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1 **Assessment of the Finite VolumE Sea Ice Ocean Model** 2 **(FESOM2.0), Part II: Partial bottom cells, embedded sea ice and** 3 **vertical mixing library CVMix**

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14 15 **Abstract**

16 The second part of the assessment and evaluation of the unstructured-mesh Finite-volumE Sea ice-Ocean
17 Model version 2.0 (FESOM2.0) is presented. It focuses on the performance of partial cells, embedded sea ice
18 and on the effect of mixing parameterisations available through the CVMix package.

19 It is shown that partial cells and embedded sea ice lead to significant improvements in the representation of
20 the Gulf Stream and North Atlantic Current as well as the circulation of the Arctic Ocean. In addition to the
21 already existing Pacanowski and Phillander (fesom_PP) and K-profile (fesom_KPP) parameterisations for
22 vertical mixing in FESOM2.0, we document the impact of several mixing parameterisations from the
23 Community Vertical Mixing (CVMix) project library. Among them are the CVMix versions of Pacanowski
24 and Phillander (cvmix_PP) and K-profile (cvmix_KPP) parameterisations, the tidal mixing parameterisation
25 (cvmix_TIDAL), a vertical mixing parameterisation based on turbulent kinetic energy (cvmix_TKE) as well
26 as a combination of cvmix_TKE and the recent scheme for the computation of the Internal Wave
27 Dissipation, Energy and Mixing (IDEMIX). IDEMIX parameterises the redistribution of internal wave
28 energy through wave propagation, nonlinear interactions and the associated imprint on the vertical
29 background diffusivity. Further, the benefit from using a parameterisation of southern hemisphere sea ice
30 melt season mixing in the surface layer (MOMIX) for reducing Southern Ocean hydrographic biases in
31 FESOM2.0 is presented. We document the implementation of different model components and illustrate their
32 behaviour. This paper serves primarily as a reference for FESOM users but is also useful to the broader
33 modelling community.

34 **1 Introduction**

35 Global unstructured-mesh ocean models start to be widely used in climate studies, including the recent
36 CMIP6 simulations (Semmler et al., 2020), although structured-mesh ocean general circulation models are
37 still more mature in terms of features, functionality and complexity due to their long development history.

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38 However, step by step, also the unstructured-mesh ocean models acquire new features and catch up in their
39 functionality. This paper continues the work by Scholz et al. (2019) in documenting the features available in
40 Finite volumE Sea ice Ocean Model version 2.0 (FESOM2.0, Danilov et al., 2017). It focuses on two
41 aspects. The first is about partial bottom cells and embedded sea ice, both of which essentially rely on the
42 Arbitrary Lagrangian Eulerian (ALE) vertical coordinates used in FESOM2.0. The second deals with mixing
43 parameterizations enabled through the use of Community Ocean Vertical Mixing (CVMix, Griffies et al.
44 2015, Van Roekel et al. 2018) package.

45 Partial bottom cells were first introduced for a finite volume model by Adcroft et al., (1997), as an attempt to
46 improve the representation of the bottom topography in general ocean circulation models. Adcroft et al.,
47 (1997) introduces partial bottom cells as a compromise solution between the less accurate but
48 computationally efficient full cell approach and the very accurate but computationally expensive shaved cell
49 approach. Partial bottom cells are implemented in FESOM2.0 by using the vertical ALE approach of
50 FESOM2.0 numerical core documented in Danilov et al. 2017.

51 Another feature made available through using ALE in FESOM2.0 is related to the sea ice-ocean interaction.
52 Naturally, sea ice, more precisely the loading of sea ice, contributes to the ocean pressure. However in many
53 ocean models, especially in the absence of surface mass fluxes or on fixed vertical grids, the loading is
54 omitted and sea ice is treated as “levitating”. The option to consider sea ice loading is now implemented into
55 FESOM2.0, which is called “embedded” sea ice and was first mentioned by Hibler et al. (1998) and later
56 further introduced by Hutchings et al. (2005) and Campin et al. (2008). They state that the advection of sea
57 ice in combination with the coupling of “embedded” sea ice through ice loading can be an important source
58 of ocean variability especially in the vicinity of ice edges (Campin et al. 2008). The implementation of
59 embedded sea ice relies on the zstar vertical-coordinate option in FESOM2 and also on the fact that in the
60 moment the sea ice component is called on each time step of the ocean model.

61 Diapycnal mixing in the ocean is an essential process that acts on the ocean stratification and the distribution
62 of heat, salt as well as passive tracers like nutrients, biological agents or CO₂. Various processes contributing
63 to diapycnal mixing can act with different magnitudes over a wide range of horizontal and vertical scales,
64 from several kilometers down to centimeters (Robertson and Dong, 2019). Due to the finite discretisation
65 scale in all ocean models, the mixing processes can not be resolved and thus must be parameterized. The
66 parameterisations of diapycnal mixing can be done in a variety of ways with different complexity, such as
67 boundary layer schemes like the K-profile parameterisation of Large et al. (1994) or turbulent closure
68 schemes like the one of Gaspar et al. 1990 and many others. A great innovation in the ocean modelling
69 community is the development of software packages that contain a variety of vertical mixing
70 parameterisations in a format that makes it easy to integrate them into existing model code (Fox Kemper et
71 al. 2019). One of these software packages is the Community Ocean Vertical Mixing package (CVMix,
72 Griffies et al. 2015, Van Roekel et al. 2018), which now also was integrated into FESOM2.0. CVMix is
73 tailored to be used in state of the art climate models to produce vertical profiles of diffusivity and viscosity

74 (Fox Kemper et al. 2019), providing a comparable mixing implementation over a wide spread of different
75 ocean models such as MOM6, POP, MPAS and ICON. Such effort makes it easier to compare these models
76 to each other. From the CVMix package we implemented the Pacanowski and Philander 1981, the K-profile
77 parameterization of Large et al. 1994 and the tidal mixing parameterisation of Simmons et al. 2004. Further,
78 the infrastructure of the CVMix library has been used to implement the turbulent kinetic energy (TKE)
79 scheme of Gaspar et al. (1990) and the scheme for Internal Wave Dissipation and Mixing (IDEMIX) of
80 Olbers and Eden (2013) in the same way as it is done in Gutjahr et al. (2020). It should be mentioned that
81 neither TKE nor IDEMIX is yet part of the official CVMix package but will hopefully be added to the
82 package in the future.

83 Beside the prime vertical mixing schemes, like the K-profile scheme, the Pacanowski and Phillander scheme
84 and others that have the purpose to create a general mixing parameterisation for the entire ocean, and vertical
85 mixing schemes like the tidal mixing scheme of Simmons et al. 2004 or IDEMIX that are used to
86 parametrize internal wave processes which then result in a heterogeneous background diffusivity, there are
87 also mixing parameterizations that aim at resolving regional processes. One of them was proposed by
88 Timmerman and Beckmann (2004). It parameterises the wind driven mixing in the Southern Ocean
89 especially when there is insufficient mixing during the melt seasons when other mixing schemes are used. It
90 is used in FESOM2.0 to improve the otherwise too low stratification in the Southern Ocean and Weddell
91 Sea.

92 The intention of this paper is to document the performance of the newly implemented features -- partial
93 bottom cells, “embedded” sea ice, the vertical mixing parameterisations that come with the implementation
94 of CMVIX and the local mixing parameterization of Timmerman and Beckmann (2004), based on comparing
95 the associated hydrographic biases, changes in vertical convection and differences in Meridional Overturning
96 Circulation, using a relatively coarse reference mesh.

97 The paper is structured as follows. First in Section 2 we describe the mesh configuration and model setup
98 used in the simulations. The description and analysis of partial bottom cells, “embedded” sea ice and vertical
99 mixing schemes is done in Section 3. A discussion and conclusion is given in Section 4.

100 **2 Model configurations**

101 We use the FESOM2.0 coarse mesh configuration core2, which is the same mesh as in part 1. It consists of
102 ~ 0.13 M surface vertices, with a nominal resolution of 1° in the bulk of the ocean, ~ 25 km north of 50° N, $1/3^\circ$
103 in the equatorial belt and slightly enhanced resolution in the coastal regions. In the vertical, 48 unevenly
104 distributed layers are used, with a vertical grid spacing stepwise increasing from 5m at the surface to 250 m
105 towards the bottom.

106 All model simulations are initialised from the Polar Science Center Hydrographic winter Climatology
107 (PHC3.0, updated from Steele et al., 2001) and forced by the CORE interannually varying atmospheric
108 forcing fields (Large and Yeager, 2009) for the period 1948-2009. For each simulation a spin-up over three

109 full CORE cycles was applied, where each subsequent cycle was initialised with the final results from the
110 preceding cycle. All modelled data shown in this work are averaged over the period 1989-2009.

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112 All model simulations except the one with the Turbulent-Kinetic-Energy (TKE) closure mixing of Gaspar et
113 al., 1990, use a non-constant latitude-dependent vertical background diffusivity with values between 10-4
114 m²/s and 10-6 m²/s, as described in Scholz et al., 2019. Further, all simulations use the Monin-Obukhov
115 length dependent vertical mixing parameterization of Timmermann and Beckmann, 2004 in the surface
116 boundary layer south of -50°S. The effects of this parameterisation on the simulated ocean state in
117 FESOM2.0 is described in section 3.4. The horizontal viscosity is computed via a modified harmonic Leith
118 approach (Fox-Kemper and Menemenlis, 2008) plus a biharmonic background viscosity (0.01 m²/s) . For
119 coarse-mesh setups, like the one used here, FESOM2.0 uses the Gent-McWilliams (GM) parameterisation
120 for eddy stirring (Gent et al., 1995; Gent and McWilliams, 1990) and we follow the implementation after
121 Ferrari et al., 2010. The isoneutral tracer diffusion (Redi, 1982) coefficient equals to that of GM, same as in
122 Scholz et al. (2019) and in previous FESOM versions (Wang et al. 2014). GM and Redi are scaled with
123 horizontal resolution with a maximum value of 3000 m²/s at 100 km horizontal resolution and change
124 linearly to zero between a resolution of 40 km and 30 km. In the vertical, they are scaled according to Ferrari
125 et al., 2010 and Wang et al., 2014. The simulations use as default the K-profile parameterisation for vertical
126 mixing (KPP, Large et al., 1994), a linear free surface (Scholz et al., 2019), levitating sea ice and a full
127 bottom cell approaches, unless otherwise stated.

128 **3 FESOM2.0 model components and evaluation**

129 **3.1 Partial bottom cells**

130 The concept of partial cells, as an attempt to improve the bottom representation in general ocean circulation
131 models was first introduced for the finite volume approach by Adcroft et al., (1997). Although an early
132 version of partial cells was developed by Cox, (1977), and used by Semtner and Mintz, (1977) and Maier-
133 Reimer et al., (1993), it has never got officially released (Griffies et al., 2000). Adcroft et al.
134 (1997) presented three different cases. The first one is the conventional full cell approach, where the depth of
135 the ocean bottom is approximated with the nearest standard depth level of the vertical model discretization.
136 The second one is the partial cell approach in which the bottom level can take any intermediate depth within
137 the cell, thus capturing water columns more accurately. In these two cases, the bottom features a “stepped”
138 topography and the jump of the steps is smaller for the partial cell approach (Adcroft et al., 1997). The third
139 case introduced by Adcroft et al., (1997) is a shaved cell approach, which assumes a constant slope within
140 each bottom cell and gives the best approximation for a continuous bottom topography. Adcroft et al.
141 (1997) showed that the shaved cell approach gives the most accurate results, but induces a significant
142 increase in computational demand, whereas the partial cell approach is a good compromise between the low

143 computational demand of the full cell approach and the increased accuracy of the shaved cell approach.
144 Hence, most ocean models (e.g. NEMO, MOM6, MPAS, POP) including FESOM2.0 went in favor of the
145 partial cell approach.

146 For the implementation of partial cells in FESOM2.0 we follow the work of Pacanowski and Gnanadesikan,
147 (1998), which implemented partial cells for the B-grid discretization in MOM2 with efforts to minimize
148 pressure gradient errors and spurious diapycnal mixing. They addressed that calculating horizontal pressure
149 gradients needs some special attention for partial cells since not all grid points within the bottom layer are at
150 the same depth. In FESOM2.0, we compute pressure gradient force based on the density Jacobian approach
151 as used by Shchepetkin, (2003) and not the pressure Jacobian approach proposed by Pacanowski and
152 Gnanadesikan, (1998). The density Jacobian approach is less prone to pressure-gradient error than using
153 pressure Jacobian, and therefore the model is more stable. Furthermore, we limited the thickness of the
154 partial bottom cell to be at least half of the full cell layer thickness to reduce the possibility of violating the
155 vertical Courant–Friedrichs–Lewy (CFL) criterion.

156 Using a B-grid like discretisation, where the scalars are located at vertices of a triangular mesh while the
157 velocities are located at the centroids of the triangular elements, makes it necessary to define the partial cells
158 at both locations. First, the partial bottom depth is defined at the centroids of the triangular elements based
159 on the real bottom topography considering the aforementioned limitation. Then, the vertex partial bottom
160 depth is derived from the deepest partial bottom of the surrounding triangular elements (see schematic
161 representation in Suppl. 1).

162 In order to demonstrate the effect of the partial cells on the simulated ocean state we performed two model
163 simulations using the full cell and partial cell approaches, respectively. We investigate, first, the temperature
164 biases of the full cell approach with respect to the data of the World Ocean Atlas 2018 (WOA18, Locarnini
165 et al., 2018; Zweng et al., 2018, in the left column of Fig. 1) and, second, the temperature differences
166 between partial cell and full cell (partial-full) averaged over five different depth ranges 0-250m, 250-500m,
167 500-1000m, 1000-2000m and 2000-4000m (in the right column of Fig. 1).

168 The full cell setup (Fig. 1, left) shows positive climatological temperature bias in the northern and southern
169 Pacific, the Atlantic equatorial ocean as well as in the central Indian Ocean through the depth ranges of 0-
170 250m, 250-500m and 500-1000m. In the same depth ranges there are also negative biases in the North
171 Atlantic (NA) subtropical gyre and in the equatorial and southern subtropical Pacific. The depth ranges of
172 250-500m and 500-1000m indicate cold biases in the Southern Ocean (SO) and around the coast of
173 Antarctica. The deeper depth ranges (1000-2000m and 2000-4000m.) indicate small negative temperature
174 biases in most of the world oceans, except for the Atlantic and Arctic Ocean (AO), which possess a small
175 warming bias in the depth ranges. The Arctic warming anomaly at these depths originates largely from a
176 vertically too much extended Atlantic water inflow branch (not shown), which is a typical feature of coarse
177 resolution models (e.g., Ilıcak et al. 2016).

178 Using partial cells (Fig. 1, right) leads to profound changes especially at the position of zonal fronts in the

179 North and South Atlantic. In the depth ranges of 0-250 m, 250-500 m and 500-1000 m in the NA, partial
180 cells lead to a cooling in the Labrador Sea (LS) and Irminger Sea (IS) as well as along the path of the Gulf
181 Stream (GS) and North Atlantic Current (NAC), except for the area around -30°W , 50°N which is
182 characterised by warming. In the upper South Atlantic (SA), partial cells lead to a northward shift of Brazil–
183 Malvinas Confluence Zone expressed by a dipole of warmer South Atlantic Current (SAC) and cooler
184 Antarctic Circumpolar Current (ACC). Further, partial cells lead to a predominant cooling in the SO Atlantic
185 sector and parts of the Indian Ocean sector, while the Pacific sector of the SO and most of the Antarctic
186 coastal areas are dominated mostly by warming anomalies. The Arctic Ocean features a slight warming
187 anomaly at all depths, except for the surface, when using partial cells instead of full cells. The table in Suppl.
188 2 shows the regional ($-80^{\circ}\text{W} < \text{lon} < 5^{\circ}\text{E}$, $35^{\circ}\text{N} < \text{lat} < 70^{\circ}\text{N}$) temperature standard deviation and root mean
189 square error with respect to WOA18, with and without partial cells. It proves that partial cell lead to a
190 significant improvement especially in the upper and intermediate ocean depth range, while the biases in the
191 very deep ocean marginally increase.

192 Fig. 2 shows the same as Fig. 1 but for salinity. Here, with respect to WOA18, the full cell run indicates a
193 generally fresher AO for the surface- and the 250-500 m depth range. Further negative salinity biases can be
194 found within the upper three depth ranges in the equatorial Pacific, north and south subtropical Atlantic, at
195 the position of the Atlantic northwest corner, northern IO as well as parts of the SO. Strong positive salinity
196 biases with full cells can be found in the surface depth range of the North Pacific and in the Chukchi- and
197 Beaufort Sea. Further positive salinity biases in the 250-500 m and 500-1000 m depth ranges are found along
198 the pathway of the Gulf Stream as well as in the equatorial Atlantic and central IO. The deep depth range of
199 1000-2000m has positive salinity anomalies in the Northern and Southern Atlantic and negative salinity
200 biases in the Mediterranean outflow branch and IO.

201 Using partial cells leads to an increase in salinity throughout all depth ranges of the AO relative to using full
202 cells. Further, a salinity increase at the position of the “cold blob”, in the GIN sea, in the eastern South
203 Atlantic and parts of the SO can be observed within the upper three depth ranges. Compared to full cells,
204 using partial cells reduces salinity along the pathway of the GS, the Antarctic Circumpolar Current (ACC) in
205 the South Atlantic and along the coast of Antarctica.

206 The differences in the horizontal velocity speed between partial and full cells (Fig. 3), for the depth ranges of
207 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m, 2000-4000 m and at the bottom, reveal that with partial
208 cells the velocity in the East Greenland Current (EGC), West Greenland Current (WGC) and Labrador
209 Current (LC) are stronger by up to 0.02 m/s through all depth ranges presented here. The upper differences
210 reveal that partial cells lead to a weakening and a slight southwards shift of the NAC between -45°W and -
211 30°W , and a more pronounced tendency towards a northwest bend of the NAC between -30°W and -15°W ,
212 which is nevertheless still too far eastward. By using partial cells the pathway of the Irminger Current (IC)
213 moves closer to the continental slope.

214 In terms of absolute northern and southern hemispheric maximum mixed layer depth (MLD), using full cell

215 (Fig. 4a and 4b), FESOM2.0 features known intensive convection in the Labrador Sea and Irminger Sea,
216 northern Greenland Sea as well as central Weddell Sea (Marshall and Schott 1999, Sallée et al. 2013,
217 Danabasoglu et al. 2014).

218 The anomalous northern and southern hemispheric maximum mixed layer depth (MLD), using partial cells
219 features a slight MLD decrease in the southern LS, IS and northern Greenland-Iceland-Norwegian (GIN)
220 Seas, and a slight MLD increase along the pathway of the IC and in the southern and central GIN Seas (Fig.
221 4c). In the southern hemisphere, partial cells have a more pronounced effect, leading to a significant, up to
222 1000 m, decrease in MLD in the central Weddell Sea (WS) and a minor increase in MLD of around 300 m
223 along the eastern continental slope of the Antarctic Peninsula.

224 The differences between using full cells and partial cells in Global-, Atlantic- and Indo-Pacific Overturning
225 Circulation (Fig. 5) are rather small with magnitudes of less than 1Sv. Both cases feature an upper AMOC
226 circulation cell of ~ 16 Sv and an Antarctic Bottom Water (AABW) cell with strength between -1 Sv and -2
227 Sv. One can summarize that partial cells lead to an improvement of the circulation pattern, especially
228 regarding the reduced zonality of the Gulf Stream and NAC branch even in rather coarse resolved
229 configurations.

230 **3.2 Embedded sea ice**

231 As described in Scholz et al. (2019), FESOM2.0 supports the full free surface formulation with two possible
232 options, zlevel and zstar (Adcroft and Campin, 2004). Both options allow for surface freshwater exchanges
233 which can modify the thickness of the surface layer and thus decrease or increase salinity in the surface
234 layer. This avoids the need of virtual salinity fluxes, which are required in the linear free surface (linfs)
235 approach when the layer thicknesses are kept fixed. Using virtual salinity fluxes has the potential to affect
236 the model integrity on long timescales and change local salinities with certain biases (Scholz et al., 2019).

237 In reality part of sea ice is embedded in the ocean with impact on the ocean pressure below. In the model,
238 when the sea ice loading is omitted, the “levitating” sea ice (Campin et al., 2008) does not impose pressure
239 on the ocean. This is the default case in the case of linfs but also applicable to zlevel and zstar. The other
240 case when ice-loading is considered has “embedded” sea ice (Rousset et al., 2015), which depresses the sea
241 surface according to its mass. Since it affects the layer thicknesses, this case is only available for the full free
242 surface cases of zlevel and zstar. Although freezing and melting have no direct effect on the oceanic
243 pressure, the divergence of the ice transport does modify the ice-loading fields and influences the hydrostatic
244 pressure (Campin et al., 2008). As mentioned by Campin et al., 2008, this effect could be compensated by
245 the divergence of the oceanic transport in the special case where sea ice and ocean velocities match, but in
246 reality sea ice and ocean velocities are not identical especially in the presence of high frequency wind
247 forcing. Therefore, sea ice dynamics in combination with the ice-loading coupling can be a source of oceanic
248 variability especially near the ice-edge where ice divergence/convergence is large (Campin et al., 2008).
249 However, using embedded sea ice harbours the risk that the amount of sea ice loading due to excessive

250 accumulation and the resulting depression in the surface elevation may result in a depletion of the surface
251 layer thickness, when the zlevel option is used, where only the surface layer is allowed to change. To avoid
252 this issue, we limit in FESOM2.0 the maximum ice loading to a sea ice height of 5m when the zlevel option
253 is used. In case of using zstar, the problem is less severe, since here the change in elevation is distributed
254 over all vertical layers, except for the bottom one. This makes zstar to be the recommended option when
255 using embedded sea ice, as also stated by Campin et al., 2008.

256 To show the effect of embedded sea ice on the simulated ocean state, two simulations were carried out using
257 the zstar option of FESOM2.0, one with levitating (omitting the effect of sea ice loading on ocean pressure)
258 the other with embedded sea ice (including the effect of sea ice loading on ocean pressure).

259 Fig. 6 shows the sea ice concentration (SIC) for March and September in the levitating sea ice case and the
260 difference between the embedded and levitating sea ice cases. Superimposed are the simulated (solid) and
261 observed (dashed, Cavalieri et al., 1996) contour line of the 15% sea ice extent. The northern hemispheric
262 March sea ice edge (Fig. 6a) shows a good agreement with observational data for the LS, IS and Bering Sea
263 but reveals a too far southwards extension in the Greenland Sea and Barents Sea. The simulated northern
264 hemispheric (September) sea ice extent (Fig. 6b) is larger than the observations. The southern hemispheric
265 (March) sea ice extent is underestimated in the simulation, while the simulated southern hemispheric
266 (September) sea ice extent is in good agreement with the observation.

267 Using the embedded sea ice leads to an increase in the SIC in the Greenland Sea by around 6% in March. In
268 September, embedded sea ice leads to positive SIC anomalies in the eastern- and negative anomalies in the
269 western AO. In the southern hemisphere, embedded sea ice leads to a heterogeneous pattern of small positive
270 and negative changes along the sea ice edge. The corresponding results for the sea ice thickness are shown in
271 Suppl. 4, here both March and September northern hemisphere sea ice thickness anomalies reveal a dipole
272 like pattern with reduced sea ice thickness in the area of the Beaufort gyre and increased sea ice thickness in
273 the eastern AO and region of the transpolar drift when using embedded sea ice.

274 Regarding the changes in the ocean, Fig. 7 shows the temperature (left column) and salinity (right column)
275 differences between the embedded and levitating (embedded minus levitating) sea ice cases averaged over
276 the depth ranges 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m and 2000-4000 m. The temperature and
277 salinity differences reveal that a significant warming of up to 0.5°C and a salinification of up to 0.10 psu
278 occurs in almost the entire AO due to embedded sea ice, except in a thin stripe along the eastern continental
279 shelf of the AO that shows negative anomalies in the depth ranges of 0-250 m, 250-500 m and 500-1000 m.
280 The changes in temperature and salinity can be explained by the changes in ocean currents. Figure 8 depicts
281 the speed of the horizontal currents in levitating (1st column) and embedded (2nd column) sea ice cases as
282 well as their difference (3rd column). Using embedded sea ice leads to an increase in the speed along the
283 entire boundary current of the Eurasian Basin and along the Lomonosov Ridge, that can be found in all three
284 presented depth ranges. The increase in the velocity of the boundary currents, caused by using embedded sea
285 ice, leads to an enhanced heat and salt transport in the Atlantic water layer originating from the Fram Strait,

286 which results in a warmer and more saline intermediate depth in the Arctic Ocean. The increase in
 287 temperature and salinity, especially in the surface layers of the AO using embedded sea ice reduces existing
 288 local biases (see Fig. 1 and Fig. 2) that occur when using levitating sea ice. On the whole it can be stated that
 289 using embedded sea ice instead of levitating sea ice has some significant effect on the ocean dynamics of the
 290 AO, but no effect in the Southern Ocean or Antarctic marginal seas.

291 **3.3 Implementation and evaluation of vertical mixing schemes**

292 Besides the already existing Pacanowski and Philander (fesom_PP, Pacanowski and Philander, 1981) and
 293 MOM4 K-profile (fesom_KPP, Large et al., 1994) vertical mixing parameterizations in FESOM2.0 that were
 294 based on the implementation in the predecessor version FESOM1.4, the vertical mixing parameterizations of
 295 the Community Vertical Mixing (CVMix, Griffies et al., 2015) project have been now added as well. This
 296 includes the CVMix vertical mixing of: Pacanowski and Philander (cvmix_PP), the POP (Parallel Ocean
 297 Program) K-profile (cvmix_KPP) parameterization, the tidal mixing parameterization of Simmons et al.,
 298 (2004) (cvmix_TIDAL) and the turbulent kinetic energy (cvmix_TKE) mixing of (Gaspar et al., 1990) in
 299 combination with the Internal Wave Dissipation, Energy and Mixing (IDEMIX) parameterization (Olbers
 300 and Eden, 2013 and Eden and Olbers, 2014) . Although cvmix_TKE and IDEMIX are not yet a part of the
 301 CVMix project, they use its libraries in the background and will join the project in the future. CVMix is used
 302 by a variety of models, such as MOM6, POP, MPAS or ICON and provides an opportunity of a cross model-
 303 spanning vertical mixing implementation that allows for an enhanced cross-model intercomparison.

304

305 **3.3.1 Comparison of cvmix_KPP, cvmix_PP with previous fesom_KPP and fesom_PP** 306 **implementation**

307 In FESOM2.0 we implemented cvmix_PP and cvmix_KPP in addition to its previous implementations
 308 fesom_PP and fesom_KPP that were adopted from FESOM1.4. The difference between cvmix_PP and
 309 fesom_PP lies in the background coefficient for viscosity which is considered in cvmix_PP but not in
 310 fesom_PP when computing the diffusivity, following the experience with FESOM1.4 which did not need to
 311 be more diffusive. The difference between cvmix_KPP and fesom_KPP lies mainly in the treatment of the
 312 squared velocity shear and buoyancy difference with respect to the surface, although CVMix does not make
 313 any specific requirements here. In cvmix_KPP we synchronized the implementation with our project partner
 314 models MPIOM and ICON-o and compute the cvmix_KPP surface quantities by averaging over 10% of the
 315 boundary layer depth as recommended by Griffies et al. 2015 while in fesom_KPP the surface values are
 316 linked to the first layer in the model which was inspired by the implementation in the older MOM4.

317 Suppl. 5 displays the temperature (1st and 2nd column) and salinity (3rd and 4th column) biases of fesom_KPP
 318 with respect to WOA18 (1st and 3rd column) as well as the difference between fesom_PP and fesom_KPP (2nd
 319 and 4th column). In the surface depth range the climatological temperature and salinity biases of fesom_KPP
 320 with respect to WOA18 are largely negative in the tropical and subtropical Pacific, North and South Atlantic

321 as well as AO, and positive in tropical Atlantic and Indian Ocean, Southern Ocean, Labrador Sea, GIN Seas
 322 and the marginal seas of the North Pacific. The subsurface depth ranges of 250-500 m and 500-1000 m are
 323 dominated by largely positive temperature biases, except for the Southern Ocean, the pathway of the GS and
 324 NAC and the northern Indian Ocean. The salinity biases in the 250-500 m and 500-1000 m depth range
 325 preserve largely the pattern from the surface layer except for an increasing and expanding positive salinity
 326 bias in the tropical Atlantic, reduced positive salinity biases in the Indian Ocean and northern Pacific as well
 327 as reduced negative biases in the Arctic Ocean. The 1000-2000 m depth range features small warm biases in
 328 the AO and GIN seas, positive temperature and salinity biases in the LS and the South Atlantic, negative
 329 temperature and salinity biases in the eastern North Atlantic (possibly due to weak mediterranean outflow)
 330 and small negative temperature and salinity biases in the Pacific and Indian Ocean. The very deep depth
 331 range of 2000-4000 m reveals rather small warming bias for the entire Atlantic and SO.

332 fesom_KPP and fesom_PP produced rather small temperature and salinity differences (note different
 333 colorbar ranges between 1st & 2nd and 3rd & 4th column), considering the biases with respect to the WOA18
 334 climatology. Employing fesom_PP has the tendency to be slightly warmer almost everywhere in the
 335 subsurface layers and slightly saltier especially in the AO and fresher in the surface layer of the subtropical
 336 and equatorial ocean compared to using fesom_KPP. Looking at the maximum MLD between fesom_PP and
 337 fesom_KPP (Suppl. 6) it can be seen that fesom_PP has the tendency to produce an up to 500m shallower
 338 deep convection in LS and WS when compared to fesom_KPP.

339 Fig. 9 shows the difference in temperature (1st column), salinity (2nd column) and vertical diffusivity (3rd
 340 column) between cvmix_KPP and fesom_KPP (cvmix_KPP minus fesom_KPP) averaged over five different
 341 depth ranges. The last column presents the fesom_KPP vertical diffusivity as a reference. Also here, the
 342 temperature and salinity differences are rather small compared to the climatological biases shown in Suppl.
 343 5. cvmix_KPP has the tendency to produce in the marginal seas of the AO a slightly fresher surface ocean,
 344 while the central AO shows an increase in salinity by ~ 0.1 psu.

345 The absolute value of the vertical diffusivity in fesom_KPP is larger than that in cvmix_KPP in the surface
 346 layers as well as in regions of unstable stratification (buoyancy frequency < 0), superimposed on a non-
 347 constant background diffusivity as described in Scholz et al., 2019. The different treatment of the squared
 348 velocity shear and buoyancy difference with respect to the surface in cvmix_KPP leads to a reduction of the
 349 vertical diffusivity (3rd column) in the Labrador and Irminger Seas and to an increase in the AO locally by up
 350 to one order of magnitude (especially in the deep ocean).

351 The differences in MLD between fesom_KPP and cvmix_KPP are presented in Fig. 10, where and a) and b)
 352 show the absolute MLD value for fesom_KPP in the northern hemisphere in March and in the southern
 353 hemisphere in September respectively. Fig. 10 c) and d) display the corresponding anomalies between
 354 cvmix_KPP and fesom_KPP (cvmix_KPP-fesom_KPP). The absolute MLD values for fesom_KPP in March
 355 show high values of up to 3300 m in the entire LS and parts of the Irminger Sea, intermediate values of up to
 356 2000 m in the northern and eastern GIN seas and values of ~ 900 m along the eastern continental slope of the

357 North Atlantic. In the southern hemisphere in September, fesom_KPP simulates a large MLD of ~2500 m in
 358 the central Weddell Sea and weaker MLD of ~500 m in the band of the Antarctic Circumpolar Current
 359 (ACC). Compared to the fesom_KPP, cvmix_KPP leads to a ~200 m weaker MLD in the boundary currents
 360 of the LS, southern LS and along the northeastern continental slope of the GIN seas, and slightly larger MLD
 361 values in the IS and southwestern GIN Seas. The KPP ocean boundary layer depth (OBLd, Large et al. 1994)
 362 for fesom_KPP and the difference in OBLd between cvmix_KPP and fesom_KPP is additionally presented
 363 in Suppl. 7, where it is shown that cvmix_KPP produces a around 150 m shallower OBLd which is largely
 364 attributed to the different treatment of the surface quantities by averaging over 10% of the boundary layer
 365 depth.

366 Fig. 11 presents the differences in temperature (1st column), salinity (2nd column) and vertical diffusivity K_v
 367 (3rd column) between cvmix_PP and fesom_PP (cvmix_PP minus fesom_PP) as well as the absolute values
 368 of vertical diffusivity for fesom_PP (4th column). For the upper two surface depth ranges, cvmix_PP shows
 369 an overall small warming anomaly, except for the Gulf of Guinea in the 250-500 m depth range where the
 370 anomaly is negative. The salinity with cvmix_PP has overall slight positive anomalies, except for coastal
 371 Arctic areas and the Gulf of Guinea which indicate a slight freshening anomaly when compared to
 372 fesom_PP. The depth ranges below 500 m show no significant temperature or salinity differences between
 373 cvmix_PP and fesom_PP. The absolute value of K_v in fesom_PP also shows larger values all over the
 374 surface layer as well as in the areas of unstable stratification similar to fesom_KPP, but with a lower
 375 magnitude and a more extended region of increased K_v in the LS and IS. The K_v difference between
 376 cvmix_PP and fesom_PP shows sporadically positive values along the coastal Arctic Ocean and in parts of
 377 the North Atlantic and GIN Seas. As one would expect, cvmix_PP has an order of magnitude larger values in
 378 the very deep ocean layer where the background viscosity enters the computation of K_v in cvmix_PP.

379 Fig. 12 presents the absolute and anomalous MLD between fesom_PP and cvmix_PP. The MLD in
 380 fesom_PP in March is deep in the entire LS and in parts of the IS, but slightly weaker and less spatially
 381 extended when compared to fesom_KPP (Fig. 10). The MLD in the GIN seas is very similar between
 382 fesom_PP and fesom_KPP. In the southern hemisphere the September MLD in fesom_PP shows a pattern in
 383 the central Weddell Sea which is similar to that in fesom_KPP, but shallower by ~500 m. The MLD
 384 difference between cvmix_PP and fesom_PP in the northern hemisphere indicates a very heterogeneous
 385 pattern for the North Atlantic and in the southern hemisphere an up to ~150 m deeper MLD in the Weddell
 386 Sea MLD for cvmix_PP compared to fesom_PP. Overall, the difference in the simulation results induced by
 387 the difference in the two implementations of mixing schemes is generally small when considering the model
 388 biases relative to observations.

389 **3.3.2 Effects of tidal mixing parameterization of Simmons et al. (2004)**

390 The tidal mixing parameterization of Simmons et al., (2004) provided by CVMix has been added to
 391 FESOM2.0. This mixing parameterization takes into account effects from internal wave generation due to
 392 tides over rough bottom topography. The breaking of internal waves in the vicinity of topographic features

excites small-scale turbulence and leads to an enhanced vertical mixing. The tidal mixing parameterization uses a two dimensional map of tidal energy dissipation flux due to bottom drag and energy conversion into internal waves from Jayne and St. Laurent, (2001). It is transformed under consideration of a vertical redistribution function, the modelled buoyancy frequency and a tidal dissipation efficiency and mixing efficiency into a 3D map of diapycnal tidal vertical mixing, which is added to a primary vertical mixing scheme like PP, KPP or TKE. To show the effect of the tidal mixing parameterization we conducted a simulation using both `cvmix_KPP` and the tidal vertical mixing (`cvmix_KPPTIDAL`). This simulation will be compared with a control run with `cvmix_KPP` in which the tidal mixing is not considered. The differences in temperature (1st column), salinity (2nd column) and vertical diffusivity K_v (3rd column) between `cvmix_KPPTIDAL` and `cvmix_KPP` averaged over five different depth ranges are presented in Fig. 13. The last column of Fig. 13 shows the `cvmix_KPP` K_v as a reference. The temperature anomalies of the upper three depth ranges indicate that `cvmix_KPPTIDAL` is colder especially in the marginal seas of the North Pacific, e.g. Sea of Japan, Sea of Okhotsk and Bering Sea, within the branch of the Gulf Stream (GS) and North Atlantic Current (NAC) as well as in the GIN- and Barents Seas. The Arctic Ocean shows a cooling anomaly for the 500-1000 m and 1000-2000 m depth range. In the southern hemisphere the entire Southern Ocean is slightly colder when including the tidal vertical mixing. The tropical and subtropical ocean indicates a slight warming for `cvmix_KPPTIDAL`.

The salinity anomalies between `cvmix_KPPTIDAL` and `cvmix_KPP` show a pattern similar to that of the temperature, with a freshening in the marginal seas of the North Pacific, GS, NAC, GIN- and Barents Seas as well as for the Southern Ocean. The upper depth range indicates an increase in salinity for the AO, while the subsurface depth ranges show an AO freshening when including the tidal mixing. The tropical and subtropical ocean shows largely an increase in salinity under `cvmix_KPPTIDAL`.

The difference in vertical diffusivity shows for `cvmix_KPPTIDAL` an increase by an order of magnitude along the sloping bottom topography (e.g. the Midatlantic Ridge or Indonesian region) but also along the continental shelf regions which is induced by the tidal vertical mixing parameterization. On top of that the central AO shows a reduced vertical diffusivity by at least an order of magnitude for the 250-500 m, 500-1000 m and 1000-2000 m depth ranges, which comes from a change in local hydrography when including the tidal vertical mixing parameterization and the associated difference in the KPP mixing scheme.

To further understand the effect of the tidal vertical mixing, Fig. 14 shows the global zonal mean temperature and salinity differences between the case of `cvmix_KPP` and the WOA18 (a, c) and the differences between `cvmix_KPPTIDAL` and `cvmix_KPP` (b, d). The temperature of `cvmix_KPP` shows a rather strong warming bias until 1000 m for the tropical and subtropical ocean as well as until ~2500 m for the ocean north of 50°N with respect to WOA18 (Fig. 14a). The deep ocean features small negative temperature anomalies for the tropical and subtropical ocean and slightly positive biases for the deep SO, when compared to WOA18. The salinity biases of the `cvmix_KPP` case (Fig. 14c) indicate a more heterogeneous but nevertheless similar picture. Also here positive salinity biases can be seen in the tropical and subtropical ocean until around 1000m as

well as until ~2500m for the ocean north of 50°N. Looking at the temperature and salinity difference between `cvmix_KPPTIDAL` and `cvmix_KPP`, it can be seen that the tidal mixing of Simmons et al., (2004) leads to a cooling and freshening of the Southern Ocean and the ocean north of 50°N as well as a warming and salinification for the tropical and subtropical ocean until around 1500m. The deep ocean experiences a general slight warming and freshening due to the inclusion of the tidal mixing parameterization. In general one can summarize that the tidal mixing parameterization of Simmons et al., (2004) helps to improve some of the biases with respect to WOA18. The last panel in Fig 14e shows the global zonal averaged vertical diffusivity profiles between `cvmix_KPPTIDAL` and `cvmix_KPP` and reveals a general strong increase in K_v along the continental slope in the southern ocean, in the northern hemisphere north of 50°N as well as in the deep ocean interior.

To illustrate the effect of Simmons et al., (2004) tidal mixing parameterization onto the MLD, Fig. 15 presents the northern hemisphere (March) (a) and southern hemisphere (September) (b) MLD in the case of `cvmix_KPP`, and the difference in MLD between `cvmix_KPPTIDAL` and `cvmix_KPP` also for northern hemisphere (March) (c) and southern hemisphere (September) (d). In the northern hemisphere in March, tidal mixing leads to an increase in the MLD within the boundary currents of the LS, southern and eastern GIN Seas as well as in the Sea of Okhotsk. In the southern hemisphere (September), tidal mixing leads to a significant ~1000 m increase in the Weddell Sea MLD. This significant increase originates largely from enhanced mixing of very cold surface waters along the continental slope of the Weddell Sea due to the tidal mixing parameterization. Suppl. 8 shows the KPP OBLd for `cvmix_KPP` and the difference in OBLd between `cvmix_KPP` with and without the tidal mixing of Simmons et al., (2004). It shows that with `cvmix_KPPTIDAL` the OBLd enhances especially in the western LS.

450

3.3.3 Effects of Turbulent-Kinetic-Energy (TKE) mixing parameterisation

More elaborate parameterizations of the vertical mixing in the ocean can be achieved by using closure schemes of turbulent kinetic energy (TKE) and the associated turbulent mixing within the mixed layer and below. One of these turbulent closure schemes is by Gaspar et al. (1990) that has been implemented via CVMix (`cvmix_TKE`) into FESOM2.0 based on the work of Eden et al. (2014) and Gutjahr et al. (2020). The turbulence closure scheme requires the solving of the second-order equation for TKE which is closed by connecting the vertical diffusivity with the turbulent kinetic energy and a length scale for its dissipation (Eden et al., 2014). For the background diffusivity we do not use the latitude and depth dependent background diffusivity as in the previous mixing schemes. Instead, a constant minimum value of TKE is assumed, which takes into account the ocean interior mixing by internal wave breaking. To understand the effect of `cvmix_TKE` on oceanic hydrography, Fig. 16 presents the temperature and salinity biases of `cvmix_TKE` with respect to WOA18 (1st and 3rd column). To relate `cvmix_TKE` to the other vertical mixing schemes (e.g. KPP), the temperature and salinity differences between `fesom_KPP` and `cvmix_TKE` (2nd and 4th column) are shown as well. In general, the `cvmix_TKE` temperature and salinity biases with respect to

465 WOA18 look largely very similar to the biases of fesom_KPP shown in Supp2. 1 (1st and 3rd column) in
466 terms of the spatial patterns. A closer inspection of temperature and salinity differences between cvmix_TKE
467 and fesom_KPP (Fig. 16, 2nd and 4th column) reveals that cvmix_TKE produces an up to 0.5°C colder ocean
468 within the 0-250 m, 250-500 m and 500-1000 m depth ranges in most of the ocean, a strong warming along
469 the pathway of the NAC and the southern polar front in the South Atlantic, and small warming biases in the
470 AO and SO. The salinity differences between cvmix_TKE and fesom_KPP indicate a salinification of the
471 AO throughout the 0-250 m, 250-500 m and 500-1000 m depth ranges, but most pronounced in the surface
472 depth range. The surface saline bias largely stems from reduced mixing under sea ice, which shields the
473 ocean from the wind stress, a large source term of TKE. Furthermore, there are positive salinity anomalies in
474 the North Atlantic (in the pathway of the GS and NAC), North Pacific and Southern Ocean, and largely
475 negative salinity anomalies in the southern hemisphere. The temperature and salinity differences between
476 cvmix_TKE and fesom_KPP in the depth ranges of 1000-2000 m and 2000-4000 m are rather marginal. It
477 should be mentioned that a part of the anomalies described here could also be attributed to the different
478 treatment of the background diffusivity. fesom_KPP takes a latitude and depth dependent value (Scholz et
479 al., 2019), while cvmix_TKE assumes a constant value of minimum TKE on the surface ($10e-4 \text{ m}^2/\text{s}^2$) and
480 for the interior mixing ($10e-6 \text{ m}^2/\text{s}^2$).

481 **3.3.4 Effects of energy consistent combination of TKE with the Internal Wave Dissipation** 482 **Energy and Mixing (IDEMIX) parameterisation**

483 Besides the standard implementation of vertical background diffusivity in cvmix_TKE using a constant
484 minimum value of TKE to parameterize the effect of breaking of internal waves, cvmix_TKE also allows for
485 the usage of a more sophisticated parameterization of internal wave breaking when combined with the
486 IDEMIX parameterization (Olbers and Eden, 2013; Eden et al., 2014) which describes the energy transfer
487 from sources towards sinks of internal waves by using a radiative transfer equation of weakly interacting
488 internal waves. The resulting dissipation of energy is then treated as a source term in the turbulent kinetic
489 energy balance equation leading at the end to an energetically more consistent interpretation of the internal
490 ocean mixing process (Eden et al., 2014; Gutjahr et al., 2020). Thereby, IDEMIX solves for the propagation
491 of low-mode internal waves far from their generation sites, which is considered by Fox-Kemper et al., (2019)
492 as one of the most difficult components of the internal wave energy budget. Different from the tidal mixing
493 parameterization of Simmons et al., (2004), which only represents the generation of internal waves by
494 barotropic tides and their breaking at rough topography, IDEMIX considers both the internal waves due to
495 barotropic tides and the internal waves induced by wind-stress fluctuations and exiting at the base of the
496 mixed layer (Gutjahr et al., 2020). The combination of cvmix_TKE and IDEMIX to improve the energetic
497 consistency of ocean models is a rather new approach in the modelling community. It has been evaluated for
498 stand-alone ocean models (Eden et al., 2014; Nielsen et al., 2018; Pollmann et al., 2017) and coupled models
499 (Nielsen et al., 2019). Further, the computed TKE dissipation rates from IDEMIX have been evaluated
500 against observational Argo float-derived dissipation rates by Pollmann et al. (2017) and have been found to

501 be in good agreement (Gutjahr et al., 2019). In this part of the FESOM2 documentation, two FESOM2.0
 502 simulations with `cvmix_TKE`, one with and one without the usage of IDEMIX, are compared to assess the
 503 effect of IDEMIX on the modelled hydrography.

504 Fig. 17 presents the temperature (1st column), salinity (2nd column) and vertical diffusivity (3rd column)
 505 differences between `cvmix_TKE` with IDEMIX versus without it, averaged over five different depth layer
 506 ranges. As a reference the vertical diffusivity of `cvmix_TKE` without IDEMIX is also shown in the 4th
 507 column. The temperature differences indicate a clear warming of all equatorial and mid-latitude oceans
 508 and a cooling in the AO, SO and the marginal seas of the North Pacific throughout almost all the depth
 509 ranges, when `cvmix_TKE` is used with IDEMIX. There is a particularly strong warming in the surface and
 510 subsurface depth range of the North Atlantic, in the subsurface depth range of the south Pacific and in the
 511 deeper depth ranges of the Indian Ocean. The salinity differences (2nd column) have a similar spatial pattern,
 512 showing a rather strong salinification of the equatorial and mid-latitude global oceans and a freshening of
 513 the AO, SO and North Pacific from the surface to 500-1000 m depth range. The depth ranges below indicate
 514 a predominant general freshening almost everywhere, except for the Mediterranean outflow and Indian
 515 Ocean which indicate a slight salinification. The differences in the vertical diffusivity between `cvmix_TKE`
 516 with and without IDEMIX are only very small in the upper layer depth range. Therefore, all subsurface depth
 517 layers indicate considerable positive vertical diffusivity differences by up to two orders of magnitude
 518 especially along all major topographic features as well as in the SO. This shows in particular how IDEMIX
 519 parameterizes the vertical mixing due to the breaking of upwards propagating internal wave excited by
 520 barotropic tides along the ocean bottom topography but also the vertical mixing related to the internal wave
 521 breaking of downward propagating internal waves radiated out of the mixed layer like e.g. in the SO.

522 Fig. 18 presents the global zonal mean temperature and salinity differences of `cvmix_TKE` with respect to
 523 the WOA18 (a, c) as well as the temperature, salinity and vertical diffusivity differences between
 524 `cvmix_TKEIDEMIX` and `cvmix_TKE` (b, d, e). The zonal mean temperature biases of `cvmix_TKE` with respect
 525 to WOA18 (Fig. 18a) are positive for the upper SO, the equatorial and mid-latitude oceans between 500m
 526 until 1000m, and the high-latitude ocean north of 60°N where the warming bias extends nearly from the
 527 surface until a depth of ~2500m. A rather weak warming bias is also present for the very deep >2500m SO.
 528 General cooling biases can be seen for the equatorial and mid-latitude surface oceans, between a depth of
 529 ~1000m to 2000m as well as for the very deep ocean. The salinity biases for `cvmix_TKE` (Fig. 18c) show too
 530 high salinities for the high-latitude ocean north of 40°N and for the surface SO. Small salinity biases can be
 531 found in the equatorial and mid-latitude surface layers as well as around 40°N between ~1000 and 3000
 532 m.

533 The temperature differences between `cvmix_TKE` with and without IDEMIX (Fig. 18b) shows that the
 534 IDEMIX leads to a general warming of the equatorial and mid-latitude oceans especially between ~500 m
 535 and ~2000 m, but a cooling in the northern and southern high-latitude oceans. The salinity differences
 536 between `cvmix_TKE` with and without IDEMIX reveal a similar pattern with an increase in salinity for the

537 equatorial and mid-latitude ocean from the surface until a depth ~ 2000 m and a freshening bias in the same
 538 depth range for the high-latitude oceans and for the entire deep ocean as well.

539 The corresponding vertical diffusivity difference is shown in Fig. 18e. There, using IDEMIX results in an
 540 increase in vertical diffusivity along the bottom topographic slopes in the SO and north of 50°N until 70°N .
 541 Further, an increase in vertical diffusivity can be observed for almost the entire upper ocean until ~ 2000 m
 542 with deeper reaching positive anomalies between $-60^\circ\text{S} - 30^\circ\text{S}$ and $30^\circ\text{N} - 50^\circ\text{N}$. A reduction of the vertical
 543 diffusivity can be observed for the entire AO from the surface to bottom, for the equatorial and mid-
 544 latitude deep ocean >3000 m as well as for the deep (>4000 m) SO.

545 The effect of IDEMIX on the MLD is presented in Fig. 19, which shows the northern hemisphere (March) a)
 546 and southern hemisphere (September) b) cvmix_TKE MLD and the corresponding anomalies between
 547 cvmix_TKE with and without IDEMIX. It indicates that the use of IDEMIX leads to an increase in northern
 548 hemisphere MLD within the boundary currents of the LS by up to ~ 1000 m and in the southeastern GIN Seas
 549 by up to ~ 1800 m. In the southern hemisphere (September), IDEMIX leads to a significant increase of the
 550 Weddell Sea MLD up to ~ 1800 m. We observe that using $\text{cvmix_KPP}_{\text{TIDAL}}$ or $\text{cvmix_TKE}_{\text{IDEMIX}}$ the model
 551 cannot maintain the upper halocline in the Weddell Sea. Hence the warm water that shall stay deep is
 552 exposed to the surface and the ocean loses heat. It can be well seen from Fig. 14.b and 18.b as blobs of
 553 negative temperature differences beneath the surface. As a consequence, the enlarged MLDs in the Weddell
 554 Sea appear. We therefore recommend to combine $\text{cvmix_KPP}_{\text{TIDAL}}$ or $\text{cvmix_TKE}_{\text{IDEMIX}}$ with the partial
 555 bottom cell approach, which has a partly compensating effect on the stratification in the Weddell Sea (see
 556 section 3.1 and Suppl. 3) and leads to a reduction of the MLD (Suppl. 9) due to improvements of the current
 557 circulation in the Weddell Sea.

558 **3.4 Implementation of Monin-Obukhov length dependent vertical mixing**

559 In this section the effect of the Monin-Obukhov length vertical mixing (MOMIX) of Timmermann and
 560 Beckmann (2004) in FESOM2.0 is discussed. In an attempt to decrease the climatological biases especially
 561 in the Southern Ocean, which were otherwise prone to significant cooling and salinification (not shown),
 562 MOMIX has been implemented into FESOM2.0 as well. MOMIX serves as a parameterisation of the wind
 563 driven mixing in the Southern Ocean, effective especially in the melting season, which helps to reduce
 564 winter deep convection in the Weddell Sea, thus affecting the basin wide ocean- and meridional overturning
 565 circulation (Timmermann and Beckmann, 2004). MOMIX computes the Monin-Obukhov length based on
 566 heat flux, freshwater flux, wind stress, sea ice concentration and sea ice velocity following the approach of
 567 Lemke (1987), and subsequently increases the vertical diffusivity within the Monin-Obukhov length to a
 568 value of $0.01\text{m}^2/\text{s}$.

569 Due to its success in reducing the aforementioned mean biases, MOMIX is applied at the moment in
 570 FESOM2.0 per default south of -50°S . In the following, the effects of MOMIX are discussed, based on
 571 simulation of fesom_KPP and cvmix_TKE each with and without MOMIX.

572 Fig. 20 presents the temperature (1st and 2nd column) and salinity (3rd and 4th column) differences between
 573 simulations with and without MOMIX for both the fesom_KPP and cvmix_TKE schemes, averaged over
 574 five different depth ranges. Using MOMIX in the Southern Ocean leads to a significant warming of up to
 575 1°C for almost the entire Southern Ocean south of -60°S throughout all considered depth ranges, except for
 576 the surface depth range of the southern Weddell Sea and subsurface southern Pacific which exhibits cooling
 577 anomalies. The warming anomaly is slightly more pronounced for fesom_KPP than cvmix_TKE. The usage
 578 of MOMIX in the Southern Ocean leads in fesom_KPP to a warming of the Gulf Stream and to a cooling of
 579 the NAC. For cvmix_TKE this behaviour is reversed. The salinity anomalies indicate a freshening for the
 580 entire Southern Ocean surface depth range when using MOMIX, while the subsurface depth ranges indicate
 581 predominantly a slight increase in salinity, except for the southern Weddell Sea 250-500m depth range.

582 To emphasize the effect of MOMIX on the Weddell Sea MLD, Fig. 21 presents the Southern Ocean
 583 September MLD for fesom_KPP (a) and cvmix_TIDAL (b) without MOMIX and the corresponding
 584 anomalies with minus without MOMIX (c, d). The MLD for fesom_KPP (a) and cvmix_TKE (b) are very
 585 large over the entire Weddell Sea and parts of the Ross Sea. The MLD values are higher and more extended
 586 with fesom_KPP than with cvmix_TKE. However, for both vertical mixing schemes without using MOMIX,
 587 the MLD values are way too high within the Weddell Sea and Ross Sea. The figures c) and d) visualize what
 588 happens with the Southern Ocean MLD for fesom_KPP and cvmix_TKE when MOMIX is used. Especially
 589 for fesom_KPP, MOMIX leads to a significant decrease in the MLD in almost the entire Weddell Sea of up
 590 to ~3000 m, except for the southwestern Weddell Sea close to the continental shelf which exhibits an
 591 increase in MLD. Also the large MLD patch in the Ross Sea becomes strongly reduced when using MOMIX.
 592 Both fesom_KPP and cvmix_TKE face the same pattern in MLD reduction when using MOMIX, only the
 593 magnitude in the MLD decrease is larger in fesom_KPP than in cvmix_TKE.

594 Since MOMIX has a rather strong effect in reducing the Weddell Sea open-ocean deep-water formation it
 595 will also consequently affect the formation of Antarctic Bottom Water (AABW) and the Meridional
 596 Overturning Circulation (MOC). Fig. 22 shows the fesom_KPP global (a), Atlantic (b) and Pacific (c) MOC
 597 when MOMIX is switched off and the difference from the case with MOMIX (bottom row). It can be seen
 598 that on a global but also basin-wide scale, the use of MOMIX leads to a reduction in the strength of the
 599 AABW, in the Atlantic by ~0.6 Sv and in the Pacific by up to ~1.7 Sv. Also the strength of the upper AMOC
 600 cell is reduced by ~1 Sv when using MOMIX. We conclude that using MOMIX helps to alleviate the
 601 problem of large MLDs in the Weddell Sea which we addressed above. Hence, the options cvmix_KPP_TIDAL
 602 or cvmix_TKE_IDEMIX are strongly recommended to be used in combination with MOMIX, which is per
 603 default active only South of -50°S.

604

605 4 Discussion and Conclusions

606 This paper describes the two new features -- partial cells and embedded sea ice introduced to FESOM2.0 and

607 the implementation of the vertical mixing library CVMix (cvmix_PP, cvmix_KPP, cvmix_TKE, IDEMIX
608 and cvmix_TIDAL), together with the elaboration of the effect of MOMIX. These new features expand the
609 functionality of FESOM2.0, its applicability and its ability to be better compared to other state of the art
610 ocean general circulation models. With its model components implemented, FESOM2.0 is mature for its
611 practical applications and holds its leading role in the competition of the global unstructured ocean models.

612 We demonstrate the effect of using partial cells by comparing them against the full cell approach. It is shown
613 that partial cells lead to an improved representation of the Gulf Stream branch, with a reduction in the cold
614 bias in the northwest corner of the North Atlantic associated with an improved NAC pathway. Further,
615 partial cells lead to a “northwest corner like” meridional deflection of the NAC between -30°W and -15°W
616 which is still too far east, but leads to an improved representation in a rather coarse configuration which
617 would otherwise be dominated by a rather zonal NAC. Partial cells also lead to a general speed up of the
618 boundary currents shown as an example for the North Atlantic.

619 The improvement of the NAC pathway and the speedup of the boundary currents especially in the subpolar
620 gyre by using partial cells is described by a variety of publications (e.g. Barnier et al., 2006; Käse et al.,
621 2001; Myers, 2002). Besides all its advantages, partial cells also harbor the risk of increasing the existing
622 biases, like in our coarse configuration the deep Arctic warm bias, which is largely inherited from the
623 Atlantic Water inflow branch that expands too deep. The tendency of partial cells to increase the velocity in
624 the boundary currents leads to an enhancement of the Atlantic Water inflow to the Arctic Ocean. As the
625 temperature in the Arctic Atlantic Water layer is already overestimated without using partial cells, the warm
626 bias becomes even larger when partial cells are used. However, this is not the principle drawback of partial
627 cells, but rather an issue of model tuning for the pan-Arctic region, which is part of our on-going work (for
628 example, evaluating different numerical schemes of momentum viscosity). In the southern hemisphere, using
629 partial cells leads to a significant reduction of the otherwise rather high MLD in the Weddell Sea. Regarding
630 the configuration used in this paper, using partial cells leads to a strengthening of the warm deep water
631 current (Vernet et al. 2019) that crosses the Weddell Sea interior. Thus it enhances the local stratification
632 (see Suppl. 3 white arrow) and reduces vertical convection. It can be summarized that the usage of partial
633 cells clearly improves the general circulation within FESOM2.0 and that the benefits outweigh the
634 drawbacks.

635

636 The second feature that was presented, is the effect of embedded sea ice vs. the standard case of levitating
637 sea ice. Embedded sea ice allows for a further step towards a more realistic and physical ocean-sea ice
638 interaction by adding the sea ice loading to the ocean pressure. This has the potential of increasing ocean
639 variability especially near the sea ice edge. Our results indicate that the embedded sea ice has only a minor
640 effect on the sea ice distribution itself. Nevertheless the effect is the strongest for the Northern Hemisphere
641 summer, when the sea ice edge retracts towards the Arctic Ocean interior. Here embedded sea ice leads to an
642 up to 9% increase in the sea ice concentration in the eastern Arctic Ocean marginal seas, which also leads to

643 an increase in the bias of the sea ice edge, and to a 6% decrease in the marginal seas of the western Arctic
644 Ocean, which slightly reduces the sea ice extent bias there. The effect of embedded sea ice on the
645 hydrography of the Arctic Ocean is much more significant, with an increase in temperature and salinity of up
646 to 0.5°C and 0.1psu, respectively through most of the upper 1000 m. The increase in temperature and salinity
647 is connected to a particular increase of the boundary currents especially along the eastern boundaries of the
648 Eurasian Basin but also to a strengthening of the cyclonic current along the Lomonosov Ridge, which was
649 otherwise rather weakly represented in the levitating sea ice case. The deficiencies of the Arctic Ocean
650 currents representation in our model configuration can be partially attributed to the rather coarse resolution.
651 However, with embedded sea ice we seem to be able to at least partly counteract the effect of low resolution
652 and improve the Arctic Ocean current structure at rather low costs. We note that embedded sea ice could also
653 deteriorate the model results in some cases. Since the boundary currents around the Eurasian Basin get
654 enhanced, the already existing Atlantic Water layer biases get enhanced. However, as mentioned above, this
655 is an issue of model tuning with this coarse resolution setup, not a drawback of embedded sea ice itself.

656

657 To further expand the functionality and comparability of FESOM2.0 we implemented the vertical mixing
658 library CVMix and its components, which in our implementation include `cvmix_PP`, `cvmix_KPP`,
659 `cvmix_TIDAL`, `cvmix_TKE` and `cvmix_TKE+IDEMIX`. At first, the vertical mixing parameterizations
660 `fesom_KPP` and `fesom_PP`, which have been already implemented in FESOM2.0, are briefly evaluated. It is
661 shown that `fesom_PP` produces a slightly colder tropical and subtropical but warmer polar oceans on the
662 surface, with a largely warmer ocean below the surface layer depth range, when compared to `fesom_KPP`.
663 This makes between these two, `fesom_KPP` the preferred vertical mixing option at least in terms of mean
664 temperature biases. In terms of salinity biases, `fesom_PP` performs better in the surface and subsurface AO
665 as well as in the equatorial Atlantic and Indian Ocean, while otherwise `fesom_KPP` indicates smaller biases.
666 In the next instance, `fesom_KPP` and `cvmix_KPP` have been compared to each other, since there are slight
667 differences in their implementation. The difference in implementation leads only to minor differences in
668 temperature throughout all considered depth ranges. Regarding the salinity differences, `cvmix_KPP` produces
669 a considerably fresher surface AO compared to `fesom_KPP`, which is attributed to a reduced near surface
670 vertical diffusivity in `cvmix_KPP` that leads to an over-stabilisation of the AO halocline. This enhances the
671 mean salinity bias in that region. In terms of vertical diffusivity, `cvmix_KPP` has the tendency to produce by
672 up to one order of magnitude lower value (especially in the very deep depth range) in the main convection
673 areas of Labrador Sea and Greenland Sea, throughout all considered depth ranges, accompanied by increased
674 diffusivity in the subsurface of the Arctic Ocean. The reduced diffusivity in the main convection areas is
675 attributed to the different treatment of the shear- and buoyancy difference with respect to the surface in
676 `cvmix_KPP` that leads to a reduction of the local ocean boundary layer depth and to slightly reduced
677 maximum MLD in Labrador and Greenland Sea, while the maximum MLD in the Weddell Sea becomes
678 slightly enhanced, when using `cvmix_KPP` over `fesom_KPP`.

679 Since the implementation of `cvmix_PP` and `fesom_PP` are also slightly different, we also compare them.
680 Although the produced diffusivities between `cvmix_PP` and `fesom_PP` are very similar, `cvmix_PP` indicates
681 a further warming and salinification in the surface and 250-500 m depth ranges except for the upwelling
682 region in the Gulf of Guinea which indicates a cooling and freshening and the surface depth range of the
683 Arctic Ocean where it creates a predominant freshening, when compared the `fesom_PP`. The MLD values
684 indicate that `cvmix_PP` leads in FESOM2.0 to a slightly stronger convection in the Weddell Sea. The
685 differences between `fesom_PP` and `cvmix_PP` are related to the different treatment of the background
686 coefficient for viscosity when computing the diffusivity see Pacanowski and Philander (1981).

687 The effect of implementing `cvmix_TIDAL` in combination with `cvmix_KPP` was further assessed.
688 `cvmix_TIDAL` serves here as a resourceful way to heterogenize the effect of tidally induced internal wave
689 breaking that is otherwise homogenized in a constant or latitude dependent value for the background
690 diffusivity. Using `cvmix_TIDAL` clearly leads to an enhancement of the vertical diffusivity along the slopes
691 of the bottom topography, where tidally related internal wave breaking is induced. This leads especially in
692 the high-latitude marginal seas, e.g. Sea of Okhotsk and Bering Sea but also Arctic Ocean and Southern
693 Ocean, to a decrease in temperature and salinity due to the enhanced mixing along their shelves. This enables
694 `cvmix_TIDAL` to improve some of the existing local temperature and salinity biases within FESOM2.0 at
695 rather low computational costs. However, the enhanced vertical diffusivity along the shelf of the Weddell
696 Sea weakens the stratification and leads to a further increase in the MLD of the Weddell Sea of up to 1000
697 m.

698 Further, the implications of TKE vertical mixing parameterisation in FESOM2.0, added by Eden et al. (2014)
699 and Gutjahr et al. (2020) to the CVMix library, was evaluated based on a comparison with `fesom_KPP`. It is
700 shown that the mean temperature and salinity differences between `cvmix_TKE` (Fig. 17) and `fesom_KPP`
701 (Fig. 9) show very similar patterns. `cvmix_TKE` tends to produce a generally colder tropical and
702 extratropical ocean together with slightly warmer polar oceans when compared to `fesom_KPP`. The salinity
703 differences between `cvmix_TKE` and `fesom_KPP` shows that `cvmix_TKE` tends to produce a significantly
704 saltier surface layer AO, revealing a much smaller salinity bias for the Arctic Ocean interior. This is largely
705 connected to enhanced surface vertical mixing along the Arctic Ocean shelf break (not shown) within
706 `cvmix_TKE`, that helps to partly destabilize the AO halocline. The improvement of the Arctic Ocean
707 hydrography when using `cvmix_TKE` is also found by Gutjahr et al. (2020) in the coupled ocean-atmosphere
708 Max Planck Institute Earth System Model (MPI-ESM1.2). Further, `cvmix_TKE` leads to a salinity increase in
709 the entire North Atlantic and northwest Pacific marginal seas, while the southern hemisphere, except for the
710 Southern Ocean, shows a freshening when compared to `fesom_KPP`. The reduced temperatures and salinities
711 in the tropics and extratropics when using `cvmix_TKE` are connected to the reduced vertical mixing.
712 However the regions of strong vertical shear, e.g. the branch of the Gulf Stream and NAC as well as
713 Southern Ocean show stronger vertical mixing in `cvmix_TKE`, when compared to `fesom_KPP` (not shown),
714 which is accompanied by positive temperature and salinity anomalies between `cvmix_TKE` and `fesom_KPP`.

715 Following the comparison of `cvmix_TKE` and `fesom_KPP`, a side by side comparison of `cvmix_TKE` with
716 and without IDEMIX was carried out. Here IDEMIX provides an alternative formulation of the background
717 diffusivity in `cvmix_TKE` using a radiative transfer equation of weakly interacting internal waves (Olbers
718 and Eden 2013), where energy is transferred from sources of internal waves to wave sinks, such as the
719 breaking of internal waves, which provide a source for TKE, leading to an energetically more consistent
720 treatment of internal mixing (Eden et al. 2014). As compared to the tidal background mixing
721 parameterization of Simmons et al (2004), IDEMIX allows not only for the generation of internal waves by
722 barotropic tides interacting with marine topography, but also for their propagation in the horizontal and
723 vertical directions away from region of generation and their damping due to wave-wave interaction or
724 interaction with the continental shelf. Further, IDEMIX allows for the excitation of internal waves at the base
725 of the mixed layer by high frequency wind forcing (Eden et al. 2014).

726 The combined TKE + IDEMIX approach was already applied in a couple of publications (Eden et al. 2014,
727 Nielsen et al. 2018, Gutjahr et al. 2020). It was shown in Pollmann et al. 2017 that TKE dissipation rates
728 from the combined TKE+IDEMIX approach are comparable to dissipation rates estimated from Argo floats.
729 In FESOM2.0, the usage of TKE+IDEMIX leads to a significant increase in the tropical and extratropical,
730 and to a decrease in the high-latitude, temperature and salinity over depth when compared to the case of only
731 using `cvmix_TKE`. These differences compensate for some of the biases in the surface and intermediate
732 depth ranges when IDEMIX is not used. The usage of IDEMIX leads to an enhanced heterogeneous
733 representation of vertical mixing especially below the mixed layer along the continental shelves and
734 topographic slopes. However the temperature gain for the deeper depth ranges below 1000 m seems to be
735 strongly overestimated when using `cvmix_TKE+IDEMIX`, hinting at a too strong vertical mixing in the deep
736 ocean. When it comes to the MLD, `cvmix_TKE+IDEMIX` leads in the northern hemisphere to a significant
737 increase in the MLD along the Labrador Sea boundary currents and in the southern GIN seas, which can be
738 attributed to the enhanced mixing along the continental slope of the North Atlantic and in the vicinity of the
739 overflow regions. In the southern hemisphere using IDEMIX leads to an enhancement of the vertical
740 diffusivity along the continental slope of the Weddell Sea. This leads to an enhanced mixing of cold and
741 salty waters, which further reduces the stratification and significantly increases the MLD of the Weddell Sea
742 and to a rather overestimation of the otherwise already high MLD values.

743 This is in contrast to the findings of Gutjahr et al. 2020, who found that in their coupled MPI-ESM1.2
744 simulation, IDEMIX led to a reduction of the vertical mixing in the Weddell Sea allowing for more local
745 stratification. One possibility to overcome the lack of performance of IDEMIX but also of `cvmix_TIDAL` in
746 the Southern Ocean and Weddell Sea could be its combination with partial bottom cells, which had the
747 tendency to significantly reduce the deep convection in the Weddell Sea. At this point it needs further studies
748 also with FESOM2.0 to analyse the different behaviour of IDEMIX that could be influenced by local
749 resolution, coupled ocean-atmosphere feedback or just different background water mass structure.
750 Nevertheless, the achievable energetic consistency with the combined `cvmix_TKE+IDEMIX` approach is an

751 interesting feature that should find more applications in the ocean modelling community, although there is
752 still some way to go to better understand and improve its integration.

753 The last part in this paper deals with the vertical mixing parameterisation MOMIX of Timmermann and
754 Beckmann, (2004) in FESOM2.0 that helped us to overcome some major biases in the model. Since the very
755 beginning of FESOM2.0 the model suffered from a severe cooling and salinification bias in the Southern
756 Ocean and marginal seas around Antarctica, that was accompanied by a strongly overestimated MLD values
757 and too weak stratification in the Weddell Sea. It is shown here that applying MOMIX south of -50°S helped
758 to significantly reduce the biases and bring the MLD depth values in the Weddell Sea into a reasonable
759 range. MOMIX increases the vertical diffusivity within the depth range of the Monin-Obukhov mixing
760 length. This helps the warmer and fresher surface water masses from the melting season to connect with
761 colder and saltier subsurface water masses from the freezing season and thus increase the stratification and
762 reduce the vertical convection. Further, the using of MOMIX in combination with fesom_KPP leads to a
763 cooling and freshening in the branch of the NAC that seemed to be connected to a weakening of the upper
764 AMOC cell by 1 Sv and thus to a slight reduction of the meridional heat transport. The reason why
765 FESOM2.0 in the Southern Ocean is so dependent on MOMIX, which was not the case with FESOM1.4,
766 needs further research. Our actual best practise FESOM2.0 configuration uses the zstar approach with partial
767 cells and MOMIX switched on as a default, together with fesom_KPP for the vertical mixing, although
768 cvmix_TKE + IDEMIX shows some promising improvements especially for Arctic applications.

769 To summarize, this paper is the second part of the documentation of the development of important key
770 components of FESOM2.0 in a realistic global model configuration. We described the implementation of
771 partial cells and embedded sea ice and their impact on the modelled hydrography. Furthermore, we briefly
772 described the already existing vertical mixing parameterisation of fesom_KPP and fesom_PP as well as the
773 newly introduced mixing parameterization of cvmix_PP, cmix_KPP, cmix_TIDAL, cvmix_TKE and
774 cvmix_TKE+IDEMIX that came with the incorporation of the vertical mixing library CVMix into
775 FESOM2.0.

776 **5 Code availability**

777 The FESOM2.0 version used to carry out the simulations reported here is available on zenodo through
778 <https://doi.org/10.5281/zenodo.4742242>. The used mesh, as well as the temperature, salinity and vertical
779 velocity (for the calculation of the MOC) data of all conducted simulations, can be found under
780 https://swiftbrowser.dkrz.de/tcl_s/hituvPNH3xwiIy/FESOM2.0_evaluation_part2_scholz_etal. Simulated
781 results can of course also be obtained from the authors upon request. Mesh partitioning in FESOM2.0 is
782 based on a METIS version 5.1.0 package developed at the Department of Computer Science and Engineering
783 at the University of Minnesota (<http://glaros.dtc.umn.edu/gkhome/views/metis>, last access: 18 November
784 2019). METIS and the pARMS solver (Li et al., 2003) present separate libraries which are freely available
785 subject to their licenses. The Polar Science Center hydrographic climatology (Steele et al., 2001) used for

786 model initialization and the CORE-II atmospheric forcing data (Large and Yeager, 2009) is freely available
 787 online. The vertical mixing library CVMix is freely available from <https://github.com/CVMix/CVMix-src> or
 788 <https://doi.org/10.5281/zenodo.1000801>

789

790 **Author contributions**

791 SD, DS, PS and NK worked on the development of the FESOM2.0 model code and the tuning of the model.
 792 All simulations shown in this paper were carried out by PS who were also responsible for preparing the basic
 793 manuscript. QW, SD, NK, DS and TJ have contributed to the final version of the manuscript.

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803 **References**

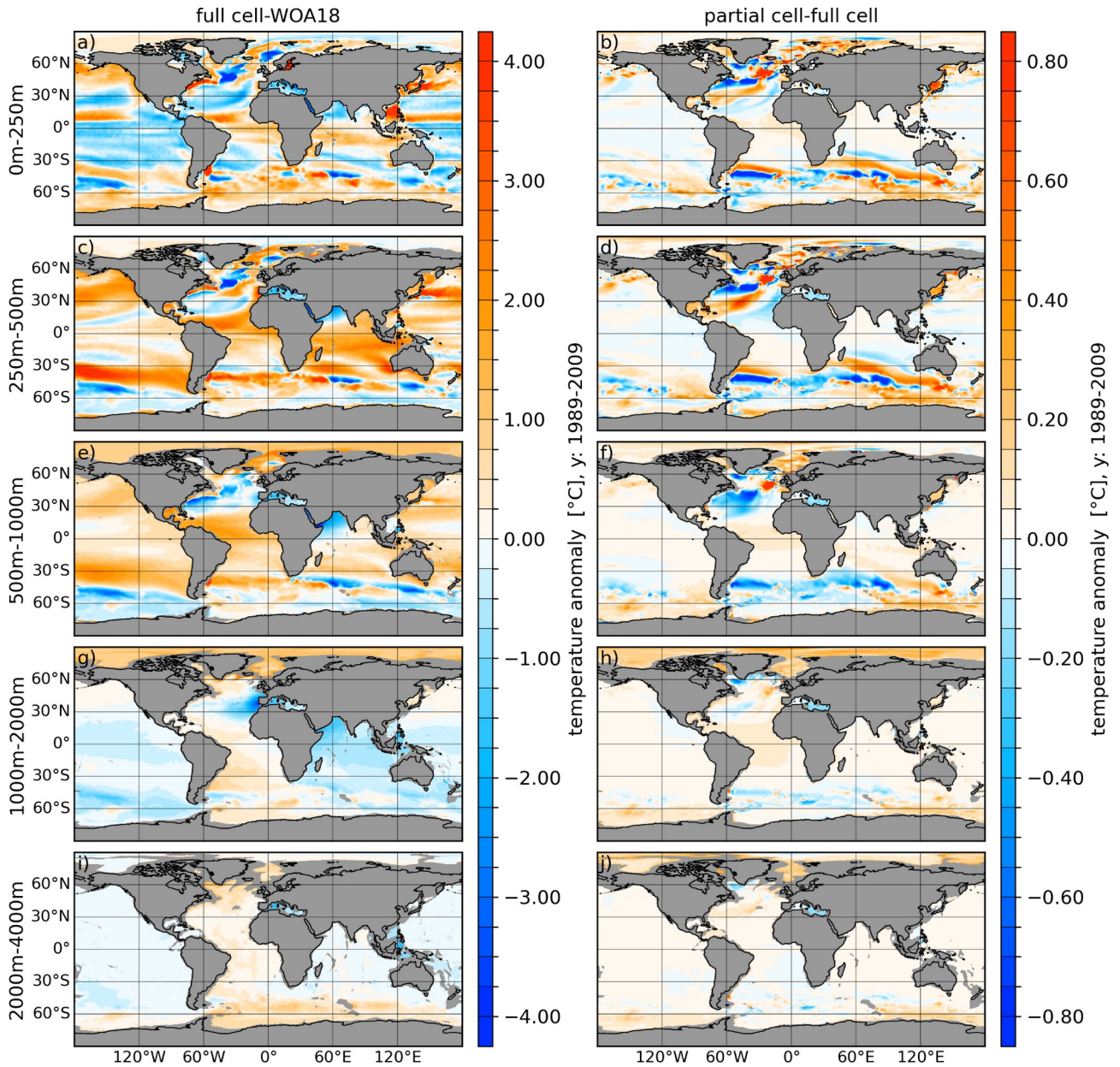
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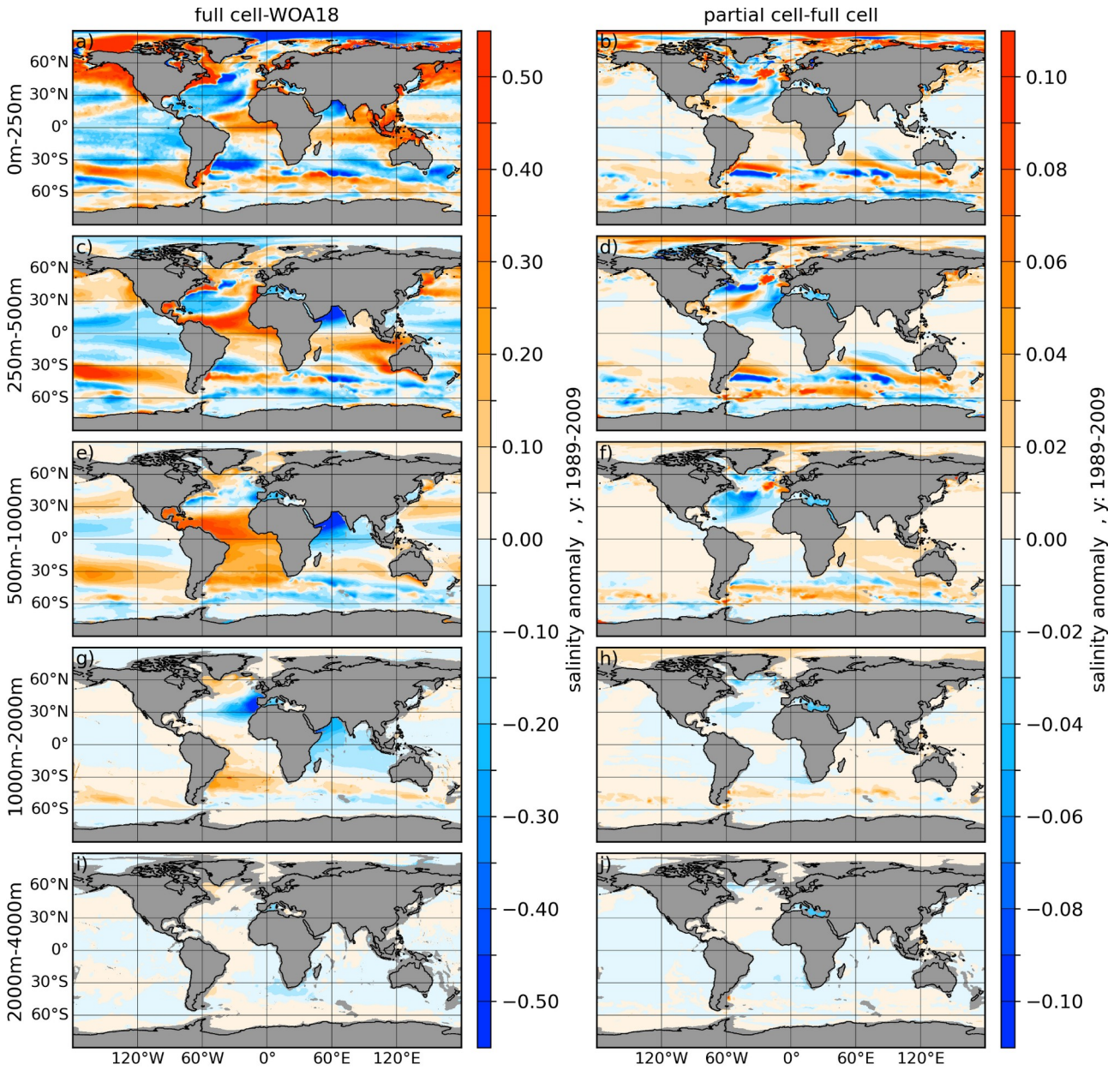
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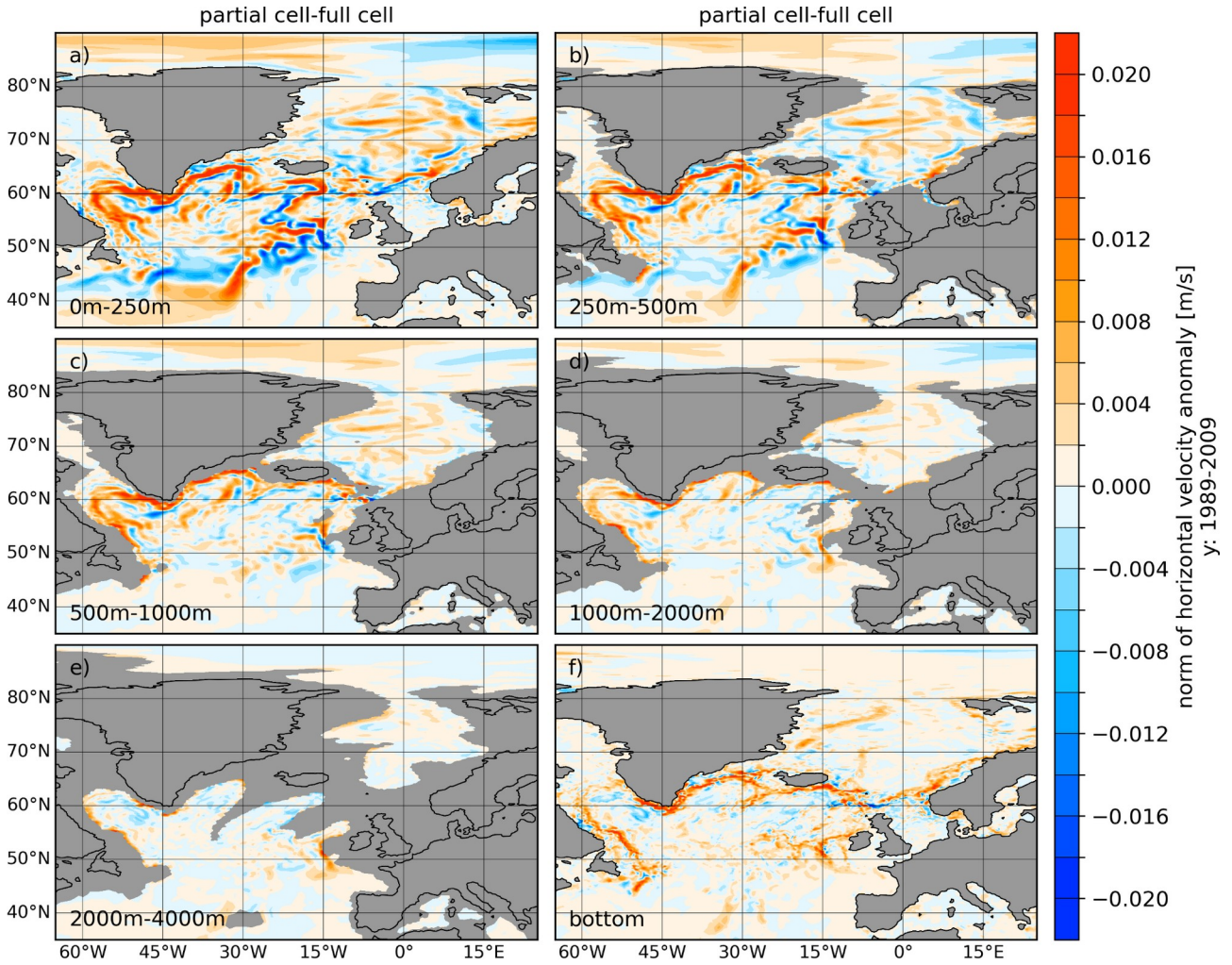
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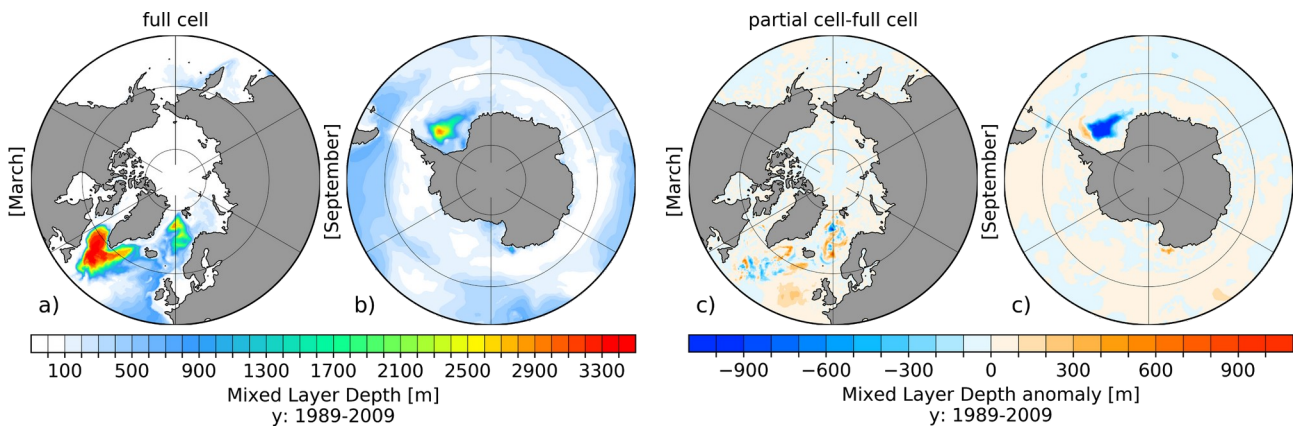
942 **Figure 1:** (Left column) Temperature biases full cells referenced to the World Ocean Atlas 2018 (WOA18,
 943 Zweng et. al 2018) averaged over the period 1989-2009. The right column shows the temperature difference
 944 between partial and full cells (partial minus full). From top to bottom the panels show the vertically averaged
 945 fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m, and 2000-4000 m.
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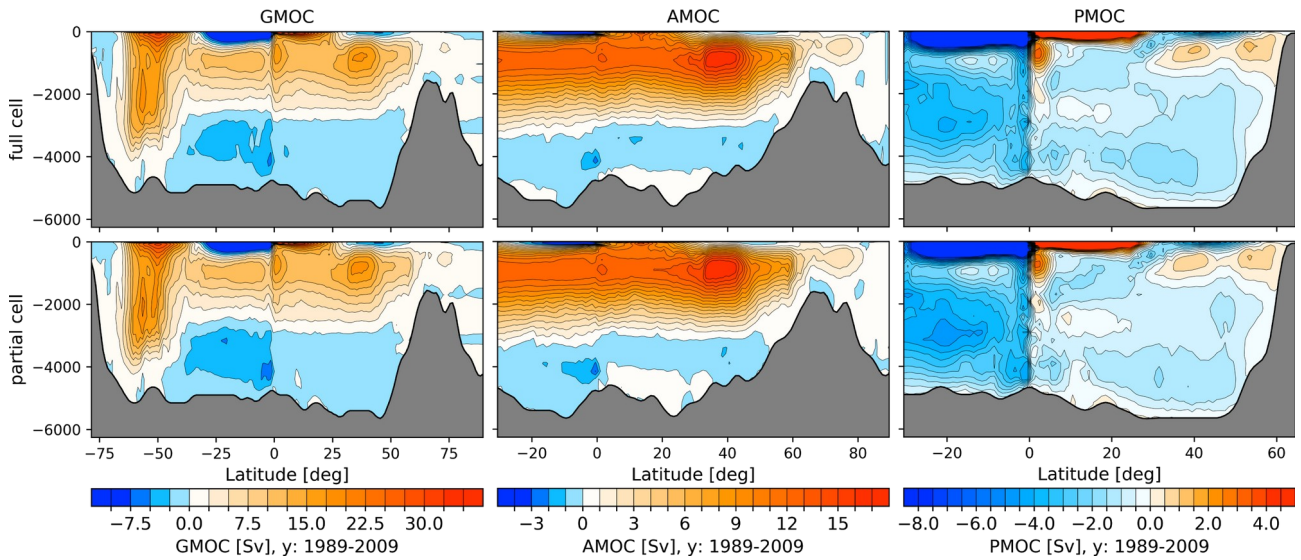
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950 **Figure 2:** Same as Fig. 1, but for salinity.



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 952 **Figure 3:** Difference of the horizontal velocity norm between simulations with partial and full cells (partial-
 953 full) averaged over the period 1989-2009 and averaged over the depth ranges of 0-250 m, 250-500 m, 500-
 954 1000 m, 1000-2000 m and 2000-4000 m as well as the bottom value.
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 958 **Figure 4:** Northern hemispheric March (a) and southern Hemispheric September (b) mixed layer depth
 959 (MLD) with full cells as well as corresponding anomalous MLD with partial minus full cells (c, d), averaged
 960 for the period 1989-2009.

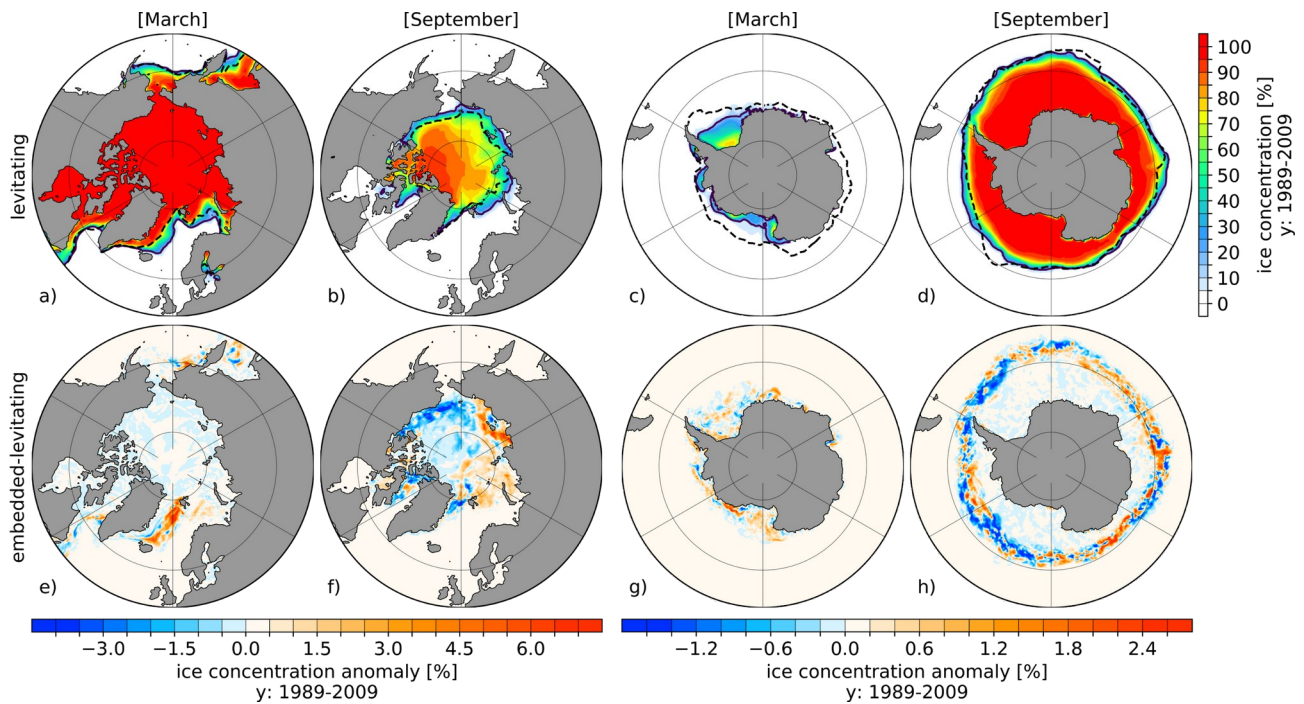


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962 **Figure 5:** Global (GMOC, left column), Atlantic (AMOC, middle column) and Indo-Pacific (PMOC, right
 963 column) Meridional Overturning Circulation for full cell (upper row) and partial cell (lower row) averaged
 964 for the time period 1989-2009.

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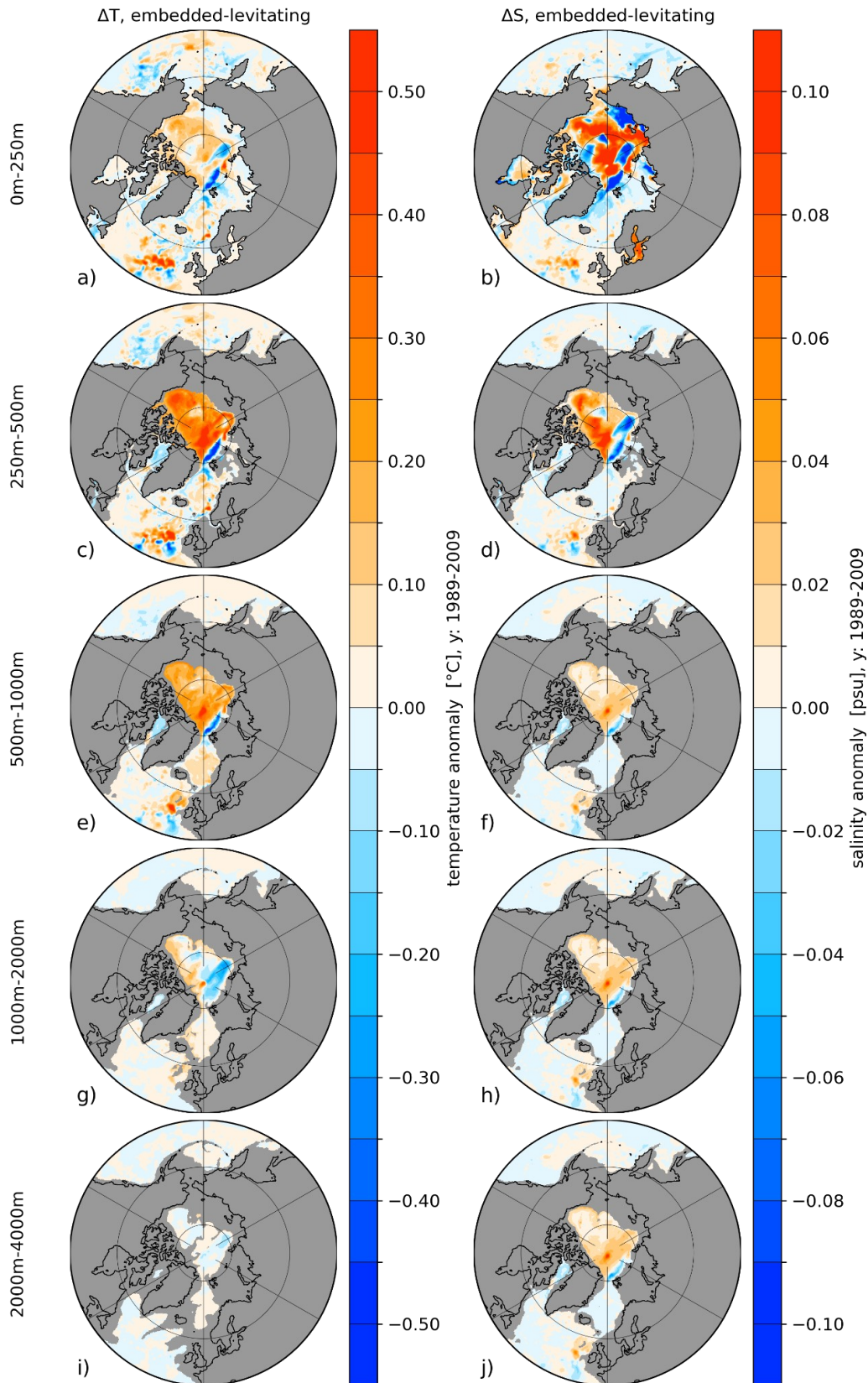
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968 **Figure 6:** Levitating (upper row) northern and southern hemispheric March (a, c) and September (b, d) sea
 969 ice concentration averaged for the period 1989-2009. Solid and dashed lines indicate the simulated and
 970 observed (Cavaliere et al., 1996) contour of the 15% sea ice extent. The lower row shows the corresponding
 971 sea ice concentration anomalies between embedded and levitating sea ice (embedded minus levitating)
 972 averaged over the same period.

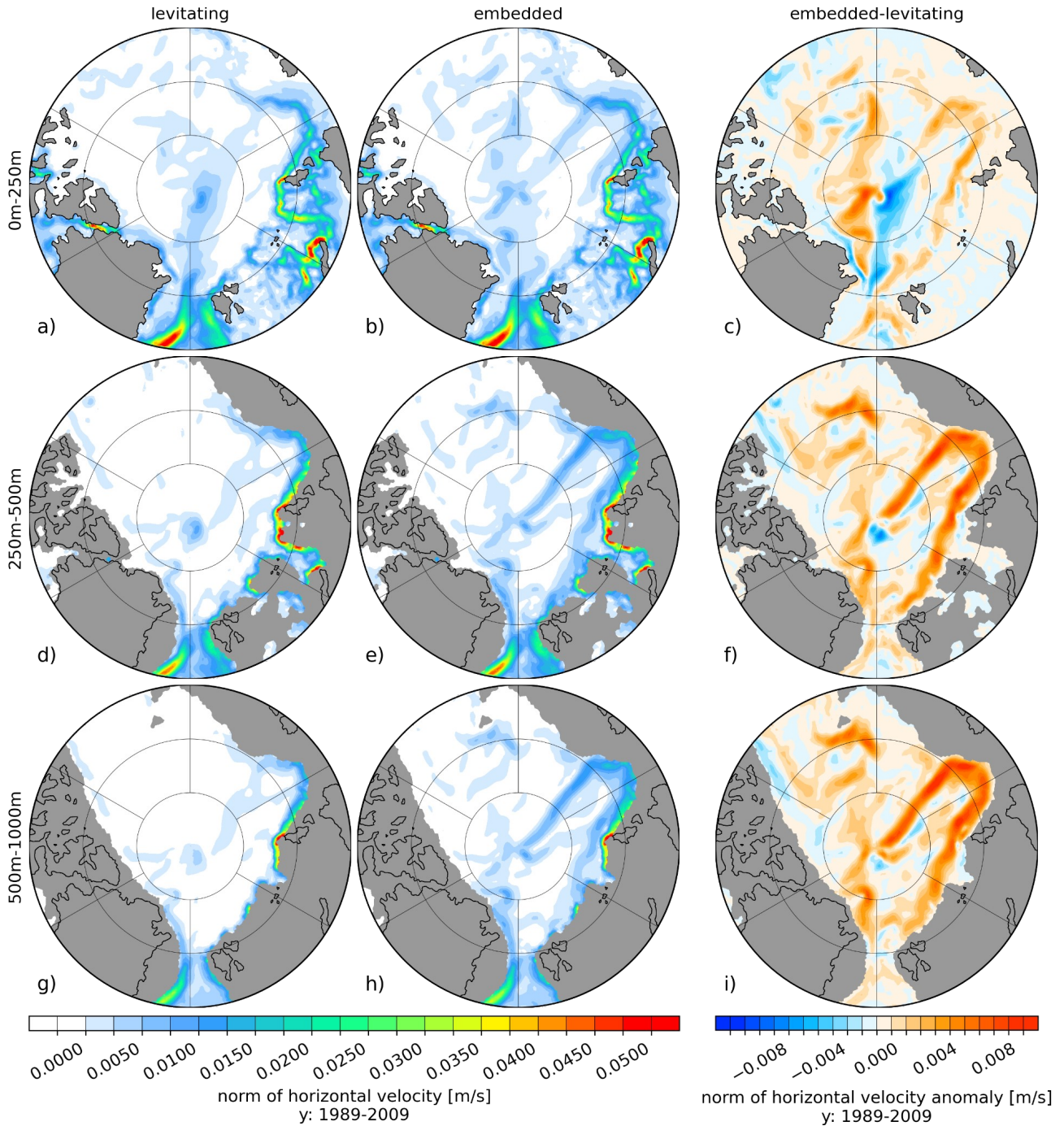
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975 **Figure 7:** Temperature (left column) and salinity (right column) difference between embedded- and
 976 levitating sea ice averaged for the period 1989 to 2009. From top to bottom, panels show the vertically
 977 averaged fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m and 2000-4000 m.

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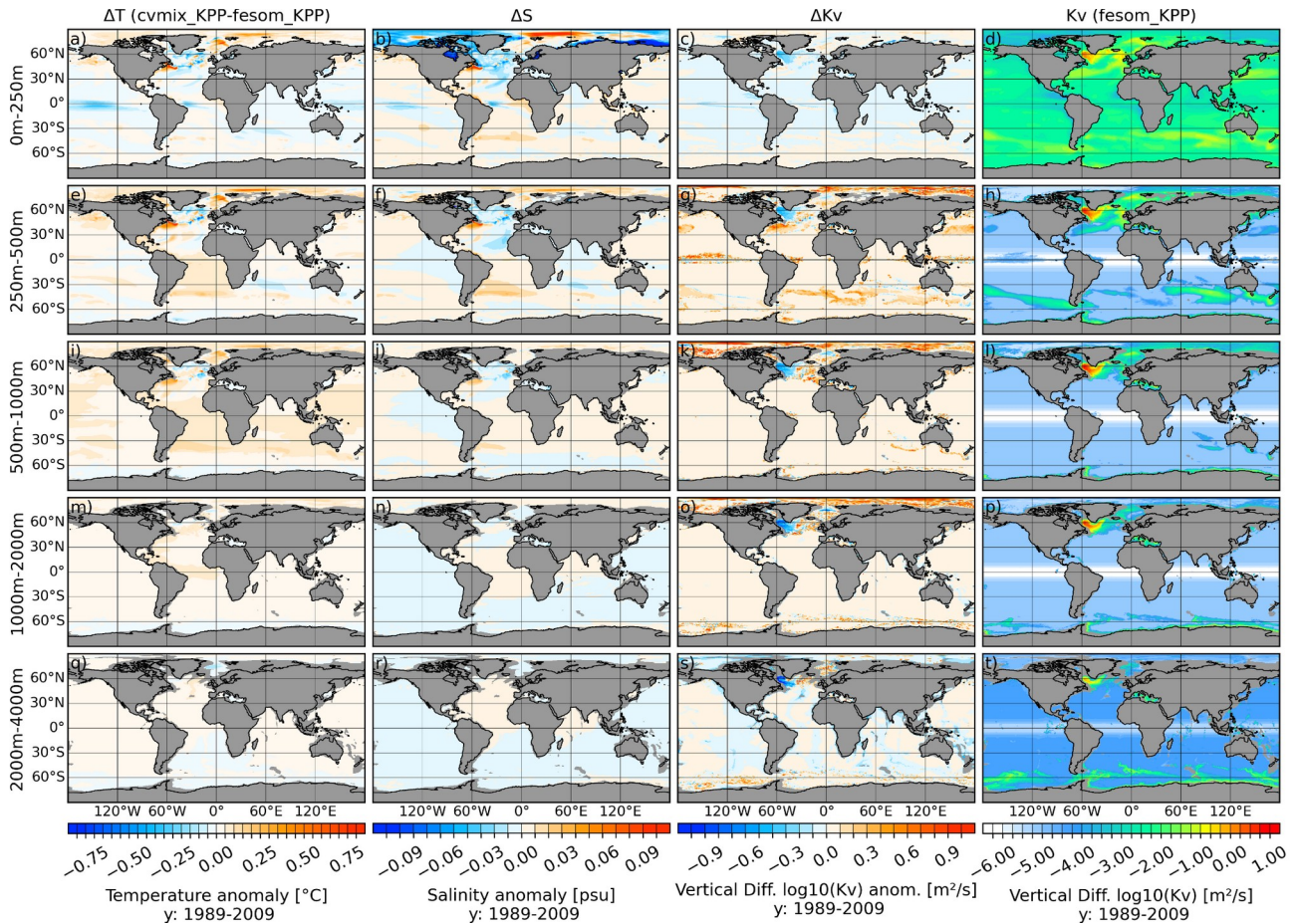
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980 **Figure 8:** Norm of ocean velocity for levitating (left column) and floating (middle column) and the
 981 difference between embedded and levitating (right column) sea ice averaged for the period 1989 to 2009.
 982 From top to bottom, the panels show the vertically averaged fields for the depth ranges of 0-250 m, 250-500
 983 m and 500-1000 m.

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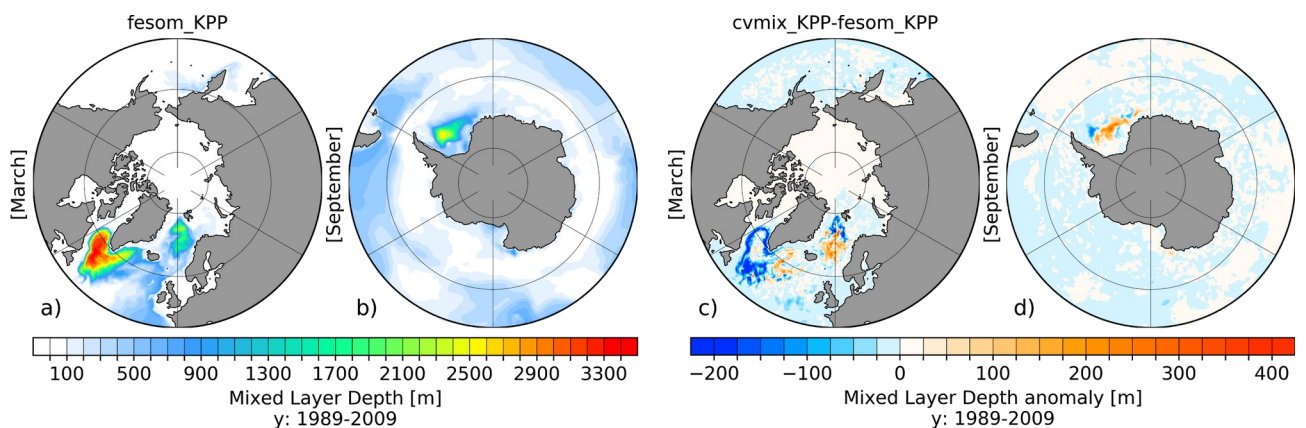


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988 **Figure 9:** Temperature (1st Column), salinity (2nd column) and vertical diffusivity (3rd column) difference
 989 between *cvmix_KPP* and original *fesom_KPP* implementation as well as the absolute vertical diffusivity
 990 values (4th column) for *fesom_KPP* averaged for the period 1989 to 2009. From top to bottom, panels show
 991 the vertically averaged fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m and
 992 2000-4000 m.

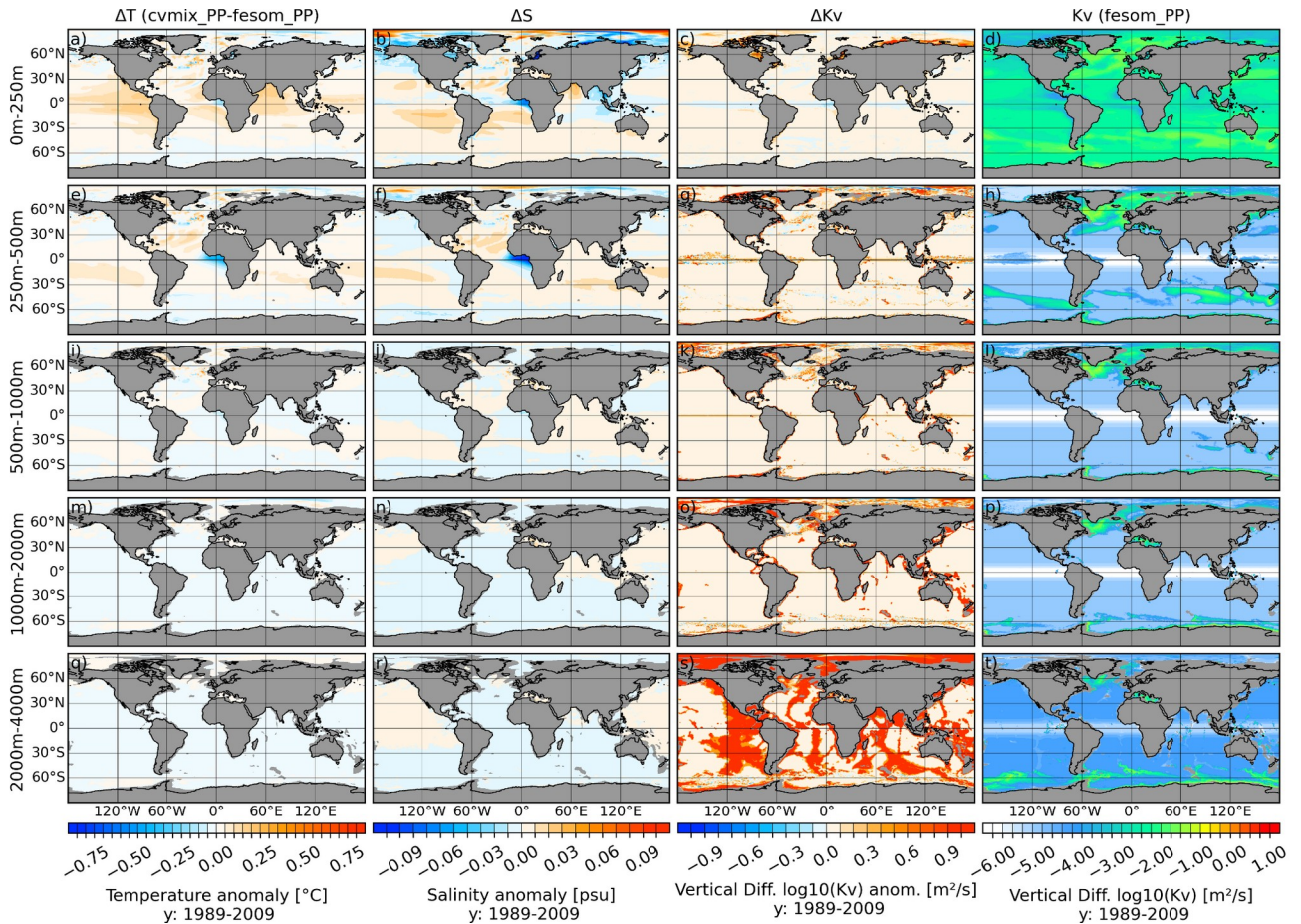
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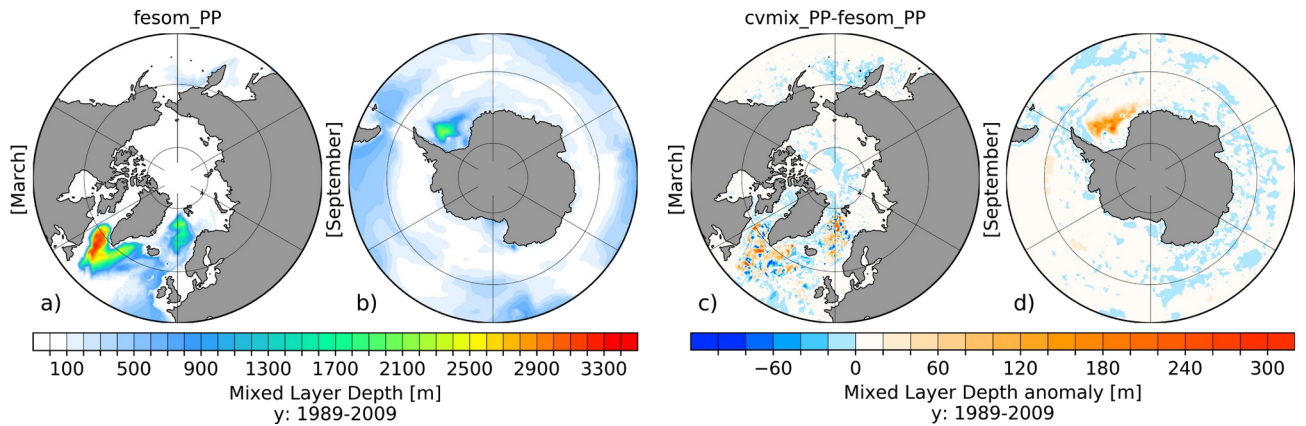
996 **Figure 10:** Northern hemispheric March (a) and southern Hemispheric September (b) mixed layer depth
 997 (MLD) for *fesom_KPP* implementation as well as corresponding anomalous MLD between *cvmix_KPP*
 998 and *fesom_KPP* implementation (c, d), averaged for the period 1989-2009.



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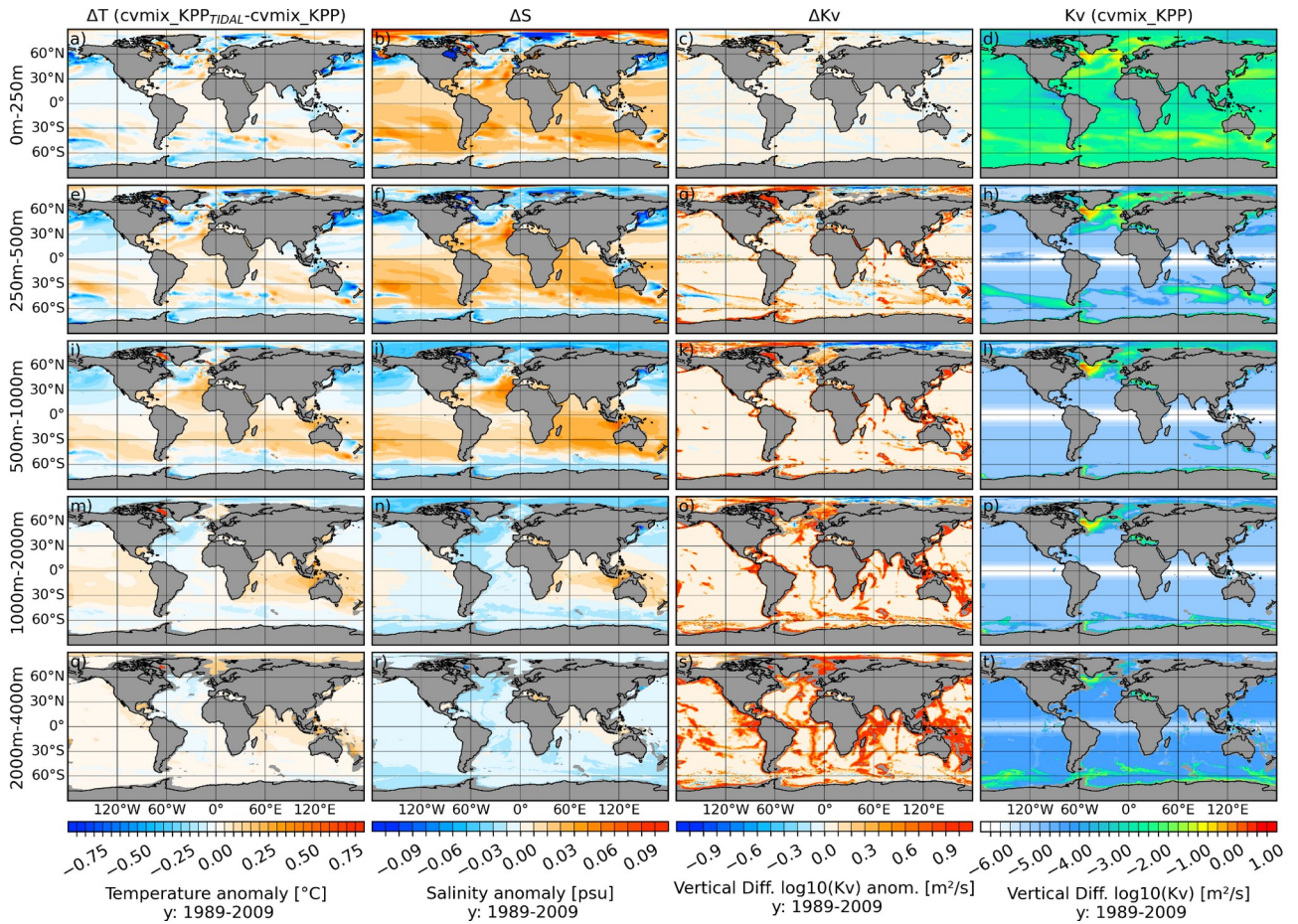
1000 **Figure 11:** Temperature (1st Column), salinity (2nd column) and vertical diffusivity (3rd column) difference
 1001 between `cvmix_PP` and original `fesom_PP` implementation as well as the absolute vertical diffusivity values
 1002 (4th column) for `fesom_PP` averaged for the period 1989 to 2009. From top to bottom, panels show the
 1003 vertically averaged fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m and 2000-
 1004 4000 m.

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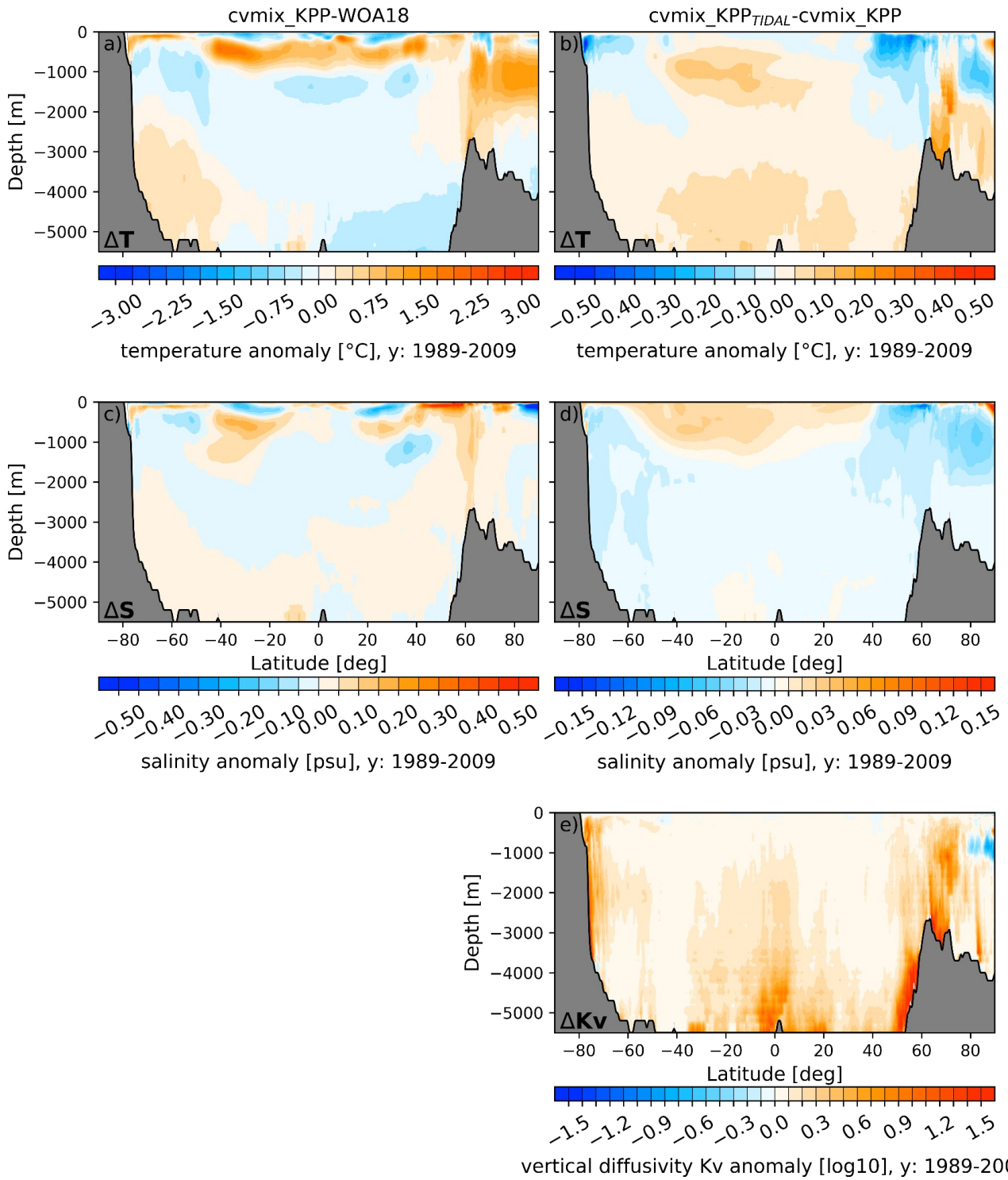
1007 **Figure 12:** Northern hemispheric March (a) and southern Hemispheric September (b) mixed layer depth
 1008 (MLD) for `fesom_PP` implementation as well as corresponding anomalous MLD between `cvmix_PP` and
 1009 `fesom_PP` implementation (c, d), averaged for the period 1989-2009.



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1011 **Figure 13:** Temperature (1st Column), salinity (2nd column) and vertical diffusivity (3rd column) difference
 1012 between cvmix_KPP with and without TIDAL mixing of Simmons et al. (2004) as well as the absolute
 1013 vertical diffusivity values (4th column) for cvmix_KPP without TIDAL mixing averaged for the period 1989
 1014 to 2009. From top to bottom, panels show the vertically averaged fields for the depth ranges of 0-250 m,
 1015 250-500 m, 500-1000 m, 1000-2000 m and 2000-4000 m.

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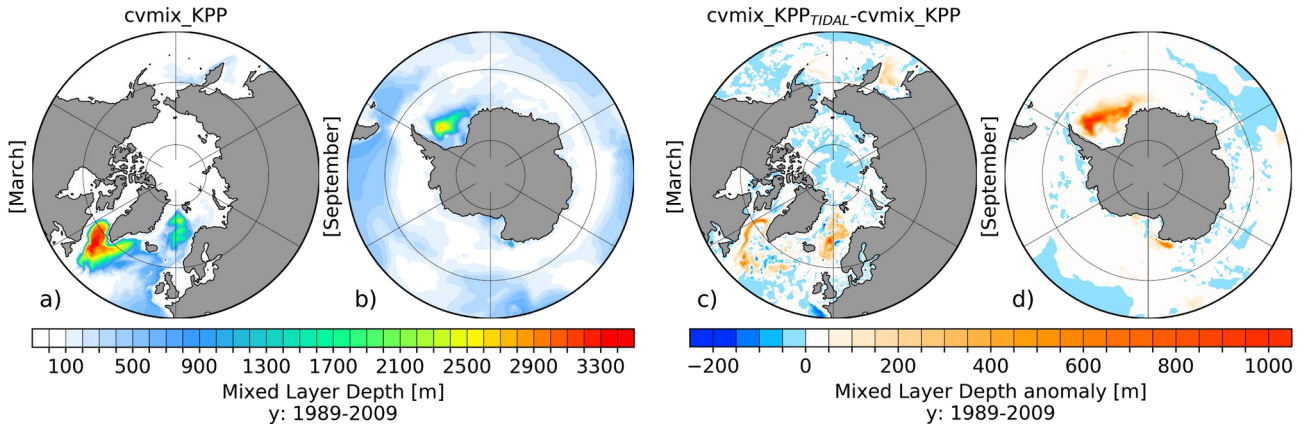
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1018 **Figure 14:** Left column: presents global zonal averaged climatological temperature (a) and salinity (c)
 1019 profiles of cvmix_KPP with respect to WOA18. Right column: shows the global zonal averaged biases of
 1020 temperature (b), salinity (d) and vertical diffusivity (e) between cvmix_KPP with tidal mixing of Simmons
 1021 et al. (2004) versus without.

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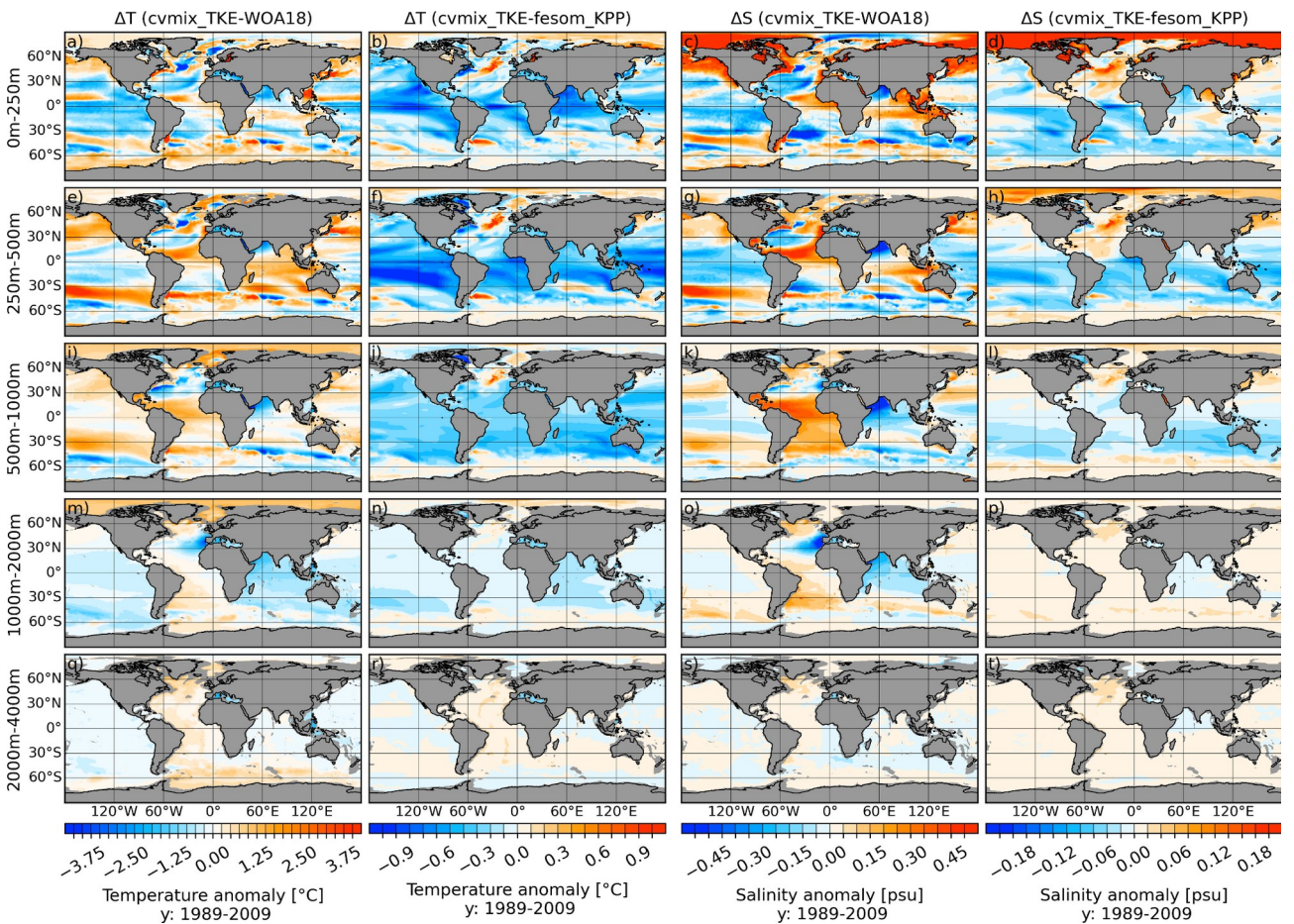
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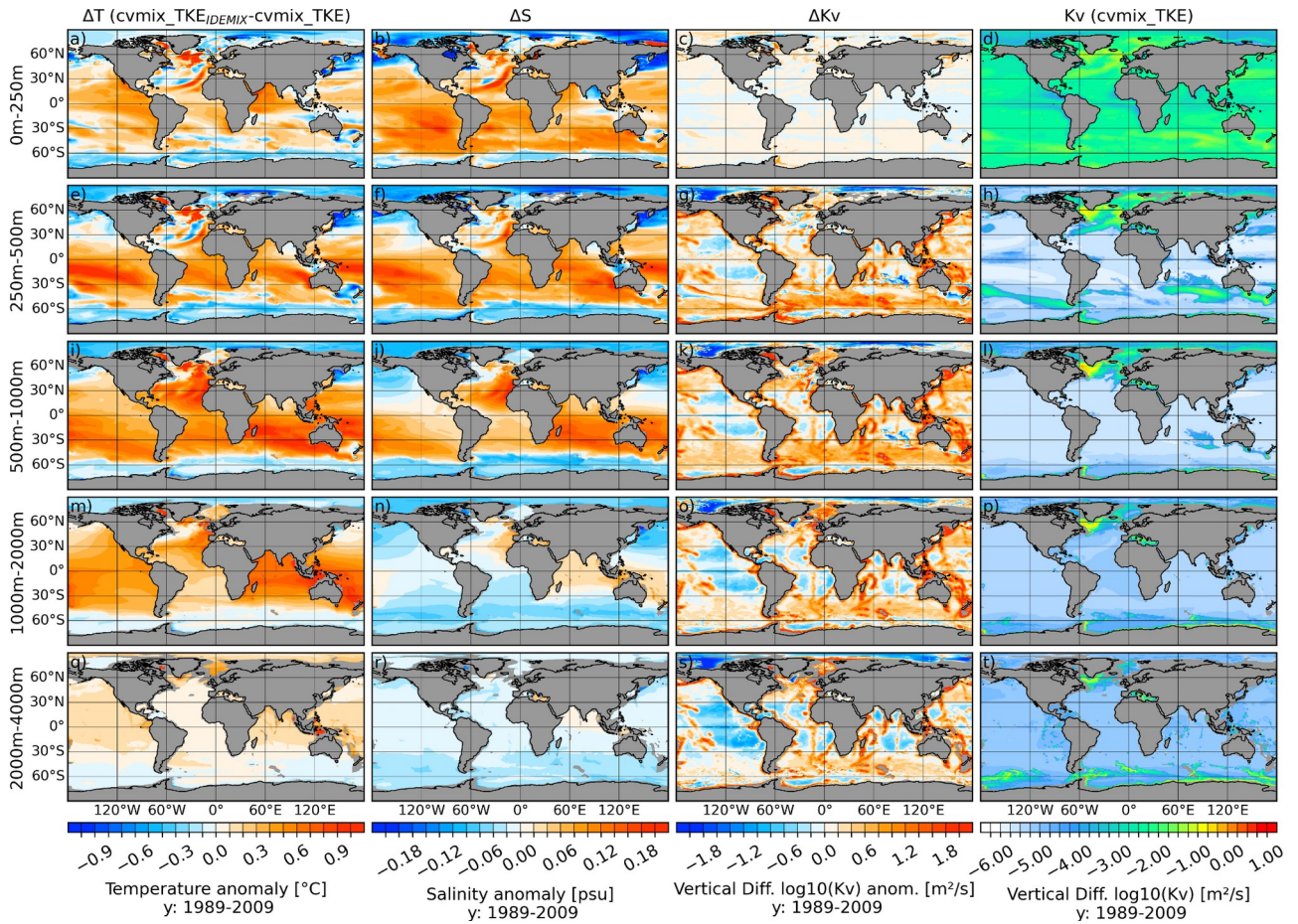
1026 **Figure 15:** Northern hemispheric March (a) and southern Hemispheric September (b) mixed layer depth
 1027 (MLD) for cvmix_KPP without TIDAL mixing as well as corresponding anomalous MLD between
 1028 cvmix_KPP with minus without TIDAL mixing of Simmons et al. (2004)(c, d), averaged for the period
 1029 1989-2009.

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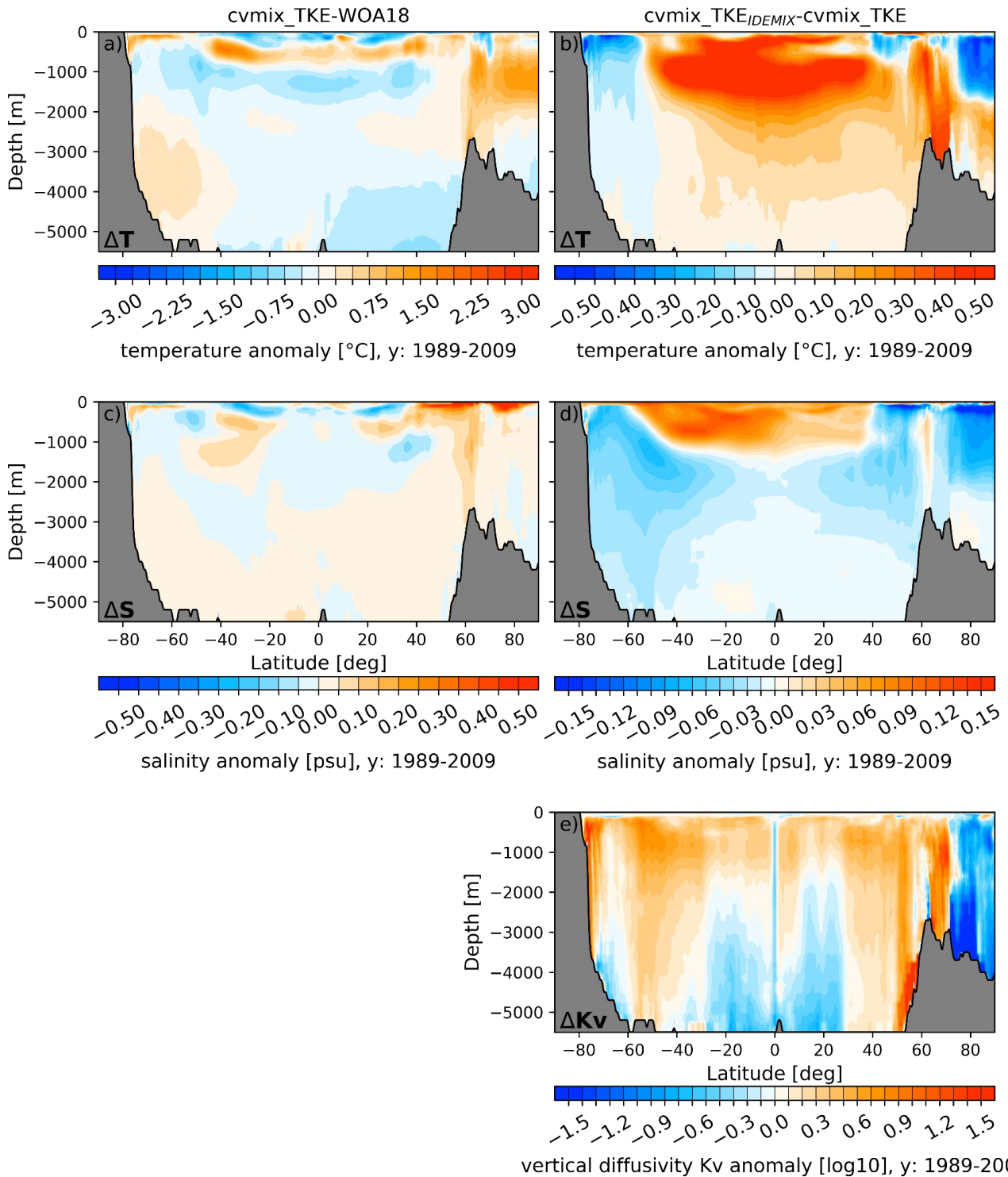
1032 **Figure 16:** Temperature (1st and 2nd column), salinity (3rd and 4th column) difference between cvmix_TKE
 1033 and WOA18 (1st and 3rd column) as well as between cvmix_TKE and fesom_KPP (2nd and 4th column)
 1034 averaged for the period 1989 to 2009. From top to bottom, panels show the vertically averaged fields for the
 1035 depth ranges of 0-250 m, 250-500 m, 500-1000 m, 1000-2000 m and 2000-4000 m.
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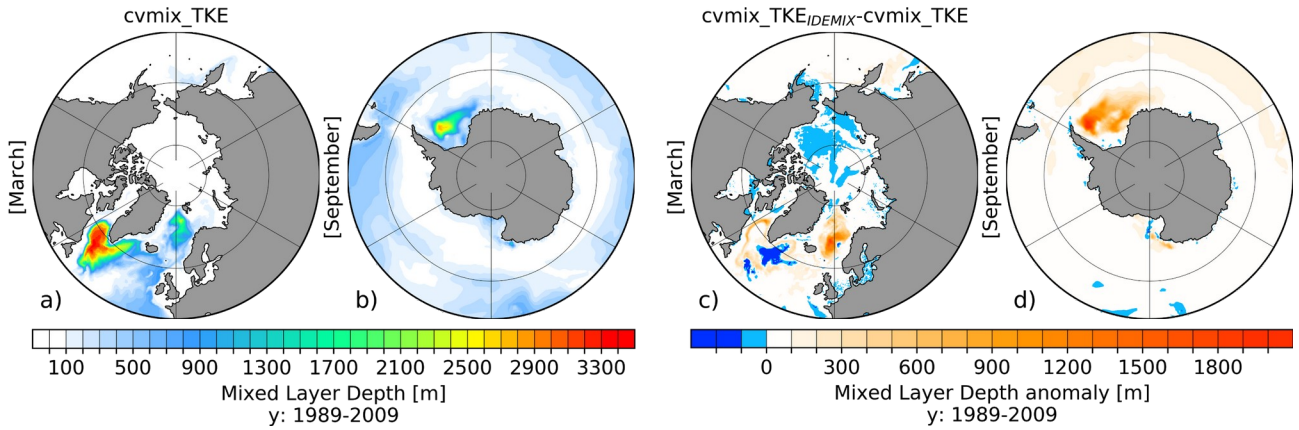
1038 **Figure 17:** Temperature (1st Column), salinity (2nd column) and vertical diffusivity (3rd column) difference
 1039 between cvmix_TKE with and without IDEMIX as well as the absolute vertical diffusivity values (4th
 1040 column) for cvmix_TKE without IDEMIX mixing averaged for the period 1989 to 2009. From top to
 1041 bottom, panels show the vertically averaged fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m,
 1042 1000-2000 m and 2000-4000 m.

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1045 **Figure 18:** Left column: presents global zonal averaged climatological temperature (a) and salinity (c) bias
 1046 profiles of cvmix_TKE with respect to WOA18. Right column: shows the global zonal averaged biases of
 1047 temperature (b), salinity (d) and vertical diffusivity (e) between cvmix_TKE with IDEMIX versus without.

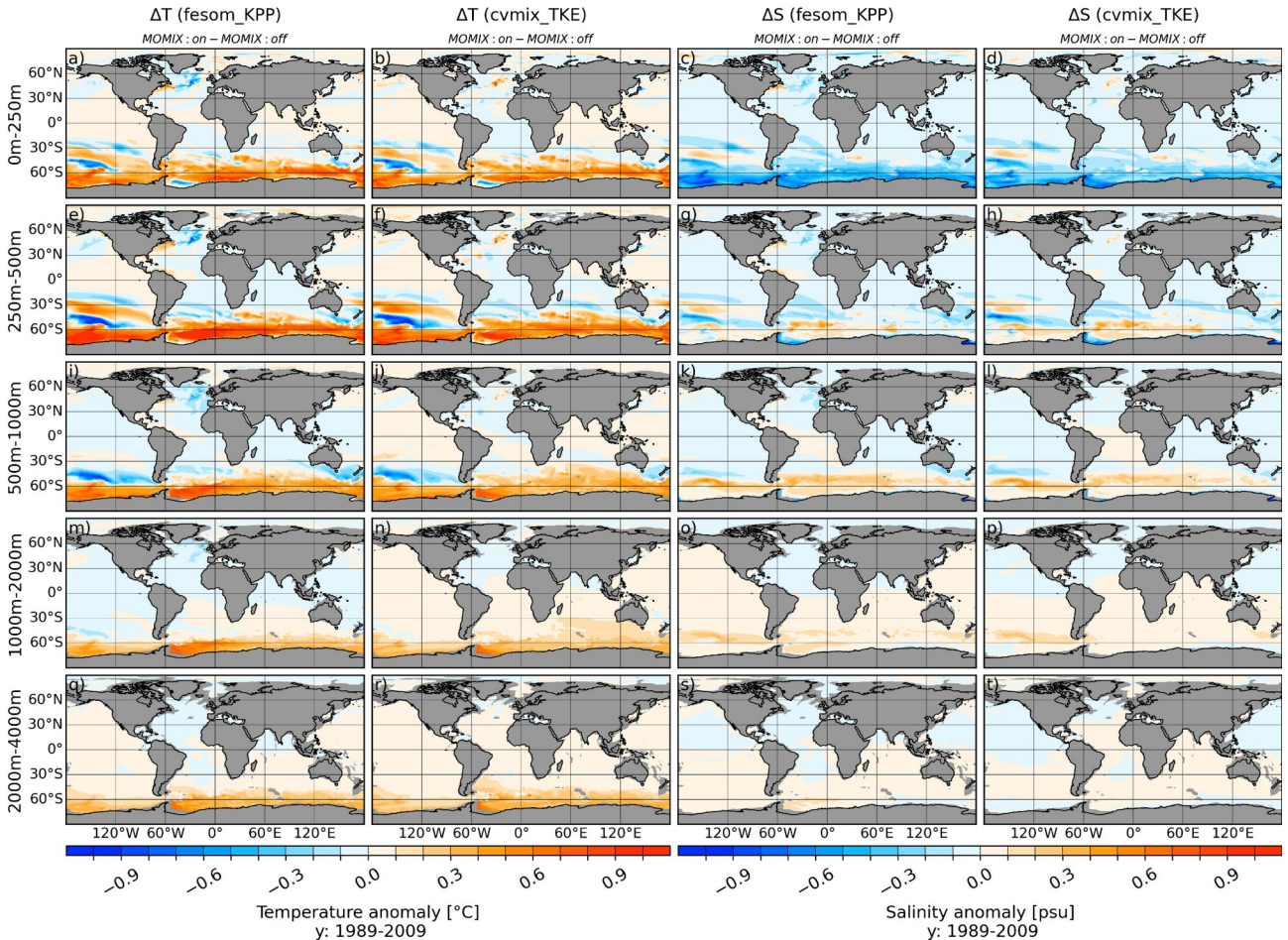


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1049 **Figure 19:** Northern hemispheric March (a) and southern Hemispheric September (b) mixed layer depth
 1050 (MLD) for cvmix_TKE without IDEMIX mixing as well as corresponding anomalous MLD between
 1051 cvmix_TKE with minus without IDEMIX mixing, averaged for the period 1989-2009.

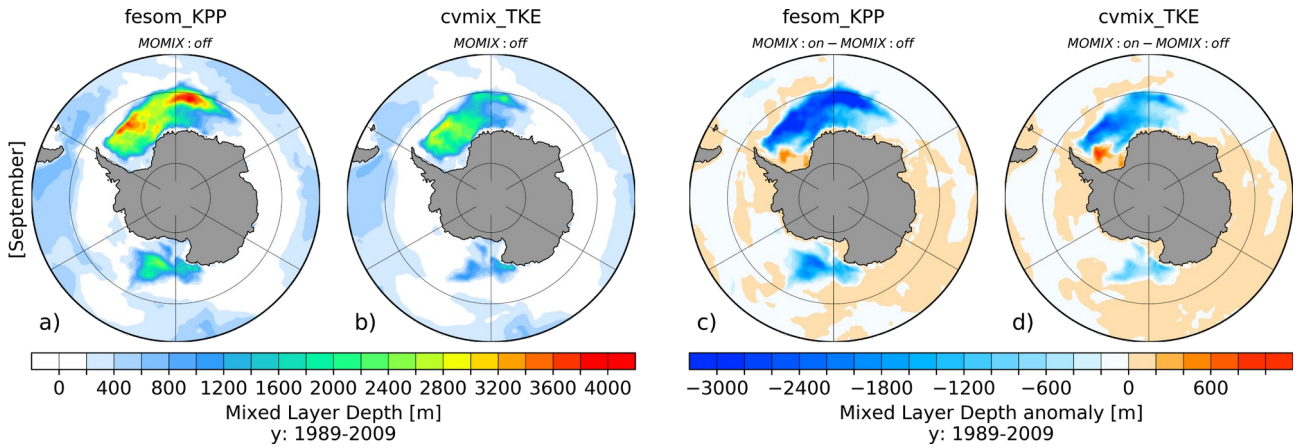
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1055 **Figure 20:** Temperature (1st and 2nd column), salinity (3rd and 4th column) difference between fesom_KPP
 1056 and cvmix_TKE vertical mixing parameterisation with Monin-Obukov vertical mixing (MOMIX) switch
 1057 on and off (MOMIX: on minus MOMIX: off) averaged for the period 1989 to 2009. From top to bottom,
 1058 panels show the vertically averaged fields for the depth ranges of 0-250 m, 250-500 m, 500-1000 m,
 1059 1000-2000 m and 2000-4000 m.

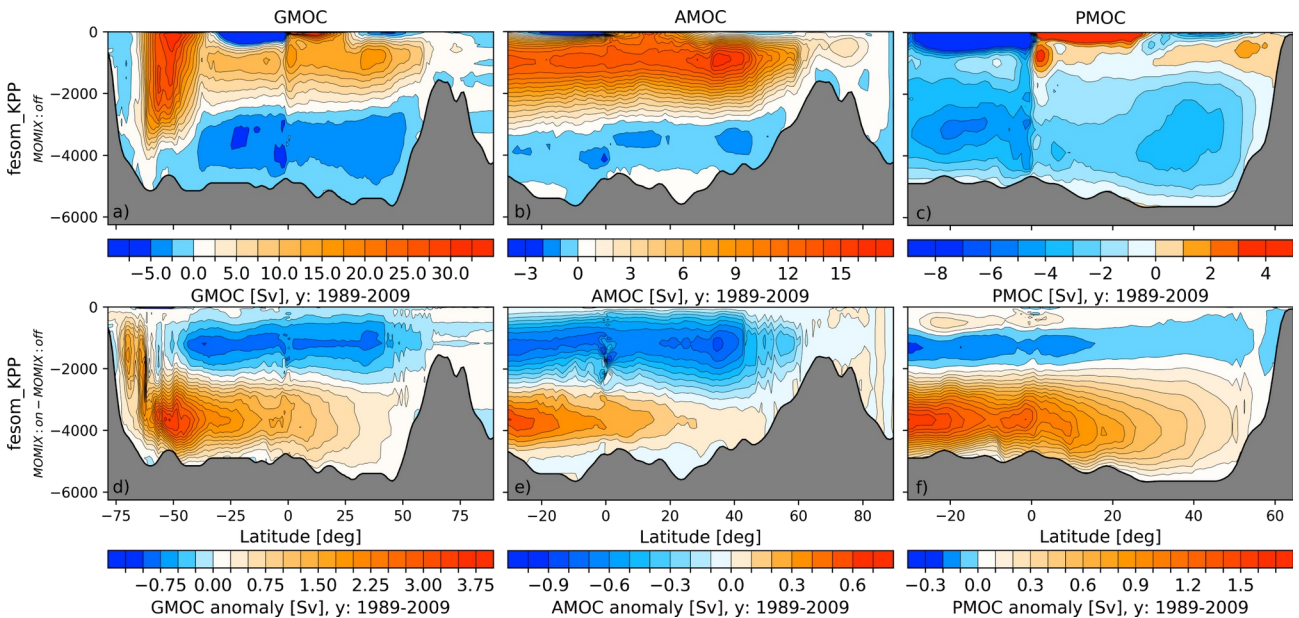


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1061 **Figure 21:** Southern Hemispheric September mixed layer depth (MLD) for fesom_KPP (a) and cvmix_TKE
 1062 (b) with switch off Monin-Obukov vertical mixing (MOMIX) parameterisation as well as corresponding
 1063 anomalous MLD between switched on and off MOMIX parameterisation (c, d, MOMIX: on minus MOMIX:
 1064 off), averaged for the period 1989-2009.

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1068 **Figure 22:** Absolute (upper row) and anomalous (lower row) Global (GMOC, left column), Atlantic
 1069 (AMOC, middle column) and Indo-Pacific (PMOC, right column) Meridional Overturning Circulation,
 1070 averaged for the time period 1989-2009. Absolute values are shown for fesom_KPP with switched off
 1071 Monin-Obukov vertical mixing (MOMIX) parameterisation, anomalous values show the difference between
 1072 fesom_KPP with switch on/off MOMIX parameterisation MOMIX: on minus MOMIX: off).

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