Introducing Graupel Density Prediction in Weather Research and Forecasting (WRF) Double-Moment 6-Class (WDM6) Microphysics and Evaluation of the Modified Scheme During the ICE-POP Field Campaign

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Abstract

The Weather Research and Forecasting (WRF) Double-Moment 6-class (WDM6) scheme was modified by incorporating predicted graupel density. Explicitly predicted graupel density, in turn, modifies graupel characteristics such as the fall velocity–diameter and mass–diameter relationships of graupel. The modified WDM6 has been evaluated based on a two-dimensional (2D) idealized squall line simulation and winter snowfall events that occurred during the International Collaborative Experiment for Pyeongchang Olympics and Paralympics (ICE-POP 2018) field campaign over the Korean Peninsula. From the 2D simulation, we confirmed that the modified WDM6 can simulate varying graupel density, ranging from low values in an anvil clouds region to high values in the convective region at the mature stage of a squall line. Simulations with the modified WDM6 increase graupel amounts at the surface and decreased graupel aloft because of the faster sedimentation of graupel for two winter snowfall cases during the ICE-POP 2018 campaign, as simulated in the 2D idealized model. The altered graupel sedimentation in the modified WDM6 influenced the magnitude of the major microphysical processes of graupel and snow, subsequently reducing the surface snow amount and precipitation over the mountainous region. The reduced surface precipitation over the mountainous region mitigates the surface precipitation bias observed in the original WDM6, resulting in better statistical skill scores for the root mean square errors. Notably, the modified WDM6 reasonably captures the relationship between graupel density and its fall velocity, as retrieved from 2D video disdrometer measurements, thus emphasizing the necessity of including predicted graupel density to realistically represent the microphysical properties of graupel in models.

1. Introduction

Over the past decades, the parameterization of ice microphysics traditionally represents ice-phase particles as pre-defined categories of solid-phase hydrometeors in bulk-type cloud microphysics (Lin et al., 1983; Rutledge and Hobbs, 1983; Cotton et al., 1986; Ferrier 1994; Meyers et al., 1997; Thompson et al., 2004; Hong and Lim, 2006; Seifert and Beheng, 2006; Morrison et al., 2009), bin-type cloud microphysics schemes (Reisin et al., 1996; Geresdi 1998; Khain et al., 2004; Lebo and Seinfeld, 2011) and Lagrangian ”Super particle” microphysics schemes (Grabowski et al., 2019; Morrison et al., 2020; Shima et al., 2020). Solid-phase hydrometeors in cloud microphysics schemes are classified into typical particle types, such as ice crystals, aggregates, graupel and hail. Each category of hydrometeors is characterized by static parameters defining density, diameter–mass relationship and diameter–fall velocity relationship, which are expressed differently in each microphysics scheme. Several studies reported that the simulated convection was considerably sensitive to the manner of categorization of solid-phase hydrometeors (Morrison and Milbrandt, 2011; Bryan and Morrison, 2012; Adams-Selin et al., 2013). Morrison and Milbrandt (2011) demonstrated that different approaches in treating graupel or hail produce distinct differences in storm structure, precipitation, and cold pool strength for idealized supercells. This is because graupel leads to more anvil condensate and weaker cold pool compared to hail. Bryan and Morrison (2012) showed that the fall velocities of graupel and hail affect the simulated reflectivity and dynamics for an idealized squall line. Simulations with graupel instead of hail produce convective regions that are too wide and have lower reflectivity, primarily due to the slower fall velocity of graupel compared to hail. Adams-Selin et al. (2013) reported that the development of a bow echo is highly sensitive to the parameters defining the fall velocities of graupel and hail. The simulations with slower-falling graupel-like particle created a wider stratiform region and stronger cold pool, allowing for more melting and evaporation, which helped generating bowing segments earlier than in the faster-falling hail-like simulations.

Since the study of Wisner et al. (1972), research on microphysics schemes has focused on augmenting the parameterisation of cold rain processes by increasing the number of solid-phase categories or introducing new prognostic variables for these categories (Cotton et al., 1986; Ferrier 1994; Reisner et al., 1998; Milbrandt and Yau, 2005; Bae et al.,

2019). More recently, modeling approaches have evolved toward ways of predicting solid-phase characteristics or considering various shapes of ice crystals (Morrison and Grabowski, 2008; Mansell et al., 2010; Milbrand and Morrison, 2013; Morrison and Milbrandt, 2015; Jensen et al., 2017; Tsai and Chen, 2020; Jensen et al., 2023). Morrison and Grabowski (2008) devised a new method that allows the changing mass−dimension and projected-area−dimension relationships of ice particles to evolve according to the predicted rime mass fraction and particle dimension. Mansell et al. (2010) and Milbrandt and Morrison (2013, hereafter MM13) implemented a new approach of incorporating a prognostic graupel density. By advancing the study of MM13, Morrison and Milbrandt (2015) later developed the Predicted Particle Properties (P3) bulk microphysics scheme that predicts the rime mass fraction and rime density for a single generic ice-phase category. Meanwhile, Jensen et al. (2017) introduced the Ice-Spheroids Habit Model with Aspect-ratio Evolution (ISHMAEL) bulk microphysics scheme, which predicts the evolution of the ice-particle aspect ratio for two ice species, namely, planar-nucleated and columnar-nucleated particles. Chen and Tsai (2020) proposed a bulk-type microphysics scheme that allows variations in the shape and density of solid-phase hydrometeors. Recently, Jensen et al. (2023) implemented a prognosed density graupel category into the Thompson–Eidhammer scheme (Thompson and Eidhammer, 2014), following the approach of Mansell et al. (2010) and MM13.

Various studies demonstrated the merits of considering the prognostic density of solid-phase hydrometeors when simulating convective storms (Johnson et al., 2016; Jouan and Milbrandt, 2019) Johnson et al. (2016) evaluated the reproducibility of the polarization signatures in supercell storms for several partially or fully two-moment (2M) schemes. Realistic signatures were obtained only with those microphysics schemes that predicted graupel density. Predicted graupel density assigns high-density frozen drops to the graupel category, resulting in relatively high-density graupel that can later grow into hail. These differences in the treatment of rimed-ice processes allow hail to grow larger and produce a much more prominent hail signature. Jouan and Milbrandt (2019) demonstrated that variations in the simulated storm reflectivity and precipitation structure exhibit more pronounced differences when using predicted particle density instead of a fixed particle density in the 2M scheme, particularly related to different number concentrations of cloud condensation nuclei (CCN) in a mid-latitude continental squall line. Since CCN concentration affects cloud droplet number concentration and mean droplet diameter, the model's microphysical response depends on how well parameterized processes involving the ice phase account for droplet size effects. Mean droplet size impacts graupel growth directly through the collection efficiency between graupel and droplets. Additionally, predicted graupel density influences graupel growth by increasing graupel fall speeds and enhancing accretion rates. Based on their analysis, they suggested that an accurate representation of graupel in microphysics schemes is crucial for appropriately simulating the effects of changes in the concentration of cloud condensation nuclei in selected systems.

The Weather Research and Forecasting (WRF) Double-Moment 6-class (WDM6) scheme (Lim and Hong, 2010), a bulk-type microphysics scheme, has been widely evaluated for predicting deep convective precipitation in summer season (Min et al., 2015; Song and Sohn, 2018; Kim et al., 2022) and snowfall events in winter season (Liu et al., 2011; McMillen and Steenburgh, 2015; Morrison et al., 2015; Comin et al., 2018; Lim et al., 2020; Ko et al., 2022). Several studies showed that the WDM6 scheme produces excess graupel compared to other microphysics schemes during the summer and winter seasons. Li et al. (2019) showed that the simulated precipitation exhibits significant sensitivity to changes in graupel density in the WDM6 scheme. Specifically, a lower-graupel density tends to contribute more to one-month precipitation amounts below 100 mm and less to those above 100 mm during the autumn season. Conversely, a higher-graupel density shows the opposite pattern. Recognizing the sensitivity and importance of the representation of graupel to simulate precipitation, we introduced a new prognostic variable, the graupel volume mixing ratio, to predict graupel density based on the study of MM13. The impact of the modified WDM6 scheme on the simulated convections was evaluated through a two-dimensional (2D) idealized squall line experiment and by considering snowfall events that occurred during the International Collaborative Experiment for Pyeongchang Olympics and Paralympics (ICE-POP 2018) field campaigns over the Korean Peninsula. The

novelty of our study lies in comparing the simulated graupel characteristics in the WDM6 scheme with the specialized observed data during ICE-POP 2018.

The remainder of this paper is organized as follows. Section 2 explains the implemented method of the new prognostic variable, namely, the graupel density. The experimental setups, including the case description, model setup and observations for verification, are described in Section 3. The results and a summary are provided in sections 4 and 5, respectively.

2. New prediction variable (graupel density) in the WDM6 scheme

In the original WDM6 scheme, characteristics of hydrometeors are pre-defined using the static value of density (ρ_X), constant coefficients for the mass (M_X)–diameter (D) and fall velocity (V_X)–D relationships. Here, X represent the species of hydrometeors including cloud water, rain, cloud ice, snow, and graupel. The specific values of parameters are available in Table A1 of the Appendix. In the WDM6 scheme, 'snow' is defined as an unrimed ice phase (large crystals-aggregates) with a standard density of 100 kg m^{-3}, indicating that it does not undergo riming. Conversely, 'graupel' is characterized as heavily rimed crystal particles that have not undergone wet growth. In nature, graupel has a wide range of densities according to the degree of riming. However, the original WDM6 scheme is unable to simulate this variability in graupel density as it undergoes riming because it uses a predefined constant value for graupel density. This study introduces a prognostic variable, namely, the volume mixing ratio (B_G). B_G varies dynamically in both time and space, reflecting the formation and growth mechanisms of graupel. The conservation equation for B_G is given by

$$\frac{\partial B_G}{\partial t} = -\vec{V} \cdot \nabla_3 B_G - \frac{1}{\rho_a}\frac{\partial}{\partial z}\left(\rho_a B_G V_{B_G}\right) + S_{B_G}, \quad (1)$$

The first, second and third terms on the right-hand side of Eq. (1) represent the 3D advection, sedimentation of B_G and sources and sinks of B_G (S_{B_G}). $\vec{V}$ and V_{B_G}represent the three-dimensional 3D wind fields and the B_G-weighted mean terminal velocities of graupel, respectively; ρ_a is the air density. S_{B_G} comprises several microphysical source/sink processes for mass mixing ration of graupel (q_G) and density of specific hydrometeors (ρ_X), as defined in Eq. (2).

$$S_{B_G} = \begin{cases} \frac{Piacr}{\rho_R} + \frac{Praci}{\rho_I} + \frac{Pracs}{\rho_S} + \frac{Psacr}{\rho_R} + \frac{Pgaci}{\rho_I} + \frac{Pgacw}{\rho_R} + \frac{Psacw}{\rho_R} + \frac{Pgacr}{\rho_R} + \frac{Pgdep}{\rho_G} + \frac{Pgfrz}{\rho_R} & (T < T_0) \\ \frac{Pgmlt}{\rho_G} + \frac{Pgeml}{\rho_G} + \frac{Pgevp}{\rho_G} & (T \geq T_0) \end{cases}. \quad (2)$$

The meanings of the microphysical processes in Eq. (2) are summarized in Table 1, and their detailed descriptions are available in the literature (Appendix B of Park and Lim, 2023). Meanwhile, ρ_G can be predicted once q_G and B_G are updated using Eq. (3).

$$\rho_G = \frac{q_G}{B_G}. \quad (3)$$

Table 1. Meanings of the microphysical source/sink processes in Eq. 2.

Symbol	Meaning	SI unit
Paacw	Production rate for accretion of cloud water by snow or graupel	$kg\,kg^{-1}\,s^{-1}$
Pgaci	Production rate for accretion of cloud ice by graupel	$kg\,kg^{-1}\,s^{-1}$
Pgacr	Production rate for accretion of rain by graupel	$kg\,kg^{-1}\,s^{-1}$

Pgacw	Production rate for accretion of cloud water by graupel	$kg\,kg^{-1}\,s^{-1}$
Pgdep (Pgsub)	Production rate for deposition (sublimation) rate graupel	$kg\,kg^{-1}\,s^{-1}$
Pgeml	Production rate induced by enhanced melting of graupel	$kg\,kg^{-1}\,s^{-1}$
Pgevp	Production rate for evaporation of melting graupel	$kg\,kg^{-1}\,s^{-1}$
Pgfrz	Production rate for freezing of rainwater to graupel	$kg\,kg^{-1}\,s^{-1}$
Pgmlt	Production rate for melting of graupel to form rain	$kg\,kg^{-1}\,s^{-1}$
Piacr	Production rate for accretion of rain by cloud ice (graupel)	$kg\,kg^{-1}\,s^{-1}$
Praci	Production rate for accretion of cloud ice (graupel) by rain	$kg\,kg^{-1}\,s^{-1}$
Pracs	Production rate for accretion of snow by rain	$kg\,kg^{-1}\,s^{-1}$
Psacr	Production rate for accretion of rain by snow	$kg\,kg^{-1}\,s^{-1}$
Psacw	Production rate for accretion of cloud water by snow	$kg\,kg^{-1}\,s^{-1}$

The M_G–D relationship can be expressed as $M_G(D) = c_G D^{d_G}$. Here, c_G and d_G are set as $\frac{\pi\rho_G}{6}$ and 3.0, respectively, because the graupel is assumed to be a sphere in the original WDM6 scheme. Further, c_G is treated as a constant since ρ_G in the original WDM6 scheme is set as a constant (500 kg m^{-3}). In our modified WDM6, c_G varies with the predicted ρ_G (Eq. (3)). The coefficients of the area (A_G)–D relationship ($A_G = \gamma D^{\sigma}$), γ and σ, are set to $\frac{\pi}{4}$ and 2.0, respectively due to the sphere-shaped graupel in the WDM6 scheme. Meanwhile, Mitchell (1996) addressed that the Reynolds number (Re)–Best number (χ) relationship produces the power-law expressions of fall velocity according to ice particle types based on the relationships of mass and projected area with the dimensions as Eq. (5).

$$Re = a_1 \chi^{b_1}, \tag{5}$$

The Re–χ relationship was further refined by Khvorostyanov and Curry (2002) to derive the continuous power law of ice-particle dimension by adopting varying drag terms (a_1 and b_1) (Eqs. (6) and (7)).

$$a_1 = \frac{C_2[(1+C_1\chi^{1/2})^{1/2}-1]^2}{\chi}, \tag{6}$$

$$b_1 = \frac{C_1\chi^{1/2}}{2[(1+C_1\chi^{1/2})^{1/2}-1](1+C_1\chi^{1/2})^{1/2}}. \tag{7}$$

The non-dimensional surface roughness parameters, namely C_1, C_2, δ_0 and C_0, in Eqs. (6) and (7) are assumed as $4/(\delta_0{}^2 C_0{}^2)$, $\delta_0{}^2/4$, 5.83 and 0.6, respectively. The Best number, χ, is expressed as a function of ρ_G shown in Eq. (8).

$$\chi = \frac{4\,\rho_G\,g\,\rho_a\,D_{GM}{}^3}{3\,\eta^2}, \tag{8}$$

where g is the acceleration due to gravity, and η represents the dynamic viscosity. D_{GM} is the maximum dimension of the graupel. Eq. (9) represents the V_G–D relationship.

$$V_G = a_G D^{b_G}, \tag{9}$$

Here, a_G and b_G are derived from the study of Mitchell and Heymsfield (2005). By assuming the shape of graupel as a sphere, a_G and b_G can be expressed as shown in Eqs. (10) and (11).

$$a_G = a_1 v^{(1-2b_1)} \left(\frac{2\, c_G\, g}{\rho_a\, \gamma}\right)^{b_1}, \quad (10)$$

$$b_G = b_1(c_G - \sigma + 2) - 1, \quad (11)$$

where v is the kinematic viscosity of air. Further, c_G and d_G represent the coefficients of the M_G–D relationship, while γ and σ are the coefficients of the A_G–D relationship, respectively. Note that a_1 and b_1 can be obtained from Eqs. (6) and (7).

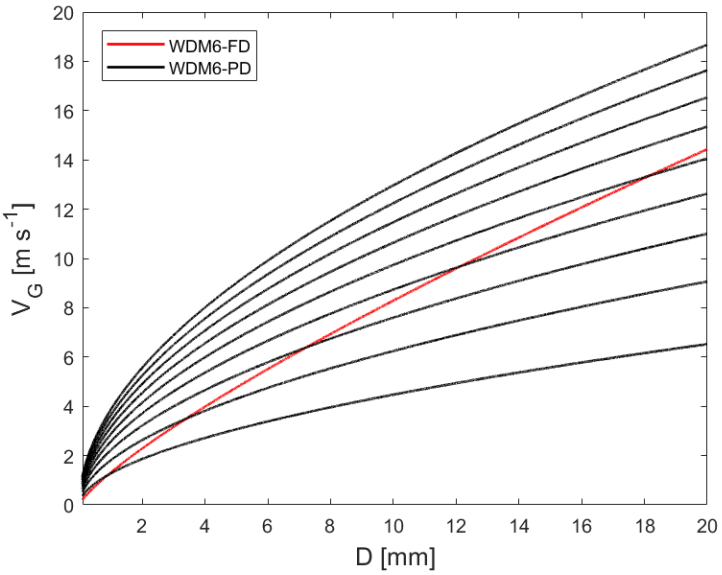
a_G and b_G in the V_G–D relationship are derived at the predicted ρ_G, which is in the range of 100–900 kg m^{-3}, at intervals of 100 kg m^{-3} to facilitate the transition between aggregate and rime particles (Straka and Mansell, 2005), using the least-squares method in a log–log space over a range of D_G of 0.3–20 mm (Table 2). Therefore, the modified WDM6 incorporates varying a_G and b_G parameters in the V_G–D relationship and c_G in the M_G–D relationship by implementing predicted graupel density. Note that the coefficients, a_G and b_G, are assumed as 330 m^{1-b} s^{-1} and 0.8 in the original WDM6 scheme and these values differ significantly from those in Table 2. However, we adhere to the methodology presented in Milbrandt and Morrison (2013) to preserve the originality of the method.

The several microphysics processes in the WDM6 can be affected by the newly derived V_G–D and M_G–D relationships. The microphysical processes of Pgmlt, Pgacw, Pgdep, Pgevp, and Ngacw are affected by a_G and b_G in the V_G–D relationship and Pgmlt, Pgaci, Pgacr, Pgdep, Pgevp, Pgacw, Ngaci, Ngacr, Ngeml, and Ngacw are affected by c_G in the M_G–D relationship. Since these processes act as source/sink for both mass mixing ratio and number concentration of cloud water, rain, cloud ice, snow, and graupel (Fig. A1 in the appendix), varying parameters with predicted graupel density can affect the mass mixing ratio and number concentration of liquid-phase hydrometeors as well as solid-phase hydrometeors. Figure 1 shows the retrieved V_G–D relationship in the modified WDM6 with ρ_G varying from 100 to 900 kg m^{-3}. The newly retrieved relationship can represent the wide range of V_G with varying ρ_G and D, unlike the relationship in the original WDM6. The modified scheme is an extension of the WDM6 scheme, and it is incorporated with the prognostic cloud ice number concentration (Park and Lim, 2023).

Table 2. Fitted parameters of a_G and b_G in the graupel fall velocity (V_G)–diameter (D) relationship with varying graupel density (ρ_G) (Eq. 9).

ρ_G (kg m^{-3})	a_G (m^{1-b} s^{-1})	b_G
100	54.9153	0.5446
200	74.2262	0.5375
300	88.8313	0.5339
400	101.0411	0.5316
500	111.7359	0.5299
600	121.3625	0.5286
700	130.1841	0.5275
800	138.3714	0.5266
900	146.0422	0.5258

Figure 1: V_G (m s^{-1}) as a function of D (mm) with various ρ_G between 100 and 900 (kg m^{-3}), utilizing a_G and b_G values from Table 2. The V_G–D relationship in the original WDM6 scheme (WDM6_FD) is shown by a red line.



3. Experimental setup

3.1 Case description and model setup

3.1.1 Two-dimensional idealized squall line

The experimental design for the 2D idealized squall line simulation follows that of the study conducted by Lim and Hong (2010). A warm bubble with a 4 km radius and a maximum perturbation of 3 K at the centre of the domain drives the convection. A wind of 12 m s^{-1} is applied in the positive x direction at the surface, and it decreases to zero at a height of 2.5 km above the ground; there is no wind above this level. Additionally, no Coriolis force or friction is added, and an open boundary condition is applied for the simulation. By using the fixed initial conditions and considering only cloud microphysics parameterisation as the physical option, the impact of predicted graupel density on the simulated squall line can be distinguished and identified. The grid in the x direction comprises 601 points with a grid spacing of 1 km, and 80 vertical layers are configured. The model integration duration is 6 h with a time step of 5 s.

3.1.2 Snowfall during the ICE-POP field campaign

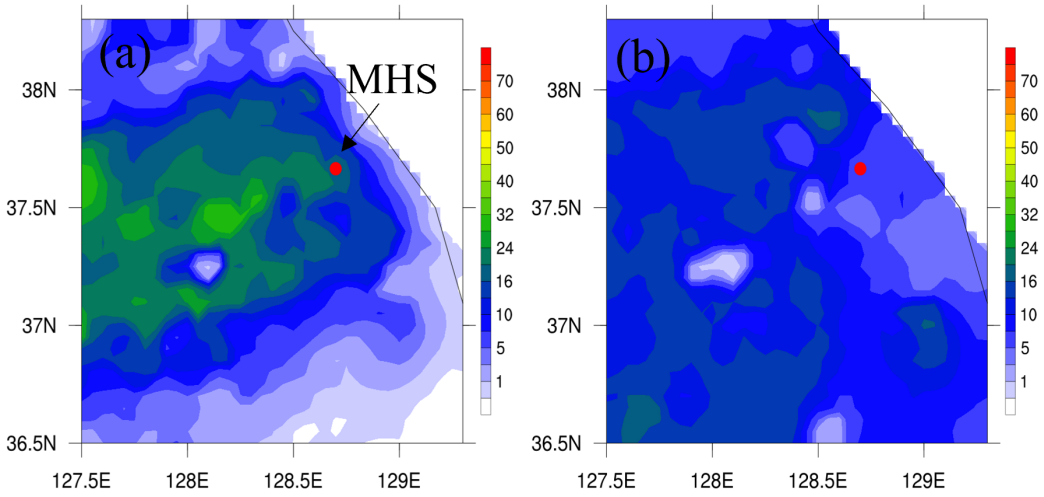
Eight snowfall events were observed during the ICE-POP field campaign period. These events can be classified into three categories (cold low, CL; warm low, WL; and air–sea interaction) according to the synoptic characteristics (Jeoung et al., 2020). Ko et al. (2022) used these eight events to compare the performances of various bulk-type microphysics schemes in simulating snowfall events. In this study, we also selected eight identical cases, following Ko et al. (2022). Table 3 lists the model forecast and analysis periods, synoptic features and observed accumulated precipitation (mm) for each simulation case during the analysis period. For an in-depth analysis, we selected cases 1 and 2 as the representative examples for the CL and WL categories because these two cases exhibit the most representative features of precipitation distribution for each category. Although Case7 is listed in Table 3 as an air-sea interaction event, it is not selected for detailed analysis because only one event from this category was identified during the ICE-POP field campaign. Further details regarding the characteristics of each category are provided in literature (Jeoung et al., 2020; Kim et al., 2021).

Table 3. Forecast and analysis periods of the selected snowfall events during International Collaborative Experiment for Pyeongchang Olympics and Paralympics (ICE-POP 2018) field campaign. The observed precipitation (mm) during the analysis period, obtained from the automatic weather station (AWS) by the Korea Meteorological Administration (KMA), and the synoptic features of the cases, addressed in previous studies (Jeoung et al., 2020; Ko et al., 2022) are noted.

Case	Forecast Period (UTC)	Analysis period (UTC)	Synoptic Feature	Observed precipitation (mm)
Case1	11.24.2017. 12:00 ~ 11.26.2017. 12:00	11.24.2017. 20:00 ~ 11.26.2017. 00:00	Cold Low	32.09
Case2	12.23.2017. 12:00 ~ 12.24.2017. 18:00	12.23.2017. 20:00 ~ 12.24.2017. 12:00	Warm Low	18.6
Case3	01.22.2018. 00:00 ~ 01.23.2018. 06:00	01.22.2018. 03:00 ~ 01.23.2018. 00:00	Cold Low	6.03
Case4	02.27.2018. 18:00 ~ 03.01.2018. 00:00	02.27.2018. 23:00 ~ 02.28.2018. 18:00	Warm Low	57.12
Case5	03.04.2018. 00:00 ~ 03.05.2018. 12:00	03.04.2018. 08:00 ~ 03.05.2018. 09:00	Warm Low	55.17
Case6	03.07.2018. 00:00 ~ 03.08.2018. 12:00	03.07.2018. 05:00 ~ 03.08.2018. 10:00	Warm Low	33.07
Case7	03.15.2018. 00:00 ~ 03.16.2018. 00:00	03.15.2018. 08:00 ~ 03.15.2018. 18:00	Air–sea interaction	25.52
Case8	03.20.2018. 12:00 ~ 03.21.2018. 18:00	03.20.2018. 18:00 ~ 03.21.2018. 14:00	Warm Low	25.83

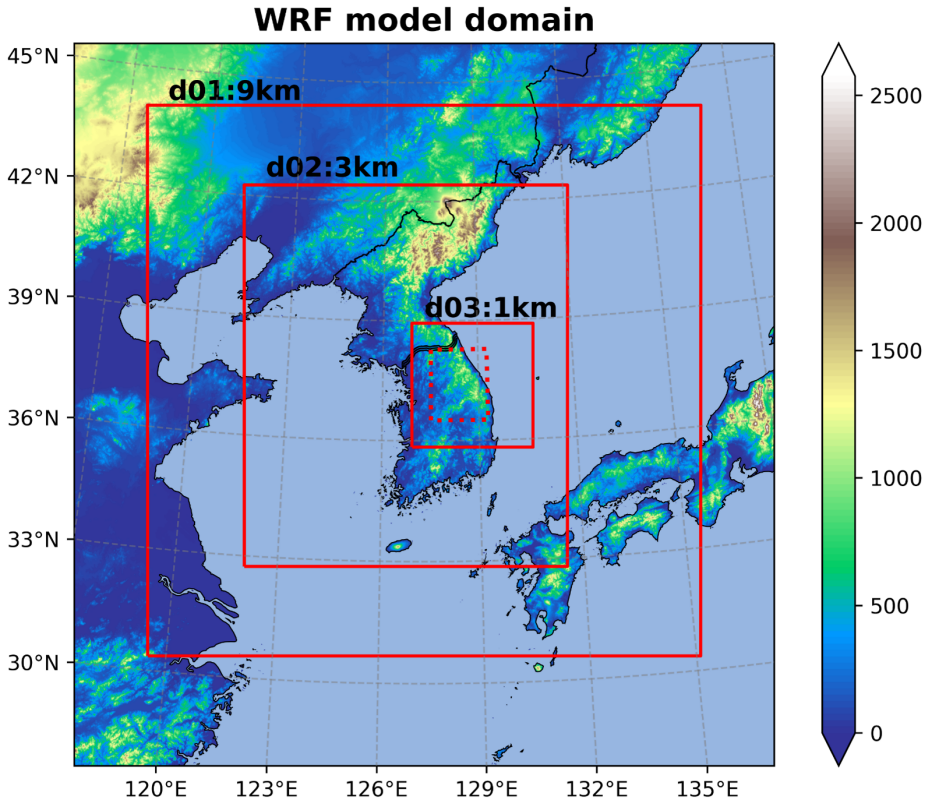
Figure 2 shows the accumulated precipitation amount (mm) obtained from a heated tipping rain gauge at automatic weather station (AWS). The dot in Fig. 2 indicates the location of the MHS (MayHills Supersite; 37.6632°N, 128.6996°E, 289 m mean sea level, MSL), where observation data from a 2D video disdrometer (2DVD) were collected to verify the model simulation results. These data will be explained in Section 3.2 together with the AWS data. In the CL case, the low-pressure region is located to the north of the polar jet stream and crosses over the middle of the Korean Peninsula, leading to significant precipitation in the that region (Fig. 2a). Meanwhile, in the WL case, the low pressure is positioned to the south of the polar jet stream and crosses over the southern part of the Korean Peninsula, heading towards the southeast and resulting in abundant precipitation in the coastal region in the WL case (Fig. 2b).

Figure 2: Accumulated precipitation amount (mm) during the analysis period, obtained from AWS observation for (a) CL and (b) WL cases. The location of the observation site over the mountain, MayHills Supersite (MHS), is marked as a red dot.



The winter snowfall simulations during the ICE-POP 2018 field campaign were conducted using three nested domains (Fig. 3) with a horizontal grid spacing of 9, 3 and 1 km consisting of 170 × 170, 295 × 349 and 331 × 340 grid points, respectively. The model integration applies a one-way nesting. The top layer for the model is placed at 50 hPa, with a total of 65 vertical levels. Different integration time steps are used for each domain: 45 s for D01, 15 s for D02 and 5 s for D03. The ERA–Interim reanalysis data are used from the European Centre for Medium-Range Weather Forecasts (ECMWF) for the initial and boundary conditions (Dee et al., 2011a). For physics parameterisation, the Kain–Fritsch cumulus parameterisation scheme (Kain, 2004) is used and applied only to the outer grid (9 km). The Revised MM5 Monin–Obukhov surface layer (Jiménez et al., 2012) and the Rapid Radiative Transfer Model for General Circulation Models (RRTMG) long- and short-wave radiative schemes (Iacono et al., 2008) are used. For planetary boundary layer schemes and land surface models, Yonsei University (YSU) (Hong et al., 2006) and Noah Multi-Parameterisation (Noah-MP) models (Chen and Dudhia, 2001) are used.

Figure 3: Three nested-model domains with horizontal resolutions of 9, 3 and 1 km with the terrain height (m) (shaded). The dashed box denotes the analysis domain.



3.2 Numerical experiments and observation data for verification

The WRF version 4.1.3 (Skamarock et al., 2008) is used to simulate the 2D-idealized squall line and the wintertime snowfall cases during the ICE-POP 2018 field campaign. Two experiments, named, WDM6_FD and WDM6_PD, are conducted for each case to examine the impact of the predicted graupel density on the simulated convections. WDM6_FD uses the original WDM6 scheme with a fixed density (FD) (Lim and Hong, 2010; Park and Lim, 2023), and WDM6_PD uses the modified WDM6 scheme with predicted density (PD).

To evaluate the simulated precipitation, AWS data, from stations operated by the Korea Meteorological Administration (KMA), are used. South Korea has a total of 604 AWS surface sites. To match the horizontal resolution of the AWS, we interpolate the 1 km model simulation results to a 5 km grid. Additionally, we used the 2DVD measured data of the diameter, fall velocity and geometry of each hydrometeor falling into a sampling area of 100 cm^2 to validate whether the model effectively reproduces the observation-derived density–fall velocity relationship of graupel. Particle fall velocity was directly measured by the 2DVD, but particle density was estimated based on the study of Huang et al. (2015), who adopted the Böhm method (Böhm, 1989) using the observed geometry and the 2DVD fall velocity. This method leverages the capability of the 2DVD to measure individual particles using two orthogonal cameras, making it possible to reliably estimate particle geometry, fall velocity and density. To ensure accurate measurement of the fall velocity, any instances when the collocated anemometer recorded 1-min wind speeds exceeding 3.0 m s^{-1} were excluded from the analysis.

Relying solely on the 2DVD-based particle characteristics makes it challenging to differentiate graupel from other hydrometeors because of the unproven pre-defined assumptions on the shape, diameter and fall velocity of graupel particles in developing a hydrometeor classification algorithm. Therefore, in addition we used a collocated multi-angle snowflake camera (MASC), which captures pictures of each hydrometeor at three different angles, offering significant advantages in identifying the degree of riming and habit classification. The MASC can provide the riming index (0–1) and the complexity

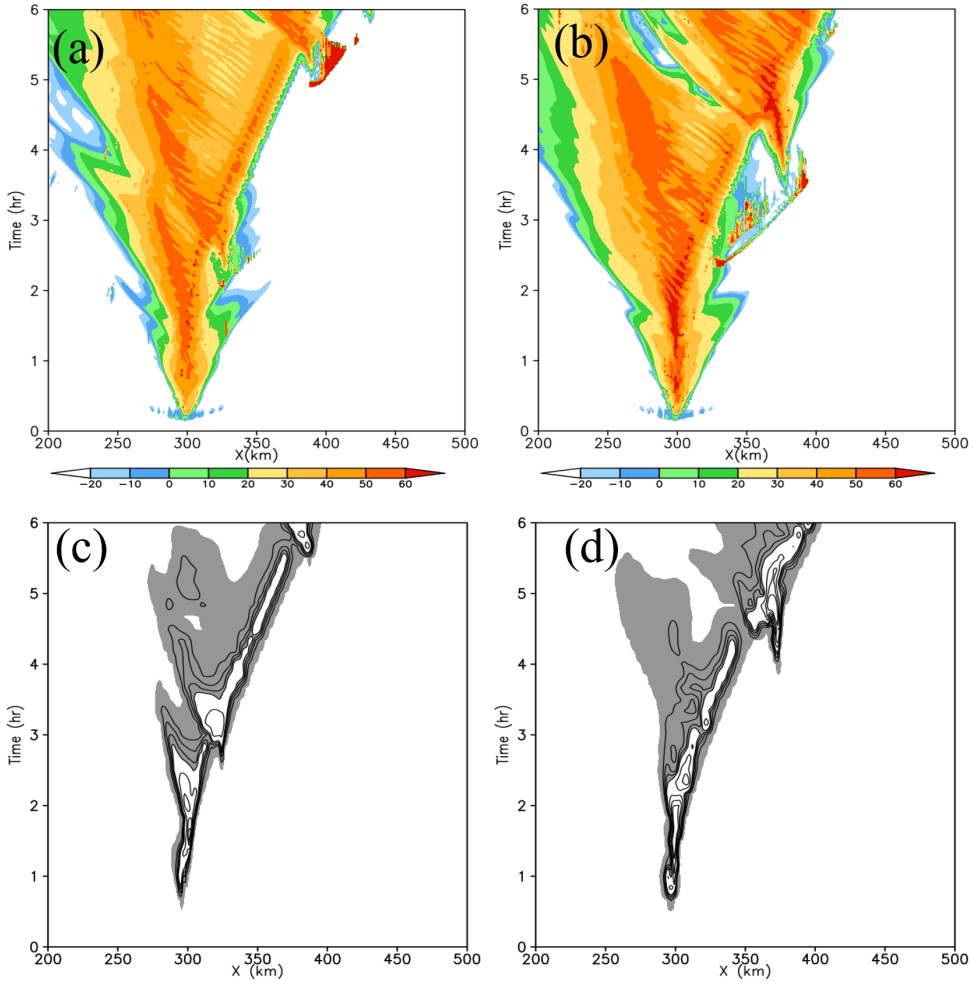
of the particle, which decreases as a particle becomes more spherical. These two parameters are obtained using the hydrometeor classification algorithm (Praz et al., 2017), which determines the riming index by using a pre-trained supervised machine learning model and the computed geometric parameters of each particle. To identify the graupel-dominant period, the following stringent criteria are considered. The 10-min median riming index should be 1, and the 10 min median complexity of the particles should be less than 1.35. Using our criteria, we identified 11,995 graupel particles over an accumulated period of 81 min in Case 6 (Table 3).

4. Results

4.1 Two-dimensional idealized squall line experiment

The Hovmöller plots of the maximum reflectivity and surface rainfall rate for WDM6_FD and WDM6_PD illustrate the typical evolution of a storm associated with squall line development (Fig. 4). The reflectivity is calculated using a simulated equivalent reflectivity factor, which is defined as the sixth moment of the particle size distribution based on the available mass mixing ratios and number concentrations for precipitation species including rain, snow and graupel. Both WDM6_FD and WDM6_PD simulate the strong reflectivity along the convective core region and the trailing weak reflectivity over the stratiform region, which is the general feature of squall lines (Figs. 4a and 4b). WDM6_PD simulates a stronger reflectivity over both, convective and stratiform regions, but compared to WDM6_FD, WDM6_PD simulates lower precipitation activities along the leading edge of the convection before 4 h (Figs. 4c and d).

Figure 4: Maximum reflectivity (dBZ) for WDM6_FD and WDM6_PD are shown in (a) and (b) with the Hovmöller plots of the surface rainfall rate for (c) WDM6 _FD and (d) WDM6_PD. The contour interval is 1 mm/10 min for rates of 0–4 mm/10 min, and 3 mm/10 min for the rates greater than 4 mm/10 min in (c) and (d). The grey regions represent the stratiform rain region receiving precipitation at rates of 0.05–4 mm/10 min.



The vertical distributions of the time-domain-averaged mass mixing ratio of hydrometeors for WDM6_FD and WDM6_PD and the differences between the simulations are presented in Fig. 5. The sum of the mass mixing ratios of snow and graupel is indicated by the red line. The mass mixing ratio of rain increases below the 6 km level, while that of cloud water decreases over the 4–9 km levels in WDM6_PD (Fig. 5c). Additionally, compared to WDM6_FD, WDM6_PD produces a higher snow mass mixing ratio above the 3 km level and a lower graupel mass mixing ratio over the entire layers. Furthermore, in WDM6_PD, the total mass mixing ratio of snow and graupel is lower below the 7 km level and higher above that level (Fig. 5c). Compared to the results of WDM6_FD, the generation of solid-phase hydrometeors is less effective in the lower layers and more effective in the upper layers in WDM6_PD. Meanwhile, the cloud ice mass mixing ratio does not show any remarkable difference between WDM6_FD and WDM6_PD.

Figure 5: Vertical profiles for the time-domain-averaged mass mixing ratios (g kg^{-1}) of hydrometeors for (a) WDM6_FD and (b) WDM6_PD. In (a) and (b), the cloud ice mass mixing ratio (q_I) is multiplied by 10. The difference between the mass mixing ratios (g kg^{-1}) of WDM6_PD and WDM6_FD (WDM6_PD minus WDM6_FD) is plotted in (c).

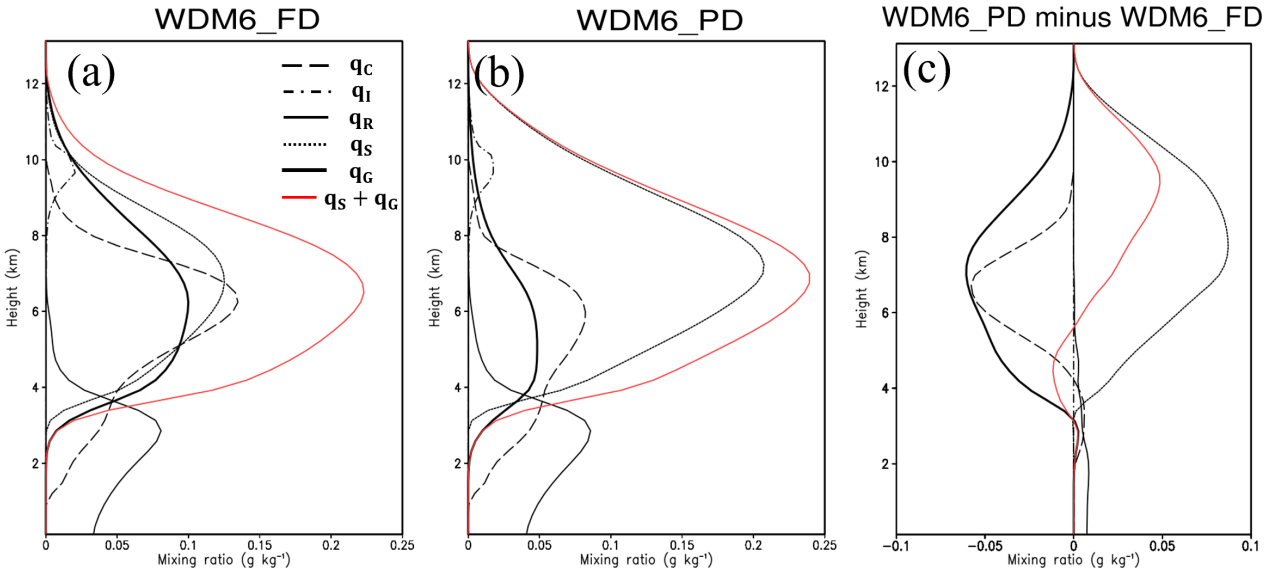
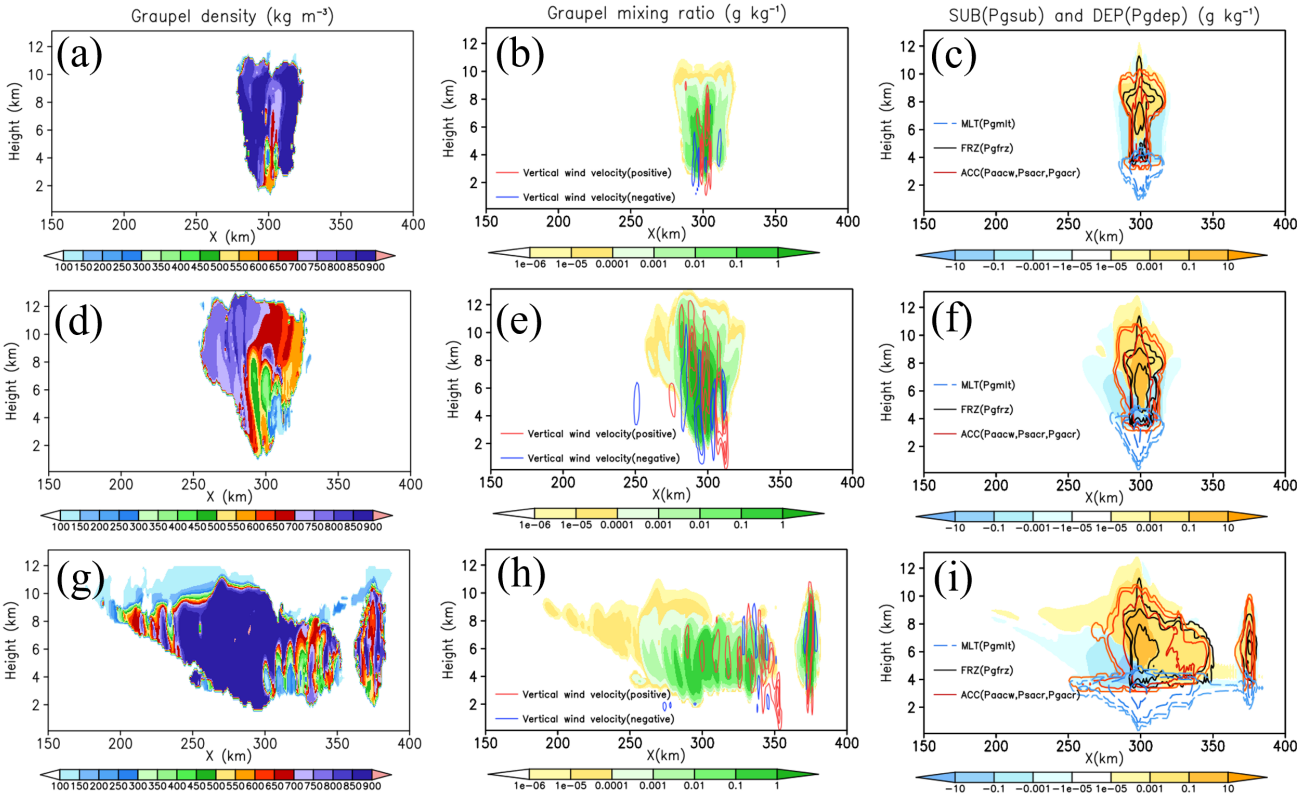


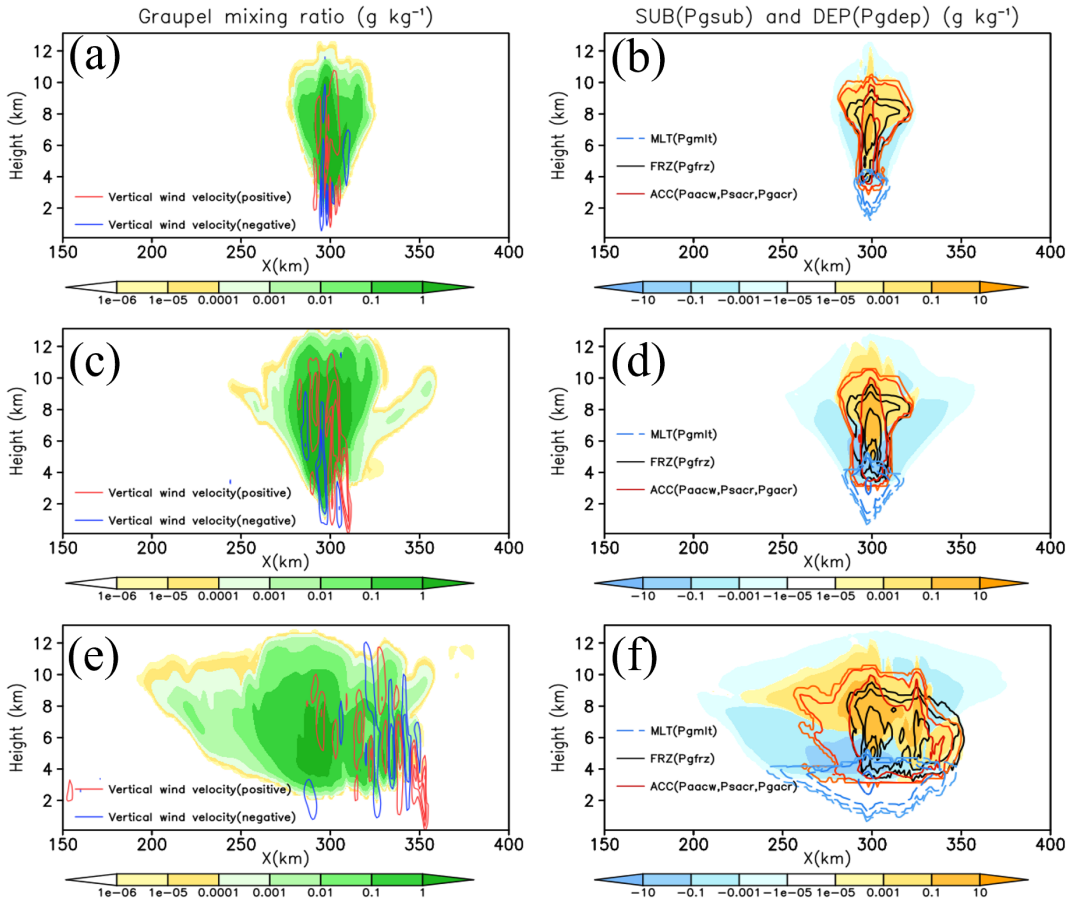
Figure 6 shows the spatial distributions of ρ_G and q_G, with the major source/sink microphysics processes of q_G in WDM6_PD at 1 h (Fig. 6a–c), 2 h (Fig. 6d–f) and 4 h (Fig. 6g–i). Note that ρ_G in WDM6_FD is pre-defined as 500 kg m^{-3}. During the early development stage of convections, at 1 h, a graupel mass mixing ratio with relatively low density is generated over the strong updraft region, and some of the particles are transported to the upper level of 11 km (Figs. 6a and b). The main source processes contributing to the graupel mass mixing ratio are deposition (DEP), accretion (ACC) and freezing (FRZ), and the main sink processes are sublimation (SUB) and melting (MLT), as seen in Fig. 6c. Major ACC processes include the accretion process between cloud water and snow or graupel, that between rain and graupel, and that between rain and snow. At 2 h, graupel continues to be generated through DEP, ACC and FRZ, with a relatively low density of 550–800 kg m^{-3} compared to the density in the initial stage (Figs. 6a, c, d and f). The higher values of the graupel mass mixing ratios are concentrated along the updraft core, resulting in a relatively lower ρ_G (Fig. 6d and e). At 4 h, graupel with a relatively lower ρ_G, which can be considered as aggregation-like particles, is transported into the anvil cloud region. Over the corresponding region, DEP and ACC are the primary active processes for growing graupel.

Figure 6: Spatial distribution of ρ_G (kg m^{-3}) (left column), q_G (g kg^{-1}) (middle column) and the major source/sink microphysics processes (g kg^{-1} s^{-1}) related to q_G (right column) in WDM6_PD at 1 h (a–c), 2 h (d–f) and 4 h (g–i). In (a), (d) and (g), the solid red (blue) line represents positive (negative) vertical wind velocity (m s^{-1}). Contour lines for positive (negative) values are at 2, 5 and 8 (−2 and −5) m s^{-1}. In (c), (f) and (i), the main source processes, namely, deposition (Pgdep; DEP), accretion (mean of Paacw, Psacr and Pgacr; ACC) and freezing (Pgfrz; FRZ) are plotted with the major sink processes, namely, sublimation (Pgsub; SUB) and melting (Pgmlt; MLT). Red (blue) colours represent DEP (SUB). The processes of FRZ, ACC and MLT are indicated by solid black, solid red and blue dashed lines, respectively. The contour lines for ACC and FRZ (MLT) values are at 1e−5, 0.001, 0.01 and 10 (−1e−5, −0.001, −0.01 and −10) (g kg^{-1} s^{-1}). Detailed descriptions of the microphysical processes are provided in Table 1.



Same microphysical properties as in Figure 6, but for WDM6_FD, are shown in Fig. 7 except ρ_G. Note that ρ_G in WDM6_FD is pre-defined as 500 kg m^{-3}. Throughout the simulation period, WDM6_FD produces a more abundant mass mixing ratio of graupel, reaching higher vertical levels and simulating a wider region for SUB (compare Figs. 7 and 6). At 2 h, graupel continues to be generated through DEP, ACC and FRZ, and the region with active SUB expands compared to the initial stage (Figs. 7c and d). At 4 h, more graupel is transported into the anvil cloud region at relatively lower levels compared to WDM6_FD due to active DEP and ACC in the corresponding region (Figs. 7e and f). The vertical profiles for the domain-averaged major source/sink microphysics processes are presented in Figure S1 of the Supplement. ACC and MLT are analyzed as the most active source and sink processes in both WDM6_PD and WDM6_FD. As we mentioned in section 2, varying parameters with the predicted graupel density can affect the mass mixing ratio and number concentration of other hydrometeors. The spatial distribution of the mass mixing ratio of other variables (cloud water, cloud ice, and snow) and the relative humidity with respect to ice (RHice) during the development stage of convection are available in Figures S2 to S5 of the supplement. Meanwhile, Diao et al. (2017) suggested 125-130% of RHice threshold value is more realistic for an idealized squall line scenario when compared with the National Science Foundation (NSF) Deep Convective Clouds and Chemistry (DC3) field campaign. The increase of RHice from 108% to 130% in our 2D squall line setup does not affect the predicted graupel density features (not shown).

Figure 7: Same as Figure 6, but for WDM6_FD.



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4.2 Snowfall experiments

Figure 8 shows the simulated surface precipitation in WDM6_FD and WDM6_PD. In the CL case, most of the simulated rainfall in WDM6_PD is concentrated over the central part of the Korean Peninsula, similar to the AWS observations (Figs. 2a and 8a). The surface snow amount is similar to the surface graupel one in both WDM6_FD and WDM6_PD for CL case. Compared to WDM6_FD, WDM6_PD simulates less precipitation along the coast and mountainous region and more precipitation over the western part of the analysis domain (as indicated by the shading in Fig. 8b). This results in a precipitation spatial distribution that is more comparable to the observed precipitation distribution. WDM6_PD reduces the surface snow amount over the mountainous region and increases the amount of surface graupel over regions with abundant precipitation, relative to WDM6_FD (Figs. 8c and d). Specifically, the total surface snow is reduced by 93% (domain-averaged snow amount is 0.80 mm in WDM6_FD and 0.75 mm in WDM6_PD), and surface graupel shows an increase of 124% (domain-averaged graupel amount is 0.51 mm in WDM6_FD and 0.64 mm in WDM6_PD) in WDM6_PD compared to WDM6_FD. These changes in WDM6_PD alleviate the precipitation deficiency in WDM6_FD. Although the bias score for the CL case (Case 1) deteriorates in WDM6_PD, the root mean square error (RMSE) score for all CL cases (Cases 1 and 3) is much improved (Table 4). In the WL case, the amount of surface snow exceeds that of the surface graupel; WDM6_PD effectively alleviates the positive bias of surface precipitation, which occurs in WDM6_FD, over most of the domain (Fig. 8f). Surface snow decreases significantly in WDM6_PD, compared to WDM6_FD, while the surface graupel increases slightly (Figs. 8g and h). Surface snow decreases significantly by 92% in WDM6_PD (domain-averaged snow amount is 0.84 mm in WDM6_FD and 0.77 mm in WDM6_PD), compared to WDM6_FD, while the surface graupel increases by 121 % (domain-averaged graupel amount is 0.18 mm in WDM6_FD and 0.21 mm in. WDM6_PD) (Figs. 8g and h). The reduction in surface precipitation amount in WDM6_PD results in an improvement in the RMSE scores for all WL cases, as well as biases for all WL cases except for

Case5 (Table 4). Overall, the equitable threat score (ETS) scores between the two experiments are quite similar. Despite these similar ETS scores, this comparison confirms that both WDM6_FD and WDM6_PD perform comparably well in predicting snowfall events.

Figure 8: Accumulated surface precipitation amount (mm) for (a) CL and (e) WL cases with WDM6_PD during the analysis period. The differences in the amounts of surface precipitation (mm) between WDM6_PD and WDM6_FD (WDM6_PD minus WDM6_FD) for CL and WL cases are shaded in (b) and (f). The red (blue) solid lines represent the positive (negative) differences between WDM6_FD and AWS observations (WDM6_FD minus AWS). The contour lines for positive (negative) values are plotted at 3, 5, 7 and 10 (−3, −5, −7 and −10) mm. The differences in the amounts of surface snow (mm) between WDM6_PD and WDM6_FD (WDM6_PD minus WDM6_FD) for CL and WL cases are plotted in (c) and (g). The differences in the amounts of surface graupel (mm) are shown in (d) and (h).

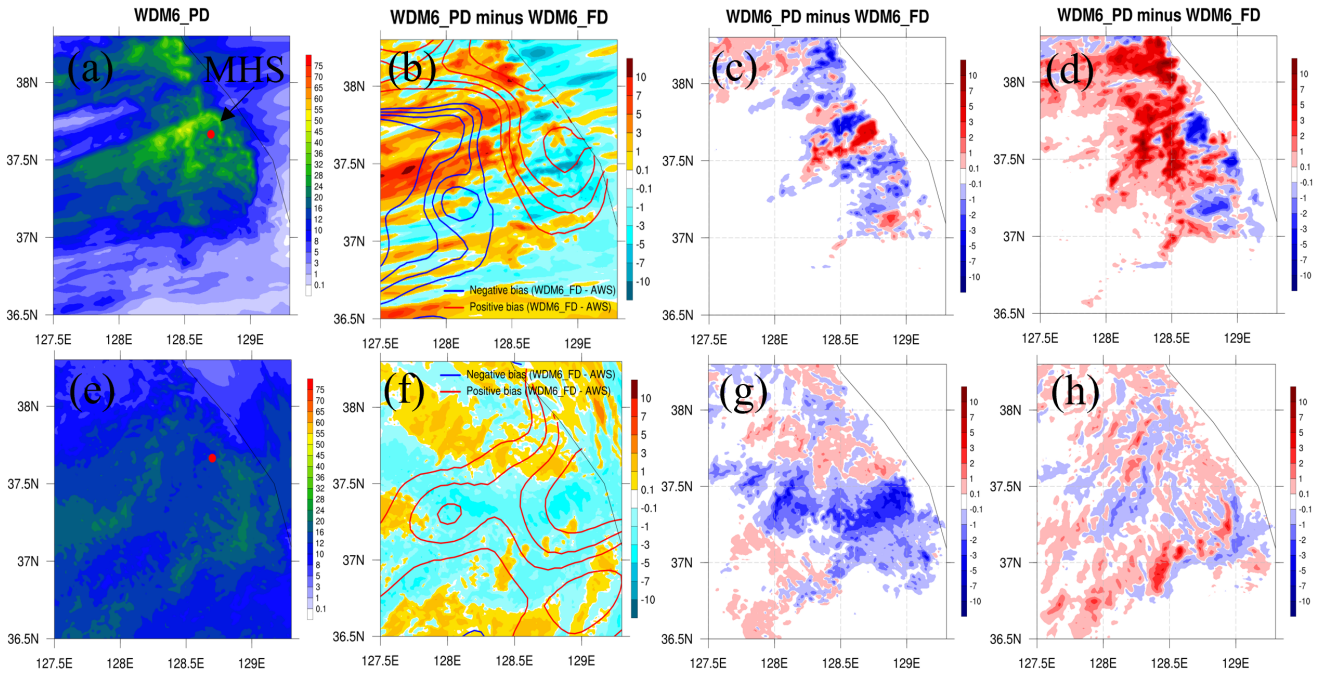


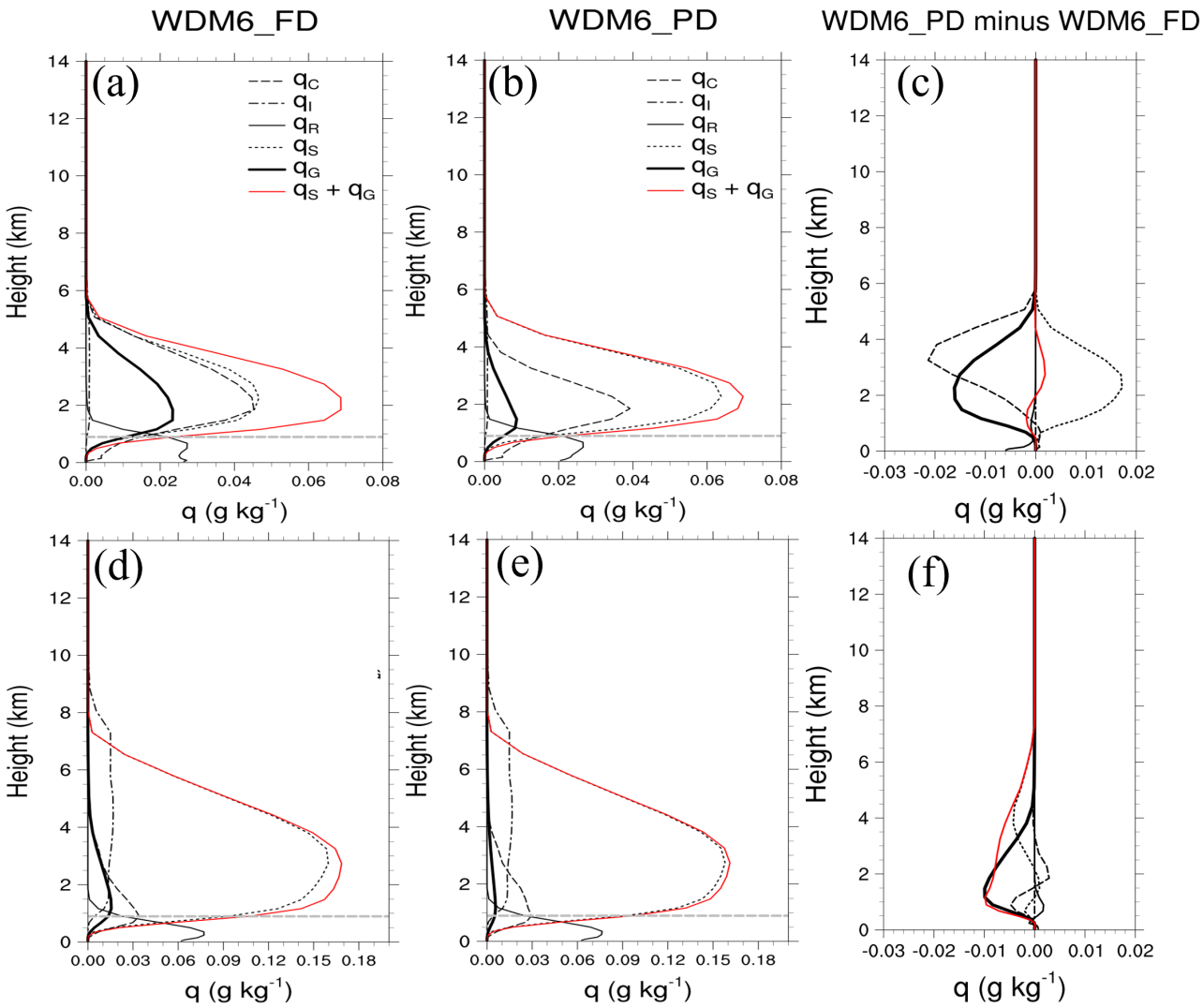
Table 4. Statistical skill scores for surface precipitation, including the root mean square error (RMSE) (mm), bias (mm) and equitable threat score (ETS) for different cases with WDM6_FD and WDM6_PD.

Case	Experiment	RMSE (mm)	BIAS (mm)	ETS
Case1	WDM6_FD	6.58	1.27	0.30
	WDM6_PD	6.01	1.61	0.31
Case2	WDM6_FD	5.49	5.03	0.16
	WDM6_PD	4.36	3.56	0.17
Case3	WDM6_FD	1.81	1.31	0.19
	WDM6_PD	1.63	1.26	0.18
Case4	WDM6_FD	9.51	2.83	0.07
	WDM6_PD	9.00	0.63	0.06
Case5	WDM6_FD	13.95	12.69	0.14
	WDM6_PD	13.79	13.27	0.12

Case6	WDM6_FD	3.94	2.87	0.10
	WDM6_PD	3.55	1.31	0.07
Case7	WDM6_FD	1.67	−1.47	0.10
	WDM6_PD	1.62	−1.36	0.11
Case8	WDM6_FD	2.63	1.20	0.17
	WDM6_PD	1.87	−0.36	0.20

The vertical distributions of the time-domain-averaged mass mixing ratios for WDM6_FD and WDM6_PD are shown in Fig. 9. In the CL case, the simulated mass mixing ratios for all hydrometeors are pronounced below the 6 km level (Figs. 9a and b), while in the WL case, hydrometeors are simulated up to the 10 km level (Figs. 9d and e). This is because the WL case comprises deeper systems than the CL case. The relative proportion of graupel to the total hydrometeors is greater in the CL case than in the WL case. Additionally, for the CL case, the graupel mass mixing ratio decreases, and the snow mass mixing ratio increases in WDM6_PD than in WDM6_FD. Therefore, the total mass mixing ratio of snow and graupel increases above the 2 km level, while it decreases below the level in WDM6_PD relative to WDM6_FD in the CL case, as seen in the 2D idealized case. In WDM6_PD, the overall cloud water mass mixing ratio decreases, and the rain mass mixing ratio slightly decreases near the surface (Fig. 9c). The change in graupel mass mixing ratio in the WL case is similar to those in the CL case (Fig. 9f). The graupel mass mixing ratio decreases significantly below the 5 km level in WDM6_PD. The snow mass mixing ratio also decreases throughout the layers except at the 1–2 km level, resulting in a smaller total mass mixing ratio of snow and graupel in WDM6_PD compared to WDM6_FD (Fig. 9f). Meanwhile, the rain, cloud water, and cloud ice mass mixing ratios of WDM6_FD and WDM6_PD differ only slightly. A noteworthy characteristic of WDM6_PD is the reduction in the graupel mass mixing ratio over the whole layers regardless of simulation cases, resulting in an increase in the amount of surface graupel deposited (Figs. 8d and h). The reason for the lower graupel mass (Figs. 9c and f), despite the greater surface graupel accumulation (Figs. 8d and h) in WDM6_PD, will be analyzed in the subsequent Figures 10 and 11.

Figure 9: Vertical profiles for the time-domain-averaged mass mixing ratios (g kg^{-1}) of hydrometeors for (a) CL and (d) WL cases with WDM6_FD. (b) and (e) are same as (a) and (d), but for WDM6_PD. The differences in the mass mixing ratios of WDM6_PD and WDM6_FD (WDM6_PD minus WDM6_FD) for CL and WL cases are plotted in (c) and (f). In (a), (b), (d) and (e), the cloud ice mass mixing ratio (q_I) is multiplied by 100. The sum of snow and graupel mass mixing ratios (g kg^{-1}) is indicated by red lines, and the 0°C level by the grey dashed horizontal line.



The vertical profiles for the time-domain-averaged ρ_G for CL and WL cases are compared in Fig. 10. As shown in Fig. 9, convective cells develop more extensively in the vertical direction in the WL case than in the CL case. In the presence of graupel, the time-domain-averaged ρ_G is simulated up to a higher level in the WL case than in the CL case (Figs. 10a and c). The value of ρ_G is taken as 500 kg m^{-3} in WDM6_FD, whereas it has relatively smaller values of up to 250 and 350 kg m^{-3} in WDM6_PD for the CL and WL cases, respectively. The time-domain-averaged mass-weighted mean diameter (D_m) in WDM6_PD is greatly reduced compared to WDM6_FD (Figs. 10b and d). In the CL case, the range of D_m is quite wider below the 4-km level, indicating more variability in graupel sizes than the WL case. In both cases, WDM6_PD presents smaller graupel than WDM6_FD, especially over the lower level. In WDM6_PD, the time-domain and vertical-averaged D_m is simulated as 0.110 and 0.191 mm for the CL and WL cases, respectively, whereas in WDM6_FD, it is simulated as 0.133 mm (CL) and 0.199 mm (WL), indicating that WDM6_PD simulates smaller graupel diameters. Despite smaller values of ρ_G and D_m in WDM6_PD compared to WDM6_FD, the former simulates a higher graupel fall velocity when considering the simulated D_m in both simulations (see Fig. 1), leading to more surface graupel in WDM6_PD for CL and WL cases (Figs. 8d and h).

In the CL case, WDM6_PD simulates ρ_G with a maximum value of 220 kg m^{-3} and D_m with a maximum value of 0.44 mm at around the 2 km level (Figs. 10a and b). The maximum level of falling graupel is simulated at a lower altitude of 2 km in the WDM6_PD compared to WDM6_FD, in which the maximum level is located at 3.5 km (Fig. 11a). As graupel falls quickly in WDM6_PD, graupel deposition (Pgdep) decreases, leading to the suppression of graupel growth and sublimation (Pgsub) (Fig. 11b). Meanwhile, the deposition of snow (Psdep) in WDM6_PD, the red lines in Fig. 11b, increases

below the 3.5 km level owing to the surplus water vapor relative to WDM6_FD, leading to an increase in the snow mass mixing ratio in the atmosphere (Fig. 9c). Furthermore, the northeastern inland area, receiving abundant precipitation, exhibits more positive snow advection at the 850 hPa level in WDM6_PD compared to WDM6_FD (Fig. S6 in the Supplement). Increased snow advection towards the inland area enhances the snow mass mixing ratio in WDM6_PD. Additionally, efficient Paacw with more available snow mass can contribute to the increased snow mass mixing ratio in WDM6_PD. In the WL case, graupel, which exists up to the 10 km level, ρ_G increases significantly up to a value of 350 kg m^{-3} at 1 km level (Fig. 10c). Even though D_m of WDM6_PD is larger than that of WDM6_FD above the 3-km level, graupel particles in WDM6_PD have a greater falling velocity (Figs.10d and 1) and falls from a relatively higher level of 8 km in WDM6_PD than in WDM6_FD (Fig. 11c). The maximum amount of falling graupel is simulated at a relatively lower level of 1.8 km in WDM6_PD than in WDM6_FD, as seen in the CL case. Pgdep efficiently occurs at a higher level in WDM6_PD than in WDM6_FD (Fig. 11d) possibly because the former simulates more graupel with a steep increase in ρ_G between the 5 km and 8 km levels. The increase in Pgdep in WDM6_PD leads to a reduction in the available water vapor, in turn, causing a reduction in the Psdep and snow mass mixing ratio values in the atmosphere. The significantly enhanced graupel fall velocity, attributed to the newly derived parameters in the V_G–D relationship in WDM6_PD, accelerates the sedimentation of graupel. This, in turn, increases the surface graupel amount while decreasing the graupel mass mixing ratio in the atmosphere.

Figure 10: Vertical profiles for the time-domain-averaged ρ_G (kg m^{-3}) for (a) CL and (c) WL cases with WDM6_PD. Time-domain-averaged D_m (mm) with WDM6_PD and WDM6_FD for CL and WL cases are in (b) and (d). The solid and dashed lines represent WDM6_FD and WDM6_PD, respectively.

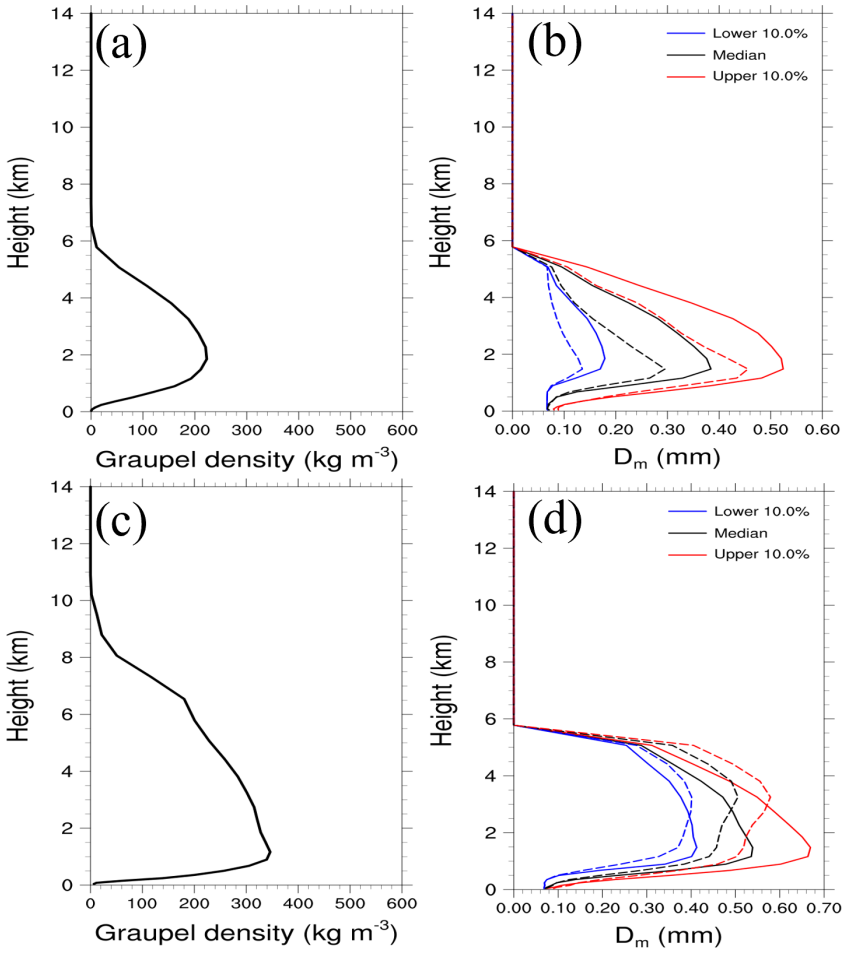
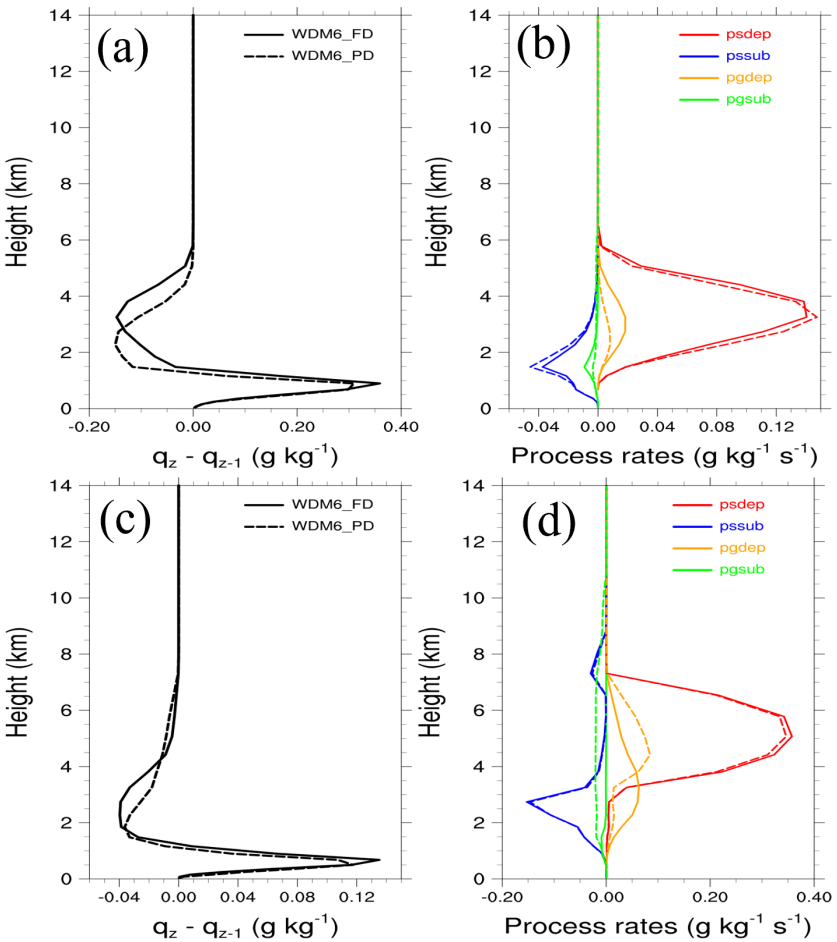


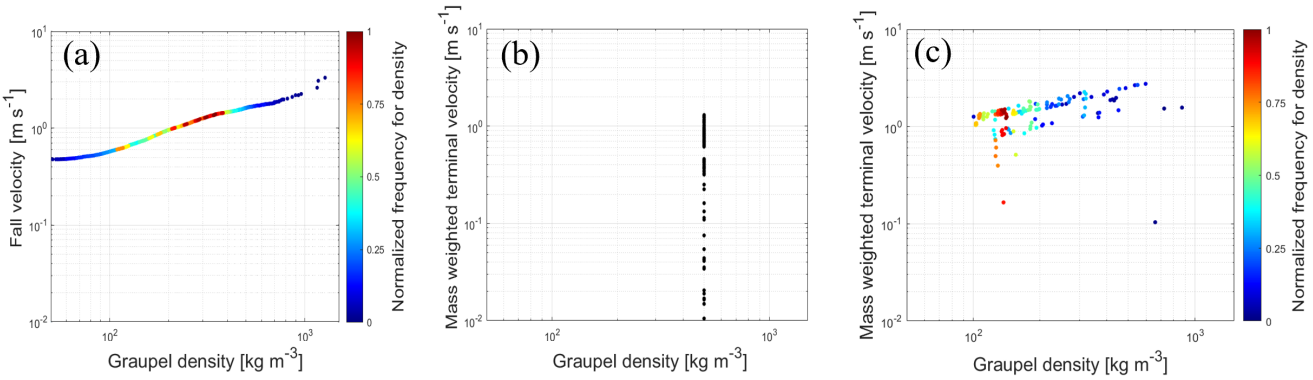
Figure 11: Time-domain averaged difference in graupel mass mixing ratio between the levels 'z' (q_z) and 'z-1' (q_{z-1}) due to sedimentation in (a) and (c) for CL and WL cases. (b) and (d) show the vertical profiles of time-domain averaged sources/sinks of graupel and snow mass mixing ratio for the CL and WL cases. The solid and dashed lines represent WDM6_FD and WDM6_FD_500, respectively. Only the major microphysical processes are represented. In (d), Pgdep and Pgsub are multiplied by 10.



The ρ_G–V_G relationships obtained from the 2DVD measurement at the MHS site, as well as those simulated from WDM6_PD and WDM6_FD, are shown in Fig. 12. The observed ρ_G values are in the range of 43.6–1267 kg m^{-3} (Fig. 12a). The maximum normalized frequency of the observed ρ_G is shown in the range of approximately 300–400 kg m^{-3}, with the frequent normalized frequency of ρ_G values between 100 and 400 kg m^{-3}. WDM6_FD only presents a single value of ρ_G (500 kg m^{-3}; Fig. 12b), as it is treated as the fixed value in the model and shows a much lower range of graupel fall velocity than the observed value. Meanwhile, in WDM6_PD, the range of ρ_G is simulated from 100 to 900 kg m^{-3}, as our study sets the possible range of ρ_G within this range. WDM6_PD presents the majority of simulated ρ_G at relatively lower values of 150 kg m^{-3} compared to the observed value (Figs. 12a and c). The fall velocity of graupel, varying with ρ_G, shows a relatively larger value in WDM6_PD than in the observations. Although WDM6_PD simulates larger ranges of fall velocity and lower ranges of ρ_G, it is closer to the observations than WDM6_FD. Our analysis highlights that WDM6_PD with varying graupel density results in faster fall velocities, leading to more efficient sedimentation processes, which affect the spatial distribution and amount of graupel mass mixing ratio both in the atmosphere and on the surface. By predicting graupel density, WDM6_PD can produce more realistic characteristics of graupel particles, including their density and fall velocity.

Figure 12:ρ_G– V_G relationships are shown: (a) 2DVD measurement, (b) WDM6_FD and (c) WDM6_PD. Colour bars in (a) and (b) represent the normalized frequency of ρ_G. In (a), graupel particle characteristics measured at the MHS site during the analysis

period of Case 6 are used. For (b) WDM6_PD and (c) WDM6_FD, model-simulated graupel characteristics are extracted over 16-grid points centred at the MHS site during the analysis period for Cases 2 and 6.



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5. Summary and conclusion

This study introduces a method to predict graupel density and incorporates the predicted graupel density into the
465 WDM6 microphysics scheme (Park and Lim, 2023). By using the new prognostic variable (graupel volume mixing ratio), graupel density can be predicted based on the ratio of graupel mass mixing ratio and its volume mixing ratio, following the study of Milbrandt and Morrison (2013). Therefore, the mass–diameter and fall velocity–diameter relationships of graupel are updated with varying graupel density. To assess the impact of predicted graupel density on the simulated precipitation system, numerical simulations are conducted for 2D idealized squall line and winter snowfall cases during the ICE-POP 2018 field
470 campaign using the WRF model version 4.1.3. The modified WDM6 requires 22.8% more computational time, considering only cloud microphysical processes, compared to the original WDM6.

In the idealized 2D squall line framework, simulations using the original WDM6 and modified WDM6 yield similar surface rain rates associated with squall line development. However, compared to the original WDM6, the modified WDM6 gives higher maximum reflectivity in both the convective cores and the stratiform regions. A comparison of the vertical profiles
475 of the mass mixing ratios with the modified and original WDM6 confirms a significant decrease in the graupel mass mixing ratio and an increase in the snow mass mixing ratio throughout the vertical layers. The vertical cross sections of graupel fields over time reveal that the modified WDM6 can represent a range of graupel densities, from low to high at varying times and in different spaces. For graupel mass mixing ratio, the main source processes are analyzed as deposition, accretion, and freezing, while the sink processes as sublimation and melting throughout the squall line evolution.

480 For the winter snowfall cases during the ICE-POP 2018 field campaign, the original WDM6 exhibits a positive bias by simulating more precipitation along the coastal and mountainous regions, irrespective of the specific case. In a shallow system, classified as a CL case in our study, the modified WDM6 provides a better RMSE score than the original WDM6 by reducing surface precipitation over the regions representing positive bias and enhancing it over the western part of the analysis domain. Although the maximum density of graupel in the modified WDM6 is smaller than that in the original WDM6, the fall
485 velocity of graupel is greater in the modified WDM6 because of the newly employed graupel fall velocity relationship. Faster sedimentation of graupel leads to inefficient graupel deposition. This, in turn, results in a decrease in the graupel mass mixing ratio and presence of more snow suspended in the atmosphere. The increased snow is a result of efficient snow deposition with surplus water vapor. Therefore, a decrease in surface snow over the mountainous region and an increase in surface graupel over regions with abundant precipitation mitigate the surface precipitation deficiency in the original WDM6.

490 In the deep system, classified as a WL case, the modified WDM6 reduces surface snow to mitigate the excessive precipitation bias observed in the original WDM6 simulation over the entire domain. In this case, the surface amounts of snow

exceed those of graupel, unlike in a CL case where the simulated amounts of surface snow and graupel are similar. Therefore, the change in surface precipitation is mainly attributed to changes in the surface snow. A greater graupel deposition in the 4–8 km level in the modified WDM6 consumes more water vapor, leading to inefficient snow deposition in the corresponding level. Hence, the snow mass mixing ratio in the atmosphere and at the surface decreases in the modified WDM6, leading to improved RMSE scores in all WL cases than in the original WDM6.

The simulated fall velocity–density relationship of graupel is verified using 2DVD measurement data for a WL snowfall case that occurred during the ICE-POP 2018 field campaign. Although the modified WDM6 simulates slightly larger ranges of fall velocity and lower ranges of graupel density, it captures the observed relationship between graupel density and fall velocity fairly well. In contrast, the original WDM6, with a fixed graupel density, not only underestimates the graupel fall velocities but also predicts a lower range of fall velocity compared to the observed values. It is worth noting that our study is distinguished by its attempt to compare simulated graupel characteristics with observed data during ICE-POP 2018. The co-located MASC measurements, coupled with the 2DVD measurement, enhance the quality of graupel identification in our research. The V_G–D relationship in the modified WDM6 is derived using the least-squares method in a log–log space at the given graupel density. The derived V_G–D relationship in our research could be refined by incorporating a broader range of graupel observational data, including hexagonal, conical, lump graupel, or graupel-like snow. Improvements in the representation of V_G–D relationship can lead to better simulation of precipitation and microphysical processes in environments where various types of graupel are generated. Additionally, the potential benefits of the predicted graupel density could be further evaluated in future works through comparison with additional observational data such as sonde and satellite.

Code and data availability. The WRF model version 4.1.3 is available at https://github.com/wrf-model/WRF/releases (last access: January 2022). The ERA-Interim reanalysis data from the European Centre for Medium-Range Weather Forecasts (ECMWF) for initial and boundary conditions is available at https://apps.ecmwf.int/datasets/data/interim-full-daily/levtype=pl/and https://apps.ecmwf.int/datasets/data/interim-full-daily/levtype=sfc/ (last access: October 2019). The model codes, model output, and scripts and that cover every data and figure processing action for all the results reported in this paper are available at https://zenodo.org/records/12065447. The 2DVD data are available at https://doi.org/10.5281/zenodo.10126522.

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Appendix: Description of WDM6 Microphysics Scheme

a) Parameters for hydrometeor characteristics

WDM6 microphysics scheme is originally described in Park and Lim (2023). It employs the double-moment approach for the mass mixing ratio (q_x) of X = {c, r, i, s, g} and the total number concentration (N_x) of X = {c, r, i}. Here, c, r, i, s, and g indicate cloud, rain, cloud ice, snow, and graupel, respectively. The characteristics of hydrometeor in the WDM6 scheme are determined by density (ρ_x), the fall velocity (V_x)–diameter (D) relationship, the mass (M_x)– D relationship, and the size distribution ($N_x(D)$). The size distribution of each hydrometeor category X, except cloud water, which does not sediment, is represented by a complete gamma function of the following form:

$$N_X(D)\ [m^{-4}] = N_{0X}\ D^{\mu X}\ \exp\{-(\lambda_X\ D)\}, \tag{A1}$$

$$N_{0X}\ [m^{-4}] = N_X\ \lambda_X^{\mu X+1}, \tag{A1-1}$$

$$\lambda_X[m^{-1}] = \left[\frac{c_X\ N_X}{\rho_a\ q_X}\frac{\Gamma(\mu_X+d_X+1)}{\Gamma(\mu_X+1)}\right]^{1/d_X}. \tag{A1-2}$$

Here, $N_x(D)$ indicates the number concentration of each hydrometeor corresponding to D. μ_X and λ_X represent the shape and slope parameters of the size distribution. N_{0X} and N_x are the intercept parameter and the total number concentration of each hydrometeor, respectively.

Meanwhile, the V_x – D and M_x – D relationships can be expressed as Eqs. (A2) and (A3):

$$V_x\ [m\ s^{-1}] = a_x D^{b_x}, \tag{A2}$$

$$M_x\ [kg] \quad = c_x D^{d_x}, \tag{A3}$$

where a_x, b_x, c_x, and d_x are coefficients that can vary depending on the type of hydrometeor. All particles in the original WDM6 scheme are assumed to be spherical with constant bulk densities. Thus, for each category, $c_x = \pi\rho_x/6$ and d_x=3. The coefficients defining the characteristics of hydrometeors in the original WDM6 scheme are summarized in Table A1.

Table A1. Parameters for hydrometeor (rain, ice, snow and graupel) characteristics in WDM6 scheme.

	V_x – D_x relationship		M_x – D_x relationship		Shape parameter (μ_x)	Density (ρ_x)
	a_x	b_x	c_x	d_x		
Rain	841.9	0.8	$\frac{\pi\rho_R}{6}$	3	1	1000
Cloud ice	2.71×10^3	1.0	$\frac{\pi\rho_I}{6}$	3	0	500
Snow	11.72	0.41	$\frac{\pi\rho_S}{6}$	3	0	100
Graupel	330.0	0.8	$\frac{\pi\rho_G}{6}$	3	0	500

b) Microphysical Processes

The governing equations of the mass mixing ratio and the number concentration for each hydrometeor are given by Eqs. (A5) and (A6), respectively:

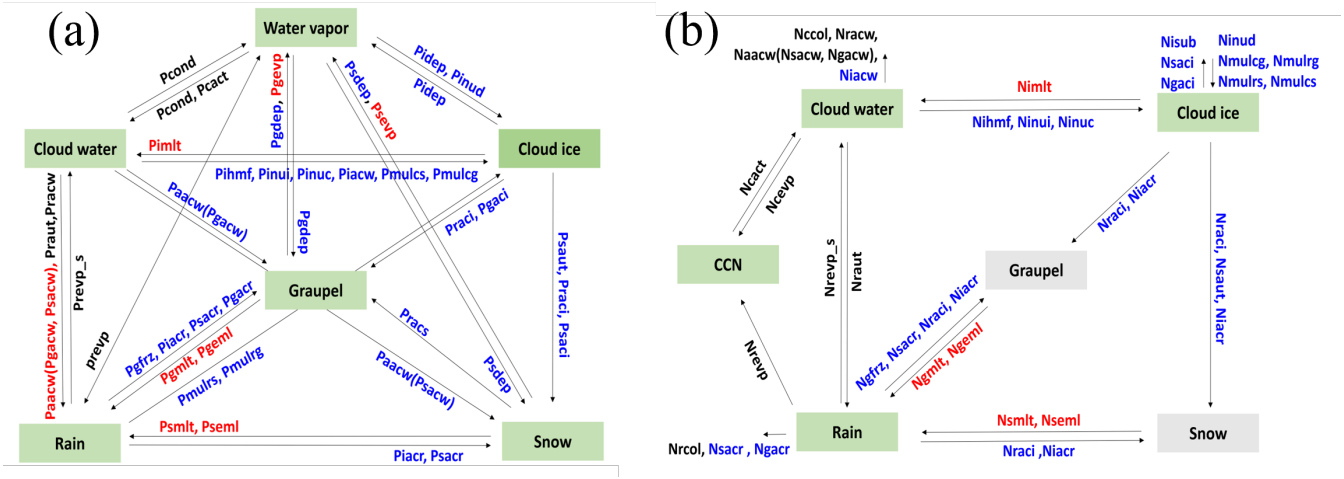
$$\frac{\partial q_x}{\partial t} = -\vec{V} \cdot \nabla_3 q_x - \frac{1}{\rho_a}\frac{\partial}{\partial z}\left(\rho_a q_x V_{q_x}\right) + S_{q_x}, \quad \text{(A5)}$$

$$\frac{\partial N_x}{\partial t} = -\vec{V} \cdot \nabla_3 N_x - \frac{1}{\rho_a}\frac{\partial}{\partial z}\left(\rho_a N_x V_{N_x}\right) + S_{N_x}, \quad \text{(A6)}$$

where the first and second terms on the right-hand side of Eq. (A5) represent the 3D advection and sedimentation for q_x, respectively. The third term represents the source and sink of q_x. $\vec{V}$ and V_{q_x} represent the three-dimensional 3D wind fields and the q_x-weighted mean terminal velocities of X, respectively; ρ_a is the air density. Eq. (A6) is identical to Eq. (A5) but for the number concentration.

The production terms (S_{q_x} and S_{N_x}) for each hydrometeor category are composed of several microphysical processes including melting, accretion, and nucleation, as shown in Figure A1. One of the accretion processes, Psacr, represents the accretion between snow and rain particles, which primarily contributes to the formation of graupel or snow. When the mass mixing ratios of both rain and snow are greater (smaller) than 1.e-4 kg kg^{-1}, it contributes to the formation of graupel (snow). This process acts as a source process for the graupel or snow mass mixing ratio and as a sink process for the rain mass mixing ratio (Fig. A1a). Detailed descriptions and parameterization equations of these microphysical processes are available in previous studies by Park and Lim (2023) and Lim and Hong (2010).

Figure A1. Flowcharts of microphysical processes for predicting (a) mass mixing ratio (S_{q_x}) and (b) number concentration (S_{N_x}) of hydrometeors in WDM6 scheme. The number concentrations of hydrometeors in the green boxes are predicted only (e.g., cloud water, cloud ice, rain, and cloud condensation nuclei (CCN)). Microphysical terms drawn with red (blue) are activated when the temperature is above (below) 0°C. Terms drawn in black are activated regardless of temperature.



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