



1 **An Improved Parameterization of Sea Spray-Mediated**
2 **Heat Flux Using Gaussian Quadrature: Case Studies with**
3 **a Coupled CFSv2.0-WW3 System**

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8



9 **Abstract.** Sea spray-mediated heat flux plays an important role in air-sea heat transfer. Heat flux
10 integrated over droplet size spectrum can well simulate total heat flux induced by sea spray droplets.
11 Previously, a fast spray-flux scheme assuming single-radius droplets (A15) was widely used since the
12 full-size spectrum integral is computational expensive. Based on the Gaussian Quadrature (GQ) method,
13 a new fast scheme (SPRAY-GQ) of sea spray-mediated heat flux is derived. The performance of SPRAY-
14 GQ is evaluated by comparing heat fluxes with those estimated from the widely-used A15. The new
15 scheme shows a better agreement with the original spectrum integral. To further evaluate the performance
16 of A15 and SPRAY-GQ, the two schemes are implemented into a coupled CFSv2.0-WW3 system, and
17 a series of 56-day simulations in summer and winter are conducted and compared. The comparisons with
18 satellite measurements and reanalysis data show that the SPRAY-GQ scheme could simulate air-sea heat
19 flux more reasonably than the A15 scheme. For experiments based on SPRAY-GQ, the sea surface
20 temperature at mid-high latitudes of both hemispheres, particularly in summer, is significantly improved
21 compared with the experiments based on A15. The simulation of 10-m wind speed and significant wave
22 height at mid-low latitudes of the Northern Hemisphere is improved as well. The computational time of
23 SPRAY-GQ is about the same as that of A15. Thereby, the newly-developed SPRAY-GQ scheme has a
24 potential to be used for improving air-sea heat flux in coupled models.
25



26 **1 Introduction**

27 Sea spray droplets, ejected from oceans, include film drops, jet drops and spume drops (Veron, 2015).
28 The first two types of droplets are generated from bubble bursting caused by ocean surface wave breaking,
29 with radius ranging from 0.5 μm to 50 μm (Resch and Afeti, 1991; Thorpe, 1992; Melville, 1996; Spiel,
30 1997; Andreas, 1998; Lhuissier and Villermaux, 2012). Spume drops are generated by strong winds (>
31 7-11 m/s) which directly tear the wave crests, with larger radius ranging from tens to hundreds μm
32 (Koga, 1981; Andreas et al., 1995; Andreas, 1998). Sea spray droplets play an important role in weather
33 and climate processes (Fox-Kemper et al., 2022). On one hand, sea spray droplets contribute to local
34 marine aerosols and subsequently modify the local radiation balance (Fairall et al., 1983; Burk, 1984;
35 Fairall and Larsen, 1984). On the other hand, sea spray droplets affect the fluxes of heat, momentum,
36 salt, and freshwater between atmosphere and ocean (Andreas, 1992; Andreas et al., 2008; Andreas, 2010;
37 Andreas et al., 2015; Ling and Kao, 1976; Fairall et al., 1994; Andreas and Decosmo, 2002).

38 The sea spray-mediated heat transfer mainly occurs within the droplet evaporation layer (DEL) near
39 the sea surface (Andreas and Decosmo, 1999, 2002; Fairall et al., 1994). Sea spray droplets with the same
40 temperature as ocean surface can lead to sensible heat flux in DEL, while water evaporated from these
41 droplets can further release latent heat to the atmosphere (Andreas, 1992; Borisenkov, 1974; Bortkovskii,
42 1973; Wu, 1974; Monahan and Van Patten, 1988; Ling and Kao, 1976). Part of the sea spray-mediated
43 sensible heat is absorbed by droplet evaporation, which further increases the air-sea temperature
44 difference, and thus increases the sea spray-mediated sensible heat flux (Fairall et al., 1994; Andreas and
45 Decosmo, 2002). Since strong winds produce more sea spray droplets with larger radius, sea spray-
46 mediated heat fluxes increase with wind speed (Fairall et al., 1994), and contribute more than 10% of the
47 total surface heat flux after reaching the threshold speed (> 11 m/s for sensible heat flux and > 13 m/s
48 for latent heat flux)(Andreas et al., 2008). In addition, when a droplet is released into the air, it is
49 accelerated due to surface winds (Edson and Andreas, 1997; Fairall et al., 1994; Van Eijk et al., 2011;
50 Wu et al., 2017). If the droplet could fall back into the ocean, additional momentum would be injected
51 into the ocean from the atmosphere (Andreas, 1992, 2004).

52 The usual bulk parameterizations in numerical models for surface fluxes only include the interfacial
53 (turbulent) fluxes (e.g., Fairall et al., 1996), while neglecting the significant contributions of sea spray



54 droplets in DEL (Andreas et al., 2008; Fairall et al., 1994; Smith, 1997; Emanuel, 1995). Andreas and
55 Emanuel (2001) implemented sea spray-mediated heat flux and momentum flux parameterizations into
56 a simple tropical cyclone model, and found that the sea spray-induced heat flux significantly enhances
57 the tropical cyclone intensity, offsetting the negative effect of enhanced surface drag by strong wind and
58 waves. The similar enhancement of tropical cyclone intensity was also shown in recent regional coupling
59 systems by including sea spray-mediated heat flux (Xu et al., 2021a; Liu et al., 2012; Garg et al., 2018;
60 Zhao et al., 2017). In the First Institute of Oceanography Earth System Model, Bao et al. (2020) first
61 incorporated the sea spray-mediated heat flux in global climate simulation. Following Bao et al. (2020),
62 Song et al. (2022) found the sea spray-mediated heat flux can lead to cooling at the air-sea interface and
63 strengthening westerlies in the Southern Ocean, and thus improves estimates of sea surface temperature
64 (SST).

65 Since the parameterization of sea spray-mediated heat flux derived from observations requires full-
66 size spectral integral and demands huge amount of computational time (Andreas, 1989, 1990, 1992;
67 Andreas et al., 2015), a simplified parameterization based on a single radius of sea spray droplets
68 (Andreas et al., 2015; Andreas et al., 2008) is widely used in atmosphere-ocean coupling systems (Xu et
69 al., 2021a; Liu et al., 2012; Garg et al., 2018; Zhao et al., 2017; Song et al., 2022; Bao et al., 2020), and
70 apt to produce significant biases. To reduce biases induced by the single radius of sea spray droplets, we
71 develop a new parameterization of sea spray-mediated heat flux based on the Gaussian Quadrature (GQ)
72 method, a fast and accurate way to calculate spectral integral. The GQ method has been successfully
73 used for the estimation of domain-averaged radiative flux profiles (Li and Barker, 2018). The
74 performance of the GQ-based parameterization of the sea spray-mediated heat flux is evaluated and
75 compared with the simplified parameterization for single radius of Andreas et al. (2015), referred to as
76 A15 hereafter. The results are first compared with the original parameterization using full-size spectral
77 integral (A92, hereafter). Then the parameterizations are implemented in a global coupled atmosphere-
78 ocean-wave system (Shi et al., 2022), and the results are compared with global satellite measurements
79 and reanalysis data.

80 The rest of the paper is structured as follows: observation and reanalysis data for comparisons are
81 introduced in Section 2; the derivation of the GQ-based parameterization and the global coupling system



82 are described in Section 3; the performance of the new parameterization is evaluated in Section 4. Finally,
83 a summary and discussion are given in Section 5.

84 2 Data

85 The fifth generation European Centre for Medium-Range Weather Forecasts (ECMWF) Reanalysis
86 (ERA5; Hersbach et al., 2020) data assimilated huge amounts of historical data and thus provided reliable
87 hourly estimates. ERA5 10-m wind speed (WSP10), 2-m air temperature, 2-m dewpoint temperature,
88 surface pressure and significant wave height (SWH) with a spatial resolution of 0.5° are used.
89 Additionally, WSP10, 2-m air temperature and 2-m specific humidity data from the Objectively
90 Analyzed air-sea Fluxes (OAFflux) products (Yu et al., 2008) are also applied for comparison, with $1^\circ \times 1^\circ$
91 resolution. The daily average satellite Optimum Interpolation SST (OISST) data are obtained from the
92 National Oceanic and Atmospheric Administration (NOAA) with a spatial resolution of 0.25° (Reynolds
93 et al., 2007). The global monthly mean salinity observation from European Space Agency (ESA;
94 https://climate.esa.int/sites/default/files/SSS_cci-D1.1-URD-v1r4_signed-accepted.pdf) are applied.

95 3 Methods

96 3.1 Development of a Fast Algorithm Based on GQ

97 The effects of sea spray droplets on sensible and latent heat fluxes ($H_{S,SP}$, $H_{L,SP}$) contribute to the total
98 sensible and latent heat fluxes ($H_{S,T}$, $H_{L,T}$) at the air-sea interface. That is,

$$H_{S,T} = H_S + H_{S,SP}, \quad (1)$$

$$H_{L,T} = H_L + H_{L,SP}. \quad (2)$$

99 where H_S and H_L are the sensible and latent heat fluxes at the air-sea interface due to the air-sea
100 differences of temperature and humidity. Based on eddy correlation observations, A92 (Andreas, 1989,
101 1990, 1992; Andreas et al., 2015) integrates the sea spray-mediated sensible and latent heat flux
102 spectrums over initial droplet radius ($Q_S(r_0)$ and $Q_L(r_0)$) to estimate $H_{S,SP}$ and $H_{L,SP}$ (details in
103 Appendix A). The distributions of $Q_S(r_0)$ and $Q_L(r_0)$ spectrums as functions of initial droplet radius
104 r_0 under various atmosphere and ocean state are shown in Fig. 1, indicating that Q_S and Q_L spectrums



105 are more sensitive to the change of 10-m wind speed, and less sensitive to other variables, including 2-
106 m air temperature, 2-m relative humidity, sea surface temperature, surface air pressure and sea surface
107 salinity.

108 The calculation of $H_{S,SP}$ and $H_{L,SP}$ in A92 requires huge amount of computational time due to full-
109 size spectral integral (Eqn. A5-A6 of Appendix A), therefore it is difficult to apply A92 directly in
110 coupled modeling systems. A15 (Andreas et al., 2015) developed a fast algorithm by using a single
111 representative droplet radius (details in Appendix B), which was widely adopted in recent regional and
112 global coupling systems (Xu et al., 2021a; Liu et al., 2012; Garg et al., 2018; Zhao et al., 2017; Song et
113 al., 2022; Bao et al., 2020). In this study, we apply a 3-node GQ method (details in Appendix C) to
114 develop a new fast algorithm to approximate the full-size spectral integral of A92. Notably, GQ can
115 converge exponentially to the actual integral only for a smooth function (McClarren, 2018). Since as
116 functions of r_0 , Q_S and Q_L are not smooth (Fig. 1), a data sorting from largest to smallest is required.
117 After sorting, Q_S and Q_L become Q_{SS} and Q_{LS} , and then GQ can be used to estimate the integral of
118 Q_{SS} and Q_{LS} . However, the sorting leads to high complexity of GQ comparable to A92. Therefore, it is
119 necessary to find the general law of GQ nodes for Q_{SS} and Q_{LS} to avoid the sorting in application.

120 To derive the general law of GQ nodes, we calculate the distribution of the sea spray-mediated heat
121 flux spectral following A92, based on the global daily WSP10, 2-m air temperature, 2-m dewpoint
122 temperature, surface pressure and SWH of ERA5 and OISST from August 1, 2018 to August 31, 2018.
123 The ESA monthly salinity is also applied since the sea spray-mediated heat flux is the least sensitive to
124 salinity (Fig. 1e&f) and only monthly salinity observation data is available. From the global spectrums,
125 we sort Q_S and Q_L from largest to smallest. The GQ nodes corresponding to r_0 of the sensible (latent)
126 heat flux after sorting are denoted as r_{S1} , r_{S2} and r_{S3} (r_{L1} , r_{L2} and r_{L3}), whose distribution of
127 occurrence frequency in percentage is shown in Fig. 2. It is noted that except that r_{L3} is related to
128 WSP10 (Fig. 2c), all other five nodes have frequency roughly concentrated at a constant (peak
129 frequency >65%), that is

$$r_{S1} = 459.056, r_{S2} = 294.185, r_{S3} = 166.771, \quad (3)$$

$$r_{L1} = 443.914, r_{L2} = 251.0498, \quad (4)$$



$$r_{L3} = \begin{cases} 60.310WSP10^{0.1161}, & WSP10 \geq 2 \text{ m/s} \\ 58.086, & WSP10 < 2 \text{ m/s} \end{cases}, \quad (5)$$

130 where the unit of the radius is micrometer. And then the 3-node GQ to approximate the full-size spectral
131 integral of A92 are

$$\int_a^b Q_S(r_0) dr_0 \approx \frac{b-a}{2} \sum_{i=1}^3 \omega_i Q_S(r_{Si}), \quad (6)$$

$$\int_a^b Q_L(r_0) dr_0 \approx \frac{b-a}{2} \sum_{i=1}^3 \omega_i Q_L(r_{Li}). \quad (7)$$

132 Here a and b are the lower and upper limits of r_0 , which are set to $2\mu\text{m}$ and $500\mu\text{m}$ based on Andreas
133 (1990), and ω_i is the corresponding weight ($\omega_1=\omega_3=0.556$, $\omega_2=0.889$), obtained from McClarren
134 (2018). Thus, we can directly use Eqn. (3-7) to estimate the GQ-based $H_{S,SP}$ and $H_{L,SP}$ approximations,
135 avoiding sorting. The new fast algorithm is referred to as SPRAY-GQ hereafter.

136 3.2 CFSv2.0-WW3 Coupling System

137 A coupled system based on Climate Forecast System model version 2.0 (CFSv2.0) and
138 WAVEWATCH III (WW3) is employed to evaluate and compare the effects of sea spray-mediated heat
139 flux parameterized by A15 and SPRAY-GQ. The CFSv2.0-WW3 has three components, the Global
140 Forecast System (GFS; <http://www.emc.ncep.noaa.gov/GFS/doc.php>) as the atmosphere component of
141 CFSv2.0, the Modular Ocean Model version 4 (MOM4; Griffies et al., 2004) as the ocean component of
142 CFSv2.0, and the WW3 (WAVEWATCH III Development Group, 2016) as the ocean surface wave
143 component. The variables between CFSv2.0 and WW3 are interpolated and passed using the Chinese
144 Community Coupler version 2.0 (C-Coupler2; Liu et al., 2018).

145 The CFSv2.0 is mainly applied for intraseasonal and seasonal prediction (e.g., Saha et al., 2014). The
146 atmosphere component GFS uses a spectral triangular truncation of 382 waves (T382) in the horizontal,
147 equivalent to a grid resolution of nearly 35 km, and 64 sigma-pressure hybrid layers in the vertical. The
148 MOM4 is integrated on a nominal 0.5° horizontal grid with enhanced horizontal resolution to 0.25° in
149 the tropics, and there are 40 levels in the vertical. The latitude range of WW3 is 78°S – 78°N with a spatial
150 resolution of $1/3^\circ$. In the coupling system, the WW3 obtains 10-m wind and ocean surface current from
151 CFSv2.0, and then provides wave parameters to CFSv2.0. Several wave-mediated processes, including



152 upper ocean mixing modified by Stokes drift-related processes, air-sea fluxes modified by surface current
153 and Stokes drift, and momentum roughness length, are considered. Details of this system are referred to
154 Shi et al. (2022).

155 A series of numerical experiments is conducted to evaluate the effects of the two parameterizations
156 (A15 and SPRAY-GQ) of sea spray-mediated heat flux on ocean, atmosphere and waves in two 56-day
157 periods, from January 3 to February 28, 2017 and from August 3 to September 28, 2018 for boreal winter
158 and boreal summer, respectively. For each period, two sensitivity experiments are carried out. The first
159 is the SPRAY-A15 experiment, in which A15 is used with two-way fully coupling. The second is the
160 SPRAY-GQ experiment, in which SPRAY-GQ parameterization is used instead of A15.

161 4 Results

162 4.1 Comparison with A92

163 Based on the daily global WSP10, 2-m air temperature, 2-m dewpoint temperature, surface pressure
164 and SWH of ERA5, the daily global OISST, and the ESA monthly global salinity, $H_{S,SP}$ and $H_{L,SP}$
165 from A15, SPRAY-GQ and A92 are calculated (Fig. 3). The computational time for SPRAY-GQ is about
166 the same as that for A15, and about 36 times less than the time for A92. Compared with A92 (the black
167 dotted line), A15 (red) overestimates $H_{S,SP}$ for low $H_{S,SP}$ (<50 W/m²) and underestimates $H_{S,SP}$ for
168 high $H_{S,SP}$ (>50 W/m²) with a root mean square error (RMSE) of 3.40 W/m² (Fig. 3a), while A15 shows
169 consistent overestimations with a RMSE of 2.98 W/m² for $H_{L,SP}$ (Fig. 3b). Overall, the RMSE of A15
170 is about 2.69 W/m² for sea-spray mediated total heat flux ($TH_{SP} = H_{S,SP} + H_{L,SP}$; Fig. 3c). Compared with
171 A15, SPRAY-GQ (blue) has less deviation from A92 for both $H_{S,SP}$ and $H_{L,SP}$ (Fig. 3a&b). The
172 corresponding RMSEs of SPRAY-GQ for $H_{S,SP}$, $H_{L,SP}$ and TH_{SP} are 0.83 W/m², 0.92 W/m² and 0.62
173 W/m², all significantly lower ($P < 0.05$ in Student's t-test) than those of A15.

174 To test robustness of the results, we also use WSP10, 2-m air temperature and 2-m specific humidity
175 of OAFflux dataset to estimate $H_{S,SP}$ and $H_{L,SP}$. As shown in Fig. 4, SPRAY-GQ has significantly
176 ($P < 0.05$ in Student's t-test) lower deviations and RMSEs than A15, consistent with Fig. 3. Note that the
177 values of $H_{S,SP}$ and $H_{L,SP}$ in Fig.4 are larger than those in Fig. 3, since the equivalent neutral wind



178 speed from OAFlux is generally overestimated compared to the observed wind speed (Seethala et al.,
179 2021; Praveen Kumar et al., 2012). In addition, since it is common to derive SWH from empirical
180 equations (e.g., Andreas et al., 2008; Andreas et al., 2015; Andreas and Decosmo, 2002; Andreas, 1992),
181 we also use SWH generated by empirical equations of WSP10 (Andreas, 1992) instead of ERA5 SWH
182 to estimate $H_{S,SP}$ and $H_{L,SP}$ (Fig. 5). Again, the RMSEs decrease significantly ($P < 0.05$ in Student's t-
183 test) in SPRAY-GQ compared to A15, though the RMSEs become higher for all estimates due to the
184 enhanced biases of SWH. Thereby, it is clear that the performance of SPRAY-GQ is always better than
185 A15. Next, we will evaluate and compare the two fast algorithms in an atmosphere-ocean-wave coupled
186 system (CFSv2.0-WW3).

187 **4.2 Comparison in the CFSv2.0-WW3 Coupling System**

188 In this section, comparisons are made for simulated SSTs, WSP10s as well as SWHs against OISST
189 and ERA5 reanalysis (Figs. 6-11). The results in the first three days are excluded in the comparison, since
190 the wave influences are weak at the beginning of the simulations. The computational time is about the
191 same for experiments SPRAY-GQ and SPRAY-A15.

192 **4.2.1 Sea Surface Temperature (SST)**

193 In the austral summer, compared with OISST, large SST biases (>1 °C or <-1 °C) of SPRAY-A15
194 occur in the Southern Hemisphere (SH; Fig. S1a in supplementary), especially in the Southern Ocean. It
195 is always a challenge for reducing the large SST biases in the Southern Ocean for climate models (e.g.,
196 Alessandro et al., 2019; Wang et al., 2014; Li et al., 2013; Bodas-Salcedo et al., 2012; Ceppi et al., 2012).
197 In Fig. 6a, SSTs north (south) of 50°S in experiment SPRAY-A15 are mainly underestimated
198 (overestimated). The domain-averaged RMSE (0-360°E, 40-75°S) increases in the first month and then
199 levels off (red line in Fig. 6c). While the domain-averaged RMSE in experiment SPRAY-GQ levels off
200 about a week earlier (black line in Fig. 6c). The time series of RMSE in SPRAY-GQ is significantly
201 lower than that in SPRAY-A15 ($P < 0.05$ in Student's t-test). The decreased SST RMSE in SPRAY-GQ
202 is resulted from the increased (decreased) SSTs north (south) of 50°S (Fig. 6b).

203 To understand the effects of sea spray droplets on SST, we calculate the total heat flux ($TH = H_{S,T} + H_{L,T}$)



204 differences between SPRAY-GQ and SPRAY-A15 (Fig. 12g). The TH differences are significantly
205 correlated with SST differences (Fig. S1b in the supplementary), with the spatial correlation coefficient
206 of -0.41 ($P < 0.05$ in Student's t-test). We further decompose direct and indirect effects of sea spray
207 droplets on heat fluxes following Song et al. (2022). The direct effect ($H_{S,SP}$ and $H_{L,SP}$) is induced
208 directly by sea spray droplets, calculated from A15 (Eqn. B1-B4 of Appendix B) and SPRAY-GQ
209 (Section 3.1). The indirect effect (H_S and H_L) is the heat flux variation induced by changes of
210 atmosphere and ocean variables (including wind, pressure, humidity and temperature) caused by direct
211 effect, estimated by subtracting $H_{S,SP}$ and $H_{L,SP}$ from the output heat fluxes ($H_{S,T}$ and $H_{L,T}$) of
212 experiment SPRAY-A15 and SPRAY-GQ.

213 In the Southern Ocean, although direct differences of $H_{S,SP}$ and $H_{L,SP}$ are relatively small (< 10
214 W/m^2 , Fig. 12b, e, &h), the resulting changes of temperature and humidity lead to relatively large
215 differences in indirect effects of H_S and H_L (Fig. 12c, f, &i). Enhanced (reduced) $TH_{S,SP}$ from ocean
216 to atmosphere in the summer leads to increased (decreased) air-sea temperature difference and thus
217 enhances (weakens) H_S . Meanwhile the warmer (cooler) air also causes more (less) evaporation and thus
218 more (less) H_L . Finally, the enhanced (reduced) TH cools (warms) SST.

219 In the boreal summer, large SST biases ($> 1 \text{ }^\circ\text{C}$ or $< -1 \text{ }^\circ\text{C}$) of SPRAY-A15 mainly occur at mid-high
220 latitudes of the Northern Hemisphere (NH; Fig. S2a in supplementary). Significant underestimations
221 occur in the western and northern part of the North Pacific and at mid latitudes of the North Atlantic,
222 while large positive SST biases mainly occur in the eastern part of the North Pacific and at high latitudes
223 of the North Atlantic (Fig. 7a). In experiment SPRAY-GQ, SSTs are warmer (cooler) in the previously
224 underestimated (overestimated) regions (Fig. 7b). Therefore, the domain-averaged RMSE ($0\text{-}360^\circ\text{E}$, 20-
225 75°N) in SPRAY-GQ is significantly lower ($P < 0.01$ in Student's t-test) than in SPRAY-A15 after the
226 first three weeks (Fig. 7c). The spatial correlation coefficient between TH differences and SST
227 differences (Fig. 13g&Fig. S2b) is -0.32 ($P < 0.05$ in Student's t-test). Consistent with the austral summer,
228 the SST changes are related to the changes of heat flux (Fig. 13). The indirect effects of latent heat flux
229 (Fig. 13c) play a major role in TH differences, which are modified by the direct effects (Fig. 13b, e, &h).
230 In addition, the changes of surface wind also contribute to the changes of SST. The enhanced (reduced)
231 winds lead to stronger (weaker) ocean mixing, and thus cooler (warmer) SST (Fig. S3&S4).



232 4.2.2 10-m Wind Speed (WSP10) and Significant Wave Height (SWH)

233 Compared with experiment SPRAY-A15, significant improvements of WSP10 in SPRAY-GQ occur
234 at mid-low latitudes of the NH (0-360°E, 0-60°N) in both winter and summer (Fig.8&9). The domain-
235 averaged bias of WSP10 (SPRAY-A15 minus ERA5) is 0.37 m/s and 0.24 m/s in winter and summer,
236 respectively, mainly due to the overestimations over the Pacific and the Atlantic Ocean (red in
237 Fig.8a&9a). Whereas in SPRAY-GQ, the domain-averaged bias (SPRAY-GQ minus ERA5) is 0.26 m/s
238 and 0.03 m/s in winter and summer respectively. The domain-averaged RMSEs of WSP10s increase with
239 time in the first two weeks and then gradually level off (Fig. 8c&9c). The differences of WSP10 RMSEs
240 between SPRAY-GQ (black) and SPRAY-A15 (red) are very small in the first two weeks. Afterwards
241 the time series of RMSE in SPRAY-GQ is lower than that in SPRAY-A15 significantly at 99%
242 confidence level in both boreal winter (Fig. 8c) and boreal summer (Fig. 9c).

243 The simulated SWHs changes are closely related to the changes of WSP10 (Shi et al. 2022). Therefore,
244 the differences of SWHs (Fig.10&11) are consistent with those of WSP10s (Fig.8&9), with
245 overestimated (underestimated) WSP10s corresponding to overestimated (underestimated) SWHs
246 compared with ERA5. The SWHs in SPRAY-GQ improve compared with those in SPRAY-A15 (Fig.
247 10b&11b). In winter (summer), the SWH RMSE averages for SPRAY-A15 and SPRAY-GQ are 1.31 m
248 (0.98 m) and 1.23 m (0.87 m), and after the first two weeks the time series of RMSE in SPRAY-GQ is
249 lower than that in SPRAY-A15 significantly at 99% confidence level in both winter (Fig. 10c) and
250 summer (Fig. 11c).

251 The direct and indirect effects of sea spray droplets on heat fluxes can influence estimates of WSP10
252 and then SWH. The changes of WSP10s are related to the direct effects ($H_{S,SP}$ and $H_{L,SP}$; Fig. 12b, e,
253 &h; Fig. 13b, e, &h). The spatial correlation coefficients between WSP10 differences (Fig. S3b&S4b)
254 and TH_{SP} differences (Fig. 12h&13h) are 0.51 and 0.69 ($P < 0.01$ in Student's t-test) in winter and
255 summer, respectively. Because the directly increased (decreased) heat fluxes enhance (reduce)
256 turbulence, promote (hinder) the downward transmission of momentum from the upper layer of
257 atmosphere, and then accelerate (decelerate) the surface wind speed (Wallace et al., 1989). While the
258 accelerated (decelerated) WSP10s further result in increased (decreased) interfacial heat transport (H_S ,
259 H_L), as well as increased (decreased) SWHs.



260 5 Conclusions and Discussions

261 Based on a GQ method, we develop a new fast algorithm based on Andreas's (1989, 1990, 1992) full-
262 size microphysical parameterization (A92) for sea spray-mediated heat fluxes. Using global satellite
263 measurements and reanalysis data, SPRAY-GQ parameterization is validated to approximate A92 more
264 accurately than the A15 fast algorithm (Andreas et al., 2015). To evaluate the SPRAY-GQ/A15
265 parameterization, we implement them in the two-way coupled CFSv2.0-WW3 system. A series of 56-
266 day simulations from January 3 to February 28, 2017 and from August 3 to September 28, 2018 are
267 conducted. The results are compared against OISST satellite measurements and ERA5 reanalysis. The
268 comparison shows that the sea spray-mediated heat flux in SPRAY-GQ can reasonably modulate total
269 heat flux, significantly improve the SST biases in the Southern Ocean (mid-high latitudes of the NH) for
270 the austral (boreal) summer, as well as WSP10 and SWH at mid-low latitudes of the NH for both boreal
271 winter and summer. Overall, our fast algorithm based on GQ is applicable to sea spray-mediated heat
272 flux parameterization in coupled models.

273 In addition to the variables aforementioned, the changes of simulated cloud fraction were also
274 compared. However, the effects of sea spray-mediated heat flux on cloud fraction are non-significant for
275 the 2-month simulation, so the results are not shown. Besides, for simulated WSP10 and SWH, the
276 SPRAY-GQ parameterization used in the study mainly improves the biases at mid-low latitudes of the
277 NH, while the significant overestimations in the SH are only slightly improved (Fig. S3-S6 in
278 supplementary). As Andreas (2004) indicated, sea spray droplets also influence the surface momentum
279 flux by injecting more momentum into the ocean from the atmosphere, which might further decrease the
280 surface wind speed. We will consider this process in the future study.

281 Sea spray-mediated heat fluxes are sensitive to the sea spray generation function dF/dr_0 . Based on
282 a number of laboratory and field observations, varieties of dF/dr_0 were derived (e.g., Koga, 1981;
283 Monahan et al., 1982; Troitskaya et al., 2018; Andreas, 1992, 1998, 2002; Fairall et al., 1994; Veron,
284 2015), whereas their differences can reach six orders of magnitude (Andreas, 1998). There is currently
285 no consensus on the most suitable choice. In this study, we use dF/dr_0 of Fairall et al. (1994),
286 recommended by Andreas (2002). It is also consistent with recent observations of Xu et al. (2021b).
287 Since the new scheme based on GQ is independent of sea spray generation function, the new scheme can



288 also be applied to sea spray-mediated heat fluxes estimation with different dF/dr_0 .

289 **Appendix A**

290 **Microphysical Parameterization of A92**

291 Based on the cloud microphysical parameterization of Pruppacher and Klett (1978), Andreas (1989,
 292 1990, 1992) proposed a parameterization of sea spray-related heat fluxes for droplets with different radius,
 293 from formation at sea surface to equilibrium with environment, that is,

$$Q_S = \rho_w C_{ps} (T_w - T_{eq}) \left[1 - \exp\left(-\frac{\tau_f}{\tau_T}\right) \right] \left(\frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), \quad (A1)$$

$$Q_L = \begin{cases} \rho_w L_v \left\{ 1 - \left[\frac{r(\tau_f)}{r_0} \right]^3 \right\} \left(\frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), & \tau_f \leq \tau_r, \\ \rho_w L_v \left\{ 1 - \left(\frac{r_{eq}}{r_0} \right)^3 \right\} \left(\frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), & \tau_f > \tau_r. \end{cases} \quad (A2)$$

294 Here Q_S , Q_L are sensible heat flux and latent heat flux resulted by sea spray droplets with initial radius
 295 r_0 , ρ_w is the sea water density, C_{ps} is the specific heat, L_v is the latent heat of vaporization of water,
 296 T_w is the water temperature, T_{eq} is the temperature of droplet when it reaches thermal equilibrium with
 297 ambient condition, r_{eq} is the radius of droplet when it reaches moisture equilibrium with ambient
 298 condition, τ_f is the residence time for droplets in the atmospheric, $r(\tau_f)$ is the corresponding radius,
 299 τ_T is the characteristic e-folding time of droplet temperature, and τ_r is the characteristic e-folding time
 300 of droplet radius. The detailed calculation of these microphysical quantities can be found in Andreas
 301 (1989, 1990, 1992). And dF/dr_0 is the sea spray generation function, which represents the number
 302 produced of droplets with initial radius r_0 (Andreas, 1992). For this term, the function of Fairall et al.
 303 (1994) was recommended by Andreas (2002). According to the review in Andreas (2002), the dF/dr_0
 304 of Fairall et al. (1994) is related on that of Andreas (1992) as

$$\frac{dF}{dr_0} = 38 \times 3.84 \times 10^{-6} U_{10}^{3.41} r_0^{-0.024} \frac{dF_{A92}}{dr_{80}} \Big|_{U_{10}=11 \text{ m/s}}, \quad (A3)$$

$$\frac{dF_{A92}}{dr_{80}} \Big|_{U_{10}=11 \text{ m/s}} = \begin{cases} e^{(4.405-2.646(\log r_{80})-3.156(\log r_{80})^2+8.902(\log r_{80})^3-4.482(\log r_{80})^4)}, & r_{80} \leq 15 \mu\text{m}; \\ 1.02 \times 10^4 r_{80}^{-1}, & 15 \leq r_{80} \leq 37.5 \mu\text{m}; \\ 6.95 \times 10^6 r_{80}^{-2.8}, & 37.5 \leq r_{80} \leq 100 \mu\text{m}; \\ 1.75 \times 10^{17} r_{80}^{-8}, & r_{80} \geq 100 \mu\text{m} \end{cases} \quad (A4)$$

305 Here U_{10} is the 10-m wind, $r_{80} = 0.518 r_0^{0.976}$.



306 The total sea spray fluxes are obtained by integrating Q_S and Q_L corresponding to all r_0 . Based on
 307 Andreas (1990), the lower and upper limits of r_0 is $2\mu\text{m}$ and $500\mu\text{m}$, that is,

$$\overline{Q_S} = \int_2^{500} Q_S(r_0) dr, \quad (\text{A5})$$

$$\overline{Q_L} = \int_2^{500} Q_L(r_0) dr. \quad (\text{A6})$$

308 While $\overline{Q_S}$ and $\overline{Q_L}$ are nominal sea spray fluxes but not the actual $H_{S,SP}$ and $H_{L,SP}$ (Andreas and
 309 Decosmo, 1999, 2002), because there are interactions between these two terms and the microphysical
 310 functions also lead to uncertainties (Fairall et al., 1994). Therefore, $\overline{Q_S}$ and $\overline{Q_L}$ are tuned by non-
 311 negative constants α , β and γ (Andreas and Decosmo, 2002; Andreas et al., 2008; Andreas et al., 2015;
 312 Andreas, 2003) as

$$H_{S,SP} = \beta \overline{Q_S} - (\alpha - \gamma) \overline{Q_L}, \quad (\text{A7})$$

$$H_{L,SP} = \alpha \overline{Q_L}. \quad (\text{A8})$$

313 In Eqn. (A8), the α term indicates the sea spray-mediated latent heat flux from the top of DEL to
 314 atmosphere. Because the evaporation of droplets absorbs heat, which is provided by sea spray-mediated
 315 sensible heat (Fairall et al., 1994), the negative α term appears in Eqn. (A7). Whereas the evaporation
 316 also cools DEL and thus increases the air-sea temperature difference, therefore it contributes to a positive
 317 γ term in Eqn. (A7). Different values of α , β and γ were given in Andreas and Decosmo (2002),
 318 Andreas (2003), Andreas et al. (2008) and Andreas et al. (2015), to minimize the bias between
 319 estimations and observations of turbulent heat fluxes measured by eddy correlation. And Andreas et al.
 320 (2015) validated the most observation data, which are 4000 sets, to derive $\alpha = 2.46$, $\beta = 15.15$, $\gamma =$
 321 1.77 .

322 Appendix B

323 Fast Algorithm of A15

324 Andreas (2003) and Andreas et al. (2008, 2015) developed a fast algorithm to approximate $H_{S,SP}$,
 325 $H_{L,SP}$ by a characteristic radius, that is,

$$H_{S,SP} = \beta \overline{Q_S} - (\alpha - \gamma) \overline{Q_L} \approx \rho_w c_{ps} (T_w - T_{eq,100}) V_s(u_*), \quad (\text{B1})$$

$$H_{L,SP} = \alpha \overline{Q_L} \approx \rho_w L_v \left\{ 1 - \left[\frac{r(\tau_{f,50})}{50\mu\text{m}} \right]^3 \right\} V_L(u_*). \quad (\text{B2})$$



326 Here $T_{eq,100}$ is T_{eq} of droplets with $r_0=100$ μm , $\tau_{f,50}$ is τ_f of droplets with $r_0=50$ μm , V_s and
327 V_L are functions of the bulk friction velocity u_* . As indicated by Andreas et al. (2008, 2015), the
328 characteristic radiuses of 100 μm and 50 μm for sensible and latent heat fluxes are chosen,
329 respectively, because Q_s and Q_L show a large peak in the vicinity of these values (Fig. 1). V_s and V_L
330 are calculated in Andreas et al. (2015) as

$$V_s = \begin{cases} 3.92 \times 10^{-8}, & 0 \leq u_* \leq 0.1480 \text{ m/s} \\ 5.02 \times 10^{-6} u_*^{2.54}, & u_* \geq 0.1480 \text{ m/s} \end{cases} \quad (\text{B3})$$

$$V_L = \begin{cases} 1.76 \times 10^{-9}, & 0 \leq u_* \leq 0.1358 \text{ m/s} \\ 2.08 \times 10^{-7} u_*^{2.39}, & u_* \geq 0.1358 \text{ m/s} \end{cases} \quad (\text{B4})$$

331 Appendix C

332 Gaussian Quadrature (GQ)

333 GQ is a method to approximate the definite integral of a function $f(x)$ via the function values at a
334 small number of specified nodes (Gauss, 1815; Jacobi, 1826). In this study we use the form of n-node
335 Gauss–Legendre quadrature on $[-1, 1]$ as

$$\int_{-1}^1 f(x) dx \approx \sum_{i=1}^n \omega_i f(x_i). \quad (\text{C1})$$

336 Here x_i is the specified node, and ω_i is the corresponding weight. For $n=3$, $x_1=-0.775$, $x_2=0$,
337 $x_3=0.775$, $\omega_1=\omega_3=0.556$, $\omega_2=0.889$.

338 While for a function $g(\xi)$ on $[a, b]$, Eqn. (C1) can be transformed to

$$\begin{aligned} \int_a^b g(\xi) d\xi &= \int_{-1}^1 g\left(\frac{b-a}{2}x + \frac{a+b}{2}\right) \frac{d\xi}{dx} dx \\ &\approx \frac{b-a}{2} \sum_{i=1}^n \omega_i g\left(\frac{b-a}{2}x_i + \frac{a+b}{2}\right). \end{aligned} \quad (\text{C2})$$

339 Code and data availability

340 The code of sea spray can be found under <https://doi.org/10.5281/zenodo.7100345> (Shi and Xu, 2022).
341 The code for CFSv2.0-WW3 system can be found under <https://doi.org/10.5281/zenodo.5811002> (Shi et
342 al., 2021) including the coupling, preprocessing, run control and postprocessing scripts. The initial fields
343 for CFSv2.0 are generated by the real time operational Climate Data Assimilation System, downloaded
344 from the CFSv2.0 official website (<http://nomads.ncep.noaa.gov/pub/data/nccf/com/cfs/prod>). The daily



345 average satellite Optimum Interpolation SST (OISST) data are obtained from NOAA
346 (<https://www.ncdc.noaa.gov/oisst>). The fifth generation European Centre for Medium-Range Weather
347 Forecasts (ECMWF) Reanalysis (ERA5) are available at the Copernicus Climate Change Service (C3S)
348 Climate Data Store (<https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels>).
349 The daily Objectively Analyzed air-sea Fluxes (OAFlex) products are available at
350 <https://oaflex.whoi.edu/heat-flux>. The global monthly mean salinity observation of European Space
351 Agency (ESA) are from <https://climate.esa.int>.

352 **Author contribution**

353 FX and RS designed the experiments and RS carried them out. RS developed the code of coupling
354 parametrizations and produced the figures. RS prepared the manuscript with contributions from all co-
355 authors. FX contributed to review and editing.

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360 **Competing Interests**

361 The contact author has declared that neither they nor their co-authors have any competing interests.

362 **References**

- 363 Alessandro, J. D., Diao, M., Wu, C., Liu, X., Jensen, J. B., and Stephens, B. B.: Cloud phase and relative
364 humidity distributions over the Southern Ocean in austral summer based on in situ observations and
365 CAM5 simulations, *Journal of Climate*, 32, 2781-2805, 2019.
- 366 Andreas, E. L.: Thermal and size evolution of sea spray droplets, 1989.
- 367 Andreas, E. L.: Time constants for the evolution of sea spray droplets, *Tellus B*, 42, 481-497, 1990.
- 368 Andreas, E. L.: Sea spray and the turbulent air - sea heat fluxes, *Journal of Geophysical Research*:



- 369 Oceans, 97, 11429-11441, 1992.
- 370 Andreas, E. L., Edson, J. B., Monahan, E. C., Rouault, M. P., and Smith, S. D.: The spray contribution
371 to net evaporation from the sea: A review of recent progress, *Boundary-Layer Meteorology*, 72, 3-52,
372 1995.
- 373 Andreas, E. L.: A new sea spray generation function for wind speeds up to 32 ms⁻¹, *Journal of Physical*
374 *Oceanography*, 28, 2175-2184, 1998.
- 375 Andreas, E. L., and Decosmo, J.: Sea spray production and influence on air-sea heat and moisture fluxes
376 over the open ocean, in: *Air-sea exchange: physics, chemistry and dynamics*, Springer, 327-362, 1999.
- 377 Andreas, E. L., and Emanuel, K. A.: Effects of sea spray on tropical cyclone intensity, *Journal of the*
378 *atmospheric sciences*, 58, 3741-3751, 2001.
- 379 Andreas, E. L.: A review of the sea spray generation function for the open ocean, *Advances in Fluid*
380 *Mechanics*, 33, 1-46, 2002.
- 381 Andreas, E. L., and Decosmo, J.: The signature of sea spray in the HEXOS turbulent heat flux data,
382 *Boundary-layer meteorology*, 103, 303-333, 2002.
- 383 Andreas, E. L.: 3.4 AN ALGORITHM TO PREDICT THE TURBULENT AIR-SEA FLUXES IN
384 HIGH-WIND, SPRAY CONDITIONS, 2003.
- 385 Andreas, E. L.: Spray stress revisited, *Journal of physical oceanography*, 34, 1429-1440, 2004.
- 386 Andreas, E. L., Persson, P. O. G., and Hare, J. E.: A bulk turbulent air-sea flux algorithm for high-wind,
387 spray conditions, *Journal of Physical Oceanography*, 38, 1581-1596, 2008.
- 388 Andreas, E. L.: Spray-mediated enthalpy flux to the atmosphere and salt flux to the ocean in high winds,
389 *Journal of physical oceanography*, 40, 608-619, 2010.
- 390 Andreas, E. L., Mahrt, L., and Vickers, D.: An improved bulk air - sea surface flux algorithm, including
391 spray - mediated transfer, *Quarterly Journal of the Royal Meteorological Society*, 141, 642-654, 2015.
- 392 Bao, Y., Song, Z., and Qiao, F.: FIO - ESM version 2.0: Model description and evaluation, *Journal of*
393 *Geophysical Research: Oceans*, 125, e2019JC016036, 2020.
- 394 Bodas-Salcedo, A., Williams, K., Field, P., and Lock, A.: The surface downwelling solar radiation
395 surplus over the Southern Ocean in the Met Office model: The role of midlatitude cyclone clouds, *Journal*
396 *of Climate*, 25, 7467-7486, 2012.



- 397 Borisenkov, E.: Some mechanisms of atmosphere-ocean interaction under stormy weather conditions,
398 *Probl Arct Antarct*, 43, 73-83, 1974.
- 399 Bortkovskii, R.: On the mechanism of interaction between the ocean and the atmosphere during a storm,
400 *Fluid Mech Sov Res*, 2, 87-94, 1973.
- 401 Burk, S. D.: The generation, turbulent transfer and deposition of the sea-salt aerosol, *Journal of*
402 *Atmospheric Sciences*, 41, 3040-3051, 1984.
- 403 Ceppi, P., Hwang, Y. T., Frierson, D. M., and Hartmann, D. L.: Southern Hemisphere jet latitude biases
404 in CMIP5 models linked to shortwave cloud forcing, *Geophysical Research Letters*, 39, 2012.
- 405 Edson, J. B., and Andreas, E. L.: Modeling the role of sea spray on air-sea heat and moisture exchange,
406 *Final Rep*, 6, 18, 1997.
- 407 Emanuel, K. A.: Sensitivity of tropical cyclones to surface exchange coefficients and a revised steady-
408 state model incorporating eye dynamics, *Journal of Atmospheric Sciences*, 52, 3969-3976, 1995.
- 409 Fairall, C., Davidson, K., and Schacher, G.: An analysis of the surface production of sea - salt aerosols,
410 *Tellus B*, 35, 31-39, 1983.
- 411 Fairall, C., and Larsen, S. E.: Dry deposition, surface production and dynamics of aerosols in the marine
412 boundary layer, *Atmospheric Environment (1967)*, 18, 69-77, 1984.
- 413 Fairall, C., Kepert, J., and Holland, G.: The effect of sea spray on surface energy transports over the
414 ocean, *Global Atmos. Ocean Syst*, 2, 121-142, 1994.
- 415 Fairall, C., Bradley, E. F., Rogers, D. P., Edson, J. B., and Young, G. S.: Bulk parameterization of air -
416 sea fluxes for tropical ocean - global atmosphere coupled - ocean atmosphere response experiment,
417 *Journal of Geophysical Research: Oceans*, 101, 3747-3764, 1996.
- 418 Fox-Kemper, B., Johnson, L., and Qiao, F.: Ocean near-surface layers, in: *Ocean Mixing*, Elsevier, 65-
419 94, 2022.
- 420 Garg, N., Ng, E. Y. K., and Narasimalu, S.: The effects of sea spray and atmosphere-wave coupling on
421 air-sea exchange during a tropical cyclone, *Atmospheric Chemistry and Physics*, 18, 6001-6021, 2018.
- 422 Gauss, C. F.: *Methodvs nova integralivm valores per approximationem inveniendi*, apvd Henricvm
423 Dieterich, 1815.
- 424 Griffies, S. M., Harrison, M. J., Pacanowski, R. C., and Rosati, A.: A technical guide to MOM4, GFDL



- 425 Ocean Group Tech. Rep, 5, 342, 2004.
- 426 WAVEWATCH III Development Group: User manual and system documentation of WAVEWATCH
427 III version 5.16, NOAA/NWS/NCEP/MMAB Technical Note 329, 326, 2016.
- 428 Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz - Sabater, J., Nicolas, J., Peubey,
429 C., Radu, R., and Schepers, D.: The ERA5 global reanalysis, Quarterly Journal of the Royal
430 Meteorological Society, 146, 1999-2049, 2020.
- 431 Jacobi, C. G. J.: Ueber Gauss neue Methode, die Werthe der Integrale näherungsweise zu finden, 1826.
- 432 Koga, M.: Direct production of droplets from breaking wind - waves—its observation by a multi -
433 colored overlapping exposure photographing technique, Tellus, 33, 552-563, 1981.
- 434 Lhuissier, H., and Villermaux, E.: Bursting bubble aerosols, Journal of Fluid Mechanics, 696, 5-44, 2012.
- 435 Li, J., Waliser, D., Stephens, G., Lee, S., L'Ecuyer, T., Kato, S., Loeb, N., and Ma, H. Y.: Characterizing
436 and understanding radiation budget biases in CMIP3/CMIP5 GCMs, contemporary GCM, and reanalysis,
437 Journal of Geophysical Research: Atmospheres, 118, 8166-8184, 2013.
- 438 Li, J. N., and Barker, H. W.: Computation of domain - average radiative flux profiles using Gaussian
439 quadrature, Quarterly Journal of the Royal Meteorological Society, 144, 720-734, 2018.
- 440 Ling, S., and Kao, T.: Parameterization of the moisture and heat transfer process over the ocean under
441 whitecap sea states, Journal of Physical Oceanography, 6, 306-315, 1976.
- 442 Liu, B., Guan, C., Xie, L. a., and Zhao, D.: An investigation of the effects of wave state and sea spray on
443 an idealized typhoon using an air-sea coupled modeling system, Advances in Atmospheric Sciences, 29,
444 391-406, 2012.
- 445 Liu, L., Zhang, C., Li, R., and Wang, B.: C-Coupler2: a flexible and user-friendly community coupler
446 for model coupling and nesting, Geoscientific Model Development Discussions, 11, 1-63,
447 <http://dx.doi.org/10.5194/gmd-11-3557-2018>, 2018.
- 448 McClarren, R.: Gauss Quadrature and Multi-dimensional Integrals, Computational Nuclear Engineering
449 and Radiological Science Using Python; Academic Press: Cambridge, MA, USA, 287-299, 2018.
- 450 Melville, W. K.: The role of surface-wave breaking in air-sea interaction, 1996.
- 451 Monahan, E., Davidson, K., and Spiel, D.: Whitecap aerosol productivity deduced from simulation tank
452 measurements, Journal of Geophysical Research: Oceans, 87, 8898-8904, 1982.



- 453 Monahan, E., and Van Patten, M. A.: The climate and health implications of bubble-mediated sea-air
454 exchange, 1988.
- 455 Praveen Kumar, B., Vialard, J., Lengaigne, M., Murty, V., and McPhaden, M. J.: TropFlux: Air-sea
456 fluxes for the global tropical oceans—Description and evaluation, *Climate dynamics*, 38, 1521-1543,
457 2012.
- 458 Pruppacher, H. R., and Klett, J. D.: Microstructure of atmospheric clouds and precipitation, in:
459 *Microphysics of Clouds and Precipitation*, Springer, 9-55, 1978.
- 460 Resch, F., and Afeti, G.: Film drop distributions from bubbles bursting in seawater, *Journal of*
461 *Geophysical Research: Oceans*, 96, 10681-10688, 1991.
- 462 Reynolds, R. W., Smith, T. M., Liu, C., Chelton, D. B., Casey, K. S., and Schlax, M. G.: Daily high-
463 resolution-blended analyses for sea surface temperature, *Journal of climate*, 20, 5473-5496, 2007.
- 464 Saha, S., Moorthi, S., Wu, X., Wang, J., Nadiga, S., Tripp, P., Behringer, D., Hou, Y., Chuang, H., and
465 Iredell, M. D.: The NCEP Climate Forecast System Version 2, *Journal of Climate*, 27, 2185-2208,
466 <http://dx.doi.org/10.1175/JCLI-D-12-00823.1>, 2014.
- 467 Seethala, C., Zuidema, P., Edson, J., Brunke, M., Chen, G., Li, X. Y., Painemal, D., Robinson, C.,
468 Shingler, T., and Shook, M.: On assessing ERA5 and MERRA2 representations of cold - air outbreaks
469 across the Gulf Stream, *Geophysical research letters*, 48, e2021GL094364, 2021.
- 470 Shi, R., Xu, F., Liu, L., Fan, Z., Yu, H., Li, H., Li, X., and Zhang, Y.: The effects of ocean surface waves
471 on global intraseasonal prediction: case studies with a coupled CFSv2. 0–WW3 system, *Geoscientific*
472 *Model Development*, 15, 2345-2363, 2022.
- 473 Smith, R. K.: On the theory of CISK, *Quarterly Journal of the Royal Meteorological Society*, 123, 407-
474 418, 1997.
- 475 Song, Y., Qiao, F., Liu, J., Shu, Q., Bao, Y., Wei, M., and Song, Z.: Effects of sea spray on large-scale
476 climatic features over the Southern Ocean, *Journal of Climate*, 1-51, 2022.
- 477 Spiel, D. E.: More on the births of jet drops from bubbles bursting on seawater surfaces, *Journal of*
478 *Geophysical Research: Oceans*, 102, 5815-5821, 1997.
- 479 Thorpe, S.: Bubble clouds and the dynamics of the upper ocean, *Quarterly Journal of the Royal*
480 *Meteorological Society*, 118, 1-22, 1992.



481 Troitskaya, Y., Kandaurov, A., Ermakova, O., Kozlov, D., Sergeev, D., and Zilitinkevich, S.: The “bag
482 breakup” spume droplet generation mechanism at high winds. Part I: Spray generation function, *Journal*
483 *of physical oceanography*, 48, 2167-2188, 2018.

484 Van Eijk, A., Kusmierczyk - Michulec, J., Francius, M., Tedeschi, G., Piazzola, J., Merritt, D., and
485 Fontana, J.: Sea - spray aerosol particles generated in the surf zone, *Journal of Geophysical Research:*
486 *Atmospheres*, 116, 2011.

487 Veron, F.: Ocean spray, *Annu. Rev. Fluid Mech.*, 47, 507-538, 2015.

488 Wallace, J. M., Mitchell, T., and Deser, C.: The influence of sea-surface temperature on surface wind in
489 the eastern equatorial Pacific: Seasonal and interannual variability, *Journal of Climate*, 2, 1492-1499,
490 1989.

491 Wang, C., Zhang, L., Lee, S.-K., Wu, L., and Mechoso, C. R.: A global perspective on CMIP5 climate
492 model biases, *Nature Climate Change*, 4, 201-205, 2014.

493 Wu, J.: Evaporation due to spray, *Journal of Geophysical Research*, 79, 4107-4109, 1974.

494 Wu, L., Cheng, X., Zeng, Q., Jin, J., Huang, J., and Feng, Y.: On the upward flux of sea - spray spume
495 droplets in high - wind conditions, *Journal of Geophysical Research: Atmospheres*, 122, 5976-5987,
496 2017.

497 Xu, X., Voermans, J., Liu, Q., Moon, I.-J., Guan, C., and Babanin, A.: Impacts of the Wave-Dependent
498 Sea Spray Parameterizations on Air - Sea-Wave Coupled Modeling under an Idealized Tropical Cyclone,
499 *Journal of Marine Science and Engineering*, 9, 1390, 2021a.

500 Xu, X., Voermans, J., Ma, H., Guan, C., and Babanin, A. V.: A Wind-Wave-Dependent Sea Spray
501 Volume Flux Model Based on Field Experiments, *Journal of Marine Science and Engineering*, 9, 1168,
502 2021b.

503 Yu, L., Jin, X., and Weller, R. A.: 2008: Multidecade global flux datasets from the Objectively Analyzed
504 Air-Sea Fluxes (OAFlux) Project: Latent and sensible heat fluxes, ocean evaporation, and related surface
505 meteorological variables. Woods Hole Oceanographic Institution OAFlux Project Tec. Rep, 2008.

506 Zhao, B., Qiao, F., Cavaleri, L., Wang, G., Bertotti, L., and Liu, L.: Sensitivity of typhoon modeling to
507 surface waves and rainfall, *Journal of Geophysical Research: Oceans*, 122, 1702-1723, 2017.

508

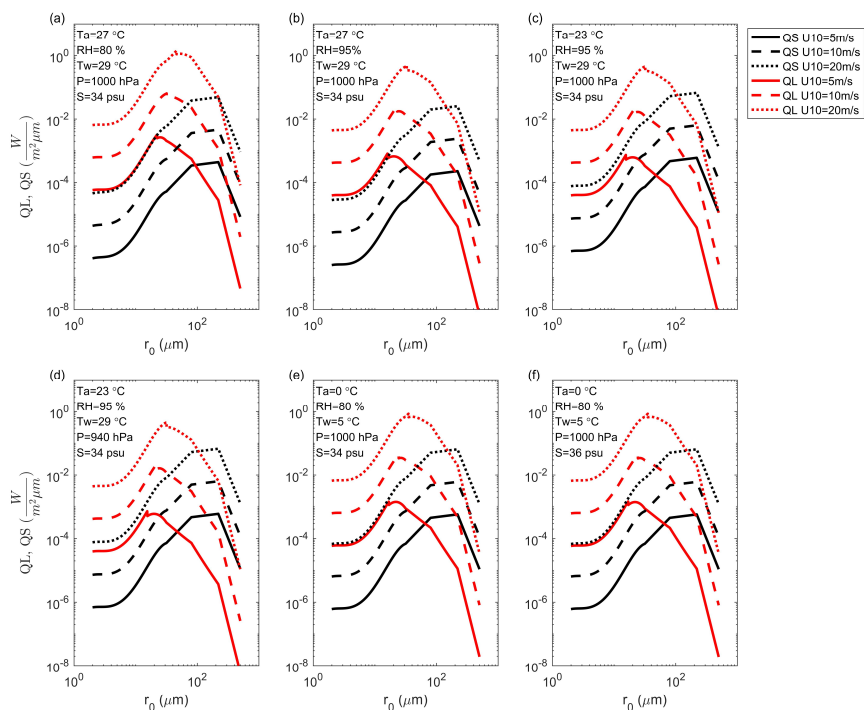


Figure 1. The radius-specific sea spray-mediated sensible (Q_S ; black) and latent (Q_L ; red) heat fluxes as functions of initial radius r_0 : U_{10} , T_a , RH , T_w , P and S are 10-m wind speed, 2-m air temperature, 2-m relative humidity, sea surface temperature, surface air pressure and surface salinity, respectively.

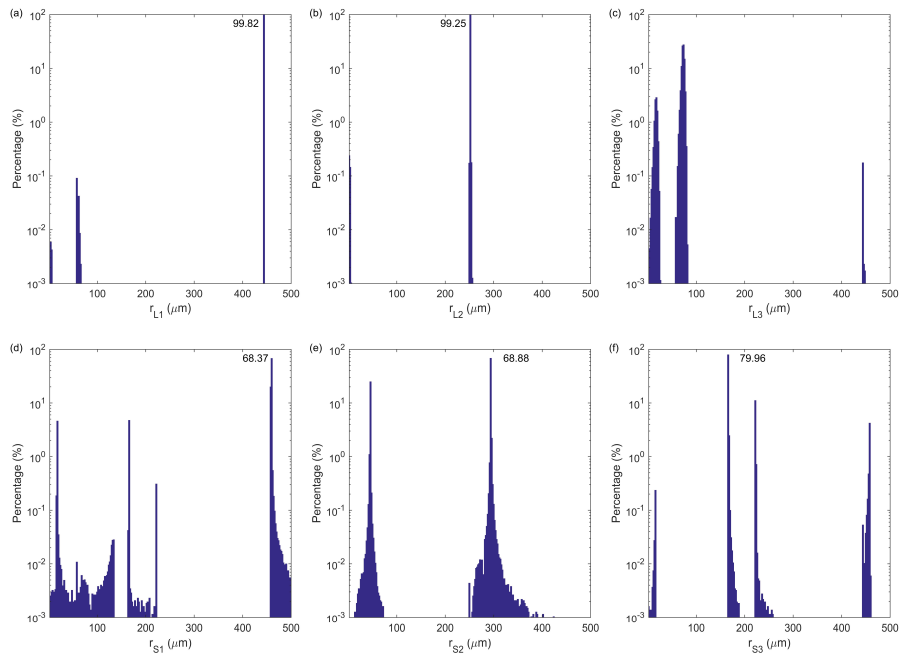


Figure 2. The distribution of occurrence frequency in percentage for GQ radius nodes: (a) the first node of latent heat flux; (b) the second node of latent heat flux; (c) the third node of latent heat flux; (d) the first node of sensible heat flux; (e) the second node of sensible heat flux; (f) the third node of sensible heat flux. The peak frequencies are marked.

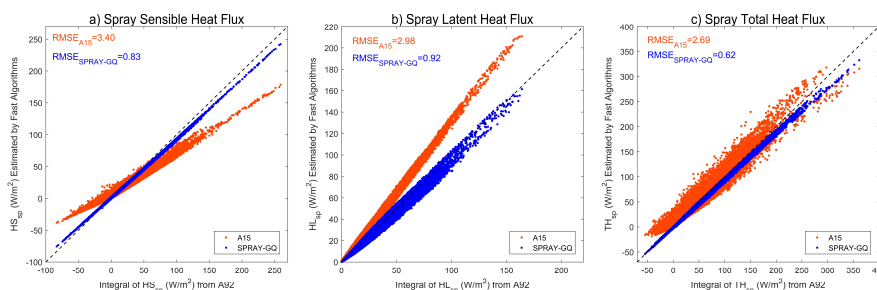


Figure 3. Scatter plots of $H_{S,SP}$ (a), $H_{L,SP}$ (b) and total heat flux $TH_{SP} = H_{S,SP} + H_{L,SP}$ (c) estimated by fast algorithms (y-axis) vs those estimated by spectral integral in microphysical parameterization (x-axis): The dotted black line is $y=x$. The corresponding RMSEs are marked in the upper left corner.

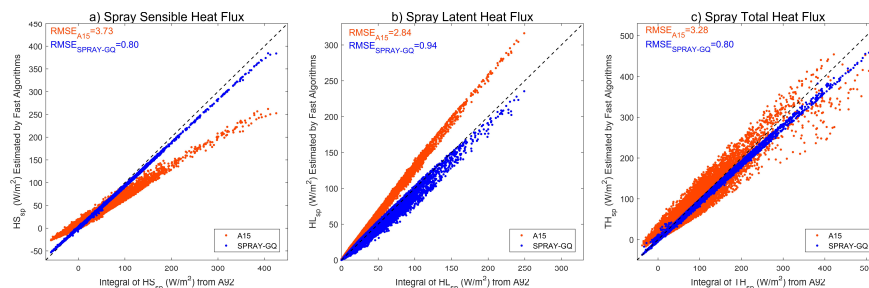


Figure 4. The same as Figure 3, but WSP10, 2-m air temperature and 2-m specific humidity of OAF flux are used.

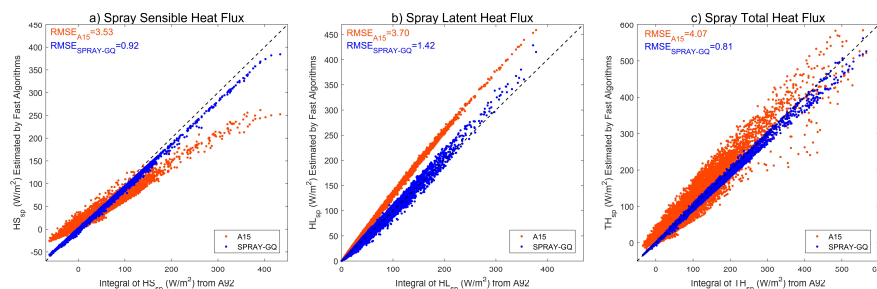


Figure 5. The same as Figure 4, but SWH are derived by WSP10 instead of ERA5 SWH.

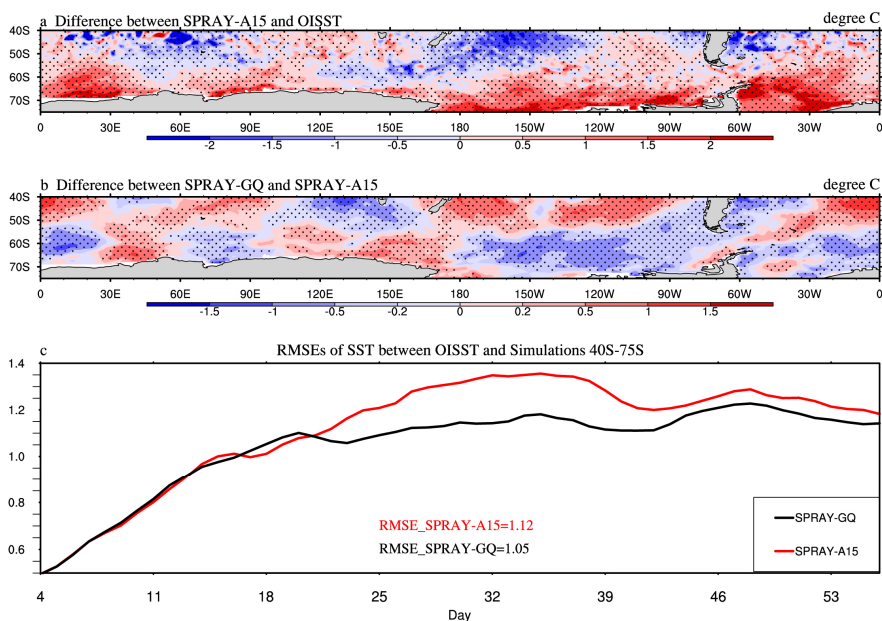


Figure 6. The 53-day average SST ($^{\circ}\text{C}$) differences between SPRAY-A15 and OISST (a; SPRAY-A15 minus OISST), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE (c; 0-360 $^{\circ}\text{E}$, 40-75 $^{\circ}\text{S}$) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.

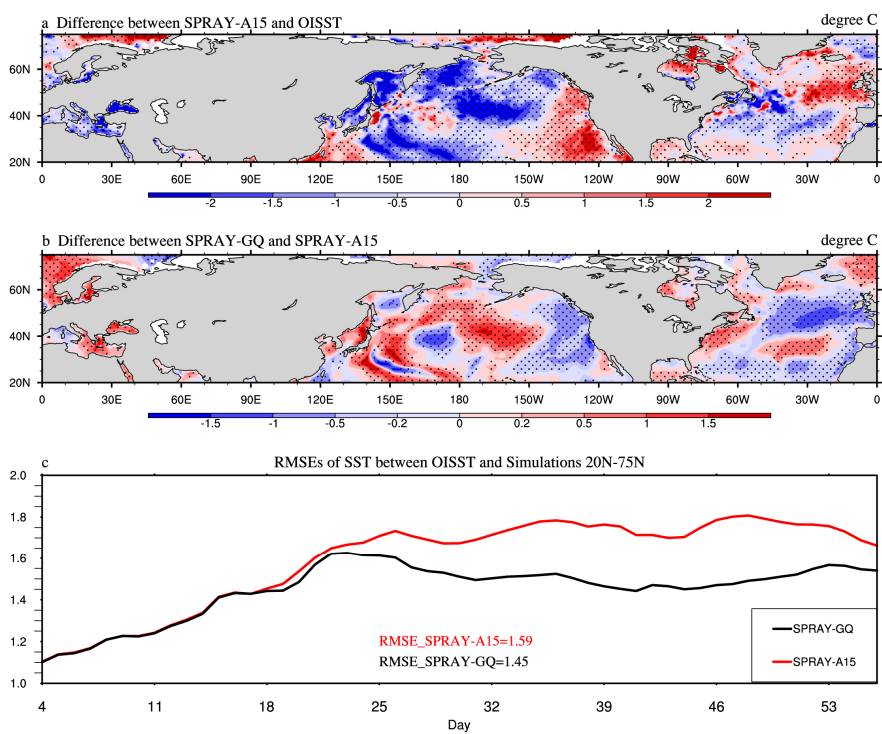


Figure 7. The same as Figure 6, but for Aug-Sep, 2018 in 0-360°E, 20-75°N.

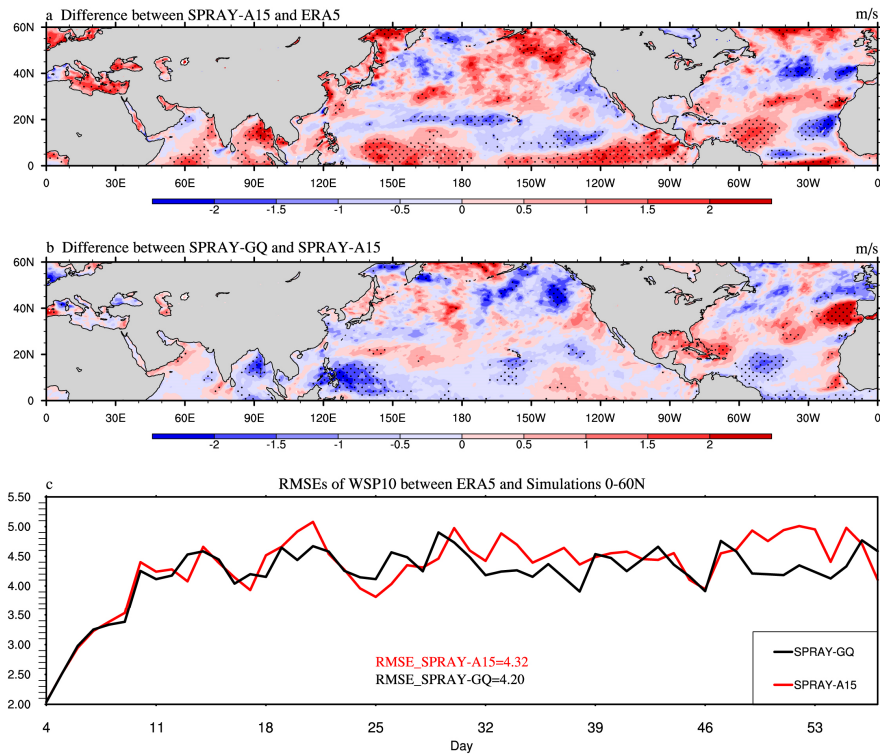


Figure 8. The 53-day average WSP10 (m/s) differences between SPRAY-A15 and ERA5 (a; SPRAY-A15 minus ERA5), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE (c; 0-360°E, 0-60°N) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.

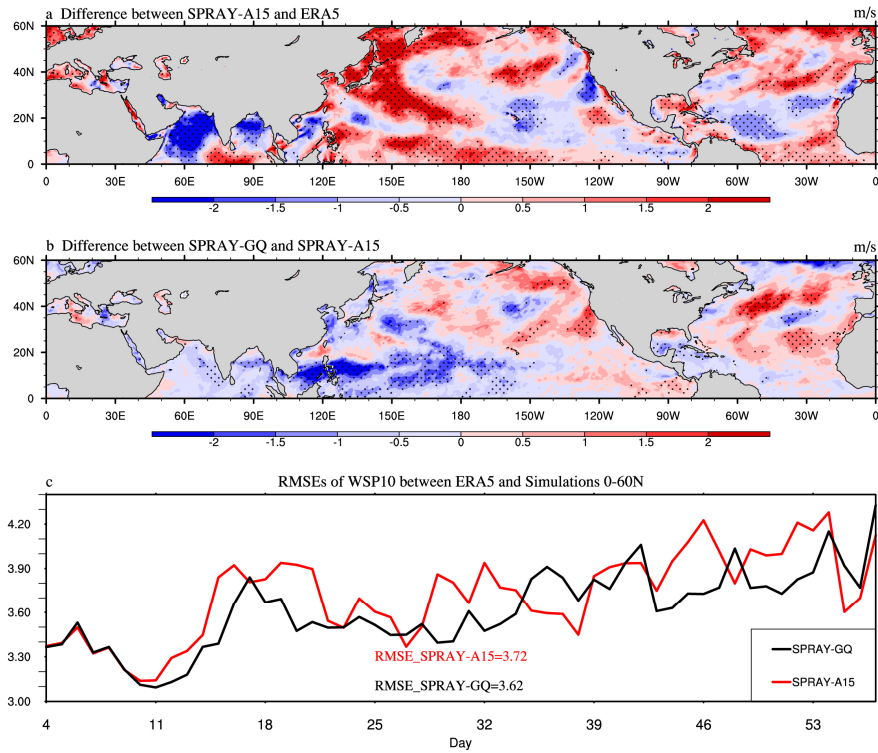


Figure 9. The same as Figure 8, but for Aug-Sep, 2018.

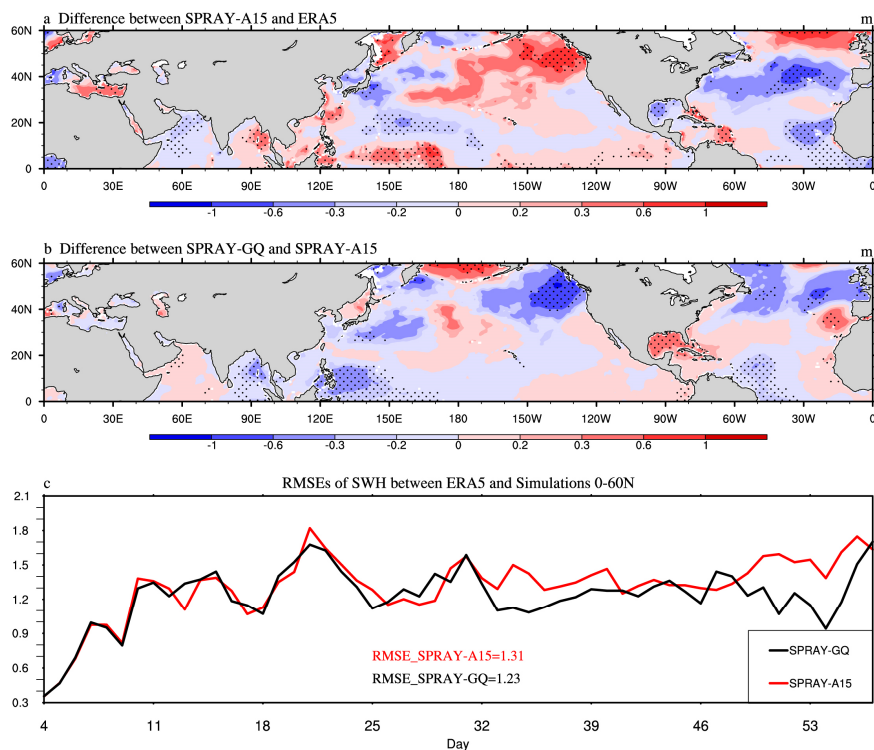


Figure 10. The 53-day average SWH (m) differences between SPRAY-A15 and ERA5 (a; SPRAY-A15 minus ERA5), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE (c; 0-360°E, 0-60°N) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.

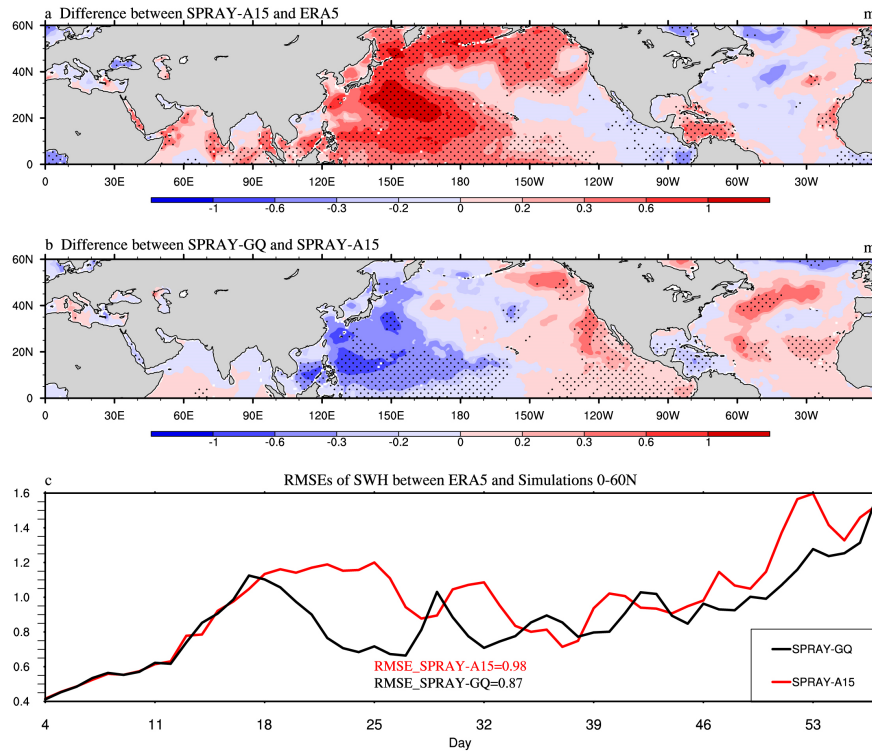


Figure 11. The same as Figure 10, but for Aug-Sep, 2018.

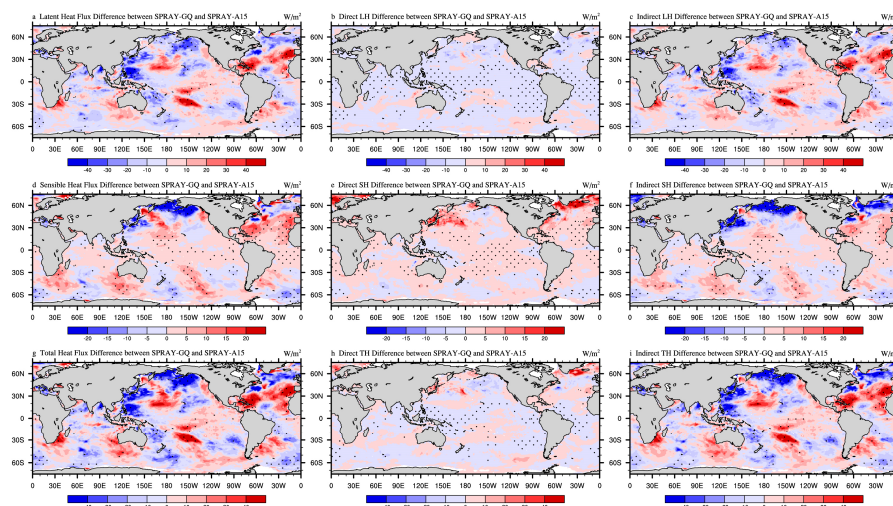


Figure 12. The 53-day average differences of latent heat flux (a-c), sensible heat flux (d-f) and total heat flux (g-i) between SPRAY-A15 and SPRAY-GQ (SPRAY-GQ minus SPRAY-A15) in Jan-Feb, 2017. The direct differences indicate sea spray-mediated heat flux differences (b, e, h), and the indirect differences indicate interfacial (bulk) heat flux differences resulted by sea spray (c, f, i). The dotted areas are statistically significant at 95% confidence level. A positive value of flux indicates an upward direction.

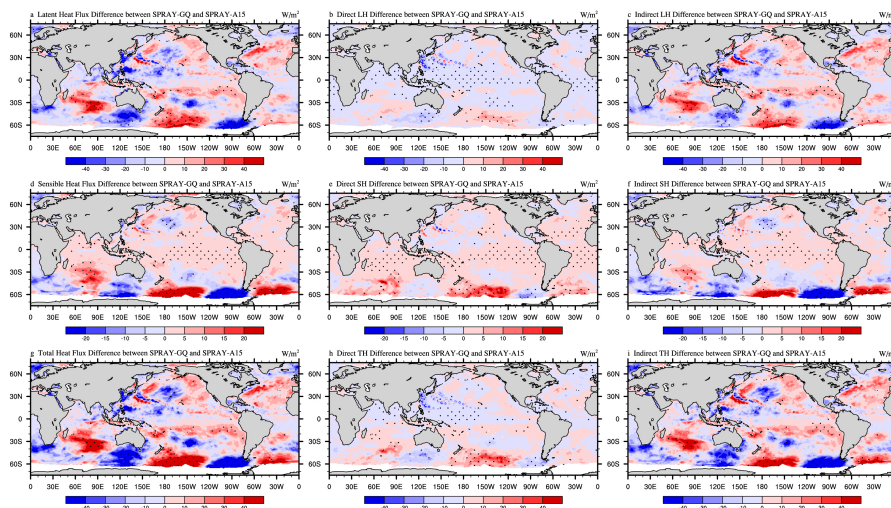


Figure 13. The same as Figure 12, but for Aug-Sep, 2018.