



1 **To quantify the impact of SST feedback periodicity on**
2 **atmospheric intraseasonal variability in the tropical regions**

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8 **Abstract**

9 This study couples a high-resolution 1-D TKE ocean model (the SIT model) with
10 the Community Atmosphere Model 5.3 (CAM5.3; hereafter CAM5–SIT)
11 configuration, to highlight significant experiments that investigate the influence of
12 different periods of sea surface temperature (SST) feedback, such as 30 minutes, 1, 3,
13 6, 12, 18, and 30 days, on the Madden-Julian Oscillation (MJO). It substantially
14 breaks through the limitations of flux coupler through air–sea coupling. The aim is to
15 assess the scientific reproducibility and consistency of the findings across different
16 SST feedback cycles in the field of modeling science. Comparing the results to the
17 fifth generation ECMWF reanalysis (ERA5), the high-frequency experiments (C–
18 CTL, C–1 day, and C–3 days) and low-frequency experiments (C–6 days, C–12 days,
19 and C–18 days) exhibit higher fidelity in capturing various aspects of MJO, except for
20 the C–30 days experiment. These aspects in characterizing the basic features of the
21 MJO such as encompass intraseasonal periodicity, eastward propagation, coherence in
22 the MJO band, tilting vertical structure, the lead–lag relationship between MJO-
23 related atmosphere and SST variation, phase 2 column-integrated moisture static
24 energy (MSE) tendency, and the projection of all MSE terms onto the MSE tendency
25 of ERA5 across the Maritime Continent (MC). The MJO simulation performance of
26 this study can be assessed in two ways. Firstly, the high-frequency experiments
27 generally capture MJO characteristics, albeit with slightly lower results compared to
28 ERA5 and NOAA data. Secondly, the low-frequency experiments show robust MJO
29 simulations, which can be attributed to the accumulation of energy (temperature) in
30 the upper ocean. This leads to the accumulation of shortwave and longwave
31 radiations, as well as surface heat fluxes from the atmosphere.



32 1. Introduction

33 The Madden–Julian Oscillation (MJO) is a large-scale tropical circulation that
34 propagates eastward from the tropical Indian Ocean (IO) to the western Pacific (WP)
35 with a periodicity of 30–80 days (Madden and Julian, 1972). In the Indo-Pacific
36 region, there is increasing evidence that MJO processes are involved in intraseasonal
37 variability of sea surface temperature (SST) (Chang et al., 2019; DeMott et al., 2014,
38 2015; Jiang et al., 2015, 2020; Krishnamurti et al., 1998; Li et al., 2014; Li et al.,
39 2020a; Newman et al., 2009; Pei et al., 2018; Stan, 2018; Tseng et al., 2015). These
40 studies confirm that including air–sea interactions significantly improves the
41 simulation of the MJO.

42 The ocean's response to intraseasonal atmospheric variability, such as surface
43 shortwave radiation, turbulent heat fluxes controlled by wind speed, and ocean
44 processes driven by wind stress, plays a crucial role in causing intraseasonal SST
45 variability related to the MJO (Li et al., 2014). Incorporating two-way coupling
46 between the ocean and atmosphere is expected to be valuable for simulating and
47 predicting intraseasonal variability (e.g., DeMott et al., 2014; Lan et al., 2022; Stan,
48 2018; Tseng et al., 2015, 2020). However, the influence of sub-seasonal (e.g., beyond
49 a phase) air–sea coupling on convection and related oceanic features is still not fully
50 understood.

51 In this study, we aim to investigate the specific effects of oceanic feedback
52 frequency (FF) in sub-seasonal periodicity through air–sea coupling on the eastward
53 propagation of the MJO as simulated by the Community Atmosphere Model 5.3
54 (CAM5.3) coupled with the one-column ocean model Snow–Ice–Thermocline (SIT),
55 referred to as CAM5–SIT (Lan et al., 2022). The tropical air–sea interaction,
56 influenced by the upper ocean, plays a crucial role in determining MJO characteristics



57 due to the high heat capacity of the upper ocean, which acts as a significant source of
58 heat energy for atmospheric variability (Liang and Du, 2022). The SIT model,
59 consisting of 41 vertical layers, enables the simulation of SST and upper-ocean
60 temperature variations with high vertical resolution. The vertical resolution is set to
61 12 layers within the first 10.5 m and 6 layers between 10.5 m and 107.8 m. The fine
62 resolution simulates the upper ocean warm layer, which includes a layer at 0.05 m
63 that replicates the cool skin of the ocean surface (Tseng et al., 2015, 2020; Lan et al.,
64 2010, 2022). Previous studies have emphasized the importance of vertical resolution
65 in accurately simulating the MJO, with Tseng et al. (2015) demonstrating the
66 necessity of a 1 m vertical resolution when coupling SIT with the European
67 Centre/Hamburg Model version 5 (ECHAM5), referred to as ECHAM5–SIT in the
68 tropics. Furthermore, Shinoda et al. (2021) indicated the positive impact of high
69 vertical resolution near the ocean surface on MJO prediction abilities based on
70 simulations of the National Oceanic and Atmosphere Administration (NOAA)
71 Climate Forecast System. Ge et al. (2017) highlighted the presence of a high vertical
72 temperature gradient within the upper 10 m of the MJO event, particularly during dry
73 and clear periods, underscoring the need for a resolution of approximately 1 m to
74 accurately capture intraseasonal SST variability.

75 Several recent studies have made significant progress in understanding the
76 impact of air–sea coupling on the MJO, particularly at sub-daily scales (e.g., DeMott
77 et al., 2015; Kim et al., 2018; Seo et al., 2014; Voltaire et al., 2022; Zhao and
78 Nasuno, 2020). However, there is relatively limited discussion on air–sea coupling at
79 the sub-seasonal scale. Several studies have undertaken investigations into the impact
80 of intraseasonal SST on the MJO by conducting various model experiments,
81 encompassing both coupled and uncoupled models. (e.g., DeMott et al., 2014; Gao et
82 al., 2020b; Klingaman, and Demott, 2020; Pariyar et al., 2023; Stan, 2018). Stan



83 (2018) found that in the air–sea coupling run, the peak in surface fluxes (latent heat
84 and sensible heat) is stronger and occurs earlier compared to the uncoupling run with
85 sub-5-day SST variability. Additionally, the absence of 1–5-day variability in SST
86 promotes the amplification of westward power associated with Rossby waves. Based
87 on these modeling studies, it is concluded that the atmospheric response to sub-
88 seasonal SST variances can be determined. Replay simulations using time-varying
89 coupled global climate model (CGCM) SSTs as atmospheric general circulation
90 model (AGCM) boundary conditions showed a reduced dynamic range of SST
91 anomalies, leading to weakened air–sea heat fluxes and eastward propagation
92 (DeMott et al., 2014; Gao et al., 2020b; Klingaman, and Demott, 2020; Pariyar et al.,
93 2023). Stan (2018) also demonstrated that eliminating 1–5-day variability of surface
94 boundary forcing reduces the intraseasonal variability of the tropics during boreal
95 winter in the case of CGCM SSTs as AGCM boundary conditions. However, the
96 effect of sub-seasonal SST variances on the MJO is still not fully understood in both
97 coupled and uncoupled experiments.

98 As demonstrated by Fu et al. (2017), underestimation (overestimation) of the
99 air–sea coupling's impact on MJO simulations occurs when there is weakness (strong)
100 in the intraseasonal SST anomaly. Understanding the manifestation of heat fluxes in
101 the significant intraseasonal oscillation (ISO) is crucial for the development of
102 intraseasonal SST variability (Liang et al., 2018). In aquaplanet simulations
103 conducted by Arnold et al. (2013), where equatorial SST were set at approximately
104 26°, 29°, 32°, and 35° C, it was observed that the intraseasonal variance
105 (wavenumbers 1–3, periods 20–100 days) exhibited a significant and consistent
106 increase with increasing SST. Furthermore, Savarin and Chen (2022) have found that
107 improved air–sea heat fluxes result in systematic enhancements in precipitation,
108 winds, SST, and the mixed layer in the ocean. Hence, the combination of higher



109 tropical SST and enhanced SST variances collectively contribute to an intensified
110 eastward propagation of the MJO.

111 Improvements in the MJO in coupled simulations can be attributed to several
112 factors. Firstly, enhanced low-level convergence and convective instability to the east
113 of convection, as well as enhanced latent heat fluxes and SST cooling to the west of
114 convection, contribute to the improved eastward propagation and regulation of MJO
115 periodicity (DeMott et al., 2014). SST gradients have been found to induce patterns of
116 mass convergence and divergence within the marine boundary layer (MBL), initiating
117 atmospheric convection (de Szoeke and Maloney, 2020; Lambaerts et al., 2020). The
118 basic state SST or basic state moist static energy (MSE) plays a crucial role in MJO
119 instability (Wang et al., 2016). Moisture convergence in the MBL accumulates MSE
120 and increases convective instability to the east of the main convection, facilitating the
121 eastward propagation of the MJO (Hsu and Li, 2012; Wang et al., 2016). The
122 increased low-level convergence is associated with shallow convection induced by
123 SST-induced convective instability (DeMott et al., 2014). An analysis of MSE
124 convergence by de Szoeke and Maloney (2020) demonstrates that intraseasonal SST
125 fluctuations drive the overall MSE tendency, contributing to MJO generation and
126 propagation. Arnold et al. (2013) demonstrate that the vertical advection projection
127 exhibits a positive trend. Specifically, they find that it acts as a strong damping
128 mechanism at low SST, whereas it transitions into an energy source at high SST.
129 Based on this observation, we can infer that alterations in vertical MSE advection are
130 probably accountable for the amplified variability of the MJO in relation to SST.

131 The structure of this paper is organized as follows. Section 2 introduces the
132 models, data, methodologies, and experiments employed in this study. The
133 performance of the CAM5–SIT models in simulating the MJO is discussed in Section
134 3, while Section 4 focuses on the impact of different sub-seasonal periodicity



135 configurations on MJO simulations through detailed MJO diagnostics. Finally,
136 Section 5 presents the conclusions drawn from this study.

137

138 **2. Data, model experiments, and methodology**

139 **2.1 Observational, atmospheric, and oceanic data**

140 An observational data set used in this study includes precipitation from the
141 Global Precipitation Climatology Project (GPCP, 1° resolution, 1997–2010; Adler et
142 al., 2003), outgoing longwave radiation (OLR, 1° resolution, 1997–2010; Liebmann,
143 1996), and daily SST (optimum interpolated SST, OISST, 0.25° resolution, 1989–
144 2010; Banzon et al., 2014) from the National Oceanic and Atmosphere
145 Administration.

146 The atmospheric variables used in this study were obtained from the fifth-
147 generation reanalysis of the European Centre for Medium-Range Weather Forecasts
148 (ECMWF) known as the fifth generation ECMWF reanalysis (ERA5), with a
149 resolution of 0.25° for the period of 1989–2020 (Hersbach and Dee, 2016). Various
150 variables from ERA5 were considered, including zonal wind, meridional wind,
151 vertical velocity, temperature, specific humidity, sea level pressure, geopotential
152 height, latent heat, sensible heat, and shortwave and longwave radiation. For the
153 initial conditions of a SIT model, SST data was obtained from the Hadley Centre Sea
154 Ice and Sea Surface Temperature dataset version 1 (HadISST1), with a resolution of
155 1° for the period of 1982–2001 (Rayner et al., 2003). The ocean subsurface data,
156 including climatological ocean temperature, salinity, and currents in 40 layers, were
157 retrieved from the National Centers for Environmental Prediction (NCEP) Global
158 Ocean Data Assimilation System (GODAS) with a resolution of 0.5° for the period of
159 1980–2012 (Behringer and Xue, 2004). These data were used for nudging in the SIT
160 model.



161

162 2.2 Experimental design

163 In this study, we investigate the role of oceanic FF in sub-seasonal periodicity
164 using the coupled model CAM5–SIT and the uncoupled AGCM (A–CTL). Previous
165 studies (Lan et al., 2022; Tseng et al., 2022) have provided a detailed description of
166 the every timestep coupling CAM5–SIT model and its performance in simulating
167 atmospheric variability and the MJO. This study involved a series of 30-year
168 numerical experiments (as shown in Table 1). We overcame the limitations of the
169 National Center for Atmospheric Research (NCAR) Climate System Model (CSM)
170 Flux Coupler (CPL) by implementing similarly asymmetric exchange frequencies
171 between the atmosphere and the ocean. The SST value is fixed at each timestep within
172 the experimental periodicity through a straightforward approach to create various
173 intraseasonal SST (e.g., 30 minutes, 1, 3, 6, 12, 18, and 30 days) feedback
174 atmospheric experiments. It is important to note that every timestep involves
175 bidirectional interaction in the CPL.

176 Two sets of experiments were conducted, each representing a different SST
177 feedback frequency:

178 (1) The high-frequency SST feedback set: This set includes the control
179 experiment (C–CTL) with SST feedback at every timestep (FF as 48/day), as
180 well as experiments with SST feedback once a day (C–1day: FF as 1/day)
181 and every 3 days (C–3days: FF as 1/3days), respectively.

182 (2) The low-frequency SST feedback set: This set includes experiments with
183 SST feedback returning to the atmosphere every 6 days (C–6days: FF as
184 1/6days), 12 days (C–12days: FF as 1/12days), 18 days (C–18days: FF as
185 1/18days), and 30 days (C–30days: FF as 1/30days), respectively.

186 In all experiments, there is a common configuration: CAM5 forces SIT at each



187 timestep, SIT has the same vertical resolution, and coupling is implemented between
188 30° N to 30° S in the entire tropics. The only difference lies in the frequency of SIT's
189 SST feedback into the atmosphere. This choice is driven by two factors related to
190 tropical coupling.

191 Firstly, the MJO predominantly occurs in tropical regions (Jiang et al., 2020;
192 Kang et al., 2020; Shinoda et al., 2021), hence coupling was specifically implemented
193 between 30° N to 30° S. This focuses the coupling on the region where the MJO is
194 most active.

195 Secondly, coupling a one-dimensional ocean model without surface flux
196 correction to the extratropics would neglect the influence of strong ocean currents,
197 such as the Kuroshio and Gulf Streams, leading to significant biases. Therefore,
198 coupling is limited to the tropical region to avoid these biases and ensure a more
199 realistic representation of the air–sea interactions relevant to the MJO.

200 Forcing of the coupled and uncoupled models' initial conditions was done using
201 a climatological monthly-mean HadSST1 dataset. The monthly Global Ocean Data
202 Assimilation System (GODAS) dataset was linearly interpolated to obtain daily
203 values of oceanic temperature, salinity, u-current, and v-current for nudging purposes.
204 The ocean was weakly nudged (using a 30-day time scale) between depths of 10.5 m
205 and 107.8 m, and strongly nudged (using a 1-day time scale) below 107.8 m, based on
206 the climatological ocean temperature data from NCEP GODAS. No nudging was
207 applied in the upper-most 10.5 meters.

208 During the simulation, the SIT recalculated the SST within the tropical air–sea
209 coupling region, which spans from 30° S to 30° N. Outside this coupling region, the
210 prescribed annual cycle of HadSST1 was used. The ocean bathymetry for the SIT was
211 derived from the NOAA ETOPO1 data (Amante and Eakins, 2009). To ensure
212 consistency and comparability, all observational, atmospheric, oceanic, and reanalysis



213 data were interpolated into a horizontal resolution of $1.9^\circ \times 2.5^\circ$ for model
214 initialization, nudging, and comparison of experimental simulations.

215

216 **2.3 Methodology**

217 The analysis focused primarily on the boreal winter period (November–April),
218 which exhibits the most pronounced eastward propagation of the MJO. To identify
219 intraseasonal variability, the CLIVAR MJO Working Group diagnostics package
220 (CLIVAR, 2009) and a 20–100-day filter (Wang et al., 2014) were employed. MJO
221 phases were defined following the index (namely, RMM1 and RMM2) proposed by
222 Wheeler and Hendon (2004), which utilizes the first two principal components of
223 combined near-equatorial OLR and zonal winds at 850 and 200 hPa. The band-pass
224 filtered data were employed to calculate the index and define the MJO phases.

225 Furthermore, an analysis of column-integrated MSE budgets was conducted to
226 investigate the association between the tropical convection and large-scale
227 circulations. The column-integrated MSE budget equation (e.g., Sobel et al., 2014) is
228 approximately given by

$$229 \left\langle \frac{\partial h}{\partial t} \right\rangle' = - \left\langle u \frac{\partial h}{\partial x} \right\rangle' - \left\langle v \frac{\partial h}{\partial y} \right\rangle' - \left\langle w \frac{\partial h}{\partial p} \right\rangle' + \langle LW \rangle' + \langle SW \rangle' + \langle SH \rangle' + \langle LH \rangle' \quad (1)$$

230 where h denotes the moist static energy;

$$231 h = c_p T + gz + L_v q \quad (2)$$

232 where T is temperature (K); q is specific humidity (Kg Kg^{-1}); c_p is dry air heat
233 capacity at constant pressure ($1004 \text{ J K}^{-1} \text{ kg}^{-1}$); L_v is latent heat of condensation
234 (taken constant at $2.5 \times 10^6 \text{ J kg}^{-1}$); u and v are horizontal and meridional velocities
235 (m s^{-1}), respectively; w is the vertical pressure velocity (Pa s^{-1}); LW and SW are the
236 longwave and shortwave radiation fluxes (W m^{-2}), respectively; and LH and SH are
237 the latent and sensible surface heat fluxes (W m^{-2}), respectively. The angle brackets



238 $\langle \langle * \rangle \rangle$ represent mass-weighted vertical integration from 1000 to 100 hPa; and the
239 intraseasonal anomalies are represented as $\langle * \rangle'$, which were isolated using a 20–100-
240 day bandpass filter (Wang et al., 2014).

241

242 **3. Results**

243 **3.1 The basic state SST variability**

244 The variability of SSTs plays a crucial role in the dynamics of the MJO. In the
245 absence of interseasonal SST variability, as observed in the uncoupled A–CTL
246 simulations, the eastward propagation of the MJO is disrupted, resulting in weakened
247 or fragmented MJO activity. Studies based on observations from TOGA COARE and
248 DYNAMO have revealed that MJO events exhibit a stronger ocean temperature
249 response compared to average conditions (de Szoeke et al., 2014). Interseasonal SST
250 variability in the tropics, resulting from air–sea coupling, significantly impacts the
251 behavior of the MJO behavior and atmospheric circulation. Warmer SSTs to the east of
252 convection enhance the release of latent heat, triggering atmospheric convection and
253 strengthening the MJO. Conversely, cooler SSTs in this region create a more stable
254 atmospheric environment, which is less favorable for the development and propagation
255 of the MJO (DeMott et al., 2015). The activity and strength of the MJO are influenced
256 by SST in the region. Cooler than average sea surface temperatures (SSTs) in this
257 region are associated with the passage of MJO activity and a tendency towards
258 decreased intensity.

259 Table 2 presents the oceanic temperature anomalies for the DJF seasonal mean,
260 including the differences in oceanic temperature between the SST and depths of 10m
261 $(\overline{\Delta T}_{0-10m})$ and 30m $(\overline{\Delta T}_{0-30m})$, as well as phase anomalies of 20–100 days maximum
262 and minimum SST and oceanic temperature at 10m depth (T_{10m}). The region of 110–
263 130° E and 5–15° S was selected because it shows the largest variation in the 20–100-
264 day bandpass-filtered SST when the MJO passes over the Indo-Pacific region. Except



265 for C=30days, the DJF seasonal mean SST shows a slight increase with the higher SST
266 feedback periodicity, while the SST standard deviation remains within 0.8 K. In the
267 critical region (110–130° E, 5–15° S), experiments with high frequency SST feedback
268 periodicity exhibit a mean SST of less than 1.4 K during DJF, while experiments with
269 low frequency SST feedback periodicity range from -1.0 K to 0.5 K compared to the
270 OISST dataset.

271 Understanding the variations in SST during DJF in the Indo-Pacific region is
272 critical for predicting and interpreting the MJO's behavior. The temperature differences
273 between observed monthly mean SST and NCEP GODAS reanalysis data ($\overline{\Delta T_{0-10m}}$
274 and $\overline{\Delta T_{0-30m}}$) as well as AGCM are not compared here. The $\overline{\Delta T_{0-10m}}$ in high-
275 frequency experiments maintain 0.1K temperature difference. In low-frequency
276 experiments, $\overline{\Delta T_{0-10m}}$ increase from 0.1 to 1.0 K as SST feedback periodicity
277 increases correspondingly. The temperature difference ($\overline{\Delta T_{0-30m}}$) in both high-
278 frequency and low-frequency experiments remains approximately 0.8K, except for C=30
279 days. In the daily OISST SST phase anomalies, the maximum and minimum values
280 are approximately maintained at $\pm 0.2K$. However, compared to OISST or model
281 simulations, the uncoupled A-CTL, which uses monthly mean OISST, shows
282 significantly smaller mean anomalies in the SST phase, on the order of 1–2 magnitudes
283 smaller. In the high-frequency experiments, SST phase anomalies exhibit similar
284 magnitudes of $\pm 0.2K$ as observed. The SST means in both the high-frequency and
285 low-frequency experiments reach their maximum in phase 3, lagging about 1 phase
286 behind the OISST. The maximum and minimum T_{10m} values indicate that the
287 atmospheric heat/cooling ocean process is consistently mixed in the C-CTL
288 experiment, but not in the low-frequency experiments.

289 According to CLIVAR diagnostics, there are diverse behaviors observed in MJO
290 simulations, as indicated by the slight difference between phase anomalies of C=3days



291 maximum SST and T_{10m} compared to C-CTL and C-1day, which indicates diverse
292 behaviors of MJO simulations, according to CLIVAR diagnostics. Fu et al. (2017)
293 indicated that too weak intraseasonal SST anomaly in coupled models would lead to
294 the underestimation of the impacts of air-sea coupling on MJO simulations.

295

296 **3.2 MJO simulation: high-frequency and low-frequency SST feedback** 297 **experiments**

298 **3.2.1 General structure**

299 We conducted SST feedback experiments with high-frequency and low-frequency
300 responses, as well as uncoupled AGCMs, to compare the simulated characteristics of
301 the MJO. The propagation characteristics of the different experiments were analyzed
302 using the wavenumber-frequency spectrum (W-FS). The spectra of unfiltered U850 in
303 ERA5 reanalysis, A-CTL, C-CTL, C-1day, C-3days, C-6days, C-12days, C-
304 18days, and C-30days are shown in Fig. 1a-i, respectively. The C-CTL experiment
305 accurately captures the eastward propagating signals at zone wavenumber 1 and for
306 periods of 30 to 80 days (Fig. 1a and 1c), although with a slightly larger amplitude
307 than ERA5. However, the uncoupled A-CTL produces an unrealistic spectral shift to
308 time scales longer than 30-80 days (Fig. 1b) and exhibits westward propagation at
309 wavenumber 2.

310 C-3days tend to reduce the interseasonal variability of the MJO compared to the
311 C-CTL experiment under coupled runs, which is consistent with the results of Stan
312 (2018) in uncoupled experiments that force the atmosphere by surface boundary. de
313 Boisséson et al. (2012) also found that hindcasts of the MJO are sensitive to changes
314 in SST boundary conditions, although daily and weekly SST forecasts are similar. In
315 this study, it was observed that the high-frequency experiments limited the variance of
316 the MJO. According to Stan (2018), the lack of 1-5-day SST variability favors an
317 increase in westward power associated with Rossby waves. The W-FS of the C-1day



318 experiment showed two peaks for zone wavenumber 1 over the 30 to 80-day period.
319 This might be attributed to the inconsistency in day and night variations when the SST
320 feedback of C-1day is returned to the atmosphere at different locations. Except for C-
321 30days, the low-frequency experiments enhance the W-FS of U850 during
322 interseasonal periods. In this study, low-frequency SST variability is not enhanced in
323 the unrealistic westward W-FS by increasing SST feedback periodicity until C-
324 18days.

325 The Hovmöller diagrams in Fig. 2a-i depict the evolution of 10° N- 10° S
326 averaged precipitation and U850 anomalies on intraseasonal timescales, represented
327 by lagged correlation coefficients between precipitation averaged over 10° S- 5° N,
328 $75-100^{\circ}$ E. In GPCP/ERA5, there is observed eastward propagation of precipitation
329 and U850 from the eastern IO to the dateline, with precipitation leading U850 by
330 approximately a quarter of a cycle. The propagation speed of the 30-80-day filtered
331 U850 anomaly is 5 m s^{-1} (Fig. 2a). However, the A-CTL simulations exhibit
332 westward-propagating signals over the IO and weak, slow eastward propagation over
333 the MC and WP (Fig. 2b), which is also reflected in the W-FS shown in Fig. 1b,
334 indicating enhanced westward propagation in wavenumber 2. The Hovmöller
335 diagrams of the high-frequency and low-frequency experiments (Fig. 2c-h) display
336 the key eastward propagation characteristics of both precipitation and U850, as well
337 as the phase relationship between them, except for C-30days. The simulated
338 correlations between precipitation and U850 anomalies in the experiments are
339 generally weaker compared to GPCP and ERA5, particularly when crossing the MC
340 into the WP. Fig. 2b and Fig. 2c-h highlight the contrast, indicating that coupling a 1-
341 D TKE ocean model can significantly enhance an AGCM ability to simulate key
342 characteristics of the MJO, such as amplitude, propagation direction and speed, and
343 the phase relationship between precipitation and circulation. When crossing the MC,



344 the Hovmöller diagram of C–3days precipitation exhibits a substantial weakening
345 compared to other high-frequency and low-frequency experiments (except for C–
346 30days). This weakening is accompanied by a weaker easterly zonal wind in the MC.
347 This finding is consistent with the results from the W-FS in Fig. 1e. Neither
348 precipitation nor U850 exhibit clear eastward propagation characteristics over C–
349 30days. Further detailed discussions on this topic will be presented in the subsequent
350 chapter.

351 We conducted a cross-spectral analysis to examine the phase lag and coherence
352 between the tropical circulation and convection. Figures 3a–i illustrate the symmetric
353 part of OLR and U850 for NOAA/ERA5 data, A–CTL, C–1day, C–3days, C–6days,
354 C–12days, C–18days, and C–30days, respectively. The MJO band exhibits a high
355 degree of coherence, indicating a strong correlation between NOAA MJO-related
356 OLR signal and wavenumbers 1–3 (Fig. 3a). The simulated phase lag in the 30–80-
357 day band is approximately 90° , consistent with previous studies (Ren et al., 2019;
358 Wheeler and Kiladis 1999). All model experiments show significant coherence within
359 wavenumber 3 in the MJO band, with a phase lag similar to NOAA/ERA5 data.
360 However, A–CTL at wavenumber 1 only exhibits half of the observed coherency
361 peaks, and the coherence at wavenumbers 2–3 for the 30–80-day period is weaker
362 compared to NOAA/ERA5 data. The experiments C–CTL, C–1day, C–3days, C–
363 6days, C–12days, and C–18days exhibit similar coherency peaks to NOAA/ERA5 at
364 wavenumber 1. Additionally, as the SST feedback periodicity increases, the
365 experiments between C–12days and C–30days simulate unrealistic coherency over
366 wavenumber 9 in the MJO band (Fig. 3g–i).

367 The 20–100-day filtered precipitation anomalies (shaded) and SST anomalies
368 (contour) were averaged over the 10° S– 10° N region (Fig. 4a–i). Phase-longitude
369 diagrams were used to analyze the relationship between precipitation and SST



370 fluctuations and to establish the connection between air–sea coupling and convection.
371 Except for C–30days, both GPCP/OISST and the coupled experiments clearly showed
372 the eastward propagation of enhanced convection with positive SST anomalies (Fig.
373 4a and 4c–i). The amplitude of SST increases in low-frequency experiments, as
374 indicated in Table 1 and Fig. 4f–h, resulting in precipitation anomalies lagging by
375 approximately 2–3 phases than SST, particularly when crossing the MC. Liang et al.
376 (2018) indicated SST leading precipitation by 10 days implies air–sea interactions at
377 the intraseasonal timescale during MJO events, with SST playing a crucial role in
378 modulating the MJO's intensity and propagation. The A–CTL simulations exhibited
379 weak SST anomalies and stationary precipitation when using the monthly average
380 SST interpolation from OISST. In contrast, the C–30days experiment showed
381 unrealistic SST and precipitation variability. Overall, eastward propagation of the
382 MJO is not favored by either minimal or large SST fluctuations (Fig. 4b and 4i). By
383 comparing the coupled experiments with the aforementioned simulations, it became
384 evident that air–sea interaction plays a crucial role in facilitating eastward
385 propagation. Fu et al. (2017) found that a robust intraseasonal SST anomaly is
386 associated with successive MJO events and supports the propagation of MJOs, as
387 supported by NOAA OLR and TRMM precipitation. This study highlights the
388 significant improvement in eastward propagation simulations achieved by
389 incorporating the air–sea interaction process into the model with distinct high-
390 frequency and low-frequency experiments, even with a simple 1-D ocean model like
391 SIT.

392

393 **3.2.2 Vertical structures of the MJO in the atmosphere**

394 Air–sea interaction plays a significant role in influencing atmospheric moisture
395 and convection associated with the MJO (Savarin and Chen, 2022). During periods of



396 convective suppression, the surface air temperature generally tracks the SST closely
397 (de Szoeke et al., 2014). A warmer upper ocean enhances low-level atmospheric
398 convergence, leading to increased low-level moisture and preconditioning that
399 facilitate eastward propagation and deep convection (DeMott et al., 2014). Hovmöller
400 diagrams in Fig. 5a–i illustrate the relationship between air temperature anomalies
401 (contoured, in K) and the vertically tilting structure of specific humidity (shading, in g
402 kg^{-1}) from the surface to the upper troposphere (200 hPa) over the 10°S – 10°N and
403 120 – 150°E regions. Positive air temperature anomalies lead positive specific
404 humidity anomalies by approximately 2–3 phases, with the maximum specific
405 humidity occurring between 700–500 hPa. In ERA5 and the coupled experiments
406 (excluding C–30days), there are two relatively high values of air temperature at 300
407 and 700 hPa, respectively. However, in A–CTL, the maximum specific humidity
408 anomaly occurs at 700 hPa, and there is a vertically stationary structure in specific
409 humidity anomaly and an opposite tilting in air temperature (Fig. 5b). A–CTL also
410 exhibits a decrease in low-level moisture anomaly due to negative air temperature
411 anomalies below 700 hPa. C–30days, on the other hand, shows an unrealistic vertical
412 tilting structure in both specific humidity and air temperature anomalies (Fig. 5i).

413 According to the WISHE-moisture mode theory (Fuchs and Raymond, 2017), the
414 combination of mean easterly zonal winds and moisture plays a role in the
415 propagation and destabilization of the MJO. East of the convective MJO, enhanced
416 easterly winds induce atmospheric destabilization and moistening, leading to the
417 propagation of the MJO (Sentić et al., 2020). Figure 6 displays the averaged p-
418 vertical velocity anomaly (OMEGA, Pa s^{-1} , shaded) and zonal wind anomaly (m s^{-1} ,
419 contour, interval 0.5) between phase 3 and phase 4 over the 15°N – 15°S region. We
420 specifically selected the phase between 3 and 4 to examine the period leading up to
421 the MJO convection crossing the MC. Prior to the onset of the MJO in this phase,



422 there is typically a buildup of convection over the land areas of the MC, which
423 encompass countries such as Indonesia, Malaysia, and the Philippines. This land
424 convection acts as a precursor to the MJO as it creates favorable conditions and sets
425 the stage for the subsequent development of organized atmospheric disturbances. This
426 can be observed in the low-level ascending OMEGA shown in Figure 6a, specifically
427 between 120–150° E. The land convection over the MC is driven by a combination of
428 factors, including the local geography, land-ocean temperature contrasts, and large-
429 scale atmospheric conditions. The complex topography and the presence of extensive
430 water bodies surrounding the MC provide favorable conditions for the uplift of moist
431 air, which leads to the formation of local convection. Additionally, the temperature
432 differences between the warm ocean waters and the relatively cooler land surfaces
433 contribute to the instability and uplift of air masses.

434 In C–CTL, there is an enhanced easterly wind anomaly between 120° E and 180°
435 E at 800–600 hPa (Fig. 6c). The stronger easterly winds, coupled with radiative
436 heating, such as net downwelling surface solar radiation, lead to warmer upper ocean
437 temperatures (not shown). This heat stored in the upper ocean influences surface
438 fluxes and drives convection in the atmosphere (de Szoeke et al., 2014; Hsu et al.,
439 2019). In the western IO and MC region (Fig. 6c–h), there is a spatial distribution of
440 negative OMEGA (ascending motion) anomalies during phase 3–4, accompanied by
441 westerly wind anomalies to the west of MJO convection below 500 hPa in the coupled
442 experiments (except C–30days). In A–CTL during phase 3–4, negative OMEGA
443 anomalies are observed both east and unrealistically west of the MC (Fig. 6b).
444 Generally, the low-frequency experiments exhibit stronger negative OMEGA,
445 westerly wind anomalies and land convection compared to the high-frequency
446 experiments, except for C–30days. In the case of C–30days, deep convection in the



447 IO, MC, and WP regions is weakened as local convection occurs randomly during
448 phase 3–4 (Fig. 6i).

449

450 **3.2.3 The vertical structure of the ocean responds to the MJO**

451 Understanding the interaction between the atmosphere and upper ocean is
452 essential for studying the MJO, particularly the upper ocean's response to strong
453 atmospheric forcing. Accurate representation of air–sea interactions, including
454 momentum and heat fluxes associated with the MJO, is crucial for capturing the MJO
455 in coupled model simulations, as emphasized by Hong et al. (2017). It is crucial to
456 properly couple an ocean model that incorporates MJO air–sea interaction for a
457 comprehensive understanding. Such coupling can lead to warmer or cooler surface
458 oceans and shallower or deeper mixed layer depths before or after MJO convection in
459 the tropics, resulting from improved vertical resolution in the upper ocean (Tseng et
460 al., 2015; Lan et al., 2022). These oceanic changes, in turn, induce atmospheric
461 responses through the ocean feedback process. In this study, we employ a SIT model
462 coupled with CAM5 to investigate the frequency of air–sea coupling and its impact on
463 MJO simulation. This ocean model incorporates a high vertical resolution that
464 captures important features such as the cool skin layer and diurnal warm layer, as well
465 as the gradient of temperature in the upper ocean. In the OISST, high-frequency, and
466 low-frequency experiments, the strongest phase anomalies of maximum SST occur
467 between phases 2 and 3 (as shown in Table 1), particularly in the region of (110–130 °
468 E, 5–15° S), where SST variations associated with the MJO are most prominent.
469 Figure 7 illustrates the average oceanic temperature between 0- and 60-meters depth
470 during phase 2–3, filtered for the 20–100-day period, represented by shaded and
471 contour plots with an interval of 0.03 Kelvin. In the high-frequency experiments, the
472 upper oceanic temperatures exhibit warming patterns within 30 meters depth at 100–



473 140° E, while cooling is observed near the dateline (as shown in Fig. 7a–c). During
474 phase 2–3, as the MJO convection progresses into the IO (60–90° E), it interacts with
475 the ocean surface, leading to a cooling effect in the upper ocean in the C–CTL
476 experiment (Fig. 7a), which is more pronounced compared to the C–3days experiment
477 (Fig. 7c), characterized by stronger interseasonal MJO variability. In the low-
478 frequency experiments, the spatial distribution of warmer upper ocean temperatures is
479 more extensive than in the high-frequency experiments, spanning from the MC to the
480 WP. Additionally, the vertical temperature gradient in this region is greater in the low-
481 frequency experiments compared to the high-frequency experiments. However, in the
482 Indo-Pacific region, the C–30days experiment exhibits an unrealistic spatial
483 distribution of oceanic temperature anomalies, with small areas of both positive and
484 negative anomalous temperature fluctuations (Fig. 7g).

485

486 **4. Discussion**

487 **4.1 Empirical Orthogonal Function (EOF) analysis**

488 Empirical orthogonal functions (EOF) analysis helps identify spatial patterns and
489 their associated temporal variations, providing insights into the underlying dynamics
490 and relationships within the dataset. The first EOF mode captures the largest fraction
491 of variance in the data, while subsequent modes capture progressively smaller
492 amounts of variance and represent additional patterns. This study builds upon
493 previous research utilizing uncoupling simulations (e.g., DeMott et al., 2014; Stan,
494 2018) and investigates the influence of interseasonal SST feedback on the MJO by
495 incorporating real air–sea coupling. Figure 8 illustrates the near-equatorial variance
496 explained by the Real-time Multivariate MJO series 1 (RMM1) and series 2 (RMM2),
497 which represent the combined variance explained by the first two empirical
498 orthogonal functions (EOF1 and EOF2) according to Wheeler and Hendon (2004).



499 These RMM1 and RMM2 components have proven useful for estimating and
500 characterizing the MJO and its variability. The coupled experiments, when combined
501 with RMM1 and RMM2, demonstrate improved MJO performance compared to A–
502 CTL, with the exception of C–30days. The extension of interseasonal SST feedback
503 periodicity corresponds to an increase in RMM1+RMM2. Generally, the
504 RMM1+RMM2 percentages are larger for the low-frequency experiments compared
505 to the high-frequency experiments, except for C–30days. Among the high-frequency
506 experiments, C–3days shows a slight degradation in RMM1+RMM2, consistent with
507 the observed MJO-related results such as the W-FS for 850-hPa zonal wind (Fig. 1e),
508 the Hovmöller diagram of precipitation crossing the MC (Fig. 2e), the OLR power
509 spectrum at a zonal wavenumber-frequency wavelength (Fig. 3e), the maximum
510 phase-vertical Hovmöller diagram of 20–100-day specific humidity between 700–500
511 hPa (Fig. 5e), and the cooling effects in the upper ocean (Fig. 7c). However, C–
512 30days exhibits lower skill in terms of RMM1+RMM2 compared to the other coupled
513 simulations due to the presence of excessive local convection and weak large-scale
514 circulation, which is reflected in the unrealistic spatial distribution of oceanic
515 temperature.

516

517 **4.2 The dynamic lead–lag relationship of intraseasonal variability**

518 The lead–lag relationship refers to a situation where one variable (leading) is
519 cross-correlated with the values of another variable (lagging) in subsequent phases,
520 particularly in the case of SST fluctuations and MJO-related atmospheric variations
521 between phase 1 and 8 within the domain of 110–130° E and 5–15° S (Fig. 9). The
522 analyzed variables consist of 20–100-day filtered latent heat flux (LHF, indicated by
523 green shading), OLR (indicated by a yellow bar chart), net surface solar radiation
524 (FSNS, indicated by an orange bar chart), U850 (indicated by a purple bar chart), 30-



525 meter depth oceanic temperature (30-m T multiplied by 100, indicated by a black
526 line), and SST (multiplied by 10, indicated by an orange line) which positive values
527 are represented by an upward direction in LHF and FSNS. The graphical
528 representation of variables marked with "(L)" employs the left y-axis, while variables
529 marked with "(R)" utilize the right y-axis.

530 The decrease in LHF, which indicates a reduction in heat loss from the ocean,
531 and the negative FSNS, indicating that solar radiation is heating the ocean, coincide
532 with easterly zonal winds that contribute to positive SST anomaly in ERA5 (Fig. 9a).
533 This lead–lag relationship depicts the changes in LHF, FSNS, OLR, U850 and SST
534 which positive SST anomaly prior to the MJO convection period emphasizing the
535 interconnectedness of oceanic heat fluxes, solar radiation, and atmospheric circulation
536 patterns. As the MJO convection progresses through the region (110–130° E and 5–
537 15° S), several changes in atmospheric and oceanic variables occur. These changes
538 include a shift in OLR from positive to negative values, a decrease in SST, a transition
539 to westerly winds, and an increase in positive FSNS and LHF (Fig. 9a). With the
540 exception of experiments of A–CTL and C–30days, both the high-frequency and low-
541 frequency SST feedback experiments exhibit similar simulation of lead–lag
542 relationships when compared to ERA5 (Fig. 9c–h). It is worth noting that in
543 experiments C–CTL, C–1day, C–3days, and C–6days, the variations in LHF are
544 underestimated. Conversely, in experiment C–18days, the variations in LHF are
545 overestimated. In experiment C–12days, the variations in LHF are similar to the
546 expected values. The magnitude of SST fluctuations is directly related to the
547 variations in LHF, FSNS, OLR, and U850 in the lead–lag relationship. In ERA5,
548 phase 2 corresponds to the occurrence of the maximum positive SST anomaly within
549 the domain of 110–130° E and 5–15° S, while phase 7 corresponds to the occurrence
550 of the most negative SST anomaly. When comparing the high-frequency and low-



551 frequency SST feedback experiments to ERA5, except for experiments A–CTL and
552 C–30days, the maximum positive SST anomaly is consistently delayed by one phase.

553 Additionally, the occurrence of the most negative SST anomaly aligns with the
554 same phase in both types of experiments. The maximum positive anomaly in the 30-m
555 T is delayed by one phase compared to the SST, indicating the transfer of heat from
556 the ocean surface into the upper ocean progressively. Similarly, the occurrence of the
557 most negative 30-m T anomaly is also delayed by one phase compared to SST,
558 revealing the buffering role of the upper ocean when the MJO convection extracts
559 heat (energy) from the ocean (Fig. 9c–i). In the A–CTL experiment, which utilizes
560 monthly OISST data, the SST anomalies are relatively small. This is reflected in the
561 weak anomalies observed in OLR and FSNS (Fig. 9b). On the other hand, in the C–
562 30days experiment, there is a misalignment in the lead–lag relationship, and the OLR
563 and FSNS anomalies are also weak (Fig. 9i).

564

565 **4.3 The extreme frequency of oceanic feedback can sustain MJO propagation**

566 In previous studies, it has been observed that most models incorporate both
567 coupled and uncoupled simulations. DeMott et al. (2014) specifically noted that in
568 uncoupled experiments, SPCAM3 exhibited strong eastward propagation for 5-day
569 running means, but relatively weaker propagation for monthly means. This raises the
570 question of how much SST feedback periodicity is necessary to maintain robust
571 eastward propagation in coupled experiments. This section aims to discuss this topic
572 and explore strategies for achieving robust eastward propagation. It is observed that
573 the aforementioned criteria are met with increased feedback periodicity for SST until
574 the C–30days experiment. SST feedback periodicity, characterized by SST-forced
575 atmospheric variability, exhibits notable differences between coupled and uncoupled
576 experiments. In uncoupled experiments (A–CTL), the SST lacks responsiveness to



577 atmospheric changes, leading to unrealistic intraseasonal variability in atmospheric
578 circulation. Spatially, Through air–sea interaction, most of the coupled experiments
579 showed improved MJO simulation with realistic strength and eastward propagation
580 speeds (e.g., C–CTL, C–1day, C–3days, C–6days, C–12days, and C–18days), where
581 higher MJO variance was associated with increased SST feedback periodicity.

582 Generally, C–18days exhibited an overestimation of intraseasonal variability
583 while maintaining eastward propagation of the MJO. Figure 10 highlights
584 considerable differences in the simulation of robust (disordered) MJOs at phase 4
585 between C–18days and C–30days. In C–18days, negative OLR anomalies are
586 widespread across the MC and extend to the WP near the equator in the northern
587 hemisphere (Fig. 10b). Concurrently, U200 exhibits divergence patterns that coincide
588 with the negative OLR anomaly. Negative OLR anomalies are indicative of the
589 presence of deep convection. In the C–CTL experiment, the spatial distribution of
590 negative OLR overlaps with positive net surface heat flux and solar radiation
591 anomalies, indicating heat loss from the ocean to the atmosphere (Fig. 10g). Notably,
592 in C–18days, there is irregular heat flux loss from the surface ocean near the equator
593 in the western Pacific (Fig. 10h), which is not observed in C–CTL.

594 Furthermore, in the C–18days experiment, there is a notable 75% increase in
595 solar radiation anomalies (with upward direction indicating positive values), resulting
596 in reduced solar radiation reaching the ocean surface in the southeastern IO when
597 compared to C–CTL. Positive anomalies in LHF (Fig. 10e) are predominantly
598 observed within and the west of the convective region, coinciding with westerly
599 winds and a cooling of SST (Fig. 10k). Liang et al. (2018) investigated the variability
600 of the heat fluxes, a major contributor of the intraseasonal SST variability. In C–CTL
601 at phase 4, relatively weak westerly winds and latent heat flux are observed in the IO
602 (Fig. 10d). Upon the passage of deep convection across the MC, the IO experiences



603 intensified westerly winds and latent heat flux anomalies (not shown). These positive
604 latent heat flux anomalies, resulting from ocean evaporation, contribute negative SST
605 anomalies and provide a negative feedback in the atmosphere. Wu and Kirtman
606 (2005) suggest that through air–sea coupling, SST-forced atmospheric changes in
607 surface winds and heat fluxes exert a strong negative feedback on SSTs in the Indo-
608 Pacific region. Jayakumar et al. (2011) conducted a series of experiments using an
609 ocean general circulation model to investigate the individual contributions of different
610 processes. Their findings during the period of 1997–2006 reveal that wind stress
611 accounted for approximately 20% of the intraseasonal SST variability in the IO
612 region, while heat fluxes made up about 70% of the variability. Among the heat flux
613 components, shortwave radiation exerted the most significant influence, contributing
614 75%, while the remaining 25% was attributed to other flux components. Gao et al.
615 (2020a) corroborate that the temporal variations in SST anomaly are primarily driven
616 by shortwave radiative heating, and LHF playing a secondary role.

617 In both C–CTL and C–18days simulations, there is evidence of a negative
618 feedback in the lag–lead relationships among SST, surface winds, rainfall anomalies,
619 and heat fluxes (Fig. 9c and 9h), which supports the findings of previous studies (Wu
620 and Kirtman, 2005; Jayakumar et al., 2011; Gao et al., 2020a). With increased
621 feedback periodicity of SST in C–CTL and C–18days, the ocean continues to receive
622 atmospheric forcing, but the feedback response is delayed, leading to the
623 accumulation of energy (temperature) in the upper ocean, as seen in the SST
624 distribution in the WP (Fig. 10k). In C–30days, SST exhibits a perturbed
625 unrealistically spatial distribution (Fig. 10l) driven by plus-minus latent heat flux and
626 10m wind anomalies (Fig. 10f), net surface heat flux, and solar radiation (Fig. 10i).
627 Consequently, these perturbed SST plus-minus patterns trigger numerous local



628 convections among the IO, MC, and WP and does not manifest as organized the large-
629 scale circulation.

630

631 **4.4 The moist static energy (MSE) analysis**

632 A budget analysis of MSE is used to investigate the underlying mechanisms
633 driving the onset and eastward propagation of the MJO event. Analyzing the MSE
634 budget provides valuable insights into the physical processes and feedback
635 mechanisms influencing the behavior of the MJO, including vertical MSE advection,
636 zonal MSE advection, meridional MSE advection, surface heat fluxes, atmospheric
637 radiative term, and residual components.

638

639 **4.4.1 Preconditioning phase**

640 Analysis of the column-integrated MSE budget has revealed that both vertical
641 and horizontal MSE advection contribute to the east-west asymmetry of MSE
642 tendency, thereby facilitating the eastward propagation of the MJO (Wang and Li,
643 2020). Figure 11 illustrates the physical processes associated with each term
644 contributing to the column-integrated MSE tendency ($\langle \text{dmdt} \rangle$) in Eq. (1), as outlined
645 in Tseng et al. (2022), preceding deep convection over the MC area ($10^\circ \text{S} - 0^\circ \text{N/S}$,
646 $120 - 150^\circ \text{E}$) during phase 2 over the ERA5 and model simulations. The MJO
647 convection in the eastern Indian Ocean at phase 2, the column-integrated vertical
648 advection ($-\langle \text{wdmdp} \rangle$) over the MC area takes a dominant role in the MSE budget,
649 while horizontal MSE advection ($-\langle \text{vdm} \rangle$) plays a secondary role. These findings,
650 along with significant compensation from longwave radiation, were identified by
651 Wang and Li (2020) and Tseng et al. (2022). Generally, the $-\langle \text{wdmdp} \rangle$ accounts for
652 approximately 72–86% of ERA5, except for A–CTL and C–30days, while the
653 $\langle \text{vdm} \rangle$ increases from 40% to 80% of ERA5 due to the heightened feedback



654 periodicity of SST (Fig. 11). Those results indicate that all model simulations exhibit
655 weaker 20–100-day filtered MSE advection anomalies prior to the eastward
656 propagation of the MJO over the MC compared to ERA5. Similarly, the precipitation
657 results in Fig. 4c–h demonstrate the same trend. Moreover, the LH term exhibits an
658 opposite trend to the $\langle vdm \rangle$ term due to the increased feedback periodicity of SST,
659 while SH and shortwave radiation fluxes ($\langle SW \rangle$) contribute less to the negative MSE
660 tendency in both ERA5 and model simulations. These findings indicate that, in the
661 early phase, the negative contribution primarily stems from the LH and longwave
662 radiation fluxes ($\langle LW \rangle$) term. Tseng et al. (2022) identify the negative LH bias as a
663 key factor in enhancing the leading MSE tendency during MJO preconditioning
664 phases. In general, coupling enhances the budget simulation by increasing the positive
665 contribution of vertical and horizontal advection and the negative contribution of LH
666 and $\langle LW \rangle$ in MSE tendency, primarily due to the intensified feedback periodicity of
667 SST during the initial phase of the MJO. Although the $\langle dmdt \rangle$ term can be further
668 decomposed into variations of $\langle wdmdp \rangle$, $\langle vdm \rangle$, and LH in model simulations, the
669 total column-integrated MSE tendency does not exhibit a clear difference in response
670 to the increasing feedback periodicity of SST experiments during the initial phase of
671 the MJO.

672

673 **4.4.2 Phase of strongest convection across the MC**

674 We compared the spatial distribution of 20–100-day $\langle dmdt \rangle$ (shading),
675 precipitation (contours), and 850-hPa wind (vectors) during phase 5, which represents
676 the period of strongest convection across the MC (Fig. 12). In ERA5, the main
677 convection is accompanied by positive precipitation anomalies and low-level
678 convergence in the 850-hPa wind across the MC extending into the WP (Fig. 12a). A
679 positive MSE tendency, peaking near 15° N and 15° S, is observed to the east of the



680 MJO convection located near the Equator. Conversely, a negative integrated MSE
681 tendency is observed to the west of the MJO convection accompanied by negative
682 precipitation anomalies to the west of this region. The meridionally confined structure
683 near the Equator exhibits characteristics indicative of an equatorial Kelvin wave
684 propagated toward the east as fundamental dynamics of the MJO. With the exception
685 of A-CTL and C-30days, the model simulations display a similar structure to ERA5
686 in terms of the 20–100-day filtered $\langle \text{dmdt} \rangle$, precipitation, and 850-hPa wind vectors
687 (Fig. 12c–h). C-CTL exhibits relatively weak precipitation anomalies in the MC and
688 weak westerly winds in the IO until C-6days, where robust precipitation and low-
689 level convergence in the 850-hPa wind occur in response to the feedback periodicity
690 of SST increasing. On the contrary, A-CTL exhibits abnormal positive precipitation
691 anomalies distributed over the western IO, while localized maximum of $\langle \text{dmdt} \rangle$
692 occur near 15° N (Fig. 12b). In contrast, C-30days displays plus-minus precipitation
693 anomalies near the Equator, consequently disrupting the spatial distribution of the
694 $\langle \text{dmdt} \rangle$ relative to MJO convection (Fig. 12i).

695 To quantify the impact of SST feedback periodicity on atmospheric
696 intraseasonal variability in the tropics, we adopt the approach of Tseng et al. (2022)
697 and Jiang et al. (2018) to project all MSE terms onto the 20–100-day filtered ERA5
698 $\langle \text{dmdt} \rangle$ (Fig. 12a) during phase 5. The MC has been frequently identified as a barrier
699 to the eastward propagation of the MJO, as noted by Li et al. (2020b). Additionally, a
700 considerable proportion, approximately 30–50%, of the MJO experiences stalling
701 over the MC, as reported by Zhang and Han (2020). To mitigate the influence of
702 weaker MJO events that dissipate prior to reaching the MC, our focus is specifically
703 on phase 5 of the MJO. Figure 13(a) illustrates the determination of the contribution
704 of each component of the MSE tendency during phase 5 by projecting the spatial
705 pattern of each MSE budget term over the MC region (20° S–20° N, 90–210° E),



706 where F_s is total surface fluxes including sensible and latent heat fluxes, and Q_r is
707 vertically integrated radiative (short-wave and long-wave) heat fluxes. The dominant
708 contribution of horizontal advection to the MSE tendency (Fig. 13a) are simulated
709 well in both the high-frequency and low-frequency SST feedback experiments, but
710 not in the A-CTL simulation. The $\langle vdm \rangle$ term increases in response to the
711 increasing feedback periodicity of SST, resulting from stronger low-level
712 convergence, which enhances MJO convection. Vertical advection $\langle wmdp \rangle$ is not
713 the dominant term over the MC region (20°S – 20°N , 90 – 210°E) in both ERA5 and
714 model simulations during phase 5. Furthermore, F_s and Q_r make a minor contribution
715 to the MSE tendency, with the sensible and latent heat fluxes exhibiting a tendency
716 towards greater recessive behavior in response to the increasing feedback periodicity
717 of SST.

718 The total horizontal MSE advection is further decomposed into its zonal (\langle
719 $udmdx \rangle$) and meridional zonal ($\langle vmdy \rangle$) components for high-frequency SST
720 feedback experiments (C-CTL, A-CTL, C-1day, and C-3days) and low-frequency
721 SST feedback experiments (C-6days, C-12days, C-18days, and C-30days) in order
722 to examine their individual effects (Fig. 13b–c). Both components contribute
723 positively, but the $\langle vmdy \rangle$ exhibits a larger amplitude, consistent with findings by
724 Tseng et al. (2022) during phase 4. The $\langle vmdy \rangle$ of high-frequency SST feedback
725 experiments (C-CTL, C-1day, and C-3days) closely resemble ERA5 in terms of the
726 projected magnitude. Comparatively, the $\langle vmdy \rangle$ term in low-frequency SST
727 feedback experiments (C-6days, C-12days, C-18days, and C-30days) exhibits a
728 more positive contribution than in high-frequency SST experiments, leading to a
729 dominant contribution to the increase in $\langle vdm \rangle$ and $\langle dmdt \rangle$.

730 We generated a spatial representation of the 20–100-day column-integrated
731 vertical MSE advection ($\text{J kg}^{-1} \text{s}^{-1}$, represented by shading), column-integrated



732 horizontal MSE advection ($\text{J kg}^{-1} \text{s}^{-1}$, shown as contours with an interval of 6.0), and
733 200-hPa wind (green vectors) relative to a reference vector (3 m s^{-1}) during phase 5
734 (Fig. 14). This figure complements the information provided by the bar chart in Fig.
735 13a. In ERA5, the wind divergence at 200 hPa during phase 5 (Fig. 14a), overlaid
736 with the 850-hPa convergence (Fig. 12a), indicates a vertically tilting structure of
737 zonal wind anomalies. Except for A-CTL and C-30days, the model simulations
738 exhibit a similar structure to ERA5 in terms of low-level convergence and high-level
739 divergence. In ERA5, the negative $\langle \text{wdmdp} \rangle$ and $\langle \text{vdm} \rangle$ anomalies (Fig. 14a) are
740 observed to the west of the MJO convection, which is characterized by positive
741 precipitation anomalies (Fig. 12a). The spatial distribution of the negative $\langle \text{vdm} \rangle$
742 anomaly (dashed-red contours) extends from the IO to the MC, exhibiting a pattern
743 similar to $\langle \text{dmdt} \rangle$ with enhanced anomalies. This results in the projection of the
744 spatial pattern of the $\langle \text{vdm} \rangle$ term being greater than 1. The positive $\langle \text{wdmdp} \rangle$
745 anomaly (shading) is located in the western IO and east of the dateline, which results
746 in a spatial distribution unlike that of $\langle \text{dmdt} \rangle$ comparatively. This difference reduces
747 the projection of the spatial pattern of $\langle \text{vdm} \rangle$ to a value lower than 1. On the
748 contrary, in the A-CTL experiment, the positive $\langle \text{vdm} \rangle$ anomaly (solid-blue
749 contours) exhibits a spatial distribution near 120° E (Fig. 14b), while the negative -
750 $\langle \text{vdm} \rangle$ anomaly (dashed-red contours) is distributed on both the positive left and
751 right sides. Although the negative $\langle \text{vdm} \rangle$ anomaly in high-frequency SST feedback
752 experiments (C-CTL, C-1day, and C-3days) underestimates that of ERA5 (Fig. 14c-
753 e), the spatial distribution remains similar to ERA5 due to an approximately 80%
754 projection of $\langle \text{vdm} \rangle$ compared to ERA5. The low-frequency SST feedback
755 experiments (C-6days, C-12days, and C-18days) yield greater $\langle \text{vdm} \rangle$ anomalies
756 (Fig. 14f-h) compared to ERA5, with projection values greater than 1. We noticed
757 that, in the low-frequency SST feedback experiments, although the anomalies of -



758 <wdmdp> intensify, the spatial distribution of those shift eastward, leading to a
759 decrease in projection values.

760

761 **5. Conclusions**

762 This study builds upon the work of Lan et al. (2022) and Tseng et al. (2022) by
763 coupling a high-resolution 1-D TKE ocean model (the SIT model) with the CAM5,
764 specifically the CAM5–SIT configuration, to investigate the extreme effects of
765 interseasonal SST feedback on the MJO. We introduced asymmetric exchange
766 frequencies between the atmosphere and the ocean, ensuring bidirectional interaction
767 at each timestep within the experimental periodicity by fixing the SST value in the
768 Coupler. This allowed us to create various intraseasonal SST feedback atmospheric
769 experiments, including intervals of 30 minutes, 1, 3, 6, 12, 18, and 30 days.
770 Systematic sensitivity experiments were conducted to divide into two groups: those
771 feedback periodicity within a phase (high-frequency SST) and those beyond a phase
772 (low-frequency SST).

773 The aim is to assess the scientific reproducibility and consistency of the findings
774 across different SST feedback cycles in the field of modeling science. With the
775 exception of the C–30days experiment, both the high-frequency (C–CTL, C–1day,
776 and C–3days) and low-frequency (C–6days, C–12days, C–18days) experiments
777 demonstrate realistic simulations of various aspects of the MJO when compared to
778 ERA5. These aspects include intraseasonal periodicity (as shown in Fig. 1), eastward
779 propagation (as observed in Fig. 2 and 4), coherence in the low-frequency band (as
780 depicted in Fig. 3), tilting vertical structure (evident in Fig. 5, 12, and 14 for zonal
781 wind), intraseasonal SST (as summarized in Table 2) and oceanic temperature
782 variances (as shown in Fig. 7), the lead–lag relationship of intraseasonal variability
783 (as characterized in Fig. 9), phase 2 column-integrated MSE tendency terms



784 (including decomposition items) (illustrated in Fig. 11), and the projection of all MSE
785 terms onto the ERA5 column-integrated MSE tendency during phase 5 (depicted in
786 Fig. 13).

787 The lead–lag relationship provides a visual representation of the variations in
788 20–100-day filtered LHF, FSNS, OLR, U850 and SST, while positive SST leading up
789 to the onset of the MJO convection (Fig. 9). This relationship highlights the
790 interconnected nature of oceanic heat fluxes, solar radiation, and atmospheric
791 circulation patterns, underscoring their mutual influence and interplay. Table 3
792 provides a comprehensive overview of several variables during the boreal winter,
793 including the average values of 20–100-day filtered OLR, LHF, FSNS, U850,
794 $\langle \text{dmdt} \rangle$, $\langle \text{wdmdp} \rangle$, and $\langle \text{vdm} \rangle$. These variables are categorized based on the states
795 of SST warming and cooling. The categorization is performed over two specific
796 domains: (110–130° E, 5–15° S), as referenced in Fig. 9, and (120–150° E, 0–10° S)
797 marked as background gray, as referenced in Fig. 11. We highlight the characteristics
798 of the MJO-related atmosphere with red letters, which correspond closely to the
799 values in ERA5. In synthesizing the findings from Arnold et al. (2013) regarding the
800 high SST enhances MJO simulation, the improved MJO simulation through
801 intraseasonal SST variability by Liang et al. (2018), the information provided in
802 Tables 2 and 3, and the corresponding figures, it becomes evident that the high-
803 frequency (low-frequency) SST experiments tended to underestimate (overestimate)
804 the MJO simulation. Notably, the experiment C–6days demonstrated the closest
805 similarity to ERA5 in terms of MJO simulation.

806 Among the high-frequency experiments, C–3days shows a less close
807 resemblance to the observed MJO characteristics. The result of the C–3days
808 experiment is consistent with Stan (2018), as the absence of 1–5-day variability in
809 SST promotes the amplification of westward power associated with Rossby waves. In



810 addition, the C–1day experiment confirms the scientific reproducibility of Hagos et al.
811 (2016) and Lan et al. (2022) that demonstrates that the removal of the diurnal cycle
812 enhances the MJO.

813 The increasing feedback periodicity of SST in low-frequency experiments leads
814 to the accumulation of short-wave and long-wave radiations and surface heat fluxes
815 from the atmosphere, resulting in an increase in the upper oceanic temperature and its
816 variances (Table 2). SST variances that are higher than OISST contribute to
817 robust/overestimated simulations of the MJO (as observed in Fig. 1–14 and Table 3).
818 In contrast, the C–30days experiment exhibits variances with both positive and
819 negative anomalies in precipitation (Fig. 4 and 10), oceanic temperature (Fig. 7), net
820 surface heat fluxes (Fig. 10), and column-integrated vertical and horizontal MSE
821 advection (Fig. 14). These anomalies have an unrealistically spatial distribution and
822 an unrealistic vertical tilting structure in both specific humidity and air temperature
823 anomalies (Fig. 5i) over the Indo-Pacific region. As a result, local convection appears
824 randomly among the IO, MC, and WP, and does not manifest as organized MJO
825 convection.

826 Finally, in Fig. 15, the interseasonal SST feedback experiments on MJO are
827 depicted schematically. These experiments include the uncoupled model (A–CTL),
828 high-frequency SST experiments (C–CTL, C–1day, and C–3days), low-frequency
829 SST experiments (C–6days, C–12days, C–18days), and disorganized convection and
830 circulation (C–30days) which figure concept is based on DeMott et al. (2014) in Fig.
831 11. In the absence of interseasonal SST variability, the uncoupled A–CTL disrupts the
832 eastward propagation of the MJO, leading to weakened or fragmented MJO activity as
833 shown in Fig. 15a. On the other hand, the high-frequency SST experiments generally
834 capture the characteristics of the MJO. The time-varying SSTs in the coupled
835 simulation provide a certain level of organization and sufficient surface fluxes, which



836 facilitate the development of MJO circulations, as illustrated in Fig. 15b. Moreover, in
837 the coupled model, the presence of land convection over the MC ahead of the MJO
838 convection (Fig. 6) contributes to the instability and uplift of moist air masses.
839 Conventionally, the MJO has been regarded as a tropical atmospheric variability,
840 given that its existence is primarily attributed to the interplay between organized
841 convection and large-scale circulations. This dynamic process plays a crucial role in
842 triggering the eastward propagation of the MJO. Furthermore, the low-frequency SST
843 experiments demonstrate robust simulations of the MJO. This can be attributed
844 comprehensively to the increased SST variances, accumulation of surface fluxes,
845 enhanced low-level convergence (Fig. 12) and high-level divergence (Fig. 14), as well
846 as horizontal MSE advection, as depicted in Fig. 15c. On the other hand, the C–
847 30days experiment simulates frequent, disorganized convection, as shown in Fig. 15d.
848 This experiment exhibits both positive and negative anomalies in precipitation, SST,
849 surface heat fluxes, and vertical and horizontal MSE advection, which fail to generate
850 the expected circulation anomalies.

851
852 *Code and data availability.* The model code of CAM5–SIT is available at
853 <https://doi.org/10.5281/zenodo.5510795>. Input data of CAM5–SIT using the
854 climatological Hadley Centre Sea Ice and Sea Surface Temperature dataset and
855 GODAS data forcing, including 30-year numerical experiments, are available at
856 <https://doi.org/10.5281/zenodo.5510795>.

857
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859 Taiwan Earth System Model project. YYL is the CAM5–SIT model developer and
860 writes the majority part of the paper. WLT assists in MSE analysis.

861



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863

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1145 *Sy.*, 12, e2020MS002058, <https://doi.org/10.1029/2020MS002058>,
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1147 Table 1. Two sets of marine feedback frequency with high-frequency
 1148 SST feedback (C-CTL, C-1day and C-3days) and low-frequency
 1149 SST feedback (C-6days, C-12days, C-18days and C-30days) under
 1150 SST sub-seasonal variability.

1151

subseasonal sets	high-frequency SST (< 6 days)			low-frequency SST (6-30 days)			
	C-CTL	C-1day	C-3days	C-6days	C-12days	C-18days	C-30days
atmosphere to ocean frequency				48/day			
ocean to atmosphere Frequency	48/day	1/1day	1/3days	1/6days	1/12days	1/18days	1/30days

1152



1153 Table 2. The average DJF temperature difference between SST and 10m depth (
 1154 $\overline{\Delta T_{0-10m}}$) and 30m depth ($\overline{\Delta T_{0-30m}}$), and the boreal winter phase mean of 20–100-
 1155 day bandpass filter with max/mini SST and oceanic 10m depth temperature (T_{10m}) in
 1156 the area of (110–130° E, 5–15° S), with observation (OISST), AGCM (A–CTL), high-
 1157 frequency experiments (C–CTL, C–1day and C–3days) and low-frequency
 1158 experiments (C–6days, C–12days, C–18days and C–30days)
 1159

		(110–130° E, 5–15° S)								
		obs.	AGCM	high-frequency			low-frequency			
experiments		OI SST ¹	A– CTL ²	C– CTL	C– 1day	C– 3days	C– 6days	C– 12days	C– 18days	C– 30days
DJF seasonal mean	SST	302.2 ±0.96	302.2 ±0.77	300.8 ±0.76	301.2 ±0.76	301.2 ±0.75	301.2 ±0.75	301.4 ±0.75	301.6 ±0.80	302.7 ±1.71
	$\overline{\Delta T_{0-10m}}$	-	-	0.1 ± 0.22	0.1 ± 0.22	0.1 ± 0.21	0.1 ± 0.23	0.2 ± 0.25	0.3 ± 0.32	1.0 ± 0.95
	$\overline{\Delta T_{0-30m}}$	-	-	0.8 ± 0.79	0.7 ± 0.70	0.6 ± 0.69	0.8 ± 0.70	0.8 ± 0.70	1.0 ± 0.73	2.1 ± 1.54
phase's mean in boreal winter	max SST (phase)	0.21 (ph2)	0.02 (ph2)	0.24 (ph3)	0.26 (ph3)	0.22 (ph3)	0.32 (ph3)	0.36 (ph3)	0.43 (ph3)	0.62 (ph2)
	max T_{10m} (phase)	-	-	0.15 (ph4)	0.17 (ph4)	0.14 (ph3)	0.19 (ph3)	0.21 (ph3)	0.26 (ph3)	0.35 (ph2)
	mini SST (phase)	-0.21 (ph7)	-0.003 (ph8)	-0.17 (ph7)	-0.22 (ph7)	-0.19 (ph7)	-0.25 (ph7)	-0.28 (ph7)	-0.38 (ph7)	-0.60 (ph6)
	mini T_{10m} (phase)	-	-	-0.11 (ph8)	-0.12 (ph7)	-0.11 (ph8)	-0.15 (ph7)	-0.17 (ph7)	-0.24 (ph7)	-0.33 (ph6)

1160 Note: ¹daily average data, ² monthly average data.



1161 Table 3. The average 20–100-day filtered outgoing longwave radiation (OLR), latent
 1162 heat flux (LHF), net surface solar radiation (FSNS), 850-hPa zonal wind (U850),
 1163 column-integrated MSE tendency (<dmdt>), column-integrated vertical MSE
 1164 advection (<wdmdp>), and column-integrated horizontal MSE advection (<vdm>)
 1165 during the boreal winter are categorized into SST warming and SST cooling states.
 1166 This categorization is performed over two domains, namely (110–130° E, 5–15° S)
 1167 and (120–150° E, 0–10° S), as mentioned in the note.

experiments	obs.	AGCM		high-frequency			low-frequency			
	ERA5/ NOAA	A– CTL	C– CTL	C– 1day	C– 3days	C– 6days	C– 12days	C– 18days	C– 30days	
SST warming	OLR ¹ (phase)	16.3 (ph1)	6.3 (ph2)	14.8 (ph2)	16.5 (ph2)	16.0 (ph2)	18.5 (ph2)	19.5 (ph1)	19.3 (ph1)	11.1 (ph8)
	LHF ¹ (phase)	-10.1 (ph3)	-11.1 (ph3)	-7.3 (ph3)	-7.3 (ph3)	-6.0 (ph2)	-8.6 (ph2)	-11.3 (ph3)	-19.3 (ph2)	-21.9 (ph1)
	FSNS ¹ (phase)	-15.7 (ph1)	-8.9 (ph2)	-15.7 (ph2)	-17.9 (ph2)	-15.9 (ph2)	-19.5 (ph2)	-18.6 (ph1)	-16.8 (ph2)	-9.5 (ph1)
	U850 ¹ (phase)	-3.0 (ph2)	-2.3 (ph3)	-3.0 (ph3)	-2.8 (ph3)	-2.3 (ph3)	-2.9 (ph3)	-2.8 (ph3)	-3.4 (ph2)	-2.2 (ph2)
	<dmdt> ² (phase)	10.7 (ph3)	9.1 (ph3)	8.2 (ph3)	8.2 (ph3)	5.6 (ph3)	7.9 (ph3)	8.1 (ph2)	7.0 (ph2)	4.1 (ph3)
	<wdmdp> ² (phase)	18.2 (ph1)	8.4 (ph2)	12.9 (ph1)	19.2 (ph1)	13.9 (ph1)	17.9 (ph1)	18.1 (ph1)	21.9 (ph1)	10.4 (ph1)
	<vdm> ² (phase)	11.5 (ph2)	5.3 (ph3)	7.9 (ph3)	7.9 (ph3)	4.4 (ph3)	8.4 (ph3)	9.0 (ph3)	9.1 (ph2)	14.0 (ph1)
	OLR ¹ (phase)	-19.2 (ph5)	-8.9 (ph6)	-11.3 (ph6)	-14.2 (ph6)	-15.0 (ph6)	-20.9 (ph5)	-20.3 (ph5)	-22.5 (ph5)	-11.0 (ph5)
	LHF ¹ (phase)	15.6 (ph6)	17.3 (ph7)	7.4 (ph7)	8.0 (ph6)	7.0 (ph6)	8.7 (ph6)	15.2 (ph6)	18.1 (ph6)	29.8 (ph6)
SST cooling	FSNS ¹ (phase)	19.7 (ph5)	10.5 (ph5)	11.6 (ph6)	16.6 (ph6)	16.1 (ph6)	21.9 (ph5)	19.1 (ph5)	21.6 (ph5)	10.4 (ph5)
	U850 ¹ (phase)	3.5 (ph6)	2.6 (ph6)	2.6 (ph7)	2.7 (ph6)	2.3 (ph7)	2.8 (ph7)	2.8 (ph6)	3.4 (ph6)	2.7 (ph6)
	<dmdt> ² (phase)	-10.6 (ph6)	-7.5 (ph7)	-9.0 (ph7)	-7.9 (ph6)	-6.0 (ph6)	-9.0 (ph6)	-8.2 (ph6)	-8.9 (ph6)	-3.8 (ph7)
	<wdmdp> ² (phase)	-23.6 (ph5)	-9.3 (ph6)	-12.6 (ph6)	-12.8 (ph6)	-15.1 (ph5)	-19.3 (ph5)	-19.5 (ph5)	-24.5 (ph5)	-16.9 (ph5)
	<vdm> ² (phase)	-12.5 (ph7)	-7.0 (ph7)	-8.6 (ph7)	-7.6 (ph7)	-5.9 (ph7)	-7.0 (ph7)	-8.5 (ph6)	-11.3 (ph6)	-17.9 (ph5)

1168 Note: ¹ domain (110–130° E, 5–15° S) refer to Table 2 and Fig. 9, and ² domain (120–
 1169 150° E, 0–10° S) refer to Fig. 11.



1170 **Figure List**

1171 **Figure 1.** Wavenumber–frequency spectra for 850-hPa zonal wind averaged over 10°
1172 S–10° N in boreal winter after removing the climatological mean seasonal cycle.
1173 Vertical dashed lines represent periods at 80 and 30 days, respectively. (a)–(i) are
1174 from ERA5 reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–
1175 18days, and C–30days, respectively.

1176

1177 **Figure 2.** Hovmöller diagrams of the correlation between the precipitation averaged
1178 over 10° S–5° N, 75–100° E and the intraseasonally filtered precipitation (color) and
1179 850-hPa zonal wind (contour) averaged over 10° N–10° S. (a)–(i) arrange in order are
1180 same as Fig. 1 from GPCP/ERA5 and all experiments.

1181

1182 **Figure 3.** Zonal wavenumber–frequency power spectra of anomalous OLR (colors)
1183 and phase lag with U850 (vectors) for the symmetric component of tropical waves,
1184 with the vertically upward vector representing a phase lag of 0° with phase lag
1185 increasing clockwise. Three dispersion straight lines with increasing slopes represent
1186 the equatorial Kelvin waves (derived from the shallow water equations)
1187 corresponding to three equivalent depths, 12, 25, and 50 m, respectively. (a)–(i)
1188 arrange in order are same as Fig. 1 from NOAA/ERA5 and all experiments.

1189

1190 **Figure 4.** Phase-longitude Hovmöller diagrams of 20–100-day filtered precipitation
1191 (mm day^{-1} , shaded) and SST anomaly (K, contour) averaged over 10° N–10° S from
1192 phase 1 to 8. Contour interval is 0.03; solid, dashed, and thick-black lines represent
1193 positive, negative, and zero values, respectively. (a)–(i) arrange in order are same as
1194 Fig. 1 from GPCP/OISST and all experiments.

1195

1196 **Figure 5.** Phase-vertical Hovmöller diagrams of 20–100-day specific humidity
1197 (shading, g kg^{-1}) and air temperature (contoured, K) averaged over 10° N–10° S, 120–
1198 150° E; solid, dashed, and thick-black curves are positive, negative, and zero values,
1199 respectively. (a)–(i) arrange in order are same as Fig. 1 from ERA5 and all
1200 experiments.

1201

1202 **Figure 6.** 15° N–15° S averaged p-vertical velocity anomaly (Pa s^{-1} , shaded) and
1203 zonal wind anomaly (m s^{-1} , contour, interval 0.5) between phase 3 and phase 4; solid,
1204 dashed, and thick-black lines represent positive, negative, and zero values,
1205 respectively.

1206



1207 **Figure 7.** The average 20–100-day filtered oceanic temperature (K, shaded and
1208 contour, interval 0.03) between 0 and 60 m depth for MJO phase 2–3. (a)–(g) are from
1209 C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, and C–30days,
1210 respectively.

1211

1212 **Figure 8.** The near-equatorial RMM1 and RMM2 variances in a bar graph based on
1213 Wheeler and Hendon (2004) with observation and reanalysis data (NOAA/ERA5),
1214 AGCM (A–CTL), high-frequency experiments (C–CTL, C–1day and C–3days) and
1215 low-frequency experiments (C–6days, C–12days, C–18days and C–30days).

1216

1217 **Figure 9.** The lead-lag relationship between MJO-related atmosphere and sub-
1218 seasonal SST variation is examined between phase 1 and 8 within the domain of 110–
1219 130° E and 5–15° S. The variables analyzed include 20–100-day filtered latent heat
1220 flux (LHF, represented by green shading), outgoing longwave radiation (OLR,
1221 represented by yellow bar chart), net surface solar radiation (FSNS, represented by
1222 orange bar chart), 850-hPa zonal wind (U850, represented by purple bar chart), 30-m
1223 depth oceanic temperature (30-m T multiplied by 100, represented by black line), and
1224 sea surface temperatures (SST multiplied by 10, represented by orange line). The
1225 graphic expression of variables denoted with (L) indicates the use of the left y-axis,
1226 while variables denoted with (R) use the right y-axis. (a)–(i) are from ERA5/OISST
1227 reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, and
1228 C–30days, respectively.

1229

1230 **Figure 10.** Phase 4 average 20–100-day filtered OLR (W m^{-2} , shaded) and 200 hPa
1231 zonal wind anomaly (m s^{-1} , vector) with the reference vector (2 m s^{-1}) shown at the
1232 top right of each panel at the top panel; latent heat flux (W m^{-2} , shaded) which
1233 positive anomaly represents upward, and 10-m wind anomaly (m s^{-1} , contour interval
1234 0.2); solid, dashed, and thick-black lines represent positive, negative, and zero values,
1235 respectively, at the second panel from the top, net surface heat flux (W m^{-2} , shaded)
1236 and net solar radiation (W m^{-2} , contour interval 3) at the third panel from the top, and
1237 SST (K, shaded) and 850 hPa zonal wind anomaly (m s^{-1} , vector) with the reference
1238 vector (1 m s^{-1}) shown at the top right of each panel at the bottom panel. The number
1239 of days used to generate the composite is shown at the bottom right corner of each
1240 panel and vertical black line of each panel indicates the dateline. (a), (d), (g) and (j)
1241 are from C–CTL; (b), (e), (h) and (k) are from C–18days, and (c), (f), (i) and (l) are
1242 from C–30days, respectively.

1243



1244 **Figure 11.** The bar chart illustrates anomalies in the average 20–100-day filtered
1245 column-integrated MSE budget terms ($\text{J kg}^{-1} \text{s}^{-1}$) across the domain (10°S – 0°N/S ,
1246 120 – 150°E) for REA5 and all model simulations. Different colors represent different
1247 datasets: green for REA5, light gray for A–CTL, red, orange and wathet blue for high-
1248 frequency experiments (C–CTL, C–1day, and C–3days), respectively, purple, blue,
1249 dark brown, and dark gray for low-frequency experiments (C–6days, C–12days, C–
1250 18days, and C–30days), respectively. The bars from left to right represent column-
1251 integrated MSE tendency ($\langle \text{dmdt} \rangle$), column-integrated vertical MSE advection ($-\langle \text{wdmdp} \rangle$),
1252 column-integrated horizontal MSE advection ($-\langle \text{vdm} \rangle$), surface latent
1253 heat fluxes (LH), surface sensible heat fluxes (SH), shortwave radiation fluxes
1254 ($\langle \text{SW} \rangle$), longwave radiation fluxes ($\langle \text{LW} \rangle$) and residual terms, respectively.
1255

1256 **Figure 12.** Phase 5 anomalies of 20–100-day filtered the column-integrated MSE
1257 tendency ($\text{J kg}^{-1} \text{s}^{-1}$, shading), precipitation (mm d^{-1} , contours interval 1.0) and 850-
1258 hPa wind (green vector) with the reference vector (2 m s^{-1}) based on (a) ERA5, (b)
1259 A–CTL, (c) C–CTL, (d) C–1day, (e) C–3days, (f) C–6days, (g) C–12days, (h)
1260 C–18days and (i) C–30days. The solid-red, dashed-blue, and thick-black curves
1261 represent positive, negative, and zero values, respectively. The vertical black line in
1262 each panel indicates the dateline.
1263

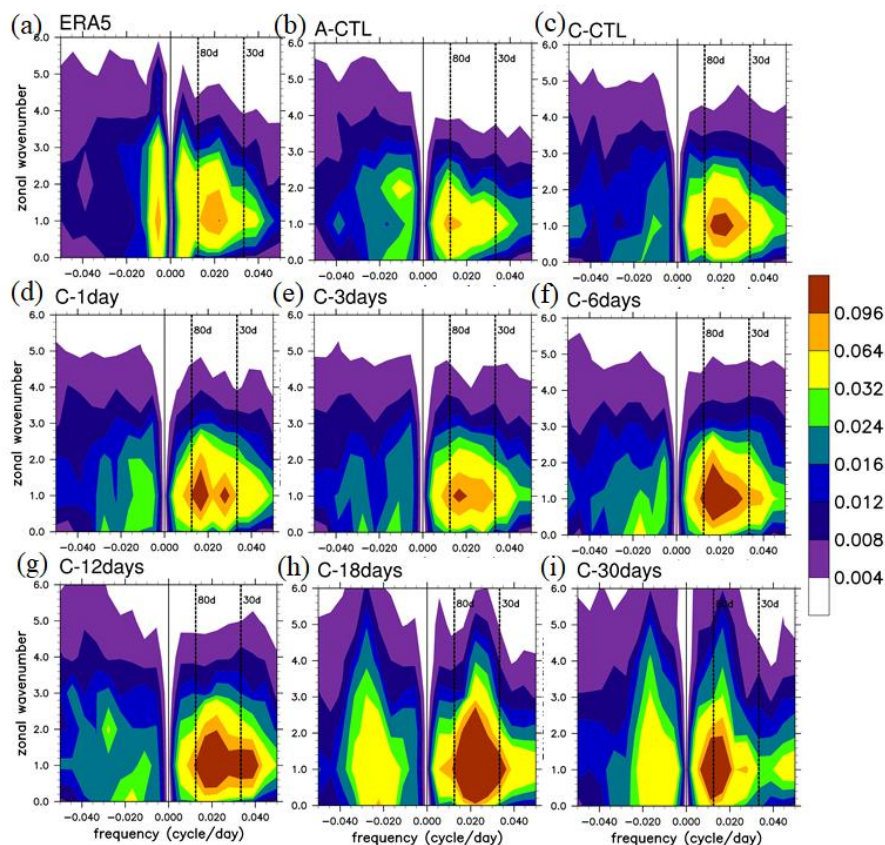
1264 **Figure 13.** (a) The relative role of each MSE component of phase 5 through the
1265 projection of the spatial pattern of each MSE budget over the MC (20°S – 20°N , 90 –
1266 210°E) onto the total MSE tendency pattern (Fig. 12a). (b–c) Decomposite of the total
1267 horizontal MSE advection based on zonal and meridional components of high-
1268 frequency SST feedback experiments (C–CTL, A–CTL, C–1day and C–3days) and
1269 low-frequency SST feedback experiments (C–6days, C–12days, C–18days and C–
1270 30days), respectively.
1271

1272 **Figure 14.** Phase 5 anomalies of 20–100-day filtered the column-integrated vertical
1273 MSE advection ($\text{J kg}^{-1} \text{s}^{-1}$, shading), column-integrated horizontal MSE advection
1274 ($\text{J kg}^{-1} \text{s}^{-1}$, contours interval 6.0) and 200-hPa wind (green vector) with the reference
1275 vector (3 m s^{-1}) based on (a) ERA5, (b) A–CTL, (c) C–CTL, (d) C–1day, (e)
1276 C–3days, (f) C–6days, (g) C–12days, (h) C–18days and (i) C–30days. The solid-blue,
1277 dashed-red, and thick-black curves represent positive, negative, and zero values,
1278 respectively. The vertical black line in each panel indicates the dateline.
1279

1280 **Figure 15.** The sketch map illustrates the equatorial circulation anomalies and
1281 moistening processes during the eastward propagation of the MJO in boreal winter for

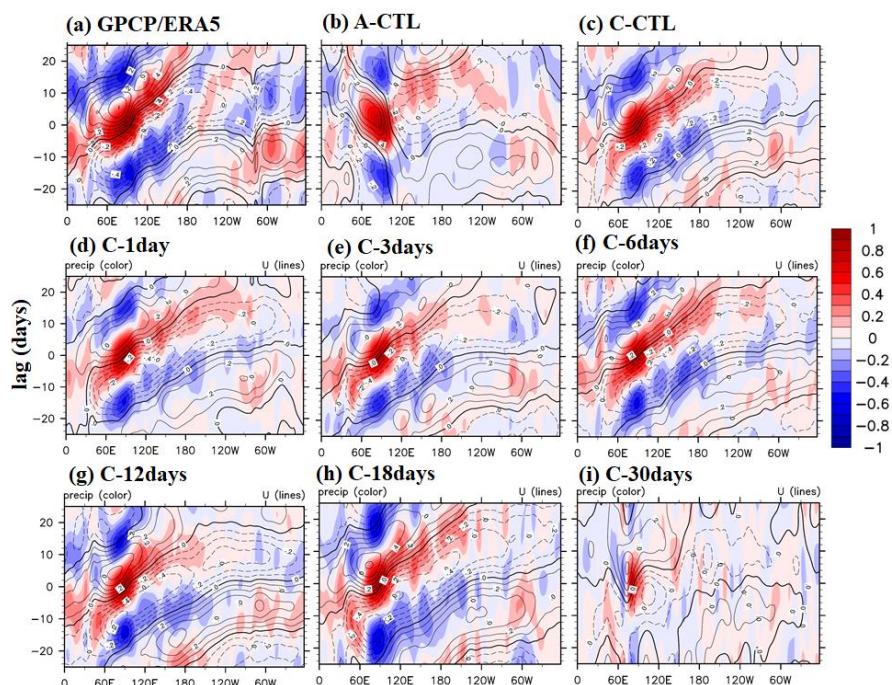


1282 various experiments: (a) uncoupled A-CTL, (b) high-frequency SST feedback
1283 experiments (C-CTL, C-1day, and C-3days), (c) low-frequency SST feedback
1284 experiments (C-6days, C-12days, and C-18days), and (d) C-30days experiment. In
1285 each panel, the horizontal line represents the equator. The clustering of gray clouds
1286 (size) indicates the strength of convective organization. A red ellipse indicates
1287 conventionally driven circulation anomalies. In the coupled simulations, light red
1288 (blue) filled ovals represent warm (cold) SST anomalies (SSTA), and a grass green
1289 filled rectangle represents latent heat flux anomalies. Unresolved convective
1290 processes are indicated by black dots representing low-level moisture. Low-level
1291 moisture convergence into the equatorial trough is shown by light blue arrows, while
1292 midlevel moisture advection is represented by left-pointing green arrows. The deeper
1293 colors or thicker lines on the map indicate stronger anomalies of the MJO factors.
1294 Note: The concept of the figure is based on DeMott et al. (2014), as depicted in Fig.
1295 11.

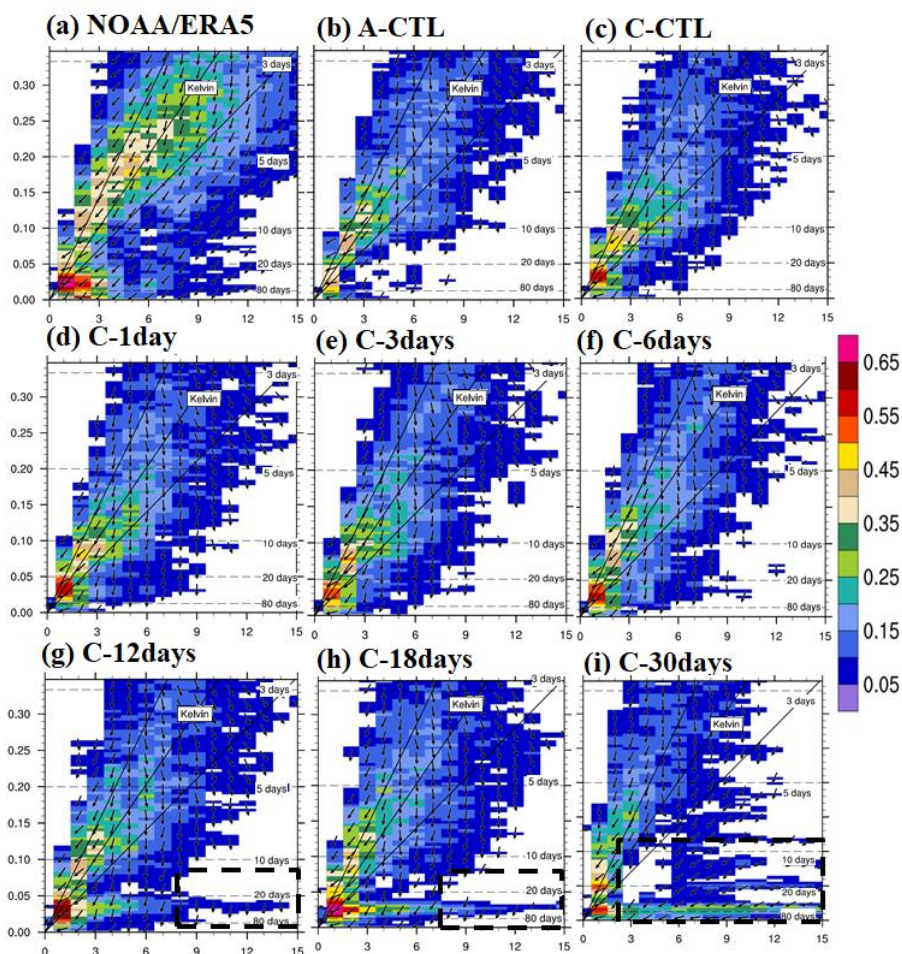


1296

1297 **Figure 1.** Wavenumber–frequency spectra for 850-hPa zonal wind averaged over 10°
1298 S–10° N in boreal winter after removing the climatological mean seasonal cycle.
1299 Vertical dashed lines represent periods at 80 and 30 days, respectively. (a)–(i) are
1300 from ERA5 reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–
1301 18days, and C–30days, respectively.

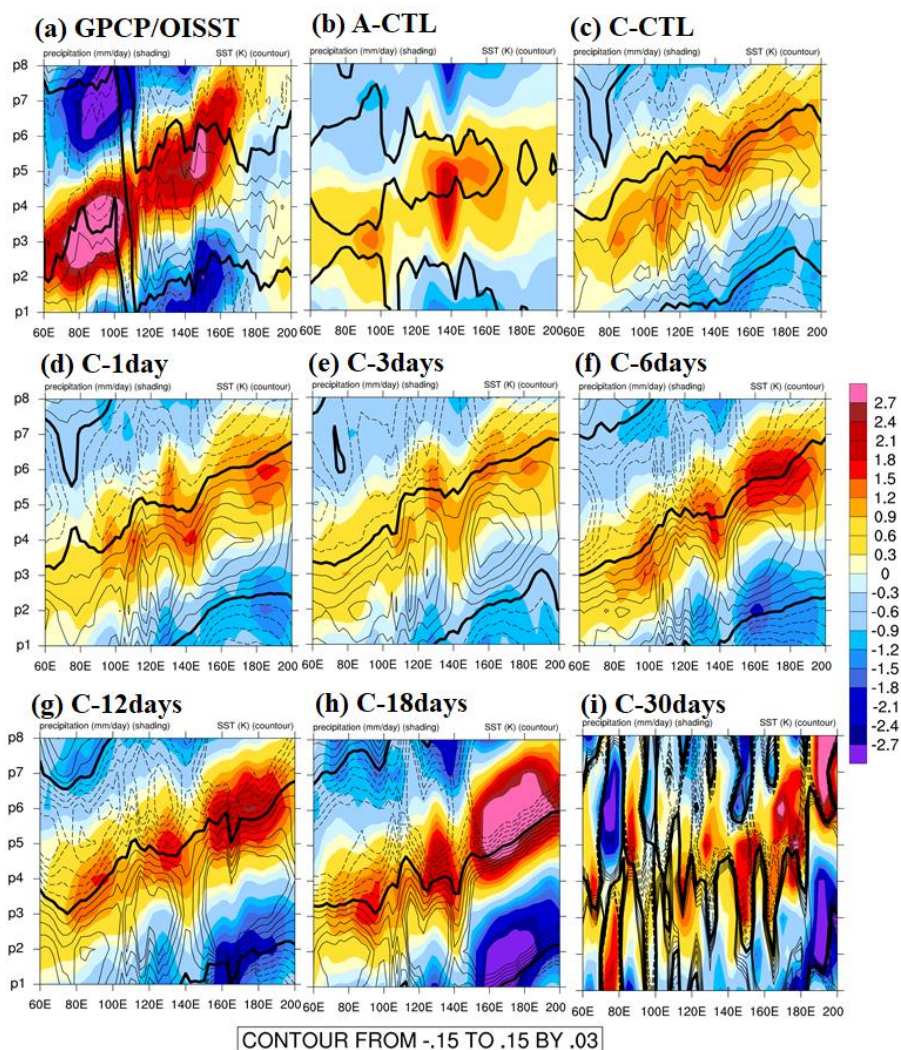


1302
1303 **Figure 2.** Hovmöller diagrams of the correlation between the precipitation averaged
1304 over 10° S– 5° N, 75° – 100° E and the intraseasonally filtered precipitation (color) and
1305 850 -hPa zonal wind (contour) averaged over 10° N– 10° S. (a)–(i) arrange in order are
1306 same as Fig. 1 from GPCP/ERA5 and all experiments.



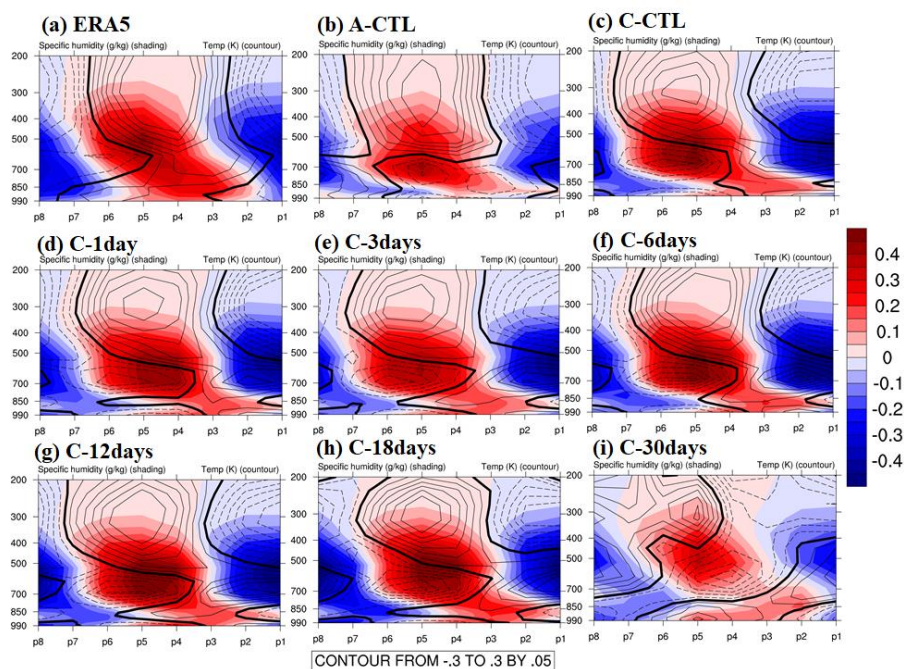
1307

1308 **Figure 3.** Zonal wavenumber–frequency power spectra of anomalous OLR (colors)
 1309 and phase lag with U850 (vectors) for the symmetric component of tropical waves,
 1310 with the vertically upward vector representing a phase lag of 0° with phase lag
 1311 increasing clockwise. Three dispersion straight lines with increasing slopes represent
 1312 the equatorial Kelvin waves (derived from the shallow water equations)
 1313 corresponding to three equivalent depths, 12, 25, and 50 m, respectively. (a)–(i)
 1314 arrange in order are same as Fig. 1 from NOAA/ERA5 and all experiments.



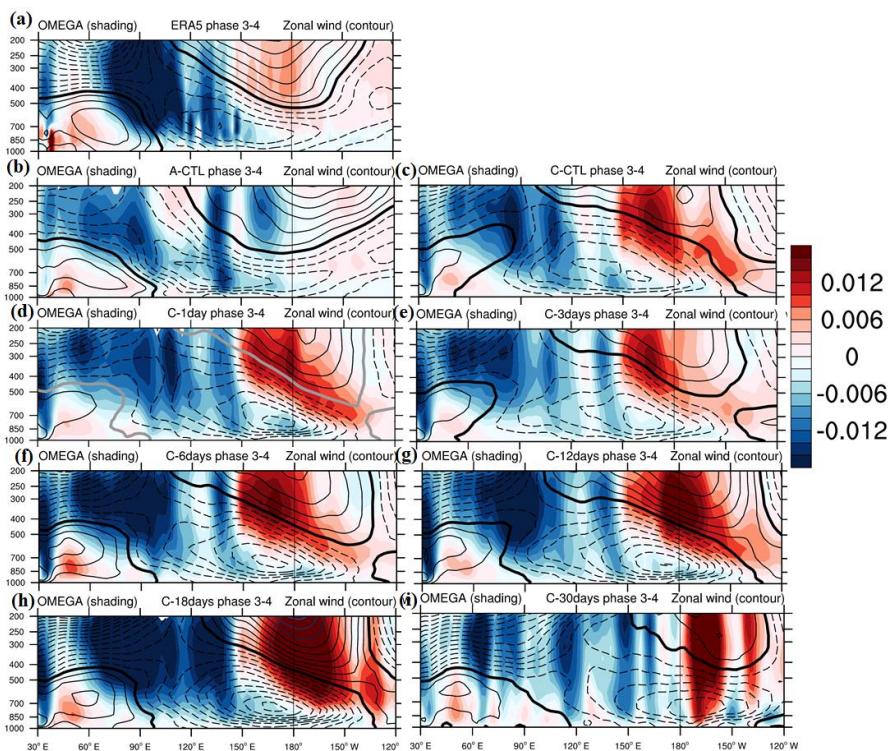
1315

1316 **Figure 4.** Phase-longitude Hovmöller diagrams of 20–100-day filtered precipitation
 1317 (mm day^{-1} , shaded) and SST anomaly (K, contour) averaged over 10°N – 10°S from
 1318 phase 1 to 8. Contour interval is 0.03; solid, dashed, and thick-black lines represent
 1319 positive, negative, and zero values, respectively. (a)–(i) arrange in order are same as
 1320 Fig. 1 from GPCP/OISST and all experiments.



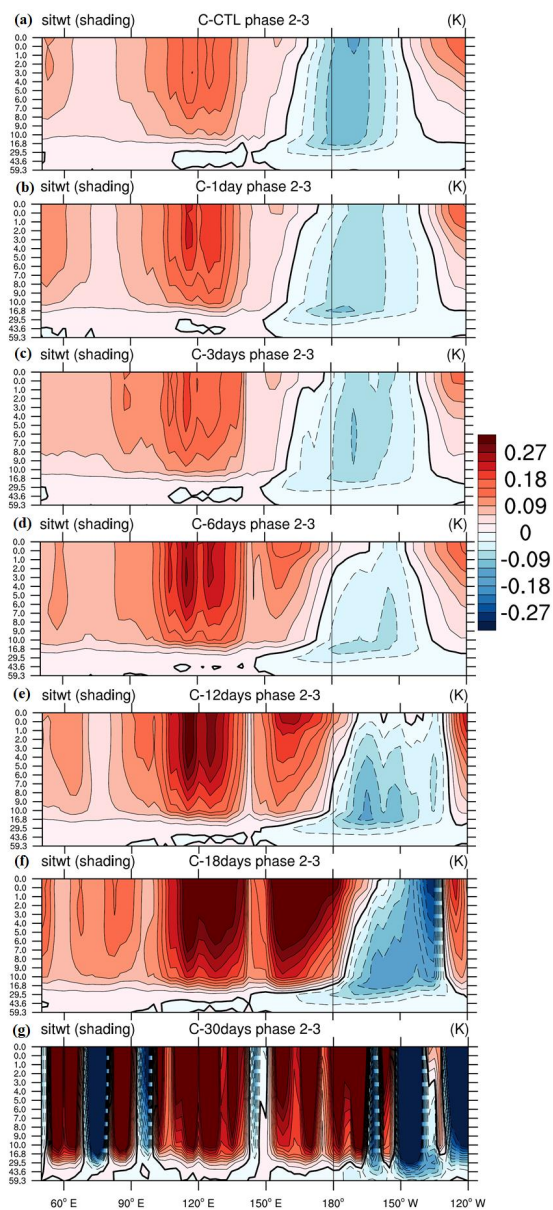
1321

1322 **Figure 5.** Phase-vertical Hovmöller diagrams of 20–100-day specific humidity
1323 (shading, g kg^{-1}) and air temperature (contoured, K) averaged over 10°N – 10°S , 120° –
1324 150°E ; solid, dashed, and thick-black curves are positive, negative, and zero values,
1325 respectively. (a)–(i) arrange in order are same as Fig. 1 from ERA5 and all
1326 experiments.



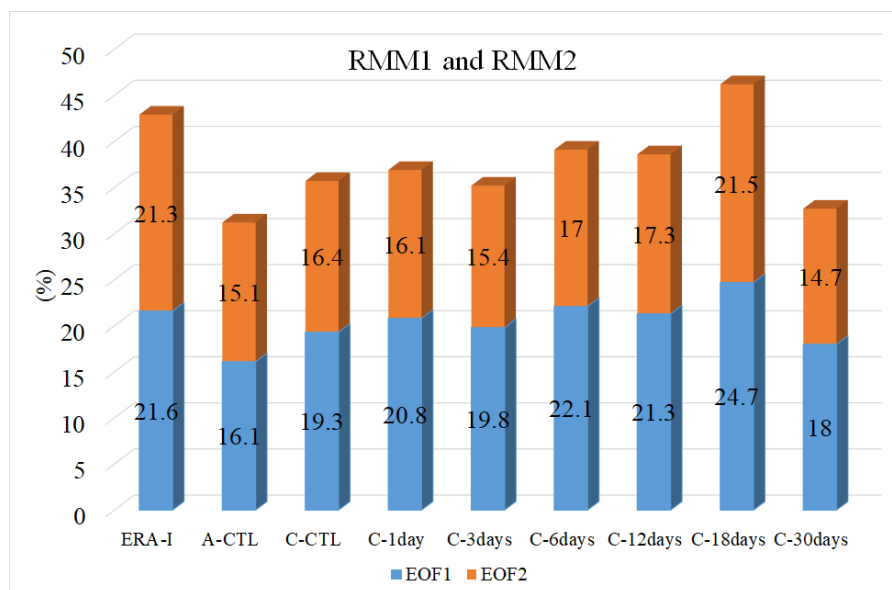
1327

1328 **Figure 6.** 15° N–15° S averaged p-vertical velocity anomaly (Pa s^{-1} , shaded) and
1329 zonal wind anomaly (m s^{-1} , contour, interval 0.5) between phase 3 and phase 4; solid,
1330 dashed, and thick-black lines represent positive, negative, and zero values,
1331 respectively.



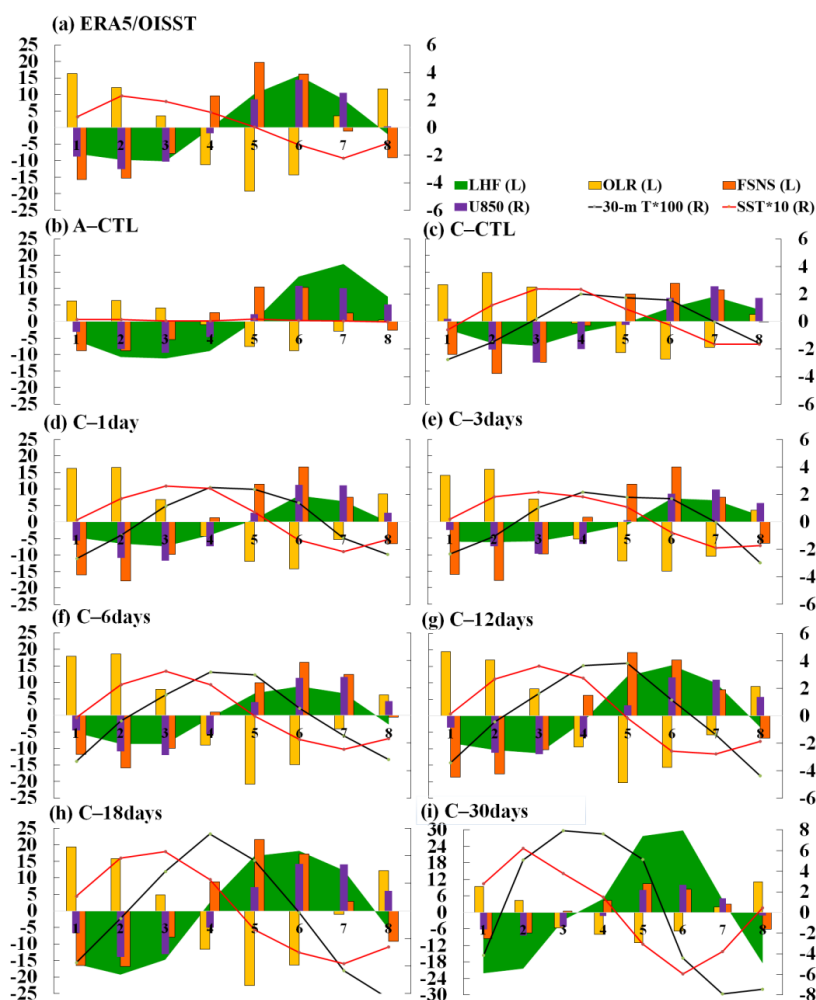
1332

1333 **Figure 7.** The average 20–100-day filtered oceanic temperature (K, shaded and
1334 contour, interval 0.03) between 0 and 60 m depth for MJO phase 2–3. (a)–(g) are from
1335 C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, and C–30days,
1336 respectively.

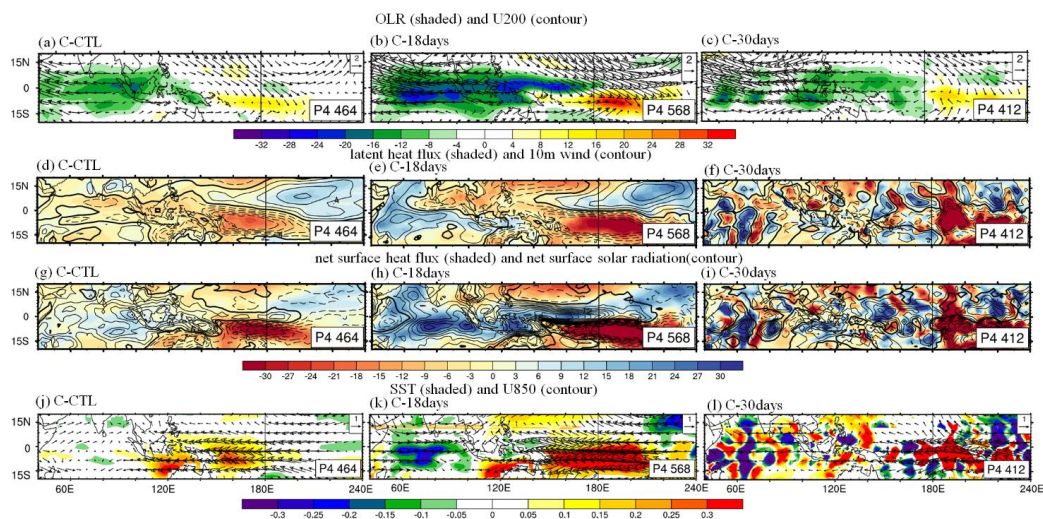


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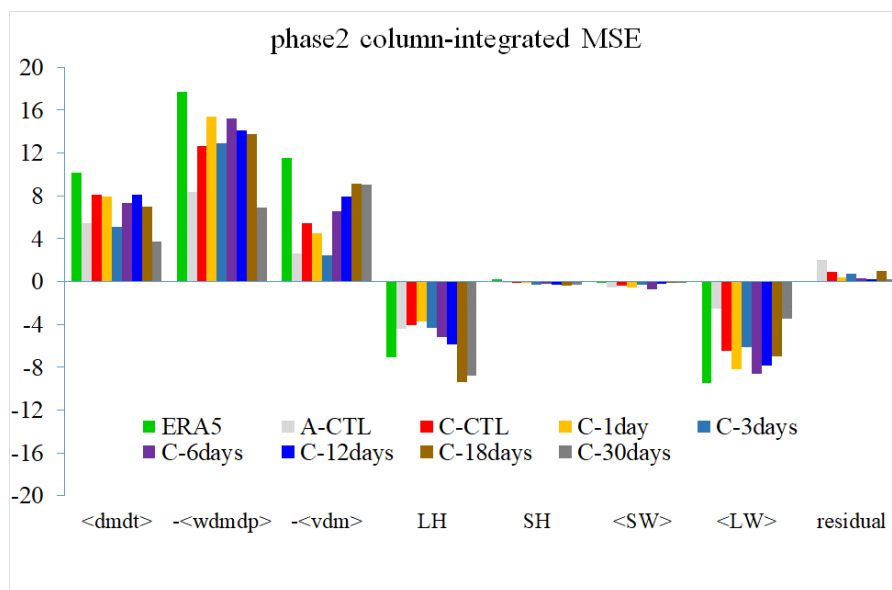
1338 **Figure 8.** The near-equatorial RMM1 and RMM2 variances in a bar graph based on
1339 Wheeler and Hendon (2004) with observation and reanalysis data (NOAA/ERA5),
1340 AGCM (A-CTL), high-frequency experiments (C-CTL, C-1day and C-3days) and
1341 low-frequency experiments (C-6days, C-12days, C-18days and C-30days).



1342
 1343 **Figure 9.** The lead-lag relationship between MJO-related atmosphere and sub-
 1344 seasonal SST variation is examined between phase 1 and 8 within the domain of 110–
 1345 130° E and 5–15° S. The variables analyzed include 20–100-day filtered latent heat
 1346 flux (LHF, represented by green shading), outgoing longwave radiation (OLR,
 1347 represented by yellow bar chart), net surface solar radiation (FSNS, represented by
 1348 orange bar chart), 850-hPa zonal wind (U850, represented by purple bar chart), 30-m
 1349 depth oceanic temperature (30-m T multiplied by 100, represented by black line), and
 1350 sea surface temperatures (SST multiplied by 10, represented by orange line). The
 1351 graphic expression of variables denoted with (L) indicates the use of the left y-axis,
 1352 while variables denoted with (R) use the right y-axis. (a)–(i) are from ERA5/OISST
 1353 reanalysis, A-CTL, C-CTL, C-1day, C-3days, C-6days, C-12days, C-18days, and
 1354 C-30days, respectively.

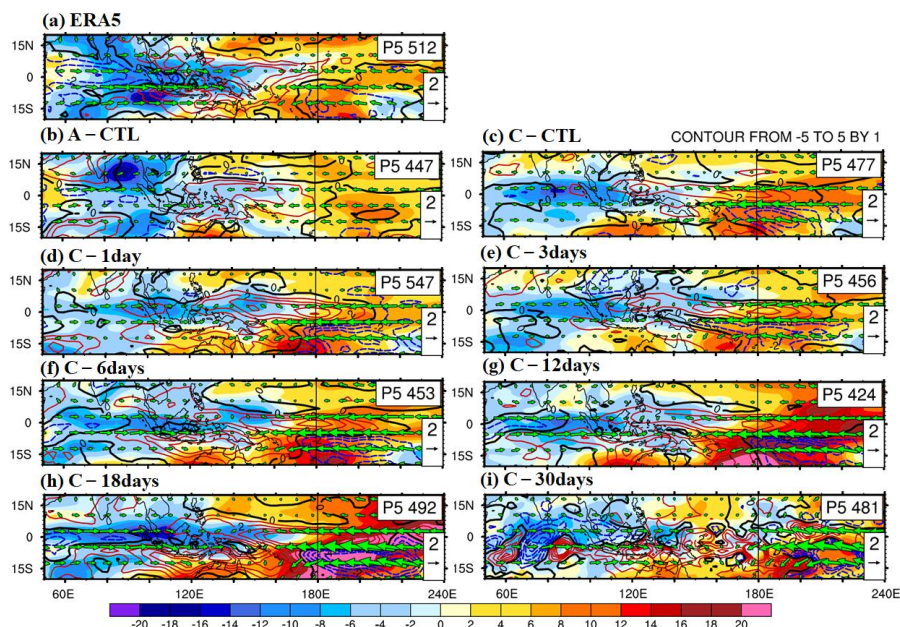


1355
 1356 **Figure 10.** Phase 4 average 20–100-day filtered OLR (W m^{-2} , shaded) and 200 hPa
 1357 zonal wind anomaly (m s^{-1} , vector) with the reference vector (2 m s^{-1}) shown at the
 1358 top right of each panel at the top panel; latent heat flux (W m^{-2} , shaded) which
 1359 positive anomaly represents upward, and 10-m wind anomaly (m s^{-1} , contour interval
 1360 0.2); solid, dashed, and thick-black lines represent positive, negative, and zero values,
 1361 respectively, at the second panel from the top, net surface heat flux (W m^{-2} , shaded)
 1362 and net solar radiation (W m^{-2} , contour interval 3) at the third panel from the top, and
 1363 SST (K, shaded) and 850 hPa zonal wind anomaly (m s^{-1} , vector) with the reference
 1364 vector (1 m s^{-1}) shown at the top right of each panel at the bottom panel. The number
 1365 of days used to generate the composite is shown at the bottom right corner of each
 1366 panel and vertical black line of each panel indicates the dateline. (a), (d), (g) and (j)
 1367 are from C-CTL; (b), (e), (h) and (k) are from C-18days, and (c), (f), (i) and (l) are
 1368 from C-30days, respectively.



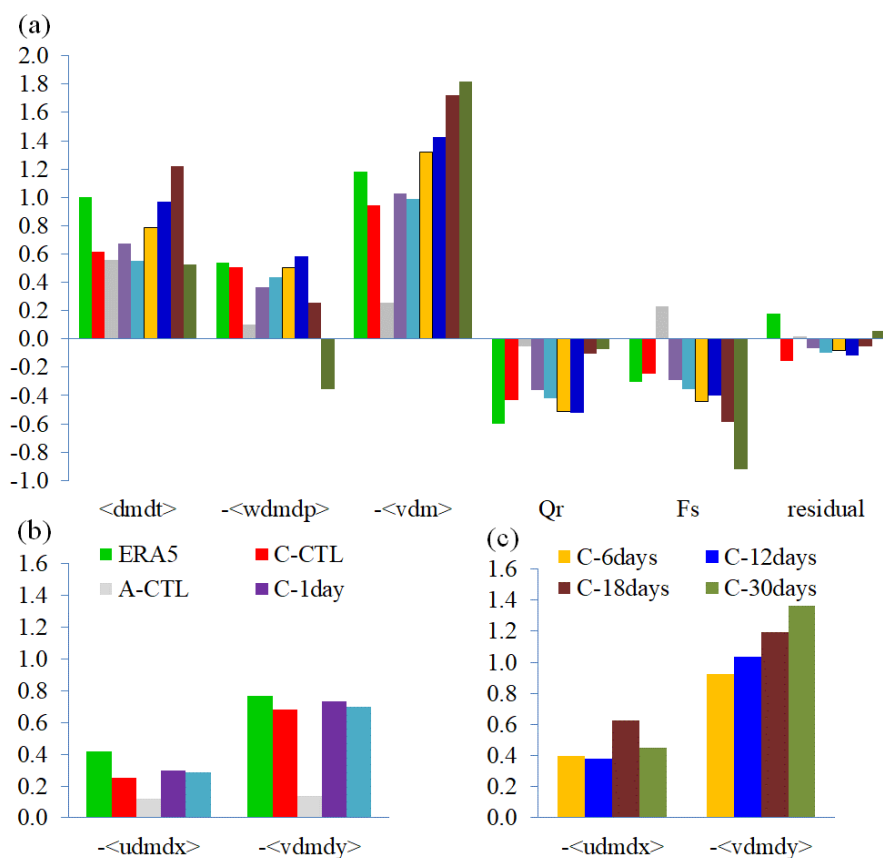
1369

1370 **Figure 11.** The bar chart illustrates anomalies in the average 20–100-day filtered
 1371 column-integrated MSE budget terms ($\text{J kg}^{-1} \text{s}^{-1}$) across the domain (10°S – 0°N/S ,
 1372 120 – 150°E) for REA5 and all model simulations. Different colors represent different
 1373 datasets: green for REA5, light gray for A–CTL, red, orange and wathet blue for high-
 1374 frequency experiments (C–CTL, C–1day, and C–3days), respectively, purple, blue,
 1375 dark brown, and dark gray for low-frequency experiments (C–6days, C–12days, C–
 1376 18days, and C–30days), respectively. The bars from left to right represent column-
 1377 integrated MSE tendency ($\langle \text{dmdt} \rangle$), column-integrated vertical MSE advection ($-\langle \text{wdmdp} \rangle$),
 1378 column-integrated horizontal MSE advection ($-\langle \text{vdm} \rangle$), surface latent
 1379 heat fluxes (LH), surface sensible heat fluxes (SH), shortwave radiation fluxes
 1380 ($\langle \text{SW} \rangle$), longwave radiation fluxes ($\langle \text{LW} \rangle$) and residual terms, respectively.

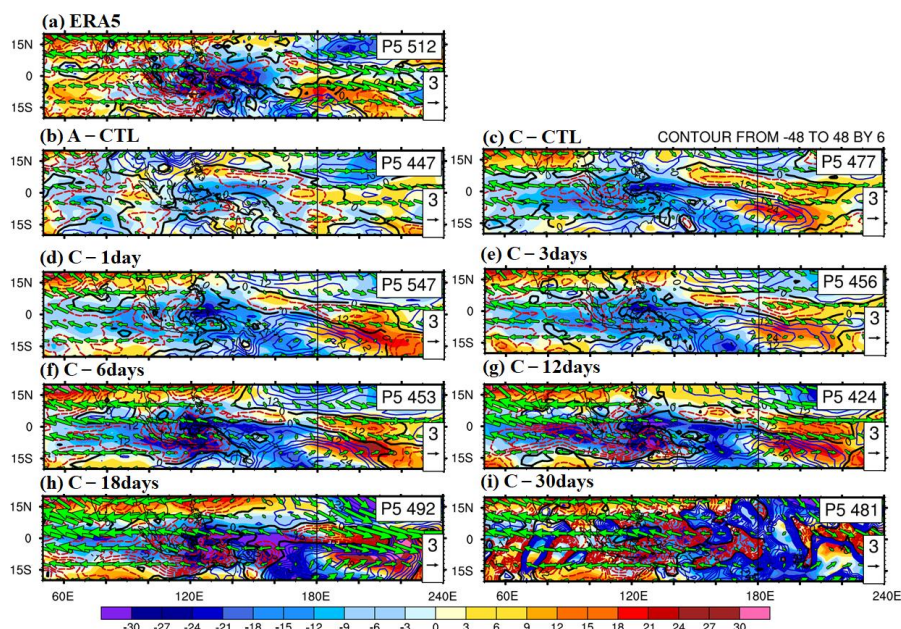


1381

1382 **Figure 12.** Phase 5 anomalies of 20–100-day filtered the column-integrated MSE
 1383 tendency ($\text{J kg}^{-1} \text{s}^{-1}$, shading), precipitation (mm d^{-1} , contours interval 1.0) and 850-
 1384 hPa wind (green vector) with the reference vector (2 m s^{-1}) based on (a) ERA5, (b)
 1385 A-CTL, (c) C-CTL, (d) C-1day, (e) C-3days, (f) C-6days, (g) C-12days, (h)
 1386 C-18days and (i) C-30days. The solid-red, dashed-blue, and thick-black curves
 1387 represent positive, negative, and zero values, respectively. The vertical black line in
 1388 each panel indicates the dateline.

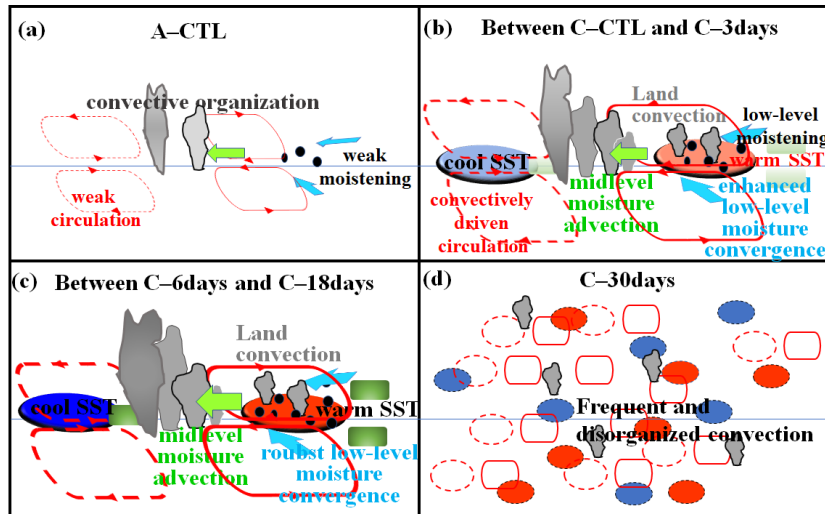


1389
 1390 **Figure 13.** (a) The relative role of each MSE component of phase 5 through the
 1391 projection of the spatial pattern of each MSE budget over the MC (20° S–20° N, 90–
 1392 210° E) onto the total MSE tendency pattern (Fig. 12a). (b–c) Decompose of the total
 1393 horizontal MSE advection based on zonal and meridional components of high-
 1394 frequency SST feedback experiments (C–CTL, A–CTL, C–1day and C–3days) and
 1395 low-frequency SST feedback experiments (C–6days, C–12days, C–18days and C–
 1396 30days), respectively.



1397

1398 **Figure 14.** Phase 5 anomalies of 20–100-day filtered the column-integrated vertical
 1399 MSE advection ($\text{J kg}^{-1} \text{s}^{-1}$, shading), column-integrated horizontal MSE advection
 1400 ($\text{J kg}^{-1} \text{s}^{-1}$, contours interval 6.0) and 200-hPa wind (green vector) with the reference
 1401 vector (3 m s^{-1}) based on (a) ERA5, (b) A-CTL, (c) C-CTL, (d) C-1day, (e)
 1402 C-3days, (f) C-6days, (g) C-12days, (h) C-18days and (i) C-30days. The solid-blue,
 1403 dashed-red, and thick-black curves represent positive, negative, and zero values,
 1404 respectively. The vertical black line in each panel indicates the dateline.



1405

1406 **Figure 15.** The sketch map illustrates the equatorial circulation anomalies and
 1407 moistening processes during the eastward propagation of the MJO in boreal winter for
 1408 various experiments: (a) uncoupled A-CTL, (b) high-frequency SST feedback
 1409 experiments (C-CTL, C-1day, and C-3days), (c) low-frequency SST feedback
 1410 experiments (C-6days, C-12days, and C-18days), and (d) C-30days experiment. In
 1411 each panel, the horizontal line represents the equator. The clustering of gray clouds
 1412 (size) indicates the strength of convective organization. A red ellipse indicates
 1413 conventionally driven circulation anomalies. In the coupled simulations, light red
 1414 (blue) filled ovals represent warm (cold) SST anomalies, and a grass green filled
 1415 rectangle represents latent heat flux anomalies. Unresolved convective processes are
 1416 indicated by black dots representing low-level moisture. Low-level moisture
 1417 convergence into the equatorial trough is shown by light blue arrows, while midlevel
 1418 moisture advection is represented by left-pointing green arrows. The deeper colors or
 1419 thicker lines on the map indicate stronger anomalies of the MJO factors. Note: The
 1420 concept of the figure is based on DeMott et al. (2014), as depicted in Fig. 11.