

# 1 **An internal solitary wave forecasting model in the northern South** 2 **China Sea (ISWFM-NSCS)**

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11 **Abstract.** Internal solitary waves (ISWs) are a ubiquitous phenomenon in the dynamic ocean system, which play a crucial role  
12 in driving transport through turbulent mixing. Over the past few decades, numerical modelling became a vital approach to  
13 investigate the generation mechanism and spatial distribution of ISWs. The northern South China Sea (NSCS) has been treated  
14 as a physical oceanographic focus of ISWs in massive numerical studies since last century. However, there was no systematic  
15 evaluation of a reliable three-dimensional (3D) model about accurately reproducing ISW characteristics in the NSCS. In this  
16 study, we implement a 3D ISW forecasting model in the NSCS and quantitatively evaluate the requirements of factors (i.e.,  
17 model resolution, tidal forcing, and stratification selection) in accurately depicting ISW properties by comparing with  
18 observational data at a mooring station in the vicinity of the Dongsha Atoll. Firstly, the 500 m-resolution model can basically  
19 reproduce the principal ISW characteristics, while the 250 m-resolution model would be a better solution to identify wave  
20 properties, specifically increasing 40% accuracy of predicting characteristic half-widths. Nonetheless, a 250 m-resolution  
21 model spends nearly fivefold computational resources of a 500 m-resolution model in the same model domain. Compared with  
22 the former two, the model with a lower resolution of 1000 m severely underestimates the nonlinearity of ISWs, resulting in an  
23 incorrect ISW field in the NSCS. Secondly, the model with eight (or thirteen) primary tidal constituents can accurately  
24 reproduce the real ISW field in the NSCS, while the one with four main harmonics (M2, S2, K1 and O1) would underestimate  
25 averaged wave-induced velocity for about 38% and averaged mode-1 wave amplitude for about 15%. Thirdly, the model with  
26 the initial condition of field-extracted stratification gives a better performance in predicting some wave properties than the  
27 model with climatological stratification, namely 13% improvement of arrival time and 46% improvement of characteristic  
28 half-width. Finally, background currents, spatially varying stratification and external (wind) forcing are discussed to reproduce  
29 a more realistic ISW field in the future numerical simulations.

## 30 **1 Introduction**

31 Numerical simulations, one of the most important approaches to investigate internal solitary waves (ISWs) in the world's  
32 oceans, have been gradually developed from two-dimensional (2D, e.g., Du et al., 2008; Buijsman et al., 2010) to three-  
33 dimensional (3D, e.g., Zhang et al., 2011; Alford et al., 2015) over the past few decades. South China Sea (SCS), the largest  
34 marginal sea in the northwest Pacific, has been commonly known as an active region of ISWs via massive in-situ observations  
35 (cf. Ramp et al., 2004, 2019; Farmer et al., 2009, 2011) and numbers of remote sensing images (cf. Liu et al., 2004; Zheng et  
36 al., 2001, 2007). Although the vertical structure and horizontal distribution on the sea surface of ISWs can be nicely illustrated  
37 by field measurements at sparse sites and satellite images, respectively, they are still of limited value for telling a complete  
38 story of ISWs in the entire northern SCS (NSCS). Complementary to in-situ and remote-sensing observations, numerical model  
39 can give a comprehensive characterization in the ISW field in case of realistic initial and boundary conditions. Hence, we take  
40 NSCS as an example to introduce a high-performance ISW forecasting model and quantitatively evaluate requirements of  
41 model configurations (i.e., resolution, tidal forcing, and stratification selection) for accurately reproducing a real ISW field.

42 With the development of higher performance computing facilities, a variety of 3D realistic numerical models with structured  
43 and unstructured grids were established for simulating ISWs in the NSCS (see Table 1), such as MITgcm (Vlasenko et al.,  
44 2010), SUNTANS (Zhang et al., 2011) and FVCOM (Lai et al., 2019). Meanwhile, the model capabilities have been  
45 continuously improved (Simmons et al., 2011). Specifically, the model resolution was effectively enhanced from 250-1000  
46 ( $\Delta x$ - $\Delta y$ ) m (Guo et al., 2011) in a limited domain to 150/300 m in a large domain including the entire NSCS (Zeng et al.,  
47 2019). From past to present, the barotropic tidal forcing dataset TOPEX/Poseidon Solution (TPXO, Egbert and Erofeeva, 2002)  
48 and climatological stratification dataset World Ocean Atlas (WOA, Locarnini et al., 2018) have been updated with higher  
49 resolutions both in horizontal and vertical, providing more realistic and precise boundary and initial conditions in the model  
50 configurations. Although it is commonly known that a higher-resolution model can tell a more complete story of ISWs, the  
51 usage of computational resources is worthy to be considered. Thus, what resolution of model is needed to give an accurate  
52 depiction of ISW fields and simultaneously save the computational cost is still a question.

53 Even though numbers of previous in-situ observations have shown the four barotropic tidal constituents (M2, K1, O1 and  
54 S2) are dominant at the Luzon Strait (Zhao and Alford, 2006; Farmer et al., 2009), the other barotropic tidal constituents (e.g.,  
55 N2, K2, P1 and Q1) are also non-negligible (Beardsley et al., 2004). Historically, numerical simulations with different numbers  
56 of tidal constituents have been widely employed to investigate the physical dynamics of ISWs in the NSCS, i.e., single K1  
57 harmonic (Li, 2014), four tidal harmonics (Buijsman et al., 2010), and eight primary tidal harmonics (Alford et al., 2015; Jin  
58 et al., 2021). Among these, eight tidal constituents were most commonly applied in the 3D models. However, other tidal  
59 constituents, such as M4, MS4, MN4, MM, and MF, were yet to be considered. The questions are whether a single tidal  
60 constituent can reproduce a real ISW field and, if not, how many tidal constituents are required for running an accurate 3D  
61 realistic ISW model.

62 Apart from resolution and tidal forcing, stratification selection is also an important factor in improving model accuracy. A  
63 horizontally homogenous stratification profile was normally implemented as an initial condition in a 3D realistic model (cf.  
64 Zhang et al., 2011; Lai et al., 2019). Specifically, a domain average of the climatological dataset (WOA) is one of the most  
65 common options (Vlasenko et al., 2010; Zeng et al., 2019), since the in-situ observational data are relatively inaccessible. Once  
66 the field data at an isolated mooring station are available, are they a better choice than the climatological data to be the model's  
67 initial condition? What if the mooring is near-field (in the vicinity of the Luzon Strait, the ISW generation site) or far-field  
68 (e.g., in the deep basin or over the continental slope and shelf)?

69 In this paper, we attempt to introduce a high-performance ISW forecasting model and evaluate the roles of different  
70 resolutions, initial and boundary conditions in accurately reproducing ISWs via a series of sensitivity 3D non-hydrostatic  
71 numerical simulations. The paper is structured as follows. In section 2, configurations of the 3D forecasting model are  
72 introduced, as well as the simultaneous remote sensing images and in-situ observations. The model calibrations are presented  
73 in section 3. In section 4, we quantitatively illuminate the requirements of model resolutions, tidal constituents, and initial  
74 stratification selection for a reliable 3D ISW forecasting model. Discussion and conclusions follow in section 5.

## 75 **2 Data and Methods**

76 To characterize the real ISW field in the NSCS, we implement an ISW forecasting model (ISWFM-NSCS) and compare the  
77 modelled wave properties on the continental slope with those observed at in-situ mooring station DS (marked as magenta star  
78 in Fig. 1a). Remote sensing images are downloaded for the model calibration as well.

### 79 **2.1 Numerical modelling**

80 Although running a 2D slice model is much more economical than running a 3D model from the perspective of  
81 computational resources, the 2D model cannot correctly reproduce the ISW field in the real ocean (see Appendix A). Therefore,  
82 we implement a realistic 3D non-hydrostatic primitive equation ocean solver (MIT general circulation model, MITgcm,  
83 Marshall et al., 1997) in the spherical coordinate to reproduce the ISWs features in the NSCS. The model domain ( $115.8^{\circ}$  –  
84  $123.8^{\circ}$ E,  $17.8^{\circ}$  –  $22.3^{\circ}$ N, see blue box in Fig. 1a) includes the main generation site of ISWs (i.e., Luzon Strait) and the mooring  
85 station DS on the continental slope. Bathymetry data are derived from the global gridded bathymetry dataset GEBCO  
86 ([https://www.gebco.net/data\\_and\\_products/gridded\\_bathymetry\\_data](https://www.gebco.net/data_and_products/gridded_bathymetry_data)). To keep the consistency with the instrumental  
87 deploying period, we start the model from 00:00 UTC 5 August 2014 and last fifteen days. Previous statistical analyses, based  
88 on SAR images in the NSCS from 1995 to 2001, also indicated that ISW occurrence frequencies were relatively high in August  
89 (Zheng et al., 2007). The initial model temperature and salinity profiles (see black and blue lines in Fig. 1b) are derived from  
90 the WOA18 climatology dataset (World Ocean Atlas 2018) by spatially averaging the monthly output in August, resulting in  
91 horizontally-uniform conditions. Density and buoyancy frequency profiles are shown as black lines in Figs. 1c and 1d.

92 To ensure ISWs can be physically derived and consider the computational efficiency, the horizontal cell ( $\Delta x$ ) is set as 500  
93 m in both zonal and meridional directions. In order to satisfy the high-mode vertical resolution requirements, 90 vertical layers  
94 are spaced in accordance with the hyperbolic tangent function (Stewart et al., 2017), namely ranging from 5 m near the surface  
95 to 120 m near the sea bed (in the deep water). We impose a time step of  $\Delta t = 10$  sec to satisfy the Courant-Friedrichs-Lewy  
96 (CFL) conditions in both horizontal and vertical. The Coriolis parameter is varying with latitudes in the entire model domain.  
97 To determine whether non-hydrostatic mode is necessary, we also run a hydrostatic model (not shown). It is noting that fake  
98 internal solitary-like wave trains, also called spurious non-hydrostatic processes (Alvarez et al., 2019), are clearly visible at  
99 first glance, suggesting that hydrostatic mode is inappropriate for a high-resolution model of ISWs. We therefore configure  
100 the model in non-hydrostatic mode.

101 The control run (Exp. 1, **500m\_8HARs**) is driven by eight main tidal constituents (M2, S2, N2, K2, K1, O1, P1, and Q1) on  
102 the four open boundaries with values originated from the Oregon State University TOPEX/Poseidon Solution (TPX08-atlas  
103 data) with  $1/30^\circ$  resolution (Egbert and Erofeeva, 2002). A 25 km wide sponge layer is imposed on each lateral boundary to  
104 absorb internal wave energy and avoid wave reflection back to the inner region. Quasi-steady conditions occur after 3 days  
105 (see Appendix B), so the model results are analyzed over the remaining 12 days (8 – 20 August). The sampling rate of model  
106 outputs is 1 h interval for the entire model domain in the control run (**500m\_8HARs**) and single-point outputs with a higher  
107 sampling rate of 1 min at the selected station DS for recording the local ISW properties, and thereby comparing to the in-situ  
108 observations. Constant horizontal and vertical eddy viscosity and diffusivity coefficients are imposed as  $A_h = 0.5 \text{ m}^2 \text{ s}^{-1}$ ;  $A_v =$   
109  $5 \times 10^{-3} \text{ m}^2 \text{ s}^{-1}$ ;  $K_h = 0.5 \text{ m}^2 \text{ s}^{-1}$ ;  $K_v = 5 \times 10^{-3} \text{ m}^2 \text{ s}^{-1}$  to eliminate grid-scale instability (Legg and Huijts, 2006). The bottom  
110 stresses are parameterized using a quadratic law with a bottom drag coefficient of  $C_d = 2.5 \times 10^{-3}$ .

## 111 **2.2 Remote sensing images**

112 Remote sensing imagery contains lots of detailed information of ISW properties, including wave crest lines and their arrival  
113 time, which was commonly applied in the NSCS (Liu et al., 2004; Zheng et al., 2007). Here we download two MODIS true-  
114 color pictures with a horizontal resolution of 250 m at 05:15 UTC on 14 August and at 02:50 UTC on 15 August 2014,  
115 respectively. In addition, we compute the horizontal gradients of sea surface height ( $|\nabla\eta|$ , in the unit of  $\text{cm km}^{-1}$ ), which detects  
116 the variations in surface roughness caused by the ISW-induced convergent and divergent currents, thereby producing  
117 analogous images to the satellite images. Note that the model is hourly sampled, so we select the closest snapshots of  $|\nabla\eta|$  at  
118 05:00 UTC on 14 August and at 03:00 UTC on 15 August 2014 to compare with MODIS images.

## 119 **2.3 In-situ measurements**

120 The through-water-column mooring station DS (magenta star in Fig. 1a) is located at  $117^\circ 44.7' \text{E}$ ,  $20^\circ 44.2' \text{N}$  in the vicinity  
121 of the Dongsha Atoll, which was deployed at a water depth of  $\sim 1250$  m from 1 August to 28 September 2014. Three acoustic  
122 Doppler current profilers (ADCPs) measured currents ranging from a depth of 1180 m to the sea surface every two minutes

123 with 16-m vertical bins in upper 900 m and 8-m vertical bins below 900 m. The mooring was configured by temperature  
 124 sensors, a conductivity-temperature-depth (CTD) sensor and conductivity-temperature (CT) sensors at different water depths.  
 125 The temperature sensors were at 10 m, 30 m, 50 m, 90 m, 130 m, 150 m, 170 m, 250 m, 350 m, 500 m, 600 m, 700 m, 800 m,  
 126 950 m, 1050 m, and 1220 m, respectively; the CTD sensor was at 1100 m; and the CT sensors were at 20 m, 40 m, 70 m, 110  
 127 m, 150 m, 200 m, 300 m, 450 m, 550 m, 650 m, 750 m, 850 m, 1000 m, and 1200 m, respectively. Temporal sampling rates  
 128 were 10 sec for the temperature and CTD sensors, and 15 sec for the CT sensors, respectively. The instruments carried by the  
 129 moorings generally functioned well, but CT sensors stopped working after 6 September 2014 due to the lack of power. Besides,  
 130 Xu et al. (2020) indicated that an anti-cyclonic eddy dominated the region of the mooring since mid-September 2014, which  
 131 significantly affected the local wave properties at the DS station. To avoid the impacts of background currents, we selected  
 132 fifteen ISWs during the spring tidal period from 00:00 UTC 8 August to 00:00 UTC 15 August as criteria to quantitatively  
 133 evaluate the performance of sensitivity numerical experiments.

### 134 **3 Model results and calibrations**

135 In this section, we validate the model accuracy from three aspects: barotropic tidal constituents via comparing with TPXO8-  
 136 atlas dataset and in-situ observational data; spatial distributions of ISWs via comparing with the remote-sensing images; wave  
 137 properties (i.e., amplitude, arrival time, wave-induced velocity and propagation direction) of ISWs via comparing with the in-  
 138 situ observations at mooring station DS.

#### 139 **3.1 Barotropic tide calibrations**

140 The 3D control run only runs for 15 days, which is too short to do the harmonic analysis. To validate the model accuracy in  
 141 simulating the barotropic currents of eight key tidal constituents, we rerun a 3D model (Exp. 2, *500m\_8HARs\_BT*) with the  
 142 same configurations as *500m\_8HARs*, but extend the duration time to 100 days and turn off the iteration of temperature and  
 143 salinity to focus on the barotropic tide regimes.

144 As M2, S2, K1, and O1 barotropic tides are dominant in the NSCS (Ramp et al., 2004; Farmer et al., 2009), here we calculate  
 145 the amplitude ( $U$ ) and phase ( $\phi$ ) of the zonal velocity ( $\mathbf{u}_{bt}$ ) by doing the harmonic analysis over the last 90 days in Exp. 2  
 146 (*500m\_8HARs\_BT*) and compare them with the TPXO8-atlas dataset. A root-mean-square error ( $RMSE$ ), referring to  
 147 Cummins and Oey (1997), is computed to evaluate the model performance in the barotropic regime, which is given by

$$148 \quad RMSE_h = \sqrt{\frac{1}{2} [(U_m^2 + U_o^2) - U_m U_o \cos(\phi_m - \phi_o)]}, \quad (1)$$

149 in which, subscript  $h$  represent four different harmonics;  $U$  and  $\phi$  are amplitude and phase of zonal barotropic currents with  
 150 the subscripts  $m$  for model and  $o$  for observation (TPXO8-atlas). We therefore obtain the horizontal distributions of  $RMSE$   
 151 for four tidal constituents (see Figs. 2a – 2d). In most model domain,  $RMSE$  is less than  $0.02 \text{ m s}^{-1}$ , but slightly larger in the

152 shallow water (e.g., Luzon Strait and the continental shelf), which is still less than  $0.2 \text{ m s}^{-1}$ . It may be because that the  
153 bathymetry derived from the GEBCO dataset and resolutions in our model differ from those in the TPX08-atlas, thereby  
154 resulting in the discrepancy.

155 In addition to comparison between this model and the global tide model, we extract the DS station outputs with a high  
156 sampling rate for comparing with the in-situ observations. To avoid the effects of massive high-frequency motions (i.e.,  
157 environmental noises) in the observational time series on the barotropic regime, we first do the harmonic analysis for zonal  
158 barotropic velocities from 5 August to 19 September, then extract the amplitude and phase of eight key tidal constituents, and  
159 restructure the time series (see red line in Fig. 2e). In terms of the model results, we obtain the time series at station DS in the  
160 same way (see black line in Fig. 2e). It is worth mentioning that the discrepancy between the eight-harmonic restructured time  
161 series and the raw data in the model is small, since the experiment is basically driven by the eight tidal constituents and does  
162 not include any affects from the background environment. By comparing the two timeseries, the model reliability is validated  
163 all through the spring and neap tides. Overall, the model presents nice performance in the barotropic regime.

### 164 **3.2 Comparison with MODIS images**

165 Apart from the model validation in barotropic tides, we then look over the control run (*500m\_8HARs*) in baroclinic (ISWs)  
166 regime by comparing the model results with MODIS images. Figs. 3a and 3b both show two successive ISWs (labeled as IW1  
167 and IW2) in the deep basin with a distance of  $\sim 120 \text{ km}$ . The lengths, curvatures and locations of IW1 and IW2 in the simulation  
168 are consistent with those in the MODIS image. However, two other ISWs occurring over the continental slope and shelf are  
169 captured in the numerical simulations, but not observed on 14 August in the MODIS-Aqua image due to the cloud covering  
170 (Fig. 3b). Conversely, the cloud disappeared on 15 August, so the MODIS-Terra sensor gives a clear seascape painting of  
171 ISWs both in the shallow water (i.e., IW2) and deep water (i.e., IW3 and IW4). Note that IW2 in Figs. 3b and 3d are the same  
172 ISW, which propagates  $\sim 250 \text{ km}$  within 19 hours and 35 mins. All ISWs (IW2, IW3 and IW4) in Figs. 3c and 3d occur at the  
173 fairly close locations with analogous wave properties. From the perspective of crestline lengths, the numerical model shows  
174 well agreement with the MODIS images, namely 131 km versus 133 km for IW2 in Figs. 3a and 3b; 187 km versus 198 km  
175 for IW3 and 74 km versus 69 km for IW4 in Figs. 3c and 3d. Note that the sea surface gradients ( $|\nabla\eta|$ ) larger than  $2 \text{ cm km}^{-1}$   
176 along the crestlines are extracted and defined as the crestline lengths of NLIWs. Besides, in the water depth shallower than  
177 500 m, the modelled IW2 exhibits an ISW train with trailing waves, which is also shown in the MODIS image. As the model  
178 neglects wind above the sea surface and other marine dynamical processes, there are still some subtle nuances of wave  
179 characteristics between them. Overall, this model nicely demonstrates spatial distributions of ISWs in the NSCS, based on the  
180 comparison with remote sensing imagery.

### 181 **3.3 Comparison with in-situ observations**

182 To further evaluate the model performance in reproducing ISWs, we introduce the in-situ observations. The vertical structure  
183 and timing of the wave arrivals, after crossing the deep basin, can be seen in details using daily plots (Figs. 4a – 4g) of the

184 temperature isotherms and baroclinic (ISW-induced) velocities from 8 to 14 August at mooring DS. For clarity, only the results  
 185 in upper 900 m are shown in Fig. 4, including the main wave-induced temperature fluctuations. On the basis of space-time  
 186 diagram of isopycnal displacements along the main propagation paths of ISWs (not shown), the averaged nonlinear internal  
 187 wave speeds are  $\sim 3.0 \text{ m s}^{-1}$  from the Luzon Strait to the deep basin, so it takes roughly 1.5 days for ISWs to propagate from  
 188 the generation site to the targeted station (DS). We move the arrival time (i.e., 00:00 UTC 8 August - 00:00 UTC 14 August)  
 189 of ISWs 1.5 days forward at the station DS, so the related barotropic tides gradually increase during the spring tidal cycle at  
 190 the Luzon Strait (i.e., 12:00 UTC 6 August - 12:00 UTC 12 August). It explains why ISWs were relatively weak and linear  
 191 from 8 to 10 August (Figs. 4a – 4c), but became significant and nonlinear from 11 to 14 August (Figs. 4d – 4g). A single ISW  
 192 was captured around 12:00 UTC from 11 to 14 August, which arrived at the location at approximately the same time every  
 193 day (termed as type-a ISWs by Ramp et al. (2004)). Meanwhile, a wave train, consisted of two dominant solitons and some  
 194 small trailing waves, arrived at the station an hour later each day, showing the same wave characteristics as type-b ISWs in  
 195 Ramp et al. (2004).

196 In terms of the model, we also use the daily plots (Figs. 4h – 4n) at station DS with 1 min sampling rate to show its similarity  
 197 to the in-situ observations. An increasing trend of wave amplitude and nonlinearity is obvious from 8 August to 14 August in  
 198 the model results, suggesting precise depictions of barotropic tides and ISWs' characteristics. Specifically, both type-a (single  
 199 solitons) and type-b ISWs (wave trains) are displayed with analogous arrival time, wave-induced (baroclinic) velocity (color  
 200 shades in Fig. 4) and wave amplitude (contours in Fig. 4) to those in the observations. It's worth noting that even the linear  
 201 internal tides and/ or hydraulic jumps around 12:00 UTC from 8 to 10 August are reproduced. Although the model omits some  
 202 small wave signals (see blue arrows in Fig. 4e) in the observations, which might be induced by non-tidal processes such as  
 203 background currents, the model still shows a well performance in the ISW reproduction.

204 To quantitatively identify the model accuracy, we select fifteen ISWs (marked as red arrows in the left column of Fig. 4),  
 205 extract their wave properties (i.e., arrival time, maximum wave-induced velocity, propagation direction and maximum mode-  
 206 1 wave amplitude) and compare between in-situ observations and numerical simulations. We obtain wave propagation  
 207 direction by computing the angle of baroclinic zonal and meridional components in the layer with maximum velocity. The  
 208 maximum mode-1 wave amplitude ( $A_1$ ) is extracted from the mooring data and model outputs by least squares fitting density  
 209 perturbation profiles  $\rho'(z)$  to normalized modal structure function  $W_n(z)$ , following the similar procedures to those described  
 210 by Buijsman et al. (2010) and Rayson et al. (2012). Although the mode-1 wave amplitude can also be extracted by least squares  
 211 fitting the horizontal baroclinic velocity, Rayson et al. (2019) suggested that the method in velocity field was fuzzy with  
 212 unidirectional internal waves. The modal structure function can be resolved by a shear-free Taylor-Goldstein equation with  
 213 the background stratification  $N^2(z)$ , which is given by

$$214 \quad \frac{d^2 W_n(z)}{dz^2} + \frac{N^2(z)}{c_n} W_n(z) = 0, \quad (2)$$

215 with the boundary conditions  $W_n(0) = W_n(-H) = 0$ . Subscript  $n$  represents the mode number and  $c_n$  is the phase speed of  
 216 the linear internal waves in  $n^{\text{th}}$  mode. The buoyancy perturbation  $b(z)$ , depending on density perturbation  $\rho'(z)$ , is written as

217 
$$b(z) = -g \frac{\rho'(z)}{\rho_0}, \quad (3)$$

218 in which,  $\rho_0$  is the reference density. Following the internal wave polarization relationships (Gerkema and Zimmerman,  
219 2008), we fit the wave amplitudes ( $A_n$ ) in different vertical modes to  $b(z)$  in both in-situ observations and numerical  
220 simulations via

221 
$$b(z) = \sum_{n=1}^5 A_n N^2(z) W_n(z), \quad (4)$$

222 Here, we select the first five vertical modes ( $n = 1 - 5$ ) to do the least squares fitting and mainly discuss the mode-1 wave  
223 amplitude ( $A_1$ ) due to its significant dominance (Fig. 4).

224 According to the above approaches, we extract the four wave properties for fifteen ISWs and plot Fig. 5, in which  
225 observation and model results are shown in red and green, respectively. First, we list the arrival time of ISWs on the two sides  
226 of Fig. 5. The bias between observation and model is always smaller than 1.5 h and the root mean square deviation (RMSD)  
227 is 0.71 h, indicating accurate depiction of ISW arrival time in the control run (*500m\_8HARs*). Second, the maximum baroclinic  
228 velocity (Fig. 5a) and the averaged values ( $0.98 \text{ m s}^{-1}$  and  $1.18 \text{ m s}^{-1}$ , respectively) are shown in the solid lines. It is suggested  
229 that the model underestimates the baroclinic velocity due to neglect of some background non-tidal signals, thereby introducing  
230 a RMSD of  $0.41 \text{ m s}^{-1}$ . Third, the averaged propagation directions of ISWs are  $\sim 285^\circ$  and  $\sim 291^\circ$ , respectively  
231 (the angle measured counterclockwise from north) in the model results and observational data with a RMSD of  $8.35^\circ$ . It is  
232 worth mentioning that the type-a ISWs mainly propagate westward while the type-b ISWs propagate north-westward in both  
233 observation and model, verifying the model's reliability to some extent. Finally, the averaged maximum mode-1 wave  
234 amplitude ( $\sim 108 \text{ m}$ ) in the model is close to that ( $\sim 99 \text{ m}$ ) in the observation. Nonetheless, the RMSD of mode-1 wave amplitude  
235 is  $37.27 \text{ m}$ . Overall, the control run can basically reproduce various wave properties of ISWs observed in the vicinity of the  
236 Dongsha Atoll in the NSCS.

#### 237 **4 Assessment of factors affecting 3D model forecasting precision**

238 In this section, based on the control run, we alter the model configurations, such as the requirements of horizontal resolutions,  
239 numbers of tidal constituents and initial stratification, to respectively estimate their effects on the model forecasting precision  
240 of ISWs in the NSCS.

241 To determine the roles of model horizontal resolutions, tidal constituents and initial stratification in reproducing ISWs in  
242 the NSCS, a set of 3D sensitivity numerical simulations are employed with different configurations, which are listed in Table  
243 2. Details in configuration changes are as follows.

244 1) Exps. 3 and 4 (*250m\_8HARs* and *1000m\_8HARs*): Comparing to *500m\_8HARs*, the horizontal resolution ( $\Delta x$ ) is set as  
245 250 m and 1000 m in both zonal and meridional directions, respectively.



246 2) Exps. 5 - 7 (*500m\_1HAR*, *500m\_4HARs*, and *500m\_13HARs*): Comparing to *500m\_8HARs*, the sensitivity experiments  
 247 are driven by single tidal constituent (M2), four main tidal constituents (M2, S2, K1, and O1), and thirteen tidal constituents  
 248 (M2, S2, N2, K2, K1, O1, P1, Q1, M4, MS4, MN4, MM, and MF), respectively.

249 3) Exp. 8 (*500m\_Real\_N2*): A real stratification profile of background temperature at the mooring station DS is imposed as  
 250 the initial condition, which is derived from the in-situ measurements. A backward-in-time low-pass filter derived from a finite  
 251 impulse response differential equation is used to compute the background temperature (Rayson et al., 2019).

$$252 \quad \frac{d\bar{T}}{dt} = \frac{1}{\tau_f}(T - \bar{T}), \quad (5)$$

253 in which,  $\tau_f$  is the filtering time scale, set to 35 h, corresponding to the local Coriolis frequency.  $T$  and  $\bar{T}$  are the  
 254 instantaneous and background temperature, respectively. Then, the background temperature at each observational time step  $i$   
 255 is given as

$$256 \quad \bar{T}^{i+1} = \bar{T}^i + \frac{\Delta t}{\tau_f}(T^{i+1} - \bar{T}^i), \quad (6)$$

257 where  $\Delta t$  is the sampling rate (10 secs for the temperature and CTD sensors, 15 secs for the CT sensors). The background  
 258 temperature profile is ultimately obtained by low-pass filtering at each layer (see red line in Fig. 1b).

#### 259 **4.1 Requirements of resolutions**

260 Various 3D model with different resolutions were implemented to simulate ISWs in the NSCS in previous studies (e.g.,  
 261 Vlasenko et al., 2010; Zhang et al., 2011; Lai et al., 2019). However, which resolution is adequate to satisfy the ISW prediction  
 262 precision and save computational resources to the utmost in the meantime has yet been discussed. Here, we run two sensitivity  
 263 experiments (Exps. *250m\_8HARs* and *1000m\_8HARs*) with horizontal resolutions of 250 m and 1000 m, to respectively  
 264 compare the model performance in different aspects with the control run (resolution of 500 m).

265 First, the spatial distributions of ISWs are exhibited via the snapshots of sea surface height gradients ( $|\nabla\eta|$ ) at 12:00 UTC  
 266 on 12 August 2014. In the control run (*500m\_8HARs*), three ISWs (labelled as IWB1, IWA1, and IWB2 from west to east)  
 267 with distinct crest lines successively occur between 116°E and 120°E (see Fig. 6a), in which IWB1 and IWB2 are internal  
 268 wave packets with trailing waves (type-b wave) and IWA1 is a single soliton (type-a wave). As IWB1 approaches the  
 269 continental slope and shelf, the leading wave front fully steepens with a narrow characteristic half-width, suggesting its strong  
 270 nonlinearity. IWB2 also shows up as a wave packet with many secondary waves in the developing stage, although its  
 271 nonlinearity is slightly weaker than IWB1's. Conversely, the single soliton IWA1 with relatively long crest line and broad  
 272 characteristic half-width is about to pass mooring station DS (marked as green star in Fig. 6). In comparison, the Exps.  
 273 *250m\_8HARs* and *1000m\_8HARs* reproduce these three waves as well, but with some subtle discrepancies between them. In  
 274 Exp. *250m\_8HARs*, more details of wave properties are clarified (Fig. 6b). Specifically, the secondary waves of IWB1 and  
 275 IWB2 are more visible than those in *500m\_8HARs*. However, in Exp. *1000m\_8HARs*, some fine structures of ISWs are not

276 well resolved. For instance, only one secondary wave is found behind the leading wave of IWB2, and the south portion of  
277 IWA1 crest line is barely observed (Fig. 6c).

278 Then, we select a transect along the main propagation path of ISWs (shown in dashed line in Fig. 6a) at 12:00 UTC on 12  
279 August 2014 to compare the vertical structure of ISWs among three experiments (see Fig. 7). In Fig. 7, blue (yellow) color  
280 shades represent westward (eastward) baroclinic velocity and contours are temperature isotherms. Linear internal waves, such  
281 as internal wave beams near the generation site ( $120^{\circ} - 121^{\circ}\text{E}$ ), are nicely reproduced in all numerical experiments. Nonetheless,  
282 nonlinear internal waves present different wave characteristics in different cases. In Exp. *500m\_8HARs*, the single soliton  
283 IWA1 and the wave packet IWB2 with a series of trailing waves are apparent in the slice, but IWB1 is not included (Fig. 7a).  
284 In Exp. *250m\_8HARs*, IWA1 and IWB2 occur at the same location as those in Exp. *500m\_8HARs*. IWA1 show similar  
285 properties in two cases, but the secondary waves of IWB2 are better described in Exp. *250m\_8HARs*. By comparison, IWA1  
286 shows its weak nonlinearity with small vertical displacement and broad characteristic half-width (i.e., horizontal distance  
287 between the wave front and wave trough) in Exp. *1000m\_8HARs*. Besides, only one secondary wave appears in the IWB2  
288 packet in Exp. *1000m\_8HARs*.

289 Last, a two-day time segment of observational temperature and baroclinic velocities from 18:00 UTC 11 August to 18:00  
290 UTC 13 August 2014 at the station DS is extracted to demonstrate the sensitivity model capability of simulating vertical  
291 structures of ISWs over the continental slope (Fig. 8). In the control run (*500m\_8HARs*, Fig. 8b), two wave packets and two  
292 single solitons successively arrive at the station, keeping the consistency with the observation, although their characteristic  
293 half-widths are slightly broader than those in the field measurements (Fig. 8a). Meanwhile, some small fluctuations, occurring  
294 in the observations, are not included in the control run. In Exp. *250m\_8HARs* (Fig. 8c), the half-widths are narrower than  
295 those in the Exp. *500m\_8HARs*, which agree better with the real internal wave field. Besides, more fluctuations, i.e., those  
296 small wave signals (09:00 UTC 12 August and 09:00 UTC 13 August) in front of the single solitons are reproduced in this  
297 experiment. Conversely, in Exp. *1000m\_8HARs*, internal wave trains can still be reproduced with relatively weak nonlinearity,  
298 but the single solitons are not correct due to their tiny amplitudes and linear wave structures.

299 To quantitatively evaluate the model performance of sensitivity experiments, we present the bias of five wave properties of  
300 fifteen ISWs (marked as red arrows in Fig. 4) between model results and observational data in Fig. 9. The biases of arrival  
301 time are generally smaller than 1 h (see black and blue circles in Fig. 9a) for Exps. *500m\_8HARs* and *250m\_8HARs*, whose  
302 RMSDs are 0.71 and 0.67 h, respectively. In contrast, the bias for Exp. *1000m\_8HARs* is larger than 1 h (red circles in Fig.  
303 9a) and its RMSD is 0.79 h. In terms of the wave-induced velocity (Fig. 9b), the RMSDs are 0.38, 0.41 and 0.48  $\text{m s}^{-1}$  in Exps.  
304 *250m\_8HARs*, *500m\_8HARs*, and *1000m\_8HARs*, respectively. The RMSDs of propagation directions are very close ( $\sim 8.5^{\circ}$ )  
305 in the three experiments (see Table 3). As for the mode-1 wave amplitudes, Exps. *250m\_8HARs* and *500m\_8HARs*  
306 overestimate the wave amplitudes in most cases (see positive biases in Fig. 9d), thereby resulting in RMSDs of 38.12 and  
307 37.27 m, respectively. Conversely, Exp. *1000m\_8HARs* would underestimate the wave amplitudes of majority ISWs with  
308 dominant negative biases in Fig. 9d, resulting in a RMSD of 40.28 m (Table 3). Last but not least, Exps. *500m\_8HARs* and  
309 *1000m\_8HARs* inaccurately depict characteristic half-widths of ISWs with RMSDs of 1.07 and 2.41 km, while Exp.

310 *250m\_8HARs* performs well with a RMSD of 0.64 km (Fig. 9e). The relative difference of RMSD suggests that Exp.  
311 *250m\_8HARs* increases 40% accuracy of predicting characteristic half-widths by comparing to Exp. *500m\_8HARs*. From the  
312 perspective of computational resources, Exps. *250m\_8HARs*, *500m\_8HARs*, and *1000m\_8HARs* spend  $20.4 \times 10^4$  CPU  
313 hours,  $4.6 \times 10^4$  CPU hours, and  $1.0 \times 10^4$  CPU hours, respectively.

314 In summary, the control run with a resolution of 500 m can basically reproduce the principal ISW field in the NSCS, while  
315 the sensitivity model with a higher resolution of 250 m would be a better solution to identify wave properties, in particular of  
316 the wave nonlinearity. Nonetheless, a 250 m-resolution model spends nearly fivefold computational resources of a 500 m-  
317 resolution model in the same model domain. Besides, the model with a lower resolution of 1000 m underestimates the  
318 nonlinearity of ISWs, thereby resulting in an inaccurate ISW field in the NSCS.

## 319 **4.2 Requirements of tidal constituents**

320 3D/2D models with different numbers of barotropic tidal constituents (e.g., single harmonic, four harmonics and eight  
321 harmonics) were commonly imposed to investigate the generation mechanisms of ISWs in the NSCS in previous studies (e.g.,  
322 Li, 2014; Buijsman et al., 2010; Jin et al., 2021). However, whether a single tidal constituent can satisfy the reproduction of a  
323 real ISW field and how many tidal constituents are required for a realistic ISW model are still questions. Here, we run three  
324 sensitivity experiments (Exps. *500m\_1HAR*, *500m\_4HARs* and *500m\_13HARs*) with different numbers of tidal harmonics to  
325 answer the questions by comparing the model performance with the control run (*500m\_8HARs*).

326 We first discuss the model requirements of tidal constituents from the point of view of the ISW horizontal distributions and  
327 look back to Fig. 6. Note that time series of zonal barotropic currents at the generation site (Luzon Strait) are presented on the  
328 bottom left for each panel, where single/four/eight tidal constituent(s) are shown in green/magenta/blue. By comparing Exp.  
329 *500m\_1HAR* (Fig. 6d) and *500m\_8HARs* (Fig. 6a), we find that the single M2 tidal harmonic is not adequate to reproduce  
330 ISWs in the NSCS, so only some linear internal tides are detected on the sea surface via  $|\nabla\eta|$ . In contrast, Exp. *500m\_4HARs*  
331 (Fig. 6e) nearly recreates the analogous scenario of ISWs to Exp. *500m\_8HARs*, where IWB1, IWA1 and IWB2 appear at the  
332 same locations. Nonetheless, the crestline length ( $\sim 134$  km) of IWB2 in Exp. *500m\_4HARs* is slightly shorter than that ( $\sim 167$   
333 km) in Exp. *500m\_8HARs*, and the secondary waves of IWB2 are unclear in Exp. *500m\_4HARs* (see Fig. 6e).  $|\nabla\eta|$  in Exp.  
334 *500m\_13HARs* are not presented in Fig. 6, since it shows the exact same spatial patterns of ISWs as those in Exp.  
335 *500m\_8HARs*, suggesting the principle eight tidal constituents are fine enough to satisfy accurate reproduction of the  
336 horizontal features of ISWs in a realistic oceanic model.

337 We then consider the difference of ISW vertical structures in sensitivity experiments with various tidal forcing via the  
338 selected transect and mooring station DS. In Exp. *500m\_1HAR*, only linear internal waves are captured from the generation  
339 site to the slope, suggesting that single M2 tidal constituent without amplification factors can only contributes to internal tides  
340 and linear internal wave beams in NSCS (see Figs. 7d and 8e), unless the magnitudes of M2 barotropic tides are amplified,  
341 ISWs are likely to be generated (e.g., Yuan et al., 2020). In Exp. *500m\_4HARs* (Figs. 7e and 8f), the single soliton IWA1 is  
342 reproduced with a smaller amplitude and weaker nonlinearity than that in Exp. *500m\_8HARs*. Besides, the secondary waves

343 of IWB2 are barely observed in Exp. *500m\_4HARs*, which are much clearer in Exp. *500m\_8HARs* (Figs. 7a and 8a). Figs. 8a  
344 and 8g depict the striking similarity of wave characteristics between Exp. *500m\_8HARs* and Exp. *500m\_13HARs*.

345 Last, we quantitatively estimate the sensitivity model capability of reproducing ISWs, by computing the biases and RMSDs  
346 of five wave properties (see Fig. 9 and Table 3) in the cases with different tidal forcing. Since Exp. *500m\_1HAR* cannot predict  
347 ISWs with significant amplitudes, we exclude it in the following analysis. In terms of Exp. *500m\_13HARs* with thirteen tidal  
348 constituents, the biases and RMSDs of five wave properties are very close to those in the control run with eight harmonics (see  
349 overlapped black circles and magenta triangles in Fig. 9 and Table 3). Conversely, Exp. *500m\_4HARs* shows significant  
350 difference in the biases and RMSDs of five wave properties from the control run. Specifically, in Fig. 9a, the RMSD of arrival  
351 time (0.81 h) is larger in Exp. *500m\_4HARs* than that in Exp. *500m\_8HARs* (0.71 h). In addition, Exp. *500m\_4HARs*  
352 underestimates averaged wave-induced velocity for about 38% and averaged mode-1 wave amplitude for about 15%, which  
353 result in large negative values of biases (see magenta triangles in Figs. 9b and 9c), corresponding to  $0.58 \text{ m s}^{-1}$  and 43.69 m of  
354 RMSDs, respectively. In terms of the characteristic half-widths, Exps. *500m\_4HARs* and *500m\_13HARs* with RMSDs of  
355 1.10 and 1.01 km show analogous performance to the control run Exp. *500m\_8HARs* with a RMSD of 1.07 km.

356 In summary, the model with eight (or thirteen) primary tidal constituents can accurately reproduce the real ISW field in the  
357 NSCS, while the sensitivity model with four key harmonics (M2, S2, K1 and O1) would underestimate the magnitudes of  
358 some secondary wave within a wave packet. In addition, the model only driven by M2 tide can only characterize wave  
359 properties of linear internal waves (tides) instead of ISWs.

### 360 **4.3 Initial stratification selections**

361 As ISWs generate via tide-topography interaction in the stratified water, the stratification selection is crucial to directly  
362 affect the model capabilities. Here, we extract the background stratification from the in-situ measurements at mooring station  
363 DS as initial condition to run the sensitivity experiment *500m\_Real\_N2*, and compare the model results with the control run  
364 (*500m\_8HARs*) with a climatological stratification from the WOA18 dataset.

365 In the model results, the spatial distribution of  $|\nabla\eta|$  in Exp. *500m\_Real\_N2* shows analogous pattern of ISWs to that in Exp.  
366 *500m\_8HARs*. Specifically, three ISWs (i.e., IWB1, IWA1, and IWB2) appear at the same location in the two experiments  
367 with similar horizontal wave characteristics (Figs. 6a and 6f). The visible difference is that the crest line length of the secondary  
368 wave of IWB2 is longer with a stronger nonlinearity in Exp. *500m\_Real\_N2*. We then look over the difference of ISW vertical  
369 structures between two cases from the perspective of  $x$ - $z$  plane along the transect (Figs. 7a and 7f) and time series at station  
370 DS (Figs. 8a and 8h). It is clearly shown that Exp. *500m\_Real\_N2* with the real stratification can better characterize the  
371 nonlinearity of the single soliton IWA1 and the secondary wave of wave train IWB2. Besides, the comparison with field  
372 measurements reveals that Exp. *500m\_Real\_N2* shows a better precision (13%) in predicting the arrival time (i.e., RMSD of  
373 0.62 h) of ISWs than the control run (i.e., RMSD of 0.71 h) with the climatological stratification. However, the RMSD of the  
374 propagation direction of ISWs is larger in the realistic-stratification case ( $14.74^\circ$ ) than that of the control run ( $8.35^\circ$ ). Last, Exp.  
375 *500m\_Real\_N2* nicely describes the characteristic half-widths of ISWs (RMSD of 0.58 km), which improves 46% accuracy

376 by comparing that in Exp. *500m\_8HARs* (RMSD of 1.07 km). To sum up, although the model with climatological stratification  
377 works well, applying the real background stratification as the model initial condition would improve the model performance  
378 in predicting some wave properties, including arrival time, wave-induced velocity, wave amplitude and characteristic half-  
379 width.

## 380 **5 Discussion and Conclusions**

381 Although the 3D realistic model, particularly in Exp. *250m\_8HARs*, has accurately reproduced the ISW features in the  
382 NSCS to some extent, the depictions of soliton numbers within an internal wave packet and propagation direction still have  
383 space for improvement, i.e., at least three following factors might be considered in the future modelling.

384 The first factor, that may affect the model accuracy, is background currents. Here, we download the global Hybrid  
385 Coordinate Ocean Model (HYCOM) dataset in 2014 and calculate the background current field by averaging from 05-AUG  
386 to 20-AUG, namely predicting time of the model (see Fig. 10a). In Fig. 10a, there is a clear counter-clockwise circulation/eddy  
387 pattern on the west side of Luzon Strait. Xie et al. (2015) suggested that wave properties of ISWs can be significantly influenced  
388 by an isolated mesoscale eddy, regardless of a cyclonic or anticyclonic eddy, during the propagation of ISWs. When an ISW  
389 pass over a cyclonic eddy, as in Fig. 10a, the crestline will be distorted, thereby modulating the oblique propagation direction  
390 of wave to some extent (Xie et al., 2016). In addition, a series of secondary trailing waves are able to form behind the leading  
391 wave in the energy-focusing region. Therefore, background currents are supposed to be considered in the future forecasting  
392 model, which shows potential improvement in the depiction of soliton numbers within an ISW packet and propagation direction  
393 in the NSCS.

394 The second factor is inhomogeneous spatial distribution of stratification. In the current forecasting model, we apply  
395 horizontally-homogeneous temperature and salinity profiles (Fig. 1d) with the maximum buoyancy frequency of  $\sim 0.02 \text{ s}^{-1}$  at a  
396 water depth of 50 m. Actually, we also implement a sensitivity experiment (EXP. *3D-TS*) with weak spatially-varying initial  
397 conditions derived from the WOA18 climatology dataset. By comparing EXPs. *3D-TS* and *800m\_HARs*, it is concluded that  
398 the weak spatially-varying initial conditions show similar performance in predicting the arrival time and horizontal  
399 distributions (Fig. C1), wave amplitudes and wave-induced velocities (Fig. C2) of ISWs to the horizontally-homogeneous  
400 initial conditions. However, the model results would be different with strong spatially-varying stratification derived from the  
401 ocean reanalysis dataset with a high resolution and sampling rate (e.g., global HYCOM dataset). Since wave speeds of ISWs  
402 and internal tides are closely related to vertical structure of stratification based on eigen-function, the inhomogeneous  
403 stratification pattern is likely to affect ISW propagation speed and then modulate their arrival time. Most of previous numerical  
404 studies (e.g., Zhang et al., 2011; Alford et al., 2015; Zeng et al., 2019) rarely considered the impacts of horizontally  
405 inhomogeneous stratification, but Chi et al. (2016) and Lai et al. (2019) applied spatially-varying stratification in 3D model  
406 and indicated that inhomogeneous stratification can achieve better model results to some extent. However, only considering  
407 spatially-varying temperature and salinity profiles with large values of horizontal gradients (e.g., HYCOM dataset in Fig. 10b)

408 as the initial conditions might lead to spurious geostrophic currents, thereby significantly affecting the true wave field. Hence,  
409 spatially-varying stratification is worthwhile to be considered together with background currents in future numerical studies  
410 in the NSCS.

411 The last element is external (wind) forcing. As is well known, ISWs are a ubiquitous phenomenon with maximum amplitudes  
412 in the ocean interior. Nonetheless, the thermoclines usually occur in the upper layers (shallower than 500 m) in the SCS, which  
413 can be significantly affected by extreme wind events (i.e., tropical cyclones, Zhang 2022). So far, wind forcing was rarely  
414 applied in the numerical modelling of ISWs, except Lai et al. (2019). As both the ISWs and tropical cyclones are active and  
415 frequent in August, September and October in the SCS, the impacts of tropical cyclones on the upper layers should be  
416 considered in the future numerical simulations, although tropical cyclone did not happen during our predicting period (see Fig.  
417 10c).

418 In summary, this study introduces a robust ISW forecasting model by comparing with in-situ observational data and remote-  
419 sensing images, and quantitatively evaluates the requirements of different factors, including the horizontal resolutions, tidal  
420 constituents and initial stratification, for accurately characterizing the ISW field with applications to the NSCS. The major  
421 findings are listed as follows.

- 422 1) A model with a 500 m resolution can basically reproduce the principal ISW field, while a model with a higher resolution  
423 of 250 m would be a better solution to identify wave properties but spends nearly fivefold computational resources of  
424 a 500 m-resolution case with the same model domain.
- 425 2) At least eight primary tidal constituents should be included in the boundary forcing.
- 426 3) Compared to climatological stratification, applying the observational background stratification could improve the  
427 model performance in predicting some wave properties, namely 13% improvement of arrival time and 46%  
428 improvement of characteristic half-width.

## 429 **Appendix A: Feasibility study of 2D slice model**

430 Differing from the 3D models, 2D slice models are fairly economical from the perspective of computational resources. In  
431 the past few decades, 2D slice models with idealized topography (double ridges) were commonly conducted to investigate  
432 ISW dynamics in the NSCS, in particular for the generation mechanisms and the affecting factors of ISWs (i.e., Cai et al.,  
433 2002; Shaw et al., 2009; Li, 2014). Here, we attempt to test the 2D model performance along different transects and clarify  
434 whether a 2D slice model can be a substitute for a 3D model in the aspect of reproducing a real ISW field in the NSCS.

435 Three parallel transects with a distance of  $0.05^\circ$  are selected along the main propagation direction of ISWs (see dashed lines  
436 in Fig. 1a), which are labelled as *2D\_500m\_8HARs*, *2D\_500m\_8HARs\_005N*, and *2D\_500m\_8HARs\_005S*.  $\Delta x$  and  $\Delta t$  are  
437 still set as 500 m and 10 sec, respectively. Initial conditions and dissipation coefficients are set the same as those in the 3D  
438 control run (*500m\_8HARs*). The 2D slice models are also driven by the barotropic tides of eight tidal constituents at both west  
439 boundary ( $115.8^\circ\text{E}$ ,  $21.1^\circ\text{N} \pm 0.05^\circ$ ) and east boundary ( $123.8^\circ\text{E}$ ,  $19.5^\circ\text{N} \pm 0.05^\circ$ ). As the transects are not strictly zonal (angle

440  $\theta = 11.2^\circ$ , see Fig. 1a), it is necessary to extract the amplitude ( $U'$ ) and phase ( $\phi'$ ) for each harmonic ( $\omega$ ) in the transect  
 441 direction from the TPXO8-atlas dataset (i.e.,  $U$ ,  $V$ ,  $\phi_U$ , and  $\phi_V$ ), given by

442

$$443 \quad U' = \sqrt{(U \cdot \cos\phi_U \cos\theta - V \cdot \cos\phi_V \sin\theta)^2 + (U \cdot \sin\phi_U \cos\theta - V \cdot \sin\phi_V \sin\theta)^2}, \quad (A1)$$

$$444 \quad \phi' = \arctan\left(\frac{U \cdot \sin\phi_U \cos\theta - V \cdot \sin\phi_V \sin\theta}{U \cdot \cos\phi_U \cos\theta - V \cdot \cos\phi_V \sin\theta}\right), \quad (A2)$$

445 Here, we apply the standard 2D experiment along the selected transect (see the black dashed line in Fig. 1a) and label it as  
 446 *2D\_500m\_8HARs*. The model is driven by eight principle tidal constituents on the both lateral boundaries, which are extracted  
 447 from the TPXO8 dataset (following Eqns. A1 and A2). Note that initial conditions and other model configurations in Exp.  
 448 *2D\_500m\_8HARs* are the same as those in the 3D control run (*500m\_8HARs*). In addition, we run two sensitivity experiments  
 449 (Exps. *2D\_500m\_8HARs\_005N* and *2D\_500m\_8HARs\_005S*) along the two parallel transects (see red dashed lines in Fig.  
 450 1b).

451 In the 2D standard case (*2D\_500m\_8HARs*), ISWs subsequently generate in the double ridge, then propagate westward,  
 452 and eventually arrive at the station in the form of wave trains (Fig. A1b). The wave amplitudes are greater than those in the  
 453 3D control run (Fig. A1a). At the station outputs (Fig. A1f), we find that Exp. *2D\_500m\_8HARs* can only reproduce ISW  
 454 packets, but cannot discriminate type-a and type-b ISWs. Although the occurrence frequency of ISWs is also twice per day in  
 455 Exp. *2D\_500m\_8HARs*, the arrival time of those ISW packets is not consistent with that in Exp. *500m\_8HARs* (Fig. A1e) and  
 456 in the field measurements (Fig. 8a). In Exp. *2D\_500m\_8HARs\_005N*, ISWs are rarely found along the transect (Fig. A1c),  
 457 likely due to the relatively gentle topography and small tidal forcing at the lateral boundaries. At the station outputs (Fig. A1g),  
 458 only small temperature fluctuations are captured. Conversely, Exp. *2D\_500m\_8HARs\_005S* show analogous wave fields to  
 459 Exp. *2D\_500m\_8HARs* (Fig. A1d). Specifically, ISW packets with a half-day cycle are dominant, but their arrival time are  
 460 postponed for about two hours (Fig. A1h).

461 To sum up, 2D slice models along different transects (even  $0.05^\circ$  apart) present totally different ISW characteristics, which  
 462 are inconsistent with the 3D model results and in-situ measurements. Therefore, 3D model is the best and sole option to  
 463 correctly reproduce the ISW field in the real ocean, while 2D model is more suitable for the mechanism investigations.

## 464 **Appendix B: Quasi-steady state of the model**

465 Due to the limitation of the computational resources, we admit that the model integrated time (3-day) might be relatively  
 466 short for the model spin-up. When we calculate the averaged baroclinic kinetic energy ( $KE_{bc}$ ) in the inner model domain (Fig.  
 467 B1), it is found that the depth-integrated  $KE_{bc}$  keeps increasing in the first 7 days (see red line in Fig. B1a), which is related  
 468 to the flooding barotropic tides (see Fig. B1b). Actually,  $\int_{-H}^0 KE_{bc} dz$  reaches  $10 \text{ kJ m}^{-2}$  in the 3<sup>rd</sup> model day, whose magnitude  
 469 is equivalent to that during the neap tides (i.e., 12<sup>th</sup> to 15<sup>th</sup> model day). It demonstrates that the 3D model reaches a quasi-  
 470 steady state after three days. Moreover, the comparison between the model results and field observations at the mooring station

471 DS verifies the model accuracy since 08 August (the 3<sup>rd</sup> model day) as well. Therefore, first 3 days are considered as the spin-  
472 up time in this work.

### 473 **Appendix C: Figures of EXPs. 3D-TS and 500m\_8HARs**

474

475 *Code and data availability.* The MODIS remote-sensing images are derived from the NASA Worldview application  
476 (<https://worldview.earthdata.nasa.gov>). The input files (including initial and boundary conditions) and relevant output data  
477 files of the 3D realistic Massachusetts Institute of Technology general circulation model in the northern South China Sea are  
478 available at a free, open access, data repository via <https://doi.org/10.5281/zenodo.6792999>.

479

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482

483 *Competing interests.* The authors declare that they have no conflict of interest.

484

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495

### 496 **References**

497 Alford, M. H., MacKinnon, J. A., Nash, J. D., Simmons, H., Pickering, A., Klymak, J. M., Pinkel, R., Sun, O., Rainville, L.,  
498 Musgrave, R., Beitzel, T., Fu, K. H., and Lu, C. W.: Energy flux and dissipation in Luzon Strait: Two tales of two  
499 ridges. *Journal of Physical Oceanography*, 41, 2211-2222, <https://doi.org/10.1175/JPO-D-11-073.1>, 2011.



500 Alford, M. H., Peacock, T., MacKinnon, J. A., Nash, J. D., Buijsman, M. C., Centurioni, L. R., ... and Paluszkiwicz, T.: The  
501 formation and fate of internal waves in the South China Sea, *Nature*, 521, 65-69, <https://doi.org/10.1038/nature14399>, 2015.

502 Álvarez, Ó., Izquierdo, A., González, C. J., Bruno, M., and Mañanes, R.: Some considerations about non-hydrostatic vs.  
503 hydrostatic simulation of short-period internal waves. A case study: The Strait of Gibraltar. *Continental Shelf Research*, 181,  
504 174-186, <https://doi.org/10.1016/j.csr.2019.05.016>, 2019.

505 Beardsley, R. C., Duda, T. F., Lynch, J. F., Irish, J. D., Ramp, S. R., Chiu, C. S., Tang, T. Y., Yang, Y. J., and Fang, G.:  
506 Barotropic tide in the northeast South China Sea, *IEEE Journal of Oceanic Engineering*, 29, 1075-1086,  
507 <https://doi.org/10.1109/JOE.2004.833226>, 2004.

508 Buijsman, M. C., Kanarska, Y., and McWilliams, J. C.: On the generation and evolution of nonlinear internal waves in the  
509 South China Sea, *Journal of Geophysical Research: Oceans*, 115, <https://doi.org/10.1029/2009JC005275>, 2010.

510 Buijsman, M. C., McWilliams, J. C., and Jackson, C. R.: East-west asymmetry in nonlinear internal waves from Luzon  
511 Strait, *Journal of Geophysical Research: Oceans*, 115, <https://doi.org/10.1029/2009JC006004>, 2010.

512 Cai, S., Long, X., and Gan, Z.: A numerical study of the generation and propagation of internal solitary waves in the Luzon  
513 Strait, *Oceanologica Acta*, 25, 51-60, [https://doi.org/10.1016/S0399-1784\(02\)01181-7](https://doi.org/10.1016/S0399-1784(02)01181-7), 2002.

514 Chen, Z., Nie, Y., Xie, J., Xu, J., He, Y., and Cai, S.: Generation of internal solitary waves over a large sill: From Knight Inlet  
515 to Luzon Strait, *Journal of Geophysical Research: Oceans*, 122, 1555-1573, <https://doi.org/10.1002/2016JC012206>, 2017.

516 Cummins, P. F., and Oey, L. Y.: Simulation of barotropic and baroclinic tides off northern British Columbia, *Journal of*  
517 *Physical oceanography*, 27, 762-781, [https://doi.org/10.1175/1520-0485\(1997\)027<0762:SOBAPT>2.0.CO;2](https://doi.org/10.1175/1520-0485(1997)027<0762:SOBAPT>2.0.CO;2), 1997.

518 Du, T., Tseng, Y. H., and Yan, X. H.: Impacts of tidal currents and Kuroshio intrusion on the generation of nonlinear internal  
519 waves in Luzon Strait, *Journal of Geophysical Research: Oceans*, 113, <https://doi.org/10.1029/2007JC004294>, 2008.

520 Egbert, G. D., and Erofeeva, S. Y.: Efficient inverse modeling of barotropic ocean tides, *Journal of Atmospheric and Oceanic*  
521 *technology*, 19, 183-204, [https://doi.org/10.1175/1520-0426\(2002\)019<0183:EIMOBO>2.0.CO;2](https://doi.org/10.1175/1520-0426(2002)019<0183:EIMOBO>2.0.CO;2), 2002.

522 Farmer, D., Li, Q., and Park, J. H.: Internal wave observations in the South China Sea: The role of rotation and non-  
523 linearity, *Atmosphere-Ocean*, 47, 267-280, <https://doi.org/10.3137/OC313.2009>, 2009.

524 Farmer, D. M., Alford, M. H., Lien, R. C., Yang, Y. J., Chang, M. H., and Li, Q.: From Luzon Strait to Dongsha Plateau:  
525 Stages in the life of an internal wave, *Oceanography*, 24, 64-77, 2011.

526 Gerkema, T., and Zimmerman, J. T. F.: An introduction to internal waves, *Lecture Notes*, Royal NIOZ, Texel, 207, 2008.

527 Guo, C., Chen, X., Vlasenko, V., and Stashchuk, N.: Numerical investigation of internal solitary waves from the Luzon Strait:  
528 Generation process, mechanism and three-dimensional effects, *Ocean Modelling*, 38, 203-216,  
529 <https://doi.org/10.1016/j.ocemod.2011.03.002>, 2011.

530 Huang, W., Johannessen, J., Alpers, W., Yang, J., and Gan, X.: Spatial and temporal variations of internal wave sea surface  
531 signatures in the northern South China Sea studied by spaceborne SAR imagery, In *Proceedings of the 2nd SeaSAR*  
532 *Symposium*, 2008.

533 Jan, S., Lien, R. C., and Ting, C. H.: Numerical study of baroclinic tides in Luzon Strait. *Journal of Oceanography*, 64, 789-  
534 802, <https://doi.org/10.1007/s10872-008-0066-5>, 2008.

535 Jin, G., Lai, Z., and Shang, X.: Numerical study on the spatial and temporal characteristics of nonlinear internal wave energy  
536 in the Northern South China sea, *Deep Sea Research Part I: Oceanographic Research Papers*, 178, 103640,  
537 <https://doi.org/10.1016/j.dsr.2021.103640>, 2021.

538 Ko, D. S., Martin, P. J., Rowley, C. D., and Preller, R. H.: A real-time coastal ocean prediction experiment for  
539 MREA04. *Journal of Marine Systems*, 69, 17-28, <https://doi.org/10.1016/j.jmarsys.2007.02.022>, 2008.

540 Lai, Z., Jin, G., Huang, Y., Chen, H., Shang, X., and Xiong, X.: The generation of nonlinear internal waves in the South China  
541 Sea: A three-dimensional, nonhydrostatic numerical study, *Journal of Geophysical Research: Oceans*, 124, 8949-8968,  
542 <https://doi.org/10.1029/2019JC015283>, 2019.

543 Legg, S., and Huijts, K. M.: Preliminary simulations of internal waves and mixing generated by finite amplitude tidal flow  
544 over isolated topography, *Deep Sea Research Part II: Topical Studies in Oceanography*, 53, 140-156,  
545 <https://doi.org/10.1016/j.dsr2.2005.09.014>, 2006.

546 Li, Q.: Numerical assessment of factors affecting nonlinear internal waves in the South China Sea, *Progress in*  
547 *Oceanography*, 121, 24-43, <https://doi.org/10.1016/j.pocean.2013.03.006>, 2014.

548 Li, D., Chen, X., and Liu, A.: On the generation and evolution of internal solitary waves in the northwestern South China  
549 Sea, *Ocean Modelling*, 40, 105-119, <https://doi.org/10.1016/j.ocemod.2011.08.005>, 2011.

550 Liu, A. K., Chang, Y. S., Hsu, M. K., and Liang, N. K.: Evolution of nonlinear internal waves in the East and South China  
551 Seas, *Journal of Geophysical Research: Oceans*, 103, 7995-8008, <https://doi.org/10.1029/97JC01918>, 1998.

552 Liu, A. K., and Hsu, M. K.: Internal wave study in the South China Sea using synthetic aperture radar (SAR), *International*  
553 *Journal of Remote Sensing*, 25, 1261-1264, <https://doi.org/10.1080/01431160310001592148>, 2004.

554 Locarnini, M. M., Mishonov, A. V., Baranova, O. K., Boyer, T. P., Zweng, M. M., Garcia, H. E., Reagan, J. R., Seidov, D.,  
555 Weathers, K. W., Paver, C. R., and Smolyar, I.: *World ocean atlas 2018, volume 1: Temperature*, 2018.

556 Marshall, J., Hill, C., Perelman, L., and Adcroft, A.: Hydrostatic, quasi-hydrostatic, and nonhydrostatic ocean  
557 modelling, *Journal of Geophysical Research: Oceans*, 102, 5733-5752, <https://doi.org/10.1029/96JC02776>, 1997.

558 Orr, M. H., and Mignerey, P. C.: Nonlinear internal waves in the South China Sea: Observation of the conversion of depression  
559 internal waves to elevation internal waves, *Journal of Geophysical Research: Oceans*, 108,  
560 <https://doi.org/10.1029/2001JC001163>, 2003.

561 Nagai, T., and Hibiya, T.: Internal tides and associated vertical mixing in the Indonesian Archipelago. *Journal of Geophysical*  
562 *Research: Oceans*, 120, 3373-3390, <https://doi.org/10.1002/2014JC010592>, 2015.

563 Ramp, S. R., Tang, T. Y., Duda, T. F., Lynch, J. F., Liu, A. K., Chiu, C. S., Bahr, F., L., Kim, H., R., and Yang, Y. J.: Internal  
564 solitons in the northeastern South China Sea, Part I: Sources and deep water propagation. *IEEE Journal of Oceanic*  
565 *Engineering*, 29, 1157-1181, 2004.

566 Ramp, S. R., Park, J. H., Yang, Y. J., Bahr, F. L., and Jeon, C.: Latitudinal structure of solitons in the South China Sea, *Journal*  
567 *of Physical Oceanography*, 49, 1747-1767, <https://doi.org/10.1175/JPO-D-18-0071.1>, 2019.

568 Rayson, M. D., Jones, N. L., and Ivey, G. N.: Temporal variability of the standing internal tide in the Browse Basin, Western  
569 Australia, *Journal of Geophysical Research: Oceans*, 117, <https://doi.org/10.1029/2011JC007523>, 2012.

570 Rayson, M. D., Jones, N. L., and Ivey, G. N.: Observations of large-amplitude mode-2 nonlinear internal waves on the  
571 Australian North West shelf, *Journal of Physical Oceanography*, 49, 309-328, <https://doi.org/10.1175/JPO-D-18-0097.1>, 2019.

572 Simmons, H., Chang, M. H., Chang, Y. T., Chao, S. Y., Fringer, O., Jackson, C. R., and Ko, D. S.: Modeling and prediction  
573 of internal waves in the South China Sea, *Oceanography*, 24, 88-99, 2011.

574 Shaw, P. T., Ko, D. S., and Chao, S. Y.: Internal solitary waves induced by flow over a ridge: With applications to the northern  
575 South China Sea, *Journal of Geophysical Research: Oceans*, 114, <https://doi.org/10.1029/2008JC005007>, 2009.

576 Stewart, K. D., Hogg, A. M., Griffies, S. M., Heerdegen, A. P., Ward, M. L., Spence, P., and England, M. H.: Vertical resolution  
577 of baroclinic modes in global ocean models, *Ocean Modelling*, 113, 50-65, <https://doi.org/10.1016/j.ocemod.2017.03.012>,  
578 2017.

579 Thompson, D. R., and Gasparovic, R. F.: Intensity modulation in SAR images of internal waves, *Nature*, 320, 345-348,  
580 <https://doi.org/10.1038/320345a0>, 1986.

581 Jackson, C. R., Da Silva, J. C., and Jeans, G.: The generation of nonlinear internal waves, *Oceanography*, 25, 108-123, 2012.

582 Vlasenko, V., Stashchuk, N., Guo, C. H. U. N. S. H. E. N. G., and Chen, X.: Multimodal structure of baroclinic tides in the  
583 South China Sea, *Nonlinear Processes in Geophysics*, 17, 529-543, <https://doi.org/10.5194/npg-17-529-2010>, 2010.

584 Xu, J., He, Y., Chen, Z., Zhan, H., Wu, Y., Xie, J., Shang, X., Ning, D., Fang, W., and Cai, S.: Observations of different effects  
585 of an anti-cyclonic eddy on internal solitary waves in the South China Sea, *Progress in Oceanography*, 188, 102422,  
586 <https://doi.org/10.1016/j.pocean.2020.102422>, 2020.

587 Zeng, Z., Chen, X., Yuan, C., Tang, S., and Chi, L.: A numerical study of generation and propagation of type-a and type-b  
588 internal solitary waves in the northern South China Sea, *Acta Oceanologica Sinica*, 38, 20-30, <https://doi.org/10.1007/s13131-019-1495-2>, 2019.

590 Zhang, Z., Fringer, O. B., and Ramp, S. R.: Three-dimensional, nonhydrostatic numerical simulation of nonlinear internal  
591 wave generation and propagation in the South China Sea, *Journal of Geophysical Research: Oceans*, 116,  
592 <https://doi.org/10.1029/2010JC006424>, 2011.

593 Zhang, H.: Modulation of Upper Ocean Vertical Temperature Structure and Heat Content by a Fast-Moving Tropical  
594 Cyclone. *Journal of Physical Oceanography*, <https://doi.org/10.1175/JPO-D-22-0132.1>, 2022.

595 Zhao, Z., Klemas, V., Zheng, Q., and Yan, X. H.: Remote sensing evidence for baroclinic tide origin of internal solitary waves  
596 in the northeastern South China Sea, *Geophysical research letters*, 31, <https://doi.org/10.1029/2003GL019077>, 2004.

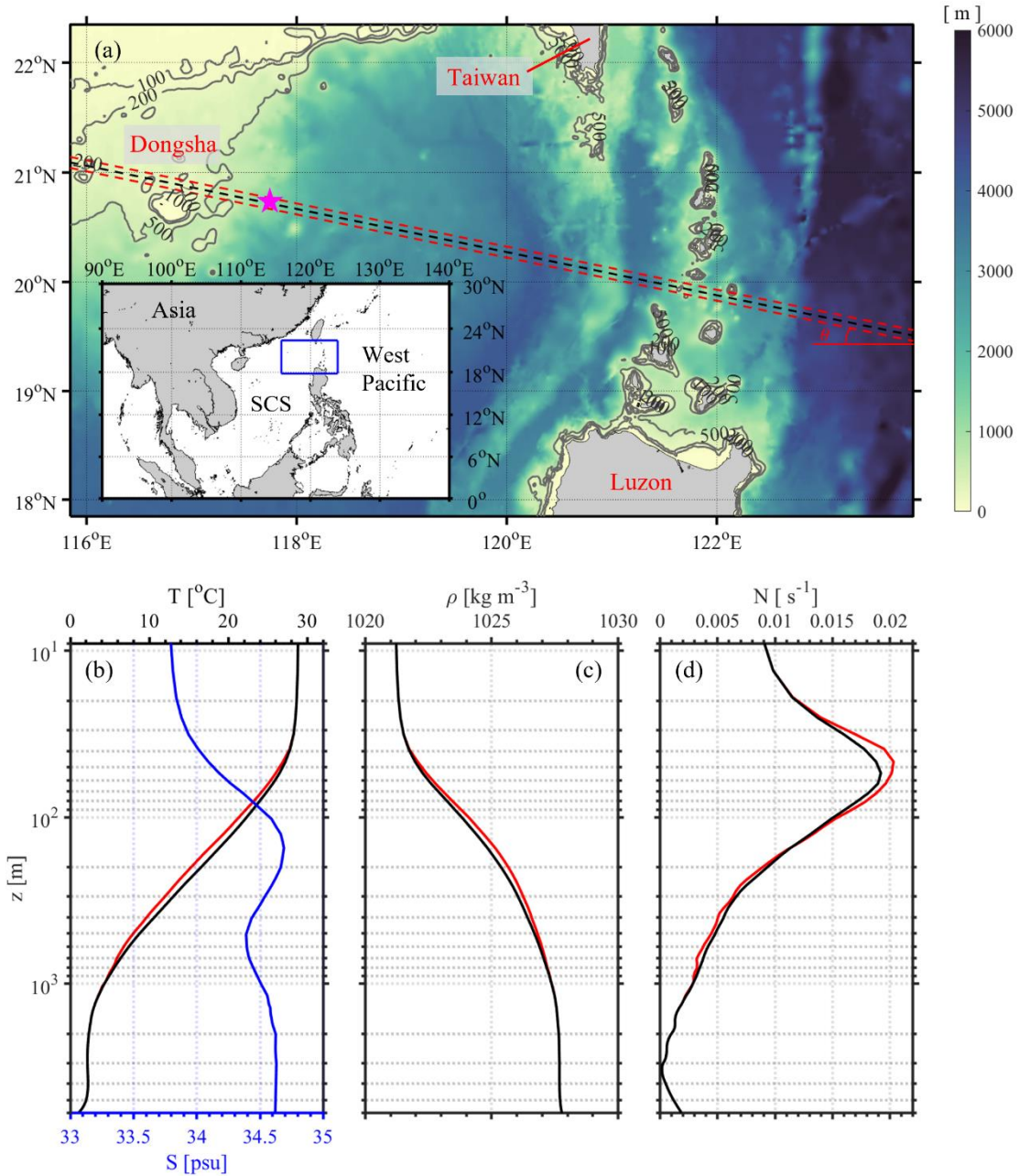
597 Zhao, Z., and Alford, M. H.: Source and propagation of internal solitary waves in the northeastern South China Sea, *Journal*  
598 *of Geophysical Research: Oceans*, 111, <https://doi.org/10.1029/2006JC003644>, 2006.

599 Zheng, Q., Yuan, Y., Klemas, V., and Yan, X. H.: Theoretical expression for an ocean internal soliton synthetic aperture radar  
600 image and determination of the soliton characteristic half width, *Journal of Geophysical Research: Oceans*, 106, 31415-31423,  
601 <https://doi.org/10.1029/2000JC000726>, 2001.

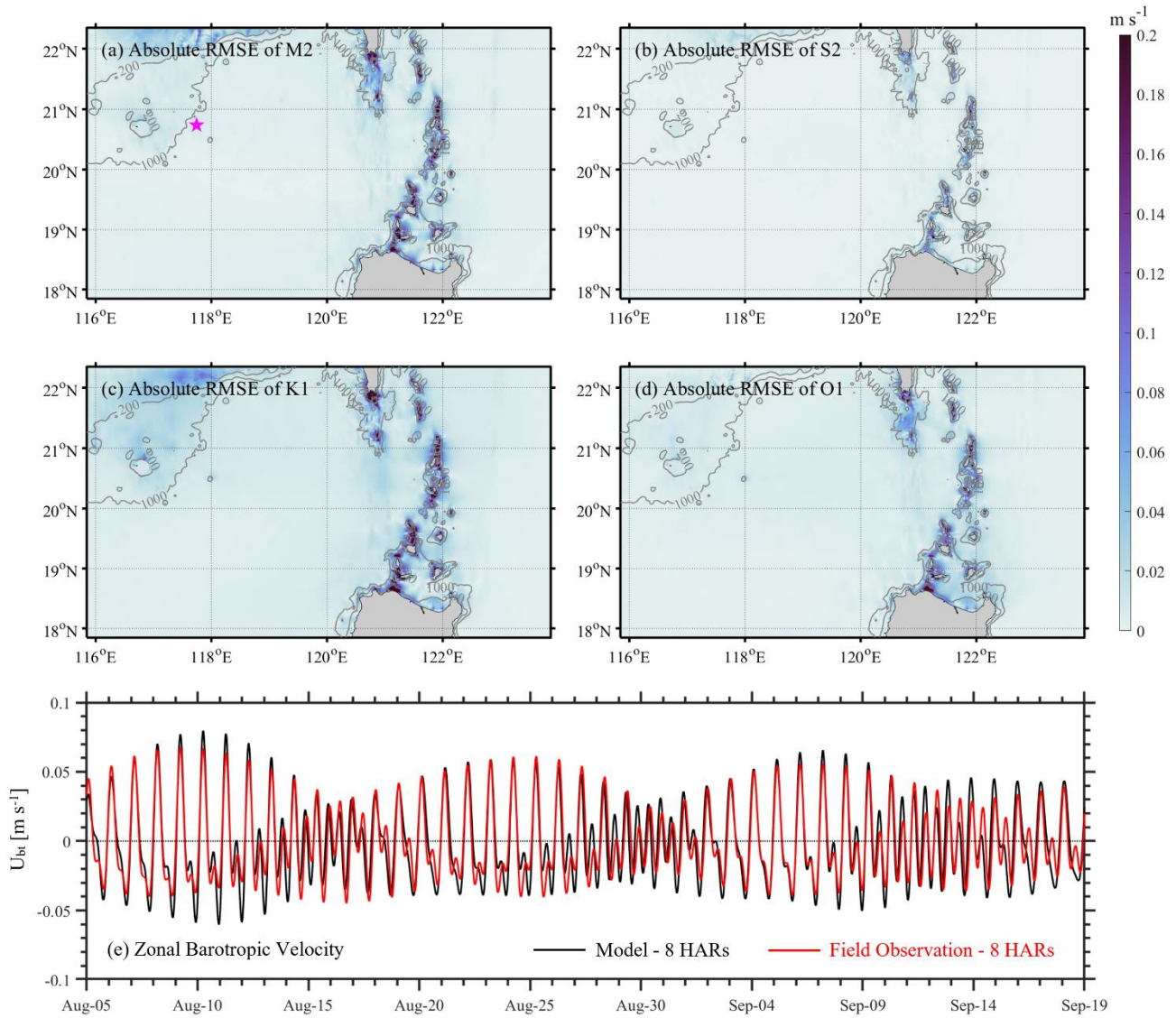
602 Zheng, Q., Susanto, R. D., Ho, C. R., Song, Y. T., and Xu, Q.: Statistical and dynamical analyses of generation mechanisms  
603 of solitary internal waves in the northern South China Sea, *Journal of Geophysical Research: Oceans*, 112,  
604 <https://doi.org/10.1029/2006JC003551>, 2007.

605

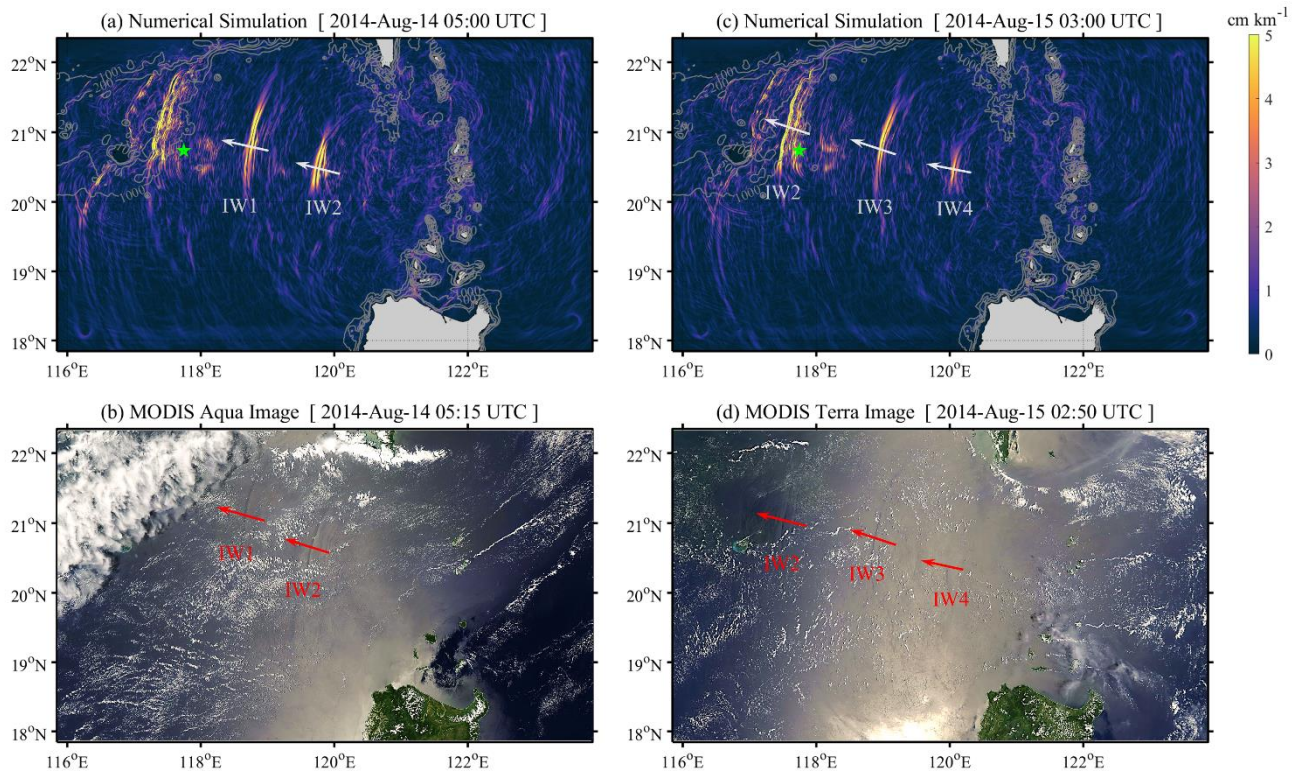
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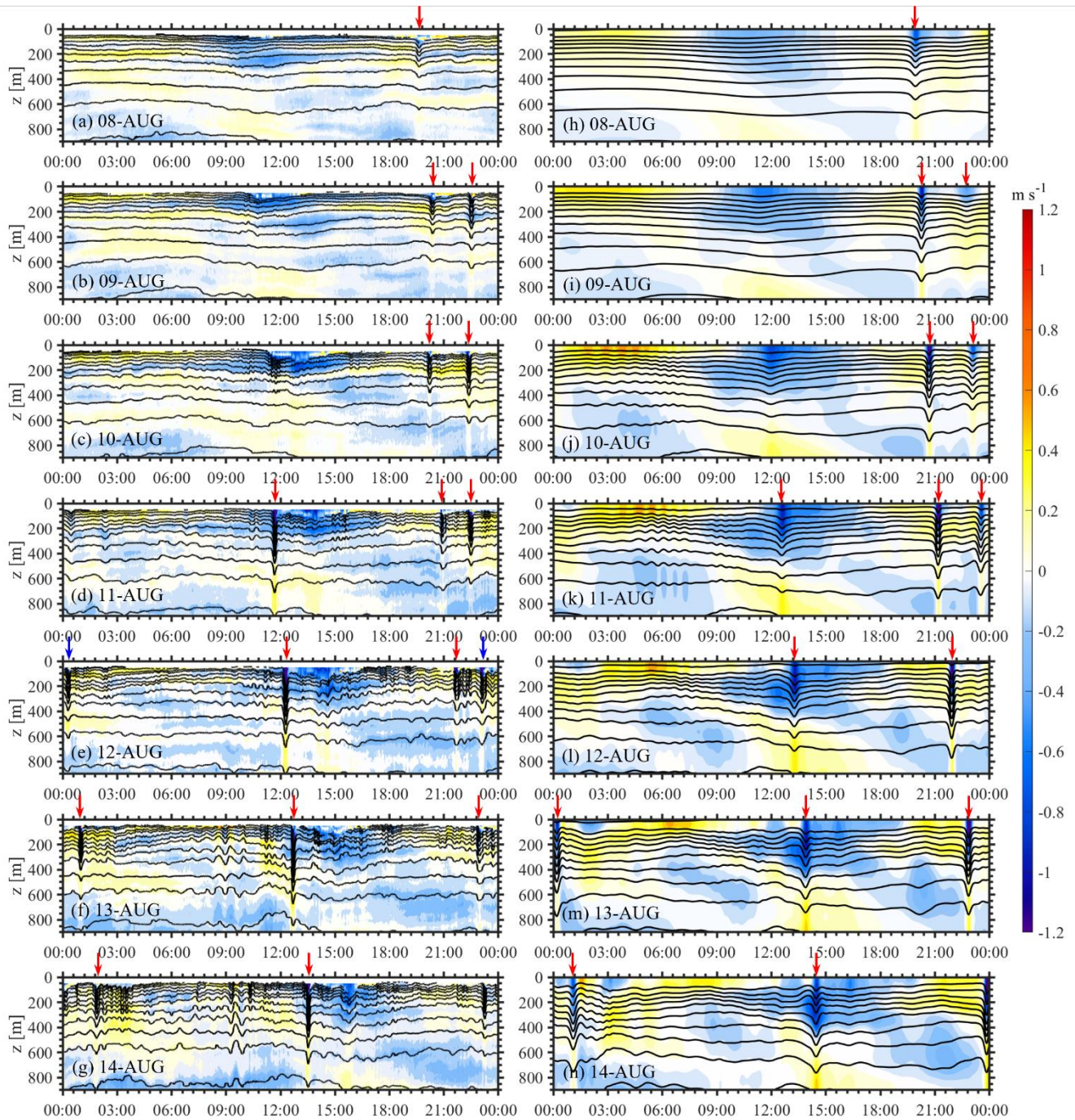
610 **Figure 1.** (a) Bathymetry map of model domain in the northern South China Sea with a mooring station DS (marked as magenta star) in the vicinity of Dongsha Atoll and the transects in 2D models, among which Exp. *2D\_500m\_8HARs* is in black dashed line while Exps. *2D\_500m\_8HARs\_005N* and *2D\_500m\_8HARs\_005S* are in red dashed lines. (b) Initial temperature and salinity profiles. (c) Density profile. (d) Buoyancy frequency profile. Note the black and red lines in (b-d) represent the data derived from the WOA18 and in-situ observations, respectively.



**Figure 2.** Absolute root-mean-square errors of zonal barotropic velocity ( $U_{bt}$ ) between the model (500m\_8HARs\_BT) and the TPXO8-Atlas dataset for M2 (a), S2 (b), K1 (c), and O1 (d). (e) Reconstructed time series of zonal barotropic velocity at station DS (marked as magenta star in Fig. 2a) of Exp. 500m\_8HARs\_BT (black line) versus measured data (red line) obtained by eight key tidal constituents.

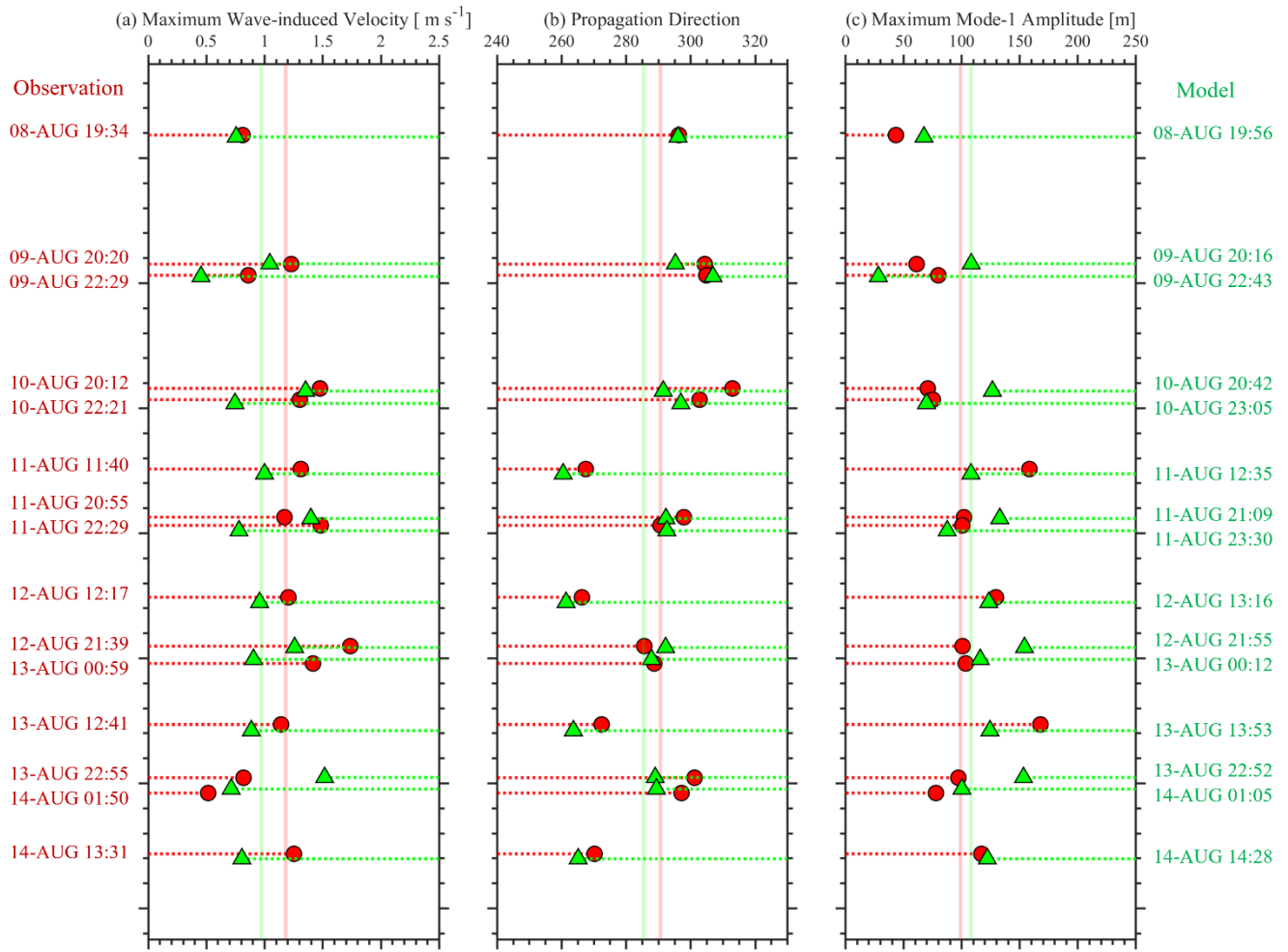


**Figure 3.** (a) Sea surface height gradients induced by internal solitary waves (ISWs) at 05:00 UTC on 14 August 2014 and (b) MODIS-Aqua image obtained at 05:15 UTC on 14 August 2014. (c) Same as (a) but at 03:00 UTC on 15 August 2014. (d) Same as (b) but for MODIS-Terra at 02:50 UTC on 15 August 2014. Note that the MODIS images in (b) and (d) are freely downloaded from the NASA Worldview application (<https://worldview.earthdata.nasa.gov>, open source).



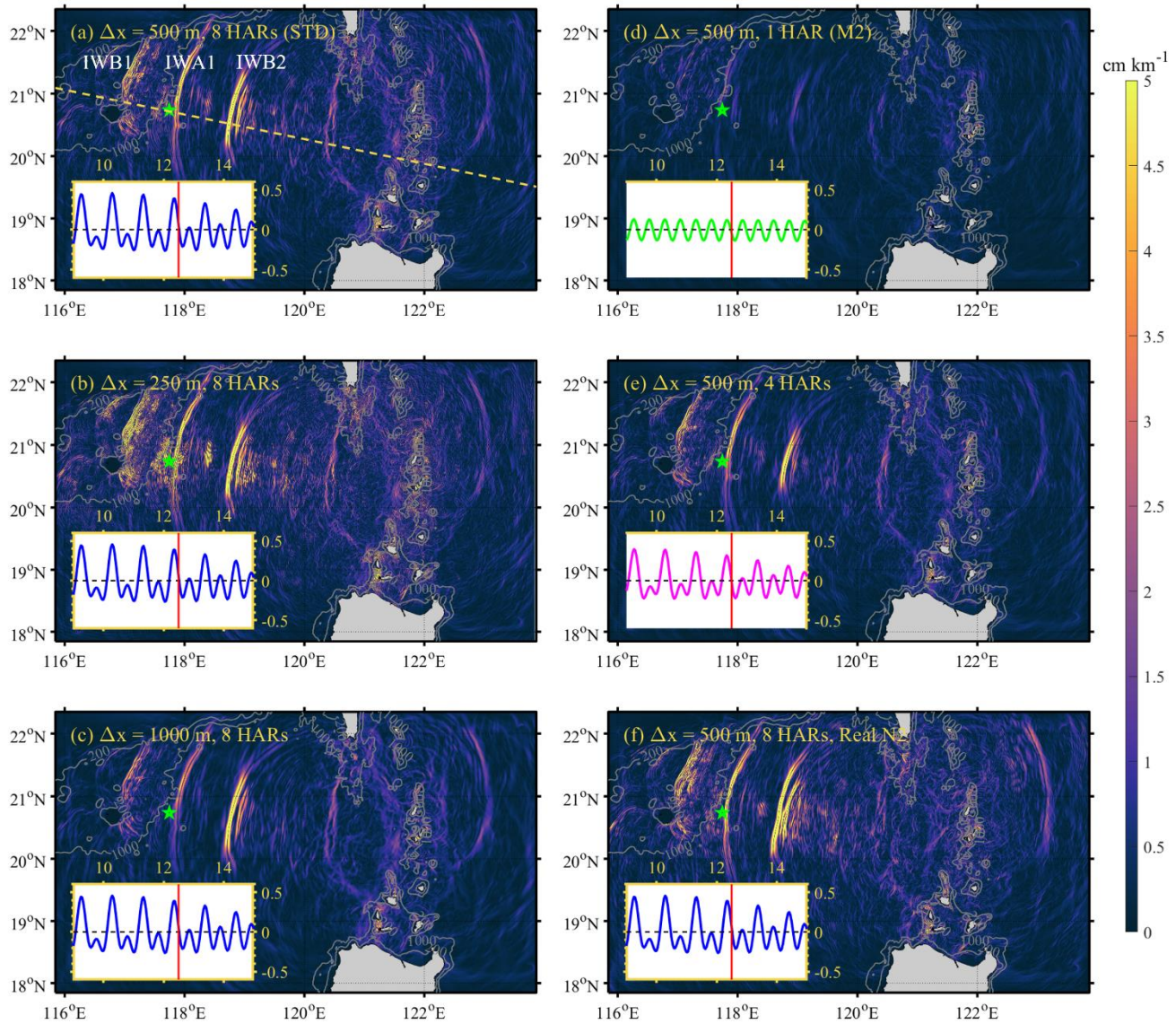
**Figure 4.** (a - g) Temperature isotherms (contours) and baroclinic velocities (shades) in the wave propagation direction from 08 August to 14 August at station DS from in-situ observation. (h - n) Same as (a - g) but for the model (*500m\_8HARS*). Red arrows indicate ISWs that model captured, while blue arrows present the missed ones.





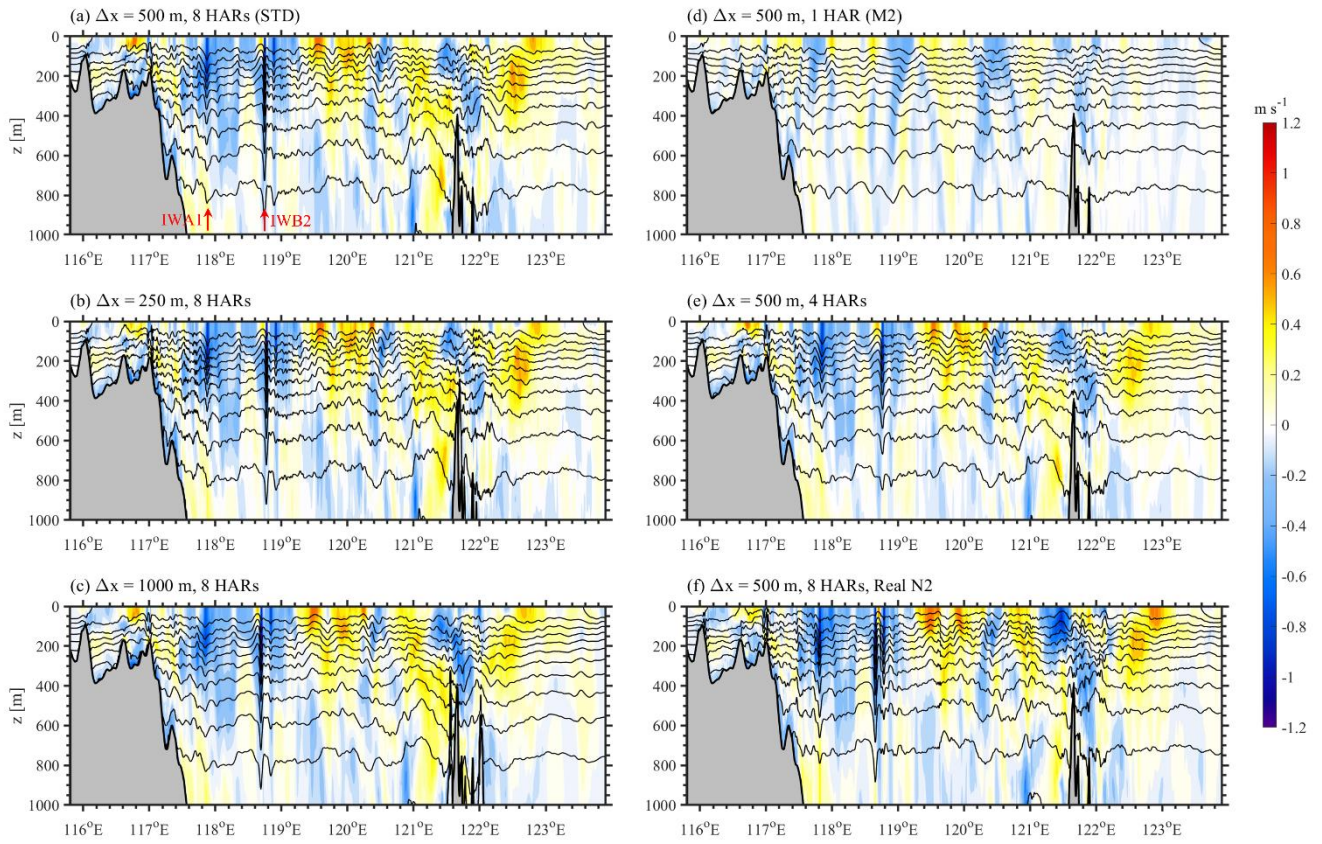
**Figure 5.** Maximum wave-induced velocities (a), propagation directions (b) and maximum mode-1 wave amplitudes (c) of fifteen ISWs at station DS from in-situ observations (red circles) and numerical models (green triangles). Averaged values are

630 shown by solid lines.

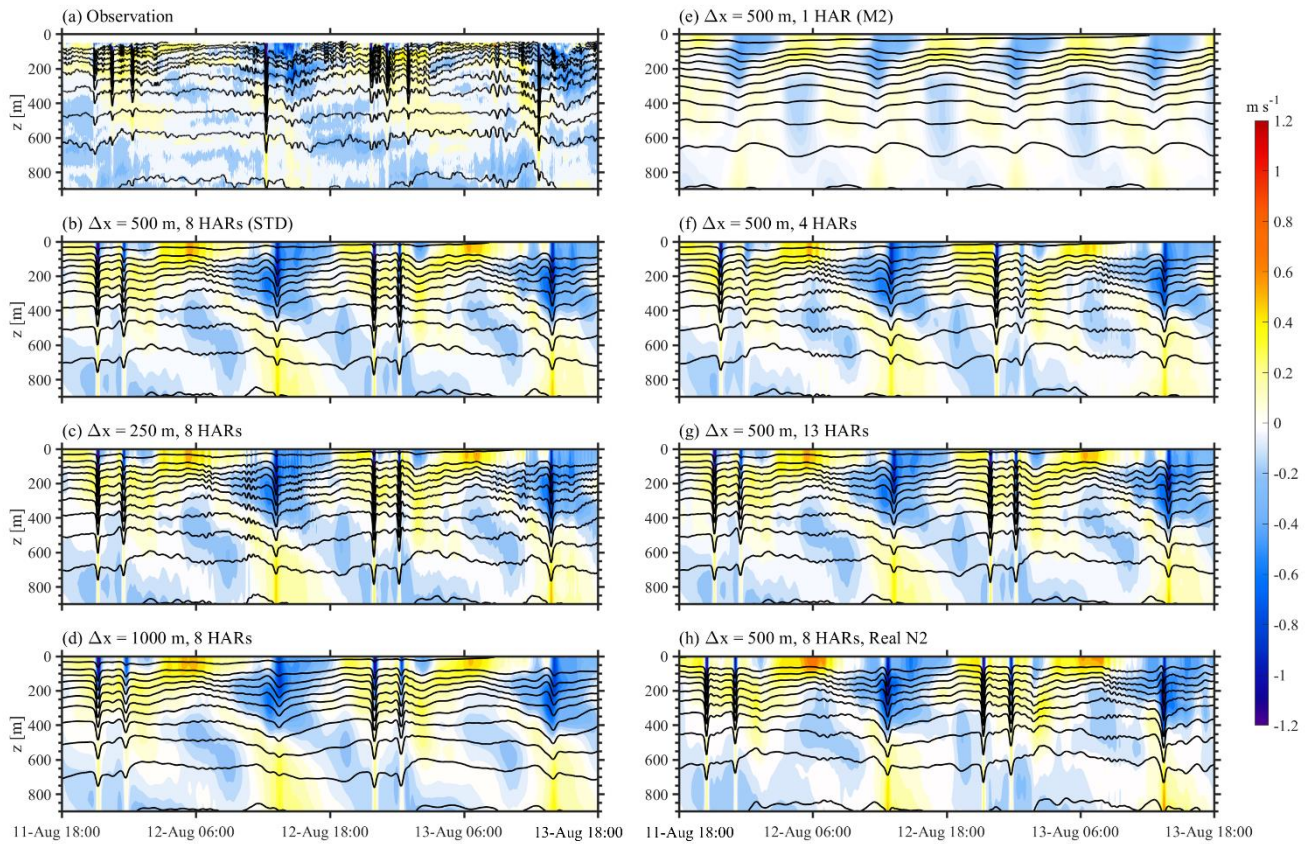


**Figure 6.** Sea surface height gradients at 12:00 UTC on 12 August 2014 in the model (a) *500m\_8HARs*, (b) *250m\_8HARs*, (c) *1000m\_8HARs*, (d) *500m\_1HAR*, (e) *500m\_4HARs*, and (f) *500m\_Real\_N2*. Note that dashed line in (a) is selected transect to present vertical structure of ISWs. Small panels on the bottom left indicate the zonal barotropic velocity (unit in  $\text{m s}^{-1}$ ) in the Luzon Strait with the solid lines showing the tidal conditions at the selected time.

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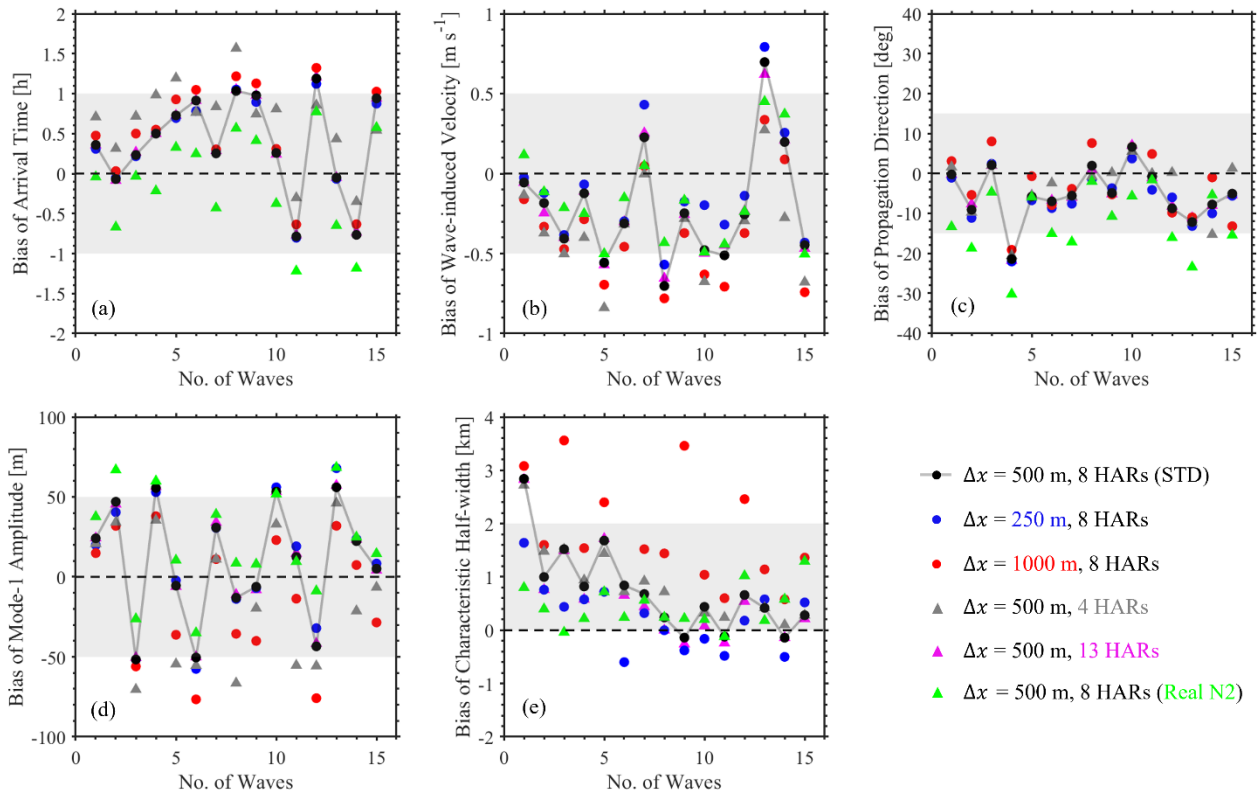


**Figure 7.** Temperature isotherms (contours) and baroclinic velocities (shades) along the transect (dashed line in Fig. 6a) at 12:00 UTC on 12 August 2014 in the model (a) *500m\_8HARs*, (b) *250m\_8HARs*, (c) *1000m\_8HARs*, (d) *500m\_1HAR*, (e) *500m\_4HARs*, and (f) *500m\_Real\_N2*. Note that waves IWA1 and IWB2 are labelled in (a) with red arrows.

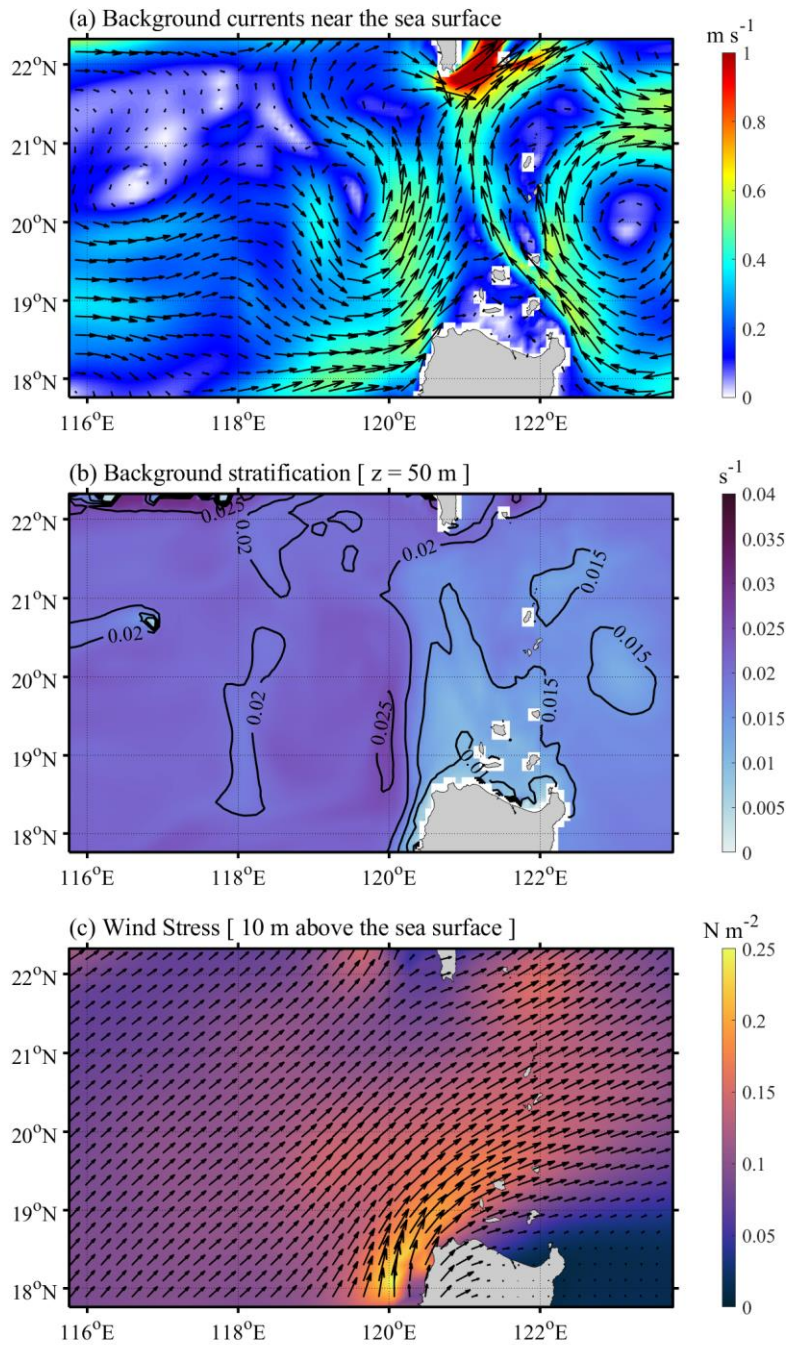


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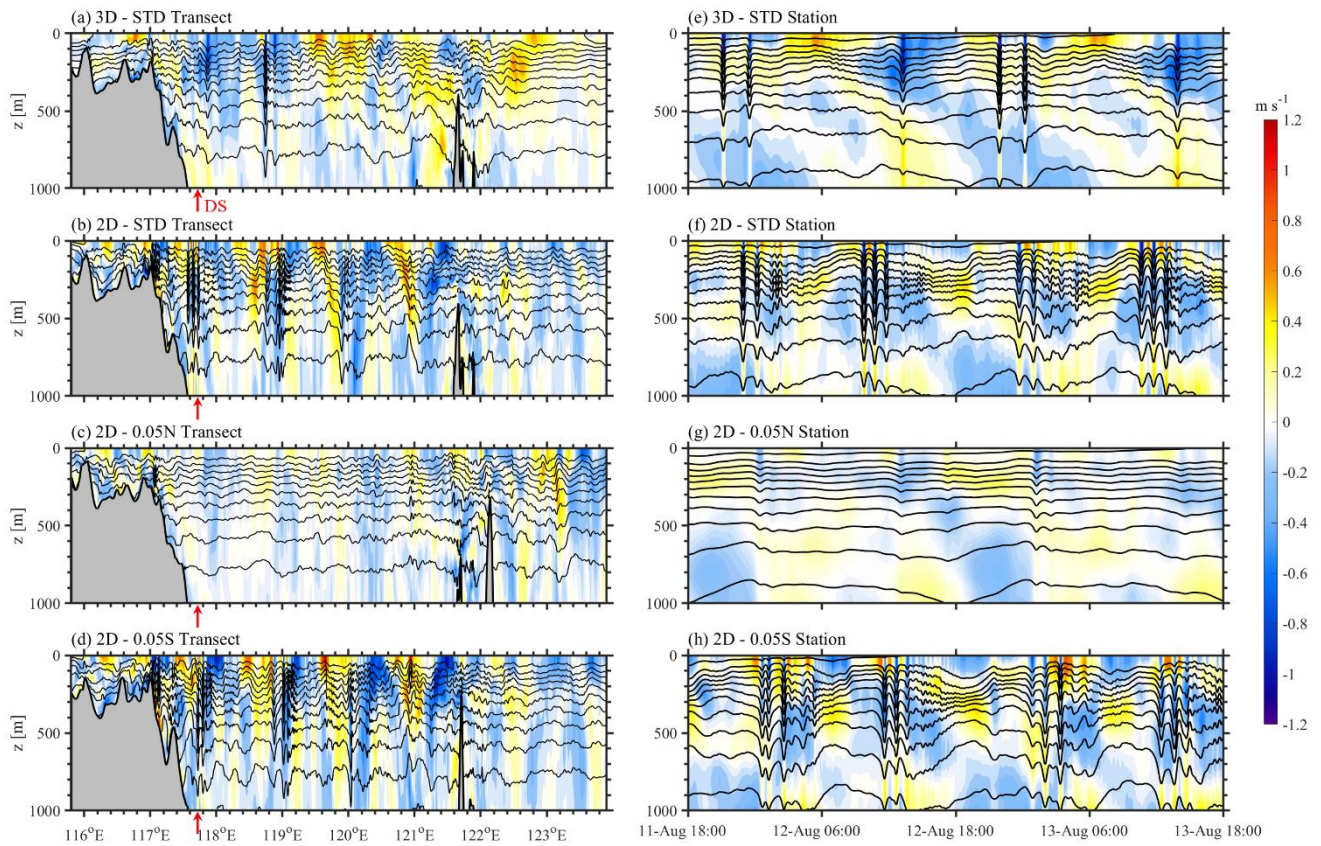
**Figure 8.** Time series of temperature isotherms (contours) and baroclinic velocities (shades) at station DS from 18:00 UTC on 11 August to 18:00 UTC on 13 August 2014 in the observation (a) and in the model (b) *500m\_8HARs*, (c) *250m\_8HARs*, (d) *1000m\_8HARs*, (e) *500m\_1HAR*, (f) *500m\_4HARs*, (g) *500m\_13HARs*, and (h) *500m\_Real\_N2*.



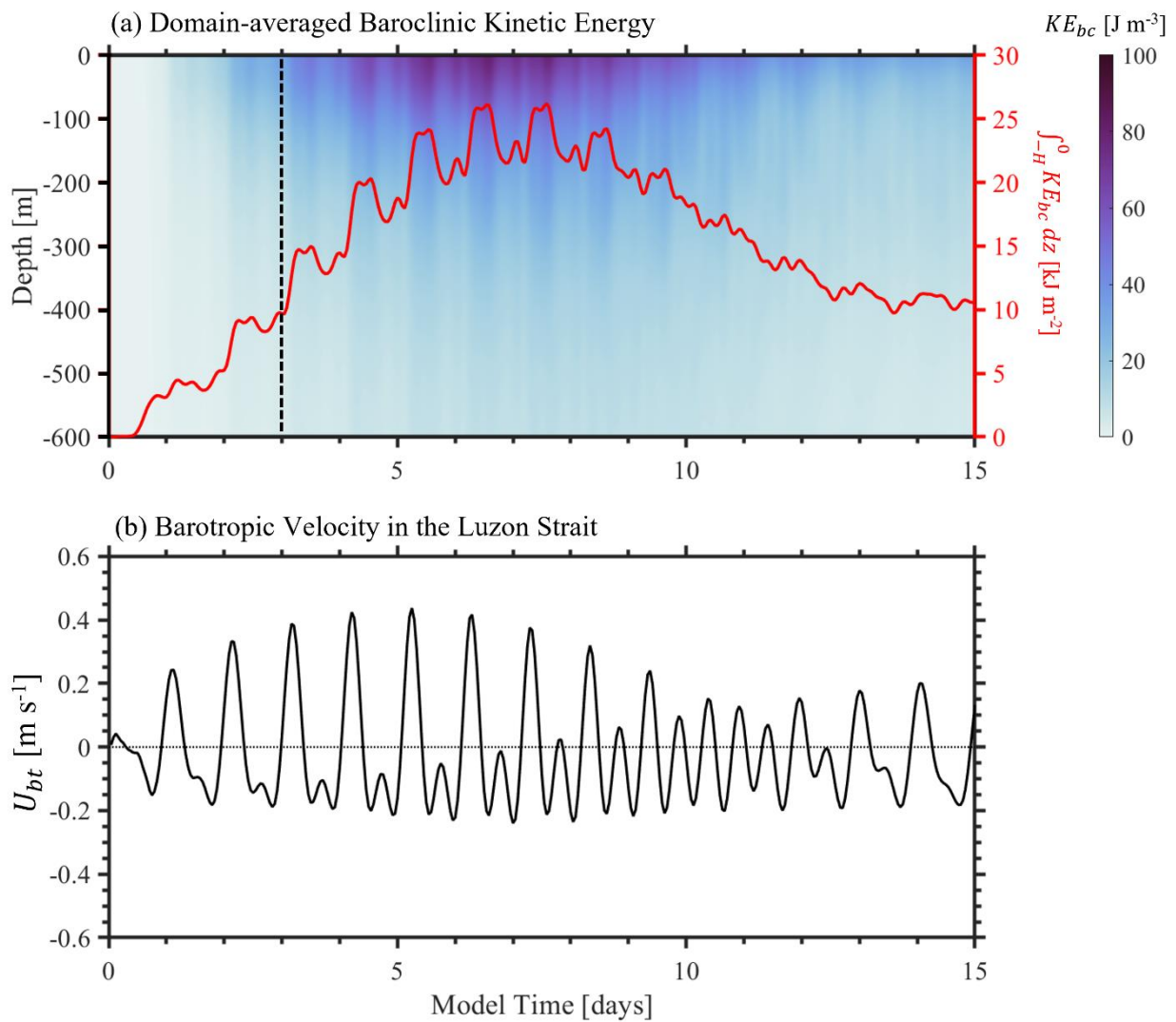
645 **Figure 9.** Bias of arrival time (a), maximum wave-induced velocities (b), propagation directions (c), maximum mode-1 wave amplitudes (d), and characteristic half-widths (e) for fifteen ISWs at station DS. Colours present different experiments.



**Figure 10.** (a) Background currents near the sea surface (averaged from 05-AUG to 20-AUG 2014, derived from the global HYCOM dataset). (b) Background buoyancy frequency at a water depth of 50 m. (c) Time-averaged wind stress at 10 m above the sea surface, which is derived from NCEPv2 hourly dataset.

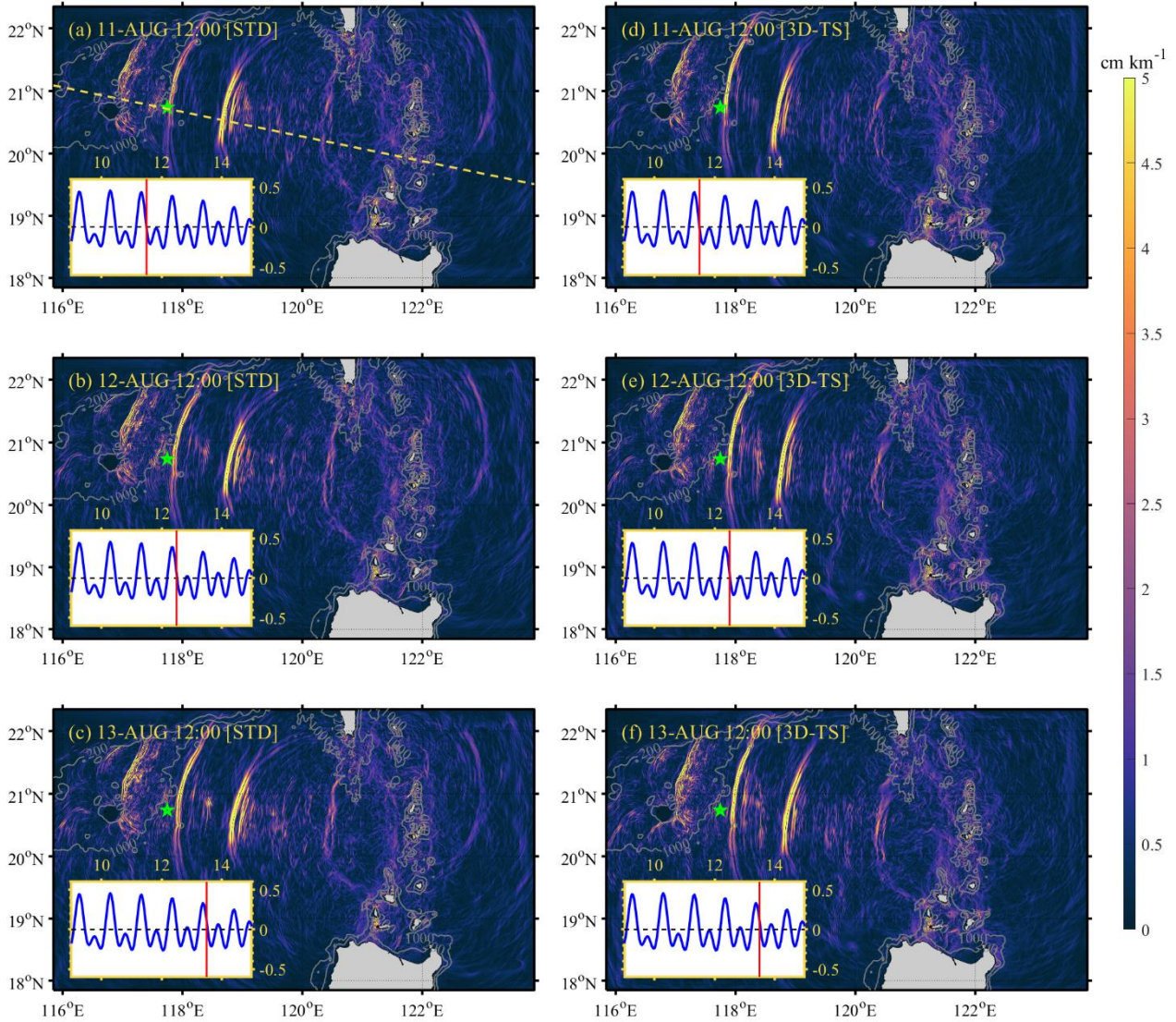


**Figure A1.** Temperature isotherms (contours) and baroclinic velocities (shades) along the transect at 12:00 UTC on 12 August 655 2014 in the 3D model (a) *500m\_8HARs*, in the 2D model (b) *2D\_500m\_8HARs*, (c) *2D\_500m\_8HARs\_005N*, and (d) *2D\_500m\_8HARs\_005S*. (e – h) Corresponding time series at the stations, which are marked as red arrows in (a – d).

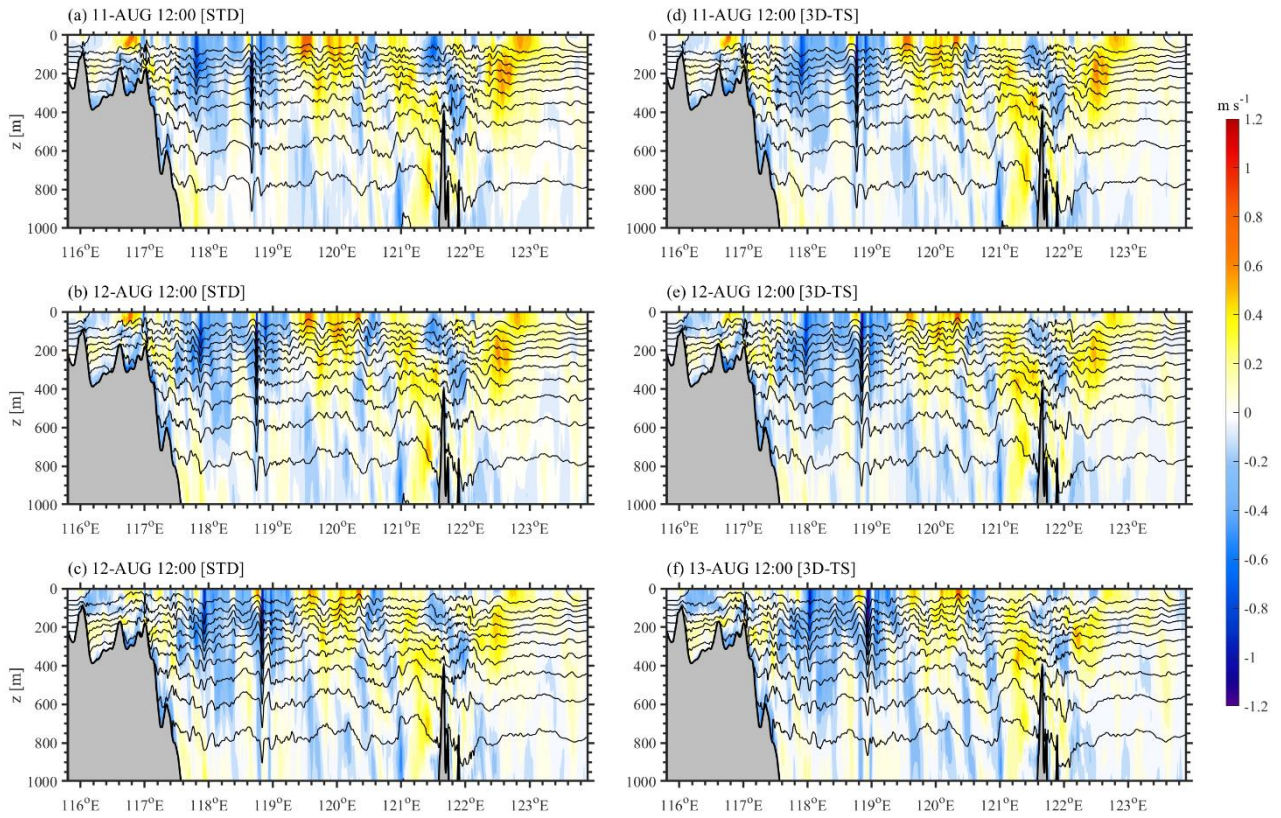


660 **Figure B1.** (a) Domain-averaged baroclinic kinetic energy ( $KE_{bc}$ , in the unit of  $J m^{-3}$ ) in the inner model domain. Note that the red solid line is domain-averaged depth-integrated  $KE_{bc}$  ( $\int_{-H}^0 KE_{bc} dz$ , in the unit of  $kJ m^{-2}$ ). (b) Time series of barotropic velocity in the Luzon Strait.





**Figure C1.** (a-c) Snapshots of sea surface gradients ( $|\nabla\eta|$ ) at 12:00 UTC on 11, 12 and 13 August in the standard experiment (EXP. *500m\_8HARs*), respectively. (d-f) Same as (a-c) but in the sensitivity experiment with horizontally inhomogeneous temperature and salinity (EXP. *3D-TS*).



**Figure C2.** (a-c) Temperature isotherms (contours) and baroclinic velocities (shades) along the transect (dashed line in Figure R1a) at 12:00 UTC on 11, 12 and 13 August in the standard experiment (EXP. *500m\_8HARs*), respectively. (d-f) Same as (a-c) but in the sensitivity experiment with horizontally inhomogeneous temperature and salinity (EXP. *3D-TS*).

670

**Table 1.** Summary of previous 3D non-hydrostatic models for internal solitary waves in the northern South China Sea, which are discussed in the text. Further details can be found in the references.

References	Model	Resolution	Tidal constituents	Model domain
Vlasenko et al. (2010) Guo et al. (2011)	MITgcm	$\Delta x = 250$ m, $\Delta y = 1000$ m	8 HARs	118.0° – 122.5°E 20.0° – 21.0°N
Zhang et al. (2011)	SUNTANS	~1358 m (75 – 4740 m)	8 HARs	115.0° – 124.0°E 18.0° – 23.0°N
Alford et al. (2015)	MITgcm	250 m	8 HARs	119.6° – 122.3°E 18.8° – 21.8°N
Lai et al. (2019)	FVCOM	~200 – 500 m (near the shoreline) ~3 km (shelf-slope region)	8 HARs	105.0° – 130.0°E 12.0° – 30.0°N
Zeng et al. (2019)	MITgcm	$\Delta x = 150$ m, $\Delta y = 300$ m	8 HARs	115.5° – 124.5°E 17.5° – 22.5°N

**Table 2.** Summary of all experimental configurations.

No.	Experiment name	Grid spacing	Tidal forcing	Stratification
1	<i>500m_8HARs</i>	500 m	8 HARs (M2, S2, N2, K2, K1, O1, P1, Q1)	WOA18
2	<i>500m_8HARs_BT</i>	500 m	8 HARs	-
3	<i>250m_8HARs</i>	250 m	8 HARs	WOA18
4	<i>1000m_8HARs</i>	1000 m	8 HARs	WOA18
5	<i>500m_1HAR</i>	500 m	1 HAR (M2)	WOA18
6	<i>500m_4HARs</i>	500 m	4 HARs (M2, S2, K1, O1)	WOA18
7	<i>500m_13HARs</i>	500 m	13 HARs (M2, S2, N2, K2, K1, O1, P1, Q1, M4, MS4, MN4, MM, MF)	WOA18
8	<i>500m_Real_N2</i>	500 m	8 HARs	DS Station

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**Table 3.** Root mean square deviation (RMSD) of wave properties between field observation and 3D sensitivity simulations at the mooring station in the vicinity of the Dongsha Atoll.

No.	Experiment name	RMSD of arrival time [h]	RMSD of wave-induced velocity [ $\text{m s}^{-1}$ ]	RMSD of propagation direction [ $^{\circ}$ ]	RMSD of mode-1 wave Amplitude [m]	RMSD of characteristic half-width [km]
1	<i>500m_8HARs</i>	0.71	0.41	8.35	37.27	1.07
2	<i>500m_8HARs_BT</i>	-	-	-	-	-
3	<i>250m_8HARs</i>	0.67	0.38	8.89	38.12	0.64
4	<i>1000m_8HARs</i>	0.79	0.49	8.54	40.28	2.41
5	<i>500m_1HAR</i>	-	-	-	-	-
6	<i>500m_4HARs</i>	0.81	0.58	8.22	43.69	1.10
7	<i>500m_13HARs</i>	0.71	0.40	8.23	37.36	1.01
8	<i>500m_Real_N2</i>	0.62	0.34	14.74	37.88	0.58