§1 Response to Reviewer #1

(Note: Referee comments in black, *reply in bold italics*)

This paper develops a unique ultrahigh scalability parallelized NEMO ocean model on the Sunway supercomputer architecture. A new many-core optimization using remote memory access (RMA) blocking and dynamic cache scheduling can effectively accelerate the performance more 90% of ideal bandwidth. The strategical optimization based on mixed precision improves the parallel performance to achieve more than 99% with appropriate 28 million cores. This represents significant progress in the ocean modelling parallelization. The impact will be tremendous. However, there are two major issues to be addressed. *Reply: We would like to express our sincere thanks for your valuable comments. The revised manuscript has been refined according to your suggestions. These comments and suggestions greatly help us in improving the quality of this manuscript.*

Major issues:

1. A very important aspect of improving the parallel performance is to ensure the reproducibility. This study provide a significant speed up combining hardware and software optimization. However, using the mixed precision can change the solution if different cores are used? Can the mixed precision affect the reproducibility and consistency? The authors should address and discuss this issue to ensure the robustness of the proposed model. *Reply: Thank you for your valuable suggestions. Firstly, this work proposed the optimization algorithm for NEMO, based on the new generation Sunway platform. We tested several times and the results can be reproduced, even with different processes. Although this work focused on the NEMO and Sunway platform, the algorithms, such as longitude-latitude-depth, double-single-half mixed precision, are general methods and can be used for other OGCMs or platforms. Certainly, as we used several features of new generation Sunway platform (e.g., the RMA commination between CPEs, half-precision in CPEs) enabling the efficiency, the speed up may become lower in other platforms. Secondly, we ran the error growth tests based on the method proposed by Baker et al. 2016*

after the mixed-precision optimization. Yes, the mixed-precision affects the results. And the effects are similar with these of the perturbation coefficient as $O(10^{-10})$ (Fig r1), which can be accepted we think.

Following your suggestion, we added the discussion on the tests in section 3.3.



Fig r1. Z-score biases of the sea surface temperature in ensemble run (grey lines) with perturbation coefficient as $O(10^{-10})$ and the mixed-precision experiment (red line)

2. The other issue is related to the commonly used ensemble simulation while different precision is used. Baker et al. (2016) evaluated the consistency and proposed the perturbation requires half precision (see the large variation of SST simulation in Fig. 3 of Baker et al., 2016). The mixed-precision OGCM can causes the Bit-to-bit inconsistency within ocean model. Is that correct? How can this MP approach compare with the reduced convergence accuracy in the solver, which can also speed up the simulation?

Reply: Thank you for the constructive suggestion. Yes, the mixed-precision can cause the bit-to-bit inconsistency within ocean model. In order to verify the correctness of the mixedprecision results, we provide the perturbation simulation experiment for the temperature results following Baker et al. (2016), in which random disturbance conditions for the initial temperature are configured within NEMO program. At the same time, we also selected 101 sets of data as experimental simulation results to verify the correctness of the results of NEMO_v4.0, of which 100 sets are temperature results with perturbation conditions, and the remaining one is the mixed-precision experiment of swNEMO_v4.0.

According to the Baker et al. (2016), we also selected $O(10^{-14})$ as the perturbation coefficient, but found that the Z-score obtained by mixed-precision simulation was completely out of the shadow area formed by 100 simulations with double-precision (Fig r2). Therefore, we increased the perturbation coefficient and he mixed-precision Z-score gradually approached the shadow area. We found that the disturbance had a greater influence in the first few years, then it gradually decreased and tended to be stable after several years(Fig r2, r3). As shown Fig r3, when the perturbation coefficient is $O(10^{-11})$, Z-score of mixed-precision simulation fall partially in the region formed by doubleprecision simulations. When the perturbation coefficient equals to $O(10^{-10})$, the Z-score completely falls in the shadow area (Fig r1), which indicates the effects of mixed-precision are similar with these of the perturbation coefficient as $O(10^{-10})$.

Following your suggestions, we added the discussion on the tests in section 3.3.



Fig r2. Z-score biases of the sea surface temperature in ensemble run (grey lines) with perturbation coefficient as O(10^-14) and the mixed-precision experiment (red line)



Fig r3. Z-score biases of the sea surface temperature in ensemble run (grey lines) with perturbation coefficient as O(10^-11) and the mixed-precision experiment (red line)

Minor issues:

1. Line 7, Abstract: DMA is not defined. what do you mean by DMA? Do you refer to remote memory access (RMA) or something else (Direct memory access)?

Reply: Thank you. DMA means Direct memory access. The definition is added in the revised abstract.

2. Line 21, change "the one of most important directions of OGM development" to " one of the most important directions for the OGCM development".

Reply: Thank you. It was refined.

3. Line 23, change "horizontal resolution doubled" to "doubled horizontal resolution". *Reply: Thank you. It was refined.*

4. Line 31, what do you mean by 6.8x? Do you mean by a factor of 6.8? If so, I suggest to change this rather than symbol x. This can be seen elsewhere.

Reply: Thank you. 6.8x means 6.8 times. It was refined in the revision.

5. Line 31, "achieved the performance of 408 Intel Westmere cores on four K20 GPUs". What do you mean by this? What performance is achieved? Equivalent performance of 408 Intel Westmere cores using 4 K20 GPUs? However, how many gpu cores for the K20 GPUs? The cores of Intel processors are not equivalent to the cores of GPU processors, right? *Reply: Thank you. Yes, for the calculation example of POM designed on GPU, the computing performance by using 4 K20 GPUs is equivalent to the performance by using 408 Intel Xeon x5670 CPUs.*

It was refined as "achieved the equivalent performance of 408 Intel Westmere cores by using four K20 GPUs" for clarity in the revision.

6. Line 27-43, Table 1 and the review of performance improvement are impressive. However, are they all for the improvement of ocean models? FUNWAVE seems to be a wave model? What about MUSNUM? I suggest to separate wave model to a different category since the architecture of a wave model is totally different from the ocean dynamical model. Also, what's the difference between POP2 and CESM-HR? It seems they are both 3600x2400 resolution, right? While the performances are similar but the maximum scales quite different (~4 times). I suggest to tabulate the representative ocean model performance development here (exclude other types of models) and discuss the most significant development.

Repy: Thank you for the suggestions. The Hydrostatic LAM is the atmosphere model. FUNWAVE and MASNUM are both the ocean surface wave model. CESM-HR is the highresolution version of CESM, which including the POP ocean model. We tried to give progress on the numerical earth model, including the atmosphere model and ocean model at first. However, we total agreed with you that it can confuse the reader indeed. Therefore, wea remove the Hydrostatic LAM, FUNWAVE, MASNUM, and CESM-HR and only leave the progress on OGCMs. And we also changed the title of Table 1 to "Research on the OGCMs based on heterogeneous architectures" in the revision.

7. Line 44-54, the discussion here also mixes the parallelization of atmosphere model, ocean hydrodynamic model and ocean wave models. Particularly, the required global barriers are also different. This can significantly impact the model overall performance. Don't mix the

ocean hydrodynamical model with other types of model in the comparison because the solvers are totally different. Also, this paragraph mixes the different limitations of different models to improve their performance without specific focus. I suggest to reorganize this discussion to be more focused and related to the improvement relevant to this study.

Reply: Thank you the valuable suggestions. We total agree with you. It may confuse the reader. Therefore, we only leave the OGCMs and re-organized this paragraph in the revision.

8. Line 46, change "only improved" to "is only improved".

Reply: Thank you. It was refined.

9. Line 56, change "Exa-scale to "Exascale".

Reply: Thank you. It was refined.

10. Line 78, is "GYRE-PISCES" abbreviation? If it is not a well-known typical benchmark test name, I suggest to described this briefly here or used a whole name.

Reply: Thank you. GYRE-PISCES is the benchmark abbreviation of the Gyre Pelagic Interactions Scheme for Carbon and Ecosystem Studies. The detail of GYRE-PISCES is described in section 4, therefore we added the whole name of GYRE-PISCES here in the revision.

11. Section 2 describes the architecture of Sunway TaihuLight. The detailed information has been provided extensively. I suggested to remove the technical details but comment and address on the specific features facilitating the performance enhancement used in this paper here.

Reply: Thank you. In the revision, we removed "MPE is based on SW64 instruction set, with a 32KB L1 instruction cache, a 32KB L1 data cache and 512KB L2 cache."

12. Section 2 also describes NEMO model. What's the difference between NEMO and NEMO4 you raised at line 81? I suggest to move NEMO description into section 3 in associated the porting of NEMO.

Reply: Thank you. In the revision, we moved NEMO description into section 3 in associated the porting of NEMO.

13. Line 120, how "adaptive" works in this four level parallelization? Two levels are using domain decomposition. One level is MPE-CPE asynchronous parallel. Is this performed at compiler level (processor specific) or user specific level? One level is the vector reconstruction. This should be done within the compiler level. Can the author comment which level contributes mostly to help the performance in the current implementation?

Reply: Thank you. The main contribution of this optimization scheme comes from the division of tasks to the CPEs, which enable the model using the slave processer. In terms of adaptability, SW26010pro has heterogeneous architecture, which is different from the traditional homogeneous CPU architecture. MPE-CPE parallelization cannot be automatically implemented by the compiler. Code-level optimization is required to achieve specific data division and efficient transmission. Therefore, we re-consider the task division and parallelism according to the hardware characteristics of Sunway to fully using the computing capacity. Vectorization parallelism can usually be completed automatically by the compiler, but for complicated code logic, the compiler cannot be well optimized, so we manually implemented vectorization code to achieve better performance.

In the revision, we added the explanation on the different parallelization schemes to clarify clearly in section 3.

14. Line **130**, a reference is helpful for this MPE-CPE asynchronous parallelization. As described in line 131, IO can be independently separated for sure. However, how boundary data exchange can be parallelized aside from the computation? Normally, the ocean model kernel requires some global communication to solve the pressure equation (normally at least 3, can reduced to 1 in some parallelization). How can the data exchange be performed using MPE-CPE asynchronous parallelization. Some information will be helpful for the readers.

Reply: Thank you for your constructive suggestions. We added the references in the revision. Gu et al. (2022, doi:10.1016/j.scib.2022.03.009) proposed multi-level optimization method to make use of the heterogeneous architecture. In the first level of the method, they designed pre-communication, communication, and post-communication in the code based on MPE-CPE asynchronous parallelism architecture. As the default barotropic solver in NEMO4 is explicit method with small time step, which is more accurate and more suitable for high resolution without filter, instead of implicit or split-explicit methods (e.g., PCG), there is no global communication. Therefore, it is only necessary to update the information of the halo region between different processes. Moreover, in explicit method, most boundary information exchanges are independent of the partition data in the process and can be used for asynchronous parallelization.

Following your suggestions, the description of boundary data exchange features is added in section 3.1.2 in the revision.

15. 1.3, for latitude-depth decomposition, since this depth is not parallel friendly dimension. The parallelization requires level dependence. That means if the depth dimension is changed, the user needs to adjust something for LDA. Is that correct?

Reply: Thank you. As we design the dynamical block size methodology based on the level number and solve the data dependency problem by exchanging boundary data via the RMA (detail please find in Section 3.2.1), there is no need to adjust codes or parameters for LDA if the depth dimension is changed.

16. Line 171-line 174, What is alpha_1, beta_2 and beta_1, beta_2 within the equations. The notations are not standard mathematically. Is f a function? or a value represented by the 2nd line? These equations should be labeled numbers. What is x? is x an array? Please rewrite the formula in a more mathematical way?

Reply: Thank you for your suggestions. We forgot it. In fact, alpha_1, beta_1, and beta_2 are only the coefficient. And f is the mathematical formula for the loop segment, x means the x-axis (longitude axis) in the coordinate system. We revised the formula in the revision.

17. 2 discusses the optimization used here. It seems 3.2.1 is used as level 3 described in 3.1. Is that correct? Or combining the 4 level parallelization? Is 3.2.2 used in the MPE-CPE asynchronous parallel or something different? If so, I suggest to reorganize this discussion and make this clear. Section 3.3 discusses the mixed precision optimization, which I believe is different from the four level parallelization. Also, line 108-113, describes three major contributions while the 2nd one is used within the 1st four-level parallelization, right? *Reply: Thank you. The section 3.1 introduces mainly the design of the overall parallel framework of NEMO, which emphasizes the connection among different levels in the parallel framework and the systematic framework constructed for the unique on-chip heterogeneity of Sunway. The section 3.2.1 described the paralleling-optimization scheme of local computing hot-spots based on Sunway. In other words, section 3.1 presents a general view of optimization, while section 3.2.1 gives the optimization in detail for local computing hot-spots.*

In the revision, we added the brief introduction to these optimization scheme before section 3.1.

18. Line 216, the maximum biases reach 0.05%. Are these biases the deviation between DP and HP? However, considering the chaotic behavior with time, can this bias propagate? Can the biases become larger with time? If this is the case, can the model result get bit-to-bit consistency which is a very important feature for ocean model within an earth system model? For the pressure solver within the ocean dynamical kernel, do you still use DP? If you still use DP, the convergence will still take time. Can you compare this optimization with another easier way by reducing the pressure solver criteria to a lower level (change from 10^-13 to 10^-7)? Changing the pressure solver criteria to a lower level can significantly reduce the precision? Do I miss something? Normally for the ocean model, the most intensive computational cost is the pressure solver rather than the tracer equation, right? Why not use this approach while still preserving the precision?

Reply: Thank you for the constructive suggestion.

On the one hand, the mixed-precision can cause the bit-to-bit inconsistency within ocean model. In order to get the tolerance of the mixed-precision results, we provide the perturbation simulation experiment for the temperature results following the Baker et al. (2016). According to the Baker et al. (2016), we also selected $O(10^{-14})$ as the perturbation coefficient, but found that the Z-score obtained by mixed-precision simulation was completely out of the shadow area formed by 100 simulations with double-precision. Therefore, we adjusted the perturbation coefficient. The mixed-precision Z-score gradually approached the shadow area when increasing the perturbation coefficient. In the process, we found that the disturbance had a greater influence in the first few years, then it gradually decreased and tended to be stable after several years(Fig r2, r3). As shown Fig r3, when the perturbation coefficient is $O(10^{-11})$, Z-score of mixed-precision simulation falls partially in the region formed by double-precision simulations. The mixed-precision Zscore completely fell in the shadow area when the perturbation coefficient equals to $O(10^{-10})$.

On the other hand, as the default barotropic solver in NEMO4 is explicit method with small time step, which is more accurate and more suitable for finer resolution without filter, instead of implicit or split-explicit methods (e.g., PCG). According to analysis of hotspot testing, we found that the most intensive computational cost is the tracer equation.

The above description was added in the Conclusion and Discussion section in the revision.

19. Line 223, change "periodical" to "periodic". What do you mean by "North Pole folding"?Do you mean "Displaced North Pole"?

Reply: Thank you. It's tripolar grid, not the dual-polar grid with Displaced North Pole.

20. Line 230, change "is equal to" to "equals to".

Reply: Thank you. It was refined.

21. Line 229-234, this paragraph is confusing. It describes "three experiments with 2 km, 1 km, and 500m". However, each experiment uses 8 different parallel scales (Table 3),

resolution ranging from 9km to 1km. Do you use 2km, 1km and 500m or 9km to 1km? I suggest to clarify these numerical experiments. What's your definition of weak scaling and strong scaling.

Reply: Sorry for confusing you. Besides the strong scalability experiments with 2 km, 1 km, and 500 m, we also carried out the weak scalability experiments. The strong scaling is tested by running the model with different numbers of threads, while keeping the same resolution. The weak scaling is tested by running the model with a fixed grids-per-thread ratio. In other words, the weak scaling means keep similar grids per thread. Therefore, we should fine the resolution with increasing used threads (Table 3).

22. Line 242, what is "CPEs parallel method"? Is this your control experiment? This has nothing to do with the MPE-CPEs parallelization, right? However, does CPEs parallelization still use four-level parallelization? Can you isolate the individual performance enhance resulting from the approaches discussed in section 3?

Reply: Thank you for your suggestions. CPEs parallel method is the third level of the fourlevel parallelism method, which is the parallelization of 64 CPEs, while MPE-CPES is the second level parallelism, which regards the CPEs as a component, and it is described the parallelism between the component and the main processing element.

In the revision, we added the explanation on the different parallelization schemes to clarify clearly.

23. Line 248-253, do you include the performance increase due to the mixed-precision approach here or just the DMA and FLOPS for the DP? The timing may be different. *Reply: Thank you. The performance results are from the model based on all the optimizations, including the four level and mixed-precision approaches.*

In the revision, we added the explanations to clarify clearly.

24. Line 256, can you describe these five kernels briefly? What's the major differences? *Reply: Thank you. In fact, the five kernels are the most time-consuming chunks, which are only a fraction of the physical process. However, they are all specific implementations of*

Stencil computing. To avoid confusing reader, we added the explanations for five kernels in the revision.

25. 8, do you use the real time? Or measure the clock? These are built-in hardware, is it right? Therefore, these values only refer to the access time, right?

Reply: Sorry for confusing you. It is the clock time measured by built-in hardware. In the revision, we revise the y-axis of Fig. 8 from Runtime to Clock time. We made a small typo in the last paragraph of section 4.1. The sentence "the clock cycle is reduced from 61 x 10^3 seconds to 0.6 x 10^3 seconds" has been changed to "the clock cycle is reduced from 61 x 10^-3 seconds to 0.6 x 10^-3 seconds".

26. Section 4.2, is the implementation only performed for the tracer equations? Fig. 9 shows only the tracer integration which is only a very small portion of the overall run time. Can the author show the dynamical solver part which requires the most intensive computation (particularly the barotropic solver) instead of this tracer solver?

Reply: Thank you. We run the performance-testing tool and found that one of the most time-consuming subroutines is tracer integration, so we focus on it for optimization. We think the barotropic solver being changed in NEMO4 leads to different bottleneck. The default barotropic solver in NEMO4 is explicit method with small time step, which is more accurate and more suitable for finer resolution without filter, instead of implicit or splitexplicit methods (e.g., PCG, needing a lot of global communication). As there is no global communication and only necessary to update the information of the halo region between different processes, the barotropic solver is not the bottleneck anymore.

27. Since this is GMD rather than computational journal, can the authors show the final results? It will be useful to examine if the GYRE-PISCES configuration reaches the expected solution as others. A figure with velocity and temperature fields will be enough, particularly what specific features can be found at 500m resolution. The potential impact of mixed precision optimization can also be discussed.

Reply: Thank you for the constructive suggestions. Yes, it will be better if we can show the results with 2 km, 1km or 500 m resolutions. However, the output is too huge! We tried to store the results with 1 km resolution, but the data volume is more than 65 TB per output. Therefore, we did not store the output. And it's also the reason we did the validation for mix-precision by using the low resolution (0.5-degree). The experiment shows that the mixed-precision affects the results, but when the perturbation coefficient is around $O(10^{-10})$, effects are very small and can be accepted.

28. Line 286, the description is very superficial, any supporting evidence? *Reply: Thank you. It is a general description and summary for the following paragraph. To avoid confusion, we remove this paragraph in the revision.*