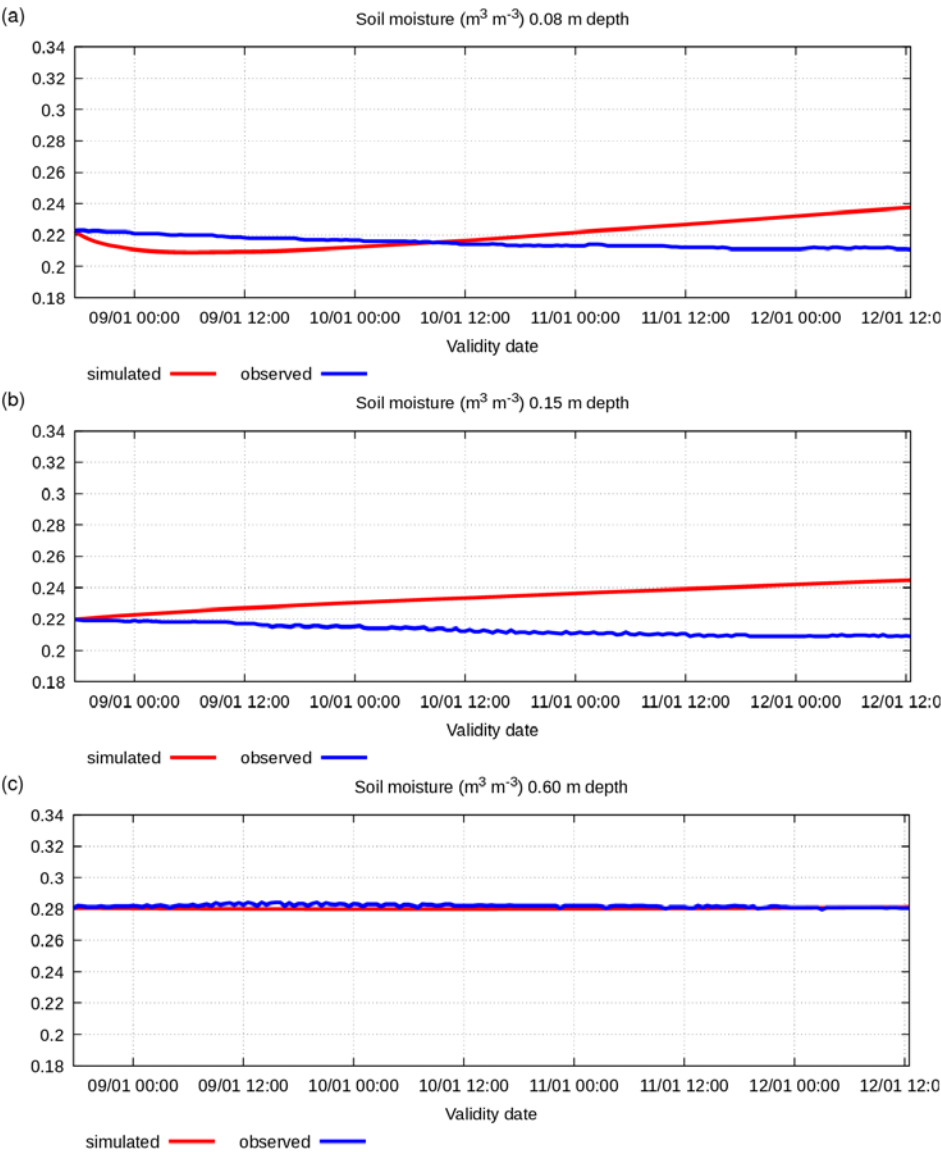
Figure A6. Simulated and observed 8-12 January 2005 soil specific volumetric water content (m3 m-3) at various depths: (a) -0.08 m; (b) -0.15 m; (c) -0.60 m.

In this winter case the initial condition for the soil temperature has a very small vertical gradient. For this reason, the simulated

935   results do not demonstrate numerical unbalance. The simulated soil temperature is very close to observed values. At the same

time, the initial condition for soil moisture has a significant vertical gradient following observed data. So, the simulated soil

moisture has characteristic of numerical disequilibrium, similarly to the summer case. However, in this case the observed moisture has an odd behavior, it remains almost constant at all vertical levels. The observed soil moisture data indicate that water conductivity is close to zero, but it does not correspond to conductivity value declared for the observation point (see table A1). Probably, there are some measurement inaccuracies.

To summarise, it can ascertain that Pochva scheme is able to simulate the soil temperature and moisture enough correctly. The observed values of soil physical parameter, of forcing scheme parameter and of initial condition parameters have been used in Pochva simulations with no manipulation, and simulations show results close to observation data.

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