

1 **Accelerated Estimation of Sea Spray-Mediated Heat Flux**  
2 **Using Gaussian Quadrature: Case Studies with a Coupled**  
3 **CFSv2.0-WW3 System**

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8

9 **Abstract.** Sea spray-mediated heat flux plays an important role in air-sea heat transfer. Heat flux  
10 integrated over droplet size spectrum can well simulate total heat flux induced by sea spray droplets.  
11 Previously, a fast algorithm of spray-flux assuming single-radius droplets (A15) was widely used since  
12 the full-size spectrum integral is computationally expensive. Based on the Gaussian Quadrature (GQ)  
13 method, a new fast algorithm (SPRAY-GQ) of sea spray-mediated heat flux is derived. The performance  
14 of SPRAY-GQ is evaluated by comparing heat fluxes with those estimated from the widely-used A15.  
15 The new algorithm shows a better agreement with the original spectrum integral. To further evaluate the  
16 numerical errors of A15 and SPRAY-GQ, the two algorithms are implemented into a coupled CFSv2.0-  
17 WW3 system, and a series of 56-day simulations in summer and winter are conducted and compared.  
18 The comparisons with satellite measurements and reanalysis data show that the SPRAY-GQ algorithm  
19 could lead to more reasonable simulation than the A15 algorithm by modifying air-sea heat flux. For  
20 experiments based on SPRAY-GQ, the sea surface temperature at mid-high latitudes of both hemispheres,  
21 particularly in summer, is significantly improved compared with the experiments based on A15. The  
22 simulation of 10-m wind speed and significant wave height at mid-low latitudes of the Northern  
23 Hemisphere after the first two weeks is improved as well. [These improvements are due to the reduced](#)  
24 [numerical errors.](#) The computational time of SPRAY-GQ is about the same as that of A15.  
25 [Therefore/Thereby,](#) the newly-developed SPRAY-GQ algorithm has a potential to be used for calculation  
26 of spray-mediated heat flux in coupled models.

27

## 28 **1 Introduction**

29 Sea spray droplets, ejected from oceans, include film drops, jet drops and spume drops (Veron, 2015).  
30 The first two types of droplets are generated from bubble bursting caused by ocean surface wave breaking,  
31 with radius ranging from 0.5  $\mu\text{m}$  to 50  $\mu\text{m}$  (Resch and Afeti, 1991; Thorpe, 1992; Melville, 1996; Spiel,  
32 1997; Andreas, 1998; Lhuissier and Villermaux, 2012). Spume drops are generated by strong winds ( $>$   
33 7-11 m/s) which directly tear the wave crests, with larger radius ranging from tens to hundreds of  
34 micrometers (Koga, 1981; Andreas et al., 1995; Andreas, 1998). Sea spray droplets play an important  
35 role in weather and climate processes (Fox-Kemper et al., 2022). On one hand, sea spray droplets  
36 contribute to local marine aerosols and subsequently modify the local radiation balance (Fairall et al.,  
37 1983; Burk, 1984; Fairall and Larsen, 1984). On the other hand, sea spray droplets affect the fluxes of  
38 heat, momentum, salt, and freshwater between atmosphere and ocean (Andreas, 1992; Andreas et al.,  
39 2008; Andreas, 2010; Andreas et al., 2015; Ling and Kao, 1976; Fairall et al., 1994; Andreas and  
40 Decosmo, 2002).

41 The sea spray-mediated heat transfer mainly occurs within the droplet evaporation layer (DEL) near  
42 the sea surface (Andreas and Decosmo, 1999, 2002; Fairall et al., 1994). Sea spray droplets with the same  
43 temperature as ocean surface can lead to sensible heat flux in DEL, while water evaporated from these  
44 droplets can further release latent heat to the atmosphere (Andreas, 1992; Borisenkov, 1974; Bortkovskii,  
45 1973; Wu, 1974; Monahan and Van Patten, 1988; Ling and Kao, 1976). Part of the sea spray-mediated  
46 sensible heat is absorbed by droplet evaporation, which further increases the air-sea temperature  
47 difference, and thus increases the sea spray-mediated sensible heat flux (Fairall et al., 1994; Andreas and  
48 Decosmo, 2002). Since strong winds produce more sea spray droplets with larger radius, sea spray-  
49 mediated heat fluxes increase with wind speed (Fairall et al., 1994), and contribute [to](#) more than 10% of  
50 the total surface heat flux after reaching the threshold speed ( $>$  11 m/s for sensible heat flux and  $>$  13 m/s  
51 for latent heat flux)(Andreas et al., 2008). In addition, when a droplet is released into the air, it is  
52 accelerated due to surface winds (Edson and Andreas, 1997; Fairall et al., 1994; Van Eijk et al., 2011;  
53 Wu et al., 2017). If the droplet could fall back into the ocean, additional momentum would be injected  
54 into the ocean from the atmosphere (Andreas, 1992, 2004).

55 The usual bulk parameterizations in numerical models for surface fluxes only include the interfacial

56 (turbulent) fluxes (e.g., Fairall et al., 1996), while neglecting the significant contributions of sea spray  
57 droplets in DEL (Andreas et al., 2008; Fairall et al., 1994; Smith, 1997; Emanuel, 1995). Andreas and  
58 Emanuel (2001) implemented sea spray-mediated heat flux and momentum flux parameterizations into  
59 a simple tropical cyclone model, and found that the sea spray-mediated heat flux can significantly  
60 enhance tropical cyclone intensity. ~~It is well known that strong winds and high waves induced by tropical  
61 cyclones can enhance sea surface roughness and thus surface drag coefficients. Although it is under  
62 debate whether the increased surface drag coefficients directly reduce tropical cyclone intensity (e.g.,  
63 Emanuel, 1995; Smith et al., 2014), the increased momentum flux due to surface drag coefficients does  
64 enhance sea surface cooling and thus suppress tropical cyclone intensification (Liu et al., 2022), which  
65 tend to reduce tropical cyclone intensity (Emanuel, 1995). Furthermore, the accelerated sea spray  
66 droplets by surface winds also lead to more dissipation of tropical cyclone kinetic energy (Andreas, 1992,  
67 2004). These negative effects could be offset by the sea spray-mediated heat flux.~~ The similar  
68 enhancement of tropical cyclone intensity was also noticed in recent regional coupling systems by  
69 including sea spray-mediated heat flux (Xu et al., 2021a; Liu et al., 2012; Garg et al., 2018; Zhao et al.,  
70 2017). In the First Institute of Oceanography Earth System Model, Bao et al. (2020) first incorporated  
71 the sea spray-mediated heat flux in global climate simulation. Following Bao et al. (2020), Song et al.  
72 (2022) found that the sea spray-mediated heat flux can lead to cooling at the air-sea interface and  
73 [westerlies](#) strengthening ~~westerlies~~ in the Southern Ocean, and thus improves estimates of sea surface  
74 temperature (SST).

75 Since the parameterization of sea spray-mediated heat flux derived from observations requires full-  
76 size spectral integral and thus [is](#) computationally expensive for large-scale models (Table 1, details in  
77 Section 4.2; Andreas, 1989, 1990, 1992; Andreas et al., 2015), a simplified algorithm based on a single  
78 radius of sea spray droplets (Andreas et al., 2015; Andreas et al., 2008) is widely used in atmosphere-  
79 ocean coupling systems (Xu et al., 2021a; Liu et al., 2012; Garg et al., 2018; Zhao et al., 2017; Song et  
80 al., 2022; Bao et al., 2020), and apt to produce numerical errors. To reduce these numerical errors induced  
81 by the single radius of sea spray droplets, we develop a new fast algorithm of sea spray-mediated heat  
82 flux based on the Gaussian Quadrature (GQ) method, a fast and accurate way to calculate spectral integral.  
83 The GQ method has been successfully used for the estimation of domain-averaged radiative flux profiles

84 (Li and Barker, 2018). The performance of the GQ-based fast algorithm of the sea spray-mediated heat  
85 flux is evaluated and compared with the simplified algorithm for single radius of Andreas et al. (2015),  
86 referred to as A15 hereafter. The results are first compared with the original parameterization using full-  
87 size spectral integral (A92, hereafter). Then the parameterizations with different algorithms are  
88 implemented in a global coupled atmosphere-ocean-wave system (Shi et al., 2022), and the results are  
89 compared with global satellite measurements and reanalysis data.

90 The rest of the paper is structured as follows: observation and reanalysis data for comparisons are  
91 introduced in Section 2; the derivation of the GQ-based fast algorithm and the global coupling system  
92 are described in Section 3; the performance of the new fast algorithm is evaluated in Section 4. Finally,  
93 a summary and discussion are given in Section 5.

## 94 **2 Data**

95 The fifth generation European Centre for Medium-Range Weather Forecasts (ECMWF) Reanalysis  
96 (ERA5; Hersbach et al., 2020) 10-m wind speed (WSP10), 2-m air temperature (T02), 2-m dewpoint  
97 temperature, surface pressure and significant wave height (SWH) with a spatial resolution of  $0.5^\circ$  are  
98 used. Additionally, WSP10, T02 and 2-m specific humidity (SPH) data from the Objectively Analyzed  
99 air-sea Fluxes (OAFflux) products (Yu et al., 2008) are also applied for comparison, with  $1^\circ \times 1^\circ$  resolution.  
100 The daily average satellite Optimum Interpolation SST (OISST) data are obtained from the National  
101 Oceanic and Atmospheric Administration (NOAA) with a spatial resolution of  $0.25^\circ$  (Reynolds et al.,  
102 2007). The global monthly mean salinity observations from European Space Agency (ESA;  
103 [https://climate.esa.int/sites/default/files/SSS\\_cci-D1.1-URD-v1r4\\_signed-accepted.pdf](https://climate.esa.int/sites/default/files/SSS_cci-D1.1-URD-v1r4_signed-accepted.pdf)) are applied.  
104 Besides, we also use the monthly global ocean RSS Satellite Data Products for WSP10  
105 ([https://data.remss.com/wind/monthly\\_1deg/](https://data.remss.com/wind/monthly_1deg/)) and the Reprocessed L4 Satellite Measurements for SWH  
106 (<https://doi.org/10.48670/moi-00177>), to validate the simulation results and ERA5 data.

## 107 3 Methods

### 108 3.1 Development of a Fast Algorithm Based on GQ

109 The effects of sea spray droplets on sensible and latent heat fluxes ( $H_{S,SP}$ ,  $H_{L,SP}$ ) contribute to the total  
110 turbulent sensible and latent heat fluxes ( $H_{S,T}$ ,  $H_{L,T}$ ) at the air-sea interface. That is,

$$H_{S,T} = H_S + H_{S,SP}, \quad (1)$$

$$H_{L,T} = H_L + H_{L,SP}. \quad (2)$$

111 where  $H_S$  and  $H_L$  are the sensible and latent heat fluxes at the air-sea interface due to the air-sea  
112 differences of temperature and humidity. Based on observations of total turbulent heat fluxes and the  
113 COARE algorithm (Andreas et al., 2015; Fairall et al., 1996), A92 integrates the sea spray-mediated  
114 sensible and latent heat flux spectrums over initial droplet radius ( $Q_S(r_0)$  and  $Q_L(r_0)$ ) to estimate  $H_{S,SP}$   
115 and  $H_{L,SP}$  (details in Appendix A; Andreas, 1989, 1990, 1992; Andreas and Decosmo, 2002). The  
116 distributions of  $Q_S(r_0)$  and  $Q_L(r_0)$  spectrums as functions of initial droplet radius  $r_0$  under various  
117 atmosphere and ocean states are shown in Fig. 1, indicating that  $Q_S$  and  $Q_L$  spectrums are more  
118 sensitive to the change of WSP10, and less sensitive to other variables, including T02, 2-m relative  
119 humidity, SST, surface air pressure and sea surface salinity.

120 Since the calculation of  $H_{S,SP}$  and  $H_{L,SP}$  in A92 is computationally expensive due to full-size  
121 spectral integral (Eqn. A5-A6 of Appendix A), ~~therefore~~ it is difficult to apply A92 directly in coupled  
122 modeling systems. A15 (Andreas et al., 2015) developed a fast algorithm by using a single representative  
123 droplet radius (details in Appendix B), which was widely adopted in recent regional and global coupling  
124 systems (Xu et al., 2021a; Liu et al., 2012; Garg et al., 2018; Zhao et al., 2017; Song et al., 2022; Bao et  
125 al., 2020). In this study, we apply a 3-node GQ method (details in Appendix C) to develop a new fast  
126 algorithm to approximate the full-size spectral integral of A92. Notably, GQ can converge exponentially  
127 to the actual integral only for a smooth function, which is a prerequisite for GQ (McClarren, 2018). Since  
128 as functions of  $r_0$ ,  $Q_S(r_0)$  and  $Q_L(r_0)$  are not smooth (Fig. 1), a data sorting from largest to smallest  
129 is required. After sorting, local  $Q_S(r_0)$  and  $Q_L(r_0)$  become  $Q_{S\_sort}(m)$  and  $Q_{L\_sort}(m)$ , and then GQ  
130 can be used to estimate the integral of  $Q_{S\_sort}(m)$  and  $Q_{L\_sort}(m)$ . Note that the independent variable  
131  $m$  is not equivalent to the original  $r_0$ , but only indicates the position. In this way, according to Appendix

132 C,  $m_1=443$ ,  $m_2=251$ ,  $m_3=58$  are three GQ nodes of  $Q_{S\_sort}(m)$  and  $Q_{L\_sort}(m)$ , and we can get the  
 133 corresponding  $r_0$  for local  $Q_S(Q_L)$ , denoted as  $r_{S1}(r_{L1})$ ,  $r_{S2}(r_{L2})$  and  $r_{S3}(r_{L3})$ . However, the  
 134 sorting leads to high complexity of GQ comparable to A92, and the values of  $r_{S1}(r_{L1})$ ,  $r_{S2}(r_{L2})$  and  
 135  $r_{S3}(r_{L3})$  vary under various atmosphere and ocean [states/environments](#) in the globe. Therefore, it is  
 136 necessary to find the general approximate values of  $r_{S1}(r_{L1})$ ,  $r_{S2}(r_{L2})$  and  $r_{S3}(r_{L3})$  via global  
 137 statistical analyses, to avoid the sorting in application.

138 To derive the general approximate values of  $r_{S1}(r_{L1})$ ,  $r_{S2}(r_{L2})$  and  $r_{S3}(r_{L3})$ , we calculate the  
 139 distribution of the sea spray-mediated heat flux spectral following A92, based on the global daily WSP10,  
 140 T02, 2-m dewpoint temperature, surface pressure and SWH of ERA5 and OISST from August 1, 2018  
 141 to August 31, 2018. Since the sea spray-mediated heat flux is not sensitive to salinity (Fig. 1e&f) and  
 142 only monthly observational data is available, the ESA monthly salinity is applied. From the global  
 143 spectrums, we sort  $Q_S$  and  $Q_L$  from largest to smallest to obtain local  $r_{S1}$ ,  $r_{S2}$  and  $r_{S3}$  ( $r_{L1}$ ,  $r_{L2}$  and  
 144  $r_{L3}$ ) for every grid point, whose global distribution of occurrence frequency in percentage is shown in  
 145 Fig. 2. It is noted that except for  $r_{L3}$ , all other five nodes have frequency roughly concentrated at a  
 146 constant (peak frequency >65% in Fig. 2a, b, d-f; Eqn. 3&4), while for  $r_{L3}$ , there is a 92.53%  
 147 concentration between 55 and 90  $\mu m$  (Fig. 2c). Then we found that  $r_{L3}$  (55-90  $\mu m$ ) is related to WSP10  
 148 (Fig. S1 in supplementary), thereby we set the approximate values as

$$r_{S1} = 459.056, r_{S2} = 294.185, r_{S3} = 166.771, \quad (3)$$

$$r_{L1} = 443.914, r_{L2} = 251.0498, \quad (4)$$

$$r_{L3} = \begin{cases} 60.310WSP10^{0.1161}, & WSP10 \geq 2 \text{ m/s} \\ 58.086, & WSP10 < 2 \text{ m/s} \end{cases}, \quad (5)$$

149 where the unit of the radius is micrometer. Afterwards, we directly use Eqn. 3-5 to approximate the full-  
 150 size spectral integral of A92 without sorting as

$$\int_a^b Q_S(r_0)dr_0 \approx \frac{b-a}{2} \sum_{i=1}^3 \omega_i Q_S(r_{Si}), \quad (6)$$

$$\int_a^b Q_L(r_0)dr_0 \approx \frac{b-a}{2} \sum_{i=1}^3 \omega_i Q_L(r_{Li}). \quad (7)$$

151 Here a and b are the lower and upper limits of  $r_0$ , which are set to  $2\mu m$  and  $500\mu m$  based on Andreas  
 152 (1990), and  $\omega_i$  is the corresponding weight ( $\omega_1=\omega_3=0.556$ ,  $\omega_2=0.889$ ), obtained from McClarren

153 (2018). The new fast algorithm for approximations of  $H_{S,SP}$  and  $H_{L,SP}$  is referred to as SPRAY-GQ  
154 hereafter.

### 155 3.2 CFSv2.0-WW3 Coupling System

156 A coupled system based on Climate Forecast System model version 2.0 (CFSv2.0) and  
157 WAVEWATCH III (WW3) is employed to evaluate and compare the effects of sea spray-mediated heat  
158 flux parameterized by A15 and SPRAY-GQ. The CFSv2.0-WW3 has three components, the Global  
159 Forecast System (GFS; <http://www.emc.ncep.noaa.gov/GFS/doc.php>) as the atmosphere component of  
160 CFSv2.0, the Modular Ocean Model version 4 (MOM4; Griffies et al., 2004) as the ocean component of  
161 CFSv2.0, and the WW3 (WAVEWATCH III Development Group, 2016) as the ocean surface wave  
162 component. The variables between CFSv2.0 and WW3 are interpolated and passed using the Chinese  
163 Community Coupler version 2.0 (C-Coupler2; Liu et al., 2018).

164 The CFSv2.0 is mainly applied for intraseasonal and seasonal prediction (e.g., Saha et al., 2014). The  
165 atmosphere component GFS uses a spectral triangular truncation of 382 waves (T382) in the horizontal,  
166 equivalent to a grid resolution of nearly 35 km, and 64 sigma-pressure hybrid layers in the vertical. The  
167 MOM4 is integrated on a nominal  $0.5^\circ$  horizontal grid with enhanced horizontal resolution to  $0.25^\circ$  in  
168 the tropics, and there are 40 levels in the vertical. The CFSv2.0 initial fields at 00:00 UTC of the first  
169 day for experiments were generated by the real time operational Climate Data Assimilation System  
170 (Kalnay et al., 1996), downloaded from the CFSv2.0 official website  
171 (<http://nomads.ncep.noaa.gov/pub/data/nccf/com/cfs/prod>). The latitude range of WW3 is  $78^\circ\text{S}$ – $78^\circ\text{N}$   
172 with a spatial resolution of  $1/3^\circ$ . The initial wave fields were generated from 10-day simulations starting  
173 from rest in a stand-alone WW3 model, forced by ERA5 10-m winds and ice concentration. The open  
174 boundary conditions of WW3 were also obtained by the global simulation of the stand-alone WW3 model.

175 In the coupling system, the WW3 obtains 10-m wind and ocean surface current from CFSv2.0, and  
176 then provides wave parameters to CFSv2.0. Several wave-mediated processes, including upper ocean  
177 mixing modified by Stokes drift-related processes, air-sea fluxes modified by surface current and Stokes  
178 drift, and momentum roughness length, are considered. Details of this system are referred to Shi et al.  
179 (2022).



180 A series of numerical experiments is conducted to evaluate the effects of the two fast algorithms (A15  
181 and SPRAY-GQ) of sea spray-mediated heat flux on ocean, atmosphere and waves in two 56-day periods,  
182 from January 3 to February 28, 2017 and from August 3 to September 28, 2018 for boreal winter and  
183 boreal summer, respectively. For each period, two sensitivity experiments are carried out. The first is the  
184 SPRAY-A15 experiment, in which A15 is used with two-way fully coupling. The second is the SPRAY-  
185 GQ experiment, in which SPRAY-GQ fast algorithm is used instead of A15. In addition, we also carry  
186 out another 7-day experiment using A92 (SPRAY-A92) to test the runtime.

## 187 4 Results

### 188 4.1 Comparison with A92

189 Based on the daily global WSP10, T02, 2-m dewpoint temperature, surface pressure and SWH of  
190 ERA5, the daily global OISST, and the ESA monthly global salinity,  $H_{S,SP}$  and  $H_{L,SP}$  from A15,  
191 SPRAY-GQ and A92 are calculated (Fig. 3). The computational time for SPRAY-GQ is about the same  
192 as that for A15, and about 36 times less than the time for A92. Compared with A92 (the black dotted  
193 line), A15 (red) overestimates  $H_{S,SP}$  for low  $H_{S,SP}$  ( $<50$  W/m<sup>2</sup>) and underestimates  $H_{S,SP}$  for high  
194  $H_{S,SP}$  ( $>50$  W/m<sup>2</sup>) with a root mean square error (RMSE= $\sqrt{\sum_{i=1}^n(\hat{y}_i - y_i)^2/n}$ ,  $\hat{y}_i$  is A15 value,  $y_i$  is  
195 A92 value, and  $n$  is the total number of grid points) of 3.40 W/m<sup>2</sup> (Fig. 3a), while A15 shows consistent  
196 overestimations with a RMSE of 2.98 W/m<sup>2</sup> for  $H_{L,SP}$  (Fig. 3b). Overall, the RMSE of A15 is about  
197 2.69 W/m<sup>2</sup> for sea-spray mediated total heat flux ( $TH_{SP} = H_{S,SP} + H_{L,SP}$ ; Fig. 3c). Andreas et al. (2015)  
198 derived A15 from A92 using single-radius droplets as bellwethers and wind functions, and extrapolated  
199 the wind functions at high wind speeds  $>25$  m/s. Since the wind speeds in the study are less than 25 m/s  
200 (Fig. S1), the large difference between A15 and A92 is mainly due to the use of single-radius droplets.  
201 Compared with A15, SPRAY-GQ (blue) has less deviation from A92 for both  $H_{S,SP}$  and  $H_{L,SP}$  (Fig.  
202 3a&b). The corresponding RMSEs of SPRAY-GQ for  $H_{S,SP}$ ,  $H_{L,SP}$  and  $TH_{SP}$  are 0.83 W/m<sup>2</sup>, 0.92  
203 W/m<sup>2</sup> and 0.62 W/m<sup>2</sup>, all significantly lower ( $P<0.05$  in Student's t-test) than those of A15.

204 To test robustness of the results, we also use WSP10, T02 and SPH of OAFlux dataset to estimate  
205  $H_{S,SP}$  and  $H_{L,SP}$ . As shown in Fig. 4, SPRAY-GQ has significantly ( $P<0.05$  in Student's t-test) lower

206 deviations and RMSEs than A15, consistent with Fig. 3. Note that the values of  $H_{S,SP}$  and  $H_{L,SP}$  in  
207 Fig.4 are larger than those in Fig. 3. It is because OAFlux only provides neutral wind speeds, calculated  
208 from wind stress and the corresponding roughness by assuming air is neutrally stratified. The neutral  
209 winds from OAFlux are larger than winds in ERA5 as indicated by previous studies (Lindemann et al.,  
210 2021; Seethala et al., 2021).

211 In addition, since it is common to derive SWH from empirical equations (e.g., Andreas et al., 2008;  
212 Andreas et al., 2015; Andreas and Decosmo, 2002; Andreas, 1992), we also use SWH generated by  
213 empirical equations of WSP10 (Andreas, 1992) instead of ERA5 SWH to estimate  $H_{S,SP}$  and  $H_{L,SP}$   
214 (Fig. 5). Again, the RMSEs decrease significantly ( $P < 0.05$  in Student's t-test) in SPRAY-GQ compared  
215 to A15, though the RMSEs become higher for all estimates due to the enhanced biases of SWH. The  
216 difference between SPRAY-GQ and A92 is always smaller than that between A15 and A92. Next, we  
217 will evaluate and compare the two fast algorithms in an atmosphere-ocean-wave coupled system  
218 (CFSv2.0-WW3).

#### 219 **4.2 Comparison in the CFSv2.0-WW3 Coupling System**

220 To compare the computational time of different parameterizations in the large-scale modeling system,  
221 the runtime of the fully coupled experiments for 7-day forecast is given in Table 1 as an example. It is  
222 shown that the runtime is about the same for SPRAY-GQ and SPRAY-A15. Both experiments run about  
223 17 times faster than SPRAY-A92.

224 To illustrate the numerical errors of the two fast algorithms discussed in the context of the coupled  
225 system, comparisons are made for simulated SSTs, WSP10s as well as SWHs against OISST and ERA5  
226 reanalysis. The results in the first three days are excluded in the comparison, since the wave influences  
227 are weak at the beginning of the simulations. Overall, the WSP10s of simulations are generally in the  
228 range of 0-25 m/s globally. At mid-high latitudes, the WSP10s generally exceed 10 m/s (Fig. S2&S3 of  
229 the supplementary), at which the effects of sea spray can become significant (Andreas et al., 2015;  
230 Andreas et al., 2008).

#### 231 4.2.1 Sea Surface Temperature (SST)

232 In the austral summer, compared with OISST, large SST biases ( $>1$  °C or  $<-1$  °C) of SPRAY-A15  
233 occur in the Southern Hemisphere (SH; Fig. S4a in supplementary), especially in the Southern Ocean. It  
234 is always a challenge ~~for to reducing~~ reduce the large SST biases in the Southern Ocean for climate  
235 models (e.g., Alessandro et al., 2019; Wang et al., 2014; Li et al., 2013; Bodas-Salcedo et al., 2012;  
236 Ceppi et al., 2012). In Fig. 6a, SSTs north (south) of 50°S in experiment SPRAY-A15 are mainly  
237 underestimated (overestimated). The domain-averaged RMSE (0-360°E, 40-75°S) in experiment  
238 SPRAY-A15 increases in the first month and then levels off (red solid line in Fig. 6c); ~~w~~ While the  
239 domain-averaged RMSE in experiment SPRAY-GQ levels off about a week earlier (black solid line in  
240 Fig. 6c). The mean RMSE in SPRAY-GQ is significantly lower than that in SPRAY-A15 ( $P<0.05$  in  
241 Student's t-test). The increased (decreased) SSTs north (south) of 50°S in SPRAY-GQ compared to those  
242 in SPRAY-A15 (Fig. 6b) reduce the RMSE of SST in SPRAY-GQ. We also calculate the mean absolute  
243 error,  $MAE = \sum_{i=1}^n |\hat{y}_i - y_i|/n$ , where  $\hat{y}_i$  is simulated value and  $y_i$  is OISST data, and  $n$  is the total  
244 number of grid points. The MAEs are consistent with RMSEs (dotted line in Fig. 6c). Furthermore, the  
245 mean errors,  $ME = \sum_{i=1}^n (\hat{y}_i - y_i)/n$  (Fig. S5a in the supplementary), are smaller in SPRAY-GQ than  
246 SPRAY-A15.

247 To understand the effects of sea spray droplets on SST, we calculate the total heat flux ( $TH = H_{S,T} + H_{L,T}$ )  
248 differences between SPRAY-GQ and SPRAY-A15 (Fig. 7a). The TH differences are significantly  
249 correlated with SST differences (Fig. S4b in the supplementary), with the spatial correlation coefficient  
250 of -0.41 ( $P<0.05$  in Student's t-test). We further decompose direct and indirect effects of sea spray  
251 droplets on heat fluxes following Song et al. (2022). The direct effect ( $H_{S,SP}$  and  $H_{L,SP}$ ) is induced  
252 directly by sea spray droplets, calculated from A15 (Eqn. B1-B4 of Appendix B) and SPRAY-GQ  
253 (Section 3.1). The indirect effect ( $H_S$  and  $H_L$ ) is the heat flux variation induced by changes of  
254 atmosphere and ocean variables (including wind, pressure, humidity and temperature) caused by direct  
255 effect, estimated by subtracting  $H_{S,SP}$  and  $H_{L,SP}$  from the output heat fluxes ( $H_{S,T}$  and  $H_{L,T}$ ) of  
256 experiment SPRAY-A15 and SPRAY-GQ.

257 In the Southern Ocean, although direct differences of  $H_{S,SP}$  and  $H_{L,SP}$  are relatively small ( $<10$   
258  $W/m^2$ , Fig. 7b, e, &h), the resulting changes of temperature and humidity lead to relatively large

259 differences in indirect effects of  $H_S$  and  $H_L$  (Fig. 7c, f, &i). Enhanced (reduced)  $TH_{SP}$  from ocean to  
260 atmosphere in the summer leads to increased (decreased) air-sea temperature difference and thus  
261 enhances (weakens)  $H_S$ . Meanwhile the warmer (cooler) air also causes more (less) evaporation and thus  
262 more (less)  $H_L$ . Finally, the enhanced (reduced) TH cools (warms) SST.

263 In the boreal summer, large SST biases ( $>1$  °C or  $<-1$  °C) of SPRAY-A15 mainly occur at mid-high  
264 latitudes of the Northern Hemisphere (NH; Fig. S6a in supplementary). Significant underestimations  
265 occur in the western and northern part of the North Pacific and at mid latitudes of the North Atlantic,  
266 while large positive SST biases mainly occur in the eastern part of the North Pacific and at high latitudes  
267 of the North Atlantic (Fig. 8a). In experiment SPRAY-GQ, SSTs are warmer (cooler) in the previously  
268 underestimated (overestimated) regions (Fig. 8b). Therefore, the domain-averaged RMSE and MAE (0-  
269 360°E, 20-75°N) in SPRAY-GQ are significantly lower ( $P<0.01$  in Student's t-test) than in SPRAY-A15  
270 after the first three weeks (Fig. 8c). Compared to SPRAY-A15, the overall underestimation is reduced in  
271 SPRAY-GQ (Fig. S5b). The spatial correlation coefficient between TH differences and SST differences  
272 (Fig. 9a&Fig. S6b) is -0.32 ( $P<0.05$  in Student's t-test). Consistent with the austral summer, the SST  
273 changes are related to the changes of heat flux (Fig. 9). The indirect effects of latent heat flux (Fig. 9f)  
274 play a major role in TH differences, which are modified by the direct effects (Fig. 9b, e, &h). In addition,  
275 the changes of surface wind also contribute to the changes of SST. The reduced winds weaken the upper  
276 ocean mixing, the water becomes more stratified, and then the SST tends to be warmer, and vice versa  
277 (Fig. S7&S8).

#### 278 4.2.2 10-m Wind Speed (WSP10) and Significant Wave Height (SWH)

279 Compared with experiment SPRAY-A15, significant differences of WSP10 in SPRAY-GQ occur at  
280 mid-low latitudes of the NH (0-360°E, 0-60°N) in both winter and summer (Fig.S7b&S8b). As we know,  
281 satellite scatterometer and altimeter data are usually used to validate WSP10 and SWH for short term  
282 weather forecast (e.g., Accadia et al., 2007; Djurdjevic and Rajkovic, 2008; Myslenkov et al., 2021).  
283 However, due to the spatial and temporal coverage of satellite data, we can only obtain the monthly  
284 averaged satellite data for the globe. [So-Therefore](#), we compare the monthly averaged WSP10 and SWH  
285 from simulations with the corresponding satellite data (Fig. S9-S12). The comparison results (Fig.

286 S9a&c-S12a&c) are consistent with those compared with ERA5 (Fig. S9b&d-S12b&d). From Fig. S9e-  
287 S12e, the differences of WSP10s between ERA5 and the satellite data are always less than 1 m/s and the  
288 differences of SWHs are always less than 0.3 m. Since ERA5 provides daily data for comparison, we  
289 will use ERA5 for validation in the following.

290 The ME of WSP10 (SPRAY-A15 minus ERA5) is 0.28 m/s and 0.47 m/s in winter and summer (red  
291 in Fig. S5c&d), respectively, mainly due to the overestimations over the Pacific and the Atlantic Ocean  
292 (red in Fig.10a&11a). Whereas in SPRAY-GQ, the ME (SPRAY-GQ minus ERA5) is 0.15 m/s and 0.33  
293 m/s in winter and summer respectively (black in Fig. S5c&d). The domain-averaged RMSEs and MAEs  
294 of WSP10s increase with time in the first two weeks and then gradually level off (Fig. 10c&11c). The  
295 differences of WSP10 RMSEs and MAEs between SPRAY-GQ (black) and SPRAY-A15 (red) are very  
296 small in the first two weeks. Afterwards the mean values of RMSE and MAE in SPRAY-GQ are lower  
297 than those in SPRAY-A15 significantly at 95% confidence level in both boreal winter (Fig. 10c) and  
298 boreal summer (Fig. 11c).

299 The simulated SWHs changes are closely related to the changes of WSP10s (Shi et al., 2022).  
300 Therefore, the differences of SWHs (Fig.12&13) are consistent with those of WSP10s (Fig.10&11), with  
301 overestimated (underestimated) WSP10s corresponding to overestimated (underestimated) SWHs  
302 compared with ERA5. The SWHs in SPRAY-GQ are significantly different [with-from](#) those in SPRAY-  
303 A15 (Fig. 12b&13b). In winter (summer), the SWH RMSE averages for SPRAY-A15 and SPRAY-GQ  
304 are 1.31 m (0.98 m) and 1.23 m (0.87 m), and after the first two weeks the RMSE and MAE in SPRAY-  
305 GQ are lower than those in SPRAY-A15 significantly at 95% confidence level in both winter (Fig. 12c)  
306 and summer (Fig. 13c).

307 The direct and indirect effects of sea spray droplets on heat fluxes can influence estimates of WSP10  
308 and then SWH. The changes of WSP10s are related to the direct effects ( $H_{S,SP}$  and  $H_{L,SP}$ ; Fig. 7b, e, &h;  
309 Fig. 9b, e, &h). The spatial correlation coefficients between WSP10 differences (Fig. S7b&S8b) and  
310  $TH_{SP}$  differences (Fig. 7b&9b) are 0.51 and 0.69 ( $P<0.01$  in Student's t-test) in winter and summer,  
311 respectively. [Because](#)  $TH_{SP}$  differences can influence the sea level pressure (SLP) distribution (Fig.  
312 S15&S16), and subsequently surface winds. For example, compared with SPRAY-A15, the decreased  
313  $TH_{SP}$  of SPRAY-GQ in the Northwest Pacific in summer (Fig. 9b) leads to higher SLP and smaller

314 pressure gradient (Fig. S16), and thus decreased WSP10 (Fig. 11b); while the increased  $TH_{SP}$  in the  
315 Gulf of Alaska (Fig. 9b) leads to lower SLP and larger pressure gradient (Fig. S16), and thus enhanced  
316 WSP10 (Fig. 11b). The accelerated (decelerated) WSP10s further result in increased (decreased)  
317 interfacial heat transport ( $H_S$ ,  $H_L$ ), as well as increased (decreased) SWHs.

## 318 **5 Conclusions and Discussion**

319 Based on a GQ method, we develop a new fast algorithm based on Andreas's (1989, 1990, 1992) full-  
320 size microphysical parameterization (A92) for sea spray-mediated heat fluxes. Using global satellite  
321 measurements and reanalysis data, we found that the difference between SPRAY-GQ and A92 is  
322 significantly smaller than that between A15 and A92 (Andreas et al., 2015). To evaluate the numerical  
323 error of SPRAY-GQ/A15 fast algorithm, we implement them in the two-way coupled CFSv2.0-WW3  
324 system. A series of 56-day simulations from January 3 to February 28, 2017 and from August 3 to  
325 September 28, 2018 are conducted. The results are compared against satellite measurements and ERA5  
326 reanalysis. The comparison shows that the sea spray-mediated heat flux in SPRAY-GQ can reasonably  
327 modulate total heat flux compared with SPRAY-A15, and significantly reduce the SST biases in the  
328 Southern Ocean (mid-high latitudes of the NH) for the austral (boreal) summer, as well as WSP10 and  
329 SWH after the first two weeks at mid-low latitudes of the NH for both boreal winter and summer. Overall,  
330 our fast algorithm based on GQ is applicable to sea spray-mediated heat flux parameterization in coupled  
331 models.

332 To investigate the effects of spray-mediated heat flux on simulations, two 56-day experiments without  
333 sea spray effect (CTRL) in boreal winter and summer ~~respectively~~ are conducted respectively, and the  
334 differences of simulated SST, WSP10, SWH, T02 and SPH between SPRAY-GQ and CTRL are  
335 compared in Fig. S17-S21 in the supplementary. The introduction of sea spray cannot significantly  
336 reduce the global overall errors of simulations, but it leads to regional improvements (blue in Fig.  
337 S17e&f-S21e&f). For example, compared with CTRL in Jan-Feb, 2017, SST MAE of SPRAY-GQ in  
338 the southeast of Australia decreases (Fig. S17e), because of warmer SST (Fig. S17c) related to reduced  
339 wind (Fig. S18c). The reduced wind here also leads to lower SWH (Fig. S19c) and thus reduced SWH  
340 overestimation (Fig. S19e). Meanwhile, SPRAY-GQ reduces MAE of T02 and SPH (Fig. S20e&S21e)

341 by increasing temperature and moisture (Fig. S20c&S21c). The reduced errors are related to the relatively  
342 large WSP10s over the areas (Fig. S2&S3), since the effects of sea spray become important at wind  
343 speeds larger than 10 m/s.

344 In addition to the variables aforementioned, the changes of simulated cloud fraction were also  
345 compared. However, the effects of sea spray-mediated heat flux on cloud fraction are non-significant for  
346 the 2-month simulation, so the results are not shown. Besides, the lack of other processes related to sea  
347 spray may be one of [the](#) reasons why the global overall error cannot be reduced effectively. For example,  
348 for simulated WSP10 and SWH in SPRAY-GQ, the significant overestimations in the SH still exist  
349 especially in Aug-Sep, 2018 (Fig. S18&S19 in supplementary). As Andreas (2004) indicated, sea spray  
350 droplets also influence the surface momentum flux by injecting more momentum into the ocean from the  
351 atmosphere, which might further decrease the surface wind speed. We will consider this process in the  
352 future study.

353 Sea spray-mediated heat fluxes are related to the sea spray generation function (SSGF). Based on a  
354 number of laboratory and field observations, varieties of SSGF were derived (e.g., Koga, 1981; Monahan  
355 et al., 1982; Troitskaya et al., 2018; Andreas, 1992, 1998, 2002; Fairall et al., 1994; Veron, 2015),  
356 whereas their differences can reach six orders of magnitude (Andreas, 1998). There is currently no  
357 consensus on the most suitable choice. In this study, we use SSGF of Fairall et al. (1994), recommended  
358 by Andreas (2002), to get a mean bias of 3.70 W/m<sup>2</sup> and 0.095 W/m<sup>2</sup> for latent and sensible heat flux  
359 respectively (Andreas et al., 2015), consistent with recent observations of Xu et al. (2021b). [Even](#)  
360 [though](#)[However](#), the improved SST and other variables cannot be reliably assigned to the usage of the  
361 GQ method, due to the uncertainties of the coupled model itself and SSGF.

362 When wind speed is larger than 10 m/s, spray-mediated heat flux can become as important as the  
363 interfacial heat flux (Andreas and Decosmo, 1999, 2002). Particularly, even in the absence of air-sea  
364 temperature difference, the spray-mediated sensible heat flux is still present (Andreas et al., 2008). As  
365 indicated by previous studies (e.g., Garg et al., 2018; Song et al. 2022), it is necessary to superimpose  
366 the spray-mediated heat flux on the bulk formula to complete the physics of turbulent heat transfer for  
367 coupled simulation. Since the full microphysical parameterization (A92) is computationally expensive,  
368 an efficient algorithm that captures the main features of A92 can be beneficial to large-scale climate

369 systems or operational storm models. The GQ method proposed in the study can efficiently calculate the  
 370 spray-mediated heat flux, and agree better with A92 than A15. ~~Thereby~~Therefore, the GQ based spray-  
 371 mediated heat flux is promising to be widely applied in large-scale climate systems and operational storm  
 372 models.

373

## 374 Appendix A

### 375 Microphysical Parameterization of A92

376 Based on the cloud microphysical parameterization of Pruppacher and Klett (1978), Andreas (1989,  
 377 1990, 1992) proposed a parameterization of sea spray-related heat fluxes for droplets with different radius,  
 378 from formation at sea surface to equilibrium with environment, that is,

$$Q_S = \rho_w C_{ps} (T_w - T_{eq}) \left[ 1 - \exp\left(-\frac{\tau_f}{\tau_T}\right) \right] \left( \frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), \quad (A1)$$

$$Q_L = \begin{cases} \rho_w L_v \left\{ 1 - \left[ \frac{r(\tau_f)}{r_0} \right]^3 \right\} \left( \frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), & \tau_f \leq \tau_r, \\ \rho_w L_v \left\{ 1 - \left( \frac{r_{eq}}{r_0} \right)^3 \right\} \left( \frac{4\pi r_0^3}{3} \frac{dF}{dr_0} \right), & \tau_f > \tau_r. \end{cases} \quad (A2)$$

379 Here  $Q_S$ ,  $Q_L$  are sensible heat flux and latent heat flux resulted ~~by~~from sea spray droplets with initial  
 380 radius  $r_0$ ,  $\rho_w$  is the sea water density,  $C_{ps}$  is the specific heat,  $L_v$  is the latent heat of vaporization of  
 381 water,  $T_w$  is the water temperature,  $T_{eq}$  is the temperature of droplet when it reaches thermal  
 382 equilibrium with ambient condition,  $r_{eq}$  is the radius of droplet when it reaches moisture equilibrium  
 383 with ambient condition,  $\tau_f$  is the residence time for droplets in the atmospheric,  $r(\tau_f)$  is the  
 384 corresponding radius,  $\tau_T$  is the characteristic e-folding time of droplet temperature, and  $\tau_r$  is the  
 385 characteristic e-folding time of droplet radius. The detailed calculation of these microphysical quantities  
 386 can be found in Andreas (1989, 1990, 1992). ~~And~~ $dF/dr_0$  is the sea spray generation function, which  
 387 represents the ~~produced~~produced number of droplets with initial radius  $r_0$  (Andreas, 1992). For this  
 388 term, the function of Fairall et al. (1994) was recommended by Andreas (2002). According to the review  
 389 in Andreas (2002), the  $dF/dr_0$  of Fairall et al. (1994) is related on that of Andreas (1992) as

$$\frac{dF}{dr_0} = 38 \times 3.84 \times 10^{-6} U_{10}^{3.41} r_0^{-0.024} \frac{dF_{A92}}{dr_{80}} \Big|_{U_{10}=11 \text{ m/s}}, \quad (A3)$$



$$\left. \frac{dF_{A92}}{dr_{80}} \right|_{U_{10}=11 \text{ m/s}} = \begin{cases} e^{(4.405-2.646(\log r_{80})-3.156(\log r_{80})^2+8.902(\log r_{80})^3-4.482(\log r_{80})^4)}, r_{80} \leq 15 \mu\text{m}; \\ 1.02 \times 10^4 r_{80}^{-1}, 15 \leq r_{80} \leq 37.5 \mu\text{m}; \\ 6.95 \times 10^6 r_{80}^{-2.8}, 37.5 \leq r_{80} \leq 100 \mu\text{m}; \\ 1.75 \times 10^{17} r_{80}^{-8}, r_{80} \geq 100 \mu\text{m} \end{cases} \quad (\text{A4})$$

390 Here  $U_{10}$  is the 10-m wind,  $r_{80} = 0.518r_0^{0.976}$ .

391 The total sea spray fluxes are obtained by integrating  $Q_S$  and  $Q_L$  corresponding to all  $r_0$ . Based on  
392 Andreas (1990), the lower and upper limits of  $r_0$  is  $2\mu\text{m}$  and  $500\mu\text{m}$ , that is,

$$\overline{Q_S} = \int_2^{500} Q_S(r_0) dr, \quad (\text{A5})$$

$$\overline{Q_L} = \int_2^{500} Q_L(r_0) dr. \quad (\text{A6})$$

393 ~~While~~ Note that  $\overline{Q_S}$  and  $\overline{Q_L}$  are nominal sea spray fluxes but not the actual  $H_{S,SP}$  and  $H_{L,SP}$  (Andreas  
394 and Decosmo, 1999, 2002), because there are interactions between these two terms and the microphysical  
395 functions also lead to uncertainties (Fairall et al., 1994). Therefore,  $\overline{Q_S}$  and  $\overline{Q_L}$  are tuned by non-  
396 negative constants  $\alpha$ ,  $\beta$  and  $\gamma$  (Andreas and Decosmo, 2002; Andreas et al., 2008; Andreas et al., 2015;  
397 Andreas, 2003) as

$$H_{S,SP} = \beta \overline{Q_S} - (\alpha - \gamma) \overline{Q_L}, \quad (\text{A7})$$

$$H_{L,SP} = \alpha \overline{Q_L}. \quad (\text{A8})$$

398 In Eqn. (A8), the  $\alpha$  term indicates the sea spray-mediated latent heat flux from the top of DEL to  
399 atmosphere. Because the evaporation of droplets absorbs heat, which is provided by sea spray-mediated  
400 sensible heat (Fairall et al., 1994), the negative  $\alpha$  term appears in Eqn. (A7). ~~Whereas~~ The evaporation  
401 also cools DEL and thus increases the air-sea temperature difference, therefore it contributes to a positive  
402  $\gamma$  term in Eqn. (A7). Different values of  $\alpha$ ,  $\beta$  and  $\gamma$  were given in Andreas and Decosmo (2002),  
403 Andreas (2003), Andreas et al. (2008) and Andreas et al. (2015), to minimize the bias between  
404 estimations and observations of turbulent heat fluxes measured by eddy correlation. And Andreas et al.  
405 (2015) validated the most observation data, which are 4000 sets, to derive  $\alpha = 2.46$ ,  $\beta = 15.15$ ,  $\gamma =$   
406 1.77.

407 **Appendix B**

408 **Fast Algorithm of A15**

409 Andreas (2003) and Andreas et al. (2008, 2015) developed a fast algorithm to approximate  $H_{S,SP}$ ,  
 410  $H_{L,SP}$  by a characteristic radius, that is,

$$H_{S,SP} = \beta \overline{Q_S} - (\alpha - \gamma) \overline{Q_L} \approx \rho_w c_{ps} (T_W - T_{eq,100}) V_S(u_*), \quad (B1)$$

$$H_{L,SP} = \alpha \overline{Q_L} \approx \rho_w L_v \left\{ 1 - \left[ \frac{r(\tau_{f,50})}{50 \mu\text{m}} \right]^3 \right\} V_L(u_*). \quad (B2)$$

411 Here  $T_{eq,100}$  is  $T_{eq}$  of droplets with  $r_0=100 \mu\text{m}$ ,  $\tau_{f,50}$  is  $\tau_f$  of droplets with  $r_0=50 \mu\text{m}$ ,  $V_S$  and  
 412  $V_L$  are functions of the bulk friction velocity  $u_*$ . As indicated by Andreas et al. (2008, 2015), the  
 413 characteristic radiuses of 100  $\mu\text{m}$  and 50  $\mu\text{m}$  for sensible and latent heat fluxes are chosen,  
 414 respectively, because  $Q_S$  and  $Q_L$  show a large peak in the vicinity of these values (Fig. 1).  $V_S$  and  $V_L$   
 415 are calculated in Andreas et al. (2015) as

$$V_S = \begin{cases} 3.92 \times 10^{-8}, & 0 \leq u_* \leq 0.1480 \text{ m/s} \\ 5.02 \times 10^{-6} u_*^{2.54}, & u_* \geq 0.1480 \text{ m/s} \end{cases} \quad (B3)$$

$$V_L = \begin{cases} 1.76 \times 10^{-9}, & 0 \leq u_* \leq 0.1358 \text{ m/s} \\ 2.08 \times 10^{-7} u_*^{2.39}, & u_* \geq 0.1358 \text{ m/s} \end{cases} \quad (B4)$$

416 **Appendix C**

417 **Gaussian Quadrature (GQ)**

418 GQ is a method to approximate the definite integral of a function  $f(x)$  via the function values at a  
 419 small number of specified nodes (Gauss, 1815; Jacobi, 1826). In this study we use the form of n-node  
 420 Gauss–Legendre quadrature on  $[-1, 1]$  as

$$\int_{-1}^1 f(x) dx \approx \sum_{i=1}^n \omega_i f(x_i). \quad (C1)$$

421 Here  $x_i$  is the specified node, and  $\omega_i$  is the corresponding weight. For  $n=3$ ,  $x_1=-0.775$ ,  $x_2=0$ ,  
 422  $x_3=0.775$ ,  $\omega_1=\omega_3=0.556$ ,  $\omega_2=0.889$ .

423 ~~While for~~ a function  $g(\xi)$  on  $[a, b]$ , Eqn. (C1) can be transformed to

$$\int_a^b g(\xi) d\xi = \int_{-1}^1 g\left(\frac{b-a}{2}x + \frac{a+b}{2}\right) \frac{d\xi}{dx} dx \quad (C2)$$

$$\approx \frac{b-a}{2} \sum_{i=1}^n \omega_i g\left(\frac{b-a}{2}x_i + \frac{a+b}{2}\right).$$

424 **Code and data availability**

425 The code of sea spray can be found under <https://doi.org/10.5281/zenodo.7100345> or  
426 <https://zenodo.org/record/7100345#.Y66vRtVByHt> (Shi and Xu, 2022). The code for CFSv2.0-WW3  
427 system can be found under <https://doi.org/10.5281/zenodo.5811002> (Shi et al., 2021) including the  
428 coupling, preprocessing, run control and postprocessing scripts. The initial fields for CFSv2.0 are  
429 generated by the real time operational Climate Data Assimilation System, downloaded from the CFSv2.0  
430 official website (<http://nomads.ncep.noaa.gov/pub/data/nccf/com/cfs/prod>). The daily average satellite  
431 Optimum Interpolation SST (OISST) data are obtained from NOAA (<https://www.ncdc.noaa.gov/oisst>).  
432 The fifth generation European Centre for Medium-Range Weather Forecasts (ECMWF) Reanalysis  
433 (ERA5) are available at the Copernicus Climate Change Service (C3S) Climate Data Store  
434 (<https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-single-levels>). The daily Objectively  
435 Analyzed air-sea Fluxes (OAFlux) products are available at <https://oaflux.who.edu/heat-flux>. The global  
436 monthly mean salinity observations of European Space Agency (ESA) are from <https://climate.esa.int>.  
437 The monthly global ocean RSS Satellite Data Products for 10-m wind speed are from  
438 [https://data.remss.com/wind/monthly\\_1deg/](https://data.remss.com/wind/monthly_1deg/), and the Reprocessed L4 Satellite Measurements for  
439 significant wave height are from <https://doi.org/10.48670/moi-00177>.

440 **Author contribution**

441 FX and RS designed the experiments and RS carried them out. RS developed the code of coupling  
442 parametrizations and produced the figures. RS prepared the manuscript with contributions from all co-  
443 authors. FX contributed to review and editing.

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#### 449 **Competing Interests**

450 The contact author has declared that neither they nor their co-authors have any competing interests.

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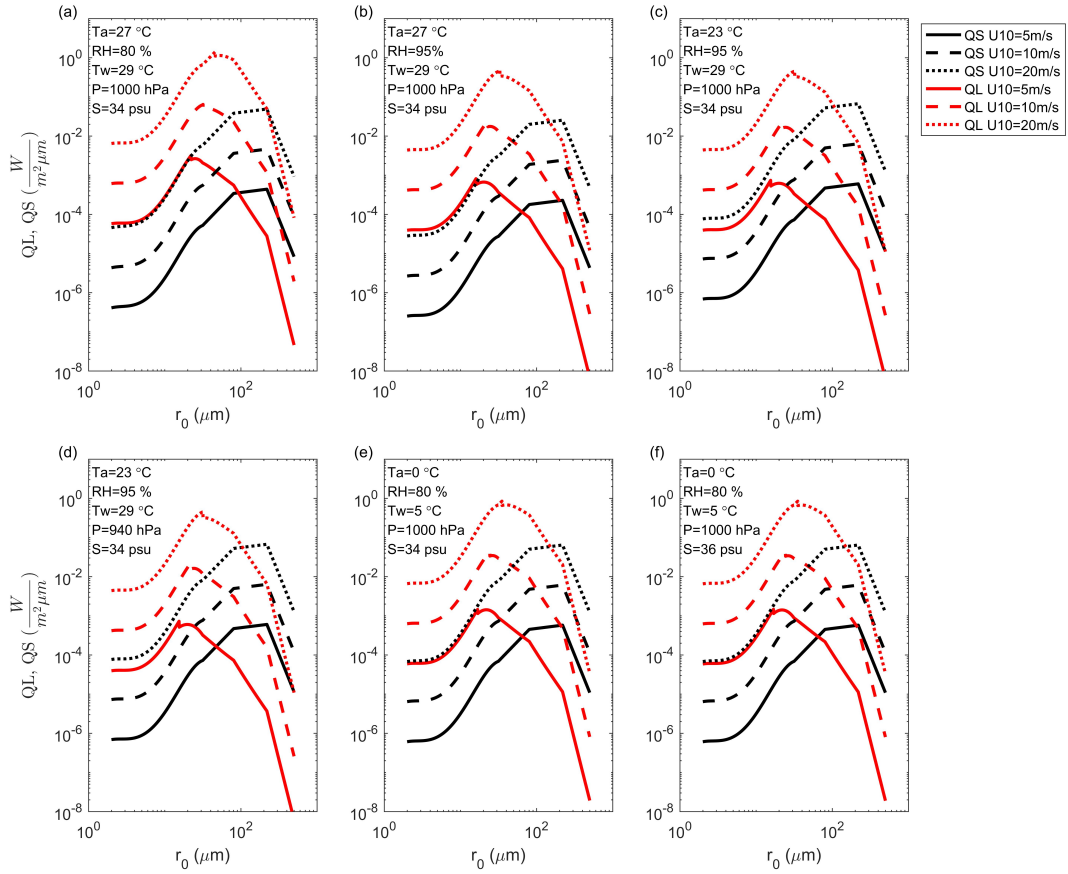
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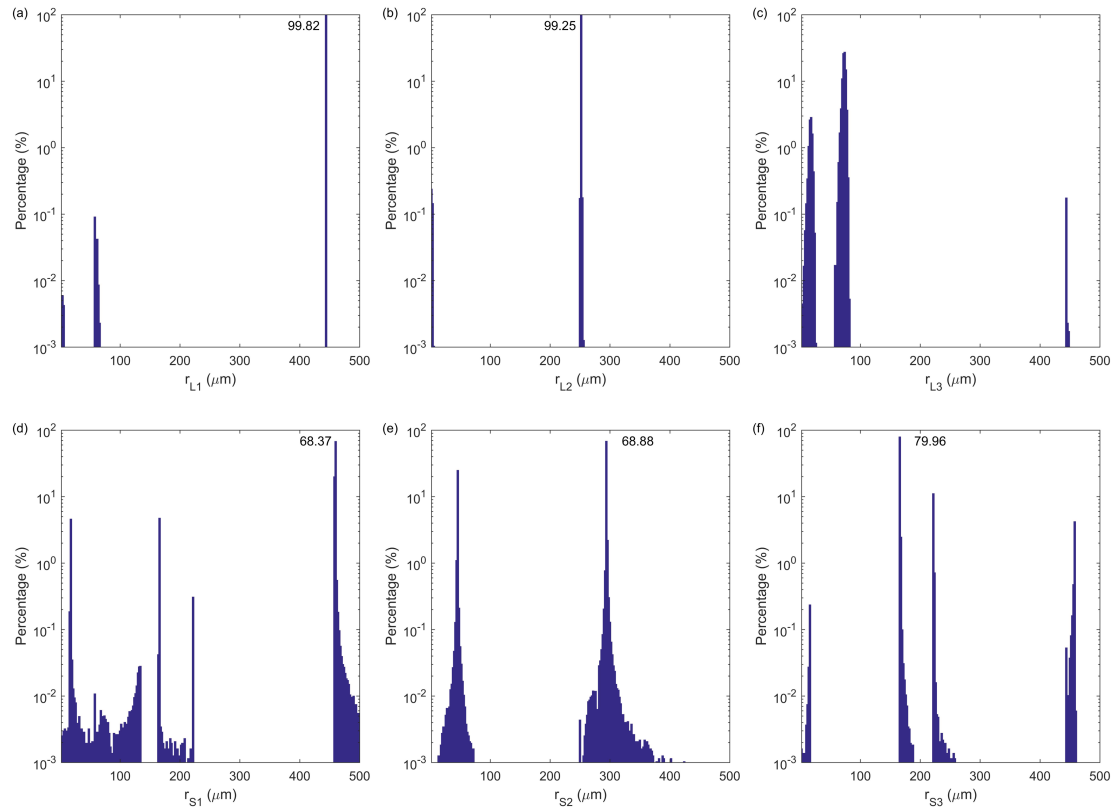
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**Table 1.** The runtime of CFSv2.0-WW3 global experiments for 7-day forecast with different parameterizations.

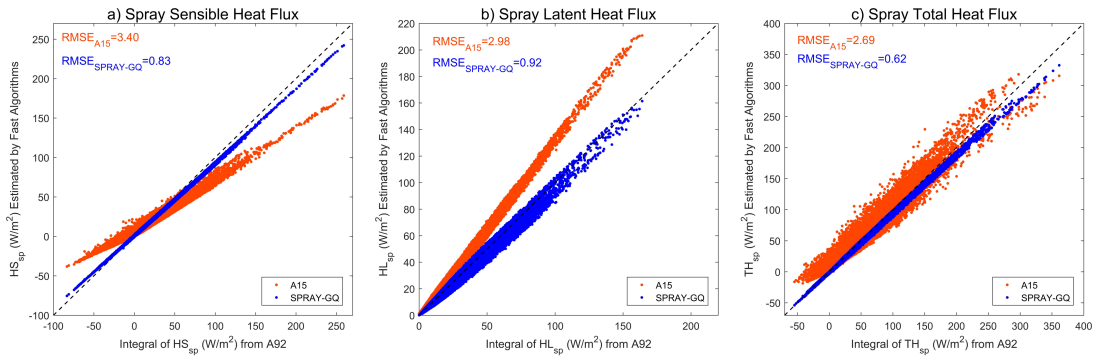
<b>7-day Forecast</b>	<b>Runtime (h)</b>
SPRAY-A92	126.94
SPRAY-A15	7.60
SPRAY-GQ	7.67



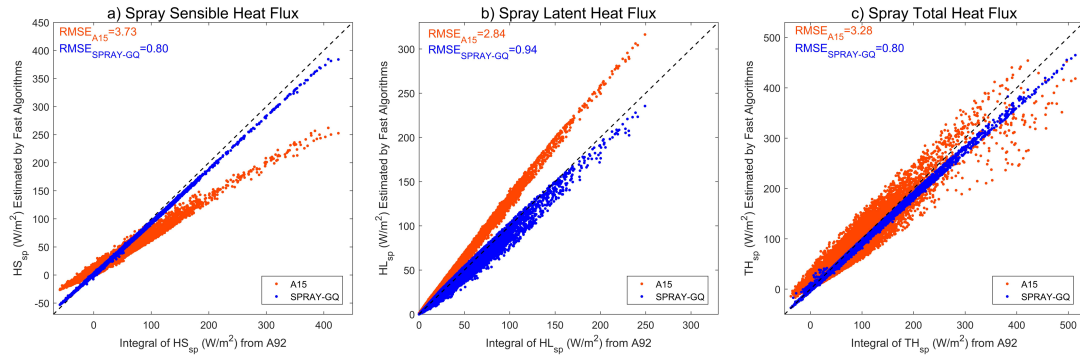
**Figure 1.** The radius-specific sea spray-mediated sensible ( $Q_S$ ; black) and latent ( $Q_L$ ; red) heat fluxes as functions of initial radius  $r_0$ :  $U_{10}$ ,  $T_a$ ,  $RH$ ,  $T_w$ ,  $P$  and  $S$  are 10-m wind speed, 2-m air temperature, 2-m relative humidity, sea surface temperature, surface air pressure and surface salinity, respectively.



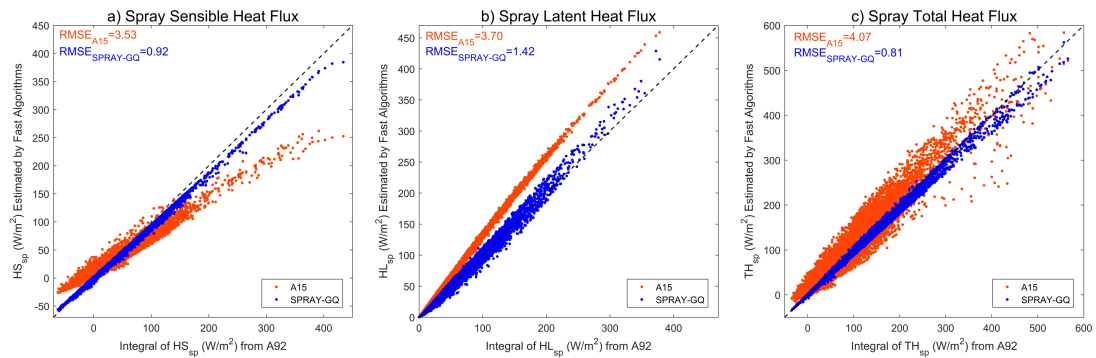
**Figure 2.** The distribution of occurrence frequency in percentage for GQ radius nodes: (a) the first node of latent heat flux; (b) the second node of latent heat flux; (c) the third node of latent heat flux; (d) the first node of sensible heat flux; (e) the second node of sensible heat flux; (f) the third node of sensible heat flux. The peak frequencies are marked.



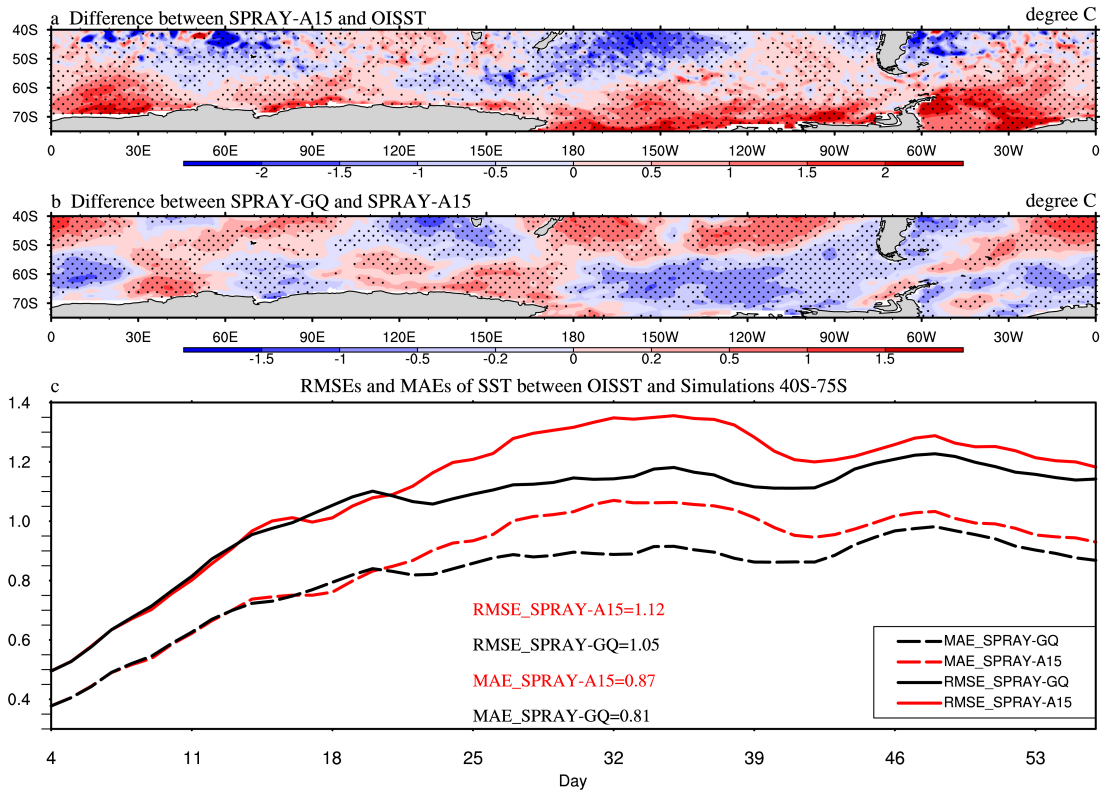
**Figure 3.** Scatter plots of  $H_{S,SP}$  (a),  $H_{L,SP}$  (b) and total heat flux  $TH_{SP} = H_{S,SP} + H_{L,SP}$  (c) estimated by fast algorithms (y-axis) vs those estimated by spectral integral in microphysical parameterization (x-axis): The dotted black line is  $y=x$ . The corresponding RMSEs are marked in the upper left corner.



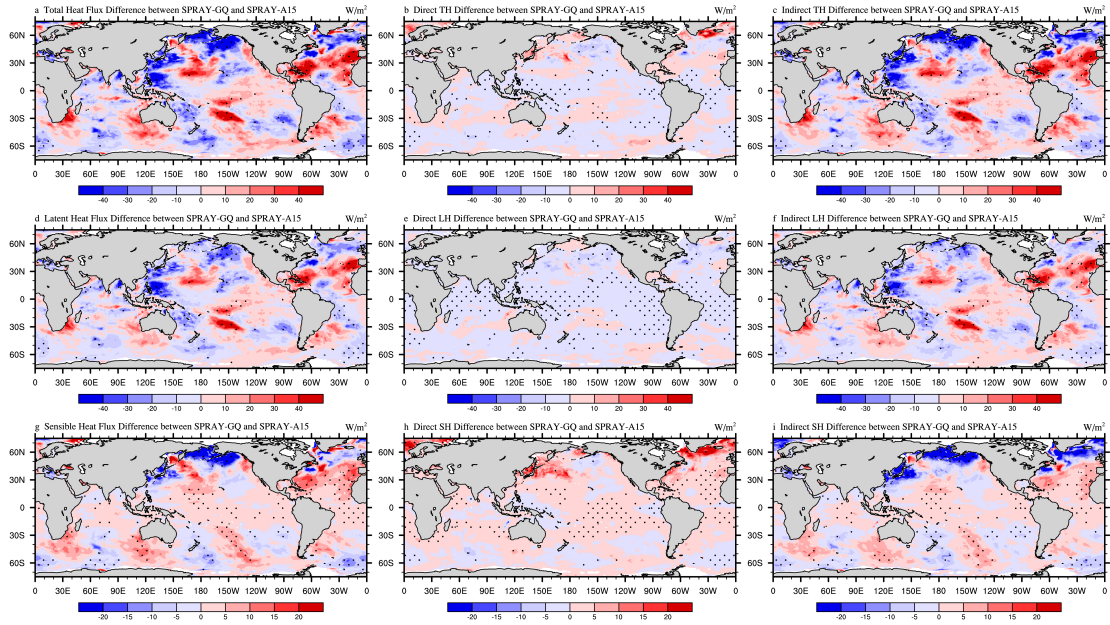
**Figure 4.** The same as Figure 3, but WSP10, 2-m air temperature and 2-m specific humidity of OAF flux are used.



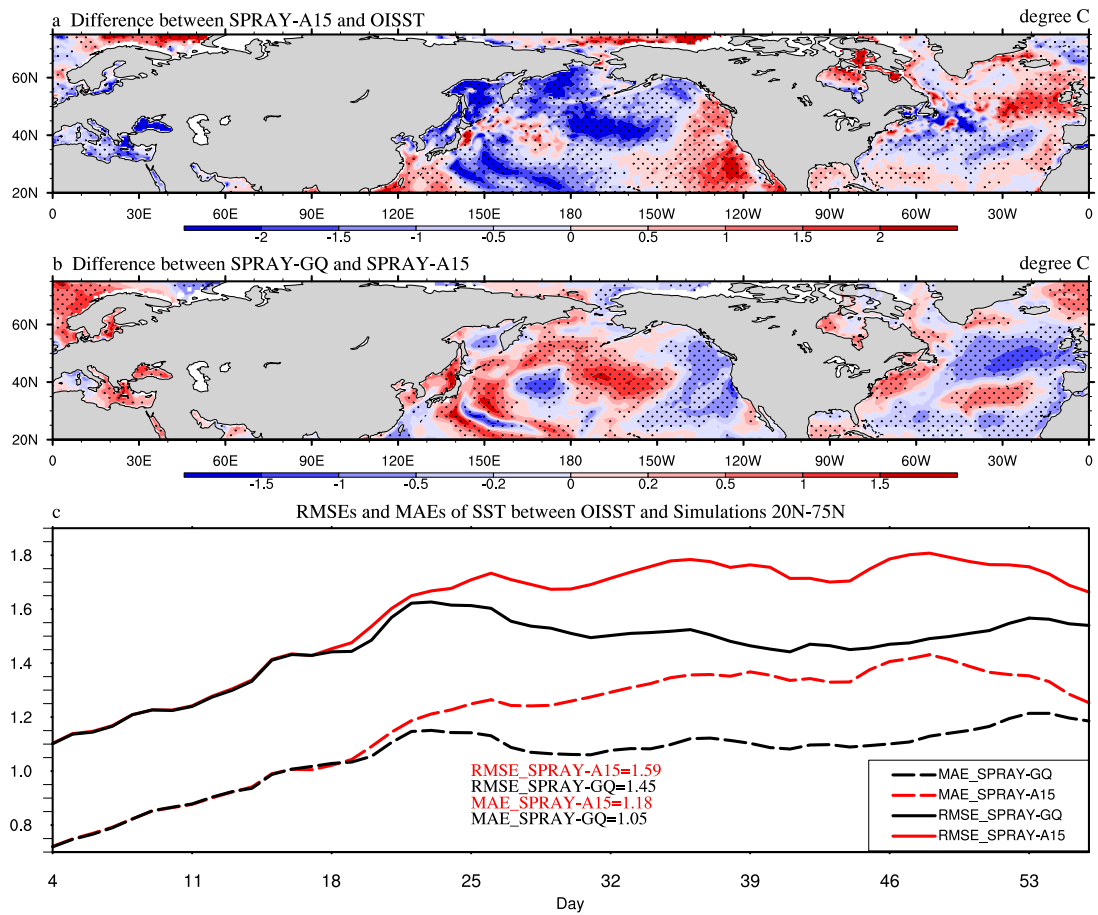
**Figure 5.** The same as Figure 4, but SWH is derived by WSP10 instead of ERA5 SWH.



**Figure 6.** The 53-day average SST ( $^{\circ}\text{C}$ ) differences between SPRAY-A15 and OISST (a; SPRAY-A15 minus OISST), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE and MAE (c; 0-360 $^{\circ}\text{E}$ , 40-75 $^{\circ}\text{S}$ ) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.



**Figure 7.** The 53-day average differences of total heat flux (a-c), latent heat flux (d-f), and sensible heat flux (g-i) between SPRAY-GQ and SPRAY-A15 (SPRAY-GQ minus SPRAY-A15) in Jan-Feb, 2017. The direct differences indicate sea spray-mediated heat flux differences (b, e, h), and the indirect differences indicate interfacial (bulk) heat flux differences resulted by sea spray (c, f, i). The dotted areas are statistically significant at 95% confidence level. A positive value of flux indicates an upward direction.



**Figure 8.** The same as Figure 6, but for Aug-Sep, 2018 in 0-360°E, 20-75°N.



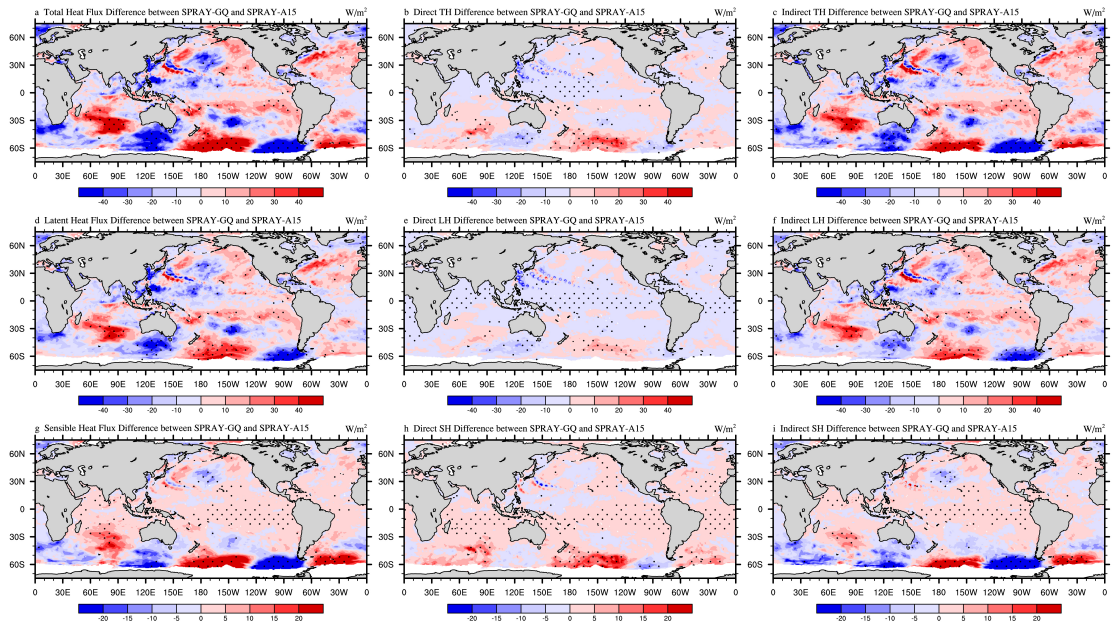
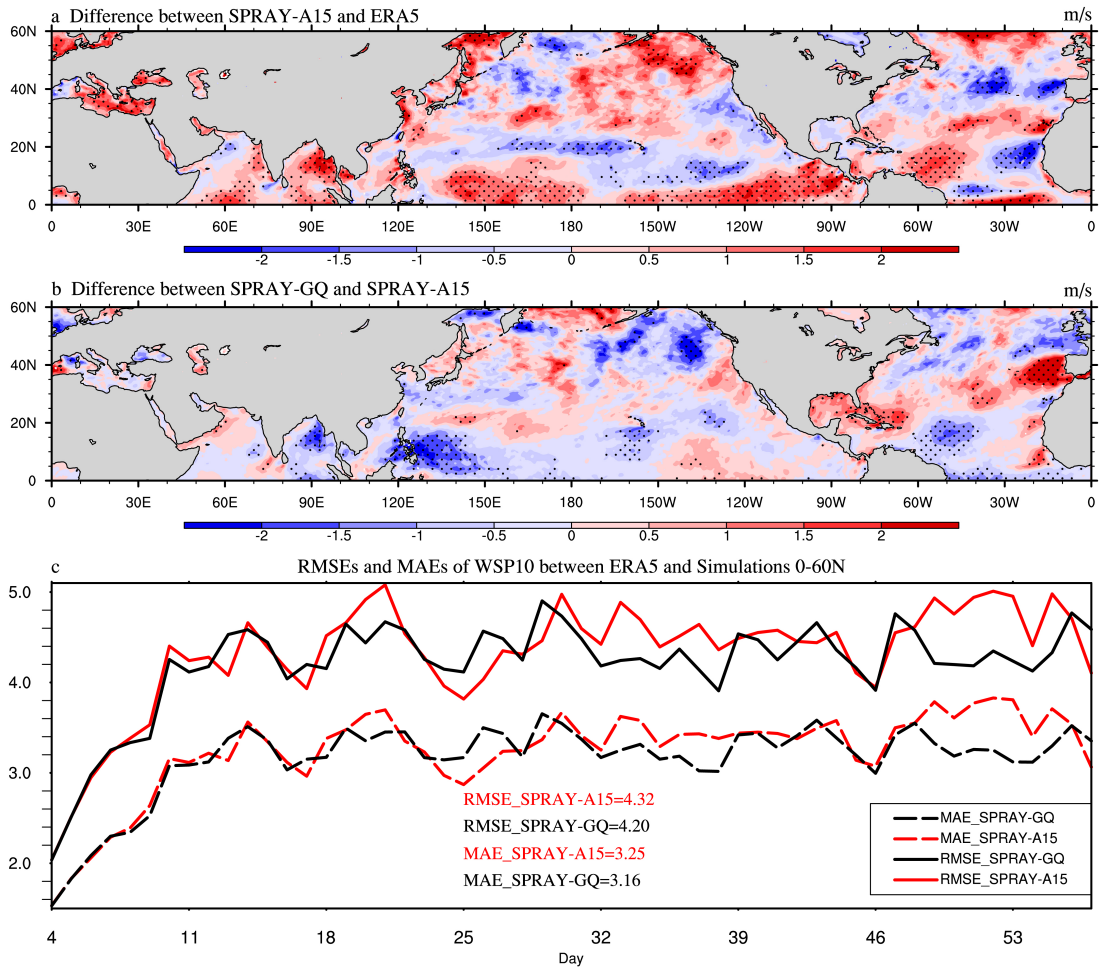
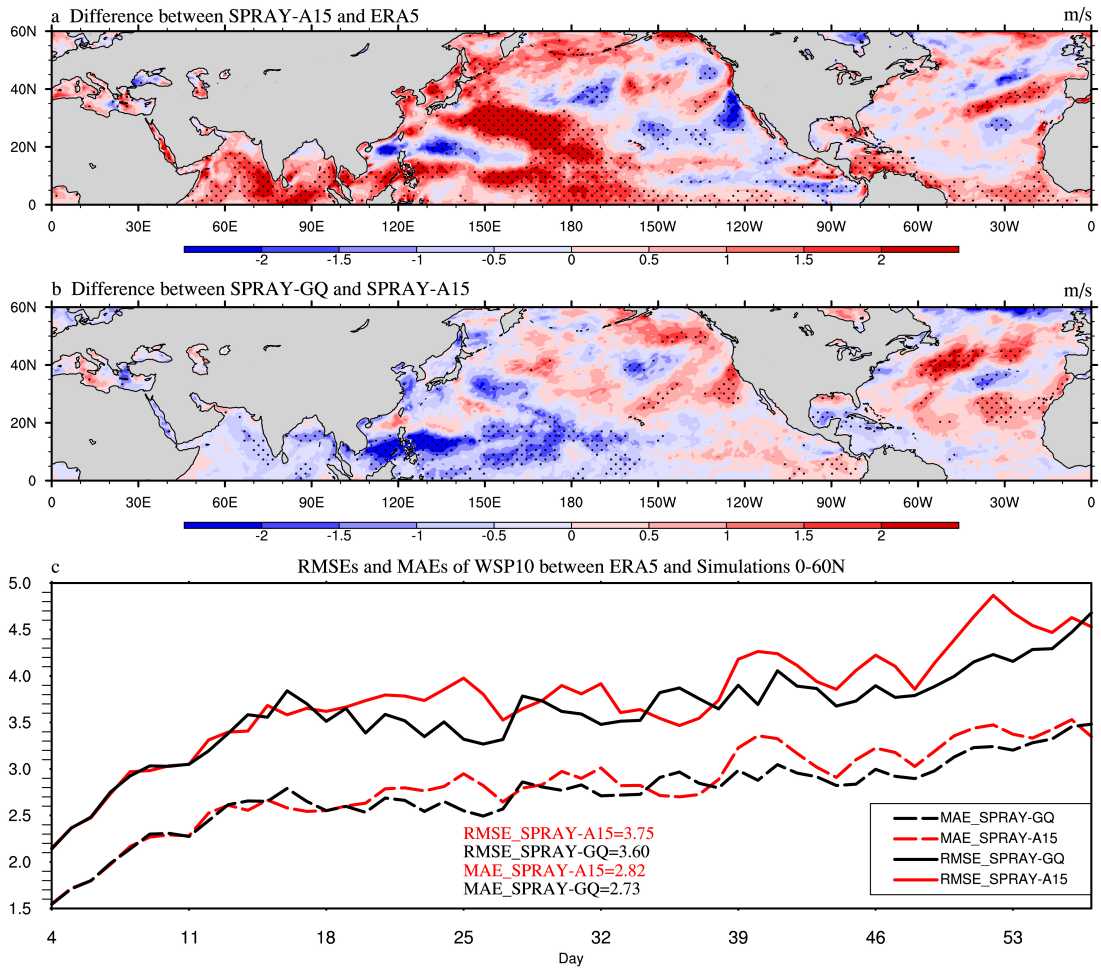


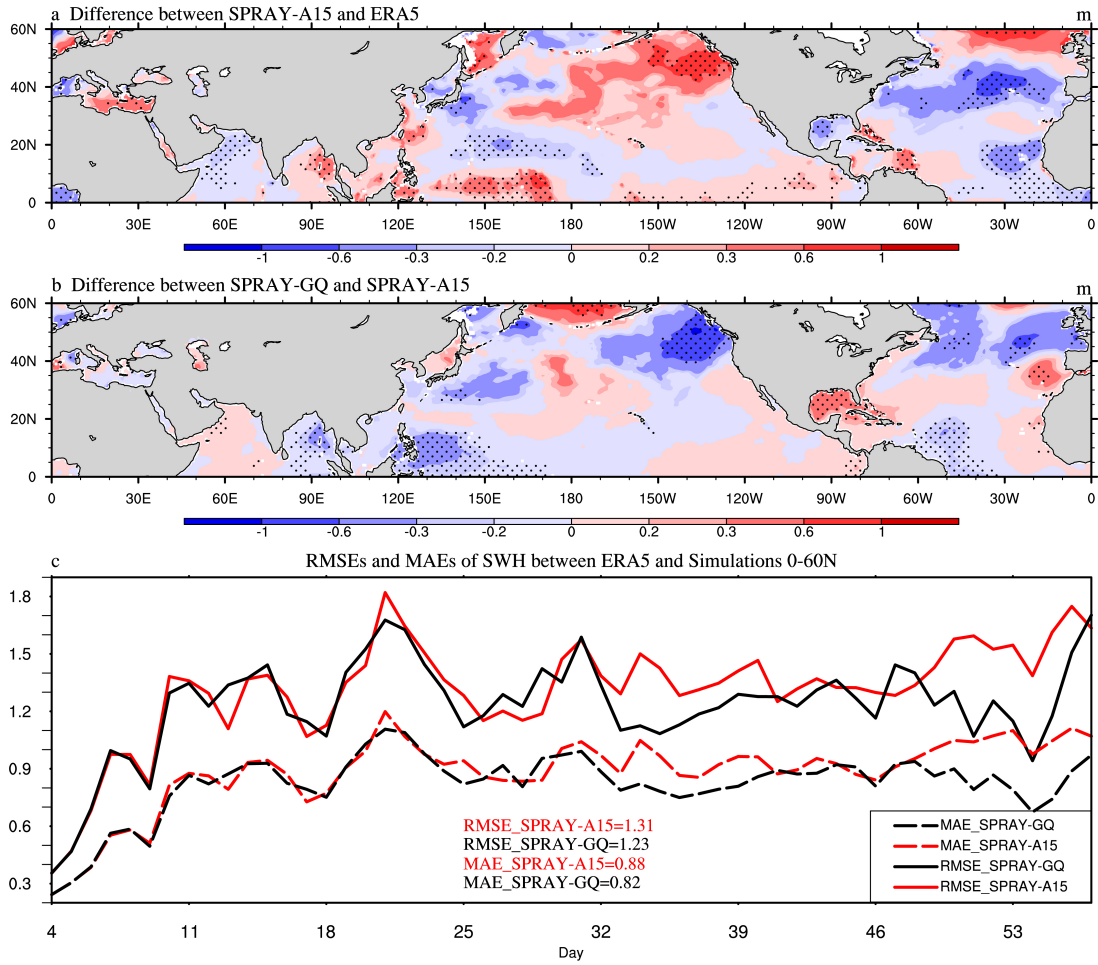
Figure 9. The same as Figure 7, but for Aug-Sep, 2018.



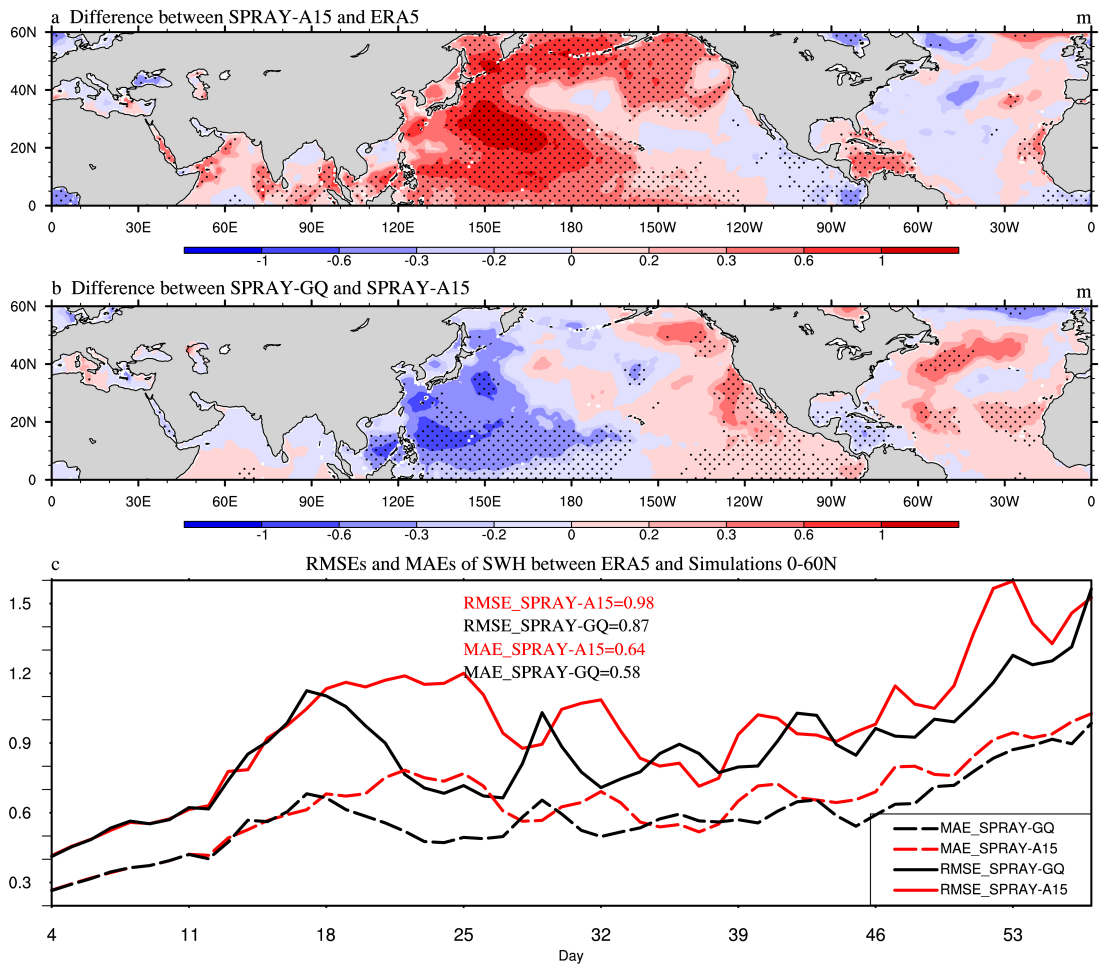
**Figure 10.** The 53-day average WSP10 (m/s) differences between SPRAY-A15 and ERA5 (a; SPRAY-A15 minus ERA5), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE and MAE (c; 0-360°E, 0-60°N) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.



**Figure 11.** The same as Figure 10, but for Aug-Sep, 2018.



**Figure 12.** The 53-day average SWH (m) differences between SPRAY-A15 and ERA5 (a; SPRAY-A15 minus ERA5), the differences between SPRAY-GQ and SPRAY-A15 (b; SPRAY-GQ minus SPRAY-A15), and the time series of domain-averaged RMSE and MAE (c; 0-360°E, 0-60°N) in Jan-Feb, 2017. The first 3-day simulation is discarded. The dotted areas are statistically significant at 95% confidence level.



**Figure 13.** The same as Figure 12, but for Aug-Sep, 2018.