

STORM v.2: A simple, stochastic ~~decision-support tool~~ rainfall model for exploring the impacts of climate ~~,~~ and climate change at, and near the land surface in gauged watersheds

Manuel F. Rios Gaona¹, Katerina Michaelides^{2,3,5}, and Michael Bliss Singer^{1,4,5}

¹School of Earth and Environmental Sciences, Cardiff University, CF10 3AT Cardiff, UK

²School of Geographical Sciences, University of Bristol, BS8 1SS Bristol, UK

³Cabot Institute for the Environment, University of Bristol, BS8 1QU Bristol, UK

⁴Water Research Institute, Cardiff University, CF10 3AX Cardiff, UK

⁵Earth Research Institute, University of California Santa Barbara, Santa Barbara, CA, USA

Correspondence: manuel (RiosGaonaM@cardiff.ac.uk)

Abstract. Climate change is expected to have major impacts on land surface and subsurface processes through its expression on the hydrological cycle, but the impacts to any particular basin or region are highly uncertain. Non-stationarities in the frequency, magnitude, duration, and timing of rainfall events have important implications for human societies, water resources, and ecosystems. The conventional approach for assessing the impacts of climate change is to downscale global climate model output and use it to drive regional and local models that express the climate within hydrology near the land surface. While this approach may be useful for linking global general circulation models to regional hydrological cycle, it is limited for examining the details of hydrological response to climate forcing for a specific location over timescales relevant to decision makers. For example, management of flood or drought hazard requires detailed information that includes uncertainty based on variability in storm characteristics, rather than on differences between models within an ensemble. To fill this gap, we present the second version of our STOchastic Rainfall Model (STORM), an open-source ~~,~~ parsimonious and user-friendly modeling framework for simulating climatic expression as rainfall fields over a basin. This work showcases the use of STORM in simulating ensembles of realistic sequences, and spatial patterns of rainstorms for current climate conditions, and bespoke climate change scenarios that are likely to affect the water balance near the Earth's surface. We outline, and detail STORM's new approaches: one copula for linking marginal distributions of storm intensity and duration; orographic stratification of rainfall using the copula approach; a radial decay-rate for rainfall intensity which takes into consideration potential, but unrecorded, maximum storm intensities; an optional component to simulate storm start date-times via circular/directional statistics; and a simple implementation for modelling future climate scenarios. We also introduce a new pre-processing module that facilitates the generation of model input in the form of probability density functions (PDFs) from historical data for subsequent stochastic sampling. Independent validation showed that the average performance of STORM falls within a 5.5% of the historical seasonal total rainfall in the Walnut Gulch Experimental Watershed (Arizona, USA) that occurred in the current century.

1 Introduction

22 In earlier research (Singer et al., 2018; Singer and Michaelides, 2017), we introduced the STOchastic Rainstorm Model (STORM)¹, presented the justification for its creation, and demonstrated its application to simulating spatial rainfall fields
24 at Walnut Gulch Experimental Watershed (WGEW; Sec. 2.1), an intensely gauged semi-arid watershed in Arizona, USA. In this paper, we introduce STORM v.2 and highlight the novel aspects of the model that warrant a new version number. We made
26 several changes to the model that make it more user-friendly and enhance its capability for simulating rainfall in a manner that supports computation of the water balance over gauged watersheds under historical climate or under various user-defined
28 scenarios of climate change. Specifically, STORM v.2: a) treats rainstorm intensity and duration as joint variables in a copula framework, rather than as independent variables, which overcomes a shortcoming in the previous version of the model; b) of-
30 fers an elevation stratification to account for orographic characteristics influencing precipitation, where the aforementioned copula framework can also be applied; c) improves on the radial decay-rate model for rainfall intensity to incorporate potential,
32 but unrecorded, maximum storm intensities; d) accounts for storm start date-times from the perspective of circular/directional statistics, which supports more realistic diurnal and seasonal timing of rainfall; and e) contains a pre-processing module that au-
34 tomatically generates all the input probability density functions (PDFs) required for storm simulation. These advances, which will be discussed in detail below, were required to create a model that is faithful to the underlying rainfall processes (e.g.,
36 capturing relationships between rainstorm intensity, duration, and frequency), while also enabling broad uptake and easy use of the model for a range of purposes, and for any small basin with available storm rainfall data.

38 An individual rainstorm (discrete in space and time) has an intensity that varies spatially from the center of the storm to its margins, and a duration over which an average intensity is expressed. Rainstorm intensity and duration are related in
40 the sense that the highest intensity storms are generally short-lived, while long rainstorms have low average intensity. The functional form of the relationship between rainfall intensity and duration is typically characterized as a negative exponential,
42 where intensity declines with duration (Nicholson, 2011). However, in rain gauge data, there can be dramatic scatter in this relationship, so a single-valued function cannot represent the phase space between intensity and duration. To overcome this
44 limitation, the previous version of STORM fitted the relationship for the upper envelope of the intensity-duration phase space and then used the functional form of the fitted curve to fit additional curves that pass through the entire phase space (Singer
46 et al., 2018). These empirical intensity-duration curves are then treated as a stochastic variable for random selection within the original STORM code. To further enable complete sampling of the entire phase space of intensity and duration, STORM 1.0
48 also includes a fuzzy tolerance such that storm intensity for the selected duration can vary up or down away from the selected curve.

50 This representation of intensity and duration is the crux of STORM 1.0, as it forms the basis for rainstorm characteristics that affect rainfall totals during a storm, over a season, and over the longer term. However, this approach has several weaknesses:
52 a) it is based on debatable, heuristic rules of probability designation; b) it does not capture the inherent multi-valued relationship between rainfall intensity and duration; c) the functional form of the relationship is assumed based on the upper envelope of

¹<https://github.com/blissville71/STORM>

54 the phase space; and d) there is an arbitrary number of curves used to represent the phase space. Notably, we also use the curve
55 number probabilities to represent orography in STORM 1.0. This means that the representation of orography in STORM 1.0
56 contains these same weaknesses.

The relationship between rainfall intensity and duration is a critical attribute of rainstorms that affects the characteristics
58 of water delivery to the land surface, which affect the balance between infiltration and evapotranspiration, and the corre-
sponding antecedent moisture condition at any point in time and space. Thus, it is critical to characterize the distribution of
60 storm intensity-duration from historical records, as well as the frequency of their occurrence. STORM v.2 now offers a better
characterization of storm intensity-duration relationship by adopting a copula approach.

62 *Copulas* (or *copulae*), from the Latin word for “tie”, represent a way forward for characterizing the complex relationship
between intensity and duration from the perspective of joint frequency of occurrence (Vandenberghe et al., 2011). A copula is
64 a function that links/couples a multi-variate distribution function to its univariate marginals, regardless any prior knowledge
of such marginals (see Sec. 2.6). The copula approach obviates the need for fitting intensity-duration curves, and for the
66 arbitrary assignment of curve probabilities. Once the intensity-duration copula is fit, it can be sampled randomly to simulate
the rainstorm characteristics.

68 Another shortcoming in STORM 1.0 was its reliance on user-developed PDFs as input to the model. We recognize that this
requirement may be a major limitation which prevents some users from deciding to use STORM for rainstorm simulation.
70 To make STORM more user-friendly, we added the pre-processing, and visualization modules that respectively allow the
automation in computing the best fit of PDFs on (input) gauge data, and the visualization of the (output-modelled) storms (see
72 Sec. 2.9).

We provide STORM v.2 (and its pre-processing, and visualization modules, along with test/processed input data, and pa-
74 rameters) as open source code². Unlike STORM 1.0, STORM v.2 is written only in Python 3 (Van Rossum and Drake, 2009).
From here onwards, we will refer to STORM v.2 simply as STORM.

76 STORM is our contribution to the wealth of Stochastic Rainfall Generators (SRG) currently available. A state-of-the-art
review on SRG lies beyond the scope of this work. Nevertheless, here we briefly acknowledge some of the vast work carried
78 out in this field during the last two decades. Stochastorm, developed by Wilcox et al. (2021), is a high spatio-temporal (“on
the order of kilometers and minutes”) SRG for convective storms. It is event-based (like STORM), built upon a meta-Gaussian
80 framework, and also able to generate rainfall fields. Vu et al. (2018) evaluated the performance of five Stochastic Weather
Generators (SWG), namely: CLIGEN, ClimGen, LARS-WG, RainSim and WeatherMan. Nevertheless, Vu et al. (2018) focused
82 their analyses, for the aforementioned five models, on characteristics of rainfall such as occurrence, intensity, and wet/dry
spells, over three climatic regions around the globe. Unlike STORM, which only focuses on rainfall, SWG (e.g., Papalexou
84 et al., 2021; Peleg et al., 2017) are frameworks build to also model climatic variables other than rainfall, e.g. temperature, wind
velocity/direction. Like STORM, another open-source framework is that of Benoit et al. (2018), which generates conditional
86 or unconditional high-resolution (100m; 2min) continuous rain fields over small areas. Kleiber et al. (2012) developed a
Gaussian-processes framework that allows the generation of gridded rainfall fields (accounting for uncertainties in their

²<https://github.com/feliperiosg/STORM2>

88 estimates too). Similar to STORM, their model captures local and domain aggregated rainfall from daily to seasonal to annually
90 scales. Other open-source SRG frameworks, both based on Neyman-Scott process, are STORAGE (STOchastic RAInfall
90 GEnerator; De Luca and Petroselli, 2021) that generates long and high-resolution (1or5min) time-series; and NEOPRENE
(Neyman-Scott Process Rainfall Emulator; Diez-Sierra et al., 2023) that simulates rainfall from hourly to daily scale. Like
92 STORM, NEOPRENE is also coded in Python. Other SRG based on Poisson process are: RainSim V3 (Burton et al., 2008),
designed for catchments up to 5000 km² and time scales from hourly to yearly; and Let-It-Rain (Kim et al., 2017) that generates
94 stochastic 1 – h rainfall time series. AME (Advanced Meteorology Explorer) is a SRG for high spatial-resolutions at daily
temporal scales. Developed by Dawkins et al. (2022), AME is based on a Hidden Markov Model (HMM), able not only
96 to capture observed rainfall but also meteorological drought behaviour. STREAP (Space-Time Realizations of Areal Pre-
cipitation; Paschalis et al., 2013) is also a high-resolution (10 min to daily in time; few tens-of-km in space) SRG. Both
98 Dawkins et al. (2022) and Paschalis et al. (2013) provide a plethora of references to alternative stochastic frameworks in
rainfall simulation. The latter, also provides a detailed review on advances on stochastic spatio-temporal rainfall modelling,
100 grouped into for categories, namely, point process theory, random fields theory, multifractal processes, and “multisite temporal
simulation framework”.

102 Our model differs from the aforementioned ones in several features. STORM is an open-source framework (accessible
via it repositories), and build upon a free/open-source software platform (i.e., Python). This implies that anybody, from any
104 computational platform, can modify and improve STORM accordingly to their needs. Some of the SRG here cited are not
open-source; and those that are freely available (e.g., De Luca and Petroselli, 2021; Benoit et al., 2018; Kim et al., 2017) were
106 built upo commercial applications (i.e., not open-source software). In our opinion, this is a key factor that plays against their
widespread usability and/or deployability. Most of the SRG parameterize the 'inter-arrival' time (i.e., time between storms) via
108 a PDF. STORM, via its circular framework, indirectly, and rather straightforward, characterizes this parameter by modelling
instead storm starting datetimes (see Sec. 2.7). Throughout a couple of scaling factors (see Sec. 2.8), STORM is able to simulate
110 rainfall fields from potential climate change scenarios. This is a clever and modular functionality not present in many of the
SRG.

112 2 Data and Methods

STORM is a stochastic model built upon continuous PDFs for seven variables, i.e., total seasonal rainfall (TOTALP), maximum
114 storm radius/extent (RADIUS), rainfall decay rate from the storm center outwards (BETPAR), maximum intensity (MAXINT),
average duration (AVGDUR), storm start date (DOYEAR), and storm start time (DATIME). Here we model the relation be-
116 tween the storm's maximum intensity and its average duration via a copula approach (COPULA). STORM also allows for
the stratification of the copula approach based on the orography of the region, where one can specify maximum_intensity-
118 average_duration copulas for every elevation band into which the catchment is split. This “elevation stratification”, along with
the storm start time are optional features in STORM. A digital elevation model (DEM) is required to model orographic effects;
120 whereas a specific circular statistics library must be installed to model the starting times of rainstorms.

122 STORM also preserves STORM 1.0's functionality to simulate the impact of plausible climate change either on the total
123 seasonal rainfall or the storm's maximum intensity. Such functionality is applied through two types of mutually exclusive
124 factors: `_SC` (i.e., Step-Change) which is constantly applied to every and each of the simulated years; and `_SF` (i.e., Scaling-
125 Factor) which is progressively applied to all of the simulated years. Hence, for potential/climate impacts on the total seasonal
126 rainfall these factors are dubbed as `PTOT_SC`, and `PTOT_SF`; whereas for potential/climate impacts on the maximum rainfall
intensity these factors are dubbed as `STORMINESS_SC`, and `STORMINESS_SF` (see Sec. 2.8).

2.1 Walnut Gulch Experimental Watershed

128 The Walnut Gulch Experimental Watershed³ is the catchment selected to calibrate and validate STORM. With an area of
129 147.75 km², and managed by the USDA-ARS⁴ Southwest Watershed Research Center (SWRC), it is located near Tombstone,
130 southwestern Arizona, USA. WGEW is situated at the transition between the Chihuahuan and Sonoran Deserts, and is located
on a bajada sloping gently westwards from the Dragoon Mountains, reaching the San Pedro River at Fairbank, Arizona.
132 The climate is semi-arid with low average annual rainfall of ~ 312 mm for the period 1956 – 2005 (Goodrich et al., 2008).
Convective thunderstorms during the summer monsoon season (July-September) generate 60% of the annual precipitation, and
134 are characterized by high spatial variability, limited areal extent, high intensity-short duration rainfall (Osborn, 1983; Osborn
and Lane, 1969; Renard and Keppel, 1966). In this watershed, storm events have frequently been found to exceed intensities of
136 100 mm · h⁻¹ at the centre of the storm, lasting on the order of minutes (Nicholson, 2011; Renard and Laursen, 1975). Keefer
and coauthors (2007) offer a detailed report on physiography, instrumentation, and different applications on the WGEW.

138 Dating back from the early/mids 1950s (Meles et al., 2022; Stillman et al., 2013), the WGEW is, according to Moran et al.
(2008), “one of the most highly instrumented semiarid experimental watersheds in the world”. Its rain gauge network is one
140 the densest in the world, for watersheds greater than 10 km² (~ 0.6 gauges · km⁻² (Goodrich et al., 2008); or one gauge
per 1.7 km² (Meles et al., 2022)). Storm rainfall data dates back from 1953 (Moran et al., 2008), and up to 1999 the entire
142 gauge network was analog. From 2000 to the present, the gauge network was updated to a digital network (Meles et al., 2022;
Goodrich et al., 2008). From the dataset used in this work, there were a total of 93 digital stations (as of 2022), averaging 84
144 stations per year since 2000. Supplemental Fig. B8 shows the gauge network used in this study.

We parameterize STORM using 37 years of analog data (i.e., from 1963 through 1999). Even though there are gauge records
146 for the WGEW from 1953, we use them starting from 1963 to account at least for 80 gauges per year); ~~and we validate~~.
This analog network amounts to 118 gauges sparsely deployed over the whole WGEW. We carried out simulations of 30 runs,
148 each run having 23 simulated years (i.e., 690 simulation-years in total, per simulation), in order to evaluate the performance
of STORM ~~over the on~~ features such as: seasonal total rainfall (over a small catchment), number of storms generated, and

³Historical storm data (among many other hydrological and hydrometeorological data) from the WGEW is freely available at
<https://www.tucson.ars.ag.gov/dap/>

⁴U.S. Department of Agriculture - Agricultural Research Service, <https://www.ars.usda.gov/pacific-west-area/tucson-az/southwest-watershed-research-center/>

150 modelled climate impacts in rainfall intensity. The output of this evaluation exercise(s) were compared against 23 years of
151 storm data from the aforementioned digital/automatic data-network, i.e., the one from 2000 onwards (see Sec. 3.1).

152 The richness and careful curation (for more than half a century) of this dataset, especially with regard to high density of
153 rain gauges and detailed and lengthy rainstorm records, was the main reason our model was designed and built with a focus
154 on this particular catchment. Nevertheless, nothing precludes the application of STORM to other (small) catchments in any
155 climatic zone, as long as some detailed rainstorm records exist for the related area/catchment. The effect of the number and
156 extension of rainstorm data on the performance of STORM is beyond the scope of the present work. Given the set up of our
157 model, it is expected that the richer the (rain-gauge) records the more robust the parameterization is, and therefore the better
158 the performance of STORM will be.

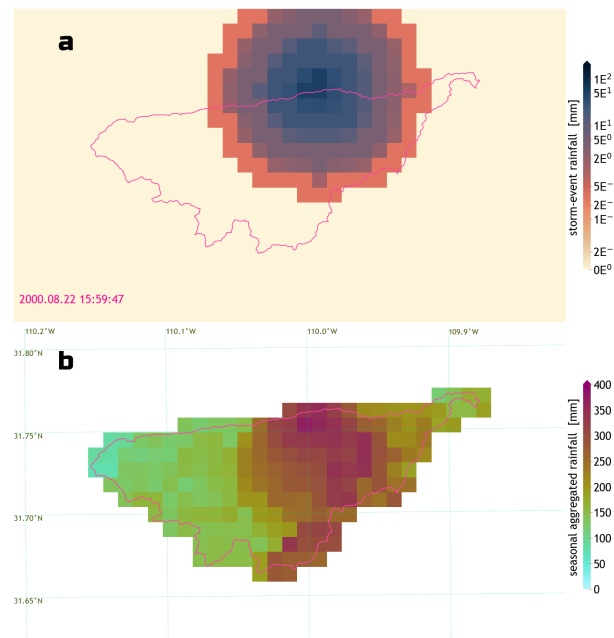


Figure 1. Spatio-temporal distribution of simulated storm rainfall over the WGEW (see Sec. 2.1). Spatial resolution of 1×1 km. **Top**-Panel **a** - One large simulated storm **start-starting** at $\sim 17:41 \sim 16:00$ on **July 21st August 22nd**, with a radius of $\sim 11 \text{ km} \sim 7 \text{ km}$, $\sim 2.5 \text{ h} \sim 4.5 \text{ h}$ of duration, and a maximum intensity of $\sim 19 \text{ mm} \sim 51.3 \text{ mm}$ (i.e., $7.57 \text{ mm} \cdot \text{h}^{-1} \sim 11.37 \text{ mm} \cdot \text{h}^{-1}$). Please note its logarithmic color scale. **Bottom**-Panel **b** - Cumulative seasonal distribution of 116 storms for the wet season, i.e., from June through October. Even though the grid is presented in “lat-lon” coordinates (i.e., CRS WGS-84), the actual projection (in both panels) is the 2D-Cartesian coordinate system known as NAD83 / UTM zone 12N (i.e., EPSG:26912; <https://epsg.io/26912>).

2.2 Total Seasonal Rainfall [TOTALP]

160 In order to remain faithful to the total seasonal rainfall distribution across a basin of interest, STORM stops a given simulation
season once the median of the cumulative rainfall over the catchment surpasses the sampled TOTALP value for the season

162 under consideration. The TOTALP value is sampled from a PDF of historical medians of total seasonal storm rainfall. Each
of these historical medians represents the spatial median of the cumulative seasonal rainfall recorded by the gauge network
164 spread within the catchment. To avoid sampling negative values of rainfall, the fitting (and the sampling) of the PDF is done
in (natural) logarithmic space, i.e., $TOTALP = e^{TOTALP_{(sampled)}}$. Reaching the (catchment) median sampled from a distribution of
166 historical medians offers a more accurate method for stochastic modelling of seasonal totals. Figure 1 (bottom panel) shows
the spatial distribution of rainfall at the end of one simulation run, i.e., once the median of the cumulative rainfall over the
168 catchment is larger than the sampled value for TOTALP.

2.3 Maximum Storm Extent [RADIUS]

170 Storm radii are defined in STORM by grouping two or more gauges, computing the distance of each gauge to the centroid of
the set/group of gauges, and selecting the maximum computed distance. Here, a “set/group of gauges” means all those gauges
172 for which the time-stamp of any storm start time is identically recorded among them in the historical database. A PDF of radii
was generated from such groups with at least two rain gauges. We are aware that this assumption does not consider the extent,
174 evolution, and/or trajectory of any storm in particular throughout the gauge data. Nevertheless, by assuming that identical
time-stamps in storm start times imply that the whole storm is being simultaneously captured by the gauge network, one can
176 easily estimate an extension of the storm from gauge records. This premise also relies on the assumption of a circular-shape
model for storm cells, and on a gauge network with consistent spatial density. Supplemental Figure B1 shows the distribution
178 of maximum storm (estimated) radii for the WGEW calibration dataset (i.e., storms recorded from August 1953 through
October 1999; see Sec. 2.1). Figure 1 (top panel) shows a simulated storm with a radius of ~ 11 km. This approach is biased
180 towards spatially-large storms given that small-radii storms, i.e., storms not captured by a single gauge are disregarded in this
methodology.

182 The minimum radius that can be sampled is restricted by the spatial resolution the user might set for the model output. For
instance, for a model output resolution of 0.5×1.0 km, the minimum possible (sampled) radius would be 1 km. This is achieved
184 by truncating the RADIUS PDF, and then sampling from it. Instead of using a “maximum” criterion for the selection of storm
radii, the user can also modify this criterion to be, e.g., the mean (or median or whatever) distance of a group of gauges and
186 their centroid. This change can be implemented by the user, via the `pre_processing.py` script. STORM 1.0 did not use a
“radius” approach. Instead, storm area values were sampled from a pre-determined, fixed PDF.

188 2.4 Rainfall Decay Rate [BETPAR] & Maximum Storm Intensity [MAXINT]

Following the approach of STORM 1.0, we model individual storms as isotropic circular cells for which maximum intensities
190 (I_{max}) are (always) located at their centres, with a quadratic exponential decay (β^2) as the distance from such centres (r)
increases:

$$192 \quad I(r) = I_{max} \cdot e^{-2 \cdot \beta^2 \cdot r^2}, \quad (1)$$

where $I(r)$ (in $\text{mm} \cdot \text{h}^{-1}$) is the rainfall intensity at a distance r (in km) from the storm centre. β has units of km^{-1} . We
194 acknowledge that real storms may not be circular, but this assumption simplifies the mathematical representation of storms in
the model.

196 In this new version, we use the quadratic exponential decay model to fit both the decay rate (β), and maximum intensity
(I_{max}). This is done via *scipy*'s module `curve_fit`, i.e., a non-linear least squares approach, for which the Trust Region
198 Reflective method is applied, given the constraints we enforce to our minimization problem (Virtanen et al., 2020; Branch et al.,
1999). Such constraints simply refer to the limits for which one intends β and I_{max} (in this case) to be within. For instance,
200 and following Eagleson et al. (1987, Fig. 17), we bound β between 0 and 3; whereas we set I_{max} to be 3 times the highest
intensity found in the gauge data as the upper limit, and a value slightly above zero as the lower limit ($0.07 \text{ mm} \cdot \text{h}^{-1}$, in our
202 case). Morin et al. (2005), and Eagleson et al. (1987) previously used the same model to fit rainfall decay rate from radar and
gauge data, respectively, for the WGEW. Figure 1 (top panel) shows a simulated storm with a steep β of $\sim 0.18 \text{ km}^{-1}$, and
204 $I_{max} = 18.77 \text{ mm}$.

We fit the model for storms simultaneously registered by four or more gauges (i.e., with identical starting time-stamps).
206 Along with the optimal values for which the model is fitted, `curve_fit` also returns the estimated covariance of such
optimal values. We only kept optimal values for which their covariance is equal or smaller than 5, and equal or larger than 0.
208 These “clean” optimal values are the ones over which the PDFs (BETPAR and MAXINT) are then constructed. We obtained
similar results (not shown here) to Morin et al. (2005), and Eagleson et al. (1987) for the PDF of β . In our case, $\beta_{mean} \approx 0.1$,
210 compared to ~ 0.4 for the Morin et al. (2005), and Eagleson et al. (1987) studies. This is mainly attributed to our methodology
of simultaneously fitting both I_{max} and β . We also hit the $\mu \approx 0.4$ when we only fit for β , using a larger number of storm
212 records than they did in those previous studies.

We assume that in the vast majority of the cases, the rainfall recorded by the gauge network does not correspond to the
214 maximum intensity of the storm event; thus, we required a method to model maximum storm intensity (MAXINT). Eq. (1)
is an adequate model that allows us to easily estimate the maximum rainfall intensity from gauge records (given the current
216 computational tools, and the extensive rainfall records). Supplemental Fig. B2 shows the difference between PDFs accounting
(and not) for maximum intensity. Accounting for maximum storm rainfall intensity is a feature not present in STORM 1.0.

218 **2.5 Storm Average Duration [AVGDUR]**

The AVGDUR PDF is constructed from the corresponding optimal values for maximum intensity (MAXINT) (see Sec. 2.4).
220 Once a “group of gauges” affected by a storm is established (see Sec. 2.3), storm duration is modelled as the average of all
storm durations registered within this group. Nevertheless, the storm total duration registered by each gauge does differ from
222 gauge to gauge, mainly due to the movement of the storm front over the gauge network. Thus, for every fit of Eq. (1) to a group
of gauges (for which I_{max} and β are estimated) an average storm duration is also retrieved. And after selecting the best fits,
224 average storm durations included, then we proceed to fit the AVGDUR PDF.

2.6 Copula Approach [MAXINT-AVGDUR COPULA]

226 The cornerstone of a copula framework is (set on) Sklar's theorem (e.g., Hofert et al. (2018, chap. 1), Joe (2014, chap. 1),
 Nelsen (2006, chap. 2)), which states that for any d -dimensional (joint) distribution function H with univariate marginals
 228 (margins) F_1, \dots, F_d , there exists a d -dimensional copula C such that:

$$H(\mathbf{x}) = C(F_1(x_1), \dots, F_d(x_d)), \quad \mathbf{x} \in \mathbb{R}^d. \quad (2)$$

230 If the univariate marginals F_1, \dots, F_d are continuous, then C is uniquely defined on $[0, 1]^d$. In simpler terms, a copula is a
 function that links/couples (thus its etymology) a multivariate (joint) distribution function to its univariate marginals, with no
 232 prior knowledge of the actual shape (or type) of such marginals (e.g., Zhang and Singh, 2019; Hofert et al., 2018; Dai et al.,
 2014; Vandenberghe et al., 2011; Nelsen, 2006).

234 Elliptical copulas (which show elliptically contoured density level surfaces) refer to copulas from elliptical distributions (e.g.,
 Tjøstheim et al. (2022, chap. 5), Mai and Scherer (2017, chap. 4)). An elliptical distribution represents a linear transformation of
 236 spherical distributions (Mai and Scherer, 2017, chap. 4), these latter being extensions of multinormal distributions (Fang et al.,
 1990, chap. 2). The vast majority of application from elliptical copulas are found in financial sciences (Genest et al., 2009; The
 238 Economist, 2009). Nonetheless, there are recent applications of elliptical copulas in hydrometeorology such as modelling radar
 rainfall uncertainty (Dai et al., 2014), and establishing seasonal correlation between El Niño Southern Oscillation (ENSO),
 240 Pacific Decadal Oscillation (PDO) and precipitation (Khedun et al., 2014), for example. Chen and Guo (2019), and Zhang and
 Singh (2019) provide a thorough review of recent advances and applications of copulas (elliptical among others) in several areas
 242 of hydrology fields such as extreme analysis, drought(s), rainfall, flood (frequency, forecasting, and risk), streamflow, water
 quality, and suspended sediment transport. Elliptical copulas are very common and advantageous as they allow the specification
 244 of different levels of global correlation between marginals (Tjøstheim et al., 2022, chap. 5). Nevertheless they offer no simple
 closed-form expressions, that is, they have only implicit analytical expressions/solutions (Mai and Scherer, 2017, chap. 4).

246 A (d -variate) Gaussian (namely, standard normal) copula belongs to the parametric family of the elliptical copulas (e.g., Mai
 and Scherer, 2017, Fig. 4.1), and it is described by the functional form (e.g., Mai and Scherer (2017, chap. 4)):

$$248 C_P^{Ga}(\mathbf{u}) = \Phi_P(\Phi^{-1}(u_1), \dots, \Phi^{-1}(u_d)), \quad (3)$$

where Φ_P is the joint cumulative distribution function (CDF) of a d -variate Gaussian distribution; Φ^{-1} is the univariate
 250 Gaussian inverse CDF (i.e., the quantile function); P is the $d \times d$ correlation matrix of multivariate normal random vector; with
 C_P^{Ga} denoting the copula is parameterized by the $\frac{1}{2}d(d-1)$ parameters of the correlation matrix (McNeil et al., 2015, chap. 7).

252 STORM uses a bi-variate Gaussian copula to model the dependence between storm rainfall intensity and duration. In a d -
 variate Gaussian copula the $d \times d$ correlation matrix could be replaced by a/the covariance matrix (Mai and Scherer, 2017, chap.
 254 4). For the bi-variate case, i.e. $d = 2$, C_P^{Ga} becomes C_ρ^{Ga} , with ρ the (scalar) Pearson correlation coefficient (e.g., Tjøstheim
 et al. (2022, chap. 5), McNeil et al. (2015, chap. 7), Joe (2014, chap. 4)). In doing so the parameterization is reduced to its

256 minimum (only dependent on ρ); thus its (relatively) easy implementation, and therefore its popularity. Still, a bi-variate (or
 any d -variate, for that matter) Gauss copula does not have a simple closed form, but can be expressed as an integral over the
 258 density of a bi-variate normal random vector (e.g., McNeil et al. (2015, chap. 7), Ross (2013, chap. 6)):

$$C_{\rho}^{Ga}(u, v) = \int_{-\infty}^{\Phi^{-1}(u)} \int_{-\infty}^{\Phi^{-1}(v)} \frac{1}{2\pi\sqrt{1-\rho^2}} \cdot \exp\left\{-\frac{u^2 + v^2 - 2\rho uv}{2(1-\rho^2)}\right\} dv du,$$

with $0 \leq u, v \leq 1$, and $\rho \in [-1, 1]$. (4)

260 STORM constructs the bi-variate Gaussian copula via the `GaussianCopula` module from the `statsmodels` package (Joe,
 2014; Seabold and Perktold, 2010). First, during the pre-processing stage (Sec. 2.9) the Pearson correlation coefficient ρ is
 262 obtained through Greiner’s equality (Berger, 2016):

$$\tau = \frac{2}{\pi} \cdot \arcsin(\rho),$$
 (5)

264 where τ is Kendall’s rank correlation (also known as Kendall’s tau) (Virtanen et al., 2020; Kendall, 1945). A rank correlation is
 a copula-based measure of (strength of) dependence, i.e., only depends on the copula (of a bi-variate distribution), and not on
 266 the marginals (McNeil et al., 2015, chap. 7). It is computed from the ranks of the (empirical) data, which means one only needs
 the ordering of the random variables, and not the actual values, i.e., storm intensity and duration in this case. Eq. (5) generally
 268 holds for elliptical copulas (from which the bi-variate Gaussian is a member); offering a simple approach to compute ρ without
 the estimation of variances and covariances (Langworthy et al., 2021; McNeil et al., 2015, chap. 6). Then, during a simulation
 270 (or validation) run, the bi-variate normal distribution is constructed from Eqs. (5) and (4) by using the probability integral
 transform (Seabold and Perktold, 2010). Once the (bi-variate) Gaussian copula is built, n samples are randomly sampled from
 272 it. These samples are drawn from the $0 \leq u, v \leq 1$ CDF-space; hence, each sample, i.e., (u, v) -point, must be transformed
 (back) into the intensity-duration space. This transformation is done throughout the marginal PDFs (and their `ppf` objects,
 274 from `scipy`’s module `stats`). During the pre-processing stage STORM builds the marginal PDFs for intensity and duration
 from the input gauge data.

276 Figure 2 shows a comparison between storm rainfall measured by rain gauges, and simulated from a bi-variate Gaussian
 copula. From this figure, one can see that for the simulated exercise (Fig. 2b) STORM generates storms with higher (and
 278 lower) intensities than those actually observed by the gauge network (Fig. 2a), supporting a wider distribution of potential
 storm characteristics.

280 2.7 Day of Year [DOYEAR] & Time of Day [DATIME]

Realistic storm start dates and times can now be sampled in STORM through a modular implementation of directional (or
 282 circular) statistics. Directional statistics takes into consideration the periodicity of random variables that can be distributed in a

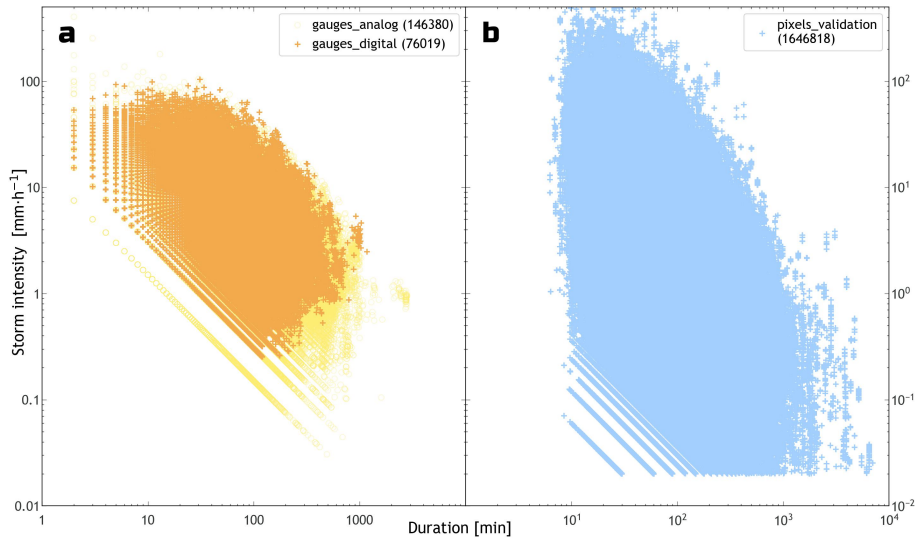


Figure 2. Scatter plots of storm intensity (y-axis, $\text{mm} \cdot \text{h}^{-1}$) against storm duration (x-axis, min), in log-log scale, for gauge, and validation datasets. Panel **a** - Recorded storms for the wet season (i.e., June through October) over the WGEW (see Sec. 2.1). The orange markers/crosses are records from the digital network, i.e., gauges from 2000 onwards (from June 2000 through October 2022, i.e., the validation dataset). The yellow markers/circles are records from the analog network, i.e., gauges prior to 2000 (from August 1953 through October 1999, i.e., the calibration dataset). Panel **b** - 23 years of simulated storm, each year having 30 runs. These storm intensity-duration “pairs” are obtained from the marginal PDFs fitted in the pre-processing module (see Sec. 2.9) for storm maximum intensity (MAXINT), and average duration (AVGDUR), after being randomly sampled (in the $0 \leq u, v \leq 1$ CDF-space) from a bivariate Gaussian copula (Eq. (4)) with $\rho = -0.31622$.

closed space, e.g., torus, sphere, circle (Breitenberger, 1963). The day of the year (DOY), and the time of the day (TOD), of an
 284 occurring storm, belong to such a set of variables. This innovation supports the analysis of how rainfall accumulates throughout
 a season, and how rainfall timing might be biased by the diurnal cycle (e.g., afternoon rainfall occurrence due to convective
 286 heating of the land surface).

STORM models storm start dates and times throughout a finite mixture of unimodal von Mises (vM) distributions. The
 288 vM distribution (also known as the Tikhonov distribution, e.g., Shmaliy (2005)) is a widely used PDF (in the circle space)
 given its simplistic parameterization, and mathematical tractability (e.g., Pewsey et al., 2013; Mardia and Jupp, 1999). The vM
 290 distribution is a close approximation of distributions such as the Cardiod, the wrapped Cauchy, and the wrapped normal. This
 latter (as its name suggests) is the equivalent of wrapping the normal distribution (from the linear space) into the circular space
 292 (Mardia and Jupp, 1999, chap. 3).

The model for a finite mixture of vM (MvM) PDFs (for a random variable θ) is given by (e.g., Jammalamadaka and Sen-
 294 Gupta, 2001, chap. 4.3):

$$f(\theta | \{p, \mu, \kappa\}_{i=1}^M) = \sum_{i=1}^M p_i \cdot \frac{e^{\kappa_i \cdot \cos(\theta - \mu_i)}}{2\pi \cdot I_0(\kappa_i)},$$

with $0 \leq \theta, \mu_i < 2\pi$, $0 \leq p_i \leq 1$, and $\sum_{i=1}^M p_i = 1$. (6)

296 In Eq. (6), p_i is the mixing proportion of the i -unimodal vM distribution (i.e., everything to the right of p_i); κ {for $\kappa \geq 0$ }
 is the concentration parameter that quantifies the sparseness/spreadness of the distribution around its mean direction μ ; and
 298 $I_0(\kappa)$ is the modified Bessel function of the first kind with order 0, and argument κ . Jammalamadaka and SenGupta (2001, Eq.
 2.2.7), and/or Mardia and Jupp (1999, Eq. 3.5.19), for instance, define $I_0(\kappa)$ as:

$$300 I_0(\kappa) = \frac{1}{2\pi} \int_0^{2\pi} e^{\kappa \cdot \cos(\theta)} d\theta = \sum_{s=0}^{\infty} \frac{1}{(s!)^2} \left(\frac{\kappa}{2}\right)^{2 \cdot s}. \quad (7)$$

This latter, i.e., the term most to the right in Eq. (7), is the power series expansion (in infinite series form). Parameters μ , and
 302 $1/\kappa$ (Eq. (6)) are analogous to the mean μ , and variance σ^2 of the normal distribution.

Eq. (6) has no analytical solution. Hence, STORM uses the `vonMisesMixtures`⁵ package, which computes the pa-
 304 rameters (μ, κ, p) via Maximum Likelihood Estimators within an Expectation-Maximization framework (e.g., Hornik and
 Grün, 2013; Dhillon and Sra, 2003). The description of such an algorithm is beyond the scope of this work. At its core, the
 306 `vonMisesMixtures` package uses the `iv` object from `scipy`'s module `special` for the Modified Bessel function (Virtanen
 et al., 2020; Temme, 1975), and the `fsolve` object from `scipy`'s module `optimize` for the root finding (of non-linear
 308 functions). `fsolve`, ultimately is a wrapper for a modified Powell's hybrid method (Moré et al., 1980, p. 57-64, 71-78); this
 latter, an algorithm for nonlinear optimization (Powell, 2009, 1970).

310 Table 1 presents the estimated parameters for mixtures of 1, 3, and 5 vM-PDFs. Given the storm start DOY and TOD,
 STORM transforms those date-time stamps into radians, and feeds them to the `vonMisesMixtures` package, along with
 312 the number of vM PDFs to compute the mixture. The conversion from decimal-based days (d_{dec}) into radians (d_{rad}), follows:
 $d_{rad} = \pi(2 \cdot d_{dec}/365 - 1)$; for $0 \leq d_{dec} \leq 365$, and $-\pi \leq d_{rad} \leq +\pi$. Similarly, the conversion from decimal-based hours
 314 (h_{dec}) into radians (h_{rad}), follows: $h_{rad} = \pi(h_{dec}/12 - 1)$; for $0 \leq h_{dec} \leq 24$, and $-\pi \leq h_{rad} \leq +\pi$. Figure 3 shows the
 fitted mixtures reconstructed from the parameters in Table 1, along with the circular distribution of DOY, and TOD. In Fig. 3b,
 316 the optimal (and more parsimonious) fit for TOD is given by 3 MvM-PDFs. A fit for 5 MvM-PDFs is also presented in Fig. 3b,
 even though it is overshadowed by the 3 MvM-PDFs. This shows the preference (and optimality) of the latter model not only
 318 to capturing in detail the (potential) multimodality of the TOD distribution (e.g. afternoon and nighttime storms being the most
 common between June and October) but also offering a less burdensome/intensive parameter estimation, with regard to the
 320 former model (i.e., a 5 MvM-PDFs). Disregarding its circular framework, the TOD histogram presented in Fig. 3 is consistent
 with that of Eagleson et al. (1987, Fig. 5). Appendix A presents the rationale behind the optimum selection of 5 MvM-PDFs for
 322 DOY, and 3 MvM-PDFs for TOD, which are the default settings in STORM. Still, we encourage the user to assess the optimal
 number of vM PDFs on an case-by-case basis.

⁵<https://framagit.org/fraschelle/mixture-of-von-mises-distributions>

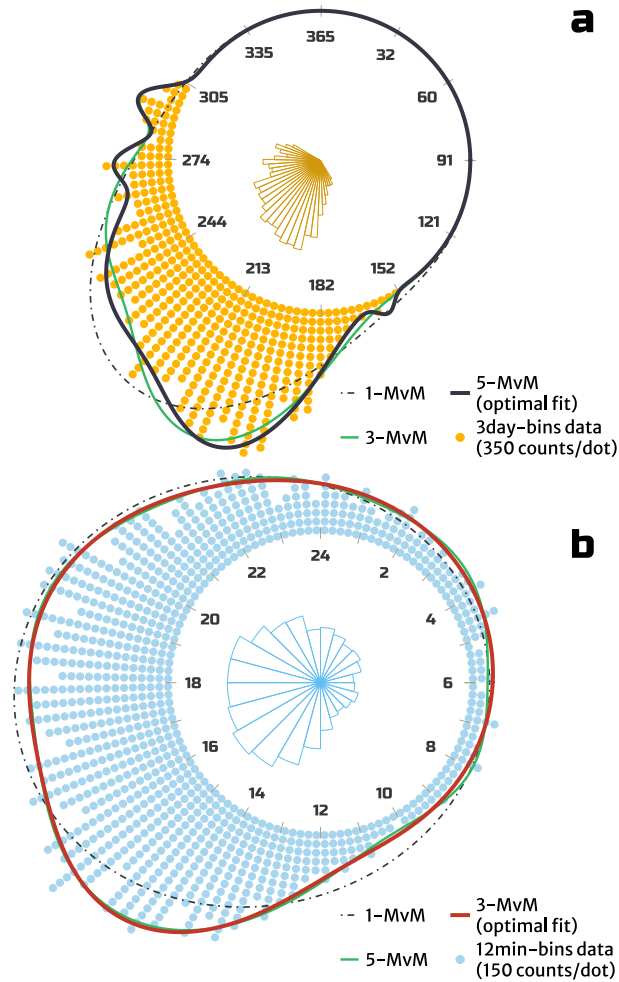


Figure 3. Panel **a** - Circular distribution for 3-day binned-data of (storm start) days of year (DOY; orange dots, each dot representing 350 counts). The black continuous curve indicates the optimal mixture of von Mises (MvM) probability density functions (PDFs), a mixture of 5 vM-PDFs, in this case (see Appendix A). The green curve represents a fit for 3 MvM-PDFs. A 5 day-bin circular histogram is also plotted on the inside. Panel **b** - Circular distribution for 12-min binned-data of (storm start) times of day (TOD; blue dots, each dot representing 150 counts). The red continuous curve indicates the optimal MvM-PDFs, i.e., 3 MvM-PDFs, in this case. The (almost imperceptible) green curve represents a fit for 5 MvM-PDFs. A 1 h-bin circular histogram is plotted on the inside. In both panels, the dashed black curves represent a fit of just 1 vM-PDF. The size of the sample is $\sim 146k$ values, for both DOY and TOD, encompassing the wet seasons (June through October) from 1953 through 1999, in the WGEW (see Sec. 2.1). Table 1 (Sec. 2.7) displays the parameters μ , κ , and p which the vM PDFs are constructed from.

324 The choice to implement an approach like the MvM-PDFs allows the end-user to account for potential multimodality (and
 326 installing/running the `vonMisesMixtures` package (as it is not shipped through the `conda` channels (Anaconda Software

Distribution, 2023)); or that they simply do not want to follow such an approach, STORM can still run without this feature (once
 328 it is turned off). In that case, STORM finds the best fit throughout a set of discrete probability mass functions (PMFs) for the
 DOY; and samples TOD from a uniform distribution (upscaled to the 00:00 – 24:00 h domain). Supplemental Figure B3 shows
 330 the best fit of a PMF for DOY in the WGEW dataset. In sup. Fig. B3, one can see the advantages of using a more elaborate
 model. i.e., MvM-PDFs, with regard to a simple PMF model. Having a statistical model for DOY is another improvement over
 332 STORM 1.0. Thus, we avoid modelling inter-arrival, and do not contradict the notion of rainfall modelling from a (Poisson)
 point-process perspective (e.g., Eagleson et al., 1987).

334 Both TOD, and DOY sampling take place independently from one another. Then, they are glued together into full date-time
 stamps (i.e., DOYEAR, and DATIME). Although theoretically possible, the probability of having two storms simulated at the
 336 same location with the very same date-time stamp is extremely low.

Table 1. Mean dates, and times μ (in decimal days of year for DOY, and in decimal hours for TOD, respectively), concentration parameters κ , and mixing proportions p for 1, 3, and 5 mixtures of von Mises (MvM) probability density functions (PDFs). For instance, for the time of day (TOD), and for the 3 MvM PDFs, μ (in radians) are 0.691, 1.707, and 2.557, i.e., (in decimal hours) 14.64, 18.52, and 21.77 (where $0_{\text{rad}} = 12:00$, and $-\pi / +\pi = 00:00/24:00$). The parameters for the 5, and 3 MvM PDFs are respectively the default for the DOY, and TOD models in STORM. These defaults are defined in the `pre_processing.py` script/module (and in the input file `ProbabilityDensityFunctions_ONE-ANALOG.csv`). The fitted PDFs presented in Fig. 3 (and sup. Fig. B3) can be reconstructed by plugging these parameters into Eqs. (7) and (6).

	#-MvM	pdf-1	pdf-2	pdf-3	pdf-4	pdf-5	
DOY	1	μ	-	-	223.9547	-	-
		κ	-	-	3.9086	-	-
		p	-	-	1.0000	-	-
	3	μ	-	207.1516	252.9430	-	294.0633
		κ	-	9.3424	9.2696	-	122.8981
		p	-	0.6533	0.3062	-	0.0405
	5	μ	158.0482	201.3853	238.3692	273.6777	293.2942
		κ	287.1728	15.5872	9.4628	129.0467	104.7193
		p	0.0118	0.4657	0.4250	0.0445	0.0531
TOD	1	μ	-	-	-	17.5157	-
		κ	-	-	-	1.0544	-
		p	-	-	-	1.0000	-
	3	μ	-	-	14.6420	18.5217	21.7681
		κ	-	-	6.3909	3.0643	0.4700
		p	-	-	0.2492	0.3245	0.4263
	5	μ	3.3158	8.0591	15.0518	19.0519	22.4794
		κ	4.6405	8.4354	3.7416	5.9302	3.7813
		p	0.0825	0.0424	0.4667	0.2400	0.1683

2.8 Scaling Factors & Orographic Stratification

338 One key feature carried on from its predecessor is STORM's capability to model potential future climate change scenarios
throughout two scaling factors (f_1, f_2), applied to TOTALP (total seasonal rainfall), and MAXINT (maximum storm intensity).
340 Equation (8) is a generic equation where U represents the variable to be scaled (i.e., TOTALP or MAXINT), U^* its new value
after being modified by factors f_1 or f_2 , and k the iterator for the number of years per simulation, namely NUMSIMYRS.

$$342 \quad U^* = U \cdot (1 + f_1 + (f_2 \cdot k)), \quad 0 < k \leq \text{NUMSIMYRS}. \quad (8)$$

Equation (8) implies that for every simulated year one can apply either a factor f_1 , which yields a constant increase (or
344 decrease) for every year throughout the whole span of the simulation, or a factor f_2 which progressively increases (or decreases)
with regard to the previous simulated year. For instance, a factor $f_1 = -0.1$ will decrease by 10% every sampled TOTALP in
346 any given n -years simulation, indicating a progressively drying climate; whereas a factor $f_2 = +0.1$ will double the value of
sampled TOTALP at the end of a 10-year simulation, characterizing a climate that is getting wetter, for instance. Both factors
348 (f_1, f_2) are expressed as percentages, and are mutually exclusive, i.e., STORM ensures they cannot be applied at the same
time, even though Eq. (8) suggests the opposite (this constraint can easily be removed in the source code, though). Otherwise,
350 the effect of each factor in the output becomes somewhat challenging to disentangle.

For TOTALP, $f_1 = \text{PTOT_SC}$, and $f_2 = \text{PTOT_SF}$; whereas for MAXINT, $f_1 = \text{STORMINESS_SC}$, and $f_2 = \text{STORMINESS_SF}$
352 (i.e., variables used in the script `rainfall.py`). A legacy from STORM 1.0, PTOT_SC is a factor that simulates (percentage)
step changes in the catchment wetness (seasonal precipitation totals); whereas PTOT_SF is a fractional scaling factor (progres-
354 sive percentage) that simulates temporal trends in seasonal totals. Similarly, STORMINESS_SC simulates step changes in
storminess (increase/decrease in maximum storm intensities); whereas STORMINESS_SF is a fractional scaling trend in max-
356 imum intensities. Section 3.2 shows the results for one simulation where PTOT_SC = +0.5 (Fig. 8; and sup. Fig. B7b); and
another where STORMINESS_SF = -0.035 (Fig. 7; and sup. Fig. B7a).

358 STORM now offers the possibility to simulate storm rainfall (e.g., intensity and duration) at different elevation bands, so
orographic effects are taken into account. The basic (and simplest) setup of STORM only requires the catchment shapefile
360 (SHP) to determine the spatial domain over which the simulation(s) will take place. In this is scenario, it is not possible to
determine any elevation bands from the SHP, and STORM reverts back to sampling storm intensity-duration pairs from the
362 "global" copula, i.e. the copula model retrieved from all gauge data (see Sec. 2.6, and Fig. 2). On the other hand, if the user
provides a SHP and its digital elevation model (DEM), STORM can compute as many copulas as elevation bands the catchment
364 is split into (e.g., based on hypsometric analysis). To this end, and during the pre-processing stage (see Sec. 2.9.1), the user must
define such elevation bands, and STORM will compute one copula per elevation band (as long as as the storm/gauge dataset
366 also provides the elevation of the gauge network, which is almost always the case). During the simulation/validation stage, the
extent of the storm is defined, then overlapped to the DEM, and STORM calculates the median elevation, which is ultimately
368 used to infer which copula (band) maximum rainfall intensity must be sampled from. By default, STORM calculates the median
elevation of the storm extent over the DEM. Nevertheless, this metric can be changed to another statistic, for instance, the mean

370 (see Sec. 2.9.1). [Supplemental Fig. B5](#) shows the capability of STORM to account for orography, in this case, the simulation
 of different sets of storms at three elevation bands, e.g., up to 1350, between 1350 and 1500, and above 1500 m.a.s.l. We found
 372 [no significant differences in simulated or measured storms among any of these three bands, which can be attributed to the low
 orographic gradient within the WGEW.](#)

374 2.9 Extras

2.9.1 Pre-Processing Module

376 This module is divided in two parts: 1) the actual module that processes all gauge data and generates the [pdfs-PDFs](#) that
 STORM uses as input; and 2) the file *parameters.py*, where all “soft-” and “hard-coded” parameters/variables are placed, and
 378 can be read/ingested by STORM.

Table 2. First and last four rows of the (sorted) storm event-based gauge data used by the script *pre_processing.py* to compute the
 best-fit parameters presented in Table 4. In the S column, W indicates a storm occurring within the established wet season, whereas D is for
 storms out of such a wet season. The complete table/data can be found in the file *gage_data-1953Aug18-1999Dec29_eventh-ANALOG.csv*,
 located in the folder/path *model_input/data_WG*.

Gage	Year	DOY	Hour	S	Duration (min)	Depth (mm)
RG022	1953	230	13.000	W	20	1.02
RG022	1953	233	13.083	W	29	8.38
RG022	1953	243	8.000	W	24	1.52
RG036	1953	230	0.167	W	24	6.10
⋮	⋮	⋮	⋮	⋮	⋮	⋮
RG100	1999	259	20.400	W	146	3.30
RG100	1999	262	21.133	W	44	0.25
RG100	1999	263	23.250	W	153	2.54
RG100	1999	265	18.550	W	12	1.78

The standalone script *pre_processing.py* ingests event- and aggregated-based gauge data to best-fit PDFs for several
 380 variables (see Tables 2, and 3). These storm variables are: total seasonal rainfall - TOTALP, maximum extent - RADIUS, rainfall
 decay rate - BETPAR, maximum intensity - MAXINT, average duration - AVGDUR, intensity-duration copula - COPULA,
 382 starting date - DOYEAR, and starting time - DATETIME. [The best-fitted PDFs are generated through Python’s library *fitter*](#)
 (Cokelaer et al., 2023). [For a given variable/parameter, STORM’s pre-processing module passes to *fitter* post-processed data](#)
 384 [along with several families of probability distributions that might be adequate for its fitting. At its core, *fitter* uses *scipy*’s](#)
[object *fit* \(from the *stats* module; see Sec. 2.6\) “to extract the parameters of that distribution that best fit the data”. This](#)
 386 [is done via either the Maximum Likelihood Estimation method or the Method of Moments \(Virtanen et al., 2020\). Because](#)

several probability distributions are passed to *fitter* (distributions which users can modify according to their needs), the latter finds the best-fitted parameters for such distributions, and computes several assessment metrics: Error Sum of Squares (SSE), AIC (Akaike’s information criterion), and BIC (Bayesian information criterion; see Appendix A). The pre-processing module selects the fitted PDF with the lowest BIC (this assessment metric can be modified too by the user). The impact of parameter misspecification and estimation error and/or uncertainty on the performance of STORM is also beyond the scope of the present work. Tools like *fitter* are practical implementations that ultimately reduce to a minimum these sort of potential impacts in STORM’s performance/outcomes.

Table 3. Twelve rows of the storm aggregated gauge data used by the script `pre_processing.py` to compute the best-fit for total seasonal rainfall (TOTALP in Table 4). In the S column, W indicates a month within the established wet season, whereas D is for months out of such a wet season. The complete table/data can be found in the file `gage_data-1953Aug-1999Dec_aggregateh-ANALOG.csv`, located in the folder/path `model_input/data_WG`.

Gage	Year	month	S	Rain (mm)
⋮	⋮	⋮	⋮	⋮
RG080	1990	1	D	11.94
RG080	1990	2	D	17.78
RG080	1990	3	D	9.65
RG080	1990	4	D	4.57
RG080	1990	5	D	4.32
RG080	1990	6	W	17.53
RG080	1990	7	W	150.88
RG080	1990	8	W	97.54
RG080	1990	9	W	59.69
RG080	1990	10	W	18.29
RG080	1990	11	D	24.13
RG080	1990	12	D	29.97
⋮	⋮	⋮	⋮	⋮

~~The statistical distribution parameters are~~ After the PDF fitting and selection is done, the PDF best-fitted parameters are then exported to a CSV (Comma-Separated Values) file (stored in the `model_input/data_WG` folder) that is later read during the simulation/validation stage. Appending the tags “_PDF” (probability density function), “_RHO” (copula ρ -parameter), and “_VMF” (von Mises PDF) allows STORM to read all the necessary statistical parameters stored in one single file (see Table 4). The number 1 appended to the PDF, RHO, and VMF tags indicates that the preprocessing was done for only one wet season. If analyses are carried out for more than one wet season, STORM replicates the same analyses for every season, appending numerical tags accordingly (e.g., file `ProbabilityDensityFunctions_TWO-ANALOG-py.csv`). If the analysis requires elevation stratification, STORM generates MAXINT, and AVGDUR PDFs for each elevation band, and appends a “Z#” tag to distinguish them from the all-gauges-based PDFs (see Table 4, rows 6-11 and 13-15). For the directional/circular variables DOYEAR, and

Table 4. Parameters of PDFs that best fit the WGEW gauge data for a given random variable. `_PDF` indicates probability density functions; `_RHO` refers to the copula ρ -parameter; and `_VMF` indicates a von Mises PDF. The number next to the aforementioned nomenclature refers to the wet season for which the variable is estimated/fit. In this case there is only one wet season, thus the number 1. The “Z#” tag refers to the elevation band for which the parameters (of the random variable) are estimated. If the variable does not present such a tag (i.e., rows 1 – 5, 12, and 16 – 23) that means that the parameters were estimated/fit regardless elevation. Except for COPULA, DATIME, and DOYEAR, the end-string indicates the pdf-family to which the parameters belong to; so STORM (via *scipy*) can construct the adequate PDF. For variables built upon PDFs, i.e., rows 1-11, par-1 and par-2 columns are respectively for the mean, and the variance. If the PDF presents more than two parameters (i.e., par-3, and/or par-4) they are for location, and scale. For COPULA, par-1 represents the correlation parameter ρ (see Sec. 2.6). For DOYEAR, and DATIME, “m#” indicates the number of vM-PDFs that make up the mixture, i.e., 5-vM for DOYEAR (see Sec. 2.7), and 3-vM for DATIME; and columns par-1, par-2, par-3 respectively represent their p , μ (in radians), κ parameters (see Table 1). This table is produced by the script `pre_processing.py`, exported as *ProbabilityDensityFunctions_ONE-ANALOG.csv* into the *model_input* folder/path, and later ingested by STORM.

Variable's pdf (or parameter)	par-1	par-2	par-3	par-4
TOTALP_PDF1+gumbel_1	5.512	0.226		
RADIUS_PDF1+johnsonsb	1.519	1.270	-0.279	20.798
BETPAR_PDF1+exponnorm	8.287	0.018	0.010	
MAXINT_PDF1+expon	0.106	6.996		
AVGDUR_PDF1+geninvgauss	-0.090	0.770	2.843	82.079
MAXINT_PDF1+Z1+expon	0.109	5.761		
MAXINT_PDF1+Z2+expon	0.106	7.114		
MAXINT_PDF1+Z3+expon	0.305	7.353		
AVGDUR_PDF1+Z1+geninvgauss	-0.106	0.609	5.046	74.205
AVGDUR_PDF1+Z2+geninvgauss	-0.084	0.812	2.380	83.780
AVGDUR_PDF1+Z3+fisk	1.434	10.178	57.545	
COPULA_RHO1+	-0.316			
COPULA_RHO1+Z1	-0.277			
COPULA_RHO1+Z2	-0.313			
COPULA_RHO1+Z3	-0.440			
DATIME_VMF1+m1	0.249	0.692	6.391	
DATIME_VMF1+m2	0.325	1.707	3.064	
DATIME_VMF1+m3	0.426	2.557	0.470	
DOYEAR_VMF1+m1	0.045	1.570	129.047	
DOYEAR_VMF1+m2	0.012	-0.421	287.173	
DOYEAR_VMF1+m3	0.466	0.325	15.587	
DOYEAR_VMF1+m4	0.425	0.962	9.463	
DOYEAR_VMF1+m5	0.053	1.907	104.719	

DATETIME, STORM appends as many “m#” tags as the number of vM PDFs required for the given mixture (see Table 4, last 404 8 rows).

2.9.2 Visualization Tool

406 GIF (Graphics Interchange Format)⁶ animations of selected simulations are created via the script `animation.py` (located in STORM’s *xtras* folder/path). STORM’s simulations (or validations) are stored in NetCDF (Network Common Data Form)⁷ 408 files, i.e., one file per each season containing m -simulations each one of n -years. Once the NetCDF files are produced for a given simulation/validation, the user can easily create animations (and/or snapshots) depicting the evolution of storm events 410 during the wet season, along with its seasonal aggregation within the defined catchment. An example of such an animation can be found in the README.md (page) of STORM’s repository⁸. The snapshots from which the animation is built upon look like 412 Fig. 1.

2.10 STORM’s skeleton

414 Starting from the pre-processing module (see Algorithm 1), STORM ingests pre-processed storm data in the format presented in Tables 2, and 3. The output of this pre-processing module is the file *ProbabilityDensityFunctions_ONE-ANALOG.csv*, 416 containing the parameters of several PDFs needed to stochastically model rainfall storms. Table 4 presents the aforementioned file in its entirety.

418 Algorithm 2 is the cornerstone of STORM. This algorithm shows the main steps required to simulate storm rainfall, relating all the stochastic variables previously described. Algorithm 3 (script `storm.py`) is the wrapper responsible for: 1) gathering 420 the input files/parameters (scripts `parameters.py`, and `parse_input.py`); 2) verifying that all the necessary file/parameters, and variables are correctly set, and allocated (script `check_input.py`); and 3) ultimately call Algorithm 2 (i.e., script 422 `rainfall.py`).

Algorithm 1 Pre-Processing module

```
create CSV file {all the processes below write into this file}
read (pre-processed) gauge data and metadata
fit (wet) seasonal PDF
estimate and fit radii PDF
estimate and fit rainfall decay rate and maxima intensity
compute intensity-duration copula {with stratification or not}
compute and fit DOY and TOD PDFs
```

⁶software developed by CompuServe (<https://www.w3.org/Graphics/GIF/spec-gif87.txt>)

⁷software developed by UCAR/Unidata (<http://doi.org/10.5065/D6H70CW6>)

⁸<https://github.com/feliperiosg/STORM2>

Algorithm 2 Computes and exports storm rainfall

```
for  $i \leq$  SEASONS do
  create NetCDF file
  for  $j \leq$  NUMSIMS do
    for  $k \leq$  NUMSIMYRS do
      TOTALP  $\leftarrow$  sample total seasonal rainfall
      TOTALP  $\leftarrow$  TOTALP  $\cdot (1 + f_1 + f_2 \cdot k)$ 
      NUM_S  $\leftarrow$  40 * 5 {initial number of storms}
      CUM_S  $\leftarrow$  0 {initial cumulative rainfall}
      while CUM_S < TOTALP  $\wedge$  NUM_S  $\geq$  2 do
        CENTERS  $\leftarrow$  sample center geolocations
        BETPAR  $\leftarrow$  sample rainfall decay rates
        RADIUS  $\leftarrow$  truncated sampling of radii
        stratification {if requested}
        MAXINT, AVGDUR  $\leftarrow$  copula sampling
        MAXINT  $\leftarrow$  MAXINT  $\cdot (1 + f_1 + f_2 \cdot k)$ 
        DOYEAR, DATIME  $\leftarrow$  sample of date-times
        rasterisation
        interpolation
        aggregation {CUM_S updated}
        NUM_S  $\leftarrow$  NUM_S/2
      end while
      write into NetCDF file
    end for
  end for
  close NetCDF file
end for
```

Algorithm 3 STORM in a nutshell

```
Require: input parameters {passed to the shell or read from a file}
Ensure: input parameters make sense
  call Algorithm 2 {simulates rainfall}
```

3 Results and Discussion

424 3.1 Evaluation of STORM

We carried out a validation run to evaluate the performance of STORM. In STORM, a “validation” run is equivalent to a
426 “simulation” run (thus we interchangeably use these terms). The difference is that for a “simulation” run the catchment mask
is exported along with the output file, whereas for the “validation” run the mask of the gauge network (for which the validation
428 exercise is carried out) is the one stored in the output. We ran through STORM 30 simulation runs, each comprising 23 years.
The above is equivalent to having $\sim 1.65 \times 10^6$ storms, compared against the $\sim 76,000$ storms (for the wet season) measured
430 by the automatic network from 2000 through 2022, i.e., the validation dataset.

In general terms, STORM does well what it was set up to do, that is, to reach the median precipitation over the entire
432 catchment. This can be seen from the boxplots presented in Fig. 4a where the (pixel/gauge aggregated) median for the validation
dataset (228.3 mm) is just 5% larger than the median for the gauge data (217.4 mm). This difference is mainly due to STORM
434 always stopping after the (sampled) median seasonal total (TOTALP) is reached. Therefore, STORM seasonal aggregates (on
average) will always be larger than the sampled value of reference. One advantage of such a stochastic approach is the ability
436 to reach maxima (and minima) seasonal totals (per station/pixel) outside the inter-quartile range of the gauge dataset; thus
accounting for unrecorded (but potential) extreme events.

438 Due to the introduction of a new statistical characterization of storm start date/time (DOY, and TOD), STORM now captures
some of the intra-seasonal variability of rainfall. This can be seen in the percentile time series of cumulative seasonal rainfall
440 presented in Fig. 4b. This latter plot shows how (on average) the cumulative rainfall, over the WGEW, slowly rises to a peak
(inflexion point in the solid orange line) halfway through the wet season, from which then follows a slow and steady decline
442 until November. Such a seasonal intra-variability is replicated by STORM (solid blue line), having a final underestimation of
5.5% (i.e., 236.1 mm) with regard to the actual seasonal (cumulative) median of 249.9 mm. In the case that any user does not
444 follow the circular statistics approach (see Sec. 2.7), STORM does also replicate rainfall intra-seasonal variability by using
a discrete pmf (dashed black line in Fig. 4b). However, it should be emphasized that STORM does not represent other local
446 hydrometeorological patterns, and global teleconnections (e.g., Sarachik and Cane, 2010; Diaz and Markgraf, 2000; Philander,
1990) that might contribute to intra- and inter-seasonal rainfall variability. The [modelling of teleconnection phenomena/patterns](#)
448 [in STORM was beyond the scope of this work. Nevertheless, such patterns could be empirically represented for particular](#)
[seasons by altering either the rainfall total PDF \(TOTALP\) or maximum storm intensity \(MAXINT\) respectively via the scaling](#)
450 [factors PTOT or STORMINESS \(see Sec. 2.8\). For a control run, i.e., one without climate drivers \(see Sec. 3.2\), the scatter](#)
plot presented in Fig. 5 ~~clearly~~ shows STORM’s inability to depict extreme stormy seasons, either wetter or drier than those
452 in the historical distribution (i.e., a very low coefficient of determination ($\rho^2 = 0.0028$); $\rho^2 = 0.0028$). For instance, gauge data
tell us that the years 2022, and 2020 had the wettest and driest seasons of the last two decades, respectively. The seasonal
454 averages (for the whole gauge network) were 429.9 mm for 2022, and 82.5 mm for 2020. These seasonal (mean) extremes
contrast with the systematic simulations (30 runs for each year) for which the validation dataset averages 237.0 mm for 2022,
456 and 222.2 for 2020. Nonetheless, and regardless of the intra- and inter-annual rainfall variabilities, the seasonal average pixel

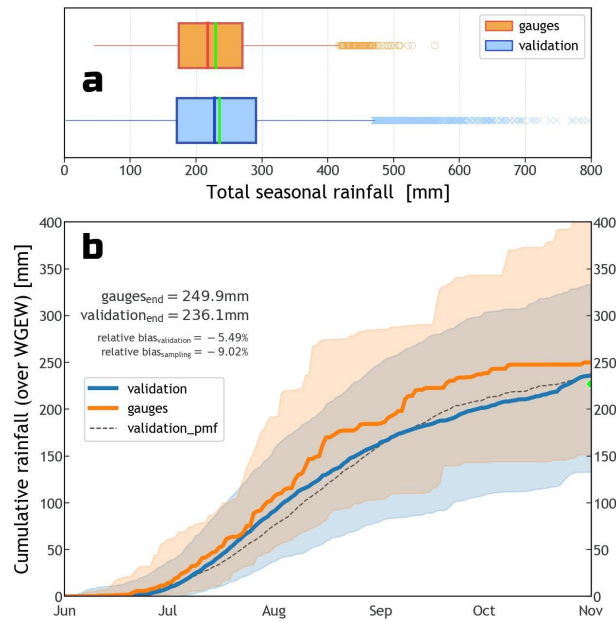


Figure 4. Panel **a** - Distribution of storm rainfall totals (for the wet season) year-by-year, and station/pixel-based, i.e., not spatially averaged over the catchment. Blue represents the validation dataset ($\sim 50.6\text{k}$ samples), whereas orange is for the gauge dataset ($\sim 1.9\text{k}$ samples). The bright green line (inside the boxplots) represents the mean of the distribution, i.e., 229.2mm and 235.4mm respectively for gauge and validation sets. Panel **b** - Percentile time series for the 90^{th} -percentile of all time series from June through October (wet season), for the validation (blue), and gauge (orange) datasets. The solid lines represent the median(s) of each dataset (50^{th} -percentile). The dashed black line represents the median for a validation where DOY was modeled through a discrete pmf (see sup. Fig. B3). The green marker at the end of the time series indicates the median of the sampled (simulated) values of total seasonal rainfall (TOTALP). Supplemental Fig. B4 shows percentile time series for the 100^{th} -percentile.

total (235.4mm) is just 3.3% 3.2% larger than the seasonal average gauge total (228.0mm). ~~The modelling of teleconnection phenomena/patterns in STORM was beyond the scope of this work; but it could be represented empirically by altering the rainfall total PDF (TOTALP) by the scaling factors for particular seasons.~~ 228.1mm). Having a low (auto)-correlation is not considered a bad feature in STORM and other stochastic models. As suggested and demonstrated by e.g., (Kim et al., 2017), a model performing better in metrics such as mean rainfall (and variance) rather than in auto-correlation (and probability of zero rainfall) is more suitable in practical applications because watershed response variables like runoff volume and peak flow are much more sensitive to the former than to the latter. We emphasize again here that STORM is not designed to reproduce accurate time series of rainfall (compared to the historical data) but to produce multiple plausible rainstorms while remaining faithful to catchment-wide rainfall “global” statistics.

The boxplots in Fig. 6a represent the distribution of number of storms during the wet season for both validation (blue), and gauge (orange) datasets. Once again, one can see how STORM, despite being close to the average number of storms in a season (32), fails to account for the inter-annual variability in storm rainfall present in the gauge records. The average number

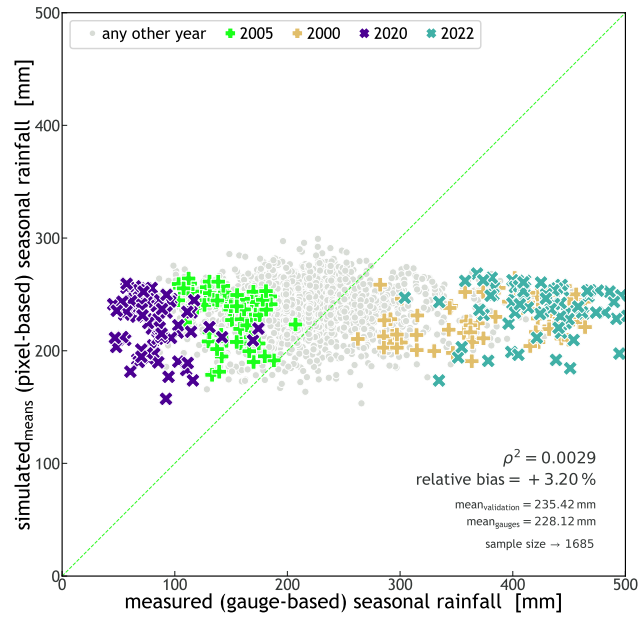


Figure 5. Scatter plot of simulated (means) seasonal rainfall against measured seasonal rainfall. Each marker ~~cross~~ represents a pixel/station for which the seasonal totals of 30 simulations were averaged (y-axis), and the actual seasonal total recorded for that location (x-axis). The color scale varies over x-markers indicate the 23 simulated years wettest (2022) and driest seasons (2020), from 2000 through 2022. Within the plot, it is indicated the coefficient of determination (ρ^2 , which is the square of the coefficient of correlation); the medians of the datasets; the relative bias between them; and the size of the sample (an average of 73.3 gauges per year). The green line indicates a 1 : 1 line.

of storms for the gauge data is (39). When disaggregated by year (see Fig. 6a), the maximum average number of storms (66.3) is found for the year 2022 (with a global maxima of 79 storms), whereas the minimum average (20.6) is for 2020 (13 of global minima). As illustrated in the scatter plot, 2022, and 2020 match the years for maximum and minimum (average) seasonal totals, respectively; indicating the direct relationship between the number of storms in a given season, and its total precipitation.

We selected three gauges sparsely located throughout the WGEW, and compared the temporal distribution of their median, and mean storm intensities. The boxplots in Fig. 6b (all three rows) show that the median yearly storm intensities produced by STORM (blue boxes) are consistently lower than the median yearly intensities measured by the gauge network (orange boxes). On average, and throughout the whole validation exercise, the average median storm intensities from gauge data (4.0 mm · h⁻¹) is 48.8% larger than the average from the medians of simulated storms (2.7 mm · h⁻¹). Nonetheless, and when accounting for the mean, recorded storm intensities (7.1 mm · h⁻¹) are 16.2% lower than the mean of simulated storm intensities (8.5 mm · h⁻¹). This is mainly attributed to extremely large simulated storms (see sup. Fig. B6a). In spite of its inability to model inter-annual storm variability, the stochasticity embedded in STORM allows for plausible storm intensities larger and smaller than those (ever) recorded by the gauge network (see sup. Fig. B6a where the average maximum simulated intensities is 12.6 mm · h⁻¹; with maxima over 100 mm · h⁻¹, see Sec 2.1).



Figure 6. Yearly boxplots for the validation (blue), and gauge (orange) datasets. Panel **a** - Distribution of the number of storms in a wet season. Panel **b** - Distribution of storm intensities of three stations, i.e., RG012, RG042, and RG072 inside the WGEW. In both panels, the green line within each boxplot represents the mean of the distribution. Please note the logarithmic scale of the y-axes in panel **b** (i.e., rainfall intensity). Supplemental Fig. B8 shows the (sparse) location of the aforementioned gauges.

484 One final validation exercise was to compare the top 10th-percentile of all storm intensities, of both gauge and validation
datasets (simulated maximum intensities also included). The storms maxima (by design, see Sec. 2.4) are found in the centres
486 of the storms, and can only be retrieved for the simulation dataset. The boxplots presented in sup. Fig. B6b show that, despite
STORM's ability to simulate (on average) extreme rainfall intensities about twice as large/high as those recorded by the
488 gauge network; the top 10th % of maxima simulated intensities are 44% larger than the top 10th % of storm intensities in the
gauge set. Supplemental Fig. B6a shows that on average, mean maxima intensities ($12.6 \text{ mm} \cdot \text{h}^{-1}$) are 76.5% larger than the
490 mean of actual/recorded intensities ($7.1 \text{ mm} \cdot \text{h}^{-1}$); and 47.9% larger than average simulated intensities. The above suggest
the robustness of the methodology here developed to account for maximum intensities when simulating the storms. It also
492 incorporates the theoretical understanding that individual gauges are unlikely to have recorded the maximum storm intensities.

3.2 Testing Climate Drivers

494 To evaluate the ability of STORM to account for potential future climate change scenarios, we carried out two additional
validation exercises. One where TOTALP is increased by a fixed scalar throughout the whole period, i.e., $\text{PTOT_SC} = +0.5$,
496 representing a wetter climate. The other where MAXINT is reduced by a progressive scalar, i.e., $\text{STORMINESS_SF} = -0.035$,
representing a decline in storm intensity. We are aware that these two scalars might not be realistic or even at all plausible.
498 Still, we chose those numbers as they enable drastic changes in the final outputs, thus allowing for straightforward comparisons
between these “climate-change” results, and the ones presented for the default validation (i.e., where no climate controls are
500 simulated).

With a progressive factor $\text{SF} = -0.035$, applied to the MAXINT variable, we force the sampled maximum storm intensity
502 of every simulated year to be 3.5% less than the year before. Hence, for a validation run of 23 years, one can expect that in
the last simulated year the (mean) decrease in maximum storm intensity would be 77% (i.e., $(23 - 1) \times 0.035$) less than the
504 first simulated year. The above can be seen in the yearly boxplots presented in Fig. 7. For any of the gauges presented in Fig.
7 (e.g., gauge RG042), one can see how the median rainfall intensity of the validation dataset, i.e., $0.68 \text{ mm} \cdot \text{h}^{-1}$ at the end of
506 the simulated period (2022) is 76% less than the median at the starting of the simulation (2000), i.e., $2.82 \text{ mm} \cdot \text{h}^{-1}$. 86.7%
less when compared to the the median at the end of the actual records (i.e., $5.08 \text{ mm} \cdot \text{h}^{-1}$). In STORM 1.0, the progressive
508 factor SF (over the MAXINT variable) is referred as “temporal trend in storminess” (Singer et al., 2018).

With a constant factor $\text{SC} = +0.5$, applied to the TOTALP variable, we force the sampled seasonal total rainfall of every
510 simulated year to be 50% higher than it normally would. Hence, no matter what year of a given validation one is running,
the expected (mean) increase in seasonal total will be roughly constant. This effect can be seen in the scatter plot presented in
512 Fig. 8. In this figure, the cloud of points (scatter) has shifted upwards ~~48.4%~~ 48.5% of the mean value for simulated seasonal
totals presented in Fig. 5, corresponding to a validation were no climate change scaling factor was applied. In STORM 1.0, the
514 constant factor SC (over the TOTALP variable) is referred as “step change in wetness”.

Supplemental Fig. B7 shows how the number of storms (in a wet season) is modified due to the (two) above mentioned
516 climate change factors. For the case in which TOTALP is increased by a fixed scalar (i.e., Fig. 8), STORM generates (on
average) more storms per season in order to reach the increased total seasonal rainfall. For the case in which MAXINT is

518 progressively reduced by a progressive scalar (i.e., Fig. 7), STORM is forced to continually increase the number of storms in order to reach the median (sampled) seasonal total.

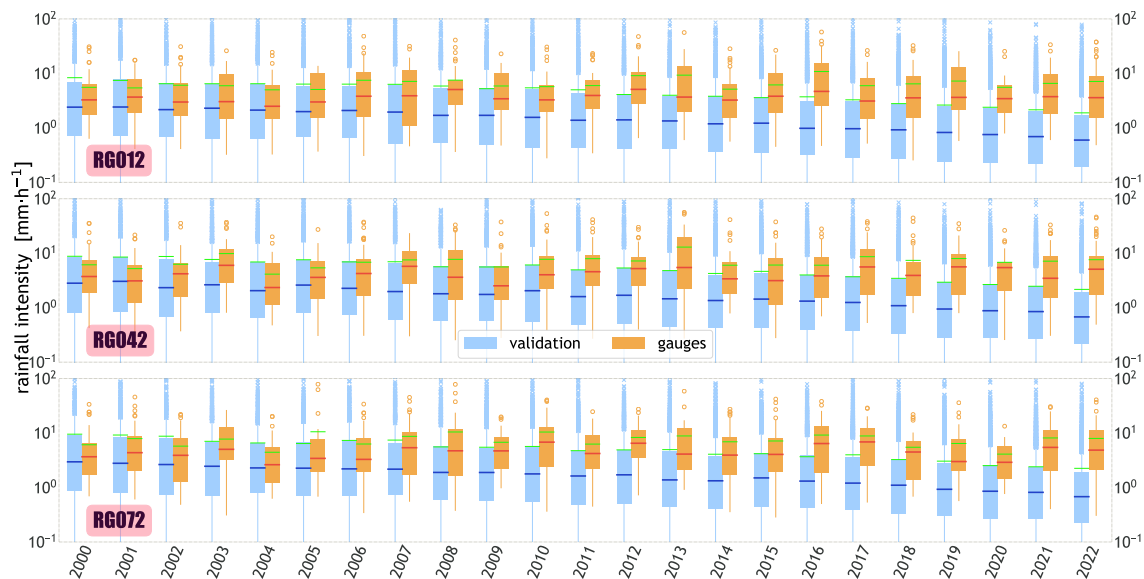


Figure 7. Distribution Yearly boxplots for the validation (blue), and gauge (orange) datasets. The boxplots represent the distribution of storm intensities of three stations, i.e., RG012, RG042, and RG072 inside the WGEW, for a validation dataset (blue) respectively top, middle, and bottom row. In all rows, the gauge set green line within each boxplot represents the mean of the distribution. Please note the logarithmic scale of the y-axis (orange, i.e., rainfall intensity). Supplemental Fig. B8 shows the (sparse) location of the aforementioned gauges. This plot is equivalent to Fig. 6b, except that here we force the sampled maximum storm intensity (MAXINT) to be 3.5% lower than the previous year (through the whole period). Thus, and after 23 years of any given simulation, the (mean) decrease in maximum storm intensity is 77% (less).

520 3.3 STORM Applications

522 These improvements to STORM 1.0 now make STORM suitable as a climate driver of other watershed response models that simulate hydrology (surface runoff, infiltration, streamflow) (Michaelides and Wilson, 2007; Michaelides and Wainwright, 2002), groundwater recharge during and after rainfall events (Quichimbo et al., 2021), interactions between streamflow and alluvial aquifers (Evans et al., 2018), or even for representing ecohydrological responses of vegetation to climate forcing (e.g., Warter et al., 2023). It also enables STORM to be useful in water balance models (e.g., Land Surface Models) to assess water availability to plants through dynamic eco-hydrological simulation of plant-climate interactions and water utilization (Warter et al., 2021; D’Odorico et al., 2007; Caylor et al., 2006; Laio et al., 2006), as well as energy/carbon fluxes between the land surface and the atmosphere (Best et al., 2011; Bonan, 1996). Finally, STORM can also be used to drive geomorphic models that characterize erosion and deposition processes within drainage basins in response to sequences of rainfall and runoff

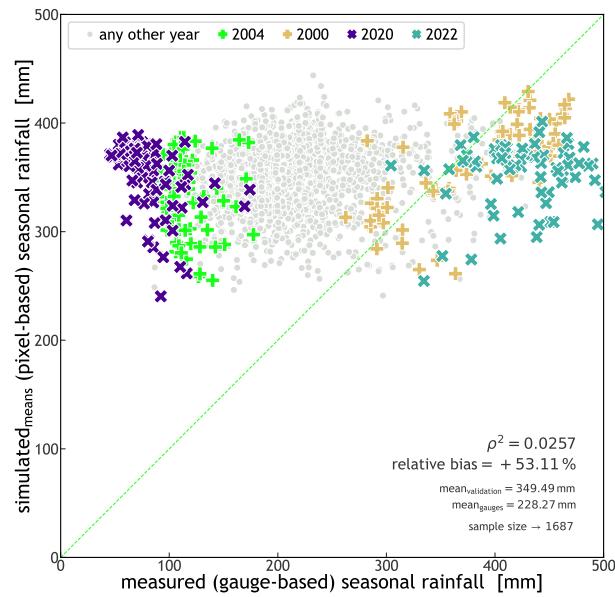


Figure 8. Scatter plot of simulated (means) seasonal rainfall against measured seasonal rainfall. This plot is equivalent to Fig. 5 except that here we force all simulated seasonal totals to be (every time) 50% larger than the sampled total seasonal rainfall (TOTALP).

530 (Michaelides and Singer, 2014; Michaelides and Martin, 2012), and even landscape evolution models that simulate landform
 532 development over longer timescales (Hobley et al., 2017; Tucker and Hancock, 2010). Coupling STORM to such models would
 enable a wide range of scientists to investigate key problems in the environment that have their origin in the climate system.
 These problems range from which water sources are used by plants (Sabathier et al., 2021; Sargeant and Singer, 2016; Singer
 534 et al., 2014; Dawson and Ehleringer, 1991) to what is the dominant source and timing of groundwater recharge (Quichimbo
 et al., 2020; Cuthbert et al., 2016; Wheeler et al., 2010; Scanlon et al., 2006) to the role of climate in shaping landscape
 536 morphology (Michaelides et al., 2018; Singer and Michaelides, 2014; Tucker and Bras, 2000; Tucker and Slingerland, 1997).
 The new STORM could also be integrated with stochastic models characterizing atmospheric evaporative demand (e.g., Asfaw
 538 et al., 2023), which would allow for closure of the water balance.

4 Summary and Conclusions

540 Built upon STORM 1.0, STORM⁹ is an improved Stochastic Rainfall ~~generator focused on gauged watersheds~~ Generator
applicable to (small) gauged watersheds (with detailed rainstorm records) in any climatic zone. This stochastic framework
 542 heavily relies on PDFs of total seasonal rainfall (TOTALP), maximum storm radius (RADIUS), decay rate of maximum rain-
 fall from the storm's centre towards its maximum radius (BETPAR), maximum rainfall intensity (MAXINT), average storm
 544 duration (AVGDUR), the copula's correlation parameter (COPULA), storm start date (DOYEAR), and the (optional) storm

⁹<https://github.com/feliperiosg/STORM2>

start time (DATIME). The main modelling features of STORM with regard to its predecessor are: storm intensity and duration
546 represented via a (bivariate) Gaussian copula framework; intensity-duration copulas at different elevation bands within the
catchment; storm time occurrence via a circular statistics approach (i.e., mixture of von Mises PDF) or via discrete PMFs;
548 storm start times via a circular statistics (optional); alternative implementation of future climate scenarios; output compressed
into (geo-referenced) NetCDF files, readily available for visualization; and pre-processing module to construct all necessary
550 PDFs from gauge data. Added to STORM, and with a future mindset of its applicability at larger scales, we implemented
capabilities such as: PDFs easily defined by the user (or retrieved from gauge data); storm simulation with regard to elevation
552 (provided a Digital Elevation Model - DEM); customizable spatial resolution (and Coordinate Reference System - CRS); spa-
tial operations under a raster framework, thus adding speed, versatility, and scalability; and optimal output storing in NetCDF
554 format.

To develop the stochastic model, we derived and calibrated all PDFs to 37 years of storm data, collected by an analog
556 network of 118 gauges sparsely deployed over the WGEW (148 km²). To test the performance of the model, we carried out
one validation exercise consisting of 30 runs, each one having 23 simulated years (i.e., 690 simulation-years in total). The
558 output of such a validation run was compared against 23 years of storm data, collected by the digital network of ~~94~~⁹³ gauges
located within the WGEW. To evaluate STORM's ability to model rainfall under potential future climate scenarios, we carried
560 out two more validation runs, each one comprising 690 simulation-years too. These results were also compared against the
digital/automatic gauge network.

562 Results showed that the seasonal total rainfall reached by STORM is 5.5% lower than the actual records, when accounted
as the spatial median of all the stations/pixels within WGEW (see Fig. 4b). If accounted on a temporal basis, i.e., without
564 any spatial averaging, this relative difference amounts to +5% (see Fig. 4a). On a seasonal basis, the storm mean rainfall
intensity recorded by the gauge network is 16.2% smaller than simulated storm intensities (see sup. Fig. B6a). Nevertheless,
566 the stochasticity embedded in our model allows for un-recorded but very plausible, either larger and/or smaller, storm intensities
(see Fig. 6b, and sup. Fig. B6). Results obtained for the varying-climate simulations showed that STORM is also able to imprint
568 seasonal variability on rainfall (either in intensities or totals) in long-term analyses.

5 Constraints and Recommendations

570 Future plans for improvement of STORM will be focused on moving from drainage basins to regions, allowing for a wider
range of applications such as land surface modeling. To achieve this, further improvements will be needed to characterize how
572 rainstorm characteristics vary across a region, so they can be represented within STORM's PDFs. Finally, it will necessitate
the use of gridded rainfall products for STORM to inform on the input PDFs.

574 The choice of a bivariate Gaussian copula was mainly driven on its simplicity/easy-configuration, and applicability. Nev-
ertheless, a further improvement (at least conceptually) might be the implementation of a more elaborate copula models (and
576 truly applicable to the intensity-duration case) like Extreme-Values, Archimedean, etc. (e.g., Chen and Guo, 2019; Zhang and
Singh, 2019; Salvadori and De Michele, 2006).

578 STORM’s current weakness is its inability to account for other local hydrometeorological patterns, and global teleconnec-
tions that may contribute to intra- and inter-seasonal rainfall variability (see Figs. 5, and 6a). This is something expected as
580 STORM (by design) does not incorporate any PDF that describes the behaviour of such inter-annual variability. Nevertheless,
STORM’s flexibility allows to roughly model the eventual impact of such teleconnections via the scaling factors PTOT_ or
582 STORMINESS_ (see Sec. 2.8).

Code and data availability. The current version of STORM v.2 is available from the project website: <https://github.com/feliperiosg/STORM2>
584 under the GPLv3 licence. The exact version of the model used to produce the results used in this paper is archived on Zenodo 8071820 (Rios
Gaona, 2023), as are pre- and post-processed data, and scripts to run the model. Documentation to run the model, and tools for its output
586 visualization are also provided in the aforementioned links.

Appendix A: BIC Estimation

588 The Bayesian information criterion (BIC; also known as Schwarz’s Bayesian criterion - SBC) is a metric used for the unbiased
assessment of the optimal number of M-unimodal vM distributions (e.g., Rios Gaona and Villarini, 2018; Lark et al., 2014).
590 Such a criterion allows the selection of the least complex of all the models in consideration, that is, the one with the lowest BIC.
From a mathematical point of view (Eq. (A1)), BIC (or similar models, i.e., AIC - Akaike’s information criterion) combines
592 the maximized log likelihood of the fitted model with a penalization term that is related to the number of estimated parameters
(Pewsey et al., 2013, Eq. (6.3)).

$$594 \text{BIC} = \nu \cdot \ln(n) - 2 \cdot \ell_{max}, \tag{A1}$$

where ℓ_{max} is the maximized (full) log-likelihood of a model with ν degrees of freedom, and n the number of observations.

596 Unfortunately, the `vonMisesMixtures` package does not offer a way to retrieve the maximized log-likelihood from
which to compute the BIC of the mixture of M-unimodal vM PDFs. Unlike Python’s `vonMisesMixtures` package, R (R
598 Core Team, 2023), jointly with the `movMF` package (Hornik and Grün, 2014), does offer the possibility to easily retrieve BIC
estimates for fitted MvM PDFs (Supp. Fig. A1). The implementation of such a feature in STORM was beyond the scope of
600 this work. Nevertheless, STORM does offer the script `pre_processing_circular.R`, which the entire circular analyses
(BIC included) can be computed from. Once this analysis is carried out, the user will have all the necessary elements to discern
602 the optimal fit for their “circular” data.

Figure A1 shows the DOY, and TOD BICs for mixtures ranging from 1 to 9 vM PDFs. Strictly speaking, and for the DOY
604 case, the lowest BIC found in the figure is for a mixture of 9 vM, i.e., -318370.54 . One can argue that a 9-MvM model
certainly over-fits the multimodality of DOY (see Fig. 3a), without even mentioning its computationally intensive parameter-
606 estimation. Nevertheless, if one looks at the 5-MvM model (BIC equals to -317840.12), one can see that the improvement
of the BIC metric is increasingly very small beyond this point in comparison to the 1-, to 4-MvM models. Therefore, we are

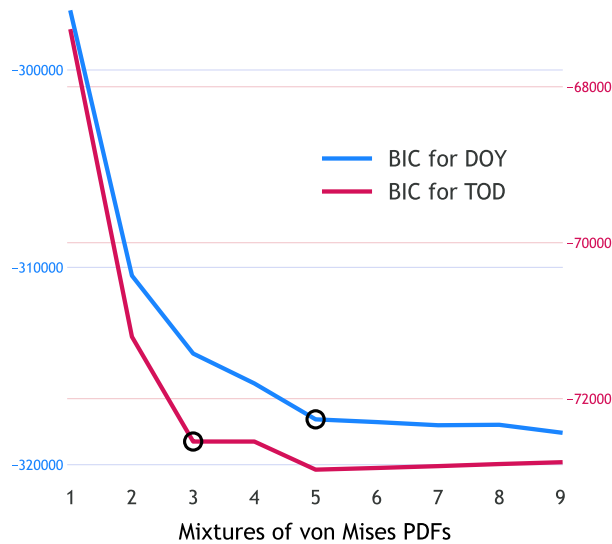


Figure A1. Bayesian information criterion (BIC) for mixtures that go from 1 to 9 von Mises (vM) probability density functions (PDFs). The blue line is for the BIC of day-of-year (DOY); whereas the red line is for the BIC of time-of-day (TOD). The color of the y-axes indicate the values of their respective BICs. The black circles indicate one of the lowest point of the related BIC curve. The lower the BIC the more optimal the number of vM PDFs (in the mixture) that best describes the sample multimodality. Thus, to avoid the selection of a model with too many vM-PDFs, the black circles also indicate where the change, in slope, is more drastic even if they are not global minima.

608 confident that a 5-MvM model not only accurately describes the multimodality of DOY (for the WGEW dataset) but also is
 610 faster in its parameter-estimation with regard to any larger (i.e., more vM PDFs) model. Hence, a mixture of 5 vM-PDFs is the
 default configuration for DOY in STORM. Following that train of thought, we found the 3-MvM model the optimal mixture
 for TOD, and thus its default settings in STORM.

612 **Appendix B: Supplemental Figures**

Author contributions. M.F. Rios Gaona wrote and extensively tested the code, did the analyses and visualizations, and completed the early
 614 version of this manuscript. M.B. Singer developed the idea, wrote the early version of this manuscript, revised the finished version of the
 manuscript, and provided valuable feedback. K. Michaelides revised the finished version of this manuscript.

616 *Competing interests.* The authors declare no competing interests.

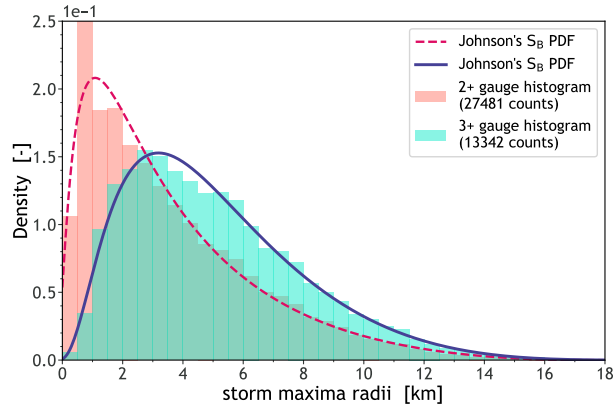


Figure B1. Probability density functions (PDFs) for maximum storm extent (RADIUS; see Sec. 2.3). The cyan area represents the histogram of maxima radii estimated from three or more gauges; whereas the salmon area is for a maxima radii distribution (obtained) from two or more gauges. The blue solid line indicates the best fit for the cyan histogram, i.e., a Johnson's S_B PDF (see Table 4, row 2). The red dashed line is also a Johnson's S_B PDF (with parameters: $a = 1.54$, $b = 0.953$, $loc = -0.228$, and $scale = 18.289$).

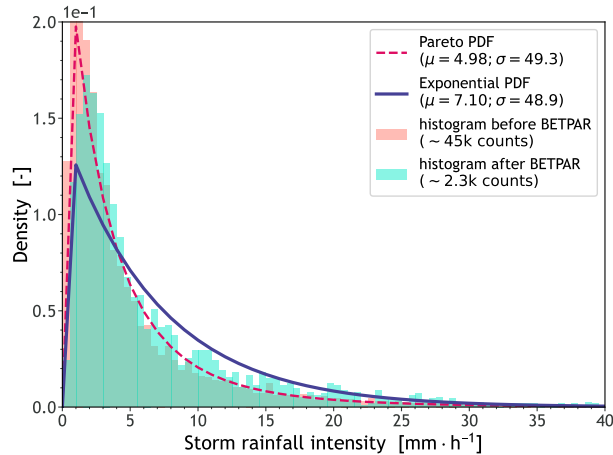


Figure B2. Probability density functions (PDFs) for storm rainfall measured by gauge data (salmon histogram), and for estimated maxima (cyan histogram). The blue solid line indicates the best fit for the cyan histogram, i.e., an exponential PDF (see Table 4, row 4); whereas the red dashed line (also a best fit) is a Pareto PDF. Maximum intensities are retrieved by fitting an exponential (quadratic) model $I(r) = I_{max} \cdot e^{-2 \cdot \beta^2 \cdot r^2}$ to measured storm rainfall (see Sec. 2.4). Note how the mean from estimated maximum intensities ($\mu = 7.10$) is larger than the mean of rainfall intensities measured by gauges ($\mu = 4.98$) prior any model fitting.

Disclaimer: The authors take no responsibility for the use or misuse of the provided code.

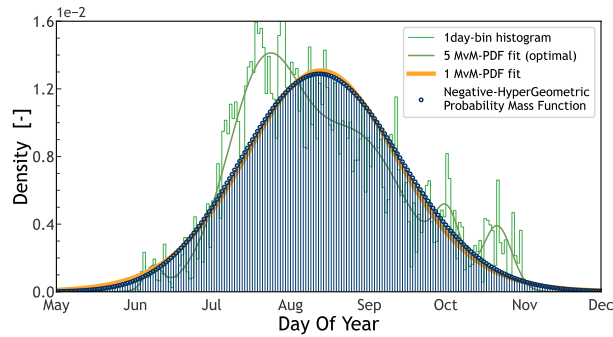


Figure B3. Probability mass function (PMF - vertical lines ending in blue circles) of a negative hyper-geometric family, fitted (best fit) to a distribution of storm start day-of-year (DOY - green histogram). The coarser green line represents the optimal fit of a mixture of 5 von Mises (MvM) PDFs for the aforementioned distribution; presented also in Fig. 3 (over a “circular” space; see Sec. 2.7). The orange line is a 1 MvM-PDF. Note its similarity with the PMF, and its poor fit of the underlying DOY-distribution with regard to the 5 MvM-PDFs fit.

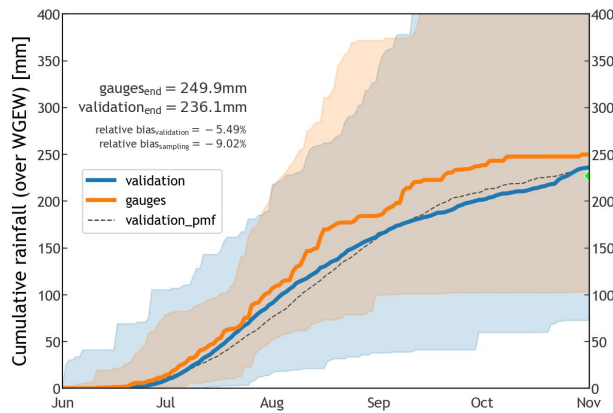


Figure B4. Percentile time series for the 100th-percentile of all time series from June through October (wet season), for the simulation/validation (blue), and gauge (orange) datasets. The solid lines represent the median(s) of each dataset (50th-percentile). The dashed black line represents the median for a validation where DOY was modeled through a discrete pmf (see sup. Fig. B3). The green marker at the end of the time series indicates the median of the sampled (simulated) values of total seasonal rainfall (TOTALP). By design, STORM stops once the sampled seasonal total is reached or surpassed (the probability of reaching exactly the sampled value is extremely low). Hence, the actual (median) simulated seasonal total will always be greater than the sampled TOTALP.

618 *Acknowledgements.* This work was supported by the European Union Horizon 2020 programme (DOWN2EARTH; grant no. 869550). We thank Owen Jones for his suggestions and comments.

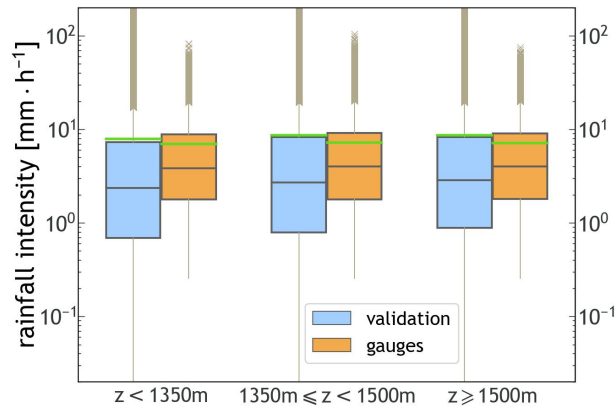


Figure B5. Distribution of storm station/pixel-based intensities by elevation bands (i.e., orography). Blue is for the validation dataset, whereas orange is for gauge data. The green lines represent the mean of the distributions. Please note the logarithmic scale of the y-axis. The x-axis, from left to right, indicate three elevation bands for which analyses were carried out, i.e. up to 1350 m.a.s.l., between 1350 and 1500 m.a.s.l., and above 1500 m.a.s.l. Given the low gradient in relative orography within the WGEW, rainstorm variability with regard to orography is not a stark characteristic in this case.

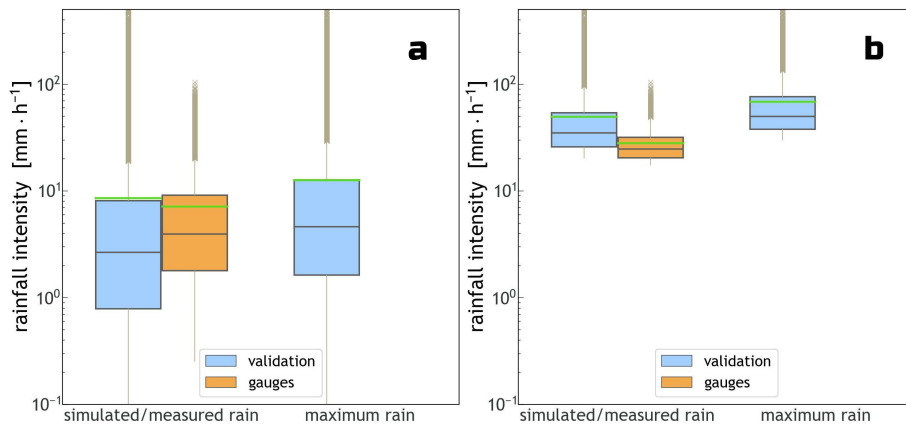


Figure B6. Distribution of storm station/pixel-based intensities. Panel **a** - for all data, i.e., 100th-percentile. Panel **b** - for the top 10th-percentile of all storm intensities. Blues-Blue is for the validation dataset, whereas orange is for gauge data. The green lines represent the mean of the distributions. Please note the logarithmic scale of the y-axes in both panels. The column most to the right is for the maxima intensities found in the storm centres (see Sec. 2.4). Such storm centre maxima are only retrieved for the validation dataset (no way to account for them in the gauge set).

620 **References**

Anaconda Software Distribution: Conda, <https://anaconda.com>, 2023.

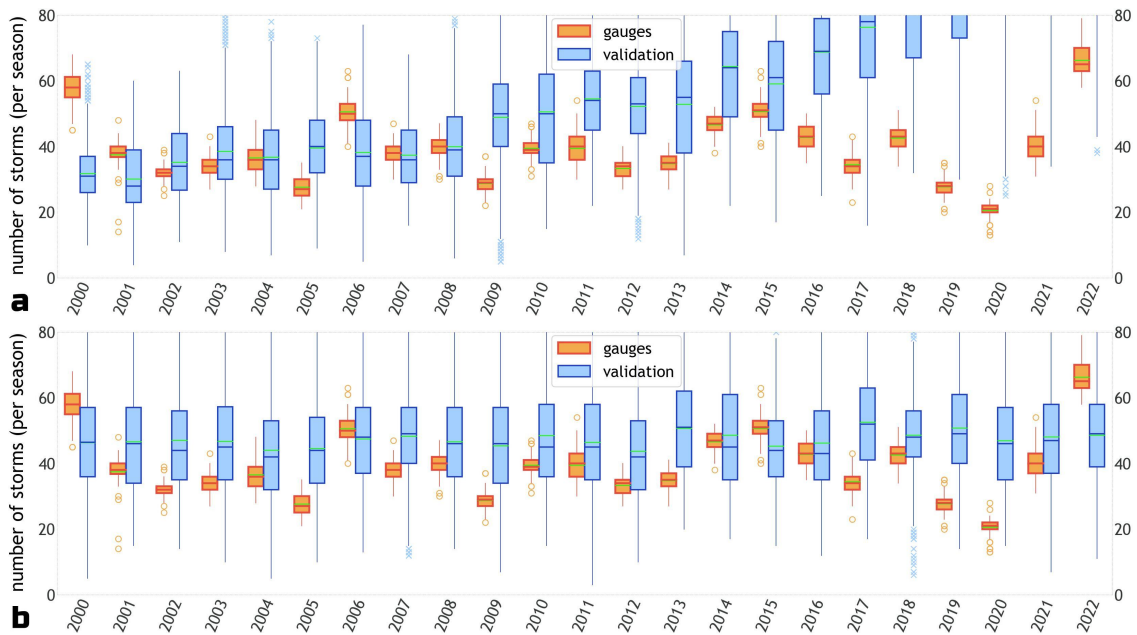


Figure B7. Distribution of the number of storms in a wet season, for the validation (blue), and gauge (orange) datasets. Panel **a** - Validation case for which MAXINT is reduced by a progressive scalar, i.e., $STORMINESS_SF = -0.035$ (see Fig. 7). Panel **b** - Validation case for which TOTALP is increased by a fixed scalar throughout the whole period, i.e., $PTOT_SC = +0.5$ (see Fig. 8). All y-axes are consistent with Fig. 6, panel **a**, to allow (visually) equivalent comparisons. Note how in panel **a** STORM generates more storms per season in order to reach the now increased total seasonal rainfall; whereas in panel **b** the progressive decrease in storm intensity forces STORM to continually increase the number of storms in order to reach the median (sampled) seasonal total.

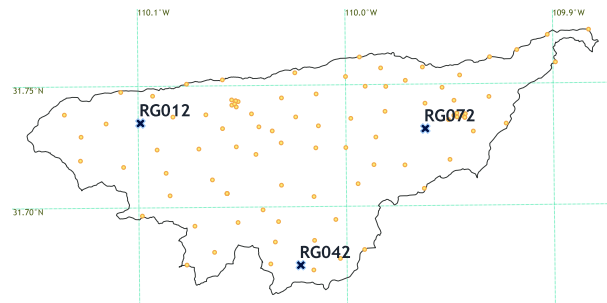


Figure B8. Digital gauge network for the WGEW (from 2000 through 2022). The 3 bold markers, i.e., gauges/stations RG012, RG042, and RG072, indicate the geo-location of the gauges referred to in Figs. 6, and 7. Even though the grid is presented in “lat-lon” coordinates (i.e., CRS WGS-84), the actual projection (in both panels) is the 2D-Cartesian coordinate system known as NAD83 / UTM zone 12N (i.e., EPSG:26912).

622 Asfaw, D. T., Singer, M. B., Rosolem, R., MacLeod, D., Cuthbert, M., Quichimbo, E. A., Rios Gaona, M. F., and Michaelides, K.: stoPET
v1.0: a stochastic potential evapotranspiration generator for simulation of climate change impacts, *Geosci. Model Dev.*, 16, 557–571,
624 <https://doi.org/10.5194/gmd-16-557-2023>, 2023.

- Benoit, L., Allard, D., and Mariethoz, G.: [Stochastic Rainfall Modeling at Sub-kilometer Scale, Water Resour. Res., 54, 4108–4130, https://doi.org/10.1029/2018WR022817, 2018.](https://doi.org/10.1029/2018WR022817)
- Berger, D.: Kendall's Rank Correlation vs Pearson's Linear Correlation: A Proof Of Greiner's Relation, <https://doi.org/10.2139/ssrn.2837712>, 2016.
- Best, M. J., Pryor, M., Clark, D. B., Rooney, G. G., Essery, R. L. H., Ménard, C. B., Edwards, J. M., Hendry, M. A., Porson, A., Gedney, N., Mercado, L. M., Sitch, S., Blyth, E., Boucher, O., Cox, P. M., Grimmond, C. S. B., and Harding, R. J.: The Joint UK Land Environment Simulator (JULES), model description - Part 1: Energy and water fluxes, *Geosci Model Dev*, 4, 677–699, <https://doi.org/10.5194/gmd-4-677-2011>, 2011.
- Bonan, G. B.: A Land Surface Model (LSM Version 1.0) for Ecological, Hydrological, and Atmospheric Studies: Technical Description and User's Guide (No. NCAR/TN-417+STR), Tech. Rep. NCAR/TN-417+STR, University Corporation for Atmospheric Research, <https://doi.org/10.5065/D6DF6P5X>, 1996.
- Branch, M. A., Coleman, T. F., and Li, Y.: A Subspace, Interior, and Conjugate Gradient Method for Large-Scale Bound-Constrained Minimization Problems, *SIAM J. Sci. Comput.*, 21, 1–23, <https://doi.org/10.1137/S1064827595289108>, 1999.
- Breitenberger, E.: Analogues of the normal distribution on the circle and the sphere, *Biometrika*, 50, 81–88, <https://doi.org/10.1093/biomet/50.1-2.81>, 1963.
- Burton, A., Kilsby, C., Fowler, H., Cowpertwait, P., and O'Connell, P.: [RainSim: A spatial-temporal stochastic rainfall modelling system, Environ. Modell. Softw., 23, 1356–1369, https://doi.org/10.1016/j.envsoft.2008.04.003, 2008.](https://doi.org/10.1016/j.envsoft.2008.04.003)
- Caylor, K. K., D'Odorico, P., and Rodriguez-Iturbe, I.: On the ecohydrology of structurally heterogeneous semiarid landscapes, *Water Resour Res*, 42, <https://doi.org/10.1029/2005WR004683>, 2006.
- Chen, L. and Guo, S.: Copulas and Its Application in Hydrology and Water Resources, no. 2364-8198 in Springer Water, Springer Singapore, 152 Beach Road, #21-01/04 Gateway East, Singapore 189721, Singapore, 1 edn., <https://doi.org/10.1007/978-981-13-0574-0>, 2019.
- Cokelaer, T., Kravchenko, A., lahdjirayhan, msat59, Varma, A., L. B., Stringari, C. E., Brueffer, C., Broda, E., Pruesse, E., Singaravelan, K., Li, Z., mark padgham, and negodfre: [cokelaer/fitter: v1.6.0, https://doi.org/10.5281/zenodo.8226571, 2023.](https://doi.org/10.5281/zenodo.8226571)
- Cuthbert, M. O., Acworth, R. I., Andersen, M. S., Larsen, J. R., McCallum, A. M., Rau, G. C., and Tellam, J. H.: Understanding and quantifying focused, indirect groundwater recharge from ephemeral streams using water table fluctuations, *Water Resour Res*, 52, 827–840, <https://doi.org/10.1002/2015WR017503>, 2016.
- Dai, Q., Han, D., Rico-Ramirez, M. A., and Islam, T.: Modelling radar-rainfall estimation uncertainties using elliptical and Archimedean copulas with different marginal distributions, *Hydrol. Sci. J.*, 59, 1992–2008, <https://doi.org/10.1080/02626667.2013.865841>, 2014.
- Dawkins, L. C., Osborne, J. M., Economou, T., Darch, G. J., and Stoner, O. R.: [The Advanced Meteorology Explorer: a novel stochastic, gridded daily rainfall generator, J. Hydrol., 607, 127 478, https://doi.org/10.1016/j.jhydrol.2022.127478, 2022.](https://doi.org/10.1016/j.jhydrol.2022.127478)
- Dawson, T. E. and Ehleringer, J. R.: Streamside trees that do not use stream water, *Nature*, 350, 335–337, <https://doi.org/10.1038/350335a0>, 1991.
- De Luca, D. L. and Petroselli, A.: [STORAGE \(STOchastic RAInfall GEnerator\): A User-Friendly Software for Generating Long and High-Resolution Rainfall Time Series, Hydrology, 8, https://doi.org/10.3390/hydrology8020076, 2021.](https://doi.org/10.3390/hydrology8020076)
- Dhillon, I. and Sra, S.: Modeling Data using Directional Distributions, Tech. Rep. TR-03-06, University of Texas: Department of Computer Science, Austin, TX, USA, https://www.cs.utexas.edu/users/inderjit/public_papers/tr03-06.pdf, 2003.
- Diaz, H. F. and Markgraf, V., eds.: *El Niño and the Southern Oscillation: Multiscale Variability and Global and Regional Impacts*, Cambridge University Press, <https://doi.org/10.1017/CBO9780511573125>, 2000.

Diez-Sierra, J., Navas, S., and del Jesus, M.: NEOPRENE v1.0.1: a Python library for generating spatial rainfall based on the Neyman–Scott process, *Geosci. Model Dev.*, 16, 5035–5048, <https://doi.org/10.5194/gmd-16-5035-2023>, 2023.

664

D’Odorico, P., Caylor, K., Okin, G. S., and Scanlon, T. M.: On soil moisture-vegetation feedbacks and their possible effects on the dynamics of dryland ecosystems, *J. Geophys. Res. G: Biogeosci.*, 112, <https://doi.org/10.1029/2006JG000379>, 2007.

666

Eagleson, P. S., Fennessey, N. M., Qinliang, W., and Rodriguez-Iturbe, I.: Application of spatial Poisson models to air mass thunderstorm rainfall, *J. Geophys. Res. D: Atmos.*, 92, 9661–9678, <https://doi.org/10.1029/JD092iD08p09661>, 1987.

668

Evans, C. M., Dritschel, D. G., and Singer, M. B.: Modeling Subsurface Hydrology in Floodplains, *Water Resour Res.*, 54, 1428–1459, <https://doi.org/10.1002/2017WR020827>, 2018.

670

Fang, K.-T., Kotz, S., and Ng, K. W.: Symmetric Multivariate and Related Distributions, no. 36 in Monographs on Statistics and Applied Probability, Chapman & Hall/CRC, 6000 Broken Sound Parkway NW, Suite 300 Boca Raton, FL 33487-2742, 1 edn., <https://doi.org/10.1201/9781351077040>, 1990.

672

Genest, C., Rémillard, B., and Beaudoin, D.: Goodness-of-fit tests for copulas: A review and a power study, *Insurance Math. Econom.*, 44, 199–213, <https://doi.org/10.1016/j.insmatheco.2007.10.005>, 2009.

674

Goodrich, D. C., Keefer, T. O., Unkrich, C. L., Nichols, M. H., Osborn, H. B., Stone, J. J., and Smith, J. R.: Long-term precipitation database, Walnut Gulch Experimental Watershed, Arizona, United States, *Water Resour Res.*, 44, <https://doi.org/10.1029/2006WR005782>, 2008.

676

Hobley, D. E. J., Adams, J. M., Nudurupati, S. S., Hutton, E. W. H., Gasparini, N. M., Istanbuloglu, E., and Tucker, G. E.: Creative computing with Landlab: an open-source toolkit for building, coupling, and exploring two-dimensional numerical models of Earth-surface dynamics, *Earth Surf. Dyn.*, 5, 21–46, <https://doi.org/10.5194/esurf-5-21-2017>, 2017.

678

Hofert, M., Kojadinovic, I., Mächler, M., and Yan, J.: Elements of Copula Modeling with R, no. 2197-5744 in *Use R!*, Springer Cham, Gewerbestrasse 11, 6330 Cham, Switzerland, 1 edn., <https://doi.org/10.1007/978-3-319-89635-9>, 2018.

682

Hornik, K. and Grün, B.: On maximum likelihood estimation of the concentration parameter of von Mises–Fisher distributions, *Comput. Statist.*, 29, 945–957, <https://doi.org/10.1007/s00180-013-0471-0>, 2013.

684

Hornik, K. and Grün, B.: movMF: An R Package for Fitting Mixtures of von Mises-Fisher Distributions, *J Stat Softw.*, 58, 1–31, <https://doi.org/10.18637/jss.v058.i10>, 2014.

686

Jammalamadaka, S. R. and SenGupta, A.: Topics in Circular Statistics, no. 5 in Series on Multivariate Analysis, World Scientific, P O Box 128, Farrer Road, Singapore 912805, <https://doi.org/10.1142/4031>, 2001.

688

Joe, H.: Dependence Modeling with Copulas, no. 134 in Monographs on Statistics and Applied Probability, Chapman & Hall/CRC, 6000 Broken Sound Parkway NW, Suite 300 Boca Raton, FL 33487-2742, 1 edn., <https://doi.org/10.1201/b17116>, 2014.

690

Keefer, T. O. and coauthors: Southwest Watershed Research Center and Walnut Gulch Experimental Watershed, Tech. Rep. SWRC Publ. Reference No. 1588, Southwest Watershed Research Center, 2000 East Allen Road, Tucson, AZ 85719, <http://www.tucson.ars.ag.gov/unit/publications/PDFfiles/1588.pdf>, 2007.

692

Kendall, M. G.: The Treatment of Ties in Ranking Problems, *Biometrika*, 33, 239–251, <https://doi.org/10.1093/biomet/33.3.239>, 1945.

694

Khedun, C. P., Mishra, A. K., Singh, V. P., and Giardino, J. R.: A copula-based precipitation forecasting model: Investigating the interdecadal modulation of ENSO’s impacts on monthly precipitation, *Water Resour Res.*, 50, 580–600, <https://doi.org/10.1002/2013WR013763>, 2014.

696

Kim, D., Cho, H., Onof, C., and Choi, M.: Let-It-Rain: a web application for stochastic point rainfall generation at ungaged basins and its applicability in runoff and flood modeling, *Stoch. Env. Res. Risk A.*, 31, 1023–1043, <https://doi.org/10.1007/s00477-016-1234-6>, 2017.

698

Kleiber, W., Katz, R. W., and Rajagopalan, B.: Daily spatiotemporal precipitation simulation using latent and transformed Gaussian processes, *Water Resour. Res.*, 48, <https://doi.org/10.1029/2011WR011105>, 2012.

700

Laio, F., D'Odorico, P., and Ridolfi, L.: An analytical model to relate the vertical root distribution to climate and soil properties, *Geophys Res Lett*, 33, <https://doi.org/10.1029/2006GL027331>, 2006.

Langworthy, B. W., Stephens, R. L., Gilmore, J. H., and Fine, J. P.: Canonical correlation analysis for elliptical copulas, *J. Multivariate Anal.*, 183, 104715, <https://doi.org/10.1016/j.jmva.2020.104715>, 2021.

Lark, R. M., Clifford, D., and Waters, C. N.: Modelling complex geological circular data with the projected normal distribution and mixtures of von Mises distributions, *Solid Earth*, 5, 631–639, <https://doi.org/10.5194/se-5-631-2014>, 2014.

Mai, J.-F. and Scherer, M.: Simulating Copulas, no. Vol. 6 in *Quantitative Finance*, World Scientific, 5 Toh Tuck Link, Singapore 596224, 2 edn., <https://doi.org/10.1142/10265>, 2017.

Mardia, K. and Jupp, P.: *Directional Statistics*, Wiley Series in Probability and Statistics, John Wiley & Sons, Ltd., West Sussex, PO19 1UD England, <https://doi.org/10.1002/9780470316979>, 1999.

McNeil, A. J., Frey, R., and Embrechts, P.: *Quantitative Risk Management: Concepts, Techniques and Tools*, Princeton Series in Finance, Princeton University Press, 41 William Street, Princeton, New Jersey 08540, revised edn., <https://doi.org/10.5555/2811305>, 2015.

Meles, M. B., Demaria, E. M. C., Heilman, P., Goodrich, D. C., Kautz, M. A., Armendariz, G., Unkrich, C., Wei, H., and Perumal, A. T.: Curating 62 Years of Walnut Gulch Experimental Watershed Data: Improving the Quality of Long-Term Rainfall and Runoff Datasets, *Water*, 14, <https://doi.org/10.3390/w14142198>, 2022.

Michaelides, K. and Martin, G. J.: Sediment transport by runoff on debris-mantled dryland hillslopes, *J. Geophys. Res. Earth Surf.*, 117, <https://doi.org/10.1029/2012JF002415>, 2012.

Michaelides, K. and Singer, M. B.: Impact of coarse sediment supply from hillslopes to the channel in runoff-dominated, dryland fluvial systems, *J. Geophys. Res. Earth Surf.*, 119, 1205–1221, <https://doi.org/10.1002/2013JF002959>, 2014.

Michaelides, K. and Wainwright, J.: Modelling the effects of hillslope-channel coupling on catchment hydrological response, *Earth Surf Proc Land*, 27, 1441–1457, <https://doi.org/10.1002/esp.440>, 2002.

Michaelides, K. and Wilson, M. D.: Uncertainty in predicted runoff due to patterns of spatially variable infiltration, *Water Resour Res*, 43, <https://doi.org/10.1029/2006WR005039>, 2007.

Michaelides, K., Hollings, R., Singer, M. B., Nichols, M. H., and Nearing, M. A.: Spatial and temporal analysis of hillslope-channel coupling and implications for the longitudinal profile in a dryland basin, *Earth Surf Proc Land*, 43, 1608–1621, <https://doi.org/10.1002/esp.4340>, 2018.

Moran, M. S., Holifield Collins, C. D., Goodrich, D. C., Qi, J., Shannon, D. T., and Olsson, A.: Long-term remote sensing database, Walnut Gulch Experimental Watershed, Arizona, United States, *Water Resour Res*, 44, <https://doi.org/10.1029/2006WR005689>, 2008.

Moré, J. J., Garbow, B. S., and Hillstom, K. E.: User Guide for MINPACK-1, Tech. Rep. ANL-80-74, Argonne National Laboratory, Argonne, IL, USA, <https://www.math.utah.edu/software/minpack/>, 1980.

Morin, E., Goodrich, D. C., Maddox, R. A., Gao, X., Gupta, H. V., and Sorooshian, S.: Rainfall modeling for integrating radar information into hydrological model, *Atmos Sci Lett*, 6, 23–30, <https://doi.org/10.1002/asl.86>, 2005.

Nelsen, R. B.: *An Introduction to Copulas*, no. 2197-568X in *Springer Series in Statistics*, Springer New York, New York, NY 10013, USA, 2 edn., <https://doi.org/10.1007/0-387-28678-0>, 2006.

Nicholson, S. E.: *Dryland Climatology*, Cambridge University Press, The Edinburgh Building, Cambridge CB2 8RU, UK, <https://doi.org/10.1017/CBO9780511973840>, 2011.

Osborn, H. B.: Timing and duration of high rainfall rates in the southwestern United States, *Water Resour Res*, 19, 1036–1042, <https://doi.org/10.1029/WR019i004p01036>, 1983.

Osborn, H. B. and Lane, L.: Precipitation-runoff relations for very small semiarid rangeland watersheds, *Water Resources Res.*, 5, 419–425,
740 <https://doi.org/10.1029/WR005i002p00419>, 1969.

[Papalexiou, S. M., Serinaldi, F., and Porcu, E.: Advancing Space-Time Simulation of Random Fields: From Storms to Cyclones and Beyond, Water Resour. Res., 57, e2020WR029466, https://doi.org/10.1029/2020WR029466, 2021.](https://doi.org/10.1029/2020WR029466)
742 [Paschalis, A., Molnar, P., Faticchi, S., and Burlando, P.: A stochastic model for high-resolution space-time precipitation simulation, Water Resour. Res., 49, 8400–8417, https://doi.org/10.1002/2013WR014437, 2013.](https://doi.org/10.1002/2013WR014437)
744 [Peleg, N., Faticchi, S., Paschalis, A., Molnar, P., and Burlando, P.: An advanced stochastic weather generator for simulating 2-D high-resolution climate variables, J. Adv. Model. Earth Syst., 9, 1595–1627, https://doi.org/10.1002/2016MS000854, 2017.](https://doi.org/10.1002/2016MS000854)
746

Pewsey, A., Neuhäuser, M., and D., R. G.: *Circular Statistics in R*, Oxford University Press, Great Clarendon Street, Oxford, OX2 6DP,
748 United Kingdom, 1 edn., 2013.

Philander, S. G.: El Niño, La Niña, and the Southern Oscillation., no. 46 in *International Geophysics Series*, Academic Press, San Diego,
750 California 92101, US, 1990.

Powell, M. J. D.: A Hybrid Method for Nonlinear Equations, in: *Numerical Methods for Nonlinear Algebraic Equations*, edited by Rabinowitz, P., chap. 6, pp. 87–114, Gordon and Breach Science Publishers, 150 Fifth Avenue, New York, N.Y. 10011, U.S., 1970.

Powell, M. J. D.: On nonlinear optimization since 1959, in: *The Birth of Numerical Analysis*, edited by Bulthee, A. and Cools, R., pp.
754 141–160, World Scientific, 5 Toh Tuck Link, Singapore 596224, https://doi.org/10.1142/9789812836267_0009, 2009.

Quichimbo, E. A., Singer, M. B., and Cuthbert, M. O.: Characterising groundwater-surface water interactions in idealised ephemeral stream
756 systems, *Hydrol. Process.*, 34, 3792–3806, <https://doi.org/10.1002/hyp.13847>, 2020.

Quichimbo, E. A., Singer, M. B., Michaelides, K., Hogley, D. E. J., Rosolem, R., and Cuthbert, M. O.: DRYP 1.0: a parsimonious hydrological
758 model of DRYland Partitioning of the water balance, *Geosci. Model Dev.*, 14, 6893–6917, <https://doi.org/10.5194/gmd-14-6893-2021>, 2021.

760 R Core Team: *R: A Language and Environment for Statistical Computing*, R Foundation for Statistical Computing, Vienna, Austria, <https://www.R-project.org/>, 2023.

762 Renard, K. G. and Keppel, R. V.: Hydrographs of Ephemeral Streams in the Southwest, *J. Hydr. Eng. Div-asce.*, 92, 33–52, <https://doi.org/10.1061/JYCEAJ.0001419>, 1966.

764 Renard, K. G. and Laursen, E. M.: Dynamic Behavior Model of Ephemeral Stream, *J. Hydr. Eng. Div-asce.*, 101, 511–528, <https://doi.org/10.1061/JYCEAJ.0004340>, 1975.

766 Rios Gaona, M. F.: ~~feliperiosg~~/STORM2: v2-~~1.1~~-2.0, <https://doi.org/10.5281/zenodo.10159533>, 2023.

Rios Gaona, M. F. and Villarini, G.: Characterization of the diurnal cycle of maximum rainfall in tropical cyclones, *J Hydrol*, 564, 997–1007,
768 <https://doi.org/10.1016/j.jhydrol.2018.07.062>, 2018.

Ross, S. M.: *Simulation*, Academic Press, Radarweg 29, PO Box 211, 1000 AE Amsterdam, The Netherlands, 5 edn.,
770 <https://doi.org/10.1016/C2011-0-04574-X>, 2013.

Sabathier, R., Singer, M. B., Stella, J. C., Roberts, D. A., and Caylor, K. K.: Vegetation responses to climatic and geologic controls on water
772 availability in southeastern Arizona, *Environ. Res. Lett.*, 16, 064029, <https://doi.org/10.1088/1748-9326/abfe8c>, 2021.

Salvadori, G. and De Michele, C.: Statistical characterization of temporal structure of storms, *Adv Water Resour*, 29, 827–842,
774 <https://doi.org/10.1016/j.advwatres.2005.07.013>, 2006.

Sarachik, E. S. and Cane, M. A.: *The El Niño-Southern Oscillation Phenomenon*, Cambridge University Press, The Edinburgh Building,
776 Cambridge CB2 8RU, UK, <https://doi.org/10.1017/CBO9780511817496>, 2010.

778 Sargeant, C. I. and Singer, M. B.: Sub-annual variability in historical water source use by Mediterranean riparian trees, *Ecohydrology*, 9,
1328–1345, <https://doi.org/10.1002/eco.1730>, 2016.

780 Scanlon, B. R., Keese, K. E., Flint, A. L., Flint, L. E., Gaye, C. B., Edmunds, W. M., and Simmers, I.: Global synthesis of groundwater
recharge in semiarid and arid regions, *Hydrol Process*, 20, 3335–3370, <https://doi.org/10.1002/hyp.6335>, 2006.

782 Seabold, S. and Perktold, J.: Statsmodels: Econometric and Statistical Modeling with Python, in: Proceedings of the 9th Python in Science
Conference, edited by Stéfan van der Walt and Jarrod Millman, pp. 92–96, <https://doi.org/10.25080/Majora-92bf1922-011>, 2010.

784 Shmaliy, Y. S.: Von Mises/Tikhonov-based distributions for systems with differential phase measurement, *Signal Process*, 85, 693–703,
<https://doi.org/10.1016/j.sigpro.2004.11.008>, 2005.

786 Singer, M. B. and Michaelides, K.: How is topographic simplicity maintained in ephemeral dryland channels?, *Geology*, 42, 1091–1094,
<https://doi.org/10.1130/G36267.1>, 2014.

788 Singer, M. B. and Michaelides, K.: Deciphering the expression of climate change within the Lower Colorado River basin by stochastic
simulation of convective rainfall, *Environ Res Lett*, 12, 104011, <https://doi.org/10.1088/1748-9326/aa8e50>, 2017.

790 Singer, M. B., Sargeant, C. I., Piégay, H., Riquier, J., Wilson, R. J. S., and Evans, C. M.: Floodplain ecohydrology: Climatic, an-
thropogenic, and local physical controls on partitioning of water sources to riparian trees, *Water Resour Res*, 50, 4490–4513,
<https://doi.org/10.1002/2014WR015581>, 2014.

792 Singer, M. B., Michaelides, K., and Hogley, D. E. J.: STORM 1.0: a simple, flexible, and parsimonious stochastic rainfall generator for
simulating climate and climate change, *Geosci Model Dev*, 11, 3713–3726, <https://doi.org/10.5194/gmd-11-3713-2018>, 2018.

794 Stillman, S., Zeng, X., Shuttleworth, W. J., Goodrich, D. C., Unkrich, C. L., and Zreda, M.: Spatiotemporal Variability of Summer Precipi-
tation in Southeastern Arizona, *J Hydrometeorol*, 14, 1944–1951, <https://doi.org/10.1175/JHM-D-13-017.1>, 2013.

796 Temme, N.: On the numerical evaluation of the modified bessel function of the third kind, *J. Comput. Phys.*, 19, 324–337,
[https://doi.org/10.1016/0021-9991\(75\)90082-0](https://doi.org/10.1016/0021-9991(75)90082-0), 1975.

798 The Economist: In defense of the Gaussian copula, electronic periodical, [https://www.economist.com/free-exchange/2009/04/29/
in-defense-of-the-gaussian-copula](https://www.economist.com/free-exchange/2009/04/29/in-defense-of-the-gaussian-copula), accessed on: 2022-10-05, 2009.

800 Tjøstheim, D., Otneim, H., and Støve, B.: Statistical Modeling Using Local Gaussian Approximation, Academic Press, 125 London Wall,
London EC2Y 5AS, United Kingdom, <https://doi.org/10.1016/C2017-0-02646-0>, 2022.

802 Tucker, G. E. and Bras, R. L.: A stochastic approach to modeling the role of rainfall variability in drainage basin evolution, *Water Resour*
Res, 36, 1953–1964, <https://doi.org/10.1029/2000WR900065>, 2000.

804 Tucker, G. E. and Hancock, G. R.: Modelling landscape evolution, *Earth Surf Proc Land*, 35, 28–50, <https://doi.org/10.1002/esp.1952>, 2010.

806 Tucker, G. E. and Slingerland, R.: Drainage basin responses to climate change, *Water Resour Res*, 33, 2031–2047,
<https://doi.org/10.1029/97WR00409>, 1997.

808 Van Rossum, G. and Drake, F. L.: Python 3 Reference Manual, CreateSpace, Scotts Valley, CA, [https://dl.acm.org/doi/book/10.5555/
1593511](https://dl.acm.org/doi/book/10.5555/1593511), 2009.

810 Vandenberghe, S., Verhoest, N. E. C., Onof, C., and De Baets, B.: A comparative copula-based bivariate frequency analysis of observed and
simulated storm events: A case study on Bartlett-Lewis modeled rainfall, *Water Resour Res*, 47, <https://doi.org/10.1029/2009WR008388>,
2011.

812 Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., Burovski, E., Peterson, P., Weckesser, W., Bright, J.,
van der Walt, S. J., Brett, M., Wilson, J., Millman, K. J., Mayorov, N., Nelson, A. R. J., Jones, E., Kern, R., Larson, E., Carey, C. J., Polat,
814 Ī., Feng, Y., Moore, E. W., VanderPlas, J., Laxalde, D., Perktold, J., Cimrman, R., Henriksen, I., Quintero, E. A., Harris, C. R., Archibald,

816 A. M., Ribeiro, A. H., Pedregosa, F., van Mulbregt, P., and SciPy 1.0 Contributors: SciPy 1.0: Fundamental Algorithms for Scientific
Computing in Python, *Nat. Methods*, 17, 261–272, <https://doi.org/10.1038/s41592-019-0686-2>, 2020.

818 [Vu, T. M., Mishra, A. K., Konapala, G., and Liu, D.: Evaluation of multiple stochastic rainfall generators in diverse climatic regions, *Stoch. Env. Res. Risk A*, 32, 1337–1353, <https://doi.org/10.1007/s00477-017-1458-0>, 2018.](https://doi.org/10.1007/s00477-017-1458-0)

820 Warter, M. M., Singer, M. B., Cuthbert, M. O., Roberts, D., Caylor, K. K., Sabathier, R., and Stella, J.: Drought onset and propagation into
soil moisture and grassland vegetation responses during the 2012–2019 major drought in Southern California, *Hydrol. Earth Syst. Sci.*,
25, 3713–3729, <https://doi.org/10.5194/hess-25-3713-2021>, 2021.

822 Warter, M. M., Singer, M. B., Cuthbert, M. O., Roberts, D., Caylor, K. K., Sabathier, R., and Stella, J.: Modeling seasonal vegetation
phenology from hydroclimatic drivers for contrasting plant functional groups within drylands of the Southwestern USA, *Environ. Res.:
Ecology*, 2, 025001, <https://doi.org/10.1088/2752-664X/acb9a0>, 2023.

826 Wheater, H. S., Mathias, S. A., and Li, X.: *Groundwater Modelling in Arid and Semi-Arid Areas*, Cambridge University Press,
<https://doi.org/10.1017/CBO9780511760280>, 2010.

828 [Wilcox, C., Aly, C., Vischel, T., Panthou, G., Blanchet, J., Quantin, G., and Lebel, T.: Stochastorm: A Stochastic Rainfall Simulator for
Convective Storms, *J. Hydrometeorol.*, 22, 387–404, <https://doi.org/10.1175/JHM-D-20-0017.1>, 2021.](https://doi.org/10.1175/JHM-D-20-0017.1)

830 Zhang, L. and Singh, V. P.: *Copulas and their Applications in Water Resources Engineering*, Cambridge University Press, University Printing
House, Cambridge CB2 8BS, United Kingdom, <https://doi.org/10.1017/9781108565103>, 2019.