# A spatiotemporally separated framework for reconstructing the source of atmospheric radionuclide releases

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8 Abstract. Determining the source location and release rate are critical tasks in assessing the environmental consequences of 9 atmospheric radionuclide releases, but remain challenging because of the huge multi-dimensional solution space. We propose 10 a spatiotemporally separated two-step framework that reduces the dimension of the solution space in each step and improves 11 the source reconstruction accuracy. The separation process applies a temporal sliding-window average filter to the observations, 12 thereby reducing the influence of temporal variations in the release rate on the observations and ensuring that the features of 13 the filtered data are dominated by the source location. A machine learning model is trained to link these features to the source 14 location, enabling independent source location estimations. The release rate is then determined using projected alternating 15 minimization with the L1-norm and total variation regularization algorithm. This method is validated against the local-scale 16 SCK-CEN <sup>41</sup>Ar field experiment and the first release of the continental-scale European Tracer Experiment, for which the 17 lowest source location errors are 4.52 m and 5.19 km, respectively. This presents higher accuracy and a smaller uncertainty 18 range than the correlation-based and Bayesian methods in estimating the source location. The temporal variations in release 19 rates are accurately reconstructed, and the mean relative errors of the total release are 65.09% and 72.14% lower than the 20 Bayesian method for the SCK-CEN experiment and European Tracer Experiment, respectively. A sensitivity study 21 demonstrates the robustness of the proposed method to different hyperparameters. With an appropriate site layout, low error 22 levels can be achieved from only a single observation site or under meteorological errors.

## 23 **1. Introduction**

Atmospheric radionuclide release is a major environmental concern of the nuclear industry, including nuclear energy and its heat applications, isotope production, and the post-processing of radioactive waste. Such releases occurred after the Chernobyl nuclear accident (Anspaugh et al., 1988) and the Fukushima nuclear explosion (Katata et al., 2012), with partially known source information, i.e. the location. Recently, there have been several atmospheric radionuclide leaks from unknown sources, such as the 2017 <sup>106</sup>Ru leakage (Masson et al., 2019) and the 2020 <sup>134/137</sup>Cs detection in northern Europe (Ingremeau and Saunier, 2022), which have raised global concerns regarding the subsequent hazard to public health. Identification of source 30 information in these events is critical for the safe operation of nuclear facilities, consequence assessment, and emergency

31 response.

32 During these events, source data often cannot be directly measured or determined because of the lack of information on the 33 source of the leak. Instead, source information can only be reconstructed through inversion methods, which identify the optimal 34 solution by comparing the environmental observations with atmospheric dispersion simulations using different estimates of 35 the source location and release rate. Such reconstructions simultaneously identify the source location and release rate because 36 the observations are intuitively determined by both parameters. In this case, the reconstruction searches for a solution over a 37 large multi-dimensional space, where the dimension is the sum of the number of space coordinates and the length of the 38 estimated release window. Therefore, the inversion is weakly constrained and can become ill-posed in the case of 39 spatiotemporally limited observations and uncertainties in the atmospheric dispersion models. Unfortunately, this is quite often 40 the case for atmospheric radionuclide releases.

41 To reduce the problem of ill-posedness, most previous studies have attempted to constrain the reconstruction by imposing 42 assumptions on the model-observation discrepancies or release characteristics. Assumptions on model-observation 43 discrepancies are widely used in Bayesian methods to simultaneously reconstruct the posterior distributions of spatiotemporal 44 source parameters (De Meutter et al., 2021; Meutter and Hoffman, 2020; Xue et al., 2017a). This assumes that the model-45 observation discrepancies follow a certain statistical distribution (i.e. the likelihood of Bayesian methods), with the normal 46 (Eslinger and Schrom, 2016; Guo et al., 2009; Keats et al., 2007, 2010; Rajaona et al., 2015; Xue et al., 2017a, b; Yee, 2017; 47 Yee et al., 2008; Zhao et al., 2021) and log-normal (Chow et al., 2008; Dumont Le Brazidec et al., 2020; KIM et al., 2011; 48 Monache et al., 2008; Saunier et al., 2019; Senocak, 2010; Senocak et al., 2008) distributions being two popular choices. Other 49 candidates include the t-distribution (with degrees of freedom ranging from 3–10). Cauchy distribution, and log-Cauchy 50 distribution, all of which were compared against the normal and log-normal distributions in terms of reconstructing the source 51 parameters of the Prairie Grass field experiment (Wang et al., 2017). The results demonstrate that the likelihoods are sensitive 52 to both the dataset and the target source parameters. Several studies have constructed the likelihood based on multiple metrics 53 that measure the model-observation discrepancies in an attempt to better constrain the solution (Lucas et al., 2017; Jensen et 54 al., 2019). More sophisticated methods involve the use of different statistical distributions for the likelihoods of non-detections 55 and detections (De Meutter et al., 2021; Meutter and Hoffman, 2020). Recent studies have suggested the use of log-based 56 distributions and tailored parameterization of the covariance matrix as a means of better quantifying the uncertainties in the 57 reconstruction (Dumont Le Brazidec et al., 2021). These Bayesian methods have been applied to real atmospheric radionuclide 58 releases, such as the 2017 <sup>106</sup>Ru event, and have provided important insights into the source and release process (Dumont Le 59 Brazidec et al., 2020; Saunier et al., 2019; Dumont Le Brazidec et al., 2021; De Meutter et al., 2021). However, these studies have also revealed that the likelihood in Bayesian methods must be exquisitely designed and parameterized to achieve 60 61 satisfactory spatiotemporal source reconstruction (Dumont Le Brazidec et al., 2021; Wang et al., 2017), With suboptimal 62 design, the reconstruction may exhibit a bimodal posterior distribution (Meutter and Hoffman, 2020), which remains a 63 challenge for robust applications in different scenarios.

64 Assumptions on the release characteristics aim to reduce the dimension of the solution space to 4 or 5, namely the two source 65 location coordinates, the total release, and the release time (or the release start and end time), i.e. an instantaneous release at 66 one time or constant release over a period (Kovalets et al., 2020, 2018; Efthimiou et al., 2018, 2017; Tomas et al., 2021; 67 Andronopoulos and Kovalets, 2021; Ma et al., 2018). Under these assumptions, the correlation-based method exhibits high 68 accuracy for ideal cases under stationary meteorological conditions, such as synthetic simulation experiments (Ma et al., 2018) 69 and wind tunnel experiments (Kovalets et al., 2018; Efthimiou et al., 2017). However, previous studies have also demonstrated 70 that real-world applications may be much more challenging. (Koyalets et al., 2020; Tomas et al., 2021; Andronopoulos and 71 Kovalets, 2021; Becker et al., 2007) because the release usually exhibits temporal variations and may experience non-72 stationary meteorological fields. In addition, inaccurate calculation of the meteorological field input can further intensify these 73 challenges. The interaction between the time-varying release characteristics and non-stationary meteorological fields is 74 neglected in the instantaneous-release and constant-release assumptions, leading to inaccurate reconstruction.

75 Given the assumption-related reconstruction deviations in complex scenarios, we propose a spatiotemporally separated 76 source reconstruction method that is less dependent on such assumptions. Our approach reduces the complexity of the source 77 reconstruction using the simple fact that the source location is fixed during the atmospheric radionuclide release process. In 78 this case, the spatiotemporal variations of observations are influenced by the time-varying release rate, source location, and 79 meteorology, of which the last variable is generally known. The proposed method reduces the influence of the release rate 80 through a temporal sliding-window average filter, making the filtered observations more sensitive to the source location than 81 to the release rate. After filtering, existing methods based on direct observation-simulation comparisons may be unable to 82 locate the source. Thus, the response features of the filtered observations are extracted and mapped to the source location by training a data-driven machine learning model using the extreme gradient boosting (XGBoost) algorithm (Chen and Guestrin, 83 84 2016). To fully capture the response features at each observation site, tailored time- and frequency-domain features are 85 designed and optimized using the feature selection technique of XGBoost. Using this optimized model, the source location is 86 estimated based on the filtered observations. Once the source location has been retrieved, the non-constant release rate is 87 determined using the Projected Alternating MInimization with L1-norm and Total variation regularization (PAMILT) 88 algorithm (Fang et al., 2022), which is robust to model uncertainties. The sequential spatiotemporal reconstruction reduces the 89 dimension of the solution space at each step, which helps to improve the accuracy and reliability of the reconstruction.

The proposed method is validated using the data from multi-scales field experiments, namely the local-scale SCK-CEN <sup>41</sup>Ar experiment (Rojas-Palma et al., 2004), and the first release of the continental scale European Tracer Experiment (ETEX-1) (Nodop et al., 1998), which traced emissions of Perfluoro-Methyl-Cyclo-Hexane (PMCH). The performance of the proposed method is compared with the correlation-based method in terms of source location estimation and the Bayesian method in terms of spatiotemporal accuracy. The sensitivity of the source location estimation to the spatial search range, size of the sliding window, feature type, number and combination of sites, and meteorological errors is also investigated for the SCK-CEN <sup>41</sup>Ar experiment.

#### 97 2. Materials and Methods

#### 98 **2.1 Source reconstruction models**

99 For an atmospheric radionuclide release, Eq. (1) relates the observations at each observation site to the source parameters:

100 
$$\boldsymbol{\mu} = \mathbf{F}(\mathbf{r}, \mathbf{q}) + \boldsymbol{\varepsilon}$$
, (1)

101 where  $\boldsymbol{\mu} = [\mu_1, \mu_2, \dots, \mu_N]^T \in \mathbb{R}^N$  is an observation vector composed of *N* observations, the function **F** maps the source 102 parameters to the observations, i.e. an atmospheric dispersion model, **r** refers to the source location,  $\mathbf{q} \in \mathbb{R}^S$  is the temporally 103 varying release rate, and  $\boldsymbol{\varepsilon} \in \mathbb{R}^N$  is a vector containing both model and measurement errors.

104 In most source reconstruction models,  $\mathbf{F}$  is simplified to the product of  $\mathbf{q}$  and a source–receptor matrix  $\mathbf{A}$  that depends on 105 the source location:

106 
$$\boldsymbol{\mu} = \mathbf{A}(\mathbf{r})\mathbf{q} + \boldsymbol{\varepsilon}, \tag{2}$$

107 where  $\mathbf{A}(\mathbf{r}) = [A_1(\mathbf{r}), A_2(\mathbf{r}), \dots, A_N(\mathbf{r})]^T \in \mathbb{R}^{N \times S}$  and each row describes the sensitivity of an observation to the release rate 108 **q** given the source location **r**.

#### 109 2.2 Observation filtering for spatiotemporally separated reconstruction

110 A straightforward way to solve Eq. (2) is to simultaneously retrieve the source location and release rate; however, the solution 111 space is huge and difficult to constrain. Several studies have noted that the source location can be retrieved separately without 112 knowledge of the exact release rate, on the condition that the release rate is constant (Efflimiou et al., 2018; Kovalets et al., 113 2018; Efthimiou et al., 2017; Ma et al., 2018). The key reason is that, in constant-release cases, the relative spatiotemporal 114 distribution of radionuclides is determined by the meteorological conditions and the relative positions between the source and 115 receptors, and the constant release rate only changes the absolute values. Although the release rate may counteract the influence 116 of the meteorological conditions and relative position at a single observation site, it cannot change the whole spatiotemporal 117 distribution at multiple observation sites. Therefore, by analysing the spatiotemporal distribution of radionuclides at multiple 118 observation sites, it is possible to locate the source without knowing the release rate under the constant-release assumption.

119 To provide a more general method, we take advantage of the fact that the source location has been fixed during all known 120 atmospheric radionuclide releases, such as the Chernobyl nuclear accident (Anspaugh et al., 1988), Fukushima nuclear 121 explosion (Katata et al., 2012), and 2017<sup>106</sup>Ru leakage (Masson et al., 2019). With a fixed source location, the release rate and 122 meteorology jointly determine the temporal variations of the observations (Li et al., 2019b). The influence of meteorology can 123 be pre-calculated as the source-receptor sensitivities and subsequently stored in matrix  $\mathbf{A}(\mathbf{r})$ . By reducing the influence of the 124 release rate, the constant-release case can be approximated and the sensitivity of the observations to the source location can be 125 improved, enabling separate source location and release rate estimations and reducing the solution space at each step. For this purpose, we introduce an operator matrix  $\mathbf{P} \in \mathbb{R}^{N \times N}$  to reduce the temporal variations of  $\mathbf{A}(\mathbf{r})\mathbf{q}$ : 126

# 127 $\mu_p = \mathbf{P}\boldsymbol{\mu} = \mathbf{P}\mathbf{A}(\mathbf{r})\mathbf{q} + \mathbf{P}\boldsymbol{\varepsilon}$ ,

where  $\mu_p$  refers to the filtered observations. In this study, the following operator matrix is constructed to impose a one-sided temporal sliding-window average filter (Eamonn Keogh, Selina Chu, 2004):

where T is the size of the sliding window. This one-sided filter involves the current and previous observations in the window, acknowledging that future observations are not available for filtering in practice. Although a sliding-window average filter is used in this study, Eq. (3) is compatible with more advanced processing methods.

### 134 **2.3 Source location estimation without knowing the exact release rates**

135 After applying the filter in Eq. (4), the peak observations, primarily shaped by the temporal release profile, are smoothed out. 136 However, the influences of the source position and meteorology remain relatively unchanged, as they determine the long-term 137 temporal trends of observations and are less affected by the filter. The meteorology is known, so it becomes possible to locate 138 the source using the filtered observations. Nevertheless, the specificity of source location estimation methods that rely on direct 139 observation-simulation comparisons may be substantially compromised because the peak amplitude is reduced. A better choice 140 for locating the source would be to use the response features of the filtered observations, which preserve most of the location 141 information. Therefore, it is necessary to establish a link between the response features of the filtered observations and the 142 source location. To achieve this, we train an XGBoost model that maps the response features of the filtered observations to the 143 coordinates of the source.

144 XGBoost is an optimized distributed gradient boosting library. Suppose  $D = \{(\mathbf{X}_i, \mathbf{r}_i)\}(|D| = n, \mathbf{X}_i \in \mathbb{R}^p, \mathbf{r}_i \in \mathbb{R}^2)$ , where 145 the number of samples is *n* and each sample contains *p* features.  $\mathbf{X}_i$  is the given input feature vector of the *i*-th sample and 146  $\mathbf{r}_i = (x_i, y_i)$  is the location vector. XGBoost typically uses multiple decision trees (Fig. 1) to fit the target, which can be 147 formulated as:

148 
$$\hat{\mathbf{r}}_i = G(\mathbf{X}) = \sum_{k=1}^K f_k(\mathbf{X}_i), f_k \in \mathcal{F},$$
(5)

149 where *K* is the number of trees,  $\mathcal{F} = \{f(x) = \omega_{Q(x)}\}(Q: \mathbb{R}^p \to M, \omega \in \mathbb{R}^M)$  is the space of the decision trees, and *Q* 150 represents the structure of each tree, mapping the feature vector to *M* leaf nodes. Each  $f_k$  corresponds to an independent tree 151 structure *Q* with leaf node weights  $\boldsymbol{\omega} = (\omega_1, \omega_2, \cdots, \omega_M)$ . Equation (5) is then used to predict  $\hat{\mathbf{r}}_i = (\hat{x}_i, \hat{y}_i)$  for the *i*-th sample.





Figure 1. Flowchart of XGBoost for predicting  $\hat{\mathbf{r}}_i$  based on decision tree model. The yellow squares are the root nodes within each tree, representing the input features in this paper. The purple ellipses denote the child nodes where the model evaluates input features and make decisions to split the data. The green rectangles depict the leaf nodes and refer to the prediction results. The vertical rectangles abstract the internal splitting processes of the trees, indicating decision-making not explicitly detailed in the diagram.

157 XGBoost trains  $G(\mathbf{X})$  in Eq. (5) by continuously fitting the residual error until the following objective function is minimized:

158 
$$Obj^{(t)} = \sum_{i=1}^{n} \left( \mathbf{r}_{i} - \left( \hat{\mathbf{r}}_{i}^{(t-1)} + f_{t}(\mathbf{X}_{i}) \right) \right)^{2} + \sum_{i=1}^{t} \Omega(f_{i}) , \qquad (6)$$

159 where t represents the training of the t-th tree and  $\Omega(f_i)$  is the regularization term, given by:

160 
$$\Omega(f) = YM + \frac{1}{2}\lambda \sum_{j=1}^{M} \omega_j^2$$
, (7)

where *M* is the number of leaf nodes,  $\omega_j$  is the leaf node weight for the *j*-th leaf node, and  $\Upsilon$ ,  $\lambda$  are penalty coefficients. The minimization of Eq. (6) provides a parametric model  $G(\mathbf{X})$  that maps the feature ensemble  $\mathbf{X}$  extracted from  $\boldsymbol{\mu}_p$  to the source location  $\mathbf{r}$ .

To comprehensively evaluate the influence of the source location, both time- and frequency-domain features (as outlined in Table 1) are considered during the training process and mapped to the source location by  $G(\mathbf{X})$ . Among the time-domain features, the wave rate quantifies the fluctuations of  $\boldsymbol{\mu}_p$  over time, while the temporal mean and median values are measures of the central tendency of  $\boldsymbol{\mu}_p$  (Witte and Witte, 2017). The sample entropy measures the complexity of  $\boldsymbol{\mu}_p$ , with a lower sample entropy indicating greater self-similarity and less randomness in  $\boldsymbol{\mu}_p$ . The frequency-domain features are calculated based on 169 the fast Fourier transform (FFT). The FFT mean is the mean value of the Fourier coefficients for  $\mu_p$  and the FFT shape mean 170 describes the shape of the Fourier coefficients. These quantities are formulated as follows:

171 FFT mean 
$$=\frac{1}{N}\sum_{k=1}^{N}|\mu_{ik}|$$
, (8)

172 FFT shape mean 
$$= \frac{1}{\sum_{k=1}^{N} |\mu_{ik}|} \sum_{k=1}^{N} k |\mu_{ik}|$$
, (9)

where  $\mu_{ik}$  is the Fourier coefficient and *N* is the length of  $\mu_p$ . These features are calculated from the simulated observations at each site and provided to XGBoost as initial inputs.

Attribute	Feature	Description			
	Wave rate	Difference between 90-th and 10-th quantile of normalize observation series			
Time domain	Mean	Temporal mean value of observation series			
1 ime domain	Median	Temporal median value of observation series			
	Sample entropy	Complexity of observation series			
Frequency domain	FFT mean	Amplitude of power spectral density by FFT			
	FFT shape mean	Shape of power spectral density by FFT			

175 **Table 1.** Summary of the basic information on the observation series features.

# 176 **2.4 Release rate estimation**

Once the source location has been retrieved, many existing methods can be used to inversely estimate the release rate. In this study, we choose the recently developed PAMILT method (Fang et al., 2022) because it can correct the intrinsic model errors

179 of the release rate estimation and accurately retrieve the temporal variations in the release rates.

# 180 2.5 Numerical implementation

#### 181 **2.5.1 Pre-screening of potential source locations**

To reduce the computational cost and remove low-quality samples, the search range for the source location is pre-screened by evaluating the correlation coefficients between the observations and atmospheric dispersion model simulations, where the candidate source locations are randomly sampled in the considered calculation domain. Because the release rate is unknown, it is assumed to be 1 for all simulations. Source locations corresponding to the highest 40% of correlation coefficients are selected as the search range of the subsequent refined source location estimation using XGBoost.

#### 187 **2.5.2 Samples for training XGBoost**

The samples for training  $G(\mathbf{X})$  in Eq. (5) are generated based on the simulations described in Sect. 2.5.1, and the source locations of these simulations are within the search range determined according to Sect. 2.5.1. The simulation data are scaled by a constant factor (the ratio between the median value of all observations and that of the simulations using a unit release rate), which ensures that the simulations and observations have the same order of magnitude. Gaussian noise is added to the simulation data to simulate the statistical fluctuations of the measurements. The simulations between the first and last data points above the noise level are filtered by a temporal sliding-window average filter with a window size of 5, yielding samples for feature extraction as described in Sect. 2.3.

## 195 2.5.3 Automatic optimization of XGBoost model

The XGBoost model for source location estimation is automatically optimized with respect to the hyperparameters and feature selection. Specifically, the Bayesian optimization algorithm is used to optimize the hyperparameters by minimizing the following generalization coefficient (GC) defined under the five-fold cross-validation framework:

199 
$$GC = (1 - MCV)^2 + Var(R_k^2),$$
 (10)

200 
$$MCV = \frac{1}{5} \sum_{k} R_k^2$$
, (11)

where  $R_k^2$  is the goodness of fit and k is the index of each fold (k = 1, 2, ..., 5). MCV is the mean cross-validation score  $R_k^2$ among the five folds and  $Var(R_k^2)$  measures the variance of  $R_k^2$ . This function aims to balance the average and the variance of  $R_k^2$ , thus enhancing the generalization ability of the XGBoost model. In this study, the optimized hyperparameters include max\_depth (maximum depth of a decision tree), *learning\_rate* (step size shrinkage when updating), *n\_estimators* (number of decision trees), *min\_child\_weight* (minimum sum of sample weight of a child node), *subsample* (subsample ratio of the training samples), *colsample\_bytree* (subsample ratio of columns when constructing a decision tree), *reg\_lambda* (L2 regularization term on weights), and *gamma* (minimum loss reduction required to split the decision tree).

208 The initial input features (Table 1) are optimized through a feature selection step, where MCV serves as the selection 209 criterion. The selection is implemented by recursively removing the feature with the least importance, and reassessing the 210 MCV based on cross-validation (Akhtar et al., 2019). Initially, an XGBoost model is trained with all features, and the 211 importance of each feature is assessed based on its contribution to the model accuracy. The feature with the least importance 212 is removed and the XGBoost model is retrained using the remaining features. The feature importance and MCV are updated accordingly and another feature is removed. This iterative process continues until the optimal number of features is identified, 213 214 corresponding to the highest MCV achieved during the process. The overall flowchart of the proposed spatiotemporally 215 separated source reconstruction model is shown in Fig. S1.

## 216 **2.6 Validation case**

## 217 2.6.1 Field experiments

The proposed methodology was validated against the observations of the SCK-CEN <sup>41</sup>Ar and ETEX-1 field experiments. The 218 219 SCK-CEN <sup>41</sup>Ar experiment was carried out at the BR1 research reactor in Mol, Belgium, in October 2001 as a collaboration 220 between NKS and the Belgian Nuclear Research Centre (SCK-CEN) (Rojas-Palma et al., 2004). The major part of the 221 experiment was conducted on 3-4 October, during which time <sup>41</sup>Ar was emitted from a 60-m stack with a release rate of 222 approximately  $1.5 \times 10^{11}$  Bg h<sup>-1</sup>. Meteorological data such as wind speed and direction were provided by the on-site weather 223 mast. For most of the experimental period, the atmospheric stability was neutral, and the wind was blowing from the southwest. 224 As illustrated in Fig. 2(a), the source coordinates were (650 m, 210 m). The 60-s-average ground-level fluence rates were 225 continuously collected by an array of NaI (Tl) gamma detectors, with different observation sites used on the two days. To 226 convert the measured fluence rates to gamma dose rates (mSv/h), we used the  $^{41}$ Ar parameters of a previous study (Li et al., 2019a):  $E_{\nu} = 1.2938 \text{ MeV}, f^n(E_{\nu}) = 0.9921, \mu_a = 2.05 \times 10^{-3} \text{ m}^{-1}, \text{ and } \omega = 7.3516 \times 10^{-1} \text{ Sy Gy}^{-1}$ . More details of 227 228 these measurements can be found in (Rojas-Palma et al., 2004).

229 The ETEX-1 experiment took place at Monterfil in Brittany, France, on 23 October 1994 (Nodop et al., 1998). During 230 ETEX-1, a total of 340 kg of PMCH was released into the atmosphere on 23 October 1994 at 16:00:00 UTC and 24 October 231 1994 at 03:50:00 UTC. As illustrated in Fig. 2(b), the source coordinates were (-2.0083°E, 48.058°N). A total of 3104 available 232 observations (3-h-averaged concentrations) were collected at 168 ground sites. ETEX-1 has been widely used as a validation 233 scenario for reconstructing atmospheric radionuclide releases (Ulimoen and Klein, 2023; Tomas et al., 2021). The candidate 234 source locations are uniformly sampled from the green shaded zone. We choose two groups of observation sites: the first 235 comprises four sites (i.e. B05, D10, D16, F02) randomly selected from the sites within the sample zone (Group 1, with a total 236 of 92 available observations), and the second involves four sites (i.e. CR02, D15, DK08, S09) randomly selected from the sites beyond the sample zone boundaries (Group 2, with a total of 90 available observations). Compared with the SCK-CEN <sup>41</sup>Ar 237 238 experiment, the ETEX-1 observations exhibit temporal sparsity, lower temporal resolution, and increased complexity in 239 meteorological conditions.





241 Figure 2. Release location and observation sites of two field experiments. (a) SCK-CEN <sup>41</sup>Ar experiment. The map was created based on

the relative positions of the release source and observation sites (Drews et al., 2002). The coordinates of the sample border are (500 m, -200 m) and (1180 m, 580 m) on Oct. 3, and (450 m, 10 m) and (850 m, 450 m) on Oct. 4. This figure was plotted using MATLAB 2016b, rather than created by a map provider; (b) ETEX-1 experiment. The map was created based on the real longitudes and latitudes of the release source and observation sites (Nodop et al., 1998). The coordinates of the sample border are (10°W, 40°N) and (10°E, 60°N). This figure was plotted using the cartopy function of Python, rather than created by a map provider.

#### 247 **2.6.2** Simulation settings of atmospheric dispersion model

For the SCK-CEN <sup>41</sup>Ar field experiment, the Risø Mesoscale PUFF (RIMPUFF) model was employed to simulate the 248 249 dispersion of radionuclides and calculate the dose rates at each observation site (Thykier-Nielsen et al., 1999). The simulations 250 used on-site measured meteorological data and the modified Karlsruhe-Jülich diffusion coefficients. The calculation domain measured 1800 m×1800 m and the grid resolution was 10 m×10 m. The release height of  $^{41}$ Ar was assumed to be 60 m. Other 251 252 RIMPUFF calculation settings followed those of a previous study (Li et al., 2019a), and have been validated against the 253 observations. To establish the datasets for the XGBoost model, 2000 simulations and 1000 simulations with different source 254 locations were performed by RIMPUFF for the experiments on Oct. 3 and Oct. 4, respectively. Candidate source locations 255 were randomly sampled from the shaded zones in Fig. 2(a), which were determined according to the positions of the 256 observation sites and the upwind direction. Each simulation, along with its corresponding source location, forms one 257 sample. As described in Sect. 2.5.1, we calculated the correlation coefficient for each sample and preserved the 40% of samples 258 with the highest 40% of correlation coefficients (i.e. 800 samples for Oct. 3 and 400 samples for Oct. 4). The constant factors mentioned in Sect. 2.5.2 are  $1.53 \times 10^{11}$  and  $1.48 \times 10^{11}$  for Oct. 3 and Oct. 4, respectively. 259

260 For the ETEX-1 experiment, the FLEXible PARTicle (FLEXPART) model (version 10.4) was applied to simulate the 261 dispersion of PMCH (Pisso et al., 2019). The meteorological data were obtained from the United States National Centers of 262 Environmental Prediction Climate Forecast System Reanalysis, and have a spatial resolution of  $0.5^{\circ} \times 0.5^{\circ}$  and time resolution 263 of 6 h. To rapidly establish the relationship between the varying source locations and the observations, 182 backward 264 simulations were performed using FLEXPART with a time interval of 3 h, grid size of  $0.25^{\circ} \times 0.25^{\circ}$ , and 8 vertical levels (from 265 100-50000 m). Only the lowest model output layer was used for source reconstruction. Candidate source locations were 266 uniformly sampled from the shaded zone in Fig. 2(b), resulting in a total of 6561 source locations. As described in Sect. 2.5.1, 267 2624 candidate source locations were preserved following the pre-screening step. The constant factors mentioned in Sect. 2.5.2 268 are  $5.60 \times 10^{12}$  and  $2.86 \times 10^{13}$  for Group 1 and Group 2, respectively.

#### 269 2.7 Sensitivity study

270 (1) Search range

The search range is controlled by the pre-screening threshold, which is the top proportion of the correlation coefficients in the pre-screening step. Specifically, we use source locations corresponding to the highest 20%, 40%, 50%, 60%, 80%, and 100% of correlation coefficients to define the search ranges, with a lower proportion indicating a narrower and more focused search area. 275 (2) Size of the sliding window

Temporal filtering with different sliding-window sizes is applied to separate the source location estimation from the release rate estimation. In this study, the size of the sliding window ranges from 3–10. With these filtered data, the XGBoost model is trained using the same pattern for the source location estimation.

(3) Feature type

The XGBoost model is trained using only time-domain features and only frequency-domain features to investigate the influence of these features on the source location estimation. The performance of the time-feature-only and frequency-featureonly models is compared with the all-features result.

283 (4) Number and combination of observation sites

The XGBoost model is trained and applied to the source location estimation with different numbers of observation sites, namely a single site, two sites, and three sites. For the two- and three-site cases, the model is trained using different combinations of sites and the source location is estimated accordingly.

287 (5) Meteorological errors

Meteorological errors are important uncertainties in source reconstruction, especially the random errors in the wind field (Mekhaimr and Abdel Wahab, 2019). To simulate such uncertainties, a stochastic perturbation of  $\pm 10\%$  is introduced to the observed wind speeds in the x and y components, and a  $\pm 1$  stability class perturbation is applied to the stability parameters (e.g., from C to B or D). For both days, 50 meteorological groups are generated based on these random perturbations.

In all the sensitivity tests, the source location is estimated 50 times with randomly initialized hyperparameters to demonstrate the uncertainty range of the proposed method under different circumstances. The performance of source location estimation is compared quantitatively using the metrics specified in Sect. 2.8.3.

#### 295 2.8 Performance evaluation

## 296 2.8.1 Observation filtering

297 The feasibility of filtering is demonstrated using both the synthetic and real observations of the SCK-CEN <sup>41</sup>Ar experiment 298 and the real observations of the ETEX-1 experiment. The synthetic observations are generated by a simulation using a synthetic 299 temporally varying release profile with sharp increase, stable, and gradual decrease phases (as illustrated in Fig. S2), which is 300 typical for an atmospheric radionuclide release (Davoine and Bocquet, 2007). Because several temporal observations are 301 missing at some observation sites, we only choose observations sampled between 24 October 1994 09:00:00 UTC and 26 302 October 1994 03:00:00 UTC for the source location estimation. The simulations corresponding to the synthetic and real 303 observations should first be processed following the procedure described in Sect. 2.5.2. The filtering performance is evaluated 304 by comparing the simulation-observation differences before and after the filtering step. Several statistical metrics can be used 305 to quantify this difference, including the normalized mean square error (NMSE), Pearson's correlation coefficient (PCC), and 306 the fraction of predictions within a factor of 2 and 5 of the observations (FAC 2 and FAC 5, respectively) (Chang and Hanna, 307 2004).

# 308 2.8.2 Optimization of the XGBoost model

309 The hyperparameters are optimized with respect to the GC in Eq. (10) and the features are optimized with respect to the MCV

in Eq. (11). Larger values of MCV and smaller values of GC indicate better optimization performance. In addition, the importance of each feature to the XGBoost training is evaluated with the built-in *feature importance* measure of the XGBoost model.

#### 313 **2.8.3 Source reconstruction**

The relative errors in the source location ( $\delta_r$ ) and total release ( $\delta_o$ ) are calculated to evaluate the source reconstruction accuracy:

315 
$$\delta_{\mathbf{r}} = \frac{|\mathbf{r}_{true} - \mathbf{r}_{est}|}{L_D} \times 100\% , \qquad (12)$$

316 
$$\delta_Q = \frac{Q_{true} - Q_{est}}{Q_{true}} \times 100\% , \qquad (13)$$

where  $\mathbf{r}_{true}$  and  $Q_{true}$  refer to the real source location and total release of the field experiment and  $\mathbf{r}_{est}$  and  $Q_{est}$  are the estimated location and total release, respectively.  $L_D$  represents the range of the source domain, which is the distance between the lower and upper borders of the sampled zone (Fig. 2). The values of  $\mathbf{r}_{true}$ ,  $L_D$ , and  $Q_{true}$  are listed in Table 2. In addition to the total release, the reconstructed release rates are also compared with the true temporal release profile.

# 321 **Table 2.** Parameter settings of field experiments.

Experiment	Case	Parameters				
Experiment	Case	<b>r</b> <sub>true</sub>	L <sub>D</sub>	$Q_{true}$		
SOK OEN 41 A	Oct. 3	(650 m, 210 m)	1034.8 m	423.10 GBq		
SCK-CEN <sup>41</sup> Ar	Oct. 4	(650 m, 210 m)	565.7 m	1045.09 GBq		
	Group 1	(2.0083°W, 48.058°N)	2620.5 km	340 kg		
ETEX-1	Group 2	(2.0083°W, 48.058°N)	2620.5 km	340 kg		

## 322 **2.8.4 Comparison with the Bayesian method**

The proposed method is compared with the popular Bayesian method based on the SCK-CEN <sup>41</sup>Ar and ETEX-1 experiments, with the same search range used for locating the source in both methods (Fig. 2). The Bayesian method is augmented with an in-loop inversion of the release rate at each iteration of the Markov chain Monte Carlo sampling. The prior distribution of the Bayesian method is a uniform distribution and the likelihood is a log-Cauchy distribution. More detailed information is 327 presented in Supplementary Note S1.

## 328 **2.8.5 Uncertainty range**

The uncertainty ranges are calculated and compared for the correlation-based method, the Bayesian method, and the proposed method. For the correlation-based method, the uncertainty range is calculated using the source locations with the top-50 correlation coefficients. For the proposed method, the uncertainty range is calculated from 50 Monte Carlo runs with randomly initialized hyperparameters. The Bayesian method provides the uncertainty range directly through the posterior distribution. For consistency with the other two methods, the results with the top-50 frequencies are selected for the comparison.

#### 334 3. Results and Discussion

#### 335 **3.1 Filtering performance**

336 Figure S3 displays the original and filtered observations at different observation sites for both days. The results demonstrate 337 that the peak values have been smoothed out and the long-term trends are preserved to a large degree. Figure 3 compares the 338 filtering performance for both the synthetic and real observations, where the constant-release simulations are plotted against 339 the observations before and after filtering. For the synthetic observations, the filtered data are more concentrated along the 1:1 340 line for both days, and all filtered data fall within the 2-fold lines for Oct. 3. For the real observations, the dots before filtering 341 in Fig. 3 have a dispersed distribution for both Oct. 3 and Oct. 4, indicating limited correlations with the simulations. After filtering, the dots are more concentrated towards the 1:1 line for both the SCK-CEN <sup>41</sup>Ar and ETEX-1 experiments. These 342 343 phenomena indicate a noticeably increased agreement between the filtered observations and the constant-release simulations.





**Figure 3.** Scatter plots of the original (yellow squares) and filtered (green squares) observations versus the constant-release simulation results.

SCK-CEN <sup>41</sup>Ar experiment: (a) Oct. 3 (synthetic observations); (b) Oct. 4 (synthetic observations); (c) Oct. 3 (real observations); (d) Oct. 4
 (real observations); ETEX-1 experiment: (e) Group 1 (real observations); (f) Group 2 (real observations).

Table 3 quantitatively compares the results presented in Fig. 3. For each case, all metrics are greatly improved after filtering, confirming the better agreement between the filtered observations and the constant-release simulations. The improved agreement indicates that the filtering step significantly reduces the influence of temporal variations in release rates across the observations. The filtering performs better with the synthetic observations than with the real observations because the synthetic observations are free of measurement errors. The filtering process produces a better effect with the SCK-CEN <sup>41</sup>Ar experiment than with the ETEX-1 experiment, owing to the sparser observations in the ETEX-1 experiment (Fig. S3).

**Table 3.** Quantitative metrics for the filtering validation.

Experiment	Case		NMSE	PCC	FAC2	FAC5
		Before filtering	0.6970	0.5315	0.7647	0.8235
	Oct. 3 (synthetic observations)	After filtering	0.0239	0.9514	1	1
		Before filtering	0.9290	-0.0267	0.7292	0.7292
SCK-CEN <sup>41</sup> Ar	Oct. 4 (synthetic observations)	After filtering	0.0956	0.6179	0.9412	0.9779
SUK-CEN "Af		Before filtering	1.4437	0.3572	0.3824	0.5147
	Oct. 3 (real observations)	After filtering	0.2730	0.6976	0.7273	0.8864
	Oct. 4 (real observations)	Before filtering	1.9290	-0.2099	0.3073	0.4948
		After filtering	0.3668	0.2802	0.6552	0.9310
	Group 1 (real observations)	Before filtering	10.9936	0.3414	0.1000	0.2167
ETEX-1	Group I (real observations)	After filtering	6.6769	0.5145	0.2500	0.3667
ETEA-I	Group 2 (real observations)	Before filtering	5.8705	-0.2824	0.0667	0.1167
		After filtering	4.9799	-0.2695	0.1167	0.2500

# 355 **3.2 Optimization of XGBoost model**

### 356 3.2.1 Hyperparameters

Table S1 summarizes the optimal hyperparameters and corresponding GCs used for source location estimation in this study;
 Tables S2–S5 includes all the optimal hyperparameters used in the 50 runs of the SCK-CEN <sup>41</sup>Ar and ETEX-1 experiments.
 The optimal GCs of the SCK-CEN <sup>41</sup>Ar experiment are smaller than those of the ETEX-1 experiment, indicating better fitting
 performance. This is because the sparse observations of the ETEX-1 experiment (Fig. S3) are more sensitive to the added

361 Gaussian noise (see Sect. 2.5.2).

#### 362 **3.2.2 Feature selection**

363 Figure 4 compares the importance of the selected features at each site for the two experiments. The time-domain features are dominant for both days in the SCK-CEN <sup>41</sup>Ar experiment (Fig. 4a and 4b). For Oct. 3, Site B is the most important, possibly 364 because it is farthest away in the crosswind direction. For Oct. 4, the four sites provide redundant feature information, and 365 366 many features are removed. This is because the distribution of observation sites is almost parallel to the wind direction on this 367 day. According to Fig. S3(b), the measurements from Sites A and B have a high correlation, thus leading to the removal of features from Site A on Oct. 4. In summary, the feature selection process adapts XGBoost to different application scenarios. 368 369 Figure S4(a) and S4(b) shows the variations in MCV with the number of features for the x and y coordinates. The MCV first 370 increases with the number of features, and then decreases slightly after reaching the maximum. The optimal number of features 371 for Oct. 4 is noticeably smaller than for Oct. 3. In addition, the selected features for Oct. 3 involve all four sites, whereas those 372 for Oct. 4 involve three sites. The reduced features and site numbers indicate a high level of redundancy in the observations 373 acquired on Oct. 4. This is because the observation sites are parallel to the downwind direction and provide similar location 374 information in the crosswind direction. 375 For the ETEX-1 experiment, Fig. 4c and d shows that the features of Group1 and Group2 are largely preserved after the 376 feature selection process (only one feature is removed for each case), indicating less redundancy than that in the SCK-CEN

<sup>41</sup>Ar experiment. The time-domain features are dominant, but the frequency-domain features at some sites (e.g. D16 and S09)

- also play important roles. The MCVs of the ETEX-1 experiment have similar variation trends as those for the SCK-CEN <sup>41</sup>Ar
- experiment (Fig. S4c and S4d).





381



### 383 **3.3 Source reconstruction**

# 384 3.3.1 Source locations

Figure 5 compares the best-estimated source locations of the correlation-based method, the Bayesian method, and the proposed method with the ground truth. The pre-screening zone covers the true source location for both days, but the areas with the 387 highest correlation coefficients are still too large for the point source to be accurately located. The locations with the maximum 388 correlation exhibit errors of 270.19 m and 36.06 m for Oct. 3 and Oct. 4, respectively, indicating that the correlation-based 389 method may produce biased results in the case of non-constant releases. The Bayesian method estimates the location with 390 errors of 19.62 m and 52.81 m for Oct. 3 and Oct. 4, respectively. In comparison, the proposed method achieves the best 391 performance. The estimates without feature selection are only 10.65 m (Oct. 3) and 20.62 m (Oct. 4) away from the true 392 locations. Feature selection further reduces these errors to 6.19 m (Oct. 3, a relative error of 0.60%) and 4.52 m (Oct. 4, a 393 relative error of 0.80%), which are below the grid size (10 m×10 m) of the atmospheric dispersion simulation. The ability to 394 estimate the source location with accuracy surpassing the grid size can be attributed to the strong fitting capability of the 395 optimized XGBoost model (Chen and Guestrin, 2016; Grinsztajn et al., 2022). However, this capability, although inherent, is 396 not present across all optimized XGBoost models, as external factors such as observation noises and meteorological data 397 inaccuracies can also impact the accuracy of source location estimation.

398 For the ETEX-1 experiment, the pre-screening zone also covers the true source location for Group 1 and Group 2. The 399 source locations estimated by the correlation-based method are 411.85 km and 486.41 km away from the ground truth for 400 Group 1 and Group 2, respectively. The location error of the Bayesian method estimates is only 30.50 km for Group 1, but 401 increases to 520.77 km for Group 2, indicating the sensitivity of this method to the observations. In contrast, the proposed 402 method achieves much lower source location errors of 5.19 km for Group 1 (a relative error of 0.20%) and 17.65 km for Group 403 2 (a relative error of 0.70%). Group1 exhibits a lower source location error than Group 2, because the observation sites of 404 Group 1 are closer to the sampled source locations than those of Group 2 and better characterize the plume. Feature selection 405 did not remove many features (Fig. 4c and 4d), so the estimated source locations with and without feature selection basically 406 overlap for both groups.





408 Figure 5. Source location estimation results of SCK-CEN <sup>41</sup>Ar experiment: (a) Oct. 3; (b) Oct. 4; and ETEX-1 experiment: (c) Group 1; (d)

409 Group 2. A detailed enlargement of the region around  $(2.5^{\circ}W, 47.5^{\circ}N)$  to  $(1.5^{\circ}W, 48.5^{\circ}N)$  is shown in the bottom right corner in (c) and (d) 410 to highlight the source location estimation results of the proposed method. The yellow dots denote the maximum correlation points, which

410 are the results of the correlation-based method. The green and red stars represent the results based on XGBoost before and after feature 412 selection, respectively. The cyan diamonds represent the results based on the Bayesian method.

# 413 **3.3.2 Release rates**

414 Figure 6 displays the release rates estimated by the Bayesian and PAMILT methods based on the source location estimates in

Fig. 5. For the SCK-CEN <sup>41</sup>Ar experiment (Fig. 6a and 6b), the release rates provided by the Bayesian method present several sharp peaks, corresponding to overestimates of up to 269.03% (Oct. 3) and 532.35% (Oct. 4). Furthermore, the Bayesian

sharp peaks, corresponding to overestimates of up to 269.03% (Oct. 3) and 532.35% (Oct. 4). Furthermore, the Bayesian

417 estimates exhibit unrealistic oscillations in the stable release phase. In contrast, the PAMILT method successfully retrieves the 418 peak releases without oscillations for both days. Both the Bayesian and PAMILT estimates give delayed release start times,

419 but accurately estimate the end times, especially for Oct. 3. The PAMILT estimate underestimates the total release by 30.01%

420 and 45.95% for Oct. 3 and Oct. 4, respectively; these values decrease to about 23.83% and 30.60%, respectively, after feature

421 selection. The Bayesian method gives better total releases because of the overestimated peaks.

For the ETEX-1 experiment (Fig. 6c and 6d), the Bayesian estimates exhibit notable fluctuations, leading to underestimations of 58.11% for Group1 and 51.44% for Group 2. Furthermore, the temporal profile of the Bayesian estimates for Group 2 falls completely outside the true release window. In contrast, most releases using the PAMILT estimates are within the true release time window, especially for Group 2, despite the overestimations reaching 52.38% for Group 1 and 57.65% for Group 2, after the feature selection process. Compared with the SCK-CEN <sup>41</sup>Ar experiment, the increased deviation in the ETEX-1 experiment is caused by the sparsity of observations at the four sites (Fig. S3).



428

Figure 6. Release rate estimation results with different location estimates of SCK-CEN <sup>41</sup>Ar experiment: (a) Oct. 3; (b) Oct. 4; and ETEX 1 experiment: (c) Group 1; (d) Group 2. The release rates labelled XGBoost or XGBoost+feature selection are estimated using the PAMILT
 method.

# 432 **3.3.3 Uncertainty range**

Figure 7 compares the spatial distribution of 50 estimates produced by different methods. For the SCK-CEN <sup>41</sup>Ar experiment, 433 434 the estimates of the correlation-based method are highly dispersed for both days, leading to a very uniform distribution of the 435 x coordinate for Oct. 3 and two separate distributions of both the coordinates for Oct. 4. The Bayesian method produces a 436 multimodal distribution for both days, in which the estimates are more concentrated than those of the correlation-based method. 437 The corresponding full posteriori distributions in Fig. S5(a) and S5(b) better reveal the multimodal feature of the Bayesian 438 method, with several peaks of similar probabilities in the estimates of both coordinates on Oct. 3 and the y coordinate on Oct. 439 4. The multimodal feature indicates the difficulty of constraining the solution in simultaneous spatiotemporal reconstruction, 440 as reported in a previous study (Meutter and Hoffman, 2020). In comparison, the proposed method provides the most 441 concentrated source location estimates. The feature selection moves the centre of the distribution closer to the true location 442 and narrows the distribution of the estimates, especially for Oct. 4.

443 For the ETEX-1 experiment, the estimates of the correlation-based method are quite dispersed, whereas those of the

Bayesian method are more concentrated. The Bayesian estimates are close to the truth for Group 1, but deviate noticeably for Group 2. This phenomenon indicates that the Bayesian method is sensitive to the observations, especially when the observations are sparse. Figure S5(c) and S5(d) reveals that the Bayesian-estimated posterior distribution is multimodal for both ETEX-1 groups; this can be avoided by using additional observations (Fig. S5e). In contrast, the proposed method provides estimates that are concentrated around the truth for both Group 1 and Group 2, indicating its efficiency in the case of sparse observations. Due to the shorter distance between observation sites and the sampled source locations, the uncertainty range of source location for Group 1 is narrower than that for Group 2.





452 Figure 7. Spatial distribution of 50 source location estimates of SCK-CEN <sup>41</sup>Ar experiment: (a) Oct. 3; (b) Oct. 4; and ETEX-1 experiment:
 453 (c) Group 1; (d) Group 2. Each circle denotes an individual estimate as detailed in Sect. 2.8.5, with colour variations indicating the respective method employed. Histograms along the axes represent the frequency distribution of the estimates along the respective axis.

Figure 8 compares the uncertainty range and mean total release of the release rate estimations for the SCK-CEN <sup>41</sup>Ar experiment. For Oct. 3, the Bayesian estimates significantly overestimate the mean values and have a large uncertainty range,

whereas the mean PAMILT estimate is very close to the true release and the uncertainty range is smaller than that of the Bayesian method. For Oct. 4, the mean Bayesian estimate exhibits greater deviations than the mean PAMILT estimate. Feature selection improves the mean estimate and reduces the uncertainty range of PAMILT because it improves the source location estimation, thus reducing the deviation in the inverse model of the release rate. On Oct. 3 and Oct. 4, the PAMILT method underestimates the total release by 18.30% and 47.42%, respectively, whereas the Bayesian method gives overestimations of 153.61% and 42.29%, respectively.



463

464 Figure 8. Release rate estimates over 50 calculations of SCK-CEN <sup>41</sup>Ar experiment. (a) Oct. 3-Bayesian method; (b) Oct. 3-PAMILT method;
 465 (c) Oct. 4-Bayesian method; (d) Oct. 4-PAMILT method. The shadow represents the uncertainty range between the lower quartile and the upper quartile. The shadow of each figure is amplified by an enlarged subgraph. The legends in each figure provide the mean estimates for the total release.

Figure 9 compares the uncertainty ranges of the release rate estimates for the two ETEX-1 groups. For both groups, the Bayesian estimates exhibit noticeable underestimations (including the mean estimate) and small uncertainty ranges (Fig. 9a and 9c). The Bayesian estimates fall completely outside the true release window for Group 2 (Fig. 9c). The mean PAMILT estimates are more accurate than the mean Bayesian estimates, with most releases within the true release window (Fig. 9b and 9d). However, the PAMILT estimates have a large uncertainty range for the ETEX-I experiment than for the SCK-CEN <sup>41</sup>Ar experiment, implying that the source–receptor matrices of the ETEX-1 experiment are more sensitive to errors in source location than those of the SCK-CEN <sup>41</sup>Ar experiment. This greater sensitivity originates from the complex meteorology in the

- 475 ETEX-1 experiment. As for the mean total releases, the Bayesian method produces underestimations of 70.93% for Group1
- 476 and 74.15% for Group 2. In comparison, the proposed method gives deviations of only 0.71% for Group 1 and 0.09% for Group
- 477 2, after feature selection.

478



479 Figure 9. Release rate estimates over 50 calculations of ETEX-1 experiment. (a) Group 1-Bayesian method; (b) Group 1-PAMILT method;
 480 (c) Group 2-Bayesian method; (d) Group 2-PAMILT method.

481 Table 4 lists the mean and standard deviation of the relative errors for the 50 estimates given by different methods. The 482 correlation-based method produces the largest mean relative error and standard deviation for source location estimation, except for Group 2 of ETEX-I. For the SCK-CEN <sup>41</sup>Ar experiment, the proposed method gives the smallest mean error, about half of 483 484 that of the Bayesian method. Its standard deviation is around one-quarter of that of the Bayesian method for Oct. 3, but is 485 slightly larger for Oct. 4. For the total release, the PAMILT method gives a better standard deviation of the relative error for 486 both days and a better mean relative error for Oct. 3, whereas the Bayesian method produces a better mean relative error for 487 Oct. 4. Feature selection reduces the mean relative error, except for the total release for Oct. 3, and slightly increases the 488 standard deviation of the source location and total release results for Oct. 3. The mean relative error of the total release averaged 489 on the two days is 65.09% lower than that of the Bayesian method.

For the ETEX-1 experiment, the Bayesian method exhibits case-sensitive performances with respect to the mean relative error of source location estimation, whereas the proposed method gives the most accurate source locations with small uncertainties for both groups. As for the total release, the proposed method gives smaller mean relative errors than the Bayesian methods, but the Bayesian method has a smaller standard deviation. Feature selection significantly reduces the mean relative 494 error for the two groups. The mean relative error of the total release averaged over the two groups is 72.14% lower than that

495 of the Bayesian method.

496 **Table 4.** Relative errors of source reconstruction.  $\delta_r$  represents the relative error of source location, which is positive and  $\delta_Q$  denotes the relative error of total release, where a positive value indicates overestimation and a negative value denotes underestimation.

Experiment	Case		istical	Correlation-	Bayesian	The proposed method	
			neters ve error)	based method	method	XGBoost	XGBoost+ feature selection
	Oct. 3	6	Mean	14.10%	11.88%	5.18%	4.68%
		$\delta_{\mathbf{r}}$	Std	11.37%	7.53%	1.79%	2.05%
		$\delta_Q$	Mean	-	153.61%	-16.93%	-18.30%
		$O_Q$	Std	-	189.76%	9.45%	8.01%
SCK-CEN <sup>41</sup> Ar	Oct. 4	2	Mean	14.30%	12.83%	6.83%	4.71%
		$\delta_{\mathbf{r}}$	Std	9.60%	1.68%	1.76%	1.53%
		0	Mean	-	42.29%	-54.12%	-47.42%
		$\delta_Q$	Std	-	15.05%	6.47%	5.85%
	Group 1	ç	Mean	16.95%	3.22%	2.32%	2.42%
		$\delta_{\mathbf{r}}$	Std	7.46%	2.75%	1.43%	1.43%
		0	Mean	-	-70.93%	18.12%	-0.71%
ETEX-I		$\delta_Q$	Std	-	17.87%	99.85%	102.01%
		2	Mean	21.9%	23.97%	5.21%	4.97%
	Group 2	$\delta_{\mathbf{r}}$	Std	5.05%	1.97%	2.42%	2.35%
		8	Mean	-	-74.15%	16.67%	0.09%
		$\delta_Q$	Std	-	11.68%	93.50%	109.56%

## 498 **3.4 Sensitivity analysis results**

# 499 **3.4.1 Sensitivity to the search range**

Figure 10 displays the source location errors obtained using different pre-screening thresholds to determine the search range. The error is smaller with a lower threshold, implying that a small search range helps reduce the mean and median errors. As the threshold increases, the mean and median errors, as well as the error range, show an overall tendency to increase, but not in a strictly monotonic way. The mean/median error is less than 12% for Oct. 3 and less than 22% for Oct. 4, indicating robust performance in these tests. Feature selection reduces the mean/median, range, and the lower bound of the errors in most tests, demonstrating its efficiency.



506

507 **Figure 10.** Distribution of relative error (%) over 50 runs with different search ranges. The blue and red solid lines denote average relative 508 error (%) and median relative error (%), respectively. The upper and lower boundaries represent the upper and lower quartiles of relative 509 error (%), respectively. The fences are 1.5 times the inter-quartile ranges of the upper/lower quartiles. The red circles denote data that are 510 not included between the fences. (a) Oct. 3; (b) Oct. 4.

## 511 **3.4.2** Sensitivity to the size of the sliding window

512 Figure 11 shows the source location errors obtained with different sliding-window sizes. The mean/median error is less than 513 8% for Oct. 3 and less than 11% for Oct. 4, both of which are smaller than for the various search ranges. This indicates that 514 the proposed method is more robust to this parameter than to the search range. For both days, the lowest mean/median and 515 error range occur with relatively large window sizes, i.e. window size of 9 for Oct. 3 and window size of 10 for Oct. 4. This is 516 because a large window size increases the strength of the filtering and removes the temporal variations in the release rates 517 more completely. However, a large window size leads to increased computational cost. Because the errors vary in a limited 518 range, a medium window size provides a better balance between accuracy and computational cost. Feature selection improves 519 the results for medium and small window sizes, but may have less effect with large window sizes. This tendency implies that 520 it is more appropriate to apply feature selection with medium window sizes than with large window sizes, as in this study.





#### 523 **3.4.3 Sensitivity to the feature type**

521

Figure 12 compares the results obtained with different feature types. For Oct. 3, the source location errors are quite low when using only the time-domain features for the reconstruction; indeed, the errors are only slightly larger than when using all the features. In contrast, the results obtained using only the frequency-domain features exhibit larger errors, indicating that the time-domain features make a greater contribution to the results for Oct. 3. For Oct. 4, the mean source location errors are similar when using either the time- or frequency-domain features, but the error range is higher when the frequency-domain features are used. In addition, the errors of both single-domain-feature results are higher than those of the all-feature results, indicating that both feature types should be included to ensure accurate and robust source location estimation.



#### 532 **Figure 12.** Sensitivity to the feature type. (a) Oct. 3; (b) Oct. 4.

531

# 533 **3.4.4** Sensitivity to the number and combination of observation sites

534 Figure 13 compares the results obtained with different numbers and combinations of observation sites. The results indicate 535 that the source location error may be more sensitive to the position of the observation site than to the number of sites included. 536 The error level of all-site estimations is relatively low for both days, indicating that increasing the number of observation sites 537 better constrains the solution and help improve the robustness of the model. However, the lowest error levels are achieved by 538 a subset of sites, i.e. Site ABD on Oct. 3 and Site BD on Oct. 4. This is possibly because including all observation sites may 539 cause overfitting and reduce the prediction accuracy. This overfitting can be alleviated by using only representative sites at 540 appropriate position, which capture the environmental variability and provide clear information for locating the source. For 541 Oct.3, multi-site estimations with Site B always produce low error levels, and single-site estimation using Site B also achieves 542 high accuracy. For Oct.4, multi-site estimations with Site BD always achieve relatively low error levels. These results 543 demonstrate the importance of using representative sites for source location estimation. The representative sites (Site B for 544 Oct. 3 and Site BD for Oct. 4) are consistent with the importance calculated in the feature selection step (Fig. 4), preliminarily 545 indicating the potential for feature selection to identify representative sites. In addition, feature selection reduces the mean 546 error level in most cases.



547

548 Figure 13. Sensitivity to the number and combination of observation sites. (a) Oct. 3; (b) Oct. 4.

549

# 3.4.5 Sensitivity to the meteorological errors

550 Figure 14 illustrates the distribution of mean relative source location errors (averaged across 50 groups of hyperparameters) 551 retrieved with 50 perturbed meteorological inputs. For Oct. 3, the estimates generally present a low error level (generally below 552 10%), and the 50th percentile error level is lower than the error of the unperturbed results (4.68%). In comparison, for Oct. 4, 553 most perturbed results exhibit larger errors (primarily 10%-20%) than the unperturbed result (4.71%), indicating that models 554 for Oct. 4 are more sensitive to the meteorological errors. This sensitivity difference results from the layout of the observation 555 sites (Fig. 2a). The sites on Oct. 3 were almost perpendicular to the prevailing wind direction, capturing the plume under a 556 large range of wind directions. In contrast, the sites on Oct. 4 were basically parallel to the wind direction, capturing the plume 557 only for a very limited range of wind directions. This result indicates the importance of site layout for robust reconstruction in 558 the presence of meteorological errors. Feature selection slightly changes the mean relative error distribution and its percentiles 559 for both days, indicating that meteorological errors may alter the importance of each feature and reduce the effectiveness of 560 feature selection. In addition to meteorological errors, dispersion errors such as wet deposition parameterization (Zhuang et 561 al., 2023) may influence the result, but these errors are not dominant in the two field experiments. The handling of such 562 dispersion errors will be investigated in future work.



**Figure 14.** Sensitivity to the meteorological errors. The violin plots illustrate the kernel density estimation of errors under different meteorological groups for XGBoost models before and after feature selection. The vertical black lines inside the violins depict the interquartile range, capturing the 25th, 50th (red dots), and 75th percentiles of mean relative errors. The blue dots denote the mean relative source location errors for models without meteorological perturbation, as listed in Table 4.

#### 568 4. Conclusions

563

569 In this study, we relaxed the unrealistic constant-release assumption of source reconstruction. Instead, we took advantage of 570 the fact that most atmospheric radionuclide releases have a spatially fixed source, and thus the release rate mainly influences 571 the peak values in the temporal observations. Based on this, a more general spatiotemporally separated source reconstruction 572 method was developed to estimate non-constant releases. The separation process was achieved by applying a temporal sliding-573 window average filter to the observations. This filter reduces the influence of temporal variations in the release rates on the 574 observations, so that the relative spatiotemporal distribution of the filtered observations is dominated by the source location 575 and known meteorology. A response feature vector was extracted to quantify the long-term temporal response trends at each 576 observation site, involving tailored indicators of both the time and frequency domains. The XGBoost algorithm was used to 577 train a machine learning model that links the source location to the feature vector, enabling independent source location 578 estimation without knowing the release rate. With the retrieved source location, the detailed temporal variations of the release 579 rate were determined using the PAMILT algorithm. Validation was performed against the two-day SCK-CEN <sup>41</sup>Ar field 580 experimental data and two groups of ETEX-1 data. The results demonstrate that the proposed method successfully removes

the influence of temporal variations in release rates across observations and accurately reconstructs both the spatial location and temporal variations of the source.

For the local-scale SCK-CEN <sup>41</sup>Ar experiment, source location was reconstructed with lowest errors of only 0.60% (Oct. 3) 583 584 and 0.80% (Oct. 4), significantly lower than for the correlation-based method and Bayesian method. In terms of the release 585 rate, the PAMILT method reconstructed the temporal variations, peak, and total release with high accuracy, thus avoiding the 586 unrealistic oscillations given by the Bayesian estimate. The proposed method produced smaller uncertainty ranges than the 587 Bayesian method and avoided the multimodal distribution of the Bayesian method. The feature selection process removed the 588 redundant features and reduced the reconstruction errors. For the continental-scale ETEX-1 experiment, the lowest relative 589 source location errors were 0.20% and 0.70% for Group 1 and Group 2, respectively, which were again lower than for the 590 correlation-based and Bayesian methods. The proposed method provides highly accurate mean estimates of the release rate for 591 both groups, although with a large uncertainty range.

Sensitivity analyses on the SCK-CEN <sup>41</sup>Ar experiment revealed that the proposed method exhibits stable source location estimation performance with different parameters and remains effective with only a single observation site, as long as the selected site is appropriately located. Moreover, the proposed method shows robust source location estimation in the presence of meteorological errors, with mean source location error levels below 10%, on condition that the site layout is appropriate.

These results demonstrate that spatiotemporally separated source reconstruction is feasible and achieves satisfactory accuracy in multi-scale release scenarios, thereby providing a promising framework for reconstructing atmospheric radionuclide releases. However, the proposed method does not consider the influence of temporal variations in the release rate on the plume shape. Our future efforts will be directed towards integrating spatial features to further enhance the method.

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601 *Code and data availability.* The code and data for the proposed method can be downloaded from Zenodo 602 (https://doi.org/10.5281/zenodo.10200141). More recent versions of the code and data will be published on GitHub.com 603 (https://github.com/rocket1ab/Source-reconstruction-of-non-constant-atmospheric-radionuclide-releases, last access: 23 604 November 2023). The implementation is provided in Python, and the instruction file is also available in the provided link.

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*Author contributions.* YX conducted the source reconstruction tests and wrote the manuscript draft; SF provided guidance on
 the RIMPUFF modeling and suggestions on source reconstruction tests; XD and SZ reviewed and edited the manuscript.

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609 *Competing interests.* The authors have declared that they have no conflict of interest.

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