

# A N-dimensional Fortran Interpolation Program (NterGeo.v2020a) for Geophysics Sciences - Application to a back trajectory program (Backplumes.v2020r1) using CHIMERE or WRF outputs

Bertrand Bessagnet<sup>1,2</sup>, Laurent Menut<sup>1</sup>, and Maxime Beauchamp<sup>3</sup>

<sup>1</sup>LMD/IPSL, École Polytechnique, Institut Polytechnique de Paris, ENS, PSL Université, Sorbonne Université, CNRS, 91128 Palaiseau, France

<sup>2</sup>Citepa, Technical Reference Center for Air Pollution and Climate Change, 42, rue de Paradis 75010 Paris, France

<sup>3</sup>IMT Atlantique, Lab-STICC UMR CNRS, 655 Avenue du Technopôle, 29280 Plouzané, France

**Correspondence:** Bertrand BESSAGNET (bertrand.bessagnet@lmd.polytechnique.fr)

**Abstract.** An interpolation program coded in Fortran for irregular N-dimensional cases is presented and freely available. Needs of interpolation procedures over irregular meshes or matrixes with interdependent input data dimensions is frequent in geophysical models. Also, these models often embed look-up tables of physics/chemistry modules. Fortran is a fast and powerful language highly portable. It is easy to interface models written in Fortran with each other. Our program does not need any libraries, it is written in standard Fortran and tested with two usual compilers. The program is fast and competitive compared to current Python libraries. A normalisation option parameter is provided when considering different types of units on each dimension. Some tests and examples are provided and available in the code package. Moreover, a geophysical application embedding this interpolation program is provided and discussed, it consists in determining back trajectories using chemistry transport or mesoscale meteorological model outputs, respectively from the widely used models CHIMERE and WRF.

## 10 1 Introduction

Interpolation is commonly used in geophysical sciences for post-treatment processing to evaluate model performances against ground station observations. The NCO library (Zender, 2008) is commonly used in its recent version V4.9.2 for horizontal and vertical interpolations to manage climate models outputs. The most frequent need is to interpolate in 3D spatial dimension and time therefore in 4 dimensions. Fortran is extensively used for atmosphere modelling softwares (Sun and Grimmond (2019),  
15 e.g. WRF - Skamarock et al. (2008); GFDL AM3 - Donner et al. (2011)). More generally, geophysical models can use look-up tables of complex modules instead of a full coupling strategy between these modules which is the case of the CHIMERE model (Mailler et al., 2017) with the embedded ISORROPIA module dealing with chemistry and thermodynamics (Nenes et al., 1998, 1999). In such case, the look-up table can easily exceed 5 dimensions to approximate the model. In parallel, Artificial Intelligence methods are developed and can explore the behaviour of complex model outputs that requires fast interpolation  
20 methods. While more recent modern languages like Python are used in the scientific community, Fortran remains widely in the geophysics / engineering community and is known as one of the faster language in time execution, very good on array

handling, parallelisation and above all portability. Some benchmarks are available on web site to evaluate the performances of languages on simple to complex operations (Kouatchou, 2018).

25 The parameterization techniques proposed to manage aerosol/droplet microphysical schemes (Rap et al., 2009) can employ either the modified Shepard interpolation method (Shepard, 1968) or the Hardy multiquadrics interpolation method (Hardy, 1971, 1990), and the numerical results obtained show that both methods provide realistic results for a wide range of aerosol mass loadings. For the climate community, a comparison of six methods for the interpolation of daily European climate data are proposed by (Hofstra et al., 2008), some of these methods use kriging-like methods with the capability to use co-predictors like the topography.

30 A python procedure called *scipy.interpolate.griddata* is freely available (Scipy, 2014). Unfortunately this program is not really adapted to our problem, it could be not enough optimized for our objective as it can manage fully unstructured datasets. The goal of this paper is to present a program to interpolate in a grid or a matrix which can be irregular (varying intervals) but structured with the possibility to have interdependent dimensions (e.g. a longitude interval edges which depend on longitude, latitude, altitude and time). We think this type of program can be easily implemented within models or to manage model outputs  
35 for post-treatment issues. In short, the novelty of this program is to fill the gap of interpolation issues between the treatment of very complex unstructured meshes and simple regular grids for a general dimension  $N$ .

In order to quantify the impact of such a new interpolation program and show examples of its use, it is implemented in the back-tajjectory model Backplumes, developed in the same team than the CHIMERE model, Mailler et al. (2017). This host model is well fit for this implementation, because the most important part of its calculation is an interpolation of a point in a  
40 model grid box. This paper describes (i) the methodology and the content of the interpolation program package **NterGeo**, and (ii) an application of this program embedded in the new back trajectories program **Backplumes**. These two codes are freely available (see code availability section).

## 2 Development of the interpolation program

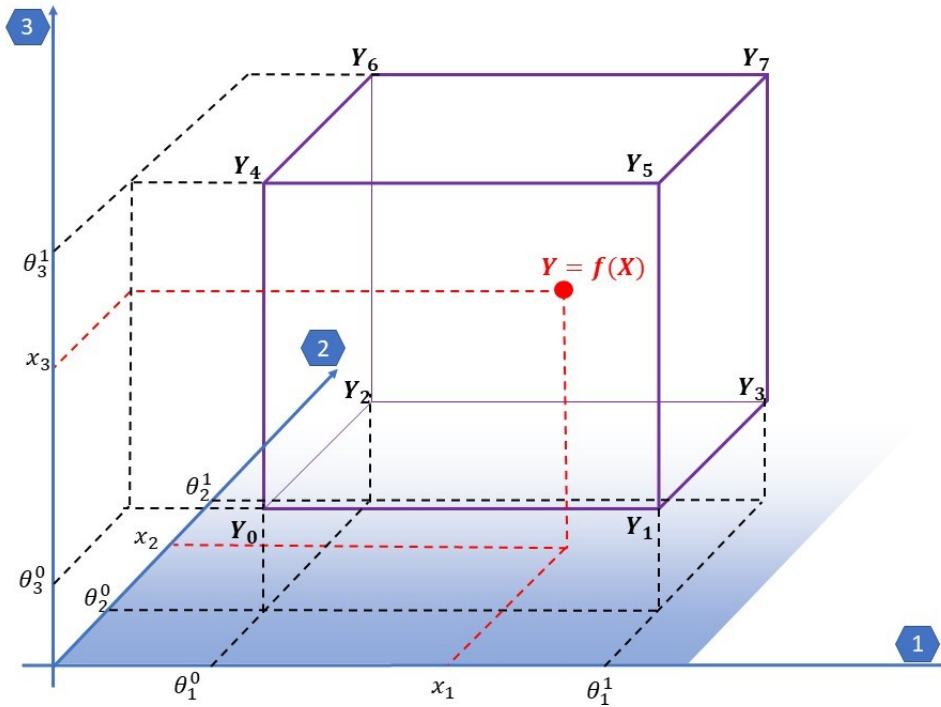
The program NterGeo is fit for exploring irregular but structured grids or look-up tables defined by a unique size for each  
45 dimension which can be of course different from one to another dimension. The space intervals can vary along a dimension and the grid interval edges in each dimension can depend on other dimensions. Two versions have been developed, (i) a version for "regular" arrays with independent dimensions and, (ii) a "general" version for possible inter-dependent dimensions, e.g. to handle 3D meshes which have time varying spatial coordinates. The code does not need any libraries and is written in standard Fortran. Our interpolation code was tested with *gfortran* (GNU Fortran project) and *ifort* (Intel). As it includes not  
50 specific options or function, version of a compiler, there is no reason to have limitations or errors with other compilers. The top shell calling script in the package provides two sets of options for "production" and "debugging" modes. Assuming the  $X$  array, the result of the function  $f$  transforming  $X$  to  $Y$  array in  $\mathbb{R}$  can be expressed as:

$$Y(x_1, \dots, x_N) = f(X(x_1, \dots, x_N)) \quad (1)$$

$N$  is the dimension of the array,  $x_i$  is the coordinates at dimension  $i \in [1, N]$  of the point  $X$  we want to interpolate.

## 55 2.1 The program for regular grids

A program `interpolation_regular.F90` for regular grids (i.e. with independent dimensions) is available. To handle this type of grids a classical multilinear interpolation is performed. Figure 1 shows the variables for  $N = 3$  defined hereafter in the section.



**Figure 1.** Description of variables for  $N=3$  with a regular grid case

For the particular case of a regular grid with independent dimensions the result  $\tilde{Y}$  of the multilinear interpolation of the  $2^N$  identified neighbours can be expressed as:

$$\begin{aligned}
 \tilde{Y} = & w_N^0 \dots w_i^0 \dots w_1^0 \times Y_0(0 \dots 0 \dots 0) \\
 & + w_N^0 \dots w_i^0 \dots w_1^1 \times Y_1(0 \dots 0 \dots 1) \\
 & + \dots \\
 & + w_N^{\delta_N} \dots w_i^{\delta_i} \dots w_1^{\delta_1} \times Y_k(\delta_N \dots \delta_i \dots \delta_1) \\
 & + \dots \\
 & + w_N^1 \dots w_i^1 \dots w_1^1 \times Y_{2^N-1}(1 \dots 1 \dots 1)
 \end{aligned} \tag{2}$$

with  $\delta_i$  the binary digit equal to 0 or 1, and the weights  $w_i^{\delta_i}$  for  $i \in [1, N]$  defined as:

$$w_i^0 = \frac{\theta_i^1 - x_i}{\theta_i^1 - \theta_i^0} \quad w_i^1 = 1 - w_i^0 \quad (3)$$

Variable  $\Theta_i$  is the list of interval edges on each dimension  $i$  and does not depend on other dimensions.  $\theta_i^{\delta_i}$  is the bottom ( $\delta_i = 0$ ) and top ( $\delta_i = 1$ ) edges on each dimension  $i \in [1 \dots N]$  so that  $x_i \in ]\theta_i^0, \theta_i^1]$ .  $Y_k$  is a 1-dimensional array with  $2^N$  elements storing the value  $Y$  of the function at the identified neighbours  $\Psi$  on each dimension:

$$Y_k(\delta_N \dots \delta_i \dots \delta_1) = f(\Psi(\theta_N^{\delta_N}, \dots, \theta_i^{\delta_i}, \dots, \theta_1^{\delta_1})) \quad (4)$$

with  $k \in [0, 2^N - 1]$

The tuple  $(\delta_N \dots \delta_i \dots \delta_1)$  is the binary transformation of integer  $k$  defined as  $\sum_{i=0}^{N-1} (\delta_i \times 2^i)$ . The coefficients  $\Gamma_k = w_N^{\delta_N} \dots w_i^{\delta_i} \dots w_1^{\delta_1}$  as a product of weighting factors on each direction can be seen as a binary suite that is convenient to handle in a compacted and optimized Fortran programming strategy for the *regular* grid version of the code (Appendix B).

## 2.2 The general program

Considering the *general* program called `interpolation_general.F90`, the coordinates of edge points are stored in a 1-dimensional array of  $n = \prod_{i=1}^N I_i$  elements with  $I_i$  the number of edges on each dimension  $i$ . The tuple of coordinates  $(j_1, \dots, j_N)$  of an interval edge  $\theta_k^i$ , with  $j_i$  the indexed coordinate on dimension  $i$ , is transformed in a 1-dimensional array indexed on  $k \in [1, n]$  by:

$$k = \sum_{j=1}^N \left( (i_j - 1) \prod_{l=0}^{j-1} I_l \right) + 1 \quad (5)$$

with  $I_0 = 1$  for initialisation.

Once the nearest neighbour is found, the result  $\tilde{Y}$  of the interpolation is a weighting procedure of the  $2^N$  closest vertice using a Shepard interpolation (Shepard, 1968) based on the inverse distance calculations:

$$\tilde{Y} = \sum_{k=0}^{2^N-1} (\Gamma_k \times Y_k) \quad (6)$$

with  $Y_k = f(\Upsilon_k)$  the value of the function  $f$  at neighbour  $\Upsilon_k$  of coordinates  $(\theta_k^1, \dots, \theta_k^N)$ , and:

$$\Gamma_k = \frac{1/d_k}{\sum_{k=0}^{2^N-1} (1/d_k)} \quad (7)$$

The distance  $d_k$  between the point of interest of coordinates  $(x_1, \dots, x_N)$  to the neighbour  $k \in [1, n]$  is calculated as:

$$d_k = \left( \sum_{i=1}^N |x_i - \theta_k^i|^p \right)^{\frac{1}{p}} \quad (8)$$



The previous formula are valid for  $d_k \neq 0$ , in the case of  $d_k = 0$  the procedure stops and exit returning the exact value of the corresponding data of the nearest neighbour. For distorted meshed or matrix, or dimensions with different units (e.g mixing time with length), a hard coded option *norm = .true.* or *.false.* is also available to normalize the intervals with an average interval  $\Delta_i$  value for the calculation of distances so that:

$$90 \quad d_k = \left( \sum_{i=1}^N \left( \frac{|x_i - \theta_k^i|}{|\Delta_i|} \right)^p \right)^{\frac{1}{p}} \quad (9)$$

### 3 Computation strategy for the general program

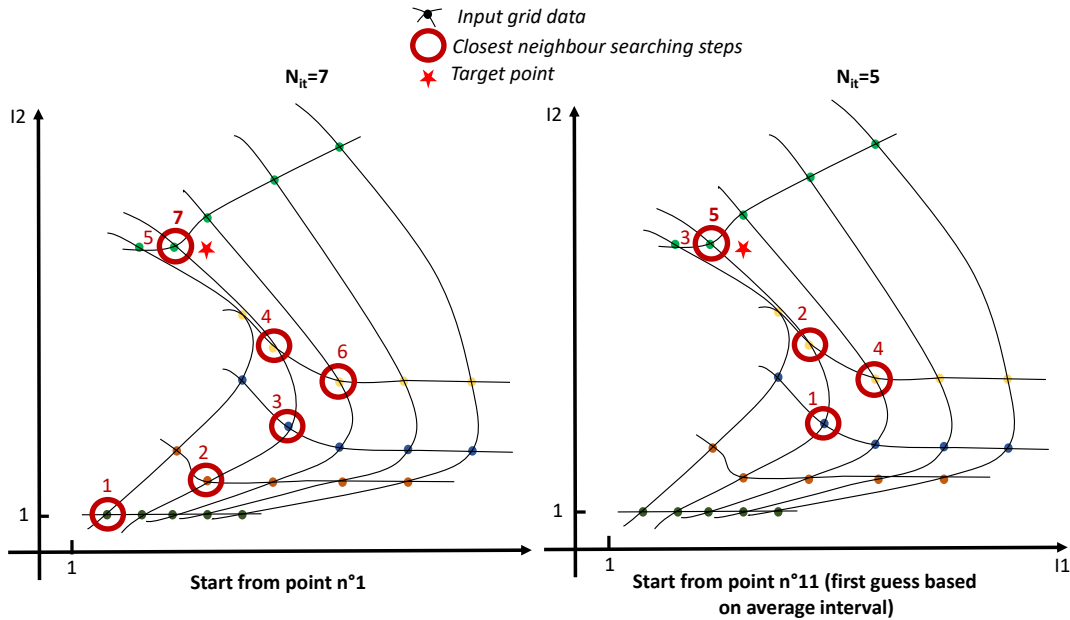
The list of input/output arguments is provided in Appendix C. In the main program calling the subroutine the key point is to transform first the N-dimension matrix into a 1D array. An example of a main program calling the subroutine is provided in the code package. The computation strategy in the subroutine can be broken down into the sequential steps as follows:

- 95 (I) Find the nearest neighbour of the input data by minimizing a distance with a simple incremental method stepping every  $\pm 1$  coordinates on each dimension (detailed later in this section).
- (II) Scan the surroundings of the nearest point within the matrix on  $\pm 1$  step on each dimension and store the corresponding block of input data to be tested. The size of the block is therefore  $(1 + 2 \times 1)^N$  but can be extended to  $(1 + 2 \times 2)^N$  if we increase the scanning process to  $\pm 2$  on each dimension (hard coded option *iconf=1* or *2* in the declaration block).
- 100 (III) Calculate the distance to the previously selected input data. A *p*-distance concept is adopted (hard coded option *pnum* in the declaration block). The *pnum* value *p* should be superior or equal to 1 to verify the Minkowski inequality and be considered as a metric.
- (IV) Sort the previous block of data in ascending order and stop the sorting process when the first  $2^N$  point are selected. The code offers the possibility to use only the first  $N + 1$  neighbours (hard coded option *neighb* in the declaration block)
- 105 that is sufficient and faster in most cases.
- (V) Calculate the weights, and then the final result.

The first step consisting in finding the first neighbour is the trickiest and is broken down into several steps. Figure 2 displays an example in 2D of the step by step procedure to find the nearest neighbour.

- 110 (i) The procedure initializes the process starting from the first point of the input data grid or taken from the last closest point if given in argument as a non-null value.
- (ii) A delta of coordinates is applied based on an average delta on each dimension to improve the initialisation. This computation step of delta is externalized as it can be time consuming and should be done once for all target points at which we want to interpolate.

- 115 (iii) A test between the target value and the input data grid points coordinates determines the  $\pm 1$  steps to add on each dimension (see Figure 2 for an example in 2D).
- (iv) If the grid point falls on the edges or outside the borders the closest coordinates within the matrix is selected.
- (v) A test on the  $p$ -distance computation between the running point and the target is performed so that if the distance calculated at Iteration  $N_{it}$  is equal to distance at Iteration  $N_{it} - 2$  the closest point is found.
- 120 (vi) If the distance is larger than the characteristic distance of the cell, the point is considered to be outside the borders of the input grid data. Therefore, the code allows a slight extrapolation if the target point is not too far from the borders.
- (vii) At this stage, the procedure can stop if the distance to the closest vertex is 0 returning to the main program with the exact value of the input data grid.



**Figure 2.** Real example in 2D of the step by step procedure to find the nearest neighbour of a target point for an irregular but structured  $5 \times 5$  grid. Left panel when starting the process from the 1<sup>st</sup> point of the grid on the lowest left corner, Right panel when starting with a first guess based on an average delta computed for each dimension.

#### 4 Visual example in 2D for a regular grid

As an example to visualize the capacity of the *general* program, the 2D function used in Scipy (2014) is used to test our procedure. The function is:

$$Y = f(X) = x_1 \times (1 - x_1) \times \cos(4\pi x_1) \times \sin(4\pi x_2^2)^2 \quad (10)$$

with  $x_1, x_2 \in [0, 1]$ .

Our input grid data is a regular grid with regular intervals of 0.02 from 0 to 1 for  $x_1$  and  $x_2$  with therefore 51 points on each dimension. We propose to interpolate on a finer regular grid with  $n=100 \times 100$ ,  $200 \times 200$  and  $300 \times 300$  points on each dimension. For these three interpolations cases a normalized root mean square error (NMSE) of the result  $\tilde{Y}_j$  for the full grid point number  $j$  can be calculated against the true value  $Y_j$  of the function as:

$$NMSE = \frac{\frac{1}{n} \sum_{j=1}^n (\tilde{Y}_j - Y_j)^2}{\frac{1}{n-1} \sum_{j=1}^n (Y_j - \bar{Y}_j)^2} \quad (11)$$

with  $\bar{Y}_j$  the mean value  $Y_j$  as  $\frac{1}{n} \sum_{j=1}^n Y_j$ .

For the three cases the CPU time for the interpolation is evaluated and displayed in Table 1 for Machine 1 (Appendix E). As expected, the time consuming is obviously proportional to the number of points in which to interpolate. Figure 3 displays the evolution of the NMSE with the parameter  $p$  of the  $p$ -distance definition. There is a discontinuity of the NMSE from  $p = 1$  to  $p = 1^+$  with a slight increase with  $p$  in an asymptotic way. The NMSE decreases with the number of points but a slight increase is observed from  $200 \times 200$  from  $300 \times 300$ .

**Table 1.** Performance for each case with  $p = 1$

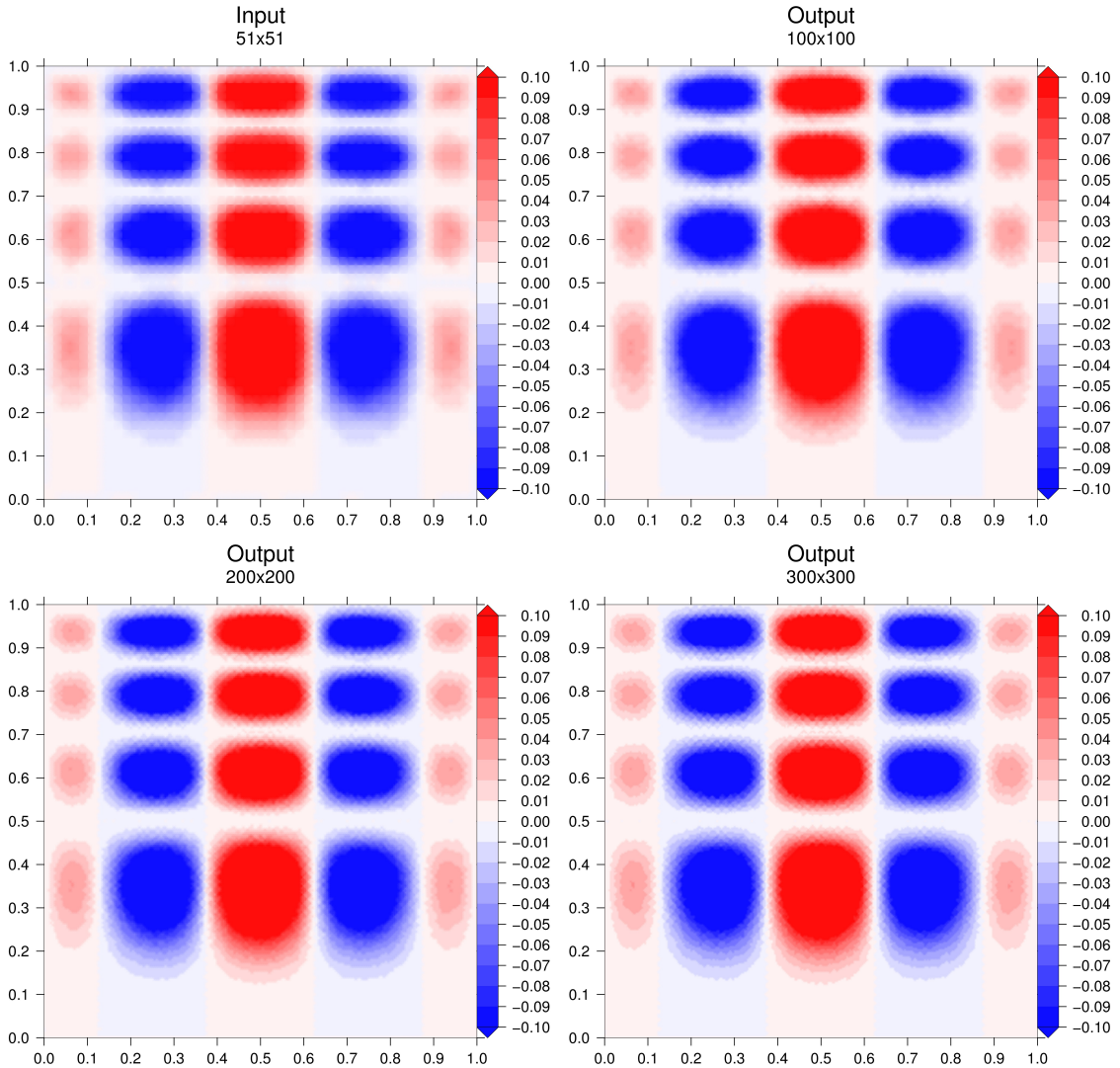
Case	100×100	200×200	300×300
NMSE (%)	0.324	0.319	0.319
CPU time (s)	0.45	1.84	4.1

#### 5 Example in 5D for a regular grid

Still using the *general* program, an example in 5D ( $N = 5$ ) is proposed using the function :

$$Y = f(X) = x_1 \times (1 - x_1) \times \cos(4\pi x_1) \times \sin(4\pi x_2) \times \cos(4\pi x_3) \times \sin(4\pi x_4) \times \cos(4\pi x_5) \quad (12)$$

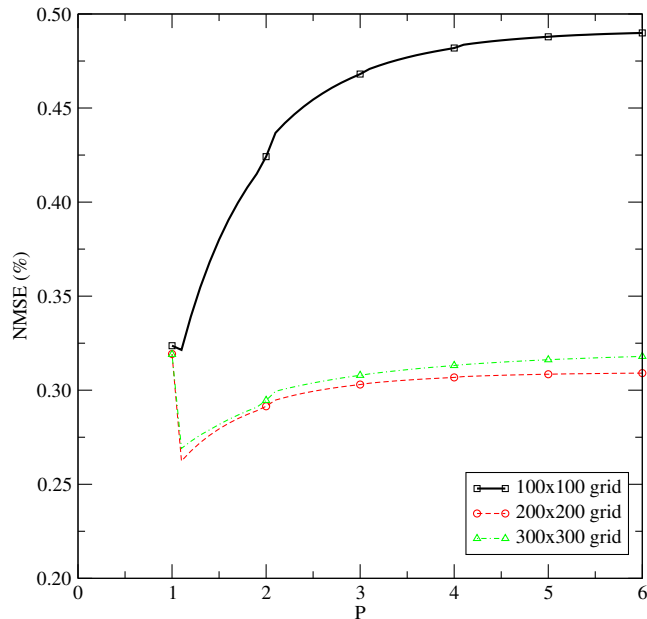
with  $x_1, x_2, x_3, x_4, x_5 \in [0, 1]$ . The input data grid is a regular grid of  $I_i = 35$  interval edges on each dimension  $i \in [1, 5]$  then  $35^5 = 52\,521\,875$  grid points. The goal is to find the results on a coarse grid of 9 elements on each dimension then  $9^5 = 59\,049$



**Figure 3.** Interpolation results for the three cases. Figures generated with the Generic Mapping Tools (Wessel et al., 2019)

grid points. This case is an opportunity to test the influence of the number of neighbours to calculate the result. In our case, the parameter  $p$  of the  $p$ -distance is set to  $p = 2$ . The interpolation seems to provide a better performance on the NMSE for our function with less neighbours (case  $N + 1$ ) and obviously with a lower CPU time. This could certainly depend on the type of function to interpolate.

Another test with the 5D case is performed to test the influence of the normalisation as defined in Equation 9 (flag *norm*) by defining an irregular grid with still  $35^5 = 52\,521\,875$  input data points but with (i) random intervals values, and (ii) one dimension depending on another. The definition of the input grid is defined in Appendix D and provided in the code package.



**Figure 4.** Evolution of performances based on the NMSE for the three cases as a function of the parameter  $p$  of the  $p$ -distance computation

**Table 2.** Performance for the 5D ( $N=5$ ) case with  $p = 2$

Number of neighbours	$2^N$	$N + 1$
NMSE (%)	1.570	0.870
CPU time (s)	17.32	6.00

With a similar order of magnitude of consumed CPU time the normalisation  $norm = .True.$  produce a  $NMSE = 0.499\%$  compared to  $NMSE = 0.822\%$  for  $norm = .False.$ . There is then an added value of using such a normalisation with comparable CPU time consuming (rising from 2.68 to 3.44 s for our case).

## 6 Comparison with Python for a regular grid

155 The code has been tested against the *Python* procedure `scipy.interpolate.griddata` freely available by (Scipy, 2014), for the following function:

$$\begin{aligned}
 Y = f(X) = & x_1 \times (1 - x_1) \times \cos(4\pi x_1) \\
 & \times \sin(4\pi x_2) \times \cos(4\pi x_3)
 \end{aligned}
 \tag{13}$$

with  $x_1, x_2, x_3 \in [0, 1]$ . The input data grid is a regular grid of  $I_i = 35$  interval edges on each dimension  $i \in [1, 5]$  then  $35^3 = 42875$  grid points. The goal is to find the results on a coarse grid of 9 elements on each dimension then  $9^3 = 729$  grid points. A case in 3D has been used for this test because the *Python* library was not able to work with very large datasets (*overflow error*) while our program could make perfectly work. `scipy.interpolate.griddata` is used with the bilinear interpolation option while our method is configured with  $p = 2$ .

Table 3 clearly shows how the Fortran code is faster compared to the Python library. However, the bilinear interpolation method seems to provide a higher accuracy than the inverse distance method embedded in our program. Nevertheless, the error produced by our method looks acceptable.

**Table 3.** Comparison of performances between our code for a 3D case with the griddata Python library. The Machine 2 is used (Appendix F).

	Our code with $N + 1$ neighbours	Our code with $2^N$ neighbours	Python
NMSE (%)	0.627	1.03	0.326
CPU time (s)	0.04	0.04	19.49

## 7 Geophysics application

### 7.1 The Backplumes model

In order to test this new interpolation program, it is implemented in a back trajectories model called "Backplumes". This model was already used in some studies such as (Mailler et al., 2016) and (Flamant et al., 2018) for example. Backplumes is open source and is available on the CHIMERE web site. Backplumes calculates back trajectories from a starting point and a starting date. It is different from other back trajectories models, such as HYSPLIT (Stein et al., 2015), STILT (Lin et al., 2003), (Nehrkorn et al., 2010) and Flexpart (Pisso et al., 2019), because it launches hundreds of particles and plot all trajectories as outputs. Thus, the answer is complementary compared to the other models: the output results is all possible trajectories, and not only the most likely.

An advantage of Backplumes for the WRF and CHIMERE users is that the code is dedicated to directly read output results of these models. Being developed by the CHIMERE developers teams, the code is completely homogeneous with CHIMERE in term of numerical libraries. Another advantage is that the code is very fast and calculates hundreds of trajectories in a few minutes. Using the wind fields of WRF or CHIMERE, and running on the same grid, the results of back trajectories are fully consistent with the simulations done by the models.

Backplumes is dedicated to calculate transport but not chemistry: only passive air particles (or tracers) are released. But a distinction could be made between gaseous or particulate tracers: for the latter one, a settling velocity is calculated to have a more realistic trajectory. The model is easy to use and light because a small set of meteorological parameters is required. These meteorological parameters are described in Table G1 for WRF and CHIMERE.

The first step of the calculation is to choose a target location as a starting point. The user must select a date, longitude, latitude and altitude, obviously included in the modelled domain and during the modelled period. From this starting point, the model will calculate trajectories back in time. The number of trajectories is up to the user and may be from one to several hundred of tracers.

At each time-step and for each trajectory, the position of the air mass is estimated by subtracting its pathway travelled as longitude  $\Delta\lambda$ , latitude  $\Delta\phi$  and altitude  $\Delta z$  to the current position. To do so, all necessary variables are interpolated with the interpolation program NterGeo.v2020a described in the previous section. The calculation is described in Appendix G.

In order to respect the Courant Friedrich Levy (CFL) number, a sub-time step may be calculated. If the input data are hourly provided (as in many regional models), the meteorological variables are interpolated between the two consecutive hours to obtain refined input data.

The goal of backplumes is to estimate all possible back trajectories. Then, starting from one unique point, it is necessary to add a pseudo-turbulence in the calculation of the altitude. Depending on the vertical position of the tracer, several hypotheses are made. Two parameters are checked for each tracer and each time-step: (i) the boundary layer height enables to know if the tracer is in the boundary layer or above in the free troposphere, (ii) the surface sensible heat fluxes enables to know if the atmosphere is stable or unstable.

When the tracer is diagnosed in the boundary layer, there are two cases: the boundary layer is stable or unstable. If the boundary layer is stable,  $Q_0 < 0$ , the tracer stays in the boundary layer at the same altitude. The new vertical position of the tracer is:

$$z_{t-1} = z_t \quad (14)$$

If the boundary layer is unstable,  $Q_0 > 0$ , the tracer is considered in the convective boundary layer and may be located at every level in this boundary layer the time before. Therefore, a random function is applied to reproduce a potential vertical mixing.

$$z_{t-1} = Rand \times \bar{h} \quad (15)$$

The random function 'Rand' calculates a coefficient, between 0 and 1 to represent a stochastic vertical transport of the tracer. It is considered that 15 mn is representative of a well-mixed convective layer, Stull (1988). If the time step is larger than 15 mn, the random function is applied. But if the time step is less than 15 mn, the vertical mixing is reduced to the vicinity of the current position of the tracer. In this case, we have:

$$z_{t-1} = Rand \times \Delta z \times [z_t] \quad (16)$$

where  $\Delta z = \frac{1}{2}(z_t^{k-1} + z_t^{k+1})$  and  $k$  is the vertical model level corresponding to  $z_t$ .

In the free troposphere, the evolution of the tracer is considered to be influenced by the vertical wind component. A random function is applied to estimate its possible vertical motion with values between 0 and  $w/2 \text{ m s}^{-1}$ , representative of all possible values of vertical wind speed in the troposphere, Stull (1988). The vertical variability of the tracer's position in the free troposphere is calculated by diagnosing the vertical velocity as:

$$z_{t-1} = z_t - (0.5 + Rand)w \frac{3600}{\Delta t} \quad (17)$$

## 7.2 Examples of back trajectories computations

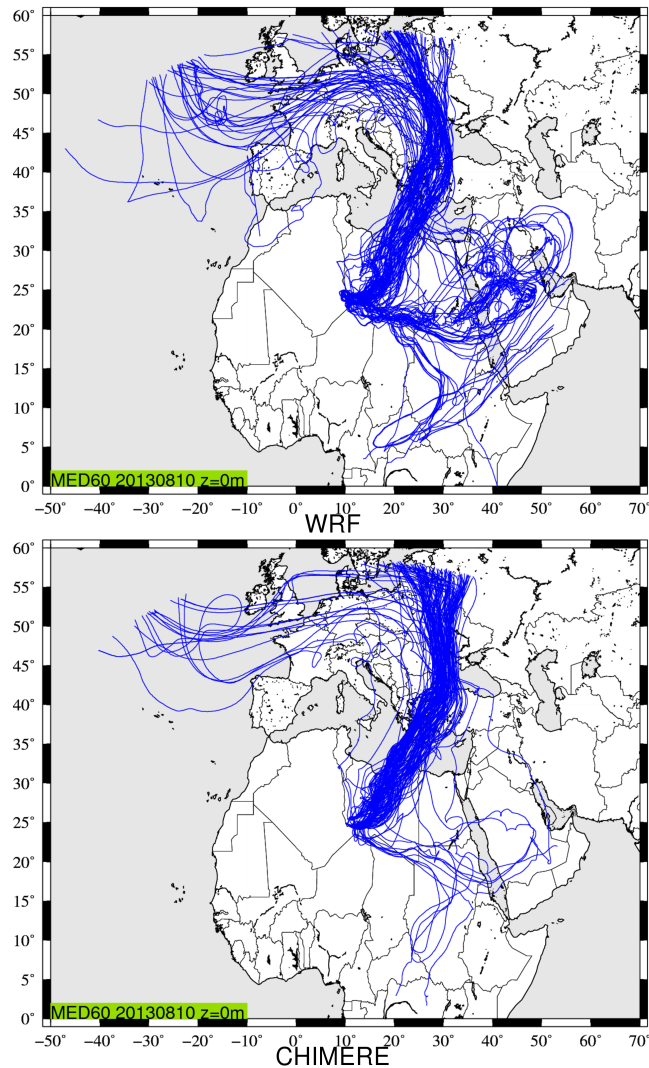
An example is presented for the same case and the WRF and CHIMERE models. The difference between the two models is the number of vertical levels (35 for WRF and 20 for CHIMERE, for the surface to 200 hPa). The online modelling system WRF-CHIMERE is used, meaning that the horizontal grid is the same (a large domain including Europe and Africa and with  $\Delta x = \Delta y = 60 \text{ km}$ ). The wind field is the same for both models: CHIMERE using directly the wind field calculated by WRF. The boundary layer height is different between the two models, WRF using the Hong et al. (2006) schemes and CHIMERE using the Troen and Mahrt (1986) scheme. The surface sensible heat flux is the same between the two models, CHIMERE using the flux calculated by WRF. WRF has more vertical model levels than CHIMERE, thus meteorological fields are interpolated from WRF to CHIMERE. It impacts the horizontal and vertical wind fields.

Figure 5 presents the results of back trajectories launched the 10 August 2013 at 12:00 UTC. The location is at longitude  $+10^\circ \text{E}$  and latitude  $+25^\circ \text{N}$ , altitude = 0 m AGL. This location has no scientific interest but is in the middle of the domain, to have the longer trajectories as possible. The complete duration of trajectories represent 10 days back in time. A total of 120 trajectories are launched at the same position and time. They are randomly mixed when they are in the boundary layer to represent the mixing and the diffusion.

The most important part of the plume comes from the North of the starting point. For this main plumes, the calculation is similar between the two models. Another large part of backplumes is modelled at the East of the starting point. However, this fraction is mainly modelled with WRF but not with CHIMERE where only a few trajectories are diagnosed. One possible explanation may be found by analyzing the vertical transport of the trajectories.

Figure 6 presents all plumes displayed in the previous figure but projected along the same time-altitude axis. The differences between the two backplumes results are mainly due to the calculation of the boundary layer height. When WRF diagnosed an altitude of  $\approx 3000 \text{ m}$ , CHIMERE diagnoses  $\approx 2000 \text{ m}$ , leading to different direction and wind speed. Then, this implies a split of the plumes with WRF but not with CHIMERE. This illustrates the sensitivity of the result to the driver model. But, in both cases, the answer in our case is clearly that the main contribution of the air masses located at the starting point are mainly coming from the North-East, crossing Tunisia, then the Mediterranean sea and Europe. The main difference between the two calculations is the eastern part of the plume, more intense with WRF than CHIMERE.

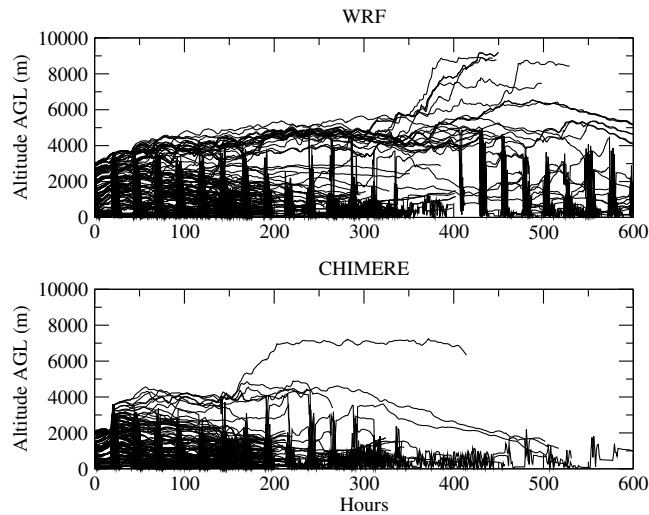




**Figure 5.** Back trajectories calculated using CHIMERE and WRF modelled meteorological fields. The starting point is at longitude  $+10^{\circ}E$  and latitude  $+25^{\circ}N$ , altitude=0 m AGL and for the day 10 August 2013 at 12:00 UTC. It corresponds to a case studied during the CHARMEX campaign (Menuet et al., 2015).

## 8 Conclusions

245 A new interpolation program written in Fortran has been developed to interpolate on N-dimensional matrices. It has been evaluated for several dimension cases up to  $N=5$ . The code is fast compared to similar Python routines and highly portable in existing geophysical codes. The interpolation program works for any dimension  $N$  above 2 and designed to work with irregular but structured grids (characterized by a size for each dimension) or look-up tables. Already used in its 'regular' version in



**Figure 6.** Projection of all back trajectories on a single time-altitude axis.

CHIMERE, the 'general' program has been tested on a new real application which calculates air mass back trajectories from two widely used atmospheric models: CHIMERE and WRF. This interpolation program can be used for any application in  
 250 Geophysics and Engineering Sciences but also to explore large structured matrices.

*Code availability.* The current version of the models are freely available. The exact version of the model used to produce the results used in this paper is archived (i) on Zenodo for NterGeo at <https://doi.org/10.5281/zenodo.3733278> under the GNU General Public License v3.0 or later, as are input data and scripts to run the model and produce the plots for all the simulations presented in this paper. The Backplumes model is an open-source code and is available on the CHIMERE model web site <https://www.lmd.polytechnique.fr/~menut/backplumes.php>.

## 255 **Appendix A: List of frequently used abbreviations**

AGL	Above Ground Level
CFL	Courant Freidrich Levy
CHIMERE	National French CTM
CTM	Chemistry-transport model
CPU	Central Processing Unit
NMSE	Normalized Root Mean Square Error
PBL	Planetary Boundary Layer
PSFC	Surface Pressure
WRF	Weather Research and Forecasting model

## Appendix B: Binary strategy

This piece of code shows the strategy to optimize the computation of weights for the "regular case". The idea is to minimize the number of operation to benefit from the calculation at each dimension. A non-optimized loop would require  $2^N - 1$  multi-  
260 plications while the optimized loop requires only  $2^{N+1} - 4$  multiplications for the weight calculations. Then, for large values of  $N \gg 2$ , the ratio of required operations between the non-optimized and the optimized loop is  $\approx (N - 1)/2$ .

```
! ...
nn=2**ndim           ! ndim is the dimension of the case study
pn=2**(ndim-1)      !
265 ! Loop to convert k in binary
do k=0,nn-1
  do j=0,ndim-1
    if (btest(k,j)) then
      ibin(j,k)=1
270    else
      ibin(j,k)=0
    endif
  enddo
enddo
275 ...
! Main optimized loop (2 loops sequence) to calculate the weighting factors benefiting from
! the previous iteration on the main dimension i
do i=1,ndim           ! Loop 1
  ni=2**i
280  pi=ni/2
  do k=0,ni-1         ! Loop 2
    delta=ibin(i-1,k)
    if (i.ne.1) then
      if (delta.eq.0) then
285        ws(k)=weight(k)
        weight(k)=weight(k)*w(i,delta) ! where w is the weight on each dimension
      else
        weight(k)=ws(k-pi)*w(i,delta)
      endif
290    else
      weight(k)=w(i,delta)
    endif
  enddo
enddo
```

## 295 Appendix C: Code design

Note that *avedelta* and *maxdelta* arrays have been externalized to optimize the calculations. In the code package an independent program is available to calculate these arrays to be implemented in your main program. The program is written in Fortran *double precision* ingesting the following arguments:

```

subroutine interpolation_general(&
300 ndim,      &! Input : Int
      maxdim,  &! Input : Int
      kdim,    &! Input : Array 1D, Int
      vect,    &! Input : Array 2D, Real
      vtable,  &! Input : Array 1D, Real
305 table,    &! Input : Array 1D, Real
      avedelta, &! Input : Array 1D, Real
      maxdelta, &! Input : Array 1D, Real
      table,   &! Input : Array 1D, Real
      resu,    &! Output : Real
310 inei,     &! Output : Integer
      neighbours, &! Output/Input : Array 2D, Int
      weights, &! Output : Array 1D, Real
      found    &! Output : Logical
      )

```

315 Some hard coded variables can be tested by the user to improve the results. They have been tested and some results are described in this paper. A recompilation is necessary if you change these values.

```

logical ,parameter      :: norm=.false.    ! Normalize or not by the average delta on each
      dimension
logical ,parameter      :: verbose=.false. ! Level of message writing (.true. for debug)
320 logical ,parameter      :: neighb=.true.  ! .true. only find up to ndim+1 closest neighbours to
      be faster
      ! .false. find up to 2NDIM closest neighbours
integer ,parameter      :: iconf=1        ! Number of cell to account for before and after
      ! the closest point, iconf=2 can be tested not more
325 real(kind=iprec),parameter :: pnum=2.0d+00 ! p-distance parameter

```

**Table C1.** Description of subroutine arguments

<b>Variable</b>	<b>Type</b>	<b>Description</b>	<b>Array dimension</b>
<i>ndim</i>	Integer	Dimension $N > 1$	nd
<i>maxdim</i>	Integer	Total number of elements of the input table $n = \prod_{i=1}^N I_i$ with $I_i$ the number of elements in each dimension $i$	nd
<i>kdim</i>	Integer 1D Array	Array of number of elements $I_i$ on each dimension $i$	(0 : $N$ )
<i>vect</i>	Real 2D Array	Array storing in a 1 dimensional array the list of edges on each dimension	(1 : $N$ , 1 : $n$ )
<i>vtable</i>	Real 1D Array	Coordinate values of the point at which to interpolate data	(1 : $N$ )
<i>table</i>	Real 1D Array	Values for the list of known points <i>vect</i> (input grid data)	(1 : $n$ )
<i>avedelta</i>	Real 1D Array	Inverse of average intervals on each dimension $N$	( $N$ )
<i>maxdelta</i>	Real 1D Array	Maximum intervals on each dimension $N$	( $N$ )
<i>resu</i>	Real	Result of interpolation for <i>vtable</i>	nd
<i>inei</i>	Integer	Number of neighbours	nd
<i>neighbours</i>	Real 2D Array	Array of neighbours coordinates	(1 : $2^N$ , 1 : $n$ )
<i>weights</i>	Real 1D Array	Weight for each neighbour	(1 : $2^N$ )
<i>found</i>	Logical	Returns <i>true</i> or <i>false</i> if respectively the result is found or not found if the point is outside the bounds	nd

## Appendix D: Irregular structured grid example in 5D

Herebelow is an example of a 5D array input griddata with irregular intervals with the last dimension (5) depending on dimension (1).

```
! Definition of main dimensions
330 isize=9           !Outputgrid size
    npoints=35       !Inputgrid size
    ndim=5           !Dimension of the example
    allocate(kdim(0:ndim)) !Number of element per dimension array
    kdim(0)=1        !Fake dimension for computation issues
335 kdim(1)=npoints
    kdim(2)=npoints
    kdim(3)=npoints
    kdim(4)=npoints
    kdim(5)=npoints
340 ! Main array allocation
    allocate(delta(ndim))
    allocate(dstart(ndim))
    allocate(vect(ndim,kdim(1),kdim(2),kdim(3),kdim(4),kdim(5)))
    allocate(rando(ndim,1:npoints-1)) !Random variable
345 maxdim=kdim(1)*kdim(2)*kdim(3)*kdim(4)*kdim(5)
    !
    ! Definition of the input grid "vect" with delta, dstart as:
    do j=1,ndim
        delta(j)=1.d+00/dfloat(npoints-1)/(dfloat(j)**3)
350 dstart(j)=1.d+00/dfloat(npoints-1)/2.d+00/(dfloat(j)**3)
    enddo
    do j=1,ndim
        do i=1,npoints-1
            rando(j,i)=dfloat(int(dlog(rand()*10.d+00+1.d+00))+2) !Random interval on each dimension
355 enddo
            rando(j,:)=dfloat(npoints-1)*rando(j,:)/sum(rando(j,:)) !Normalisation of random intervals
    enddo
    vect=0.0d+00 ! Initialisation
    ! "vect" computation
360 do i=2,kdim(1)
        vect(1,i,::,::)= vect(1,i-1,::,::)+rando(1,i-1)*delta(1)
    enddo
    do j=2,kdim(2)
        vect(2,:,j,::,::)= vect(2,:,j-1,::,::)+rando(2,j-1)*delta(2)
365 enddo
    do k=2,kdim(3)
        vect(3,::,k,::,::)= vect(3,::,k-1,::,::)+rando(3,k-1)*delta(3)
```

```

enddo
do l=2,kdim(4)
370 vect(4, :, :, :, l, :) = vect(4, :, :, :, l-1, :) + rando(4, l-1) * delta(4)
enddo
do m=2,kdim(5)
do i=1,kdim(1)
    vect(5, i, :, :, m) = vect(5, i, :, :, m-1) + rando(5, m-1) * delta(5) + &
375 & delta(5) * dfloat(i-1) / dfloat(kdim(1)-1) !Dim 5 depends on Dim. 1
enddo
enddo
! ....

```

## Appendix E: Characteristics of Machine 1

- 380
  - Architecture: x86\_64
  - CPU op-mode(s): 32-bit, 64-bit
  - Byte Order: Little Endian
  - CPU(s): 64
  - On-line CPU(s) list: 0-63
- 385
  - Thread(s) per core: 2
  - Core(s) per socket: 8
  - Socket(s): 4
  - NUMA node(s): 8
  - Vendor ID: AuthenticAMD
- 390
  - CPU family: 21
  - Model: 1
  - Model name: AMD Opteron(TM) Processor 6276
  - Stepping: 2
  - CPU MHz: 2300.000
- 395
  - CPU max MHz: 2300.0000
  - CPU min MHz: 1400.0000
  - BogoMIPS: 4599.83
  - Virtualization: AMD-V
  - L1d cache: 16K
- 400
  - L1i cache: 64K
  - L2 cache: 2048K
  - L3 cache: 6144K



- Memory block size: 128M
- Total online memory: 128G
- 405 – Total offline memory: 0B
- Linux version 3.10.0-1062.12.1.el7.x86\_64 (mockbuild@kbuilder.bsys.centos.org) (gcc version 4.8.5 20150623 (Red Hat 4.8.5-39))

## **Appendix F: Characteristics of Machine 2**

- Architecture: x86\_64
- 410 – CPU op-mode(s): 32-bit, 64-bit
- Byte Order: Little Endian
- CPU(s): 96
- On-line CPU(s) list: 0-47
- Off-line CPU(s) list: 48-95
- 415 – Thread(s) per core: 1
- Core(s) per socket: 24
- Socket(s): 2
- NUMA node(s): 2
- Vendor ID: GenuineIntel
- 420 – CPU family: 6
- Model: 85
- Model name: Intel(R) Xeon(R) Platinum 8168 CPU @ 2.70GHz
- Stepping: 4
- CPU MHz: 2701.000
- 425 – CPU max MHz: 2701.0000
- CPU min MHz: 1200.0000

- BogoMIPS: 5400.00
- Virtualization: VT-x
- L1d cache: 32K
- 430 – L1i cache: 32K
- L2 cache: 1024K
- L3 cache: 33792K
- NUMA node0 CPU(s): 0-23
- NUMA node1 CPU(s): 24-47
- 435 – Memory block size: 128M
- Total online memory: 190.8G
- Linux version 3.10.0-957.41.1.el7.x86\_64 (mockbuild@x86-vm-26.build.eng.bos.redhat.com) (gcc version 4.8.5 20150623 (Red Hat 4.8.5-36))

## Appendix G: The WRF and CHIMERE model parameters used

440 Parameters are the three-dimensional wind components, the boundary layer height  $\bar{h}$ , the surface sensible heat flux  $Q_0$  and the altitude of each model layer. The wind components are used for the horizontal and vertical transport. The boundary layer height is used to define the vertical extent of the possible mixing and the surface sensible heat flux is used to know if the current modelled hour corresponds to a stable or unstable surface layer (for when the tracer is close to the surface).

Backplumes calculates the back trajectories using longitude, latitude and altitude in meters. In case of input data with vertical  
445 levels in pressure coordinates, the altitude is calculated from pressure levels, R.A. (1984). It is the case of the WRF model and the calculation is done as:

The altitude is computed as follows:

$$p^* = p_{surf} - p_{top} \tag{G1}$$

where  $p_{surf}$  (PSFC) is the surface pressure and  $p_{top}$  is the top pressure of the model domain. If  $p_{top}$  is constant over the whole  
450 domain,  $p_{surf}$  and thus  $p^*$  are dependent on the first level grid.

$$z_0 = \frac{\Phi(1) + \Phi'(1)}{g} \tag{G2}$$

Parameter	Model variable name
<b>WRF model</b>	
Longitude, latitude	XLONG, XLAT
Parameters for altitude	P_TOP, ZNU, ZNW, P, PB PH, PHB, PSFC
Wind components	U, V, W
Q <sub>0</sub>	HFX
$\bar{h}$	PBLH
<b>CHIMERE model</b>	
Longitude, latitude	lon, lat
Altitude	hlay
Wind	winz, winm, winw
Q <sub>0</sub>	sshf
$\bar{h}$	hght

**Table G1.** List of parameters read by the Backplumes program to calculate trajectories.

where  $\Phi$  is the geopotential (PHB) and  $\Phi'$  (PH) its perturbation at vertical level  $k$ .  $g$  is the acceleration of gravity,  $g=9.81$  m  $s^{-2}$ . For each vertical level  $k$ , the layer thickness  $\Delta z$  and the cell top altitude  $z_k$  is estimated as:

$$\begin{aligned}
 d_m &= \log \left( \frac{p^* \eta_M - p_{top}}{p^* \eta_M + p_{top}} \right) \\
 d_u &= \log \left( \frac{p^* \eta_M - p_{top}}{p^* \eta_F + p_{top}} \right) \\
 z_1 &= \frac{\Phi(k) + \Phi'(k)}{g} \\
 z_2 &= \frac{\Phi(k+1) + \Phi'(k+1)}{g} \\
 \Delta z &= (z_2 - z_1) \frac{d_u}{d_m} \\
 z(k) &= z_1 + \Delta z - z_0
 \end{aligned} \tag{G3}$$

455 where  $\eta_M$  is its value on full (w) levels (ZNW) and  $\eta_F$  is the eta value on half (mass) levels (ZNU). The layer thicknesses is space and time dependent, this calculation is performed for all trajectories and all time-step.

The new position of a tracer back in time is calculated as follow:

$$\begin{aligned}
\phi_{rad} &= \phi \frac{\pi}{180} \\
\Delta x &= u \frac{3600}{\Delta t} \\
\Delta y &= v \frac{3600}{\Delta t} \\
\Delta \lambda &= \frac{\Delta x}{R \cos(\phi_{rad})} \frac{180}{\pi} \\
\Delta \phi &= \frac{\Delta y}{R} \frac{180}{\pi}
\end{aligned} \tag{G4}$$

with the wind speed is provided in  $\text{m s}^{-1}$  on an hourly basis,  $R$  is the Earth radius as  $R=6371$  km. The new position for one  
460 tracer is thus:

$$\begin{aligned}
\lambda_{t-1} &= \lambda_t - \Delta \lambda \\
\phi_{t-1} &= \phi_t - \Delta \phi
\end{aligned} \tag{G5}$$

*Author contributions.* Bertrand Bessagnet has developed the code. Laurent Menut and Bertrand Bessagnet has co-developed and implemented the code in the Backplumes.v2020r1 model. Maxime Beauchamp has supported Bertrand Bessagnet for the developments.

*Competing interests.* The author declares that there is no conflict of interest.

465 *Acknowledgements.* This research was funded by the DGA (French Directorate General of Armaments) grant number 2018 60 0074 in the frame of the project NETDESA.

## References

- Donner, L. J., Wyman, B. L., Hemler, R. S., Horowitz, L. W., Ming, Y., Zhao, M., Golaz, J.-C., Ginoux, P., Lin, S.-J., Schwarzkopf, M. D., Austin, J., Alaka, G., Cooke, W. F., Delworth, T. L., Freidenreich, S. M., Gordon, C. T., Griffies, S. M., Held, I. M., Hurlin, W. J., Klein, S. A., Knutson, T. R., Langenhorst, A. R., Lee, H.-C., Lin, Y., Magi, B. I., Malyshev, S. L., Milly, P. C. D., Naik, V., Nath, M. J., Pincus, R., Ploshay, J. J., Ramaswamy, V., Seman, C. J., Shevliakova, E., Sirutis, J. J., Stern, W. F., Stouffer, R. J., Wilson, R. J., Winton, M., Wittenberg, A. T., and Zeng, F.: The Dynamical Core, Physical Parameterizations, and Basic Simulation Characteristics of the Atmospheric Component AM3 of the GFDL Global Coupled Model CM3, *Journal of Climate*, 24, 3484–3519, <https://doi.org/10.1175/2011JCLI3955.1>, <https://doi.org/10.1175/2011JCLI3955.1>, 2011.
- 470 Flamant, C., Deroubaix, A., Chazette, P., Brito, J., Gaetani, M., Knippertz, P., Fink, A. H., de Coetlogon, G., Menut, L., Colomb, A., Denjean, C., Meynadier, R., Rosenberg, P., Dupuy, R., Dominutti, P., Duplissy, J., Bourriane, T., Schwarzenboeck, A., Ramonet, M., and Totems, J.: Aerosol distribution in the northern Gulf of Guinea: local anthropogenic sources, long-range transport, and the role of coastal shallow circulations, *Atmospheric Chemistry and Physics*, 18, 12 363–12 389, <https://doi.org/10.5194/acp-18-12363-2018>, 2018.
- Hardy, R.: Multivariate equations of topography and other irregular surfaces, *Journal of Geophysical Research*, 71, 1905–1915, 1971.
- 480 Hardy, R.: Theory and applications of the multiquadric-biharmonic method 20 years of discovery 1968–1988, *Computers and Mathematics with Applications*, 19, 163 – 208, [https://doi.org/https://doi.org/10.1016/0898-1221\(90\)90272-L](https://doi.org/https://doi.org/10.1016/0898-1221(90)90272-L), <http://www.sciencedirect.com/science/article/pii/089812219090272L>, 1990.
- Hofstra, N., Haylock, M., New, M., Jones, P., and Frei, C.: Comparison of six methods for the interpolation of daily, European climate data, *Journal of Geophysical Research: Atmospheres*, 113, <https://doi.org/10.1029/2008JD010100>, <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2008JD010100>, 2008.
- 485 Hong, S. Y., Noh, Y., and Dudhia, J.: A new vertical diffusion package with an explicit treatment of entrainment processes, *Mon Weather Rev*, 134, 2318–2341, <https://doi.org/10.1175/MWR3199.1>, 2006.
- Kouatchou, J.: NASA Modeling Guru: Basic Comparison of Python, Julia, Matlab, IDL and Java (2018 Edition), available at: <https://modelingguru.nasa.gov/docs/DOC-2676> (last access: 11 March 2020), 2018.
- 490 Lin, J. C., Gerbig, C., Wofsy, S. C., Andrews, A. E., Daube, B. C., Davis, K. J., and Grainger, C. A.: A near-field tool for simulating the upstream influence of atmospheric observations: The Stochastic Time-Inverted Lagrangian Transport (STILT) model, *Journal of Geophysical Research: Atmospheres*, 108, n/a–n/a, <https://doi.org/10.1029/2002JD003161>, <http://dx.doi.org/10.1029/2002JD003161>, 4493, 2003.
- Mailler, S., Menut, L., di Sarra, A. G., Becagli, S., Di Iorio, T., Bessagnet, B., Briant, R., Formenti, P., Doussin, J.-F., Gómez-Amo, J. L., Mallet, M., Rea, G., Siour, G., Sferlazzo, D. M., Traversi, R., Udisti, R., and Turquety, S.: On the radiative impact of aerosols on photolysis rates: comparison of simulations and observations in the Lampedusa island during the ChArMEx/ADRIMED campaign, *Atmospheric Chemistry and Physics*, 16, 1219–1244, <https://doi.org/10.5194/acp-16-1219-2016>, 2016.
- 495 Mailler, S., Menut, L., Khvorostyanov, D., Valari, M., Couvidat, F., Siour, G., Turquety, S., Briant, R., Tuccella, P., Bessagnet, B., Colette, A., Létinois, L., Markakis, K., and Meleux, F.: CHIMERE-2017: from urban to hemispheric chemistry-transport modeling, *Geoscientific Model Development*, 10, 2397–2423, <https://doi.org/10.5194/gmd-10-2397-2017>, 2017.
- 500 Menut, L., Rea, G., Mailler, S., Khvorostyanov, D., and Turquety, S.: Aerosol forecast over the Mediterranean area during July 2013 (ADRIMED/CHARMEX), *Atmospheric Chemistry and Physics*, 15, 7897–7911, <https://doi.org/10.5194/acp-15-7897-2015>, 2015.

- Nehrkorn, T., Eluszkiewicz, J., Wofsy, S., Lin, J., Gerbig, C., Longo, M., and Freitas, S.: Coupled weather research and forecasting-stochastic time-inverted lagrangian transport (WRF-STILT) model, *Meteorology and Atmospheric Physics*, 107, 51–64, <https://doi.org/10.1007/s00703-010-0068-x>, 2010.
- 505 Nenes, A., Pilinis, C., and Pandis, S.: ISORROPIA: A new thermodynamic model for inorganic multicomponent atmospheric aerosols, *Aquatic Geochem.*, 4, 123–152, 1998.
- Nenes, A., Pandis, S. N., and Pilinis, C.: Continued development and testing of a new thermodynamic aerosol module for urban and regional air quality models, *Atmos Environ*, 33, 1553–1560, 1999.
- Pisso, I., Sollum, E., Grythe, H., Kristiansen, N. I., Cassiani, M., Eckhardt, S., Arnold, D., Morton, D., Thompson, R. L., Groot Zwaafink, C. D., Evangeliou, N., Sodemann, H., Haimberger, L., Henne, S., Brunner, D., Burkhardt, J. F., Fouilloux, A., Brioude, J., Philipp, A., Seibert, P., and Stohl, A.: The Lagrangian particle dispersion model FLEXPART version 10.4, *Geoscientific Model Development*, 12, 4955–4997, <https://doi.org/10.5194/gmd-12-4955-2019>, <https://www.geosci-model-dev.net/12/4955/2019/>, 2019.
- 510 R.A., P.: *Mesoscale Meteorological Modeling*, Academic Press, 1984.
- Rap, A., Ghosh, S., and Smith, M. H.: Shepard and Hardy Multiquadric Interpolation Methods for Multicomponent Aerosol–Cloud Parameterization, *Journal of the Atmospheric Sciences*, 66, 105–115, <https://doi.org/10.1175/2008JAS2626.1>, <https://doi.org/10.1175/2008JAS2626.1>, 2009.
- 515 Scipy, C.: Interpolate unstructured D-dimensional data: <https://docs.scipy.org/doc/scipy-0.14.0/reference/generated/scipy.interpolate.griddata.html>, 2014.
- Shepard, D.: A Two-Dimensional Interpolation Function for Irregularly-Spaced Data, in: *Proceedings of the 1968 23rd ACM National Conference, ACM '68*, p. 517–524, Association for Computing Machinery, New York, NY, USA, <https://doi.org/10.1145/800186.810616>, <https://doi.org/10.1145/800186.810616>, 1968.
- 520 Skamarock, W. C., Klemp, J. B., Dudhia, J., Gill, D. O., Barker, D. M., Duda, M., Huang, X., Wang, W., and Powers, J. G.: A description of the Advanced Research WRF Version 3, NCAR Tech. Note, pp. 1 – 125, 2008.
- Stein, A. F., Draxler, R. R., Rolph, G. D., Stunder, B. J. B., Cohen, M. D., and Ngan, F.: NOAA’s HYSPLIT Atmospheric Transport and Dispersion Modeling System, *Bulletin of the American Meteorological Society*, 96, 2059–2077, <https://doi.org/10.1175/BAMS-D-14-00110.1>, 2015.
- 525 Stull, R.: *An introduction to boundary layer meteorology*, Kluwer Academic Publishers Group, 1988.
- Sun, T. and Grimmond, S.: A Python-enhanced urban land surface model SuPy (SUEWS in Python, v2019.2): development, deployment and demonstration, *Geoscientific Model Development*, 12, 2781–2795, <https://doi.org/10.5194/gmd-12-2781-2019>, <https://www.geosci-model-dev.net/12/2781/2019/>, 2019.
- 530 Troen, I. and Mahrt, L.: A simple model of the atmospheric boundary layer: Sensitivity to surface evaporation, *Boundary-Layer Meteorology*, 37, 129–148, 1986.
- Wessel, P., Luis, J. F., Uieda, L., Scharroo, R., Wobbe, F., Smith, W. H. F., and Tian, D.: The Generic Mapping Tools Version 6, *Geochemistry, Geophysics, Geosystems*, 20, 5556–5564, <https://doi.org/10.1029/2019GC008515>, <https://agupubs.onlinelibrary.wiley.com/doi/abs/10.1029/2019GC008515>, 2019.
- 535 Zender, C. S.: Analysis of self-describing gridded geoscience data with netCDF Operators (NCO), *Environmental Modelling & Software*, 23, 1338 – 1342, <https://doi.org/https://doi.org/10.1016/j.envsoft.2008.03.004>, <http://www.sciencedirect.com/science/article/pii/S1364815208000431>, 2008.