

1 **Supplementary Information**

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3 **Improving Madden–Julian Oscillation Simulation in Atmospheric General**
4 **Circulation Models by Coupling with Snow–Ice–Thermocline One-dimensional**
5 **Ocean Model**

6 Wan-Ling Tseng¹, Huang-Hsiung Hsu^{1*}, Yung-Yao Lan¹, Chia-Ying Tu¹, Pei-Hsuan
7 Kuo², Ben-Jei Tsuang³, Hsin-Chien Liang¹

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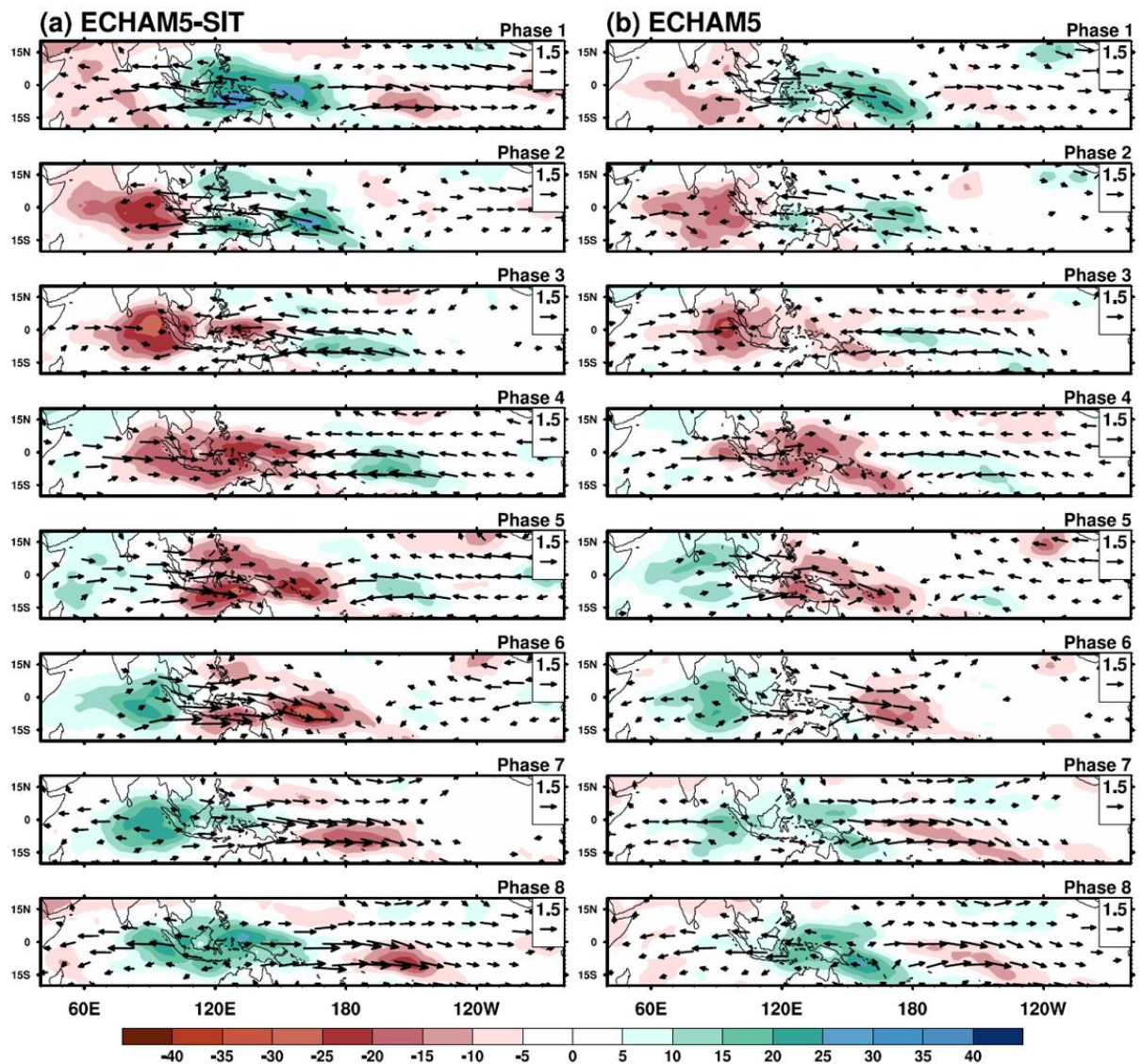
9 ¹Research Center for Environmental Changes, Academia Sinica, Taipei, Taiwan

10 ²Center Weather Bureau, Taipei, Taiwan.

11 ³National Chung-Hsing University, Taichung, Taiwan.

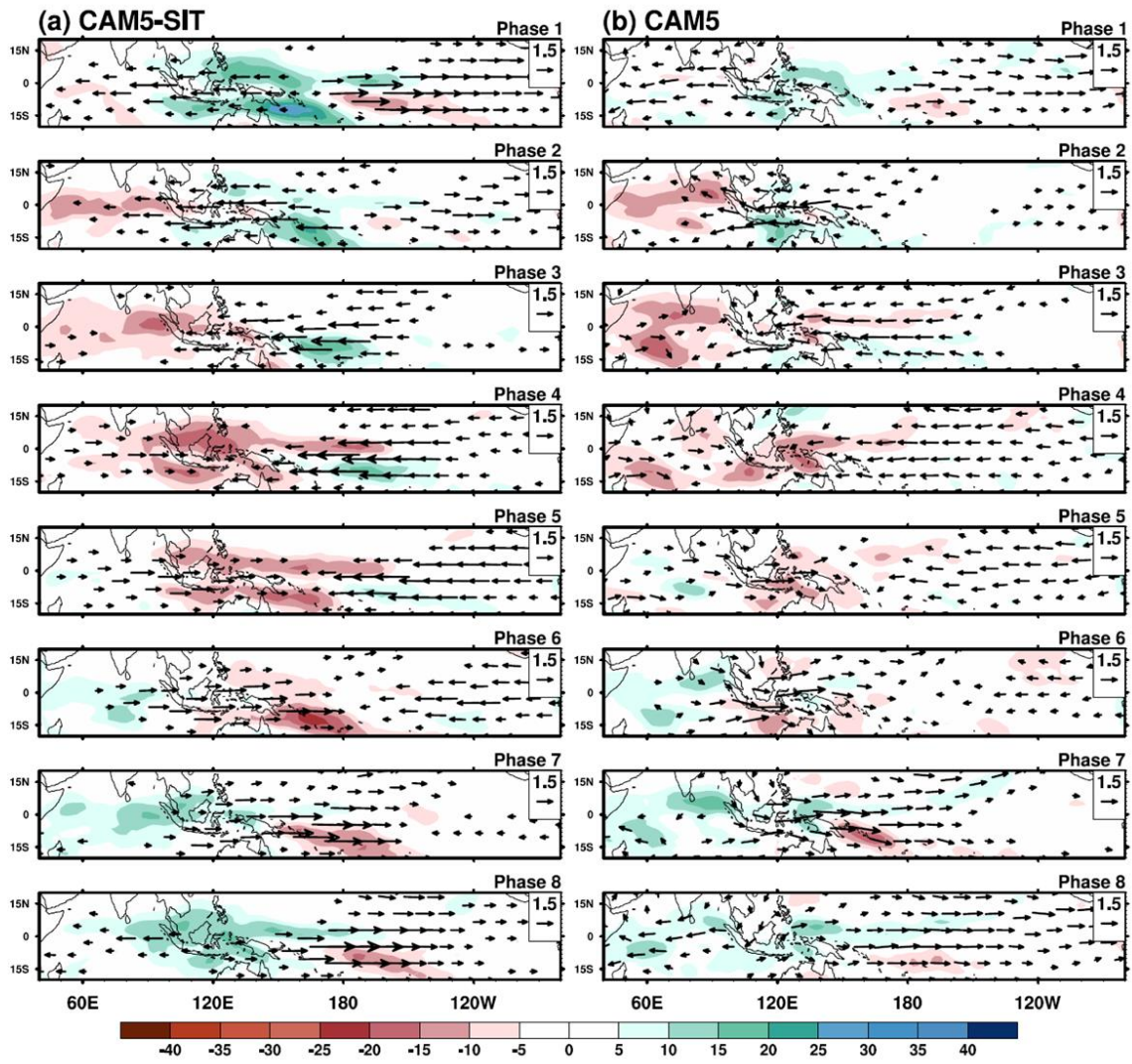
12 Corresponding author: Huang-Hsiung Hsu (hhhsu@gate.sinica.edu.tw)

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 15 **Figure S1.** Composite November–April 20–100-day OLR ($W m^{-1}$; color) and 10-m
 16 surface wind anomalies ($m s^{-1}$; vectors) as a function of the MJO phase in (a) ECHAM5-
 17 SIT and (b) ECHAM5. Vectors $<0.6 m s^{-1}$ are not shown. The reference vector in units of
 18 $m s^{-1}$ is shown at the bottom right. The number of days used to generate the composite
 19 for each phase is shown to the right of each panel.

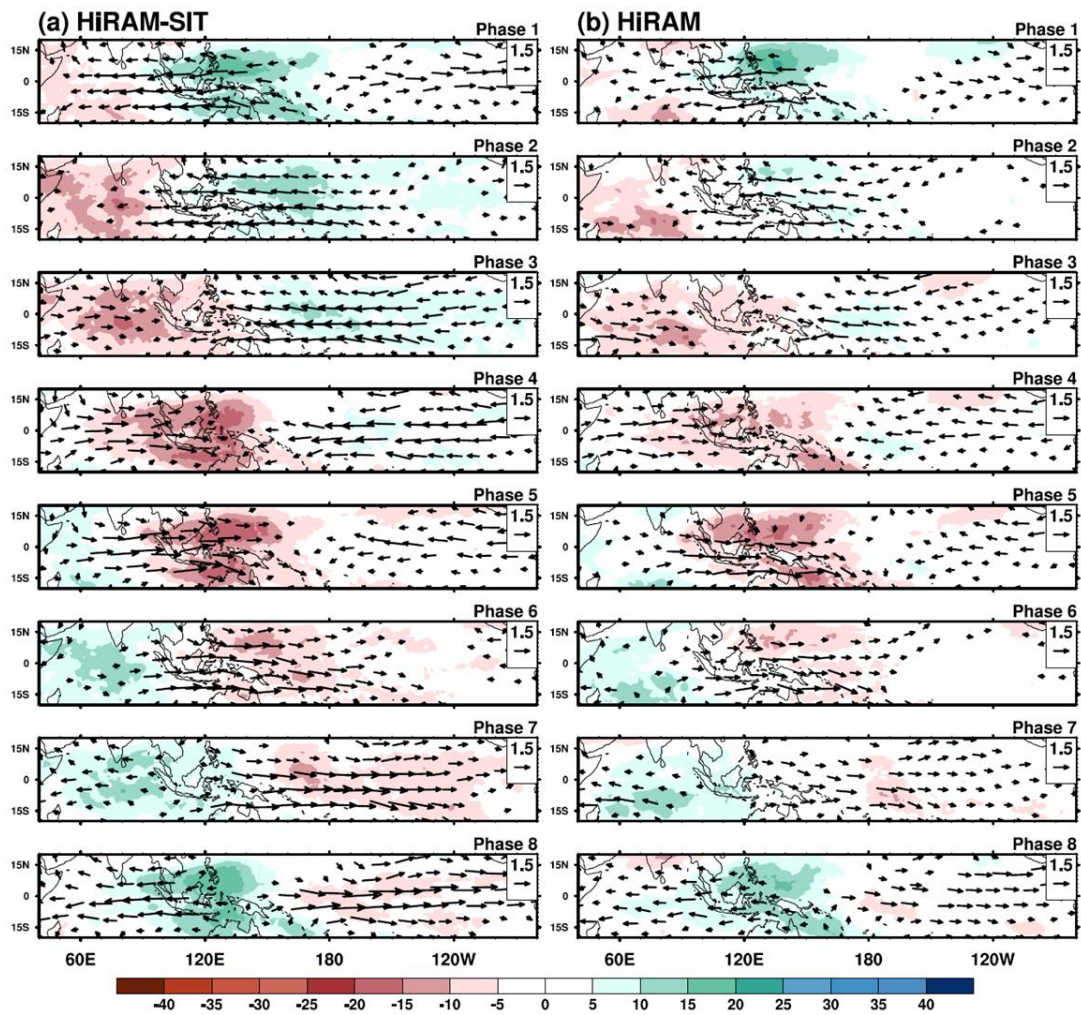
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22 **Figure S2.** Same as Fig. S1, but in (a) CAM5-SIT and (b) CAM5.

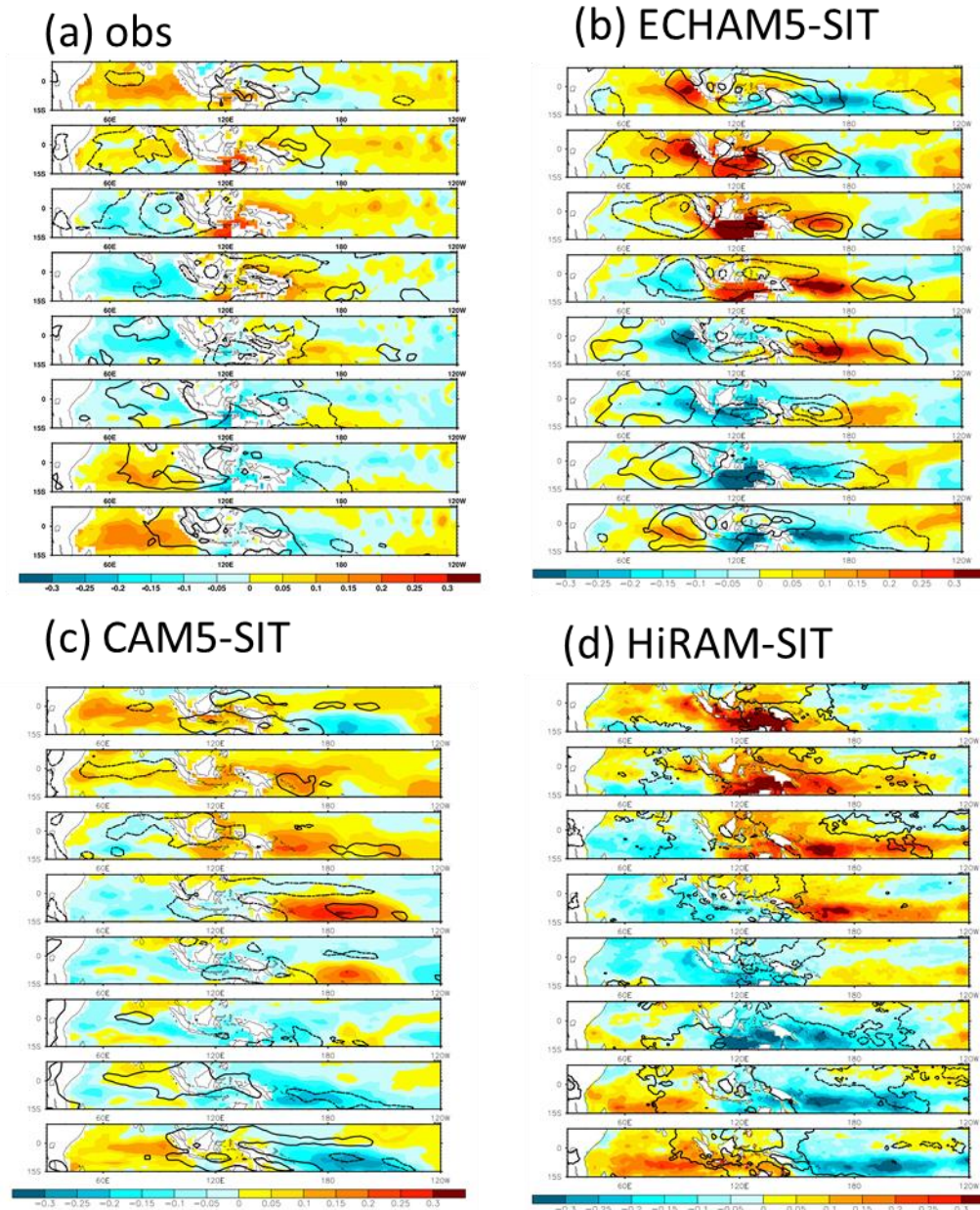
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25 **Figure S3.** Same as Fig. S1, but in (a) HiRAM-SIT and (b) HiRAM.

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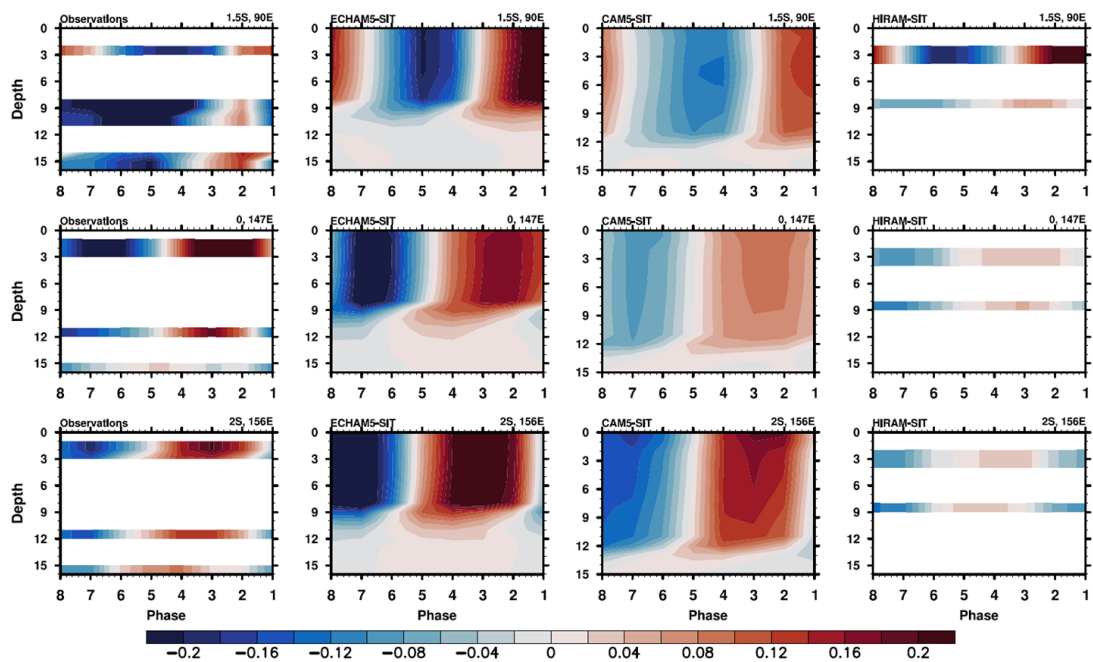


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28 **Figure S4.** Composite November–April 20–100-day filtering SST ($^{\circ}\text{C}$; color) and OLR29 anomalies (W m^{-1} ; vectors) as a function of the MJO phase based on (a) observations, (b)

30 ECHAM5-SIT, (c) CAM5-SIT, and (d) HiRAM-SIT.

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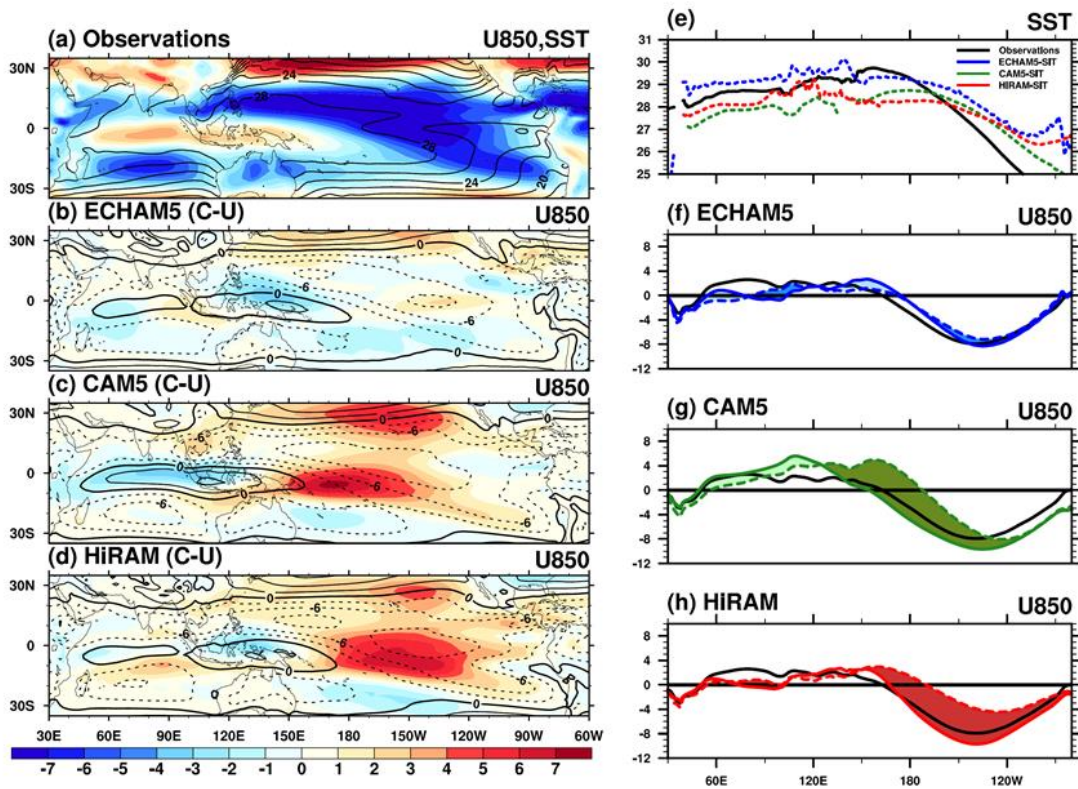


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33 **Figure S5.** Vertical ocean temperature ($^{\circ}\text{C}$) profiles with respect to MJO phases for
 34 intraseasonal anomalies (i.e., with 20–100-day filtering) in (a) observations and
 35 simulations by using the (b–d) coupled and (e–g) uncoupled AGCM. Observations are in
 36 suit with data from TAO. Because of storage limitations, only 3 and 10 m water
 37 temperatures are presented in the HIRAM-SIT simulation.

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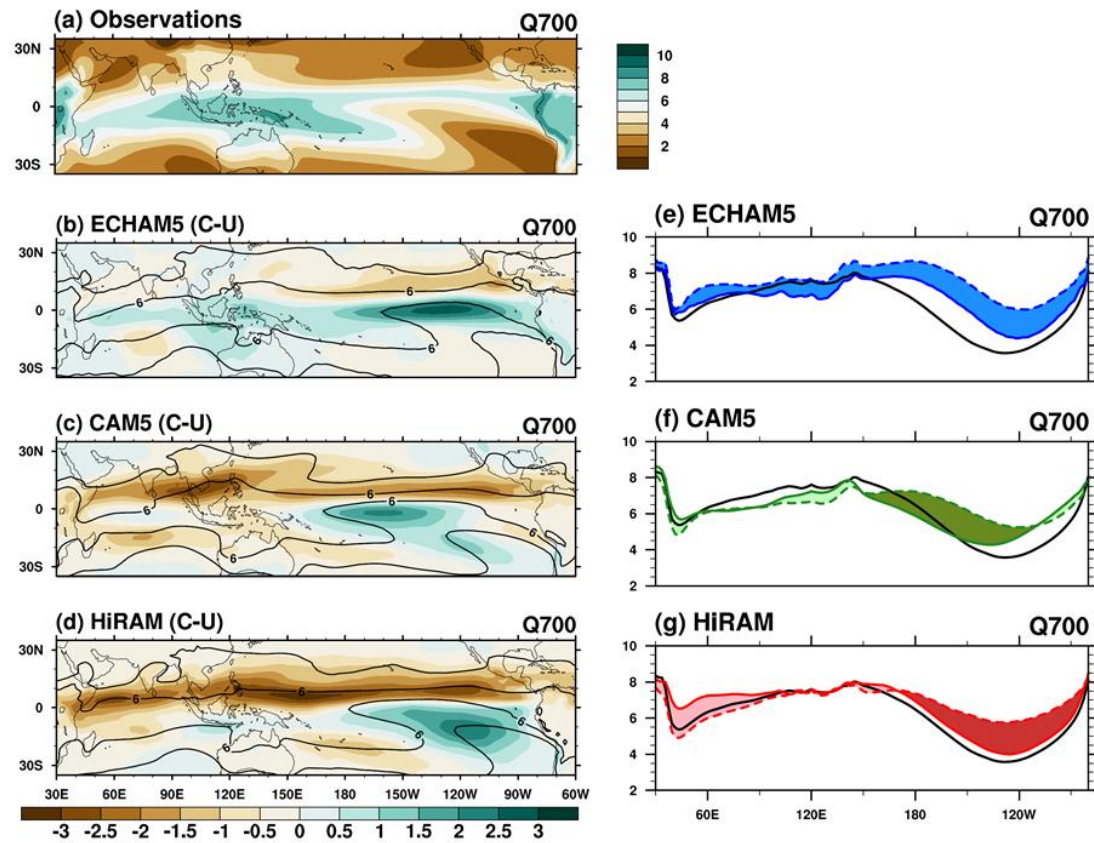


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41 **Figure S6.** (a) The observational winter (November–April) averaged the mean state in
 42 850 hPa zonal wind (m s^{-1} ; shading) and SST ($^{\circ}\text{C}$; contours). (b–d) The winter averaged
 43 850 hPa zonal wind difference of coupled and uncoupled simulations (m s^{-1} ; shading) and
 44 uncoupled 850 hPa zonal wind (m s^{-1} ; contours) in ECHAM5, CAM5, and HiRAM. (e)
 45 The 10°S –EQ averaged winter SST ($^{\circ}\text{C}$) in observation and simulations. (f–h) The 5°S –
 46 EQ averaged winter 850 hPa zonal wind (m s^{-1}) in ECHAM5, CAM5, and HiRAM. The
 47 solid line is uncoupled and the dashed line is a coupled model.

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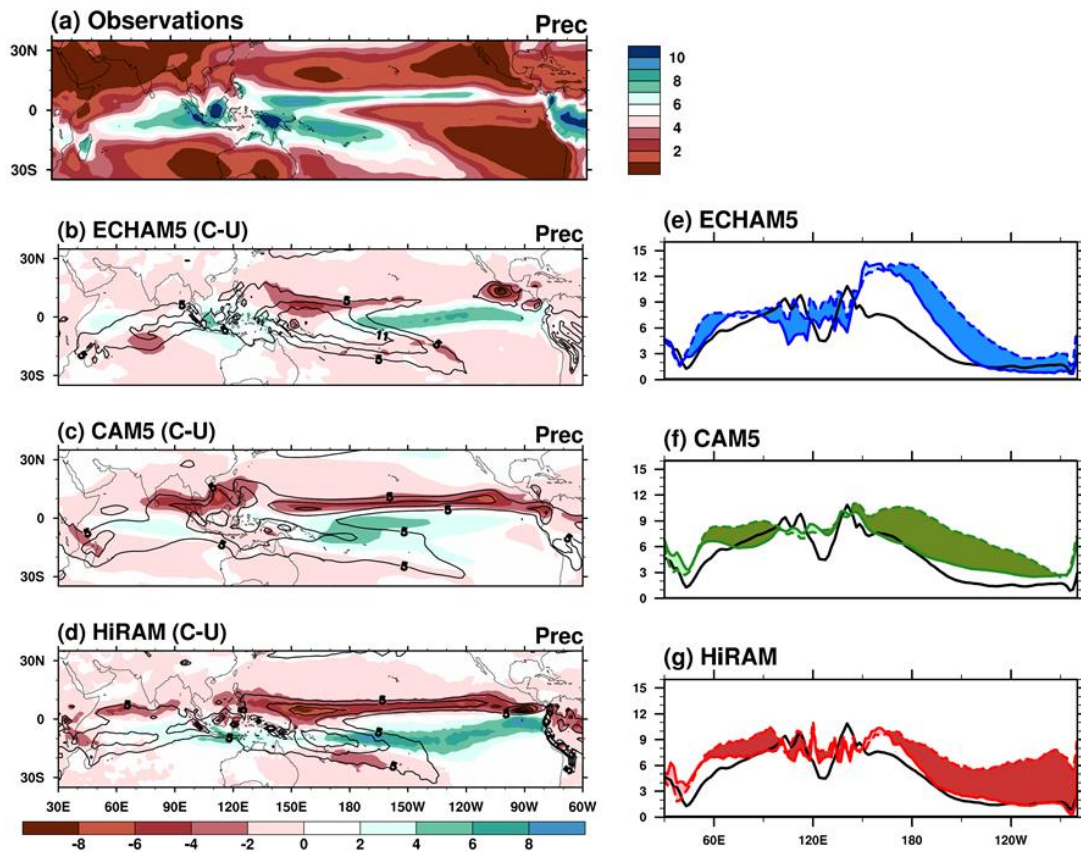
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51 **Figure S7.** (a) The observational winter (November–April) averaged mean state in
 52 specific humidity at 700 hPa (Q700; kg s^{-1} ; shading). (b–d) The winter averaged Q700
 53 difference of coupled and uncoupled simulations (mm day^{-1} ; shading) and uncoupled
 54 Q700 (kg s^{-1} ; contours) in ECHAM5, CAM5, and HiRAM. (e–g) The 10°S–EQ averaged
 55 winter Q700 (kg s^{-1}) in ECHAM5, CAM5, and HiRAM. The solid and dashed lines
 56 indicate uncoupled and coupled models, respectively.

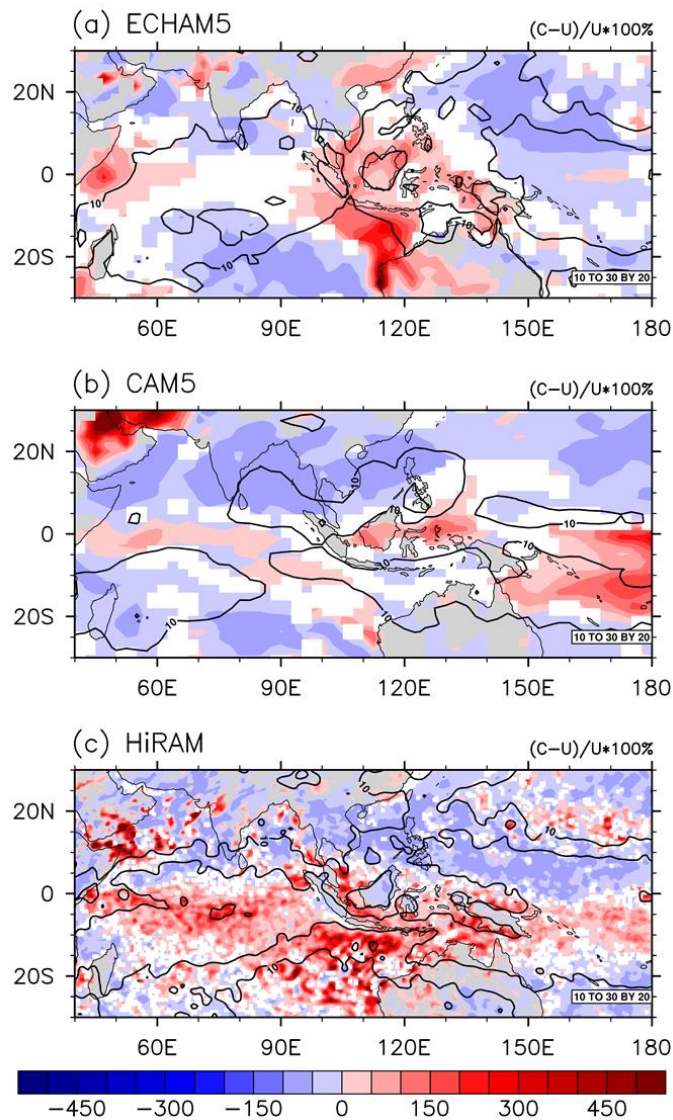
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59 **Figure S8.** (a) Observational winter (November–April) averaged mean state in
 60 precipitation (mm day^{-1} ; shading). (b–d) Winter averaged precipitation difference of
 61 coupled and uncoupled simulations (mm day^{-1} ; shading) and uncoupled precipitation (mm
 62 day^{-1} ; contours) in ECHAM5, CAM5, and HiRAM. (e–g) The 10°S –EQ averaged winter
 63 precipitation (mm day^{-1}) in ECHAM5, CAM5, and HiRAM. The solid and dashed lines
 64 indicate uncoupled and coupled models, respectively.

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67 **Figure S9.** Ratio of the precipitation variance between the coupled and uncoupled models68 on intraseasonal time scales. The ratio is defined as $(\text{coupled} - \text{uncoupled}) / \text{uncoupled} * 100\%$ 69 100% . The colored areas indicate where the ratio is statistically significant at 1% based70 on an F test. The contours show the intraseasonal precipitation variance $(\text{mm day}^{-1})^2$ in71 the uncoupled simulation. The 9-point local smoothing is applied in the intraseasonal
72 precipitation variance of HiRAM here (contours only).

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