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4 **Nonparametric estimation method for river cross-sections with**

5 **point cloud data from UAV photography**

6 **URiver-X version 1.0 -methodology development**

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8 Keywords: Nonparametric, UAV, Regression, Point Cloud, River, Cross Section

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## Abstract

26 Aerial surveying with unmanned aerial vehicles (UAVs) has been popularly employed in river  
27 management and flood monitoring. One of the major processes in UAV aerial surveying for river  
28 applications is to demarcate the cross-section of a river. From the photo images of aerial  
29 surveying, a point cloud dataset can be abstracted with the structure from motion technique. To  
30 accurately demarcate the cross-section from the cloud points, an appropriate delineation  
31 technique is required to reproduce the characteristics of natural and manmade channels,  
32 including abrupt changes, bumps, and lined shapes. Therefore, a nonparametric estimation  
33 technique, called the K-nearest neighbor local linear regression (KLR) model, was tested in the  
34 current study to demarcate the cross-section of a river with a point cloud dataset from aerial  
35 surveying. The proposed technique was tested with synthetically simulated trapezoidal, U-shape,  
36 and V-shape channels. In addition, the proposed KLR model was compared with the traditional  
37 polynomial regression model and another nonparametric technique, locally weighted scatterplot  
38 smoothing (LOWESS). The experimental study was performed with the river experiment center  
39 in Andong, South Korea. Furthermore, the KLR model was applied to two real case studies in  
40 the Migok-cheon stream on Hapcheon-gun and Pori-cheon stream on Yecheon-gun and  
41 compared to the other models. With the extensive applications to the feasible river channels, the  
42 results indicated that the proposed KLR model can be a suitable alternative for demarcating the  
43 cross-section of a river with point cloud data from UAV aerial surveying by reproducing the  
44 critical characteristics of natural and manmade channels, including abrupt changes and small  
45 bumps as well as different shapes. Finally, the limitation of the UAV-driven demarcation  
46 approach was also discussed due to the penetrability of RGB sensors to water.

47



## 48      **1. Introduction**

49      Unmanned aerial vehicles (UAVs) have been popularly employed in recent years, especially to  
50      investigate and survey earth systems, such as agriculture and coastal areas (Hugenholtz et al.,  
51      2013; Lin et al., 2018; Marfai et al., 2019; Remondino et al., 2011; Siebert and Teizer, 2014;  
52      Srivastava et al., 2020; Taddia et al., 2021; Wang et al., 2019; Watanabe and Kawahara, 2016;  
53      Yan et al., 2021). Furthermore, river management and fluvial networks have received  
54      considerable attention for UAV applications (Gracchi et al., 2021; Langhammer, 2019; Lee et al.,  
55      2019; Sanhueza et al., 2019; Tomsett and Leyland, 2019). Additionally, flood monitoring and  
56      assessment are one of the major fields in which UAV aerial surveying data have been used  
57      (Anders et al., 2020; Andreadakis et al., 2020; Izumida et al., 2017; Kaewwilai, 2019; Perks et al.,  
58      2016; Zakaria et al., 2018).

59              For example, Andreadakis et al. (2020) employed a combination of Structure from  
60      Motion (SfM) and optical granulometric techniques in estimating peak discharge and illustrated  
61      that the combined UAV technique accurately determined peak discharge. Anders et al. (2020)  
62      tested different flying altitudes and area coverage orientations in semiarid and medium-relief  
63      areas with respect to cell size and vertical and horizontal accuracy. Perks et al. (2016) applied a  
64      novel algorithm to track features associated with free-surface velocity and to allow accurate  
65      geometric correction of velocity vectors.

66              The SfM technique produces 3D information from overlapping images, where the  
67      structure refers to the relative parameters of aerial surveying, such as camera positions and focal  
68      lengths, and the relative positions of the corresponding features, while the motion refers to the  
69      movement of the camera (Javernick et al., 2014; Marteau et al., 2017; Smith et al., 2014). A



70 dense point cloud can be determined from the SfM. These point clouds are converted from an  
71 arbitrary coordinate system to a geographical coordinate system with camera position and focal  
72 length information or by associating reference points on the ground, called ground control points  
73 (GCPs), with known coordinates. A point cloud is a set of 3-dimensional points located in space.  
74 The 3D locations of a point cloud can be determined from a sensor by emitting pulses and  
75 calculating them with the position of the sensor and the pulse direction. Here, the sensor refers to  
76 a photogrammetry camera in the current study.

77 In UAV aerial surveying applications for river management and flood analysis, the  
78 demarcation of cross-section of a river is critical. Accurate demarcation of the cross-section is  
79 mostly required to calculate peak discharge and flow amount. However, the dense cloud point  
80 dataset obtained from UAV aerial surveying and the SfM technique mostly contains errors and  
81 does not provide direct cross-sectional information. An appropriate technique to demarcate the  
82 cross-section from the point cloud dataset is necessary to develop.

83 The demarcation of the cross-section in a river has been mostly made with a digital  
84 elevation model (DEM) in the literature (Gichamo et al., 2012; Petikas et al., 2020a, b; Pilotti,  
85 2016). For example, Petikas et al. (2020b) proposed a novel method to automatically extract  
86 river cross-sections from a DEM along with a parametric cross-section extraction algorithm.  
87 However, a cross-sectional algorithm for the cloud point dataset of UAV aerial surveying has not  
88 been tested in depth, since the characteristics of the point cloud dataset are far different from the  
89 DEM in that a study area for UAV aerial surveying is commonly smaller and many more points  
90 can be acquired from UAV aerial surveying.



91           Therefore, the current study proposes a demarcation technique for river cross-sections from  
92 the point clouds of UAV aerial surveying especially in a small study area. For example, about 80%  
93 of national rivers and over 40% of local rivers are maintained by the construction of dikes and  
94 revetments for flood control in South Korea. The shape of manmade rivers is mostly trapezoidal  
95 due to the stability and easy discharge. A cross-section of manmade rivers also often contains  
96 abrupt changes and small bumps as well as smooth variations from aging in natural rivers. The  
97 demarcation technique must reproduce the characteristics of manmade channels as well as the  
98 ones of typical rivers from aging in natural channels. The proposed demarcation model based on  
99 the KLR model was tested to determine whether to reproduce those characteristics.

## 100           **2. Mathematical Description**

101 With the point cloud data obtained from UAV aerial surveying and postprocessing, the river  
102 cross-section must be demarcated. Polynomial regression can be simply applied to the point data.  
103 However, a fixed function of the polynomial regression with a few parameters is limited to the  
104 highly varied shape of the cross-section. Therefore, a nonparametric regression approach is  
105 adopted in the current study, especially K-nearest neighbor local regression (KLR). The KLR  
106 model was originally developed by Lee et al. (2017) to predict and simulate hydrologic variables  
107 describing a non-linear and heteroscedasticity relationship (non-constant variance of a predictand  
108 along with a predictor). The model also presents a strong interpolation ability, especially with a  
109 large number of datasets. Therefore, the KLR model was applied to the demarcation of a river  
110 cross-section, since the UAV aerial surveying and photogrammetry produce a large number of  
111 cloud points and the elevation of a river cross-section is highly non-linear. The KLR model was  
112 compared to a parametric model (polynomial regression) and another nonparametric model  
113 (LOcally WEighted Scatterplot Smoothing, LOWESS). A detailed description of polynomial



114 regression and the proposed nonparametric regression model (KLR) is shown as well as the  
115 comparable nonparametric model, LOWESS.

## 116 **2.1. Polynomial Regression**

117 A polynomial regression model can be used when the relationship between a predictor ( $x$ ) and an  
118 explanatory variable ( $y$ ) is nonlinear or curvilinear. The  $M^{\text{th}}$ -order polynomial regression can be  
119 expressed as

$$120 \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 + \dots + \beta_k x^M + \epsilon = \sum_{i=0}^M \beta_i x^i + \epsilon = \mathbf{x}\boldsymbol{\beta} + \epsilon \quad (1)$$

121 where  $\epsilon$  is considered to be a random noise with zero mean and  $M$  is the degree of the  
122 polynomial regression model, called PolyFit. Here,  $x$  can be the distance from the base location  
123 in a river cross-section with a length unit (meter, in the current study) and  $y$  is the elevation with  
124 the same length unit (meter as well).

125 According to its degree  $M$ , the model is structured as follows.

$$126 \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 + \epsilon \quad (2)$$

$$127 \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 + \beta_3 x^3 + \epsilon \quad (3)$$

$$128 \quad y = \beta_0 + \beta_1 x + \beta_2 x^2 + \beta_3 x^3 + \beta_4 x^4 + \epsilon \quad (4)$$

129 The models in Eq. (2), Eq. (3), and Eq. (4) are defined as PolyFit2, PolyFit3, and PolyFit4,  
130 respectively, and employed in the current study.

## 131 **2.2. KNN-based Local Linear Regression (KLR)**

132 It is assumed that the current condition of the predictor  $x_i$  and its corresponding predictand  $y_i$   
133 with the observed data (or cloud point data) pairs  $(x_i, y_i)$ , for  $i = 1, \dots, n$ , is given for the  $n$  number



134 of data points (i.e., the selected cloud points). In the current study, the pair  $(x_i, y_i)$  refers to the  
135 observed data of x-coordinate (i.e. distance from the base location) and its corresponding  
136 elevation of y-coordinate for the  $i^{\text{th}}$  observed data (or cloud point data). Note that the base  
137 location refers to the point that the x-coordinate of a cross-section begins. The number of  
138 neighbors ( $k$ ) is also assumed to be known. The predictand  $Y_t$  is estimated (i.e. the predicted  
139 elevation with the length unit, meter in the current study) with the target  $x_t$  distance according to  
140 the following steps:

141 (a) Estimate the distances between the current and observed (here, point cloud data) states  
142 of the predictors for all  $n$  observations as follows:

143 
$$D_j = (x_j - x_t)^2 \quad j=1, \dots, n \quad (5)$$

144 (b) Store the location indices for the  $k$  smallest distances.

145 (c) Fit the local linear regression to the observed dataset of the selected location indices  $[x_{(p)},$   
146  $y_{(p)}]$  for  $p = 1, \dots, k$ , where  $(p)$  indicates the  $p^{\text{th}}$  decreasing ordered location index relative  
147 to the distance measure in step (a).

148 (c-1) Build the weight matrix using the simple selection weight as follows:

149 
$$\mathbf{W}_{KLR} = \text{diag} \left[ \frac{1}{\delta}, \frac{1/2}{\delta}, \dots, \frac{1/k}{\delta} \right] \quad (6)$$

150 where  $\delta = \sum_{p=1}^k 1/p$ .

151 
$$\vec{\mathbf{X}}_t = \begin{pmatrix} 1 & x_t - x_{(1)} \\ 1 & x_t - x_{(2)} \\ 1 & \vdots \\ 1 & x_t - x_{(k)} \end{pmatrix} \quad (7)$$



152 (c-3) Estimate the parameter vector  $\hat{\beta}_t^{KLR}$  with the weighted least square estimator from  
153 the weight matrix  $\mathbf{W}_{KLR}$  in Eq. (6) as

$$154 \quad \hat{\beta}_t^{KLR} = (\bar{\mathbf{X}}_t^T \mathbf{W}_{KLR} \bar{\mathbf{X}}_t)^{-1} \bar{\mathbf{X}}_t^T \mathbf{W}_{KLR} \mathbf{y}_{KLR} \quad (8)$$

155 where  $\mathbf{y}_{KLR}$  is the corresponding predicted value for the ordered observations  
156  $[\mathcal{Y}_{(1)}, \mathcal{Y}_{(2)}, \dots, \mathcal{Y}_{(k)}]^T$ .

157 (d) Estimate the current predictor as follows:

$$158 \quad y_t = \bar{\mathbf{x}}_t^T \hat{\beta}_t^{KLR} \quad (9)$$

159 where  $\bar{\mathbf{x}}_t = (1 \ x_t)$ .

160 (e) Repeat steps (a)-(d) until the required data are simulated.

161 For selecting the number of neighbors  $k$ , a heuristic approach for estimating  $k$  for the  
162 KNNR model is given by  $k = \sqrt{n}$  (Lall and Sharma, 1996; Lee and Ouarda, 2011; Lee et al.,  
163 2010). Therefore, Lee et al. (2017) suggested a heuristic approach for KLR in which they  
164 suggested that the multiplier be

$$165 \quad k = a\sqrt{n} \quad (10)$$

166 where  $a$  is a multiplier and is a positive integer (i.e., 1, 2, 3, 4).

167 As noted, only the partial dataset is employed for the observations rather than the whole  
168 observation dataset, unlike other regressions. For the point cloud dataset from UAV photography,  
169 this proposed approach in the current study is highly advantageous, since the neighboring data





170 point is sufficient and the fitting of the target point must not be affected by the points that are far  
171 away from the target point. This advantage is further discussed in the result section.

### 172 2.3. LOcally WEighted Scatterplot Smoothing (LOWESS)

173 LOWESS was proposed by Cleveland (1979) as a nonparametric regression. The  
174 LOWESS with one explanatory variable ( $x_t$ , the distance from the base location for x-coordinate)  
175 and one predictor variable ( $y_t$ , the elevation of the corresponding  $t^{\text{th}}$  point) can be defined as

$$176 \quad y_t = m(x_t) + \varepsilon_t \quad (11)$$

177 where the regression curve  $m(y_t)$  is the conditional expectation  $m(x_t) = E(Y|X = x_t)$ . The  
178 LOWESS estimate can be defined as

$$179 \quad \hat{m}_{LOWESS}(x_t) = \vec{x}_t^T \hat{\beta}_t^{LOWESS} \quad (12)$$

180 where

$$181 \quad \hat{\beta}_t^{LOWESS} = (\vec{\mathbf{X}}_t^T \mathbf{W}_t \vec{\mathbf{X}}_t)^{-1} \vec{\mathbf{X}}_t^T \mathbf{W}_t \mathbf{y} \quad (13)$$

182 with

$$183 \quad \vec{\mathbf{X}}_t = \begin{pmatrix} 1 & x_t^1 - x_1^1 \\ 1 & x_t^1 - x_2^1 \\ 1 & \vdots \\ 1 & x_t^1 - x_n^1 \end{pmatrix} \quad (14)$$

184 and

$$185 \quad \mathbf{W}_t = \mathbf{H}^{-1} \text{diag}[K_d(\mathbf{H}^{-1}(x_t - x_1)), \dots, K(\mathbf{H}^{-1}(x_t - x_n))] \quad (15)$$



186 with the bandwidth matrix,  $\mathbf{H}$ . The major characteristic of LOWESS is to employ the following  
187 kernel function:

188

$$K_d(z) = \begin{cases} (1 - |z|^3)^3 & |z| < 1 \\ 0 & \text{otherwise} \end{cases} \quad (16)$$



## 189      **2.4. Distance Measurement of the Point Cloud**

190      The point cloud data from UAV photography are presented with Transverse Mercator (TM)  
191      projection for  $x$ ,  $y$ , and  $z$ . The TM projection is a conformal projection presented by Lambert in  
192      1772. To demarcate a cross section of a river, the point cloud data must be projected to a new  
193      coordinate system.

194      As an example in Figure 1, the new coordinate system can be based on the line that  
195      connects  $N$  and  $L$  points presented with the thick red line in Panel (a). The extended thick red  
196      line is designated as the new  $x$ -coordinate, as shown in Panel (b), and the same  $z$ -axis can be  
197      defined as the original TM data. The  $y$ -coordinate can be chosen as the axis that is perpendicular  
198      to the  $x$ -coordinate. Let it be assumed that point  $M$ , as in Panel (b), is selected among the  
199      selected point clouds contained in the  $NL$  line. Note that the thick red line in Panel (a) is a group  
200      of selected points from the point cloud data for defining the cross-section of the river, as shown  
201      in Panel (b).

202      All of the selected red points must be aligned according to the distance from the datum  
203      point (here,  $N$ ) with the new coordinate system. The new distance for the new  $x$ -coordinate can  
204      be defined as  $k$ , as shown in Panel (c). This distance is estimated with the following equations.

205      The distances of  $l$ ,  $m$ , and  $n$  with the TM coordinate can be estimated as follows. For  
206      example,  $N_{TM}(x)$  represents the  $x$ -coordinate of the TM projection for point  $N$ :

$$207 \quad l = \sqrt{(N_{TM}(x) - M_{TM}(x))^2 + (N_{TM}(y) - M_{TM}(y))^2} \quad (17)$$

$$208 \quad m = \sqrt{(N_{TM}(x) - L_{TM}(x))^2 + (N_{TM}(y) - L_{TM}(y))^2} \quad (18)$$



$$n = \sqrt{(L_{TM}(x) - M_{TM}(x))^2 + (L_{TM}(y) - M_{TM}(y))^2} \quad (19)$$

From the calculated angle of MNL ( $\theta$ ) in Eq. (24), the new x-coordinate distance ( $k$ ) can be calculated as in Eq. (25) with the law of cosines (i.e.,  $n^2 = l^2 + m^2 - 2lm\cos\theta$ ) as the following:

$$\cos\theta = \frac{l^2 + m^2 - n^2}{2lm} \quad (20)$$

$$k = l \cos\theta \quad (21)$$

### 3. Simulation Study

The performance of the KLR model in fitting the point cloud data for river cross-sections is tested with the simulated point cloud data.

#### 3.1. Model Description and Fitting

A manmade river cross-section is generally trapezoidal due to maximum discharge and easy construction (Chow, 1959). Therefore, a trapezoidal channel was assumed with a 4 m top at both sides and a 6 m base width as well as a 1:1 side slope with a 6 m height, as shown by the thick solid blue line of Figure 2. The channel points were assumed to be measured with 0.1 m intervals, for a total of 161 points. It is assumed that these points work as cloud points that UAV cameras might capture in aerial surveying. The assumed cloud point dataset was generated based on the assumed 161 points (see the thick solid blue line in Figure 3), as follows:

$$Z = Y + \varepsilon \quad (22)$$



227 where  $Y$  is the assumed points, and  $\varepsilon \sim N(0, \sigma_\varepsilon^2)$ , i.e., normally distributed error. Note that the  
228 generated data ( $Z$ ) are presented with red circles in Figure 2.

229 In the current study,  $\sigma_\varepsilon^2=0.2$  was used following similar variability of observed data after  
230 testing several values. The magnitude of this error variance ( $\sigma_\varepsilon^2$ ) represents the differences in the  
231 photo locations for the same cloud point of the real ground location (i.e.,  $Y$  in this case). High  
232 variance indicates that extracted point clouds include high errors, and vice versa.

233 In Figure 2 and Figure 3, the simulated data are presented with red circles. The number of  
234 synthetically simulated data points was chosen to be 2 times and 10 times the assumably  
235 measured 161 points that were applied for the assumable measured trapezoid line (i.e., 322 and  
236 1610 points), as shown in Figure 2 and Figure 3, respectively. Note that the recommended  
237 overlap is 70–80% frontal and 60% side in general cases. In this overlapping case, each cross-  
238 section point might be captured approximately 10 times. Therefore, the number of simulated data  
239 points is set to 10 times the number of trapezoidal channel points (a total of 1610), as shown in  
240 Figure 3. Additionally, there are some portions in which overlapping might not be achieved. The  
241 minimal overlap to be a point cloud is at least 2 times, and 2 times the channel points were also  
242 tested, as shown in Figure 2.

### 243 **3.2. Simulation Results**

244 In Figure 2, the fitted cross-section line to the KLR model is shown with the dashed black  
245 line for the generated data case with 2 times the assumed target points, while the simulated data  
246 are presented with the red circles as noted. Note that the multiplier ( $a$ ) for the number of nearest  
247 neighbors as in  $k = a\sqrt{n}$  in Eq. (10) was tested in this figure. As shown in Figure 2, the multiplier  
248  $a = 1, 2, 3, 4$  is shown in each panel. The fitted KLR line with a smaller multiplier presents more



249 irregularity, while the line with a higher multiplier appears to be smooth. For example, the top  
250 part of the trapezoid channel with the 22 m of the y-coordinate shows that the KLR line with the  
251 multiplier  $a=1$  (the panel(a) of Figure 2) was drawn rather coarse, but the straight shape of the  
252 original channel is preserved. At the same time, the fitted line with the high multiplier  $a=4$  (Panel  
253 (d) of Figure 2) presents a very smooth feature and presents the original top and bottom  
254 horizontal parts, which are rather too curved.

255 The multipliers of  $a=2$  and 3 in the fitted KLR model, as shown (Panels (c) and (d) of Figure  
256 2), appear to mix the smooth and horizontal features well by fitting the top and bottom horizontal  
257 lines, and the angled part of the original channel is reproduced well. This finding indicates that  
258 an appropriate multiplier ( $a$  in Eq. (10)) is required to present the straight and angled trapezoid  
259 channel better.

260 This characteristic continues to be the case with the high number of captured cloud points, as  
261 shown in Figure 3 (i.e., 10 times the target points, for a total of 1610 points, as shown with the  
262 red circles in this figure). It is comparable to the case of 2 times the target points in Figure 2 in  
263 that all of the fitted line with the KLR model with the case of 10 times presents better the  
264 original trapezoid channel than the case of 2 times. It is obvious that a higher number of points  
265 can significantly improve the quality of the KLR model, since the nonparametric KLR model  
266 directly applies the observed data and its performance highly depends on the number of data  
267 points. In other words, while parametric models, such as linear regression and polynomial  
268 regression, estimate the parameters from the data and the parameters are employed, the  
269 nonparametric KLR model employs the data itself directly to estimate the cross-section. It can be  
270 appreciated that the UAV aerial photography usually captures a large enough number of points to  
271 produce overlapping points as many as 10 times the target points.



272 The horizontal and angled trapezoid shape (i.e., the solid thick blue line in Figure 3) is  
273 reproduced well by the KLR model (see the dashed black line), even though a coarse zig-zag line  
274 is still observed in the case of the small multiplier (i.e.,  $a=1$ , see Panel (a) of Figure 3). Also, the  
275 angled portion is too curved in the case of the high multiplier (i.e.,  $a=4$ , see Panel (d) of Figure  
276 3).

277 The results of Figure 2 and Figure 3 illustrate that a value between 2 and 3 can be a good  
278 selection for the multiplier. Further testing was performed to select the multiplier for the number  
279 of nearest neighbors by varying the multiplier from 0.5 to 5.0 with a 0.5 interval. The root mean  
280 square error (RMSE) and the mean absolute error (MAE) were estimated as

$$281 \quad RMSE = \sqrt{\frac{1}{N} \sum_{t=1}^N (y_t - Y_t^{model})^2} \quad (23)$$

$$282 \quad MAE = \frac{1}{N} \sum_{t=1}^N |y_t - Y_t^{model}| \quad (24)$$

283 where  $Y_t^{model}$  is the estimate from a model like the KLR in Eq. (9), and  $y_t$  represents the original  
284 points with N trapezoid points (here, 161 points).

285 The RMSE results of the KLR estimate with different multipliers (i.e.,  $a$  in Eq. (10)) are  
286 shown in Figure 4 for the case of 2 times (top panel) the original trapezoidal points and the case  
287 of 10 times (bottom panel). In the 2 and 10 times cases, the optimum multiplier (i.e., the smallest  
288 multiplier  $a$ ) can be selected to be between 1.5 and 2.5. To fully reveal the characteristics of the  
289 multiplier with multiple simulations, all of the multiple simulations from 1 to 12, indicating the  
290 number of overlapped photos, were tested while finding the optimum multiplier. The result in  
291 Figure 5 shows that a smaller optimum multiplier is selected with a smaller number of  
292 overlapped photos (or multiple simulation points) as much as 1.5–2.0, and vice versa as much as



293 2.0–2.5. Since the number of overlapping photos might be difficult to know and each point does  
294 not have the same number of points in real UAV aerial survey, the multiplier is suggested to be  
295 2.0 in the current study.

296 To compare other approaches to fit the point cloud in demarcating the cross-section of a  
297 river, polynomial regression and locally weighted scatterplot smoothing (LOWESS) were also  
298 tested. The result is presented in the top and bottom panels of Figure 6 and Figure 7 for the fitted  
299 line to the polynomial regression (top panel) and the LOWESS model, respectively. The fitted  
300 line to the polynomial regression of 2<sup>nd</sup> degree (see the thick dash-dotted black line with the  
301 circle marker in the top panel of Figure 6 and Figure 7) does not reproduce the top and bottom  
302 horizontal lines of the trapezoid channel well. Better performance in the 4<sup>th</sup> degree polynomial  
303 regression model is presented (see the dotted black line with the reverse triangle marker).  
304 However, the depth of the trapezoid center is overestimated. Other degrees of polynomial  
305 regression models were also tested, but no better performance was observed.

306 Furthermore, the LOWESS model was additionally fitted to the simulated trapezoid  
307 channel data. Note that the LOWESS model is also a nonparametric regression model as  
308 described already. The major difference between the LOWESS model and the KLR model is that  
309 the LOWESS model includes all of the observed data in the estimate, as shown in Eqs. (13) and  
310 (14), while the KLR model includes only the k-nearest neighbor observations, as in Eq. (7). The  
311 performances of the LOWESS and KLR models were compared in detail in Lee et al. (2017) for  
312 the heteroscedastic relation of time series data. The result in the study of Lee et al. (2017)  
313 indicated that the KLR model reproduced an abrupt change in the heteroscedastic relation. The  
314 results of the LOWESS model are presented in the bottom panels of Figure 6 and Figure 7. The





315 results indicate that the bottom part of the trapezoidal channel is reproduced well with the  
316 LOWESS model. However, the model does not reproduce the abruptly curved area well.

### 317 **3.3. Simulation tests with V-shape and U-shape cross-sections**

318 In order to further test the performance of the proposed KLR model, two additional shapes of  
319 cross-sections as U- and V-shape were tested. The U-shape channel was included, since most of  
320 natural channels present this shape and the V-shape channel can be either manmade or natural.

#### 321 *3.3.1. U-shape cross-section*

322 The U-shape cross-section that is close to a natural river was tested. The U-shape cross was  
323 modelled with a power function from Neal et al. (2015) as

$$324 \quad w_f = w_F \left( \frac{h_f}{h_F} \right)^{\frac{1}{s}} \quad (25)$$

$$325 \quad h_f = h_F \left( \frac{w_f}{w_F} \right)^s \quad (26)$$

326 where  $w_f$  indicate the flow width, while  $w_F$  is the bank-full flow width and  $h_f$  and  $h_F$  is the  
327 height of flow width and the height in a bank-full condition, respectively. Also,  $s$  is the  
328 parameter to vary the shape of the cross-section. Here,  $s=5$  was set as used in Neal et al. (2015)  
329 as a basic value. To design a similar bank to the trapezoid model in the previous test,  $h_f=5\text{m}$  and  
330  $w_F=20\text{m}$  was used. The number of points for the U-shape cross-section is divided to 262 points  
331 including the flat river bank and the designed cross-section was presented in a blue solid line  
332 with cross markers as shown in Figure 8. The synthetic point cloud data was simulated with  
333 Eq.(11) and the number of point clouds was 10 times of the U-shape cross-sections (i.e. 2620  
334 points), shown with the red dots in Figure 8.



335 This designed U-shape cross-section was fitted to the proposed KLR model and the other  
336 models as LOWESS and PolyFit, as shown in Figure 8. Note that  $a=2$  (see Eq.(10)) was applied  
337 for the KLR model from the result of the trapezoid case. The result in Figure 8 indicates that the  
338 KLR model reproduces well the U-shape cross-section without any deviation. Meanwhile, the  
339 LOWESS model fitted U-shape cross-section well in the middle part, but the connected part  
340 (between 4m and 6m of x-coordinate) of the U-shape cross-section was not fitted well. The  
341 PolyFit model fairly fitted the U-shape cross-section with the 4<sup>th</sup> model (i.e. PolyFit4) except  
342 slight deviation in the connected area between the slope and top bank. The PolyFit2 and PolyFit3  
343 models were poorly performed due to its limit of the flexibility.

#### 344 3.3.2. *V-shape cross-section*

345 One of the unique shape of cross-sections is the V-shape for a river cross-section. The V-shape  
346 weir (or triangle shape, v-notch) was often built to provide a highly accurate solution for open  
347 channel flow measurement. Also, the V-shape river cross-section can be developed naturally  
348 when the sides are cut down and attacked by weathering. In addition, the loosened material  
349 slowly creeps down the slope by gravity. A V-shape cross-section was synthetically designed as  
350 shown in Figure 9 with the height of 4m and the top width of 16m so that the slopes of both sides  
351 are in 1:2. The cross-section was divided to 121 points, including the flat river bank shown with  
352 the blue solid line with cross markers in Figure 9 and 10 times of the points was synthetically  
353 generated for point cloud data with Eq. (11) and presented with the red dots.

354 The point cloud data was fitted to KLR, LOWESS, and PolyFit models and shown in the  
355 panels (a), (b) and (c) of Figure 9, respectively. Here,  $a=2.0$  was also employed for the KLR  
356 model. The result of the KLR model indicates that the V-shape cross-section also was fitted well  
357 by the KLR model with a minimal deviation at the acute angle bottom section. Meanwhile, the



358 LOWESS model highly deviated at the acute bottom section and slight deviation was present at  
359 the top connected part. The PolyFit model did not fairly fit the V-shape model even with  
360 PolyFit4. Further higher order model was tested (i.e. PolyFit5 and PolyFit6) and no improvement  
361 was found with increasing the order for the PolyFit model.

362 Table 1 presents the estimated RMSE and MAE for three tested models of KLR, LOWESS,  
363 and PolyFit4 with trapezoidal, U-shape, and V-shape cross-section data. Note that only PolyFit4  
364 was presented, since 4<sup>th</sup>-degree was the best for the PolyFit models. The RMSE and MAE  
365 estimates present that the KLR model outperforms the other fitting models, while the other two  
366 models of PolyFit4 and LOWESS are comparable to each other for trapezoidal and U-shape  
367 cross-sections. For V-shape channel, the LOWESS much better performed than the PolyFit4,  
368 since the PolyFit4 is a parametric model that connects the points rather smoothly and abrupt  
369 change cannot be modelled well due to its limited flexibility. Overall, the simulation study  
370 indicates that the proposed KLR model is a good alternative to demarcate the different shape  
371 cross-sections.

372 Further, nonparametric models and other regression models, such as logistic regression  
373 (Ahmad et al., 1988; Elek and Márkus, 2004; Orłowsky et al., 2010; Simonoff, 1996), can be  
374 tested. However, the simulation study with the trapezoid channel that is similar to the real river  
375 cross-section shows that the presented KLR nonparametric model originally developed by Lee et  
376 al. (2017) is suitable for demarcating the cross-section of a river. The major reason for the good  
377 performance is that the KLR model employs only k-nearest neighbor observations. This  
378 approach might not be beneficial, when an overall trend is needed, and not enough observations  
379 are available. However, the point cloud data taken from UAV aerial surveying often provides a  
380 large enough number of points in the data set. Furthermore, the cross-sections in a manmade



381 river can contain irregularity and abrupt changes by river aging. This feature can be captured  
382 only through fitting nearby observations. Therefore, the KLR model might be a suitable  
383 alternative to demarcating the cross-section of a river with the cloud point dataset.

## 384 **4. Experimental Study**

### 385 **4.1. Experimental Site**

386 In order to validate the performance of the proposed KLR model, the River Experiment  
387 Center (REC) in Korea Institute of Civil Engineering and Building Technology was selected as  
388 an experimental site (Lee et al., 2022), as shown in Figure 10. The REC consists of a total area  
389 193,051 m<sup>3</sup> with three rivers of open channels with a length of 560~680 m, width of 11 m, and  
390 depth of 2 m. The three channels are (1) the steep river (U-shape), (2) the meandering river (S-  
391 shape), and (3) the straight river (I-shape) as shown in the bottom panel of Figure 10. The steep  
392 river (U-shape) with a length of 590 m has a slope of 1.4% and its flow can have a velocity up to  
393 5.0 m/s in the upstream to test the stability of bank revetment. The slope of the downstream at  
394 the steep river is 0.125% and is employed for hydraulic experiments, including vegetation  
395 development over the banks and sediment transport in the river bed. The straight river (I-shape)  
396 with a length of 560 m has a low-slope and it contains concrete compound for international  
397 cooperation study. The meandering river (S-shape) of the REC with a length of 682m has a  
398 1.2~1.7 sinuosity that can be employed for various experiments, including pollutant dispersion  
399 and flow structures.

400 On each river, six to seven cross-sections were selected, as shown in the bottom panel of  
401 Figure 10, to test the demarcation method of the current study. The channels were ground-  
402 surveyed and estimated with the UAV-based demarcation method. The steep river (S-shape) is



403 located at the bottom and 7 cross-sections were surveyed as  $U_1, U_2, \dots$ , and  $U_7$ . The straight river  
404 (I-shape) is in the middle among three rivers with 6 cross-sections as  $I_1, \dots$ , and  $I_6$ . The  
405 meandering river (S-shape) is placed at the top and 7 cross-sections were tested as  $S_1, S_2, \dots$ , and  
406  $S_7$ .

## 407 **4.2. Application Methodology**

### 408 *4.2.1. Ground Surveying*

409 For comparing demarcation methods, the real ground points were surveyed using the  
410 Global Positioning System (GPS). The EMLID Reach RS2 with centimeter precision was used  
411 for GPS surveying, as shown in panels (a) and (b) of Figure S3 of the Supplementary Material.  
412 At each channel point, about 10~15 points from the three rivers in the REC were surveyed with  
413 the GPS system.

### 414 *4.2.2. UAV Aerial Surveying*

415 For aerial surveying of the REC, the Autel Evo II shown in the panel (c) of Figure S3 of the  
416 Supplementary Material was employed with 4000x3000 pixels with the vertical and horizontal  
417 resolutions of 96 DPI and 2.41cm of the average ground sampling distance. Note that the XT701  
418 camera was applied with ISO-100 and the 1/2" CMOS. The built-in flight path module of the  
419 Autel Evo II in the controller (see the panel (d) of Figure S3) was used to automatically obtain  
420 the aerial images of the REC, especially the targeted three experiment rivers. For the UAV  
421 photogrammetry of the REC, Pix4D Mapper was employed.

## 422 **4.3. Experiment Results**

423 In order to improve its accuracy for the UAV aerial surveying, 10 GCPs were employed  
424 with ground surveying and 34 check points were estimated for checking the entire accuracy of



425 the REC. The RMSE of the GCPs was 0.007m for Z and 0.017m and 0.055m for X and Y. The  
426 RMSE of the check points was 0.047m for Z and 0.040 and 0.071 for X and Y. This result  
427 indicates that the UAV aerial surveying produced the ground positions of the REC, including the  
428 target three rivers and channels. The detailed quality report from the Pix4Dmapper is uploaded in  
429 the Mendeley Data repository on the website of  
430 <https://data.mendeley.com/datasets/xdw4cgvvhm/2>.

431 For  $I_1$  in Figure 11, the point cloud (red circles) matched fairly the observed result of  
432 ground surveying (blue solid line with x marker) with a slight difference at the edge of the  
433 channel bottom in 4m and 8m of the x-coordinate. The KLR shown in the panel(a) of Figure 11  
434 draws the cross-section of  $I_1$  following the point cloud. A similar result can be found with the  
435 LOWESS in panel(b) of Figure 11 except that the left-top part of the channel (i.e. around 0 m of  
436 the x-coordinate) is not preserved with the LOWESS. The polynomial regression of different  
437 degrees, shown in panel(c) of Figure 11, performed very similarly to each other. The method  
438 fairly depicted the cross-section of  $I_1$  except for the left-top part of the abrupt change.

439 The fifth channel of the straight river ( $I_5$ ) shown in Figure 12 presents two different bottom  
440 sections. This type of the channel is common in reality when a river bottom is renovated to use  
441 the portion of the river bottom as a playground or a parking place. The observed ground  
442 surveying data (blue solid line with x marker in Figure 12) matched well the point cloud (red  
443 circles) from the UAV aerial surveying. The KLR method demarcated this channel with two  
444 bottom sections in panel(a) of Figure 12, including the abrupt varied part of the bottom (2m, 5m,  
445 7m, and 11m of the x-coordinate) and the top (0m, 1m, and 12m of the x-coordinate). The  
446 LOWESS shown in panel(b) of Figure 12 does not depict well the channel, especially in the  
447 abrupt changed parts. With the polynomial regression in panel(c) of Figure 12, a higher degree



448 model is needed, since it includes two different bottom sections. Likely, the 4<sup>th</sup> polynomial  
449 model showed the best performance among other degree polynomials. However, the changed  
450 part was not reproduced well with any degree polynomial regression model. Similar  
451 characteristics can be observed in the other channels for I<sub>2</sub>, I<sub>3</sub>, I<sub>4</sub>, and I<sub>5</sub> shown in Figures S4-S7  
452 of the supplementary material. The RMSE and MAE results of the tested channels are presented  
453 in Table 2 and Table 3,. The performance measures reflected the superiority of the KLR model  
454 presenting the smallest RMSE and MAE for the channels of the straight river (i.e. I-shape).

455         The first channel of the steep river (i.e. U<sub>1</sub>) is presented in Figure 13 and it has a typical  
456 shape of manmade river as presented in the simulation study of section 3 in Figure 2 and Figure  
457 6. The observed data of the ground surveying (blue solid line with x marker) matches well the  
458 aerial surveying data of the point cloud (red circles) in Figure 13. The KLR model depicted well  
459 this typical trapezoid channel, as shown in panel(a) of Figure 13. Also, the LOWESS and the  
460 polynomial regression model depicted this channel with a slight deviation at the angled bottom  
461 part (3 m and 7 m in the x-coordinate) presented in panels (b) and (c) of Figure 13, respectively.

462         The second channel of the steep river (U<sub>2</sub>) shown in Figure 14 has a winding bottom. The  
463 drawn channel with the ground surveyed data shows that the varied bottom was not surveyed  
464 well. The ground surveying of the channel bottom often missed this variation due to its time limit  
465 and accessibility. In contrast, the demarcation method with the point cloud of the UAV aerial  
466 surveying depicted the detailed winding bottom. The KLR model reproduced this channel shape  
467 well, including the winding bottom as shown in panel (a) of Figure 14. The LOWESS also  
468 demarcated this channel fairly (see the panel (c) of in Figure 14). However, the polynomial  
469 regression did not depict this cross-section well by smoothing too much the winding bottom.  
470 Similar result can be observed to the other channels for U<sub>3</sub>, U<sub>4</sub>, U<sub>5</sub>, and U<sub>6</sub> shown in Figures S4-



471 S7 of the supplementary material. The performance measures of RMSE and MAE in Table 2 and  
472 Table 3, respectively, also showed that the KLR model performed the best for the channels of the  
473 steep river with U-shape.

474 The selected channels for the meandering river (S-shape) are presented in Figure 15 and  
475 Figure 16 for S<sub>3</sub> and S<sub>6</sub>, respectively. Both channels show the common natural U-shape in the  
476 simulation study of section 3.3.1. The 3<sup>rd</sup> channel of the meandering river is shown in Figure 15  
477 (i.e. S<sub>3</sub>). The observed result from the ground surveying showed a slight deviation to the point  
478 cloud with the UAV aerial surveying. This deviation is also shown in other channels for the  
479 meandering river (S<sub>1</sub>, S<sub>2</sub>, S<sub>4</sub>, S<sub>5</sub>, and S<sub>7</sub> shown in Figures S13-S17 of the supplementary material).  
480 Locating the exact cross-section might be difficult to measure especially in a meandering river  
481 and this location difficulty might result in the deviation. This U-shape channel is depicted fairly  
482 with the KLR and LOWESS models (see panels (a) and (b) of Figure 15) as well as the  
483 polynomial regression of the 4<sup>th</sup> degree ( panel (c)). The 6<sup>th</sup> channel of the meandering river (S<sub>6</sub>)  
484 performed similar to the S<sub>3</sub> with a better representation of the observed result by the point cloud.  
485 Note that the natural U-shape channel is demarcated fairly well with all three methods shown in  
486 the simulation study. The RMSE and MAE results of the tested channels of the meandering river  
487 (S-shape) are presented in Table 2 and Table 3, respectively. The KLR model showed the  
488 smallest magnitude for S<sub>1</sub>, S<sub>2</sub>, S<sub>4</sub>, S<sub>5</sub>, and S<sub>7</sub>. Meanwhile, the performance result for S<sub>3</sub> and S<sub>6</sub>  
489 showed that the polynomial regression with the 4<sup>th</sup> degree presented the best performance in  
490 Table 2 and Table 3. Note that some deviation between the observed result and the point cloud  
491 data is shown for the meandering river. Also, the S<sub>3</sub> and S<sub>6</sub> channels have the U-shape of the  
492 common natural river as discussed in the simulation study and the smooth characteristics of a U-  
493 shape channel can be reproduced well with the polynomial regression.





## 494        **5. Case Study of Hapcheon**

### 495        **5.1. Study Area and Data Acquisition**

#### 496            *5.1.1. Study Area*

497            The study area is located in the Migok-cheon stream flowing through Hapcheon-gun,  
498            South Korea, as shown in Figure 17. The Migok-cheon stream has an 8.8 km length and 13.9  
499            km<sup>2</sup> watershed area. The slope of the stream is approximately 1/50~1/400, and the study area has  
500            a slope of 1/350. This stream conjuncts to the Hwanggang River at the end of the stream, and the  
501            Hwanggang River whose major discharge was made from Hapcheon Dam above is joined into  
502            the Nakdong River directly afterward. Therefore, the Migok-cheon stream is highly affected by  
503            the water levels of the Hwanggang River. Also, the fundamental engineering plan to prevent  
504            floods for the Migok-cheon stream was made in 2004 and the plan was updated in 2019  
505            (BRTMA, 2019).

506            In the middle of the Hwanggang River, the Hapcheon dam is located for electricity  
507            generation and water resources. The upstream Hapcheon River consists of a number of  
508            mountains, and the slope is high, producing rapid floods and short concentration times to induce  
509            floods. For example, in August 2020, the Hapcheon dam outflowed a large amount of water  
510            downstream and induced a high-water level in the Hwanggang River. A number of streams  
511            joining the Hwanggang River overflowed due to the high level of the Hwanggang River,  
512            including the Migok-cheon stream (Seong et al., 2020). To reduce damage from floods in the  
513            area of the Migok-cheon stream, an early warning system for floods is being considered. For the  
514            early-warning system for floods, detailed cross-sections of the Migok-cheon stream must be  
515            obtained to decide which water level is appropriate for an alarm. In the current study, four sites



516 were selected to test the performance of the proposed model located along the Migok-cheon  
517 stream as shown in Figure 18. The Naesamhak village is located on the left side of the river,  
518 while only cultivation land is on the right side indicating that the left bank has higher importance  
519 to water managers. Also, the Unsam bridge is placed in the middle the Migok-cheon stream.

#### 520 *5.1.2. Data Acquisition*

##### 521 **Specification of Employed UAV**

522 Aerial photos over the selected Migok-cheon were obtained with the unmanned aerial vehicle  
523 (also termed drone), DJI Phantom 4. This UAV is one of the most popular professional drones on  
524 the market and contains an advanced stereo vision positioning system that provides precise  
525 hovering even without satellite positioning support (Hamdi et al., 2019). The camera applied is  
526 FC3411 with ISO-110 and the image sensor of 1/2.3” CMOS, and the images taken from DJI  
527 Phantom 4 are 5472x3648 pixels at approximately 10 M with the horizontal and vertical  
528 resolutions of 75 DPI. Pix4Dcapture was employed to map the target area. The flight with a  
529 height of 75 meters was made on July 08, 2021.

##### 530 **Ground Control Points**

531 Ground control points (GCPs) are the points on the ground that have measured or known  
532 coordinates. To obtain GCPs, 10 specific points were measured over the target area on the  
533 ground with global positioning system (GPS) surveying. The EMLID Reach RS2  
534 (<https://emlid.com/reachrs2/>), multiband RTK GNSS receiver, with centimeter precision, was  
535 employed for GPS surveying.



## 536                    **Data Processing (WebODM)**

537        The aerial photos were postprocessed to build a point cloud dataset with WebODM. The  
538        WebODM (<https://github.com/OpenDroneMap/WebODM>) is an open-source tool for generating  
539        map point clouds, and terrain and 3D surface models from aerial images.

## 540                    **5.2. Results**

### 541                    *5.2.1. Selected sites for cross-section demarcation*

542                    The four tested sites in the Migok-cheon stream are presented in Figure 18. The overall  
543        produced point cloud dataset for the UAV surveying area is presented in the top-left panel of  
544        Figure 18, and the picture of the top-left panel consists of only the collected points. Site-1 is  
545        located in the middle of the study area, while Site-2 is in the upper part of the area. Since the  
546        nearby area of Site-1 is located in the middle of the UAV surveying coverage, several images  
547        can be overlapped and captured for the same points. The other two sites (Site-3 and Site-4) that  
548        are located between Site-1 and Site-2 were added for further comparison.

549                    Therefore, the number of points for demarcating a cross-section of the river might be  
550        sufficient to capture the detailed characteristics of the cross-section (see the top-right panel of  
551        Figure 18) like in Site-1 (see the red dots in Figure 19) as well as Site-3 and Site-4 (see Figure 21  
552        and Figure 22). In contrast, Site-2 is located at the upper part of the coverage area, and  
553        overlapping images might be limited, which indicates that the number of points to capture a  
554        target cross-section is also limited as shown in the red dots in Figure 20. Furthermore, part of the  
555        cross-sectional area can be missing due to technical and environmental limitations, such as  
556        waterbodies and insufficient overlapping images as well as shadow from the sun. For example,



557 there are some areas in which no cloud point data exists, as on the right side of Site-2. This point  
558 is intentionally selected to verify the model performance in such a case.

### 559 *5.2.2. Demarcation of selected cross-sections*

560 The demarcated cross-sections for the selected sites (i.e., Site-1, Site-2, Site-3, and Site-4)  
561 are illustrated in Figure 19, Figure 20, Figure 21, and Figure 22, respectively. Also, the RMSE  
562 and MAE estimates are presented in Table 4 to show the performance of the presented models.  
563 In Figure 19, the extracted cloud points for Site-1 are presented with red circles. As noted, a  
564 number of cloud points were extracted from the UAV aerial photographs for Site-1, since the site  
565 is located with enough photo coverage. The KLR fitted line shown with the dashed black line of  
566 the panel (a) of Figure 19 indicates that the fitted line reproduces the characteristics of the natural  
567 cross-section of the river well, including the overall trapezoidal shape and the natural bumps at  
568 the bottom. This line is compared with field measurements reported in BRTMA (2019). Slight  
569 differences can be seen between field measurements (shown with the solid blue line with the x  
570 marker) and the KLR fitted line since field measurements took place approximately about 3  
571 years ago.

572 The LOWESS model and the PolyFit models with the degree of 2, 3, and 4 were also tested  
573 and their results were presented in panels (b) and (c) of Figure 19, respectively. The LOWESS  
574 fairly fitted the point cloud data except the left side between 14 m and 20 m of the x-coordinate)  
575 with deviation from major cloud points. Meanwhile, all the Polyfit models (i.e. 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup>  
576 degrees) did not fit the point cloud data fairly with high deviation from the point cloud.

577 The cross-section of Site-2 is presented in Figure 20 and shows that the middle part of the  
578 left slope of the stream has no cloud point data. The KLR fitted line shows that the overall



579 characteristics of the cross-section are reproduced. Even the missing part of the cross-section  
580 between 12 m and 17 m of the x-coordinate is also interpolated well with the KLR model by  
581 comparing field measurements (see the solid blue line with the x marker in Figure 20). Some  
582 differences between the fitted line and the field measurement might result from the year  
583 difference. This result indicates that a missing part of the aerial surveying can be filled up with  
584 the interpolation of the KLR method. This can be a good benefit of the KLR model in  
585 demarcating the cross-sections with the UAV point cloud data, since this missing data can be  
586 sometimes inevitable. Otherwise, further UAV surveying might be required to fill up the gap  
587 costing additional time and money.

588 The LOWESS model also fitted fairly well the point cloud data through all the section (see  
589 the panel(b) of Figure 20) except that slight deviation can be observable on the right side of the  
590 top bank between 40 m and 42 m of x-coordinate. Also, the missing part (between 12 m and 17  
591 m of the x-coordinate) was rather not fairly interpolated with the LOWESS model. This might be  
592 induced from the lack of the points in this missing area, since the farther left side has denser  
593 points and the predicted points from the LOWESS model might be affected by these dense points.  
594 The PolyFit does not estimate the model well due to the lack of the model flexibility to an abrupt  
595 change of the cross-sections as mentioned.

596 Site-3 contains a number of cloud points as shown in Figure 21 . The KLR model well  
597 fitted the cloud points while the LOWESS model presents the good performance (see the panel  
598 (b) of Figure 21), but the deviation from the cloud points is observed in the left bank section (i.e.  
599 between 0 m and 3 m of x-coordinate). The PolyFit4 model as shown in (see the panel (c) of  
600 Figure 21) fairly performs in fitting the cloud data points. It is because the shape of the cross-  
601 section is rather smoothly curved. The Site-4 result shown in Figure 22 indicates that the KLR



602 model (the panel(a)) performs well in fitting the cloud points from the UAV surveying, while the  
603 LOWESS model presents significant deviation from the cloud points on the right side and the  
604 PolyFit models did not fairly perform.

605 The performance measures of RMSE and MAE are presented in Table 4 for all four sites  
606 and three tested models. The RMSE value of KLR is between 0.32-0.47 while the that of  
607 LOWESS and PolyFit is between 0.45-0.94 and 0.71-1.4. This performance result indicates that  
608 KLR outperforms the LOWESS and PolyFit models for all four sites. The PolyFit model (RMSE:  
609 0.70 and MAE: 0.76) better performs than does the LOWESS model (RMSE: 0.94 and MAE:  
610 0.83) for Site-4, while LOWESS is always better for other sites. The overall result of the case  
611 study indicates that the KLR method can reproduce the characteristics of the cross-section of a  
612 natural river and be a good alternative to demarcate a cross-section in a river.

## 613 **6. Case Study of Yecheon**

### 614 **6.1. Study Area and Data Acquisition**

615 One more case site, the Pori-cheon stream in Yecheon-gun was selected to reveal the  
616 performance of the proposed KLR model with the point cloud as shown in Figure 23. Four sites  
617 were ground-surveyed with the EMLID Reach RS2 and aerial surveying was also performed  
618 with the Autel Evo II. For this site, the same UAV and GPS tool were used as the REC in  
619 section 4. The Y1 is located in the upper stream of the Pori-cheon stream than the Y4. The  
620 cross-section of Y2 is located in the right below of the bridge followed by the Y3 cross-section.  
621 The detailed shape of the cross-section is shown from Figure 24 to Figure 27 for each cross-  
622 section. At each section, 10-12 points were ground-surveyed and the point cloud were abstracted



623 with Pix4D mapper while the bottom width is about 10m. The demarcation of the cross-section  
624 with the tested KLR, LOWESS, and Polyfit models was performed.

## 625 **6.2. Results**

626 The shape of the Y1 cross-section presents the rough river bottom (Figure 24) while the  
627 left section has lower bottom and the section should be major flow passage during low  
628 streamflow. The other side of this cross-section has further ups and downs possibly by debris and  
629 riparian vegetation. These ups and downs were not measured in detail by ground surveying.  
630 Additional ground surveying can capture the characteristic. However, it requires further time  
631 consumption for measurement and the accessibility cannot be guaranteed even in such a small  
632 stream. Meanwhile, the point cloud captures the detailed characteristics of the channel bottom  
633 and KLR model describes the characteristics as shown in the top panel of Figure 24 following  
634 the major cloud data. In LOWESS, the Y1 cross-section is not presented with missing the abrupt  
635 change in both walls of the cross-section (the middle panel of Figure 24) and all the Polyfit  
636 models present similar behavior as the result of the LOWSS. The wall part (5-6m and 17-18m of  
637 the cross-section) was not well reproduced by the Polyfit models. The RMSE and MAE in Table  
638 5 present the superiority of the KLR for the Y1 cross-section. The RMSE and MAE of the Y1 is  
639 rather larger than the other cross-section. This large error might be induced from the ups and  
640 downs of the channel bottom.

641 Meantime, the Y2 cross-section in Figure 25 shows similar to the U-shape of a natural  
642 river in Figure 8. The ground-surveyed points (blue solid line with cross markers in Figure 25)  
643 are matched well with the point cloud data except the slight deviation at the left-top embankment  
644 (in 2-3m). This U-shape cross-section is demarcated well with the KLR model while slight



645 underestimation can be observed with the LOWESS model in the right embankment (13-14m).  
646 Not much good performance can be seen with all the Polyfit models shown at the bottom panel  
647 of Figure 25. The RMSE and MAE in Table 5 also show the worst performance in the Polyfit  
648 models and superiority with the KLR model.

649 The Y3 and Y4 cross-sections in Figure 26 and Figure 27, respectively, present traditional  
650 man-made trapezoid shape. These trapezoid channels were modeled both with KLR and  
651 LOWESS while the KLR presents better descriptive characteristics in the abrupt changing part of  
652 the cross-section. While the Polyfit-4 presents fair performance to model the Y4 cross-section in  
653 Figure 27, the Y3 was not demarcated well with all the Polyfit models. The RMSE of the KLR  
654 model is only 0.092 and 0.068 while the LOWESS shows 0.236 and 0.116 for the Y3 and Y4  
655 cross-sections in Table 5. The results indicate that the KLR model presents superiority among all  
656 the tested LOWESS and Polyfit models in case of all different shapes as the irregular U-shape,  
657 trapezoid-shape channels in the Pori-cheon stream, Yecheon.

## 658 **7. Discussion**

659 The results of the synthetic simulation study and two case studies as well as the experiment  
660 study of the REC site present that the proposed KLR model can demarcate the cross-sections of a  
661 river with different shapes. However, there are some limitations and conditions to apply the  
662 proposed model in the demarcation of river cross-sections. At first, UAV sensors cannot  
663 penetrate water depth unless bathymetric technology is not applied. Currently, river  
664 photogrammetry with bathymetry data has been applied to penetrate water body using  
665 specialized sensors, such as Light Detection and Ranging (LiDAR), which is called bathymetry  
666 LiDAR (Allouis et al., 2010; Fernandez-Diaz et al., 2014). The case study of the current study





667 does not use the bathymetry data, since the water depth is very shallow and not critical to  
668 illustrate a river cross-section. The proposed KLR model with the point cloud data must be  
669 carefully applied to a dry stream or very shallow river with the water surface whose level is  
670 ignorable especially for its discharge amount. Otherwise, a bathymetry data must be applied  
671 using a special sensor (e.g. bathymetry LiDAR).

672 Secondly, the KLR model should define the number of K-neighbors. The result of the  
673 tested model illustrates that the value of 1.5-2.5 for 'a' in Eq. (10) might be a good range. Further  
674 estimation procedure might be required in some cases to produce cross-sections that are more  
675 accurate. However, the value is not very sensitive at each case presented in the current study.  
676 Note that  $a=2.0$  was employed -for the U-shape and V-shape synthetic cross-section and the case  
677 study without any further estimation procedure.

678 Furthermore, traditional ground surveying might be essential to supplement UAV or  
679 LiDAR-based point clouds for the purpose of hydraulic modeling due to the penetration  
680 capability of sensors and sensitivity even with capable sensors. A ground surveying for a few  
681 cross-sections can be performed in addition to UAV surveying. The ground-surveyed cross-  
682 sections can be employed to validate the UAV-based cross-sections. This additional ground  
683 surveying might improve much the quality of the UAV-based cross-sections.

684 The UAV-based demarcation of cross-sections still has some limitations and conditions to  
685 ensure its credibility, such as water penetration and additional requirement of ground surveying  
686 Nevertheless, the proposed KLR model can be applicable to the demarcation of different cross-  
687 section shapes with UAV point cloud data. In addition, UAV sensors and photogrammetry  
688 technology have been developed so that the current KLR method might be more useful and  
689 applicable with UAV-based data. UAV surveying can be a potential surrogate for its relatively



690 cheap and time-saving. The river cross-section with UAV surveying can be beneficial when the  
691 ground surveying cannot be made. After initial ground surveying, further resources may not be  
692 available for additional ground surveying. In this case, the river cross-section with UAV  
693 surveying can extract any places inside the surveyed area.

## 694 **8. Summary and Conclusions**

695 The current study presents a nonparametric fitting method, KLR, to the point cloud data  
696 from UAV areal surveying to demarcate the cross-section of a river. Other than general fitting  
697 data, the cross-section of a natural river generally contains sudden variation, an angled shape,  
698 and even bumps as well as a linear shape. To accommodate all of those features of natural and  
699 manmade cross-sections, a highly flexible fitting model is requested. Furthermore, the observed  
700 data point from a UAV surveying is large enough for the point cloud dataset. Therefore, the KLR  
701 model can be chosen to fit the point cloud data for cross-sections. Different river shapes with  
702 simulation study and the experimental site study of the REC were made as well as two case  
703 studies of the Migok-cheon stream, Hapcheon-gun and the Pori-cheon stream, Yecheon-gun.  
704 From the extensive applications of the proposed model in the current study, the results conclude  
705 that the suggested KLR model can reproduce the critical characteristics of the different shape  
706 cross-sections of a river with the point cloud data from UAV aerial surveying.

707 The major limitation of the point cloud data employed in the current study is that RGB  
708 photographs were employed and the vegetation inside the river could generate an obscure cross-  
709 sectional shape. Further optical instruments, such as hyperspectral and lidar sensors, could be  
710 tested to overcome this limitation. However, a perfect solution that can remove the vegetation  
711 inside rivers has not yet been developed. To avoid this issue, points of the cross-section where



712 little vegetation exists can be selected. Also, a general UAV sensor cannot penetrate water body  
713 and a special sensor (e.g. bathymetry LiDAR) must be employed to capture the shape of the  
714 cross-section below water surface. Therefore, special care must be taken to apply the current  
715 model to UAV surveying data. The current demarcation method for a cross-section must be  
716 applied to a dry stream or very shallow stream whose flow does not affect the discharge amount.  
717 Otherwise, a bathymetry data must be employed for demarcating a cross-section of a river. Since  
718 the sensors that can penetrate water body and UAV technologies are developing fast, the  
719 proposed KLR model with the UAV surveying might become more suitable in near future to  
720 demarcate a cross-section.

721 The proposed KLR method can be easily adopted for other demarcation cases, such as  
722 buildings and structures. The proposed KLR method is a rather simple and direct approach for  
723 demarcating an area and structures. Additionally, other nonparametric techniques, such as  
724 LOWESS, can be further tested with extensive testing and adjustment. The current study focused  
725 on the KLR model, since the clustered data setting is obvious and easy to apply.

## 726 **9. Code and data availability**

727 The program was developed with Matlab program. All the employed code and excel files  
728 are available at Mendeley Data in <<http://dx.doi.org/10.17632/xdw4cgnvhm.1>>.

### 729 **Competing interests**

730 The author declares that they have no conflict of interest.

### 731 **Author Contribution**



732 T.L. carried out the research plan and programming as well as supervising while J.P. and  
733 S.H performed collection data and data curation. VS performed editing this manuscript and  
734 additional simulation studies.

735

736

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738 The authors thank the River Experiment Center of Korea Institute of Civil Engineering and  
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740 cooperation.

741



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- 861





862 Table 1. Performance measures of RMSE and MAE for three different models, KLR, LOWESS,  
 863 and PolyFit, for synthetically simulated data of three different shape cross-sections as trapezoidal,  
 864 U-shape, and V-shape.

	Shape	KLR	LOWESS	PolyFit4
RMSE	Trapezoid	0.0289	0.1397	0.1565
	U-shape	0.0326	0.1868	0.1728
	V-shape	0.0325	0.1353	0.2299
MAE	Trapezoid	0.1549	0.3697	0.3789
	U-shape	0.1536	0.3158	0.3518
	V-shape	0.1558	0.2807	0.4369

865

866

867 Table 2. Performance measures of RMSE for three different models as KLR, LOWESS, and  
 868 PolyFit for the river experiment center (REC).

	No	KLR	LOWESS	Polynomial		
				2	3	4
I-shape	1	<b>0.072</b>	0.125	0.183	0.183	0.138
	2	<b>0.101</b>	0.154	0.231	0.235	0.156
	3	<b>0.074</b>	0.192	0.281	0.284	0.148
	4	<b>0.054</b>	0.12	0.17	0.174	0.177
	5	<b>0.054</b>	0.17	0.33	0.291	0.289
	6	<b>0.062</b>	0.127	0.359	0.287	0.205
U-shape	1	<b>0.029</b>	0.074	0.134	0.13	0.088
	2	<b>0.066</b>	0.118	0.182	0.155	0.119
	3	<b>0.045</b>	0.072	0.113	0.111	0.094
	4	<b>0.054</b>	0.083	0.149	0.146	0.105
	5	<b>0.170</b>	0.183	0.196	0.183	0.219
	6	<b>0.131</b>	0.183	0.374	0.363	0.201
	7	<b>0.171</b>	0.246	0.419	0.427	0.204
S-shape	1	<b>0.122</b>	0.145	0.435	0.429	0.151
	2	<b>0.088</b>	0.112	0.398	0.398	0.118
	3	0.204	0.216	0.428	0.416	<b>0.203</b>
	4	<b>0.164</b>	0.197	0.452	0.467	0.178
	5	<b>0.187</b>	0.186	0.433	0.419	0.213
	6	<b>0.123</b>	0.146	0.402	0.404	0.136
	7	<b>0.145</b>	0.146	0.48	0.488	0.22

869



870 Table 3. Performance measures of MAE for three different models as KLR, LOWESS, and  
 871 PolyFit for the river experiment center (REC).

	No	KLR	LOWESS	Polynomial		
				2	3	4
I-shape	1	<b>0.062</b>	0.114	0.162	0.163	0.13
	2	<b>0.083</b>	0.135	0.194	0.197	0.125
	3	<b>0.06</b>	0.146	0.183	0.184	0.123
	4	<b>0.048</b>	0.097	0.142	0.143	0.144
	5	<b>0.04</b>	0.112	0.275	0.233	0.178
	6	<b>0.05</b>	0.098	0.299	0.224	0.139
U-shape	1	<b>0.021</b>	0.061	0.117	0.112	0.08
	2	<b>0.059</b>	0.104	0.141	0.132	0.105
	3	<b>0.035</b>	0.058	0.099	0.098	0.076
	4	<b>0.039</b>	0.072	0.126	0.126	0.091
	5	<b>0.117</b>	0.14	0.173	0.142	0.177
	6	<b>0.083</b>	0.151	0.3	0.29	0.169
	7	<b>0.148</b>	0.209	0.341	0.331	0.167
S-shape	1	<b>0.094</b>	0.113	0.377	0.339	0.12
	2	<b>0.082</b>	0.091	0.342	0.344	0.105
	3	0.167	0.173	0.36	0.33	<b>0.162</b>
	4	<b>0.142</b>	0.156	0.392	0.368	0.154
	5	<b>0.147</b>	0.136	0.379	0.374	0.19
	6	0.101	0.117	0.372	0.371	<b>0.1</b>
	7	<b>0.118</b>	0.112	0.43	0.43	0.172

872

873 Table 4. Performance measures of RMSE and MAE for three different models as KLR,  
 874 LOWESS, and PolyFit for four sites of Hapcheon-gun.

	Site No.	KLR	LOWESS	PolyFit2	PolyFit3	PolyFit4
RMSE	Site-1	0.4063	0.8389	1.8548	1.8046	1.4218
	Site-2	0.4010	0.6736	1.3762	1.1252	0.8753
	Site-3	0.3236	0.4514	1.4722	1.4327	0.9753
	Site-4	0.4786	0.9419	1.3834	1.9593	0.7068
MAE	Site-1	0.5393	0.8197	1.3034	1.2934	1.1224
	Site-2	0.4406	0.5764	1.1758	1.1611	0.9482
	Site-3	0.5746	0.7439	1.1536	1.0342	0.8221
	Site-4	0.6422	0.8307	1.1500	1.1057	0.7615



875

876

877 Table 5. Performance measures of MAE and RMSE for three different models as KLR,  
878 LOWESS, and PolyFit for Yecheon.

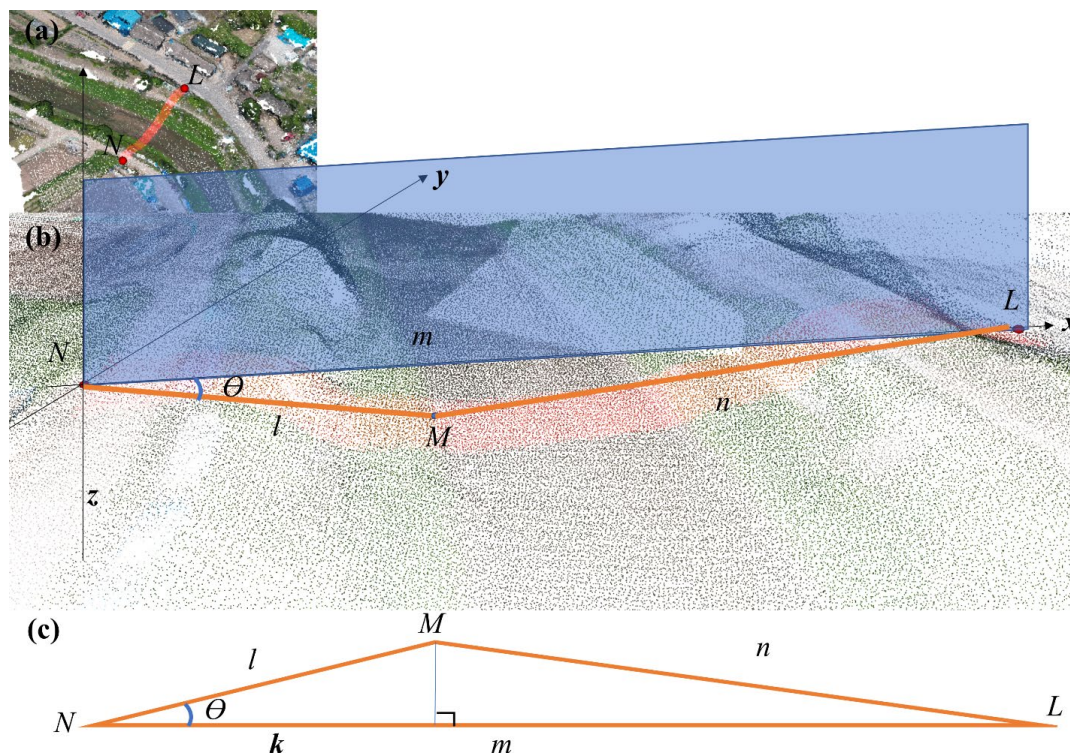
	Site No.	KLR	LOWESS	PolyFit2	PolyFit3	PolyFit4
RMSE	Y1	<b>0.235</b>	0.461	0.652	0.566	0.533
	Y2	<b>0.135</b>	0.279	0.750	0.721	0.377
	Y3	<b>0.092</b>	0.236	0.693	0.659	0.401
	Y4	<b>0.068</b>	0.116	0.425	0.362	0.124
MAE	Y1	<b>0.158</b>	0.356	0.544	0.446	0.435
	Y2	<b>0.098</b>	0.223	0.678	0.647	0.289
	Y3	<b>0.073</b>	0.178	0.634	0.571	0.353
	Y4	<b>0.047</b>	0.079	0.240	0.232	0.108

879

880



881 **Figure**



882

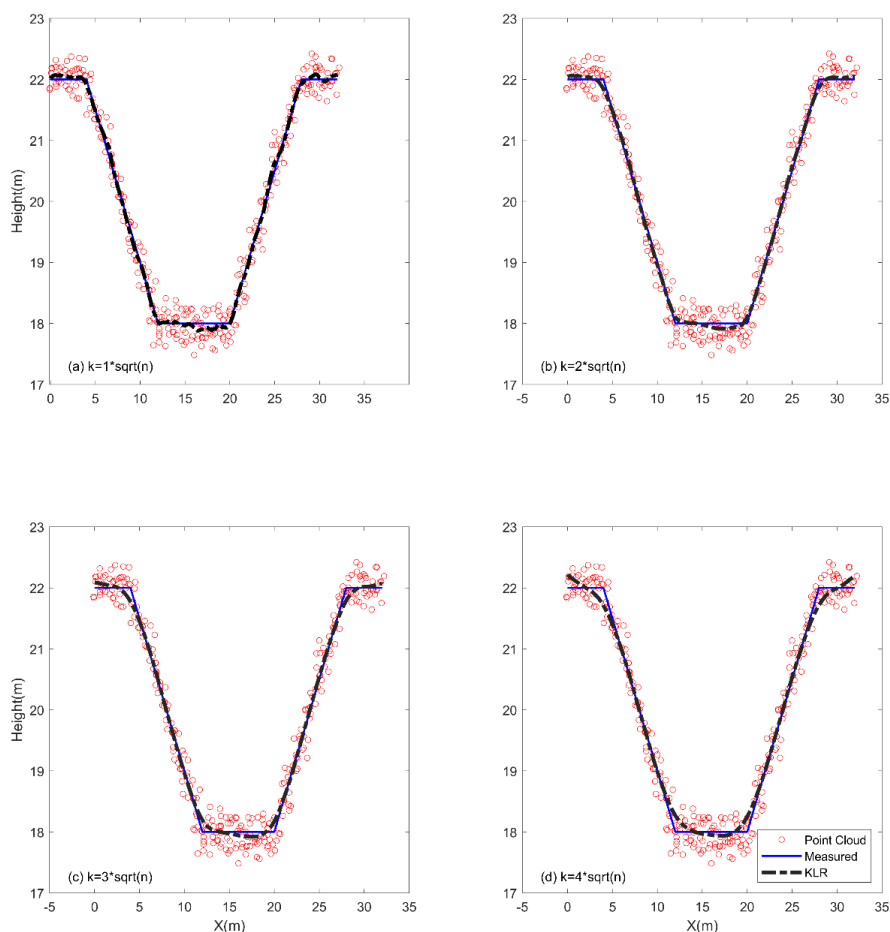
883 Figure 1. Example of the distance measurement: (a) aerial photo with a selected cross-section  
884 (two red dots, L and N, and thick red line); (b) magnified photo of Panel (a) with assisted 3D  
885 axis (x, y, and z) and the selected point (M); (c) emphasized triangle with the points of NML.  
886 Note that (1) the cross-section can be defined with the x-axis by connecting points N and L with  
887 the line; (2) the point M is the example point that contains the red line at Panel (a), which is a  
888 group of points in reality; and (3) the actual distance of M from N in the x-axis is represented as  
889  $k$ , which can be designated as N to the point that meets line NL perpendicularly from M. The  
890 aerial images were taken from the authors.

891

892



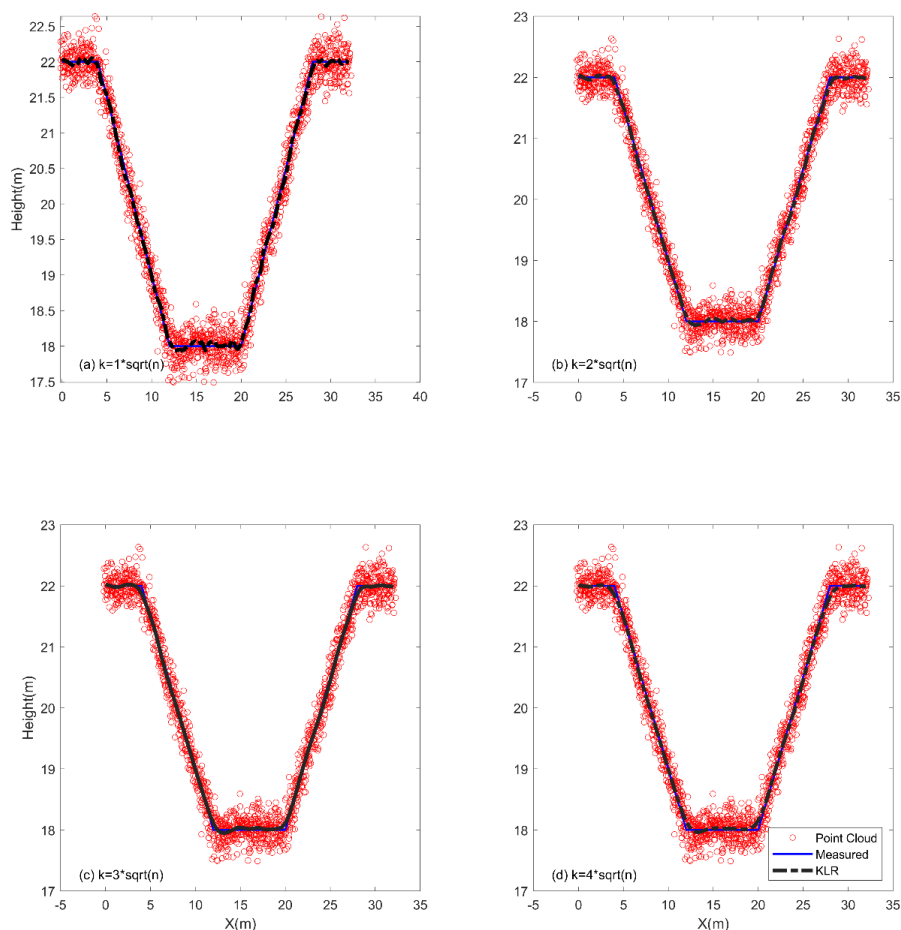
893



894

895 Figure 2. Assumed synthetic trapezoidal channel (not a real one) to test the KLR model (thick  
896 black dotted line) for the point cloud data with different portions of the number of neighbors  
897 ( $k = a\sqrt{n}$ , here  $a=1, 2, 3,$  and  $4$  at each panel). Note that (1) the trapezoidal sections are  
898 consistent with a 4 m top both sides and a 6 m base width as well as a 1:1 side slope with a 6 m  
899 height; (2) the number of points for the channel was divided at each 0.1 m to a total of 161 points  
900 (blue line); (3) 2 times the divided data are simulated with Eq.(17) to a total of 322 points (red  
901 dots); and (4) the elevation of the bottom channel was assumed to be 18 m.

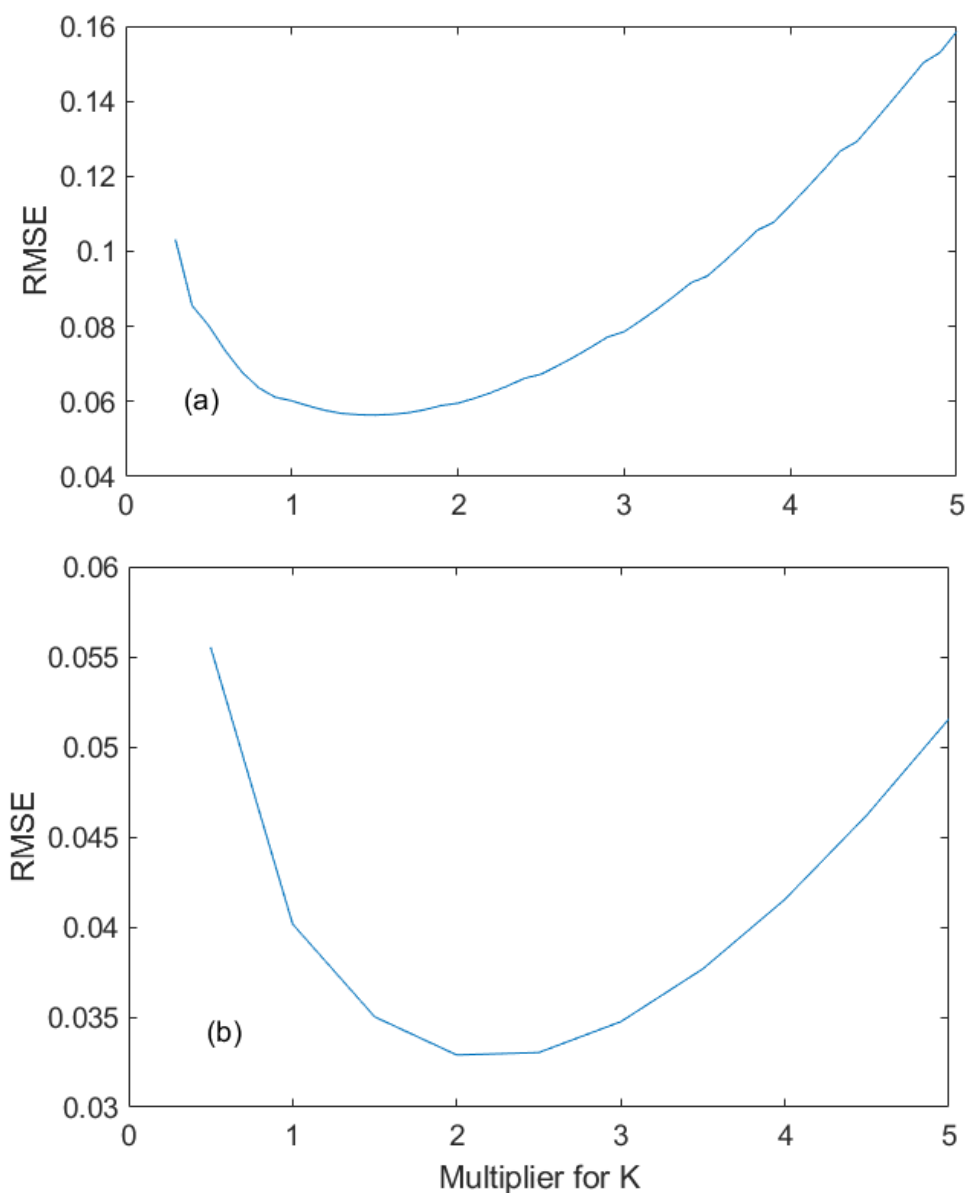
902



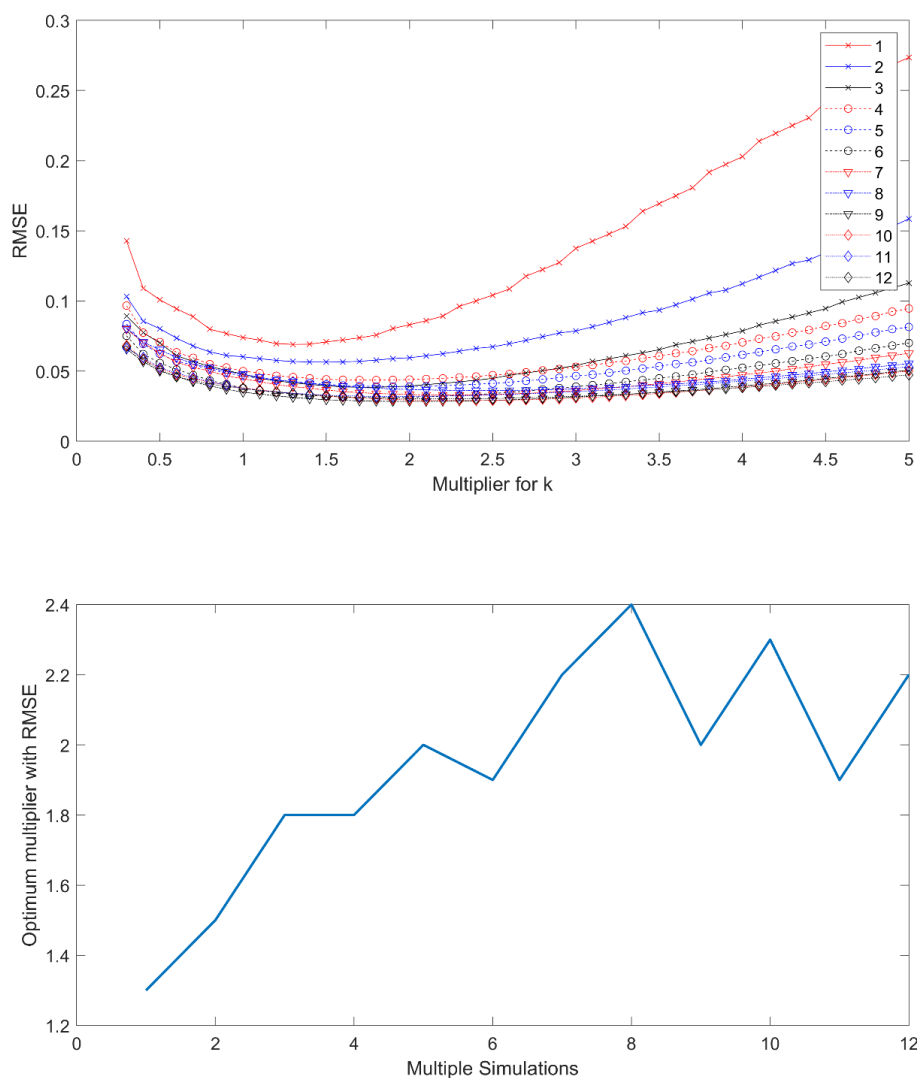
903

904 Figure 3. Assumed synthetic trapezoidal channel to test the KLR model for point cloud data with  
905 different multipliers of the number of neighbors ( $k = a\sqrt{n}$ ). Note that (1) the trapezoidal  
906 sections are consistent with a 4 m top both sides and a 6 m base width as well as a 1:1 side slope  
907 with a 6 m height; (2) the number of points for the channel was divided at each 0.1 m to a total  
908 161 points (blue line); (3) 10 times the divided data are simulated with Eq.(17), to a total of 1610  
909 points (red dots) and it is 5 times more simulated cloud points than the ones in Figure 2. The  
910 difference between the number of points in the current and the one in Figure 2 was intentionally  
911 designed to illustrate how the proposed KLR model performs when there is a small number of  
912 cloud points or a large number of cloud points; and (4) the elevation of the bottom channel was  
913 assumed to be 18 m.

914



915  
916 Figure 4. Root mean square error (RMSE) between the KLR estimate with different multipliers  
917 (a) of the number of neighbors ( $k = a\sqrt{n}$ ) and the original trapezoid points for the case of 2  
918 times the original points (panel (a)) and 10 times (panel (b)).



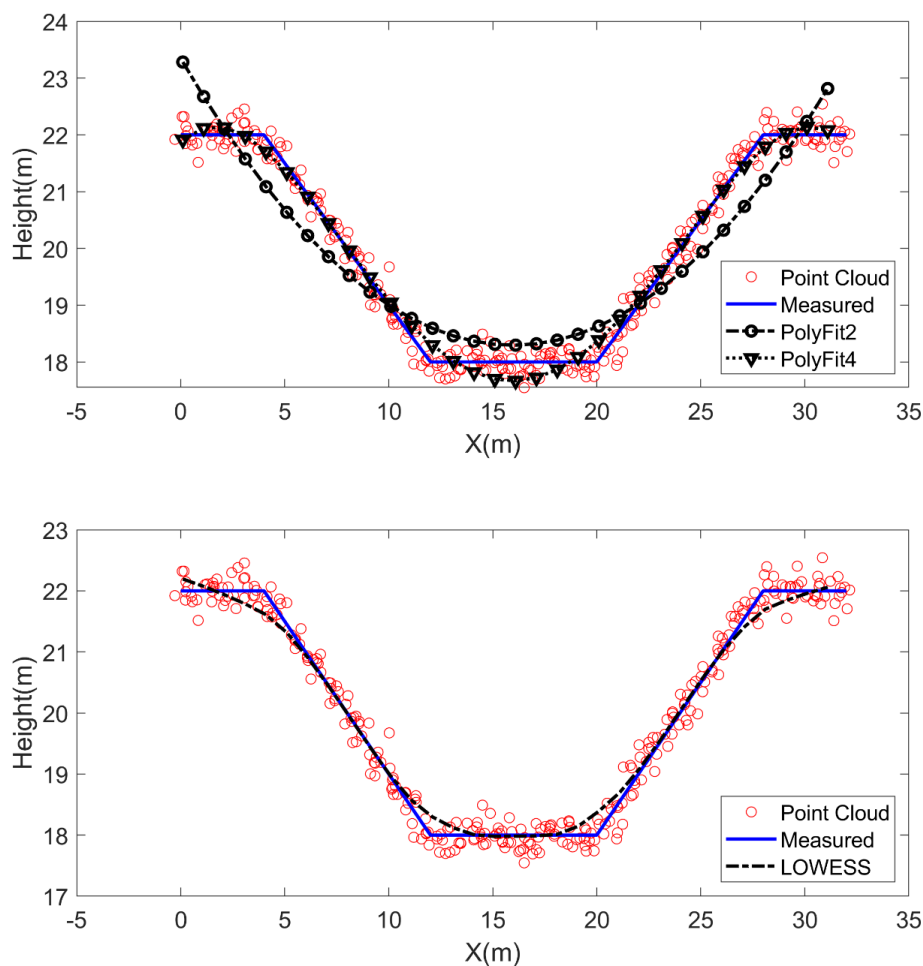
919

920 Figure 5. Root mean square error (RMSE) between the KLR estimate with different multipliers  
 921 of for number of neighbors ( $k = a\sqrt{n}$ ) and the original trapezoid points for all of the cases  
 922 between 1 and 12 times the original points (top panel) as well as the optimum multiplier with the  
 923 RMSE value at the top panel for each multiple simulation. Note that increasing the number of  
 924 multiple simulations indicates that the number of overlapped photos is increased and the cloud  
 925 points are multiplied.





926



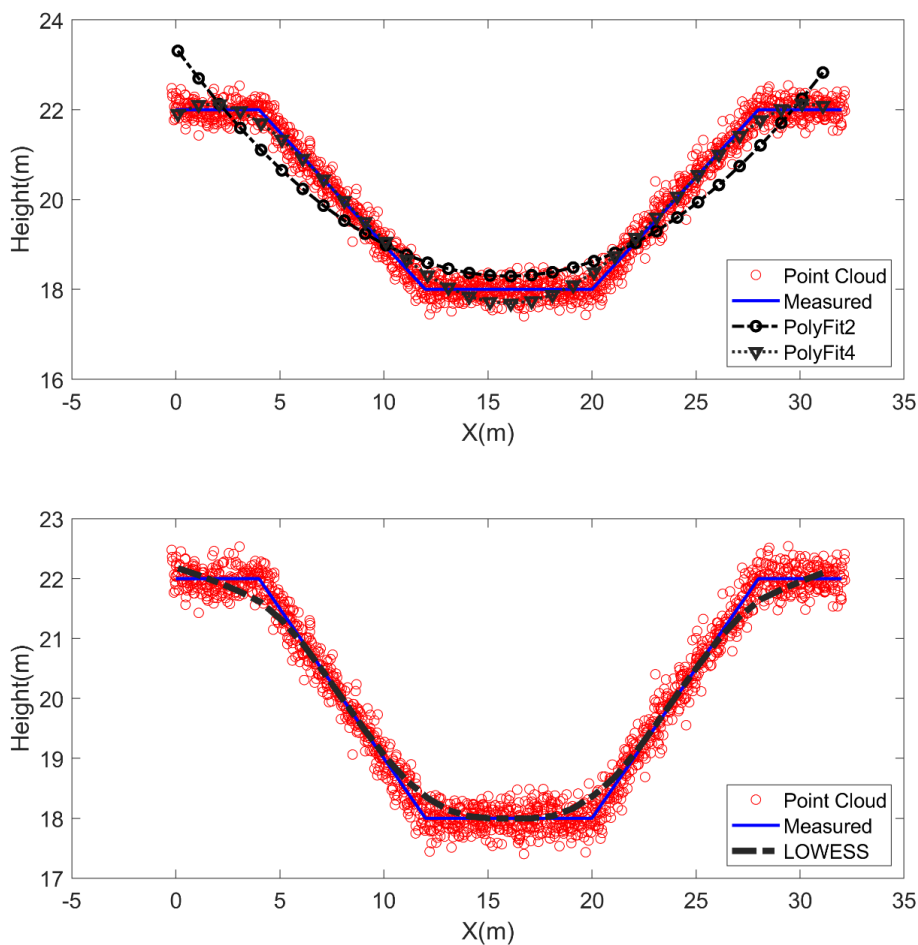
927

928 Figure 6. Polynomial regression (top panel) with the black dashed line with circles and the black  
929 dotted line with triangle markers for PolyFit2 and PolyFit4, respectively (see Eqs.(2) and (4))  
930 and LOWESS (bottom panel, dash-dotted line) were fitted to the stochastically simulated point  
931 cloud data (red circles) of 2 times the divided points (322 points) of the synthetic trapezoidal  
932 channel points (blue line).

933

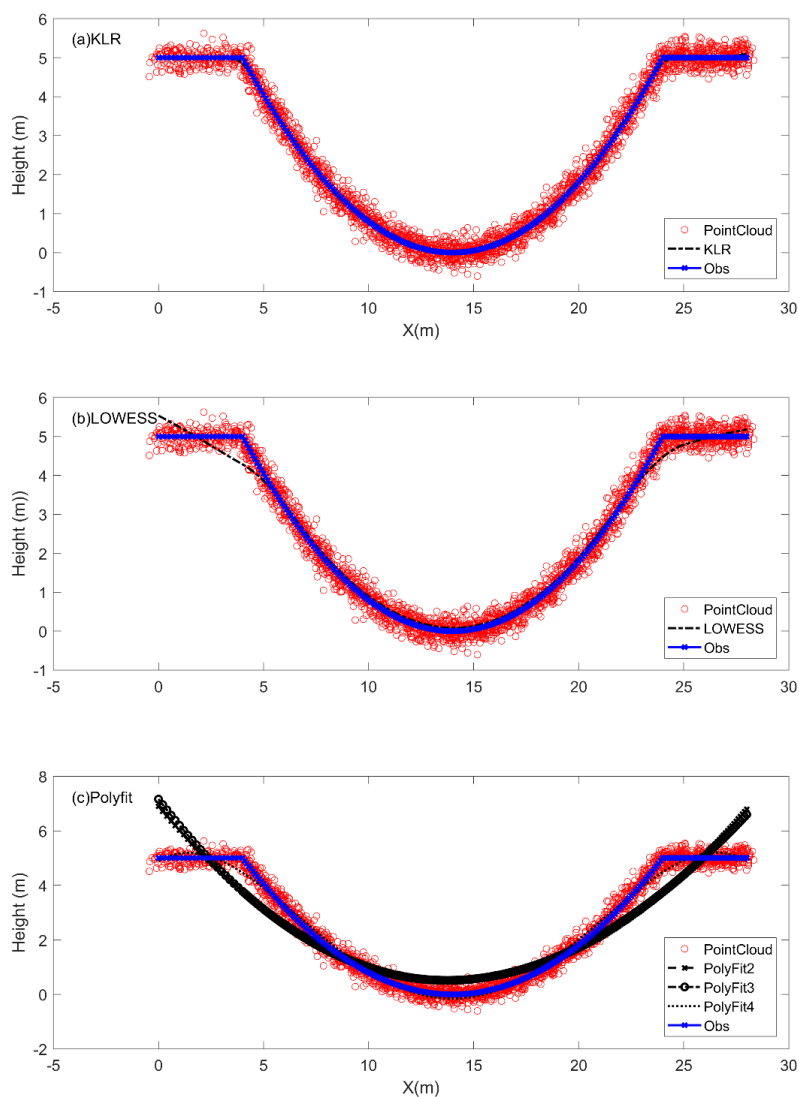


934

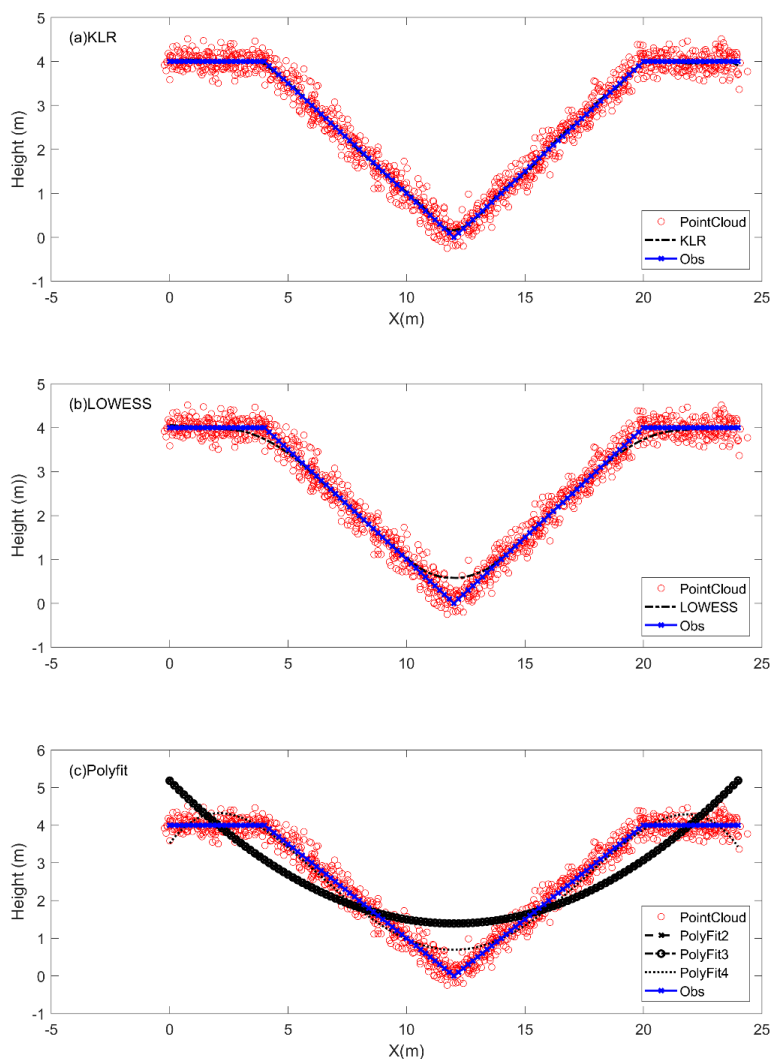


935  
936 Figure 7. Polynomial regression (top panel) with the black dashed line with circles and the black  
937 dotted line with triangle markers for PolyFit2 and PolyFit4, respectively (see Eqs. (2) and (4))  
938 and LOWESS (the dash-dotted line in the bottom panel) fitted to the simulated point cloud data  
939 (red circles) of 10 times the synthetic trapezoidal channel points (blue line) with Eq.(17).

940  
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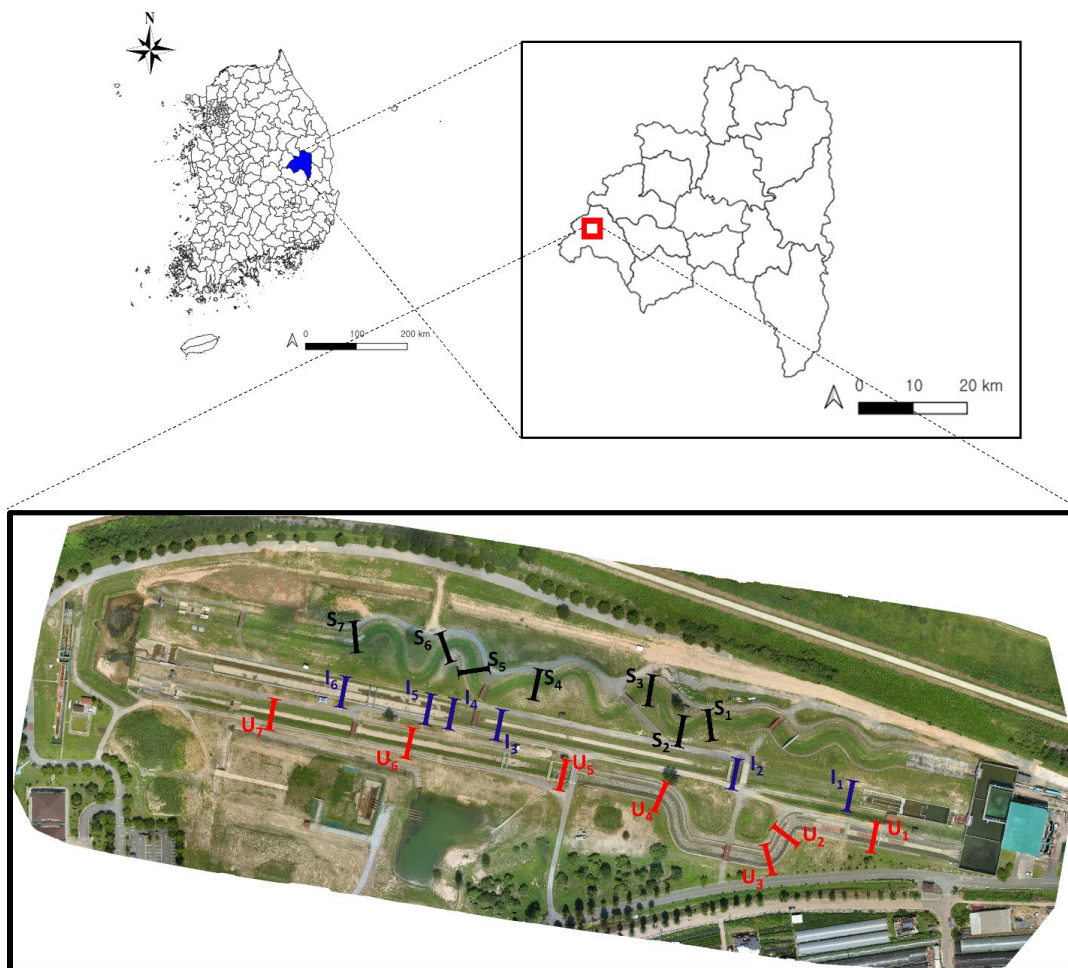


942  
943 Figure 8. Synthetic U-shape river cross-section (blue solid line with cross markers) and the  
944 simulated point cloud data (red circles) of 10 times the synthetic channel (2620 points total) with  
945 Eq.(17) as well as the fitted estimates to KLR (the panel(a)), LOWESS (the panel(b)), and  
946 PolyFit (the panel(c)). Note that the U-shape river cross-section was designed with the power  
947 function as in Eqs. (19) and (20) and the U-shape was synthetically built following the reference  
948 of Neal et al. (2015) and the section was divided into 262 points.



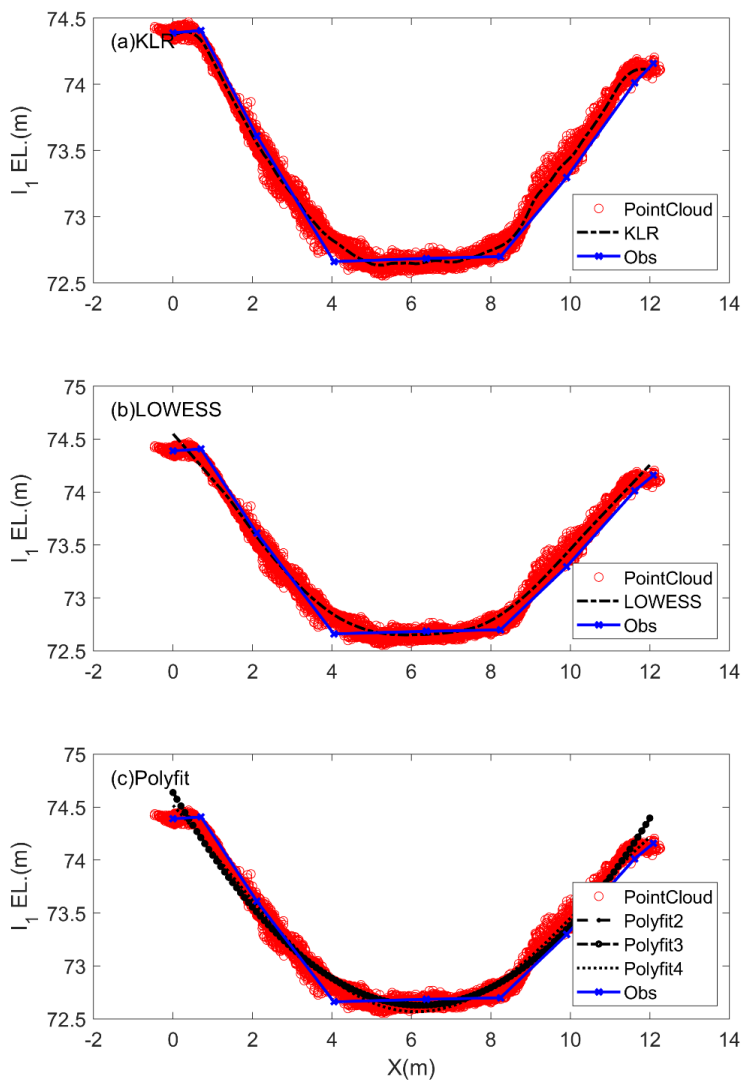
949  
950 Figure 9. Synthetic V-shape river cross-section (blue solid line with cross markers) and the  
951 simulated point cloud data (red circles) of 10 times the synthetic channel (2620 points total) with  
952 Eq.(17) as well as the fitted estimates to KLR (the panel(a)), LOWESS (the panel(b)), and  
953 PolyFit (the panel(c)). Note that (1) the V-shape river cross-section was designed with the height  
954 of 4 m and top width of 16 m and the section was divided into 121 points.

955



956  
957 Figure 10. Location of the River Experiment Center (REC) at the top panels and the selected  
958 channels of the ground surveying for the straight river with I-shape ( $I_1, \dots, I_6$ ), the meandering river  
959 with S-shape ( $S_1, \dots, S_7$ ), and the steep river with U-shape ( $U_1, \dots, U_7$ ) rivers. The aerial image is  
960 taken and produced by the authors and no copyright is required.

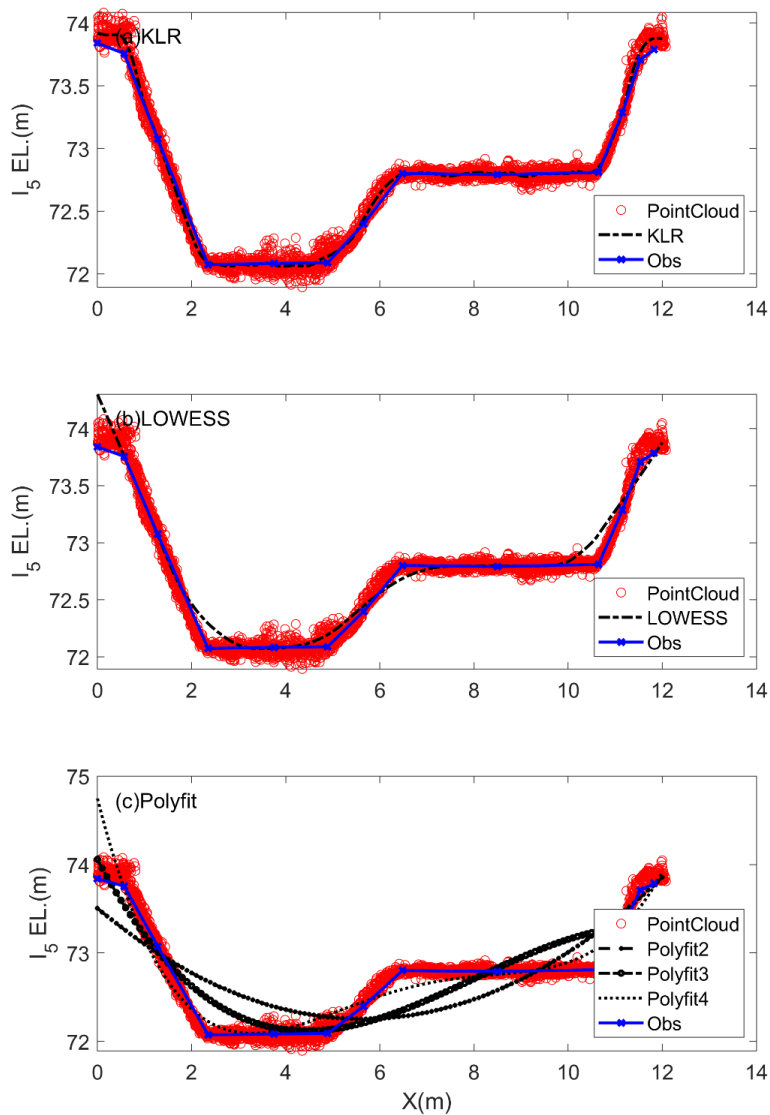
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963

964 Figure 11. Point cloud data (red circles) for the channel  $I_1$  of the REC site and model-fitted line  
965 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
966 the ground surveying.

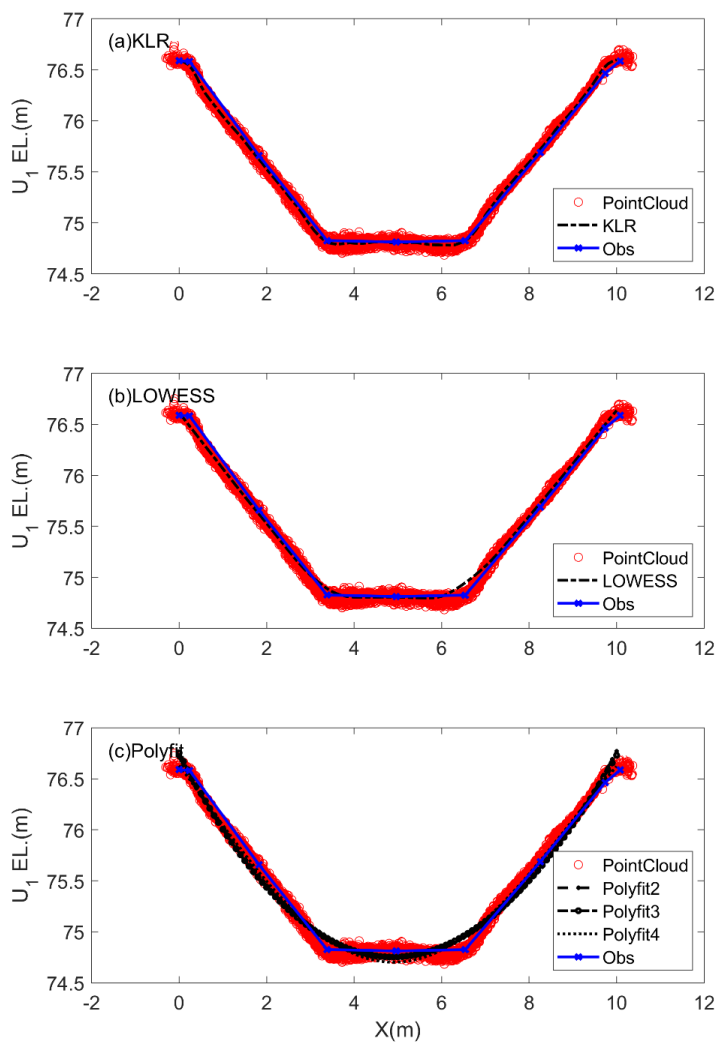
967



968

969 Figure 12. Point cloud data (red circles) for the channel  $I_5$  of the REC and model-fitted line  
970 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
971 the ground surveying.

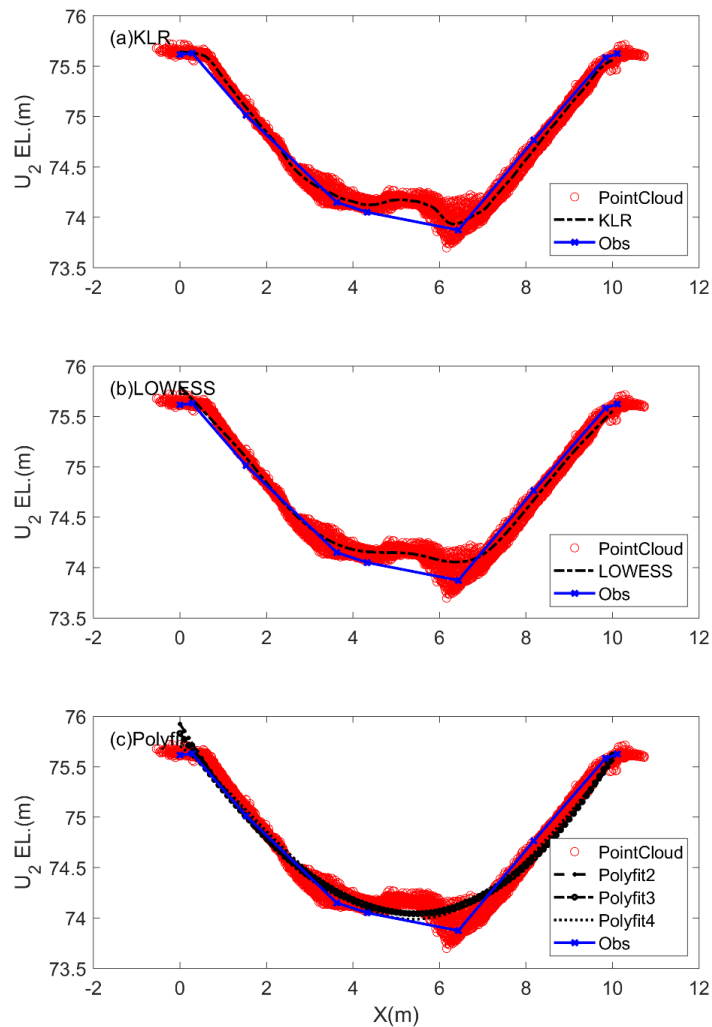
972



973  
974 Figure 13. Point cloud data (red circles) for the channel  $U_1$  of the REC and model-fitted line  
975 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
976 the ground surveying.

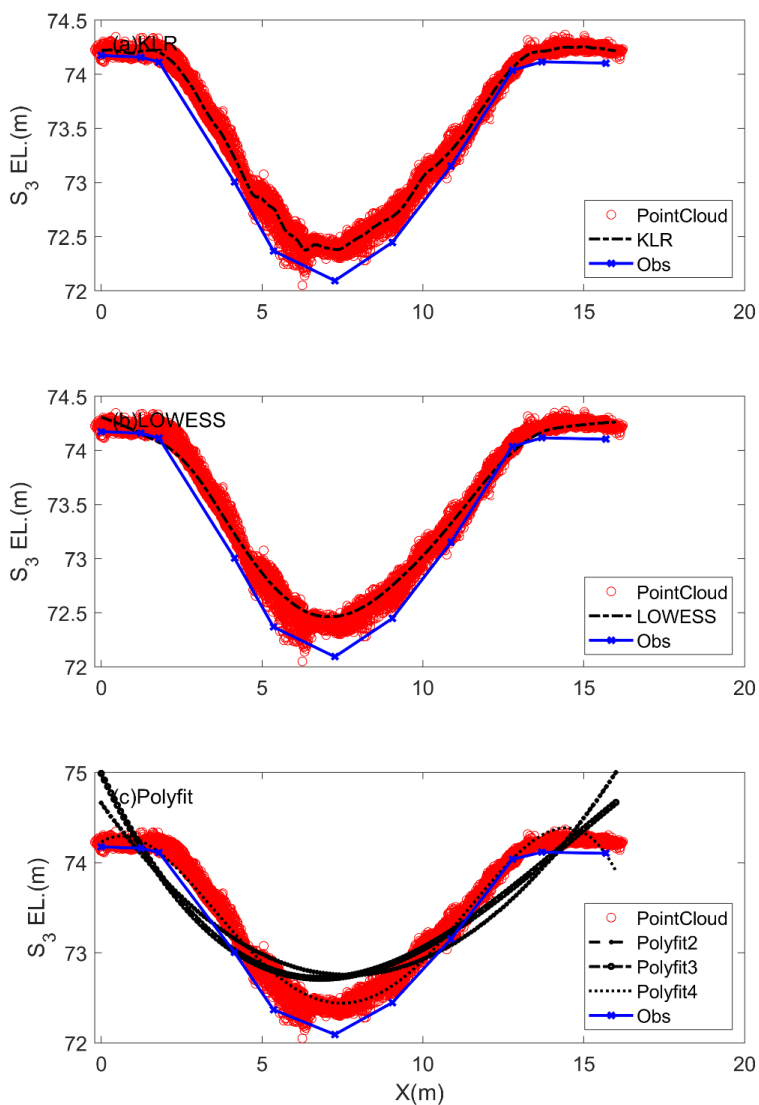
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978  
979 Figure 14. Point cloud data (red circles) for the channel  $U_2$  of the REC and model-fitted line  
980 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
981 the ground surveying.

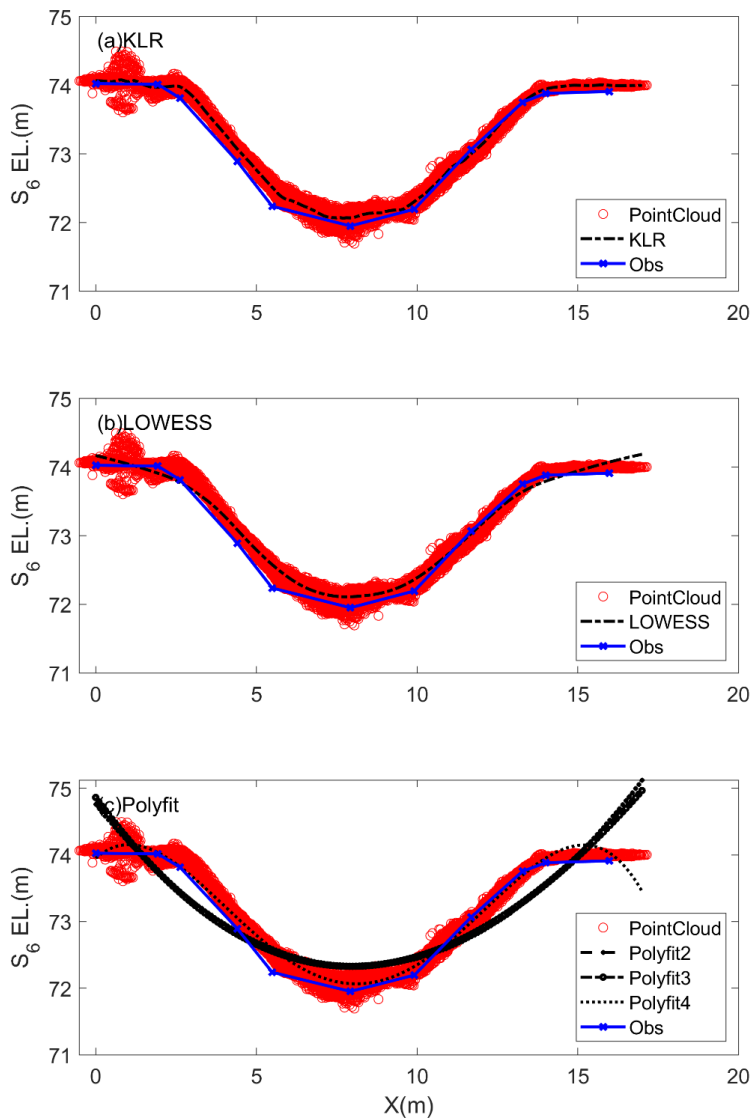
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984

985 Figure 15. Point cloud data (red circles) for the channel S<sub>3</sub> of the REC and model-fitted line  
986 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
987 the ground surveying.

988



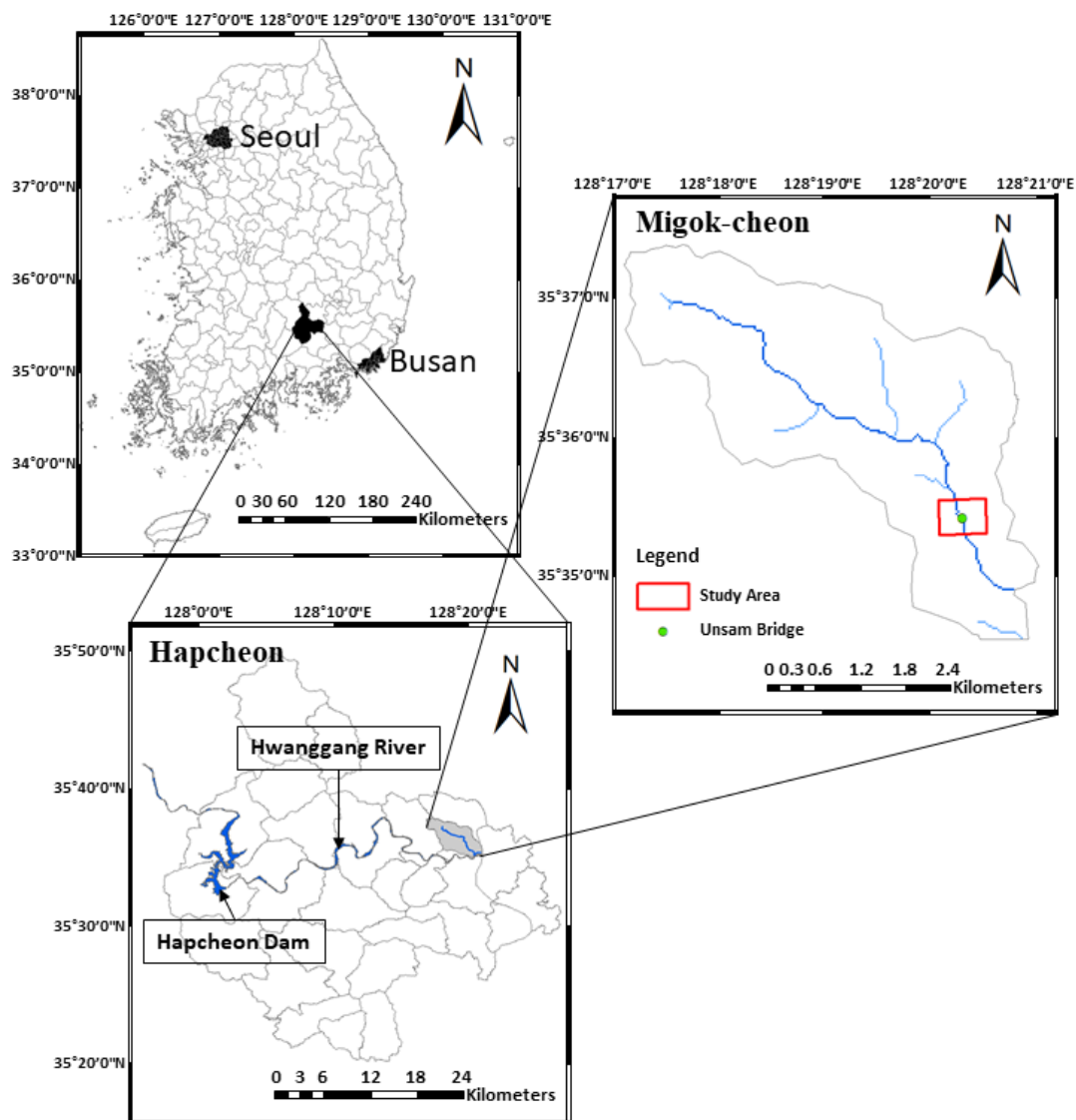
989

990 Figure 16. Point cloud data (red circles) for the channel  $S_6$  of the REC and model-fitted line  
991 (black dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as  
992 the ground surveying (blue solid line with x marker).

993



994



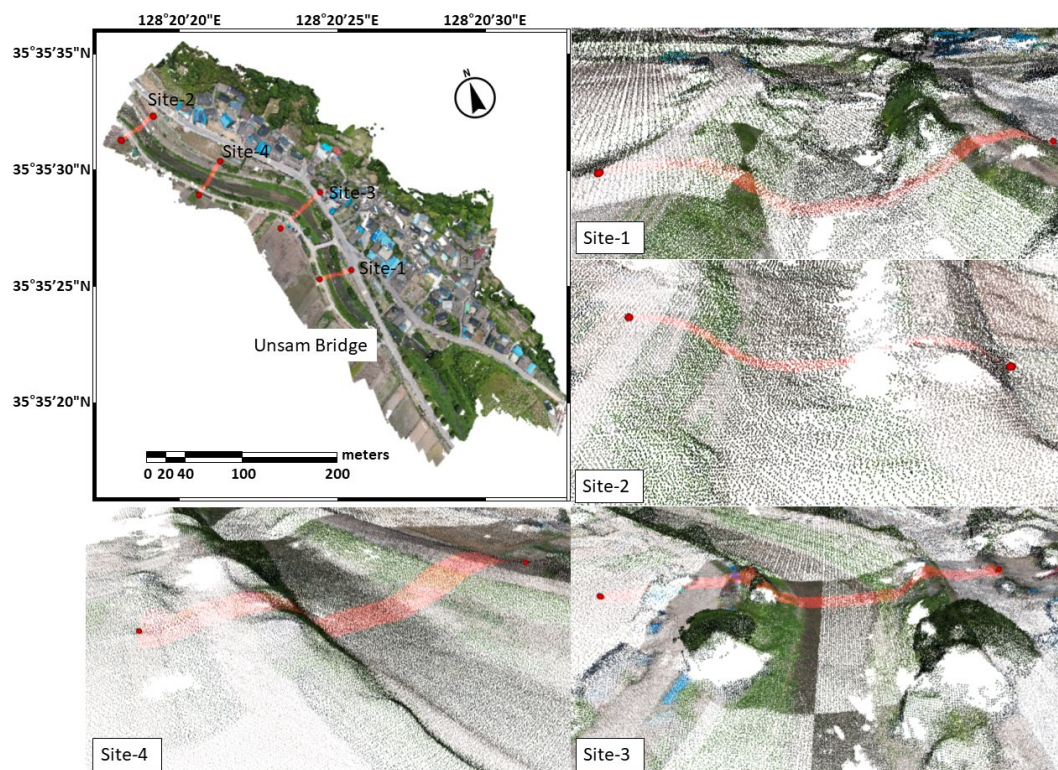
995

996 Figure 17. Study area of the applied stream, Migok-cheon in South Korea, located in the  
997 province of Hapcheon-gun.

998



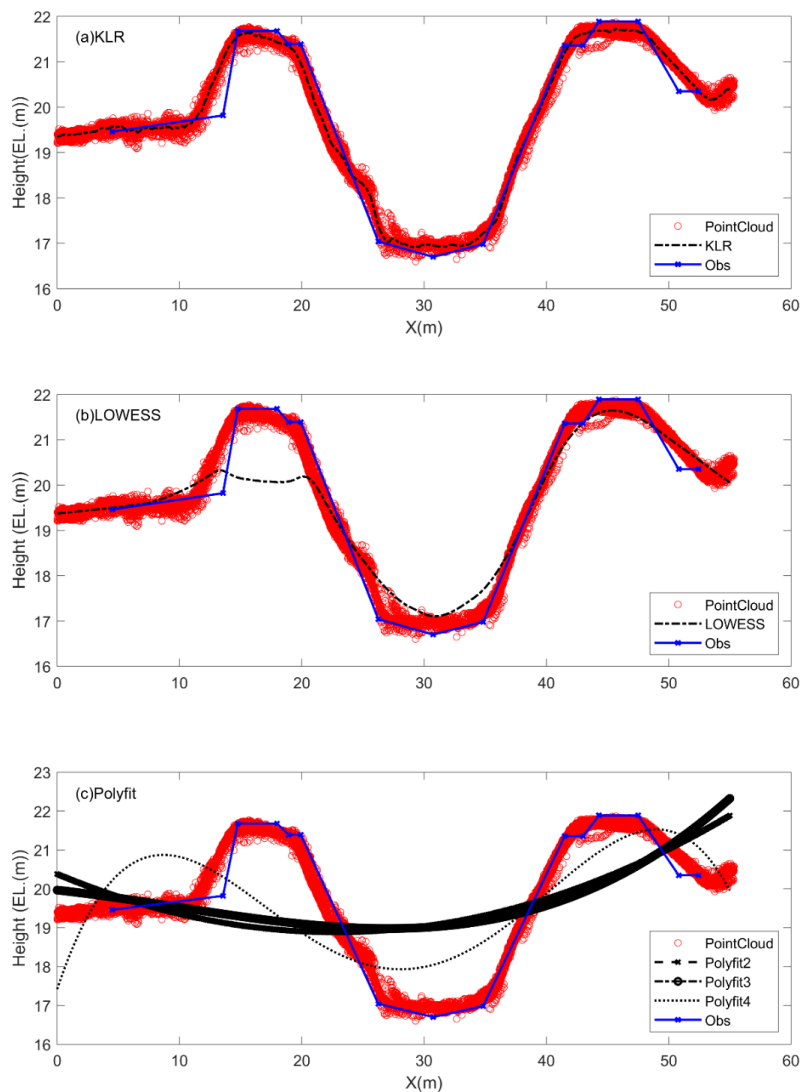
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1000  
1001 Figure 18. Locations of four tested sites in the Migok-cheon stream. Note that the other four  
1002 panels surrounding the left-top panel magnify each tested site by showing the point clouds of the  
1003 observed data taken from the UAV photographs. The aerial images were taken from the authors.  
1004  
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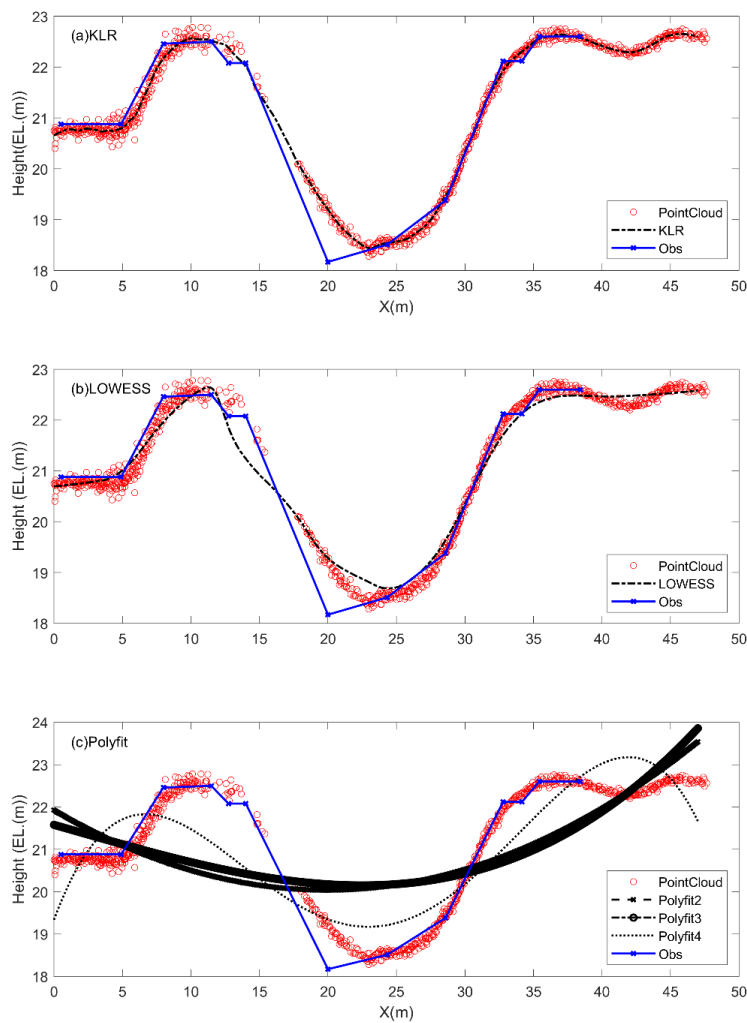


1007

1008 Figure 19. Point cloud data (red circles) for Site-1 and model-fitted line (black dashed line) with  
1009 KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the observed surveying.  
1010 Note that (1) the observed line was drawn from the previous surveying in BRTMA (2019); and  
1011 (2) the detailed information including the map is attached in Supplementary Material (Figures S1  
1012 and S2 as well as Table 1).

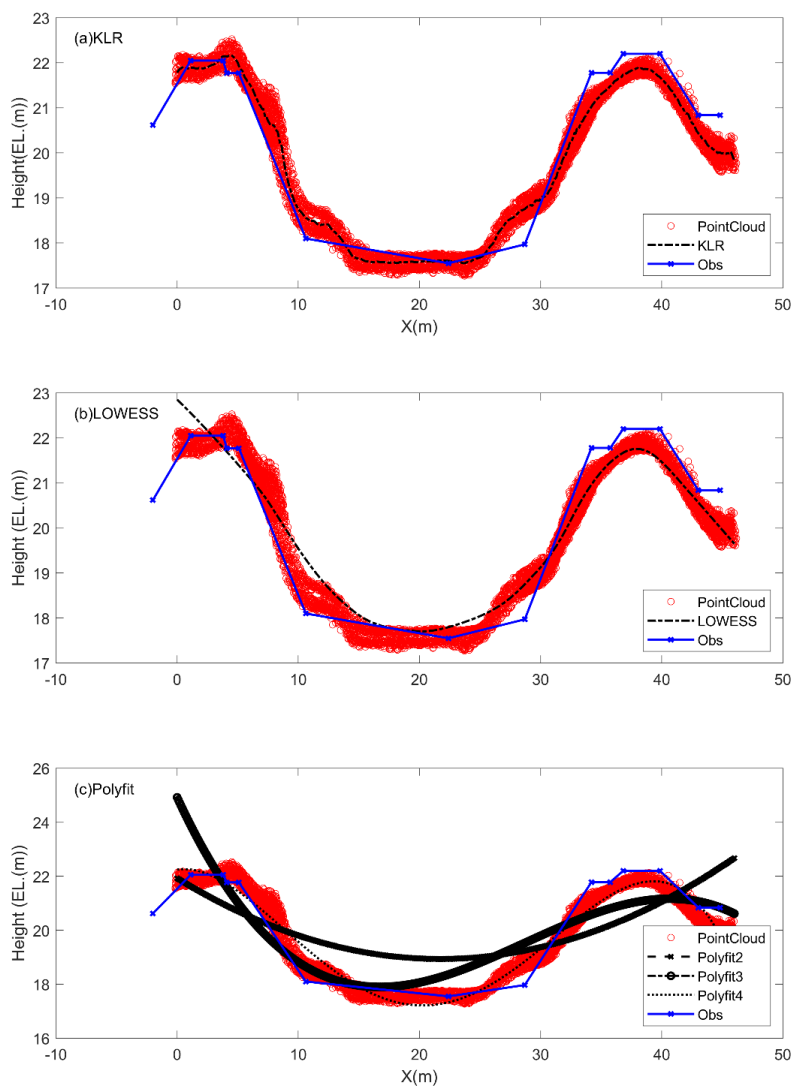


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1016  
1017 Figure 20. Point cloud data (red circles) for Site-2 and model-fitted line (black dashed line) with  
1018 KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the observed surveying.  
1019 Note that (1) the observed line was drawn from the previous surveying in BRTMA (2019); and  
1020 (2) the detailed information including the map is attached in Supplementary Material (Figures S1  
1021 and S2 as well as Table 1).

1022



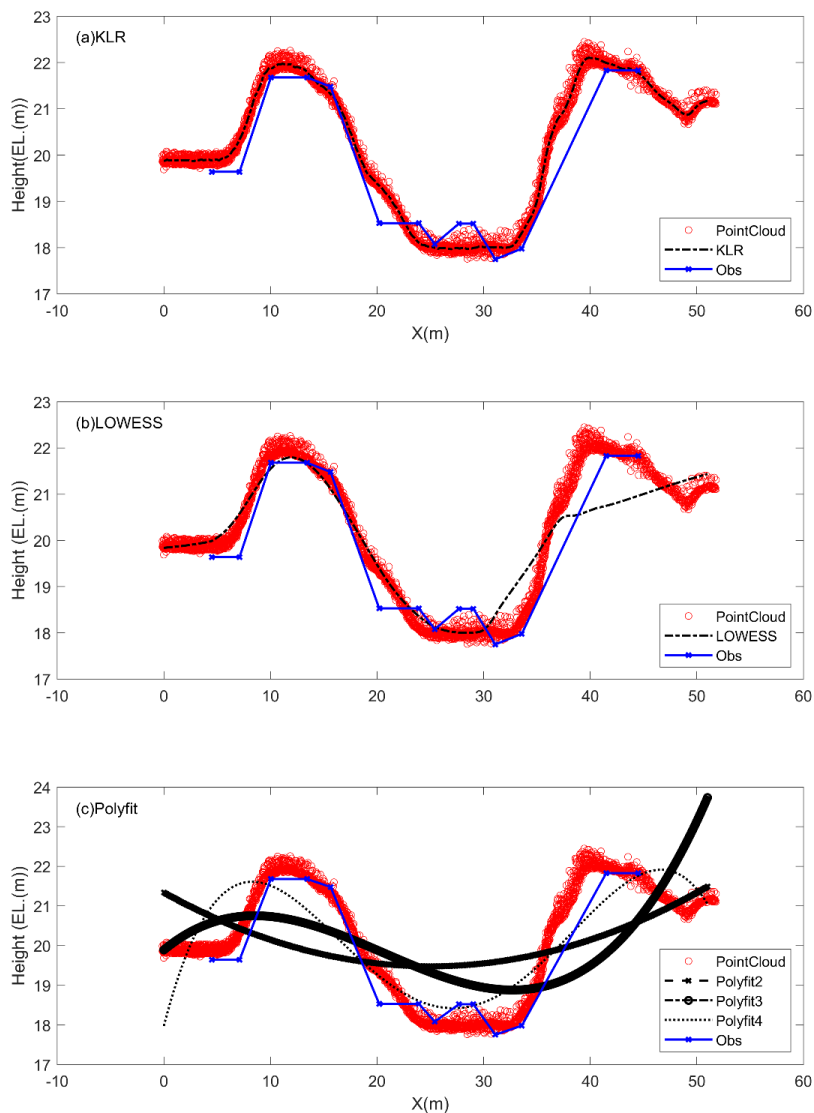
1023  
1024 Figure 21. Point cloud data (red circles) for Site-3 and model-fitted line (black dashed line) with  
1025 KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the observed surveying.  
1026 Note that (1) the observed line was drawn from the previous surveying in BRTMA (2019); and  
1027 (2) the detailed information including the map is attached in Supplementary Material (Figures S1  
1028 and S2 as well as Table 1).

1029

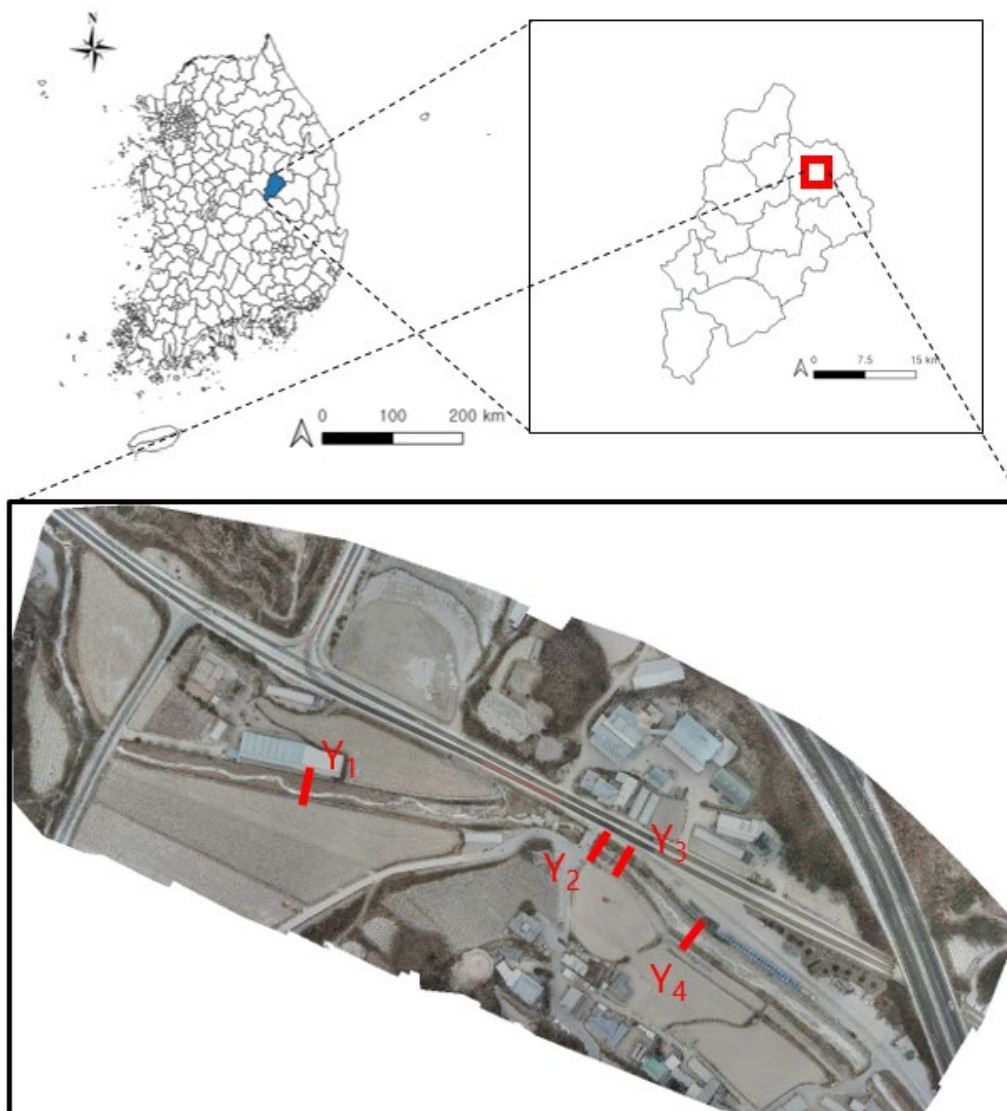




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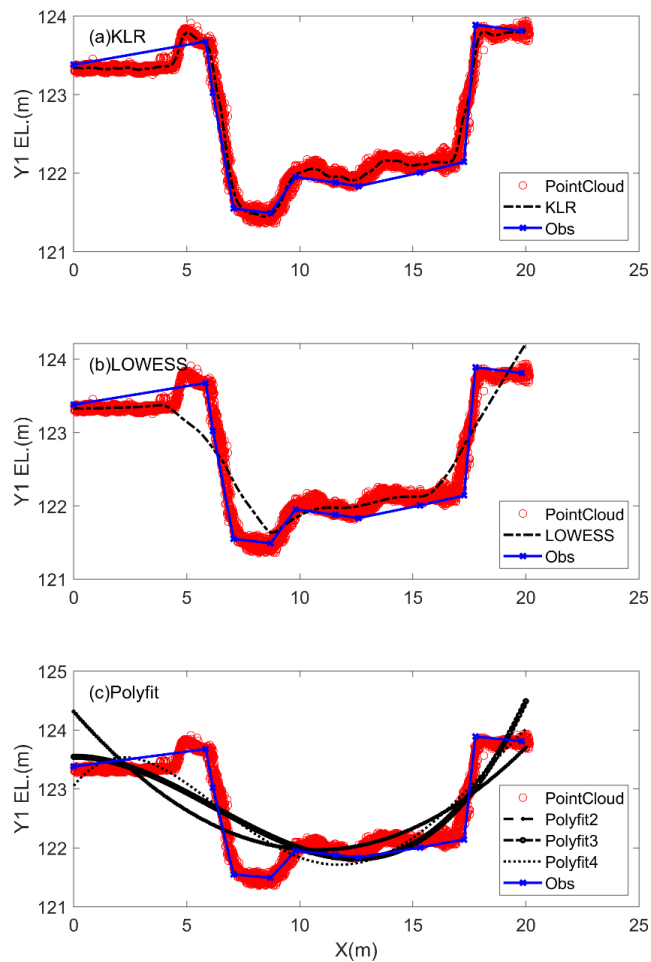


1031  
1032 Figure 22. Point cloud data (red circles) for Site-4 and model-fitted line (black dashed line) with  
1033 KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the observed surveying.  
1034 Note that (1) the observed line was drawn from the previous surveying in BRTMA (2019); and  
1035 (2) the detailed information including the map is attached in Supplementary Material (Figures S1  
1036 and S2 as well as Table 1).  
1037



1038  
1039 Figure 23. Study area of the applied stream, Pori-cheon stream in Yecheon-gun (Blue area in the  
1040 top left panel) South Korea. The aerial image is taken and produced by the authors and no  
1041 copyright is required.

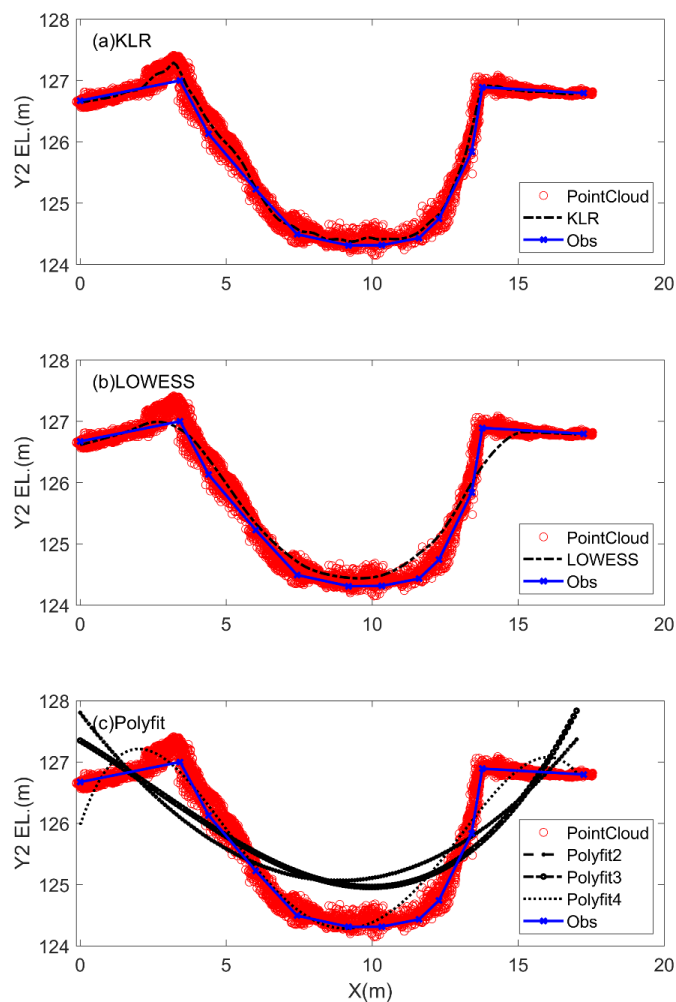
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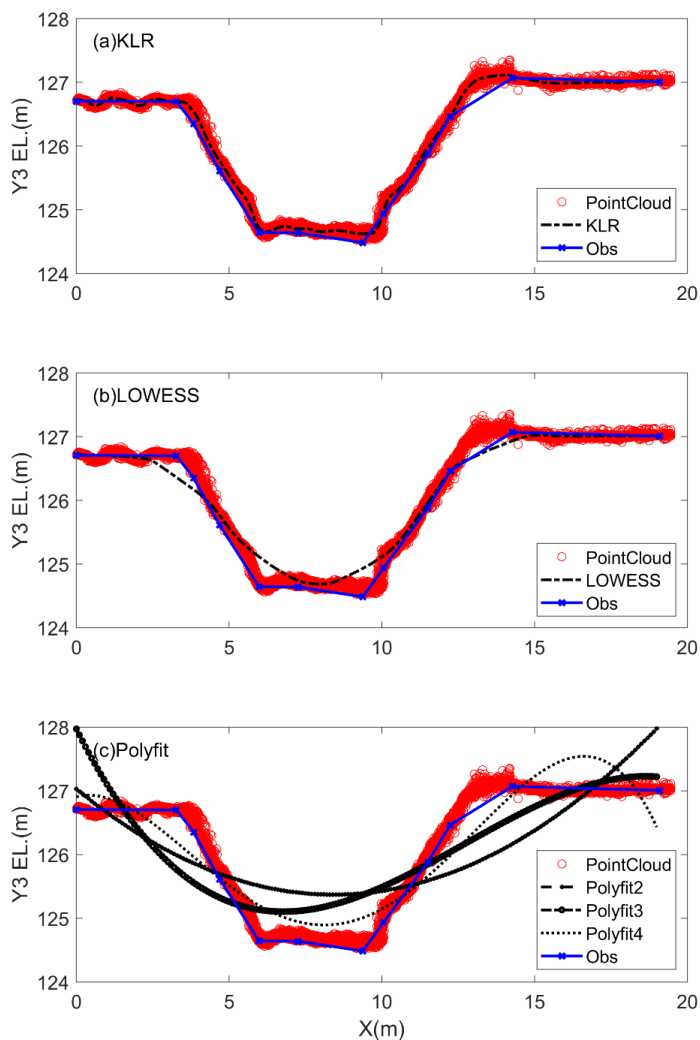
1046 Figure 24. Point cloud data (red circles) for the  $Y_1$  of Yecheon site and model-fitted line (black  
1047 dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the  
1048 ground surveying (blue solid line with x marker).

1049



1050

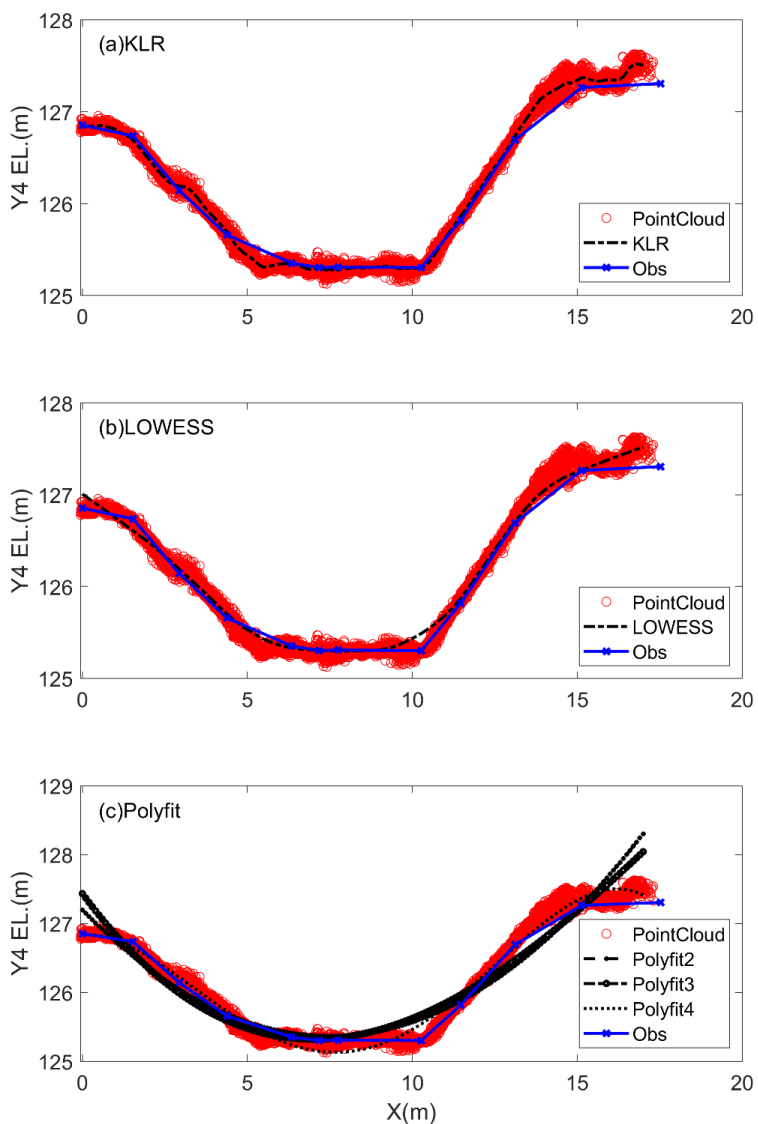
1051 Figure 25. Point cloud data (red circles) for the  $Y_2$  of Yecheon site and model-fitted line (black  
1052 dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the  
1053 ground surveying (blue solid line with x marker).



1054

1055 Figure 26. Point cloud data (red circles) for the Y<sub>3</sub> of Yecheon site and model-fitted line (black  
1056 dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the  
1057 ground surveying (blue solid line with x marker).

1058



1059

1060 Figure 27. Point cloud data (red circles) for the Y<sub>4</sub> of Yecheon site and model-fitted line (black  
1061 dashed line) with KLR (panel(a)), LOWESS (panel(b)), and PolyFit (panel(c)) as well as the  
1062 ground surveying (blue solid line with x marker).

1063

1064