

First, we would like to thank Julien Palmiéri for his careful evaluation of our manuscript and his interesting comments which we believe will help us to improve it. Please, find hereafter our response to these comments.

Major comments

1) First, the reason of the choice is not given. I understand it is greatly needed for developments like adding the mixotrophs in Eco3M. It's a huge task that require such lightweight configuration to test, verify that nothing is broken, and make sure the fluxes between each element of the model are reasonable. So, this choice is easily explained for the part 1, but less for this one.

We agree with this point. The use of a 0D configuration may seem more justified for the first part of our study as adding mixotrophs required many tests.

We chose to also use a dimensionless configuration for the part II as we wanted to provide a reliable representation of the carbonate system, which consider mixotrophs organisms, in the simplest way possible. In other words, we wanted to provide a tool which is easy to use, easy to adapt to other coastal area (by modifying the environmental forcings and the AT-S correlation) and give reliable results in a short amount of time.

Another reason to use a dimensionless configuration rather than a 3D configuration was the possibility to compare Eco3M_MIX-CarbOx to Eco3M-CarbOx in the same type of implementation. By comparing the models, we can answer several questions and especially: How mixotrophs affect carbonate variables ? Does adding them provide a more accurate representation of these variables ? and then build further relevant simulation strategies for 3D.

Considering these reasons, this dimensionless configuration can be seen as a laboratory to test and then build further relevant simulation strategies for 3D.

To justify the use of a 0D configuration, we first clarified the aim of the study at the end of the introduction (l.79):

[Here we try to provide a more realistic representation of carbonate system variables in the BoM. As a starting point, we used the concept of the dimensionless Eco3M-CarbOx model (Lajaunie-Salla et al., 2021), which aims to represent a small volume of surface water (i.e., 1 m^3) in the BoM. We developed a planktonic ecosystem model which contains, among others, mixotrophic organisms, modified the carbonate module described by Lajaunie-Salla et al. (2021) and added it to our newly developed planktonic ecosystem model to obtain the Eco3M_MIX-CarbOx model (v1.0). We implemented two types of TA formulation and compared the simulation results to in situ observations to identify which formulation was capable to deliver the more realistic results: (i) a formulation that only considers biological processes (referred to as autochthonous formulation) and (ii) a new TA formulation that depends only on salinity (referred to as allochthonous formulation). Furthermore, we simulate air-sea CO_2 fluxes to determine whether the BoM act as a sink or a source of CO_2 and provide a detailed analysis of drivers of seawater $p\text{CO}_2$ variations for two specific hydrodynamic processes typical for the BoM: (i) Rhône River intrusion and (ii) summer upwelling events. **With this study, we aim to provide a new tool which allow to obtain a reliable representation of the carbonate system in the simplest way as possible: by using a dimensionless configuration which is easy to use, adapt and give results in a short amount of time.]**

And we gave a justification of this choice in the Section 2.2 (l.111):

[In this study, we used the Eco3M_MIX-CarbOx model (v1.0) which was developed to represent the dynamics of the seawater carbonate system and mixotrophs in the BoM and was implemented using the Eco3M (Ecological Mechanistic and Molecular Modelling) platform (Baklouti et al., 2006a, b). **Eco3M_MIX-CarbOx is a dimensionless model (0D): we consider a volume of 1 m³ of surface water at SOLEMIO station, in this volume the state variables only vary over time as the model is not coupled with a hydrodynamic model. We chose to use a 0D configuration as this configuration has several advantages, especially, calculation times are low (around 45 minutes in our case). It allows us to make several test simulations to better understand the biogeochemical functioning of the BoM and its possible reactions to environmental forcings.]**

In the introduction, it's made mention of the need for high resolution model for coastal regional study, and the next sentence announce the use of a dimensionless (0D hereafter) configuration.

We understand that these sentences can be confusing. We add a sentence to make a better link between 3D introduction and use of 0D (l.65).

[Most modelling approaches to investigate carbonate system variables typically employ 3D coupled physical-biogeochemical models and focus on larger coastal areas (e.g., Artioli et al., 2014; Bourgeois et al., 2016). If the focus is on smaller areas this requires higher spatial and temporal resolution to correctly represent the relevant processes (Bourgeois et al., 2016). **However, higher spatial and temporal resolution often result in a significant increase of the calculation time which make more difficult the repetition of numerical experiments, an important step to better understanding the global functioning of the area and its reaction to environmental forcings. A solution to avoid important calculation times is to use a dimensionless model. This type of model allows to conduct large amount of test in short amount of time. For instance,** Lajaunie-Salla et al. (2021) used the dimensionless Eco3M-CarbOx model, which contains a carbonate module performing the resolution of the carbonate system based on total alkalinity (TA) and dissolved inorganic carbon (DIC). Even if the DIC, oceanic partial pressure of CO₂ (pCO₂) and total pH (pH_T) representations look reliable, Eco3m-CarbOx tends to minimize the range of TA variations during the year, resulting in a near constant TA (Lajaunie-Salla et al., 2021).]

2) A second point is that this 0D brings more questions than answers. Because it is a surface box, the model does not represent advection and mixing. The physics variable/forcing come from observations and hence include annual cycle and external forcing, including specific phenomena like summer upwellings or the Rhône waters passing by. But what about the nutrients ?

We agree that hydrodynamic processes, especially upwelling and Rhône River intrusions in the BoM are associated with nutrients inputs. In Eco3M_MIX-CarbOx, upwellings are only represented by strong variations of temperature and Rhône River intrusions are only represented by strong variations of salinity and TA inputs when allochthonous TA formulation is used. In other words, we do not consider the possible inputs of nutrients associated with these events and assumed that nutrients are fully the result of autochthonous biological processes (due to 0D configuration) which means that they are modelled based on the following state equations :

$$\frac{\partial \text{NO}_3}{\partial t} = \text{Nitrif}_{\text{NO}_3}^{\text{NH}_4} - \sum_{i=1}^2 \text{Upt}_{\text{NO}_3}^{\text{PhyN}_i} - \text{Upt}_{\text{NO}_3}^{\text{CMN}_i}$$

$$\frac{\partial \text{NH}_4}{\partial t} = \text{Excr}_{\text{NH}_4}^{\text{COPN}} + \text{Excr}_{\text{NH}_4}^{\text{NCMN}} + \text{Remin}_{\text{NH}_4}^{\text{BACN}} - \sum_{i=1}^2 \left(\text{Upt}_{\text{NH}_4}^{\text{PhyN}_i} \right) - \text{Upt}_{\text{NH}_4}^{\text{CMN}} - \text{Upt}_{\text{NH}_4}^{\text{BACN}} - \text{Nitrif}_{\text{NH}_4}^{\text{NO}_3}$$

$$\frac{\partial \text{PO}_4}{\partial t} = \text{Excr}_{\text{PO}_4}^{\text{COPP}} + \text{Excr}_{\text{PO}_4}^{\text{NCMP}} + \text{Remin}_{\text{PO}_4}^{\text{BACP}} - \sum_{i=1}^2 \left(\text{Upt}_{\text{PO}_4}^{\text{PHY}_i} \right) - \text{Upt}_{\text{PO}_4}^{\text{CMP}} - \text{Upt}_{\text{PO}_4}^{\text{BACP}} \quad (\text{Eq. S1})$$

Nitrate concentration results from nitrification and phytoplankton and CM uptakes. Ammonium concentration results from copepods and NCM excretion, bacterial remineralisation, heterotrophic bacteria, phytoplankton, and CM uptakes and losses from nitrification. Finally, phosphate concentration results from copepods and NCM excretion, bacterial remineralisation and heterotrophic bacteria, phytoplankton, and CM uptakes.

What are the external forces driving the biology of the model ?

Biology is impacted by temperature and/or irradiance. Depending on the biogeochemical process considered, both or only one of them can have an impact and this impact could be direct or indirect. Nitrification which is performed by nitrifying bacteria (organisms not considered explicitly in the model) depends on temperature and modelled dissolved oxygen concentration:

$$\text{Nitrif}_{\text{NH}_4}^{\text{NO}_3} = \text{tx}_{\text{NITRIF}} * \text{NH}_4 * f_{Q_{10}, \text{nitrif}}^T * \frac{\text{O}_2}{\text{O}_2 + K_{\text{O}_2}}$$

$$f_{Q_{10}, \text{nitrif}}^T = Q_{10, \text{nitrif}}^{\frac{T-10}{10}} \quad (\text{Eq. S2})$$

where $\text{tx}_{\text{NITRIF}}$ represents the fraction of NH_4^+ used for nitrification, K_{O_2} is the dissolved oxygen half saturation constant and $Q_{10, \text{nitrif}}$ is the temperature coefficient for nitrification.

We detailed the modelling of planktonic organisms in the companion paper (Barré et al., 2023a). To sum up, heterotrophic bacteria processes are directly impacted by temperature. Phytoplankton and CM processes are directly impacted by temperature (all processes) and irradiance (photosynthesis and grazing). Copepods and NCM processes are indirectly impacted by temperature and irradiance through the consumed preys.

This is not explained until the discussion, what is extremely frustrating, as we don't really understand what the model sees and feels or not, until the very end, when the author reveals some of the experiment limitations.

We provided all the balance equations, detailed formulations of biogeochemical processes and parameters values in the companion paper (Barré et al., 2023a). For organisms, we did not find relevant to provide them again. However, we understand the necessity of adding explanations about the nutrients in the manuscript. We decided to add a subsection in Section 2.2.1, in which we detail the modelling of nutrients and organic matter.

[2.2.1 Nutrients and organic matter representation in the model

As we use a dimensionless configuration, we assume that nutrients are fully the result of autochthonous biological processes. In other terms, we do not consider allochthonous inputs of nutrients (i.e., from rivers or atmosphere as instance). For all the simulations, nutrients dynamics are represented by the following state equations:

$$\frac{\partial \text{NO}_3}{\partial t} = \text{Nitrif}_{\text{NO}_3}^{\text{NH}_4} - \sum_{i=1}^2 \text{Upt}_{\text{NO}_3}^{\text{Phy}_i} - \text{Upt}_{\text{NO}_3}^{\text{CM}_i}$$

$$\begin{aligned}\frac{\partial \text{NH}_4}{\partial t} &= \text{Excr}_{\text{NH}_4}^{\text{COP}_N} + \text{Excr}_{\text{NH}_4}^{\text{NCM}_N} + \text{Remin}_{\text{NH}_4}^{\text{BAC}_N} - \sum_{i=1}^2 \left(\text{Upt}_{\text{NH}_4}^{\text{PHY}_{N_i}} \right) - \text{Upt}_{\text{NH}_4}^{\text{CM}_N} - \text{Upt}_{\text{NH}_4}^{\text{BAC}_N} - \text{Nitrif}_{\text{NH}_4}^{\text{NO}_3} \\ \frac{\partial \text{PO}_4}{\partial t} &= \text{Excr}_{\text{PO}_4}^{\text{COP}_P} + \text{Excr}_{\text{PO}_4}^{\text{NCM}_P} + \text{Remin}_{\text{PO}_4}^{\text{BAC}_P} - \sum_{i=1}^2 \left(\text{Upt}_{\text{PO}_4}^{\text{PHY}_{P_i}} \right) - \text{Upt}_{\text{PO}_4}^{\text{CM}_P} - \text{Upt}_{\text{PO}_4}^{\text{BAC}_P}\end{aligned}\quad (1)$$

The concentration of NO_3^- results from nitrification and phytoplankton and CM uptakes. Ammonium concentration results from copepods and NCM excretion, bacterial remineralisation, heterotrophic bacteria, phytoplankton, and CM uptakes and losses from nitrification. Phosphate concentration results from copepods and NCM excretion, bacterial remineralisation and heterotrophic bacteria, phytoplankton, and CM uptakes.

Such as nutrients dynamics, organic matter (dissolved and particulate) dynamic is only the result of autochthonous biological processes (Eq. 2 and 3).

$$\begin{aligned}\frac{\partial \text{DOC}}{\partial t} &= \sum_{i=1}^2 \left(\text{Exu}_{\text{DOC}}^{\text{PHY}_{C_i}} \right) + \sum_{i=1}^2 \left(\text{Exu}_{\text{DOC}}^{\text{MIX}_{C_i}} \right) + \text{Excr}_{\text{DOC}}^{\text{COP}_C} + \text{Mort}_{\text{DOC}}^{\text{BAC}_C} - \text{BP}_{\text{DOC}}^{\text{BAC}_C} \\ \frac{\partial \text{DON}}{\partial t} &= \sum_{i=1}^2 \left(\text{Exu}_{\text{DON}}^{\text{PHY}_{N_i}} \right) + \sum_{i=1}^2 \left(\text{Exu}_{\text{DON}}^{\text{MIX}_{N_i}} \right) + \text{Mort}_{\text{DON}}^{\text{BAC}_N} - \text{Upt}_{\text{DON}}^{\text{CM}_N} - \text{Upt}_{\text{DON}}^{\text{PICO}_N} - \text{Upt}_{\text{DON}}^{\text{BAC}_N} \\ \frac{\partial \text{DOP}}{\partial t} &= \sum_{i=1}^2 \left(\text{Exu}_{\text{DOP}}^{\text{PHY}_{P_i}} \right) + \sum_{i=1}^2 \left(\text{Exu}_{\text{DOP}}^{\text{MIX}_{P_i}} \right) + \text{Mort}_{\text{DOP}}^{\text{BAC}_P} - \text{Upt}_{\text{DOP}}^{\text{CM}_P} - \text{Upt}_{\text{DOP}}^{\text{PICO}_P} - \text{Upt}_{\text{DOP}}^{\text{BAC}_P}\end{aligned}\quad (2)$$

The concentration of dissolved organic carbon (DOC), nitrogen (DON) and phosphorus (DOP) depends on phytoplankton and mixotrophs exudation, copepods excretion, heterotrophic bacteria mortality (natural mortality) and CM, PICO and heterotrophic bacteria uptake.

$$\begin{aligned}\frac{\partial \text{POC}}{\partial t} &= \text{E}_{\text{POC}}^{\text{COP}_C} + \text{Predation}_{\text{POC}}^{\text{COP}_C} - \text{BP}_{\text{POC}}^{\text{BAC}_C} \\ \frac{\partial \text{PON}}{\partial t} &= \text{E}_{\text{PON}}^{\text{COP}_N} + \text{Predation}_{\text{PON}}^{\text{COP}_N} - \text{Upt}_{\text{PON}}^{\text{BAC}_N} \\ \frac{\partial \text{POP}}{\partial t} &= \text{E}_{\text{POP}}^{\text{COP}_P} + \text{Predation}_{\text{POP}}^{\text{COP}_P} - \text{Upt}_{\text{POP}}^{\text{BAC}_P}\end{aligned}\quad (3)$$

The concentration of particulate organic carbon (POC), nitrogen (PON) and phosphorus (POP) depends on copepods egestion, predation by higher trophic levels on copepods (closure term of the model) and heterotrophic bacteria production and uptake. POM particles are large enough to sink, however, we do not consider a term to represent their removal from the surface box by sinking. In our case, the POM, such as the DOM, stay in the box and is constantly recycling.

A detailed description and formulations of processes can be found in Barré et al. (2023a). Processes notation description can be found in Table A1 (Appendix A).]

We modified the manuscript consequently (l.111):

[In the following, we provide a detailed description of the carbonate module. **We also give a brief description of nutrients and organic matter representation.** A detailed description of other compartments, especially of mixotrophs compartment can be found in Barré et al. (2023a).]

Appendix A:

[Table A1: Description of state equation processes.

Notation	Process
Copepods	
$\text{Excr}_{\text{NutX}}^{\text{COPX}}$ $\text{NutX} \in [\text{NH}_4^+, \text{PO}_4^{3-}]$ $X \in [\text{N}, \text{P}]$	Excretion of nutrient X by copepods
$\text{Excr}_{\text{DOC}}^{\text{COPC}}$	DOC excretion by copepods
$\text{Resp}_{\text{DIC}}^{\text{COPC}}$	Copepods respiration
$\text{E}_{\text{POX}}^{\text{COPX}}$ $X \in [\text{C}, \text{N}, \text{P}]$	Copepods egestion
$\text{Predation}_{\text{POX}}^{\text{COPX}}$ $X \in [\text{C}, \text{N}, \text{P}]$	Predation by higher trophic levels on copepods
Mixotrophs (Mix \in [NCM, CM])	
$\text{Exu}_{\text{DOX}}^{\text{MixX}_i}$ $X \in [\text{C}, \text{N}, \text{P}]$	DOX exudation by mixotrophs
$\text{Resp}_{\text{DIC}}^{\text{MixC}}$	Mixotrophs respiration
$\text{Photo}_{\text{DIC}}^{\text{MixC}}$	Mixotrophs photosynthesis
$\text{Excr}_{\text{NutX}}^{\text{NCMX}}$ $\text{NutX} \in [\text{NH}_4^+, \text{PO}_4^{3-}]$ $X \in [\text{N}, \text{P}]$	Excretion of nutrient X by NCM
$\text{Upt}_{\text{NutX}}^{\text{CMX}}$ $X \in [\text{N}, \text{P}]$ $\text{NutX} \in [\text{NO}_3^-, \text{NH}_4^+, \text{PO}_4^{3-}]$	Uptake of nutrient X by constitutive mixotrophs
$\text{Upt}_{\text{DOX}}^{\text{CMX}}$ $X \in [\text{N}, \text{P}]$	Uptake of DOX by constitutive mixotrophs
Phytoplankton (Phy \in [NMPHYTO, PICO])	
$\text{Resp}_{\text{DIC}}^{\text{PhyC}}$	Phytoplankton respiration
$\text{Photo}_{\text{DIC}}^{\text{PhyC}}$	Phytoplankton photosynthesis
$\text{Upt}_{\text{NutX}}^{\text{PhyX}}$ $\text{NutX} \in [\text{NO}_3^-, \text{NH}_4^+, \text{PO}_4^{3-}]$	Uptake of nutrient X by phytoplankton
$\text{Exu}_{\text{DOX}}^{\text{PhyX}}$ $X \in [\text{C}, \text{N}, \text{P}]$	DOX exudation by phytoplankton
$\text{Upt}_{\text{DOX}}^{\text{PICOX}}$ $X \in [\text{N}, \text{P}]$	Uptake of DOX by picophytoplankton
Heterotrophic bacteria	
$\text{BP}_X^{\text{BACc}}$ $X \in [\text{DOC}, \text{POC}]$	Bacterial production
$\text{BR}_{\text{DIC}}^{\text{BACc}}$	Bacterial respiration
$\text{Upt}_{\text{POX}}^{\text{BACX}}$ $X \in [\text{N}, \text{P}]$	POX uptake by heterotrophic bacteria

$Exu_{DOX}^{PhyX_i}$
 $X \in [C, N, P]$

DOX exudation by phytoplankton

$Remin_{BACX}^{NutX}$
 $NutX \in [NH_4^+, PO_4^{3-}]$
 $X \in [N, P]$

Remineralisation of nutrient X by heterotrophic bacteria

$Mort_{DOX}^{BACX}$

Heterotrophic bacteria natural mortality

Dissolved inorganic matter (DIM)

$Diss_{DIC}^{CaCO_3}$

CaCO₃ dissolution

$Prec_{DIC}^{CaCO_3}$

CaCO₃ precipitation

Nitrif

Nitrification

$Aera_{DIC}$

Air-sea CO₂ gas exchanges (aeration)

]

Also, we propose to add the figure 2, which resumes the hypothesis used in this study and allows to visualize the OD concept, at the end of part 2.2.2 (2.2.3 in the revised manuscript).

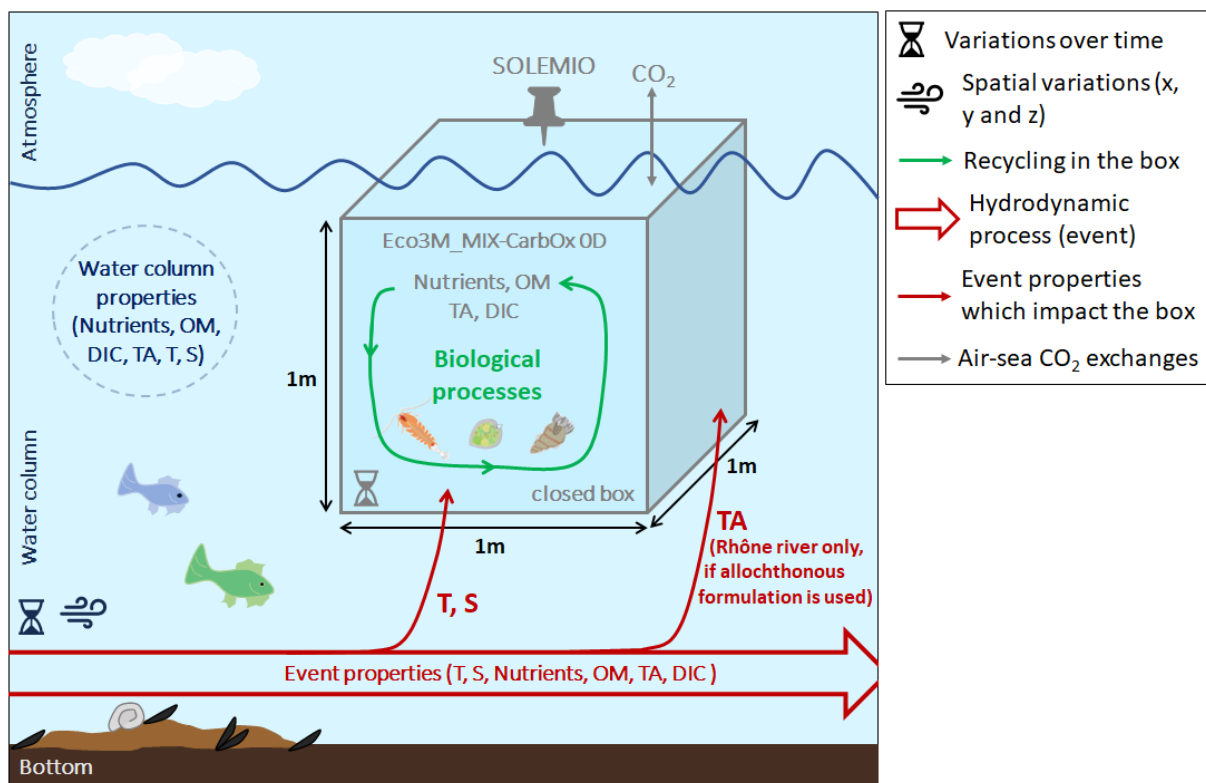


Figure 2: Schematic representation of OD concept and summary of the hypotheses used in this study with Eco3M_MIX-CarbOx. T: temperature, S: Salinity and OM: Organic matter.

We modify the manuscript consequently:

(l.181): Figure X illustrates the concept of OD and summarize the hypothesis used in this study with Eco3M_MIX-CarbOx.

3) Still about the OD, what happens to the POM ? Do they sink ? Are they removed from the surface box ? Or do they float there and are slowly remineralized (as if the bay is mixed enough to keep the particles around) ? This is important as it has an impact on TA and DIC and all other nutrients concentration.

In the model, the POC, PON and POP dynamics result from copepods egestion, higher trophic level predation on copepods (closure terms of the model) and heterotrophic bacteria uptake (Eq. S3). They do not sink and are constantly recycling in the surface box using the processes indicated above.

$$\frac{\partial \text{POC}}{\partial t} = E_{\text{POC}}^{\text{COPC}} + \text{Predation}_{\text{POX}}^{\text{COPX}} - \text{BP}_{\text{POC}}^{\text{BACC}}$$

$$\frac{\partial \text{PON}}{\partial t} = E_{\text{PON}}^{\text{COPN}} + \text{Predation}_{\text{PON}}^{\text{COPN}} - \text{Upt}_{\text{PON}}^{\text{BACN}}$$

$$\frac{\partial \text{POP}}{\partial t} = E_{\text{POP}}^{\text{COPP}} + \text{Predation}_{\text{POP}}^{\text{COPP}} - \text{Upt}_{\text{POP}}^{\text{BACP}}$$

(Eq. S3)

Using these state equations, the POM compartment is balanced (Fig. S1) which is why we do not consider a term to represent their removal from the surface box by sinking.

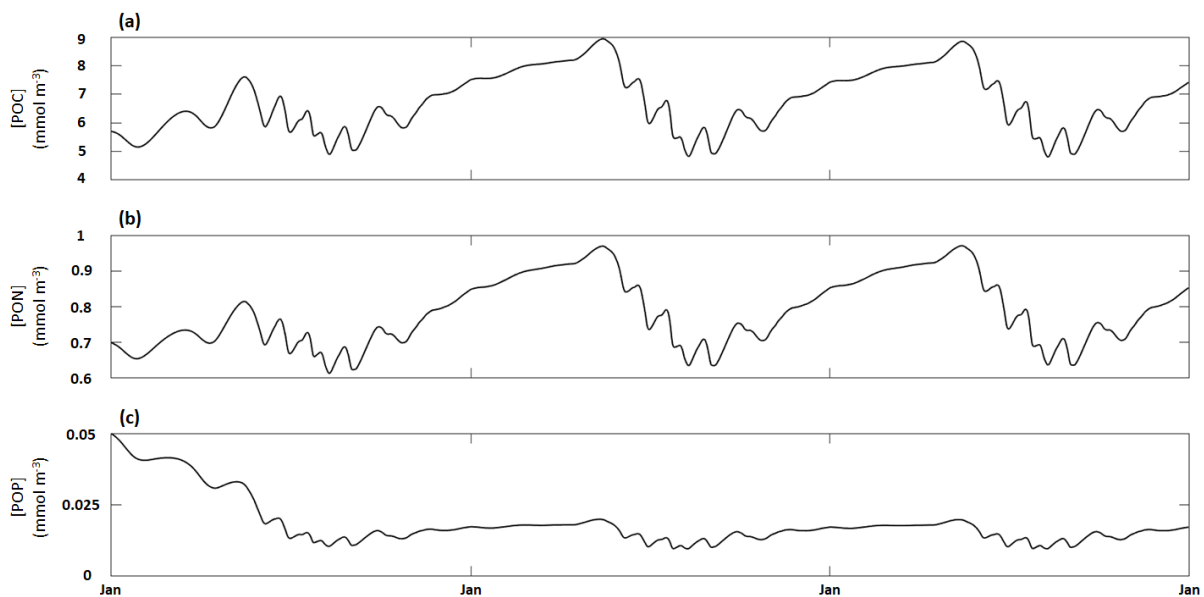


Figure S1: Time-series of daily averaged (a) POC, (b) PON and (c) POP for the three years of simulation (repetition of 2017 three times) for the reference simulation (SIMCO, Table 2 of the manuscript).

We hope that adding the part 2.2.1 (see point 2) which contains a description of dissolved and particulate organic matter representation in the model will clarify this point.

4) Somehow it looks like (and I am sorry to say that, but I am sure you agree with me) the work you've done here (changing from autochthonous TA formulation – what is what you ideally want to use – to the abiotic, allochthonous formulation) is a way to fix a problem due to the configuration choice, that is not done for this kind of study. Your conclusion (you need to switch from 0D to 3 or at least 1D) should have been one of Lajaunie-Salla et al. 2021's study.

We agree, by changing the formulation of TA from autochthonous to allochthonous, our aim was to correct a bias due to the configuration choice.

By implementing an allochthonous formulation of TA in Eco3M_MIX-CarbOx, we first wanted to explain the result obtained by Lajaunie-Salla et al. (2021) and make sure that this result was not due to a poor representation of a biological process that could affect TA dynamics. Then, with the results obtained in our study, we could confirm that the lack of variation in the AT representation of Lajaunie-Salla et al.

(2021) is explained by the fact that the 0D configuration does not allow (at first sight) the consideration of allochthonous contributions and especially of the Rhône River which is the main source of TA variations in the area.

Nevertheless, the 0D configuration has several advantages, including its short calculation time which allowed us to provide a detailed analysis of drivers of seawater $p\text{CO}_2$ variations, particularly during specific hydrodynamic processes typical for the BoM. This type of study is still uncommon in the area, as few of them investigated the carbonate system dynamics, especially the $p\text{CO}_2$ variations drivers (reference study: Wimart-Rousseau et al., 2020) and would have been more difficult to conduct in 3D. That is why we chose to keep working on the 0D configuration (therefore, looking for a way to better represent the TA on which $p\text{CO}_2$ calculation depends) and present the results obtained with this configuration as we think that, even if some points deserve to be reworked in 3D, the 0D already allows to obtain interesting results.

5) Before publication I would require the author to better explain the choice and implications of the 0D in the method section, so that the reader can really understand the experiments and the results.

- How are the nutrients managed (initialized with annual average value)?

Nutrients dynamics are the results of biological processes which take place in the box only, please see point 2 for details.

- Are total N, P, Si, Fe, Alk supposed to be conserved within the box ? Or are they allowed to fluctuate with some external sources and sinks from/to outside the box, apart from the air-sea CO_2 flux?

We do not consider Si and Fe in our model. Total N, and P are supposed to be conserved within the box as we do not consider any external source or sink from/to the water column (Fig. S2).

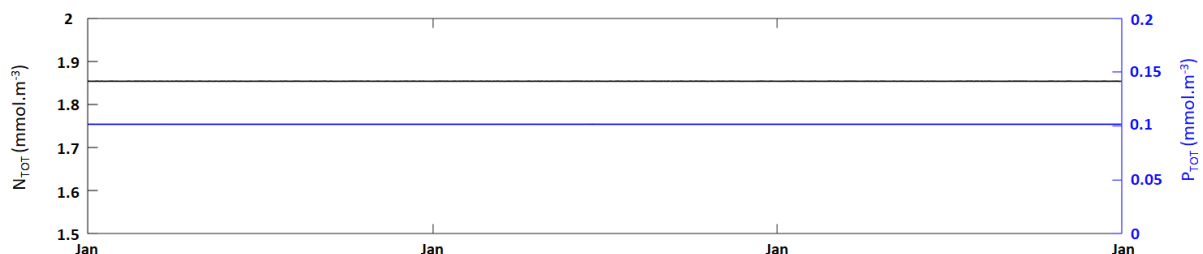


Figure S2: Time-series of daily averaged total nitrogen (N_{TOT}) and phosphorus (P_{TOT}) for the three years of simulation (repetition of 2017 three times) for the reference simulation (SIMCO, Table 2 of the manuscript).

When TA calculation is based on autochthonous formulation, TA is supposed to be conserved in the box. However, when we repeat the year 2017 three times, we observe a decreasing trend for TA ($-16\mu\text{mol kg}^{-1}$ in three years) (Fig. S3). This decrease is explained by the prevailing of precipitation compared to dissolution. For the bay of Marseille, this result seems consistent as other studies (Bensoussan & Gattuso, 2007 ; Wimart-Rousseau et al., 2020) suggest a net calcifying system, however, in our case, it means that TA is not conserved in the box.

When TA calculation is based on allochthonous formulation, the TA result is the balance between Rhône River TA sources and sinks due to the net calcifying system.

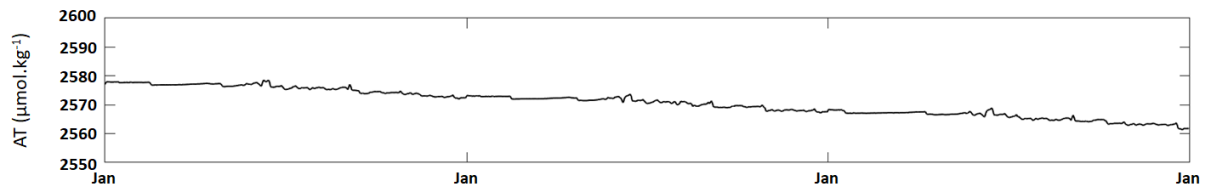


Figure S3: Time series of daily averaged TA for the three years of simulation (repetition of 2017 three times) for the reference simulation (SIMCO, Table 2 of the manuscript).

- What happens to all sinking materials ? Even if they stay in the box, we need to know.

Sinking materials (POM, organisms larger than CM and CaCO_3 in our case) stay in the box. They are constantly recycled by the biogeochemical processes which impact them (see point 3).

I ask for major revision, just to be sure this part is improved.

We hope that our responses, especially adding 2.2.1 and the figure 2 to the manuscript, clarify these points.

For the rest I cannot ask you to re-do everything in 1 or 3D, this will most probably be your next paper anyway.

Indeed, we plan to study carbonate system variables dynamics in the BoM using a 3D coupled model and to present the results of this study in another manuscript.

Modifications in the text:

The English might need some rewording. I am not an english native, so I cannot help much for that, but I would recommend a second read. For example, you make an extensive use of the word “yielding”. It is a nice word, but you should replace some of them with relevant synonyms.

As we are not native speakers, we have sent our manuscript to a native speaker before submission. So, the version provided to you was already corrected and rephrased by a native speaker, however, we took into account your suggestion and minimize the use of “yielding”.

I.140: We rephrased [As a last term we included the mixotrophic uptake of nutrients which yields the following state equation for TA] to [As a last term we included the mixotrophic uptake of nutrients. **TA is calculated as follows:**]

I.288: We modified [Both simulations yield a strong decrease of $p\text{CO}_2$ on March 15th , in response to a Rhône River intrusion in the BoM.] to [**For both simulations a strong decrease of $p\text{CO}_2$ is modelled on March 15th , in response to a Rhône River intrusion in the BoM.**]

I.301: We deleted [Regarding the coast function, simulations yielded $\text{CF} < 2$ for all variables which is considered very good ($\text{CF} < 1$) or good ($1 \leq \text{CF} < 2$) (Table 3).].

I.306: We modified [Furthermore, SIMC1 produced the best TA representation yielding the lowest values for CF, %BIAS and RMSD (Table 3).] to [Furthermore, SIMC1 produced the best TA representation **resulting in** the lowest values for CF, %BIAS and RMSD (Table 3).]

I.430: We changed [In contrast, the allochthonous formulation yielded a much high variability in TA that was close to in situ observations.] to [In contrast, the allochthonous formulation **produced** a much high variability in TA that was close to in situ observations.]

I.439: We modified [Having neglected other allochthonous drivers seems to be justified by the results which yielded a close match to observations and a generally better representation of the other carbonate system variables since DIC, $p\text{CO}_2$ and pH_T are all closely related to TA (Fig. 4 and Table 3).] by [Having neglected other allochthonous drivers seems to be justified by the results which **showed** a close match to observations and a generally better representation of the other carbonate system variables since DIC, $p\text{CO}_2$ and pH_T are all closely related to TA (Fig. 4 and Table 3).]

I.531: We changed [The reason for this discrepancy may be related to the fact that our model overestimates seawater $p\text{CO}_2$ during winter, yielding a sea-air difference close to zero (Fig. 5d). As a result, despite strong winds and low temperatures which would favour CO_2 absorption (Middelburg, 2019), the winter CO_2 sink is not well represented.] to [The reason for this discrepancy may be related to the fact that our model overestimates seawater $p\text{CO}_2$ during winter, **resulting in** a sea-air difference close to zero (Fig. 5d). As a result, despite strong winds and low temperatures which would favour CO_2 absorption (Middelburg, 2019), the winter CO_2 sink is not well represented.]

Page2 line 25 : add some “-” or () : “model – consistent with observations – predicted...”

Done.

P3-L65 : You need to add something here about the reason for 0D.

We added (I.65):

[Most modelling approaches to investigate carbonate system variables typically employ 3D coupled physical-biogeochemical models and focus on larger coastal areas (e.g., Artioli et al., 2014; Bourgeois et al., 2016). If the focus is on smaller areas this requires higher spatial and temporal resolution to correctly represent the relevant processes (Bourgeois et al., 2016). **However, higher spatial and temporal resolution often result in a significant increase of the calculation time which make more difficult the repetition of numerical experiments, an important step to better understanding the global functioning of the area and its reaction to environmental forcings. A solution to avoid important calculation times is to use a dimensionless model. This type of model allows to conduct large amount of test in short amount of time. As instance, Lajaunie-Salla et al. (2021) used the dimensionless Eco3M-CarbOx model, which contains a carbonate module performing the resolution of the carbonate system based on total alkalinity (TA) and dissolved inorganic carbon (DIC). Even if the DIC, oceanic partial pressure of CO_2 ($p\text{CO}_2$) and total pH (pH_T) representations look reliable, Eco3m-CarbOx tends to minimize the range of TA variations during the year, resulting in a near constant TA (Lajaunie-Salla et al., 2021).]**

P5-table1: You only fill the time resolution information for the wind. Does that mean they’re all the same ? It seems from the text that some data are daily. You should feel them all, or tell in the table description why the other data have no time resolution information.

All data cited in Table 1 are hourly measurements. To avoid confusion, we fill all the lines of the table.

[Table 1. Data types and their sources used to drive the environmental forcing during the 2017 model run (based on Barré et al., 2023a).

	Data type	Location	Time resolution
Sea surface temperature	Measurements	Planier station	Hourly
Salinity	Measurements	Carry buoy	Hourly
Wind	WRF model results	SOLEMIO station	Hourly
Irradiance	WRF model results	SOLEMIO station	Hourly

]

P6-L124 to 126. “ In addition to ...”. what you say there sounds obvious, but BGC-model not including mixotroph represent reasonable TA and DIC. Do you have a Reference paper for this statement ?

We added the reference Mitra et al., (2014): In this article, authors show why it is important to consider a mixotrophs compartment and how not consider it can lead to a failure to capture the true dynamics of the carbon fluxes. (Mitra, A., Flynn, K. J., Burkholder, J. M., Berge, T., Calbet, A., Raven, J. A., Granéli, E., Glibert, P. M., Hansen, P. J., Stoecker, D. K., Thingstad, F., Tillmann, U., Våge, S., Wilken, S., and Zúrov M. V.: The role of mixotrophic protists in the biological carbon pump, *Biogeosciences*, 11, 995-1005, <https://doi.org/10.5194/bg-11-995-2014>, 2014.

P7-equation1 : You should specify that all terms are define in the appendix A.

Thank you for pointing this out, we added it l.144: [where i represents the number of organisms. **Processes description can be found in Table A1 (Appendix A) and formulations are available in Barré et al. (2023a)**. In this formulation, TA only depends on biogeochemical processes (i.e., TA riverine inputs are excluded).] and l.170: [where i represents the number of organisms. **Processes description can be found in Table A1 (Appendix A) and formulations are available in Barré et al. (2023a)**. As an additional modification, we use a more recent version of the gas transfer velocity calculation introduced by Wanninkhof (2014).].

P7- equ2 and 3 : You can specify the unit at the end of the equation, and remove the following sentence.

Done.

I might be wrong but, shouldn't the “photo” terms be more like uptake terms ? Phyto absorbs more DIC than the only ones used for the photosynthesis. Isn't this equation missing the remineralization terms as a source of DIC ?

Thank you for this interesting comment. We are aware that phytoplankton can absorb more DIC than the one associated with photosynthesis process. However, in Eco3M_MIX-CarbOx, we made the choice to consider only the DIC uptake used through photosynthesis (photosynthetic organisms only use the DIC they need for photosynthesis, surplus is released through respiration process).

The term $Photo_{DIC}^{ORG_i}$ (with $ORG \in [PHYC, MIXC]$), when apply to the DIC, represents the DIC uptake linked to photosynthesis, by phytoplankton and mixotrophs. When The term $Photo_{DIC}^{ORG_i}$ is applied to phytoplankton or mixotrophs, it represents the biomass increase associated with photosynthesis. Both processes are identical, they have the same formulation (photosynthesis based on Geider et al. ,1998) except that when the process is applied to DIC, the biogeochemical flux applied is negative (positive when applied to phytoplankton and mixotrophs). We then used the same notation to be consistent.

In Eco3M_MIX-CarbOx, we consider DIC remineralization through respiration process. Especially, the DIC which comes from bacteria respiration is actually the result of POC and DOC remineralization.

P8-equ5 and L179-181 : I don't understand why you define Aera being negative when the CO₂ flux is toward the sea. In Equ 4, $\partial DIC/\partial T$ increases with Aera being positive, what means CO₂ flux toward the sea, and $pCO_{2,sw} > pCO_{2,atm}$. There's a discrepancy here you might want to correct.

Thank you for pointing this out. We corrected the balance equation for DIC (l.167, Eq.4):

$$\frac{\partial \text{DIC}}{\partial t} = \sum_{i=1}^2 \left(\text{Resp}_{\text{DIC}}^{\text{PhyC}_i} \right) + \sum_{i=1}^2 \left(\text{Resp}_{\text{DIC}}^{\text{MixC}_i} \right) + \text{Resp}_{\text{DIC}}^{\text{COPc}} + \text{BR}_{\text{DIC}}^{\text{BACc}} + \text{Diss}_{\text{DIC}}^{\text{CaCO}_3} - \sum_{i=1}^2 \left(\text{Photo}_{\text{DIC}}^{\text{PhyC}_i} \right) - \sum_{i=1}^2 \left(\text{Photo}_{\text{DIC}}^{\text{MixC}_i} \right) - \text{Prec}_{\text{DIC}}^{\text{CaCO}_3} - \text{Aera}_{\text{DIC}}$$

Equation 5 of the manuscript remains unchanged. We still consider that negative aeration values ($p\text{CO}_{2,\text{atm}} > p\text{CO}_{2,\text{sw}}$) are associated with CO_2 fluxes toward the sea and an increase of DIC, which is now consistent with the DIC balance equation.

P11-L237 : “the first three terms of Eq.(10)”, I think you refer to Eq.11, not 10.

Thank you for pointing this out, we modified: [The first three terms of the Eq. (10) can be calculated as follow:] by [**The three terms of Eq. (11) can be calculated as follow:**].

P14-Table3 : just to mention, comparing pH is tricky. Comparing pH change or bias in pH unit can be misleading. Best practice is to compare H^+ concentration. See Kwiatkowski and Orr, 2018 (<https://www.nature.com/articles/s41558-017-0054-0>).

Thank you for pointing this out. We take into account your suggestion and propose to add in Appendix the statistical indicators calculation for H^+ concentration:

[Appendix C: Statistic indicators calculation for H^+ concentration

Table C1: Comparing the different model results to surface observations at SOLEMIO station for H^+ concentration. N represents the number of observations. Mean, SD, AE, AAE and RMSD are in the same unit than the considered variable, i.e.: mmol m^{-3} for H^+ concentrations. % BIAS is without unit.

		[H^+]
N	Observations	20
Mean \pm SD	Observations	$8.08 \times 10^{-9} \pm 5.52 \times 10^{-10}$
Mean \pm SD	SIMCO	$8.89 \times 10^{-9} \pm 2.91 \times 10^{-10}$
	SIMC1	$8.39 \times 10^{-9} \pm 4.06 \times 10^{-10}$
	CarbOx	$8.52 \times 10^{-9} \pm 2.80 \times 10^{-10}$
%BIAS	SIMCO	-5.33
	SIMC1	-3.91
	CarbOx	-5.47
AE	SIMCO	-4.30×10^{-10}
	SIMC1	-3.15×10^{-10}
	CarbOx	-4.42×10^{-10}
AAE	SIMCO	6.45×10^{-10}
	SIMC1	6.05×10^{-10}
	CarbOx	6.36×10^{-10}
RMSD	SIMCO	6.98×10^{-10}
	SIMC1	7.14×10^{-10}
	CarbOx	6.93×10^{-10}

]

Please, note that based on Referee 2 suggestions we modified the statistical indicators calculated. We replaced CF which was not sensitive enough by average error (AE) and average absolute error (AAE):

$$\text{AE} = \frac{\sum_{i=1}^N (\text{O}_i - \text{M}_i)}{n}$$

(Eq. S4)

$$AAE = \frac{\sum_{i=1}^N (|O_i - M_i|)}{n}$$

(Eq. S5)

Where O represents the observations and M the model results, calculations are based on Stow et al. (2009).

And we modified the text accordingly (l.301):

[For statistical indicators, %BIAS values are systematically lower than 10 %, with the highest values obtained for pCO_2 with ~6 % while the remaining variables had values < 1 %. Similarly, pCO_2 had the highest RMSD, AAE and AE which suggests that this parameter is not as well represented in the model as the other variables. Furthermore, SIMC1 produced the best TA representation resulting in the lowest values for %BIAS, AE, AAE and RMSD (Table 3). Moreover, SIMC1 produced an annual mean-TA that was closest to the observations. While the SIMC0 and Eco3m-CarbOx results are fairly similar. SIMC0 produced a slightly better representation of TA compared to Eco3m-CarbOx (%BIAS, AE, AAE and RMSD slightly lower). For pH_T , SIMC1 outperformed SIMC0 based on %BIAS (Table 3), however, AE, AAE and RMSD values are similar for the three simulations. We then performed the calculation of statistical indicators on H^+ concentration as, according to some authors (Kwiatkowski & Orr, 2018), comparing H^+ concentrations is a better practice than comparing pH. Results are available in Appendix C. Based on Table C1, SIMC1 also outperformed SIMC0 based on AE and AAE. For studying DIC and pCO_2 , the situation is less clear as the simulations performed differently for different indicators, making it difficult to pick a clear winner. Still SIMC1 shows the best AAE and RMSD values for DIC, and the best %BIAS, AE, and AAE for pCO_2 . In conclusion, SIMC1 shows the best overall indicator values for the examined variables (more specifically, it outperformed the other simulations in 13 of 20 indicator comparisons when including H^+ concentrations comparison).]

P15 -Fig 5 : the e,f,g and h panels are not useful. There is no additional information, and it's not even zoomed-in. Instead, I would remove them, make the picture slightly bigger, and highlight the SUP like you do in Fig. 6 with a shading or something similar.

Done. We modified the caption and the text accordingly.

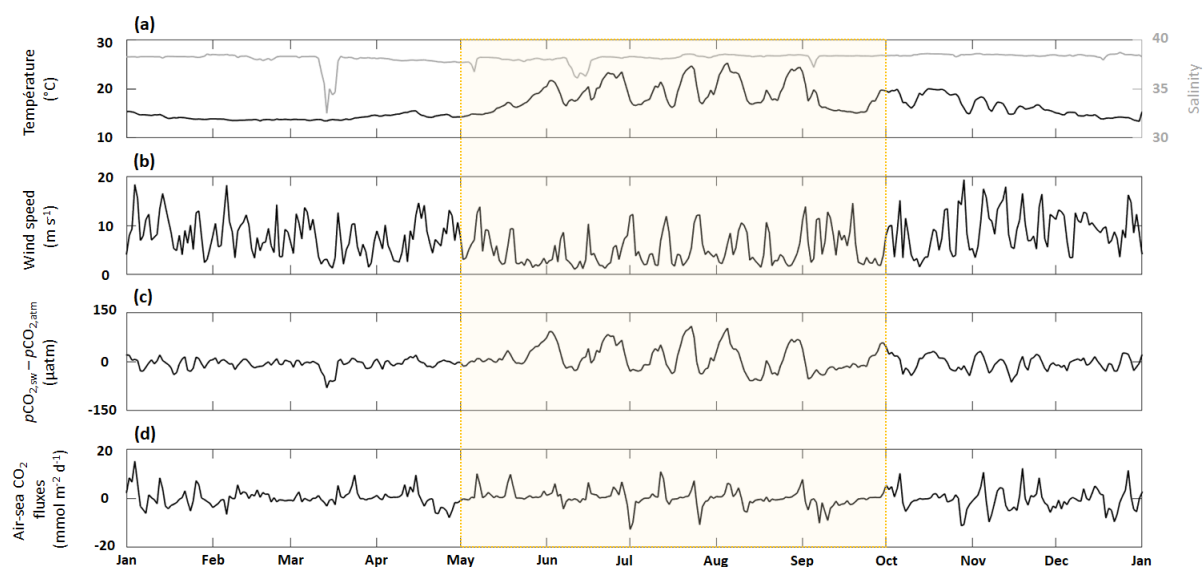


Figure 5: Time series of (a) in situ daily average sea surface temperature (black line) and salinity (grey line) (b) SIMC1 daily average wind speed (c) the difference between SIMC1 daily average seawater $p\text{CO}_2$ and in situ daily average atmospheric $p\text{CO}_2$ (d) SIMC1 daily average air-sea CO_2 fluxes (aeration process). The summer upwelling period (from 1 May to 1 October) is highlighted in yellow.

P16-Fig 6 : The panel d is quite difficult to look out, it can be quite difficult to differentiate the different blue lines (especially nTA and nDIC have very similar colours). Plus, most of the time the curves in this panel are between -100 to +100 μatm , while the y-axis goes from -600 to +600 μatm . Apart from the big events, it's quite difficult to see what's happening there. Maybe take the whole page for this picture ?

We agree. We changed the colour used for nTA representation in figure 6d. If necessary, we also propose to add an appendix which includes the enlargement of figure 6d.

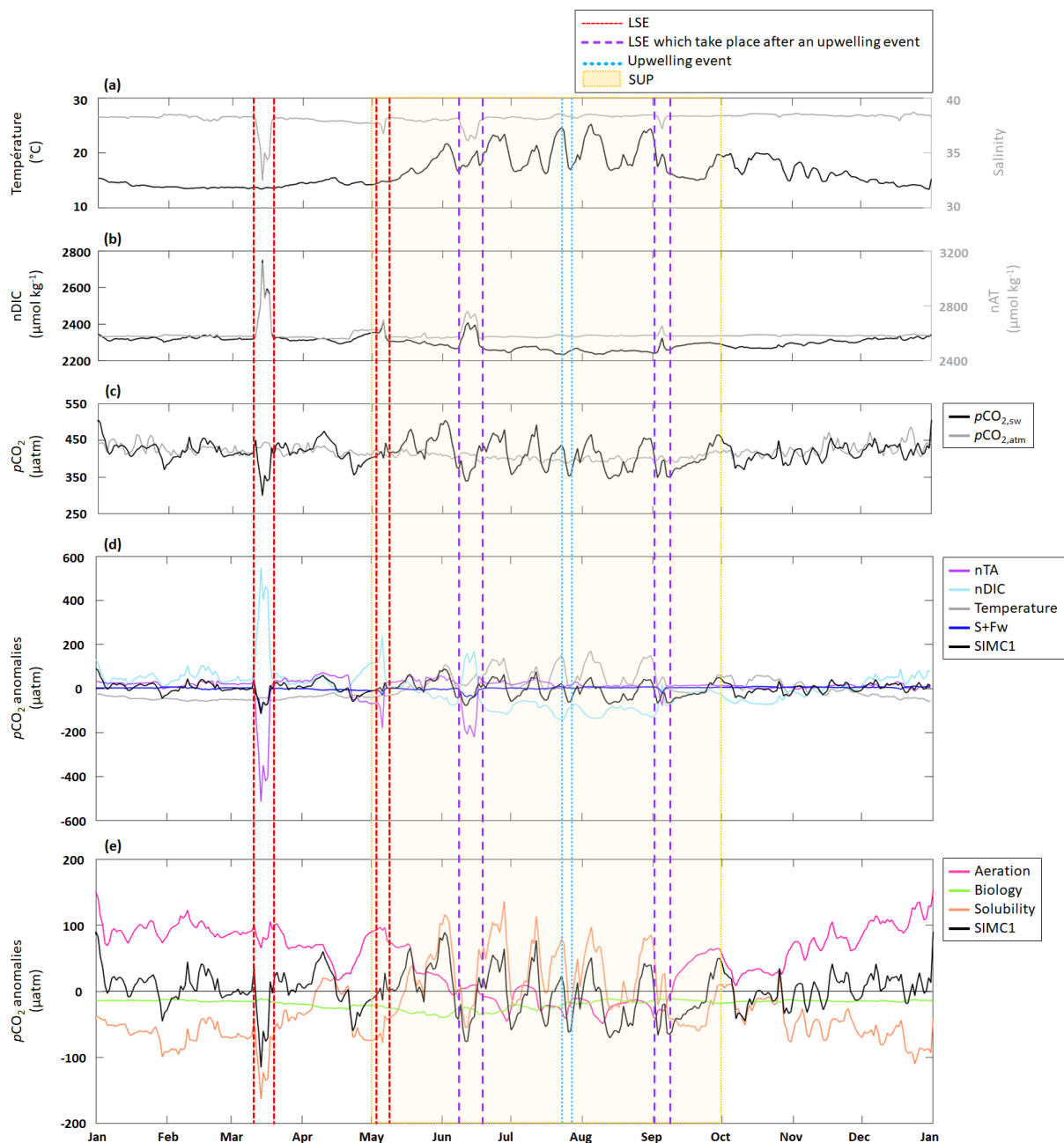


Figure 6: Time series for 2017 of daily average (a) in situ temperature and salinity (b) modelled nDIC and nTA (c) modelled seawater and in situ atmospheric $p\text{CO}_2$ (d) $p\text{CO}_2$ anomalies generated by DIC, TA, Fw+S and temperature based on the approach in Lovenduski et al. (2007) (Note: the dark blue line is sometimes obscured by the black line, especially in March. **An enlargement of the panel d is available in Appendix X.**) (e, j) $p\text{CO}_2$ anomalies generated by aeration, solubility, and biological processes based on the approach in Turi et al. (2014). LSE and an upwelling event have been highlighted. The summer upwelling period (SUP) is indicated by yellow shading.

[Appendix X: Time series of daily average $p\text{CO}_2$ anomalies generated by DIC, TA, Fw+S and temperature based on the approach described in Lovenduski et al. (2007), for 2017. Enlargement of the panel d of the figure 6.

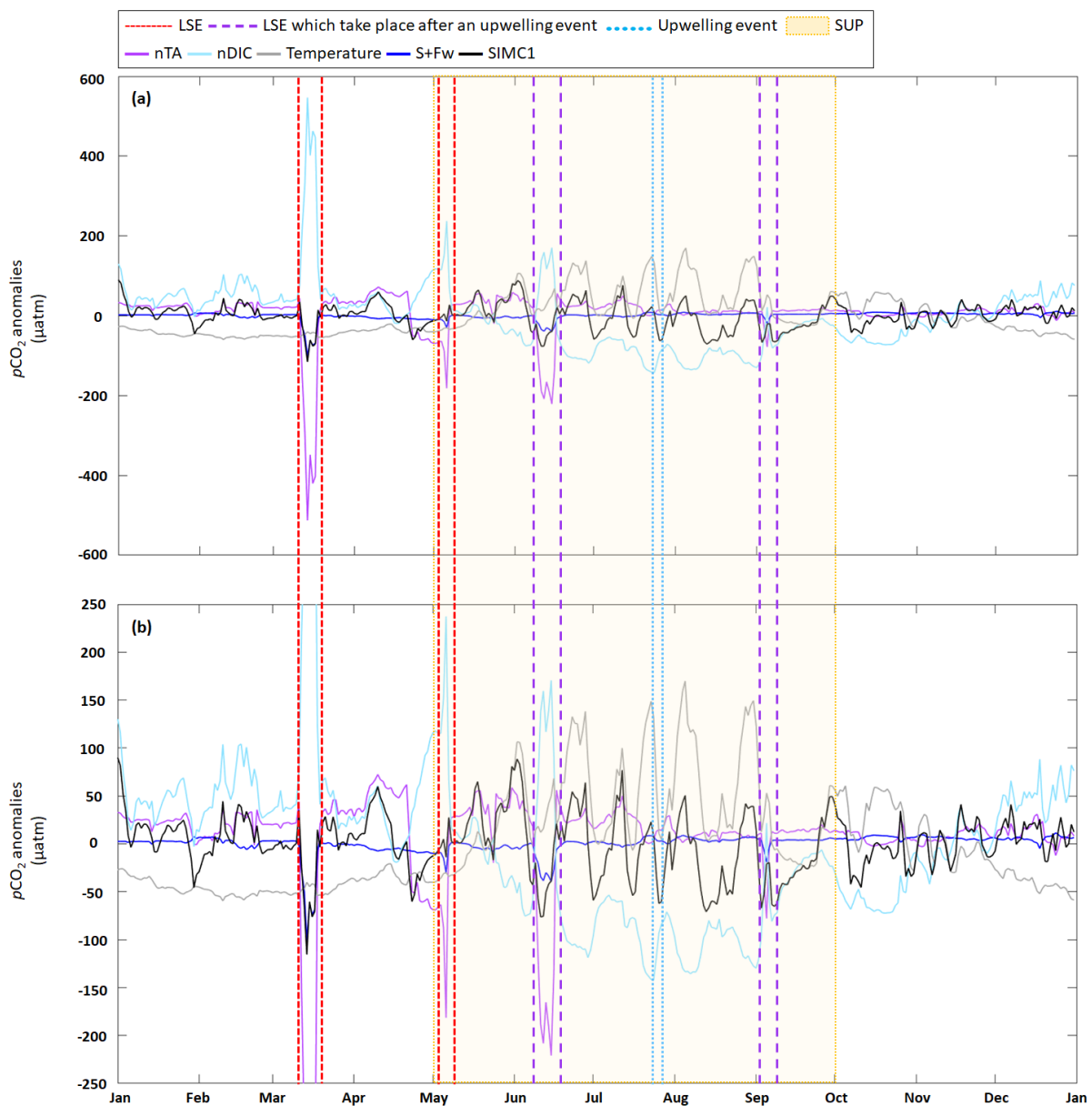


Figure C1: Time series for 2017 of daily average (a) $p\text{CO}_2$ anomalies generated by DIC, TA, Fw+S and temperature based on the approach in Lovenduski et al. (2007) (Note: the dark blue line is sometimes obscured by the black line, especially in March), (b) Enlargement of the panel a between -250 and 250 μatm . LSE and an upwelling event have been highlighted. The summer upwelling period (SUP) is

indicated by yellow shading.

]

P17-L365 to 370 : You forgot to refer to Fig. 6e somewhere in this section.

We added it (l.365-370). [The four LSE are also visible in the solubility-generated anomalies generating strong decreases (Fig. 6e). However, only two LSE are easily identifiable (15 March with a drop from -41 μatm to -163 μatm and 6 May with a drop from 8 μatm to -75 μatm) while the other two appear to be obscured by temperature-related counter-movements. Since aeration- and solubility-generated anomalies show opposite seasonality, they partly cancel each other out. While aeration seems to dominate from November to May, (apart from LSE), solubility appears to dominate from May to November and during LSE. Biological processes are never the dominant driver of $p\text{CO}_2$ variations as they are systematically smaller (by a factor of 2 to 3) than aeration and solubility-generated anomalies (Fig. 6e). Biology-induced anomalies are always negative, providing evidence that biological processes always decrease $p\text{CO}_2$.]

P19-L445 : “we could (not cloud) provide”.

Thank you for pointing this out, we corrected it.

P20 – L477-8 : “While we only considered TA inputs” (only in the allochthonous formulation, I guess), “Rhône River intrusion can also bring nutrient”. This is never explained till now. I already said it in the first part of the review, but you have to be clear about this. The reader cannot fully understand your results otherwise. The model biology only feels the environment changes/variations through the physical forcing only (T, S and light). The biology reacts to the Rhône water only because it is fresher, or to the upwelling because it is colder, but not because of the associated nutrient changes (that do not occur). It is important to tell it because the biology can react in the opposite way than otherwise expected and explain that because it is a 0D model you probably don’t have much choice (as I understand it). Knowing that, I am surprised by the DIC variations Fig. 3, that are surprisingly good.

P21-L482-4 : same remark than just above.

We hope that adding 2.2.1 and the figure 2 to the manuscript clarifies this point. However, we also modified this paragraph to better emphasize that only changes in temperature, salinity and AT are considered by the model during these events (l.477 to 482):

[In all four LSE, biological processes did not have any significant impact on $p\text{CO}_2$ variations (Fig. 6e). To interpret this result, it is important to consider the assumptions used by Eco3M_MIX-CarbOx (section 2.2). Rhône River intrusion can significantly modify the biogeochemistry of the bay as they are typically associated with temperature and salinity changes and TA, DIC and nutrients inputs (Gatti et al., 2006; Fraysse et al., 2014; Lajaunie-Salla et al., 2021). Due to its 0D configuration, Eco3M_MIX-CarbOx only represents temperature and salinity changes and TA inputs (only if the allochthonous formulation is used for the latter). Lajaunie-Salla et al. (2021) showed that nutrient inputs associated to Rhône River intrusion in the BoM led to an increase in chlorophyll concentration. This phytoplankton growth leads to further decrease in $p\text{CO}_2$, which means that by neglecting nutrient inputs we possibly underestimated the importance of biological processes, and especially of autotrophic processes during Rhône River intrusions. Moreover, the high DIC concentrations observed in Rhône River waters (2995 \pm 575 μM on average, Sempere et al., 2000) could also affect $p\text{CO}_2$ variations by increasing the nDIC contribution during intrusion events which counteract the overall of $p\text{CO}_2$ that is typically observed during these events.]

Références:

Barré, L., Diaz, F., Wagener, T., Van Wambeke, F., Mazoyer, C., Yohia, C. and Pinazo, C.: Implementation and assessment of a model including mixotrophs and the carbonate cycle (Eco3M_MIX-CarbOx v1.0) in a highly dynamic Mediterranean coastal environment (Bay of Marseille, France) (Part I): Evolution of ecosystem composition under limited light and nutrient conditions, <https://doi.org/10.5194/gmd-16-6701-2023>, 2023.

Lajaunie-Salla, K., Diaz, F., Wimart-Rousseau, C., Wagener, T., Lefevre, D., Yohia, C., Xueref-Remy, I., Nathan, B., Armengaud, A., and Pinazo, C.: Implementation and assessment of a carbonate system model (Eco3m-CarbOx v1.1) in a highly dynamic Mediterranean coastal site (Bay of Marseille, France), *Geoscience Model Development*, 14, 295–321, <https://doi.org/10.5194/gmd-14-295-2021>, 2021.

Mitra, A., Flynn, K. J., Burkholder, J. M., Berge, T., Calbet, A., Raven, J. A., Granéli, E., Glibert, P. M., Hansen, P. J., Stoecker, D. K., Thingstad, F., Tillmann, U., Våge, S., Wilken, S., and Zúrov M. V.: The role of mixotrophic protists in the biological carbon pump, *Biogeosciences*, 11, 995-1005, <https://doi.org/10.5194/bg-11-995-2014>, 2014.

Stow, C. A., Jolliff, J., McGillicuddy Jr, D. J., Doney, S. C., Allen, J. I., Friedrichs, M. A., Rose, K. A. and Wallhead, P.: Skill assessment for coupled biological/physical models of marine systems, *Journal of Marine Systems*, 76(1-2), 4-15, 2009.

First, we would like to thank referee 2 for his careful evaluation of our manuscript and his interesting comments which we believe will help us to improve it. Please, find hereafter our response to these comments.

1) Firstly, I would say that it does not fit the scope of GMD, which is there to present new developments in models. While the companion paper, with its presentation of a mixotroph compartment, meets this criterium, the main new thing in this manuscript is a diagnostic relation between TA and salinity, which may improve the results, but conceptually is a fairly small step and has been used in many different models so far. From this side I would rather recommend publication in a different journal, where the focus is more on the considered system itself, i.e. a model for the BoM.

We understand your concern, however we believe that this manuscript has its place in GMD. Eco3M_MIX-CarbOx is a new model which has been developed to consider both mixotrophs and carbonate system. We decided to present Eco3M_MIX-CarbOx in two parts to show both sides of the model distinctly. It allowed us to propose clear studies, easier to read than one which would have been longer, and at the same time to highlight the two main developments which, together, constitute the originality of our model. However, it is important to keep in mind that both parts of the study aim to present this new model. We believe that the study, as a whole (both parts), fits well the scope of GMD and especially, meet the criteria of 'model description papers'.

Moreover, both studies are strongly linked. In the first part, we focused on the planktonic ecosystem description, especially on mixotrophs. We detailed their implementation in the model and study their dynamics in the area. In the second part, we focused on the carbonate system which is barely mentioned in the first part and detailed its representation in the model. This second study is based on the first one as we present a representation of carbonate system by considering the impact of mixotrophs (photosynthesis, respiration...) on these variables. We think that the strong connection between both studies also justify their publication in the same journal.

2) The switch to a salinity-TA relationship is motivated by the desire to represent the episodic intrusion of freshwater from the nearby Rhone into the BoM, and also the influence of evaporation and precipitation. My first question here is: If these freshwater fluxes affect the TA balance so strongly, should they not also influence DIC?

First, we would like to stress the fact that "an excess of alkalinity" which likely reflects alkalinity inputs to coastal areas has been described for the entire Mediterranean Sea (Schneider et al., 2007). This study, at the global scale, has forged our conviction that, in a coastal area close to the Rhone River, alkalinity inputs from Rhone River needed to be considered even in this OD configuration.

The switch to a salinity-TA relationship is possible thanks to the fact that in the bay of Marseille, TA variations are mainly the results of rivers contributions, particularly the Rhône River one. It was demonstrated by the lack of variations observed when we modelled TA only based on biogeochemical processes which take place in the box. For DIC, a different reasoning must be adopted, mainly because the processes which impact DIC dynamics are very different than the one which impact TA dynamic. As we consider a surface layer, DIC dynamics is mostly the results of temperature and salinity changes (which are considered by the model) and biogeochemical processes (especially air-sea CO₂ exchanges) (Hassoun et al., 2015). The Rhône River can bring DIC to the BoM, these inputs are diluted (far from 2877 $\mu\text{mol kg}^{-1}$, the value observed in the Rhône River, Table S1) and, due to the action of other processes (solubility effects and biogeochemical processes) on DIC dynamics, which is more pronounced in this case, have a less significant impact than on TA dynamics.

Moreover, it is important to note that, in Eco3M_MIX-CarbOx, TA is the main driver of carbonate system. In other words, a change in TA results in significant changes in DIC, pH_T and pCO_2 as demonstrated by the Figure 4 of the manuscript. By representing the contribution of the Rhône River on TA we then indirectly apply it to the three other variables of the carbonate system. We are aware that the contribution of the Rhône River to the DIC considered in that way (through TA) is only an indirect effect. It is important to highlight that in the case of our OD configuration, it is not always possible to consider allochthonous contributions. So far, we experimented two ways to consider external contributions in Eco3M_MIX-CarbOx, which gave satisfactory results:

- By using a $VAR=f(S)$ relation (done in this paper for TA),
- By forcing the variable with a file which include an interpolation of the measurements performed at SOLEMIO for this variable (done in our first paper for nutrient concentrations)

Using a $DIC=f(S)$ relation did not produce the expected results. In fact, it is not recommended to use such a formulation to represent DIC dynamics, especially in surface water due to the numerous processes from which its dynamic results (Hassoun et al., 2015). Using an interpolation of SOLEMIO DIC measurements force us to represent the variable dynamics as a forcing, which had no real interest here given that the representation of DIC obtained was already rather correct when based on biogeochemical processes.

Table S1: Salinity-DIC couples for LSE events measured at SOLEMIO between 6 June 2016 and 26 June 2019 (last data available).

Salinity	DIC ($\mu\text{mol.kg}^{-1}$)
37.11	2321.3
37.78	2280.1
37.30	2259.3
36.82	2323.8
37.62	2288.7
37.18	2260.3
37.66	2269.8
37.32	2249.0

and nutrients as well?

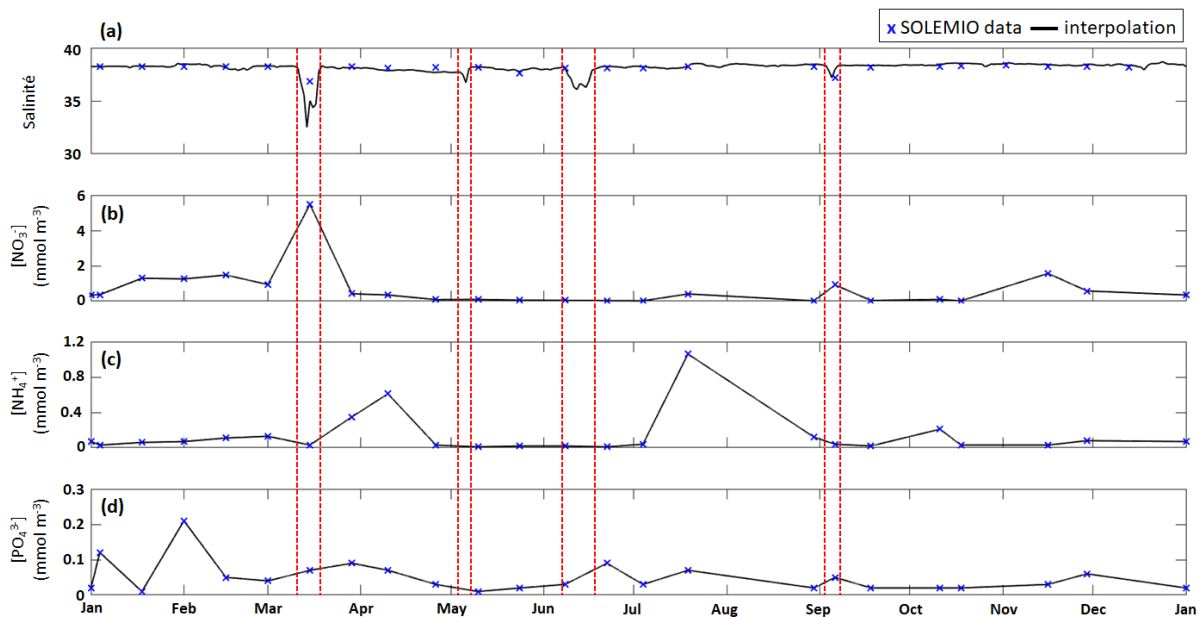


Figure S1: Time series of surface (a) salinity (CARRY measurements), and interpolated (b) NO_3^- concentration, (c) NH_4^+ concentration and (d) PO_4^{3-} concentration at SOLEMIO station. SOLEMIO data are represented by blue markers and the four LSE are indicated by the red dotted lines.

Rhône River intrusion events are associated with an increase of nutrient concentrations in the area, especially nitrate and phosphate (Frayse et al., 2014). However, in our case, the four low salinity events are not systematically associated with a nutrient increase at the station. In fact, only the first and last events (15 March and 5 September respectively) have an impact on nutrient concentrations at SOLEMIO with the first event being the most significant (Fig. S1). This pattern can be explained by the salinity data used by the model. The measurements are performed at CARRY station (near the Côte Bleue, see figure 1 of the manuscript for location) which is more significantly impacted by the Rhône River plume as it is closer to the river mouth than SOLEMIO station. In consequence, decreases of salinity measured at CARRY are not systematically observed or can be less significant at SOLEMIO. Salinity measurements are also performed at SOLEMIO, however their temporal resolution is low (fortnightly measurements) compared to the CARRY one (hourly measurements). In fact, Rhône River intrusion events duration is variable and can be less than 15 days (ex: short-lived intrusions, Frayse et al., 2014), therefore it is important to consider the highest temporal resolution possible to better catch them with measurements which is why we chose to work with CARRY measurements instead of SOLEMIO measurements (Fig. S1a).

That this may lead to biases is discussed in lines 477 to 484; but given the extremely high DIC concentration in Rhone water quoted on line 482, I wonder whether this inconsistency may not invalidate the main results.

We understand your concerns, however, as indicated in the previous point, the strong DIC value (2877 $\mu\text{mol.kg}^{-1}$) observed in the Rhône River never reaches SOLEMIO as the Rhône River plume is quickly diluted and the DIC values which really reaches SOLEMIO station are rarely higher than 2300 $\mu\text{mol.kg}^{-1}$ (mean value of 2281.5 $\mu\text{mol.kg}^{-1}$, Table S1).

Moreover, as indicated in the previous point, it is important to note that in Eco3M_MIX-CarbOx, TA is the main driver of carbonate system. In other words, a change in TA results in significant changes in DIC, pH and pCO_2 as demonstrated by the Figure 4 of the manuscript. By representing the contribution of the Rhône River on TA we then indirectly apply it to the three other variables of the carbonate system.

3) This leads me to a more conceptual difficulty with the approach. The model concept is that of an arbitrary one cubic metre volume at the surface of the bay, and that the model just represents fluxes within this volume. Spatial fluxes are excluded (except for CO_2 flux, more on that below). This only allows either to model a variable as purely forced from what is happening inside the box, or to prescribe it, e.g. as a function of salinity. For a proper modelling of how external fluxes (e.g. in mol/s) change concentrations ($\text{mol/m}^3/\text{s}$) inside the modelled region, one would have to define the volume that is affected by these fluxes. A reasonable choice might be to model a column of water within the mixed layer, as was done in many zero-dimensional models, e.g. Fasham et al, 1990 or Hurtt and Armstrong 1999. That would allow a consistent treatment of the effects of mixing on TA, DIC, nutrients.

This difficulty becomes especially clear when the authors discuss the possible reasons for their low net annual air-sea flux of CO_2 , which is in contrast to observation-based estimates. Here they state that "aeration is simulated by applying Eq (5) to 1 m^3 of surface water at the SOLEMIO station, which tends to overestimate the effect of aeration processes on DIC..." (line 534 ff). Indeed: if the control volume is that shallow, it will lead to a too fast approach of DIC towards equilibrium, and hence an underestimate of fluxes.

We understand your concern. We think that it is important to note that, in this study, we relied on Eco3M-CarbOx (Lajaunie-Salla et al., 2021) for the calculation of carbonate variables. So, Eco3M-CarbOx was our starting point to implement carbonate system variables in Eco3M_MIX-CarbOx. With our study, we aim to bring answers to the concerns raised by this previous study, we then use the same concept and try to improve the representation of carbonate cycle variables (by adding mixotrophs organisms processes to the state equations and switching TA formulation by a newly implemented allochthonous formulation). In this way, we were able to compare both models, then knowing how our modifications impact the carbonate system variables representation. Even if we did not manage to obtain a realistic representation of air-sea CO₂ fluxes, we provide some improvements to the initial concept and give some examples of suitable and unsuitable use of it (first part and second part of this study respectively), then confirming that the only way to obtain realistic fluxes is to consider a larger layer. We could have done it the way you propose but, considering that it required a complete review of our OD configuration, we decided to focus directly on the coupling of Eco3M_MIX-CarbOx, in 3D (which is still in test phase).

4) And finally, while the diagnostic TA leads to an improvement in model results, as evidenced by decreases in %BIAS, RMSD and a 'cost function' presented in Table 3, the improvements are fairly modest. Indeed I would be interested in knowing whether a model with TA prescribed constant at the average of observations would not have fared at least similarly good as the two presented model cases.

As suggested, we run a simulation with a constant TA (mean of SOLEMIO measurements for 2017 = 2591.2 $\mu\text{mol kg}^{-1}$). In Table S2, we presented the calculation of the statistical indicators presented in the manuscript. As we decided to modify them, based on your suggestions, we also provided average absolute error (AAE), and average error (AE) calculated as in Stow et al. (2009) except that, to be consistent with calculations of statistical indicators used previously (Allen et al., 2007) the difference is applied between observations and model which means that for %BIAS and AE, if a positive value is obtained the model underestimates the observations.

Table S2: Statistical indicators calculation for the simulation with a constant TA (TA = 2591.2 $\mu\text{mol kg}^{-1}$). Mean, SD, AE, AAE and RMSD are in the same unit than the considered variable, i.e.: $\mu\text{mol kg}^{-1}$ for TA and DIC and μatm for $p\text{CO}_2$. CF and %BIAS are without unit.

		TA	DIC	$p\text{CO}_2$	pH_T
N	Observation	20	20	20	20
Mean \pm SD	Observation	2591.2 \pm 19.4	2294.9 \pm 24.0	391.0 \pm 31.0	8.09 \pm 0.03
Mean \pm SD	Model	2591.2 \pm 0.22	2305.7 \pm 26.1	418.0 \pm 28.9	8.07 \pm 0.03
CF	Model	0.85	0.82	1.14	1.14
%BIAS	Model	-0.002	-0.50	-5.79	0.26
RMSD	Model	18.90	26.14	38.45	0.03
AAE	Model	16.5	19.7	35.5	0.03
AE	Model	-0.06	-11.5	-22.6	0.02

We also represented the daily mean values of TA, DIC, pH_T and $p\text{CO}_2$ for the simulations SIMCO, SIMC1 and constant TA (Fig. S2) to compare the three simulations carbonate system variables representation.

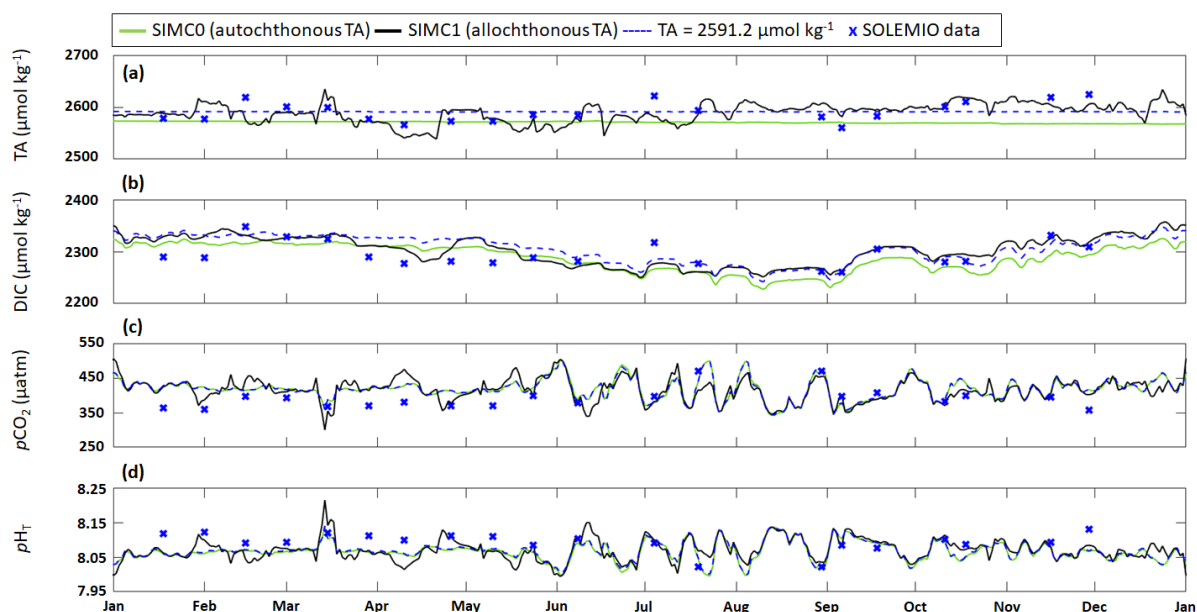


Figure S2: Comparison of model outputs from SIMCO (autochthonous formulation, Table 2 of the manuscript), SIMC1 (allochthonous formulation, Table 2 of the manuscript), and constant TA simulation, model runs showing daily average (a) TA, (b) DIC, (c) $p\text{CO}_2$ and, (d) pH_T for 2017. SOLEMIO data are represented by blue markers.

We are aware that improvements seem fairly modest, especially when studying the statistical indicators (Table S2). However, values are generally slightly better for the simulation SIMC1, especially for the three other carbonate system variables. In fact, the major improvement brought by the switch to an allochthonous formulation for TA, is that TA variations are represented which seems more realistic and tend to improve the representation of the other three carbonate system variables.

Major comments :

Figure 1 is identical to the one on the companion paper and definitively isn't needed should this paper be published in GMD.

Done. We replaced the map by the following sentence: [\[A map of the study area showing the location of stations where measurements were carried, and places of interest can be found in Barré et al. \(2023a\).\]](#) and added at the end of the 2.1.

State equation for TA, Eq. (1): The terms in the equation are not properly defined. The definition of the terms is given in the Appendix (Table A1), but the table is not referenced here.

Thank you for pointing this out, we added it l.144: [where i represents the number of organisms. [Processes description can be found in Table A1 \(Appendix A\) and formulations are available in Barré et al. \(2023a\).](#) In this formulation, TA only depends on biogeochemical processes (i.e., TA riverine inputs are excluded).] and l.170: [where i represents the number of organisms. [Processes description can be found in Table A1 \(Appendix A\) and formulations are available in Barré et al. \(2023a\).](#) As an additional modification, we use a more recent version of the gas transfer velocity calculation introduced by Wanninkhof (2014).].

The two linear S-TA relations, presented on page 7, which are valid below and above a salinity threshold of 37.8 are discontinuous at $S=37.8$. This should lead to sudden jumps in the TA value if this threshold is crossed. Are there any effects of this discontinuity visible in the results?

Thank you for this interesting comment. Indeed, using the allochthonous formulation leads to sudden jump in TA when the thresholds is crossed. These sudden jumps are also observed in pH_T and pCO_2 .

When we implemented the TA allochthonous formulation, we used two points: a first one which represents the Rhône River water at the river mouth ($S = 0$, $TA = 2885 \mu\text{mol kg}^{-1}$) and a second one which represents the Rhône River water which reach SOLEMIO during a LSE ($S = 36.82$, $TA = 2600.6 \mu\text{mol kg}^{-1}$). We chose the second point as it was the most significative LSE on the period covered by the SOLEMIO measurements (2017 and 26 June 2019). We then consider it as representative of the Rhône River water which reach the BoM. Even though TA values associated with LSE are variable and highly depend on the period of the year (Fig. S3). TA values equal or above $2600 \mu\text{mol kg}^{-1}$ do not seem the most representative (Table S3) and LSE seem associated with TA highly dependent on Rhône River seasonality (mean value = $2575 \mu\text{mol kg}^{-1}$).

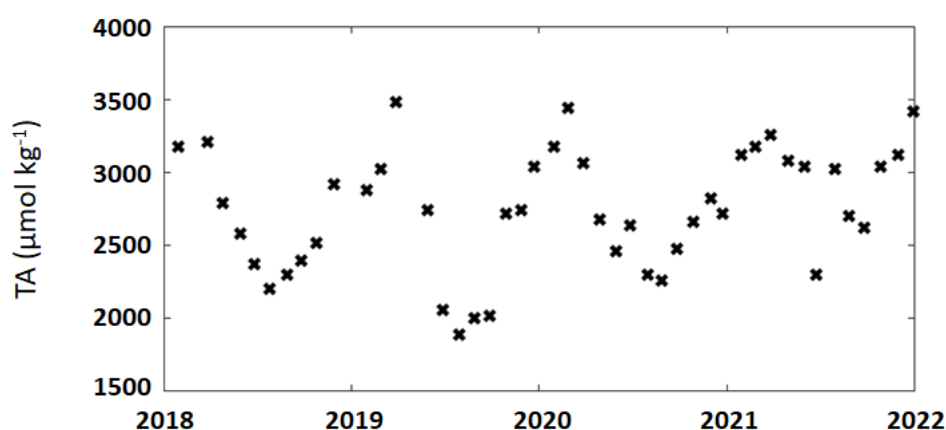


Figure S3: TA measurements in the Rhône River (data: Naiades, <https://naiades.eaufrance.fr>, first data available: January 2018).

Table S3: Salinity-TA couples for LSE events measured at SOLEMIO between 6 June 2016 and 26 June 2019 (last data available).

Salinity	TA ($\mu\text{mol kg}^{-1}$)
37.11	2603.0
37.78	2579.6
37.30	2585.5
36.82	2600.6
37.62	2585.8
37.18	2560.8
37.66	2568.4
37.32	2520.7

We think that it might be interesting to improve our allochthonous formulation to better manage the threshold crossing case. To avoid (or at least reduce these instabilities) it could be interesting to take into account Rhône River seasonality in the allochthonous formulation and we plan to do this in a future work.

Page 8, line 175: In principle the model equations would not change had you chosen to assume the effected layer to be deeper, except that then the flux would then be distributed over a larger volume. Why not take at least H as the annual average mixed layer depth> Taking it as 1m is equivalent to speeding up the gas exchange by a factor H_{real} , the real affected layer.

As suggested, we ran a simulation with a modified function for aeration process (Eq. S1, SIMR1 in the following). We considered a mean annual value of 30.5 m for mixed layer depth (mean of winter value

= 41 m and summer value = 20 m (Wimart-Rousseau et al., 2020)). Daily average of modelled carbonate system variables and air-sea CO₂ fluxes are represented in figure S4.

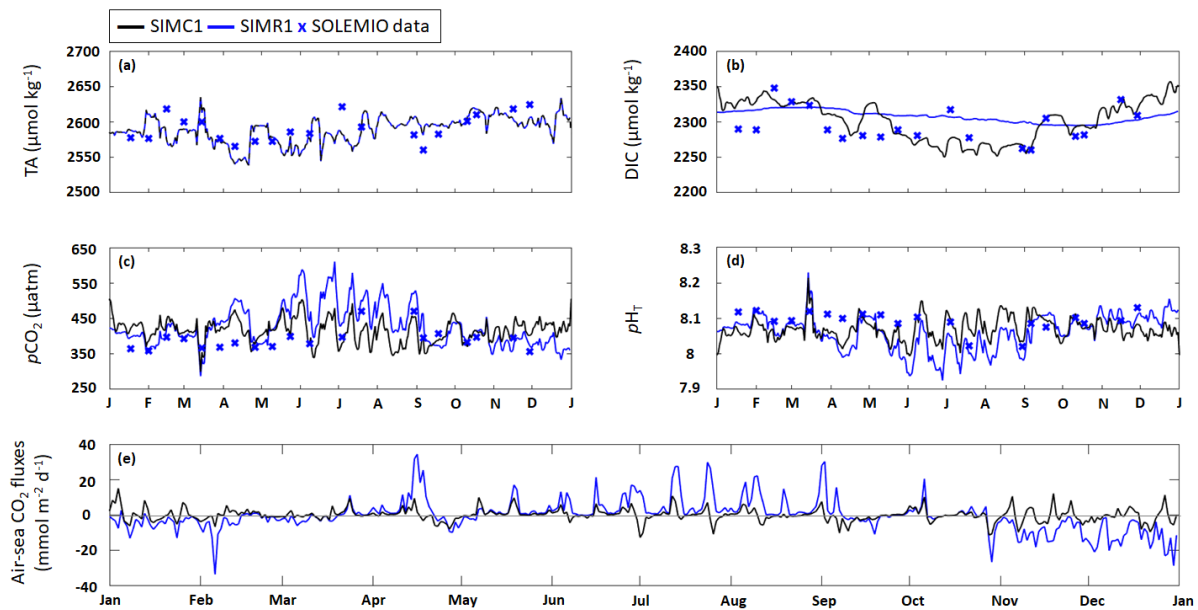


Figure S4: Comparison of model outputs from SIMC1 (aeration process apply on a 1 m layer, Table 2 of the manuscript) and SIMR1 (aeration process apply on 30.5 m layer, model runs showing daily average (a) TA, (b) DIC, (c) $p\text{CO}_2$, (d) pH_T , and Air-sea CO₂ fluxes for 2017. SOLEMIO data are represented by blue markers.

We obtained a mean annual value for air-sea CO₂ fluxes of $-113.6 \text{ mmol m}^{-2} \text{ yr}^{-1}$ which is better than the one obtained previously ($-0.21 \text{ mmol m}^{-2} \text{ yr}^{-1}$) but still lower than the value suggested by Wimart-Rousseau et al. (2020) ($-803 \text{ mmol m}^{-2} \text{ yr}^{-1}$). These results are interesting as we can see that, by considering a larger layer, we better represent the seasonality of air-sea CO₂ fluxes (sink in winter and source in summer) (Fig. 4e) which is mainly explained by the fact that we are able to represent the undersaturation observed for $p\text{CO}_2$ in winter, especially at the end of the year (Fig. S4c). In this simulation, we used a constant MLD, however, we believe that using a variable MLD (deeper in winter than in summer) could emphasize this result. These results also show that by considering a larger layer to apply the aeration fluxes, we significantly modify DIC representation (Fig. S4b). Thus, the seasonality well modelled previously, is no longer visible. DIC values are also much less variable, then far from the dynamics described by observations.

To conclude, we believe that more than modifying the thickness of the layer impacted by aeration process, we need to move to a 3D configuration to better represent air-sea CO₂ fluxes without impacting the representation of DIC which is already, rather correct.

Page 8 and Appendix B, pH and pCO₂ calculation: It is good to see that the pH scale differences are taken properly into account, and fugacity has been calculated correctly. But much of this is fairly standard, e.g. the iterative calculation of pH, described in Figure B1. This could be left away.

We considered your comment, however, as we provide some corrections to Lajaunie-Salla et al. (2021) Appendix A, we think that it is necessary to keep Appendix B in the manuscript.

Page 9, Figure 3: The quality of the Figure is awful. But also it does not convey much information, I would leave it away.

We considered your suggestion. However, we think that figure 3 allows to better visualize the model calculation steps and how these can be modified by the choice of TA formulation. We decided to modified figure 3 to increase its quality:

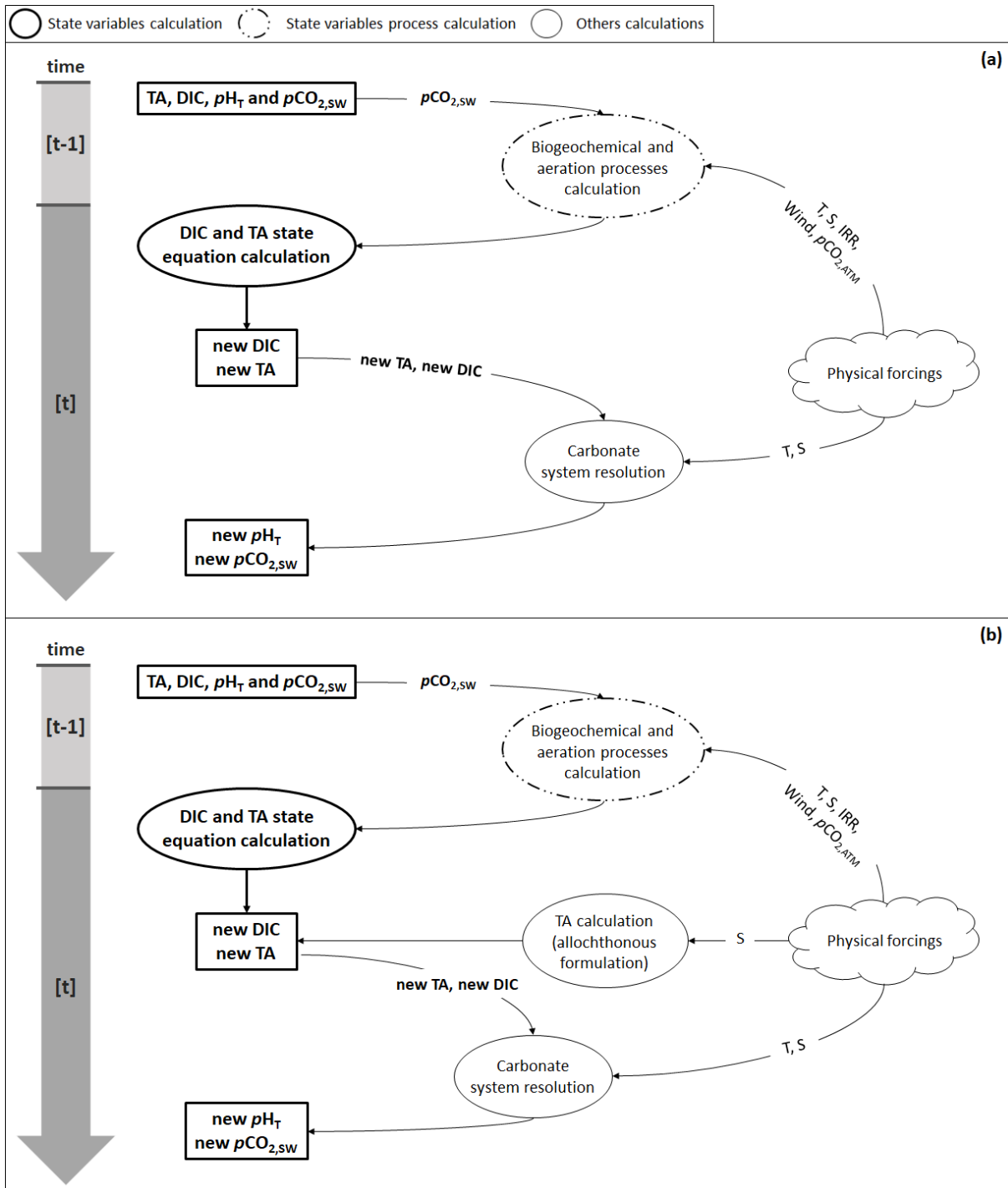


Figure 3: Flow diagram illustrating the steps needed to calculate pH_T and pCO_2 (a) using the autochthonous formulation (Eq. 1) and (b) with the allochthonous formulation (Eq. 2 and 3). Physical forcings include temperature (T), salinity (S), solar irradiance (IRR), wind speed (Wind) and atmospheric pCO_2 ($pCO_{2,ATM}$).

We hope it is clearer this way.

Page 10, lines 218-220: It is not clear to me how the salinity-normalized nTA and nDIC are exactly defined, by a linear correlation with salinity with zero intercept? If so, why do that if the observed S-TA relation in the oceanographic region is different?

Salinity-normalised changes in nTA and nDIC were calculated by dividing by in situ salinity and multiplying by mean salinity.

To clarify, we added (l.219): [Though, we isolate the changes of TA and DIC due to variations in freshwater inputs using the salinity normalised TA (nTA) and DIC (nDIC) **which are obtained by dividing the considered variable by in situ salinity and by multiplying the result by mean in situ salinity**, and adding another term to regroup them.]

page 11, definition of the statistical indicators: while the definition of RSMD and %BIAS is rather clear, that of the cost function is less clear: Typically, a cost function aggregates model-data-disagreement for different variables, possibly with different units, into a single scalar variable (Stow et al, 2009). But what exactly the variables are that enter the CF, and how the different variables are nondimensionalized and aggregated into one CF should be properly defined.

We based our CF calculation on Allen et al. (2007). In this work, CF is defined as: [The cost function gives a non-dimensional value which is indicative of the “goodness of fit” between two sets of data; it quantifies the difference between model results and measurement data (see OSPAR Commission, 1998). It is a measure of ratio of the model data misfit to a measure of the variance of the data; the closer the value is to zero the better the model.], and is calculated as follow:

$$CF = \frac{1}{N} \sum_{i=1}^N \left(\frac{|O_i - M_i|}{\sigma_O} \right)$$

Where O represents the observations, M the model results and σ_O is the standard deviation of the observations.

page 11, interpretation of statistical indicators: Whether a CF<1 is considered very good, would probably depend on the definition of CF, and cannot be stated as generally as on line 255-256. If the individual cost function terms e.g. consist of the squared model-data difference scaled by the variance in the individual variables, and are then added together, the expected height of the CF would depend on how many different variables are finally added together. Also, I don't think one can generally say (line 252-253) that a %BIAS<10% is excellent; I would think that depends on the ratio of natural variability to the mean of the variable in question. For TA, with a high background value, a 10% BIAS is rather large.

To interpret CF and %BIAS, we used the interpretation of Radach & Moll (2006) and Marechal (2004) respectively. We understand that these interpretations seem not strict enough. Moreover, CF indicator seems rather insensitive as almost all variables for the tested simulations show CF value lower than 1. To improve our statistical analysis of model results, we proposed to consider two other indicators: AE and AAE, to replace CF. We based their calculations on Stow et al. (2009) except that, to be consistent with the calculation of RMSD used previously (Allen et al., 2007), the difference is applied between observations and model which means that for AE, if a positive value is obtained the model underestimates the observations. Moreover, we added the formulation of each statistical indicators used to avoid confusion.

We modified the 2.4 accordingly:

(I.246): [We used three statistical indicators for the comparison between simulation and SOLEMIO data: the percent bias (%BIAS), the cost function (CF) and the root mean square deviation (RMSD). These indicators were used with two Eco3M_MIX-CarbOx simulations (SIMC0 and SIMC1) and the reference Eco3M-CarbOx simulation (Lajaunie-Salla et al., 2021). %BIAS is calculated according to Allen et al. (2007) and allows to quantify the model's tendency to under- or overestimate the observations. In our case, a positive %BIAS means that the model underestimated the in situ observations and vice versa. %BIAS is interpreted according to Marechal (2004). We use the absolute values of %BIAS, to assess the overall agreement between the model results and observations. The agreement is considered: excellent if %BIAS < 10 %, very good if 10 % ≤ %BIAS < 20 %, good if 20 % ≤ %BIAS < 40 % and poor otherwise. The cost function is calculated based on Allen et al. (2007). It is a dimensionless indicator that quantifies the goodness of fit between the model and observations. According to Radach and Moll (2006), CF < 1 is considered very good, 1 ≤ CF < 2 is good, 2 ≤ CF < 3 is reasonable, while CF ≥ 3 is poor. RMSD quantifies the difference between model results and observations (Allen et al., 2007). The closer RMSD is to 0, the more reliable the model. All statistical indicators are calculated using surface SOLEMIO data from 2017. The model data is averaged using the mean of the output from the date in question ± five days. Using temporal mean and standard deviation of model results allowed us to better account of variability at SOLEMIO station. By comparing the statistical indicators obtained for SIMC0, SIMC1 and Eco3M-CarbOx we also obtained an indication of how changes in the carbonate formulation affected the results.]

to: [We used four statistical indicators for the comparison between simulation and SOLEMIO data: the percentage bias (%BIAS), the average error (AE), the average absolute error (AAE) and the root mean square deviation (RMSD, also refer as root mean square error in the literature - RMSE). They were used with two Eco3M_MIX-CarbOx simulations (SIMC0 and SIMC1) and the reference Eco3M-CarbOx simulation (Lajaunie-Salla et al., 2021). The %BIAS is calculated as follow:

$$\%BIAS = \frac{\sum_{i=1}^N (O_i - M_i)}{\sum_{i=1}^N O_i} * 100 \quad (16)$$

where O represents the observations and M the model results (Allen et al., 2007). This indicator allows to quantify the model's tendency to under- or overestimate the observations. The closer the value is to 0, the better the model. Here, a positive %BIAS means that the model underestimated the in situ observations and vice versa. On an indicative basis, the %BIAS can be interpreted according to Marechal (2004): Absolute values of %BIAS allow to assess the overall agreement between the model results and observations and the agreement is considered: excellent if %BIAS < 10 %, very good if 10 % ≤ %BIAS < 20 %, good if 20 % ≤ %BIAS < 40 % and poor otherwise.

We based our calculation of AE, AAE and RMSD on Stow et al. (2009). Together, these three statistical indicators provide an indication of model prediction accuracy.

$$AE = \frac{\sum_{i=1}^N (O_i - M_i)}{n} \quad (17)$$

$$AAE = \frac{\sum_{i=1}^N (|O_i - M_i|)}{n} \quad (18)$$

$$\text{RMSD} = \sqrt{\frac{\sum_{i=1}^N (\text{O}_i - \text{M}_i)^2}{N}} \quad (19)$$

The three of them aim to measure the size of the discrepancies between model results and observations, the closer the value is to 0, the better the agreement between model results and observations. However, when interpreting AE, it is important to note that value near zero can be misleading because negative and positive discrepancies can cancel each other. That is why it is important to calculate, in addition to AE, AAE and RMSD which allow to overcome this effect (Stow et al., 2009). Such as %BIAS, a positive value of AE means that the model underestimated the in situ observations and vice versa.

The model data is averaged using the mean of the output from the date in question \pm five days. Using temporal mean and standard deviation of model results allowed us to better account of variability at SOLEMIO station. By comparing the statistical indicators obtained for SIMCO, SIMC1 and Eco3M-CarbOx we also obtained an indication of how changes in the carbonate formulation affected the results.]

We changed the Table 3 (Page 14):

[Table 3: Comparing the different model results to surface observations at SOLEMIO station for TA, DIC, seawater $p\text{CO}_2$, and pH_T . N represents the number of observations. Mean, SD, AE, AAE and RMSD are in the same unit than the considered variable, i.e.: $\mu\text{mol kg}^{-1}$ for TA and DIC and μatm for $p\text{CO}_2$. %BIAS is without unit.

		TA	DIC	$p\text{CO}_2$	pH_T
N	Observations	20	20	20	20
Mean \pm SD	Observations	2591.2 \pm 19.4	2294.9 \pm 24.0	391.0 \pm 31.0	8.09 \pm 0.030
	SIMCO	2576.1 \pm 1.5	2293.6 \pm 25.1	413.5 \pm 16.5	8.07 \pm 0.015
Mean \pm SD	SIMC1	2588.6 \pm 16.4	2301.1 \pm 24.5	409.1 \pm 21.4	8.07 \pm 0.020
	CarbOx	2574.5 \pm 3.6	2292.5 \pm 26.0	413.9 \pm 15.9	8.07 \pm 0.010
	SIMCO	0.58	0.05	-5.75	0.29
%BIAS	SIMC1	0.09	-0.27	-4.61	0.21
	CarbOx	0.64	0.1	-5.86	0.29
	SIMCO	15.12	1.25	-22.5	0.02
AE	SIMC1	2.57	-6.2	-18.02	0.02
	CarbOx	16.7	2.4	-22.9	0.02
	SIMCO	18.7	20.4	35.9	0.03
AAE	SIMC1	16.3	17.2	34.7	0.03
	CarbOx	20.1	21.2	35.3	0.03
	SIMCO	24.90	24.26	38.75	0.04
RMSD	SIMC1	20.03	21.83	40.27	0.04
	CarbOx	26.56	24.90	38.29	0.04

]

Considering a suggestion from referee 1, we also added appendix C, the calculation of statistical indicator for H^+ concentration (Kwiatkowski & Orr, 2018).

[Appendix C: Statistic indicators calculation for H^+ concentration

Table C1: Comparing the different model results to surface observations at SOLEMIO station for H⁺ concentration. N represents the number of observations. Mean, SD, AE, AAE and RMSD are in the same unit than the considered variable, i.e.: mmol m⁻³ for H⁺ concentrations. % BIAS is without unit.

		[H ⁺]
N	Observations	20
Mean ± SD	Observations	$8.08 \times 10^{-9} \pm 5.52 \times 10^{-10}$
Mean ± SD	SIMC0	$8.89 \times 10^{-9} \pm 2.91 \times 10^{-10}$
	SIMC1	$8.39 \times 10^{-9} \pm 4.06 \times 10^{-10}$
	CarbOx	$8.52 \times 10^{-9} \pm 2.80 \times 10^{-10}$
%BIAS	SIMC0	-5.33
	SIMC1	-3.91
	CarbOx	-5.47
AE	SIMC0	-4.30×10^{-10}
	SIMC1	-3.15×10^{-10}
	CarbOx	-4.42×10^{-10}
AAE	SIMC0	6.45×10^{-10}
	SIMC1	6.05×10^{-10}
	CarbOx	6.36×10^{-10}
RMSD	SIMC0	6.98×10^{-10}
	SIMC1	7.14×10^{-10}
	CarbOx	6.93×10^{-10}

]

and modified the results part (3.1) accordingly (l.301):

[Regarding the coast function, simulations yielded $CF < 2$ for all variables which is considered very good ($CF < 1$) or good ($1 \leq CF < 2$) (Table 3). The %BIAS parameter yielded “excellent” results for all variables (using the interpretation from Marechal, 2004, i.e., %BIAS < 10 %). The highest values for %BIAS (in absolute terms) were obtained for pCO₂ with ~6 % while the remaining variables had values < 1 %. Similarly, pCO₂ had the highest RMSD which suggests that this parameter is not as well represented in the model as the other variables. Furthermore, SIMC1 produced the best TA representation yielding the lowest values for CF, %BIAS and RMSD (Table 3). Moreover, SIMC1 produced an annual mean-TA that was closest to the observations. While the SIMC0 and Eco3m-CarbOx results are fairly similar. SIMC0 produced a slightly better representation of TA compared to Eco3m-CarbOx. Similar conclusions can be drawn for pH_T where SIMC1 also outperformed SIMC0 based on CF and %BIAS (Table 3). For studying DIC and pCO₂, the situation is less clear as the simulations performed differently for different indicators, making it difficult to pick a clear winner. Still SIMC1 shows the best CF and RMSD values for DIC, and the best CF and %BIAS for pCO₂. In conclusion, SIMC1 shows the best overall indicator values for the examined variables (more specifically, it outperformed the other simulations in 9 of 12 indicator comparisons).]

to: [For statistical indicators, %BIAS values are systematically lower than 10 %, with the highest values obtained for pCO₂ with ~6 % while the remaining variables had values < 1 %. Similarly, pCO₂ had the highest RMSD, AAE and AE which suggests that this parameter is not as well represented in the model as the other variables. Furthermore, SIMC1 produced the best TA representation resulting in the lowest values for %BIAS, AE, AAE and RMSD (Table 3). Moreover, SIMC1 produced an annual mean-TA that was closest to the observations. While the SIMC0 and Eco3m-CarbOx results are fairly similar. SIMC0 produced a slightly better representation of TA compared to Eco3m-CarbOx (%BIAS, AE, AAE and RMSD slightly lower). For pH_T, SIMC1 outperformed SIMC0 based on %BIAS (Table 3), however, AE, AAE and RMSD values are similar for the three simulations. We then performed the calculation

of statistical indicators on H^+ concentration as, according to some authors (Kwiatkowski & Orr, 2018), comparing H^+ concentrations is a better practice than comparing pH. Results are available in Appendix C. Based on Table C1, SIMC1 also outperformed SIMC0 based on AE and AAE. For studying DIC and pCO_2 , the situation is less clear as the simulations performed differently for different indicators, making it difficult to pick a clear winner. Still SIMC1 shows the best AAE and RMSD values for DIC, and the best %BIAS, AE, and AAE for pCO_2 . In conclusion, SIMC1 shows the best overall indicator values for the examined variables (more specifically, it outperformed the other simulations in 13 of 20 indicator comparisons when including H^+ concentrations comparison).]

Table 3, Page 14: If the variance of the observed TA and DIC values is on the order of 20 micromol/kg (note, units should be given in the table), then I'd say a RMSD of about the same order of magnitude is not an excellent agreement. It is not terrible either, though. A similar remark holds for %BIAS.

We hope that modifications mentioned above allow to clarify this point. We indicated units in the caption of Table 3.

Figure 4, page 12: The time-series of the difference between the model runs (right panel) does not convey much new information, I would remove them.

We represented the differences between simulations as we think that it allows to better visualize them and then emphasize the fact that modifying TA formulation yields different model outputs for DIC, pCO_2 and pH_T . Considering that, we decided to keep the figure 4 as is.

Also, I have a question to the data (crosses in Figure 4): to me it is not clear whether all four carbon system variables were measured independently, or whether e.g. DIC and TA were measured, and pH and pCO_2 calculated from them. If they were measured independently, how consistent are they with respect to each other, given the used set of carbon system equations?

DIC and TA are measured, and we calculate pH_T and pCO_2 by using CO2SYSv3 (Sharp et al., 2020, originally developed by Lewis and Wallas (1998)) on MATLAB. The set of constants used is the same than the one used to perform the calculation of pH_T and pCO_2 in the model.

Figure 5, page 15: The subpanels on the right are simply a cutout of the panels on the left for the summer period. What is the purpose of this duplicated information?

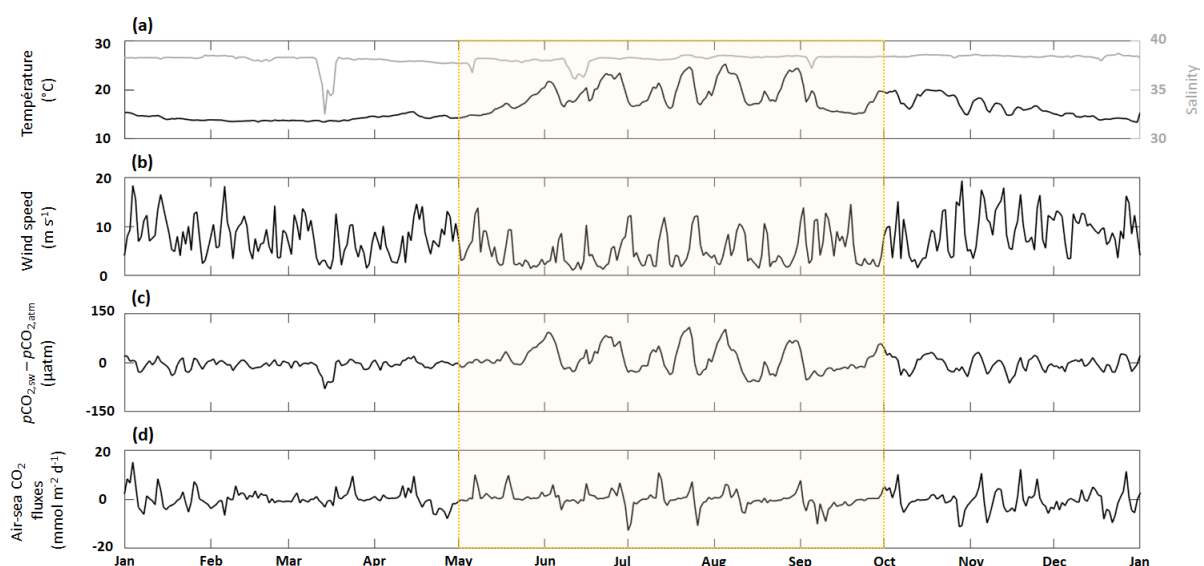


Figure 5: Time series of (a) in situ daily average sea surface temperature (black line) and salinity (grey line) (b) SIMC1 daily average wind speed (c) the difference between SIMC1 daily average seawater

$p\text{CO}_2$ and in situ daily average atmospheric $p\text{CO}_2$ (d) SIMC1 daily average air-sea CO_2 fluxes (aeration process). The summer upwelling period (from 1 May to 1 October) is highlighted in yellow.

We wanted to highlight the SUP, we agree that these panels do not bring more information and that left panel are pretty clear so we modified Figure 5 by deleting the right panels and highlighted the SUP in yellow on left panels.

Page 21, Lines 506 ff: Would including the DIC and nutrient input from upwelling improve the model-data agreement, or the converse?

As indicated in point 2), in our configuration, we can consider these inputs in two ways: by using a relation with salinity or by using an interpolation of SOLEMIO measurements which is then read by the model. For DIC, both methods do not give satisfactory results. For nutrients, we used the second methods in Barré et al. (2023a). In both cases, it is difficult to directly test (through a simulation which take them into account) their effect on model-data agreement. However, to answer your question, we propose the followings hypotheses based on DIC and nutrients measurements study. We represent a linear interpolation of SOLEMIO measurements for these variables on figure S5:

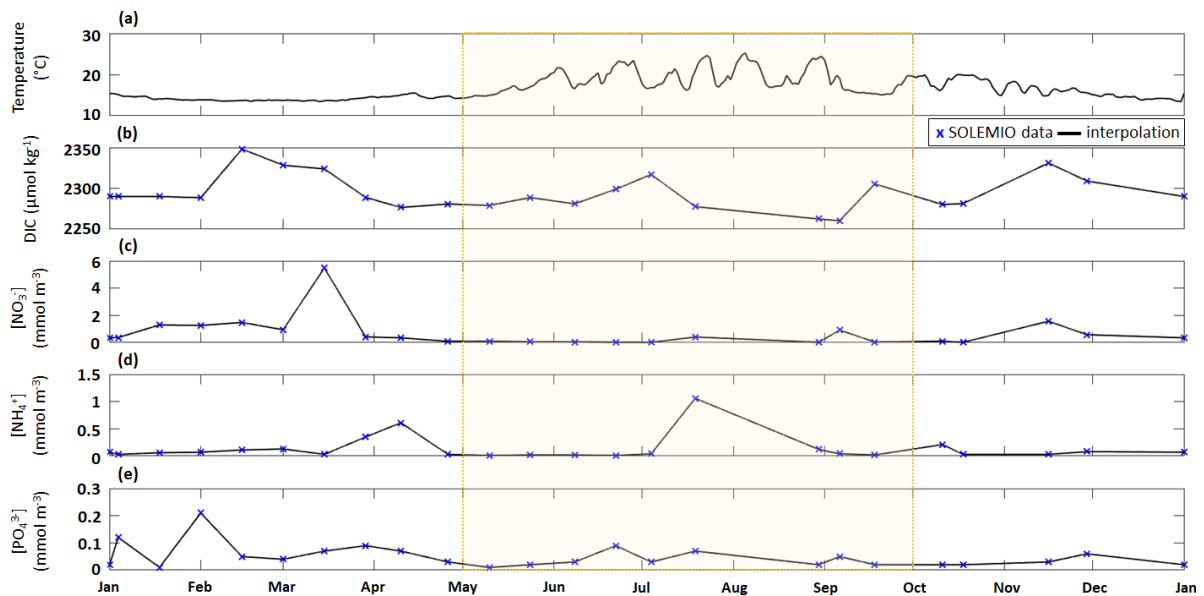


Figure S5: Time series of surface (a) temperature (PLANIER measurements), and interpolated (b) DIC, (c) NO_3^- concentration, (d) NH_4^+ concentration and (e) PO_4^{3-} concentration at SOLEMIO station. SOLEMIO data are represented by blue markers and the SUP is shaded in yellow.

For DIC, during the SUP, measurements show values around $2283 \mu\text{mol kg}^{-1}$ (mean of DIC measurements during the SUP). All upwellings of the period do not necessarily impact DIC. Only two events are noticeable: at the beginning of July and mid-September. These two events do not seem to be correlated with LSE, or Cortiou water inputs (generally associated with high NH_4^+ concentrations). The first event is not reproduced by the model, we then assume that this DIC increase could be associated with an upwelling event. However, the second one is well reproduced by the model which means that it is not resulting from an upwelling input (as, for now, we do not take these inputs into account in the model) (Fig. 4 of the manuscript). Considering these results, we believe that adding DIC inputs from upwelling could improve the realism of our representation, and consequently the data-model agreement.

For nutrients, it clearly appears that during the SUP, their dynamics are only slightly affected by upwelling events as nutrients concentrations remain close to 0 for most of the time. Only two nutrient inputs are noticeable during the SUP: in July and September. However, these events do not correspond to upwellings as the first one is associated with Cortiou water which reaches SOLEMIO (high NH_4^+ concentration) and the second one is, as showed in the manuscript associated with a Rhône River intrusion. This low impact can be explained by the fact that, when the upwelling takes place, nutrients which are upwelled are quickly consumed by the phytoplankton present in the area, then not reaching the station. Considering these results, we suppose that taking into account nutrients inputs associated with upwelling events could improve the model data agreement as it might bring some more realism to our representation, but not enough to consider them here, as their impact at the station is quite limited.

To conclude, we think that considering upwelling inputs could be a great addition to improve the realism of our representation and then the model-data agreement, especially for DIC, however, considering that, in the present configuration, these contributions can hardly be taken into account, we believe that switching to a 3D configuration will be the most appropriate way to confirm this.

Page 22, Line 530ff: Can one give a conjecture why the model overestimates $p\text{CO}_2$ during winter?

We already explained why the model overestimates $p\text{CO}_2$ during winter l.535: [Seawater $p\text{CO}_2$, air-sea CO_2 fluxes and DIC are closely connected (Appendix B, Fig. 3). In Eco3M_MIX-CarbOx, aeration is simulated by applying Eq. (5) to 1 m^3 of surface water at SOLEMIO station which tends to overestimate the impact of aeration process on DIC and, due to the close link between DIC and $p\text{CO}_2$, also on $p\text{CO}_2$].

As seawater $p\text{CO}_2$ calculation is closely linked to air-sea CO_2 fluxes and DIC, we can assume that, when we tend to overestimate the impact of aeration process on DIC, we then impact $p\text{CO}_2$ and also overestimate it in winter.

Technical comments:

Thank you for this, we take them into account.

References:

Allen, J. I., Holt, J. T., Blackford, J. and Proctor, R.: Error quantification of a high-resolution coupled hydrodynamic ecosystem coastal-ocean model: Part 2. Chlorophyll-a, nutrients and SPM, Journal of Marine Systems, 68, 381-404, <https://doi.org/10.1016/j.jmarsys.2007.01.005>, 2007.

Barré, L., Diaz, F., Wagener, T., Van Wambeke, F., Mazoyer, C., Yohia, C. and Pinazo, C.: Implementation and assessment of a model including mixotrophs and the carbonate cycle (Eco3M_MIX-CarbOx v1.0) in a highly dynamic Mediterranean coastal environment (Bay of Marseille, France) (Part I): Evolution of ecosystem composition under limited light and nutrient conditions, <https://doi.org/10.5194/gmd-16-6701-2023>, 2023.

Fraysse, M., Pairaud, I., Ross, O. N., Faure, V. M. and Pinazo, C.: Intrusion of Rhone River diluted water into the Bay of Marseille: Generation processes and impacts on ecosystem functioning, Journal of Geophysical Research: Oceans, 119, <https://doi.org/10.1002/2014JC010022>, 2014.

Kwiatkowski, L. and Orr, J. C.: Diverging seasonal extremes for ocean acidification during the twenty-first century, Nature Climate Change, 8(2), 141-145, 2018.

Lajaunie-Salla, K., Diaz, F., Wimart-Rousseau, C., Wagener, T., Lefevre, D., Yohia, C., Xueref-Remy, I., Nathan, B., Armengaud, A., and Pinazo, C.: Implementation and assessment of a carbonate system

model (Eco3m-CarbOx v1.1) in a highly dynamic Mediterranean coastal site (Bay of Marseille, France), *Geoscience Model Development*, 14, 295–321, <https://doi.org/10.5194/gmd-14-295-2021>, 2021.

Lewis, E. and Wallace, D. W. R.: Program developed for CO₂ system calculations, 1998.

Maréchal, D.: A soil-based approach to rainfall-runoff modelling in ungauged catchments for England and Wales, Ph.D. Thesis, Cranfield University, 157pp, 2004.

Radach, G. and Moll, A.: Review of three-dimensional ecological modelling related to the North Sea shelf system. Part II: model validation and data needs, *Oceanography and Marine Biology*, 44, 1–60, 2006.

Sharp, J. D., Pierrot, D., Humpbreys, M. P., Epitalon, J. -M., Orr, J. C., Lewis, E. R. and Wallace, D. W. R.: CO2SYSv3 for MATLAB (v3.0.1). Zenodo [code] <https://doi.org/10.5281/zenodo.3952803>, 2020.

Schneider, A., Douglas, W. R. W. and Körtzinger, A.: Alkalinity of the Mediterranean Sea, *Geophysical Research Letters*, 34, <https://doi.org/10.1029/2006GL028842>, 2007.

Stow, C. A., Jolliff, J., McGillicuddy Jr, D. J., Doney, S. C., Allen, J. I., Friedrichs, M. A., Rose, K. A. and Wallhead, P.: Skill assessment for coupled biological/physical models of marine systems, *Journal of Marine Systems*, 76(1-2), 4-15, 2009.

Wimart-Rousseau, C., Lajaunie-Salla, K., Marrec, P., Wagener, T., Raimbault, P., Lagadec, V., Lafont, M., Garcia, N., Diaz, F., Pinazo, C., Yohia, C., Garcia, F., Xueref-Remy, I., Blanc, P. E., Armengaud, A., and Lefèvre, D.: Temporal variability of the carbonate system and air–sea CO₂ exchanges in a Mediterranean human-impacted coastal site, *Estuar. Coast. Shelf S.*, 236, <https://doi.org/10.1016/j.ecss.2020.106641>, 2020.