Quantifying the Impact of SST Feedback Frequency on the Madden-Julian Oscillation Simulations

Yung-Yao Lan[1], Huang-Hsiung Hsu[1], and Wan-Ling Tseng[2]

[1]Research Center for Environmental Changes, Academia Sinica, Taipei 11529, Taiwan

[2]Ocean Center, National Taiwan University, Taipei 10617, Taiwan

Correspondence to: Huang-Hsiung Hsu (hhhsu@gate.sinica.edu.tw)

Abstract

This study uses the CAM5 coupled to a 1-d ocean model to investigate the effects of intraseasonal SST feedback frequency on the Madden-Julian Oscillation (MJO) simulation with intervals at 30 minutes, 1, 3, 6, 12, 18, 24, and 30 days. The large-scale nature of the MJO in simulations remains intact with decreasing feedback frequency, although becoming increasingly unrealistic in both structure and amplitude, until 1/30days when the intraseasonal fluctuations are overwhelmingly dominated by unorganized small-scale perturbations in both atmosphere and ocean, as well as at the atmosphere-ocean interface where heat and energy are rigorously exchanged. The main conclusion is less frequent the SST feedback, more unrealistic the simulations. Our results suggest that spontaneous atmosphere-ocean interaction with high vertical resolution in the ocean model is the key to the realistic simulation of the MJO and should be properly implemented in climate models.

1. Introduction

The Madden–Julian Oscillation (MJO) is a large-scale tropical circulation that propagates eastward from the tropical Indian Ocean (IO) to the western Pacific (WP) with a periodicity of 30–80 days (Madden and Julian, 1972). In the Indo-Pacific region, the MJO processes involve intraseasonal variability of sea surface temperature (SST) (Chang et al., 2019; DeMott et al., 2014, 2015; Jiang et al., 2015, 2020; Krishnamurti et al., 1998; Li et al., 2014; Li et al., 2020a; Newman et al., 2009; Pei et al., 2018; Stan,

29   2018; Tseng et al., 2015). The tropical air–sea interaction, influenced by the upper ocean,

30   plays a crucial role in determining MJO characteristics due to the high heat capacity of

31   the upper ocean within the intraseasonal range, which acts as a significant heat source

32   for atmospheric variability (Watterson 2002; Sobel and Gildor 2003; Maloney and

33   Sobel 2004; Sobel et al. 2010; Liang and Du, 2022).

34   Analyzing the mechanism of the intraseasonal oscillation (ISO) reveals that heat

35   fluxes play a critical role in the development of intraseasonal SST variability (Hong et

36   al., 2017; Liang et al., 2018). As demonstrated in Fu et al. (2017), underestimation

37   (overestimation) of the air–sea coupling's impact on MJO simulations occurs when it is

38   weak (strong) in the intraseasonal SST variability. Simulation improvements in the

39   eastward propagation and regulation of MJO periodicity in the coupled models can be

40   attributed to several factors such as enhanced low-level convergence and convective

41   instability to the east of convection, as well as enhanced latent heat fluxes (Savarin and

42   Chen, 2022) and SST cooling to the west of convection (DeMott et al., 2014). SST

43   gradients have been found to induce patterns of mass convergence and divergence

44   within the marine boundary layer (MBL), initiating atmospheric convection (de Szoeke

45   and Maloney, 2020; Lambaerts et al., 2020).

46   Several recent studies have made significant progress in understanding the impact

47   of air–sea coupling on the MJO, particularly at sub-daily scales (e.g., DeMott et al.,

48   2015; Kim et al., 2018; Seo et al., 2014; Voldoire et al., 2022; Zhao and Nasuno, 2020).

49   However, there is relatively limited discussion on the effect of air–sea coupling from

50   few days to within half of the MJO period. Several studies have investigated the impact

51   of intraseasonal SST on the MJO by coupled or uncoupled models. (e.g., DeMott et al.,

52   2014; Gao et al., 2020b; Klingaman, and Demott, 2020; Pariyar et al., 2023; Stan, 2018).

53   Simulations using time-varying SSTs from coupled global climate model (CGCM) to

54   force the atmospheric general circulation model (AGCM) showed a reduced

55   intraseasonal SST variability, leading to weakened air–sea heat fluxes and eastward

56   propagation (DeMott et al., 2014; Gao et al., 2020b; Klingaman, and Demott, 2020;

57   Pariyar et al., 2023). Moreover, the absence of few days variability in SST promotes

58   the amplification of westward power associated with Rossby waves (Stan, 2018).

59   Incorporating two-way coupling between the ocean and atmosphere has been

60   proved valuable for simulating and predicting intraseasonal variability (e.g., DeMott et

61   al., 2014; Lan et al., 2022; Stan, 2018; Tseng et al., 2015, 2020). As demonstrated in

62   recent studies (e.g., Ge et al. 2017, Lan et al., 2022, Shinoda et al. 2021, and Tseng et

63   al. 2015, 2022), incorporating high vertical resolution near the ocean surface positively

64   influences the accurate representation of intraseasonal SST variability and enhances the

65   MJO prediction capabilities. However, how frequent is the coupling needed is still not

66   fully understood, considering the fact that the ocean and atmosphere could evolve in

67   distinct time scales. And, would the coupling frequency in numerical models influence

68   the accuracy of the MJO simulation?

69   In this study, we aim to investigate the specific effects of oceanic feedback

70   frequency (FF) through air–sea coupling on the atmospheric intraseasonal variability,

71   using the National Center for Atmospheric Research (NCAR) Community Atmosphere

72   Model 5.3 (CAM5.3) coupled with the single-column ocean model named Snow–Ice–

73   Thermocline (SIT). The coupled model is referred to as CAM5–SIT. The SIT model,

74   consisting of 41 vertical layers, enables the simulation of SST and upper-ocean

75   temperature variations with high vertical resolution (Lan et al., 2022). We have

76   demonstrated in previous studies that coupling the SIT significantly improved the MJO

77   simulations in several AGCMs (Tseng et al. 2015, 2022, Lan et al. 2022). The ability of

78   the SIT with extremely high-resolutions (i.e., 12 layers within the first 10.5 m) to well

79   resolve the upper ocean warm layer and the cool skin of the ocean surface was identified

80   as the main reason for the improved simulations.

81   The structure of this paper is organized as follows. Section 2 introduces the model,

82   data, methodology, and experiments employed in this study. The performance of the

83   CAM5–SIT models in simulating the MJO is discussed in Section 3, while Section 4

84   focuses on the impact of different configurations of sub-seasonal SST feedback

85   periodicity on MJO simulations. Finally, Section 5 presents the conclusions.

86

87   **2. Data, model experiments, and methodology**

88   **2.1 Observational data**

89   Observational data sets used in this study include precipitation from the Global

90   Precipitation Climatology Project (GPCP, 1° resolution, 1997–2010; Adler et al., 2003),

91   outgoing longwave radiation (OLR, 1° resolution, 1997–2010; Liebmann, 1996), and

92   daily SST (optimum interpolated SST, OISST, 0.25° resolution, 1989–2010; Banzon et

93   al., 2014) from the National Oceanic and Atmosphere Administration, and the fifth

94   generation ECMWF reanalysis (ERA5), with a resolution of 0.25° for the period of

95   1989–2020 (Hersbach and Dee, 2016). Various variables from ERA5 were considered,

96   including winds, vertical velocity, temperature, specific humidity, sea level pressure,

97   geopotential height, latent and sensible heat, and shortwave and longwave radiation.

98   For the initial conditions of the SIT, the SST data was obtained from the Hadley Centre

99   Sea Ice and Sea Surface Temperature dataset version 1 (HadISST1), with a resolution

100   of 1° for the period of 1982–2001 (Rayner et al., 2003). The ocean subsurface data,

101   including climatological ocean temperature, salinity, and currents in 40 layers, were

102   retrieved from the National Centers for Environmental Prediction (NCEP) Global

103   Ocean Data Assimilation System (GODAS) with a resolution of 0.5° for the period of

104   1980–2012 (Behringer and Xue, 2004). These data were used for a weak nudging

105   (Tseng et al. 2015 2022; Lan et al. 2022) in the SIT model.

106

2.2 Experimental design

In this study, we investigated the role of oceanic FF using coupled CAM5–SIT and atmosphere-only CAM5 (A–CTL). Previous studies (Lan et al., 2022; Tseng et al., 2022) have provided a detailed description of the every timestep coupling CAM5–SIT model and its performance in simulating the MJO. Table 1 displays the experimental configuration, incorporating monthly HadISST1 (uncoupled region) and ice concentrations over a 30-year period centered around the year 2000 (F2000 compsets, Rasch et al., 2019). Solar insolation, greenhouse gas and ozone concentrations, and aerosol emissions representative of present-day conditions were prescribed. In the A–CTL, observed monthly-mean SST around the year 2000 was prescribed to force the CAM5. For the coupled simulations, we adjusted the Flux Coupler (CPL) restriction in the Climate Earth System Model (CESM1; Hurrell et al., 2013) by implementing asymmetric exchange frequencies between the atmosphere and the ocean. The ocean continuously receives atmospheric forcing at every time step (30 minutes) and the temperature changes accordingly, but the SST seen by the atmospheric model is fixed at each timestep for a specified time span (e.g., 1, 3, 6, 12, 18, 24, and 30 days). That is, the SST seen by the atmospheric model only changed until the end of the specified time span.

Two sets of experiments in addition to the A–CTL were conducted, each representing a different SST feedback frequency:

(1) High-frequency SST feedback set: This set includes the control experiment (C–CTL) with SST feedback at every timestep (FF as 48/day), once a day (C–1day: FF as 1/day), and every 3 days (C–3days: FF as 1/3days).

(2) Low-frequency SST feedback set: This set includes experiments with SST feedback to the atmosphere for every 6 days (C–6days: FF as 1/6days), 12 days (C–12days: FF as 1/12days), 18 days (C–18days: FF as 1/18days), 24 days (C–

5

133   24days: FF as 1/24days), and 30 days (C–30days: FF as 1/30days).

134   The SIT is coupled to CAM5 between 30° N to 30° S. The ocean was weakly

135   nudged (using a 30-day exponential time scale) between depths of 10.5 m and 107.8 m,

136   and strongly nudged (using a 1-day exponential time scale) below 107.8 m, based on

137   the climatological ocean temperature data from NCEP GODAS. No nudging was

138   applied in the upper-most 10.5 meters, allowing the simulation of rigorous air–sea

139   coupling near the ocean surface.

140   During the simulation, the SIT recalculated the SST within the tropical air–sea

141   coupling region. Outside this coupling region, the annual cycle of HadSST1 was

142   prescribed. No SST transition between the tropical air–sea coupling zone and the

143   extratropical SST-prescribed regions was applied. The ocean bathymetry for the SIT

144   was derived from the NOAA's 1 arc-minute global relief model of Earth's surface that

145   integrated land topography and ocean bathymetry (ETOPO1) data (Amante and Eakins,

146   2009). To ensure consistency and comparability, all observational, atmospheric, oceanic,

147   and reanalysis data were interpolated into a horizontal resolution of 1.9° × 2.5° for

148   model initialization, nudging, and comparison of experimental simulations.

149

150   **2.3 Methodology**

151   The analysis focused on the boreal winter period (November–April), the season

152   with the most pronounced eastward propagation of the MJO. To identify intraseasonal

153   variability, the CLIVAR MJO Working Group diagnostics package (CLIVAR, 2009)

154   and a 20–100-day filter (Wang et al., 2014) was used. MJO phases were defined based

155   on the Real-time Multivariate MJO series 1 (RMM1) and series 2 (RMM2) proposed

156   by Wheeler and Hendon (2004), which utilized the first two principal components of

157   combined near-equatorial OLR and zonal winds at 850 and 200 hPa. The band-pass

158   filtered data were used to calculate the index and define the MJO phases.

159   Analysis of column-integrated MSE budgets was conducted to investigate the

160 association between tropical convection and large-scale circulations. The column-

161 integrated MSE budget equation (e.g., Sobel et al., 2014) is approximately given by

162 $$\langle\frac{\partial h}{\partial t}\rangle' = -\langle u\frac{\partial h}{\partial x}\rangle' - \langle v\frac{\partial h}{\partial y}\rangle' - \langle w\frac{\partial h}{\partial p}\rangle' + \langle LW\rangle' + \langle SW\rangle' + \langle SH\rangle' + \langle LH\rangle' \qquad (1)$$

163 where h denotes the moist static energy

164 $$h = c_pT + gz + L_vq \qquad\qquad\qquad\qquad (2)$$

165 where T is temperature (K); q is specific humidity (Kg Kg^{-1}); c_p is dry air heat capacity

166 at constant pressure (1004 J K^{-1} kg^{-1}); L_v is latent heat of condensation (taken constant

167 at 2.5×10^6 J kg^{-1}); u and v are horizontal and meridional wind (m s^{-1}), respectively; ω

168 is the vertical pressure velocity (Pa s^{-1}); LW and SW are the longwave and shortwave

169 radiation flux (W m^{-2}), respectively; and LH and SH are the latent and sensible surface

170 heat flux (W m^{-2}), respectively. The angle bracket ($\langle * \rangle$) represents mass-weighted

171 vertical integration from 1000 to 100 hPa; and the intraseasonal anomalies are

172 represented as $\langle * \rangle'$.

173

174 **3.   Results**

175 **3.1 The mean state and intraseasonal variability of SST**

176   The variability of SSTs plays a crucial role in the dynamics of the MJO. Studies

177 based on observations from TOGA COARE and DYNAMO revealed that MJO events

178 exhibited a stronger ocean temperature response compared to average conditions (de

179 Szoeke et al., 2014). Wu et al. (2021) revealed the better MJO prediction skill in the

180 CGCM could be contributed by the improved representation of high-frequency SST

181 fluctuations related to the MJO, with warm (cold) SST anomalies to the east (west) of

182 MJO convection, through the convection–SST feedback processes (Li et al., 2020a; Wu

183 et al., 2021). It is therefore necessary to check on the influences of coupling and coupling

184 frequency on the SST fluctuations.

185   Table 2 presents the oceanic temperature anomalies for the DJF seasonal mean,

186   including the differences in oceanic temperature between the SST and depths of 10m

187   ($\overline{\Delta T}_{0-10m}$) and 30m ($\overline{\Delta T}_{0-30m}$), as well as 20–100 days maximum and minimum SST

188   and oceanic temperature at 10m depth (T_{10m}). The region of 110–130° E and 5–15° S

189   was selected because of the largest variation in the 20–100-day bandpass-filtered SST

190   when the MJO passes over the Indo-Pacific region. Simulated DJF seasonal mean SST

191   (300.8K to 302.0 K) are generally smaller than OISST (302.2 K) but increase with the

192   lower SST feedback frequency except in C–30days (302.7 K), while the SST standard

193   deviation remains within 0.8 K, smaller than OISST (0.96 K), except in C–24days (1.06

194   K) and C–30days (1.71 K).

195   The simulated subsurface (0–10m and 0–30m) ocean temperatures were compared

196   with those in the NCEP GODAS reanalysis and presented as ($\overline{\Delta T}_{0-10m}$ and $\overline{\Delta T}_{0-30m}$).

197   The $\overline{\Delta T}_{0-10m}$ in high-frequency experiments maintained 0.1 K temperature difference.

198   In low-frequency experiments, $\overline{\Delta T}_{0-10m}$ increased from 0.2 to 1.0 K with decreasing

199   SST feedback frequency. The temperature difference ($\overline{\Delta T}_{0-30m}$) in both high-frequency

200   and low-frequency experiments remains approximately 0.8K, except for C–24days and

201   C–30days with an increase as high as 1.4 K and 2.1 K, respectively. The comparison

202   revealed the cooling effect of the SIT on the seasonal mean SST, especially in the higher-

203   frequency coupling experiment due to the more rigorous heat exchanges between ocean

204   and atmosphere. However, in the lower frequency experiments, the SST became much

205   warmer and so did vertical temperature differences due likely to the unrealistically large

206   heat accumulation of loss in the ocean.

207   As for the MJO simulation, the SST fluctuation is more relevant. The OISST

208   fluctuation through a MJO cycle was about ± 0.21 K. In comparison, the uncoupled A–

209   CTL, which was forced by monthly mean HadISST1, yielded a negligible SST

210   fluctuation (-0.003–0.02 K) as expected. In the high-frequency experiments, SST

211 fluctuated in magnitudes similar to that in the daily OISST. The amplitude became

212 unrealistically larger in the low-frequency coupling experiments with C–30days

213 reaching as high as 0.6 K. The increasingly larger amplitudes were likely resulted from

214 the heat accumulation in the ocean because of less frequent feedback (or heat release) to

215 the model atmosphere. Changes in coupling frequency led to different amplitudes of SST

216 fluctuation in a MJO cycle. As will be revealed latter, this effect had marked influence

217 on the MJO simulations.

218

219 **3.2 MJO simulation: high-frequency and low-frequency SST feedback experiments**
220 **3.2.1 General structure**

221   The propagation characteristics of the different experiments were analyzed using

222 the wavenumber-frequency spectrum (W-FS). The spectra of unfiltered U850 in ERA5,

223 A–CTL, and all coupling experiments with different feedback frequency are shown in

224 Fig. 1a–j. The C–CTL experiment accurately captures the eastward propagating signals

225 at zone wavenumber 1 with 30–80-day period (Fig. 1a and 1c), although with a slightly

226 larger amplitude than ERA5 (Fig. 1a). By contrast, the uncoupled A–CTL produced an

227 unrealistic spectral shift to time scales longer than 30–80 days (Fig. 1b) and simulated

228 the unrealistic westward propagation at wavenumber 2.

229   The W-FS spectra of the C–1day and C–3day experiment show two peaks for zone

230 wavenumber 1 over the 30 to 80-day period. The low-frequency experiments (i.e., from

231 C–6days to C–30days) increasingly enhanced the amplitudes and lowered the

232 frequency of intraseasonal perturbations with decreasing feedback frequency.

233 Furthermore, unrealistic westward W-FS of U850 becomes evident in (Fig. 1h–i) in the

234 C–18days, C–24days, and C–30days experiments, reflecting the stationary nature of

235 simulated MJO.

236   The Hovmöller diagrams in Fig. 2a–j depict the evolution of 10° N–10° S averaged

237   precipitation and U850 anomalies on intraseasonal timescales, represented by the

238   lagged correlation coefficients with the precipitation averaged over 10° S–5° N, 75–

239   100° E. In GPCP/ERA5, observed precipitation and U850 propagated eastward from

240   the eastern IO to the dateline, with precipitation leading U850 by approximately a

241   quarter of a cycle and a propagation speed of about 5 m s^{-1} (Fig. 2a). The A–CTL

242   simulation was dominated by stationary features, with westward-propagating tendency

243   over the IO and weak and slow eastward propagation over the MC and WP (Fig. 2b).

244   The Hovmöller diagrams derived from high-frequency and low-frequency experiments

245   (Fig. 2c–h) display the key eastward propagation characteristics in both precipitation

246   and U850, as well as the phase relationship between them, except in C–24days and C–

247   30days that were dominated by stationary perturbations. Further decreased feedback

248   frequency from 1/C–24days to 1/C–30days also further weakened the signals of

249   precipitation and U850. More detailed discussion on this topic will be presented in the

250   subsequent chapter.

251   We conducted a wavenumber-frequency power spectral analysis (Wheeler and

252   Kiladis 1999) to examine the phase lag and coherence between the tropical circulation

253   and convection. Figures 3a–i illustrate the symmetric part of OLR and U850 for

254   NOAA/ERA5 data and all model experiments. The MJO band exhibits a high degree

255   of coherence, indicating a strong correlation between NOAA MJO-related OLR signal

256   and wavenumbers 1–3 (Fig. 3a). The phase lag in the 30–80-day band is approximately

257   90°, consistent with previous studies (Ren et al., 2019; Wheeler and Kiladis 1999). All

258   model experiments simulated the coherence within wavenumber 3 in the MJO band,

259   with a phase lag similar to NOAA/ERA5 data. However, the A–CTL spectrum exhibits

260   only half of the observed coherence peak at wavenumber 1, and also weaker coherence

261   at wavenumbers 2–3 for the 30–80-day period compared to NOAA/ERA5 data. The

262   experiments C–CTL, C–1day, C–3days, C–6days, C–12days, and C–18days yielded

263   wavenumber-1 coherence peak similar to that in NOAA/ERA5. Additionally, as the

264   SST feedback frequency decreases from 1/12days to 1/30days, the experiments

265   increasingly simulated unrealistic coherence in the very low frequency with a wide

266   range of zonal wavenumber from 1 to 12 (Fig. 3g–j), i.e., no zonal scale preference.

267   Figure 4 shows the phase–longitude diagrams in which the 20–100-day filtered

268   precipitation (shaded) and SST (contour) anomalies were averaged over 10° S to 10° N

269   to determine the relationship between precipitation and SST fluctuations and to provide

270   insights into the connection between air–sea coupling and convection. As expected, the

271   A–CTL did not simulate the eastward-propagating coupled SST-convection

272   perturbations as in observation (Fig. 4a), whereas C–CTL, C–1day, and C–3days

273   properly reproduced the observed features. The eastward-propagating coupled

274   perturbations were also simulated in C–6days, C–12days, and C–18days, but with

275   unrealistically increasing amplitudes near the dateline, especially in the C–18days

276   experiment. The perturbation amplification near the dateline was likely due to the lack

277   of ocean circulation in the CAM5–SIT. The amplification was also seen in C–24days

278   that failed to simulate the eastward-propagating intraseasonal perturbations. When

279   coupling frequency was reduced to 1/30days, the eastward propagation could no longer

280   be simulated and was replaced by unorganized standing oscillations in much smaller

281   zonal scales.

282   Liang et al. (2018) suggested that SST leading precipitation by 10 days implies

283   air–sea interactions at the intraseasonal timescale during MJO events, with SST playing

284   a crucial role in modulating the MJO's intensity and propagation. The A–CTL

285   simulation exhibited weak SST anomalies and stationary precipitation when using the

286   monthly average HadISST1. By contrast, the C–24days and C–30days experiment

287   showed no clear phase lag between SST and precipitation perturbations. A comparison

288 between simulation results and observation indicates that the air–sea interaction plays

289 a crucial role in facilitating eastward propagation and higher frequency feedback yields

290 more realistic simulations.

291

3.2.2 Vertical structures of the MJO in the atmosphere

293   Air–sea interaction plays a significant role in influencing atmospheric moisture and

294 convection associated with the MJO (Savarin and Chen, 2022). Whereas the ocean to

295 the east of deep convection warmed due to more downwelling shortwave radiation and

296 less heat fluxes into the atmosphere associated with weaker winds, near-surface

297 moisture convergence under the anomalous subsidence over the warmer water

298 preconditioned the eastward movement of the deep convection (DeMott et al., 2015;

299 Zhang, 2005). The MJO was noted to detour southward when crossing the MC region,

300 exhibiting enhanced convective activity preferentially in the southern MC area and

301 weaker convection in the central MC area (Hsu and Lee 2005, Wu and Hsu 2009, and

302 Kim et al. 2017). Hovmöller diagrams in Fig. 5a–j illustrate the relationship between

303 the vertical structure of air temperature (contoured, in K) and specific humidity

304 (shading, in g kg^{-1}) anomalies from the surface to 200 hPa averaged over 5–20° S and

305 120–150° E. In ERA5, the lower-level positive temperature anomaly in phase 3 (i.e.,

306 preconditioning phase) leads the development of deep temperature and moisture

307 anomalies (i.e., deep convection) after phase 4 over the MC, when moisture anomalies

308 reached the maxima at 700–500 hPa. This two-phase upward development was not

309 properly simulated in A–CTL, which shows sudden switch between positive and

310 negative anomalies in the entire troposphere, instead of progressively upward

311 development with time. The upward development was generally simulated in coupled

312 simulations from C–CTL to C–6days (Fig. 5c–e), although the negative temperature

313 anomalies below 500 hPa were over-simulated after phase 5. It became less well

314 simulated beyond C−12days and was gradually replaced by sudden phase switch as in

315 the A-CTL, especially in C−30days (Fig. 5f–j). The preconditioning phase completely

316 disappears in C–18 days and beyond. As identified in previous studies, the two-phase

317 upward development is a manifestation of air–sea coupling. The missing of this

318 coupling evidently resulted in the poor simulation in the A-CTL and extremely low

319 feedback frequency experiments.

320

321 **3.2.3 Vertical structures of the MJO in the ocean**

322 The 1-D turbulence kinetic energy (TKE) ocean model incorporates a high vertical

323 resolution that captures the vertical gradient of temperature in the upper ocean. Figure

324 6 (left column) illustrates the vertical structures of oceanic temperature between 0- and

325 60-meters during phase 2–3 when the deep convection occurred over the eastern IO

326 (60–90° E) and easterly anomalies prevailed over the MC and western Pacific. In the

327 high-frequency experiments (Fig. 6a, 6c, 6e), the upper oceanic temperatures exhibit

328 warming patterns within 30 meters depth at 100–140° E (i.e., east of the deep

329 convection and under the easterly anomalies), apparently due to more downwelling

330 short wave radiation and less heat flux release to the atmosphere. By contrast, the

331 cooling near the dateline was associated with westerly anomalies. With decreasing

332 feedback frequency, the cooling to the east of 150°E seen in high frequency experiments

333 was replaced by oceanic warming that amplified with further feedback frequency

334 decrease. The warming region that became more widespread and larger amplitude with

335 less frequent feedback eventually grew to cover the entire IO and WP, an area much

336 larger than the scale of the atmospheric MJO. The mismatch between the atmospheric

337 and oceanic anomalies suggested the weakening atmospheric-ocean coupling that

338 resulted in poor simulation of the MJO in the low frequency feedback simulations. The

339 emergence of small-scale unorganized structures with decreasing feedback frequency

340   is also evident in phase 4-5 (right column of Fig. 6), e.g., negative ocean temperature

341   anomalies in the Indian Ocean under the prevailing westerly anomalies.

342

343   **4. Discussion**

344   **4.1 Dynamic lead–lag relationship in intraseasonal variability**

345   The lead–lag relationship refers to a situation where one variable (leading) is

346   cross-correlated with the values of another variable (lagging) in subsequent phases,

347   particularly in the case of SST fluctuations and MJO-related atmospheric variations

348   between phase 1 and 8 within the domain of 110–130° E and 5–15° S (Fig. 7). The

349   analyzed variables include 20–100-day filtered latent heat flux (LHF, indicated by green

350   shading), OLR (indicated by a yellow bar chart), net surface solar radiation (FSNS,

351   indicated by an orange bar chart), U850 (indicated by a purple bar chart), 30-meter

352   depth oceanic temperature (30-m T multiplied by 100, indicated by a black line), and

353   SST (multiplied by 10, indicated by an orange line). Positive value in LHF and FSNS

354   represents an upward flux from ocean to atmosphere.

355   Decrease in LHF, which indicates a reduction in heat loss from the ocean, and

356   negative FSNS, indicating that solar radiation is heating the ocean, coincide with

357   easterly anomaly that contributes to positive SST anomaly in ERA5 (Fig. 7a). Reversed

358   fluxes are associated with westerly anomalies. This lead–lag relationship depicts the in-

359   situ atmospheric forcing on the oceanic variability during a MJO. As the MJO

360   convection progresses through the region (110–130° E and 5–15° S), several changes

361   in atmospheric and oceanic variables occur. These changes include a shift in OLR from

362   positive to negative values, a decrease in SST, a transition to westerly winds, and an

363   increase in positive FSNS and LHF (Fig. 7a). The temporal variations in SST anomaly

364   from C–CTL to C–12days were predominantly influenced by FSNS, with LHF playing

365   a secondary role, similar to the findings of Gao et al. (2020a). With the exception of

14

366 experiments of A–CTL, C–24days, and C–30days, both the high-frequency and low-

367 frequency SST feedback experiments simulated similar lead–lag relationships as in

368 ERA5 (Fig. 7c–h). In the C–24days and C–30days experiments, LHF was the largest

369 flux term (note the different vertical scale for the two experiments) whereas the wind,

370 OLR, and FSNS anomalies were much weaker than in other experiments. In the A–CTL

371 experiment, which was forced by monthly HasISST1 data, the SST anomalies were

372 small as expected, whereas fluxes although weak are still evident in response to

373 atmospheric perturbations (Fig. 7b). Conversely, in both C–24days and C–30days

374 experiments, a misalignment in the lead–lag relationship was observed, accompanied

375 by weak anomalies in OLR and FSNS. (Fig. 7i and 7j). This disparity between LHF and

376 wind was likely due to the unrealistically widespread and large oceanic warming as

377 shown in Fig. 6m and 6o.

378　　In the simulations, the maximum positive anomaly in 30-m T was delayed by one

379 phase compared to SST, indicating the transfer of heat from the ocean surface into the

380 upper ocean progressively. Similarly, the occurrence of the most negative 30-m T

381 anomaly was also delayed by one phase compared to SST, revealing the buffering role

382 of the upper ocean when the atmospheric component of the MJO extracted (or deposited)

383 heat (energy) from (in) the ocean (Fig. 7c–i). This delayed effect was also evident in

384 the field campaign. de Szoeke et al. (2015) observed that the warmest 10-m ocean

385 temperature occurred a few days later than the peak temperature at 0.1 m. Additionally,

386 the 0.1-m ocean temperature was typically as warm as or warmer than the 10-m

387 temperature as seen in Fig. 6. In the extreme low frequency feedback experiments, the

388 amplitude of 30-m temperature became unrealistically large due likely to the continuous

389 accumulation or loss of the ocean heat.

390

391 **4.2 Unorganized perturbations in extreme frequency feedback scenarios**

392   DeMott et al. (2014) noted that in uncoupled experiments, the NCAR CAM

393   superparameterized version 3 (SPCAM3) exhibited strong eastward propagation when

394   5-day running mean SST was prescribed, but relatively weaker propagation for monthly

395   mean SST. This raises the question of how much SST feedback periodicity is necessary

396   to maintain robust eastward propagation in coupled experiments. This tendency was

397   also seen in our study, that is, slower propagation (or weaker tendency) with decreased

398   feedback frequency until the C–24days experiment (Figs. 1–7). By 1/30days, the

399   perturbations became stationary.

400   Generally, C–18days exhibited the unrealistic overestimation of intraseasonal

401   variability while maintaining eastward propagation of the MJO. Here, we are not

402   suggesting that C–18days represents the optimal SST feedback experiment. Figure 8

403   highlights the considerable differences in the simulation of MJO perturbations at phase

404   2–3 in C–18days and C–30days experiments. In C–18days, negative OLR anomalies

405   were widespread from the western Indian Ocean to the MC, while in reality it should

406   be observed mainly in the Indian Ocean and be accompanied by positive anomalies in

407   the eastern MC, i.e., a west-east dipolar structure (Fig. 8a). In C–30days, the OLR

408   anomaly, although was still the dominant feature in the Indian Ocean-western Pacific

409   region, became much weaker and characterized by smaller scale perturbations. These

410   OLR anomalies were generally associated with upper-level convergence (not shown)

411   embedded in much weaker wind anomalies (U200) compared to those in C–18days.

412   The circulation and OLR in C–24days exhibited the characteristics similar to those in

413   C–18days but with the OLR anomalies breaking up into smaller scales.

414   Furthermore, in the C–18days and C–24days experiments, positive anomalies in

415   LHF and net surface heat flux (Fig. 8d, 8e, 8g, and 8h) were predominantly observed

416   in the convection-inactive region to the east of 150°E where low-level easterly wind

417   and negative SST anomalies prevailed (Fig. 8j). The OLR, winds, heat fluxes, and SST

418   to the west of 150°E exhibited similar correspondences between variables but in

419   opposite phase. With feedback frequency reduced to 1/30days (Fig. 8f, 8i, and 8l), the

420   heat fluxes and SST anomalies broke into unorganized smaller scaler features,

421   consistent with the ocean temperature shown in Fig. 6h. Although the wind fields in the

422   both upper and lower levels were still characterized by large-scale structure, the

423   corresponding divergence were dominated by much smaller scale perturbations (not

424   shown), similar to heat fluxes and SST. The increasingly dominant smaller scale

425   perturbations can also be inferred from Fig. 2h-j and 4h-j. In addition, the large power

426   spectra in the low frequency band spread across a wide range of wavenumbers,

427   reflecting the smaller scale nature of the simulated perturbations in C−30days (Fig. 3h-

428   j). This imparity between the scale of rotational and divergent winds suggests that the

429   poor coupling between the convection and large-scale circulation.

430   With decreased feedback frequency of SST from C–CTL to C–30days, the ocean

431   continued to receive atmospheric forcing, but the feedback response was delayed,

432   leading to the accumulation or loss of energy (temperature) in the upper ocean, as seen

433   in the SST distribution in the WP (Fig. 6 and 8). Subsequently, the C–30days

434   experiment exhibited comprehensive disorder over the Indo-Pacific region, with the

435   SST exhibiting a perturbed unrealistically spatial distribution (Fig. 8l) associated with

436   plus-minus latent heat flux and 10m wind anomalies (Fig. 8f), net surface heat flux, and

437   solar radiation (Fig. 8i). As a result, the organized large-scale circulation seen in the

438   MJO was not manifested. To this extreme, the air−sea interaction observed in the MJO

439   no longer worked properly in the model.

440

441   **4.3 Moist static energy (MSE) budget analysis**

442   We diagnosed the relative contribution of each term in Eq. (1) to the MSE tendency

443   with a focus on the second (pre-conditioning) and fifth (convection crossing the MC)

444　　phases. Figure 9 illustrates the physical processes associated with each term (averaged

445　　over 10° S–0°, 120–150° E) contributing to the column-integrated MSE tendency

446　　(<dmdt>) in Eq. (1) during phase 2 in ERA5 and model simulations. In ERA5, when

447　　the MJO convection was in the eastern Indian Ocean, the column-integrated vertical

448　　and horizontal advection (-<wdmdp> and -<vdm>) over the MC area were the dominant

449　　terms in the MSE budget and largely compensated by longwave radiation and latent

450　　heat flux, as reported in Wang and Li (2020) and Tseng et al. (2022). All experiments

451　　simulated the positive and negative contributions similar to those derived from ERA5

452　　although with different amplitudes. Notably, the C–24days and C–30days simulated

453　　relatively weak vertical advection and too strong negative latent heat flux and too weak

454　　longwave radiation flux. As a result, the C–24days and C–30days simulated relatively

455　　weak tendency compared to other experiments. The results are consistent with the poor

456　　simulation of the MJO in the extreme low frequency feedback experiments discussed

457　　above.

458　　　　We compared the spatial distribution of column-integrated MSE tendency <dmdt>

459　　(shading), precipitation (contours), and 850-hPa wind (vectors) during phase 5, i.e., the

460　　period when the strongest convection crossing the MC (Fig. 10). In ERA5, the main

461　　convection (indicated by positive precipitation anomaly) is accompanied by low-level

462　　convergence in the 850-hPa wind across the MC extending into the WP (Fig. 10a). A

463　　positive <dmdt> is observed to the east of the MJO convection to the south of the

464　　equator (Fig. 10a). Conversely, a negative tendency is observed to the west of the MJO

465　　convection accompanied by negative precipitation anomalies further to the west. The

466　　phase relationship between the MSE tendency and precipitation reflects the eastward-

467　　propagating nature of the MJO. With the exception of A–CTL, C–24days, and C–

468　　30days, the model simulations displayed a similar structure in the 20–100-day filtered

469　　<dmdt>, precipitation, and 850-hPa wind vectors (Fig. 10c–h). although the exact

470   locations may be shifted compared to those derived from ERA5. The C–CTL simulated

471   relatively weak signals compared to ERA5, whereas the signals became increasingly

472   stronger with decreasing feedback frequency. The signals became unrealistically strong

473   beyond 1/18days feedback frequency and the lead–lag relationship between the MSE

474   tendency and precipitation became less clear. For example, positive precipitation

475   anomaly became in phase with the tendency in the western Pacific south of the equator

476   in C–24days and C–30days experiments, and the tendency was much weaker in C–

477   30days. The results were consistent with the weaker eastward propagation tendency in

478   the low-frequency feedback experiments, especially in C−24days and C−30days when

479   the feedback frequency became unrealistically low.

480   The corresponding MSE budget during phase 5 is shown in Fig. 10. The MC

481   has been identified as a barrier to the eastward propagation of the MJO (Hsu and Lee,

482   2005, Wu and Hsu 2009, Tseng et al. 2017, Li et al., 2020b) and approximately 30–50%

483   of the MJO experienced stalling over the MC (Zhang and Han, 2020). To determine

484   whether the MJO has sufficient energy to traverse the MC, we focused the analysis on

485   phase 5. Figure 11 illustrates the projection of each MSE component and decomposition

486   of the horizontal MSE advection at phase 5 over the MC region (20° S–20° N, 90–

487   210° E) following the approach of Tseng et al. (2022) and Jiang et al. (2018), where

488   F_s is total surface fluxes including SH and LH, and Q_r is vertically integrated net SW

489   and LW radiation. Unlike in phase 2 when vertical advection is the dominant term, the

490   MSE tendency was dominated by the horizontal MSE advection -<vdm> in ERA5 and

491   all experiments, except the A−CTL. This contribution increased with decreasing SST

492   feedback frequency. The weaker positive vertical advection -<wdmdp> did not vary

493   systematically with decreasing feedback frequency and even turned negative in C−

494   24days and C−30days. Fs and Qr acted to damp the tendency by cancelling out the

495   effect of the advection term. Fs tended to be more negative with decreasing feedback

496   frequency and became much larger in C–30days. By contrast, Qr was unrealistically

497   weak in C–18days, C–24days, and C–30days. The uncoupled simulation yielded much

498   weaker amplitude in all terms as expected.

499   The -<vdm> that contributed most to the eastward propagation of the MJO in

500   phase 5 was further decomposed into zonal (-<udmdx>) and meridional (-<vdmdy>)

501   components to examine their relative effects (Fig. 11). Both components contributed

502   positively, but the -<vdmdy> exhibited a larger amplitude, consistent with Tseng et al.

503   (2014, 2022). The -<vdmdy> of high-frequency SST feedback experiments yielded

504   results closely similar to ERA5. Comparatively, the -<vdmdy> term in low-frequency

505   SST feedback experiments (C–18days, C–24days, and C–30days) became

506   unrealistically large with decreasing feedback frequency.

507   Spatial distributions of -<wdmdp>, -<vdm>, and 200-hPa wind at phase 5 are

508   shown in Fig. 12. In ERA5, the wind divergence at 200 hPa at phase 5 (Fig. 12a),

509   overlaid the 850-hPa convergence (Fig. 10a), reflecting a deep convection structure.

510   The model simulations exhibited a similar structure to ERA5 except in A–CTL, C–

511   24days, and C–30days experiments, and again the amplitude increased with decreasing

512   feedback frequency. In ERA5, negative -<wdmdp> and -<vdm> anomalies (Fig. 12a)

513   were observed to the west of the MJO convection (Fig. 10a). The spatial distribution of

514   the negative -<vdm> anomaly (dashed-red contours) extends from the IO to the MC

515   and positive anomaly (predominantly meridional advection from the south, not shown)

516   in the western-central Pacific south of the equator tends to facilitate the eastward

517   propagation of deep convection in the western Pacific, consistent with Tseng et al.

518   (2014, 2022). The -<wdmdp> with negative and positive anomaly to the west and east

519   of the deep convection also contributes to the eastward propagation of the MJO, but

520   with weaker contribution than -<vdm>. Again, these characteristics were not simulated

521   in A-CTL, whereas the amplitudes of both terms became increasingly larger with

522   decreasing feedback frequency until becoming unrealistically large beyond 1/18days.

523   In C–30days experiment both terms exhibited unorganized spatial structure as shown

524   in preceding discussion. In summary, the high-frequency feedback experiments

525   simulated an approximately 80% projection of -<vdm> in ERA5, whereas the low-

526   frequency SST feedback experiments overestimated -<vdm> anomalies (Fig. 12f–h).

527

528   **5. Conclusions**

529   This study built upon the work of Lan et al. (2022) and Tseng et al. (2022) by

530   coupling a high-resolution 1-D TKE ocean model (the SIT model) with the CAM5, i.e.,

531   a CAM5–SIT configuration, to investigate the effects of intraseasonal SST feedback on

532   the MJO. We introduced asymmetric exchange frequencies between the atmosphere and

533   the ocean, ensuring bidirectional interaction at each timestep within the experimental

534   periodicity by fixing the SST value in the coupler. This allowed us to create SST

535   feedback with various intervals at 30 minutes, 1, 3, 6, 12, 18, 24, and 30 days.

536   The aim is to assess the effect of SST feedback frequency, namely, how often

537   should the atmosphere-driven SST change feedback to the atmosphere and whether

538   there is a limit. With the exception of the C–24days and C–30days experiment, both the

539   high-frequency and low-frequency experiments demonstrated realistic simulations of

540   various aspects of the MJO when compared to ERA5, GPCP, and OISST data, although

541   the simulation results becoming increasingly amplified and unrealistic with decreasing

542   feedback frequency. These aspects included intraseasonal periodicity (Fig. 1), eastward

543   propagation (Fig. 2 and 4), coherence in the intraseasonal band (Fig. 3), tilting vertical

544   structure (Fig. 5), intraseasonal SST (Table 2) and oceanic temperature variances (Fig.

545   6), the lead–lag relationship of intraseasonal variability (Fig. 7), contribution of each

546   term to the column-integrated MSE tendency at the preconditioning phase (phase 2)

547   and mature phased (phase 5) (Fig. 9 and Fig. 11). The MSE tendency term was

548   dominated by the horizonal and vertical MSE advection in phase 5 and phase 2,

549   respectively, in ERA5 and most experiments. Furthermore, we deliberately extended

550   the SST feedback interval to an unrealistically long 30 days to investigate the limits of

551   delayed ocean response. The main conclusion is less frequent the update, more

552   unrealistic the simulation result.

553   The lead–lag relationship provides a visual representation of the variations in 20–

554   100-day filtered LHF, FSNS, OLR, U850 and SST with positive SST anomaly leading

555   the onset of the MJO convection (Fig. 7). This relationship highlights the

556   interconnected nature of surface heat fluxes, solar radiation, and atmospheric

557   circulation patterns, underscoring their mutual influence and interplay through air–sea

558   interaction. Our results indicate that the high-frequency (low-frequency) SST

559   experiments tended to underestimate (overestimate) the MJO simulation in CAM5–SIT

560   model. Whether this finding can be applied to other models warrants further

561   investigations.

562   The result of C–3days experiment is consistent with Stan (2018), suggesting the

563   absence of 1–5-day variability in SST would promote the amplification of westward

564   power associated with tropical Rossby waves. By comparing with the control

565   experiment in which SST feedback occurs at every time step (30 minutes), the C–1day

566   experiment (SST feedback once daily) confirmed the findings of Hagos et al. (2016)

567   and Lan et al. (2022) that the removal of the diurnal cycle would enhance the MJO. The

568   increasing feedback periodicity of SST in low-frequency experiments led to the

569   accumulation of atmospheric influences through short-wave and long-wave radiations

570   and surface heat fluxes, resulting in an unrealistically large ocean temperature

571   anomalies and variances within few tens of meters below ocean surface (Table 2). The

572   large-scale nature of the MJO remains intact with decreasing feedback frequency,

573   although becoming increasingly unrealistic in both structure and amplitude, until

574   1/30days when the intraseasonal fluctuations were overwhelmingly dominated by

575   unorganized small scale perturbations in both atmosphere and ocean, as well as at the

576   atmosphere-ocean interface where heat and energy were rigorously exchanged.

577   The reason causing the sudden change between C−24days and C−30days is not

578   entirely clear. Two possibilities are discussed here. The first possible reason leading to

579   this disorder is that when the ocean feedback is delayed for as long as 30 days (more

580   than half of the MJO period) both positive and negative fluxes would contribute to the

581   heat accumulation or loss in the ocean because of the MJO phase transition and result

582   in unorganized small scale structures in ocean temperatures, which could in turn affect

583   the heat flux and convection. The second would be the SST change become more abrupt

584   and disrupt the large-scale nature of the MJO. However, whether large-amplitude SST

585   fluctuations would induce unorganized small-scale pertrubation is debatable. As seen

586   in many hypothetic (or theoretical) studies, a sudden initiation of SST (or step-function

587   like) could induce large scale responses. This issue remains an open question that

588   warrants further studies with purposedly designed expeirment to untangle.

589   Finally, results of intraseasonal SST feedback experiments on MJO are

590   summarized schematically in Fig. 13, following DeMott et al. (2014). These

591   experiments included the uncoupled experiment (A–CTL), high-frequency SST

592   experiments (C–CTL, C–1day, and C–3days), low-frequency SST experiments (C–

593   6days, C–12days, C–18days), and extreme low-frequency experiment (C–24days and

594   C–30days). In the absence of intraseasonal SST variability, the eastward propagation of

595   the MJO was disrupted, leading to weakened or fragmented MJO activity as shown in

596   Fig. 13a. On the other hand, the high-frequency SST experiments closely mimicked

597   air–sea interaction and well captured the characteristics of the MJO. The time-varying

598   SSTs in the coupled simulation provided a certain degree of organization and sufficient

599   surface fluxes, which facilitated the development of the MJO circulation as illustrated

600   in Fig. 13b. The horizontal moist static energy tendency derived from increased low-

601   level convergence, especially due to the meridional advection of MSE, intensified the

602   MJO convection and triggered the eastward propagation over the MC region. The PBL

603   convergence ahead of the MJO convection is due to Kelvin-wave dynamics (Jiang,

604   2017), in conjunction with the background zonal flow structure (Tulich and Kiladis,

605   2021). Horizontal MSE or moisture advection in the lower troposphere, particularly the

606   seasonal mean low-level MSE influenced by the MJO's anomalous winds, has had a

607   significant impact on the MJO propagation. (Gonzalez and Jiang, 2017; Jiang, 2017).

608   This simulation result is consistent with the understanding that the MJO is primarily

609   attributed to the interaction between organized convection and large-scale circulations

610   that triggers the eastward propagation. As feedback frequency become lower, the major

611   characteristics of the MJO could still be simulated as depicted in Fig. 13c, but with

612   overestimated amplitudes and deteriorating simulations in spatial structures. In the

613   extreme low frequency experiments with frequency decreasing to 1/24days and

614   1/30days, unorganized structures started to emerge and broke up into smaller scale

615   perturbations as shown in Fig. 13d, when proper air–sea interaction did not operate

616   properly in the model. Eventually in the C–30days experiment, unrealistically and

617   spatially scattered anomalies in precipitation, SST, surface heat fluxes, and vertical and

618   horizontal MSE advection became dominant features. All these findings led to the

619   major conclusion of this study: spontaneous atmosphere-ocean interaction with high

620   resolution ocean model is a key to the proper simulation of the MJO in the climate

621   models.

622

623   *Code and data availability.* The model code of CAM5–SIT is available at

624   https://doi.org/10.5281/zenodo.5510795. Input data of CAM5–SIT using the

625   climatological Hadley Centre Sea Ice and Sea Surface Temperature dataset and

626 GODAS data forcing, including 30-year numerical experiments, are available at

627 https://doi.org/10.5281/zenodo.5510795.

628

632

634

645

646 **Reference**

647 Adler, R. F., Huffman, G. J., Chang, A., Ferraro, R., Xie, P.
648   P., Janowiak, J., Rudolf, B., Schneider, U., Curtis, S., Bolvin,
649   D., Gruber, A., Susskind, J., Arkin, P., and Nelkini, E.: The Version
650   2.1 Global Precipitation Climatology Project (GPCP) Monthly
651   Precipitation Analysis (1979 -Present), J. Hydrometeor., 4(6), 1147-
652   1167,   https://doi.org/10.1175/1525-
653   7541(2003)004<1147:TVGPCP>2.0.CO;2, 2003.

654 Amante, C., and Eakins, B. W.: ETOPO1 1 arc-minute globe relief model:
655   Procedures, data sources and analysis, NOAA Tech. Memo. NESDIS

NGDC-24, NOAA, Silver Spring, MD, 19 pp., https://doi.org/10.7289/V5C8276M, 2009.

Banzon, V. F., Reynolds, R. W., Stokes, D., and Xue, Y.: A 1/4-spatial-resolution daily sea surface temperature climatology based on a blended satellite and in situ analysis, J. Climate, 27, 8221–8228, https://doi.org/10.1175/JCLI-D-14-00293.1, 2014.

Behringer, D. W., and Xue, Y.: Evaluation of the global ocean data assimilation system at NCEP: The Pacific Ocean. Eighth Symposium on Integrated Observing and Assimilation Systems for Atmosphere, Oceans, and Land Surface, AMS 84th Annual Meeting, Washington State Convention and Trade Center, Seattle, Washington, 11-15. Derber, J.C., and A. Rosati, 1989: A global oceanic data assimilation system, J. Phys. Oceanogr., 19, 1333–1347, https://ams.confex.com/ams/pdfpapers/70720.pdf, 2004.

Chang, M.-Y., Li, T., Lin, P.-L., and Chang, T.-H.: Forecasts of MJO Events during DYNAMO with a Coupled Atmosphere-Ocean Model: Sensitivity to Cumulus Parameterization Scheme, J. Meteorol. Res., 33, 1016–1030, https://doi.org/10.1007/s13351-019-9062-5, 2019.

CLIVAR MADDEN–JULIAN OSCILLATION WORKING GROUP: MJO simulation diagnostics, J. Climate, 22, 3006–3030, https://doi.org/10.1175/2008JCLI2731.1, 2009.

DeMott, C. A., Klingaman, N. P., and Woolnough, S. J.: Atmosphere-ocean coupled processes in the Madden-Julian oscillation, Rev. of Geophysics, 53, 1099– 1154, https://doi.org/10.1002/2014RG000478, 2015.

DeMott, C. A., Stan, C., Randall, D. A., and Branson, M. D.: Intraseasonal variability in coupled GCMs: The roles of ocean feedbacks and model physics, J. Climate, 27(13), 4970– 4995. https://doi.org/10.1175/JCLI-D-13-00760.1., 2014.

de Szoeke, S. P., Edson, J. B., Marion, J. R., Fairall, C. W., and Bariteau, L.: The MJO and air–sea interaction in TOGA COARE and DYNAMO, J. Climate, 28(2), 597– 622. https://doi.org/10.1175/JCLI-D-14-00477.1, 2014.

de Szoeke, S. P., Edson, J. B., Marion, J. R., Fairall, C. W., and Bariteau, L.: The MJO and air–sea interaction in TOGA COARE and DYNAMO, J. Climate, 28, 597–622, https://doi.org/10.1175/JCLI-D-14-00477.1, 2015.

de Szoeke, S. P., and Maloney, E.: Atmospheric mixed layer convergence from observed MJO sea surface temperature anomalies, J. Climate, 33(2), 547– 558. https://doi.org/10.1175/JCLI-D-19-

700   0351.1, 2020.

701   Fu, J. X., Wang, W., Shinoda, T., Ren, H. L., and Jia, X.: Toward
702   understanding the diverse impacts of air–sea interactions on MJO
703   simulations, J. Geophys. Res.-
704   Oceans,122(11), 8855– 8875. https://doi.org/10.1002/2017JC01318
705   7, 2017.

706   Gao, Y., Hsu, P.-C., Chen, L., Wang, L., and Li, T.: Effects of high-
707   frequency surface wind on the intraseasonal SST associated with the
708   Madden-Julian oscillation, Clim. Dynam., 54, 4485–4498,
709   https://doi.org/10.1007/s00382-020-05239-w, 2020a.

710   Gao, Y., Klingaman, N. P., DeMott, C. A., and Hsu, P.-C.: Boreal
711   summer intraseasonal oscillation in a superparameterized general
712   circulation model: effects of air–sea coupling and ocean mean state,
713   Geosci. Model Dev., 13, 5191–5209, https://doi.org/10.5194/gmd-
714   13-5191-2020, 2020b.

715   Ge, X., Wang, W., Kumar, A., and Zhang, Y.: Importance of the vertical
716   resolution in simulating SST diurnal and intraseasonal variability in
717   an oceanic general circulation model, J. Climate, 30, 3963–
718   3978, https://doi.org/10.1175/JCLI-D-16-0689.1, 2017.

719   Gonzalez, A. O., and Jiang, X.: Winter mean lower tropospheric moisture
720   over the maritime continent as a climate model diagnostic metric for
721   the propagation of the Madden-Julian Oscillation, Geophys. Res.
722   Lett., 44(5), 2588–2596. https://doi.org/10.1002/2016GL072430,
723   2017.

724   Hagos, S. M., Zhang, C., Feng, Z., Burleyson, C. D., Mott, C. De, Kerns,
725   B., Benedict, J. J., and Martini, M. N.: The impact of the diurnal
726   cycle on the propagation of Madden-Julian Oscillation convection
727   across the Maritime Continent, J. Adv. Model. Earth Syst., 8, 1552–
728   1564, https://doi.org/10.1002/2016MS000725, 2016.

729   Hersbach, H., and Dee, D.: ERA5 reanalysis is in production, ECMWF
730   Newsletter, Vol. 147, p.
731   7, https://www.ecmwf.int/en/newsletter/147/news/era5-reanalysis-
732   production, 2016.

733   Hong, X., Reynolds, C. A., Doyle, J. D., May, P., and O'Neill, L.:
734   Assessment of upper-ocean variability and the Madden-Julian
735   Oscillation in extended-range air–ocean coupled mesoscale
736   simulations, Dyn. Atmos. Oceans, 78, 89–105.
737   https://doi.org/10.1016/j.dynatmoce.2017.03.002, 2017.

738   Hsu, H.-H., and Lee, M.-Y.: Topographic effects on the eastward
739   propagation and initiation of the Madden-Julian Oscillation, J.
740   Climate, 18, 795-809, https://doi.org/10.1175/JCLI-3292.1, 2005.

741   Hurrell, J. W., Holland, M. M., Gent, P. R., Ghan, S., Kay, J. E., Kushner,
742   P. J., Lamarque, J.-F., Large, W. G., Lawrence, D., Lindsay, K.,
743   Lipscomb, W. H., Long, M. C., Mahowald, N., Marsh, D. R., Neale,

744   R. B., Rasch, P., Vavrus, S., Vertenstein, M., Bader, D., Collins, W.
745   D., Hack, J. J., Kiehl, J., and Marshall, S.: The Community Earth
746   System Model: A framework for collaborative research, Bull. Amer.
747   Meteor. Soc., 94, 1339–1360, https://doi.org/10.1175/BAMS-D-12-
748   00121.1, 2013.

749   Jiang, X.,Waliser, D. E., Xavier, P. K., Petch, J., Klingaman, N. P.,
750   Woolnough, S. J., Guan, B., Bellon, G., Crueger, T., DeMott, C.,
751   Hannay, C., Lin, H., Hu, W., Kim, D., Lappen, C.-L., Lu, M.-M.,
752   Ma, H.-Y., Miyakawa, T., Ridout, J. A., Schu-bert, S. D., Scinocca,
753   J., Seo, K.-H., Shindo, E., Song, X., Stan, C., Tseng, W.-L., Wang,
754   W., Wu, T., Wu, X., Wyser, K., Zhang, G. J., and Zhu, H.: Vertical
755   structure and physical processes of the MaddenJulian oscillation:
756   Exploring key model physics in climate simulations, J. Geophys.
757   Res.-Atmos., 120, 4718–4748,
758   https://doi.org/10.1002/2014JD022375, 2015.

759   Jiang, X.: Key processes for the eastward propagation of the Madden-
760   Julian Oscillation based on multimodel simulations, J. Geophys. Res.
761   Atmos., 122, 755–770, https://doi.org/10.1002/2016JD025955, 2017.

762   Jiang, X., Adames, Á. F., Zhao, M., Waliser, D., and Maloney, E.: A
763   unified moisture mode framework for seasonality of the Madden–
764   Julian oscillation, J. Climate, 31, 4215–4224,
765   https://doi.org/10.1175/JCLI-D-17-0671.1, 2018.

766   Jiang, X., Adames, Á. F., Kim, D., Maloney, E. D., Lin, H., and Kim, H.,
767   Zhang, C., DeMott, C. A., and Klingaman, N. P.: Fifty years of
768   research on the Madden-Julian Oscillation: Recent progress,
769   challenges, and perspectives, J. Geophys. Res.-Atmos., 125,
770   e2019JD030911, https://doi.org/10.1029/2019JD030911, 2020.

771   Kim, D., Kim, H., and Lee, M.-I.: Why does the MJO detour the Maritime
772   continent during Austral summer? Geophys. Res. Lett., 44(5), 2579–
773   2587, https://doi.org/10.1002/2017gl072643, 2017.

774   Kim, H., Vitart, F., and Waliser, D. E.: Prediction of the Madden–Julian
775   oscillation: A review, J. Climate, 31(23), 9425– 9443,
776   https://doi.org/10.1175/JCLI-D-18-0210.1, 2018.

777   Klingaman, N. P., and Demott, C. A,: Mean state biases and interannual
778   variability affect perceived sensitivities of the Madden-Julian
779   oscillation to air–sea coupling, J. Adv. Model. Earth Syst., 12, 1– 22,
780   https://doi.org/10.1029/2019MS001799, 2020.

781   Krishnamurti, T. N., Oosterhof, D. K. and Mehta, A. V.: Air–sea
782   interaction on the time scale of 30 to 50 days, J. Atmos. Sci., 45,
783   1304–1322, https://doi.org/10.1175/1520-
784   0469(1988)045,1304:AIOTTS.2.0.CO;2, 1988.

785   Lambaerts, J., Lapeyre, G., Plougonven, R., and Klein, P.: Atmospheric
786   response to sea surface temperature mesoscale structures, J.
787   Geophys. Res.-Atmos., 118(17), 9611–9621.

788   https://doi.org/10.1002/jgrd.50769, 2020.

789 Lan, Y.-Y., Hsu, H.-H., Tseng, W.-L., and Jiang, L.-C.: Embedding a
790   one-column ocean model in the Community Atmosphere Model 5.3
791   to improve Madden–Julian Oscillation simulation in boreal winter,
792   Geosci. Model Dev., 15, 5689–5712, https://doi.org/10.5194/gmd-
793   15-5689-2022, 2022.

794 Li, Y., Han, W., Shinoda, T., Wang, C., Ravichandran, M., and Wang,
795   J.-W.: Revisiting the wintertime intraseasonal SST variability in the
796   tropical south Indian Ocean: Impact of the ocean interannual
797   variation, J. Phys. Oceanogr., 44, 1886–1907,
798   https://doi.org/10.1175/JPO-D-13-0238.1, 2014.

799 Li, T., Ling, J., and Hsu, P.-C.: Madden–Julian Oscillation: Its discovery,
800   dynamics, and impact on East Asia, J. Meteor. Res., 34, 20–42,
801   https://doi.org/10.1007/s13351-020-9153-3, 2020a.

802 Li, K., Yu, W., Yang, Y., Feng, L., Liu, S., and Li, L.: Spring barrier to
803   the MJO eastward propagation, Geophys. Res.
804   Lett., 47, e2020GL087788, https://doi.org/10.1029/2020GL087788,
805   2020b.

806 Liang, Y.; Du, Y.; Zhang, L.; Zheng, X.; Qiu, S. The 30–50-Day
807   Intraseasonal Oscillation of SST and Precipitation in the South
808   Tropical Indian Ocean, Atmos., 9, 69.
809   https://doi.org/10.3390/atmos9020069, 2018.

810 Liang, Y., and Du, Y.: Oceanic impacts on 50–80-day intraseasonal
811   oscillation in the eastern tropical Indian Ocean, Clim. Dynam., 59,
812   1283–1296, https://doi.org/10.1007/s00382-021-06041-y, 2022.

813 Liebmann, B.: Description of a complete (interpolated) outgoing
814   longwave radiation dataset, B. Am. Meteorol. Soc., 77, 1275–1277,
815   1996.

816 Madden, R. A., and Julian, P. R.: Description of global-scale circulation
817   cells in the tropics with a 40-50 day period, J. Atmos. Sci., 29, 1109-
818   1123, https://doi.org/10.1175/1520-
819   0469(1972)029<1109:DOGSCC>2.0.CO;2, 1972.

820 Maloney, E., and Sobel, A. H.: Surface fluxes and ocean coupling in the
821   tropical intraseasonal oscillation. J. Climate, 17, 4368–4386,
822   https://doi.org/10.1175/JCLI-3212.1, 2004.

823 Newman, M., Sardeshmukh, P. D., and Penland, C.: How important is
824   air–sea coupling in ENSO and MJO evolution? J.
825   Climate, 22, 2958– 2977, https://doi.org/10.1175/2008JCLI2659.1,
826   2009.

827 Pariyar, S.K., Keenlyside, N., Tseng, W.-L., Hsu, H.-H., and Tsuang, B.-
828   J. The role of air–sea coupling on November–April intraseasonal
829   rainfall variability over the South Pacific, Clim. Dynam., 60, 1121–
830   1136, https://doi.org/10.1007/s00382-022-06354-6, 2023.

Pei, S., Shinoda, T., Soloviev, A., and Lien, R.-C.: Upper ocean response to the atmospheric cold pools associated with the Madden-Julian Oscillation, Geophys. Res. Lett., 45, 5020–5029, https://doi.org/10.1029/2018GL077825, 2018.

Rasch, P. J., Xie, S., Ma, P.-L., Lin, W., Wang, H., Tang, Q., Bur- rows, S. M., Caldwell, P., Zhang, K., Easter, R. C., Cameron- Smith, P., Singh, B., Wan, H., Golaz, J.-C., Harrop, B. E., Roesler, E., Bacmeister, J., Larson, V. E., Evans, K. J., Qian, Y., Taylor, M., Leung, L. R., Zhang, Y., Brent, L., Branstet- ter, M., Hannay, C., Mahajan, S., Mametjanov, A., Neale, R., Richter, J. H., Yoon, J.-H., Zender, C. S., Bader, D., Flan- ner, M., Foucar, J. G., Jacob, R., Keen, N., Klein, S. A., Liu, X., Salinger, A. G., Shrivastava, M., and Yang, Y.: An overview of the atmospheric component of the Energy Exascale Earth System Model, J. Adv. Model Earth Sy., 11, 2377–2411, https://doi.org/10.1029/2019ms001629, 2019.

Rayner, N. A., Parker, D. E., Horton, E. B., Folland, C. K., Alexander, L. V., Rowell, D. P., Kent, E. C., and Kaplan, A.: Global analyses of sea surface temperature, sea ice, and night marine air temperature since the late nineteenth century, J. Geophys. Res., 108(D14), 4407, https://doi.org/10.1029/2002JD002670, 2003.

Ren, P. F., Gao, L., Ren, H.-L., Rong, X., and Li, J.: Representation of the Madden–Julian Oscillation in CAMSCSM, J. Meteor. Res., 33, 627–650, https://doi.org/10.1007/s13351-019-8118-x, 2019.

Savarin, A., and Chen, S. S.: Pathways to better prediction of the MJO: 2. Impacts of atmosphere-ocean coupling on the upper ocean and MJO propagation, J. Adv. Model. Earth Syst., 14, e2021MS002929, https://doi.org/10.1029/2021MS002929, 2022.

Shinoda, T., Pei, S., Wang, W., Fu, J. X., Lien, R.-C., Seo, H., and Soloviev, A.: Climate process team: Improvement of ocean component of NOAA climate forecast system relevant to Madden-Julian Oscillation simulations, J. Adv. Model. Earth Syst., 13(12), e2021MS002658. https://doi.org/10.1029/2021MS002658, 2021.

Seo, H., Subramanian, A. C., Miller, A. J., and Cavanaugh, N. R.: Coupled impacts of the diurnal cycle of sea surface temperature on the Madden–Julian oscillation, J. Climate, 27(22), 8422– 8443. https://doi.org/10.1175/JCLI-D-14-00141.1, 2014.

Sobel, A. H., and Gildor, H.: A simple time-dependent model of SST hot spots. J. Climate, 16, 3978–3992, https://doi.org/10.1175/1520-0442(2003)016<3978:ASTMOS>2.0.CO;2, 2003.

Sobel, A. H., Maloney, E. D., Bellon, G., and Frierson, D. M.: Surface Fluxes and Tropical Intraseasonal Variability: a Reassessment, J. Adv. Model. Earth Syst., 2, 2, https://doi.org/10.3894/JAMES.2010.2.2, 2010.

Sobel, A., Wang, S., and Kim, D.: Moist static energy budget of the MJO during DYNAMO, J. Atmos. Sci., 71(11), 4276– 4291, https://doi.org/10.1175/JAS-D-14-0052.1, 2014.

Stan, C.: The role of SST variability in the simulation of the MJO, Clim. Dynam., 51, 2943–2964, https://doi.org/10.1007/s00382-017-4058-2, 2018.

Tseng, W.-L., Tsuang, B.-J., Keenlyside, N. S., Hsu, H.-H. and Tu, C.-Y.: Resolving the upper-ocean warm layer improves the simulation of the Madden-Julian oscillation, Clim. Dynam., 44, 1487–1503, https://doi.org/10.1007/s00382-014-2315-1, 2015.

Tseng, W.-L., Hsu, H.-H., Keenlyside, N., Chang, C.-W. J., Tsuang, B.-J., Tu, C.-Y., and Jiang, L.-C.: Effects of Orography and Land–Sea Contrast on the Madden–Julian Oscillation in the Maritime Continent: A Numerical Study Using ECHAM-SIT, J. Climate, 30, 9725–9741, https://doi.org/10.1175/JCLI-D-17-0051.1, 2017.

Tseng, W.-L., Hsu, H.-H., Lan, Y.-Y., Lee, W.-L., Tu, C.-Y., Kuo, P.-H., Tsuang, B.-J., and Liang, H.-C.: Improving Madden–Julian oscillation simulation in atmospheric general circulation models by coupling with a one-dimensional snow–ice–thermocline ocean model, Geosci. Model Dev., 15, 5529–5546, https://doi.org/10.5194/gmd-15-5529-2022, 2022.

Tulich, S. N., and Kiladis, G. N.: On the Regionality of moist kelvin waves and the MJO: The critical role of the background zonal flow, J. Adv. Model. Earth Syst., 13(9), e2021MS002528. https://doi.org/10.1029/2021MS002528, 2021.

Voldoire, A., Roehrig, R., Giordani, H., Waldman, R., Zhang, Y., Xie, S., and Bouin, M.-N.: Assessment of the sea surface temperature diurnal cycle in CNRM-CM6-1 based on its 1D coupled configuration, Geosci. Model Dev., 15, 3347–3370, https://doi.org/10.5194/gmd-15-3347-2022, 2022.

Wang, W., Hung, M.-P., Weaver, S. J., Kumar, A., and Fu, X.: MJO prediction in the NCEP Climate Forecast System version 2, Clim. Dynam., 42, 2509–2520, https://doi.org/10.1007/s00382-013-1806-9, 2014.

Wang, L. and Li, T.: Effect of vertical moist static energy advection on MJO eastward propagation: Sensitivity to analysis domain, Clim. Dynam., 54, 2029–2039, https://doi.org/10.1007/s00382-019-05101-8, 2020.

Watterson, I. G.: The sensitivity of subannual and intraseasonal tropical variability to model ocean mixed layer depth, J. Geophys. Res., 107, 4020, https://doi.org/10.1029/2001JD000671, 2002.

Wheeler, M. C., and Hendon, H. H.: An all-season real-time multivariate MJO index: development of an index for monitoring and prediction, Mon. Weather Rev., 132, 1917–1932, https://doi.org/10.1175/1520-

919   0493(2004)132<1917:AARMMI>2.0.CO;2, 2004.

920   Wheeler, M., and Kiladis, G. N.: Convectively coupled equatorial waves:
921   Analysis of clouds and temperature in the wavenumber-frequency
922   domain, J. Atmos. Sci., 56, 374– 399, https://doi.org/10.1175/1520-
923   0469(1999)056<0374:CCEWAO>2.0.CO;2, 1999.

924   Wu, C.-H., and Hsu, H.-H.: Potential Influence of Topography on the
925   MJO in the Maritime Continent, J. Climate, 22, 5433-5448,
926   https://doi.org/10.1175/2009JCLI2825.1, 1999.

927   Wu, J., Li, Y., Luo, J.-J. and Jiang, X.: Assessing the role of air–sea
928   coupling in predicting Madden–Julian oscillation with an
929   Atmosphere–Ocean coupled model, J. Clim. 34 9647–63,
930   https://doi.org/10.1175/JCLI-D-20-0989.1, 2021.

931   Zhang, L., and Han, W.: Barrier for the eastward propagation of
932   Madden–Julian Oscillation over the maritime continent: A possible
933   new mechanism, Geophys. Res. Lett., 47(21),
934   e2020GL090211. https://doi.org/10.1029/2020gl090211, 2020.

935   Zhao, N., and Nasuno, T.: How Does the Air–Sea Coupling Frequency
936   Affect Convection During the MJO Passage?, J. Adv. Model. Earth
937   Sy., 12, e2020MS002058, https://doi.org/10.1029/2020MS002058,
938   2020.

939 Table 1. Two sets of experiments with different SST feedback
940 frequencies: high-frequency (C–CTL, C–1day and C–3days) and low-
941 frequency (C–6days, C–12days, C–18days, C–24days and C–30days).

942

subseasonal sets	high-frequency SST (< 6 days)			low-frequency SST (6-30 days)				
experiments	C–CTL	C–1day	C–3days	C–6days	C–12days	C–18days	C–24days	C–30days
atmosphere to ocean frequency	48/1day							
ocean to atmosphere Frequency	48/1day	1/1day	1/3days	1/6days	1/12days	1/18days	1/24days	1/30days

943

944 Table 2. Key intraseasonal (20–100-day bandpass filtered) ocean temperatures in all

945 experiments: SST, differences between SST and temperatures at 10m depth ($\overline{\Delta T}_{0-10m}$)

946 and 30m depth ($\overline{\Delta T}_{0-30m}$), t max/mini SST and 10m-depth temperature (T_{10m}) in the

947 area of (110–130° E, 5–15° S) during a MJO cycle for the observation (OISST), AGCM

948 (A–CTL), high-frequency experiments (C–CTL, C–1day, and C–3days), and low-

949 frequency experiments (C–6days, C–12days, C–18days, C–24days, and C–30days)

950

(110–130° E, 5–15° S)		obs.	AGCM	high-frequency			low-frequency				
experiments		OI SST[1]	A–CTL[2]	C–CTL	C–1day	C–3days	C–6days	C–12days	C–18days	C–24days	C–30days
DJF seasonal mean	SST	302.2 ±0.96	302.2 ±0.77	300.8 ±0.76	301.2 ±0.76	301.2 ±0.75	301.2 ±0.75	301.4 ±0.75	301.6 ±0.80	302.0 ±1.06	302.7 ±1.71
	$\overline{\Delta T}_{0-10m}$	-	-	0.1 ± 0.22	0.1 ± 0.22	0.1 ± 0.21	0.1 ± 0.23	0.2 ± 0.25	0.3 ± 0.32	0.5 ± 0.50	1.0 ± 0.95
	$\overline{\Delta T}_{0-30m}$	-	-	0.8 ± 0.79	0.7 ± 0.70	0.6 ± 0.69	0.8 ± 0.70	0.8 ± 0.70	1.0 ± 0.73	1.4 ± 0.96	2.1 ± 1.54
phase's mean in boreal winter	max SST (phase)	0.21 (ph2)	0.02 (ph2)	0.24 (ph3)	0.26 (ph3)	0.22 (ph3)	0.32 (ph3)	0.36 (ph3)	0.43 (ph3)	0.50 (ph3)	0.62 (ph2)
	max T_{10m} (phase)	-	-	0.15 (ph4)	0.17 (ph4)	0.14 (ph3)	0.19 (ph3)	0.21 (ph3)	0.26 (ph3)	0.30 (ph3)	0.35 (ph2)
	mini SST (phase)	-0.21 (ph7)	-0.003 (ph8)	-0.17 (ph7)	-0.22 (ph7)	-0.19 (ph7)	-0.25 (ph7)	-0.28 (ph7)	-0.38 (ph7)	-0.52 (ph6)	-0.60 (ph6)
	mini T_{10m} (phase)	-	-	-0.11 (ph8)	-0.12 (ph7)	-0.11 (ph8)	-0.15 (ph7)	-0.17 (ph7)	-0.24 (ph7)	-0.33 (ph6)	-0.33 (ph6)

951 Note: [1]daily average data, [2] monthly average data.

952 **Figure List**

953 **Figure 1.** Wavenumber–frequency spectra for 850-hPa zonal wind averaged over 10°

954 S–10° N in boreal winter after removing the climatological mean seasonal cycle.

955 Vertical dashed lines represent periods at 80 and 30 days. (a)–(j) are from ERA5

956 reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, C–

957 24days, and C–30days, respectively.

958

959 **Figure 2.** Hovmöller diagrams of correlation between precipitation averaged over 10°

960 S–5° N, 75–100° E and precipitation (color) and 850-hPa zonal wind (contour)

961 averaged over 10° N–10° S. (a)–(j) are arranged in the same order as in Fig. 1 for

962 GPCP/ERA5 and all experiments. All data are 20–100-day bandpass filtered.

963

964 **Figure 3.** Zonal wavenumber–frequency power spectra of anomalous OLR (colors) and

965 phase lag with U850 (vectors) for the symmetric component of tropical waves, with the

966 vertically upward vector representing a phase lag of 0° and phase lag increasing

967 clockwise. Three dispersion straight lines with increasing slopes representing the

968 equatorial Kelvin waves (derived from the shallow water equations) corresponding to

969 three equivalent depths, 12, 25, and 50 m, respectively. (a)–(j) are arranged in the same

970 order as in Fig. 1 for NOAA/ERA5 and all experiments.

971

972 **Figure 4.** Phase-longitude Hovmöller diagrams of 20–100-day filtered precipitation

973 (mm day^{-1}, shaded) and SST anomaly (K, contour) averaged over 10° N–10° S from

974 phase 1 to 8. Contour interval is 0.03; solid, dashed, and thick-black lines represent

975 positive, negative, and zero values, respectively. (a)–(j) are arranged in the same order

976 as in Fig. 1 for NOAA/ERA5 and all experiments.

977

978 **Figure 5.** Phase-vertical Hovmöller diagrams of 20–100-day specific humidity

979 (shading, g kg^{-1}) and air temperature (contoured, K) averaged over 5–20° S, 120–150°

980 E; solid, dashed, and thick-black curves are positive, negative, and zero values,

981 respectively. (a)–(j) are arranged in the same order as in Fig. 1 for NOAA/ERA5 and

982 all experiments.

983

984 **Figure 6.** The 20–100-day filtered oceanic temperature (K, shaded and contour,

985 interval 0.03) at phase 2–3 (Left column) and phase 4–5 (Right column) averaged

986 over 0–15° S between 0 and 60 m depth. (a)–(b) are from C–CTL, (c)–(d) are from

987 C–1day, (e)–(f) are from C–3days, (g)–(h) are from C–6days, (i)–(j) are from C–

988 12days, (k)–(l) are from C–18days, (m)–(n) are from C–24days, and (o)–(p) are from

989 C–30days.

990

Figure 7. The lead–lag relationship between MJO-related atmosphere and SST variation from phase 1 to 8 averaged within 110–130° E and 5–15° S. The variables analyzed include 20-100-day filtered LHF, green shading), OLR (yellow bar chart), FSNS, (orange bar chart), U850 (purple bar chart), 30-m T (multiplied by 100, black line), and SST (multiplied by 10, orange line). Variables denoted with L (R) are scaled by the left (right) y-axis. (a)–(j) are from ERA5/OISST reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, C–24days, and C–30days, respectively.

Figure 8. Averaged 20–100-day filtered fields at phase 2–3. (Upper row) OLR (W m^{-2}, shaded) and 200 hPa zonal and meridional wind anomaly (m s^{-1}, vector with reference vector shown at the top right corner, latent heat flux (W m^{-2}, shaded, positive representing upward), and 10-m wind anomaly (m s^{-1}, contour interval 0.5). (Second row) net surface heat flux (W m^{-2}, shaded) and net solar radiation (W m^{-2}, contour interval 6). (Third row) SST (K, shaded) and 850 hPa zonal and meridional wind anomaly (m s^{-1}, vector with reference vector shown at the top right corner. The number of days used to generate the composite is shown at the bottom right corner. (a), (d), (g) and (j) are from C–18days; (b), (e), (h) and (k) are from C–24days, and (c), (f), (i) and (l) are from C–30days, respectively. Solid, dashed, and thick-black lines represent positive, negative, and zero values, respectively.

Figure 9. Averaged 20–100-day filtered column-integrated MSE budget terms (J kg^{-1} s^{-1}) in 10° S–0° N/S, 120–150° E for ERA5 and all model simulations. Colors represent different datasets: green for REA5, light gray for A–CTL, red, orange and wathet blue for high-frequency experiments (C–CTL, C–1day, and C–3days, respectively), purple, black, dark brown, dark green, and dark gray for low-frequency experiments (C–6days, C–12days, C–18days, C–24days, and C–30days, respectively). The bars from left to right represent MSE tendency (<dmdt>), vertical MSE advection (-<wdmdp>), horizontal MSE advection (-<vdm>), surface latent heat flux (LH), surface sensible heat flux (SH), shortwave radiation flux (<SW>), longwave radiation flux (<LW>), and residual terms.

Figure 10. Filtered the column-integrated MSE tendency (J kg^{-1} s^{-1}, shading), precipitation (mm d^{-1}, contours interval 1.5) and 850-hPa wind (green vector, reference vector 2 m s^{-1}) in phase 5: (a) ERA5, (b) A−CTL, (c) C−CTL, (d) C−1day, (e) C−3days, (f) C−6days, (g) C−12days, (h) C−18days, (i) C−24days, and (i) C−30days. Solid-red, dashed-blue, and thick-black curves represent positive, negative, and zero values, respectively.
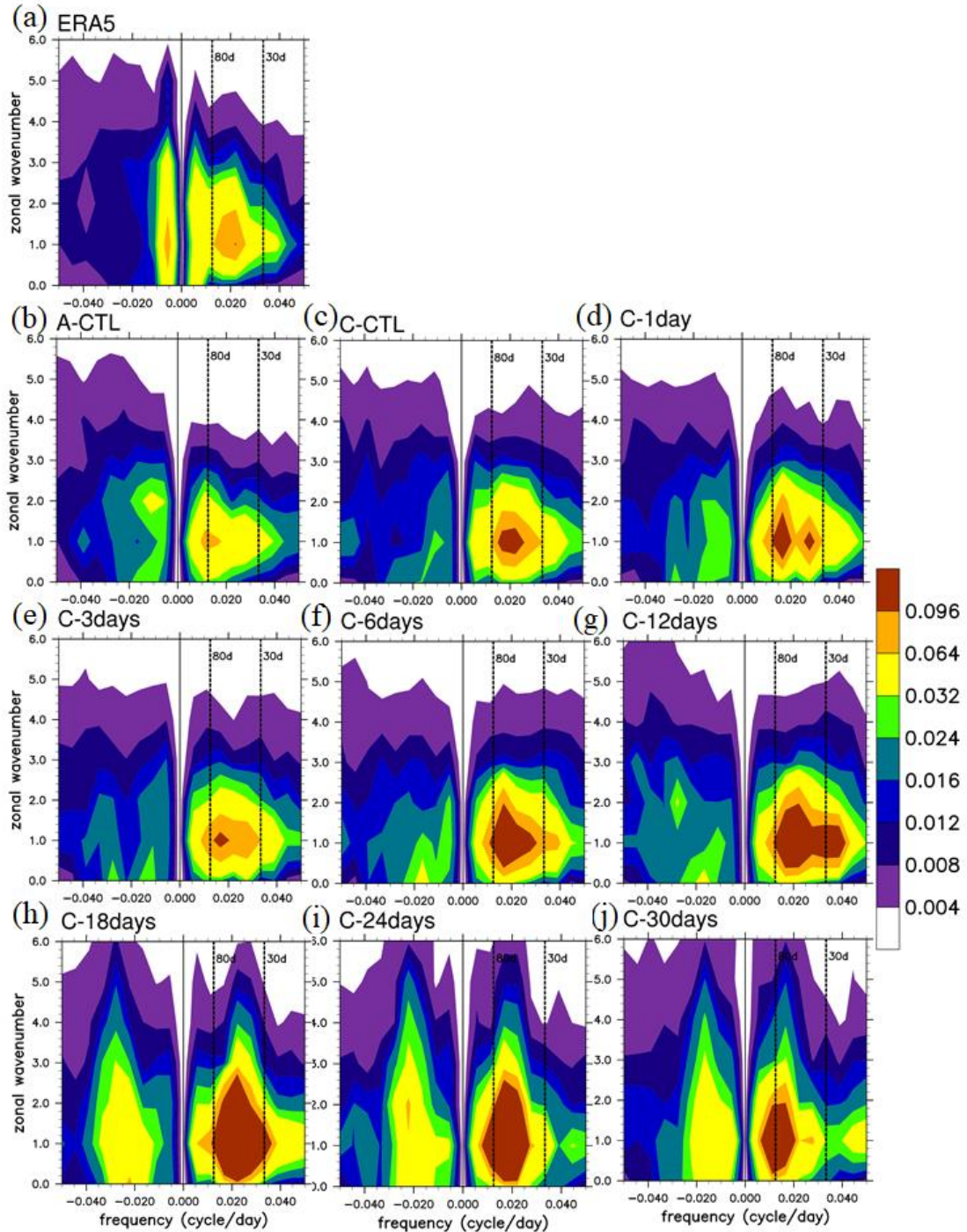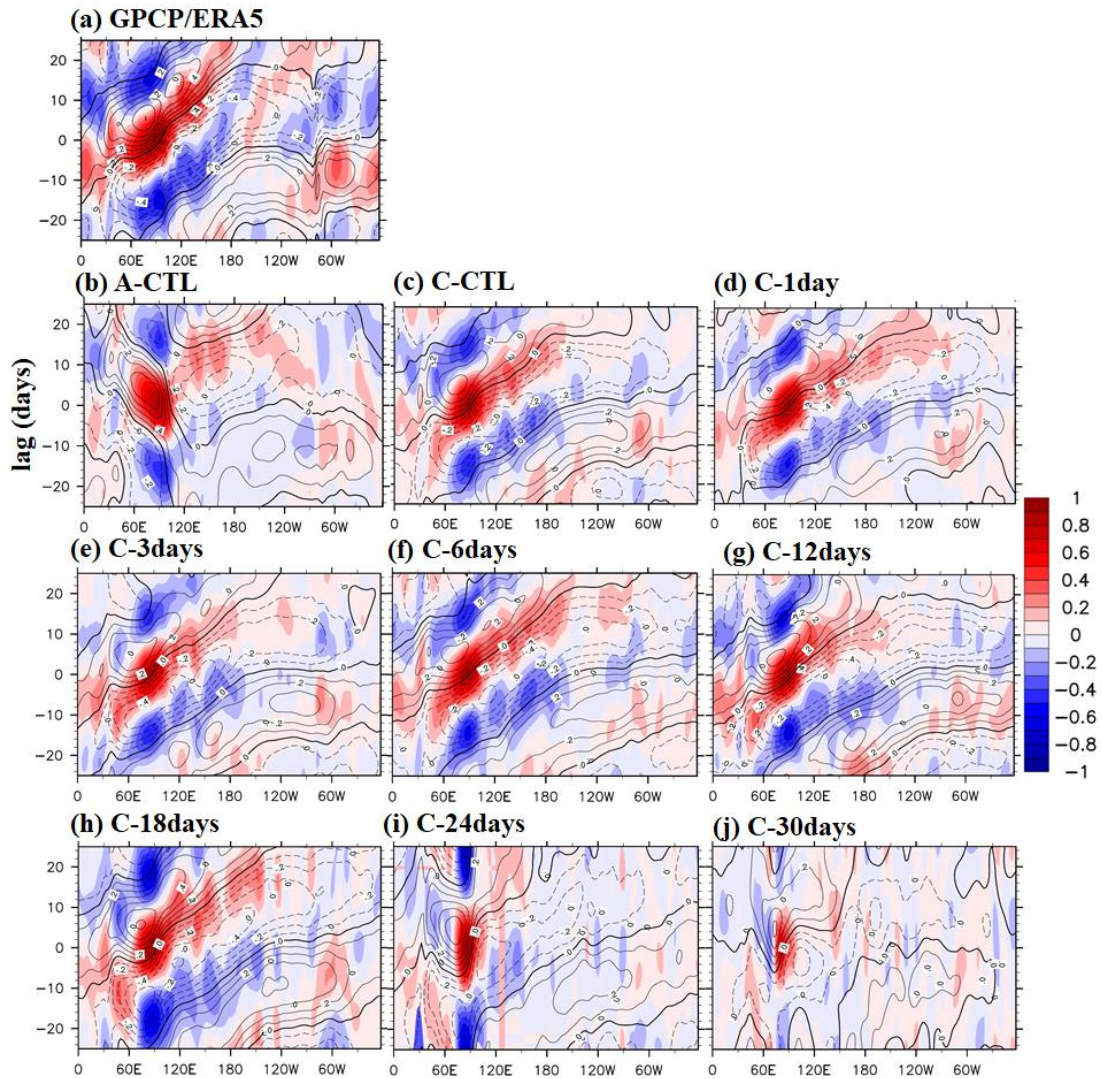
1028

1029   **Figure 11.** The projection of each MSE component onto the ERA5 column-integrated
1030   MSE tendency at phase 5 over the MC (20° S–20° N, 90–210° E): <dmdt>, -<wdmdp>,
1031   -<vdm>, Qr, Fs, and residual; decomposition of horizontal MSE advection to zonal and
1032   meridional advection (-<udmdt> and -<vdmdy>).

1033

1034   **Figure 12.** Filtered column-integrated vertical ($J\,kg^{-1}\,s^{-1}$, shading) and horizontal MSE
1035   advection ($J\,kg^{-1}\,s^{-1}$, contours interval 6.0), and 200-hPa wind (green vector with
1036   reference vector $3\,m\,s^{-1}$): (a) ERA5, (b) A−CTL, (c) C−CTL, (d) C−1day, (e) C−3days,
1037   (f) C−6days, (g) C−12days, (h) C−18days, (i) C−24days, and (j) C−30days. Solid-blue,
1038   dashed-red, and thick-black curves represent positive, negative, and zero values,
1039   respectively.

1040

1041   **Figure 13.** Schematic diagrams illustrate the anomalous circulation and moistening
1042   processes during the eastward propagation of the MJO in experiments: (a) A−CTL, (b)
1043   high-frequency SST feedback experiments (C−CTL, C−1day, and C−3days), (c) low-
1044   frequency SST feedback experiments (C−6days, C−12days, and C−18days), and (d)
1045   C−24days and C−30days experiment. In each panel, the horizontal line represents the
1046   equator. The size of clustering gray clouds indicates the strength of convective
1047   organization. A red ellipse indicates convection-driven circulation. In the coupled
1048   simulations, light red (blue) filled ovals represent warm (cold) SST anomalies,
1049   respectively, and grass green filled rectangle represent latent heat flux. Unresolved
1050   convective processes are indicated by black dots representing low-level moisture
1051   convergence. Low-level moisture convergence into the equatorial trough is shown by
1052   light blue arrows, while midlevel moisture advection is represented by left-pointing
1053   green arrows. The deeper colors or thicker lines on the map indicate stronger anomalies
1054   of the MJO perturbations. Note: The concept of the figure is based on DeMott et al.
1055   (2014).

Figure 1. Wavenumber–frequency spectra for 850-hPa zonal wind averaged over 10°
S–10° N in boreal winter after removing the climatological mean seasonal cycle.
Vertical dashed lines represent periods at 80 and 30 days. (a)–(j) are from ERA5
reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, C–
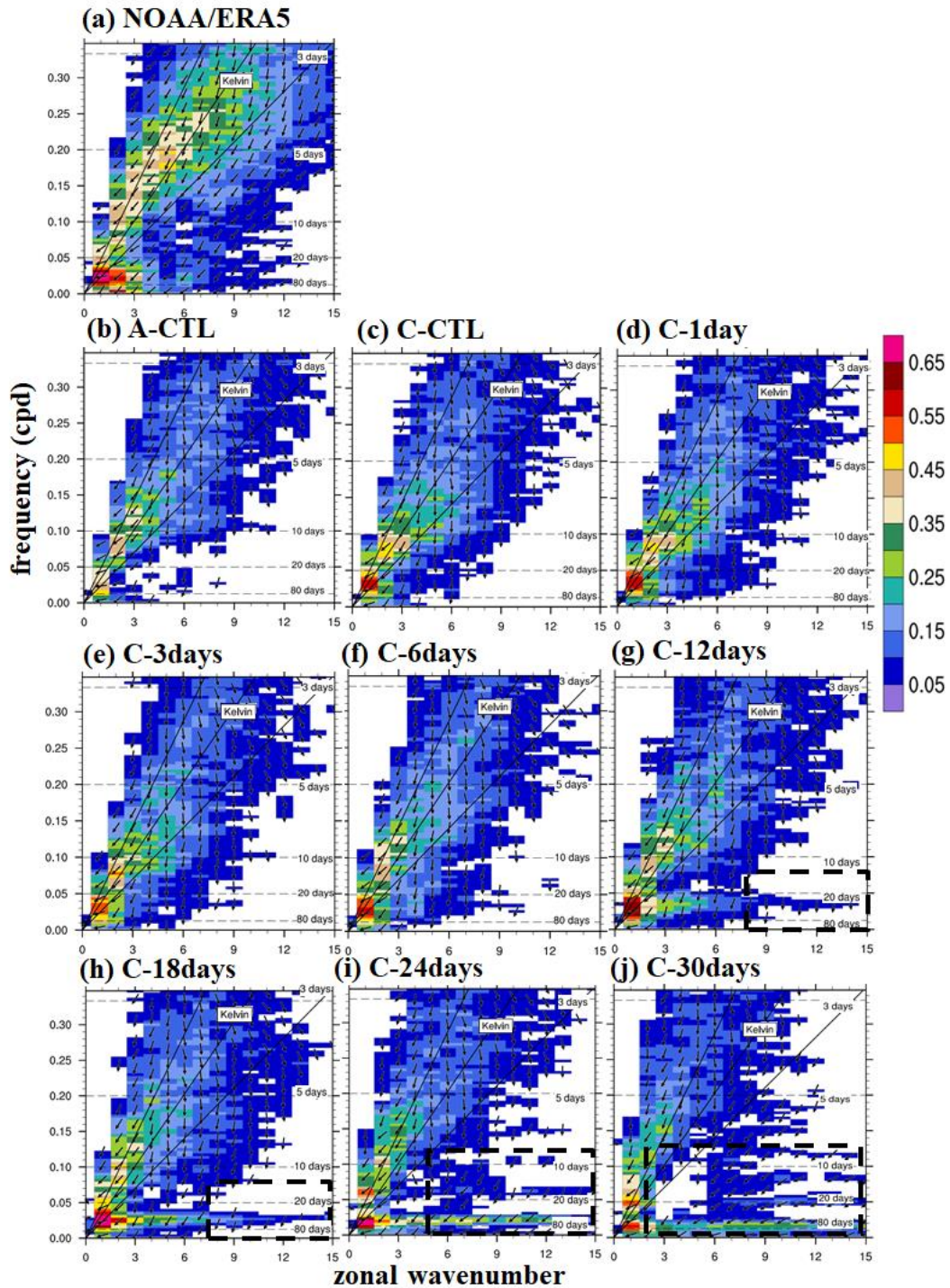24days, and C–30days, respectively.

Figure 2. Hovmöller diagrams of correlation between precipitation averaged over 10° S–5° N, 75–100° E and precipitation (color) and 850-hPa zonal wind (contour) averaged over 10° N–10° S. (a)–(j) are arranged in the same order as in Fig. 1 for GPCP/ERA5 and all experiments. All data are 20–100-day bandpass filtered.

Figure 3. Zonal wavenumber–frequency power spectra of anomalous OLR (colors) and phase lag with U850 (vectors) for the symmetric component of tropical waves, with the vertically upward vector representing a phase lag of 0° with phase lag increasing clockwise. Three dispersion straight lines with increasing slopes represent the equatorial Kelvin waves (derived from the shallow water equations) corresponding to three equivalent depths, 12, 25, and 50 m, respectively. (a)–(j) arrange in order are same order as in Fig. 1 for NOAA/ERA5 and all experiments.
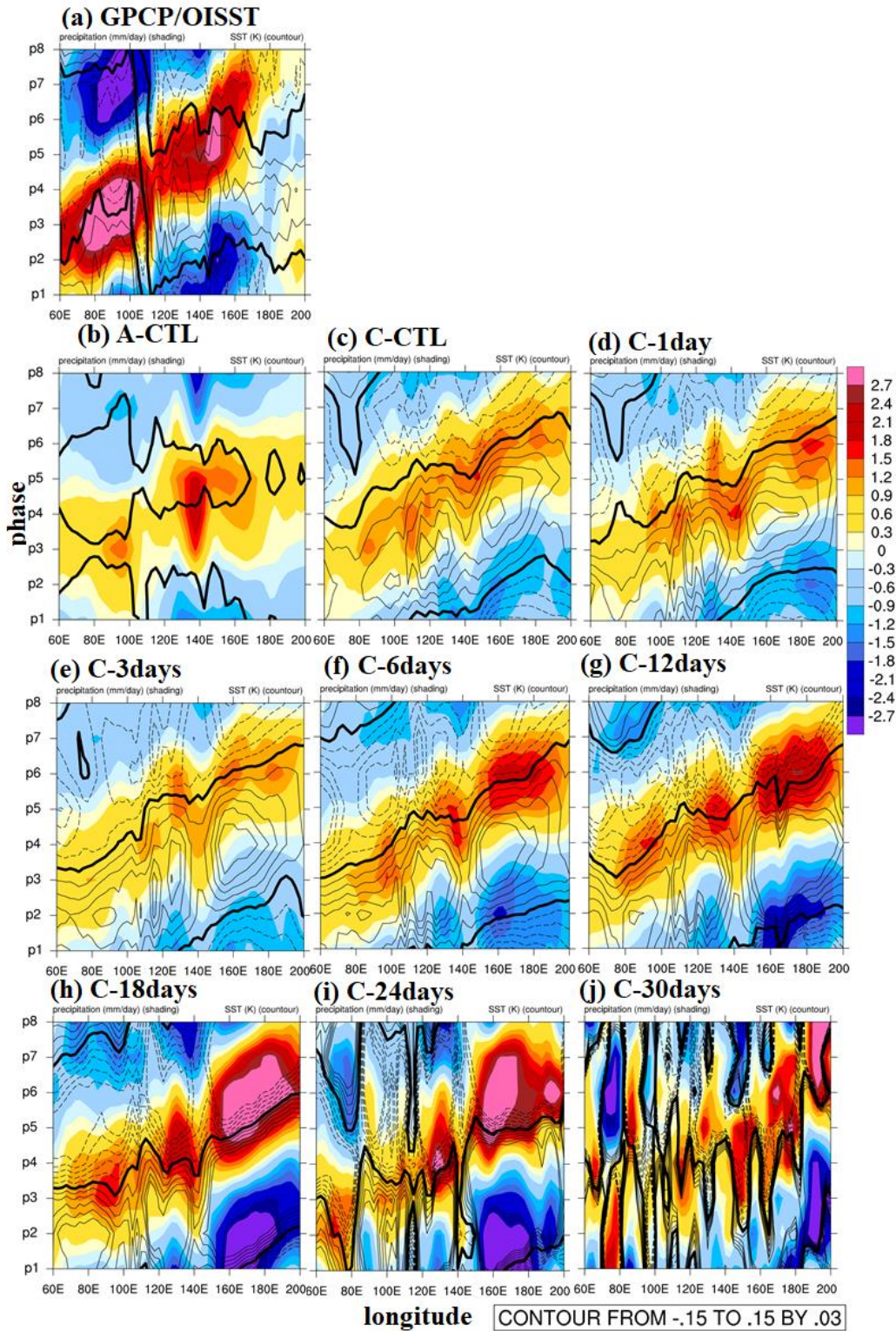
Figure 4. Phase-longitude Hovmöller diagrams of 20–100-day filtered precipitation (mm day^{-1}, shaded) and SST anomaly (K, contour) averaged over 10° N–10° S from phase 1 to 8. Contour interval is 0.03; solid, dashed, and thick-black lines represent positive, negative, and zero values, respectively. (a)–(j) are arranged in the same order as in Fig. 1 for NOAA/ERA5 and all experiments.
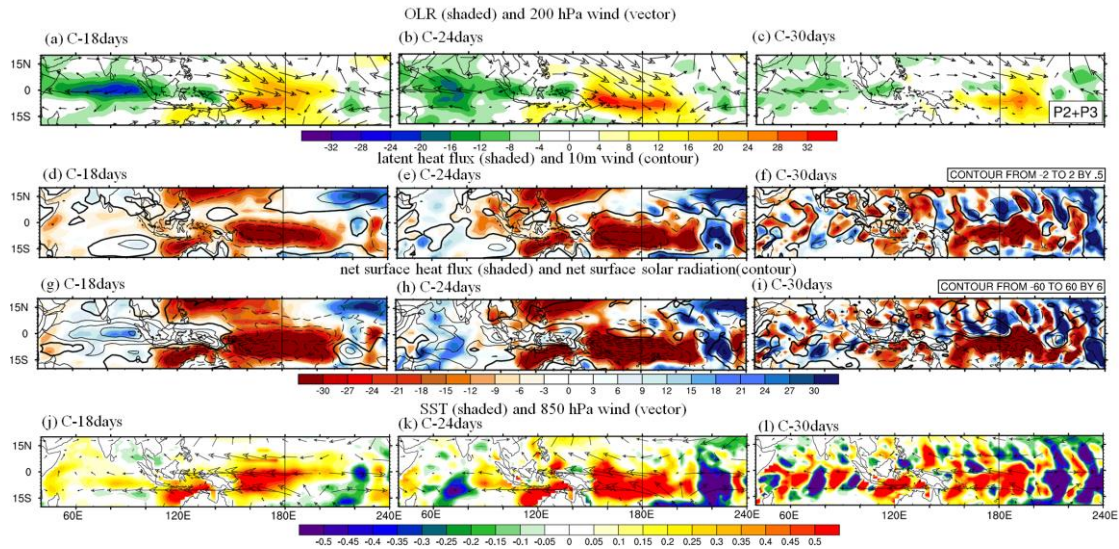
1083
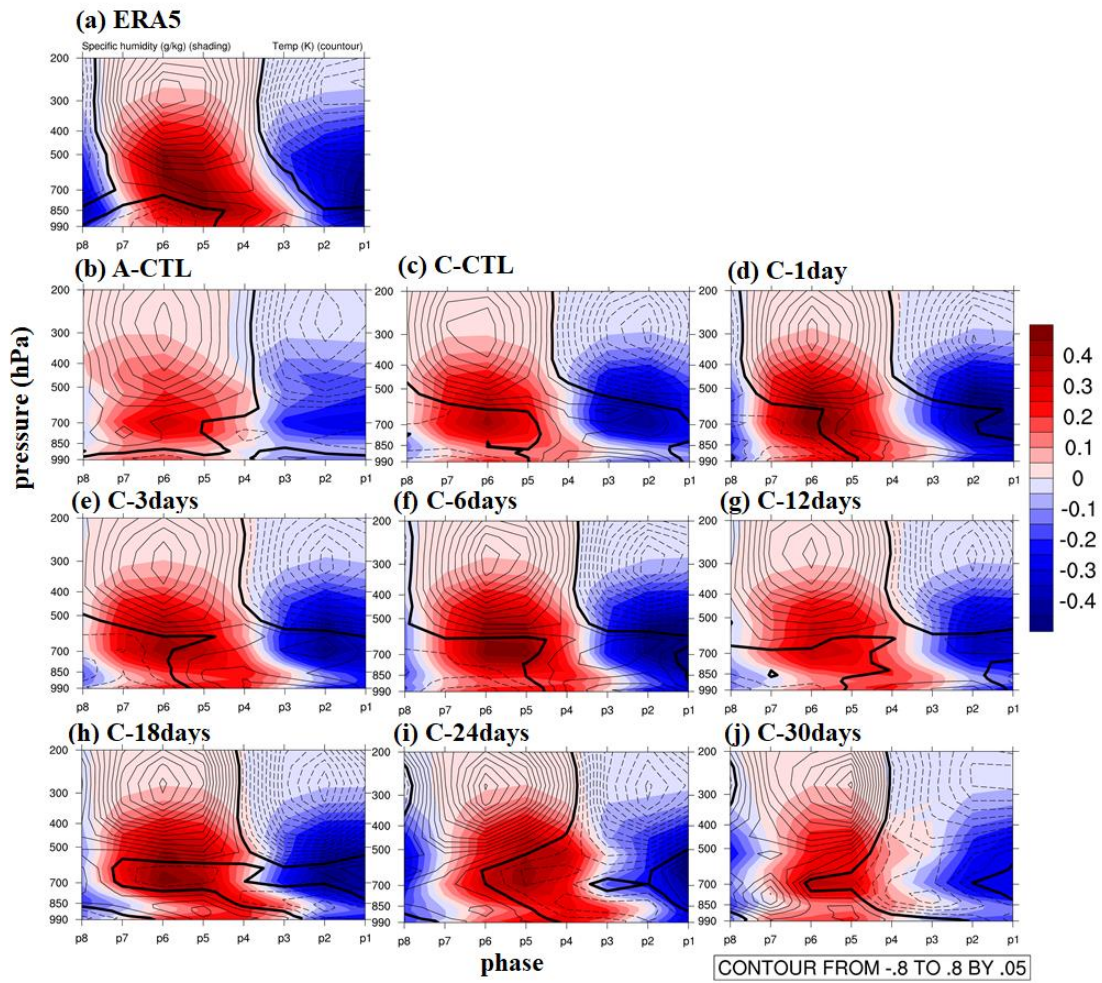
1084

1085 **Figure 5.** Phase-vertical Hovmöller diagrams of 20–100-day specific humidity
1086 (shading, g kg−1) and air temperature (contoured, K) averaged over 5–20° S, 120–150°
1087 E; solid, dashed, and thick-black curves are positive, negative, and zero values,
1088 respectively. (a)–(j) are arranged in the same order as in Fig. 1 for NOAA/ERA5 and
1089 all experiments.
1090

1091
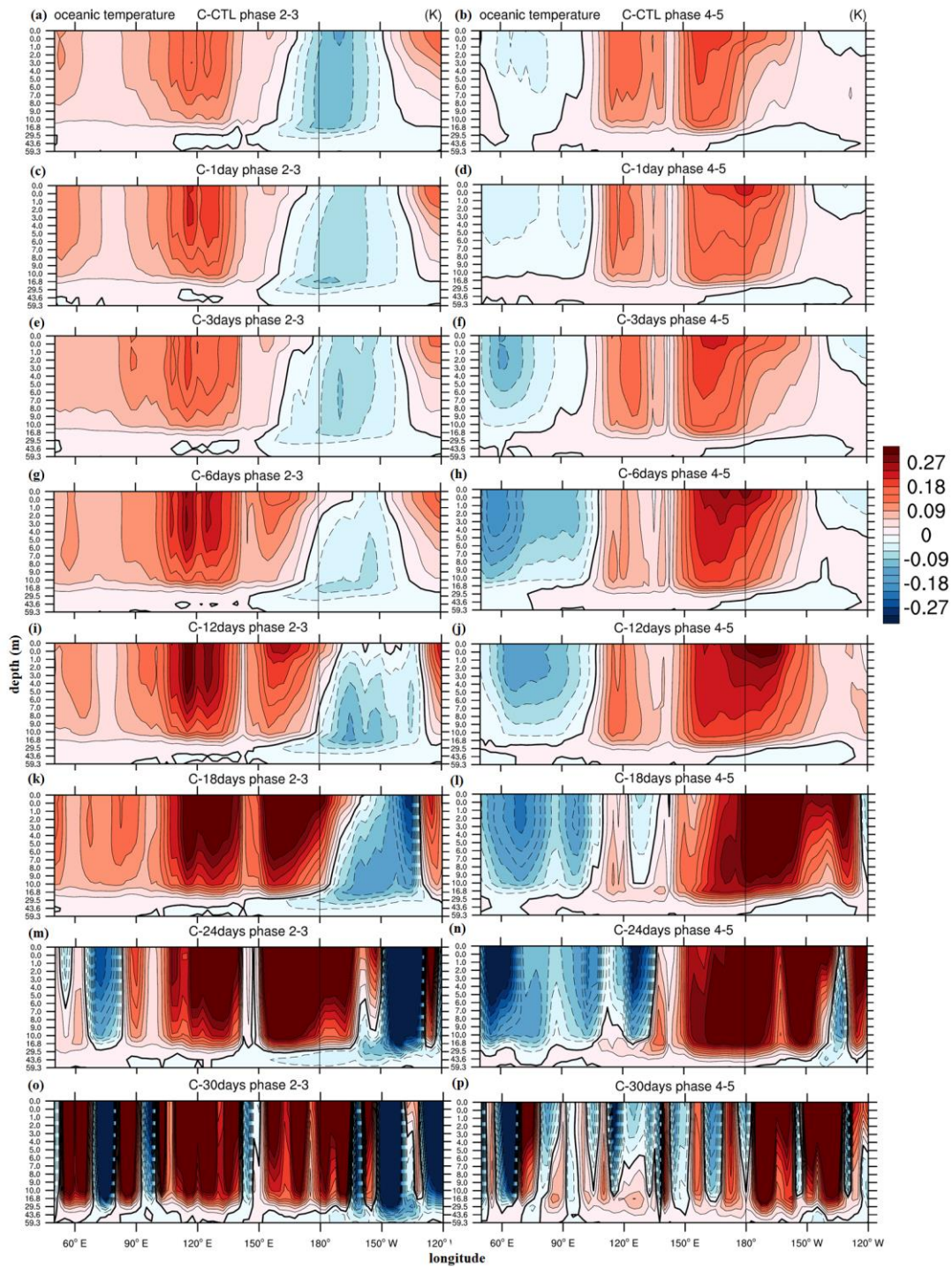
1092

Figure 6. The 20–100-day filtered oceanic temperature (K, shaded and contour, interval 0.03) at phase 2–3 (Left column) and phase 4–5 (Right column) averaged over 0–15° S between 0 and 60 m depth. (a)–(b) are from C–CTL, (c)–(d) are from C–1day, (e)–(f) are from C–3days, (g)–(h) are from C–6days, (i)–(j) are from C–12days, (k)–(l) are from C–18days, (m)–(n) are from C–24days, and (o)–(p) are from C–30days.

Figure 7. The lead–lag relationship between MJO-related atmosphere and SST variation from phase 1 to 8 averaged within 110–130° E and 5–15° S. The variables analyzed include 20-100-day filtered LHF, green shading), OLR (yellow bar chart), FSNS, (orange bar chart), U850 (purple bar chart), 30-m T (multiplied by 100, black line), and SST (multiplied by 10, orange line). Variables denoted with L (R) are scaled by the left (right) y-axis. (a)–(j) are from ERA5/OISST reanalysis, A–CTL, C–CTL, C–1day, C–3days, C–6days, C–12days, C–18days, C–24days, and C–30days, respectively.

Figure 8. Averaged 20–100-day filtered fields at phase 2–3. (Upper row) OLR (W m^{-2}, shaded) and 200 hPa zonal and meridional wind anomaly (m s^{-1}, vector with reference vector shown at the top right corner, latent heat flux (W m^{-2}, shaded, positive representing upward), and 10-m wind anomaly (m s^{-1}, contour interval 0.5). (Second row) net surface heat flux (W m^{-2}, shaded) and net solar radiation (W m^{-2}, contour interval 6). (Third row) SST (K, shaded) and 850 hPa zonal and meridional wind anomaly (m s^{-1}, vector with reference vector shown at the top right corner. The number of days used to generate the composite is shown at the bottom right corner. (a), (d), (g) and (j) are from C–18days; (b), (e), (h) and (k) are from C–24days, and (c), (f), (i) and (l) are from C–30days, respectively. Solid, dashed, and thick-black lines represent positive, negative, and zero values, respectively.
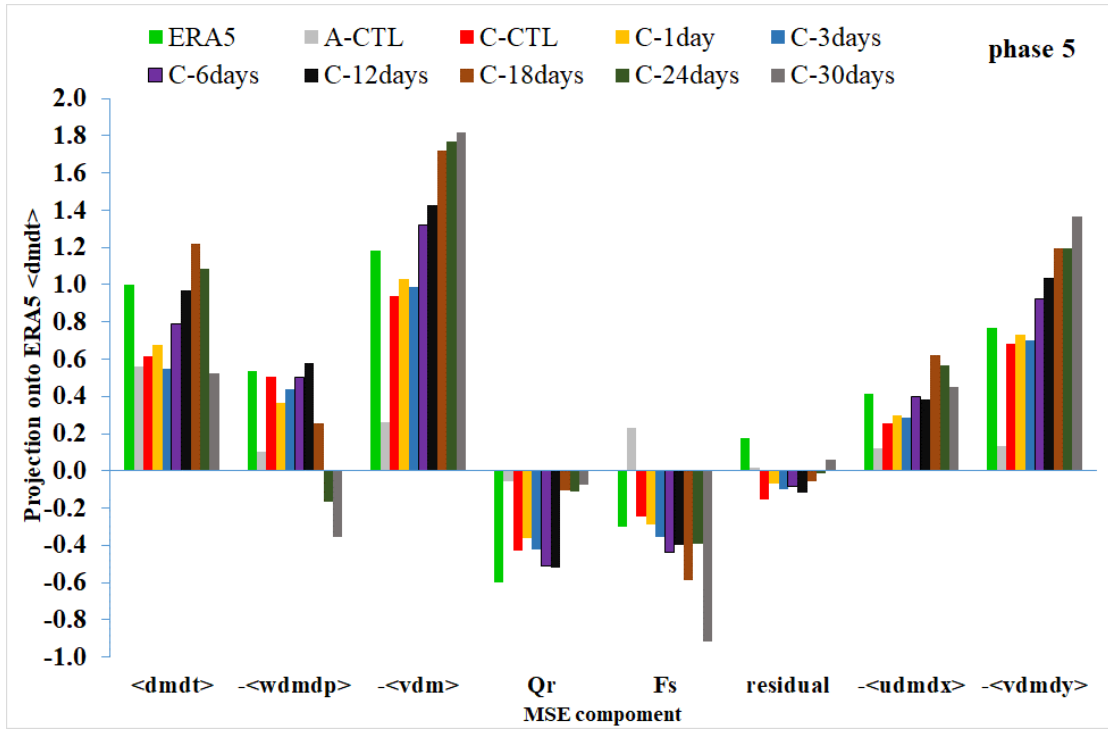
1118

1119

1120 **Figure 9.** Averaged 20–100-day filtered column-integrated MSE budget terms
1121 (J kg−1 s−1) in 10° S–0° N/S, 120–150° E for ERA5 and all model simulations.
1122 Colors represent different datasets: green for REA5, light gray for A–CTL, red, orange
1123 and wathet blue for high-frequency experiments (C–CTL, C–1day, and C–3days,
1124 respectively), purple, black, dark brown, dark green, and dark gray for low-frequency
1125 experiments (C–6days, C–12days, C–18days, C–24days, and C–30days, respectively).
1126 The bars from left to right represent MSE tendency (<dmdt>), vertical MSE advection
1127 (-<wdmdp>), horizontal MSE advection (-<vdm>), surface latent heat flux (LH),
1128 surface sensible heat flux (SH), shortwave radiation flux (<SW>), longwave radiation
1129 flux (<LW>), and residual terms.

1130


1131

Figure 10. Filtered the column-integrated MSE tendency (J kg−1 s−1, shading),
precipitation (mm d−1, contours interval 1.5) and 850-hPa wind (green vector,
reference vector 2 m s−1) in phase 5: (a) ERA5, (b) A−CTL, (c) C−CTL, (d) C−1day,
(e) C−3days, (f) C−6days, (g) C−12days, (h) C−18days, (i) C−24days, and (i)
C−30days. Solid-red, dashed-blue, and thick-black curves represent positive, negative,
and zero values, respectively.

1138

Figure 11. The projection of each MSE component onto the ERA5 column-integrated MSE tendency at phase 5 over the MC (20° S–20° N, 90–210° E): <dmdt>, -<wdmdp>, -<vdm>, Qr, Fs, and residual; decomposition of horizontal MSE advection to zonal and meridional advection (-<udmdt> and -<vdmdy>).
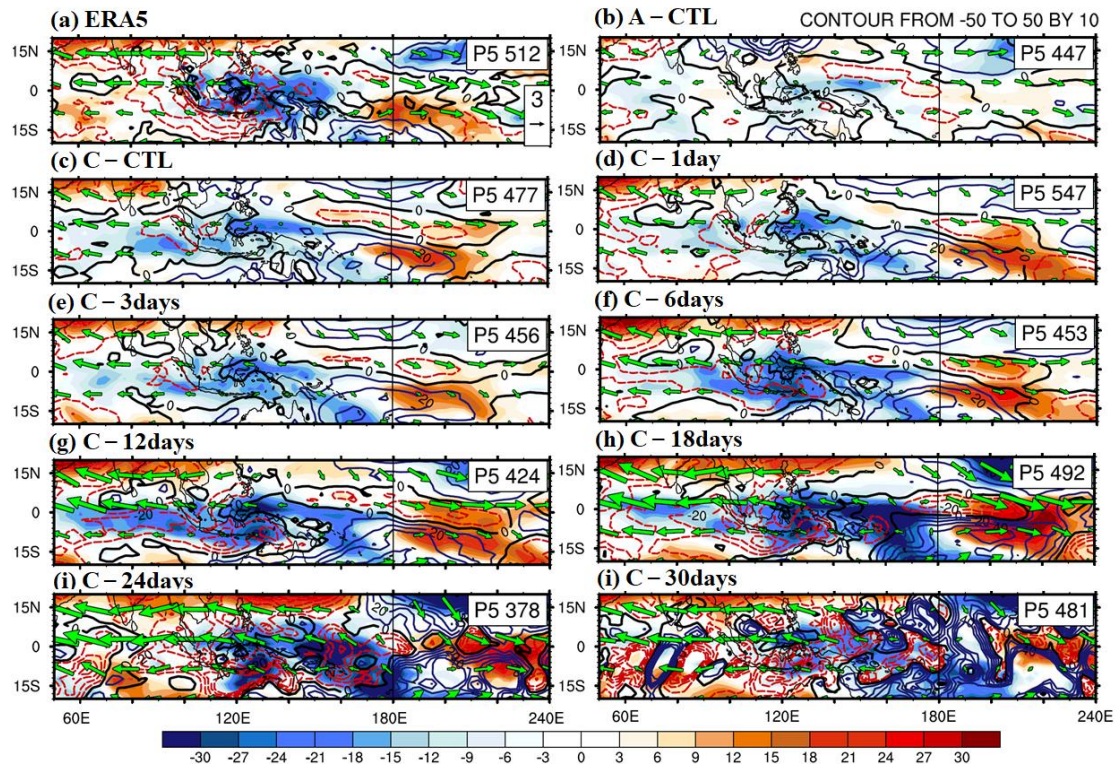
Figure 12. Filtered column-integrated vertical (J kg−1 s−1, shading) and horizontal MSE advection (J kg−1 s−1, contours interval 6.0), and 200-hPa wind (green vector with reference vector 3 m s−1): (a) ERA5, (b) A−CTL, (c) C−CTL, (d) C−1day, (e) C−3days, (f) C−6days, (g) C−12days, (h) C−18days, (i) C−24days, and (j) C−30days. Solid-blue, dashed-red, and thick-black curves represent positive, negative, and zero values, respectively.

1151
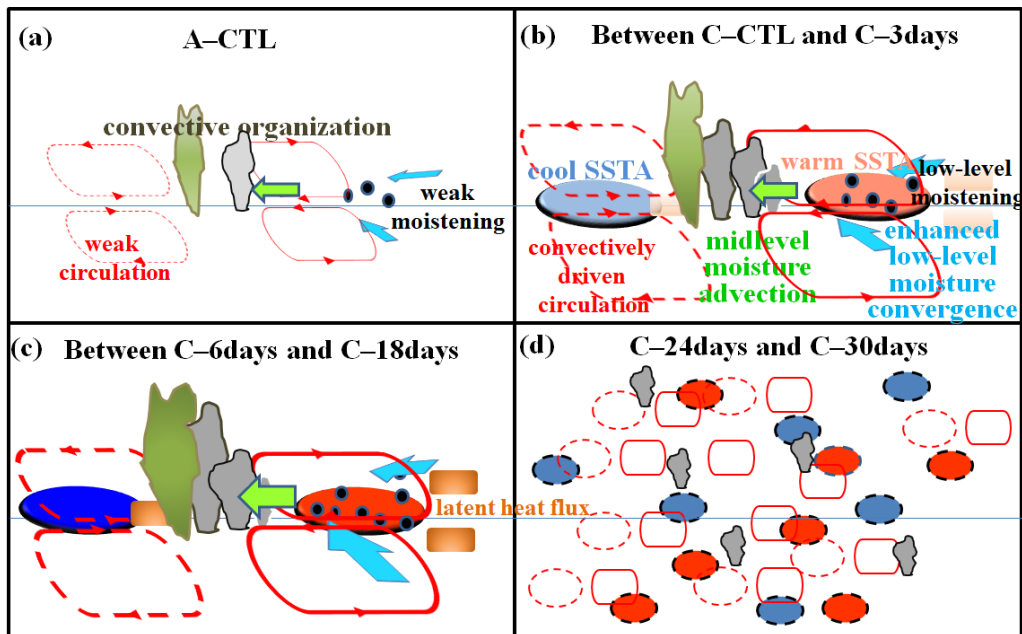
1152

1153 **Figure 13.** Schematic diagrams illustrate the anomalous circulation and moistening
1154 processes during the eastward propagation of the MJO in experiments: (a) A−CTL, (b)
1155 high-frequency SST feedback experiments (C−CTL, C−1day, and C−3days), (c) low-
1156 frequency SST feedback experiments (C−6days, C−12days, and C−18days), and (d)
1157 C−24days and C−30days experiment. In each panel, the horizontal line represents the
1158 equator. The size of clustering gray clouds indicates the strength of convective
1159 organization. A red ellipse indicates convection-driven circulation. In the coupled
1160 simulations, light red (blue) filled ovals represent warm (cold) SST anomalies,
1161 respectively, and grass green filled rectangle represent latent heat flux. Unresolved
1162 convective processes are indicated by black dots representing low-level moisture
1163 convergence. Low-level moisture convergence into the equatorial trough is shown by
1164 light blue arrows, while midlevel moisture advection is represented by left-pointing
1165 green arrows. The deeper colors or thicker lines on the map indicate stronger anomalies
1166 of the MJO perturbations. Note: The concept of the figure is based on DeMott et al.
1167 (2014).