Earth System Model Parameter Adjustment Using a Green's Functions Approach

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Abstract. We demonstrate the practicality and effectiveness of using a Green's functions estimation approach for adjusting uncertain parameters in an Earth System Model (ESM). This estimation approach had previously been applied to an intermediate-complexity climate model and to individual ESM components, e.g., ocean, sea-ice, or carbon-cycle components. Here, the Green's functions approach is applied to a state-of-the-art ESM that comprises a global atmosphere-land configuration of the Goddard Earth Observing System (GEOS) coupled to an ocean and sea-ice configuration of the Massachusetts Institute of Technology general circulation model (MITgcm). Horizontal grid spacing is approximately 110 km for GEOS and 37–110 km for MITgcm. In addition to the reference GEOS-MITgcm simulation, we ~~carry~~ carried out a series of model sensitivity experiments, in which 20 uncertain parameters are perturbed. These "control" parameters can be used to adjust sea-ice, microphysics, turbulence, radiation, and surface schemes in the coupled simulation. We ~~define~~ defined eight observational targets: sea-ice fraction, net surface shortwave radiation, downward longwave radiation, near-surface temperature, sea surface temperature, sea surface salinity, and ocean temperature and salinity at 300 m. We applied the Green's functions approach to optimize the values of the 20 control parameters so as to minimize a weighted least-squares distance between the model and the eight observational targets. The new experiment with the optimized parameters resulted in a total cost reduction of 9% relative to a simulation that had already been adjusted using other methods. The optimized experiment attained a balanced cost reduction over most of the observational targets. We also report on results from a set of sensitivity experiments that are not used in the final optimized simulation but helped explore options and guided the optimization process. These experiments include an assessment of sensitivity to the number of control parameters and to the selection of observational targets and weights in the cost function. Based on these sensitivity experiments, we selected a specific definition for the cost function. The sensitivity experiments also revealed a decreasing overall cost as the number of control variables was increased. In summary, we recommend using the Green's functions estimation approach as an additional fine-tuning step in the model development process. The method is not a replacement for modelers' experience in choosing and adjusting sensitive model parameters. Instead, it is an additional practical and effective tool for carrying out final adjustments of uncertain ESM parameters.

1 Introduction

Earth System Models (ESMs) include various parameters that govern the representation of unresolved, unrepresented, or under-observed processes in the models. The most sensitive parameters are typically adjusted during the last step of model development relative to observational targets. Currently, there is no agreed-upon methodology to adjust model parameters. As an illustration of the range of approaches and observational targets, Schmidt et al. (2017) describe the vast range of tuning strategies used for ESM development in U.S. modeling centers. Parameter adjustment aims to improve the representation of various processes or key state fields in the model relative to a ~~pre-determined~~ predetermined set of observational targets (Mauritsen et al., 2012; Hourdin et al., 2017). ~~Typically, the tuning is~~

ESM tuning is often done in a ~~sequential manner in which~~ heuristic, trial-and-error way, wherein one or more parameters are perturbed to new values based on ~~the diagnosis of the~~ diagnosing the causes of systematic error ~~,~~ with the aim of improving the model's overall behavior (e.g., Watanabe et al., 2010; Yukimoto et al., 2012; Mauritsen et al., 2019; Voldoire et al., 2019; Golaz et al., 2019; Sellar et al., 2019; Danabasoglu et al., 2020). The observational targets can include, for example, radiation balance at the top of the atmosphere, surface temperature, sea ice variability, tropospheric wind, or even a derived target such as a ~~"cloud object" (Posselt et al., 2015). Sequential ESM tuning involves running many model sensitivity experiments , where~~ "cloud object" (Posselt et al., 2015). In this approach, a typical tuning exercise comprises several iterations of suites of sensitivity experiments with one or more ~~model parameters have been perturbed and comparing the results with one or more observational targets~~ perturbed parameters. After each iteration, a comparison is made against a set of observations, and another set of sensitivity experiments targeting either the same or another set of parameters and observations is conducted based on the results. This tuning exercise is highly dependent on the experience and expertise of model developers ~~,~~ and on the application for which the model will be used.

~~In addition to sequential tuning methods with a subjective choice of the parameter values for the sensitivity suite, there are automatic parameter calibration methods that have been demonstrated, in proof of concept studies, to more systematically choose or "fine-tune" the final set of optimized parameters. These methods include the use of Latin Hypercube sampling techniques (Posselt et al., 2015), the downhill simplex method (Zhang et al., 2015), and the multiple very fast simulated annealing (Zou et al., 2014). As is the case for all of the subjective and automatic tuning methods, the choice of parameter space to explore is based on the diagnosis of errors and the modelers' intuition. Both the subjective and automatic parameter estimation methods require a large suite of experiments, which are computationally expensive and therefore have been performed with very low resolution, atmosphere-only, or even single-column experiments. The direct applicability of these methods for tuning an ESM may consequently be limited.~~

~~One major issue related to sequential tuning, whether using subjective or automatic methods,~~ There are three main drawbacks for heuristic optimization approaches. The first is that this method necessitates an analysis step between each sensitivity sweep, a time-consuming process. The second drawback is the large number of needed simulations, since a new set of experiments is required for iteration of the process. The third drawback is the interdependence of each parameter's effect on the resulting ESM simulation~~and the relationship to observational targets~~. For example, both sea ice albedo and precipitation efficiency

could affect the ~~globally averaged~~ globally-averaged radiation balance at the top of the atmosphere. ~~An experiment with both perturbed would not reveal which had the greater impact on the solution, and experiments with only one at a time perturbed would not behave as an experiment with both perturbed. The sequential methodology, therefore, for this example, may result~~

60 ~~in a sub-optimal combination of these parameters.~~ The adjustment of one parameter or set of parameters at a time will be suboptimal because estimates of empirical parameters depend on each other and on model configuration, boundary conditions, etc.

~~Another issue related to sequential tuning is the computational cost of running a suite of modern ESMs. A typical sequential tuning exercise includes a series of sensitivity experiments with one or more perturbed parameters , a comparison against a set~~

65 ~~of observations, and another set of sensitivity experiments targeting either the same or another set of observations based on the results. There are two main drawbacks of the sequential nature of this exercise. The first is that this method necessitates an analysis step between each sensitivity sweep, a time-consuming process. The second drawback is the large number of needed simulations, since a new set of experiments is required for each set of observational targets, and may also include several experiments perturbing the same parameter or set of parameters.~~ Given unrestricted computer resources, one could randomly

70 explore model parameter space exhaustively and choose the simulation that best fits all available observations. In practice, this type of exhaustive parameter exploration is not feasible ~~,~~ and we need tractable methods that combine objective methodologies with the model developer's experience to arrive at ~~the optimal~~ an optimized choice of model parameters.

~~One alternative to the sequential method to tune models~~ To mitigate the drawbacks and computational cost of above approaches, a number of more objective parameter calibration methods have been proposed for systematically choosing or

75 "fine-tuning" the final set of optimized parameters. These methods include the use of Latin Hypercube sampling techniques (Posselt et al., 2015), the downhill simplex method (Zhang et al., 2015), the multiple very fast simulated annealing (Zou et al., 2014) , and Gauss–Newton line search algorithms (Tett et al., 2013, 2017; Roach et al., 2018). The above estimation methods require a large suite of experiments, which are computationally expensive. Therefore, the sensitivity experiments are typically carried out with very low resolution, atmosphere-only, or even single-column model configurations. The direct applicability of these

80 methods for tuning an ESM may consequently be limited.

Another alternative to heuristic estimation approaches is the adjoint ~~methodology. When using this methodology~~ method. Using the adjoint method, one can adjust many parameters simultaneously~~by running one experiment~~. A successful example is ~~the ECCO state estimate that~~ provided by the Estimating the Circulation and Climate of the Ocean (ECCO) consortium, which used the adjoint ~~methodology to adjust MITgcm~~ method to adjust Massachusetts Institute of Technology general circulation

85 model (MITgcm) ocean model parameters, initial conditions, and boundary conditions (Forget et al., 2015). Although ~~this methodology~~ the adjoint method provides robust results, developing a model's adjoint is ~~onerous~~time-consuming, even when using ~~a software tool, and using it~~ an automatic differentiation software tool. Additionally, the adjoint method is computationally expensive because many forward-adjoint ESM simulations would be required to optimize a non-linear model.

In this study, we ~~use a~~ will explore the applicability of the Green's functions ~~methodology (Menemenlis et al., 2005) for~~

90 ~~the first time to tune a fully coupled model - the GEOS-MITgcm ESM . The Green's functions methodology addresses the major issues with sequential tuning identified above, and has some features of the adjoint methodology. The~~ approach of

Menemenlis et al. (2005) to the calibration of an ESM — the Goddard Earth Observing System (GEOS) land-atmosphere model coupled to the MITgcm ocean model. Compared to other methods, the key advantages of the Green's function approach are simplicity of implementation, robustness in the presence of nonlinearities, and the explicit computation of the data kernel matrix. Compared to heuristic, trial-and-error approaches, the Green's functions ~~methodology can adjust several parameters simultaneously while accounting for the potential interdependence of their effect on the simulation. The interdependence is accounted for in the constraints on the error covariance for each parameter. In addition, some of the computational expense of the sequential tuning method is alleviated, since only one set of sensitivity experiments is required , so there is little or no expense relative to an extensive range of observational targets or combinations of parameters. The no-iteration characteristic is also an advantage relative to the Gauss–Newton line search algorithm (Tett et al., 2013, 2017; Roach et al., 2018) which uses similar aproach to minimized a set of parameters simultaneously~~approach optimizes uncertain parameters all at once, as opposed to one at a time, hence taking into account linear dependencies between these parameters. Therefore, the Green's functions approach accounts for the combined impact of all the parameters while also establishing the individual impact of any one parameter on the solution and with respect to each observational target. Once the forward-model sensitivity experiments have been carried out, the optimization step can be repeated using different observational targets and weights at very small additional computational cost. Assuming that the linearization assumptions hold, only one forward-model sensitivity experiment is required per parameter to be adjusted, which reduces the computational cost relative to the heuristic and objective approaches listed in the previous paragraphs. While the application of an adjoint model requires substantial additional model-development and coding efforts, all that is required for applying the Green's function approach is the computation of ESM forward sensitivity experiments. Furthermore, while the adjoint method would require that the exact tangent linear of the ESM be well behaved, Green's functions provide an approximate linearization, which can be used to reduce the cost function even when the adjoint model is ill behaved. Finally, the explicit computation of the data kernel matrix makes available a vast array of tools from discrete linear inverse theory for deriving and for analyzing the solutions.

The ~~Green's functions methodology does assume that the effect of the perturbed parameter is approximately linear. It can also incorporate as many observational targets (with negligible computational cost) as desired as long as data constraints are available. The results described here include a proof of concept for the use of the methodology in an ESM and the examination of various 'flavors' of the optimization process~~key drawback of the Green's function approach is that computational cost increases linearly with the number of control parameters. Therefore the method is only applicable to situations where a small number of control parameters need to be estimated. Despite these drawbacks, we will demonstrate that the Green's functions approach can be an invaluable addition to the repertory of estimation tools used to adjust ESM model parameters.

The remaining of the manuscript is organized as follows. The mathematical formalism and the Green's functions method are presented in the next section. This presentation is followed by the description of the model, the experiments, and the used observational targets. Section 4 presents our chosen configuration results, followed by a Section outlining the motivation for the configuration choices. ~~The study is summarized~~ Summary and conclusions are in Section 6.

2 Earth System Model Description

The model used for this study is the GEOS-MITgcm coupled model. We briefly describe here the particular configurations of these two models as they are used in our study. The GEOS AGCM's dynamical core and suite of physical parameterizations, along with the land model and aerosol model are described in Molod et al. (2020) and in the references therein. The turbulent surface layer parameterization, relevant for this study, is a modified version of the parameterization documented in Helfand and Schubert (1995). The wind stress and surface roughness model was modified by the updates of Garfinkel et al. (2011) for a mid-range of wind speeds and further modified by the updates of Molod et al. (2013) for high winds. The GEOS AGCM's cubed-sphere grid was configured to run with a nominal horizontal grid spacing of 100 km. The vertical grid is a hybrid sigma-pressure grid with 72 levels. The time step of integration was set to 450 seconds.

MITgcm has a finite-volume dynamical core (Marshall et al., 1997). It has a nonlinear free-surface and real freshwater flux (Adcroft and Campin, 2004) and a nonlocal K-profile parameterization scheme for mixing (Large et al., 1994). The MITgcm horizontal grid is the so-called "Lat-Lon-Cap" (Forget et al., 2015), and was configured to run with a nominal grid spacing of 100 km. The vertical grid is the z^* height coordinates (Adcroft and Campin, 2004), and it has 50 vertical levels. The time step of integration was set to 450 seconds, similar to the atmospheric model.

The GEOS-MITgcm atmosphere-ocean interface includes a skin layer (Price et al., 1978), configured for the simulations described here to impose a one-day time scale on the interaction, and the communication between the ocean and atmosphere is updated at every atmospheric model time step (450 seconds). The sea-ice dynamics model is provided by MITgcm and the sea ice thermodynamics model is from CICE 4.1 (Hunke and Lipscomb, 2010).

3 Mathematical Formalism and Methodology

Algebraically, the ESM described in previous section can be expressed as a set of rules for time stepping a state vector,

$$\boldsymbol{x}(t_{i+1}) = M_i(\boldsymbol{x}(t_i)), \tag{1}$$

where $\boldsymbol{x}(t_i)$ is a discretized representation of the Earth System at time t_i and function M_i represents ESM time-stepping rules for advancing the state vector from time t_i to t_{i+1}. The discretized evolution of the true Earth System, $\boldsymbol{x}^t(t_i)$, is assumed to differ from that of the numerical model by a vector of stochastic perturbations $\boldsymbol{\eta}$ so that

$$\boldsymbol{x}^t(t_{i+1}) = M_i(\boldsymbol{x}^t(t_i), \boldsymbol{\eta}), \tag{2}$$

where $\boldsymbol{\eta}$ is assumed to have zero mean and covariance matrix $\mathbf{Q}$. Consider a set of observations represented by vector $\boldsymbol{y}^o$, which are related to the discretized, time-evolving Earth System state vector by measurement function H, that is,

$$\boldsymbol{y}^o = H(\boldsymbol{x}^t(t_0), \boldsymbol{x}^t(t_1), \ldots, \boldsymbol{x}^t(t_N)) + \boldsymbol{\varepsilon}, \tag{3}$$

where $\boldsymbol{\varepsilon}$ represents a vector noise process assumed to have zero mean and covariance matrix $\mathbf{R}$. In addition to measurement errors, vector $\boldsymbol{\varepsilon}$ includes all model and estimation "representation" errors, i.e., model-data residuals that cannot be represented by M_i and $\boldsymbol{\eta}$. The optimization problem aims to

To fit the ESM to the available observations, we aim to minimize an objective cost function

$$J = \boldsymbol{\eta}^T \mathbf{Q}^{-1} \boldsymbol{\eta} + \boldsymbol{\varepsilon}^T \mathbf{R}^{-1} \boldsymbol{\varepsilon}, \tag{4}$$

which penalizes ~~the~~ a weighted least-squares distance ~~relative to model priors and observations.~~ between optimized and prior model parameters ($\boldsymbol{\eta}^T \mathbf{Q}^{-1} \boldsymbol{\eta}$) and a weighted least-squares distance between simulation and observations ($\boldsymbol{\varepsilon}^T \mathbf{R}^{-1} \boldsymbol{\varepsilon}$), where T is the transpose operator and -1 indicates matrix inversion. It can be shown that the minimization of Equation (4) will produce the maximum likelihood solution for Gaussian inverse problems Kalnay (2002). For the Green's Functions approach, we adjust a small, carefully-chosen set of parameters $\boldsymbol{\eta}$. To do this, we combine Eqs. (2) and (3) to obtain:

$$\boldsymbol{y^o} = G(\boldsymbol{\eta}) + \boldsymbol{\varepsilon}, \tag{5}$$

where G represents ~~the convolution~~ a function the combination of observation operator H with ESM time-stepping rules M_i. We assume that (5) can be linearized about a reference ESM simulation so that:

$$\boldsymbol{y}^d = \boldsymbol{y}^o - G(\mathbf{0}) = \mathbf{G} \cdot \boldsymbol{\eta} + \boldsymbol{\varepsilon}, \tag{6}$$

where $\mathbf{0}$ is a null vector, $G(\mathbf{0})$ represents the reference ESM simulation sampled by measurement function H, vector $\boldsymbol{y}^d$ is the model-data difference between observations and the reference simulation, and kernel matrix $\mathbf{G}$ can be thought of as a first order multivariate Taylor expansion of G around $\boldsymbol{\eta} = \mathbf{0}$. The assumption here is that for small enough perturbation, the model response is linear. Kernel matrix $\mathbf{G}$ can be derived by conducting an ESM perturbation experiment for each element of vector $\boldsymbol{\eta}$. Specifically, the j-th column of matrix $\mathbf{G}$ is

$$\boldsymbol{g}_j = \frac{G(\boldsymbol{e}_j) - G(\mathbf{0})}{e_j}, \tag{7}$$

where $\boldsymbol{e}_j$ is a perturbation vector filled with zeros except for element j, which is perturbed by scalar value e_j. The minimization of (4) given (5) is a discrete linear inverse problem with solution:

$$\boldsymbol{\eta}^a = \mathbf{P} \mathbf{G}^T \mathbf{R}^{-1} \boldsymbol{y}^d, \tag{8}$$

where

$$\mathbf{P} = (\mathbf{Q}^{-1} + \mathbf{G}^T \mathbf{R}^{-1} \mathbf{G})^{-1} \tag{9}$$

is the uncertainty covariance matrix for the optimized estimate $\boldsymbol{\eta}^a$. Mathematically, the Green's function approach is equivalent to any linear, Gaussian inverse problem, for example, the adjoint method.

In practice, the Green's functions estimation method can be divided into six steps:

1. Run a reference ESM simulation using default values for model-error parameters, that is, $\boldsymbol{\eta} = \mathbf{0}$. The output from this experiment, sampled by observation operator H, provides $G(\mathbf{0})$ in (5) and (6).

2. Choose a set of observational targets, that is, define operator H and vector $\boldsymbol{y}^o$ in (3).

3. Estimate error covariance matrices $\mathbf{Q}$ and $\mathbf{R}$, the model and observation/representation errors, respectively, that are needed to define cost function J in (4).

4. Run a set of model sensitivity experiments, where each element of vector $\boldsymbol{\eta}$ is perturbed, one at a time, by scalar value e_j. These sensitivity experiments are used to construct kernel matrix $\mathbf{G}$ as per recipe given by Eq. (7). This step holds the biggest computational cost, far exceeding other steps.

5. Calculate a set of optimized model error parameters $\boldsymbol{\eta}^a$ using Eq. (8). Vector $\boldsymbol{\eta}^a$ can be used to compute an optimized linear combination and a *projected cost* under the assumption of linearity.

6. Run a new simulation using optimized parameters $\boldsymbol{\eta}^a$. This *optimized simulation* can be compared with the optimized linear combination of sensitivity experiments in order to evaluate the linearization assumption.

Note that steps the choice of the observational targets and the definition of the covariance matrices (steps 2 and 3) can be later revised without the need to rerun a new set of experiments (step 4).

4   Proof of Concept Optimization

In this section, we illustrate the application of the six steps listed above.

4.1   Reference Experiment

The 10-year long reference experiment was configured with reference values of a set of parameters that we aimed to optimize. The model was configured to run in "perpetual year" mode, meaning that the external boundary conditions (solar insolation, greenhouse gas amount and aerosol emissions) are kept to those of 2000. The "perpetual year" mode was chosen to optimize the model's equilibrium state relative to our climatology observational targets.

4.2   Observational targets

The motivation of this study was to set up a simple, systematic, reproducible, extensible, and efficient framework for improving the climatology of the new coupled model now and as it undergoes development in the future. To start, we chose eight key observational targets (Table 1), each one chosen for reasons outlined below. Ice fraction is directly relevant to all sea ice processes, and is important for an accurate representation of climate variability in the polar regions and climate feedbacks on the global scale. Accurate modeling of shortwave radiation at the surface indicates that the model can simulate the atmospheric and oceanic circulations' driving force. Shortwave radiation and downward longwave radiation indicate the realistic representation of cloud processes in the atmosphere. Near-surface temperature was added aiming to balance out ocean-only observational targets. Sea Surface Temperature (SST) is a fundamental climate variable that drives the atmosphere. Sea Surface Salinity (SSS) controls ocean circulation but also a tracer of the global water cycle. Their equivalents at 300m below sea level additionally constrain large scale ocean transports. The observational targets were calculated separately for each season - DJF, MAM, JJA, SON, and each seasonal mean was compared with corresponding model output.

Table 1. List of observational targets and covariance value.

Variable	Dataset	Years	Covariance (R)
Seaice fraction	MERRA-2[1]	1996-2004	0.14
Net surface shortwave radiation	SRB[2]	1996-2004	2250 [Wm-2]^2
Downward longwave radiation	SRB[2]	1997-2004	506 [Wm-2]^2
Near surface temperature	HadCRUT4[3]	1997-2004	35.4 [°C]^2
Sea surface temperature	ECCO[4]	1996-2004	6.67 [°C]^2
Sea surface salinity	ECCO[4]	1996-2004	2.06 [psu]^2
THETA at 300m	ECCO[4]	1996-2004	2.62 [°C]^2
Salt at 300m	ECCO[4]	1996-2004	0.05 [psu]^2

[1] GMAO (2016) [2] Stackhouse Jr et al. (2011) [3] Osborn and Jones (2014) [4] Forget et al. (2015)

4.3 Definition of cost function

215   In this study, $\mathbf{Q}^{-1}$ is set to zero, that is, the cost function does not explicitly include *a priori* knowledge about the range of possible parameter values. Some of the parameters, however, have intrinsic physical bounds for the range of values. For these parameters, the resulting optimized parameters were checked and all were found to lie within the range of physically-acceptable values. The error covariance matrix $\mathbf{R}$ is chosen to be diagonal. Because the estimation problem is highly overdetermined — the number of parameters to adjust is O(10) while the number of observations is O(10^6) — we expect that the assumption

220   that $\mathbf{R}$ is diagonal will have minimal impact on the optimized estimate η^a. In general, the addition of non-diagonal elements of $\mathbf{R}$ would indicate linear dependence among observational errors, reducing the effective degrees of freedom. Since, in our case, the number of observations is far larger than the number of optimized parameters, we would still retain a very large number of independent observations as compared to optimized parameters. The variance was calculated separately for each observational target and defined to be the global, area-weighted, mean-squared difference between the climatology of the

225   reference experiment and observations, that is:

$$R_v = \sum_{i,j,s} w_{i,j} \cdot \left(\hat{y}^o_{v,i,j,s} - \hat{x}^r_{v,i,j,s} \right)^2, \tag{10}$$

where the indices v, i, j, and s represent observation variable, longitude, latitude, and season (winter, spring, summer, and fall), the hat sign ˆ represents climatological seasonal-mean values, and $w_{i,j}$ is an area weight with $\sum_{i,j} w_{i,j} = 1/4$, giving each season a $1/4$ of the weight. The prior error variance of each variable is, therefore, a constant value. A consequence of

230   our choice of the covariance matrix and the cost function is that the cost of the reference experiment is equal to one for each variable. For eight observational targets, the total cost of the reference experiment is eight. This definition gives equal weight to each of the eight observational targets and was found to provide a balanced solution in terms of each observational target's overall influence. The cost of the optimized experiment is expected to be smaller than one for each variable.

4.4 Sensitivity Experiments

Table 2. List of perturbed parameters

#	Parameter name	Description	Reference	Perturbed	Optimized
1	AUTscale	Liquid autoconversion rate scaling	0.20	0.30	0.27
2	LTS_LOW	For LTS higher than LTS_LOW, and in marine regions, the cloud	19.0	20.0	19.2
3	MIN_EXP	fraction within the PBL is scaled using a power law, where the power	0.60	0.80	0.73
4	MAX_EXP	exponent varies between MIN_EXP and MAX_EXP.	1.50	1.70	1.32
5	CICE_AH_MAX	Used in calculating the ice albedo threshold	0.30	0.20	0.36
6	ALBICEV	Visible band ice albedo	0.73	0.82	0.79
7	ALBICEI	Near-IR band ice albedo	0.33	0.40	0.37
8	TURN_RHCRIT	The level at which the PDF of total moisture is assumed to change from its "free atmosphere" behavior to its "inside PBL" behavior.	884	750	870
9	CQfactor	A factor for the surface moisture exchange coefficient	1.0	1.5	1.2
10	Charnok1	Governs the relationship between the ocean wind stress and the wind speed. This parameter governs the behavior at high wind speed.	2.92E-3	2.19E-3	3.65E-3
11	Charnok2	Governs the relationship between the ocean wind stress and the wind speed. This parameter governs the behavior at low wind speed.	-1.10E-8	-2.00E-8	-1.70E-8
12	VSLfactor	Scales the impact of the laminar viscous sublayer over the ocean.	1.00	1.20	0.96
13	MF2CFfactor	Mass flux to cloud factor - governs the relationship between detrained cloud mass flux and cloud fraction.	1.00	0.80	1.14
14	MIN_RHCRIT	Determines the width of the assumed PDF of total water in the free troposphere.	0.90	0.85	0.91
15	TS_AUTO_ICE	Auto-conversion time scale for ice in multiples of model time step	4.0	3.0	4.5
16	BC_INFAC	The fraction of black carbon number concentration that is allowed to act as ice nucleating particles.	1.00	0.50	0.35
17	DUST_INFAC	The fraction of dust number concentration that is allowed to act as ice nucleating particles.	1.00	0.50	0.79
18	DCS	Critical diameter for ice auto-conversion.	3.5E-4	3.0E-4	3.8E-4
19	UISCALE	Scaling for the terminal velocity of ice	1.00	0.90	0.98
20	KHRADFAC	Scale factor for negatively buoyant turbulence related to cloud-top cooling	0.85	0.50	0.95

235   In addition to the reference experiment, 20 10-year long sensitivity experiments were performed using the exact model configuration as the reference experiment but perturbing one of the uncertain parameters each time. The length of the simulations needed for the Green's Function optimization is related to the application of the model being optimized. For climate projection

applications, where the long-term equilibrium of the model is paramount, it seems clear that longer simulations would be warranted in order to allow for model spin up time. The primary application of the coupled model presented here is seasonal
240 to decadal prediction, and so the optimization is done to include (ideally to minimize) the initial model drift.

The reference and perturbed parameter values, and a short description of the parameters is listed in Table 2. We used the 20 sensitivity experiments to estimate the model's sensitivity to each of the perturbed parameters based on the Green's functions formalism. The perturbed parameter values where chosen based on expert advise. For some of the parameters the value was chosen based on physically realistic values from past experience. In some of the cases, the perturbed value was chosen
245 arbitrarily due to a large parameter uncertainty. Note that there is no risk of overfitting due to the large number of observational targets (eight observational targets, two-dimensional fields, four seasons - $\approx$300,000 targets). Methods to penalize a large number of parameters are therefore not needed in this case.

4.5   Optimized Parameters

The optimized parameters are given in the last column of Table 2. It can be seen that only half of the of optimized parameter
250 values fall between the reference and the perturbed value, indicating a large unpredictability in model response to the change in those parameters. Nevertheless, the difference of the optimized parameter and the reference value ($\boldsymbol{\eta}^a$) did not exceed the difference of the perturbed parameteer value and the reference value ($\boldsymbol{\eta}$) except for one parameter - TS_AUTO_ICE. This may indicate that our choice of the perturbed values was within a realistic range. Particularly, when considering that $\mathbf{Q}^{-1}$ was set to zero, suggesting that the optimized parameter's range were not constrained by the cost function.

255 4.6   Assessing the Performance of the Green's Functions Methodology

Once the Green's functions methodology provides the optimized parameters, a projected cost can be derived directly from the sensitivity experiments using the optimized parameters. This derivation can be done before actually running the optimized simulation with the optimized parameters. The projected cost provides a first indication of the expected cost reduction assuming linearity. After a new optimized experiment is performed, the projected cost can be compared with the optimized experiment's
260 cost to assess the correctness of the assumption of linearity.

Figure 1 (and Table 3) shows that the total cost reduction of the optimized experiment (shown on the right) relative to the reference experiment (shown on the left) is 9% (similar to the cost reduction found in Zhang et al. (2015)). Figure 1 (and Table 3) also shows the projected cost, which is the cost one would get if the model response to parameter perturbations were entirely linear. Most of the cost reduction seen in the projected (second from the right) experiment is realized in the optimized
265 experiment. The total cost of each of the 20 sensitivity experiments is larger than the cost of the simulation with the optimized parameters. Figure 2 shows the normalized cost for each of the eight observational targets in the same order as in Figure 1. Figure 2 shows that the cost is the lowest in the optimized experiment (the rightmost bar in each cluster) for five out of the eight observational targets. For one of the observational targets (sea-ice fraction) the cost of the optimized experiment is smaller than the reference but several sensitivity experiments have lower cost. For two observational targets, the optimized experiment cost
270 is larger than the cost of the reference experiment. This cost increase happens for surface temperature over land and downward
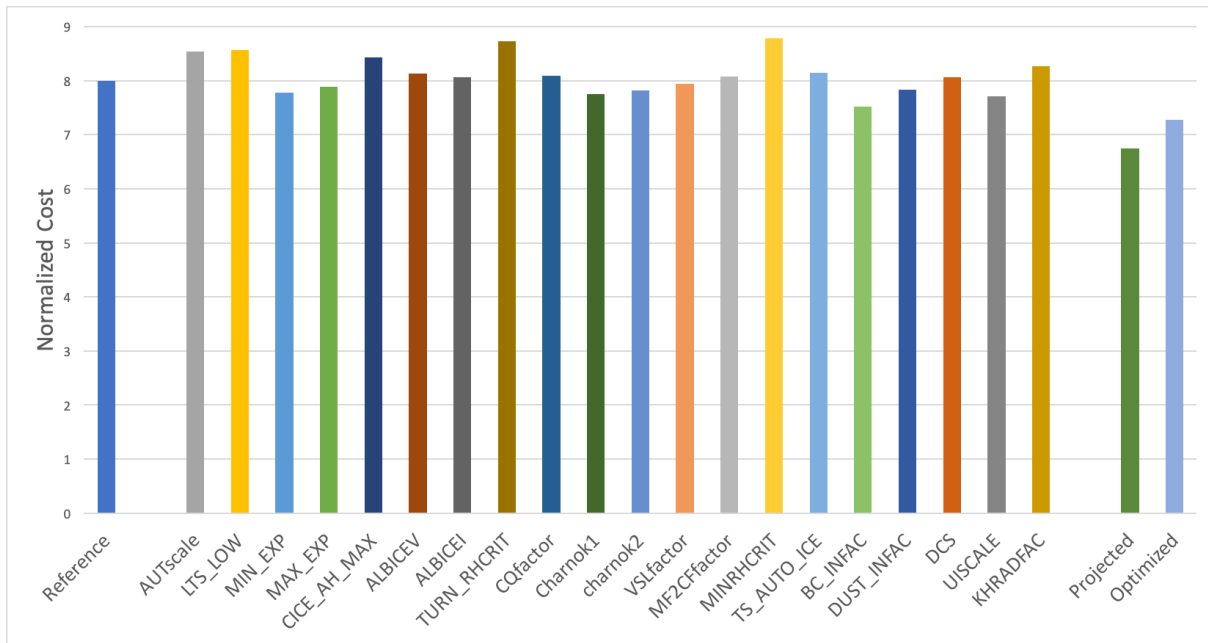
Figure 1. The total cost of the reference experiment, the optimized experiment and the 20 perturbed experiments. Projected cost is also indicated.

longwave radiation. The longwave radiation had a cost increase of 2%. The more considerable increased cost of 16% percent in the surface temperature is related to our choice of the observational targets. Five out of the eight observational targets are ocean-only variables, only one is land-only, and two cover both land and ocean. This asymmetry between land and ocean constraints seems to have pulled the parameters to values that benefit the ocean more than the land. This proof of concept 275 illustrated in this study, although clearly demonstrates the overall cost reduction with this method, also illustrates the need to choose the desired observational targets carefully.

Table 3. Explained variance in percentage. Negative values represent reduction of explained variance. TS - Near surface temperature; FR - Seaice fraction; LW - Downward longwave radiation; SW - Net surface shortwave radiation; SST - Sea Surface Temperature; SSS - Sea surface salinity; T (300) - THETA at 300m; S (300) -Salt at 300m.

	TS	FR	LW	SW	SST	SSS	T (300m)	S (300m)	Total
Projected	7.3	12.9	11.3	14.4	36.3	10.0	21.4	11.6	15.6
Optimized	-16.0	8.2	-2.0	20.0	25.6	14.5	11.3	10.6	9.0

The cost reduction was also found to be rather homogeneous across many regions around the globe. Figure 3 shows that, for net shortwave radiation, the total cost reduction was 20% relative to the reference experiment. Most of the oceans exhibit a large reduction in the cost, particularly over the Antarctic Circumpolar Current (ACC) and in the stratocumulus regions in the
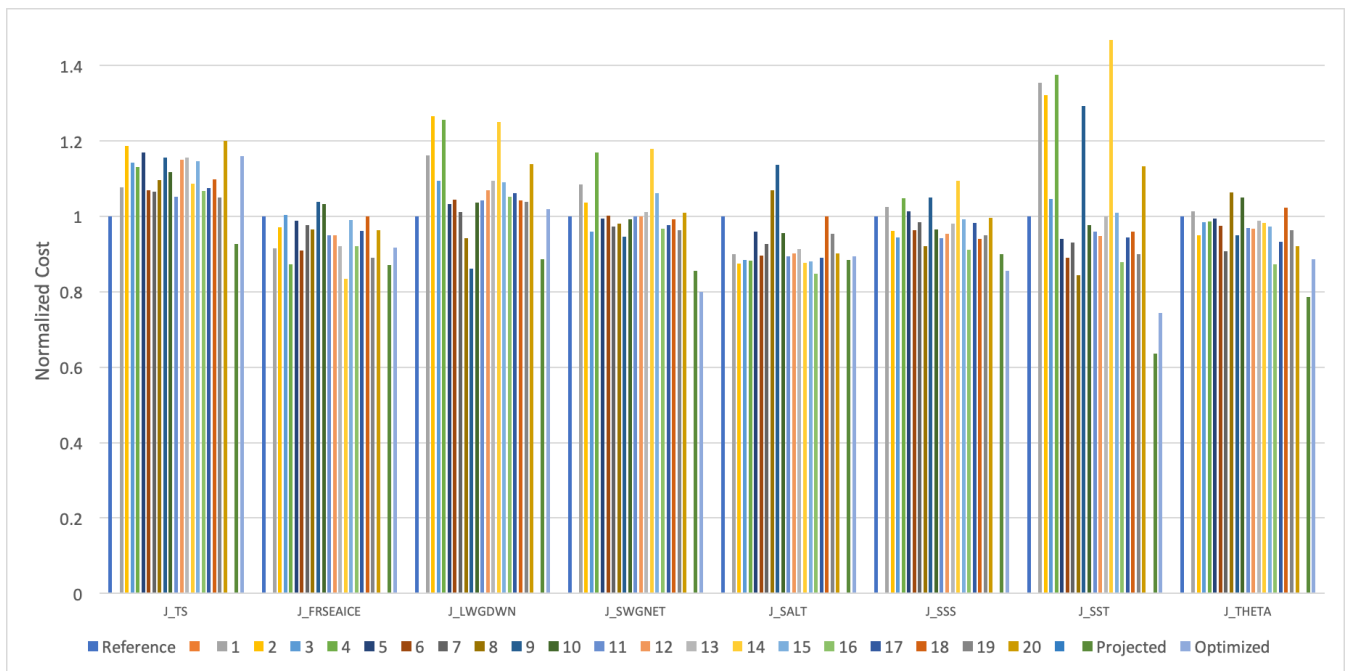
Figure 2. The cost of the reference experiment and the 20 perturbed experiments for each of the observational targets. Projected and optimized cost are also indicated.

eastern Pacific's subtropics. In comparison with these cost reductions over the oceans, the land still exhibits marginal increases in cost over wide regions of North America and south-east Asia.

The actual cost reduction of the various variables seen in the optimized experiment is also generally consistent with the projected cost. Figure 4 shows the projected cost reduction for the net shortwave radiation, which is in broad agreement with the actual cost reduction of the optimized experiment seen in figure 3c. In this case, the cost of the optimized experiment was even smaller than the projected cost. Overall agreement between the projected cost and optimized experiment cost suggests that the linearity assumption that underlies the Green's functions methodology holds sufficiently well for the approach to be useful.

The surface temperature, which exhibits an overall 16% increase in cost (Figure 5), also shows some large regions of cost reduction over North America and Greenland. However, the cost in north Asia and Europe is increased. In terms of the cost's seasonality, it was found that DJF and MAM had the highest cost increase while JJA months had the smallest overall cost reductions. These results suggest that the misrepresentation of land-ice processes in the new and the old configurations is responsible for the high cost. Surface temperature is the variable that had the least projected cost reduction. So, it was expected to exhibit the worst performance in terms of the optimized experiment cost. Including more land-related observational targets such as snow fraction and soil moisture could improve the cost of surface temperature. This inclusion can assist in constraining model performance above land, balancing the ocean-only constraints. Downward longwave radiation also exhibits
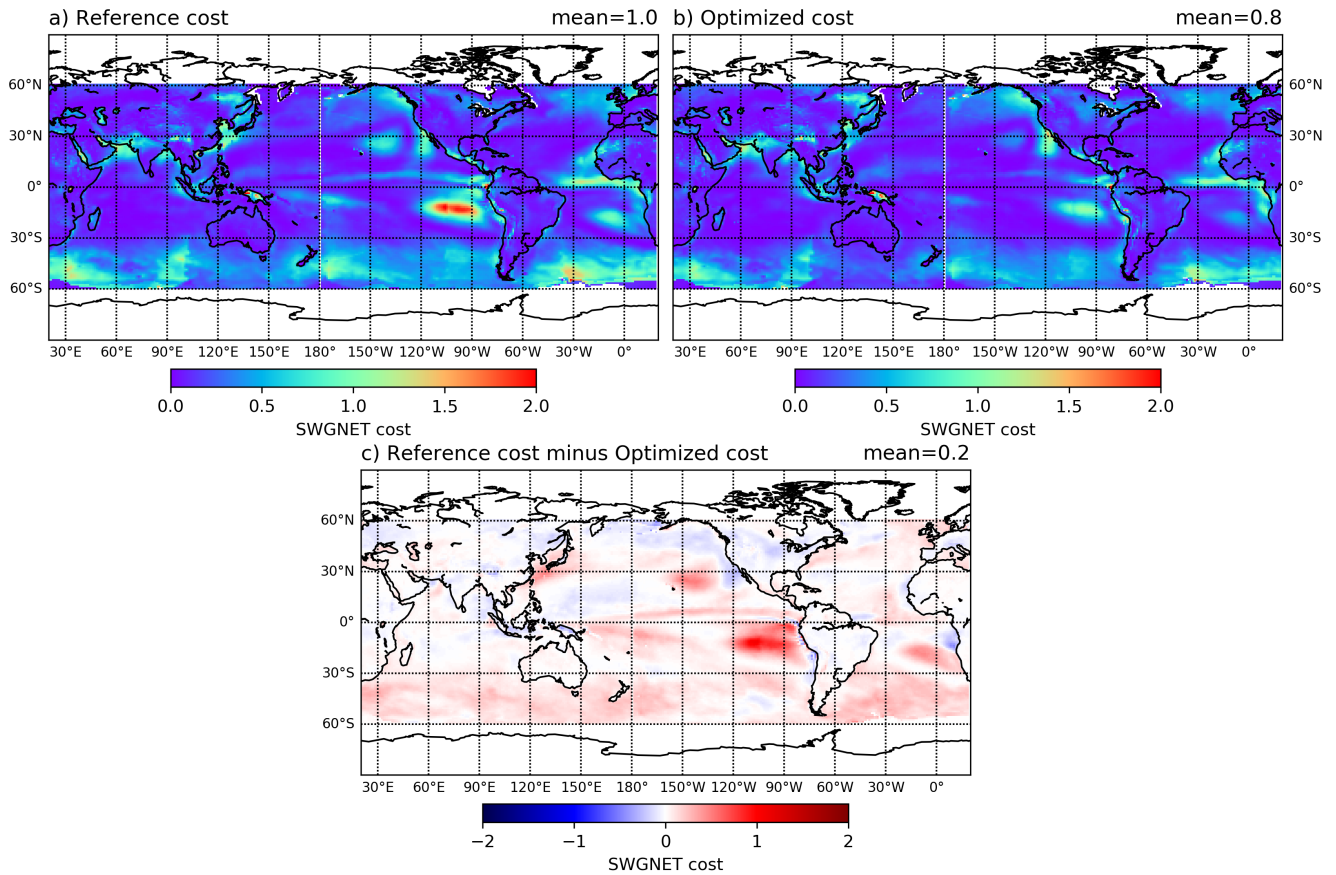
Figure 3. The net shortwave radiation cost for the reference (a), the optimized experiments (b), and their difference (c).

cost increase, but here the increase is 2%. In terms of the other variables, the cost of sea-ice fraction was reduced by 8.2%, and the four ocean-only variables showed cost reduction between 10% to 25%, indicating an improved representation of the ocean circulation.

5   Discussion: Motivation for Choices in Methodology

300   The parameter estimation experiment presented in the previous section describes our current best practice, which was guided by a series of sensitivity experiments with different configurations where different variations of the methodology were tested. Below we discuss sensitivity to the choice of (1) prior covariance matrices, (2) observational targets, and (3) the number of control parameters. Many other sensitivity experiments can be designed. The goal of this section is not to cover all the options but rather to provide an additional dimensional depth of the Green's functions methodology. In the end, the future choice of

305   the Green's function 'flavor' should reflect the goals of the optimization exercise.
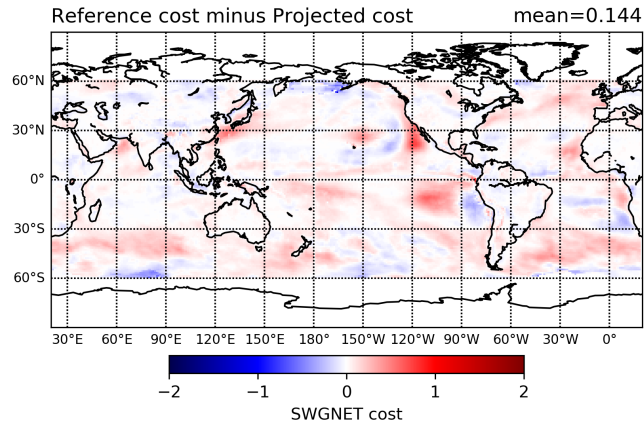
Figure 4. Net shortwave radiation cost difference between the projected value and the reference experiment

5.1 Sensitivity to choice of prior covariance matrices

In ~~order to evaluate the sensitivity to the choice of the covariance matrix , we used a simpler~~ general, the error covariance matrices $\mathbf{Q}$ and $\mathbf{R}$ are not known and difficult to estimate. For the Green's function approach, however, the number of observations is generally much larger than the number of parameters being estimated, which simplifies the selection of $\mathbf{Q}$ and $\mathbf{R}$. First, the small number of control parameters limits the solution's degrees of freedom; therefore the choice of $\mathbf{Q}$ and $\mathbf{R}$, if they are reasonable, is not expected to change the solution η^a much — but it will impact posterior uncertainty $\mathbf{P}$. Second, the data kernel matrix $\mathbf{G}$ is small enough to be defined explicitly; therefore many interesting properties of the solution can be derived and evaluated. Third, the solution of (8) and (9), once the kernel matrix $\mathbf{G}$ has been derived, is trivial; therefore it is possible to test the impact of particular choices of $\mathbf{Q}$ and $\mathbf{R}$, as is done next.

The sensitivity to the choice of covariance matrices $\mathbf{Q}$ and $\mathbf{R}$ in Equation (4) is evaluated using a pared-down configuration, perturbing only three parameters. The pared-down configuration is used to simplify the discussion and better illustrate the response of the optimized solution to different covariance matrices. The perturbed parameters were AUTscale, LTS_LOW, and two sea ice parameters (ALBICEV and ALBICEI) perturbed together. ~~Using the Green's functions methodology, one can perform experiments in which more than one parameter is perturbed.~~ The output from the methodology for this choice is a set of scaling factors for the parameters. When more than one parameter is perturbed in one experiment, the same scaling factor is applied to all the experiment parameters. In this configuration, unlike in our best practice configuration, the observational targets were multi-year means, and the cost was not computed separately for each season. The observational targets are also similar to the best practice configuration except that the $500mb$ height was used in place of the surface temperature over land, and the net radiation replaced the two radiation components.
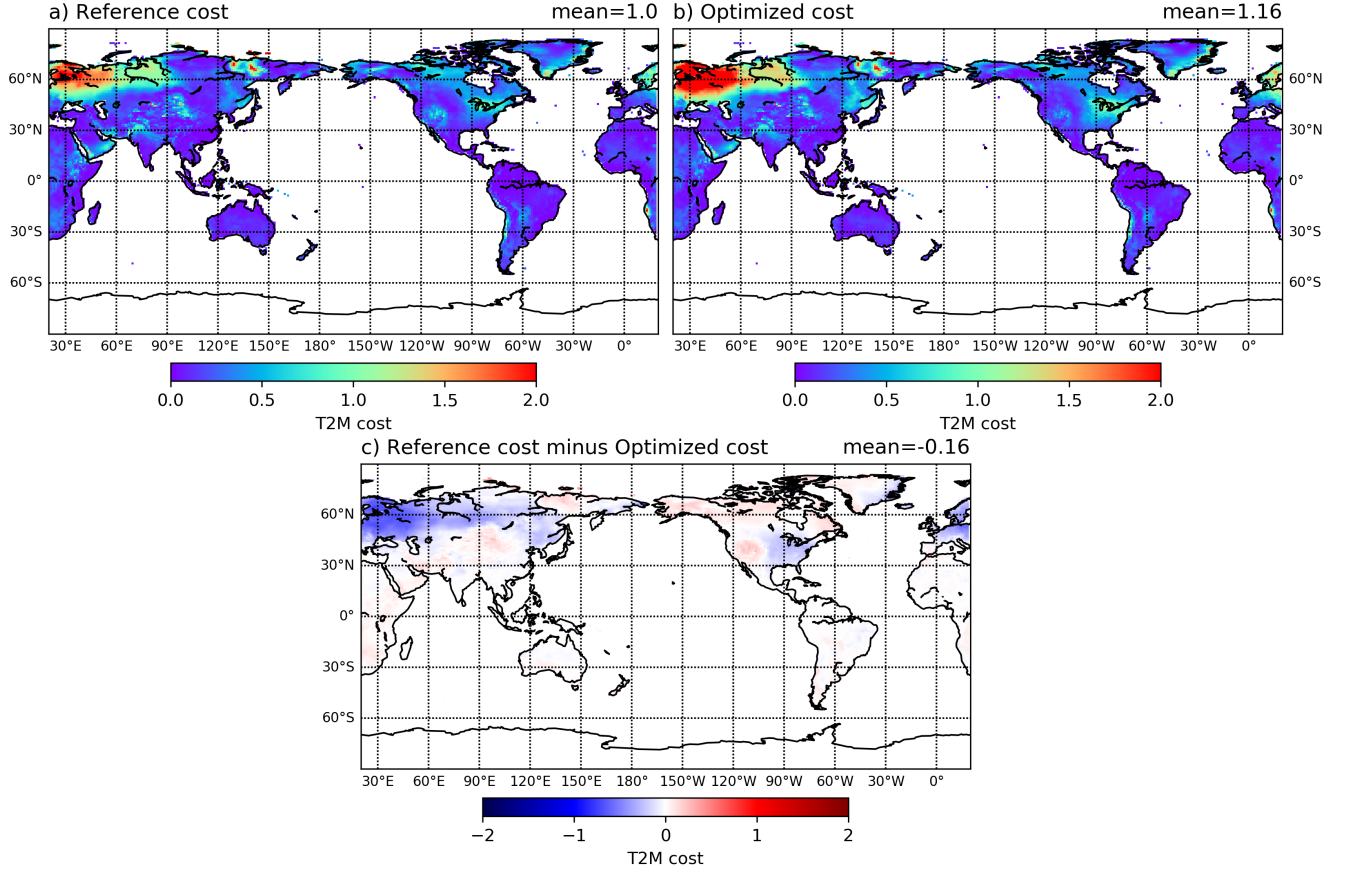
Figure 5. The 2 meter temperature cost for the reference (a) and the optimized experiments (b), and their difference (c).

We tested four different options ~~of the error covariance matrix~~ for the prior error variance, the diagonal elements of matrix R:

$$R_v = \sum_{i,j,s} w_{i,j} \cdot \left(\hat{y}^o_{v,i,j,s} - \overline{\hat{y}^o_{v,s}} \right)^2 \quad where \quad \overline{\hat{y}^o_{v,s}} = \sum_{i,j} w_{i,j} \cdot \hat{y}^o_{v,i,j,s} \tag{11a}$$

$$R_{v,i,j,s} = \frac{1}{N} \sum_{t=1}^{N} \left(\tilde{y}^o_{v,i,j,s,t} - \overline{\tilde{y}^o_{v,i,j,s}} \right)^2 \quad where \quad \overline{\tilde{y}^o_{v,i,j,s}} = \frac{1}{N} \sum_{t=1}^{N} \tilde{y}^o_{v,i,j,s,t} \tag{11b}$$

$$R_v = \left(\max \left(\hat{y}^o_{v,i,j,s} - \hat{x}^r_{v,i,j,s} \right) \right)^2 \tag{11c}$$

$$R_v = \sum_{i,j,s} w_{i,j} \cdot \left(\hat{y}^o_{v,i,j,s} - \hat{x}^r_{v,i,j,s} \right)^2 \quad (as \ in \ Eq. \ 10) \tag{11d}$$

where, v, i, j, s, t are the variable, longitude, latitude, season, time indexes. The tilde symbol (˜) represents seasonal means and N is the number of years. The first option (a) uses the area-weighted variance of the observations instead of the mean-squared misfits used in Eq. 10. The second option (b) is the spatially and seasonally variable, time variance of the observations, the

third option (c) is the square of the maximal absolute difference between observations and the reference experiment, and the fourth option (d) is an area weighted variance of the difference between the observations and the reference experiment. All four ~~options for the covariance matrix~~ estimates of $\mathbf{R}$ are calculated separately for each variable. ~~We calculated the optimal parameters~~ The four estimates of $\mathbf{R}$ aim to represent a range of plausible estimates for the actual error variance and allow us to explore the effect on the resulting parameters and cost.

We calculated optimized parameters η^a for each of the four definitions ~~assuming~~ of $\mathbf{R}$ assuming that $\mathbf{Q} = \infty$, that is, no prior information about the control parameters, and again assuming that $\mathbf{Q} = \mathbf{I}$, the identity matrix, meaning that we have the same amount of confidence about the prior values of each control parameter. These two estimates of $\mathbf{Q}$ represent two extreme situations.

Table 4 shows the eight different combinations of the parameters based on the four options for the observations covariance and two different parameters governing the covariance matrices. In general, all configurations generate realistic values in terms of the order of magnitude, but parameters differ in detail. The $\mathbf{Q} = \mathbf{I}$ case tends to keep parameters closer to their initial value (relative to $\mathbf{Q} = \infty$) as expected.

Table 5 shows the cost associated with each of the eight experiments. Looking at the $\mathbf{Q} = \infty$ cases, defining the cost based on Eq. 11a reduce the cost by 7.7% but the relative importance of each variable varied substantially. For example, $500mb$ height cost was very small for the reference (0.024) and the fact that the optimized experiment increase the cost by 33.7% did not affect the total cost. Also, the sea ice contribution to the cost was much larger than the temperature and salinity at 300m below the sea surface. Option 11b was found to provide only marginal cost reduction. Option 11c demonstrated the largest cost reduction (the smallest ratio in the J_total column). However, most of the projected cost reduction was restricted to the $500mb$ height target, while the cost of most of the other variables was not reduced, particularly in the case of the ocean targets. This is in contrast with option 11d, for which the cost reduction was spread more uniformly across the observational targets. All of these considerations led to our choice of option 11d as the best practice. The $\mathbf{Q} = \mathbf{I}$ was not chosen because the range of the parameters is in itself often quite uncertain and because optimized parameter values were found to remain reasonable without the need for adding this additional constraint to the cost function. This choice could certainly be worth revisiting in a future study.

After running a new model simulation with the optimized parameters based on Eq. 11d and $\mathbf{Q} = \infty$ case, the total cost reduction was found to be 6%, 2.9% less than the projected value, but still not small (Table 5). The $500mb$ height contributes to most of the reduction, and the seaice cost was increased by about 25%. A possible explanation for the $500mb$ target being the main contributor to the cost reduction is that there were a small number of grid points in which the error was reduced substantially, particularly at high latitudes (not shown). This result suggests an experiment in which a spatially-dependant weight is used to reduce the magnitude of the outliers. The current cost implementation has the dependency on the model squared-error. This dependency favors the correction of a small number of points with large errors relative to a large number of points with small errors. Choosing absolute error instead of squared-error would have changed the tendency to favor the correction of a small number grid points with large errors. Nevertheless, the simpler experiment configuration was a successful choice to explore the sensitivity to the covariance matrix designs.

Table 4. Optimized parameters of the 3 perturbed parameter experiments based on two different definitions of the parameters' covariance matrix **Q** and four definitions of the error covariance matrix (Eq. 11a-11d).

Parameter → Experiment ↓		LTS_LOW	ALBICEV	ALBICEV	AUTscale
Q = ∞	11a	18.68	0.846	0.420	0.241
	11b	18.31	0.774	0.364	0.237
	11c	17.79	0.871	0.440	0.116
	11d	18.48	0.855	0.428	0.163
Q = **I**	11a	18.51	0.734	0.333	0.201
	11b	18.33	0.770	0.361	0.226
	11c	18.34	0.749	0.345	0.138
	11d	18.48	0.754	0.348	0.185
ref.		18.5	0.73	0.33	0.2

Table 5. Cost of the 3 perturbed parameter experiments based on two different definitions of the parameter covariance matrix **Q** and four definitions of the error covariance matrix (Eq. 11a-11d).

Parameter → Experiment ↓			J_total	J_SEAICE	J_H	J_RADSRF	J_SALT	J_SSS	J_SST	J_THETA
Q = ∞	11a	reference	0.885	0.294	0.024	0.106	0.038	0.370	0.017	0.035
		proj. / ref.	0.923	0.909	1.337	0.969	0.896	0.886	1.076	0.973
	11b	reference	445.7	72.1	14.9	30.4	93.1	74.9	42.3	117.8
		proj. / ref.	0.987	0.964	1.058	1.015	0.976	0.970	0.995	1.003
	11c	reference	4.283	0.106	4.049	0.052	0.007	0.004	0.039	0.027
		proj. / ref.	0.445	1.356	0.398	1.174	1.255	0.974	1.160	1.168
	11d	reference	7	1	1	1	1	1	1	1
		proj. / ref.	0.921	1.099	0.689	0.966	0.997	0.872	0.844	0.979
		opt. / ref.	**0.940**	**1.253**	**0.523**	**1.045**	**1.010**	**0.864**	**0.950**	**0.937**
Q = I	11a	reference	0.885	0.294	0.024	0.106	0.038	0.370	0.0166	0.0354
		proj. / ref.	0.961	0.924	1.199	0.991	0.935	0.964	1.048	0.986
	11b	reference	445.7	72.1	14.9	30.4	93.1	74.9	42.3	117.1
		proj. / ref.	0.987	0.964	1.056	1.015	0.976	0.970	0.995	1.003
	11c	reference	4.283	0.106	4.049	0.052	0.007	0.004	0.039	0.027
		proj. / ref.	0.484	1.289	0.444	1.087	1.215	0.953	1.080	1.084
	11d	reference	7	1	1	1	1	1	1	1
		proj. / ref.	0.926	1.062	0.703	0.972	1.007	0.898	0.859	0.982

5.2 Sensitivity to choice of number of parameters

370 Here, we evaluate the sensitivity of the cost to the number of optimized parameters. We calculated the projected cost reduction for four cases which used a subset of the first 5, 10, 15 and all 20 parameters from Table 2. We focus here on an optimization based on the multi-year means. An increased number of parameters is expected to translate into a reduced cost as we fit the model to more parameters. In the following results we decided to remove the 500mb height from the cost function in order to spread the cost across more variables. Generally, there is nothing wrong with having most of the cost reduced in

375 one of observational targets, but we decided here to seek a more balanced cost reduction. An additional change here and in the following sections is the separation of the ~~surface radiation targets~~ net surface radiation target into net shortwave and downward longwave radiation, as they are independent and both have SRB observational counterparts. The choice of downward longwave rather than the net was made due to the direct dependence of upward longwave radiation on the SST (which is already a constraint).

380   We tested the projected cost reduction as a function of the optimized parameters' number (figure 6). We found that the projected cost was reduced from 6% to 25% when going from 5 optimized parameters to 20. The cost reduction was gradual showing and additional reduction with the increase of the optimized parameters. The largest cost reduction was found between 5 to 10 optimized parameters.
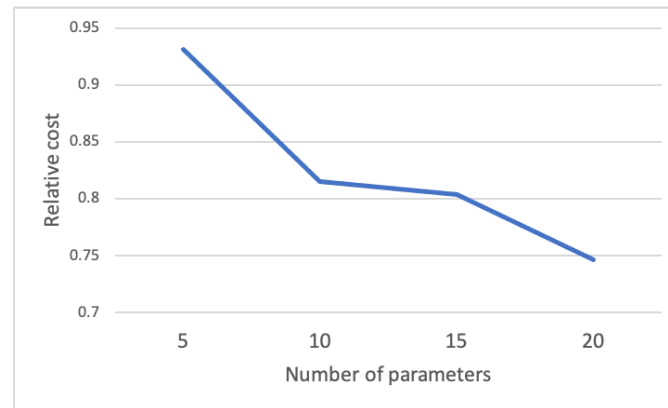
Figure 6. Cost relative to the reference experiment as a function of the number of optimized parameters based on annual means.

5.3   Annual-Mean versus Seasonal-Mean Data Constraints

385 Here, we used nine sensitivity experiments, with nine optimized parameters, to look at the sensitivity of the optimized parameters to seasonality. Two sets of parameters were calculated - based on multi-year means (annual, Table 6) and based on multi-year seasonal means (seasonal, Table 6). The calculation of the optimized parameters comes after the simulations were performed, so the input simulations are the same for both options. The only difference between the annual and seasonal suite is the configuration of the cost function provided to the Greens' functions methodology.

390   The most noteworthy difference between the annual and seasonal results was found in the Charnock parameter that controls surface winds. Although the difference between parameters is smaller than 10%, the projected cost differences are large, with the annually-based optimization reducing the cost by about 15% and the seasonally-based optimization reducing the cost by about 9%. This result is expected, as seasonally-based data have more variability and we use the same number of parameters to optimize model results to larger number of observations.

395   Optimizing for seasonal observational targets is expected to be essential for improving ~~intra-annual~~ seasonal variability. Therefore, despite the less efficient cost reduction for the seasonal targets we decided to continue to focus on experiments with seasonal observational targets. For these two sets of experiments, we did not choose to ~~re-run~~ rerun the model with optimized parameters, but instead decided to increase the number of optimized parameters by performing additional simulations.

Table 6. Optimized parameters of the 9 perturbed parameter experiments configured with $\mathbf{Q} = \infty$ and option 11d.

Parameter → Experiment ↓	AUTscale	LTS_LOW	CICE_AH_MAX	ALBICEV	ALBICEI	TURN_RHCRIT	MAX_RHCRIT	CQfactor	Charnok1
Reference	0.2	19	0.3	0.73	0.33	884	1.0	1.0	2.92E-3
Perturbed	0.3	20	0.2	0.82	0.40	750	0.8	1.5	2.19E-3
annual	0.194	19.53	0.354	0.834	1.14	850	1.14	1.25	3.54E-3
seasonal	0.203	19.38	0.334	0.797	1.12	865	1.12	1.23	3.29E-3

Table 7. Proj. / ref. cost of the 9 perturbed parameter experiment configured with $\mathbf{Q} = \infty$ and option 11d.

Target → Experiment ↓	J_total	J_SEAICE	J_H	J_RADSRF	J_SALT	J_SSS	J_SST	J_THETA
annual	0.854	0.822	0.917	0.873	0.938	0.978	0.634	0.815
seasonal	0.912	0.887	0.933	0.899	0.935	0.973	0.922	0.835

5.4 Length of Optimization Period

400 This sensitivity test was done with the 20-parameter set of simulations. We performed two The appropriate length of the sensitivity experiments was chosen based on the intended application of our tuned model for seasonal and decadal prediction. It seems clear that for a different application of the model, say climate projection, the length of the sensitivity experiments, optimization and observational targets must be long enough to reach a climate equilibrium. Within the scope of seasonal to decadal prediction, to examine the impact of optimization period we performed three Green's function calculations: one

405 that optimizes the parameters based on the first five years of the runs (2000-2005), one that uses the last five years of the runs (2005-2010) and another that uses the whole ten years (2000-2010) as in section 4. The motivation here was to avoid using years during the learn about the impact of model drift after the initialization . The initialization on the optimization. The 2000-2005 optimization projected a 15.3% cost reduction, the 2005-2010 optimization projected a 12.4% cost reductioncompared to , and the 2000-2010 optimization projected a 15.6% projected cost reductionfor the 2000-2010 experimentcost reduction. The

410 optimized experiment with the experiments were only performed with the total and latter time period optimization results, and the 2005-2010 optimized parameters had a cost reduction of 7.1% relative to 9% of for the 2000-2010 experiment. One of the plausible reasons for less cost reduction when optimizing the latter period only is that 2005-2010 had less fewer than two El ñino cycles, and therefore it was too short for the calculation of the model climatology. The 10-year experiment had three full El ñino cycles, and its climatology represents the model climatology more adequately. The 10-year optimization, therefore, is

415 found to enable better parameter optimization.

6 Summary and Concluding Remarks

This study demonstrates the applicability of the Green's functions approach, introduced in Menemenlis et al. (2005) for a forced ocean simulation, to the adjustment of uncertain parameters for a coupled ocean-atmosphere simulation. In this proof-of-concept study, we computed the response of the coupled ocean-atmosphere simulation to the perturbation of the 20 parameters listed in Table 1. These 20 perturbation experiments were subsequently used to optimize the values of the 20 parameters. The observational targets were long term seasonal-means of the eight fields listed in Table 2. The optimization increased the explained variance by up to 25% (for SST in Table 3).

The Green's functions approach assumes that the response of the model to small perturbations is approximately linear. This assumption does not rigorously hold for atmospheric, oceanic or coupled-ocean-atmosphere models because of non-linear weather and climate phenomena such as synoptic storms and El Niño-Southern Oscillation (ENSO) variability. Therefore, a key consideration is that the perturbation experiments be sufficiently long to average out non-linear weather and lower frequency phenomena. This study shows that 10-year long simulations can be sufficient to enable successful application of the Green's functions approach. ~~However, 10 years may still be too short to fully average out some important low frequency variability. This causes differences between the projected linear combination and the optimized simulation, shown as the differences in the explained variance reported on Table 3. This also causes some degradation relative to the baseline simulation for two of the observational targets, the near-surface temperature (TS) and downward longwave radiation (LW).~~

The cost reduction was spread across most of the observational targets, though our configuration of observational targets may have been responsible for the cost increase in two amongst them — the targets associated with land areas that are under-represented in our cost function. In the end, The choice of the observational targets should reflect the objective of the study and, probably, there is no single set of observational targets that is adequate for all applications *a priori*. Our proof-of-concept study and the experiments that show the impact of different choices in the details readily reflect the trade-offs among data constraints that can be important considerations.

Increasing the number of optimized parameters reduced the overall cost which seems to be quasi-linear with the number of parameters, but further investigation into this is required. Increasing the temporal resolution of the observational targets from annual to seasonal increased the cost further – a result of the increasing number of the observational targets. Adding seasonality in parameter adjustments is viewed as one of the next logical steps in this regard. We also tested four different methods to calculate the error covariance matrix, and found that using the error of the reference experiment produced the most balanced results in terms of accounting for all observational targets.

This study shows that the Green's functions methodology can benefit the ~~climate~~ earth system modeling community by providing a more structured yet practical method to tune ~~climate~~ the complex global models. The Green's functions methodology has several advantages that are worth emphasizing here: (a) It is simple to implement and it does not require internal amendments to the model code. (b) It is relatively cheap for small number of parameters – one extra sensitivity experiment per parameter. (c) One can generate virtual predictions and calculate projected cost for ~~infinite~~ a very large number of cost ~~configuration~~ configurations without running new experiments. (d) It offers a systematic way to optimize parameters account-

ing for a possible dependent response of the model to a change of different parameters. (e) The optimization process can be extended with more sensitivity experiments and it can be also revisited with different set of parameters. (f) The sensitivity experiments can be done in parallel suggesting potential scalability.

Identifying the most important uncertain parameters for applying Green's functions methodology still requires close famili-arity with models and there is no replacement for the experience of the modelers when using this methodology. Therefore it is viewed as a valuable framework to further leverage modelers' expertise to fine-tune model parameters, standardize practices across the various ~~climate~~ modelling centers, and improve ~~climate~~ model products beyond the present state of art.

Code and data availability. Data leading to this publication was made available as part of a Zenodo repository at:

 – https://doi.org/10.5281/zenodo.5507631

This repository includes models code and configuration files, post-processed data from model simulations and observational targets, and Green's functions-related scripts, including those generating the figures and tables.

Author contributions. ES ran the simulation and performed the experiments. AM, DB, AT, DM and GF contributed to the design of the experiments and writing the manuscript.

Competing interests. The authors of the manuscript declare that no competing interests are present

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