



# 1 A quantitative decoupling analysis (QDA v1.0) method for assessing 2 the contributions of meteorology, emissions, and chemistry to fine 3 particulate pollution

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11 **Abstract.** A comprehensive understanding of the effects of meteorology, emissions, and chemistry on severe haze is critical  
12 in the mitigation of air pollution. However, such an understanding is greatly hindered by the nonlinearity of atmospheric  
13 systems. In this study, we developed the quantitative decoupling analysis (QDA) method to quantify the effects of emissions,  
14 meteorology, chemical reactions, and their nonlinear interactions on fine particulate matter (PM<sub>2.5</sub>) pollution by running built-  
15 in scenario simulations in each model step. Different from previous methods, the QDA method achieves a fully decomposed  
16 analysis of hourly changes in the PM<sub>2.5</sub> concentration during pollution events into seven parts, including the pure  
17 meteorological contribution (M), the pure emissions contribution (E), the pure chemistry contribution (C), and the interactions  
18 among these processes (i.e., ME, MC, EC, and MCE). Via embedding the QDA method into the Weather Research and  
19 Forecasting–Nested Air Quality Prediction Modeling System, we employed this method and combined it with the Integrated  
20 Process Rate method to study a typical heavy haze episode in Beijing. We evaluate the model performance against *in situ*  
21 meteorological and air quality observations and describe the QDA analytical factors of this case. Results showed that M varied  
22 most significantly at different stages of the episode, from 0.21  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  during the accumulation stage to  $-11.82 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$   
23 during the removal stage, indicating that the pure meteorological contribution dominated the hourly fluctuation amplitude of  
24 the PM<sub>2.5</sub> concentration. M acted as the most important cleaner for PM<sub>2.5</sub> in non-polluting periods but stopped being effective  
25 at this and instead became a contributor in the accumulation stage such that PM<sub>2.5</sub> tended to grow rapidly under the  
26 superimposed influence of emissions and chemical processes, which would probably mark the beginning of a heavy pollution  
27 event. The contribution of E ranged from 0.63 to 0.88  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  owing to the diurnal variation of emissions. The pure chemical  
28 contribution was shown to increase with the level of haze, becoming the largest (0.37  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ) in the maintenance period,  
29 which was 25% higher than during the pre-contamination period. And C+CE made a significant contribution in the  
30 accumulation and maintenance stages, indicating that chemical reactions are more important in the polluted period than in  
31 other periods. Nonnegligible nonlinear effects exist among the processes of meteorology, emissions, and chemistry on PM<sub>2.5</sub>  
32 concentrations ( $-1.83$  to  $2.44 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ )—something that has generally been ignored in previous studies and during the



33 development of heavy-pollution control strategies. The nonlinear effects are helpful in eliminating the interference of other  
34 processes and obtaining a more purified result of the target process and have important indicative significances. The ratio of  
35 CE to C is positively correlated with the chemical speed. For precursors like  $\text{NH}_3$ , the smaller value of CE in the most polluted  
36 period indicated that  $\text{NH}_3$  was more deficient, and thus reducing emissions of it in that period would have had the most efficient  
37 controlling effect on the  $\text{PM}_{2.5}$ . This study highlights that the QDA method can be used to realize an in-depth understanding  
38 of the effects of adverse meteorological conditions in haze and to judge whether the precursors are excessive or not. Not only  
39 can the QDA method provide researchers and policymakers with valuable information for understanding the key factors behind  
40 heavy pollution, but it can also help modelers to identify the sources of uncertainties in numerical models.

## 41 1 Introduction

42 Atmospheric particulate matter, especially  $\text{PM}_{2.5}$  (fine particulates less than  $2.5 \mu\text{m}$  in diameter), can reduce visibility,  
43 degrade air quality, threaten human health, and increase mortality (Xing et al., 2021; Huang et al., 2014; Lelieveld et al., 2015;  
44 Evans et al., 2013; Fu et al., 2019; Janssen et al., 2013; Orellano et al., 2020). Over the past few decades, rapid industrialization  
45 and urbanization have led to severe haze pollution in China (Lu et al., 2019b; Chen et al., 2018; Liu et al., 2017; Hartmann et  
46 al., 2014). Beijing–Tianjin–Hebei (BTH) is one of the regions in China with the highest  $\text{PM}_{2.5}$  concentrations (Lin et al., 2015;  
47 Yang et al., 2020b). Annual concentrations of  $\text{PM}_{2.5}$  in BTH reached  $106 \mu\text{g}\cdot\text{m}^{-3}$  in 2013, almost 3 times higher than China's  
48 standard ( $35 \mu\text{g}\cdot\text{m}^{-3}$ ) and 10 times higher than that of the World Health Organization ( $10 \mu\text{g}\cdot\text{m}^{-3}$ ).

49 To mitigate the extremely severe and persistent haze in China and reduce air pollutant emissions, strict emission control  
50 policies have been implemented by the Chinese government. However, the ambient  $\text{PM}_{2.5}$  concentration is not only controlled  
51 by emissions, but also largely influenced by chemical formation processes and unfavorable meteorological conditions  
52 (Gelencsér et al., 2007; Jia et al., 2015; Wang et al., 2015; He et al., 2016; Sun et al., 2016). Numerous studies have stressed  
53 the importance of chemical formation in the occurrence of severe haze events in China (Huang et al., 2014; Sun et al., 2016;  
54 Chen et al., 2022). Unfavorable meteorological conditions associated with low wind speed, high humidity, temperature  
55 inversion, and low planetary boundary layer can lead to weak atmospheric dispersion conditions and suppress the diffusion of  
56 air pollutants (Chen et al., 2020b; Zheng et al., 2019). Moreover, the emissions, chemistry, and meteorological processes in  
57 the atmosphere also interact with each other. For example, high humidity not only promotes hygroscopic growth but also gas-  
58 to-particle partitioning, reflecting the correlation between the effect of physical and chemical processes on the concentration  
59 of  $\text{PM}_{2.5}$ . These complex atmospheric processes demand that effective  $\text{PM}_{2.5}$  control strategies must be formulated and adopted  
60 on the basis of an in-depth understanding of the effects of meteorology, emissions, atmospheric chemistry, and their  
61 interactions on the formation of  $\text{PM}_{2.5}$ . Although the basic relationships between  $\text{PM}_{2.5}$  and different influencing factors have  
62 been revealed, the quantitative influences of these factors on certain pollution episodes remains unclear, and it is difficult to  
63 quantify and distinguish the roles of each factor because of their complex interactions and different behaviours from one case  
64 to another (Li et al., 2011).



65 There have been some tools developed based on chemical transport models (CTMs) to analyse the effects of different factors  
66 on  $PM_{2.5}$  concentrations. The integrated process rate (IPR) method employed in the Community Multiscale Air Quality  
67 (CMAQ) model can quantify the contributions of different physicochemical processes in numerical models, thus providing a  
68 comprehensive understanding of the formation of air pollution (Jeffries and Tonnesen, 1994). The IPR method has been applied  
69 to study the formation processes and mechanisms of  $O_3$  and particulate matter in many cities (Liu et al., 2010; Li et al., 2014;  
70 Fan et al., 2014; Huang et al., 2016; Chen et al., 2019a; Chen et al., 2019c; Fu et al., 2020). However, the IPR method can  
71 obtain the contributions of different processes in a model, it ignores the nonlinear interactions between different processes,  
72 which may lead to uncertain results.

73 From another perspective, the scenario analysis approach (SAA) has been employed to assess the response of  $PM_{2.5}$  to  
74 emission changes by changing the emission inventory of the model inputs under fixed meteorological fields, as well as the  
75 response of  $PM_{2.5}$  to meteorological changes by changing the meteorological fields under fixed emissions. For example, Zheng  
76 et al. (2015b) found that the heavy pollution that occurred in winter 2013 in Northeast China was mainly caused by the stable  
77 weather conditions in most parts of the region, rather than a sudden increase in anthropogenic emissions, through comparison  
78 with the same period in 2012. Zhang et al. (2019a) reported that, although interannual meteorological changes may notably  
79 affect the  $PM_{2.5}$  concentration, the corresponding impact on the five-year trend of  $PM_{2.5}$  concentration in China is relatively  
80 limited (which they established by comparing results between the year 2017 and 2013). However, the traditional SAA method  
81 is also incapable of analysing the nonlinear effects. Therefore, Stein and Alpert (1993) developed the Factor Separation (FS)  
82 method to perform model sensitivity analysis and identify factors that contribute significantly to the model output. Compared  
83 with the SAA method, the FS method is superior in dealing with nonlinear processes that involve two or more factors. By  
84 performing multiple sensitivity experiments with different combinations of factors, the FS method allows one to assess the  
85 impact of a single factor in a nonlinear system as well as the interaction between that factor and other factors. This method is  
86 widely used in environmental and meteorological research (Romero et al., 2000; Alpert et al., 1999). For example, Tao et al.  
87 (2005) assessed the amount of surface  $O_3$  originated from area, mobile and point sources in the presence of biological emissions  
88 and quantified the contributions of biogenic emissions and the synergy between anthropogenic and biogenic emissions (Tao  
89 et al., 2003). The method can also be used to calculate the synergistic contributions of anthropogenic volatile organic  
90 compounds, biogenic volatile organic compounds, and nitrogen oxides ( $NO_x$ ) to surface  $O_3$  (Qu et al., 2013). However, both  
91 the SAA and FS method need to construct new simulation scenarios by changing the simulation conditions (emission source  
92 or meteorological field) and uses the differences between the simulation results of different scenarios to represent the  
93 contributions of the factors of interest. This means that the results of both the SAA and FS method are relative, being dependent  
94 on the simulation scenario employed. For example, the meteorological conditions we used to construct the simulation scenarios  
95 would alter the calculated contributions of meteorological processes to the  $PM_{2.5}$  in the SAA and FS method. In addition, the  
96 newly constructed simulation scenarios no longer represent the base simulation of the actual case because of the changed input  
97 information of the CTM.



98 In addition to the methods that use CTMs, methods based on observations have also been developed. For example, the  
99 PLMA (parameter linking air quality to meteorological conditions) index has been used to determine the contribution of  
100 meteorology and emissions to air pollution (Zhang et al., 2015; Zhang et al., 2019b; Yang et al., 2016). Studies employing  
101 principal component analysis or those targeting the correlation between  $PM_{2.5}$  and meteorological elements have suggested  
102 that a low wind speed and high humidity facilitate haze formation (Wang et al., 2013; Pang et al., 2009; Shu et al., 2017; Zhai  
103 et al., 2019). Considering that a single meteorological element does not fully explain the relationship between meteorology  
104 and  $PM_{2.5}$ , an artificial neural network model has been used to investigate the multiscale meteorological conditions, enabling  
105 the meteorological influence to be quantified by the explained variance (He et al., 2017).

106 To date, none of the above methods can meet the following conditions at the same time: (1) on the premise of not changing  
107 the base simulation conditions (without constructing other simulation scenarios as a reference system), we can quantitatively  
108 analyze the contributions of meteorological, emission, and chemical processes to the variations of air pollutant concentrations  
109 in an individual pollution case; (2) separation of the interactions between different factors; (3) the capability to analyse the  
110 meteorological contribution given its considerable importance in analysing the pollution process; and (4) equality between the  
111 sum of all analytical quantities and the simulated concentration change at any hourly time point so as to ensure that the  
112 analytical quantity can fully reveal the reasons for the concentration change. In view of the different advantages and  
113 disadvantages of these traditional methods mentioned above, we developed a novel quantitative decoupling analysis (QDA)  
114 method and assessed the effects of emissions, meteorology, chemical reactions, and their interactions on the  $PM_{2.5}$   
115 concentration in a typical pollution case in Beijing. The QDA method tracks the change in  $PM_{2.5}$  concentration in response to  
116 changes in emissions, meteorological conditions, and chemical reactions in high-pollution cases. Thus, this method provides  
117 a useful tool for identifying and quantifying the main determining factors of pollution cases, which can be used by decision-  
118 makers for selecting the optimal scheme from different air pollution control and emergency response strategies. The differences  
119 in QDA results of different model mechanisms can be compared to help identify the key process and improve its representation  
120 in atmospheric models—for example, the physicochemical structure in the boundary layer and formation mechanism of  
121 secondary air pollution (Chen et al., 2019a; Kang et al., 2019; Xing et al., 2017; Goncalves et al., 2009).

## 122 **2 Methods and data**

### 123 **2.1 Description of the QDA method**

124 In this section, we provide a detailed description of the QDA method proposed in this study, including its theoretical basis,  
125 algorithms, and its realization in a model, as well as its relationship with the SAA, FS and IPR methods.

#### 126 **2.1.1 Factors affecting $PM_{2.5}$ concentration and their contributions in CTMs**

127 The governing equation for CTMs is the three-dimensional semi-empirical Euler diffusion equation (Seinfeld and Pandis,  
128 2016; Zhao et al., 2020):



$$129 \quad \frac{\partial C_i}{\partial t} = -\left(u \frac{\partial C_i}{\partial x} + v \frac{\partial C_i}{\partial y} + w \frac{\partial C_i}{\partial z}\right) + \frac{\partial}{\partial x}\left(K_x \frac{\partial C_i}{\partial x}\right) + \frac{\partial}{\partial y}\left(K_y \frac{\partial C_i}{\partial y}\right) + \frac{\partial}{\partial z}\left(K_z \frac{\partial C_i}{\partial z}\right) + S + R_e - R_d - W_{ash} \quad \dots(1)$$

130 where  $C_i$  is the concentration of species  $i$  in the CTM;  $u$ ,  $v$  and  $w$  are the wind velocity components in the  $x$ ,  $y$  and  $z$  directions,  
131 respectively;  $K_x$ ,  $K_y$  and  $K_z$  are the diffusion coefficients in the  $x$ ,  $y$  and  $z$  directions;  $S$  denotes the direct emissions of  $C_i$ ;  $R_e$   
132 is the chemical term, mainly affected by the chemical reaction mechanism; and  $R_d$  and  $W_{ash}$  are the dry and wet deposition  
133 terms, respectively. Equation (1) is an instantaneous equation that cannot be solved analytically. In order to solve it numerically,  
134 the differential equation is calculated by the finite-difference and operator splitting method in three-dimensional CTMs  
135 (Santillana et al., 2016). We can define the advection operator as  $ADV = -\left(u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z}\right)$ , the diffusion operator as

136  $DIFF = \frac{\partial}{\partial x}\left(K_x \frac{\partial}{\partial x}\right) + \frac{\partial}{\partial y}\left(K_y \frac{\partial}{\partial y}\right) + \frac{\partial}{\partial z}\left(K_z \frac{\partial}{\partial z}\right)$ , the emission operator as EMIS, the chemical operator as CHEM, and the  
137 deposition operator as DEP, and then Eq. (1) can be rewritten as:

$$138 \quad \frac{\partial C_i}{\partial t} = ADV(C_i) + DIFF(C_i) + EMIS(C_i) + CHEM(C_i) + DEP(C_i) \quad \dots(2)$$

139 These model operators can also be classified in different ways. For example, the ADV, DIFF and DEP operators can be  
140 combined and defined as the meteorological operator (MET), and then Eq. (2) would become:

$$141 \quad \frac{\partial C_i}{\partial t} = EMIS(C_i) + MET(C_i) + CHEM(C_i) \quad \dots(3)$$

142 Furthermore, to produce refined process allocation, the DEP operator could be decomposed into a dry deposition operator and  
143 wet deposition operator, and the CHEM operator could be decomposed into a gas-phase chemistry operator, liquid-phase  
144 chemistry operator, or heterogeneous chemistry operator.

145 After the time is divided into model time steps, the calculation of Eq. (3) within one time step is carried out by the operator  
146 splitting method in the order of EMIS, MET, and CHEM, as illustrated in Eqs. (4)–(6):

$$147 \quad \frac{\partial C^1}{\partial t} = EMIS(C^1) \quad \dots(4)$$

$$148 \quad \frac{\partial C^2}{\partial t} = MET(C^2) \quad \dots(5)$$

$$149 \quad \frac{\partial C^3}{\partial t} = CHEM(C^3) \quad \dots(6)$$

150 where  $C^1$  is the initial concentration of the specific species  $i$  in a model step. If  $\Delta C^1$  is the integration result of  $\frac{\partial C^1}{\partial t}$  to  $t$  in Eq.  
151 (4) during the time step, then we can obtain  $C^2 = C^1 + \Delta C^1$  and use it as the initial value to be input into the next operator,  
152 MET, so the integration result of  $\frac{\partial C^2}{\partial t}$ , marked as  $\Delta C^2$ , would be affected by  $C^1$  and  $\Delta C^1$ . Analogously,  $C^3 = C^2 + \Delta C^2$ . The  
153 terms  $\Delta C^1$ ,  $\Delta C^2$  and  $\Delta C^3$  correspond to the contribution of emissions, meteorology, and chemistry, respectively, by the IPR  
154 method. However, if the calculation order between these operators is changed, different contribution results will be obtained.  
155 This non-uniqueness of the contribution results comes from the nonlinear effects of different operator processes on the pollutant  
156 concentration after the operator splitting. The concentration calculated by the latter operator process will be affected by the  
157 results of the former operator processes. This nonlinear effect influenced by the former processes has not been separated in



158 previous research, which will bias the results regarding the contributions of different process operators (as with the IPR  
159 method). To obtain more accurate and reliable results on the contributions of emissions, meteorological processes, and  
160 chemical processes, it is necessary to quantify the nonlinear effects among these three operator processes.

161 If all three operators use the initial concentration of time step  $C^1$  as the input value, just as in the following three equations:

$$162 \quad \frac{\partial C^1}{\partial t} = \text{EMIS}(C^1) \quad \dots(7)$$

$$163 \quad \frac{\partial C^1}{\partial t} = \text{MET}(C^1) \quad \dots(8)$$

$$164 \quad \frac{\partial C^1}{\partial t} = \text{CHEM}(C^1) \quad \dots(9)$$

165 then the contribution results obtained by integration of Eqs. (7)–(9) only depend on the value of  $C^1$  and are unaffected by the  
166 nonlinear interactions of other operator processes. Therefore, the integration results of Eqs. (7)–(9) can be regarded as pure  
167 contributions. The results obtained after the integration of Eqs. (7)–(9) are marked as  $\Delta C^E$ ,  $\Delta C^M$  and  $\Delta C^C$ , respectively, where  
168  $\Delta C^E$  is the pure contribution of the emission process to the concentration,  $\Delta C^M$  is the pure contribution of the meteorological  
169 process to the concentration, and  $\Delta C^C$  is the pure contribution of the chemical process to the concentration. On this basis, we  
170 can further explore how to quantify the nonlinear interactions of different operator processes on the concentration, so as to  
171 achieve a complete analysis of the amount of concentration change.

### 172 2.1.2 Theoretical basis of the QDA method

173 Considering the simulation of a haze case (base simulation), the simulated  $\text{PM}_{2.5}$  concentrations at step  $t+1$  ( $\text{PM}_{2.5}^{t+1}$ ) can  
174 be calculated by running all the processes in the model (including emissions, meteorology and chemistry) with the simulated  
175  $\text{PM}_{2.5}$  concentration at step  $t$  ( $\text{PM}_{2.5}^t$ ) as the initial condition. Taking the calculation of one model step (from  $t$  to  $t+1$ ) as the  
176 example, we can define the function  $F$  to denote the simulated  $\text{PM}_{2.5}$  concentration using  $\text{PM}_{2.5}^t$  as the initial concentration,  
177 where the information in parentheses represents the process operators that have been experienced in that time step:

$$178 \quad F(0,0,0) = \text{PM}_{2.5}^t \quad (10)$$

$$179 \quad F(x_1, x_2, x_3) = \text{PM}_{2.5}^{t+1} \quad (11)$$

180 Here,  $F(x_1, x_2, x_3)$  represents the simulated  $\text{PM}_{2.5}$  concentration obtained after the initial concentration has been subjected to  
181 the processes of emission ( $x_1$ ), meteorology ( $x_2$ ), and chemistry ( $x_3$ ) through this step; and  $F(0,0,0)$  is equal to the initial  
182 concentration because it has not been subjected to any process operator. Therefore, the variation in  $\text{PM}_{2.5}$  concentration in the  
183 base simulation can be written as:

$$184 \quad \Delta \text{PM}_{2.5}^{t+1} = \text{PM}_{2.5}^{t+1} - \text{PM}_{2.5}^t = F(x_1, x_2, x_3) - F(0,0,0) \quad (12)$$

185 According to Taylor series expansion, the function  $F$  can be decomposed as follows:



$$\begin{aligned}
 186 \quad & F(x_1, x_2, x_3) - F(0,0,0) = \sum_{i=1}^3 \frac{\partial F}{\partial x_i} x_i + \frac{1}{2!} \left( \sum_{i=1}^3 \frac{\partial^2 F}{\partial x_i^2} x_i^2 + 2 \frac{\partial^2 F}{\partial x_1 \partial x_2} x_1 x_2 + 2 \frac{\partial^2 F}{\partial x_2 \partial x_3} x_2 x_3 + 2 \frac{\partial^2 F}{\partial x_1 \partial x_3} x_1 x_3 \right) + \\
 187 \quad & \frac{1}{3!} \left( \sum_{i=1}^3 \frac{\partial^3 F}{\partial x_i^3} x_i^3 + \sum_{a=1}^2 3 \frac{\partial^3 F}{\partial x_1^a \partial x_2^{3-a}} x_1^a x_2^{3-a} + \sum_{a=1}^2 3 \frac{\partial^3 F}{\partial x_2^a \partial x_3^{3-a}} x_2^a x_3^{3-a} + \sum_{a=1}^2 3 \frac{\partial^3 F}{\partial x_1^a \partial x_3^{3-a}} x_1^a x_3^{3-a} + \right. \\
 188 \quad & \left. 6 \frac{\partial^3 F}{\partial x_1 \partial x_2 \partial x_3} x_1 x_2 x_3 \right) + \dots + o^n \tag{13}
 \end{aligned}$$

189 The terms in Eq. (13) that only contain partial derivatives to  $x_1$  ( $\frac{\partial F}{\partial x_1} x_1 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_1^2} x_1^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_1^3} x_1^3 + \dots$ ) can be understood as  
 190 the pure emission contribution (marked as E); the terms that only contain partial derivatives to  $x_2$  ( $\frac{\partial F}{\partial x_2} x_2 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_2^2} x_2^2 +$   
 191  $\frac{1}{3!} \frac{\partial^3 F}{\partial x_2^3} x_2^3 + \dots$ ) can be understood as the pure meteorology contribution (marked as M); and the terms that only contain partial  
 192 derivatives to  $x_3$  ( $\frac{\partial F}{\partial x_3} x_3 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_3^2} x_3^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_3^3} x_3^3 + \dots$ ) can be understood as the pure chemistry contribution (marked as C).  
 193 These pure contributions have the same meaning as  $\Delta C^E$ ,  $\Delta C^M$  and  $\Delta C^C$  in the previous section, indicating the amount of  
 194 concentration change that occurs under the influence of only one process operator. The cross-derivative terms indicate the  
 195 effects of the interaction of different operators on the  $\text{PM}_{2.5}$  concentration—for example,  $\frac{1}{2!} \frac{\partial^2 F}{\partial x_1 \partial x_2} x_1 x_2 +$   
 196  $\frac{1}{3!} \sum_{a=1}^2 \frac{\partial^3 F}{\partial x_1^a \partial x_2^{3-a}} x_1^a x_2^{3-a} + \dots$  represents the interaction between emissions and meteorology on the concentration (ME), and  
 197 the term  $\frac{1}{3!} \left( 6 \frac{\partial^3 F}{\partial x_1 \partial x_2 \partial x_3} x_1 x_2 x_3 \right) + \dots$  represents the interaction among emissions, meteorology and chemistry on the  
 198 concentration (MCE). Detailed definitions of the terms in Eq. (13) are available in Table 1. Please note that “pure” in this  
 199 context means that, within a time step, the corresponding contribution is only due to the influence of a certain process operator  
 200 on the initial value and is unaffected by other operators. For example, the pure contribution of emissions (E) depends only on  
 201 local, direct emissions, and cannot represent the indirect contribution of emissions, which include the amount of  $\text{PM}_{2.5}$   
 202 produced by the emitted precursor participating in the chemical reaction.

203 According to these definitions, the  $\text{PM}_{2.5}$  variations from step  $t$  to  $t+1$  in the base simulation can be decomposed into  
 204 seven contributions, including the analytical quantities of  $M$ ,  $E$ ,  $C$ , ME, MC, CE, and MCE, as follows:

$$205 \quad \Delta \text{PM}_{2.5}^{t+1} = M + E + C + \text{ME} + \text{MC} + \text{CE} + \text{MCE} \tag{14}$$

### 206 2.1.3 Algorithms of the QDA method and its implementation in the model

207 The QDA method uses algorithms similar to the FS method introduced by Stein and Alpert (1993) to calculate the  
 208 contributions in Eq. (14). By setting the parameters in the parentheses of  $F$  to be  $x_i$  ( $i = 1,2,3$ ) or 0 to respectively represent  
 209 the concentration at time step  $t+1$  with or without the corresponding process in the model, we can obtain the following  
 210 equations:

$$211 \quad F(x_1, 0, 0) - F(0,0,0) = \frac{\partial F}{\partial x_1} x_1 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_1^2} x_1^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_1^3} x_1^3 + \dots = E \tag{15}$$



$$212 \quad F(0, x_2, 0) - F(0,0,0) = \frac{\partial F}{\partial x_2} x_2 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_2^2} x_2^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_2^3} x_2^3 + \dots = M \quad (16)$$

$$213 \quad F(0,0, x_3) - F(0,0,0) = \frac{\partial F}{\partial x_3} x_3 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_3^2} x_3^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_3^3} x_3^3 + \dots = C \quad (17)$$

$$214 \quad F(x_1, x_2, 0) - F(0,0,0) = \frac{\partial F}{\partial x_1} x_1 + \frac{\partial F}{\partial x_2} x_2 + \frac{1}{2!} \left( \frac{\partial^2 F}{\partial x_1^2} x_1^2 + \frac{\partial^2 F}{\partial x_2^2} x_2^2 + 2 \frac{\partial^2 F}{\partial x_1 \partial x_2} x_1 x_2 \right) + \dots = E + M + ME \quad (18)$$

$$215 \quad F(x_1, 0, x_3) - F(0,0,0) = \frac{\partial F}{\partial x_1} x_1 + \frac{\partial F}{\partial x_3} x_3 + \frac{1}{2!} \left( \frac{\partial^2 F}{\partial x_1^2} x_1^2 + \frac{\partial^2 F}{\partial x_3^2} x_3^2 + 2 \frac{\partial^2 F}{\partial x_1 \partial x_3} x_1 x_3 \right) + \dots = E + C + CE \quad (19)$$

$$216 \quad F(0, x_2, x_3) - F(0,0,0) = \frac{\partial F}{\partial x_2} x_2 + \frac{\partial F}{\partial x_3} x_3 + \frac{1}{2!} \left( \frac{\partial^2 F}{\partial x_2^2} x_2^2 + \frac{\partial^2 F}{\partial x_3^2} x_3^2 + 2 \frac{\partial^2 F}{\partial x_2 \partial x_3} x_2 x_3 \right) + \dots = M + C + MC \quad (20)$$

217 where  $F(x_1, 0, 0)$ ,  $F(0, x_2, 0)$  and  $F(0, 0, x_3)$  can be calculated by the built-in scenario simulations that only consider emissions,  
 218 meteorology and chemistry from step  $t$  to  $t+1$ , respectively; and  $F(x_1, x_2, 0)$ ,  $F(x_1, 0, x_3)$  and  $F(0, x_2, x_3)$  are calculated by  
 219 the built-in scenario simulation that does not include chemistry, meteorology or emissions from step  $t$  to  $t+1$ , respectively  
 220 (Table 2). The initial concentrations in the built-in scenario simulations will be updated by the values of the base simulation  
 221 at each time step, which ensures the resulting contributions are at the same concentration starting point and can be used to  
 222 analyse the hourly concentration change of the base simulation. The codes of the built-in scenario simulations are embedded  
 223 in the original code of the CTM and the initial concentration of the built-in scenario simulations at each time step can be  
 224 synchronously updated by the base simulation—something that cannot be done by the FS or other previous methods.

225 Therefore, the values of  $F(x_1, 0, 0)$ ,  $F(0, x_2, 0)$ ,  $F(0, 0, x_3)$ ,  $F(x_1, x_2, 0)$ ,  $F(x_1, 0, x_3)$  and  $F(0, x_2, x_3)$  can be obtained from  
 226 the results of the six built-in scenario simulations, and the values of  $F(0,0,0)$  and  $F(x_1, x_2, x_3)$  can be simply obtained from  
 227 the base simulation. Based on these equations above, the contributions of the four interactions in Eq. (14) can be calculated as  
 228 follows:

$$229 \quad ME = F(x_1, x_2, 0) - F(x_1, 0, 0) - F(0, x_2, 0) + F(0,0,0) \quad (21)$$

$$230 \quad CE = F(x_1, 0, x_3) - F(x_1, 0, 0) - F(0, 0, x_3) + F(0,0,0) \quad (22)$$

$$231 \quad MC = F(0, x_2, x_3) - F(0, x_2, 0) - F(0, 0, x_3) + F(0,0,0) \quad (23)$$

$$232 \quad MCE = F(x_1, x_2, x_3) + (F(x_1, 0, 0) + F(0, x_2, 0) + F(0, 0, x_3)) - (F(x_1, x_2, 0) + F(x_1, 0, x_3) + F(0, x_2, x_3)) - F(0,0,0) \quad (24)$$

234 The above formulae are all introduced based on one time step. The QDA method uses the above algorithm in each mode time  
 235 step, and outputs the contribution analysis results of the change in PM<sub>2.5</sub> concentration per hour. The initial concentrations of  
 236 not only PM<sub>2.5</sub> but also other species (all species contained in the CTM) in the built-in scenario simulations would all be  
 237 updated by the base simulated values at the beginning of the new step. Finally, the QDA method's analytical results of the  
 238 variation at each step in the model output species, including PM<sub>2.5</sub>, can be obtained. The relationships among the seven  
 239 contributions in Eq. (14) can also be shown visually (Fig. 1), in which the processes of emissions, meteorology and chemistry  
 240 are denoted by the three circles and the interactions among the different processes are denoted by the overlapping areas (Lunt  
 241 et al., 2021).





#### 242 2.1.4 Relationship and differences with the SAA, FS and IPR methods

243 The similarity between the FS method and the QDA method is that they employ the same idea to separate the contributions  
244 of different processes, while the biggest difference between them is the target of the algorithm. The FS method commonly  
245 targets an “individual case”, in which several sets of scenario simulations will run independently for several days or even  
246 longer with different input conditions for the factors of concern. The difference among these simulations due to the input  
247 conditions will gradually accumulate with the simulation time, and this cumulative amount is understood as the contribution  
248 of the condition difference for the entire individual case. The QDA method targets the “time step”, in which the process  
249 operator is switched within the time steps of built-in scenario simulations and the concentration differences between the built-  
250 in scenario simulations of the same time step can reflect the process contribution but there is no transfer or accumulation of  
251 contribution between time steps. Therefore, the QDA method can not only obtain the process contribution for any given hour,  
252 but also the total contribution during the individual case.

253 The FS method has limitations in research and practical operations. Firstly, it can only study the relative contributions  
254 and not the absolute contributions. Relative contribution means the contribution expressed by the difference between two or  
255 more individual cases. Absolute contribution means the contribution of the process itself in an individual case. For example,  
256 by reducing or increasing specific emission sources, the concentration changes caused by the emission differences and their  
257 interactions could be obtained. If we want to study the influence of all emission sources in the geographical range of the model  
258 simulation settings, the FS method would have to construct a simulation scenario with a zero emission source, but this would  
259 lead to the concentrations of air pollutants only coming from the boundary and initial conditions in the CTM. So, after a period  
260 of simulation, the concentrations become extremely low, which is not what we want. To avoid this problem, the QDA method  
261 would synchronously update the initial concentration for the built-in scenario simulations by using the base simulation  
262 concentrations at each time step, which makes a certain process shut down for no more than one hour and ensures a physically  
263 meaningful result. To research the absolute contribution of meteorological conditions to air pollutant concentrations, we cannot  
264 construct a simulation scenario that completely closes the meteorological conditions through the FS method. FS can only be  
265 used to study the relative differences in concentration due to the changes in meteorological conditions. The QDA method has  
266 no such limitation; it is not only able to obtain the absolute contributions of operator processes at any time, but also able to  
267 calculate the relative differences in the contributions under different emission or meteorological scenarios. Secondly, FS can  
268 calculate the contribution for the case as a whole but cannot obtain the contribution for any specific hour in the case. The QDA  
269 method draws lessons from the idea of the IPR method in that it analyses the influence of factors in every time step and  
270 successfully solves the above problems.

271 By analysing the contribution of each process in the model, the IPR method can be used to resolve the contributions of  
272 different physical and chemical processes to the concentration change of every time step. Different from the fact that all  
273 physical and chemical processes in the real atmosphere are carried out almost simultaneously, the processes in CTMs are all  
274 carried out in sequence. The idea of the IPR method is that, in a time step, the operator processes are executed in sequence



275 according to the order in the model, and the concentration difference before and after the execution is calculated to represent  
276 the contribution of a single process. This makes the IPR method unable to consider the effects of the nonlinear interactions  
277 among different processes on pollutant concentrations. The order in which process operators are executed varies among  
278 different CTMs. Assuming that in CTMs calculations are performed in the order of emission, meteorological and chemical  
279 processes, the contribution of emissions obtained by the IPR method equals E in QDA, while the meteorological contribution  
280 in the IPR (the concentration change caused by atmospheric advection, diffusion and deposition) equals M + ME in QDA, and  
281 the chemical contribution equals C + CE + MC + MCE. Likewise, if one assumes that the CTM calculations are carried out in  
282 the order of emission, chemical and meteorological processes, the contribution of emissions obtained by the IPR method equals  
283 E in QDA, while the chemical contribution in the IPR equals C + CE in QDA, and the meteorological contribution equals M  
284 + MC + ME + MCE. The above two examples show that the IPR method cannot separate the interactions among different  
285 processes, which leads to the interactions being included in the obtained IPR contributions.

286 To some extent, the QDA method could be seen as a combination of the FS method and IPR method. This method  
287 combines the advantages of the IPR method for time-step analysis and the analytical advantages of FS for separating  
288 interactions, but it is different from each of the two methods.

## 289 2.2 Combination of the QDA and IPR methods

290 The above QDA method can also be combined with the IPR method to resolve more detailed information. This is achieved  
291 by applying the IPR method to each built-in scenario simulation. The premise is to ignore the nonlinear effect within one time  
292 step. In Sect. 2.1, we showed that meteorological and chemical operators can be split into smaller sub-process operators—for  
293 example, the meteorological process can be divided into advection, diffusion, dry and wet deposition processes; and the  
294 chemical process can be divided into the gas- and aqueous-phase chemistry, thermodynamic equilibrium processes, and  
295 secondary organic aerosol (SOA) reactions. That is to say, the IPR analysis can be used in the operators of emissions,  
296 meteorology and chemistry under the calculation framework of the QDA method at the same time (Fig. 2). Therefore, we can  
297 obtain the sub-process contributions among the seven quantitative analytical factors in Eq. (14).

298 The results of the base simulation and each built-in scenario simulation at  $t+1$  can be decomposed by IPR as follows:

$$299 F(x_1, 0, 0) - F(0, 0, 0) = \text{emit}_{s_1} \quad (25)$$

$$300 F(0, x_2, 0) - F(0, 0, 0) = \text{advhor}_{s_2} + \text{advvert}_{s_2} + \text{difhor}_{s_2} + \text{difvert}_{s_2} + \text{wetdep}_{s_2} + \text{drydep}_{s_2} \quad (26)$$

$$301 F(0, 0, x_3) - F(0, 0, 0) = \text{gaschem}_{s_3} + \text{ISORR}_{s_3} + \text{SOA}_{s_3} \quad (27)$$

$$302 F(x_1, x_2, 0) - F(0, 0, 0) = \text{emit}_{s_{12}} + \text{advhor}_{s_{12}} + \text{advvert}_{s_{12}} + \text{difhor}_{s_{12}} + \text{difvert}_{s_{12}} + \text{wetdep}_{s_{12}} + \text{drydep}_{s_{12}} \quad (28)$$

$$303 F(x_1, 0, x_3) - F(0, 0, 0) = \text{emit}_{s_{13}} + \text{gaschem}_{s_{13}} + \text{ISORR}_{s_{13}} + \text{SOA}_{s_{13}} \quad (29)$$

$$304 F(0, x_2, x_3) - F(0, 0, 0) = \text{advhor}_{s_{23}} + \text{advvert}_{s_{23}} + \text{difhor}_{s_{23}} + \text{difvert}_{s_{23}} + \text{wetdep}_{s_{23}} + \text{drydep}_{s_{23}} + \text{gaschem}_{s_{23}} + \\ 305 \text{ISORR}_{s_{23}} + \text{SOA}_{s_{23}} \quad (30)$$



$$F(x_1, x_2, x_3) - F(0,0,0) = \text{emit}_S + \text{advhor}_S + \text{advvert}_S + \text{difhor}_S + \text{difvert}_S + \text{wetdep}_S + \text{drydep}_S + \text{gaschem}_S + \text{ISORR}_S + \text{SOA}_S \quad (31)$$

Table 2 explains the meaning of each item on the left-hand sides of Eqs. (25)–(30);  $F(x_1, x_2, x_3)$  and  $F(0,0,0)$  represent the  $\text{PM}_{2.5}$  concentration at time  $t+1$  and time  $t$  in the base simulation S; the subscripts on the right-hand sides of Eqs. (25)–(30) denote the corresponding simulation mark; the IPR terms refer to previous research (Chen et al., 2019a; Chen et al., 2019c); and these subprocess definitions and abbreviations are detailed in Table 3. Combining Eqs. (25)–(31) and Eqs. (15)–(25), the contributions of sub-process operators in any QDA analytic quantity can be obtained.

### 2.3 Model setup and emission inventories

To illustrate the use of the QDA method, we embedded its codes into the Nested Air Quality Prediction Modeling System (NAQPMS) model and built QDA v1.0 for NAQPMS. The QDA method can be combined with other CTMs in a similar way following the QDA algorithm. NAQPMS is a three-dimensional regional Eulerian CTM developed by the Institute of Atmospheric Physics, Chinese Academy of Sciences, which has been widely used in scientific research and operational air quality prediction (Wang et al., 2014; Du et al., 2021; Kong et al., 2021; Wang et al., 2021; Akimoto et al., 2020; Yang et al., 2020a) owing to its good performance in simulating the emission, meteorological and chemical processes in the atmosphere. Within the model, the gas-phase chemistry is simulated by the “carbon bonding mechanism Z” developed by Zaveri and Peters (1999), which includes 134 reactions and 71 species. For inorganic aerosols, the ISORROPIA v1.7 thermodynamic equilibrium module (Nenes et al., 1998) is used to simulate the ammonia–nitrate–sulfate–chloride–sodium–water system. Six SOAs are processed by a two-product module in NAQPMS (Odum et al., 1997). The aqueous-phase chemistry and wet deposition are modelled using the Regional Acid Deposition Model mechanism in CMAQ version 4.6. The dry deposition of gases and aerosols is simulated based on the scheme of Wesely (1989) and the advection is simulated with an accurate mass-conservation algorithm from Walcek and Aleksic (1998). More technical details on NAQPMS could be found in Li et al. (2012).

To illustrate the feasibility of the QDA method and quantitatively analyse the magnitudes of the contributions from emissions, meteorology and chemistry to the variation in  $\text{PM}_{2.5}$  during heavy pollution, we applied the method to a week-long heavy-haze episode that took place in Beijing during 17–28 February 2014. Figure 3 shows the modelling domain of this case, which covers most of East Asia with a horizontal resolution of 45 km. Vertically, NAQPMS uses 20 nonequally distributed terrain-following layers from the surface (~100 m) to 20 km. The anthropogenic emission inventories used in the simulation were obtained from the Chinese Multi-resolution Emission Inventory (MEIC) for the year 2014 developed by Tsinghua University (<http://www.meicmodel.org>). We adjusted the original inventory with reference to the diurnal profile of the emission inventory in MICS-Asia III (Model Inter-Comparison Study for Asia III), which is shown in Fig. S1. Biogenic emissions were obtained from the Model of Natural Gas and Aerosol Emissions (MEGAN v2.0) (Guenther et al., 2006), and the biomass burning emissions were obtained from the the Global Fire Emissions Database version 4 (Randerson et al., 2017; van der Werf et al., 2010). A clean initial condition was used in the simulation with a 10-day free run of NAQPMS as a spin-up time. The top and boundary conditions of the outermost region were extracted from the global CTM MOZART (Model for



339 Ozone and Related Chemical Tracers) version 2.5, with a 3-h temporal resolution (Brasseur et al., 1998). The offline hourly  
340 meteorological fields were generated by the Weather Research and Forecasting (WRF) model version 3.7 ([http://www.wrf-](http://www.wrf-model.org/)  
341 [model.org/](http://www.wrf-model.org/)), driven by National Centers for Environmental Prediction (NCEP) Final Analysis data (FNL).

## 342 2.4 Observation data

343 The observational data used in this study included surface observations of PM<sub>2.5</sub>, particulate matter smaller than 10 μm  
344 in diameter (PM<sub>10</sub>), NO<sub>2</sub>, O<sub>3</sub>, SO<sub>2</sub> and CO obtained from the China National Environmental Monitoring Center. Surface  
345 observations of wind speed, wind direction, temperature, relative humidity, and station pressure; and vertical observations of  
346 wind speed, wind direction, temperature, and relative humidity, were retrieved from the China Meteorological Administration.  
347 The spatial distributions of the meteorological and air quality observation sites are shown in Fig. 3. To compare with the PM<sub>2.5</sub>  
348 observations, the simulated PM<sub>2.5</sub> concentrations were comprised of primary PM<sub>2.5</sub> (including black carbon, primary organic  
349 aerosol, and other directly emitted PM<sub>2.5</sub>) and secondary PM<sub>2.5</sub>, including sulfate, nitrate, ammonium, and SOA produced by  
350 chemical reactions.

## 351 3 Results and discussion

### 352 3.1 Observed pollution during the heavy-haze episode

353 A serious pollution event occurred in the Beijing area during 19–27 February 2014, with the observed mean PM<sub>2.5</sub>  
354 concentration reaching 168.9 μg m<sup>-3</sup>, more than double the national secondary standard level (75 μg m<sup>-3</sup>). As shown in Fig.  
355 S2, this pollution episode also affected a wide area of the BTH region, with severe haze mostly located in the southern part of  
356 the region before 23 February and gradually extending northwards to encompass wider areas. The SO<sub>2</sub> and NO<sub>2</sub> concentrations  
357 did not exhibit notable exceedances as the PM<sub>2.5</sub> did, indicating that this case was a typical particulate-led pollution event.

358 To investigate the characteristics of the contributions from meteorology, emissions and chemistry in different stages of  
359 this haze event, we divided the whole episode into four stages based on the temporal characteristics of the PM<sub>2.5</sub> concentration  
360 in Beijing (Fig. 4): (1) the pre-contamination stage [0800 LST (local standard time) 17 February to 1400 LST 19 February]  
361 with relatively low PM<sub>2.5</sub> concentrations and flat variation; (2) the accumulation stage (1500 LST 19 February to 0800 LST 23  
362 February) when the PM<sub>2.5</sub> concentration increased the most rapidly; (3) the pollution maintenance stage (0900 LST 23 February  
363 to 1800 LST 26 February) when the PM<sub>2.5</sub> concentration remained high with small fluctuations; and (4) the pollution removal  
364 stage (1900 LST 26 February to 0800 LST 27 February) when the PM<sub>2.5</sub> concentration rapidly dropped.

### 365 3.2 Validation of the meteorology and chemistry simulations

366 To assess the accuracy of the model, simulated meteorological parameters and air pollutant concentrations were compared  
367 with observed values. We used several evaluation indicators to quantitatively assess the model performance, including the  
368 simulated mean, observed mean, correlation coefficient (*R*), mean fractional bias (MFB), mean fractional error (MFE), mean



369 bias, mean error (MEr), normalized mean bias (NMB), normalized mean error (NME), root-mean-square error, and index of  
370 agreement (IOA), which are defined in Table S1. The verification results of meteorological elements are shown in Table S2,  
371 revealing the  $R$  of temperature (Temp), relative humidity (RH) and pressure to all be above 0.85. The correlation between wind  
372 speed (WS) and observation data ( $R=0.47$ ) is better than that of wind direction (WD:  $R=0.24$ ). Although the MEr of the  
373 simulated wind is greater than that of other meteorological elements, the NME and NMB are less than 1, which indicates that  
374 the simulation and observation match well on the whole, and the MEr may have little influence on the performance of aerosol  
375 simulation.

376 The simulations based on the NAQPMS model generally reproduced the magnitude of, and temporal variation in, the  
377  $PM_{2.5}$  concentration in the Beijing area well, with an  $R$  of approximately 0.83. The model simulation results exhibit relatively  
378 larger underestimations of the  $PM_{2.5}$  concentration from 20–23 February, which may be attributable to the overestimation of  
379 the simulated wind speed by the WRF model during this period (Figs. S3 and S4). Regarding the two important precursors of  
380  $PM_{2.5}$ , the simulated  $NO_2$  and  $SO_2$  concentrations also agree well with the observations, with  $R$  values of approximately 0.71  
381 and 0.76, respectively. In general, the simulated  $PM_{2.5}$  concentrations satisfy the NMB, NME,  $R$ , and IOA performance  
382 standards (NMB<20%, NME<45%,  $R>0.6$ , and IOA>0.7) proposed by Huang et al. (2021a), and the simulated  $SO_2$  and  $NO_2$   
383 concentrations all satisfy the MFB and MFE performance standards (MFB<30%, MFE<50%) proposed by (Boylan and Russell,  
384 2006). The simulated sulfate, nitrate and ammonium concentrations were also compared with observations, to evaluate the  
385 chemical processes in the NAQPMS model (Fig. S5). The model reproduced the variation in secondary inorganic aerosols  
386 (SIAs) well during this episode ( $R>0.82$ ), although the model underestimated the sulfate concentration, possibly due to missing  
387 reaction pathways of sulfuric acid in the model, such as heterogeneous chemistry (Zheng et al., 2015a; Cheng et al., 2016).  
388 Underestimation of the sulfate concentration is a common problem in current CTMs (Chen et al., 2019b), but one that is beyond  
389 the scope of this study. However, this could lead to uncertainty in the estimation of the contribution from chemistry to the  
390  $PM_{2.5}$  concentration. In summary, the simulation suitably reproduced the evolution of this pollution process from the pre-  
391 contamination period to the accumulation, maintenance, and removal periods, which laid a good foundation for subsequent  
392 analysis of the physical and chemical processes.

### 393 3.3 Temporal variation of the QDA results in different stages

394 Figure 5 shows the time series of the calculated contributions from emissions, meteorology, chemistry, and their  
395 interactions to the hourly variation in  $PM_{2.5}$  concentration using the QDA method. We can clearly see that in Fig. 5(b) the sum  
396 of all contributions is exactly equal to the hourly change in the  $PM_{2.5}$  concentration, indicating that the QDA method can fully  
397 resolve the variation in the  $PM_{2.5}$  concentration.

398 The characteristics of temporal variation vary among different factors. Among the seven QDA analytical factors, the  
399 fluctuation range of  $M$  is the largest, which ranges from  $-48.7$  to  $7.4 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ . When the change in  $PM_{2.5}$  concentration is  
400 positive,  $M$  plays a role in promoting the accumulation of the  $PM_{2.5}$  concentration. When the change in  $PM_{2.5}$  is negative,  $M$   
401 must play a clearing role. On the hourly scale, the value of  $E$  is not always the biggest. For example, on the afternoons of 23–



402 25 February, CE is significantly larger than E. However, on average, E is the largest mean contribution with the highest value  
403 of  $0.88 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  in two stages (Table 4). The contribution from chemistry exhibits remarkable diurnal variation, being  
404 notably larger during the daytime than at nighttime. This occurs because the atmospheric oxidation capacity during daytime is  
405 higher than at nighttime, which is more conducive to secondary  $\text{PM}_{2.5}$  formation (Huang et al., 2021b; Chen et al., 2020a; Lu  
406 et al., 2019a), and similar conclusions have been reported in other modelling studies (Chen et al., 2019a; Li et al., 2014).

407 We investigated the influences of the nonlinear effects on the  $\text{PM}_{2.5}$  concentration by summing all the contributions of  
408 the interactions among the different physical and chemical processes ( $\text{COUP}=\text{EM}+\text{CE}+\text{MC}+\text{MCE}$ ). Figure 6 and Table 5  
409 show the QDA results in the different stages of the episode. The M and EM exhibit a notable negative contribution to  $\text{PM}_{2.5}$  in  
410 the first stage, which was enough to remove the newly emitted or formed  $\text{PM}_{2.5}$  from emissions and chemical reactions  
411 ( $|\text{M}+\text{EM}|>|\text{E}+\text{C}+\text{CE}+\text{MCE}|$  in Table 4). Thus, the  $\text{PM}_{2.5}$  concentration was relatively low in the first stage. However, M shifts  
412 to a positive contribution in stage 2, and there are no other removal processes except EM during this stage. The average increase  
413 in  $\text{PM}_{2.5}$  per hour ( $\text{M}+\text{E}+\text{C}+\text{CE}+\text{MC}+\text{MCE}=1.87 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ) is significantly greater than the removal speed ( $\text{EM}=-0.08$   
414  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ), which led to rapid accumulation of the  $\text{PM}_{2.5}$  concentration. Then, M becomes negative and acts as a cleaner in  
415 stage 3, which nearly offsets the increase caused by  $\text{E}+\text{C}+\text{COUP}$  with a speed about  $1.85 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ . Hence, the  $\text{PM}_{2.5}$   
416 concentration remained at a relatively steady level. In stage 4, the removal effects of M are much larger than those in the  
417 previous stages owing to the strong northwesterly nonpolluted wind, leading to a rapid decline in the  $\text{PM}_{2.5}$  concentration.  
418 According to the IPR results (Figs. 6e–h), horizontal advection was the main removal process in M during stages 1 and 4,  
419 indicating that horizontal outward transportation facilitated  $\text{PM}_{2.5}$  reduction during the relative cleaning period (Chen et al.,  
420 2020c). Vertical advection was the main accumulation process in M during stages 1, 2 and 4, while in stage 3 it had removal  
421 effects on  $\text{PM}_{2.5}$ . It has been reported by Platis et al. (2016) that the downward transport of particles may be an important  
422 reason for increased  $\text{PM}_{2.5}$  in the entire atmospheric boundary layer. Figure 7(a) shows that, during stage 2,  $\text{PM}_{2.5}$  is transported  
423 from outside to the *in situ* area below the height of L7 via horizontal advection, while it is exported from outside in the upper  
424 layer. These positive and negative results cancel each other out and make the horizontal advection contribute little to the entire  
425 layer during this stage.  $\text{PM}_{2.5}$  can originate from other places via long-distance transport (Du et al., 2020), which would lead  
426 to weakening of boundary layer turbulence and thereby the facilitation of local pollution accumulation (Huang et al., 2020). It  
427 can also be seen that the growth rate of  $\text{PM}_{2.5}$  in L7–L9 is the highest, which is consistent with previous findings that the  
428 accumulation of aerosols near the top of the boundary layer has the largest rate of increase (Liu et al., 2020). In addition, the  
429 hourly contribution of wet deposition was zero and played a negligible role in the variation in different stages, which was due  
430 to there being no precipitation during this typical severe haze event. The C yielded positive contributions in the first three  
431 stages ( $0.23\text{--}0.37 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ) owing to the generation of SIAs and SOAs. In stage 4, C became negative ( $-0.08 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ) as  
432 the environmental conditions at this time were suitable for nitrate decomposition (Chen et al., 2020c). According to their  
433 definitions, C reflects the contribution from chemistry to  $\text{PM}_{2.5}$  made by pre-existing gases in the atmosphere, and CE reflects  
434 the same but made by newly emitted gases. Therefore, the larger the ratio of CE/C, the more efficient the chemical conversion.  
435 The results suggest that the conversion efficiency of secondary aerosols was highest during stage 3 under the most serious



436 pollution, which is consistent with the results of other studies of heavy haze (Huang et al., 2014; Zhou et al., 2022; Shang et  
437 al., 2021).

438 It is worth noting that E only contains the contributions from direct emissions of PM<sub>2.5</sub> in local space, which was  
439 determined by the emissions inventory in the model. This definition is different from the contributions of emissions in previous  
440 studies, which also included the nonlinear effects between direct emissions and other processes (Maji et al., 2020; Zhang et  
441 al., 2018). From the perspective of tracing back to the sources, the ultimate source of pollutants is only the emissions, but the  
442 directly emitted PM<sub>2.5</sub> or precursors can affect other areas through meteorological transmission or chemical reactions. From a  
443 process viewpoint, it is obviously not just the emission process that should be involved. The hourly mean contribution of CE  
444 was largest during stage 3, and thus the implementation of emissions reduction during that stage would have greater weakening  
445 effects on the chemical generation of PM<sub>2.5</sub> than in the previous two stages. M reflects the net changes in PM<sub>2.5</sub> concentration  
446 resulting from pollutants following air masses in and out of the grid boxes of the model; plus, it is also the main way to reduce  
447 air pollution most of the time. Although its specific application in developing emission reduction strategies is not the focus of  
448 this paper, it is nonetheless worth highlighting that it can provide valuable insights into these related issues.

#### 449 **3.4 Decoupling of nonlinear effects at different stages**

450 There are also nonnegligible nonlinear effects in each stage, and their contributions can sometimes even exceed pure  
451 contributions of meteorology, emissions, and chemistry. On the one hand, these nonlinear interactions are determined by the  
452 calculation method; whilst on the other hand, they are physically explainable. When emissions increase the concentrations of  
453 pollutants in the atmosphere, the amounts of pollutants transported by air masses will also increase, which is reflected by the  
454 nonlinear effect of EM. The emission process may increase the concentrations of precursors in the atmosphere. Based on the  
455 IPR results, CE reflects that newly emitted precursors produce secondary aerosols through chemical reactions and equilibrium  
456 partitioning. MC consists of two parts: the first part is the influence of meteorology on chemistry, in which meteorological  
457 processes can increase chemical production by transporting more precursors or decrease chemical production by reducing the  
458 concentrations of local precursors; while the second part involves the influence of chemistry on meteorology, since chemical  
459 processes can lead to an increase in the concentrations of secondary aerosols in the atmosphere. This may lead to an increase  
460 in pollutants carried by air masses in the corresponding region. MCE includes all meteorological, emission and chemical  
461 process interactions, which are complex and yield very small contributions. The hourly value of COUP ranged from -1.83 to  
462 2.44  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  during this haze episode, with an average value of approximately 0.30  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ . The nonlinear effect was  
463 shown to increase continuously from the beginning to heavy polluted periods. According to Table 4, from stage 1 to 3, the  
464 hourly mean value of COUP increased from 0.05 to 0.74  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ , and its proportion in the hourly variation of PM<sub>2.5</sub> also  
465 increased (from -3.68% to 740%).

466 During the entire episode, CE exhibited the largest nonlinear effect (0.27  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  on average) and increased with the  
467 concentration of PM<sub>2.5</sub>, indicating that the interactions between emissions and chemistry play an important role during heavy  
468 haze. According to the vertical distribution of CE in stage 2 (Fig. 7), the contribution of CE decreased from the surface to the



469 upper levels owing to the vertical reductions in air temperature and emissions. The contribution of MC revealed the largest  
470 variation, with a fluctuational range up to  $4.24 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ , because both the meteorology and chemistry are greatly influenced  
471 by diurnal variation. As shown in Fig. 7, MC also indicated that meteorological processes could decrease the chemical process  
472 in the surface layer and strengthen chemical formations in the upper layers (L3–L8), which could also be related to the  
473 phenomenon in Fig. 7(a) that meteorological processes transport  $\text{PM}_{2.5}$  and precursors from the lower layer to the upper layer.  
474 EM suggests that local emissions may enhance the vertical diffusion of  $\text{PM}_{2.5}$  from the surface layer to the upper layer. Primary  
475 emitted  $\text{PM}_{2.5}$  mainly occurred in the near-surface layers where the vertical wind speed was so low that vertical advection was  
476 extremely limited. Thus,  $\text{PM}_{2.5}$  emitted in the near-surface layers could reach the upper layers only through the process of  
477 vertical diffusion.

478 In previous studies, the investigation of nonlinear effects was usually ignored when analysing heavy haze. The present  
479 QDA results demonstrate that ignoring these nonlinear effects may cause bias when studying the pure contributions of  
480 meteorology, emissions or chemistry to  $\text{PM}_{2.5}$ . For example, when discussing the effect of the pure contribution of emissions  
481 on  $\text{PM}_{2.5}$ , if the effects in CE, EM and MCE are ignored, an uncertainty ranging from  $-0.86$  to  $1.86 \mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$  (CE +EM+MCE)  
482 occurs on the hourly scale, especially during the worst polluted period, and this uncertainty may accumulate with time. This  
483 suggests that quantitative analysis of the nonlinear effects is necessary to evaluate the process contributions in heavy-haze  
484 episodes.

### 485 3.5 Discussion and evaluation of QDA

#### 486 3.5.1 Chemical compositions

487 The E calculated by the QDA method is influenced directly by the emissions inventory used in the simulations. Thus, we  
488 mainly evaluated the calculated contributions of M and C in this study. However, there were no observational data linked to  
489 the pure contributions of emissions or chemistry that could be used to verify the QDA method directly. Hence, the method was  
490 evaluated with indirect results. Since the contribution from chemistry to  $\text{PM}_{2.5}$  is mainly related to the formation of secondary  
491 aerosols, the conversion rates of nitrate (NOR) and sulfate (SOR), as defined in Eqs. (32) and (33), were calculated to evaluate  
492 the temporal variation in the chemical contribution obtained with the QDA method. Daily  $\text{PM}_{2.5}$  composition data measured  
493 by the Beijing Ecological Environment Monitoring Center were used to calculate NOR and SOR values in the different stages  
494 of this haze episode:

$$495 \text{ NOR} = \frac{\text{NO}_3^-}{\text{NO}_3^- + \text{NO}_2} \quad (32)$$

$$496 \text{ SOR} = \frac{\text{SO}_4^{2-}}{\text{SO}_4^{2-} + \text{SO}_2} \quad (33)$$

497 We found that NOR and SOR increased by 0.09 and 0.02, respectively, from stage 1 to stage 2. NOR and SOR both  
498 reached their maximum value (0.54 and 0.38, respectively) in stage 3. In stage 4, NOR and SOR both experienced a significant  
499 decline. Other haze cases have also revealed that SOR and NOR greatly increased with  $\text{PM}_{2.5}$  concentration (Song et al., 2019;





500 Xu et al., 2017; Yan et al., 2015a) and the proportion of secondary aerosols often increases with worsening haze (Xu et al.,  
501 2019a; Li et al., 2017). Process analysis has also shown that the chemical reactions of  $PM_{2.5}$  in the WRF-Chem model are  
502 stronger during the day than that at night (Chen et al., 2019a), which is consistent with this study. In the QDA results, the  
503 amount that can represent the chemical reaction intensity is C+CE. It can be seen that its total contribution had been increasing  
504 from stage 1 to stage 3, and in stage 4 had decreased to its lowest level. This evidence, together with the QDA analysis results,  
505 explains the importance of chemical reactions in heavy haze (Huang et al., 2019).

506 We also analysed the QDA results for SIAs, including nitrate, sulfate and ammonium, as well as their precursors,  
507 including  $NO_x$ ,  $SO_2$ , and  $NH_3$ , to provide further insight into the roles of chemical formations during haze episodes. Figure 8  
508 shows the QDA results for SIAs, as well as their precursors, during the different stages of the episode. Notably, there were  
509 small contributions of E to the sulfate concentrations because we parameterized 2.5% of sulfate primary emissions to consider  
510 the particle formation on the sub-grid scale. As we can clearly see from Fig. 8, the chemical production of nitrate, sulfate and  
511 ammonium agreed well with the chemical depletion of their precursors, suggesting good capability of the QDA method in  
512 representing the chemical processes in the model. For example, during the first stage, the values of C for  $NO_x$ ,  $SO_2$ , and  $NH_3$   
513 were all negative where the C values for nitrate, sulfate and ammonium were positive, reflecting the conversion of reactive  
514 gases to  $PM_{2.5}$ . Consistent with the QDA results for  $PM_{2.5}$  concentration, the QDA results for SIAs and their precursors showed  
515 that chemistry provided an increasingly important role in the elevation of  $PM_{2.5}$  concentrations. From stage 1 to stage 2, the  
516 values of C for  $NO_x$  and  $SO_2$  changed from  $-0.18$  to  $-0.27 \mu g \cdot m^{-3} \cdot h^{-1}$  and from  $-0.01$  to  $-0.02 \mu g \cdot m^{-3} \cdot h^{-1}$ , respectively.  
517 Correspondingly, the values of C for nitrate and sulfate increased from  $0.21$  to  $0.26 \mu g \cdot m^{-3} \cdot h^{-1}$  and from  $0.02$  to  $0.03 \mu g \cdot m^{-3} \cdot h^{-1}$ ,  
518 respectively. Consistent with the NOR and SOR analysis, chemical processes yielded the largest contribution during stage 3,  
519 in which the values of C for  $NO_x$  and  $SO_2$  reached  $-0.45$  and  $-0.06 \mu g \cdot m^{-3} \cdot h^{-1}$ , respectively, which was 66.7% and more than  
520 twice as much as during stage 2. Correspondingly, the C value for sulfate increased from  $0.03$  to  $0.08 \mu g \cdot m^{-3} \cdot h^{-1}$  from stage 2  
521 to stage 3. However, the C value for nitrate and ammonium was found to decrease in stage 3. In addition, the values of CE for  
522 nitrate and ammonium were much larger in stage 3 than during stage 1 or stage 2, which reached up to  $0.46$  and  $0.15 \mu g \cdot m^{-3} \cdot h^{-1}$ ,  
523 respectively. More  $NH_3$  was also consumed by the interaction between chemistry and emissions during stage 3, with the value  
524 of CE reaching  $-0.15 \mu g \cdot m^{-3} \cdot h^{-1}$ . This is because  $NH_3$  was deficient during stage 3. Although more  $NO_x$  was oxidized to  $HNO_3$   
525 during stage 3, most of the newly formed  $HNO_3$  remained in the gas phase owing to the limited  $NH_3$ , leading to small C value  
526 for nitrate but large C values for  $NO_x$ . In addition, the newly emitted  $NH_3$  would react quickly with the pre-existing  $HNO_3$  to  
527 form nitrate and ammonium. That is why the values of CE for nitrate and ammonium were much larger in stage 3 than in  
528 previous stages. On the contrary, stage 1 and stage 2 were in an  $NH_3$ -rich condition, so the newly formed  $HNO_3$  and  $H_2SO_4$   
529 could react with the sufficient pre-existing  $NH_3$  to form nitrate and sulfate without relying on fresh emissions of  $NH_3$ . Therefore,  
530 there was good consistency between the C values of precursors and SIAs during stage 1 and stage 2. These results suggest that  
531 the QDA method is capable of reflecting different chemical environments during different stages of haze episodes, and  
532 emphasize that different emission control strategies should be adopted in different stages. For example, strict emissions control  
533 should be performed for  $NO_x$  and  $SO_2$  emissions during stage 1 and stage 2, while during stage 3, when the  $PM_{2.5}$  concentration



534 is highest, the control of  $\text{NH}_3$  emissions would be a more efficient approach. The high efficiency of reducing  $\text{NH}_3$  emissions  
535 in alleviating heavy haze has been attested in studies based on both observations and model results (Liu et al., 2022; Xu et al.,  
536 2019b; Qi et al., 2023; Zhai et al., 2021; Ge et al., 2019). However, these studies did not elucidate when is the most effective  
537 time to control  $\text{NH}_3$ . Not only can the QDA method quantitatively explain the role of  $\text{NH}_3$  in heavy haze, but it can also provide  
538 valuable information on when and where controlling  $\text{NH}_3$  emissions is more effective. Therefore, this method can provide  
539 policymakers with valuable insights into the development of efficient emission control strategies during different stages of  
540 pollution.

### 541 3.5.2 Meteorological processes

542 The contributions of meteorological processes were quantitatively evaluated via the analysis of weather conditions. Figure  
543 S6 clearly shows that, during stage 1, Beijing and its surrounding areas were influenced by a high-pressure system in  
544 northeastern Inner Mongolia and a low-pressure system in the southwest with high wind speeds, which promoted  $\text{PM}_{2.5}$   
545 advection across the Beijing area. With the low-pressure system in Inner Mongolia moving slowly eastwards and finally  
546 disappearing under the influence of westerly winds, Beijing was increasingly controlled by a uniform pressure field and  
547 affected by weak southerly winds, which facilitated the transportation of air pollution from the southern BTH region to Beijing.  
548 The small-scale high-pressure centre to the north of Beijing also blocked the airflow originating from the south, leading to the  
549 accumulation of air pollutants in Beijing, which is consistent with the positive pure meteorological contribution ( $M>0$ ) in stage  
550 2. The potential source contribution function (PSCF) index can reflect the potential contribution of the inflow trajectory,  
551 revealing that Baoding, Shijiazhuang and Cangzhou in Hebei in southern Beijing were the main sources of  $\text{PM}_{2.5}$  transmission  
552 in this case (Yan et al., 2015b). Research revealed that the transportation process in this case under the influence of weak  
553 southerly winds from 19 to 20 February, along with the Parameter Linking Air-quality to Meteorological conditions/haze index  
554 (PLAM), indicated a positive correlation between  $\text{PM}_{2.5}$  and atmospheric stability (Zhong et al., 2018b). An inversion layer  
555 occurred owing to the radiative cooling effect of the transported particles, which further aggravated aerosol accumulation  
556 (Zhong et al., 2018a) (Fig. 9). The key role of transmission in the formation of high concentrations of  $\text{PM}_{2.5}$  has also been  
557 found in other haze events (Sun et al., 2016; Huang et al., 2020; Zhang et al., 2019b).

558 In stage 3, the northern high-pressure system was compressed by the northwest low-pressure air system and moved to the  
559 southeast sea area. The isobaric lines in Beijing became increasingly dense and the wind speed increased, which was conducive  
560 to the diffusion of pollutants ( $M<0$ ). However, due to the positive contribution of emissions and chemistry, the air quality did  
561 not improve significantly. In stage 4, the northeast low-pressure system continued to develop and intensified, confronting the  
562 Mongolian high-pressure system, resulting in a strong northwesterly airflow in North China that transported air pollutants to  
563 the southeast sea area and greatly improved the air quality in Beijing. Therefore, the hourly contribution of  $M$  at this stage was  
564 the largest, reflecting a strong cleaning effect. This is also consistent with the analysis of this pollution case in other studies  
565 (Zhong et al., 2018b; Zhong et al., 2018a).



#### 566 4 Conclusions and perspectives

567 In this study, a new QDA method targeting PM<sub>2.5</sub> was developed and applied to analyse a typical heavy-pollution case in  
568 Beijing. By quantitatively decomposing the pure contribution of meteorology, chemical reactions, emissions, and their  
569 nonlinear interactions in the hourly change of the PM<sub>2.5</sub> concentration, the formation process of heavy haze can be analysed  
570 from a new perspective. The QDA method innovatively combines the advantages of the FS and IPR methods and highlights  
571 the differences and connections between pure contributions and nonlinear interactions in air pollution problems from the  
572 perspective of process contributions and conservation of mass as a constraint.

573 The atmosphere is a typical nonlinear system. Unfavorable meteorological conditions are a frequently discussed issue in  
574 haze events and their quantification can be biased by nonlinear effects such as EM and MC. Separating pure contributions and  
575 nonlinear interactions can clearly reveal the timing and effect of favorable or unfavorable meteorological conditions. We  
576 divided the haze event in this study into four stages according to the characteristics of PM<sub>2.5</sub> concentration. It was found that  
577 the M during the accumulation stage (stage 2) was 0.34 μg·m<sup>-3</sup>·h<sup>-1</sup>, while in other stages it was negative on average, indicating  
578 that the pure meteorological contribution only in the accumulation stage favored the accumulation of PM<sub>2.5</sub>. This means M  
579 mainly acts as a cleaner for PM<sub>2.5</sub> most of the time. However, when M continues for a period of time without removing  
580 pollution (M>0), PM<sub>2.5</sub> would lose its main mechanism to descend and therefore tend to grow rapidly under the superimposed  
581 influence of emissions and chemical processes, which would probably become the beginning of a heavy pollution event.  
582 Commonly, the effect of meteorological accumulation is the direct cause of haze formed by transportation and accumulation  
583 of PM<sub>2.5</sub>, and QDA provides a clearer interpretation of this. For the atmosphere of the entire boundary layer in particular, the  
584 direct cumulative effect of M on PM<sub>2.5</sub> is not high. M usually plays the role of the most efficient cleaner, but it is no longer  
585 effective under the circumstances of unfavorable meteorological conditions, resulting in the PM<sub>2.5</sub> (which formed by emissions  
586 and chemical reactions) not being cleaned up in time, which is why unfavorable meteorological conditions may play a dominant  
587 role in the formation of haze. The aim of this study was to develop a new analysis method rather than study its application, so  
588 QDA was only applied to one typical haze event, meaning more cases in different regions and periods should be studied in the  
589 future. The consideration of nonlinear effects provides a useful way to handle the nonlinear characteristics of the atmosphere,  
590 thus filling the gaps in traditional methods in terms of nonlinear uncertainty. The importance of nonlinear effects includes,  
591 firstly, eliminating the interference of other processes in quantifying the contribution of the target process and obtaining a more  
592 purified result; and secondly, some important implications, as follows. For chemical products, the change in the ratio of CE to  
593 C is helpful in evaluating the overall speed of the chemical processes; and the higher the proportion, the faster these processes  
594 might be. The contributions of C+CE play a significant role in stage 2 and 3, indicating that chemical reactions are more  
595 important in the most polluted period than in other periods. For the precursors (like NH<sub>3</sub>), the smaller the value of CE, the  
596 scarcer they are, and reducing their emissions in that period would have the most efficient controlling effect on the air pollution.  
597 For example, when SO<sub>2</sub> is rich and NH<sub>3</sub> is deficient, the CE values of nitrate and ammonium are usually large and that of  
598 sulfate is small. This provides a standard for judging NH<sub>3</sub>-rich or -poor periods. In addition, when EM or CE makes strong



599 positive contributions to  $PM_{2.5}$ , the suggestion is that additional benefits can be obtained by reducing  $PM_{2.5}$  emissions at that  
600 time. These implications can contribute to the formulation of refined emission reduction strategies.

601 The QDA method yields a strong general applicability and practical application prospects. Although the method was only  
602 applied to  $PM_{2.5}$ , its components, and precursors in NAQPMS in this study, not only can it also be applied to any 3D  
603 atmospheric chemistry model, but also to study any other pollutant. It can analyse the causes of pollution from different  
604 substances. For example, application to the analysis of oxidants (e.g.,  $O_3$  and oxidative radicals), which are of wide concern in  
605 CTMs, could enable in-depth studies of the nonlinear effects of chemical processes in the atmosphere. QDA can be used to  
606 track the chain reactions caused by the changes in physical parameterization schemes or chemical reactions in CTMs, so as to  
607 improve and test new mechanisms. Not only does this technique provide new reference ideas for the treatment of air pollution,  
608 but it is also an important tool for further studying the formation processes of heavy pollution and the influence of different  
609 physicochemical mechanisms.

#### 610 **Code and data availability**

611 The observational data used in this study and the source codes of the QDA method are available online via ZENODO  
612 (<http://doi.org/10.5281/zenodo.5292895>). Please contact Junhua Wang ([wangjunhua@mail.iap.ac.cn](mailto:wangjunhua@mail.iap.ac.cn)) to obtain the model data  
613 for the QDA method used in NAQPMS.

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#### 617 **Author contributions**

618 Junhua Wang prepared the original data, designed and conducted the simulation, and carried out the QDA method. Baozhu Ge  
619 and Xueshun Chen revised the paper and provided scientific guidance for the article design. Yayuan Dong gave advice on the  
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622 have read and approved the final manuscript.

#### 623 **Competing interests**

624 The authors declare that they have no conflicts of interest.

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927 **Tables & Figures:**

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**Table 1. Definitions of different factors considered in the QDA method**

Notation	Equation	Definition
E	$\frac{\partial F}{\partial x_1} x_1 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_1^2} x_1^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_1^3} x_1^3 + \dots$	Pure emission contribution
M	$\frac{\partial F}{\partial x_2} x_2 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_2^2} x_2^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_2^3} x_2^3 + \dots$	Pure meteorology contribution
C	$\frac{\partial F}{\partial x_3} x_3 + \frac{1}{2!} \frac{\partial^2 F}{\partial x_3^2} x_3^2 + \frac{1}{3!} \frac{\partial^3 F}{\partial x_3^3} x_3^3 + \dots$	Pure chemistry contribution
ME	$\frac{1}{2!} \frac{2\partial^2 F}{\partial x_1 \partial x_2} x_1 x_2 + \frac{1}{3!} \sum_{a=1}^2 \frac{3\partial^3 F}{\partial x_1^a \partial x_2^{3-a}} x_1^a x_2^{3-a} + \dots$	Interaction of meteorology and emissions
MC	$\frac{1}{2!} \frac{2\partial^2 F}{\partial x_2 \partial x_3} x_2 x_3 + \frac{1}{3!} \sum_{a=1}^2 \frac{3\partial^3 F}{\partial x_2^a \partial x_3^{3-a}} x_2^a x_3^{3-a} + \dots$	Interaction of meteorology and chemistry
CE	$\frac{1}{2!} \frac{2\partial^2 F}{\partial x_1 \partial x_3} x_1 x_3 + \frac{1}{3!} \sum_{a=1}^2 \frac{3\partial^3 F}{\partial x_1^a \partial x_3^{3-a}} x_1^a x_3^{3-a} + \dots$	Interaction of emissions and chemistry
MCE	$\frac{1}{3!} \left( \frac{\partial^3 F}{\partial x_1 \partial x_2 \partial x_3} 6x_1 x_2 x_3 \right) + \dots$	Three-way interaction of emissions, meteorology and chemistry

929 Note: The order of capital letters under “Notation” does not represent the order of operators. For example, ME and EM can represent the  
 930 same meaning, so it is uniformly expressed by ME in this paper.

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**Table 2. Descriptions of the built-in scenario simulations in the QDA method**

	Simulation notation	Processes included in the simulations	Target values (e.g., model step of $t$ to $t+1$ )
Base simulation	base	All model processes	$F(x_1, x_2, x_3)$ , $F(0,0,0)$
Built-in scenario simulations	$S_1$	Only emission process	$F(x_1, 0, 0)$
	$S_2$	Only meteorological process	$F(0, x_2, 0)$
	$S_3$	Only chemical process	$F(0, 0, x_3)$
	$S_{13}$	Emission and chemical processes	$F(x_1, 0, x_3)$
	$S_{23}$	Meteorological and chemical processes	$F(0, x_2, x_3)$
	$S_{12}$	Emission and meteorological processes	$F(x_1, x_2, 0)$

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**Table 3. Descriptions of different processes considered in the IPR method**

Description	Abbreviation
Emissions (local primary emissions in model)	emit
Horizontal advection	advhor
Vertical advection	advvert
Horizontal diffusion	difhor
Vertical diffusion	difvert
Wet deposition	wetdep
Dry deposition	drydep
Gas chemistry	gaschem
Inorganic aerosol chemistry	ISORR
Secondary aerosol chemistry	SOA

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**Table 4. Hourly average QDA results in different stages (unit:  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ )**

	Stage 1		Stage 2		Stage 3		Stage 4	
<b>Hourly change</b>	-1.36		1.79		0.1		-11.84	
<b>M</b>	-2.60	191.18%	0.34	18.99%	-1.75	-1750.00%	-12.62	106.59%
<b>E</b>	0.88	-64.71%	0.82	45.81%	0.88	880.00%	0.63	-5.32%
<b>C</b>	0.31	-22.79%	0.37	20.67%	0.23	230.00%	-0.08	0.68%
<b>COUP</b>	0.05	-3.68%	0.26	14.53%	0.74	740.00%	0.23	-1.94%
<b>EM</b>	-0.08	5.88%	-0.08	-4.47%	-0.09	-90.00%	-0.11	0.93%
<b>CE</b>	0.10	-7.35%	0.13	7.26%	0.67	670.00%	0.43	-3.63%
<b>MC</b>	-0.01	0.74%	0.20	11.17%	0.03	30.00%	-0.14	1.18%
<b>MCE</b>	0.04	-2.94%	0.01	0.56%	0.13	130.00%	0.05	-0.42%

954 Note: Hourly change= $M+C+E+COUP$ ;  $COUP=EM+CE+MC+MCE$ .

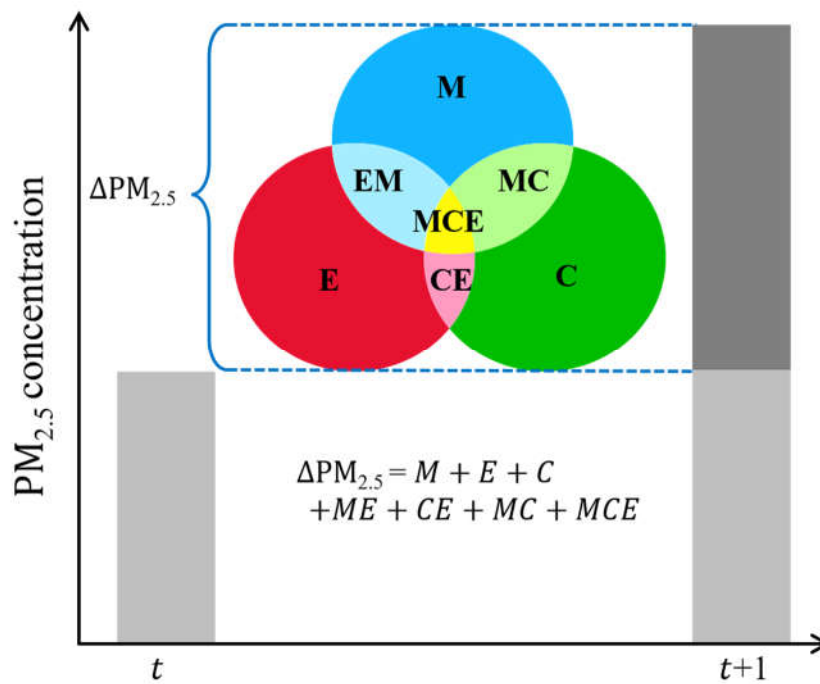
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**Table 5. Hourly average IPR results in different stages (unit:  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ )**

	emit	advhor	advvert	difhor	difvert	gaschem	drydep	ISORR	wetdep	SOA
<b>Stage 1</b>	0.88	-3.32	0.94	-0.002	-0.28	0.00	-0.02	0.44	0.00	0.02
<b>Stage 2</b>	0.82	0.03	0.58	-0.01	-0.34	0.00	-0.03	0.71	0.00	0.02
<b>Stage 3</b>	0.88	0.18	-1.45	-0.01	-0.57	0.00	-0.04	1.07	0.00	0.04
<b>Stage 4</b>	0.63	-13.26	0.71	-0.002	-0.22	0.00	-0.03	0.32	0.00	0.003

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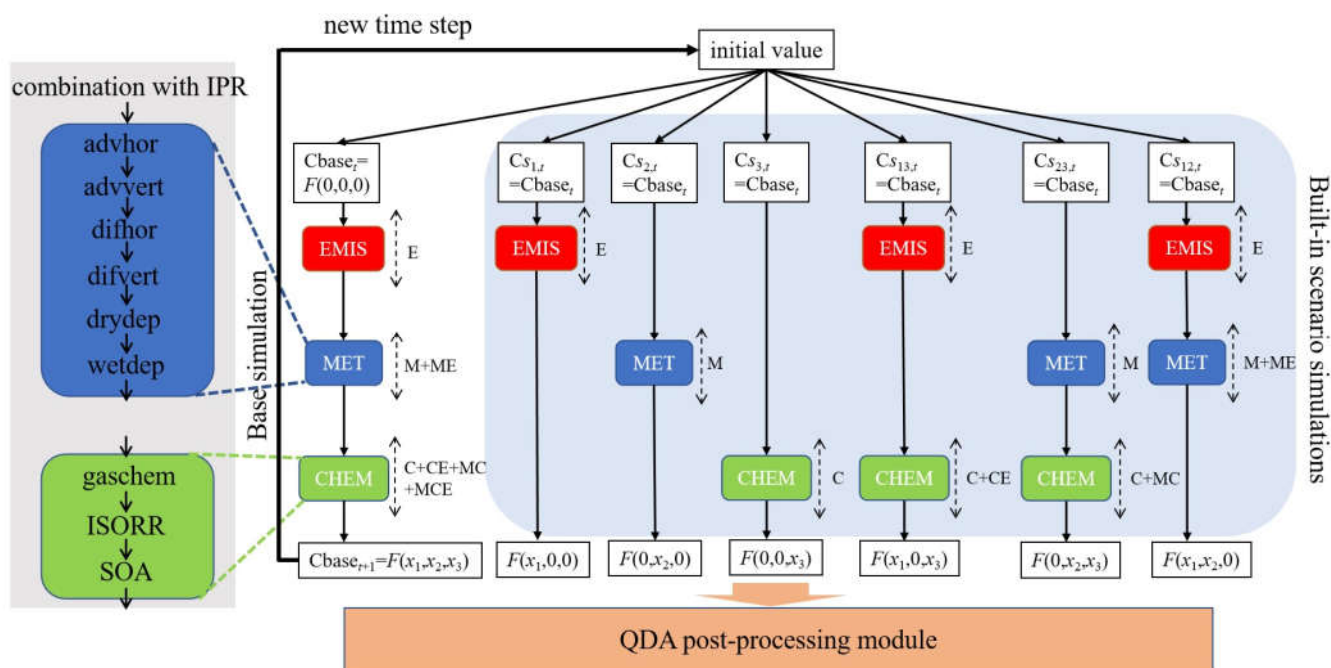


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959 **Figure 1. Graph theory of the QDA method. The total area of the colour graphics represents the hourly change in the PM<sub>2.5</sub>**  
960 **concentration between  $t$  and  $t+1$ , which can be resolved into seven quantitative analytical factors—see Table 1 for meanings of the**  
961 **abbreviations.**

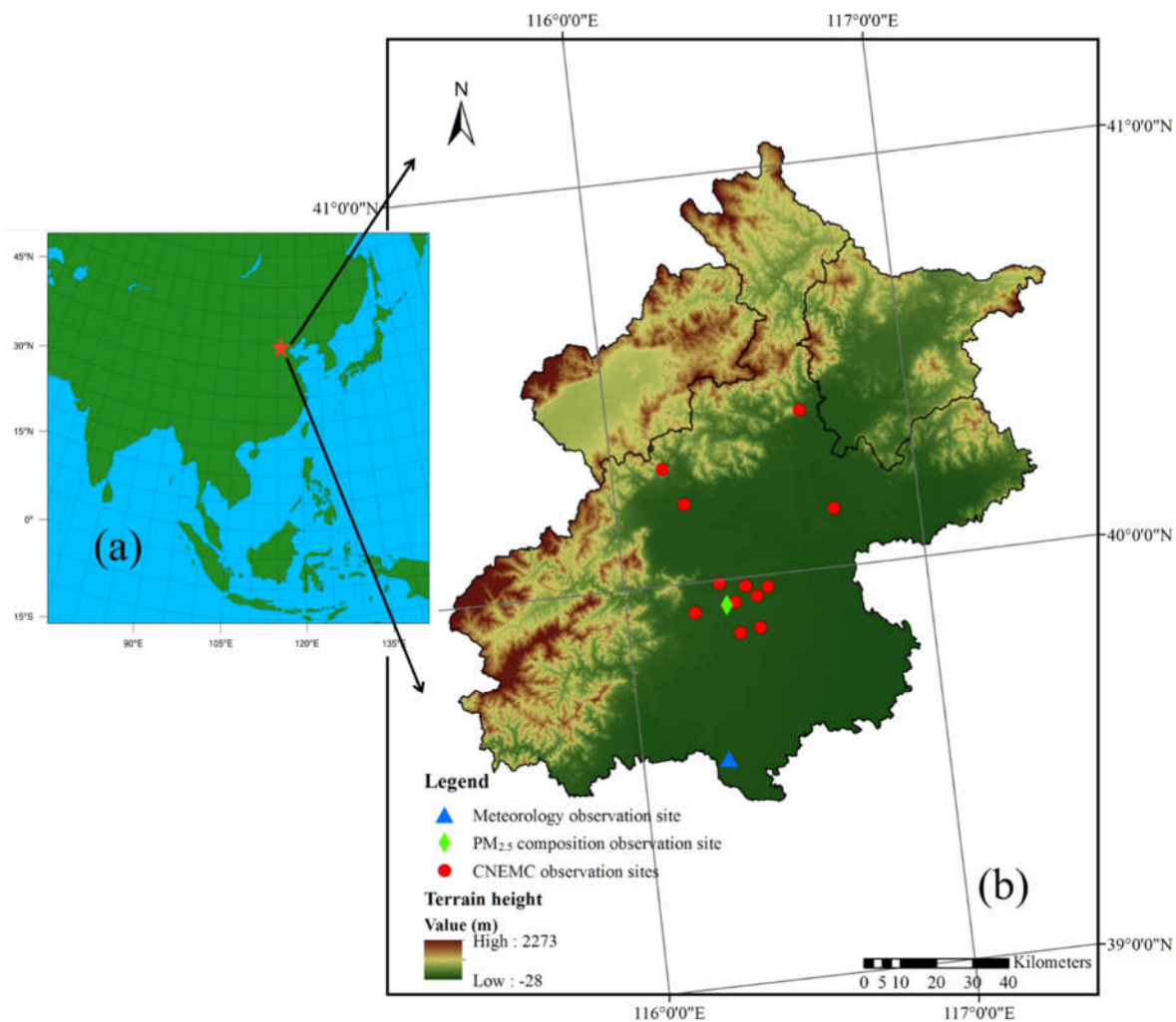
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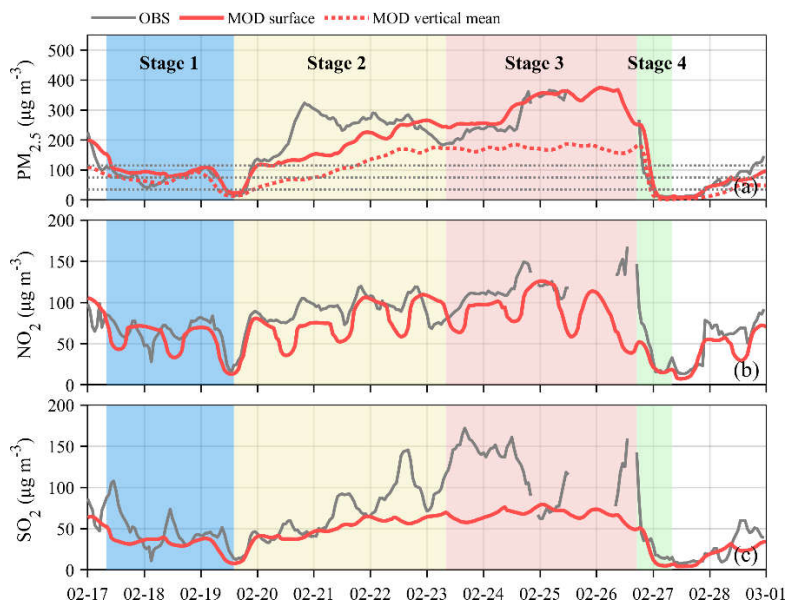


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965 Figure 2. Flow chart of the QDA method [see Eqs. (15)–(24) in Sect. 2.3 for the QDA post-processing module].



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967 **Figure 3. (a) Model domain and (b) observation sites in Beijing for the evaluation in this study.**  
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970 **Figure 4. Observations (OBS) and simulation results (MOD) for (a) PM<sub>2.5</sub>, (b) NO<sub>2</sub> and (c) SO<sub>2</sub> in Beijing. All simulation and**  
971 **observation results are averaged over the Beijing area. The three grey dotted lines indicate 35, 75 and 115 µg·m<sup>-3</sup>.**

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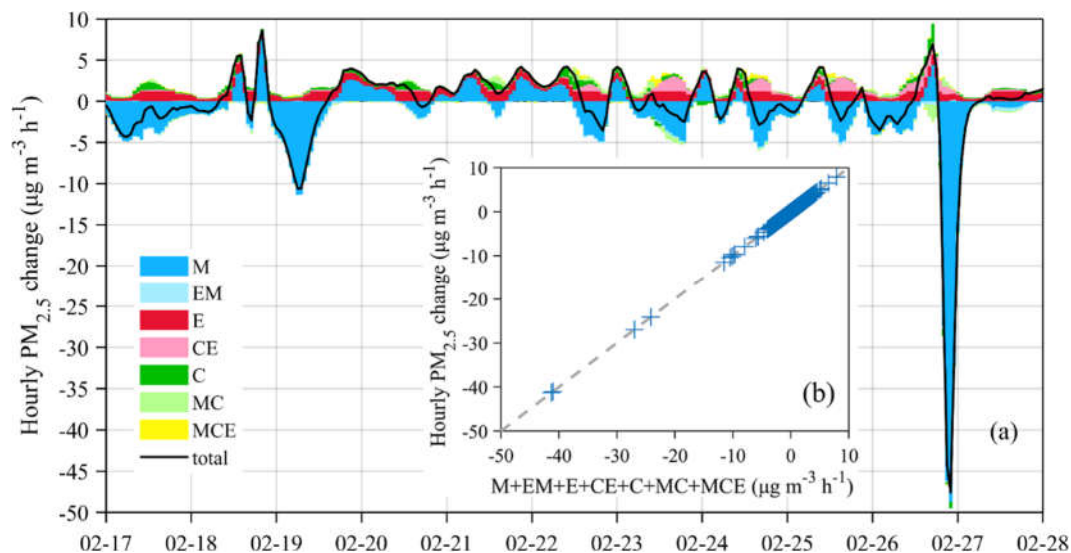
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982 **Figure 5. (a) QDA results and PM<sub>2.5</sub> hourly concentration change (black line) between adjacent hours and (b) scatterplot of the sum**  
983 **of all contributions versus the PM<sub>2.5</sub> hourly concentration change. The scattered points all fall on the 1:1 diagonal line, indicating**  
984 **that the PM<sub>2.5</sub> concentration change can be fully resolved by the QDA results.**

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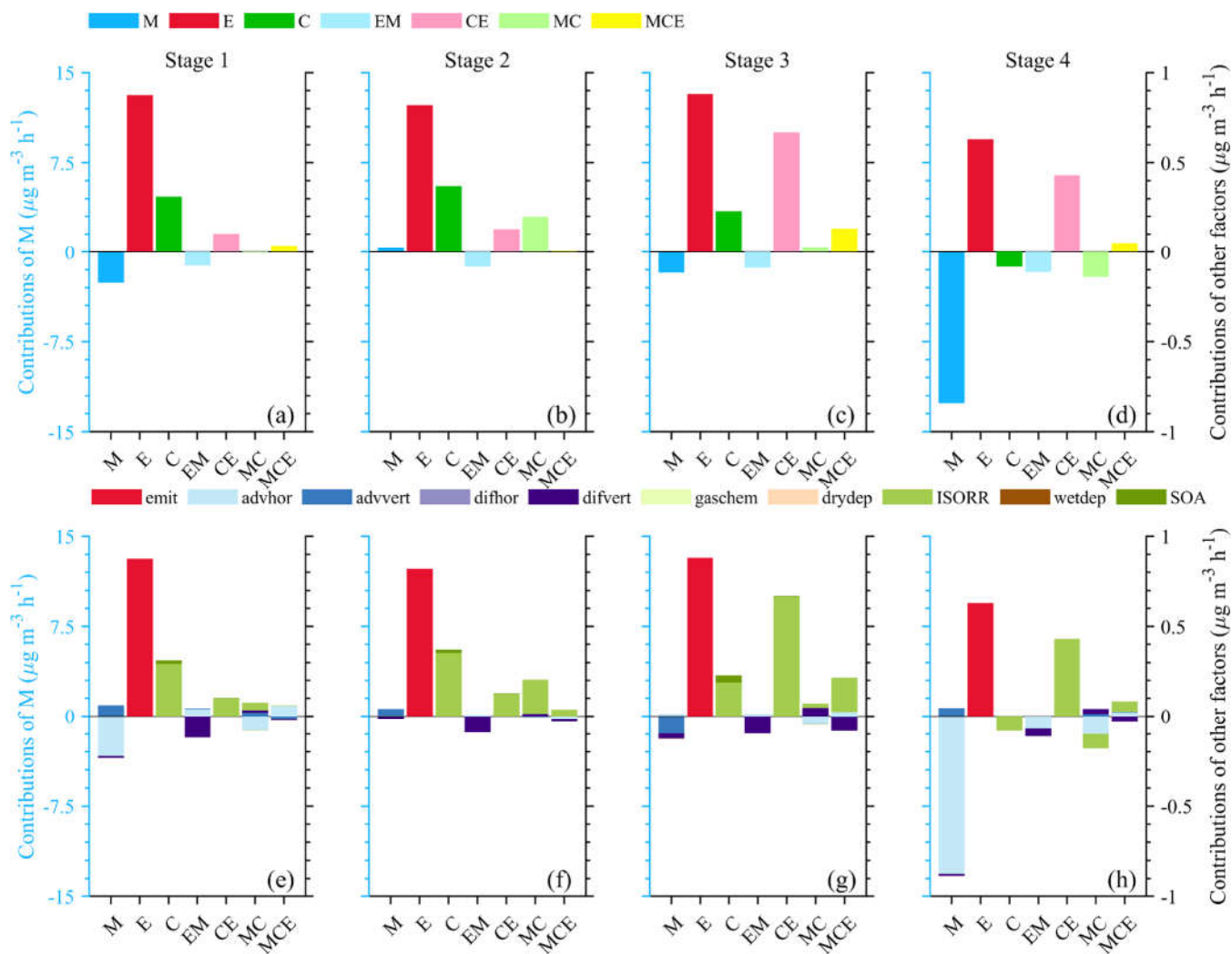
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992 **Figure 6.** Vertical mean hourly contribution of each factor in (a–d) QDA and (e–h) its IPR results that influence the hourly mean  
 993 **PM<sub>2.5</sub>** change within the model height in different stages. There is correspondence between the upper and lower subgraphs and the  
 994 **bar values are available in Tables 4 and 5.** Taking the M bar in (a) for example, M is composed of six contributing parts as displayed  
 995 **in the M bar of (e): ‘advhor’, ‘advvert’, ‘difhor’, ‘difvert’, ‘drydep’ and ‘wetdep’, respectively.**

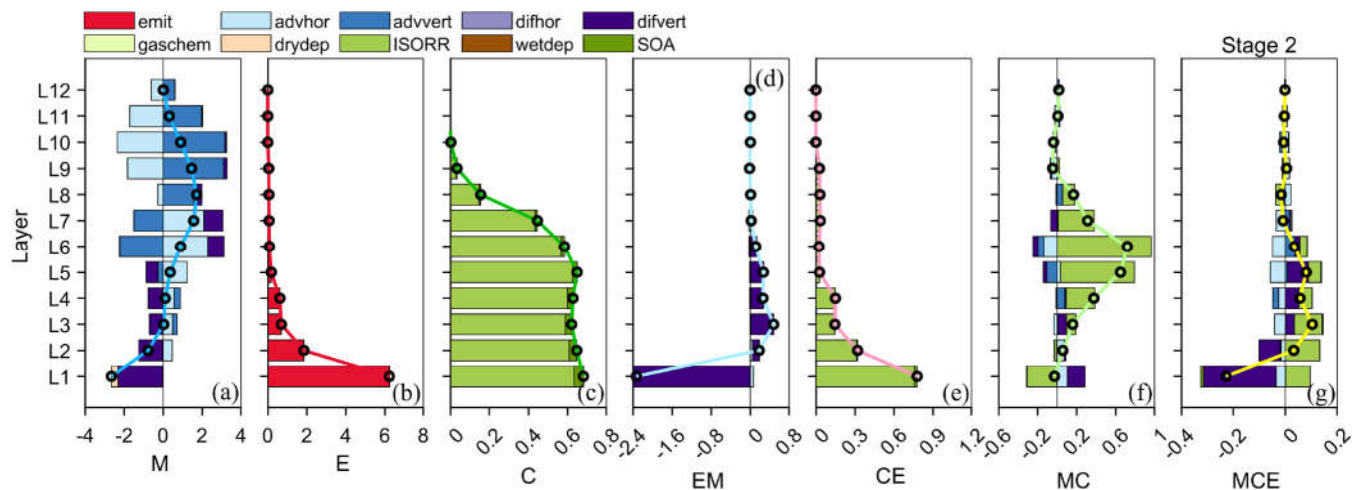
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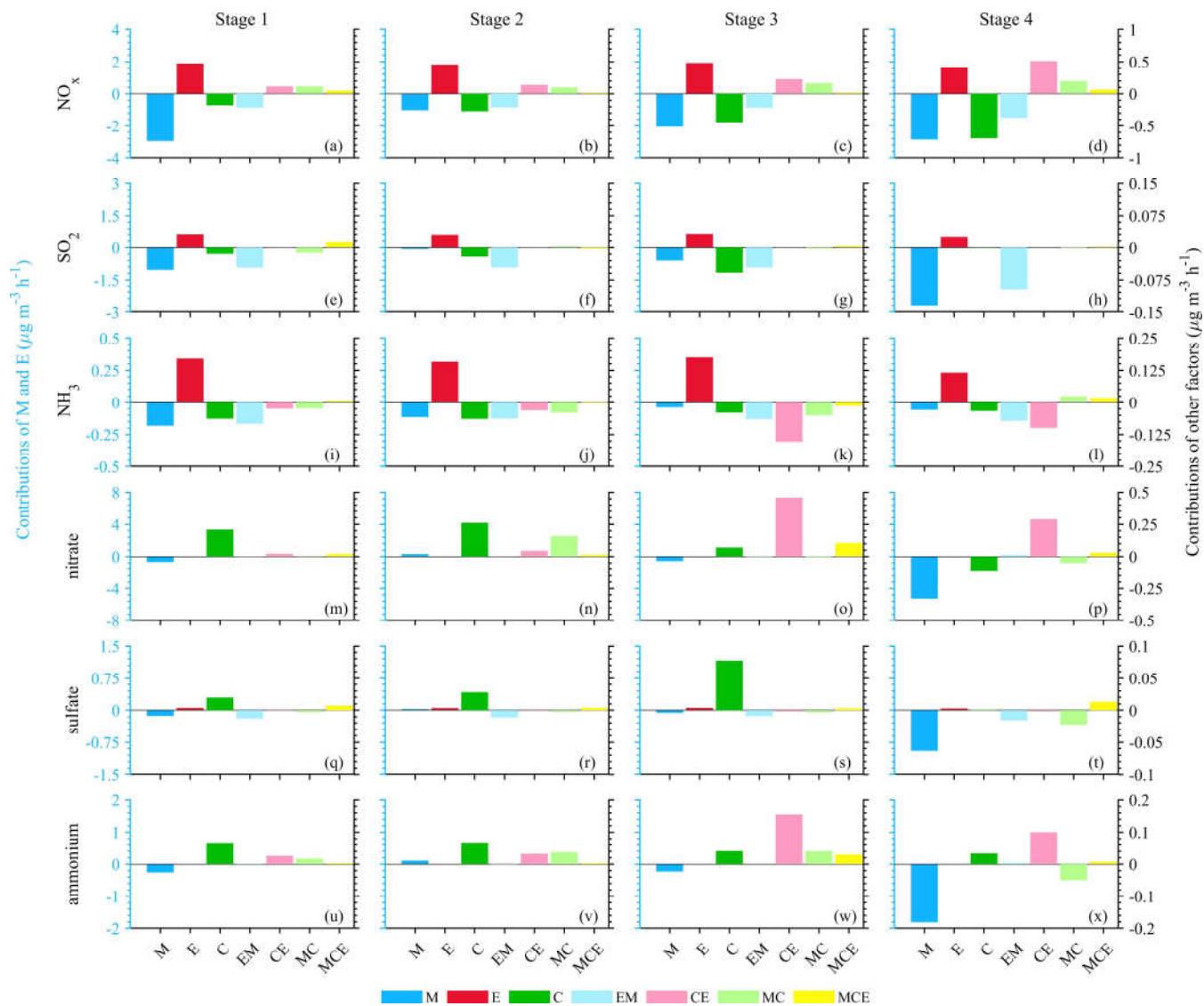
1002 **Figure 7. Vertical process decomposition of the QDA results in stage 2 (the black arrow and coloured lines indicate the average**  
1003 **change in the PM<sub>2.5</sub> concentration, and the results for other stages are shown in Figs. S7–S9; unit:  $\mu\text{g}\cdot\text{m}^{-3}\cdot\text{h}^{-1}$ ). The layer heights,**  
1004 **L1–L12 are: 112, 222, 361, 531, 740, 989, 1279, 1627, 2046, 2555, 3163, and 3890 m.**

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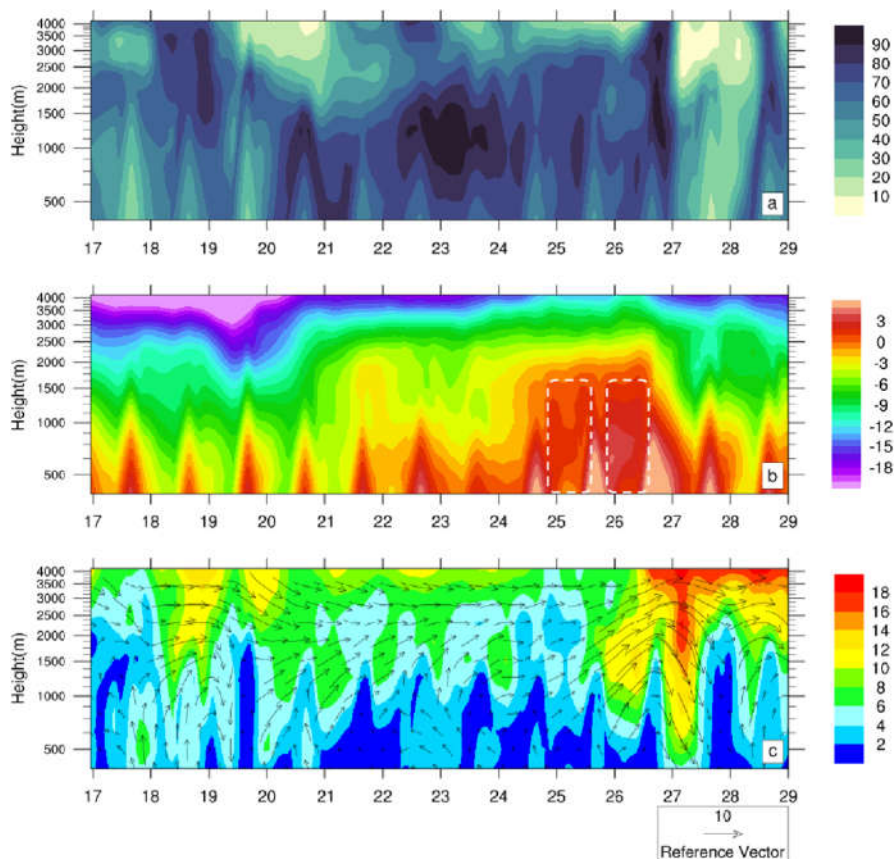
1010 **Figure 8.** QDA results for (a–d)  $\text{NO}_x$ , (e–h)  $\text{SO}_2$ , (i–l)  $\text{NH}_3$ , (m–p) nitrate, (q–t) sulfate, and (u–x) ammonium, during different stages  
 1011 of the episode.

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1016 **Figure 9. Vertical distribution of (a) RH, (b) temperature and (c) wind field from 17 to 28 February 2014 over the Beijing area in a**  
1017 **sigma- $p$  vertical coordinate. The white dotted frames in (b) represent a temperature inversion. The vector diagram in (c) represents**  
1018 **the horizontal wind field, and the shading denotes the wind speed.**

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