Using Deep Learning to integrate paleoclimate and global biogeochemistry over Phanerozoic time

Dongyu Zheng[1,2], Andrew S. Merdith[2,3], Yves Goddéris[4], Yannick Donnadieu[5], Khushboo Gurung[2], Benjamin J.W. Mills[2]

[1]State Key Laboratory of Oil and Gas Reservoir Geology and Exploitation and Key Laboratory of Deep-time Geography and Environment Reconstruction and Applications, MNR, Institute of Sedimentary Geology, Chengdu University of Technology, Chengdu
[2]School of Earth and Environment. University of Leeds. Leeds, UK
[3]School of Physics, Chemistry and Earth Sciences, University of Adelaide, Adelaide, Australia
[4]Géosciences Environnement Toulouse, CNRS–Université de Toulouse III, Toulouse, France
[5]Aix Marseille Univ, CNRS, IRD, INRAE, CEREGE, Aix-en-Provence, France

Correspondence to: Dongyu Zheng (zhengdongyu@cdut.edu.cn)

Abstract. Databases of 3D paleoclimate model simulations are increasingly used within global biogeochemical models for the Phanerozoic Eon. This improves the accuracy of the surface processes within the biogeochemical models, but the approach is limited by the availability of large numbers of paleoclimate simulations at different pCO_2 levels and for different continental configurations. In this paper we apply the Frame Interpolation for Large Motion (FILM) Deep Learning method to a set of paleoclimate model simulations to upscale their time resolution from one model run every ~25 million years to one model run every 1 million year (Myr).

Testing the method on a 5 Myr time-resolution set of continental configurations confirms the accuracy of our approach when reconstructing intermediate frames from configurations separated by up to 40 Myrs. We then apply the method to upscale the paleoclimate datastructure in the SCION climate-biogeochemical model and demonstrate that upscaled outputs for global distributions of surface temperature and runoff follow a logical progression between the original keyframes.

When updated to use the high-time-resolution climate datastructure, the SCION model predicts climate shifts that were not present in the original model outputs due to its previous use of wide-spaced datasets and simple linear interpolation. We conclude that a time resolution of ~10 Myr in paleoclimate simulations is likely sufficient for investigating the long-term carbon cycle, and that Deep Learning methods may be critical in attaining this time-resolution at a reasonable computational expense, as well as for developing new fully-continuous methods in which 3D continental processes—such as species distribution—are able to translate over a moving continental surface in deep time. Nonetheless, the efficacy of Deep Learning methods in interpolating runoff data, compared to that of paleogeography and temperature, is diminished by the heterogeneous distribution of runoff. Consequently, interpolated climates should be confirmed by running a paleoclimate model for any sound scientific conclusions.

1 Introduction

To simulate global environmental change over Phanerozoic time it is important to understand how continental surface processes operate. For example, the weathering of silicate minerals controls the removal of atmospheric CO_2, and phosphorus input from weathering plays a major role in the long-term oxygenation of the Earth (Walker et al., 1981; Lenton and Watson, 2004). Weathering rates are largely controlled by local erosion rates, temperature and hydrology (West 2012; Maher and Chamberlain, 2014), and the latest generation of Phanerozoic global biogeochemical models aim to represent these factors at the local scale using data from 3D General Circulation Model (GCM) simulations (Godderis et al., 2023). Due to the long computational timescales of GCMs (typically weeks to months per ~5000-year simulation for a fully coupled ocean-atmosphere model), they cannot be run interactively with long-term biogeochemical cycles over millions of years. Therefore, the 'spatialized' deep-time biogeochemical models such as GEOCLIM (Donnadieu et al., 2006; Godderis et al., 2014) and SCION (Mills et al., 2021) rely on either discrete time intervals, or linear interpolation between times set by previously-computed climate model simulations.

Currently both the GEOCLIM and SCION models use a set of 22 continental configurations whose climate has been simulated by the Fast Ocean and Atmosphere Model (FOAM) at a range of different CO_2 levels. This equates to one set of model runs every ~25 million years on average, although some gaps are up to 40 million years. This coarse time resolution likely has impacted the accuracy of the biogeochemical model results. For example, through plate tectonic motion, a mountain range may pass through the high-rainfall Inter-Tropical Convergence Zone (ITCZ), an event expected to cause a spike in continental weathering, but be undetected by SCION or GEOCLIM if the timespan at which the mountain range crossed the ITCZ was not represented in the time points chosen for the paleoclimate simulations. A further issue is that when these models are focused on single events, such as mass extinctions, they may not be able to incorporate the relevant continental configurations and climate fields for that time in Earth history, instead using boundary conditions for up to 20 million years before or after the event.

Deep learning has received significant attention in the field of geosciences due to its impressive capabilities in handling tasks such as regression, classification, time-series analysis, and image processing (Reichstein et al., 2019; Chen et al., 2022; Zheng et al., 2022). One notable application of deep learning is in video frame interpolation, where it synthesizes intermediate frames between two input frames (Niklaus et al., 2017; Shi et al., 2022). Such a process can be highly beneficial in creating higher-time-resolution input variables for biogeochemical models by interpolating from the original climate model runs.

In this paper we use Deep Learning to fill the gaps between the paleoclimate simulation set used in the SCION model, increasing the time-resolution around 25-fold to 1 million years. We focus on the SCION model because it runs continuously over the Phanerozoic and has previously published outputs for long-term atmospheric CO_2, O_2 and global average temperature, but our results could be used to produce new runs of the GEOCLIM model, as well as other models that require spatial surface process information.

2 Data and methodology

2.1 Model forcings at 22 distinct time intervals

65

The SCION model employs a series of 2D model forcing fields taken from annual mean (approximate) steady states of the FOAM climate model. These are paleogeography, surface air temperature, continental runoff and topographic slope (Fig. 1). These 2D fields are 40×48 cells (4.5° latitude ×7.5° longitude) and are available for 22 distinct time points roughly evenly-spaced between the Cambrian and present day. These 22 time points represent the grid-data stack times in the context of

70 climate modelling. They are also run for a large range of different CO_2 levels, and extrapolated beyond these for a total of 26 different levels by applying a linear interpolation; the original FOAM surface air temperature and continental runoff are adjusted according to a linear change in the logarithm of CO_2 concentrations. During the SCION model run, 2D linear interpolation is used to estimate these fields for the current model CO_2 level, and a weighted mean is used to produce a final estimate of bulk weathering fluxes by using the distance between the current model timestep and the available climate model

75 runs. Wide spacing in time between some of these climate model datasets means that this weighted mean technique will likely miss many important features of Phanerozoic climate change. To improve on this, we adopt a frame interpolation technique (Reda et al., 2022), widely utilized to synthesize intermediate frames between two input frames in video sources, which increases the time-resolution (e.g. increases frames per second). This technique typically finds applications in amplifying refresh rates or generating slow-motion videos (Wu et al., 2023).

2.2 The deep learning interpolation algorithm

80

Deep Learning models are complex neural networks with typically >106 parameters. The model emulates the learning process of humans by updating the parameters in the neural networks to produce optimal predictions. The principal idea of using deep learning in frame (e.g. image) interpolation is to estimate the optical flow, which symbolizes the changes between two consecutive frames, followed by a pixel synthesis process that restores the intermediate images based on the estimated optical

85 flows. The deep learning model aims to minimize the differences between model-predicted intermediate frames and the actual intermediate frames in a training dataset. This approach enables the model to accurately extrapolate the visual transformation from one frame to the next and synthesize a plausible intermediate frame that maintains temporal consistency with the surrounding frames. The inputs of the deep learning model are two end-point image frames, with the target being the intermediate frames. By understanding how intermediate frames evolve from previous and future frames across a broad

90 spectrum of video datasets, the deep learning model can discern rotation, scaling, colour changes, and more intricate deformations, making it fit for creating interpolation images for new tasks.

In our study, we employ a complex Convolution Neural Network (CNN), called Frame Interpolation for Large Motion (FILM, Reda et al., 2022), to generate image interpolations for the FOAM dataset. FILM, when contrasted with traditional interpolation algorithms and other deep learning techniques, exhibits superior proficiency in dealing with abrupt changes in brightness and

95 substantial motion. Such sudden shifts are frequent in the FOAM dataset due to the significant reorganizations that the

paleogeographic and paleoclimatic conditions underwent throughout the Phanerozoic Eon (Royer et al., 2004; Godderis et al., 2014; Scotese, 2021). We represent the FOAM dataset directly from the native R15 climate grid as a set of 40×48-sized images, each depicting the entire Earth surface. The FILM technique is then deployed to generate intermediate images between two consecutive model forcing frames from a specific dataset. This method enables the creation of an atlas of one-million-year

100   model forcing frames through several iterations of interpolation (See Fig. 1). By converting these interpolated frames back to numerical values, this atlas can be used to generate million-year-resolution 'DeepFOAM' dataset, which can then be used in the place of the original SCION model forcing set to run the SCION model. Nothing is altered at the SCION model runtime—it still uses weighted averages to interpolate bulk continental fluxes in time—however now it will interpolate between a maximum gap of 1 million years, where variations in the continental configurations are very small.

105

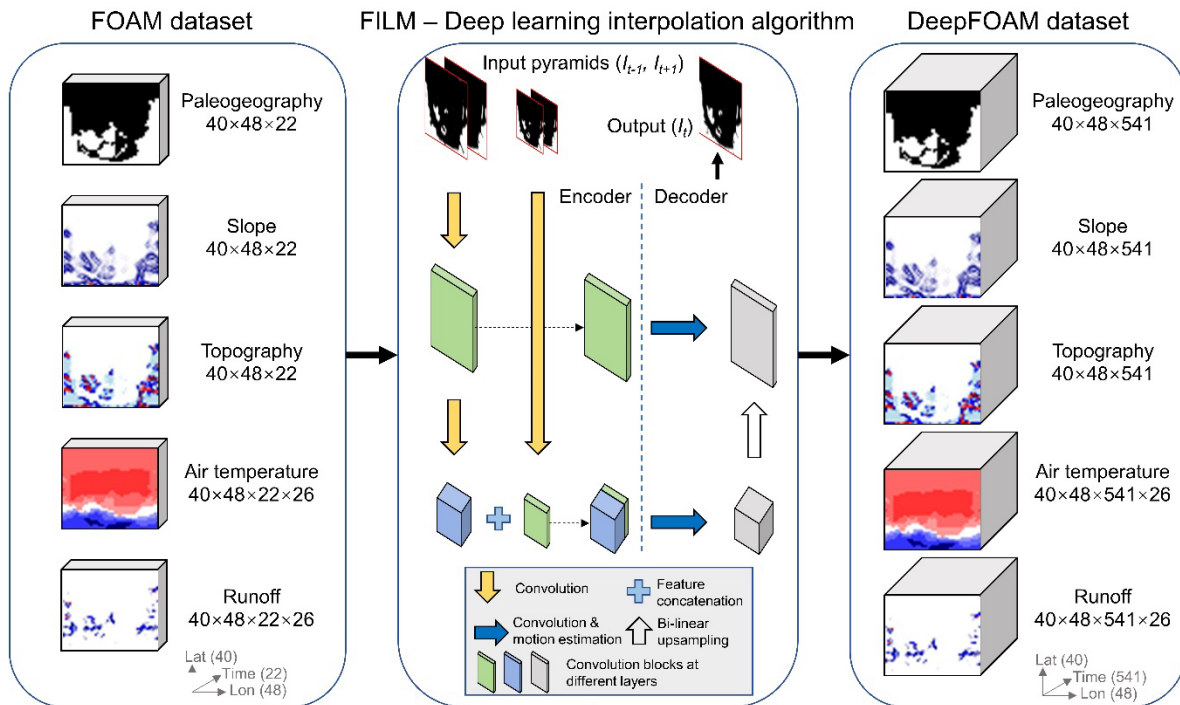



Figure 1. Deep learning interpolation workflow for FOAM dataset and simplified overview of FILM. Numerical annotations represent the dataset dimensions, e.g., for original air temperature, 40 and 48 refer to the horizontal and vertical geographic spans, 22 represents the time intervals, 26 represents the different CO_2 concentration levels. $I_{(t-1)}$ and $I_{(t+1)}$ represent the two input frames; I_t is the intermediate frame.

110   The convolution step is the matrix operation to obtain high-level feature representations; motion estimation is the change estimation achieved by the convolution operation; concatenation means the unification of two matrices of the same dimension to amalgamate features from different levels in the input pyramids; bi-linear up sampling is the technique used to reconstruct a frame from the high-level feature representation. The FILM overview is simplified based on Fig. 2 in Reda et al. (2022); we refer the reader to Reda et al. (2022) and Goodfellow et al. (2016) for further details of these techniques.

115

FILM is a U-shaped CNN encompassing both encoders and decoders (Fig. 1). Convolution, the fundamental operation in any CNN, involves multiplication between the image matrix and the filters, which are typically smaller matrices. This convolutional operation yields a higher-level representation of the original images. Deep CNNs employ hundreds or thousands of such filters to discern features in images such as shape, brightness and patterns (Hinton et al., 2006; Goodfellow et al., 2016).

120 The encoder module in FILM serves to extract high-level feature representations from input images. This is accomplished via its specialized pyramidal architecture that encompasses seven levels of feature extractors. These range from fine-level (high-resolution) to coarse-level (low-resolution), effectively allowing FILM to detect both fine and coarse changes in the images, with each successive extractor operates on an input frame with half the resolution of the previous level's inputs. These input frames then undergo several layers of convolution blocks to extract high-level feature representations and bi-directional motion

125 between the input and interpolated frames. The feature representations, coupled with the bi-directional motion, synthesize the high-level representations of the intermediate frame. The decoder module of FILM then uses these high-level representations to reconstruct the intermediate images. During the training process, the weights in the convolution blocks within both the encoder and decoder are continually adjusted to minimize the differences between the model-predicted images and the training images. Having undergone training with over 100,000 unique videos, the pre-trained FILM model exhibits the capability to

130 discern rotation, scaling, colour changes, movements, and more intricate deformations, making it ideally suited for creating interpolation images for novel tasks.

We use the pre-trained FILM model to create interpolated images without conducting additional training. By running the FILM model with our image dataset (comprising 22 images for a given CO_2 concentration at each time-interval, n, it yields 21, n-1, interpolation images. During the second round of prediction, both the original and interpolated images are used to generate

135 further interpolation images between the original images and the first-round interpolation images. By iterating this operation k times, $(2^{k-1}) \times (n-1)$ interpolation images are generated in total, and 2^{k-1} images are formed between each of the two original images. Given that the maximum age gap between the original model forcing is 55 Ma, we executed 6 iterations of prediction to produce 63 interpolation images between each pair of original images and selected at most 54 out of the 63 images to represent the dataset for each million year time point. These selections were made evenly across the 63 images to ensure a

140 uniform and representative sampling for each million year in the dataset.

3 Validating the method and interpolated datasets

3.1 Validation of interpolation using the PaleoDEM dataset

While the FILM model has demonstrated a robust ability to interpolate complex changes between input and intermediate frames, largely due to extensive training on over 100,000 videos, its performance has not yet been scrutinized in the context

145 of paleogeographic and paleoclimate datasets. To test this application, we first apply the FILM model to a high-time-resolution paleo-digital elevation dataset (PaleoDEM, Scotese and Wright, 2018) that delineates the evolving distributions of land and oceans over the past 540 million years in five million-year intervals. By partitioning the PaleoDEM dataset into input and

intermediate frames, we could contrast the FILM-predicted frames with the actual intermediate frames, quantifying their disparities. The similarity between the predicted and actual frames serves as a testament to FILM's efficacy in capturing plate

150 movements and transformations.

The PaleoDEM dataset comprises 109 files, each file includes estimations of land surface elevation and ocean depth, measured in meters, at a resolution of 1×1 degrees. Hence, the PaleoDEM is a 361× 181 dimensional dataset where 361 represents longitude (ranging from -180 to 180) and 181 denotes latitude (ranging from -90 to 90). To make the PaleoDEM comparable with our 48×40 dimensional dataset, we applied nearest-neighbour interpolation, a downsampling algorithm, to downscale the

155 PaleoDEM resolution to 48×40 by assigning the values of the closest pixel to the new pixel locations. Moreover, any location with elevation values greater than zero was characterized as land (denoted by 255 in pixel values), with the remainder classified as oceans (denoted by 0 in pixel values).

The PaleoDEM was partitioned into distinct input and output datasets using temporal intervals of 10 million years (Myrs), 20 Myrs, and 40 Myrs. This strategy facilitated three separate validation procedures. In the first validation approach, we use a 10

160 Myr interval. The PaleoDEM sequences from 540 million years ago (Ma), 530 Ma, etc., up to 0 Ma, were designated as the input dataset. Correspondingly, the sequences from 535 Ma, 525 Ma, and so forth, until 5 Ma, were selected as the output dataset which the FILM model outputs will be compared against. For the second validation process, we adopted a 20 Myr interval. This time, the input dataset comprised PaleoDEM sequences from 540 Ma, 520 Ma, etc., down to 0 Ma. The sequences from 535 Ma, 530 Ma, 525 Ma, etc., to 5 Ma served as the output dataset. An identical procedure was executed for the third

165 validation scheme, but with a 40 Myr interval. In each case we use the input dataset to make interpolation frames using FILM, and by comparing the predicted frames with the real frames in the output dataset, the model's predictive accuracy can be assessed.

For a systematic and comprehensive investigation of the FILM model performance, we calculate the Structural Similarity Index (SSIM), Peak Signal-to-Noise Ratio (PSNR), two-dimensional correlation and Normalized Root Square of the Mean

170 Square Error (NRMSE), which are the most widely utilized performance measurements for frame interpolation (Wang et al., 2004; Dong et al., 2023). These widely accepted metrics can help us gauge differences between the actual intermediate frames and the predicted frames. SSIM is a metric to detect perceived changes that takes into account luminance, contrast, and structural information of the image. Given the real intermediate frame $I^R(x, y)$ and the FILM-predicted frame $\hat{I}(x, y)$, the SSIM is defined as:

175
$$\text{SSIM} = \frac{\left(2\mu_{\hat{I}}\mu_{I^R} + c_1\right) \times \left(2\sigma_{\hat{I}I^R} + c_2\right)}{\left(\mu_{\hat{I}}^2 + \mu_{I^R}^2 + c_1\right) \times \left(\sigma_{\hat{I}}^2 + \sigma_{I^R}^2 + c_2\right)},\tag{1}$$

where $\mu_{\hat{I}}$ and μ_{I^R} are the mean of $\hat{I}$ and I^R, $\sigma_{\hat{I}}^2$ and $\sigma_{I^R}^2$ are the variance of the $\hat{I}$ and I^R, $\sigma_{\hat{I}I^R}$ is the covariance between $\hat{I}$ and I^R, c_1 and c_2 are constants to avoid instability when the denominator is close to zero. Values of SSIM ranges from -1 to 1, representing inversely identical and identical images, respectively.

The PSNR is a ratio between the maximum possible power of the image and the power of corrupting noise that affects

180 the fidelity of the image's representation, it is defined as:

$$\text{PSNR} = 10 \times \log_{10} \times \left(\frac{L^2}{\frac{1}{N} \Sigma_{x,y}^N \left(I^R(x,y) - \hat{I}(x,y) \right)^2} \right), \tag{2}$$

where L is the maximum pixel values (255 for our images), N is the number of pixels in the image. The greater the value of PSNR, the better the performance of the frame interpolation.

The two-dimension correlation is defined as the Pearson correlation coefficient calculated over the two dimensions of $I^R(x,y)$

185 and $\hat{I}(x,y)$. Values of two-dimension correlation are between -1 and 1, where 1 indicates the two images are identical, 0 means the images are uncorrelated, and -1 means the images are inversely identical. The NRMSE measures the differences in pixel values between the $I^R(x,y)$ and the $\hat{I}(x,y)$. In contrast to the other metrics, lower NRMSE values indicates better performance (range between 0 and 1).

$$\text{NRMSE} = \frac{\sqrt{\frac{1}{N} \Sigma_{x,y}^N \left(I^R(x,y) - \hat{I}(x,y) \right)^2}}{I^R(x,y)_{max} - I^R(x,y)_{min}}, \tag{3}$$

190 Figure 2 and Table 1 detail the quantitative assessments derived from our implemented numerical metrics, indicating the performance of the FILM technique when applied to the PaleoDEM dataset. During the validation phase, using a 10 Myr interval, the frames predicted by FILM demonstrated remarkable congruity with the actual frames. This is evidenced by the high values of SSIM, PSNR, and two-dimensional correlation, and a low value of NRMSE. The SSIM and 2D-correlation maintain consistently high values throughout the entire time span from 540 Ma to 0 Ma. This highlights the consistent

195 performance of FILM, and its capacity to capture the paleogeographic reorganization in the PaleoDEM dataset across Phanerozoic timescales.

Despite good performance in general, the PSNR and NRMSE depict a trend over time, with PSNR values decreasing and NRMSE values increasing over time – both suggesting a poorer fit to the real intermediate frames at time points closer to the present day. The observed trend is somewhat expected as the maps closer to the present day – which can draw on larger

200 geological evidence bases – tend to exhibit more fine scale features, such as land patches depicted as only one or a few pixels in the frames (Fig. 3). During frame interpolation, fine scale features such as minor land patches are more easily overlooked. Consequently, metrics like PSNR and NRMSE, which quantify the pixel discrepancies between the predicted and actual frames, underscore this pattern of detail loss.

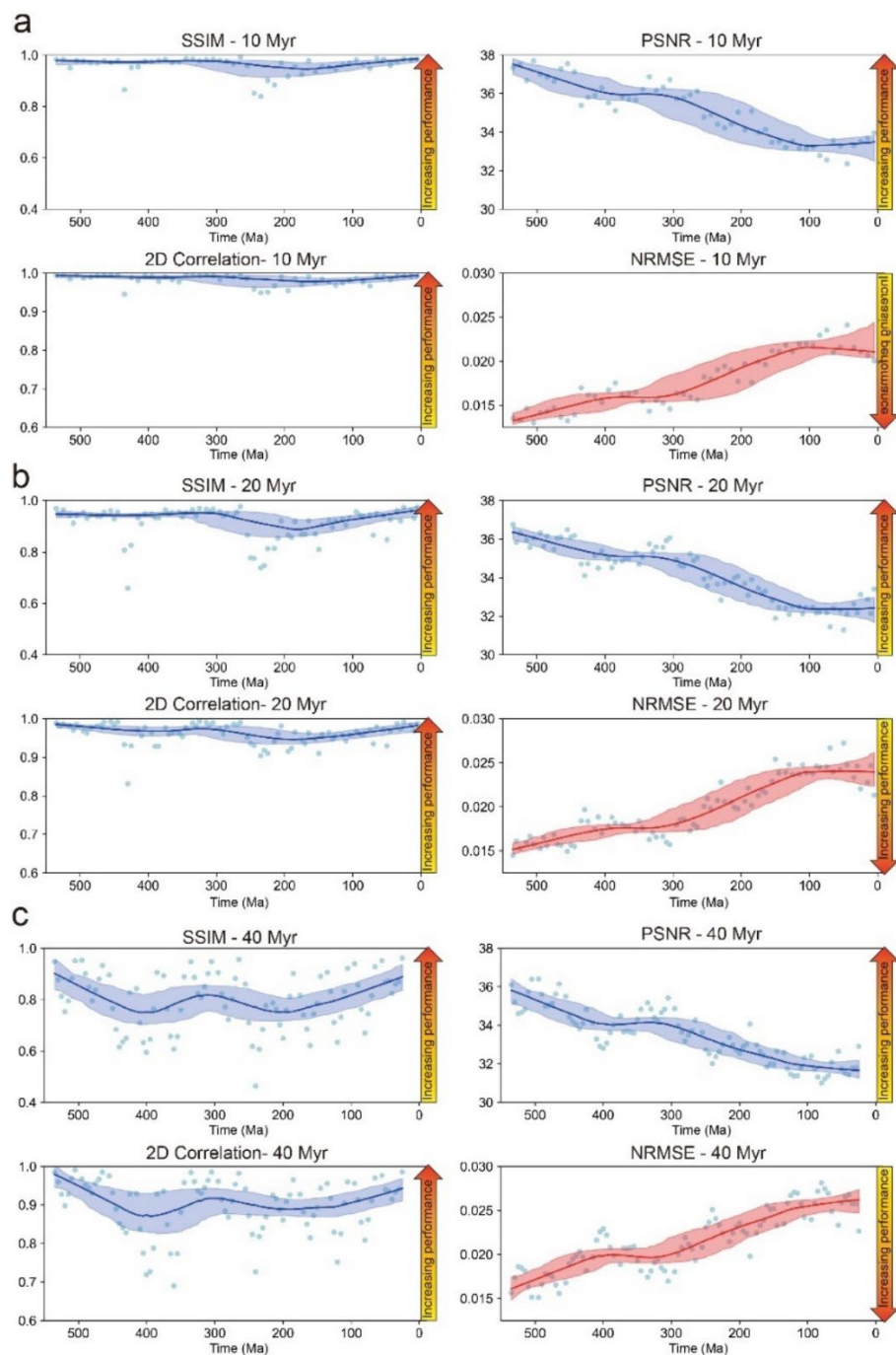



Figure 2. Comparative Evaluation of Performance Utilizing (a) 10 Ma, (b) 20 Ma, and (c) 40 Ma Intervals within the PaleoDEM Dataset. The blue line represents the LOWESS (Locally Weighted Scatterplot Smoothing) fitting curve with a fraction of 0.4, serving as an indicator of the central trend. The light blue shaded bands illustrate the confidence interval, derived from a 1000-resampling bootstrap method, providing a measure of the precision and uncertainty of the estimated fit. The NRMSE is represented in red colour because it signifies error, thus its trend is converse to the other three metrics. See text for detailed discussions.

210

Table 1. Numerical evalution on the PaleoDEM dataset

	10 Myr			20 Myr			40 Myr		
	Mean	Median	SD	Mean	Median	SD	Mean	Median	SD
SSIM	0.96	0.97	0.03	0.91	0.94	0.06	0.80	0.81	0.11
PSNR	35.12	35.25	1.50	34.17	34.50	1.47	33.46	33.49	1.38
2D correlation	0.98	0.99	0.01	0.96	0.97	0.03	0.90	0.93	0.07
NRMSE	0.02	0.02	0.00	0.02	0.02	0.00	0.02	0.02	0.00

SD, standard deviation. See text for other abbreviations.

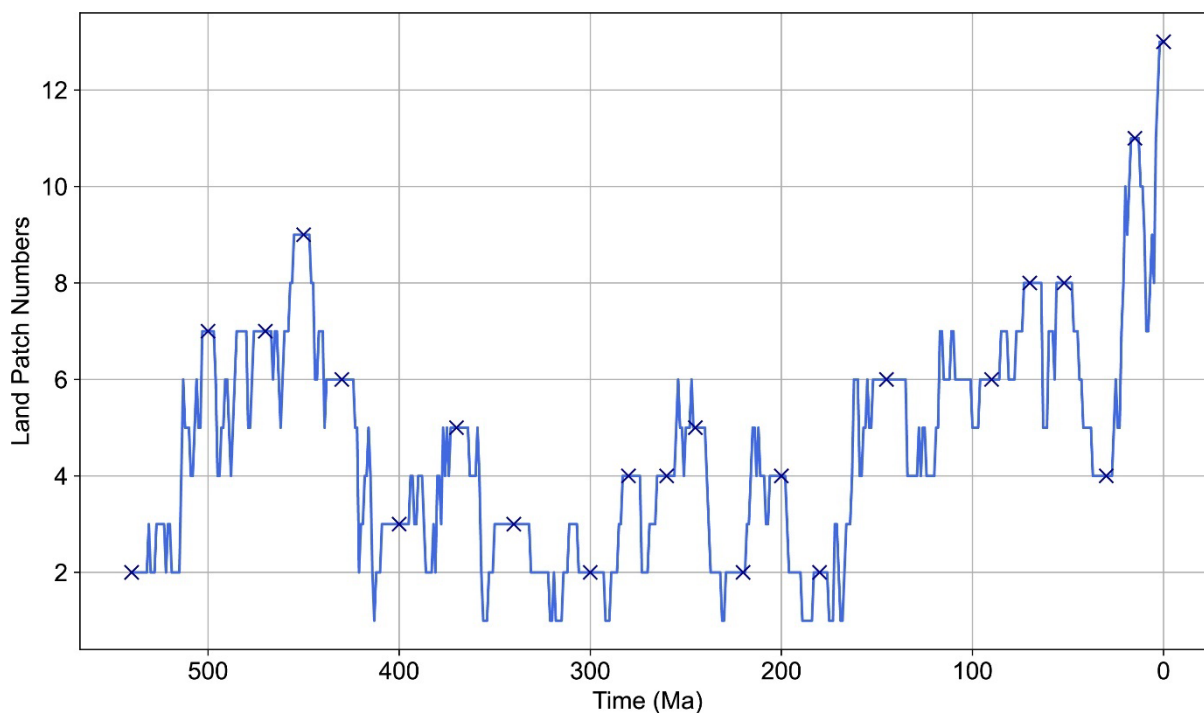



Figure 3. Temporal evolution of land patch density using PaleoDEM from 540 Ma to present. This figure indicates an overall increase of land patch density in the PaleoDEM dataset, attributed to the inclusions of more details in the more recent frames. This increasing trend
215   may account for the patterns observed in PSNR and NRMSE. A land patch is defined as a contiguous grouping of land pixels. The density is calculated by dividing the number of land patches by the total frame size (40×48). The dark blue cross indicating the twenty-two time intervals used in the FOAM dataset.

For the comparison at 10 Myr and 20 Myr intervals, a high degree of similarity between the predicted and actual frames was
220   discernible, as evidenced by the mean values of SSIM exceeding 0.8, 2D-correlation over 0.9, PSNR above 32, and NRMSE

less than 0.025. For the 40 Myr interval validation, the mean values of SSIM were greater than 0.7, the mean values of 2D-correlation was above 0.80, the mean value of PSNR was over 31, and the mean values of NRMSE remained below 0.03. As anticipated, the performance deteriorates when the time interval is increased (Argaw and Kweon, 2022), which can be attributed to the more significant changes between the two input frames.

225   In addition to the numerical evaluation, we also performed visual inspections to detect obvious discrepancies between the original frames and the predicted frames. Across different time periods, predicted frames were generally visually comparable to original ones, with greater congruency than between different paleogeographic reconstructions for the same time period (e.g. Scotese and Wright, 2018; Marcilly et al., 2021). The major deviations between the predicted and original frames were attributable to missing pixels or mismatched pixel values, and there were no changes in the placements of major land masses

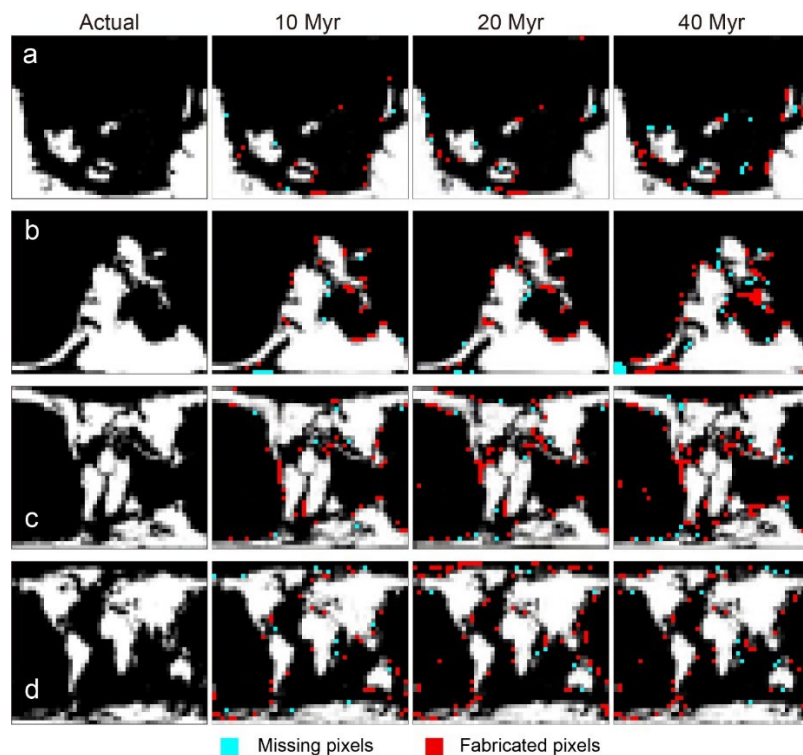
230   (Fig. 4). Given that the mean temporal interval for SCION model forcings is approximately 25 Ma, our numerical assessments and visual evaluations in comparing the FILM-predicted frames with the actual frames from the PaleoDEM dataset suggest that FILM possesses the capability to discern plate movements and transformations on a time scale appropriate to building interpolation frames for the SCION model forcings.

235

Figure 4. Comparative visualization of actual PaleoDEM and model-predicted frames at selected time intervals. This figure illustrates the comparative visualizations at (a) 535 Ma, (b) 315 Ma, (c) 105 Ma, and (d) 25 Ma. The grey pixels represent areas impacted by nearest-neighbour downsampling in the paleogeographic maps. The missing pixels indicate areas present in the original frames but absent in the model-predicted frames; the fabricated pixels show areas absent in the original frames but present in the model-predicted frames.

3.2 Output and validation of intermediate FOAM temperature and runoff datasets

Our second validation focuses on the temperature and runoff data in our interpolated DeepFOAM dataset. Given the established correlation between increased CO_2 levels and a rise in global average temperature and total runoff, we anticipated that our interpolated data should mirror this trend if FILM is effectively applied to our dataset. Consequently, the alignment of interpolated temperature and runoff trends with those of the original model forcings would underscore the successful performance of FILM in our dataset.

The SCION model forcing dataset is constructed with 26 distinct CO_2 levels, encompassing an extensive range of CO_2 concentrations, from 10 ppm to 112,000 ppm (Mills et al., 2021). This dataset has been extrapolated and in-filled from an average of 5 runs of FOAM per continental configuration, which was made possible because of a predictable logarithmic response of temperature and runoff to CO_2 change in the model. Such a wide range of CO_2 levels is required to aid in model spinup where the model conditions can be far from equilibrium. Typically, Phanerozoic runs of the SCION model do not stray beyond the range of the initial dataset from FOAM. Figure 5 plots the global average temperature and runoff over these 26 CO_2 levels, with each of the 22 lines representing a unique time interval (i.e. continental configuration) in FOAM. It exhibits an overall upward trend in temperature and runoff as CO_2 concentrations ascend. It should be briefly noted that the 0 Ma climate ensemble is computed from only one run of FOAM at preindustrial CO_2, adding a generalized trend for higher and lower CO_2 levels. This is because the SCION model is not designed to perform simulations at present day conditions, and only uses this state for spin up and parameter tuning.

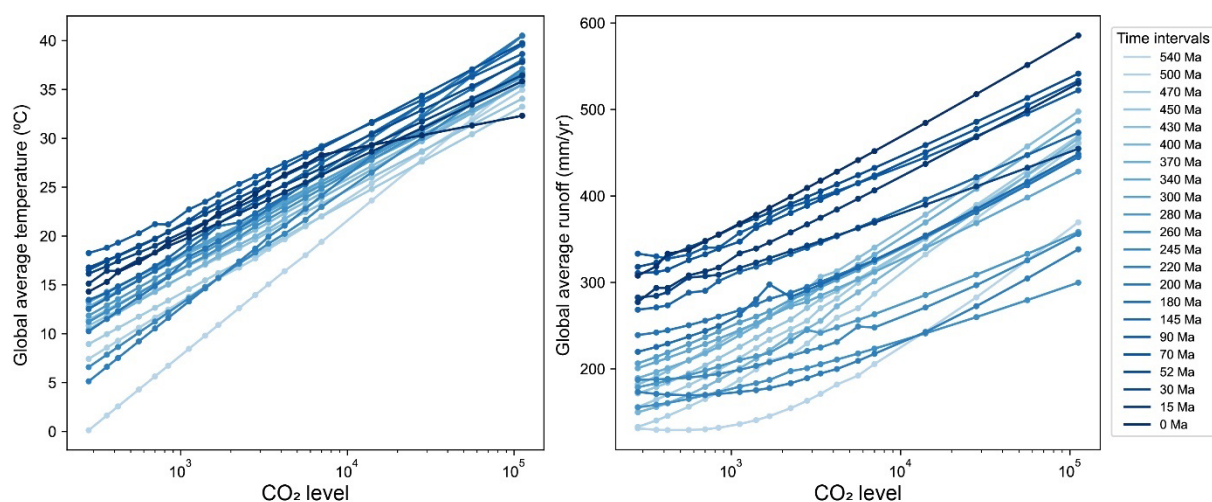



Figure 5. Global average surface air temperature and average continental runoff over CO_2 levels in the FOAM dataset. The representation is color-coded with a descending blue gradient, where light blue represents more ancient conditions, and dark blue denotes more recent scenarios. Note that the 0 Ma curve is built from only one CO_2 level (preindustrial), with an arbitrary increase in temperature and runoff applied when CO_2 levels change.

Given the known behaviour of the FOAM climate model, our FILM-interpolated temperature and runoff grids should exhibit
similar patterns, and serve as a method to evaluate the effectiveness of the FILM interpolation technique for this purpose.
Figure 6 plots global average temperature changes in response to varying CO_2 levels for each of the intermediate frames
produced by FILM. The FOAM dataset contains values across 22 time intervals, leading to the 21 subplots that show the
average temperature changes for all intermediate frames between these 22 time intervals. The interpolated temperature values
are well-aligned with the original dataset, displaying a consistent trend for escalating CO_2 concentrations. Figure 7 shows the
runoff trends in response to varying CO_2 levels. Similar to the temperature trends, they exhibit patterns with respect to CO_2
that are analogous to those of the original runoff data. Given the more scattered distributions and more substantial changes in
runoff between continental configurations, the interpolated average runoff exhibits a more varied pattern between the keyframe
images, with interpolated intermediate runoff averages that can be both higher and lower than the end-members form which
they are derived. Capturing runoff changes on small land patches remains a particularly challenging task for the deep learning
methods, unlike the case with homogeneous variables like temperature, where FILM is more adept.

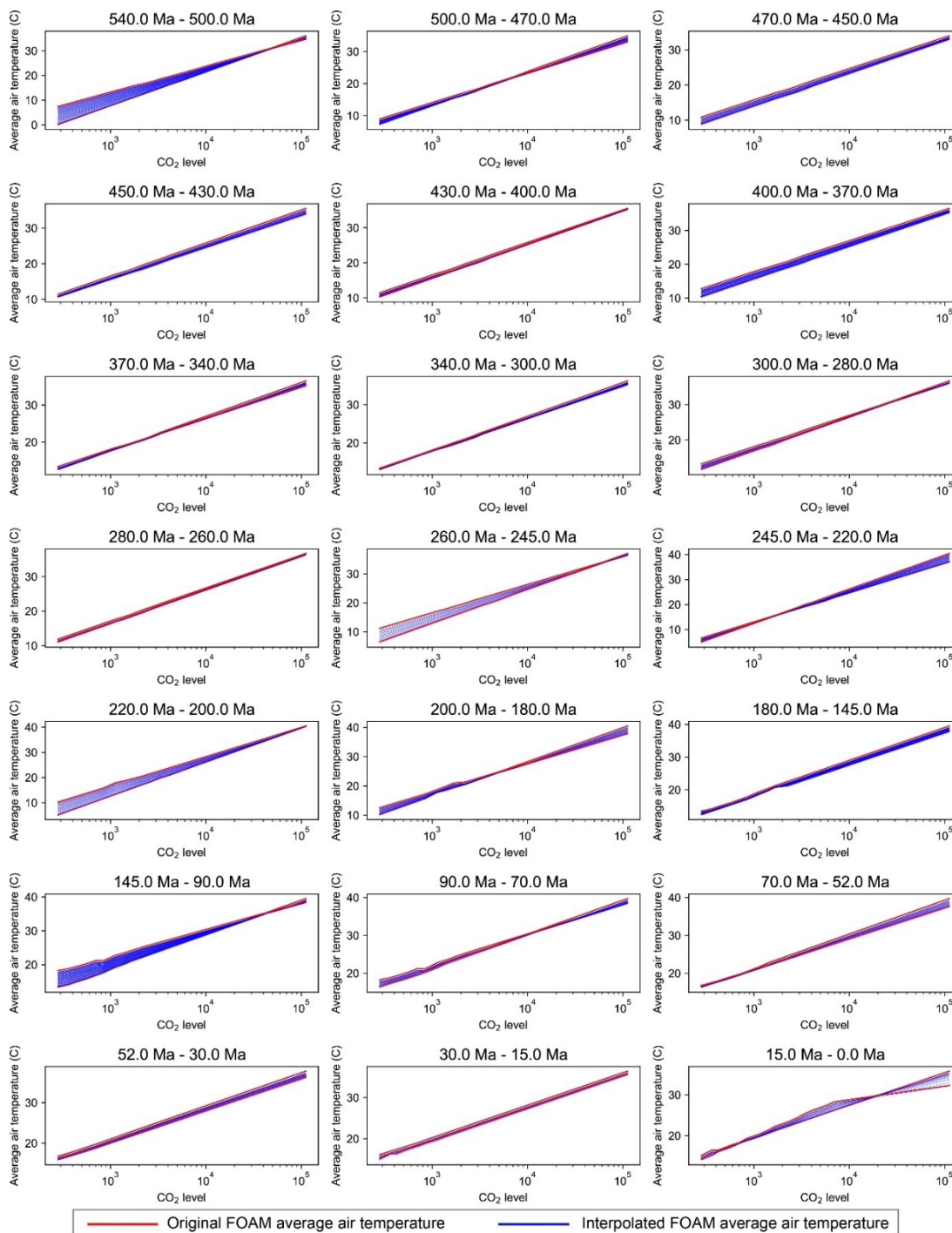



Figure 6. Trends in global temperature changes corresponding to varying CO₂ levels. Each subplot features one of the 21 distinct time intervals between members of the FOAM dataset. Within each subplot, the red lines delineate the keyframe average temperature variations and the blue lines show the Deep Learning-interpolated average temperature at each 1 Myr.

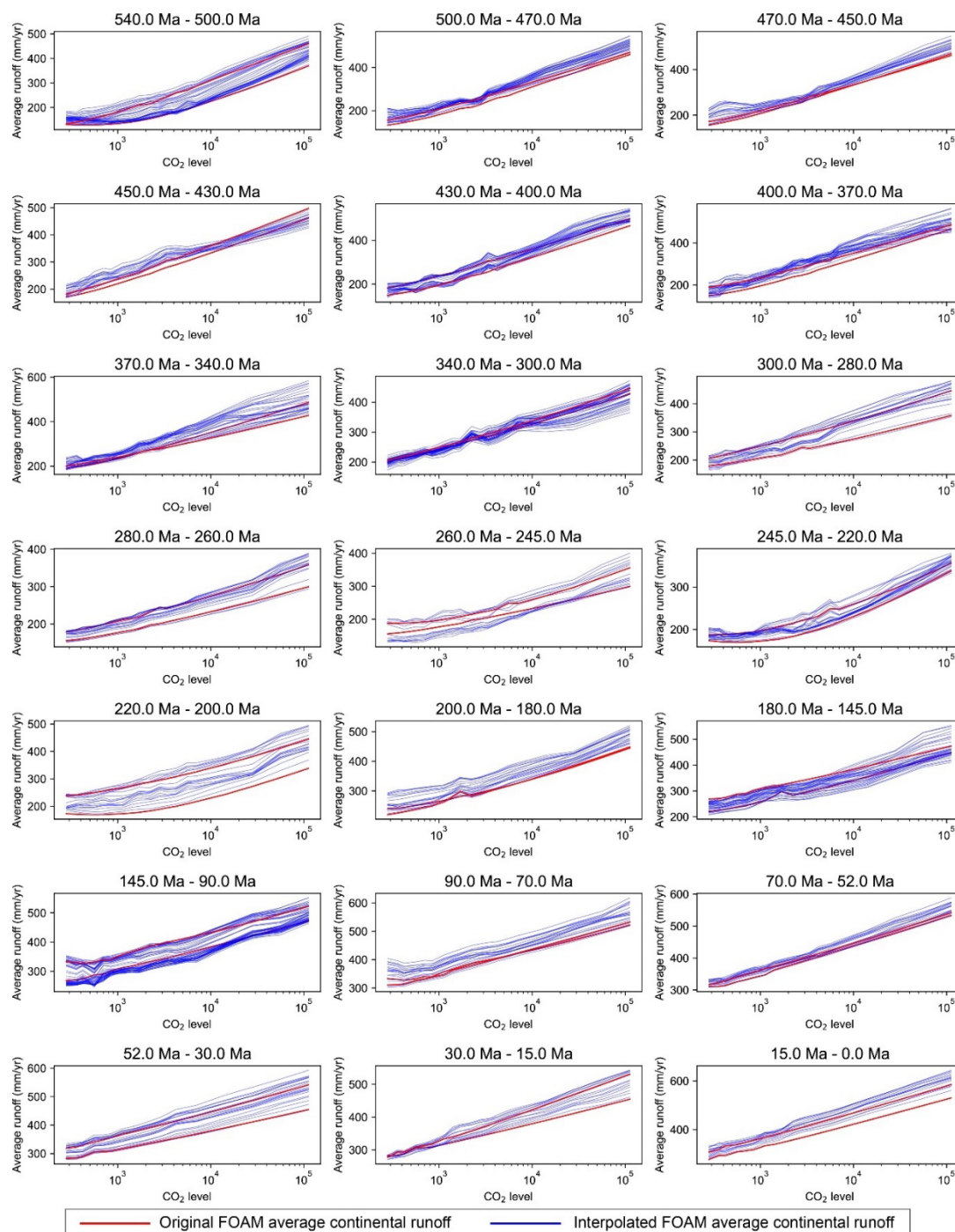



Figure 7. Trends in runoff changes corresponding to varying CO_2 levels. As with Fig. 6, the 21 subplots represent the runoff changes between the original runoff outputs from the FOAM dataset. The red lines are original average runoff in the FOAM dataset, and blue lines are Deep Learning interpolated data.

4 One-million-year-forcing outputs of the SCION model and comparisons to original model.

We now run the SCION model (version 1.1.6; github.com/bjwmills/SCION) subject to the new 'DeepFOAM' dataset, which directly replaces the FOAM dataset used in the standard model. This update requires no additional modification of the SCION model. The key model predictions for atmospheric CO_2, atmospheric O_2 and global average surface temperature are shown in
290 Fig. 8. These new model predictions follow the original model closely at the defined time points for the FOAM dataset (see red dots in Fig. 8), but they have a more detailed structure between these points and show several interesting deviations from the previous model, which are due to the new FILM-interpolated climate fields which have replaced linear interpolation between the widely-spaced previous fields.

Most notably, the SCION-DeepFOAM output for atmospheric CO_2 shows a warming spike around the Permian-Triassic
295 boundary and a cooling spike in the Early Jurassic. These results are in line with geological evidence for extreme warmth at the Permian-Triassic extinction (Berner, 2002; Fielding et al., 2019; Yang et al., 2021; Wu et al., 2023) and a cool early Jurassic (Scotese et al., 2021). To investigate these outputs, Figure 9 plots variations in runoff and chemical weathering rates spanning 260-245Ma. The original FOAM dataset contains runoff values at 260 Ma and 245 Ma, both of which indicate high runoff in the low latitudes (marked by red arrows in Fig. 9) surrounding the Paleo-Tethys Ocean. As a consequence, chemical weathering
300 rates in these zones are comparably high, being influenced by both runoff and temperature (Maffre et al., 2018; Mills et al., 2021). Contrastingly, for the 253 Ma interval, predicted via Deep Learning, the South China plate exhibits diminished runoff values and correspondingly lower chemical weathering rates (marked by green arrows in Fig. 9). The observed decrease in weathering aligns with geological records which highlight significant aridity in South China during the Permian-Triassic Boundary (Xu et al., 2023), and it is this reduced chemical weathering that leads to elevated atmospheric CO_2 predictions for
305 this time in the SCION model. However, this result requires further scrutiny, as while the Deep Learning approach affords a continuous dataset, there is no specific physical mechanisms underpinning the results. Testing this hypothesis still requires a climate model run for the period of interest.

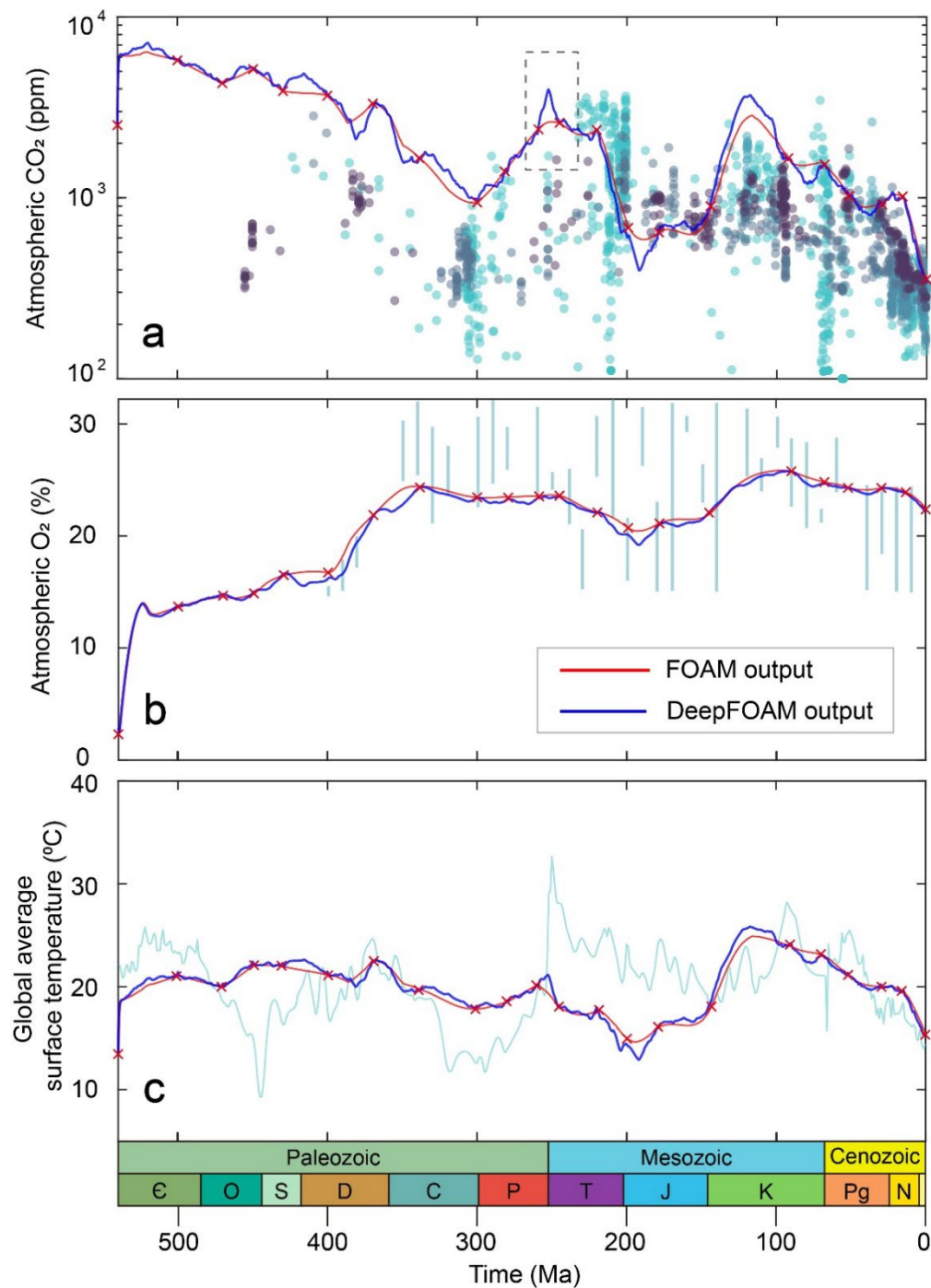



Figure 8. Phanerozoic output comparisons between the SCION-FOAM and SCION-DeepFOAM. (a) atmospheric CO_2 concentration (proxy data represented by scatter symbols; sources: Foster et al., 2017; Witkowski et al., 2018), (b) atmospheric O_2 concentration (proxy data represented by vertical lines; sources: Glasspool and Scott, 2010; Lenton et al., 2016), and (c) global average surface temperature (proxy data represented in cyan; source: Scotese et al., 2021). The twenty-two red dots correspond to the original time intervals in the FOAM dataset. The dotted box in Fig. 8a marks the significant CO_2 increase at 253Ma.

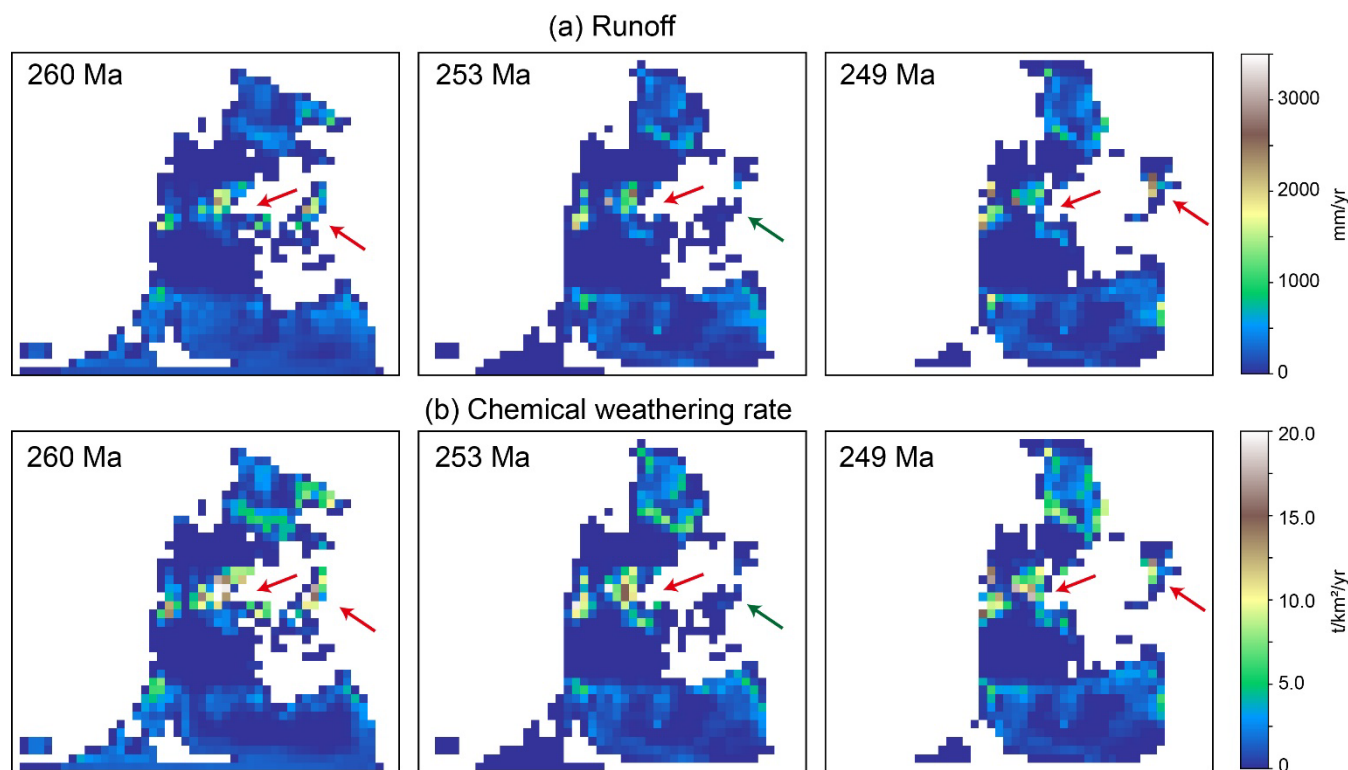



Figure 9. Runoff (a) and chemical weathering rates (b) for 260 Ma, 253 Ma, and 249 Ma. During the 260-245 Ma period, the low-latitude regions surrounding the Paleo-Tethys Ocean exhibit high runoff and corresponding high weathering (highlighted by red arrows). These characteristics are derived from the original FOAM dataset. However, during the 253 Ma interval, the Deep Learning method predicts reduced runoff and corresponding decreased weathering. This reduction is primarily attributed to the lowered runoff in eastern low-latitude plates, such as South China (marked by the green arrow).

5 Conclusions and future work

We show that deep learning can produce realistic continuous plate geographical motions, and associated paleoclimates, from snapshots approximately 20 Myrs apart. The FILM Deep Learning technique can be applied to the forcing set for the SCION climate-biogeochemical model, which reduces the need for the model to interpolate linearly between time points, and thus allows a greater degree of climate variability, as well as making the model easier to use for testing specific events at known times that are not within its original forcing set. However, the efficacy of interpolating runoff data, compared to that of paleogeography and temperature, is diminished by its heterogeneous distribution. The new forcing set creates important differences in the model output demonstrating the utility of Deep Learning for rapid preliminary analysis, but further conclusions on these differences rely on performing new climate model runs at these specific times. It is intuitively understood that these interpolation results can be enhanced with a higher-resolution original dataset, a presumption corroborated by the PaleoDEM validation. In the PaleoDEM validation process, interpolation results derived from a 10 Myr interval exhibited

superior accuracy compared to those from 20 Myr and 40 Myr intervals. Thus, future work to link paleoclimate and biogeochemistry should aim to run climate models at least every 10 Myrs, but can potentially rely on Deep Learning interpolation to upscale this to 1 Myr or finer time resolutions. Such fine time resolutions would allow more precise

335   investigation of the paleoclimate and fossil record for specific events, and may also permit new approaches where modelled surface processes (e.g. vegetation) are able to distribute in space from one timestep to the next.

Code availability

The FILM code is available at https://github.com/google-research/frame-interpolation and Zenodo repository at https://zenodo.org/records/10602810. SCION v1.1.6 code is available at https://github.com/bjwmills/SCION and permanently

340   archived at https://zenodo.org/records/7790169, codes for figure creation is available at https://zenodo.org/records/10578608.

Author contribution

DZ, AM, and BM designed this study; YG and YD provided the FOAM dataset; DZ performed the interpolation and validation; DZ and BM wrote the manuscript draft; all authors reviewed and edited the manuscript.

Competing interests

345   The authors declare that they have no conflict of interest.

Acknowledgements

The authors would like to thank Stephen Hunter for useful discussions. DZ is funded by the National Science Foundation of China (Nos. 42050104 and 42202125) and IUGS-Deep-time Digital Earth Big Science Program and BJWM is funded by the UK Natural Environment Research Council (NE/S009663/1).

350   **References**

Argaw, D. M. and Kweon, I. S.: Long-term video frame interpolation via feature propagation, in: Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, 3543–3552, 2022.

Berner, R. A.: Examination of hypotheses for the Permo-Triassic boundary extinction by carbon cycle modeling, Proc. Natl. Acad. Sci. U. S. A., 99, 4172–4177, https://doi.org/10.1073/pnas.032095199, 2002.

355   Chen, G., Cheng, Q., Lyons, T. W., Shen, J., Agterberg, F., Huang, N., and Zhao, M.: Reconstructing Earth's atmospheric oxygenation history using machine learning, Nat. Commun., 13, 5862, 2022.

Dong, J., Ota, K., and Dong, M.: Video Frame Interpolation: A Comprehensive Survey, ACM Trans. Multimed. Comput. Commun. Appl., 19, https://doi.org/10.1145/3556544, 2023.

Donnadieu, Y., Pierrehumbert, R., Jacob, R., and Fluteau, F.: Modelling the primary control of paleogeography on Cretaceous
360 climate, Earth Planet. Sci. Lett., 248, 426–437, 2006.

Fielding, C. R., Frank, T. D., McLoughlin, S., Vajda, V., Mays, C., Tevyaw, A. P., Winguth, A., Winguth, C., Nicoll, R. S., Bocking, M., and Crowley, J. L.: Age and pattern of the southern high-latitude continental end-Permian extinction constrained by multiproxy analysis, Nat. Commun., 10, https://doi.org/10.1038/s41467-018-07934-z, 2019.

Foster, G. L., Royer, D. L., and Lunt, D. J.: Future climate forcing potentially without precedent in the last 420 million years,
365 Nat. Commun., 8, 14845, 2017.

Glasspool, I. J. and Scott, A. C.: Phanerozoic concentrations of atmospheric oxygen reconstructed from sedimentary charcoal, Nat. Geosci., 3, 627–630, 2010.

Goddéris, Y., Donnadieu, Y., Le Hir, G., Lefebvre, V., and Nardin, E.: The role of palaeogeography in the Phanerozoic history of atmospheric CO2 and climate, Earth-Science Rev., 128, 122–138, https://doi.org/10.1016/j.earscirev.2013.11.004, 2014.

370 Hinton, G. E., Osindero, S., and Teh, Y.W.: A Fast Learning Algorithm for Deep Belief Nets, Neural Comput., 18, 1527–1554, 2006.

Ian Goodfellow and Yoshua Bengio and Aaron: Deep learning, 2016.

Lenton, T. M. and Watson, A. J.: Biotic enhancement of weathering, atmospheric oxygen and carbon dioxide in the Neoproterozoic, Geophys. Res. Lett., 31, 2004.

375 Lenton, T. M., Dahl, T. W., Daines, S. J., Mills, B. J. W., Ozaki, K., Saltzman, M. R., and Porada, P.: Earliest land plants created modern levels of atmospheric oxygen, Proc. Natl. Acad. Sci., 113, 9704–9709, 2016.

Maffre, P., Ladant, J. B., Moquet, J. S., Carretier, S., Labat, D., and Goddéris, Y.: Mountain ranges, climate and weathering. Do orogens strengthen or weaken the silicate weathering carbon sink?, Earth Planet. Sci. Lett., 493, 174–185, https://doi.org/10.1016/j.epsl.2018.04.034, 2018.

380 Maher, K. and Chamberlain, C. P.: Hydrologic regulation of chemical weathering and the geologic carbon cycle, Science (80-.)., 343, 1502–1504, 2014.

Marcilly, C. M., Torsvik, T. H., Domeier, M., and Royer, D. L.: New paleogeographic and degassing parameters for long-term carbon cycle models, Gondwana Res., 97, 176–203, 2021.

Mills, B. J. W., Donnadieu, Y., and Goddéris, Y.: Spatial continuous integration of Phanerozoic global biogeochemistry and
385 climate, Gondwana Res., 100, 73–86, https://doi.org/10.1016/j.gr.2021.02.011, 2021.

Niklaus, S., Mai, L., and Liu, F.: Video frame interpolation via adaptive separable convolution, in: Proceedings of the IEEE international conference on computer vision, 261–270, 2017.

Reda, F., Kontkanen, J., Tabellion, E., Sun, D., Pantofaru, C., and Curless, B.: FILM: Frame Interpolation for Large Motion, Lect. Notes Comput. Sci. (including Subser. Lect. Notes Artif. Intell. Lect. Notes Bioinformatics), 13667 LNCS, 250–266,
390 https://doi.org/10.1007/978-3-031-20071-7_15, 2022.

Reichstein, M., Camps-Valls, G., Stevens, B., Jung, M., Denzler, J., Carvalhais, N., and Prabhat: Deep learning and process understanding for data-driven Earth system science, Nature, 566, 195–204, https://doi.org/10.1038/s41586-019-0912-1, 2019.

Royer, D. L., Berner, R. A., Montañez, I. P., Tabor, N. J., and Beerling, D. J.: Co~ 2 as a primary driver of phanerozoic climate, GSA today, 14, 4–10, 2004.

395 Scotese, C. R.: An atlas of Phanerozoic paleogeographic maps: the seas come in and the seas go out, Annu. Rev. Earth Planet. Sci., 49, 679–728, 2021.

Scotese, C. R. and Wright, N.: PALEOMAP paleodigital elevation models (PaleoDEMS) for the Phanerozoic, Paleomap Proj, 2018.

Shi, Z., Xu, X., Liu, X., Chen, J., and Yang, M.-H.: Video frame interpolation transformer, in: Proceedings of the IEEE/CVF

400 Conference on Computer Vision and Pattern Recognition, 17482–17491, 2022.

Walker, J. C. G., Hays, P. B., and Kasting, J. F.: A negative feedback mechanism for the long-term stabilization of Earth's surface temperature, J. Geophys. Res. Ocean., 86, 9776–9782, 1981.

Wang, Z., Bovik, A. C., Sheikh, H. R., and Simoncelli, E. P.: Image quality assessment: from error visibility to structural similarity, IEEE Trans. image Process., 13, 600–612, 2004.

405 West, A. J.: Thickness of the chemical weathering zone and implications for erosional and climatic drivers of weathering and for carbon-cycle feedbacks, Geology, 40, 811–814, 2012.

Witkowski, C. R., Weijers, J. W. H., Blais, B., Schouten, S., and Sinninghe Damsté, J. S.: Molecular fossils from phytoplankton reveal secular P co2 trend over the Phanerozoic, Sci. Adv., 4, eaat4556, 2018.

Wu, H., Zhang, X., Xie, W., Zhang, Y., and Wang, Y.: Boost Video Frame Interpolation via Motion Adaptation, arXiv Prepr.

410 arXiv2306.13933, 2023.

Xu, G., Shen, J., Algeo, T. J., Yu, J., Feng, Q., Frank, T. D., Fielding, C. R., Yan, J., Deconink, J. F., and Lei, Y.: Limited change in silicate chemical weathering intensity during the Permian–Triassic transition indicates ineffective climate regulation by weathering feedbacks, Earth Planet. Sci. Lett., 616, https://doi.org/10.1016/j.epsl.2023.118235, 2023.

Yang, W., Wan, M., Crowley, J. L., Wang, J., Luo, X., Tabor, N., Angielczyk, K. D., Gastaldo, R., Geissman, J., and Liu, F.:

415 Paleoenvironmental and paleoclimatic evolution and cyclo-and chrono-stratigraphy of upper Permian–Lower Triassic fluvial-lacustrine deposits in Bogda Mountains, NW China—Implications for diachronous plant evolution across the Permian–Triassic boundary, Earth-Science Rev., 222, 103741, 2021.

Zheng, D., Wu, S., Ma, C., Xiang, L., Hou, L., Chen, A., and Hou, M.: Zircon classification from cathodoluminescence images using deep learning, Geosci. Front., 13, 101436, https://doi.org/10.1016/j.gsf.2022.101436, 2022.

420