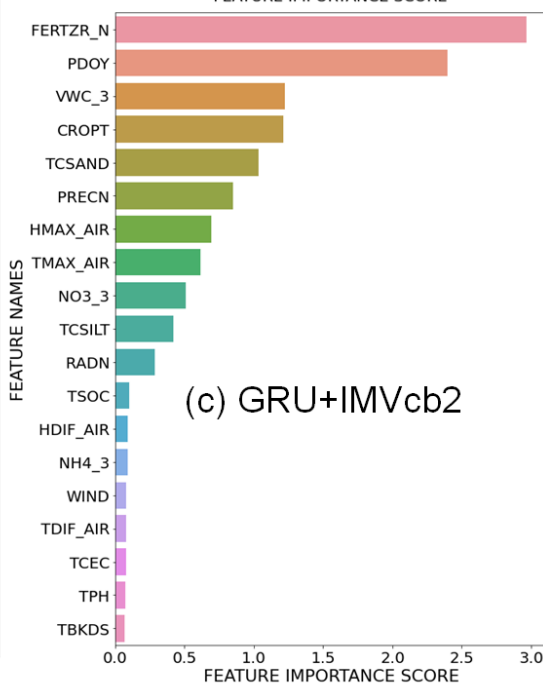
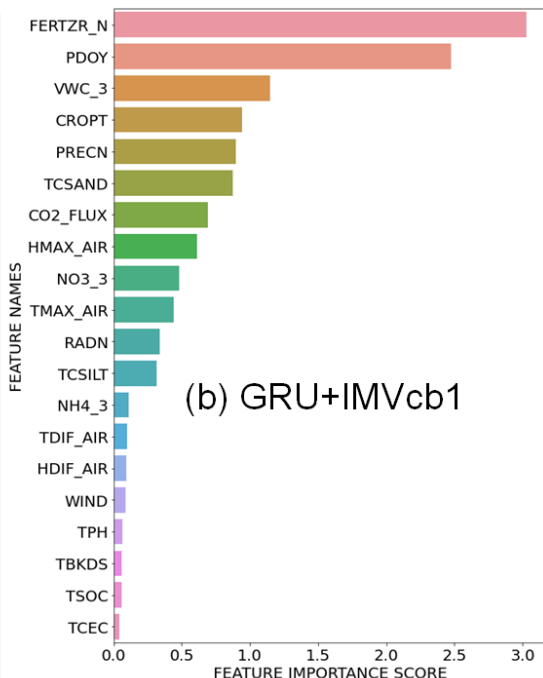
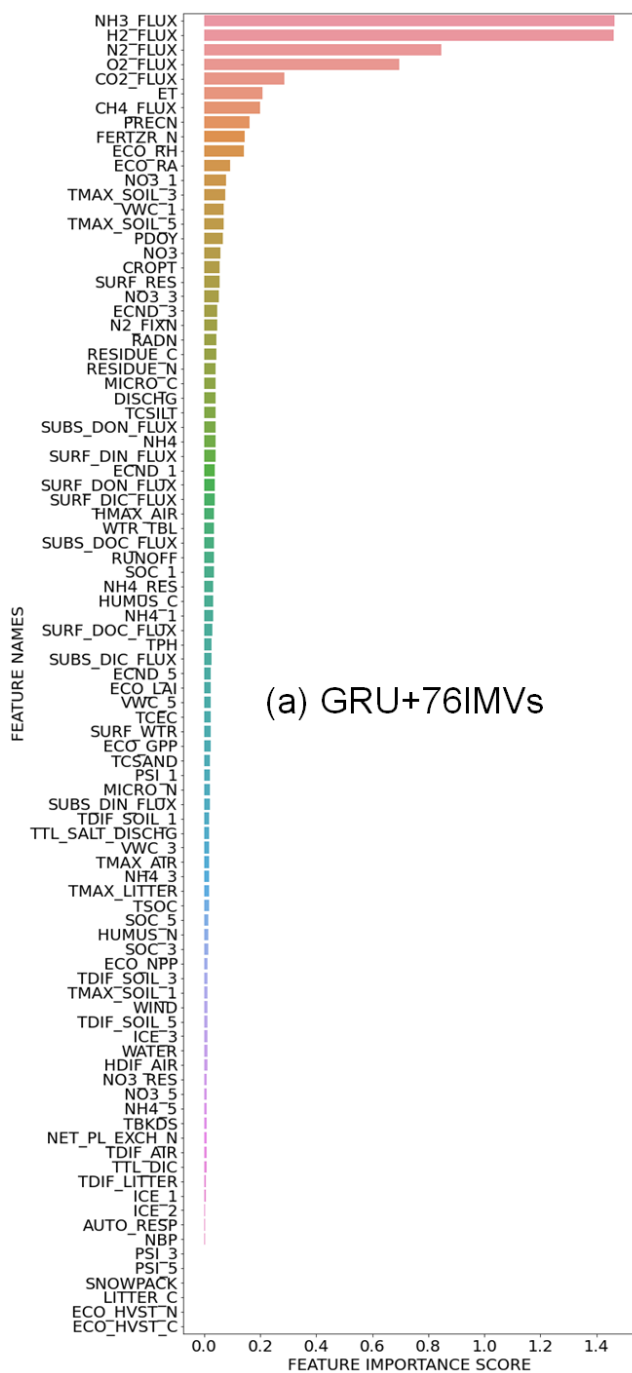
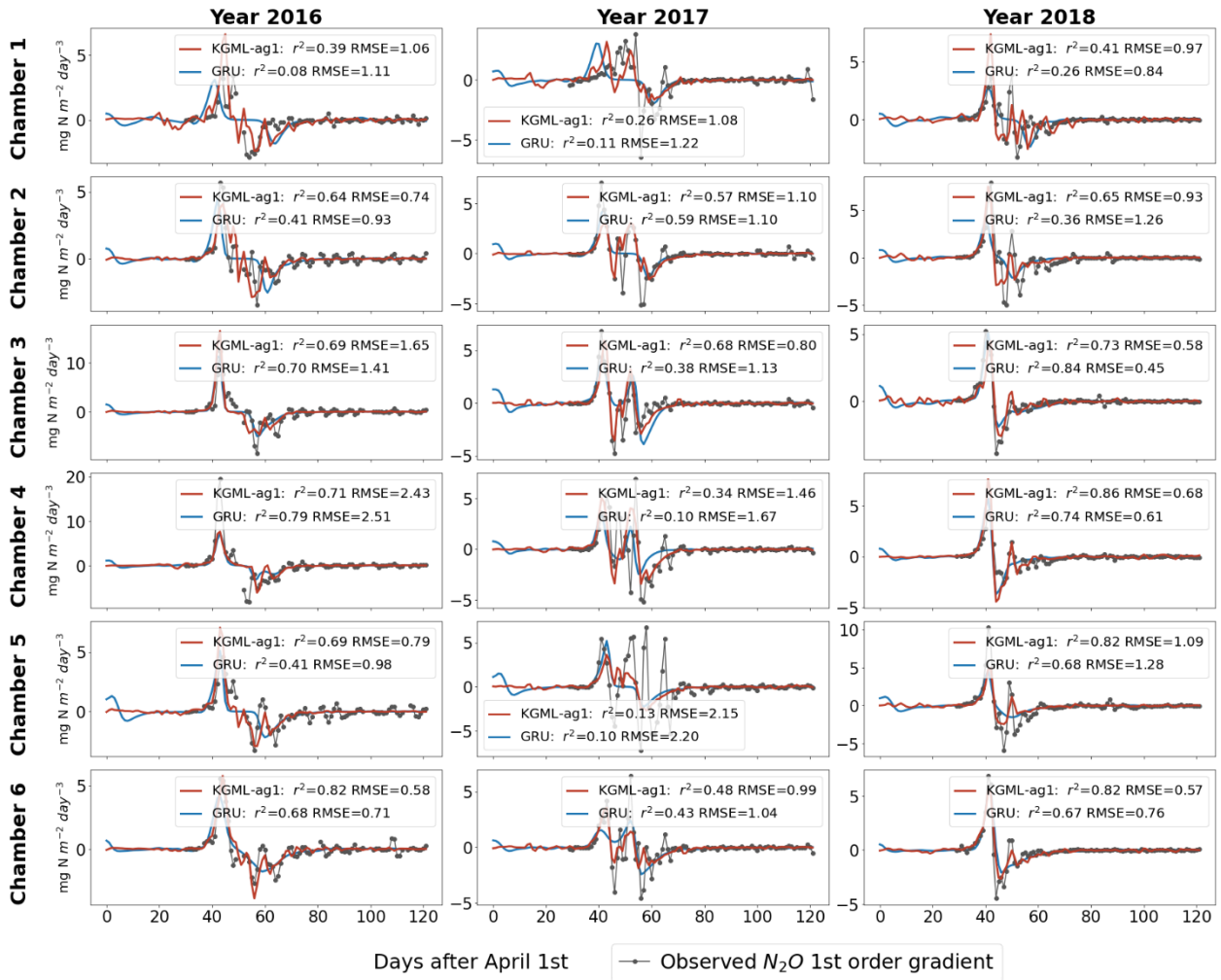


Figure S1: Time series example of observation data collected from mesocosm chamber 1. The precipitation, N fertilizer, Soil NO_3^- and NH_4^+ data are in daily time scale, while other data are in hourly time scale. Temperature presents in green; water related variables (precipitation and soil VWC) are in blue; N related variables (N fertilizer, N_2O flux, Soil NO_3^- and NH_4^+) are in purple; and CO_2 is in orange. Anomaly points will be down-weighted by daily averaging method with quality check in later processes, which is mentioned in section 2.2.2 last paragraph.



10 **Figure S2: Feature importance test for intermediate variables (IMVs) with GRU models. To be noticed the VWC, NO₃⁻, and NH₄⁺ from third layer soil, which are presented in the main text are abbreviated here as VWC_3, NO_{3_3}, and NH_{4_3} to be distinguished from the same variables from 1st and 5th layers. Details of the variables can be found in Table S1.**



15 Figure S3: N_2O flux 1st order gradient time series comparisons between non-pretrained GRU model and KGML-ag1. The black-dot line represents the observation, while blue represents GRU and red represents KGML-ag1.

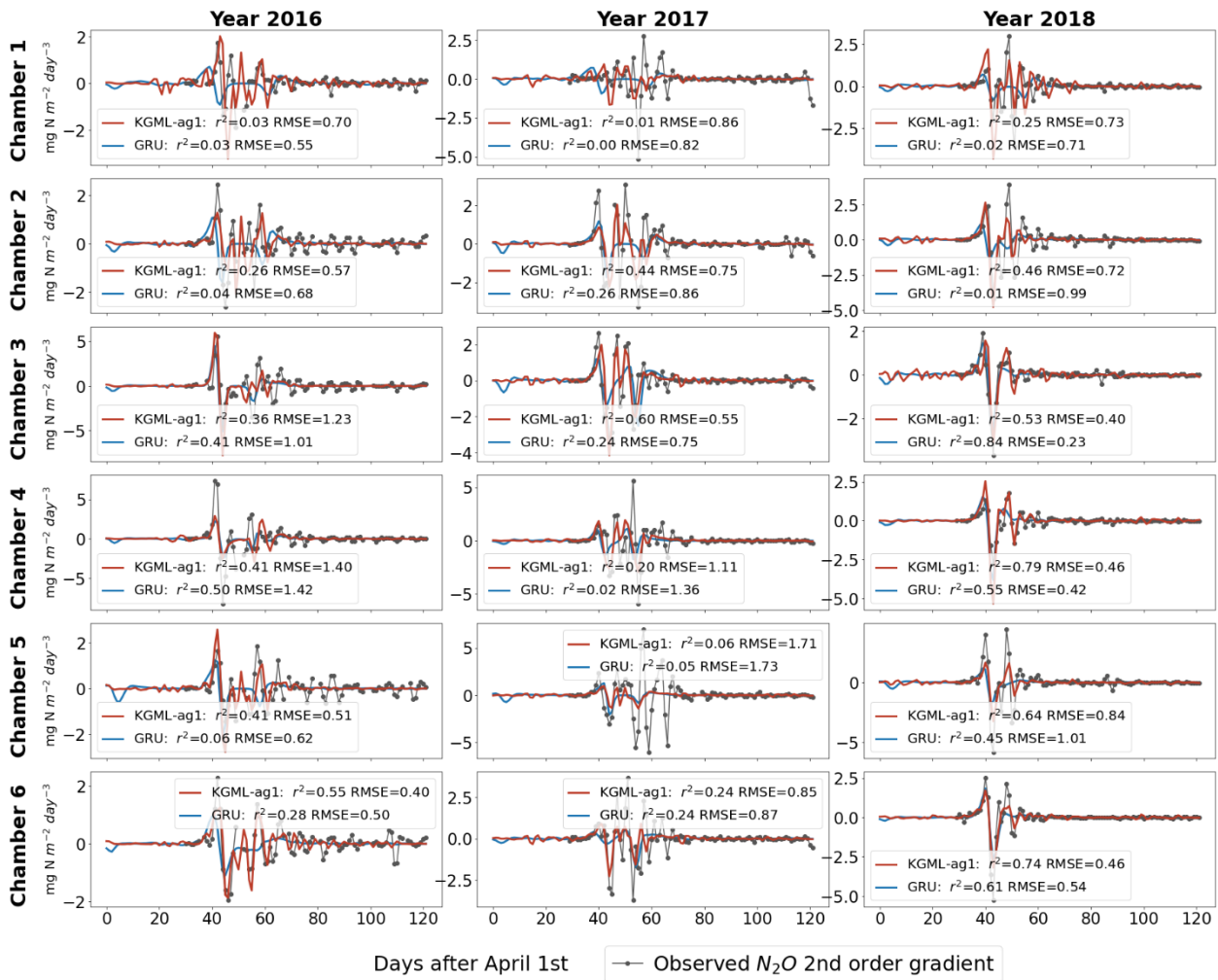


Figure S4: N_2O flux 2nd order gradient time series comparisons between non-pretrained GRU model and KGML-ag1. The black-dot line represents the observation, while blue represents GRU and red represents KGML-ag1.

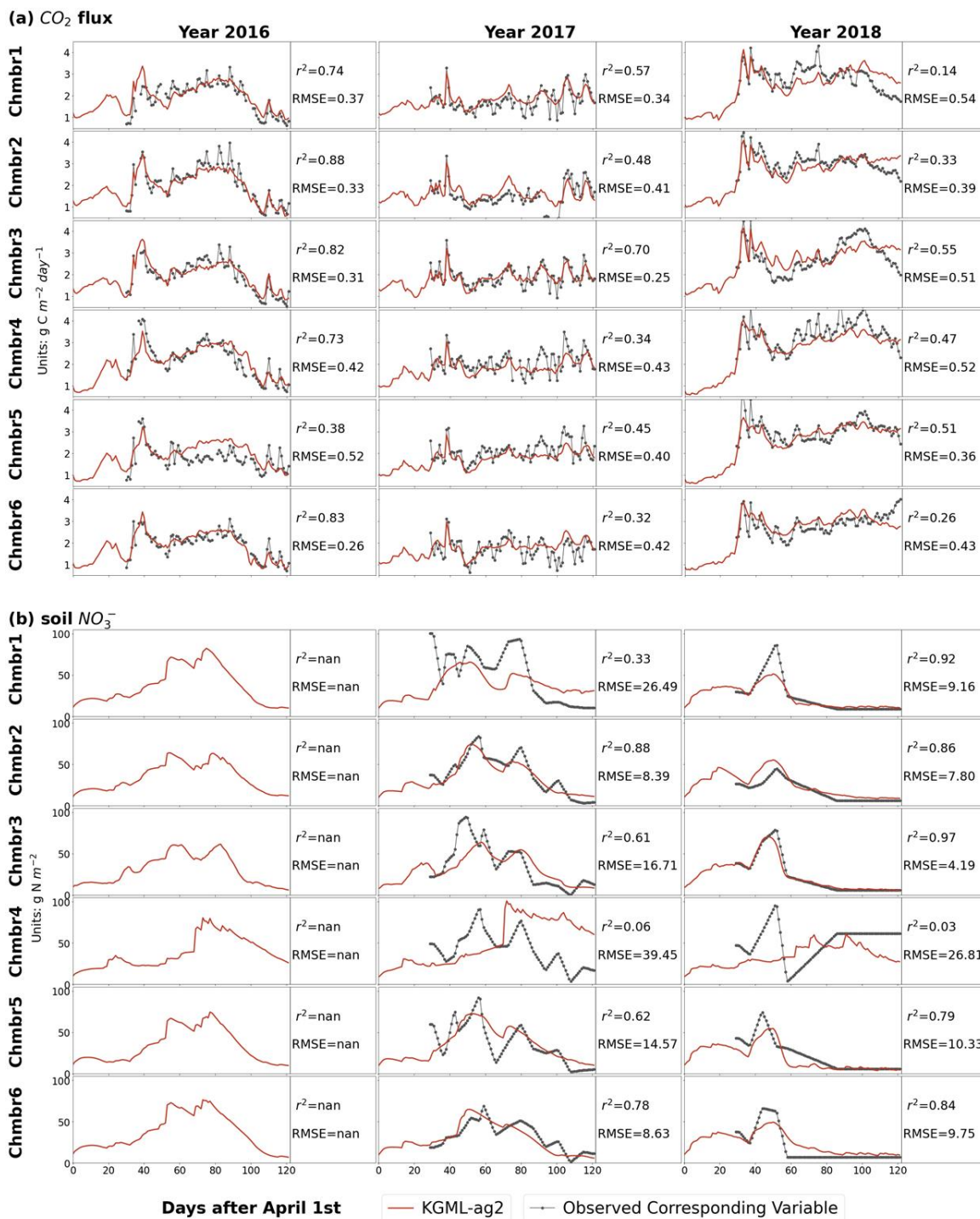
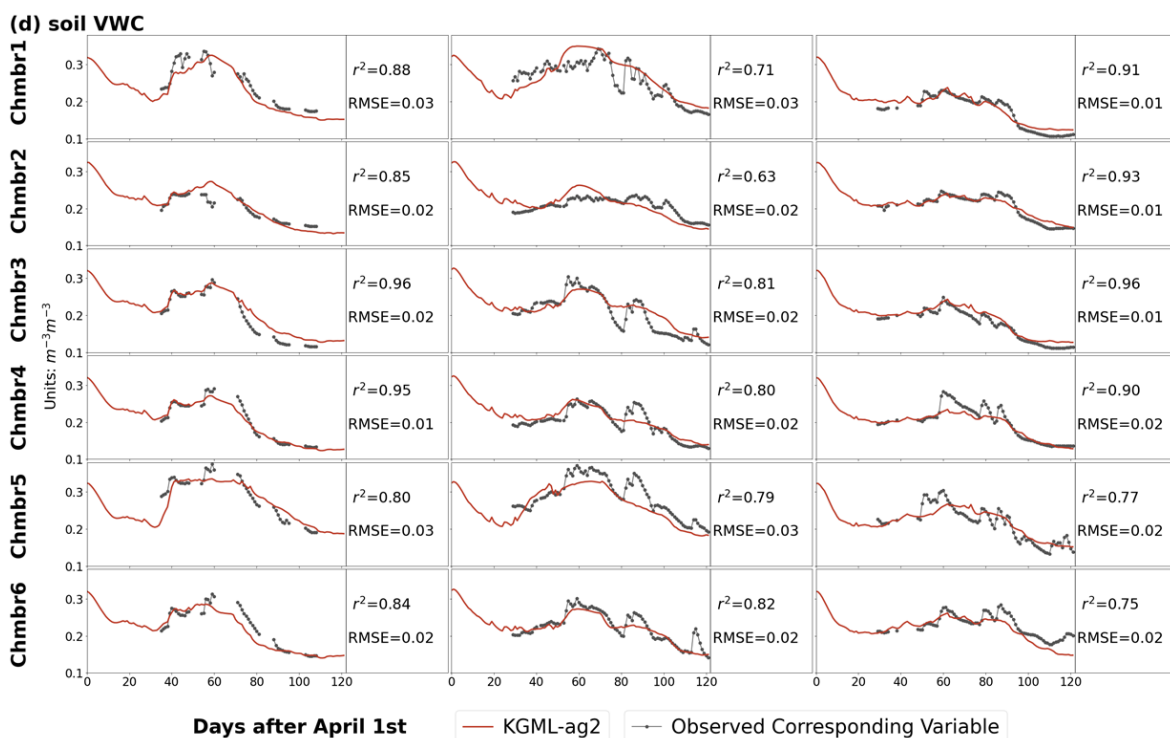
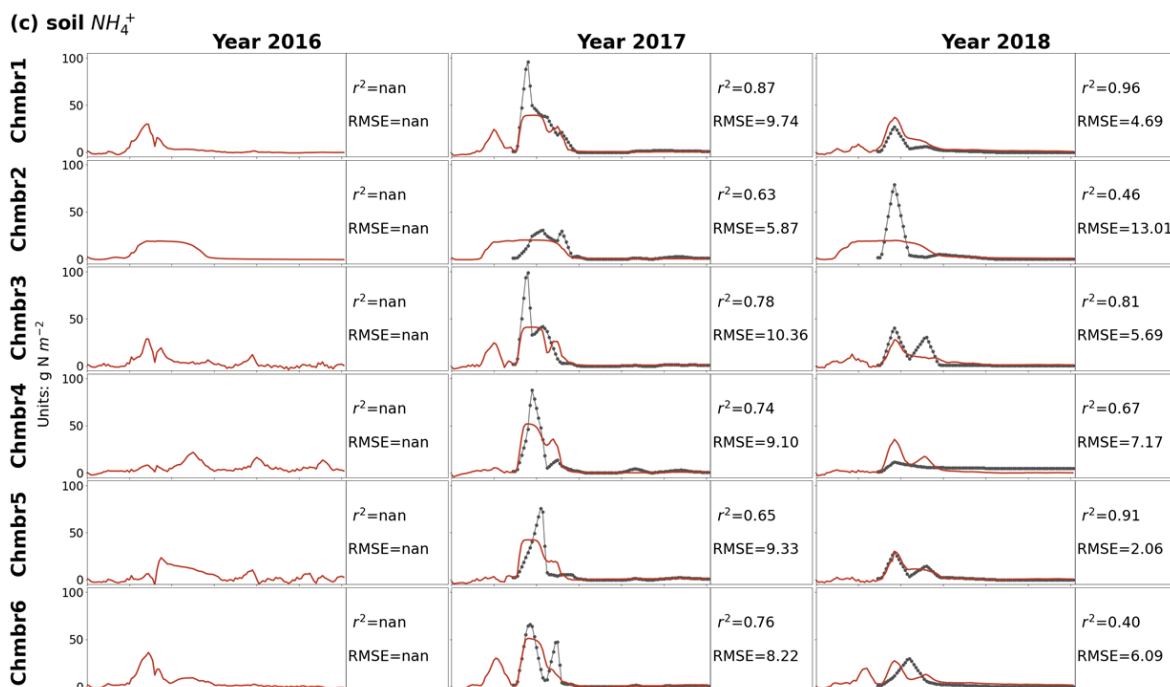
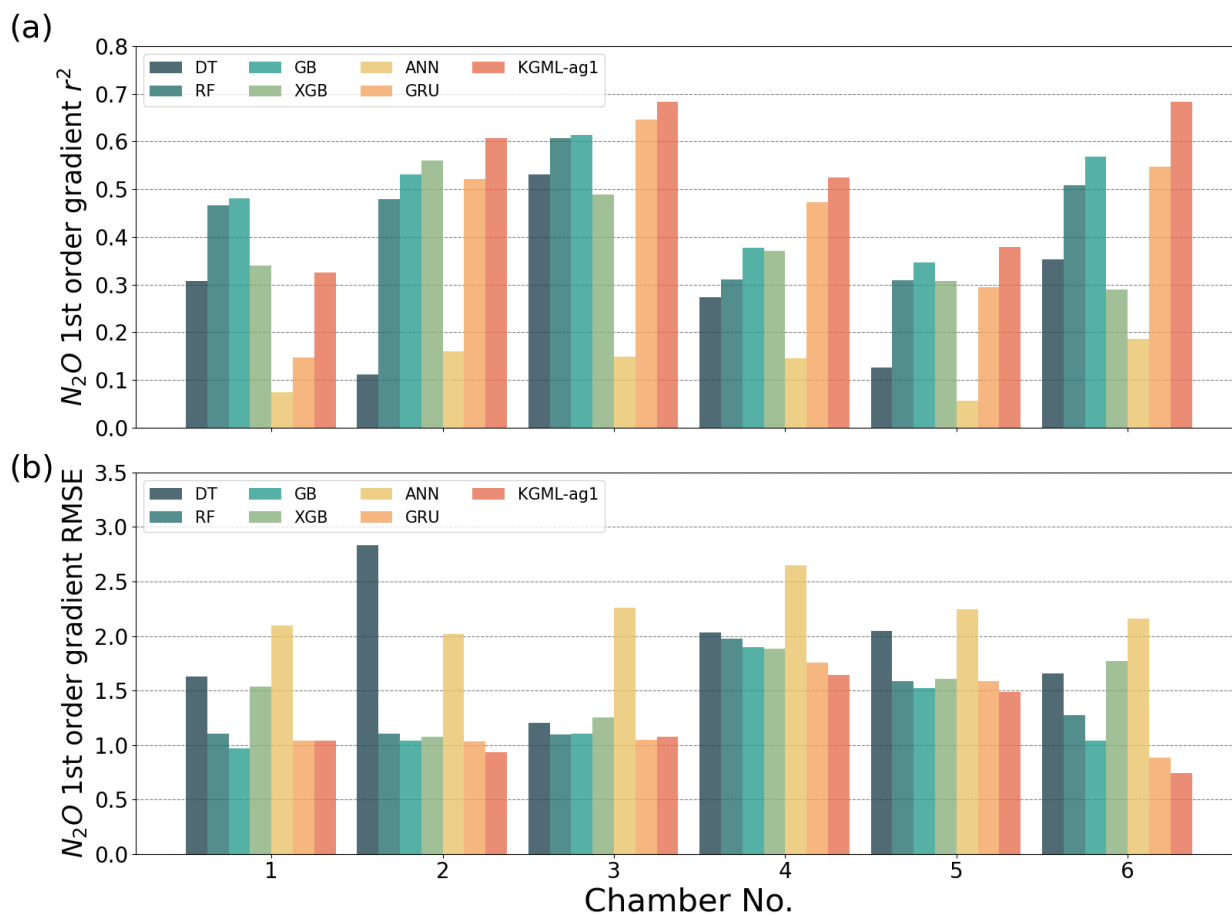


Figure S5: IMVs prediction from KGML-ag2. The black-dot line represents observations and the red line represents the results from KGML-ag2. Chmb is the abbreviation for chamber. r^2 and RMSE are calculated and present in each year and chamber.

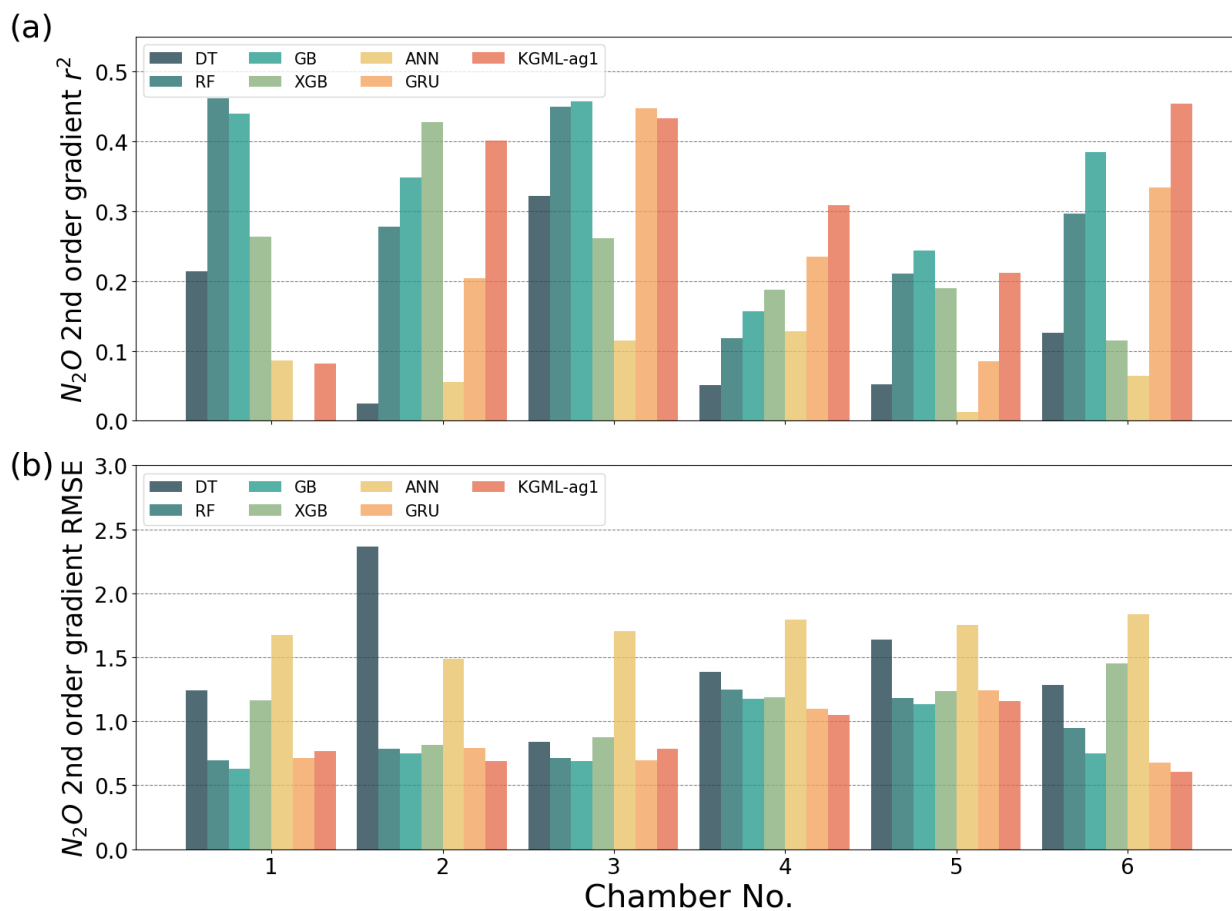


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Figure S5 contd.: IMVs prediction from KGML-ag2. The black-dot line represents observations and the red line represents the results from KGML-ag2. Chmb is the abbreviation for chamber. r^2 and RMSE are calculated and present in each year and chamber.

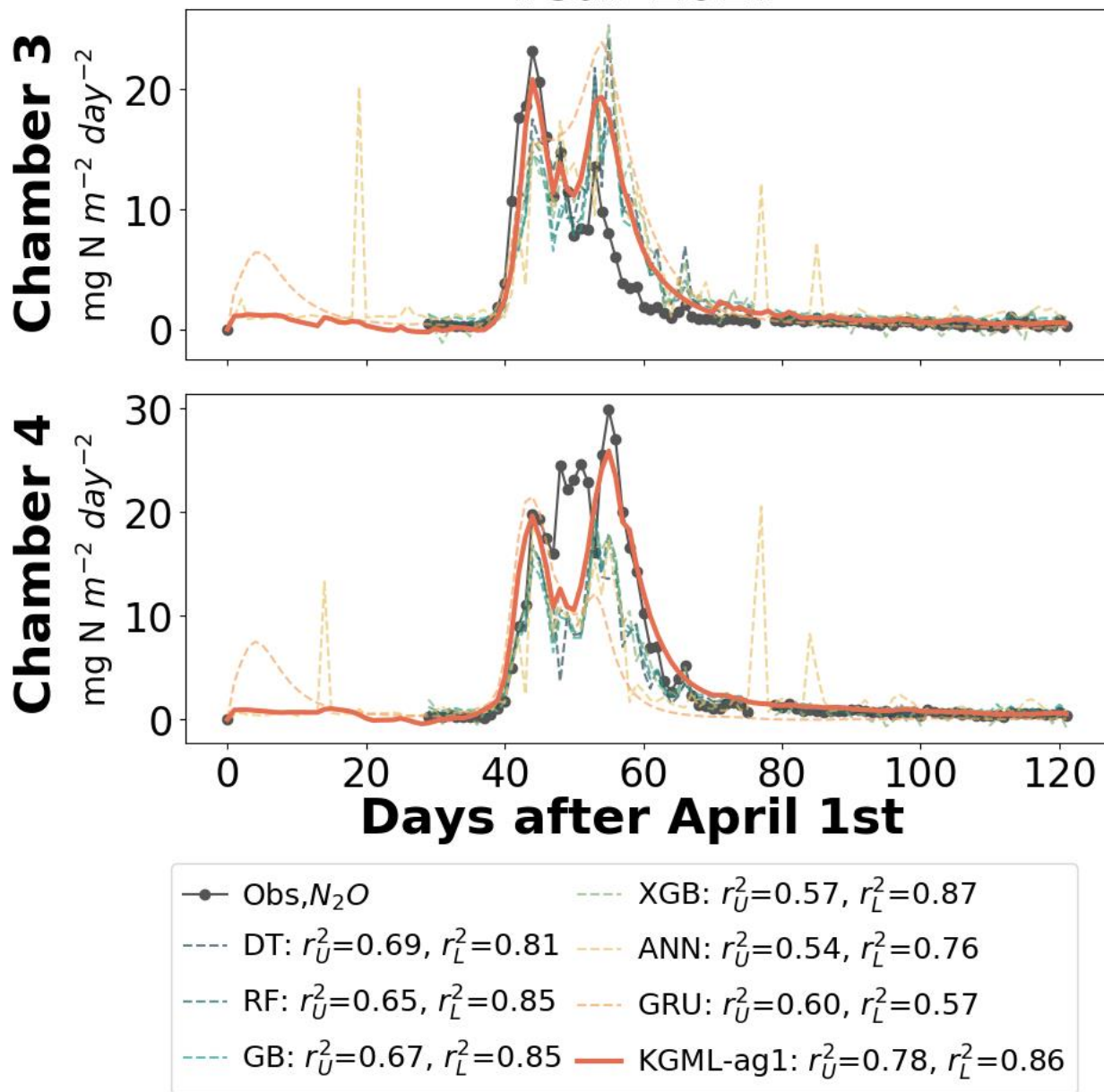


30 **Figure S6: The comparisons of N_2O 1st order gradient prediction accuracy r^2 (a) and (b) RMSE, between four tree-based ML models (DT, RF, GB and XGB), two deep learning models (ANN and GRU) and KGML-ag1 model in 6 chambers.**



35 **Figure S7: The comparisons of N₂O 2nd order gradient prediction accuracy r^2 (a) and (b) RMSE, between four tree-based ML models (DT, RF, GB and XGB), two deep learning models (ANN and GRU) and KGML-ag1 model in 6 chambers.**

Year 2017



40 Figure S8: N₂O flux time series comparisons between KGML-ag1 predictions (red solid line), pure ML models (other colored dashed line) and observations (black-dot line) from cross-validation on two representative panels of chamber 3 and 4 in 2016. The r^2 value was calculated between observations and model simulations. r_U^2 represents the r^2 value from upper panel (chamber 3) and r_L^2 represents the r^2 value from lower panel (chamber 4).

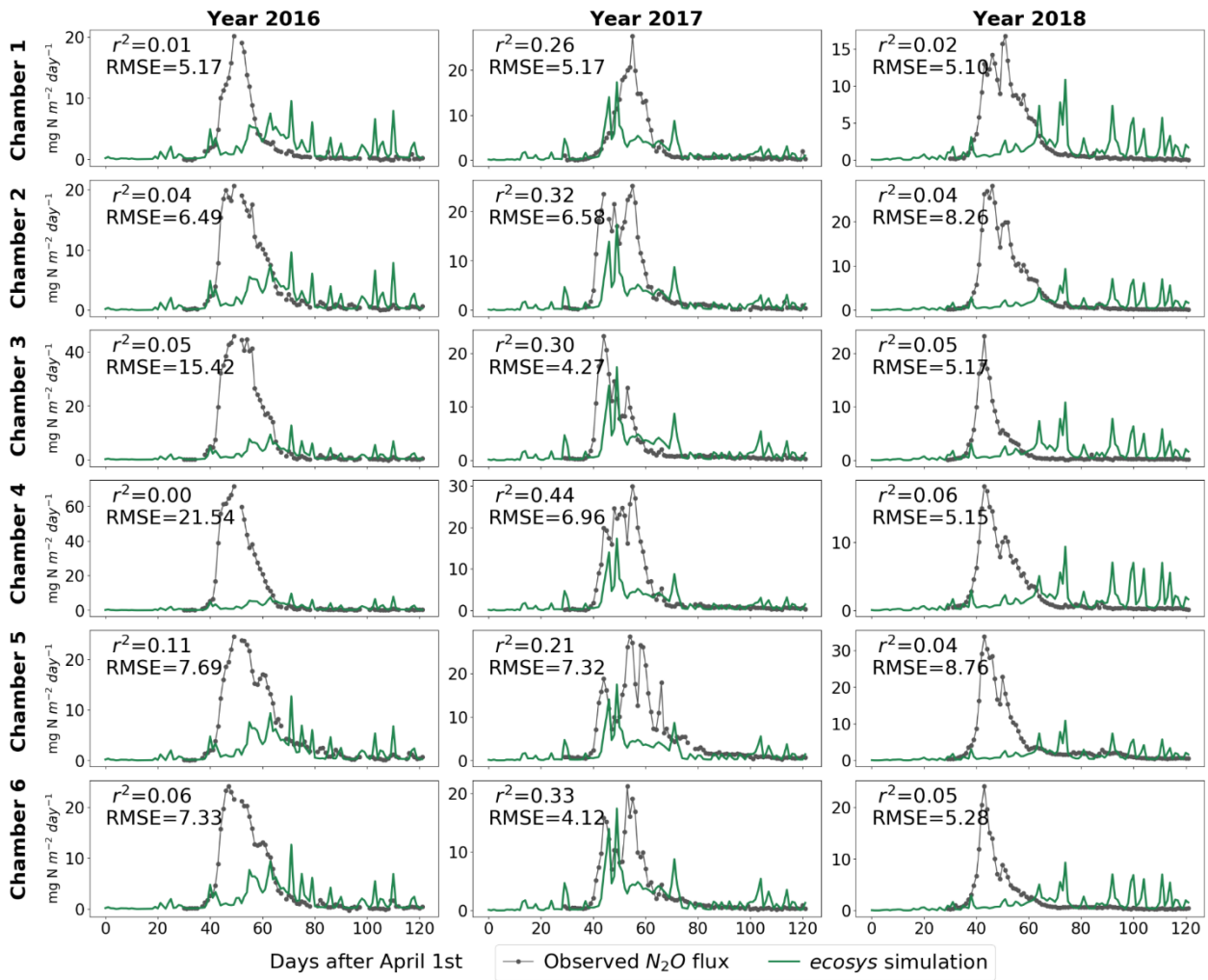


Figure S9: N_2O flux time series comparisons between *ecosys* simulations (green line) and observations (black-dot line).

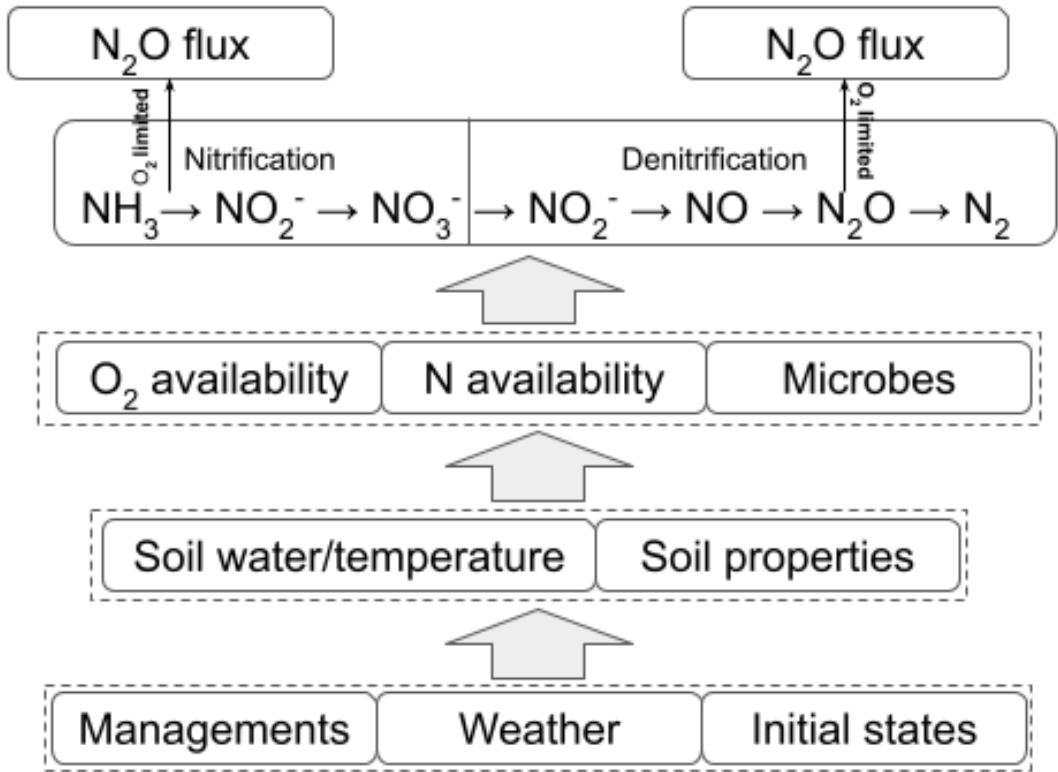


Figure S10: The simplified schema of N₂O flux related variables and processes.

50 **Table S1: Variable short abbreviation, category (IMV represents intermediate variable, W represents weather forcing, FN represents the N fertilizer rate, SCP represents soil/crop property and target variable), description and units.**

No.	Abbreviation	Variable category	Descriptions	Units
1	RESIDUE_C	IMV	Total residue C on soil surface and in soil profile	g C m ⁻²
2	HUMUS_C	IMV	Total particulate + non-particulate C in soil profile	g C m ⁻²
3	LITTER_C	IMV	C in above + below-ground litterfall	g C m ⁻²
4	CO2_FLUX	IMV	CO ₂ flux at the soil surface	g C m ⁻² day ⁻¹
5	O2_FLUX	IMV	O ₂ flux at the soil surface	g O ₂ m ⁻² day ⁻¹
6	AUTO_RESP	IMV	Below-ground autotrophic (root) respiration	g C m ⁻² day ⁻¹
7	MICRO_C	IMV	Microbial C in all residue and humus complexes	g C m ⁻²
8	SURF_RES	IMV	Residue C on soil surface and in soil profile	g C m ⁻²
9	CH4_FLUX	IMV	CH ₄ flux at the soil surface	g C m ⁻² day ⁻¹
10	SURF_DOC_FLUX	IMV	Flux of organic C across all external surface boundaries in runoff and sediment	g C m ⁻² day ⁻¹
11	SUBS_DOC_FLUX	IMV	Flux of organic C across all external subsurface boundaries in water discharge	g C m ⁻² day ⁻¹
12	SURF_DIC_FLUX	IMV	Flux of inorganic C across all external surface boundaries in runoff and sediment	g C m ⁻² day ⁻¹
13	SUBS_DIC_FLUX	IMV	Flux of inorganic C across all external subsurface boundaries in water discharge	g C m ⁻² day ⁻¹
14	NBP	IMV	Net biome productivity	g C m ⁻² day ⁻¹
15	SOC_1	IMV	Residue + humus C in soil layer 1, 5cm depth	g C m ⁻²
16	SOC_3	IMV	Residue + humus C in soil layer 3, 15cm depth	g C m ⁻²
17	SOC_5	IMV	Residue + humus C in soil layer 5, 28cm depth	g C m ⁻²
18	H2_FLUX	IMV	H ₂ flux at the soil surface	g H ₂ m ⁻² day ⁻¹
19	ECO_HVST_C	IMV	C removed in harvest	g C m ⁻²
20	ECO_LAI	IMV	Leaf area index	m ² m ⁻²
21	ECO_GPP	IMV	Gross primary productivity	g C m ⁻² day ⁻¹
22	ECO_RA	IMV	Autotrophic respiration	g C m ⁻² day ⁻¹
23	ECO_NPP	IMV	Net primary productivity	g C m ⁻² day ⁻¹
24	ECO_RH	IMV	Heterotrophic respiration	g C m ⁻² day ⁻¹
25	TTL_DIC	IMV	Total stocks of dissolved inorganic C	g C m ⁻²
26	ET	IMV	Evapotranspiration rate	mm day ⁻¹
27	RUNOFF	IMV	Overland surface flow	mm day ⁻¹
28	WATER	IMV	The total amount of water in the rooting zone of the soil profile	mm day ⁻¹
29	DISCHG	IMV	Water discharge flux through all subsurface boundaries	mm
30	SNOWPACK	IMV	The equivalent water content of snow + ice + water in the snowpack	mm
31	VWC_1	IMV	The volumetric water content in soil layer 1, 5cm depth	m ³ m ⁻³
32	VWC_3	IMV	The volumetric water content in soil layer 3, 15cm depth	m ³ m ⁻³
33	VWC_5	IMV	The volumetric water content in soil layer 5, 28cm depth	m ³ m ⁻³

34	SURF_WTR	IMV	Near surface volumetric water content	$m^3 m^{-3}$
35	ICE_1	IMV	The volumetric ice content in soil layer 1, 5cm depth	$m^3 m^{-3}$
36	ICE_2	IMV	The volumetric ice content in soil layer 3, 15cm depth	$m^3 m^{-3}$
37	ICE_3	IMV	The volumetric icecontent in soil layer 5, 28cm depth	$m^3 m^{-3}$
38	PSI_1	IMV	The matric water potential in soil layer 1, 5cm depth	Mpa
39	PSI_3	IMV	The matric water potential in soil layer 3, 15cm depth	Mpa
40	PSI_5	IMV	The matric water potential in soil layer 5, 28cm depth	Mpa
41	WTR_TBL	IMV	Depth of the water table from the surface	m
42	RESIDUE_N	IMV	Total residue N on soil surface and in soil profile	$g N m^{-2}$
43	HUMUS_N	IMV	Total particulate + non-particulate N in soil profile	$g N m^{-2}$
44	FERTZR_N	FN	N fertilizer applied	$g N m^{-2}$
45	NET_PL_EXCH_N	IMV	Net N exchange between soil and plants	$g N m^{-2} day^{-1}$
46	NH4	IMV	Total $NH_4^+ + NH_3$ in the soil profile	$g N m^{-2}$
47	NO3	IMV	Total NO_3^- in soil profile	$g N m^{-2}$
48	SURF_DON_FLUX	IMV	Flux of organic N across all external surface boundaries in runoff and sediment	$g N m^{-2} day^{-1}$
49	SUBS_DON_FLUX	IMV	Flux of organic N across all external subsurface boundaries in water discharge	$g N m^{-2} day^{-1}$
50	SURF_DIN_FLUX	IMV	Flux of inorganic N across all external surface boundaries in runoff and sediment	$g N m^{-2} day^{-1}$
51	SUBS_DIN_FLUX	IMV	Flux of inorganic N across all external subsurface boundaries in water discharge	$g N m^{-2} day^{-1}$
52	N2O_FLUX	Target variable	N_2O flux at the soil surface	$g N m^{-2} day^{-1}$
53	NH3_FLUX	IMV	NH_3 flux at soil and plant surfaces	$g N m^{-2} day^{-1}$
54	N2_FIXN	IMV	Aerobic + anaerobic non-symbiotic N_2 fixation + symbiotic N_2 fixation	$g N m^{-2} day^{-1}$
55	MICRO_N	IMV	Total microbial N in all residue and humus complexes	$g N m^{-2}$
56	NH4_1	IMV	Total $NH_4^+ + NH_3$ concentration in soil layer 1, 5cm depth	$g N m^{-2}$
57	NH4_3	IMV	Total $NH_4^+ + NH_3$ concentration in soil layer 3, 15cm depth	$g N m^{-2}$
58	NH4_5	IMV	Total $NH_4^+ + NH_3$ concentration in soil layer 5, 28cm depth	$g N m^{-2}$
59	NO3_1	IMV	Total $NO_3^- + NO_2^-$ concentration in soil layer 1, 5cm depth	$g N m^{-2}$
60	NO3_3	IMV	Total $NO_3^- + NO_2^-$ concentration in soil layer 3, 15cm depth	$g N m^{-2}$
61	NO3_5	IMV	Total $NO_3^- + NO_2^-$ concentration in soil layer 5, 28cm depth	$g N m^{-2}$
62	NH4_RES	IMV	Residue $NH_4^+ + NH_3$ on soil surface and in soil profile	$g N m^{-2}$
63	NO3_RES	IMV	Residue $NO_3^- + NO_2^-$ on soil surface and in soil profile	$g N m^{-2}$
64	ECO_HVST_N	IMV	N removed in harvest	$g N m^{-2} day^{-1}$
65	N2_FLUX	IMV	N_2 flux at the soil surface	$g N m^{-2} day^{-1}$
66	RADN	W	Solar Radiation	$W m^{-2}$
67	TMAX_AIR	W	Max air temperature	$^{\circ}C$
68	TDIF_AIR	W	Difference between max and min air temperature	$^{\circ}C$
69	HMAX_AIR	W	Max humidity	fraction

70	HDIF_AIR	W	Difference between max and min humidity	fraction
71	WIND	W	Wind speed	m s ⁻¹
72	PRECN	W	Precipitation	mm day ⁻¹
73	TMAX_SOIL_1	IMV	The maximum temperature in soil layer 1, 5cm depth	°C
74	TDIF_SOIL_1	IMV	The difference between max and min temperature temperature in soil layer 1 , 5cm depth	°C
75	TMAX_SOIL_3	IMV	The maximum temperature in soil layer 3, 15cm depth	°C
76	TDIF_SOIL_3	IMV	The difference between max and min temperature temperature in soil layer 3, 15cm depth	°C
77	TMAX_SOIL_5	IMV	The maximum temperature in soil layer 5, 28cm depth	°C
78	TDIF_SOIL_5	IMV	The difference between max and min temperature temperature in soil layer 5, 28cm depth	°C
79	TMAX_LITTER	IMV	The maximum temperature in litter	°C
80	TDIF_LITTER	IMV	The difference between max and min temperature temperature in litter	°C
81	ECND_1	IMV	Electrical conductivity in soil layer 1, 5cm depth	dS m ⁻¹
82	ECND_3	IMV	Electrical conductivity in soil layer 3, 15cm depth	dS m ⁻¹
83	ECND_5	IMV	Electrical conductivity in soil layer 5, 28cm depth	dS m ⁻¹
84	TTL_SALT_DISCHG	IMV	Total salt discharge through water through all subsurface boundaries	g Mg ⁻¹ day ⁻¹
85	PDOY	SCP	Plant day of the year	day
86	CROPT	SCP	Crop type, 1 for corn and 0 for soybean	unitless
87	TBKDS	SCP	Depth weighted averaged bulk density in soil profile	Mg m ⁻³
88	TCSAND	SCP	Depth weighted averaged sand content in soil profile	g kg ⁻¹
89	TCSILT	SCP	Depth weighted averaged silt content in soil profile	g kg ⁻¹
90	TPH	SCP	Depth weighted averagedpH in soil profile	unitless
91	TCEC	SCP	Depth weighted averaged cmol+ kg-1 in soil profile	cmol ⁻¹ kg ⁻¹
92	TSOC	SCP	Depth weighted averaged soil organic carbon in soil profile	g C kg ⁻¹

55 **Table S2: N₂O prediction accuracy comparisons between LSTM and GRU models on synthetic data, with different combinations of IMVs (+9 or +58IMVs) and different sliding window settings during training (e.g. 2y1y represent window size is 2 years and the window move 1 year after 1 iteration). Training Efficiency is also compared between LSTM and GRU models for the first two experiments, with changing the training counties = 3, 10, 30, 70, validation counties = 1, 2, 5, 10, and batch size (county numbers input in each iteration) = 1, 5, 5, 5.**

Experiment settings	N ₂ O prediction accuracy		Training efficiency			
	Test r ²	Test RMSE	Train=3, val=1, batch =1	Train=10, val=2, batch =5	Train=30, val=5, batch =5	Train=70, val=10, batch =5
LSTM+9IMVs+1y1y	0.74	1.32	3.8s	3.3s	9.2s	22s
GRU+9IMVs+1y1y	0.81	1.08	3.5s	2.7s	7.2s	17s
LSTM+58IMVs+1y1y	0.91	0.6				
GRU+58IMVs+1y1y	0.92	0.59				
LSTM+58IMVs+2y2y	0.86	0.76				
GRU+58IMVs+2y2y	0.9	0.66				
LSTM+58IMVs+2y1y	0.89	0.67				
GRU+58IMVs+2y1y	0.91	0.6				

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