Supplementary materials: "Implementation of RCIP scheme and its performance on 1D age computation in ice sheet models"

Saito, Obase and Abe-Ouchi

S1 Comprehensive experiment sheets

In addition to the experiments presented in the main paper, several experimental configuration combinations of parameters are examined. In this Supplement, some representative results of them are provided. All of the experiments shown are examined under non-steady surface mass balance configurations. Each page contains two figures: the upper one is the result obtained using a square-wave type surface mass balance input, while the lower is one with the same configuration except for applying a cosine-wave type input. One figure contains five sub-figures. (a) profiles of the computed age, (b,d) The computed age differences relative to the result of the RCIP+corr case, and (c,e) the annual layer thickness. The upper sub-figures (a-c) show the profiles in terms of depths, while the lower sub-figures (d-e) show them in terms of the computed ages. The surface mass balance input used in each experiment is shown in the lower left figure for only first 200 or 100 kyr. The prescribed time evolution of ice-thickness is also shown in the lower left figure for the non-steady thickness experiments. The grey and black lines in (a,c,e) correspond to 'benchmark' profiles which are computed using constant surface/basal mass balance and thickness.

Figures S1 to S6 are the results of a most standard experiments: constant $H = 3000\,\mathrm{m}$, $a_\mathsf{H}, a_\mathsf{L} = 3, 1.5\,\mathrm{cm\,yr^{-1}}$, $P_\mathsf{T} = 100\,\mathrm{kyr}$, $P_\mathsf{H} : P_\mathsf{L} = 1 : 1$, and the uniform discretization of 129 levels (see Eq.57 in the main text about definition of a_H, a_L, P_T, P_H and P_L). Basal mass balances are set as constant $M_\mathrm{b} = 0\,\mathrm{mm\,yr^{-1}}$ (S1,S2), $M_\mathrm{b} = 0.3\,\mathrm{mm\,yr^{-1}}$ (S3,S4), and $M_\mathrm{b} = 3\,\mathrm{mm\,yr^{-1}}$ (S5,S6). All of the results are the snapshots at $t = 1\,\mathrm{Myr}$.

Figures S7 to S12 are the same combination as presented above except for $a_\mathsf{L} = 0.75\,\mathrm{cm\,yr^{-1}}$. Figures S13 to S18 are the same except for $a_\mathsf{L} = 0\,\mathrm{cm\,yr^{-1}}$. Figures S19 to S22 are the same except for $a_\mathsf{L} = -15\,\mathrm{cm\,yr^{-1}}$.

Two types of sensitivity experiments regarding to the shape of prescribed time-evolution of surface mass balance inputs are performed: one type obtained using a different $P_\mathsf{H} : P_\mathsf{L}$, and the other using a different P_T. Figures S23 to S26 are the results obtained using a longer P_H, as $P_\mathsf{H} : P_\mathsf{L} = 7 : 1$, and Figures S27 to S30 are the results using a shorter P_H, as $P_\mathsf{H} : P_\mathsf{L} = 1 : 7$. Figures S31 to S38 are the results obtained using $P_\mathsf{T} = 50\,\mathrm{kyr}$, Figures S39 to S46 using $P_\mathsf{T} = 20\,\mathrm{kyr}$, and Figures S47 to S54 using $P_\mathsf{T} = 10\,\mathrm{kyr}$.

Two types of sensitivity experiments regarding to the shape of prescribed time evolution of ice-thickness are performed: one type with $\tau_H = 10\,\mathrm{kyr}$ (Figs.S55 to S58), and the other with $\tau_H = 3\,\mathrm{kyr}$ (Figs.S59 to S62). (see Eq.61 in the main text about definition of τ_H).

The series of experiments obtained using constant $H = 3000\,\mathrm{m}$ and $M_\mathrm{b} = 0\,\mathrm{mm\,yr^{-1}}$ are repeated by higher resolution configurations. Figures.S63 to S70 are the results of $P_\mathsf{T} = 100\,\mathrm{kyr}$; Figures.S71 to S94 are results obtained using a uniform discretization of 513 levels. Figures.S95 to S126 are the same results but using a smooth non-uniform discretization of 513 levels. Figures.S127 to S158 are the same results but using a non-smooth non-uniform discretization of 477 levels. The snapshots at $t = 2\,\mathrm{Myr}$ are plotted for those experiment with higher resolutions. Designs of these higher resolution discretization are shown in Fig. 16 in the main text.
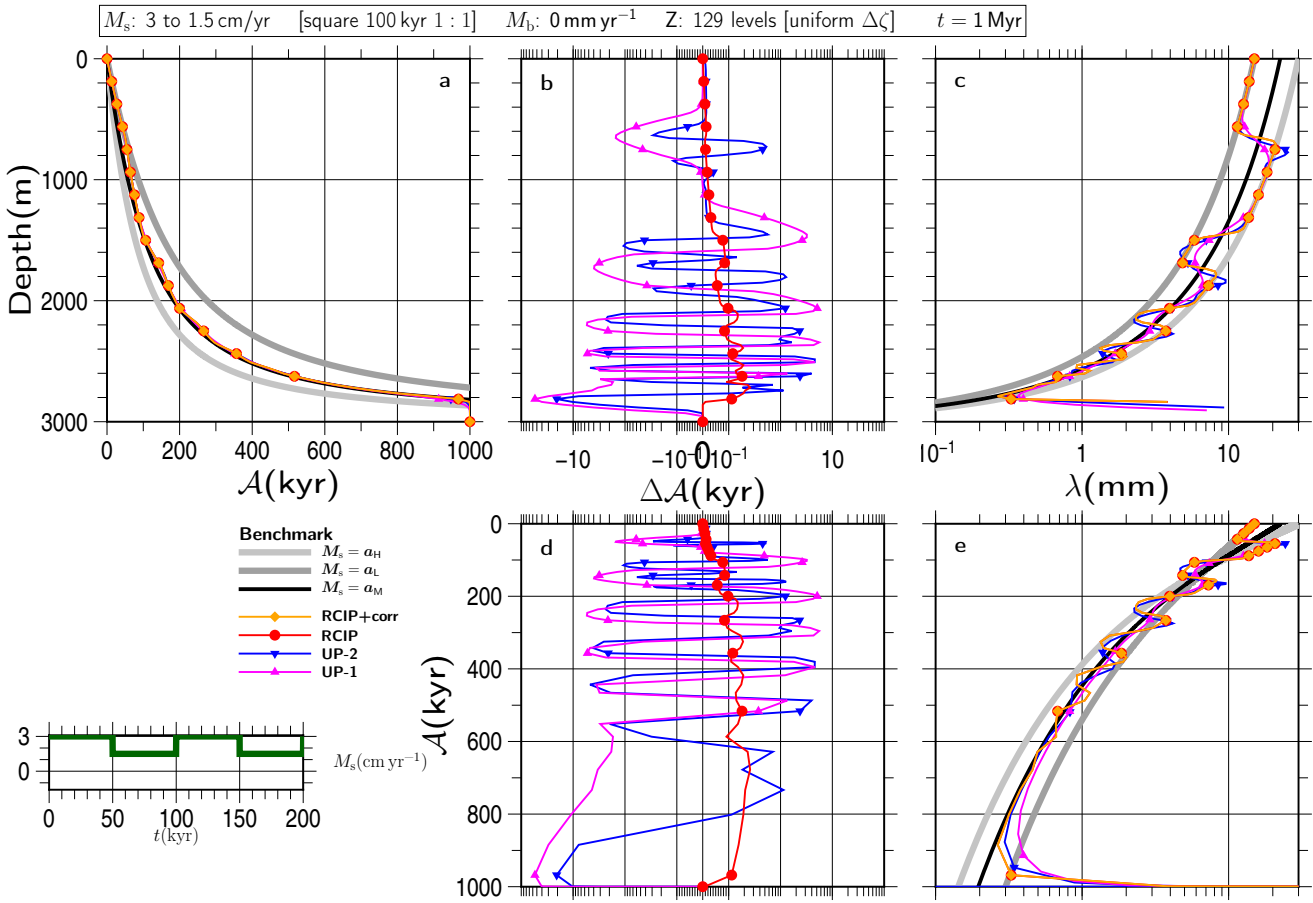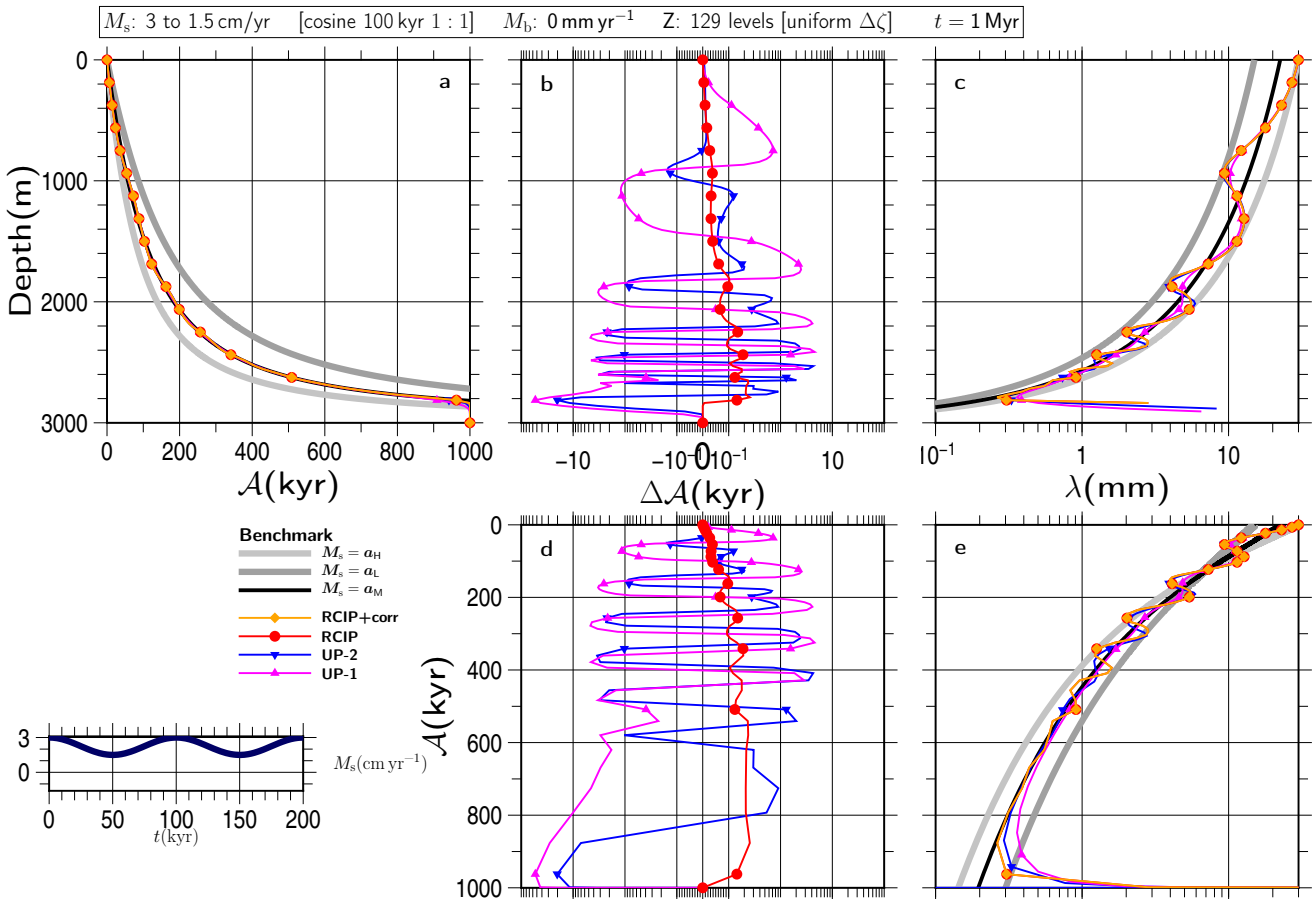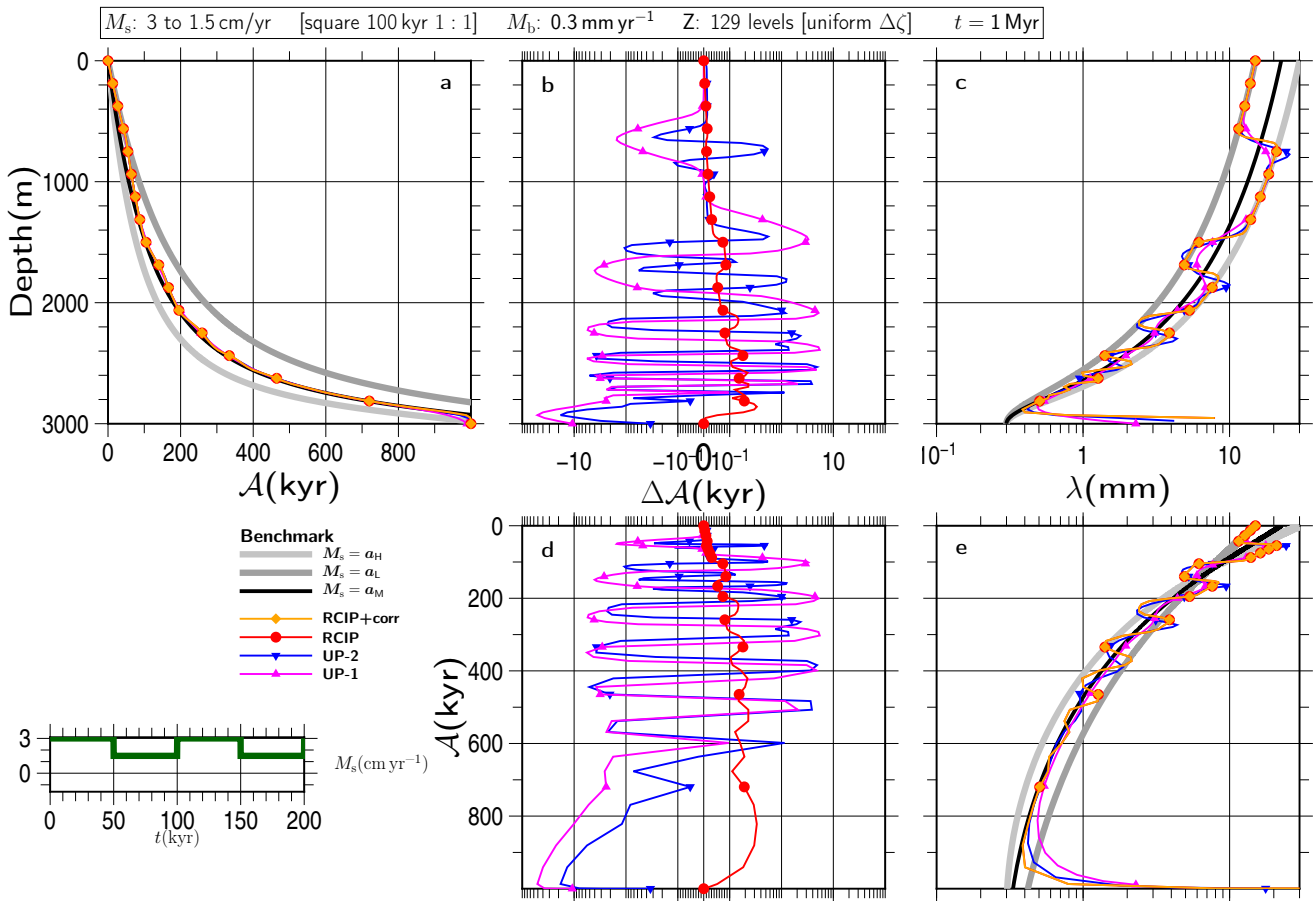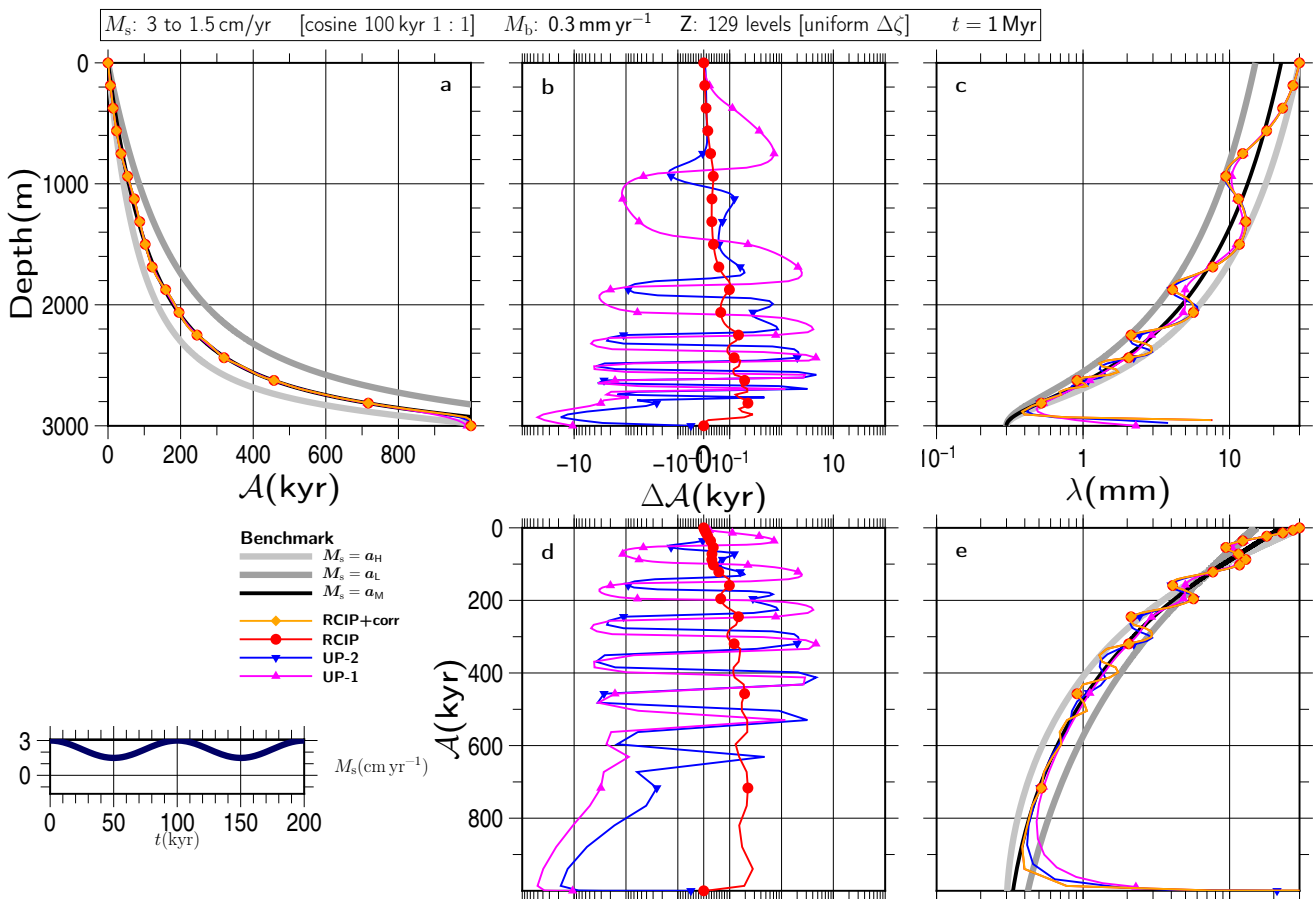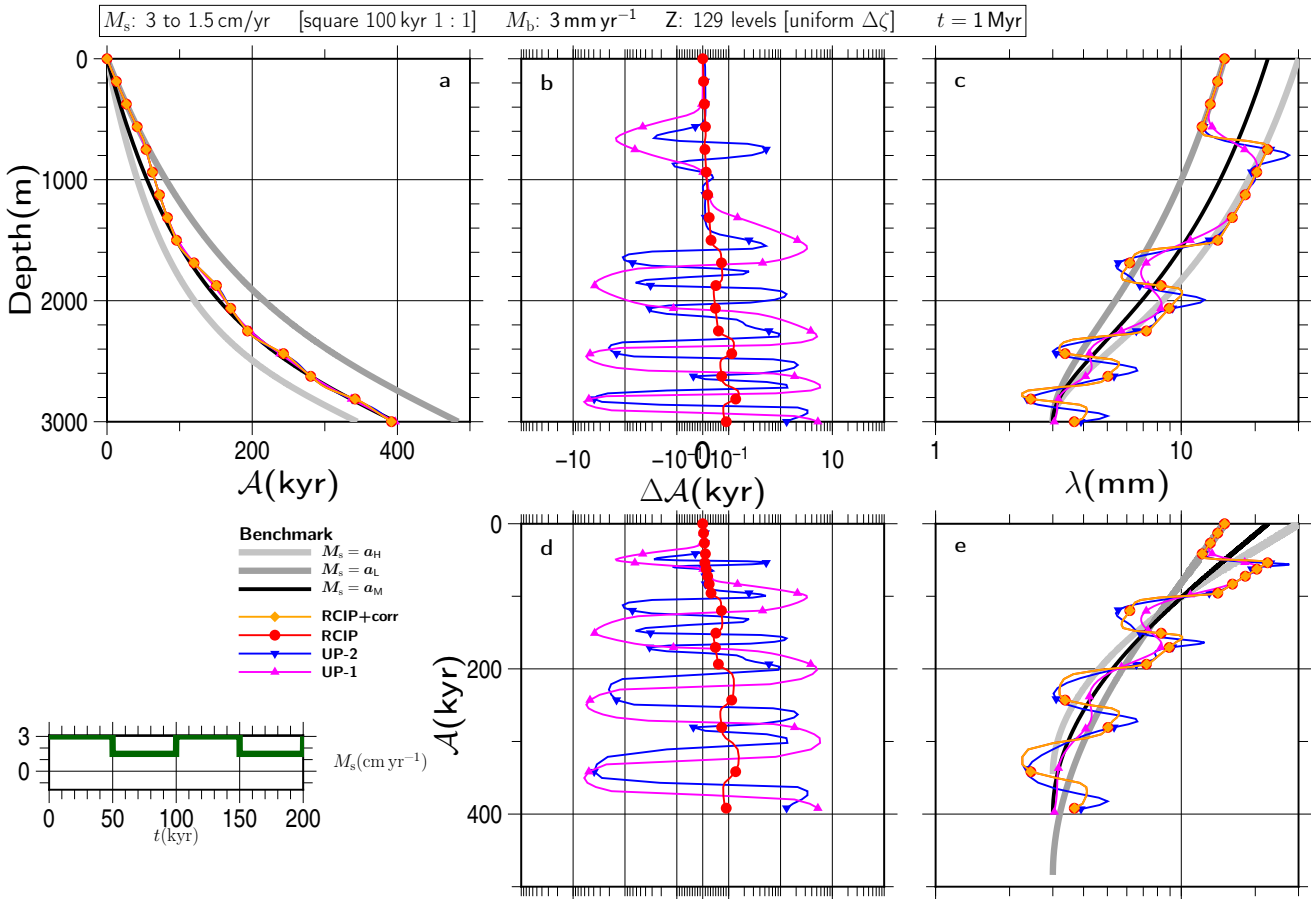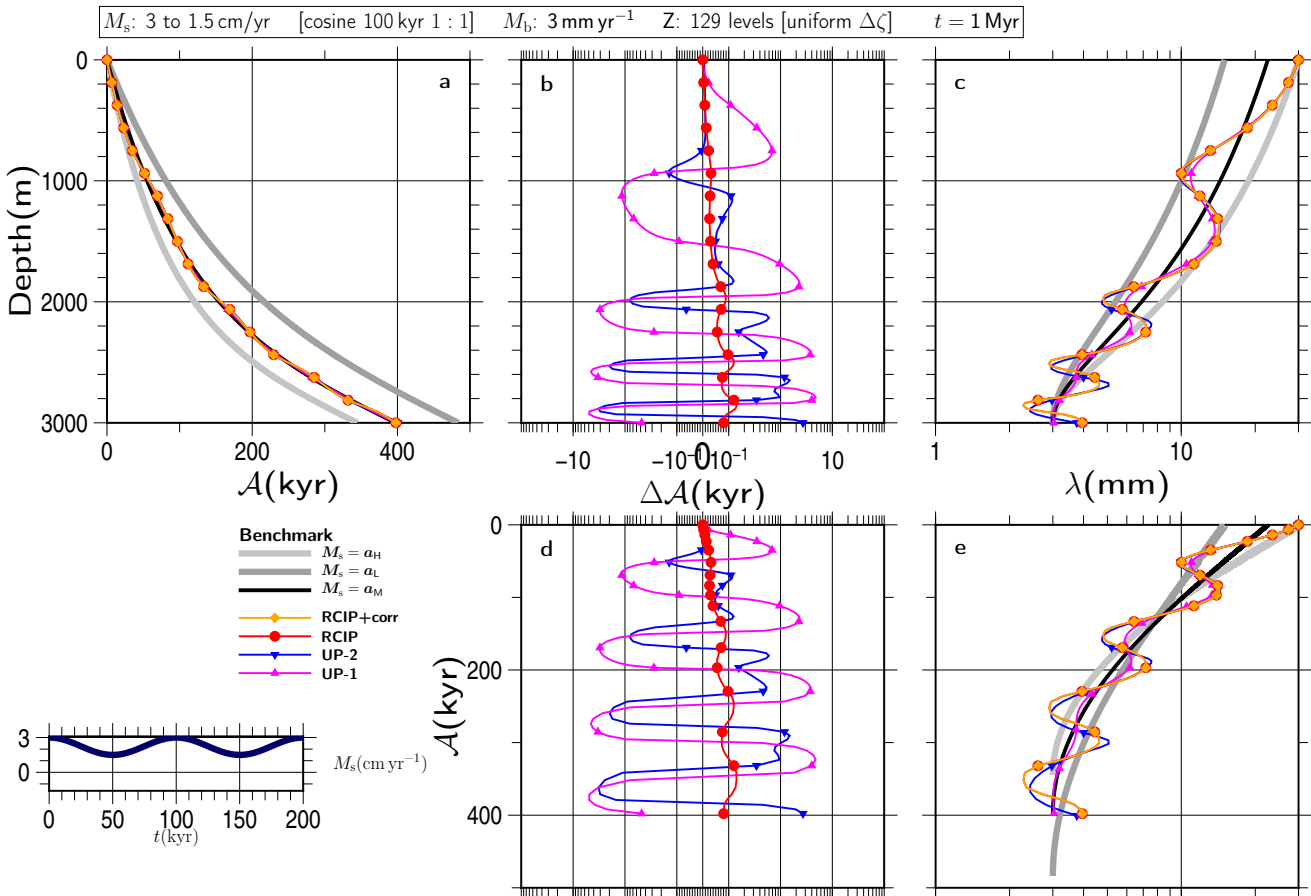
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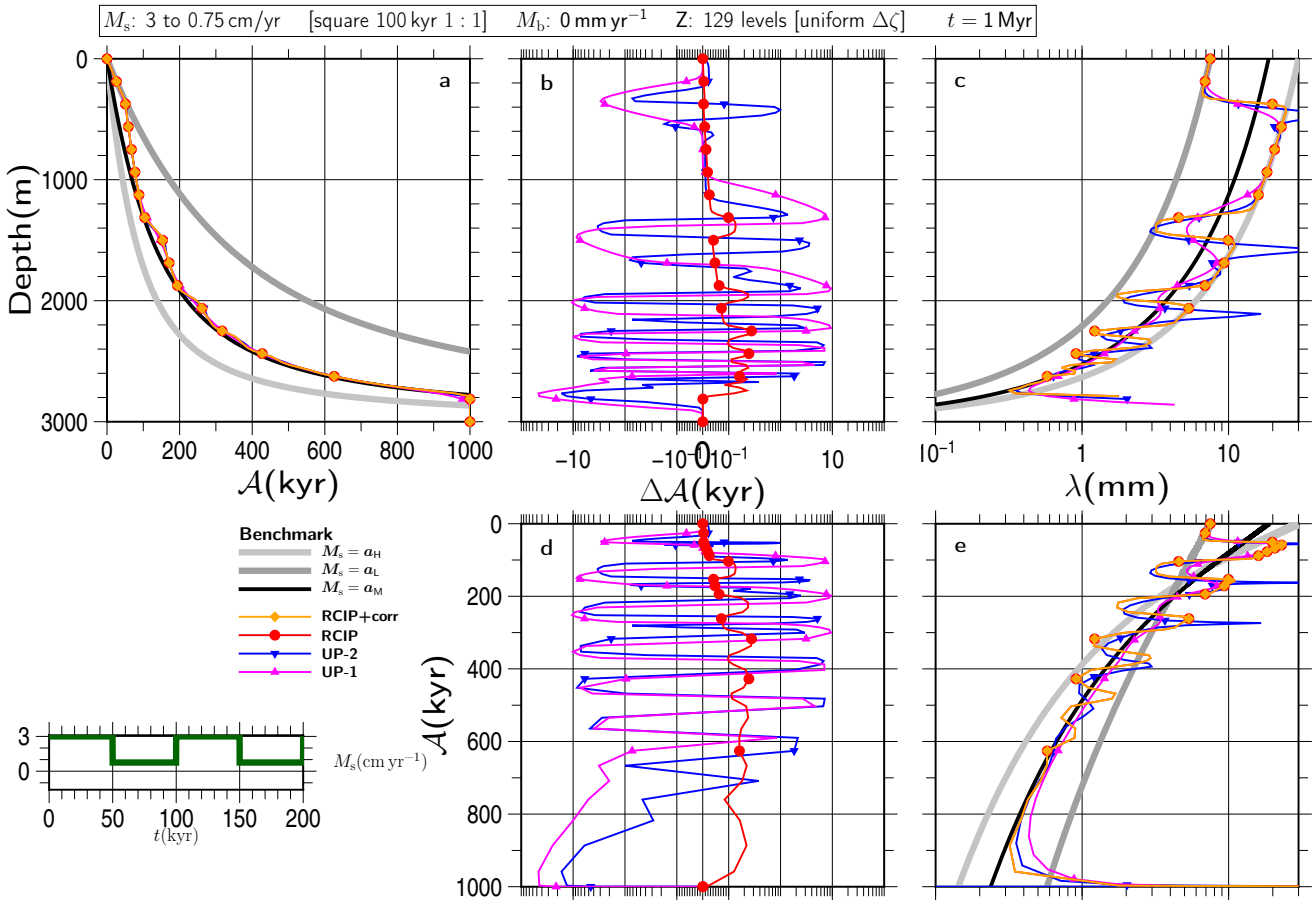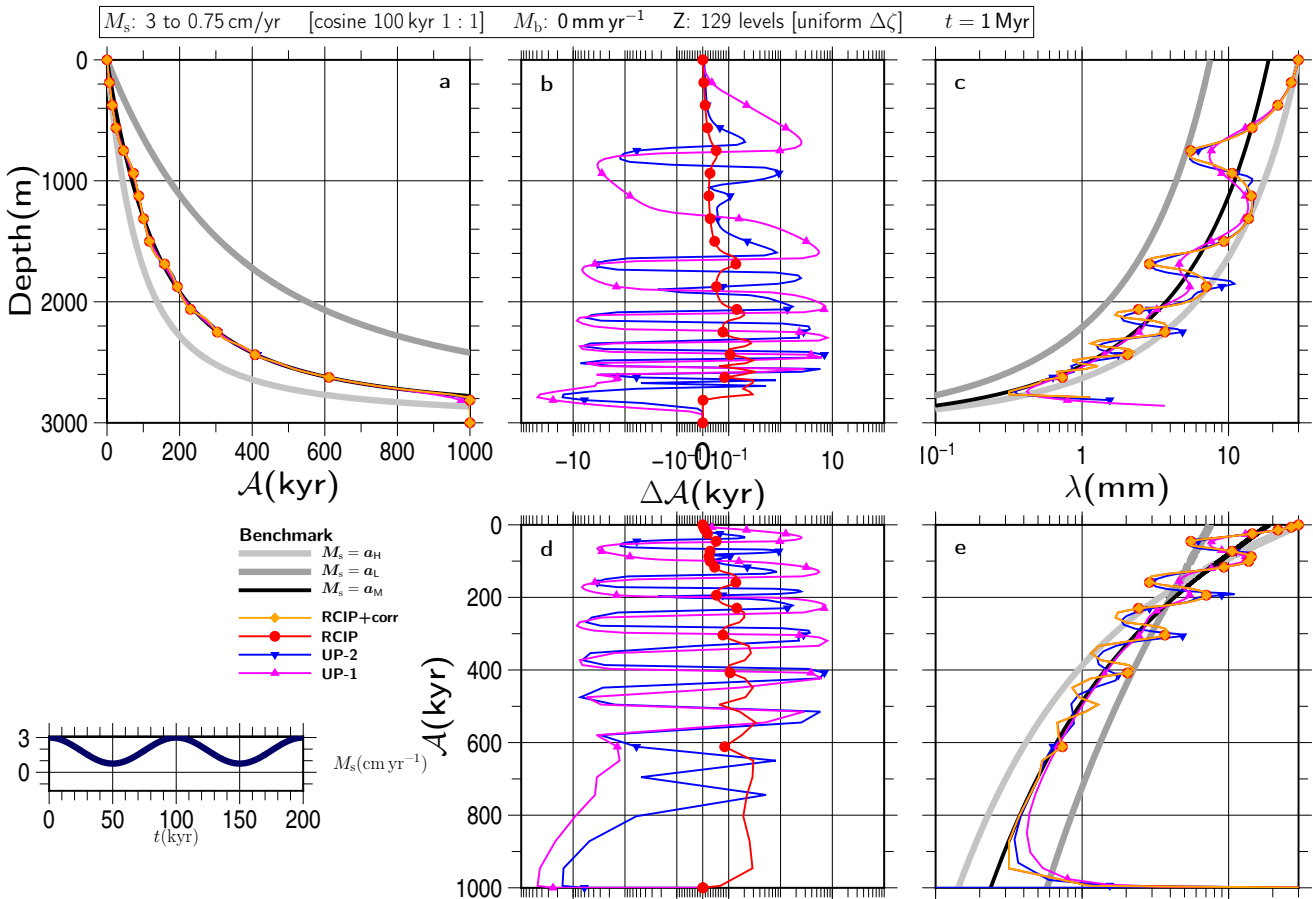Figure S2:

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Figure S7:

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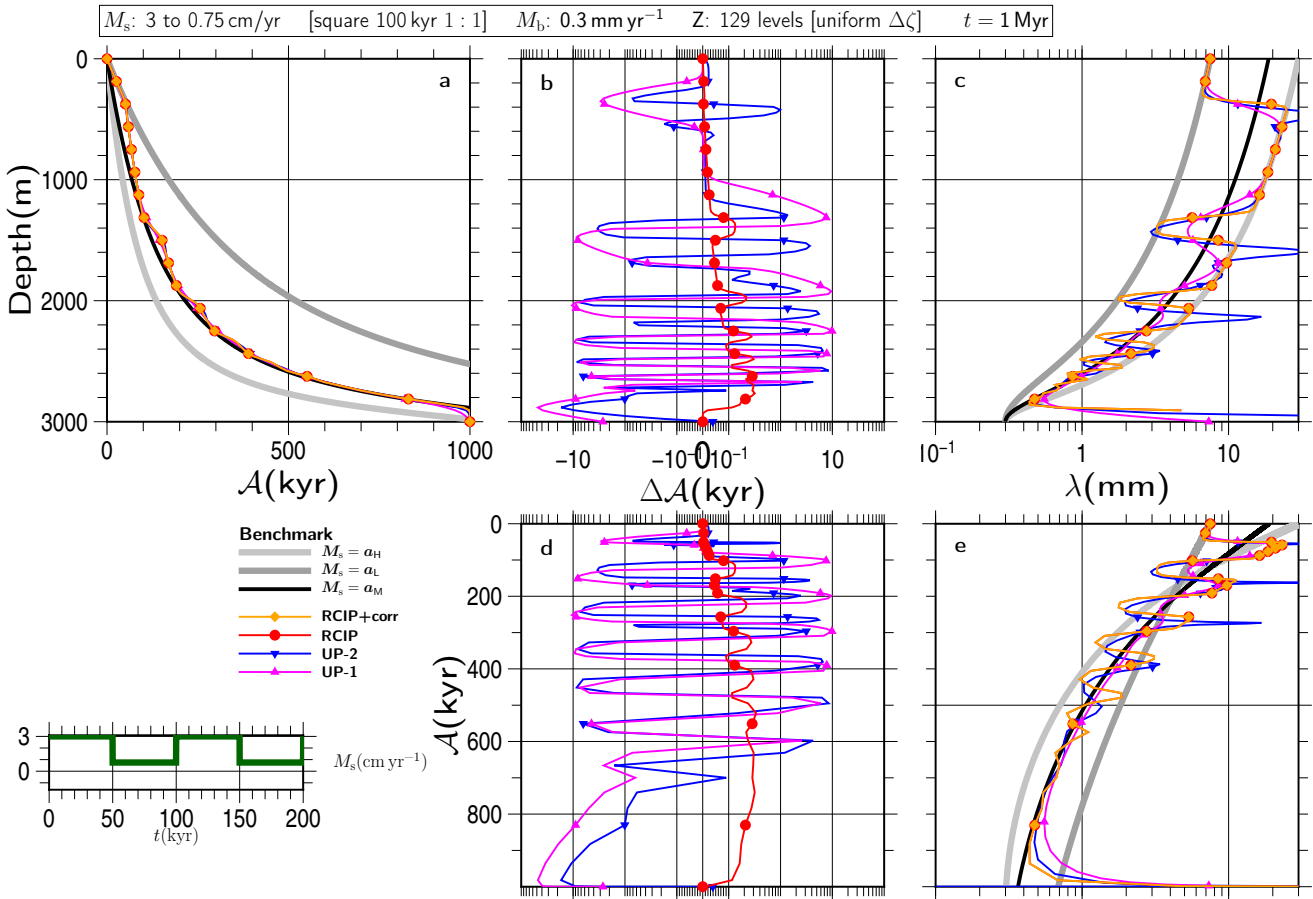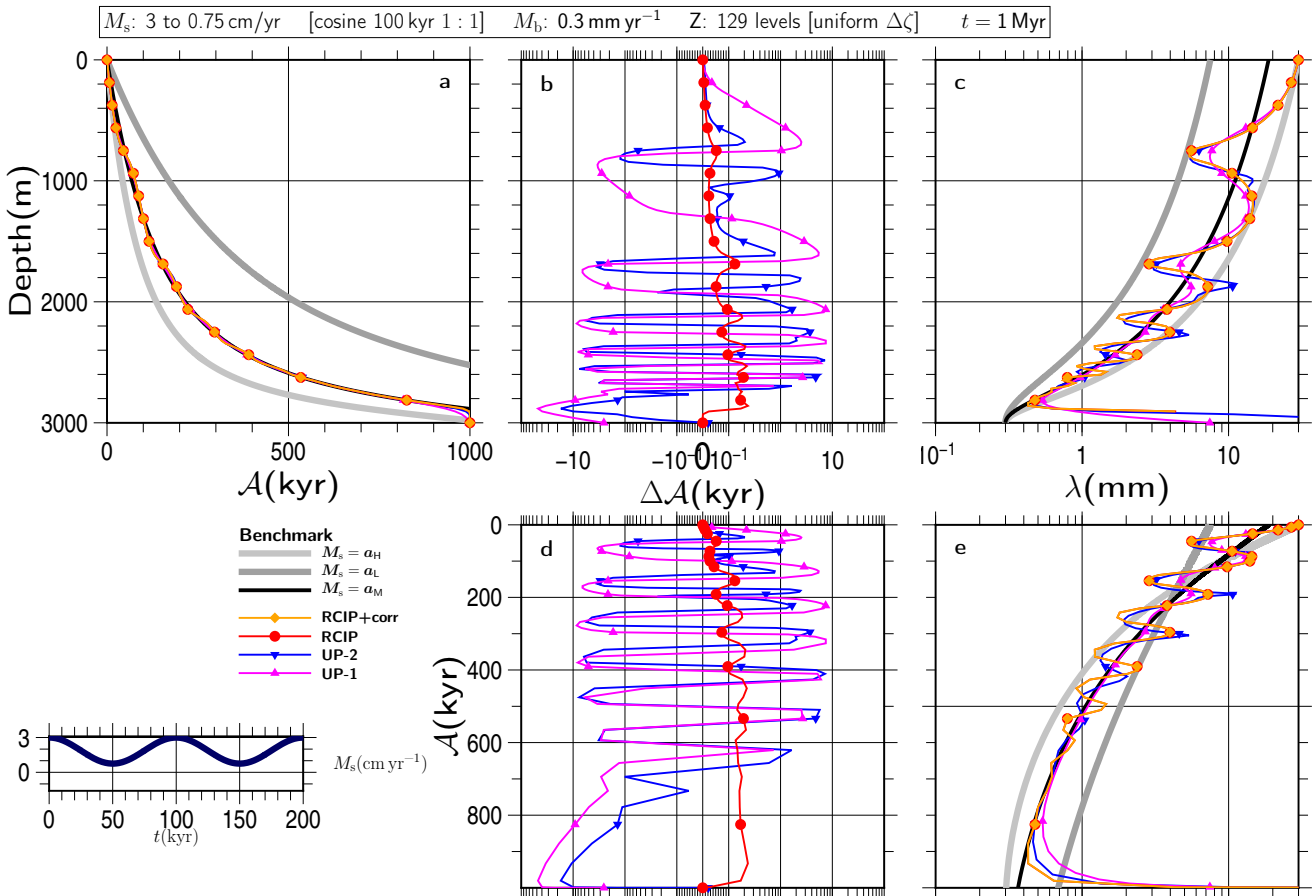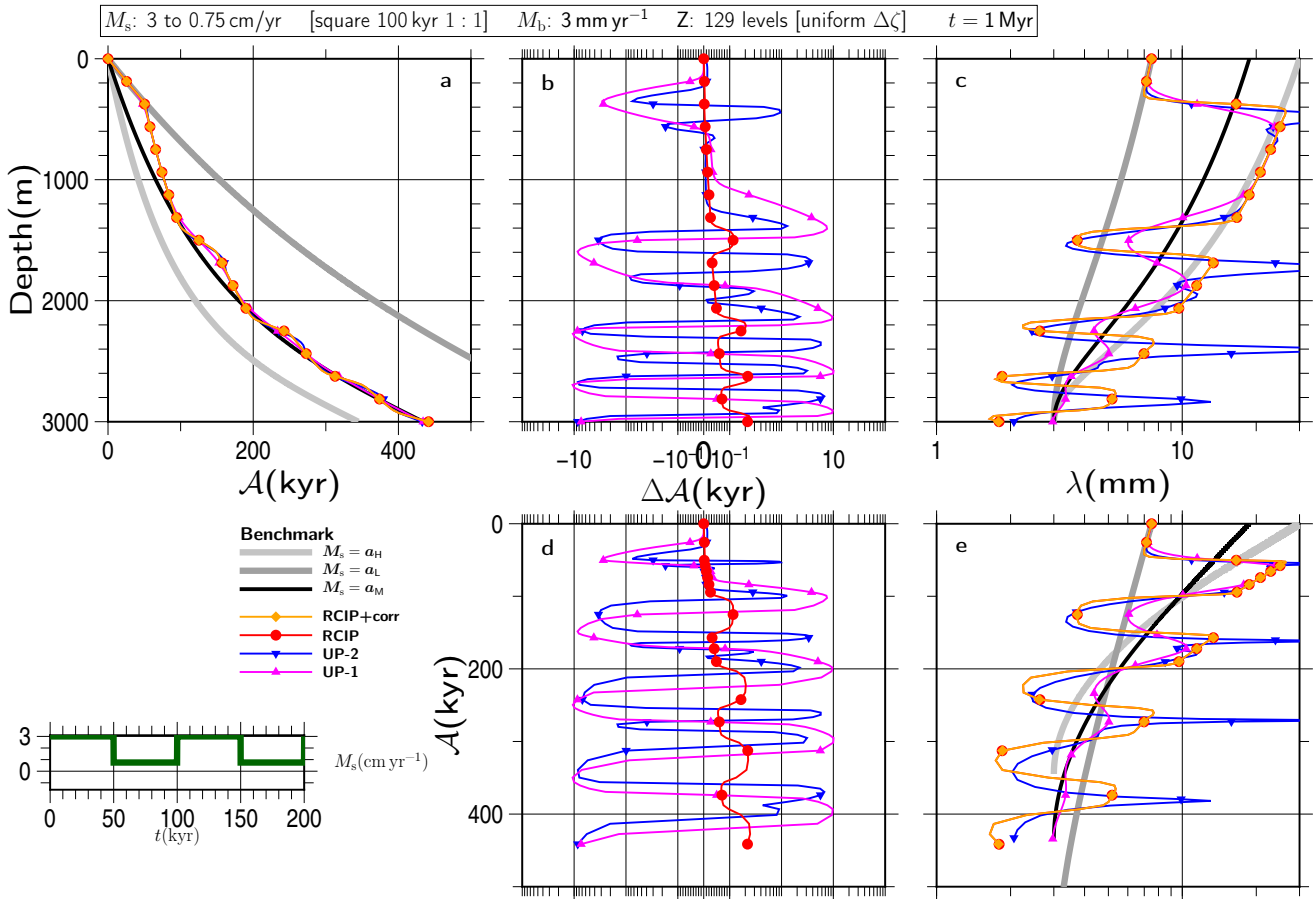
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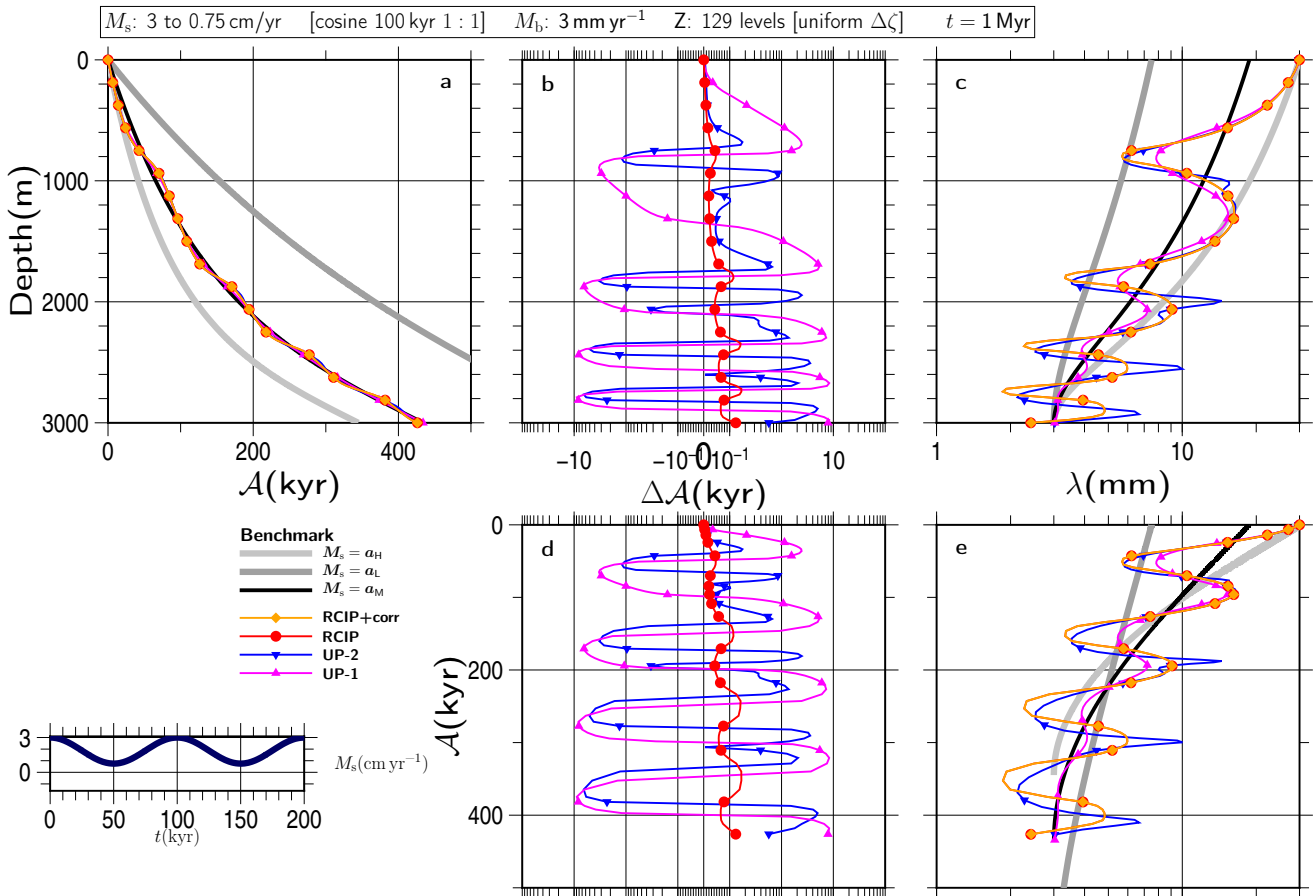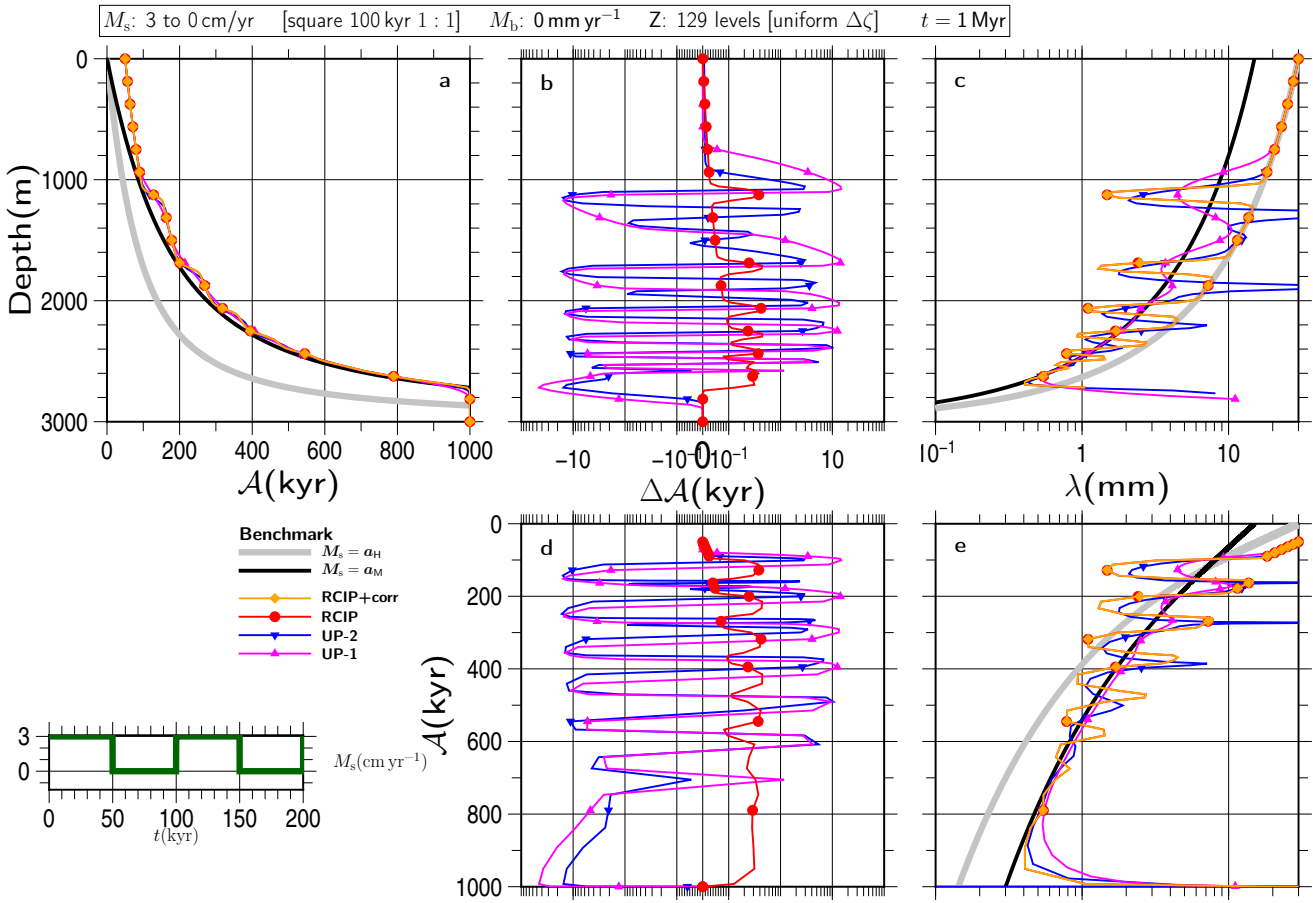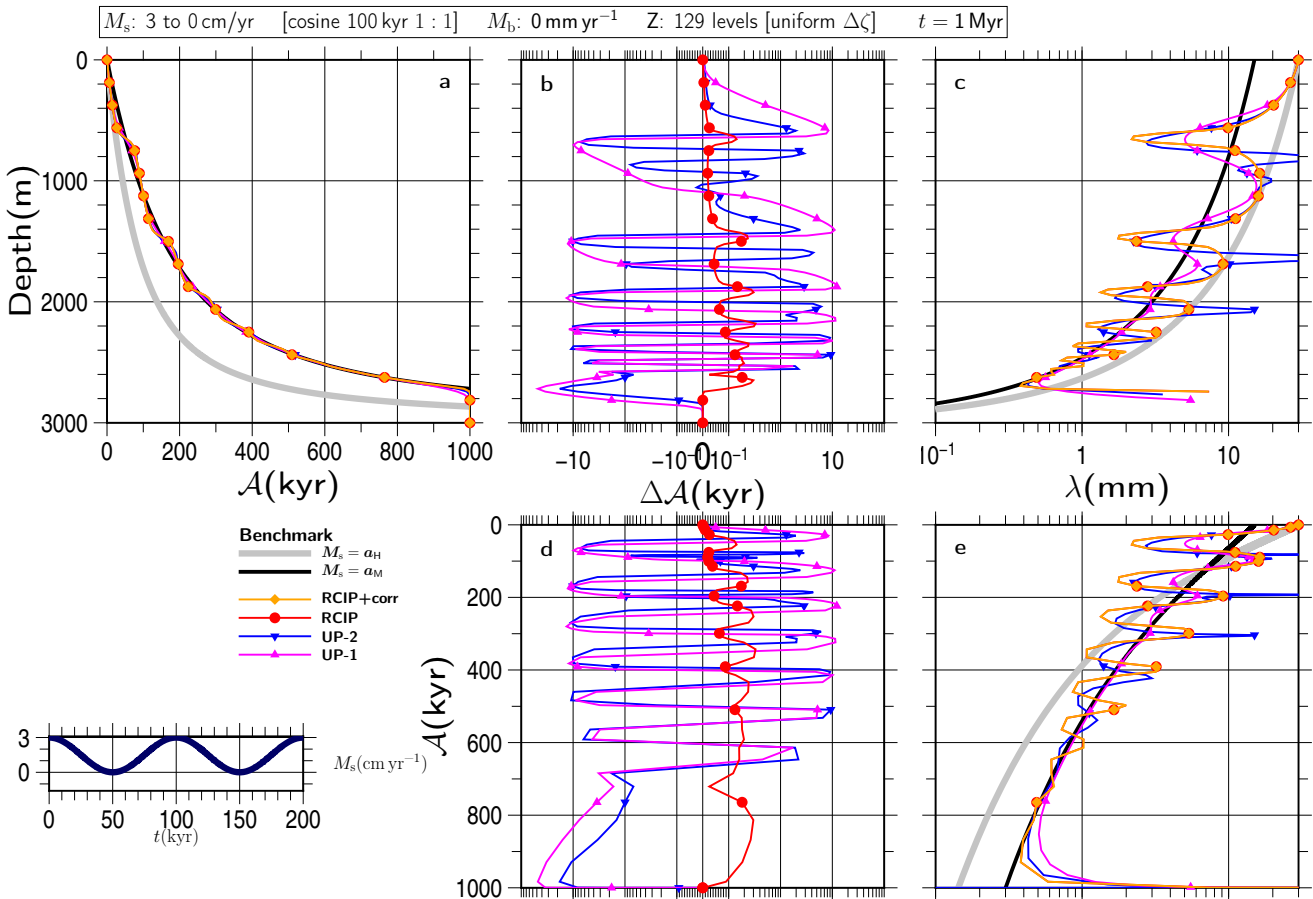Figure S12:

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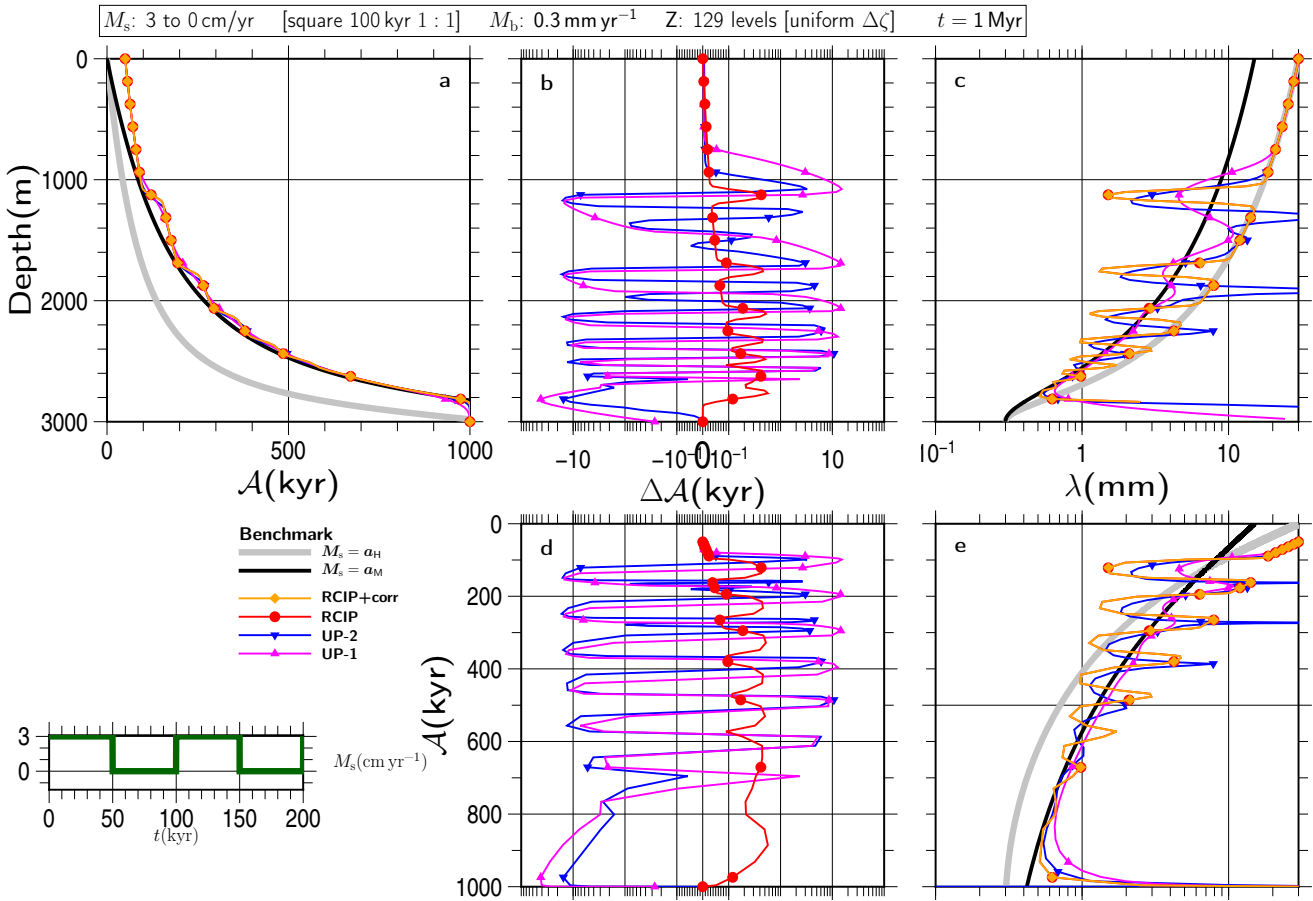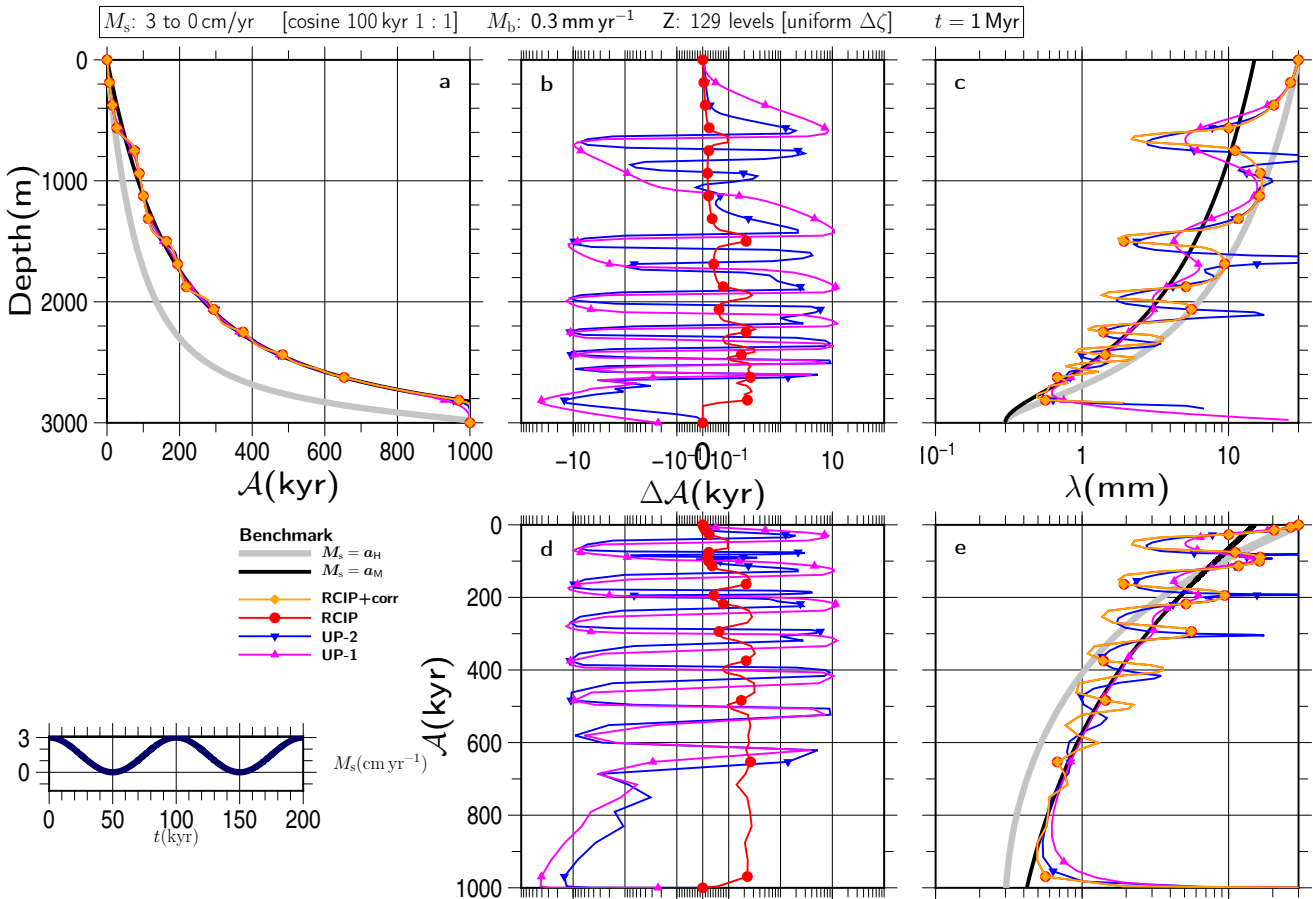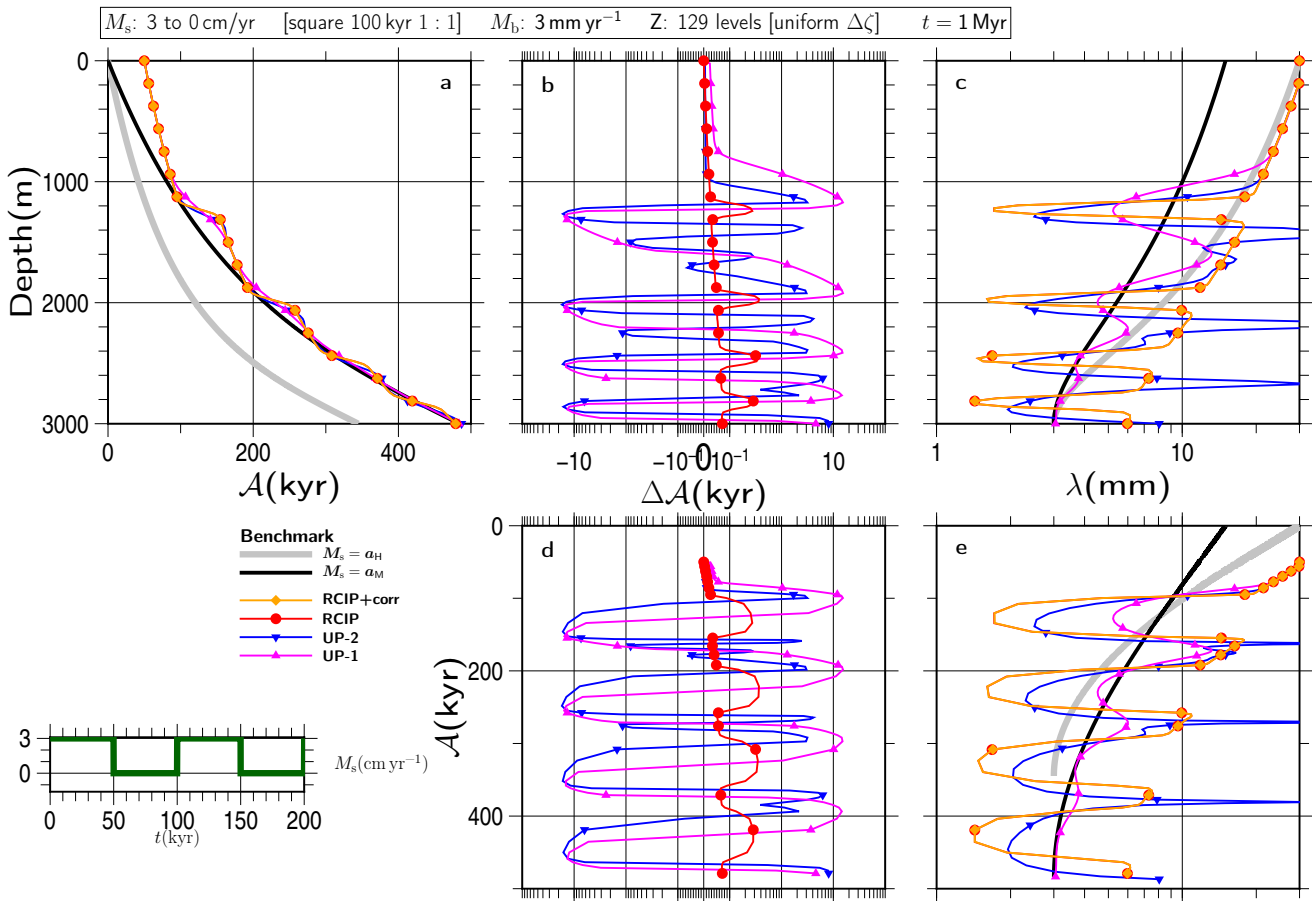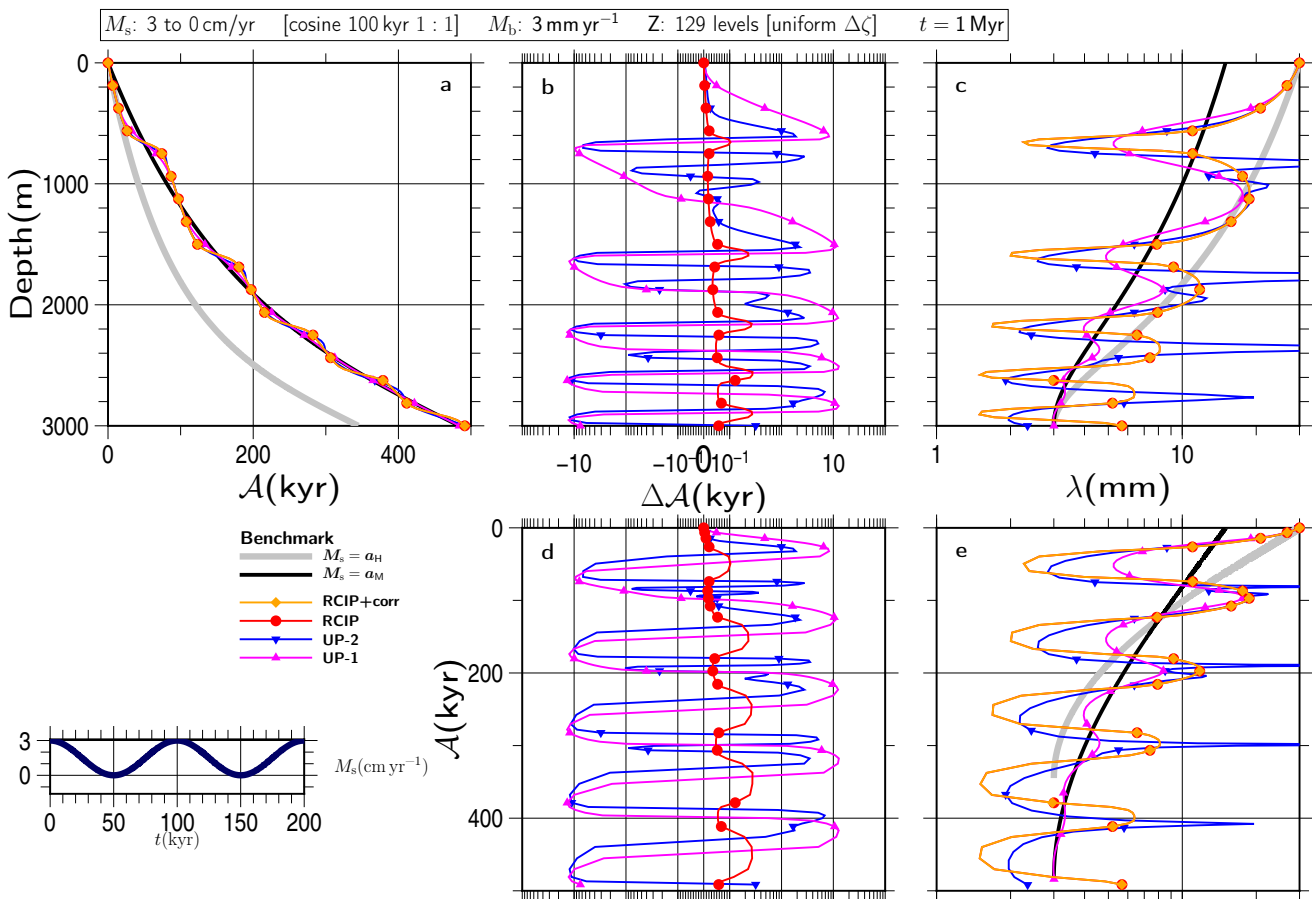
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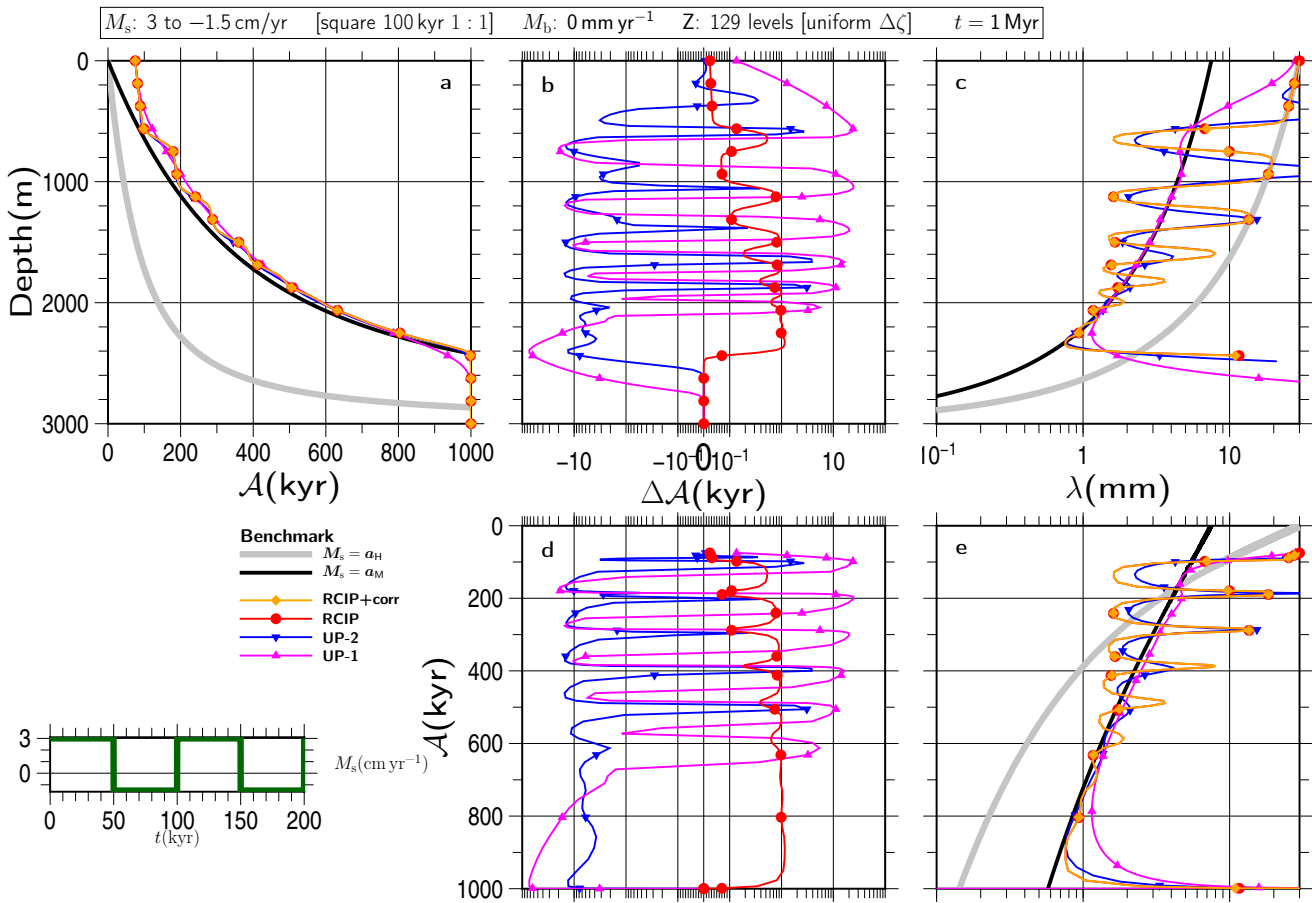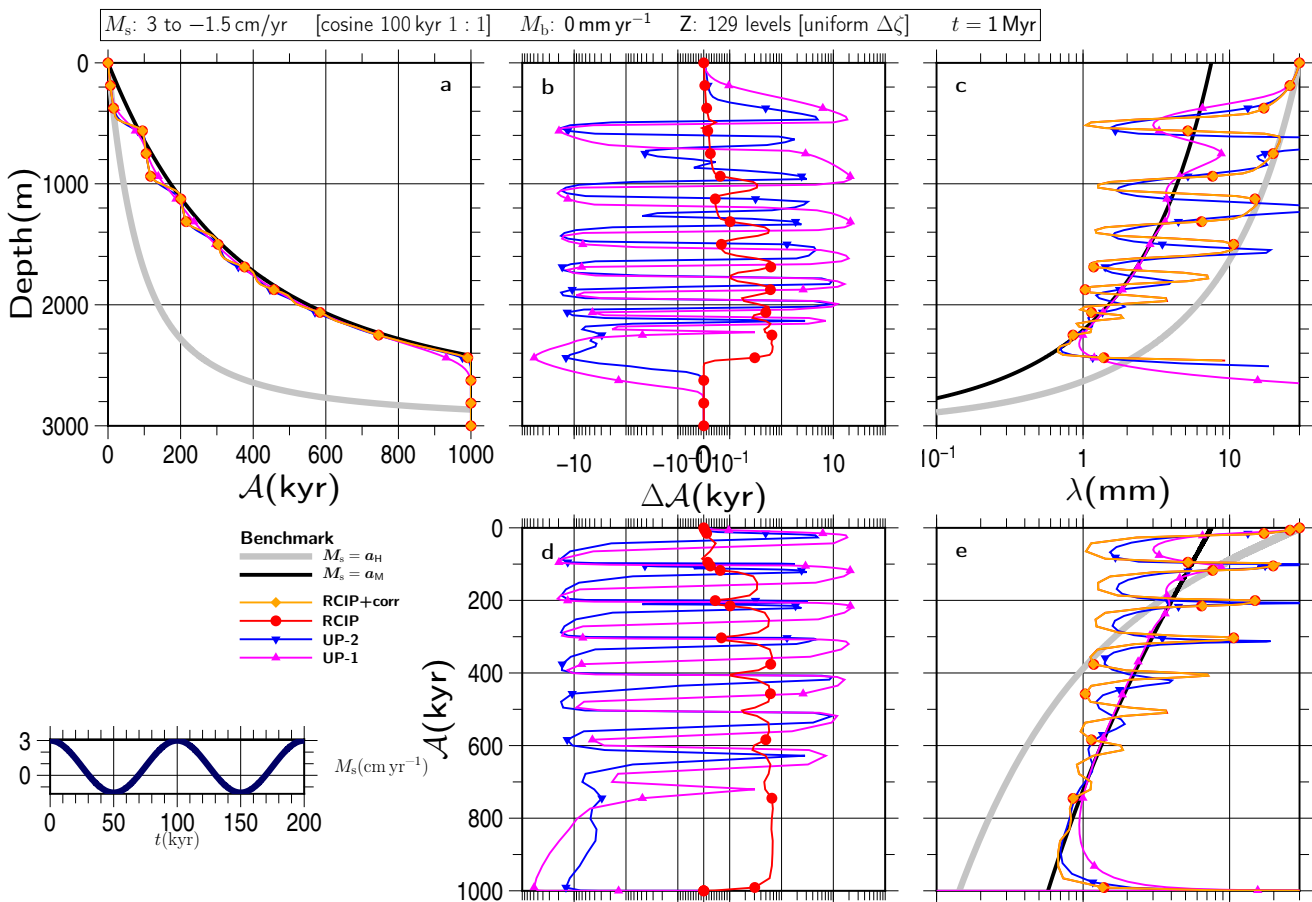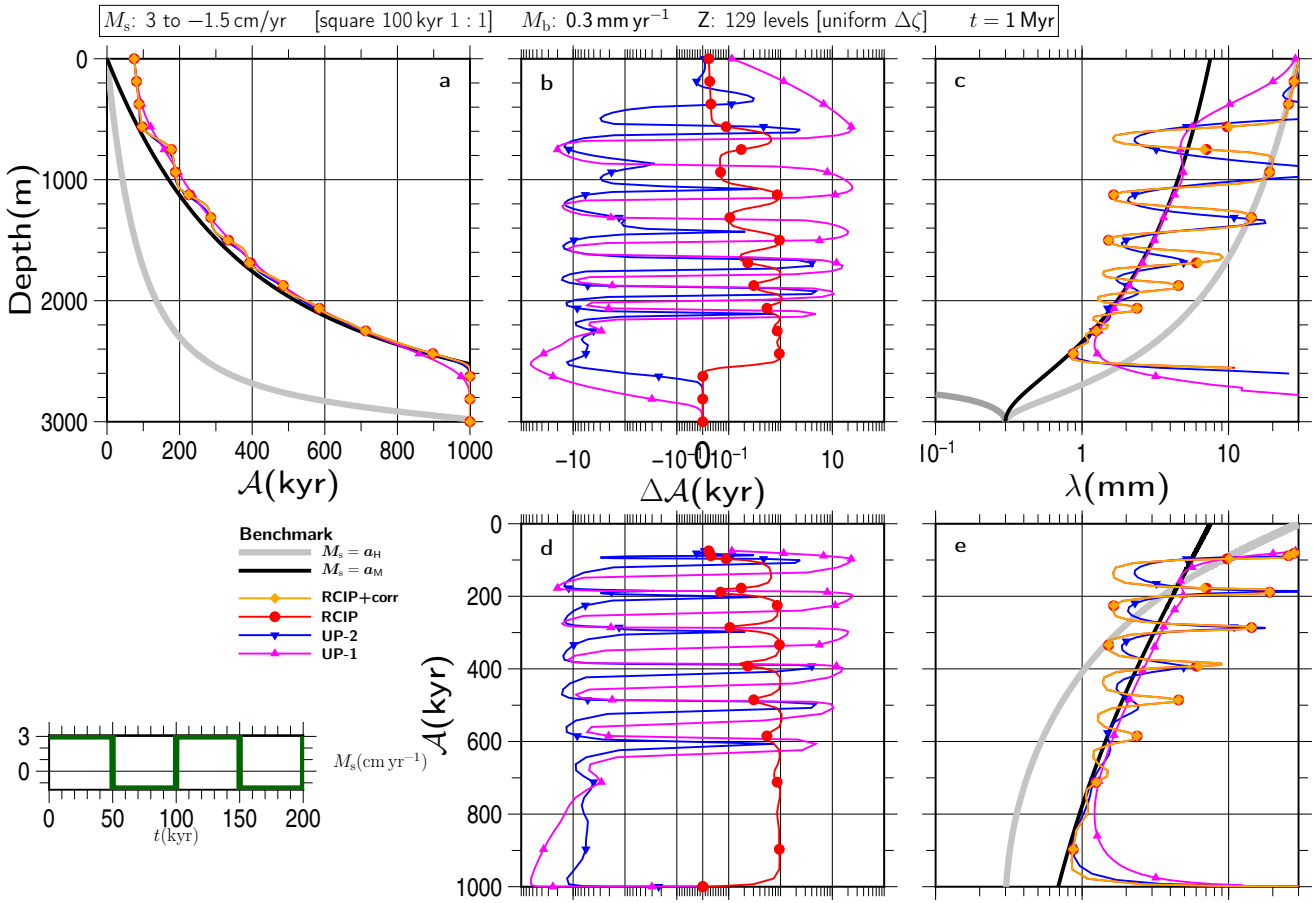
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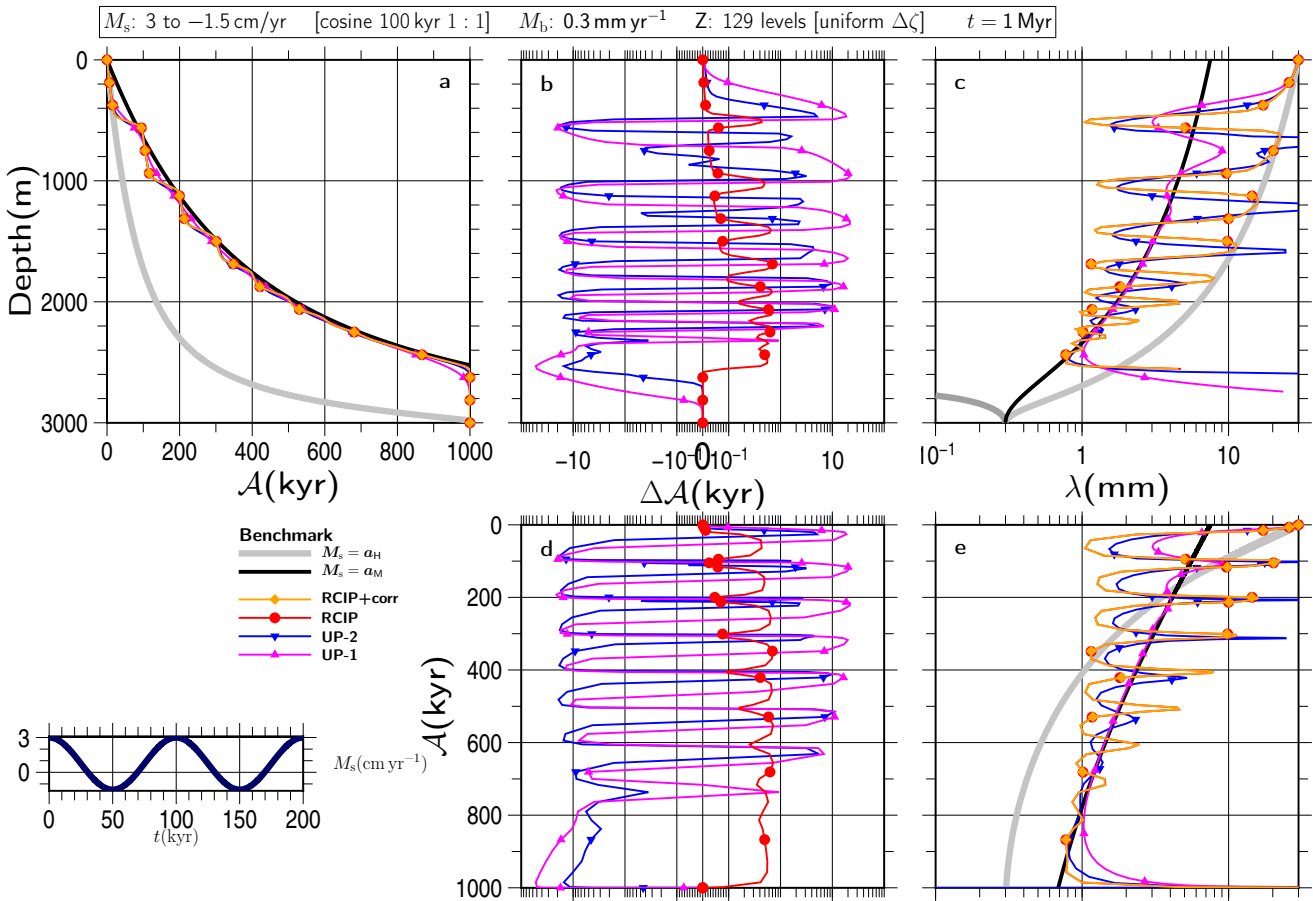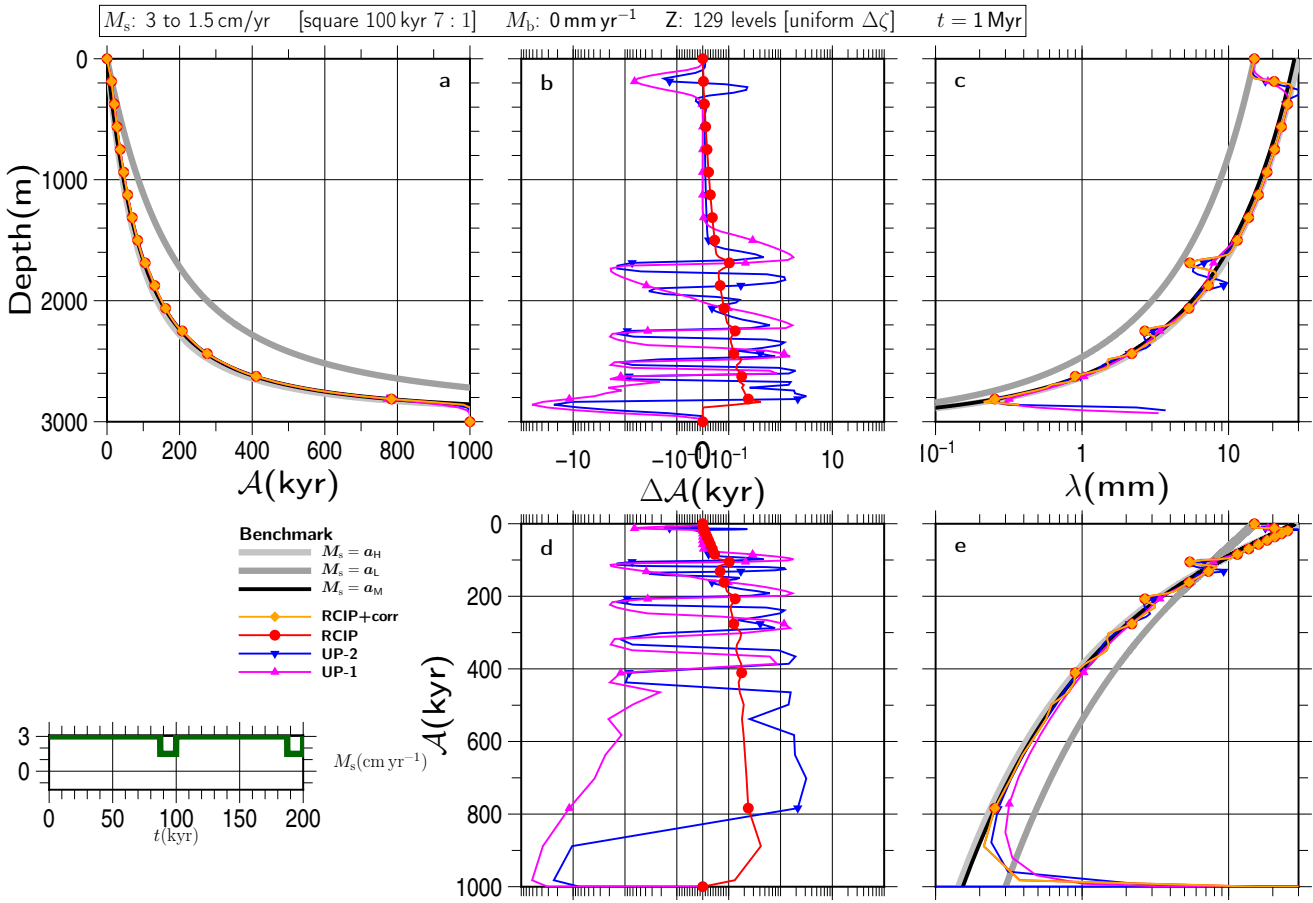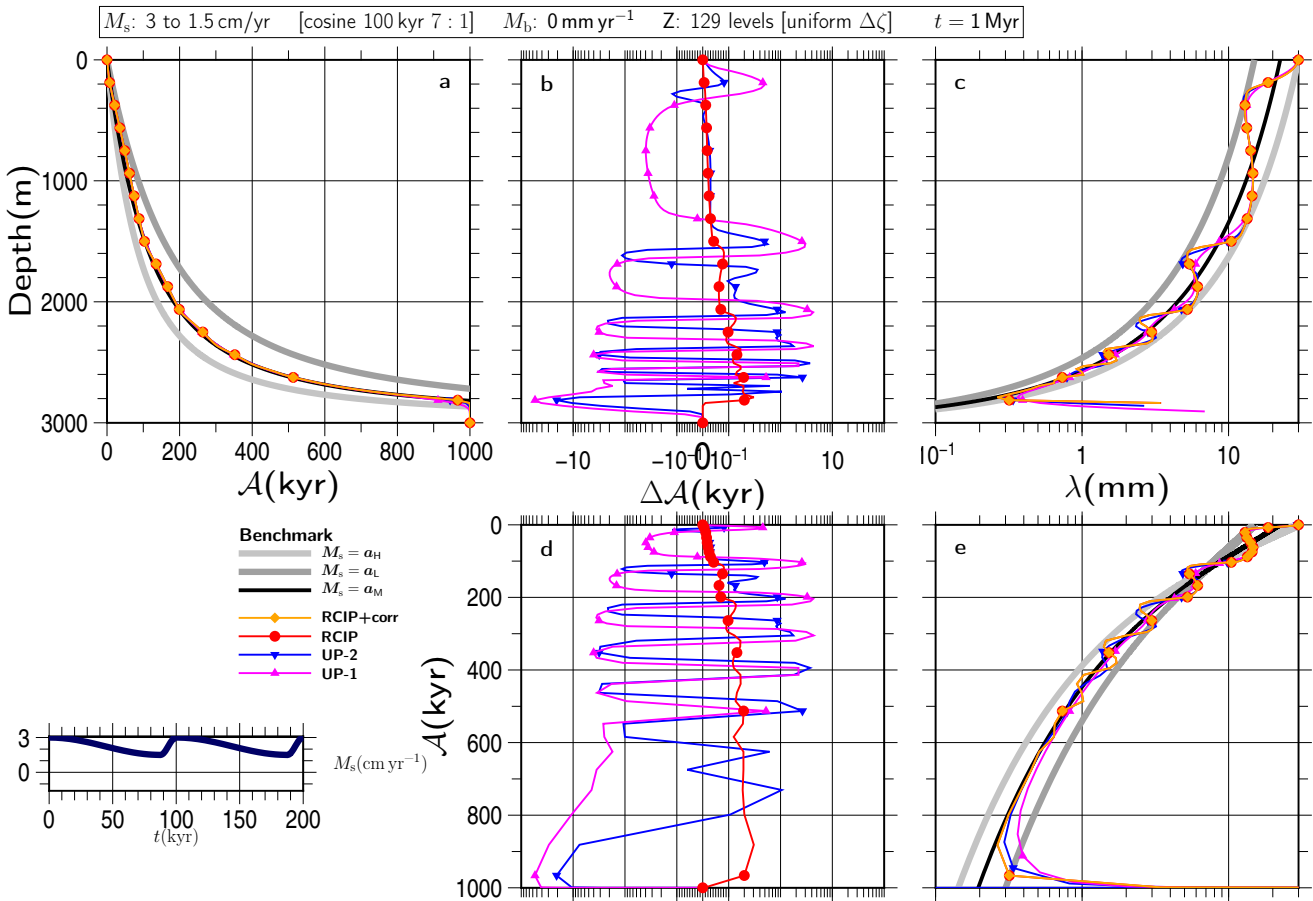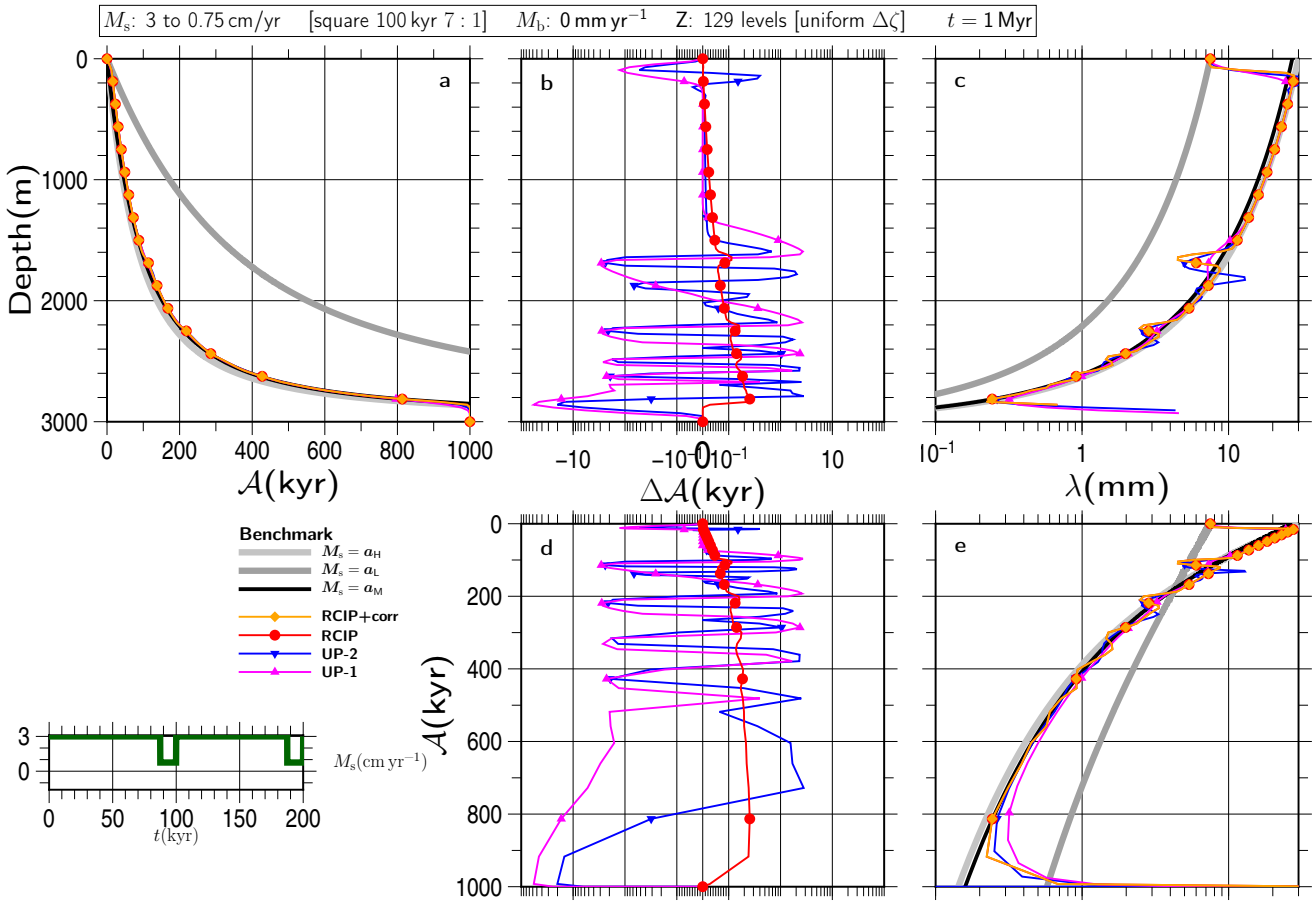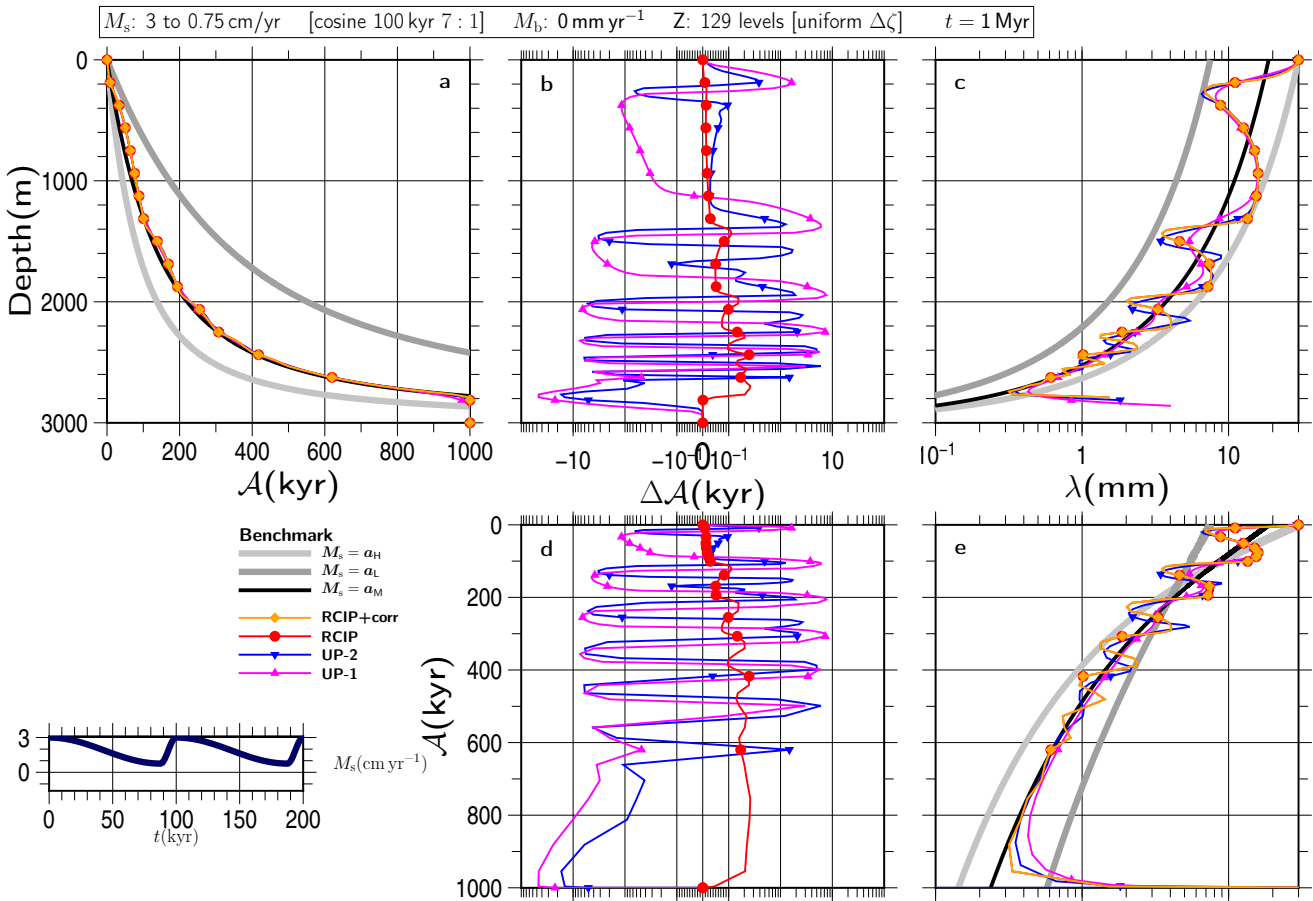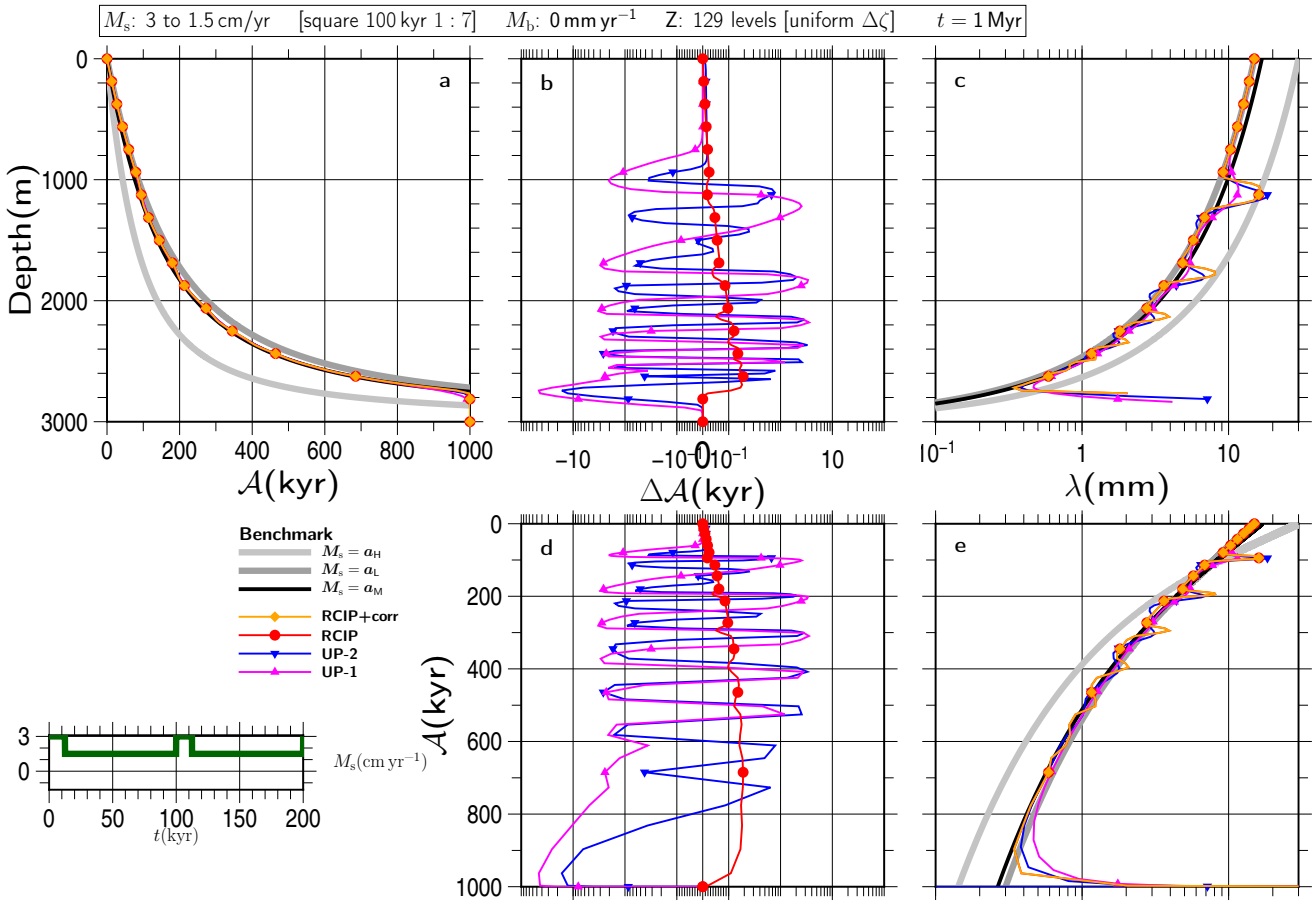

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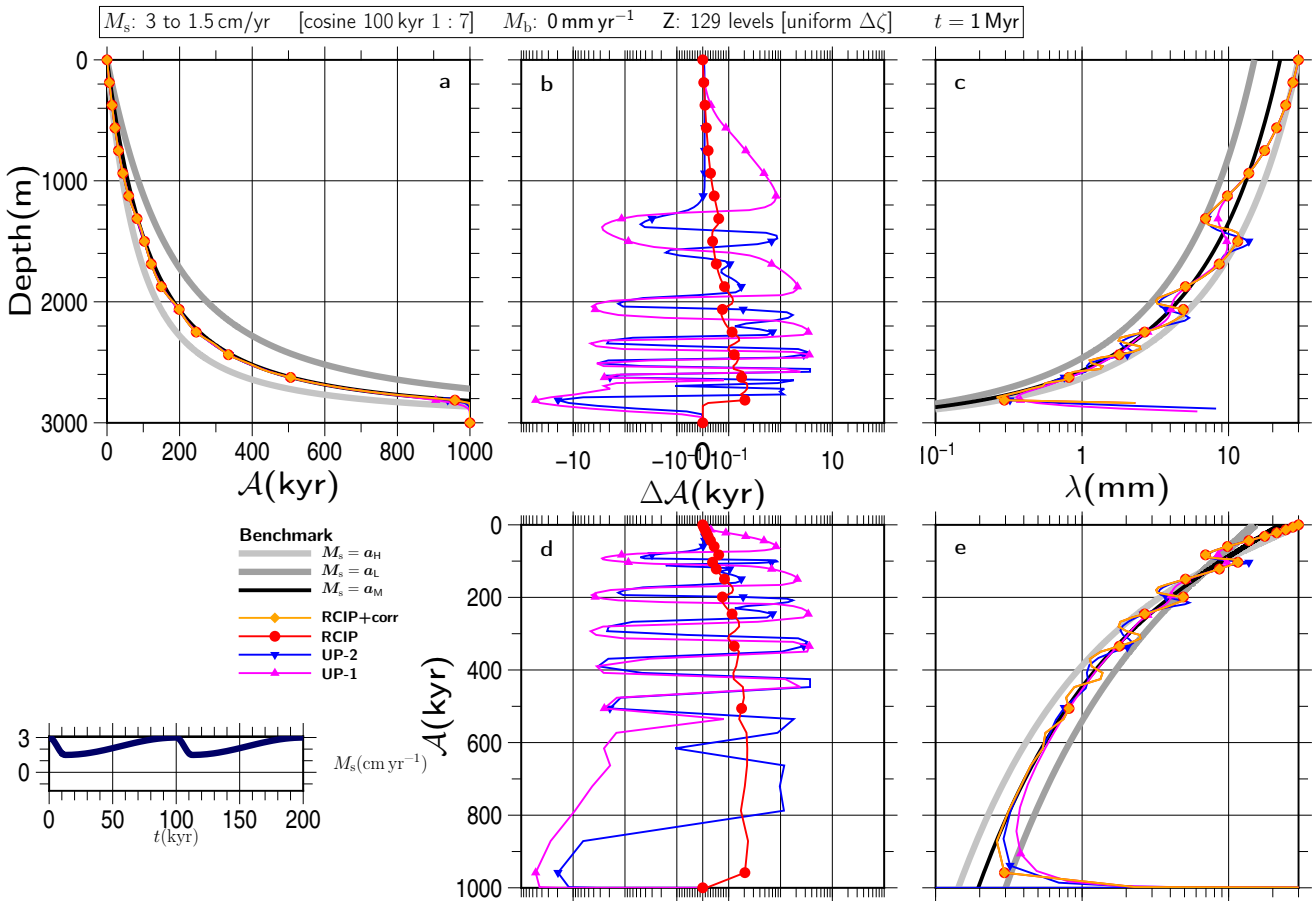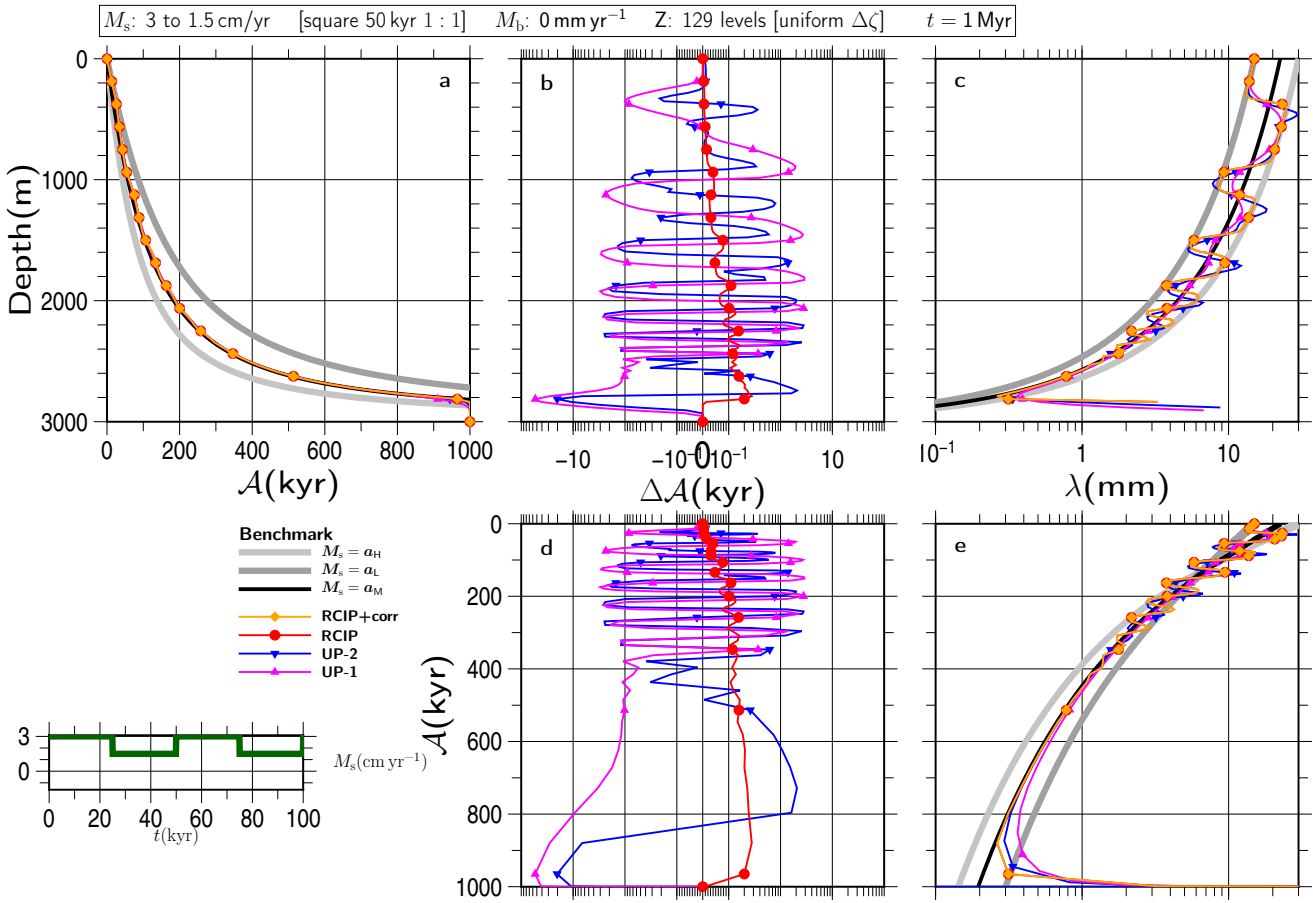Figure S23:

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Figure S25:

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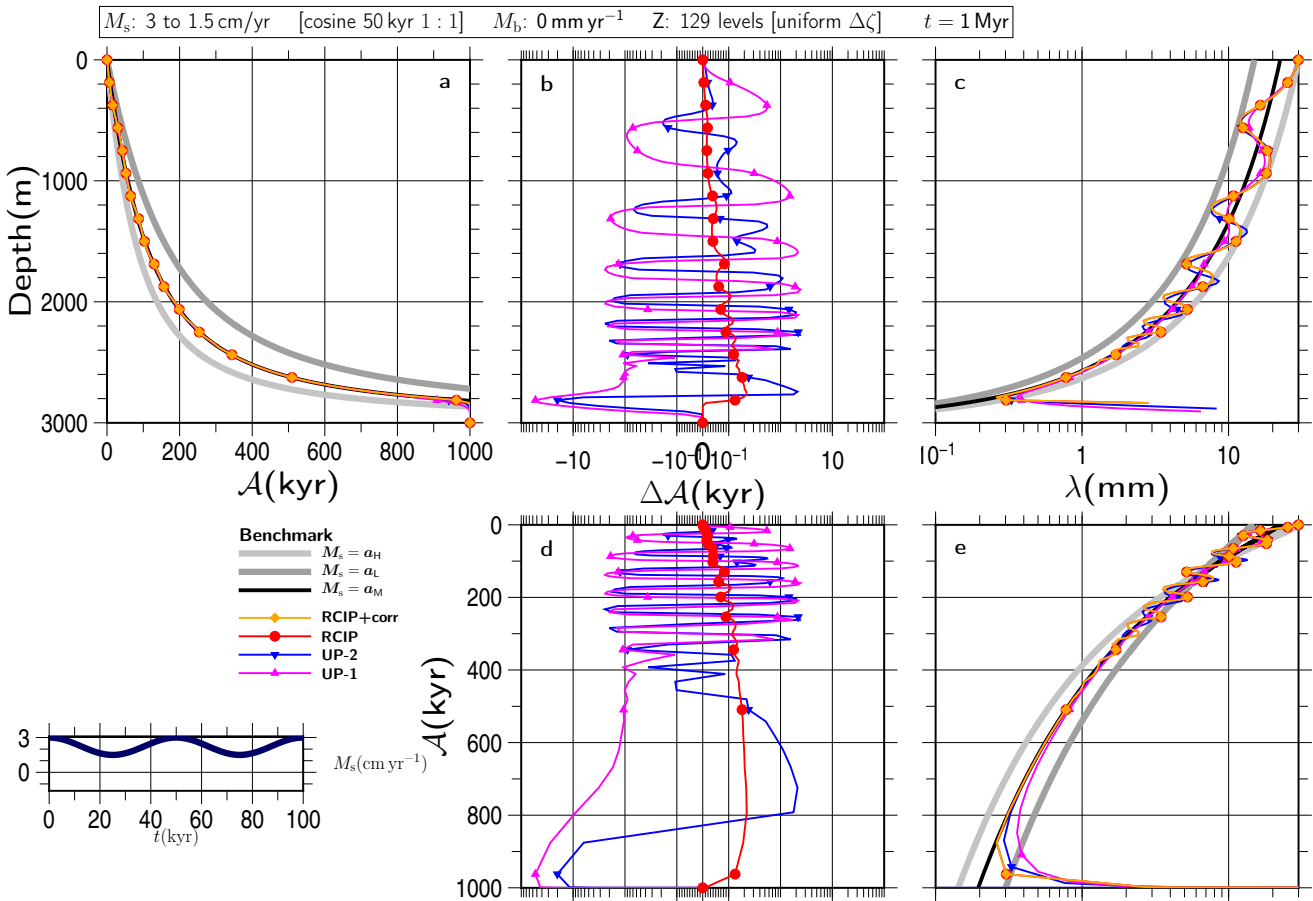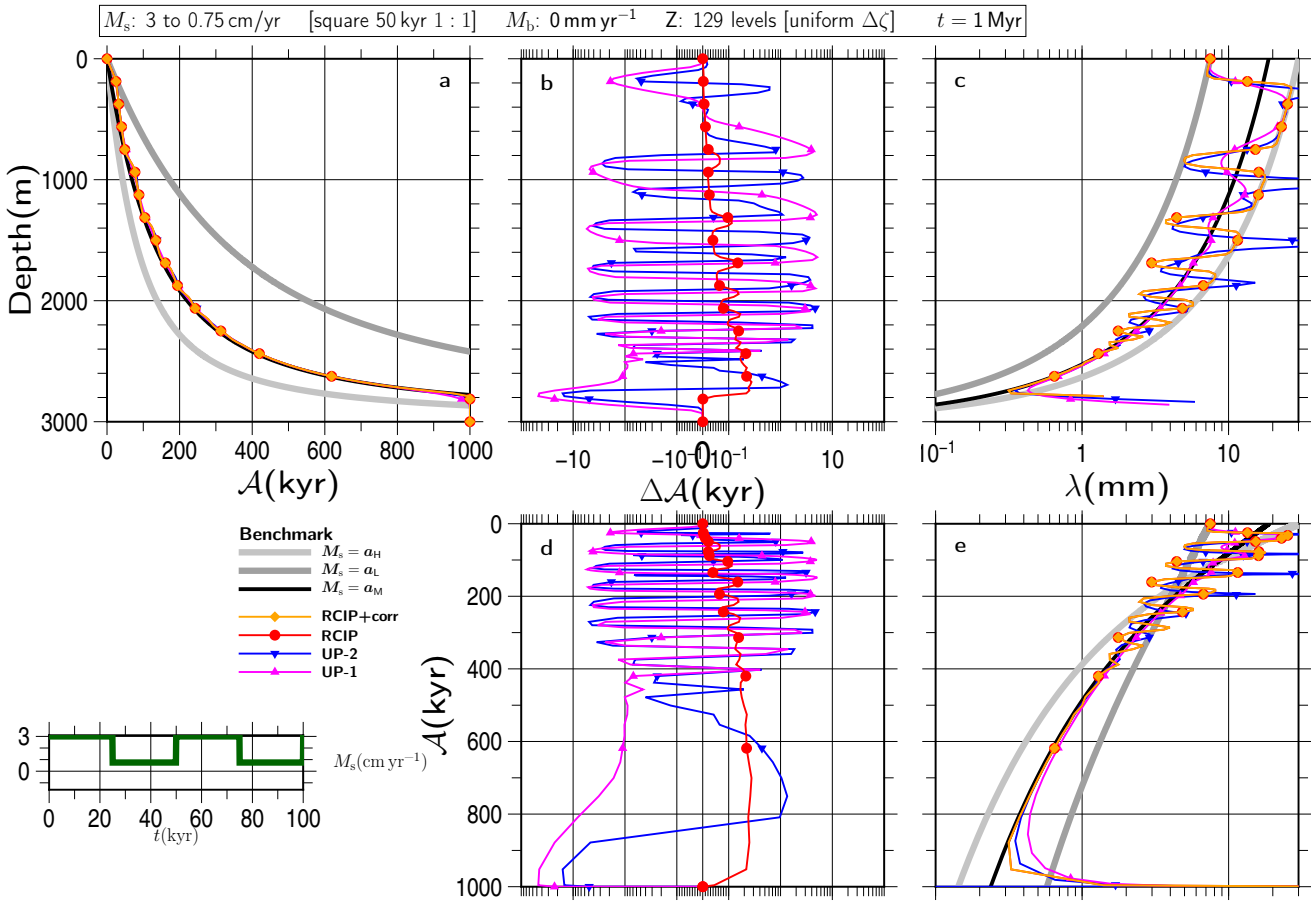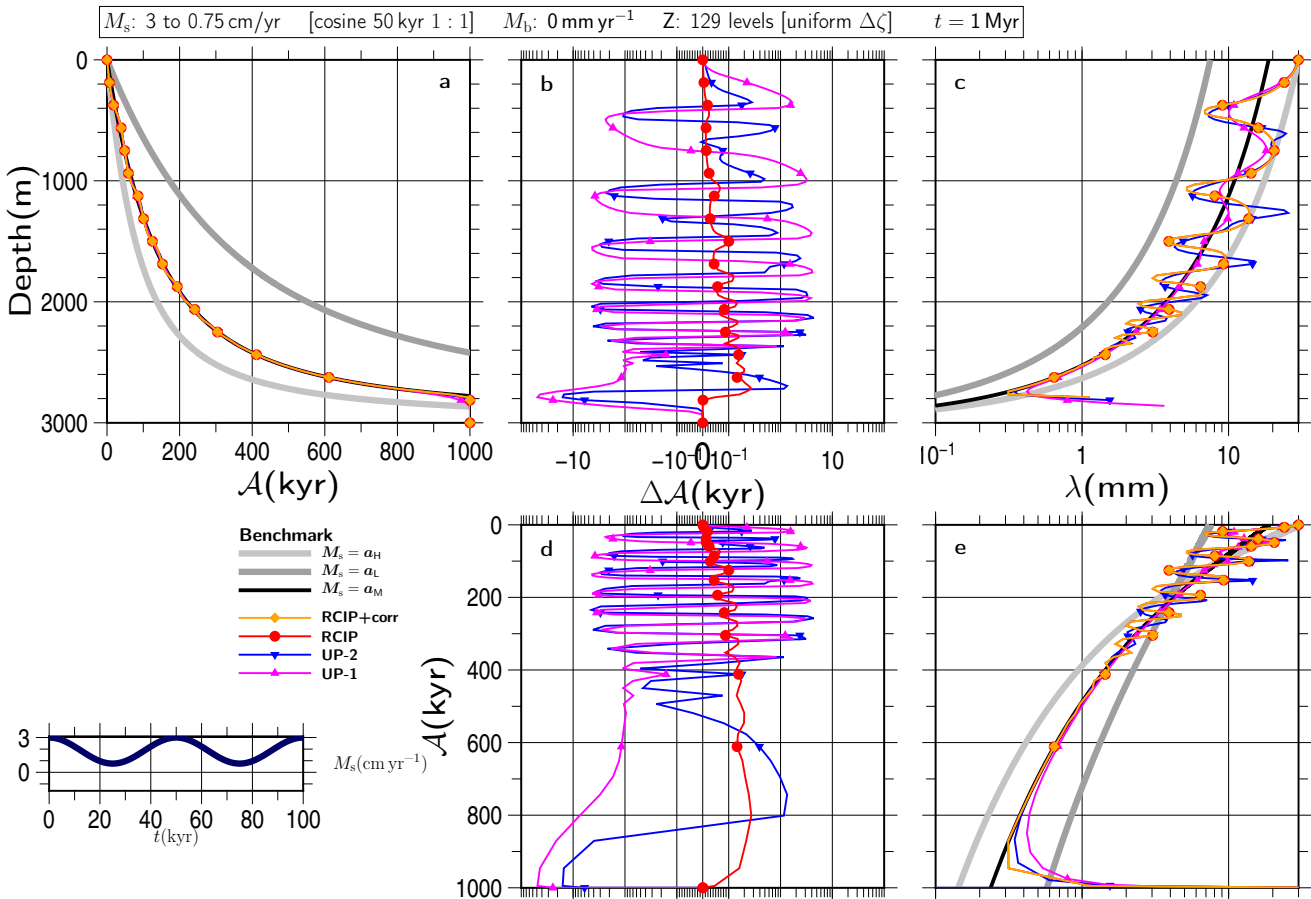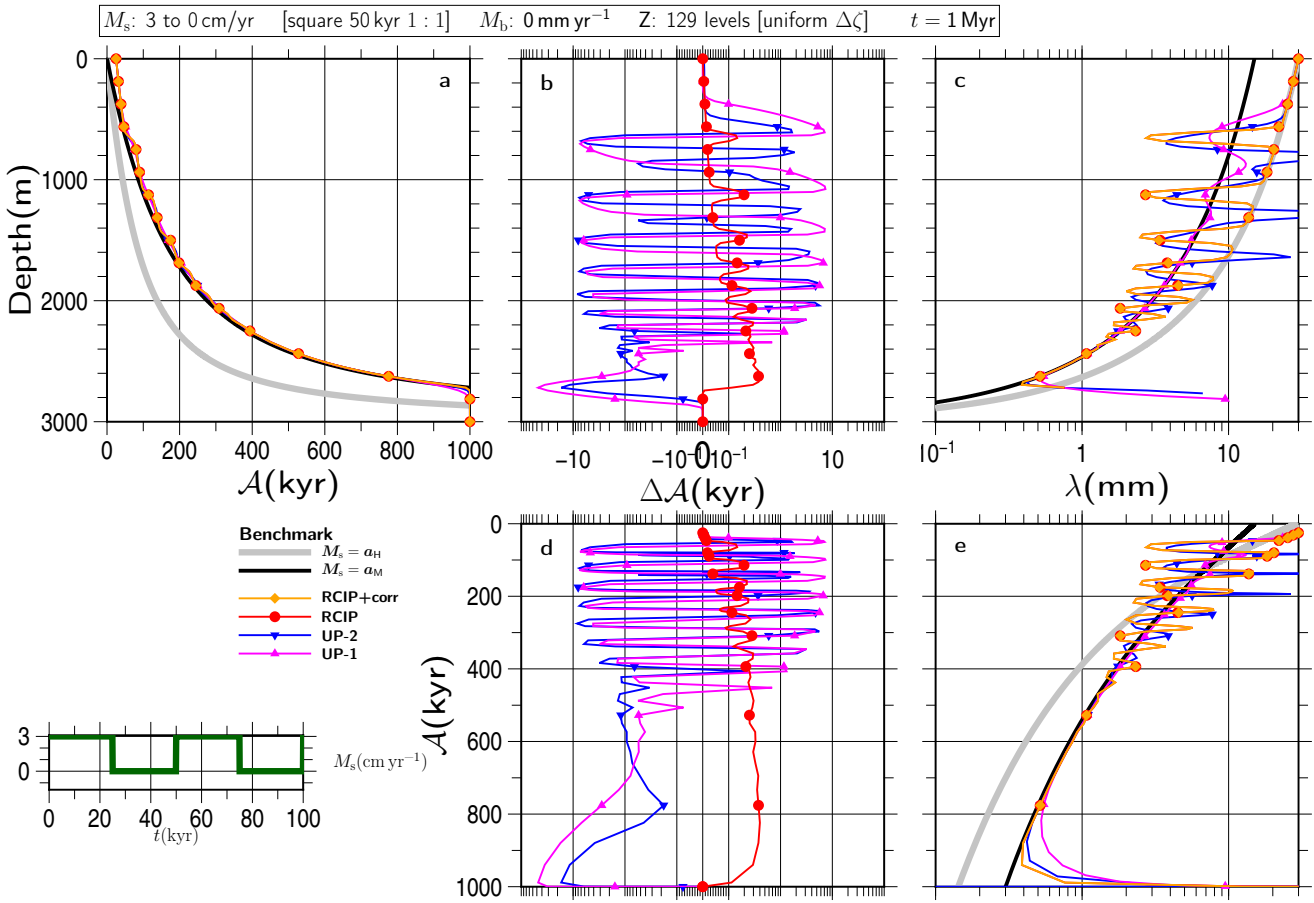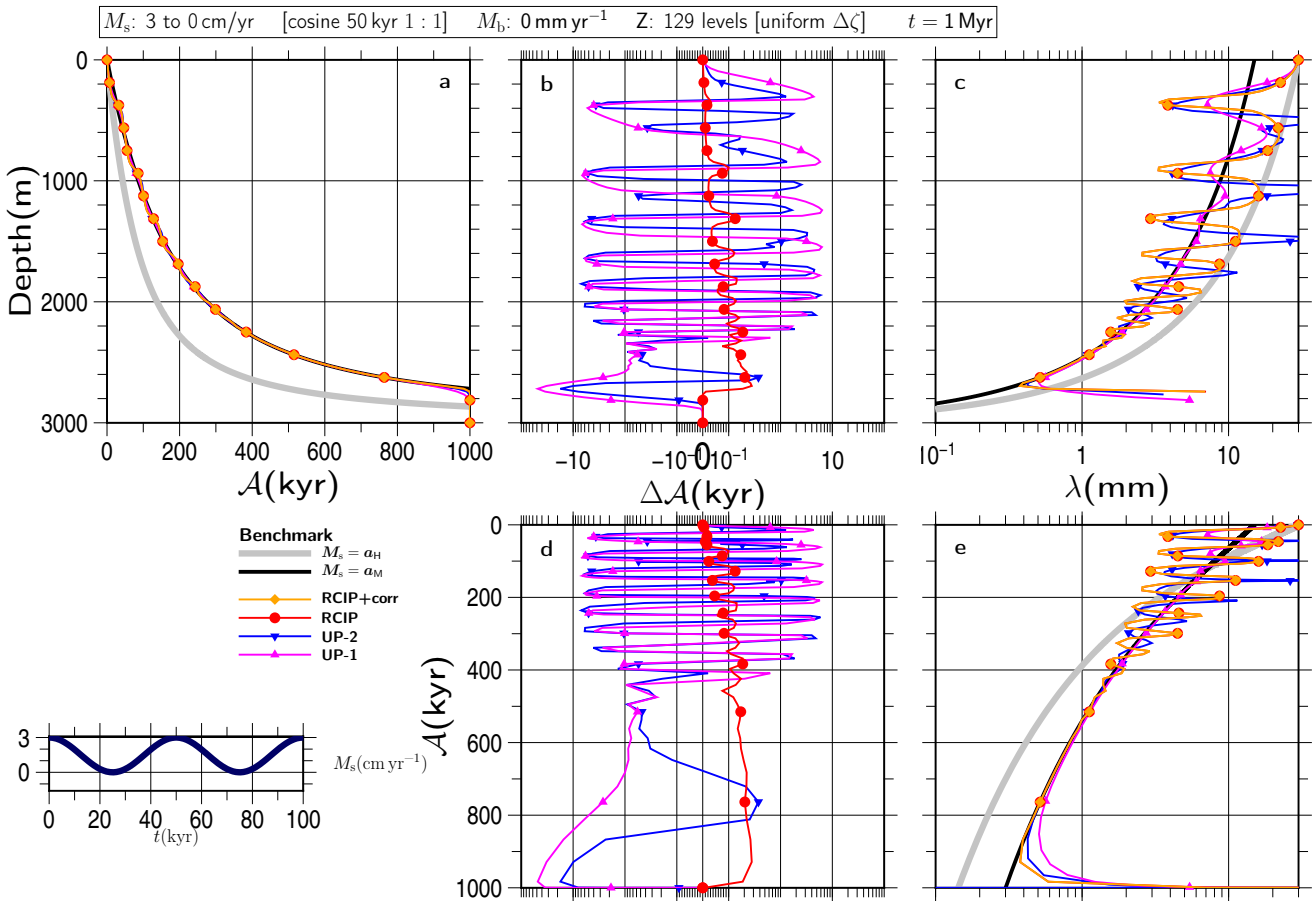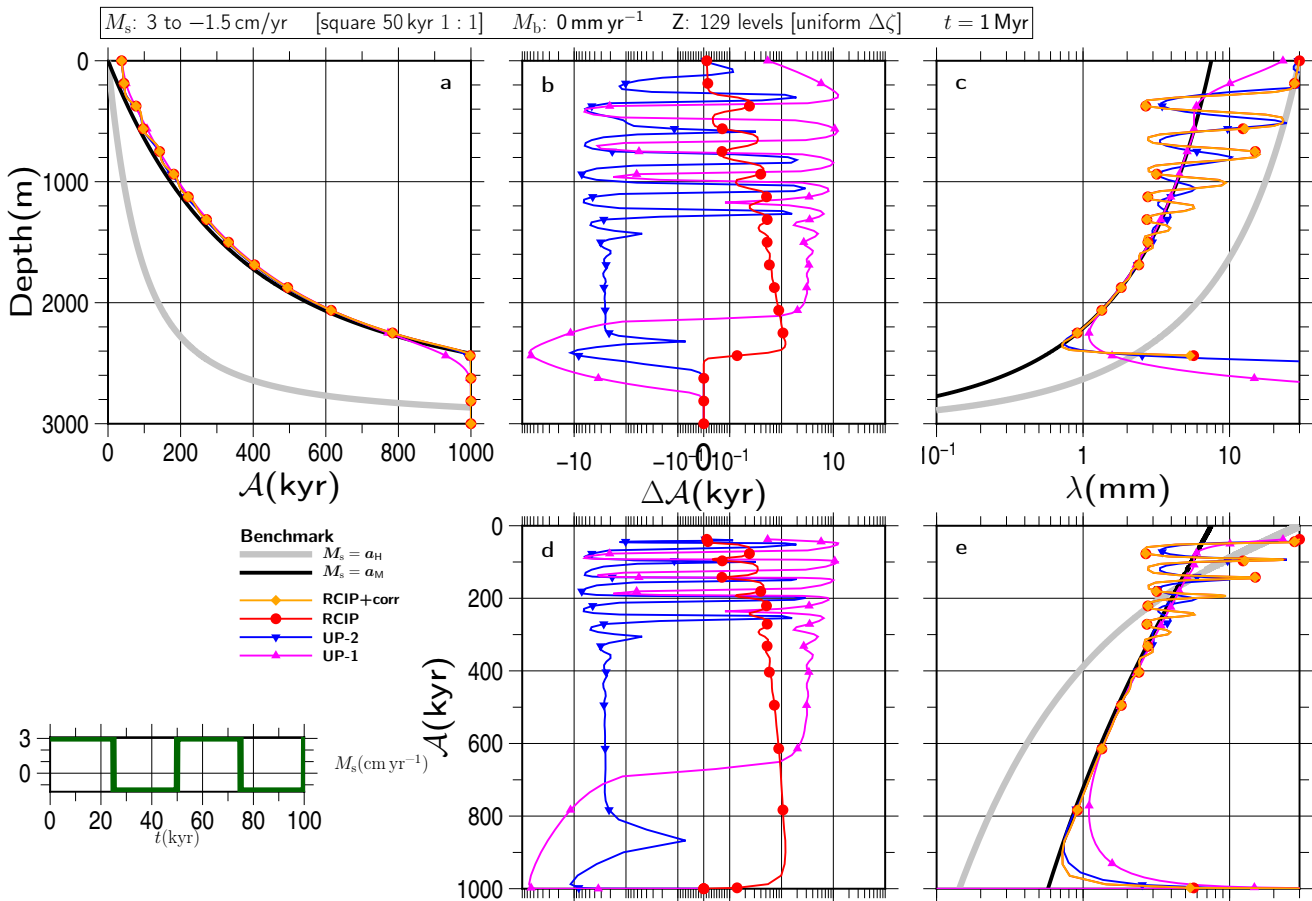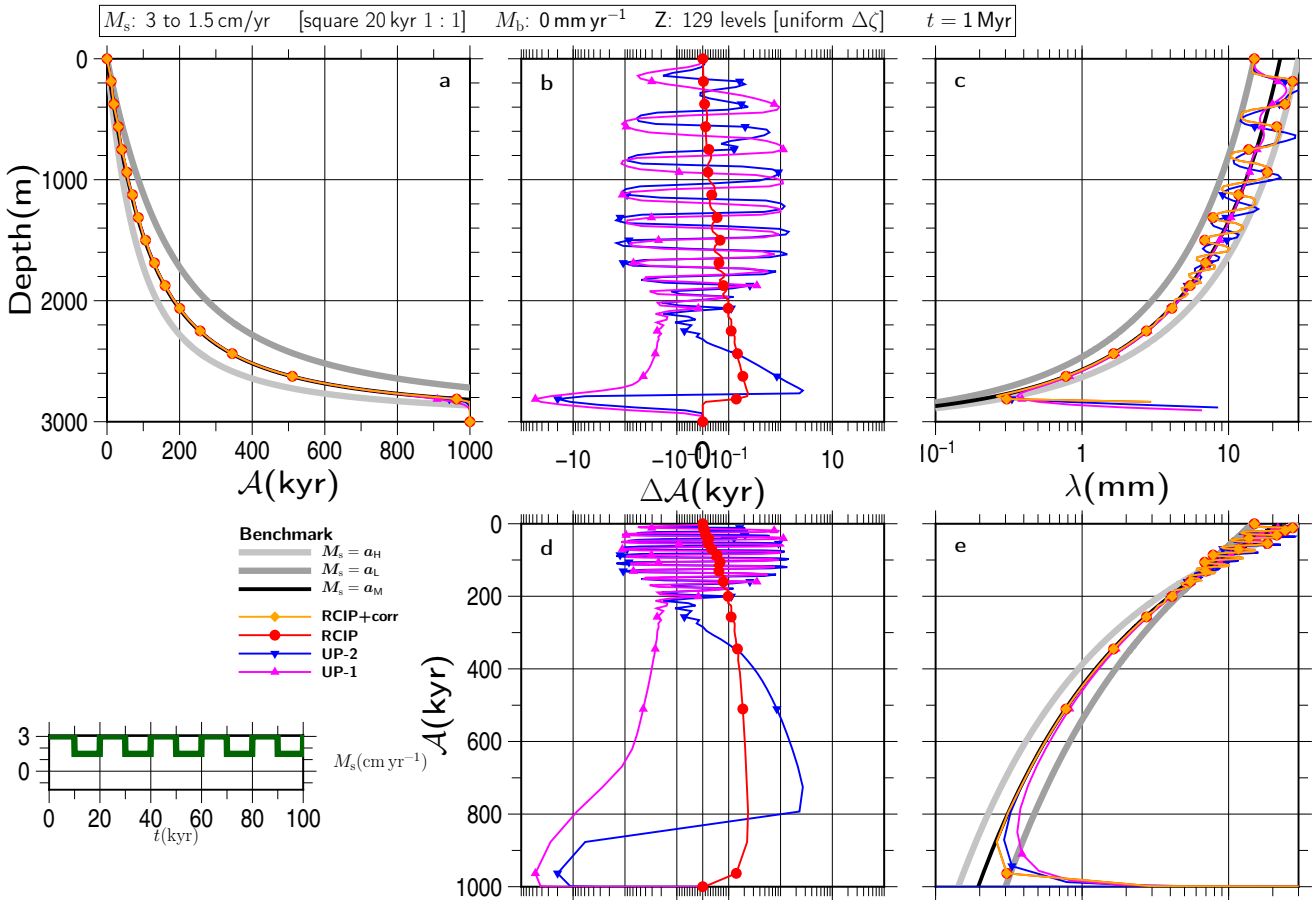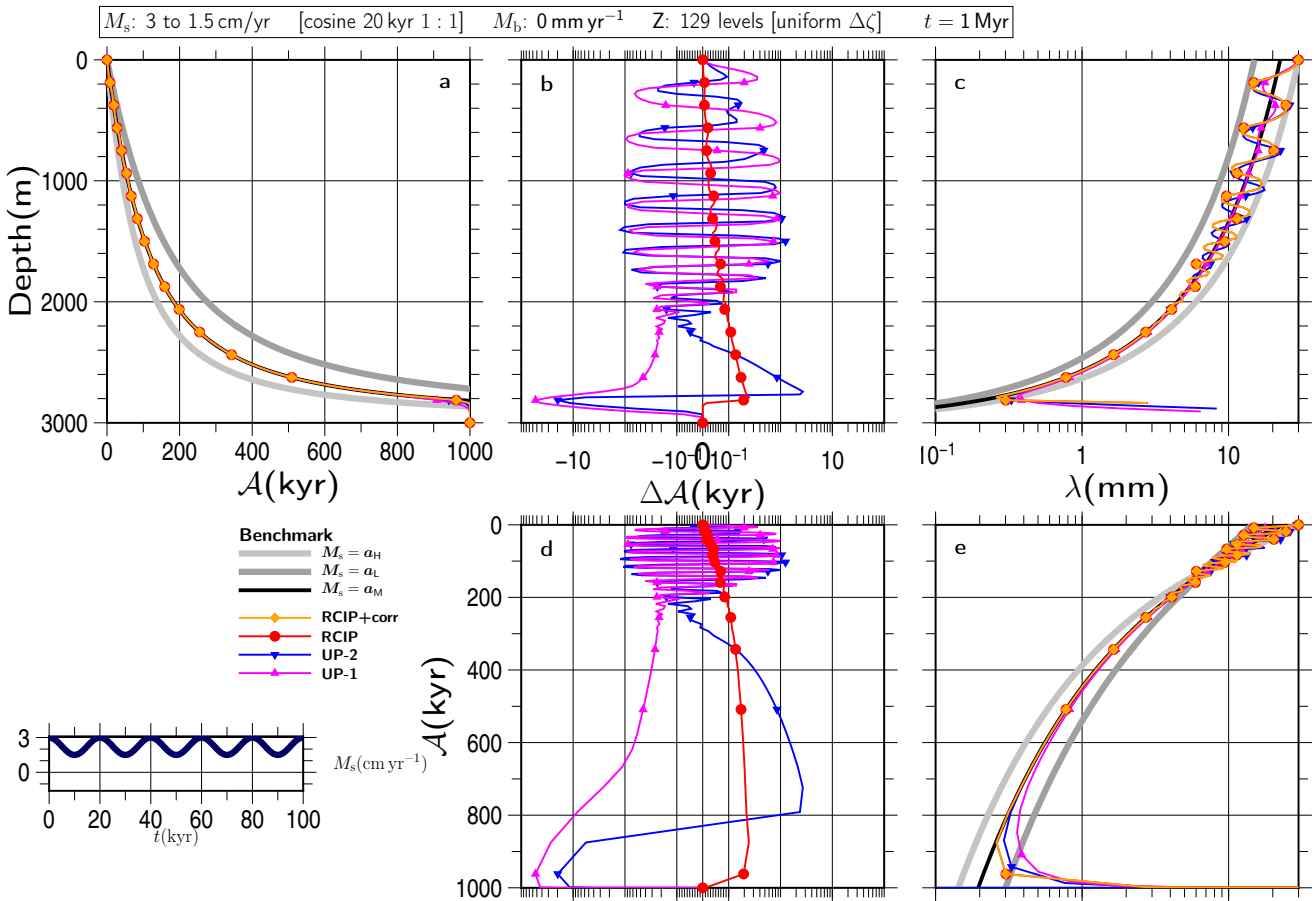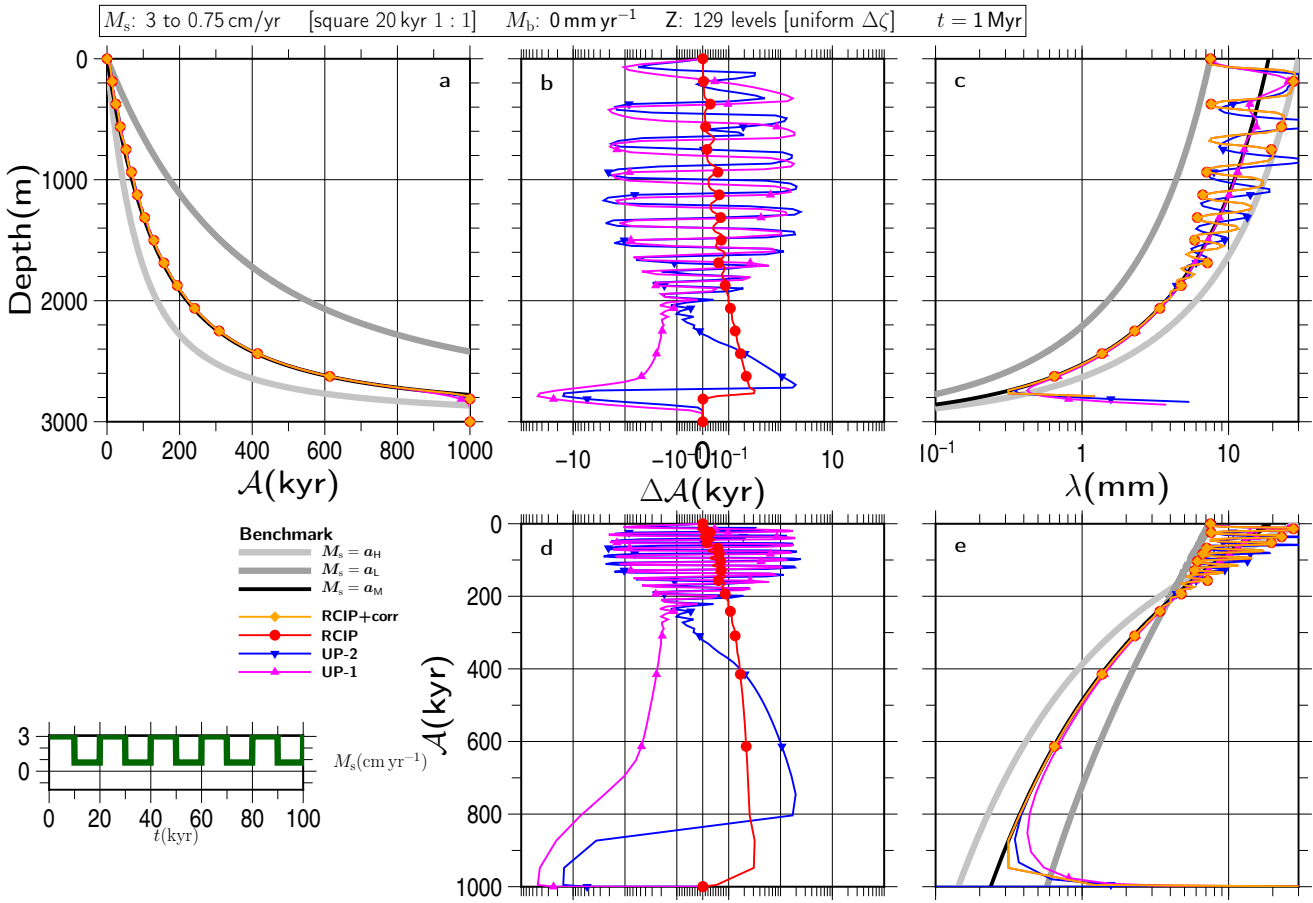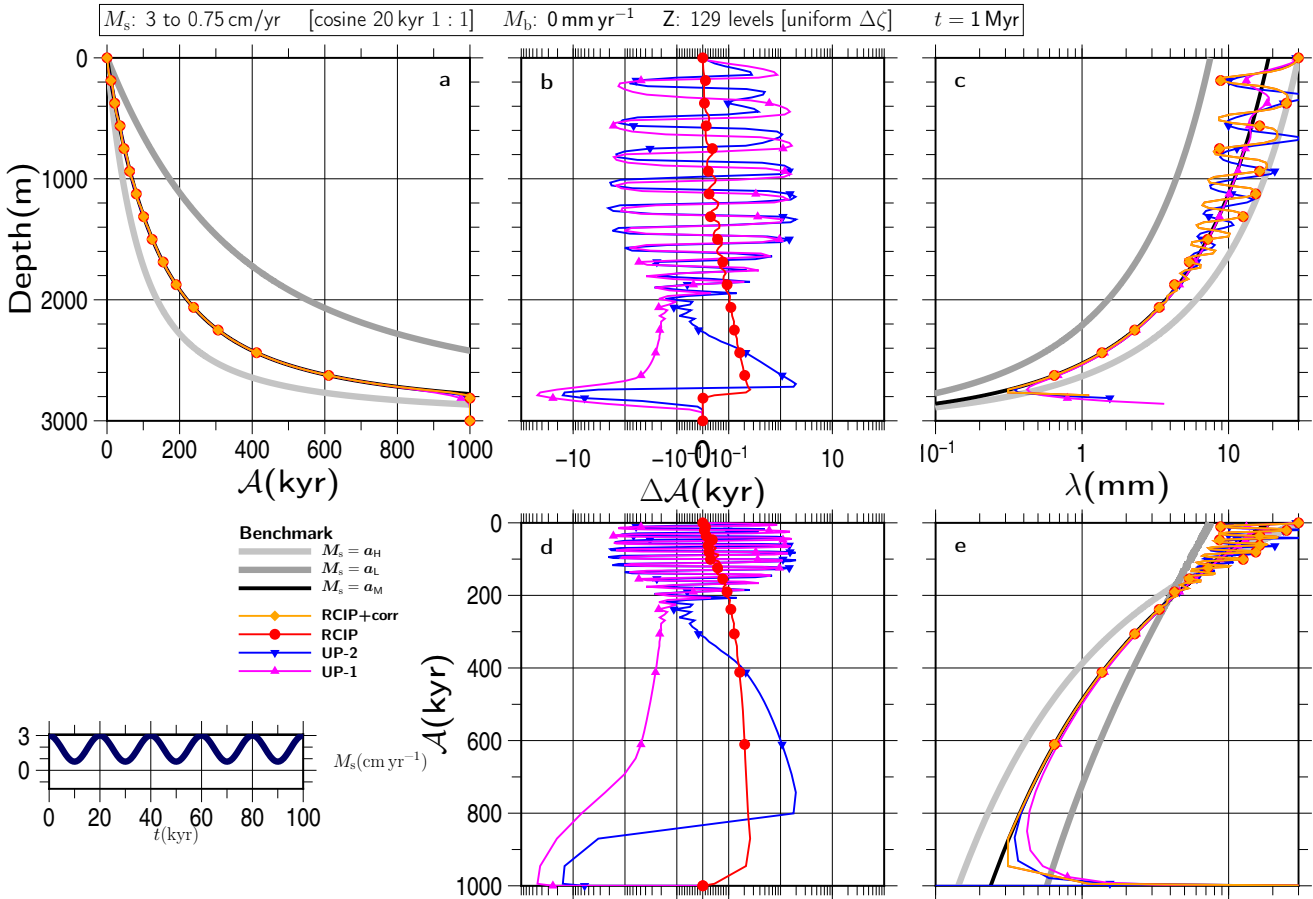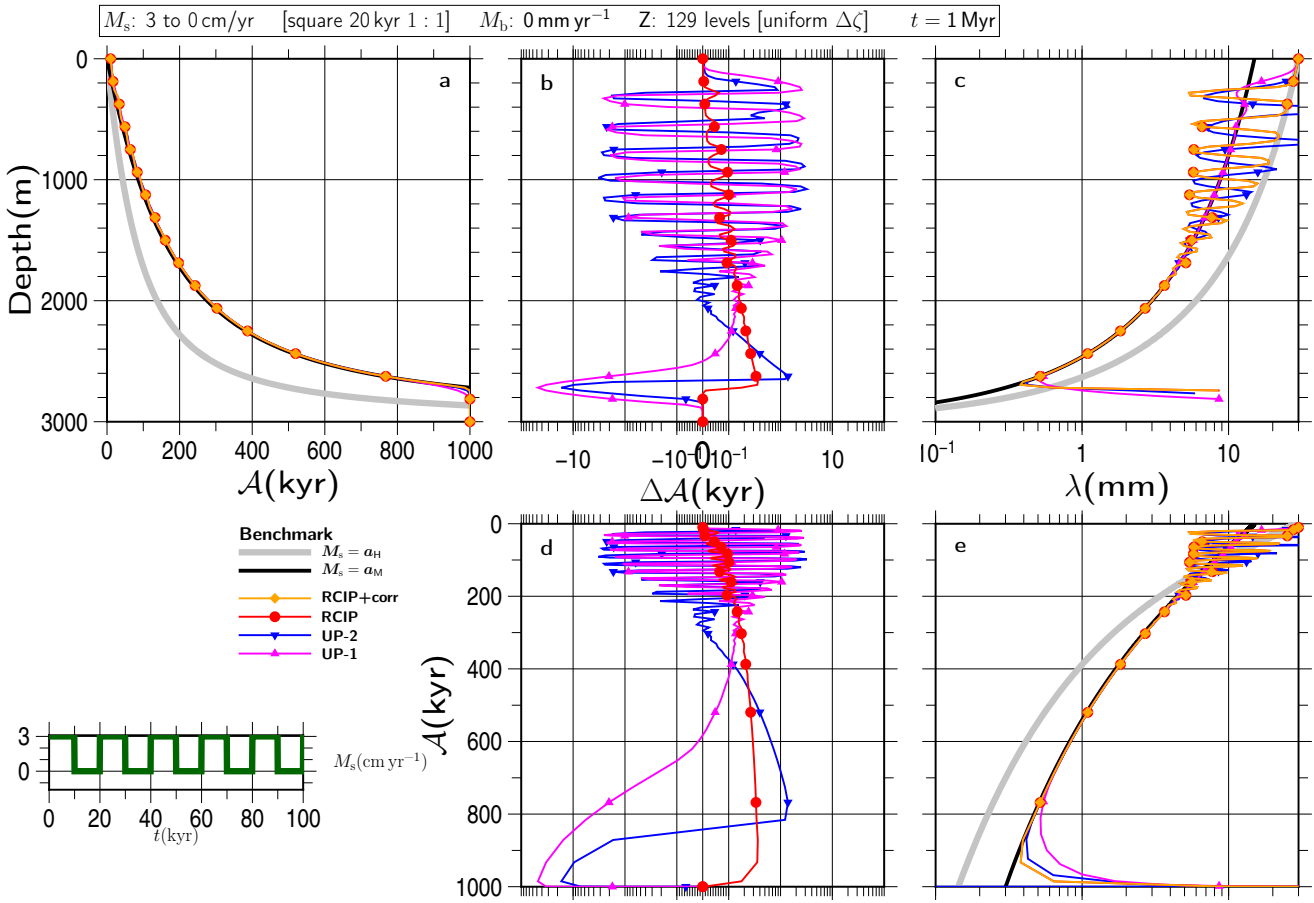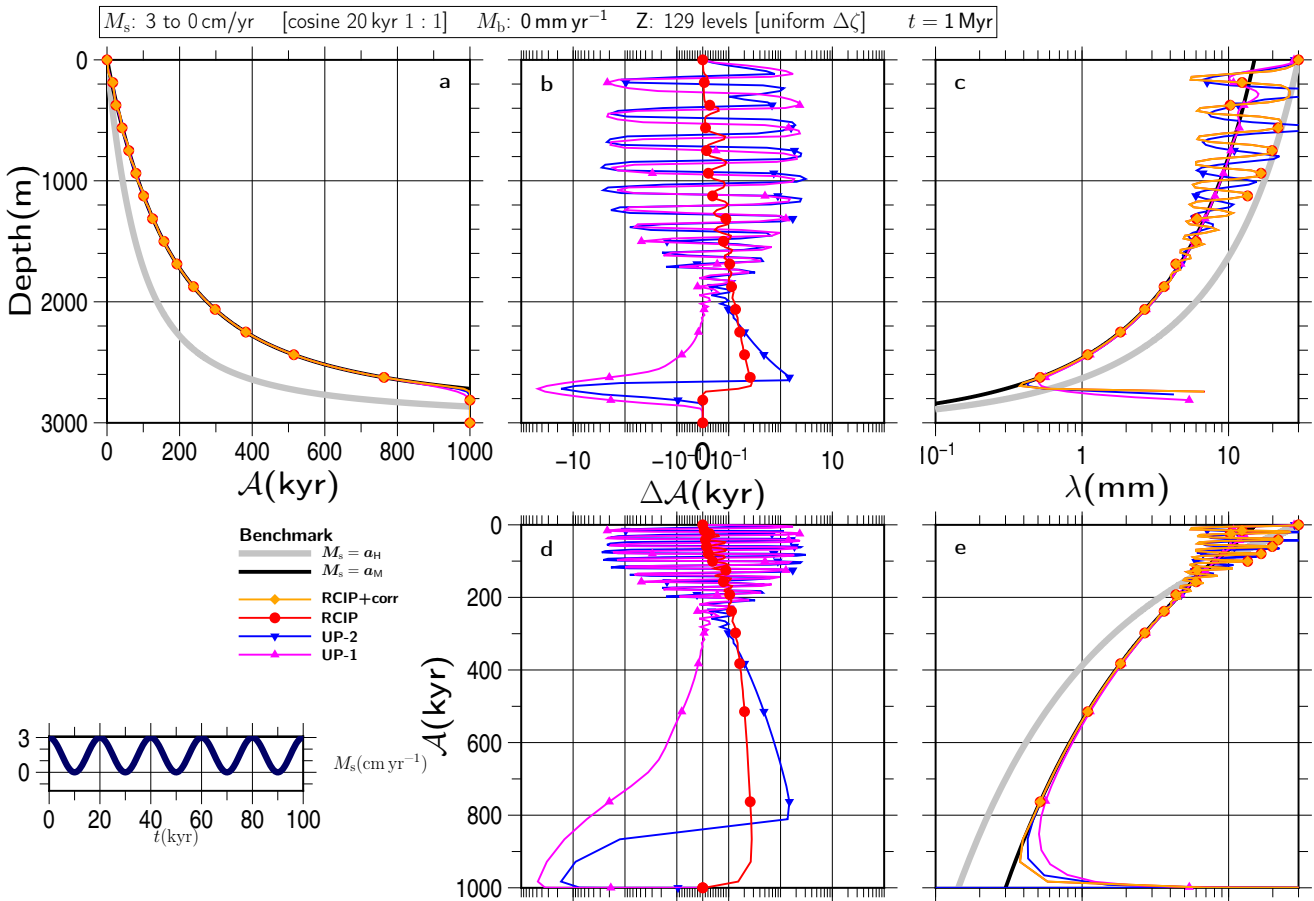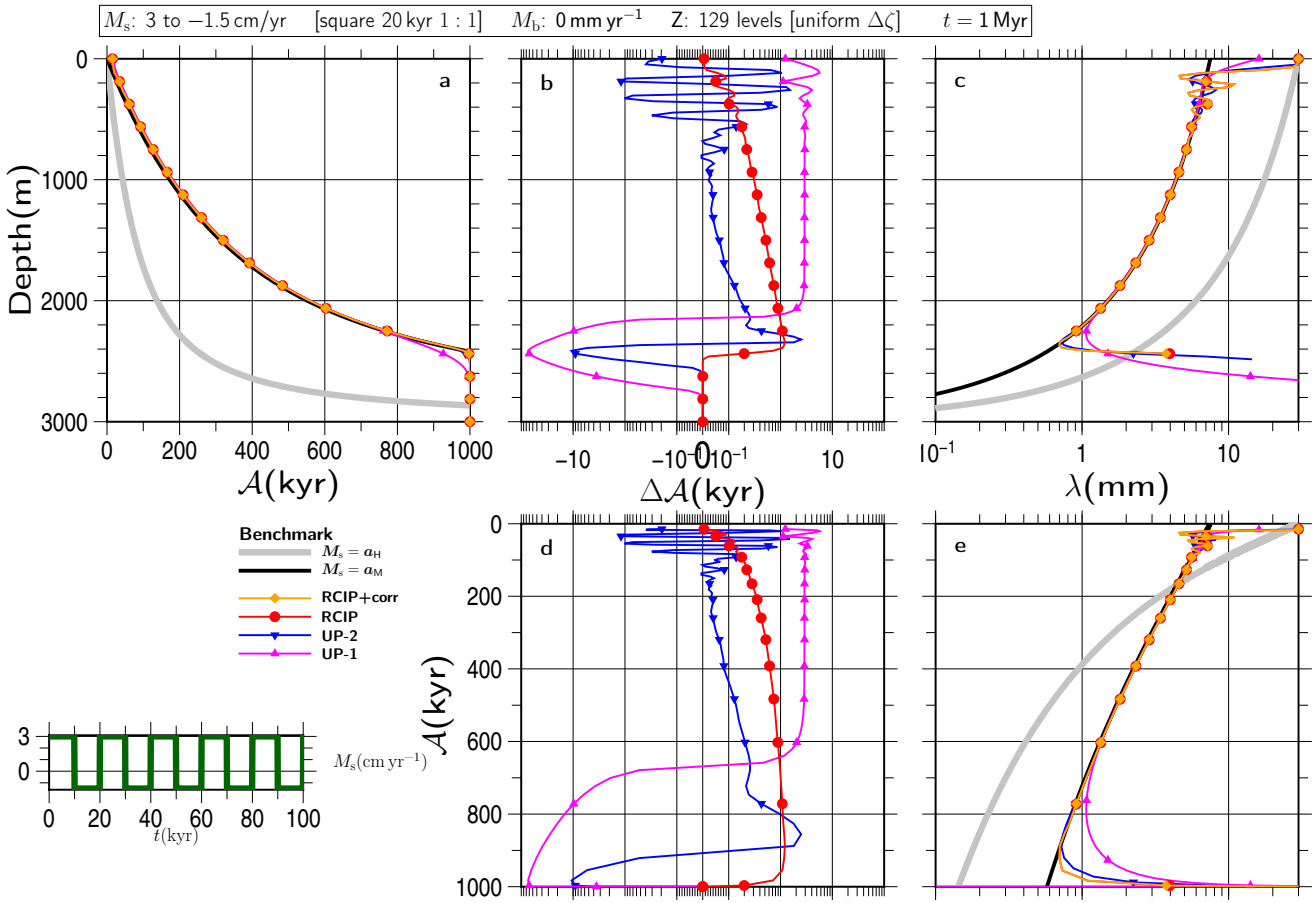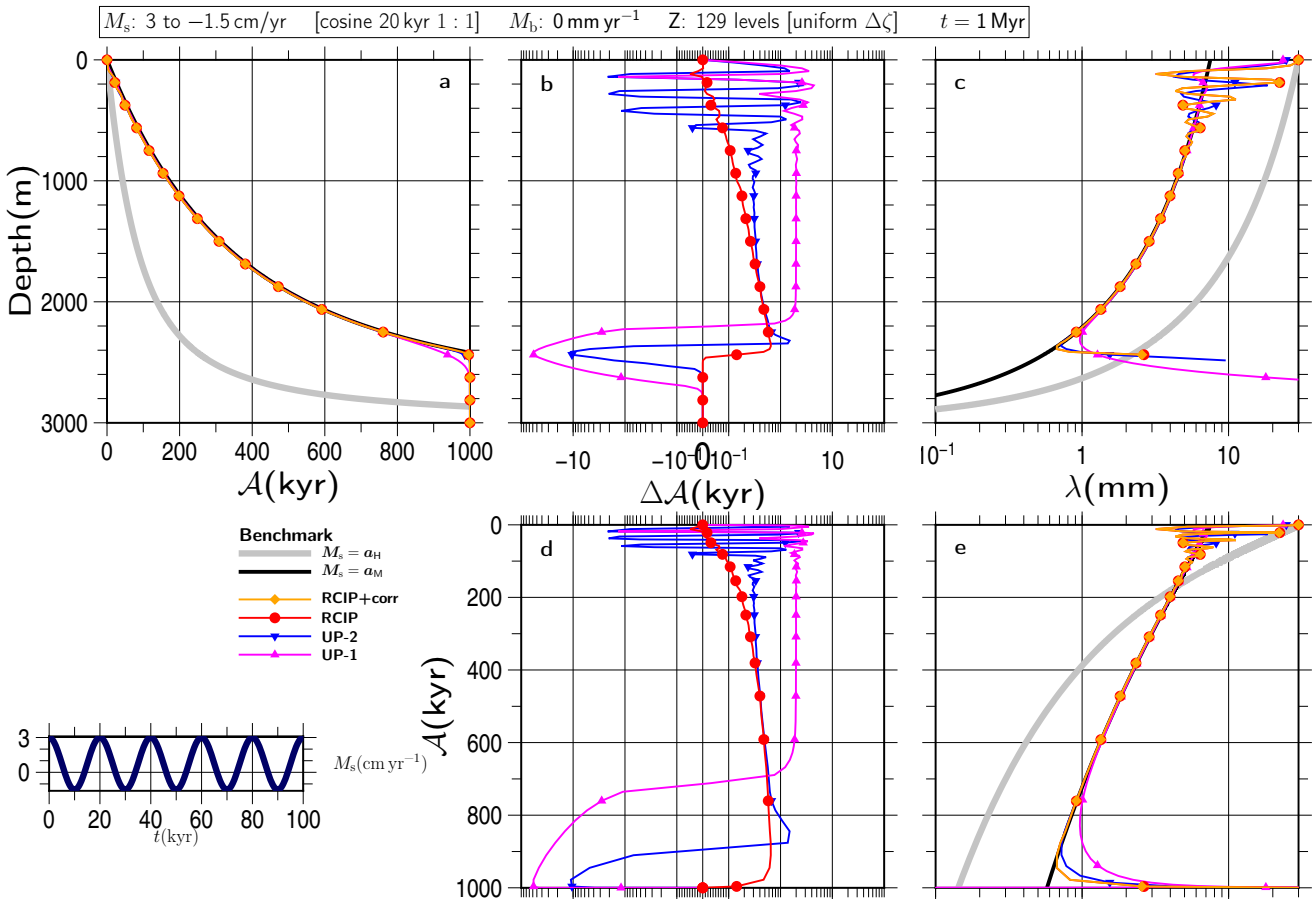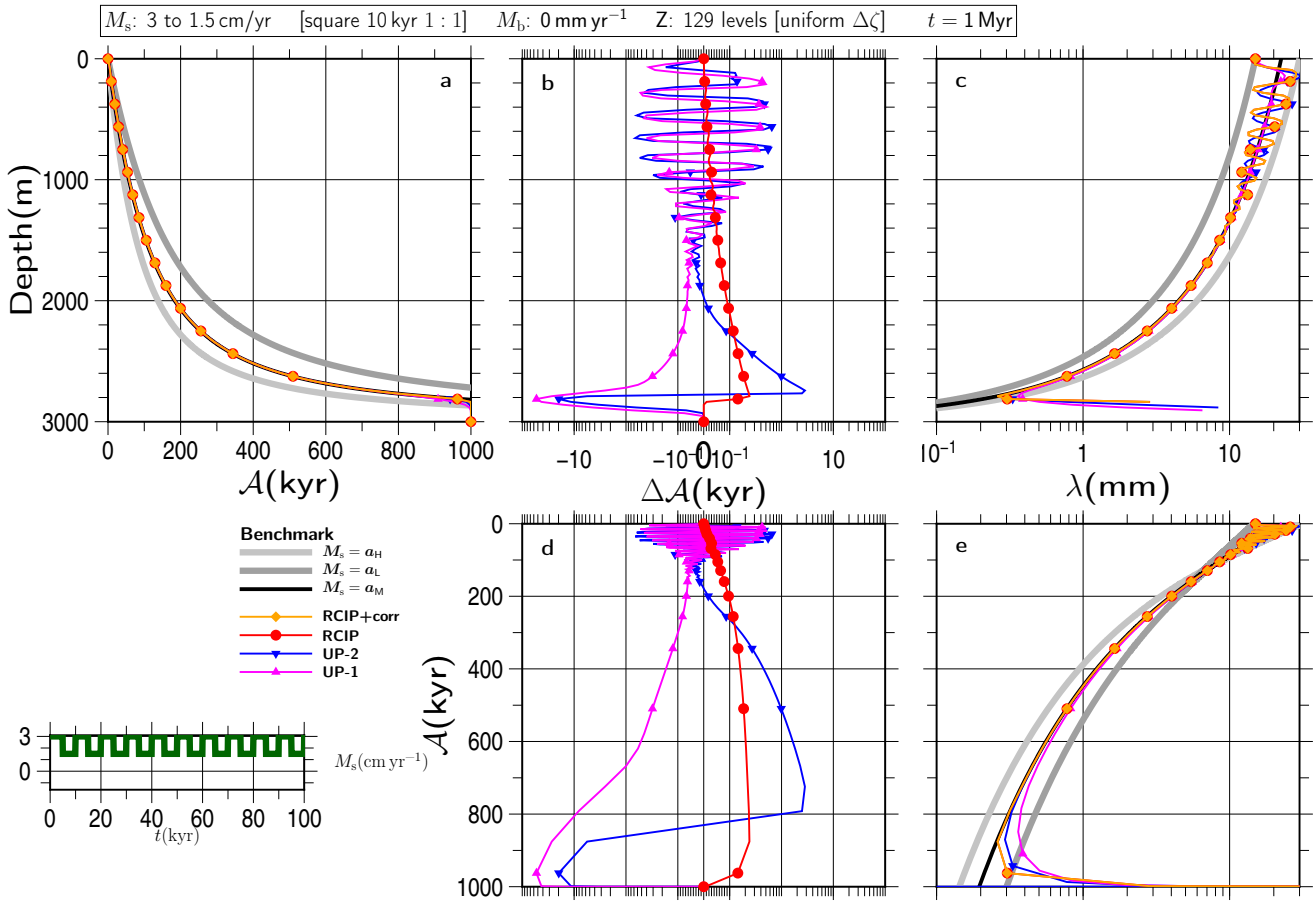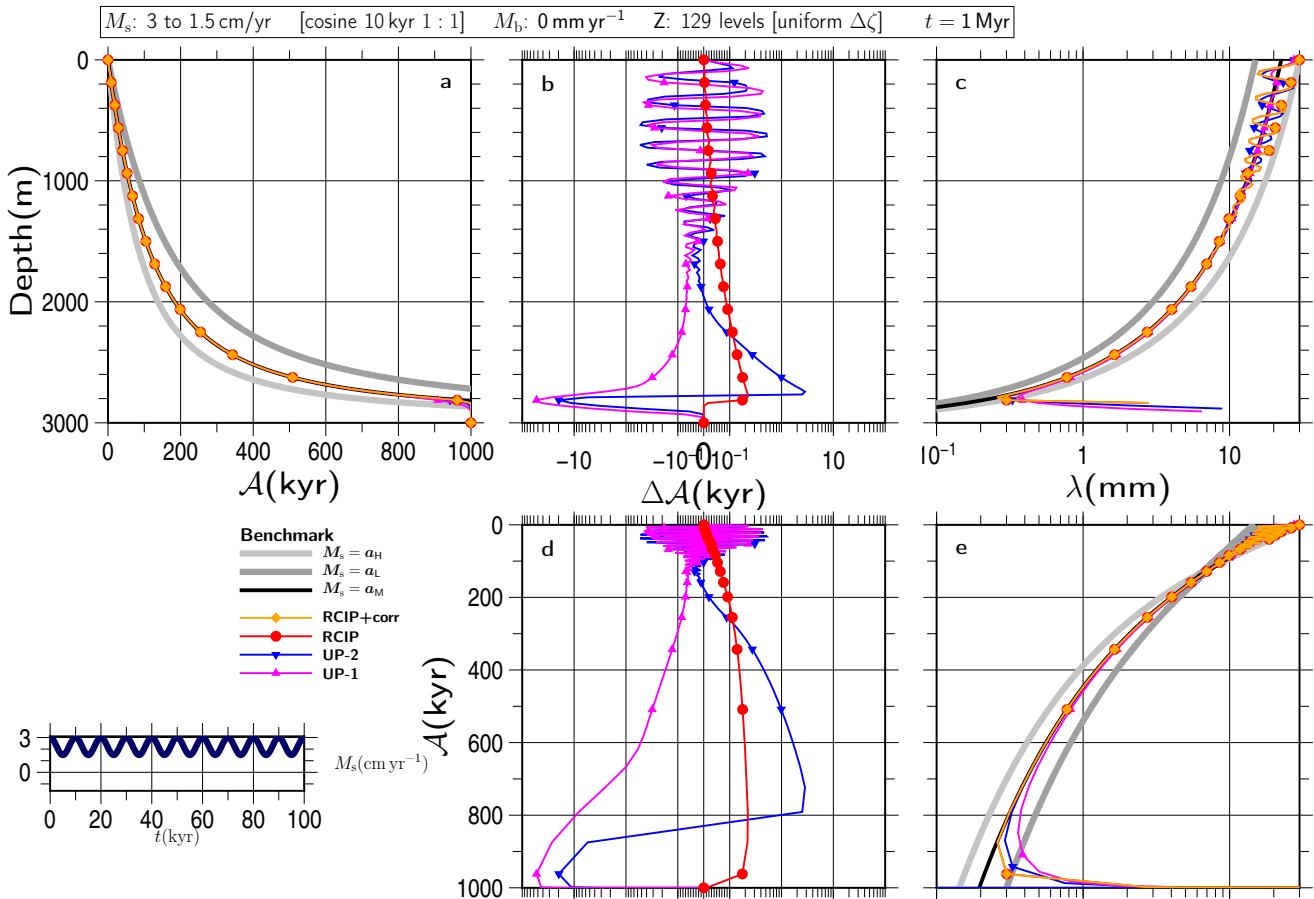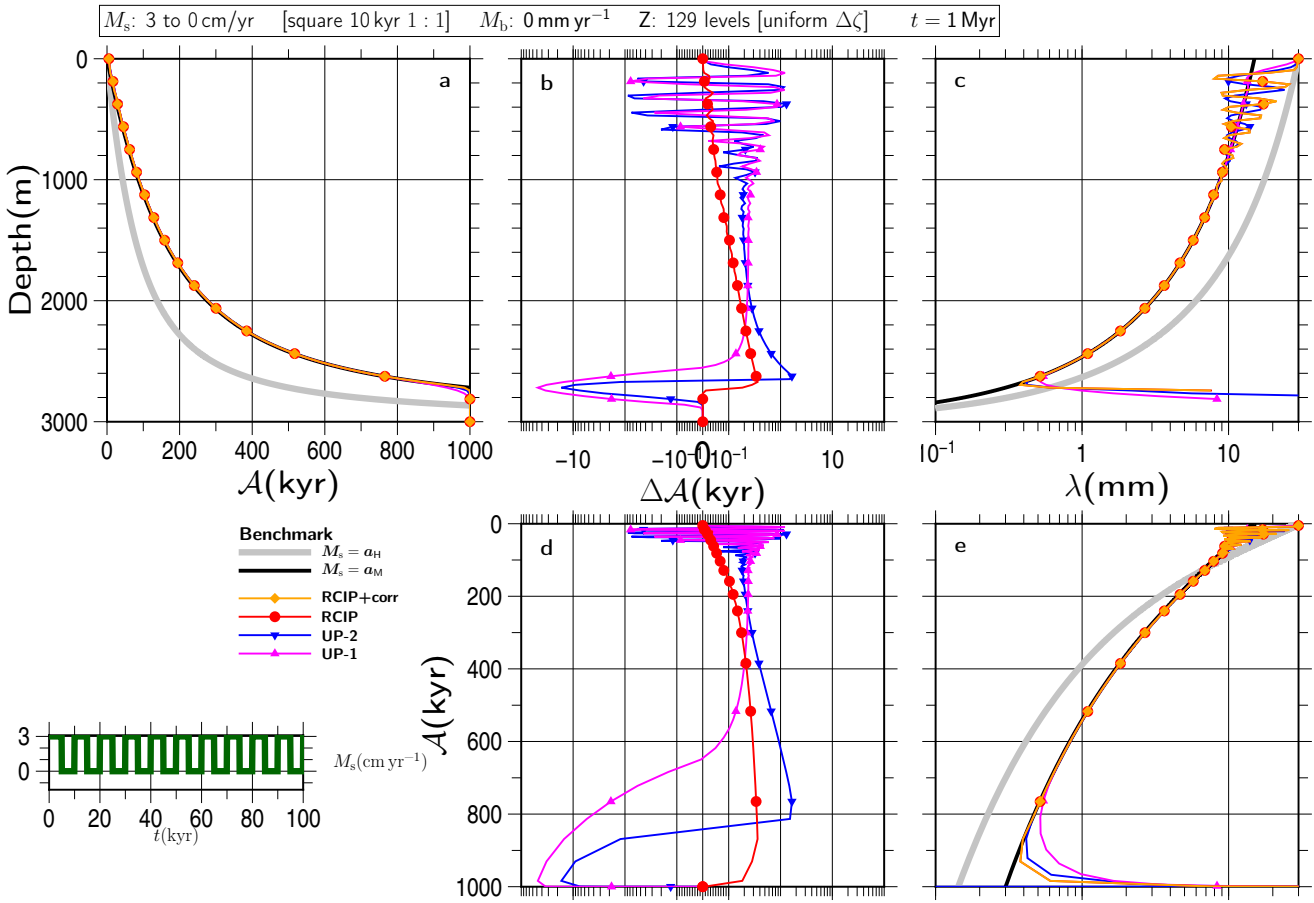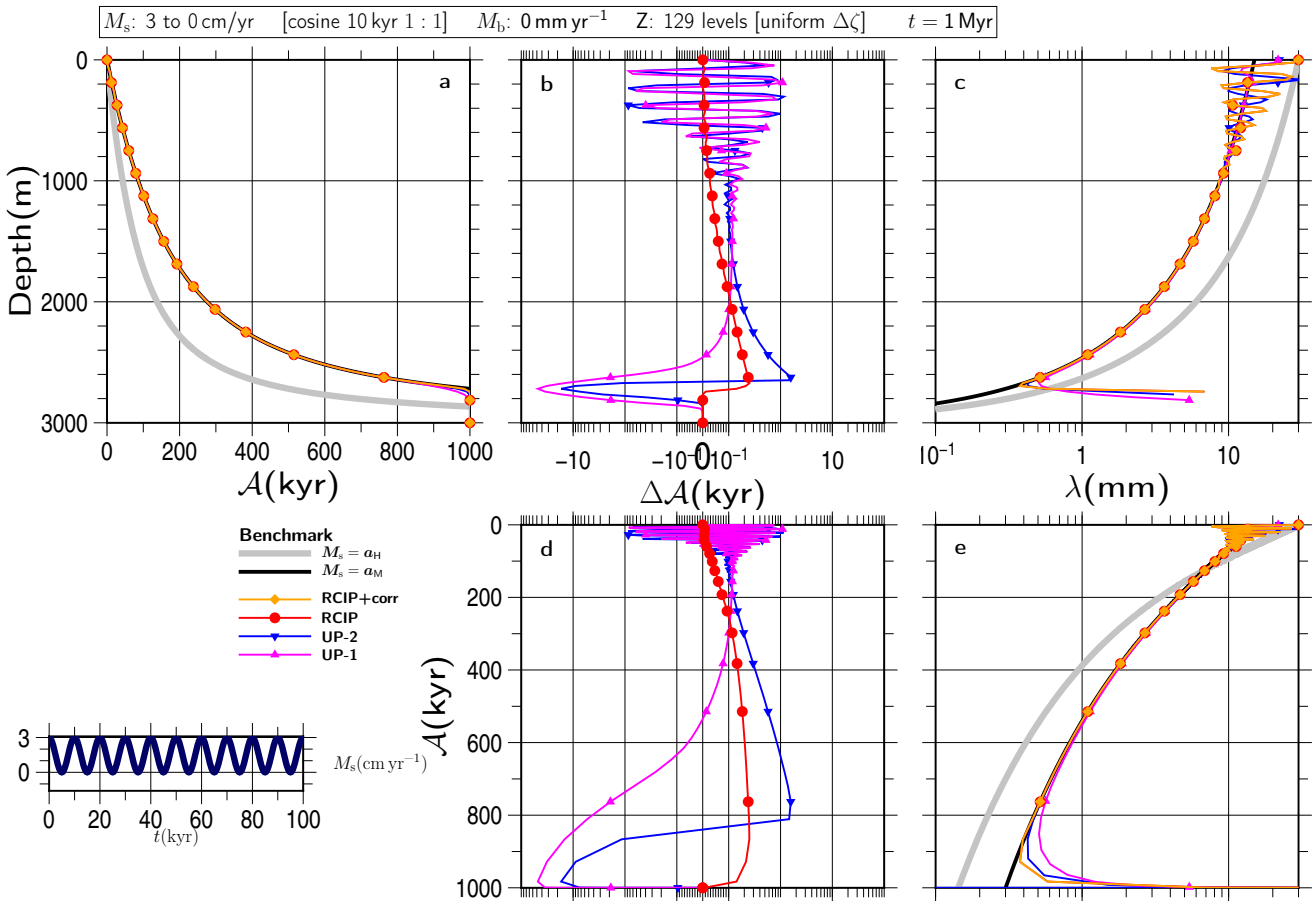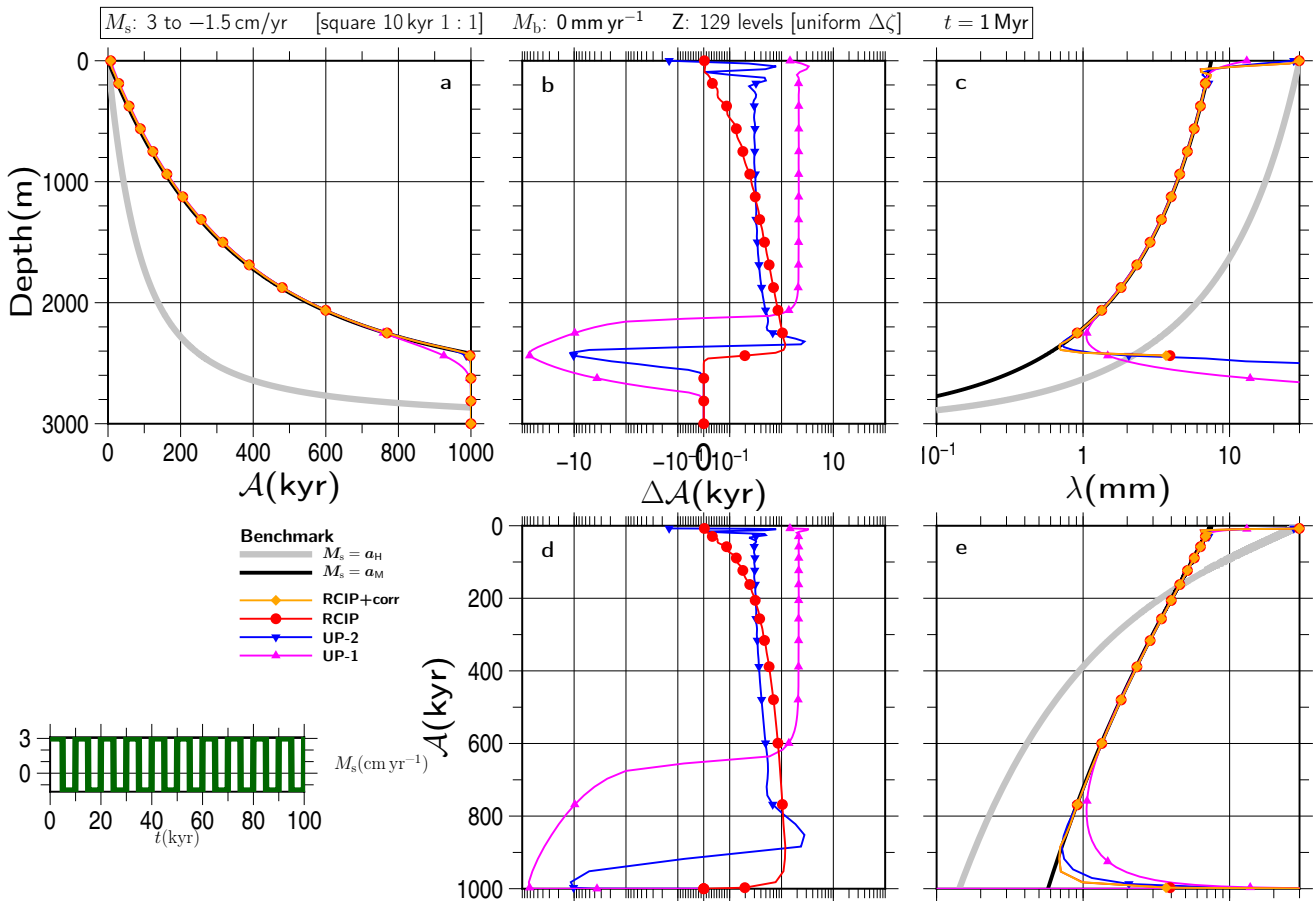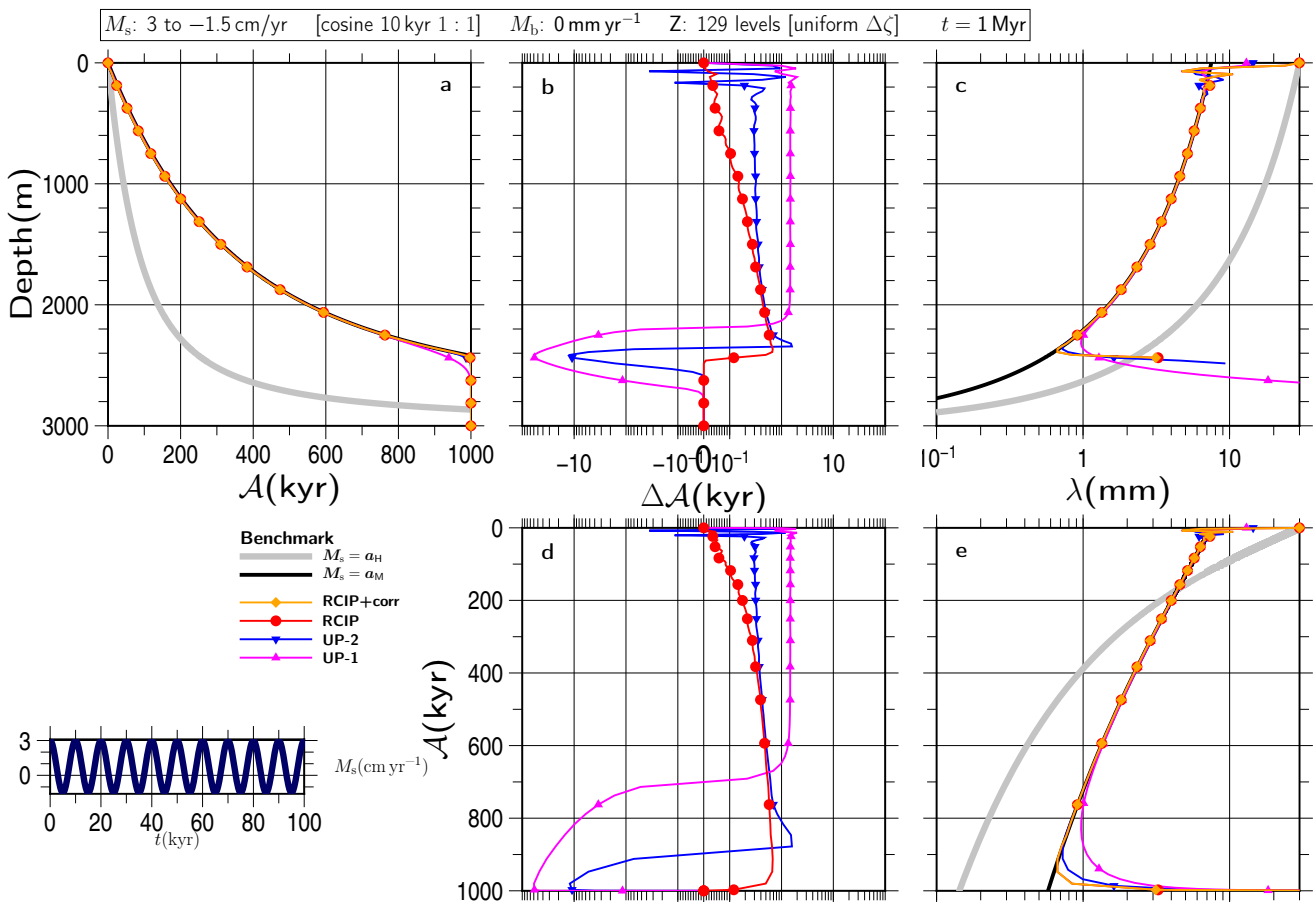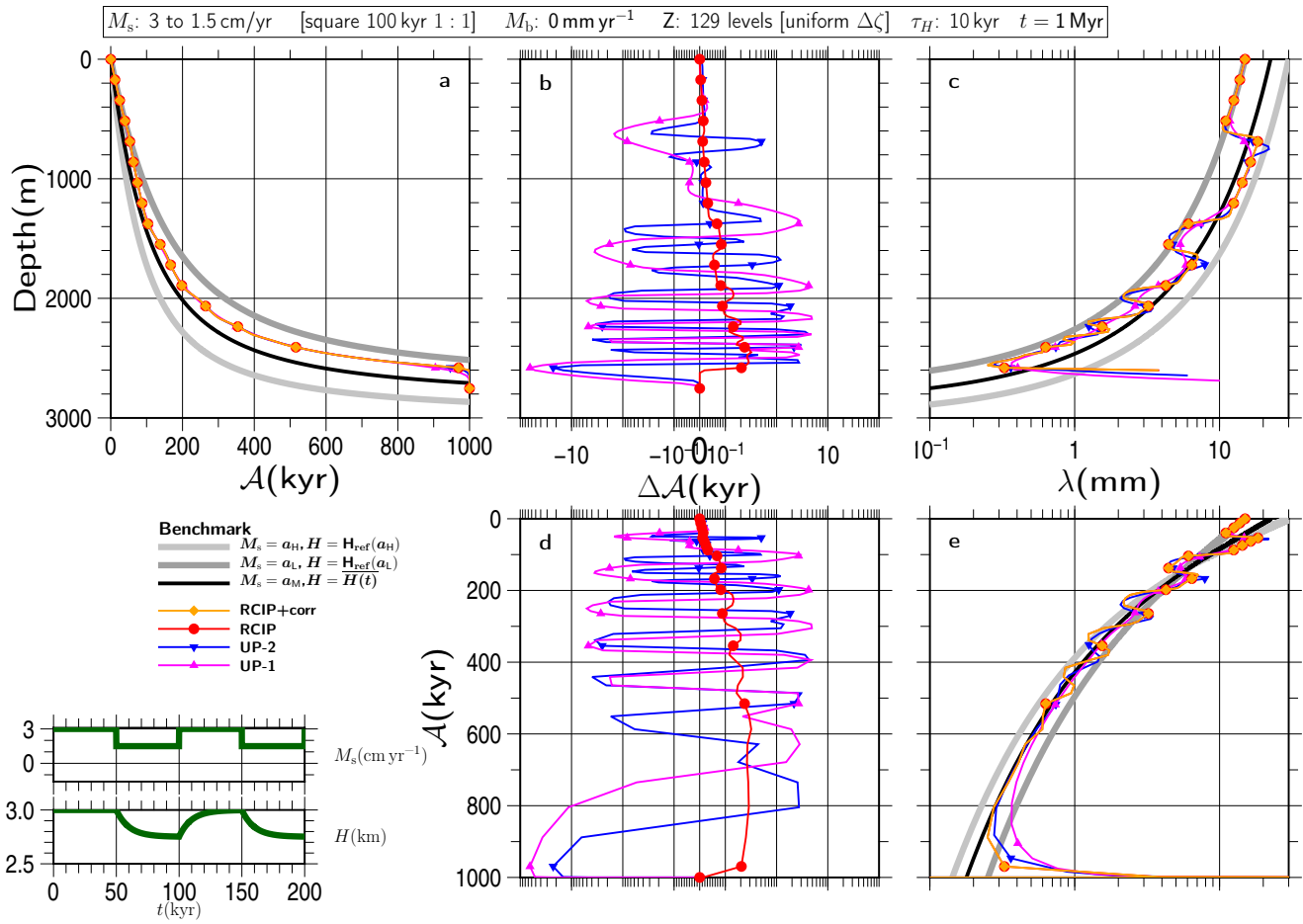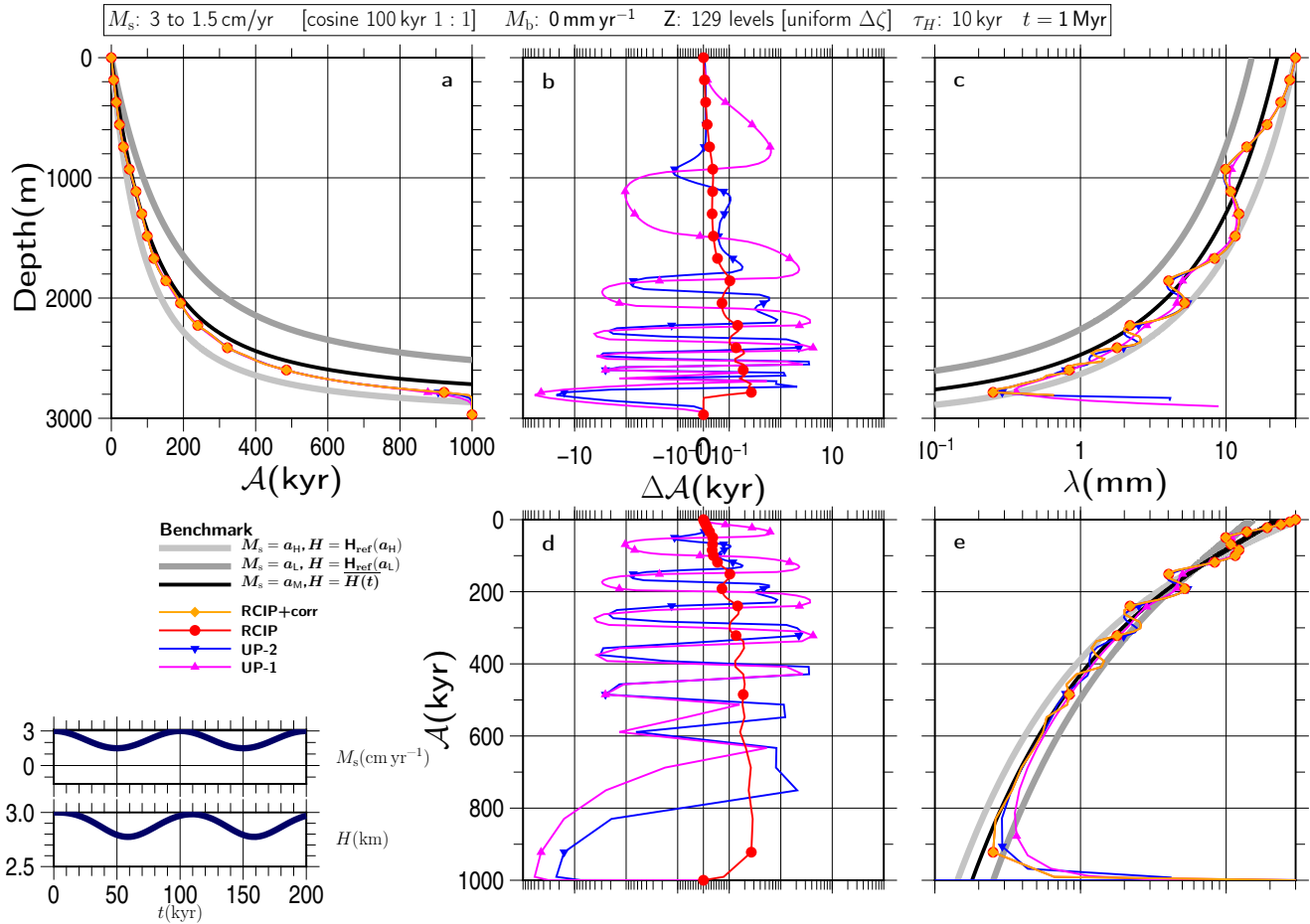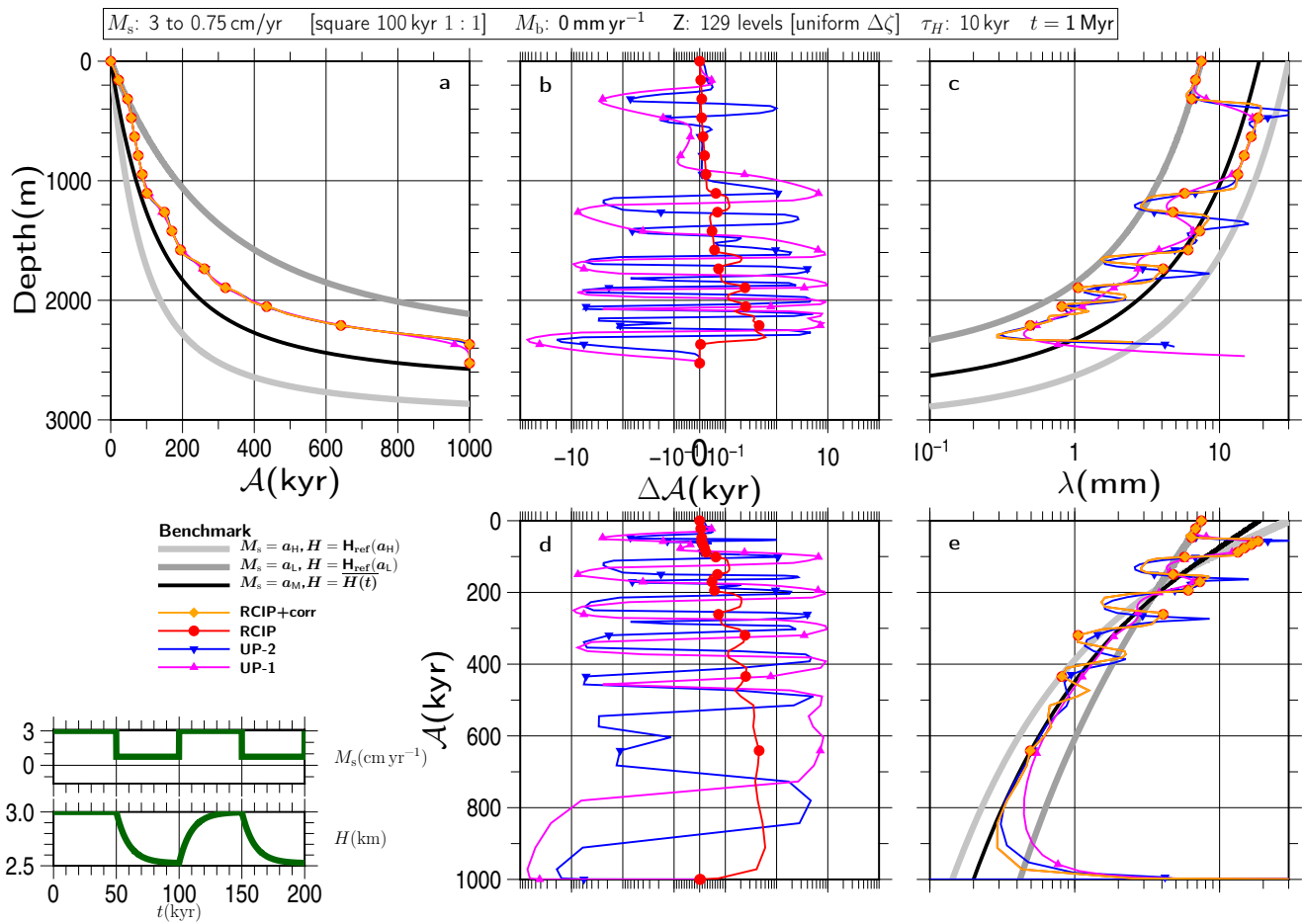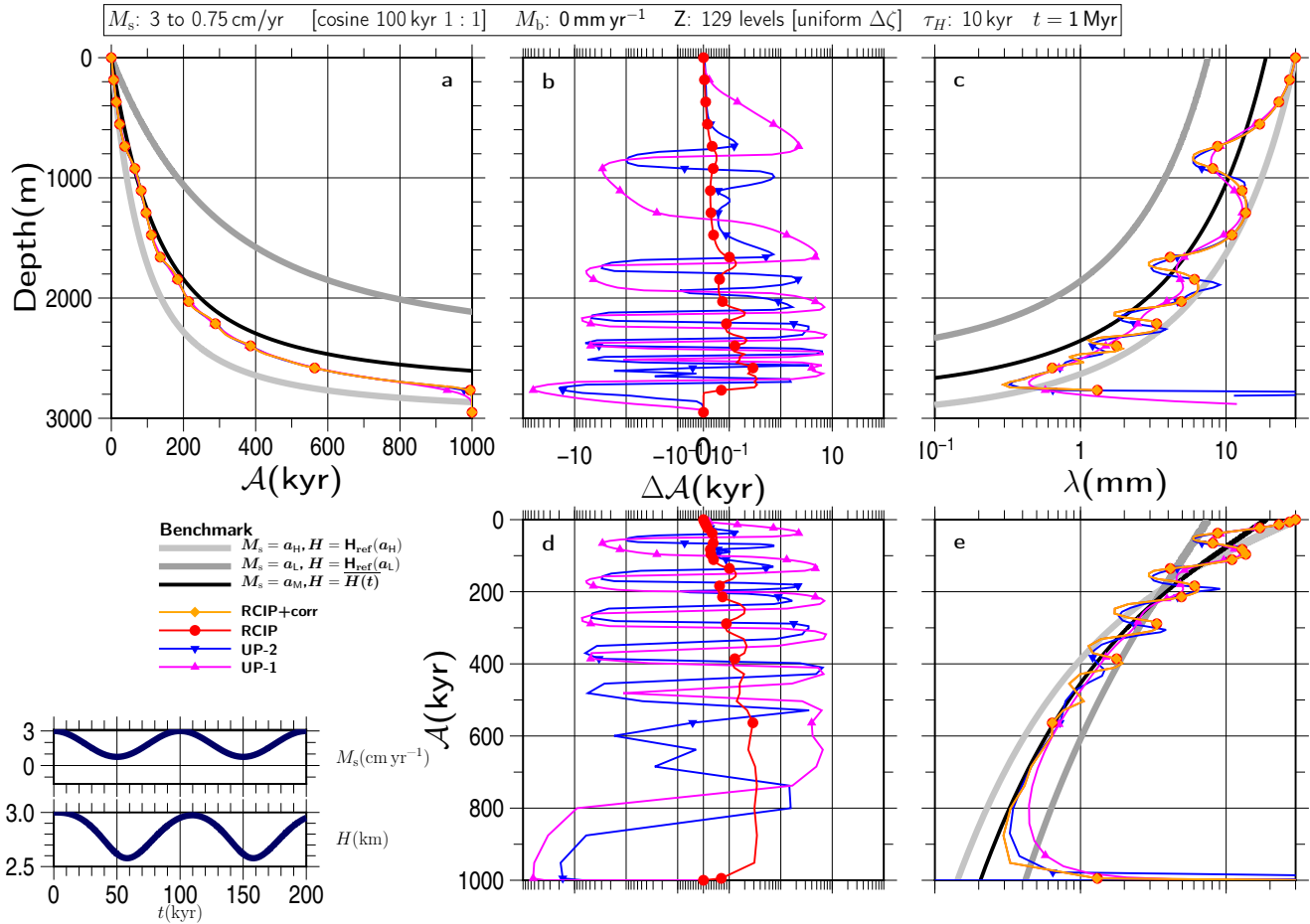
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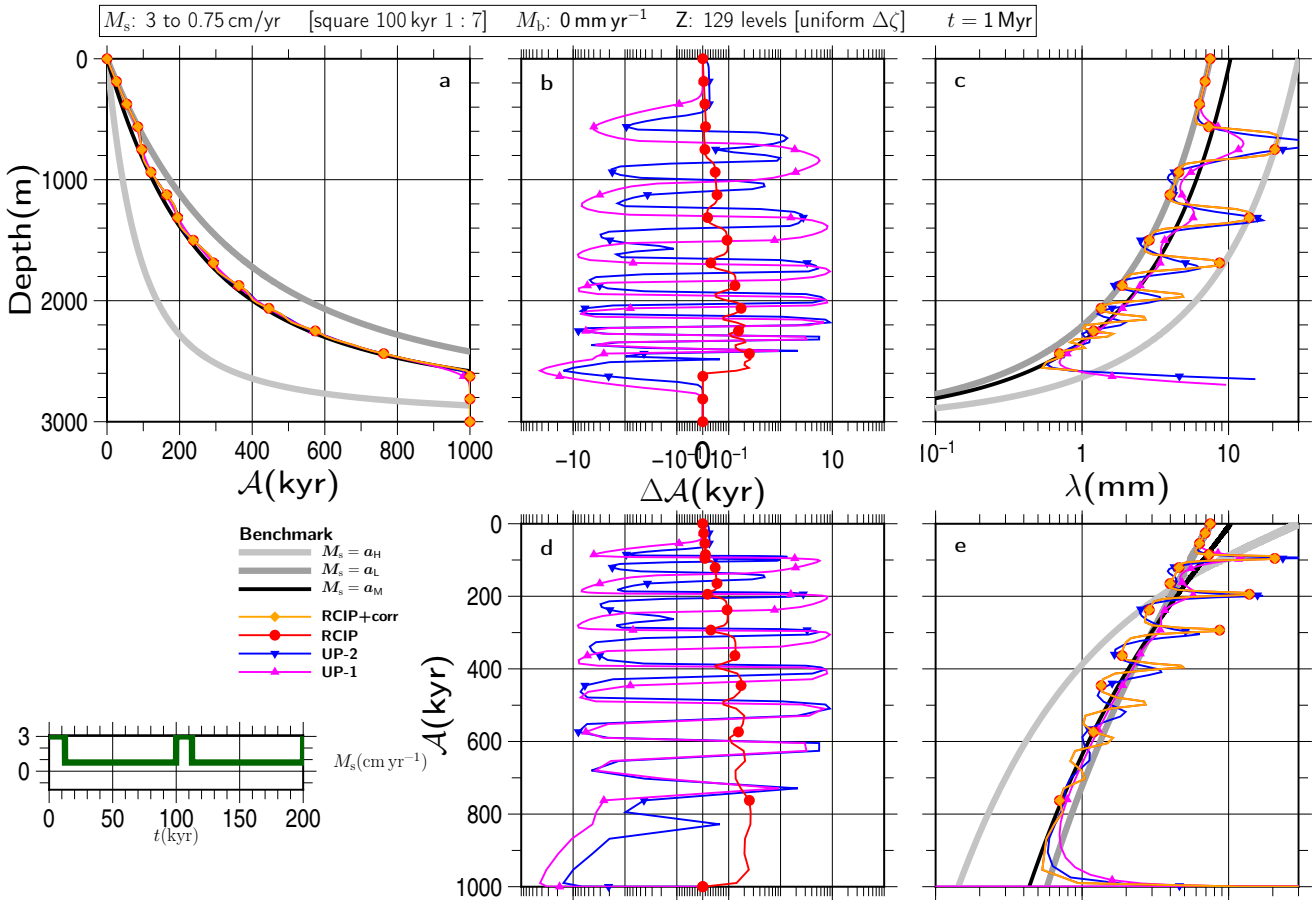
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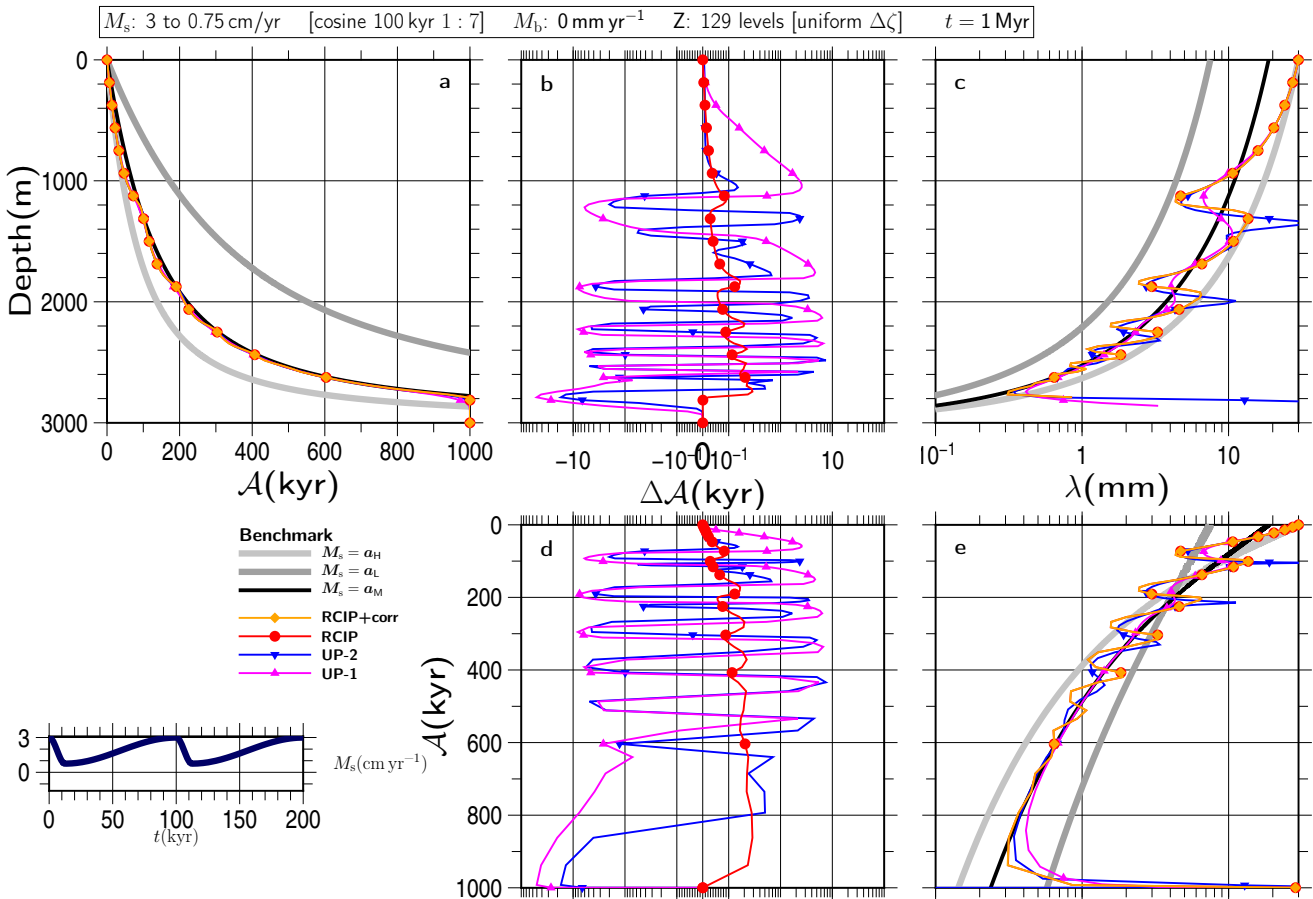
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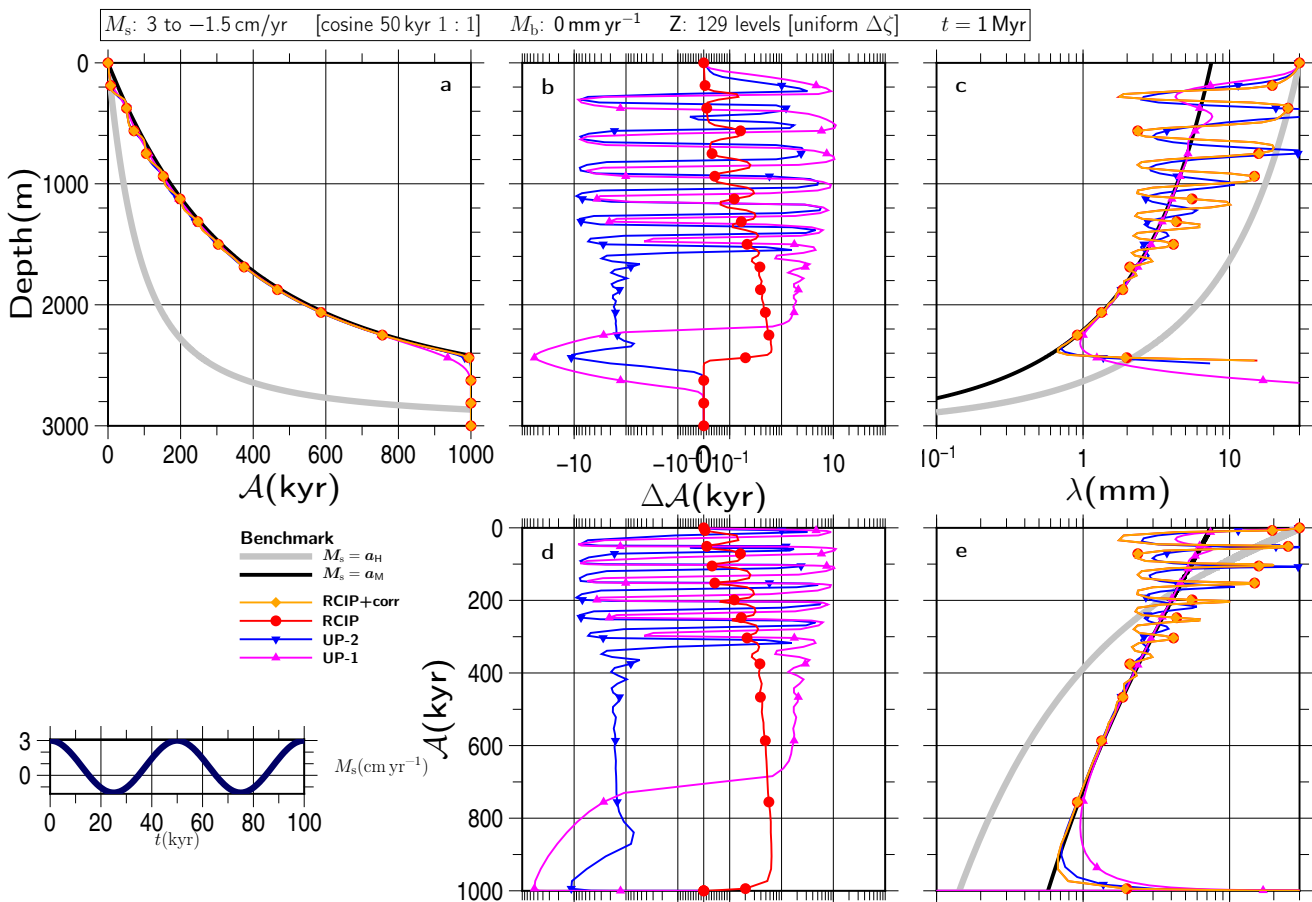
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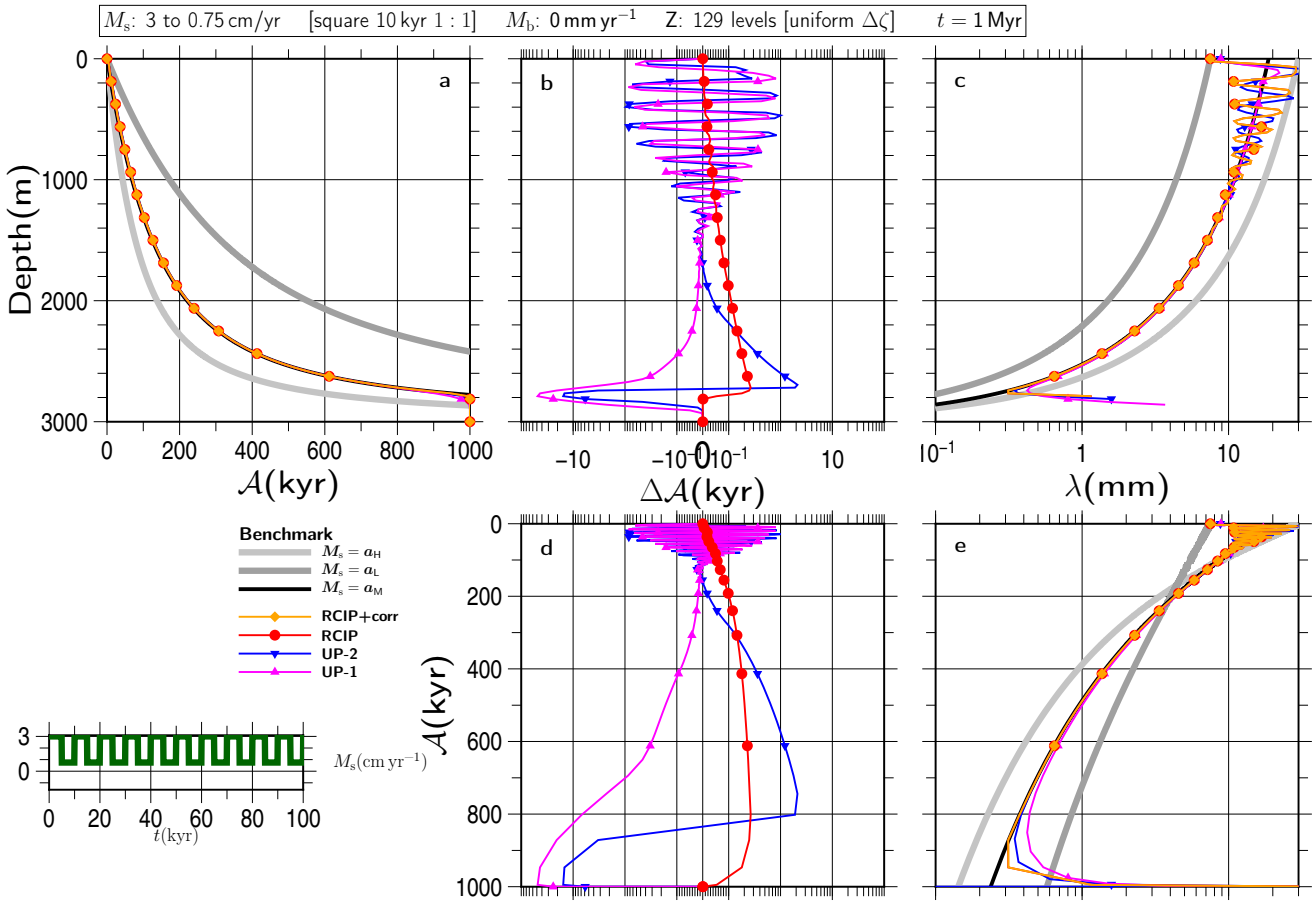
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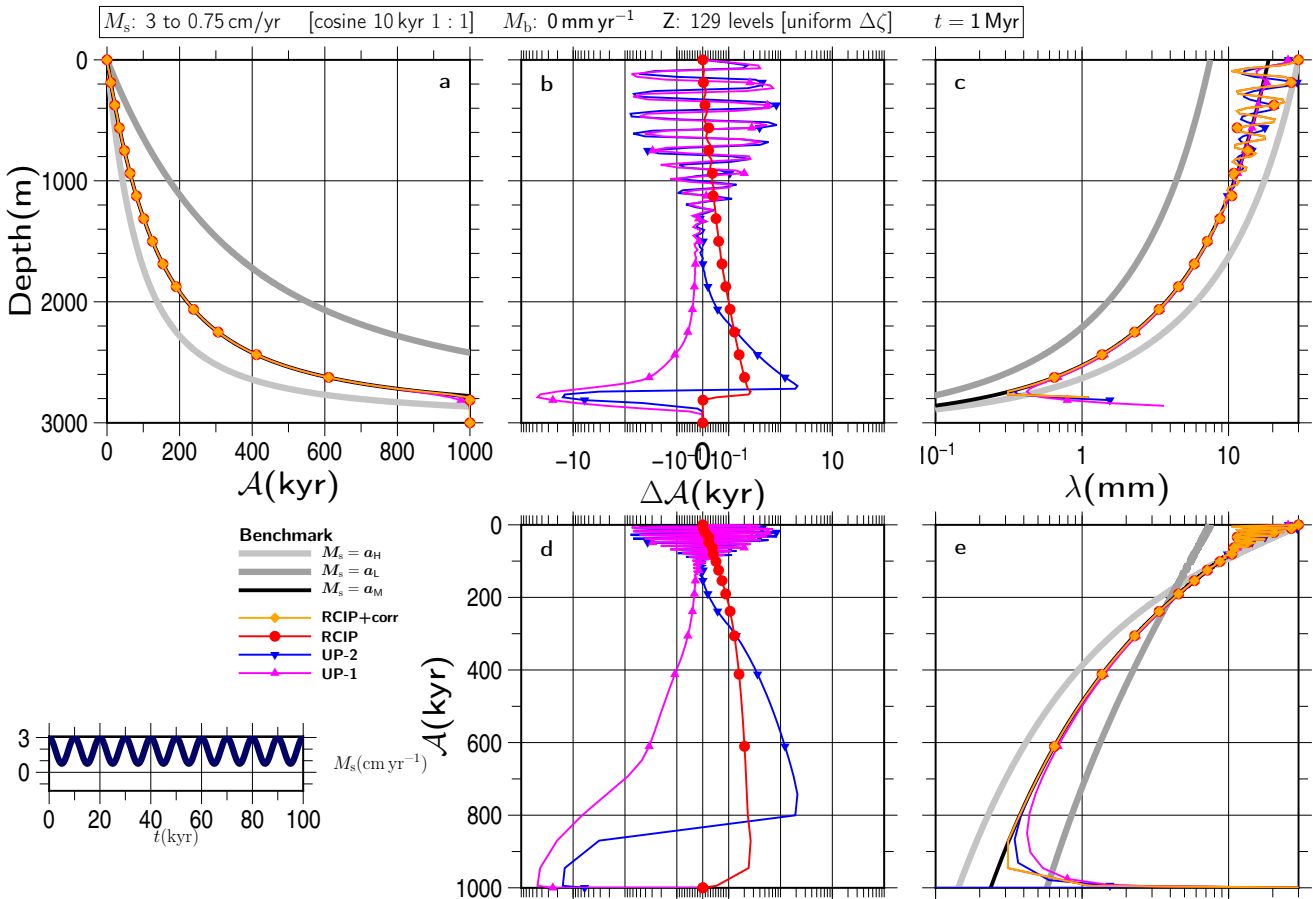
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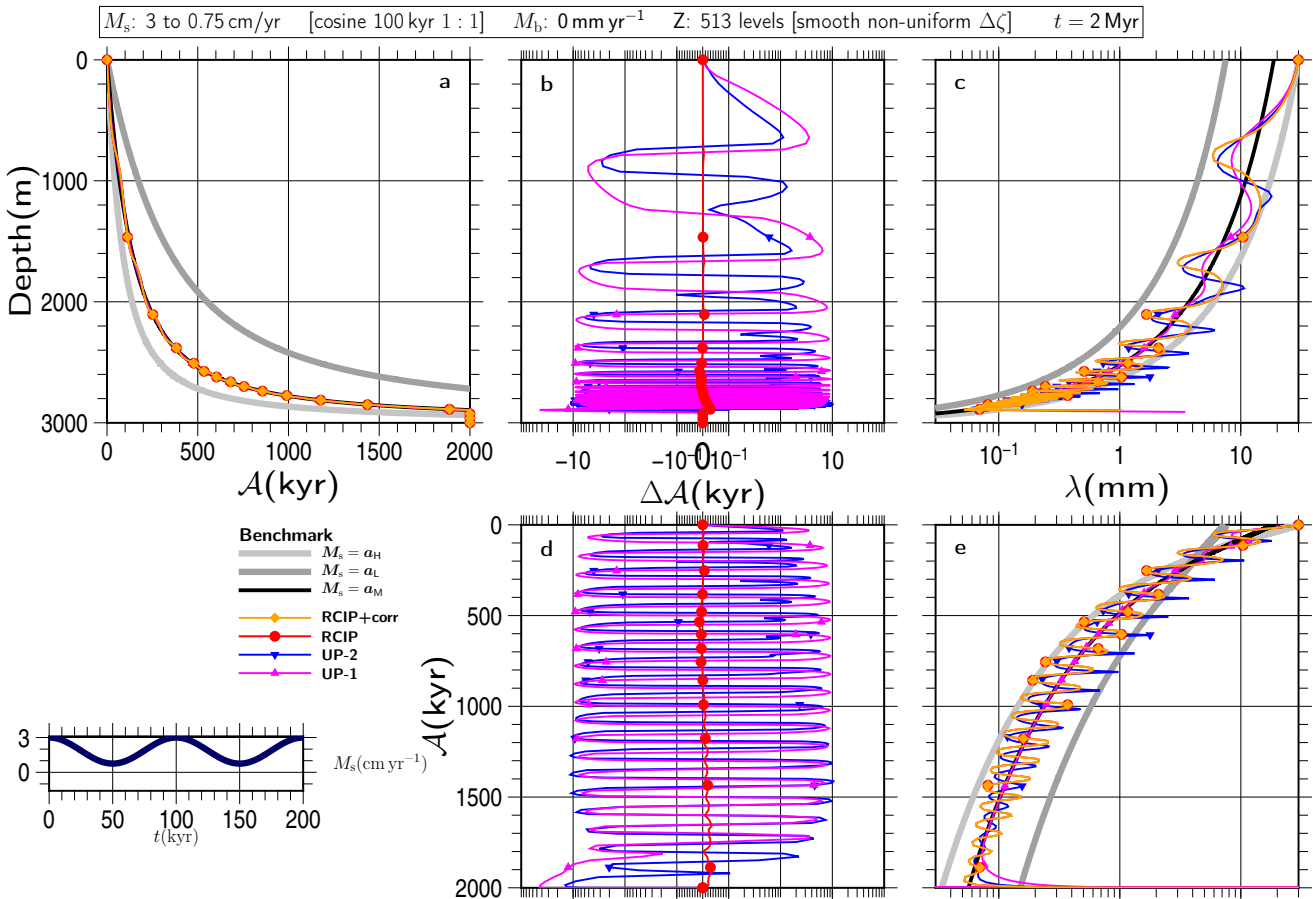

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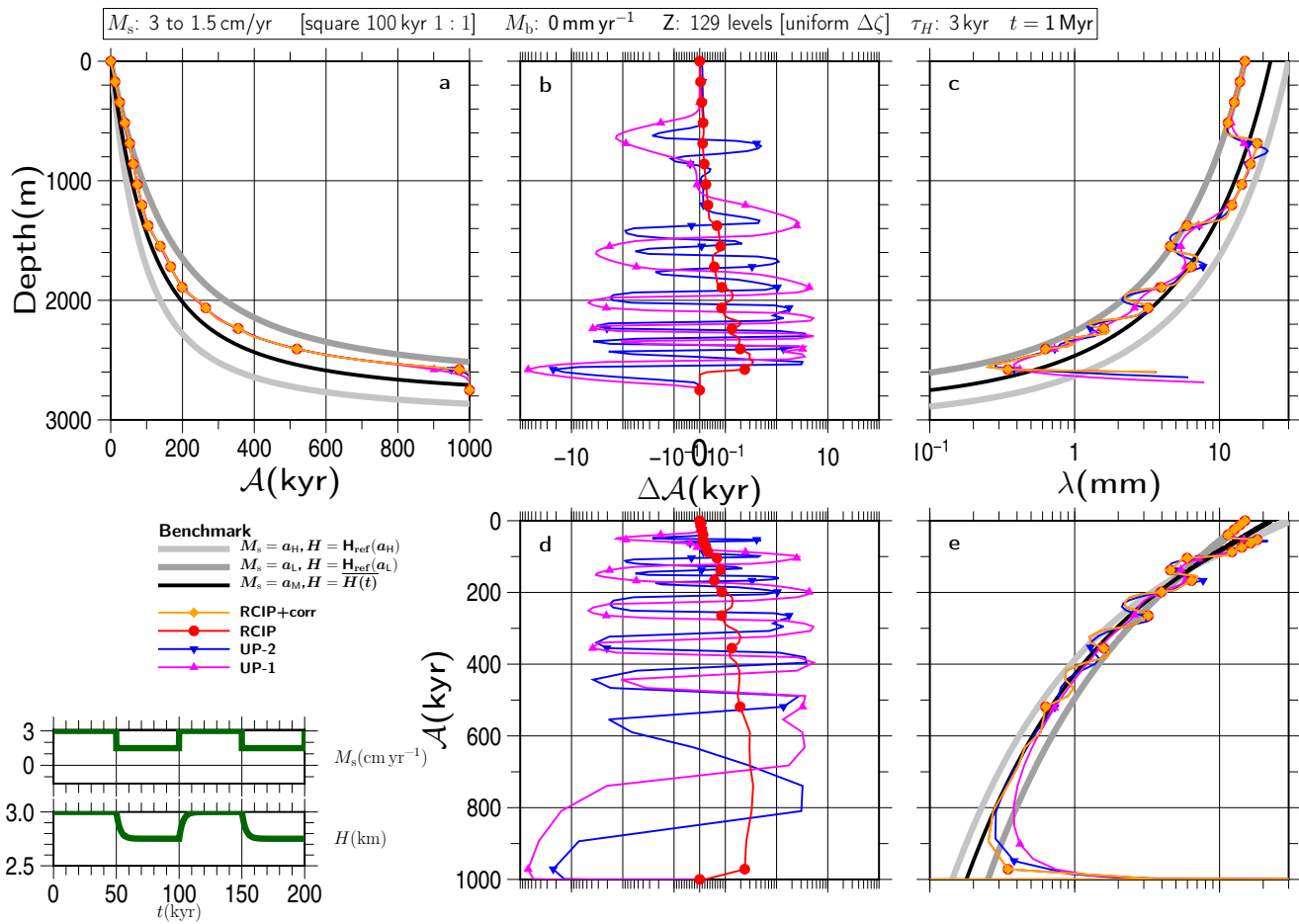
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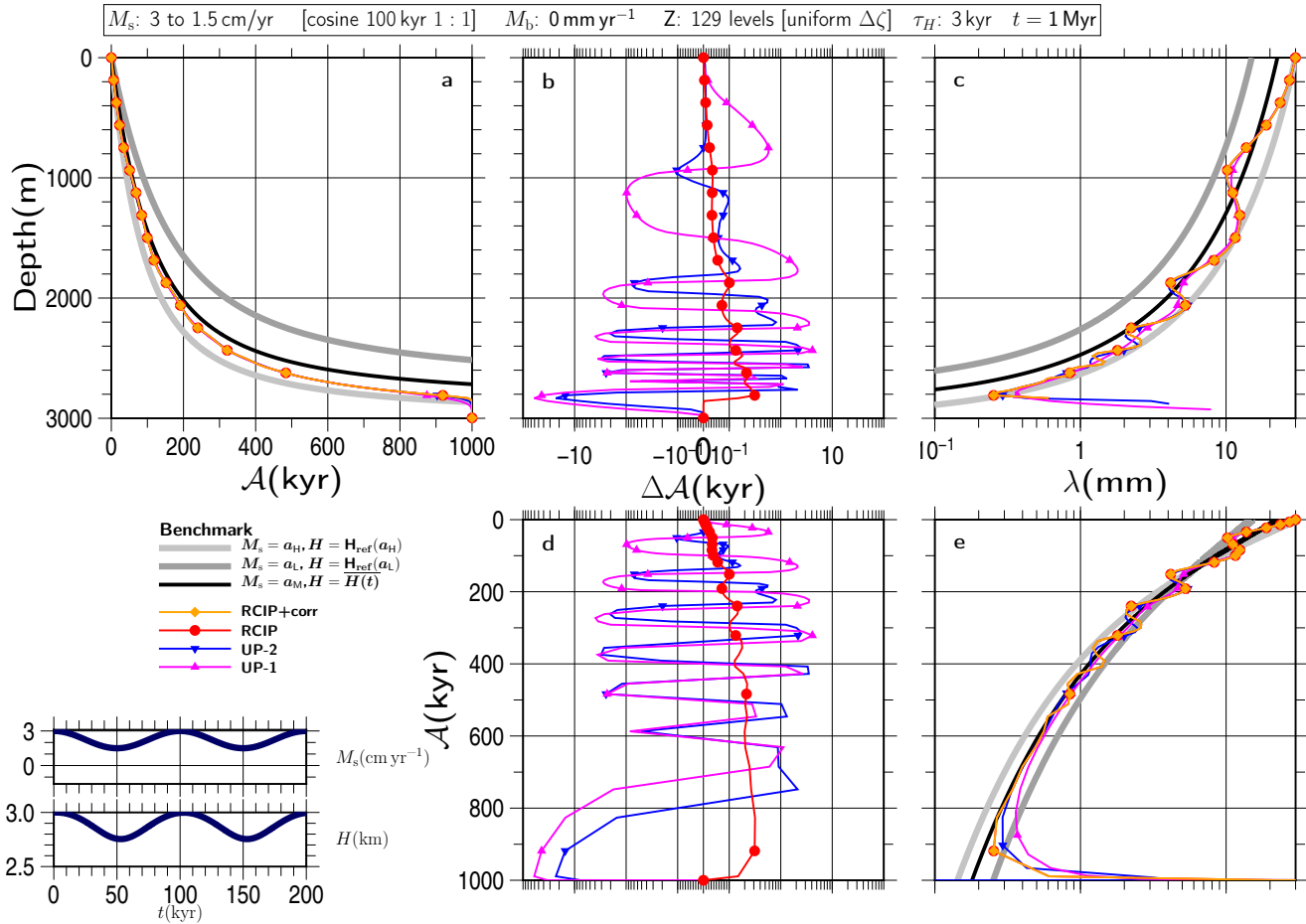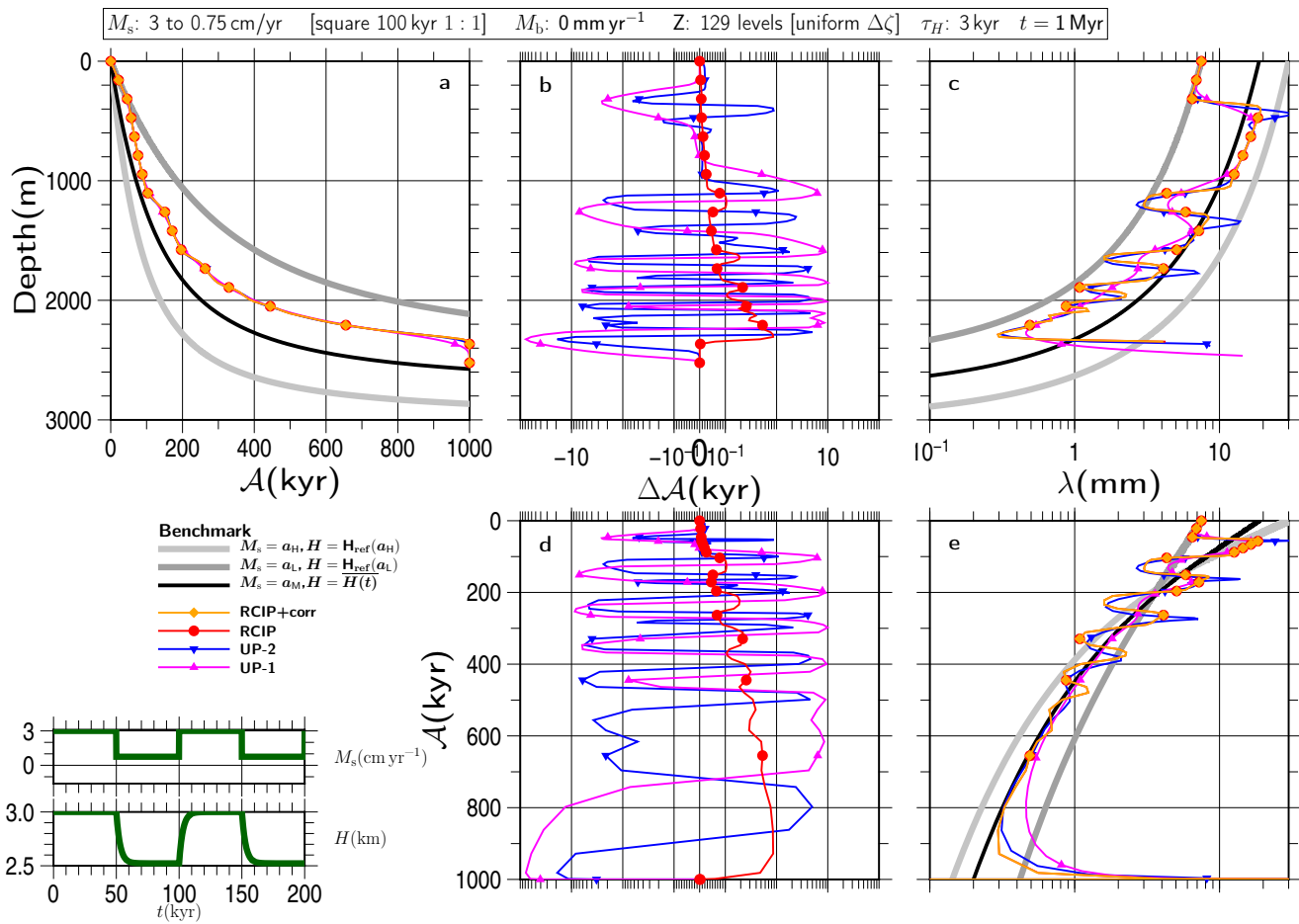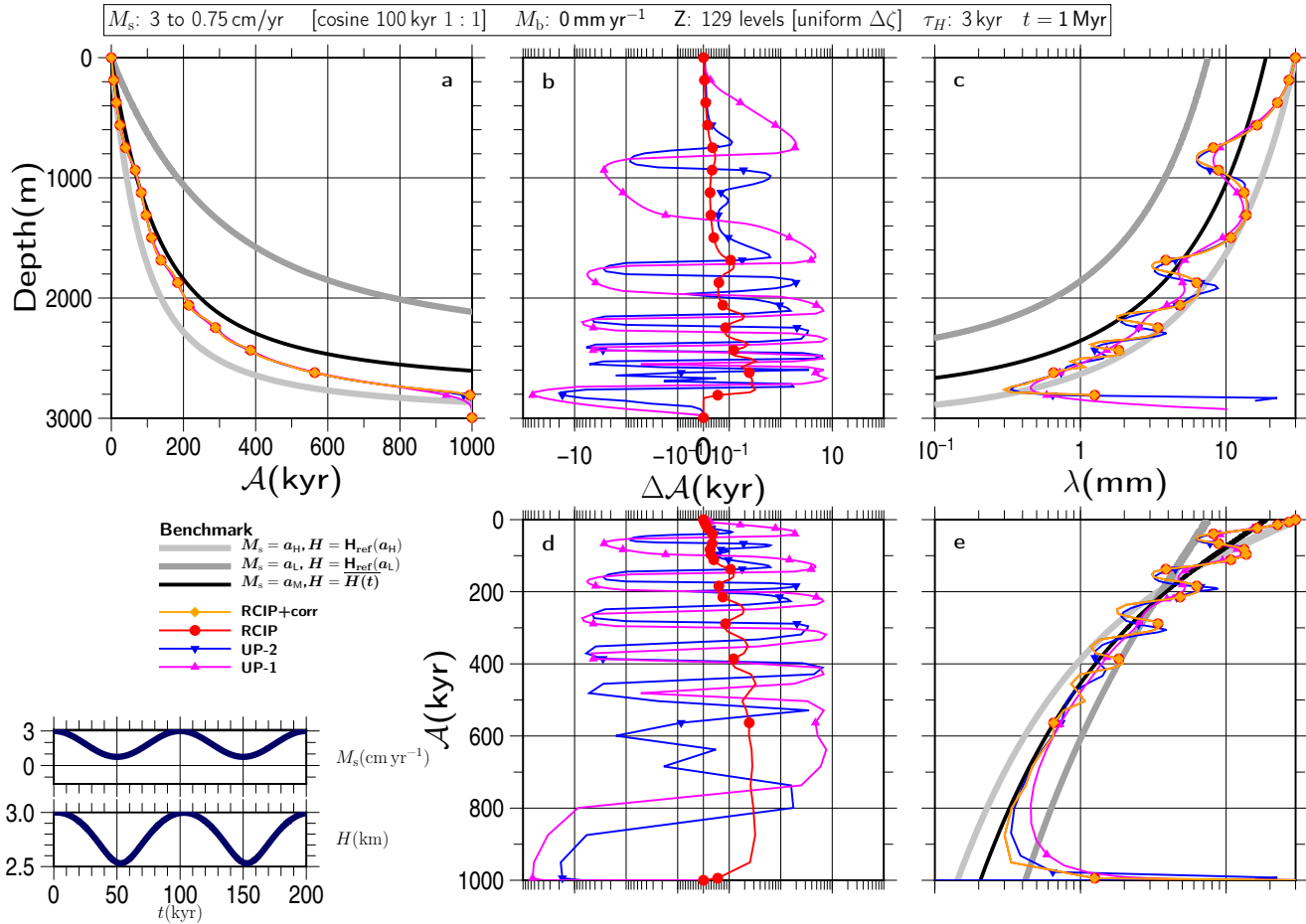
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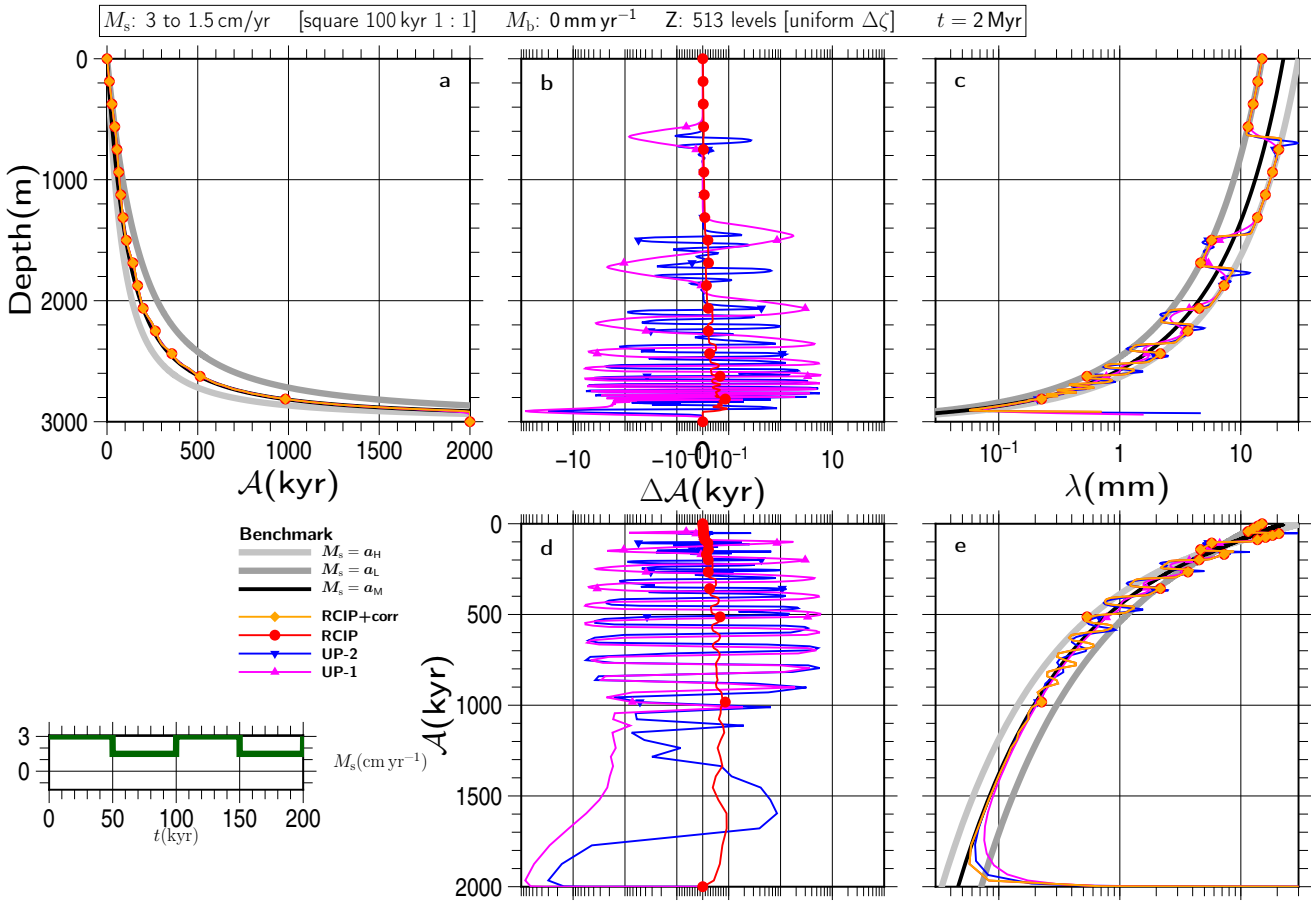
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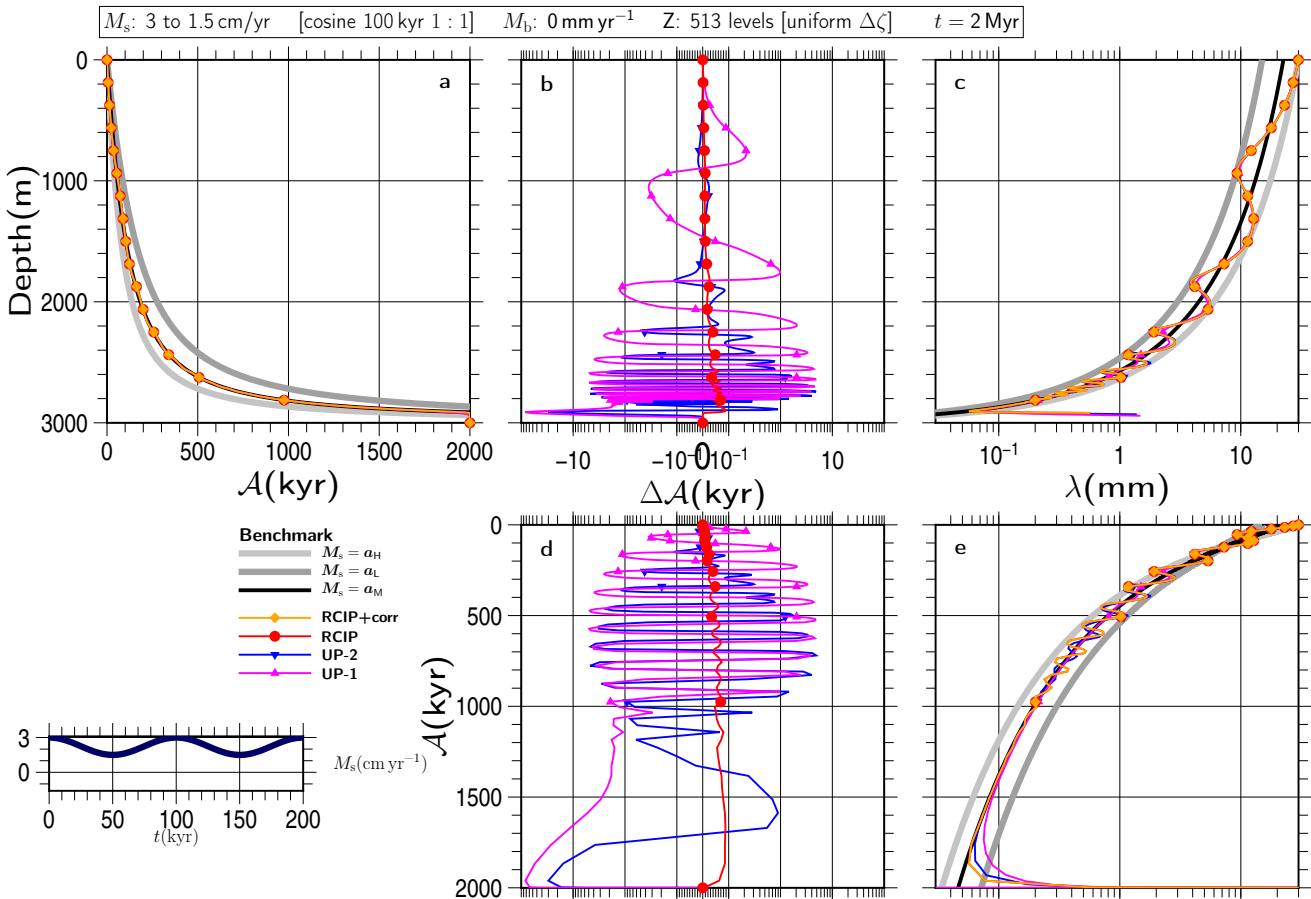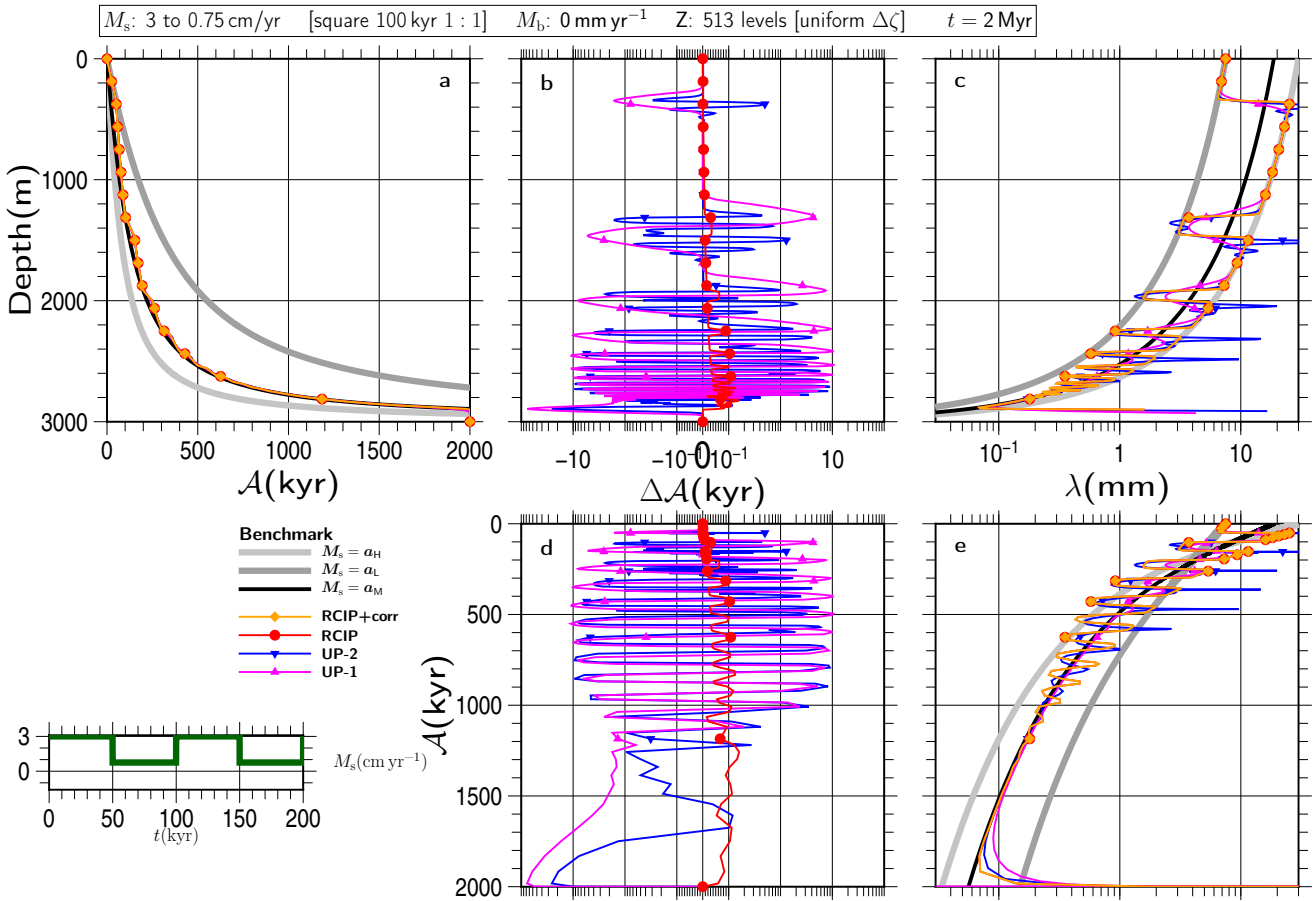
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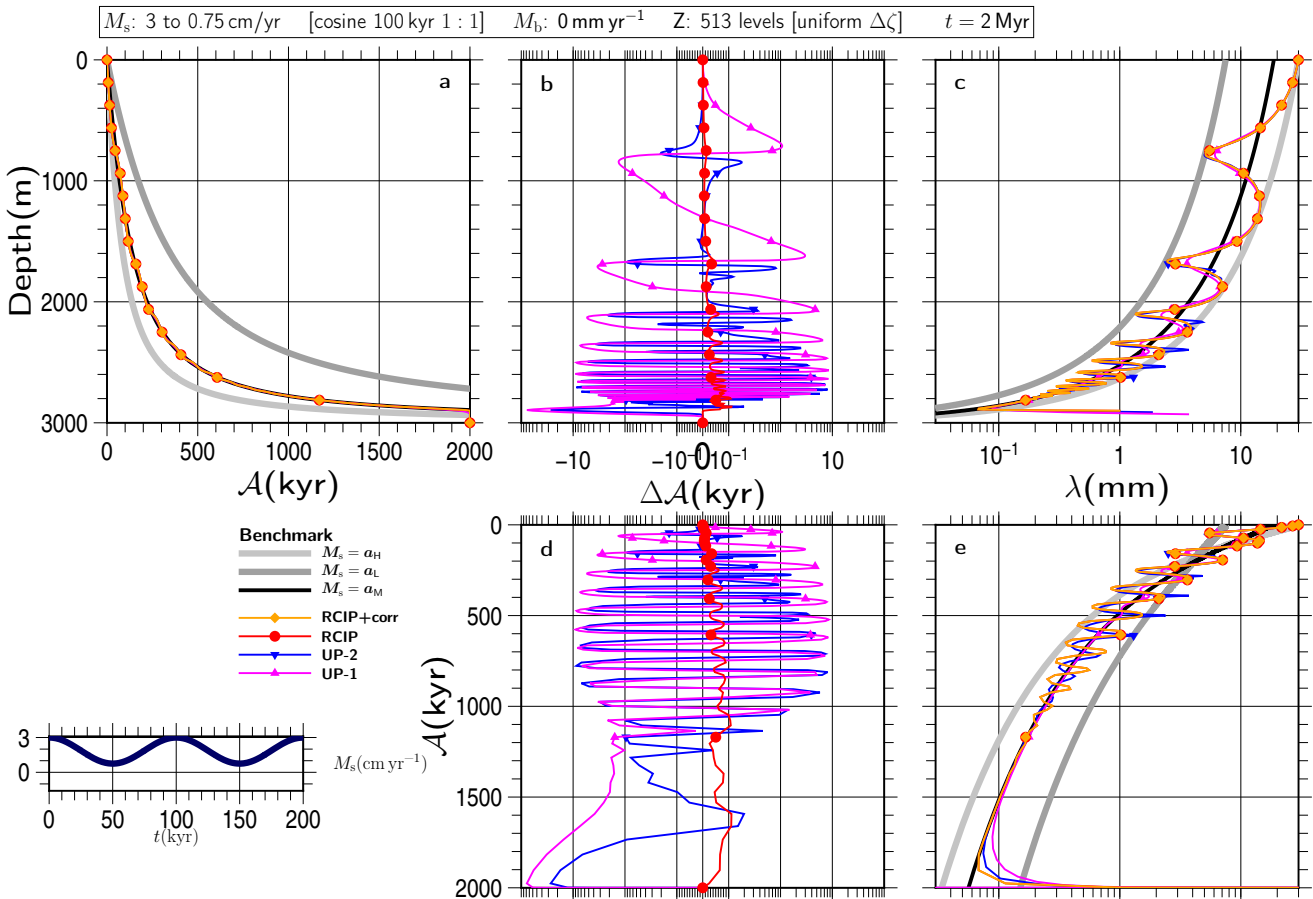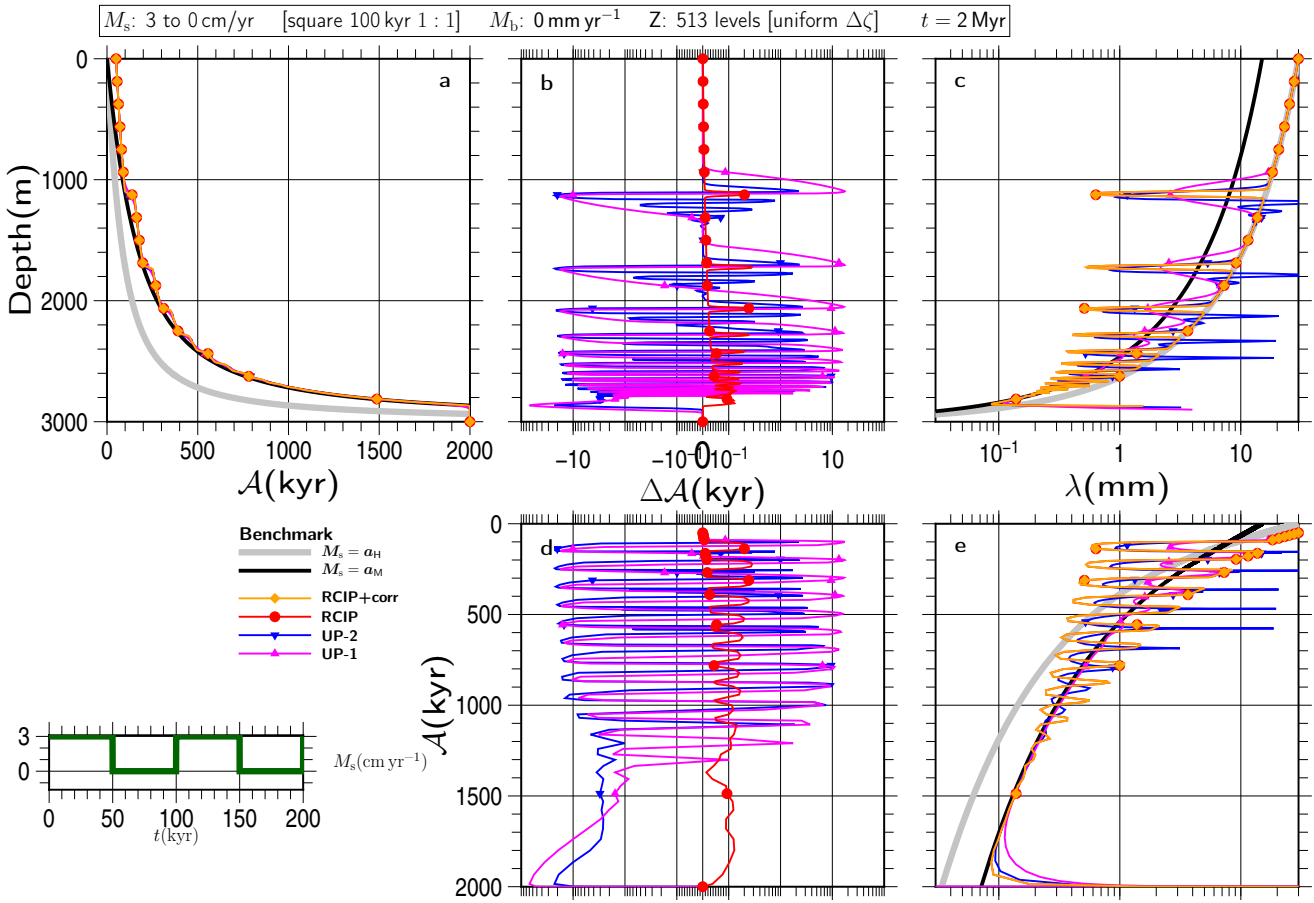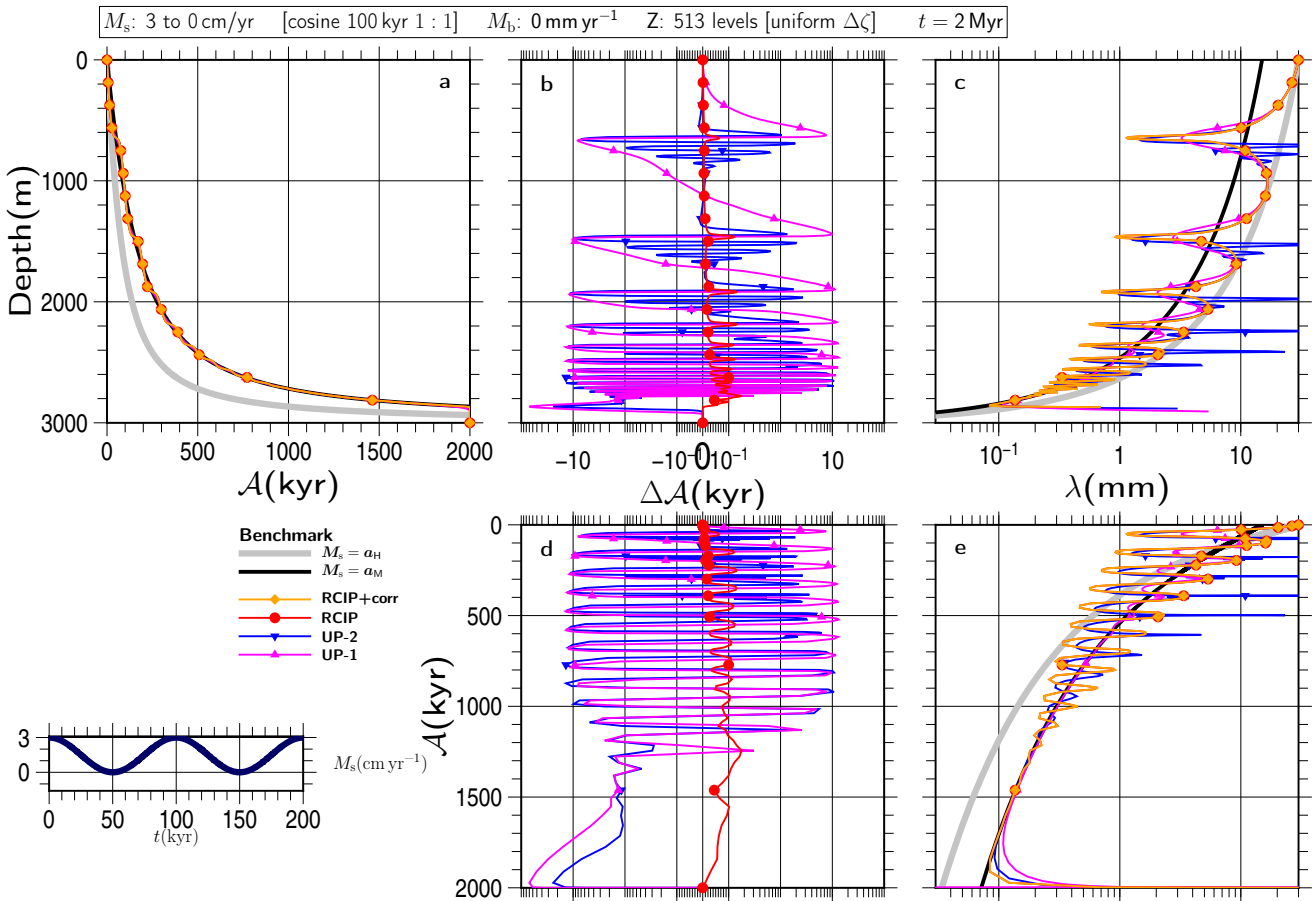
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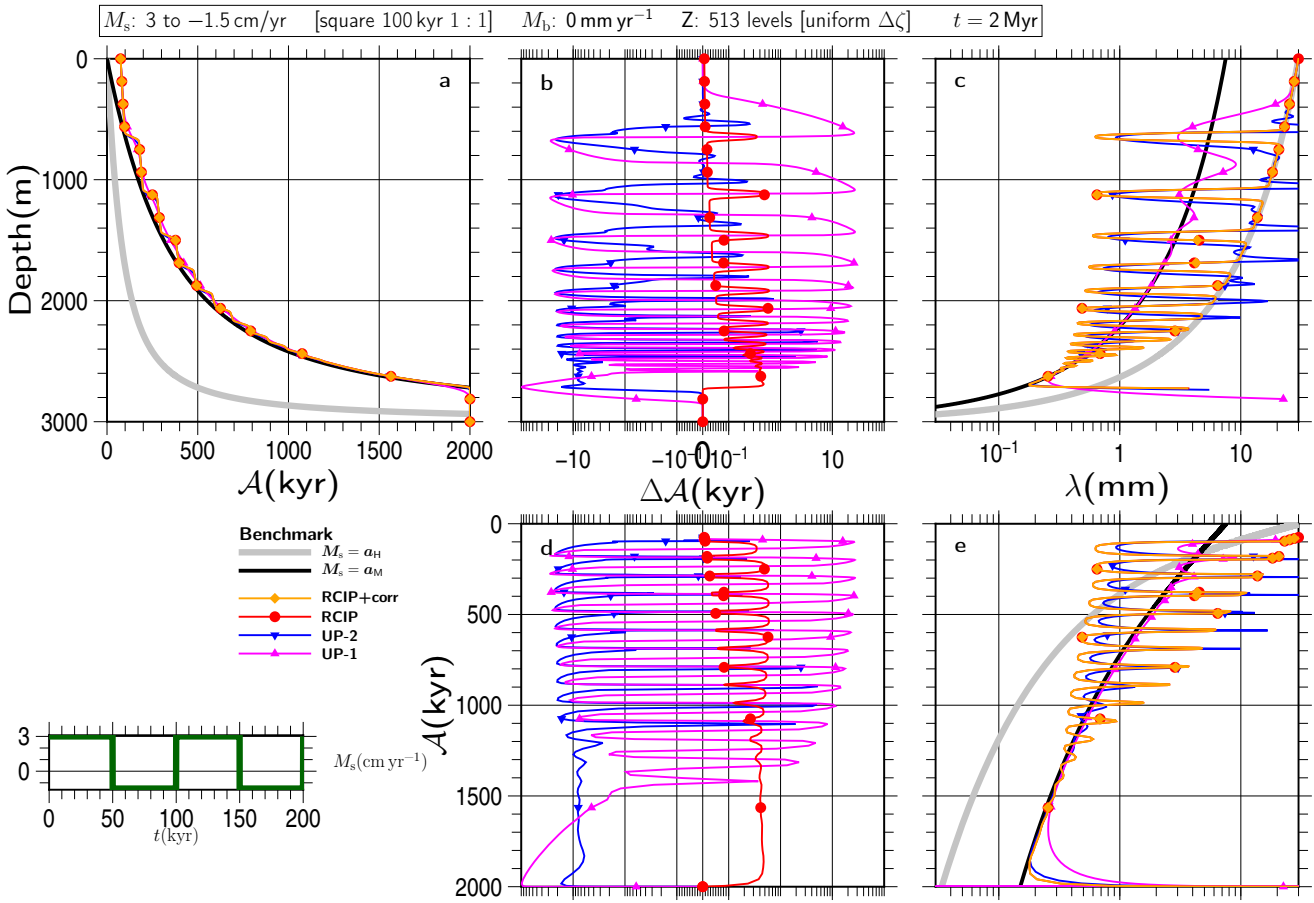
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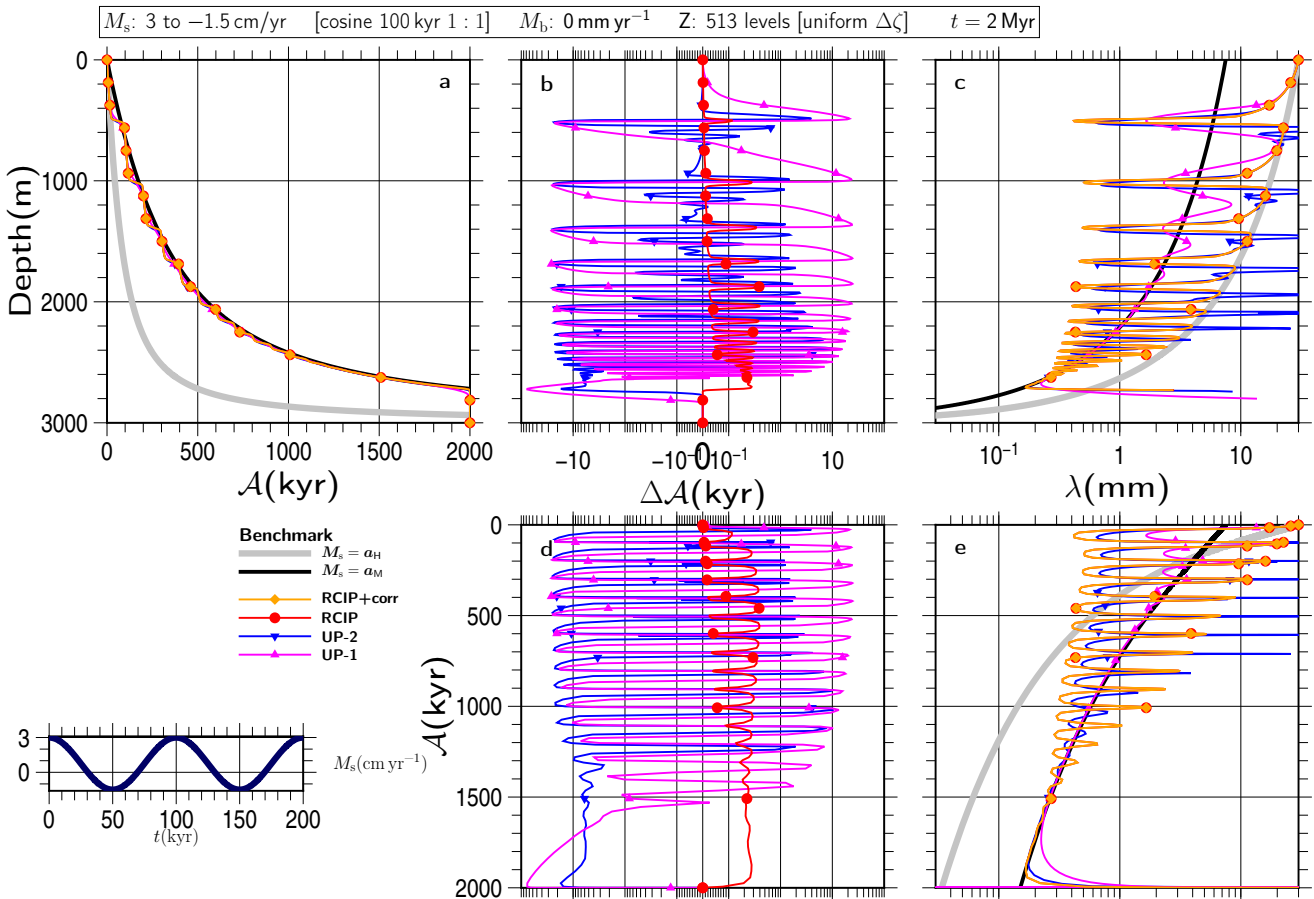
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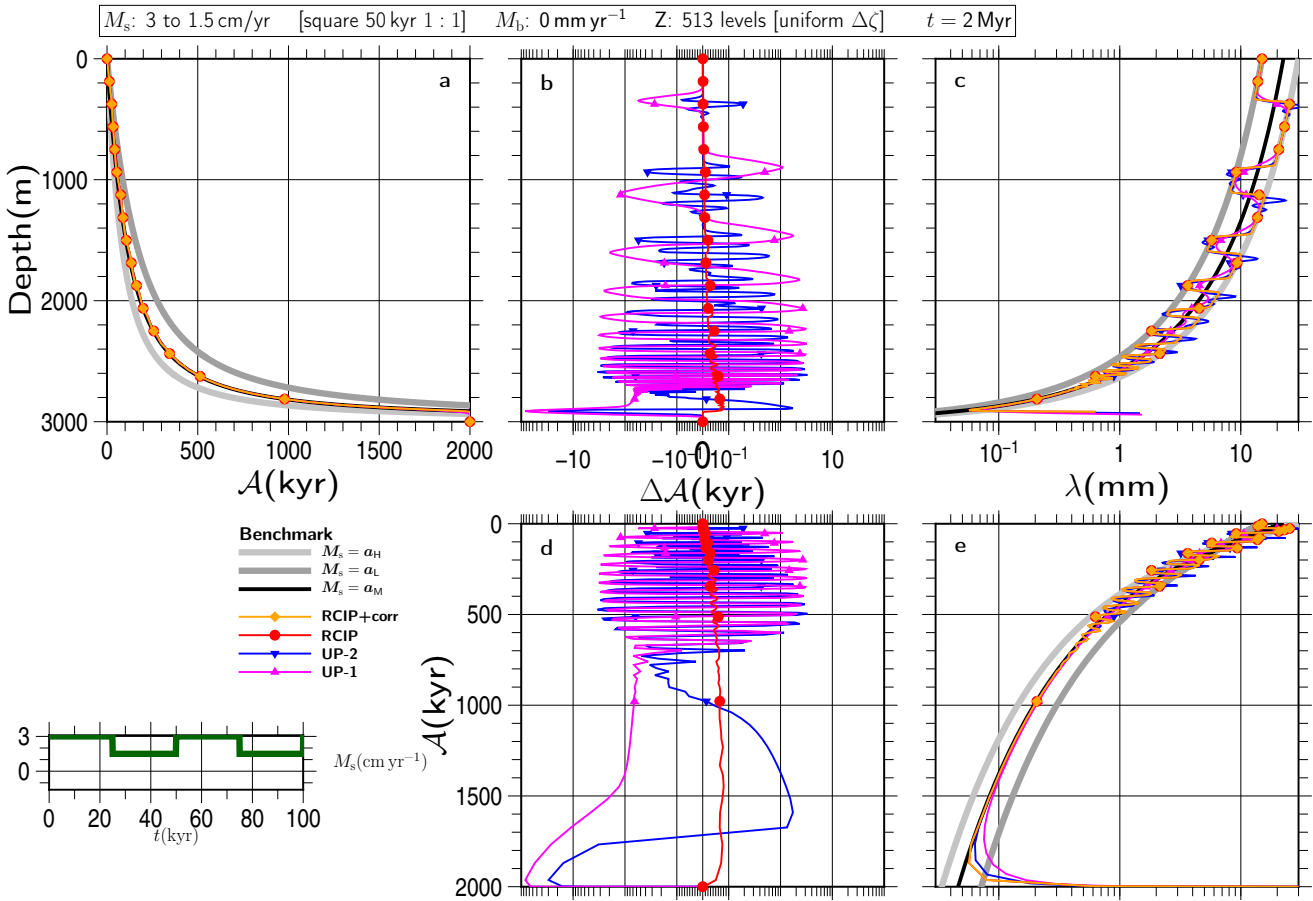
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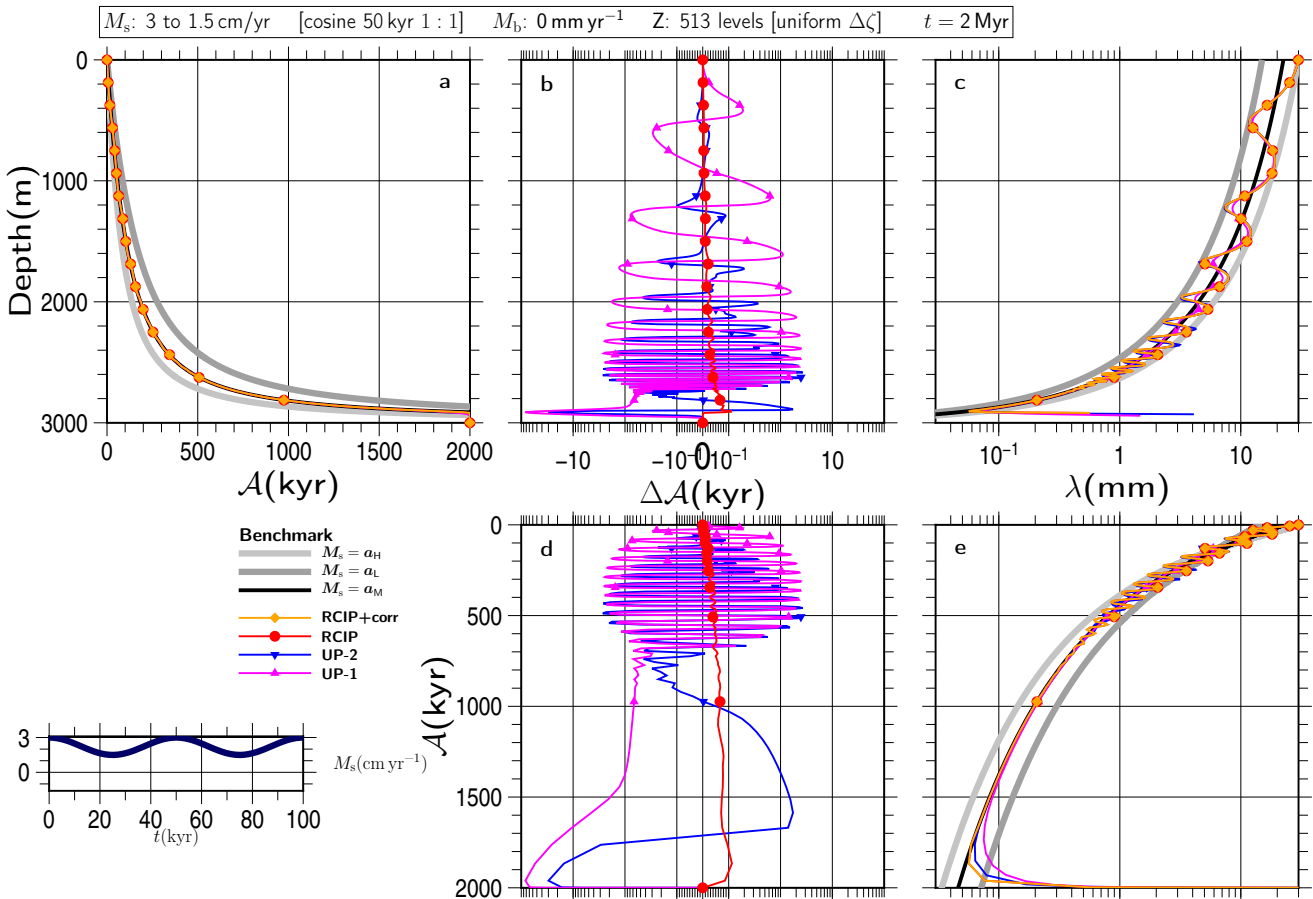
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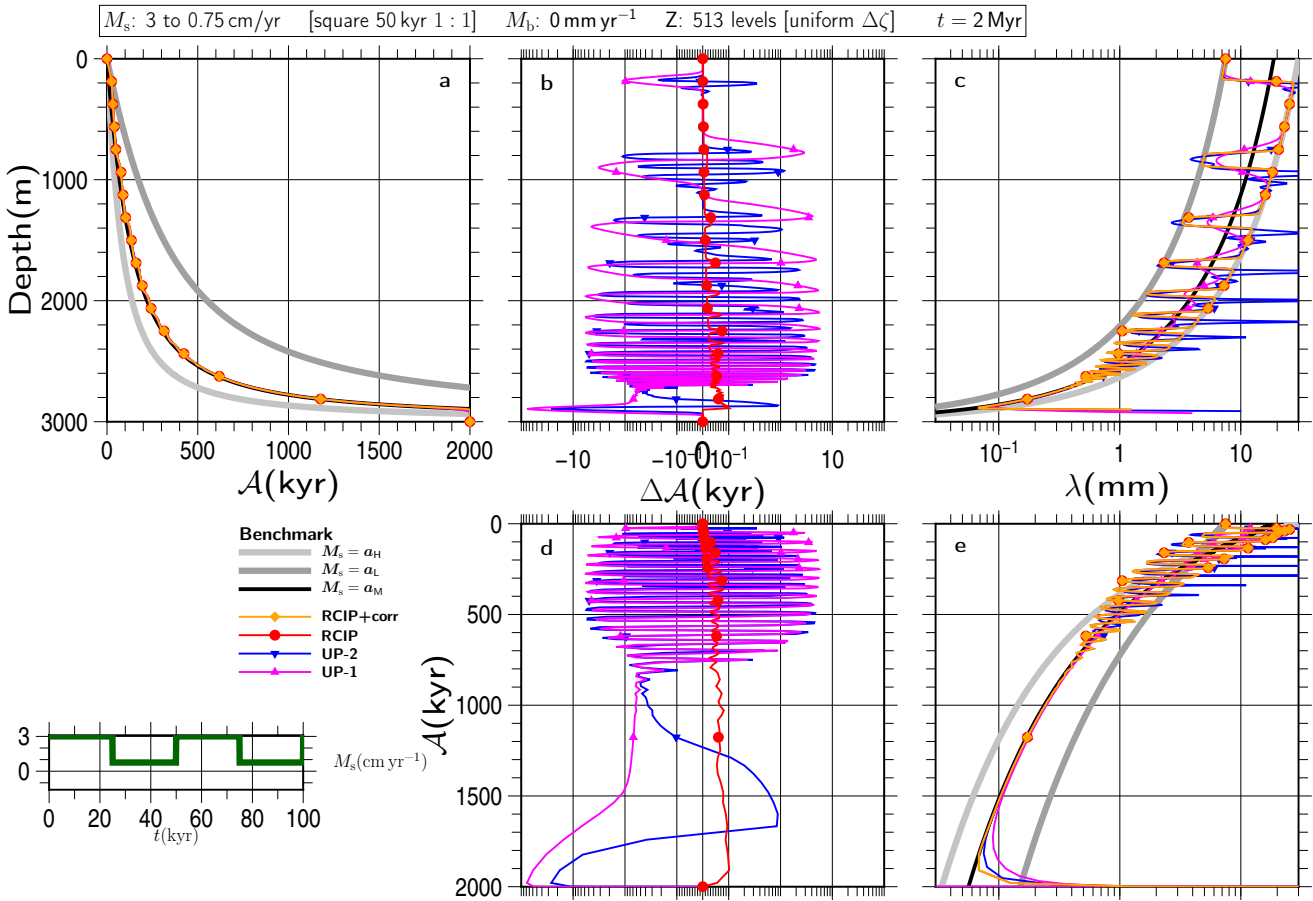
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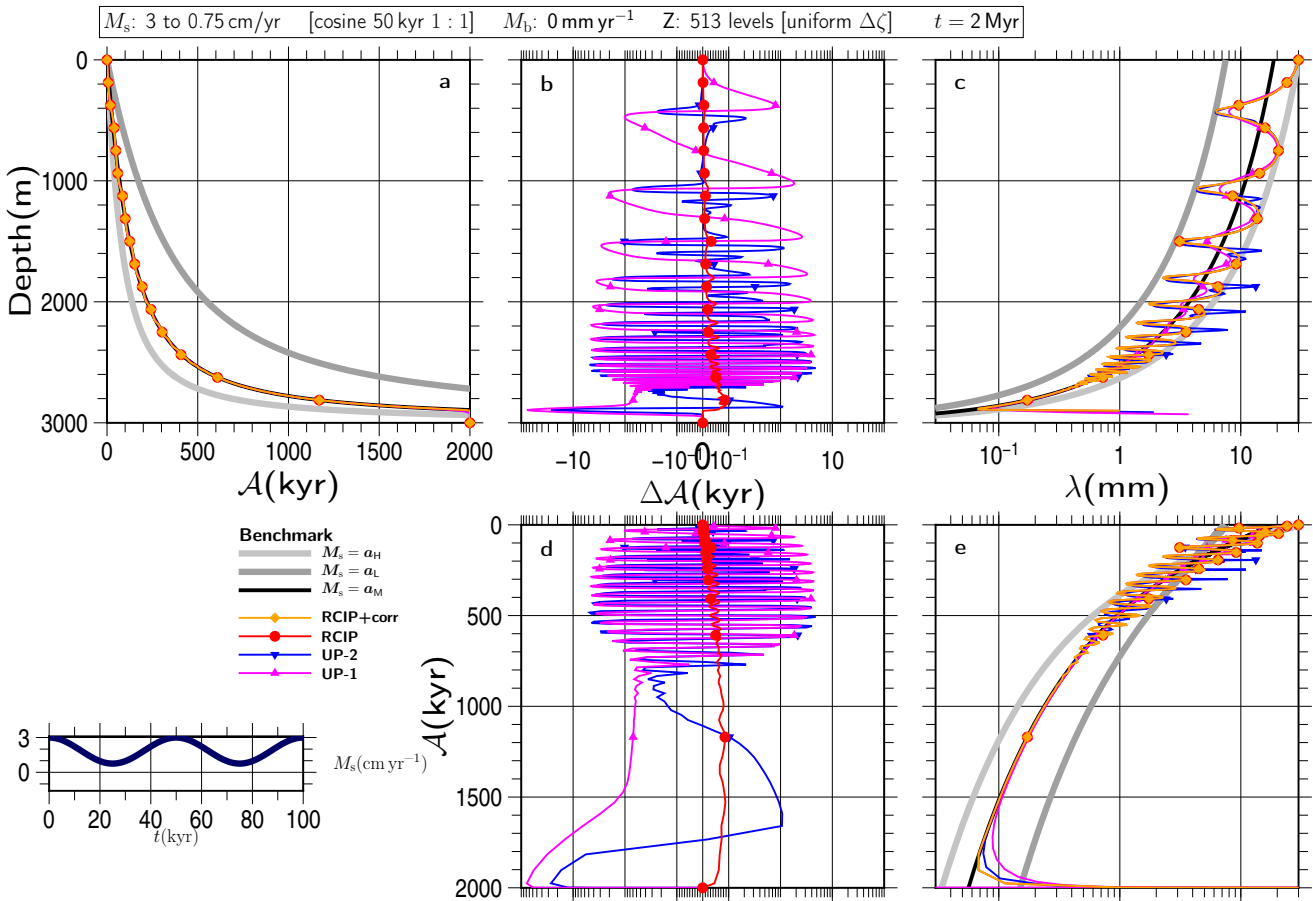
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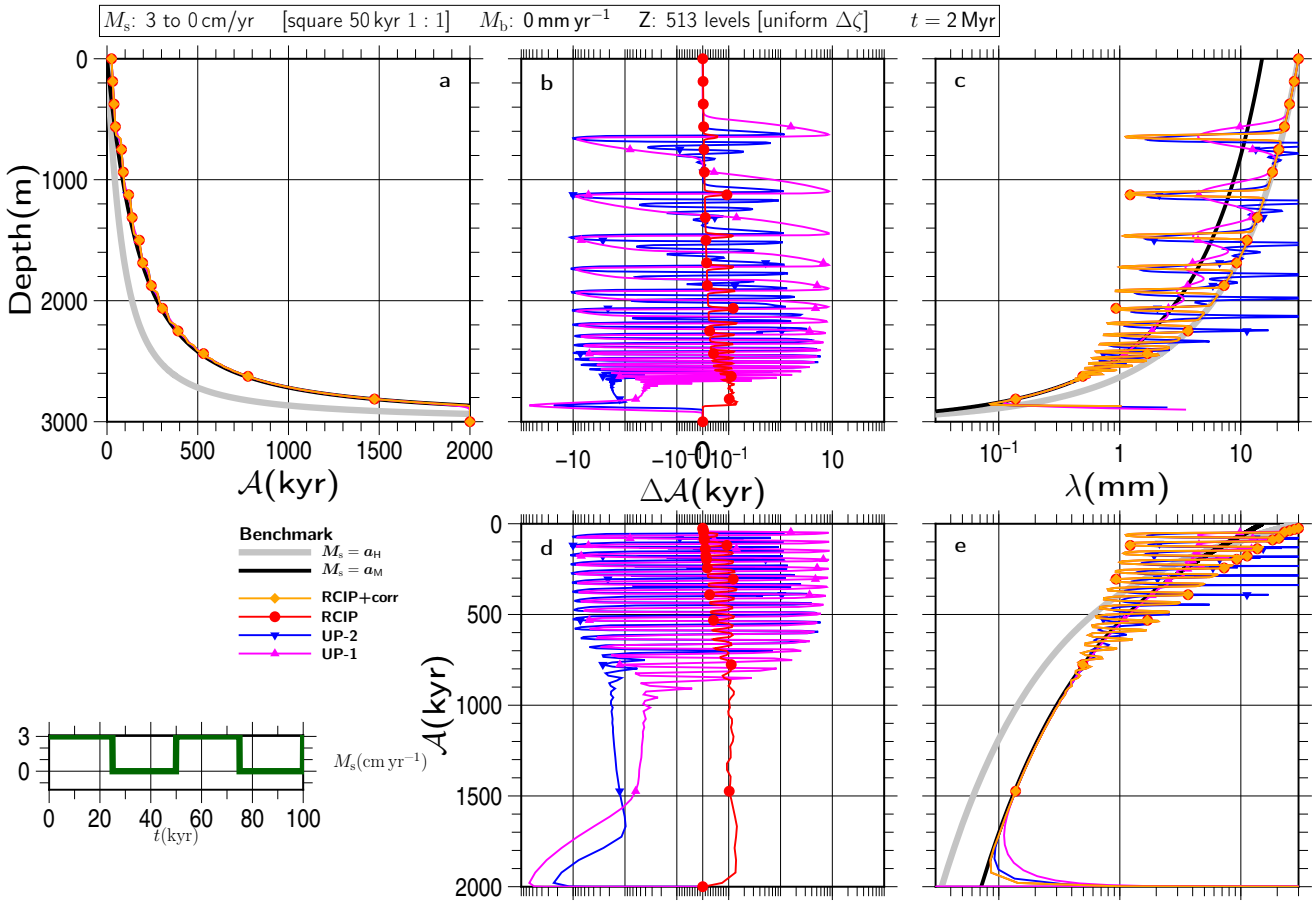
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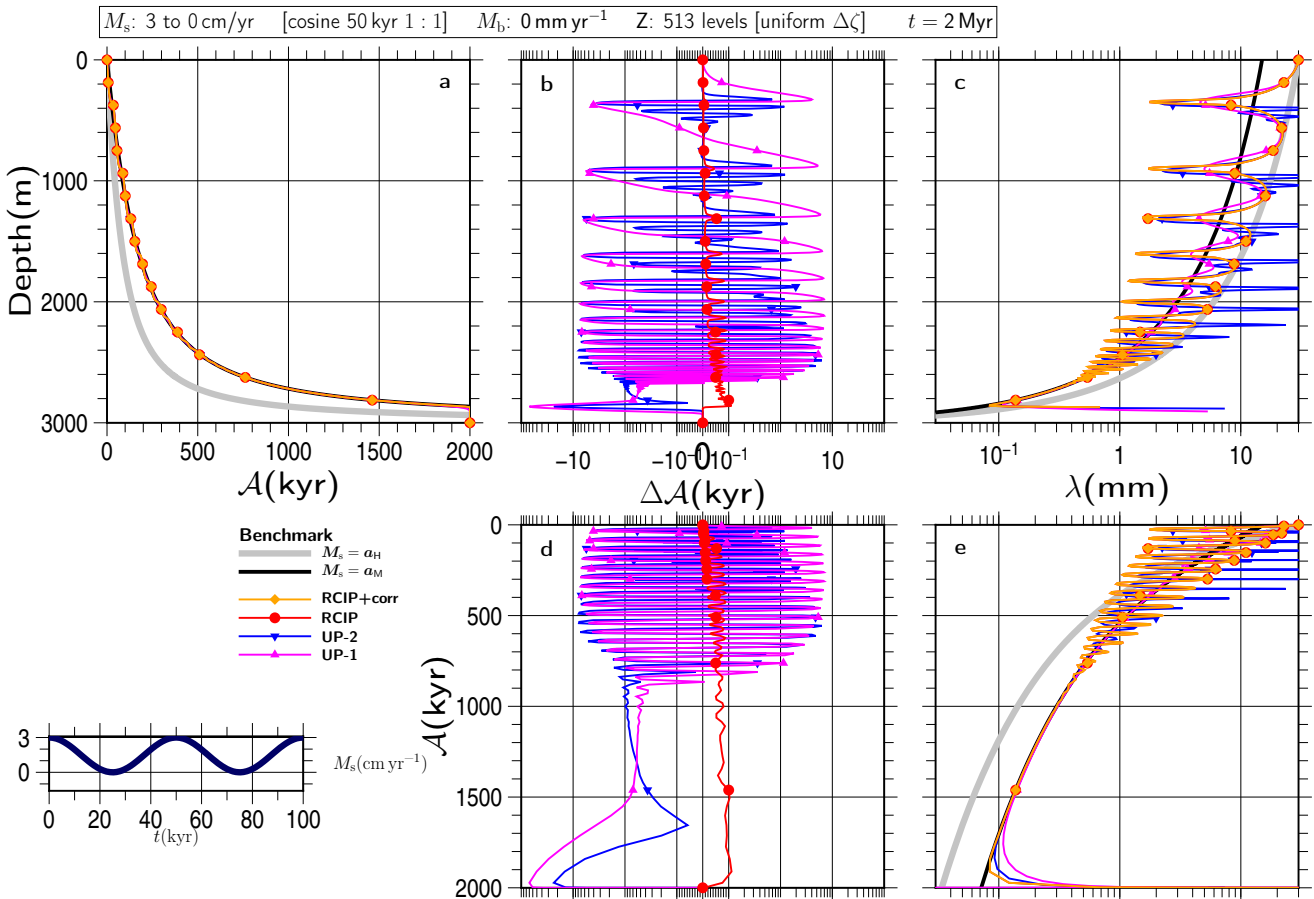
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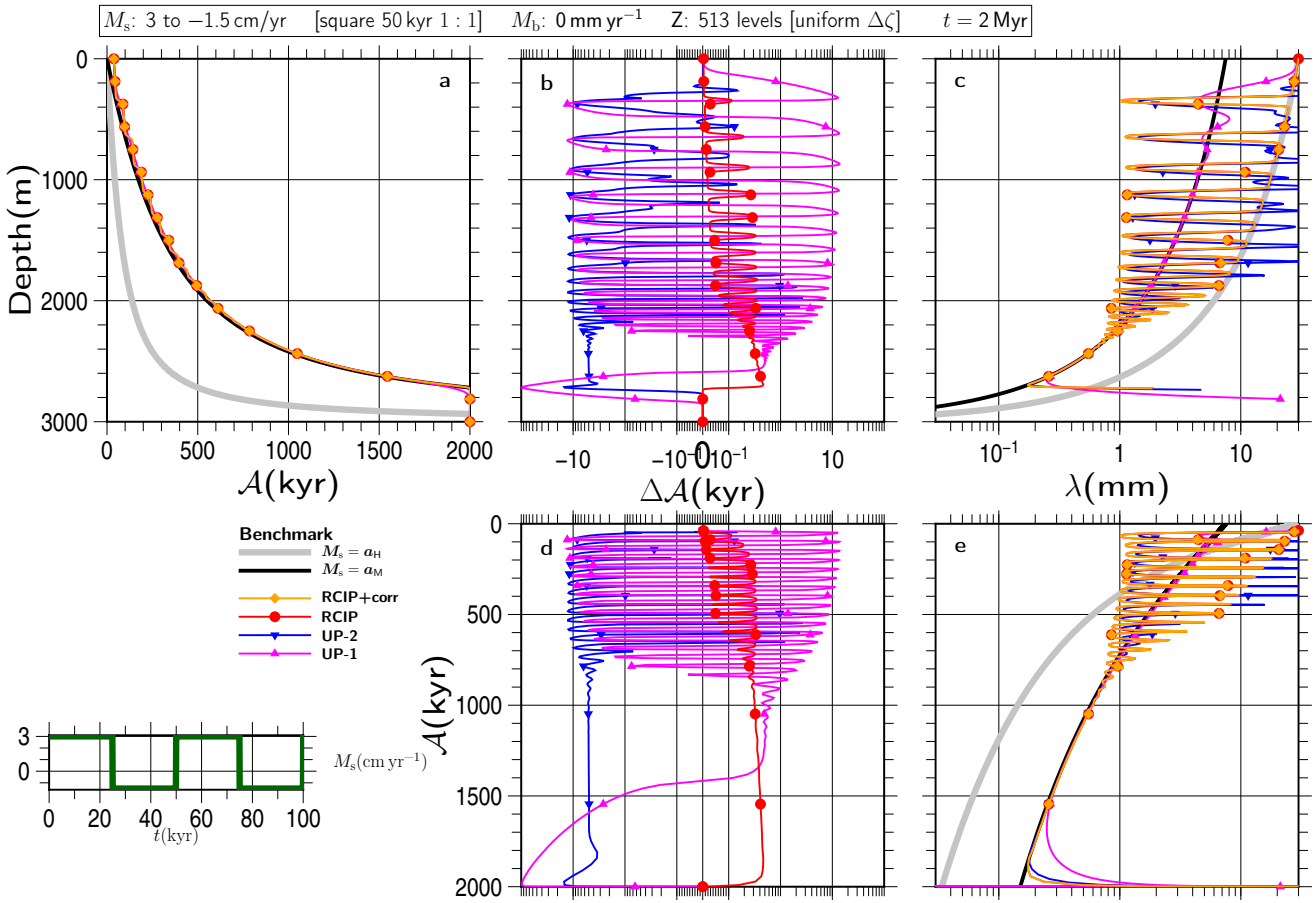
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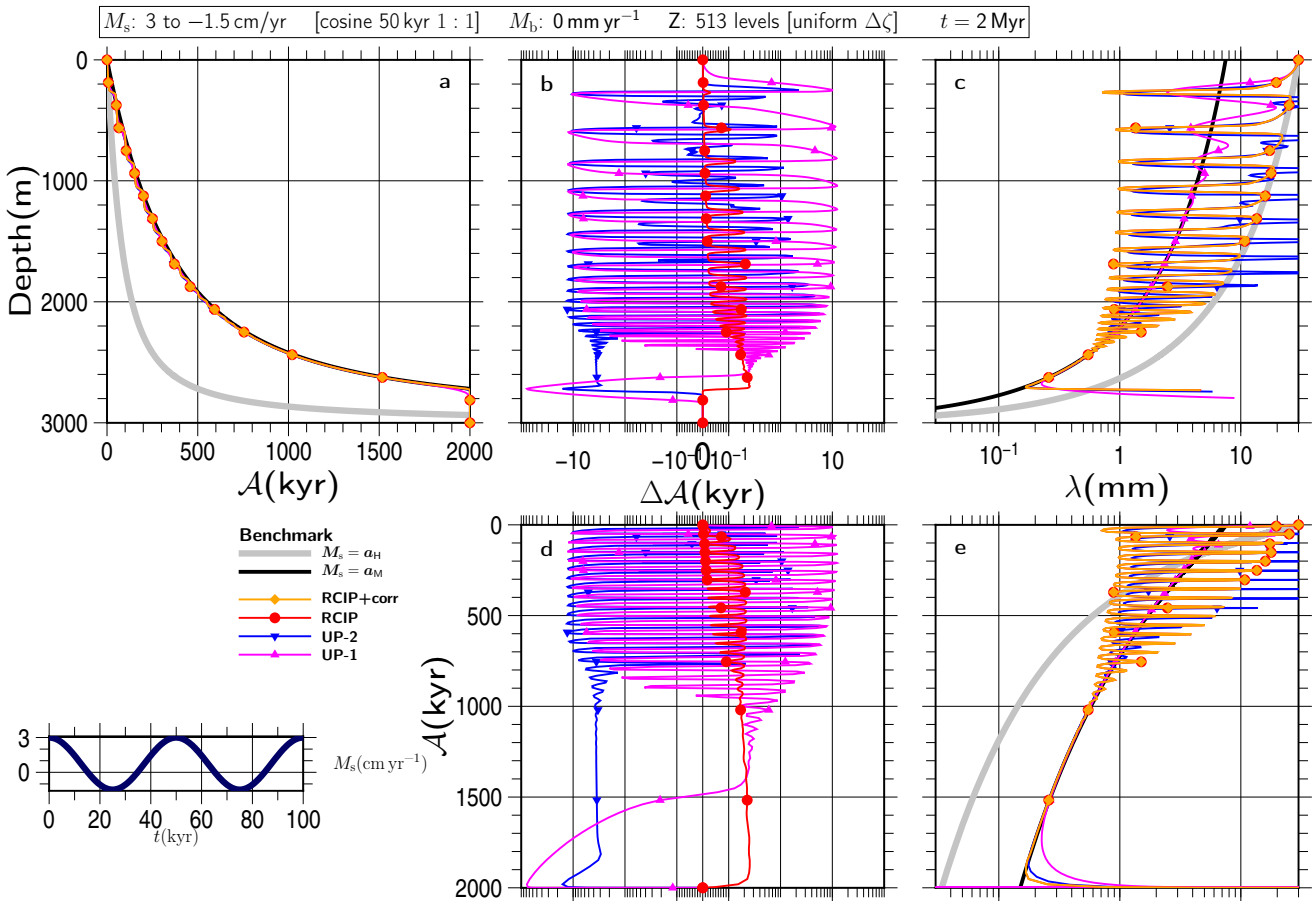
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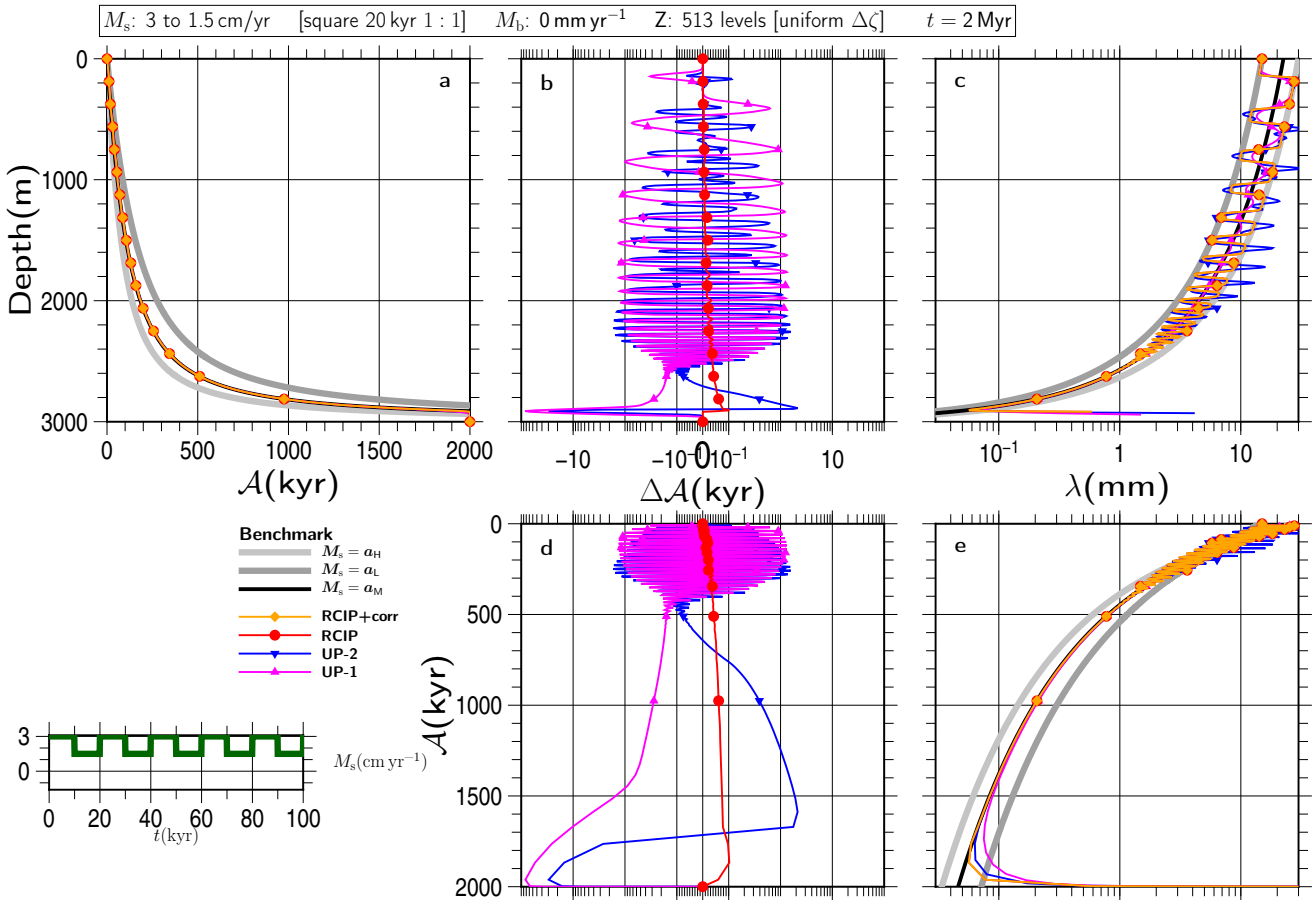
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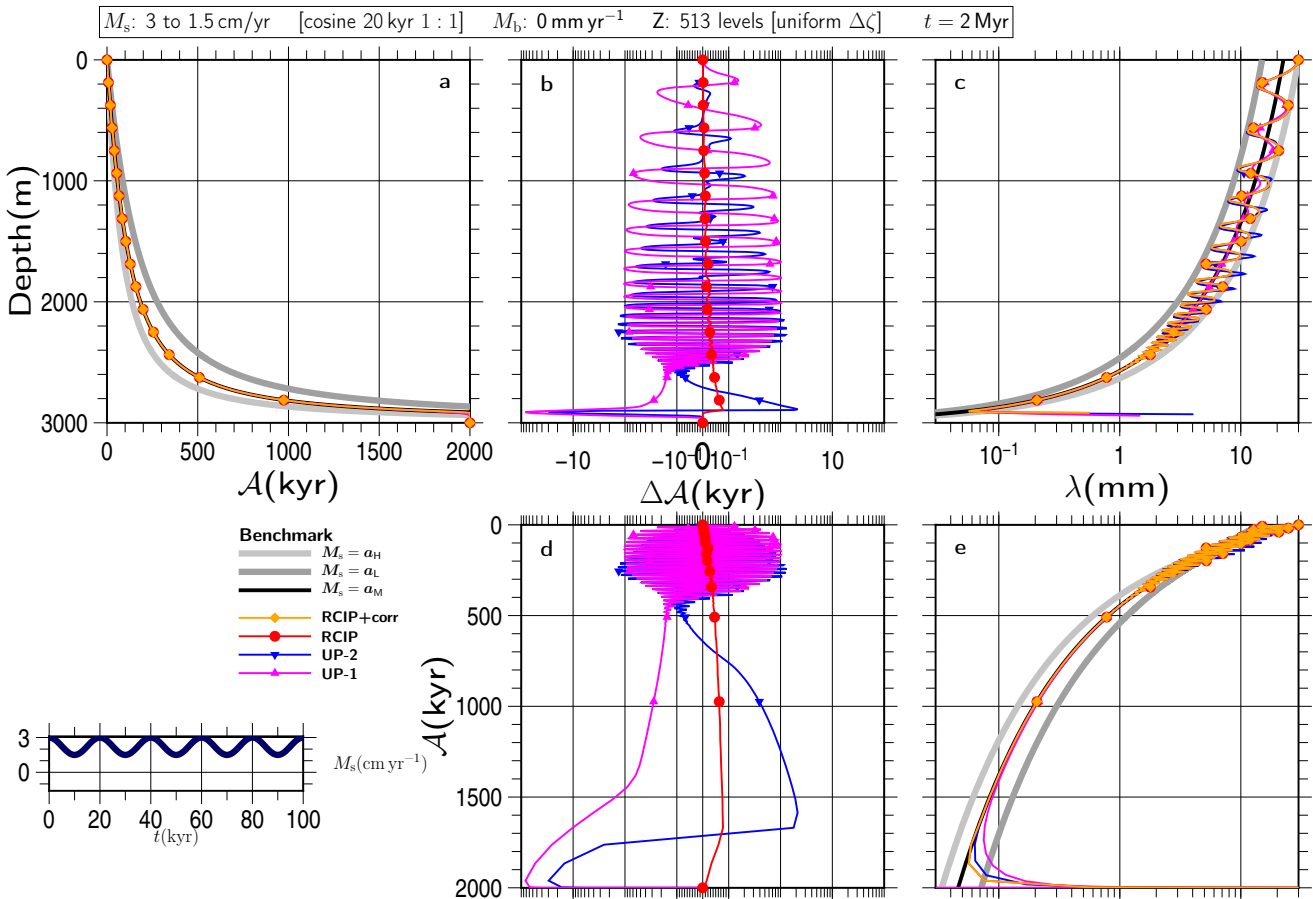
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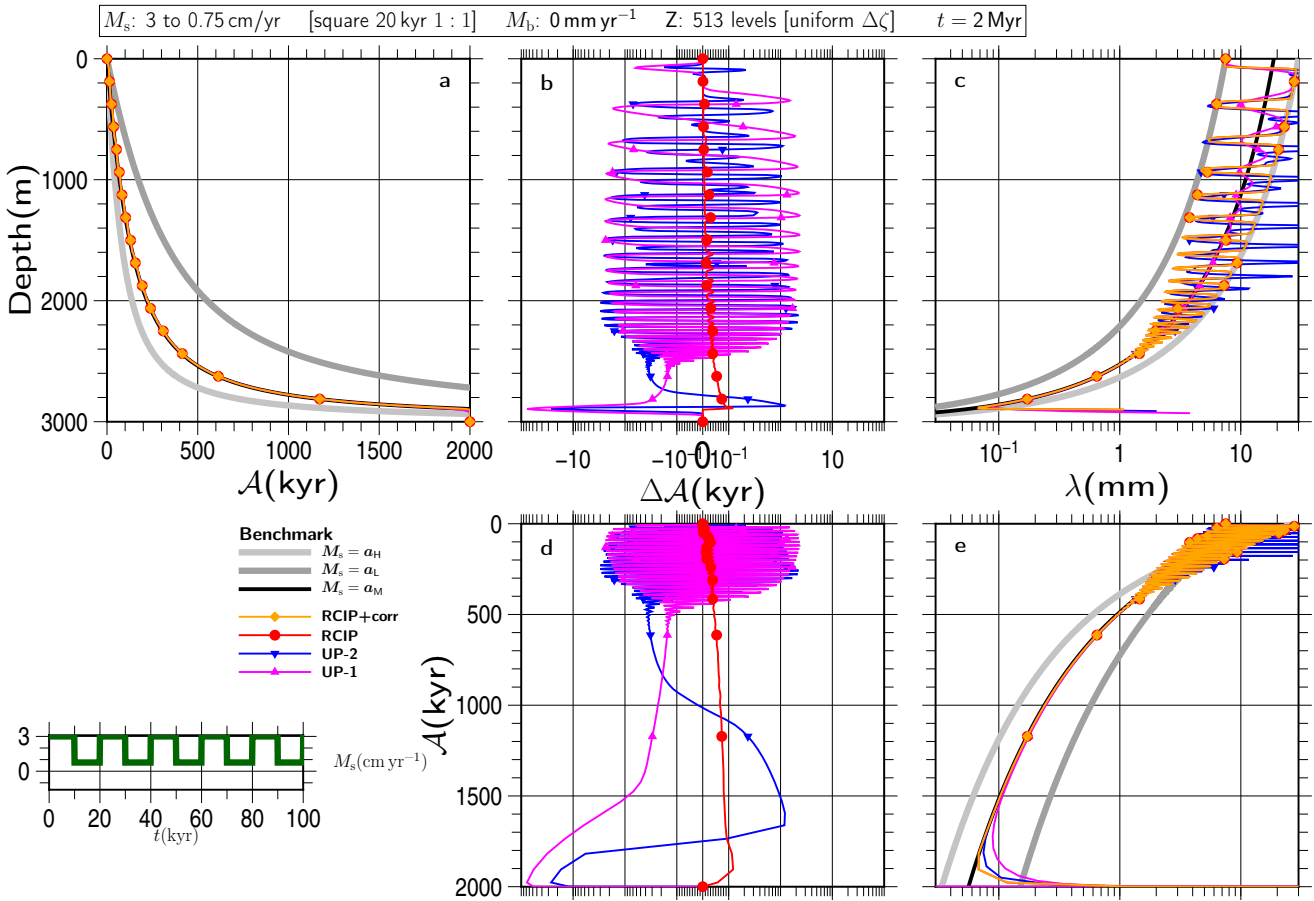
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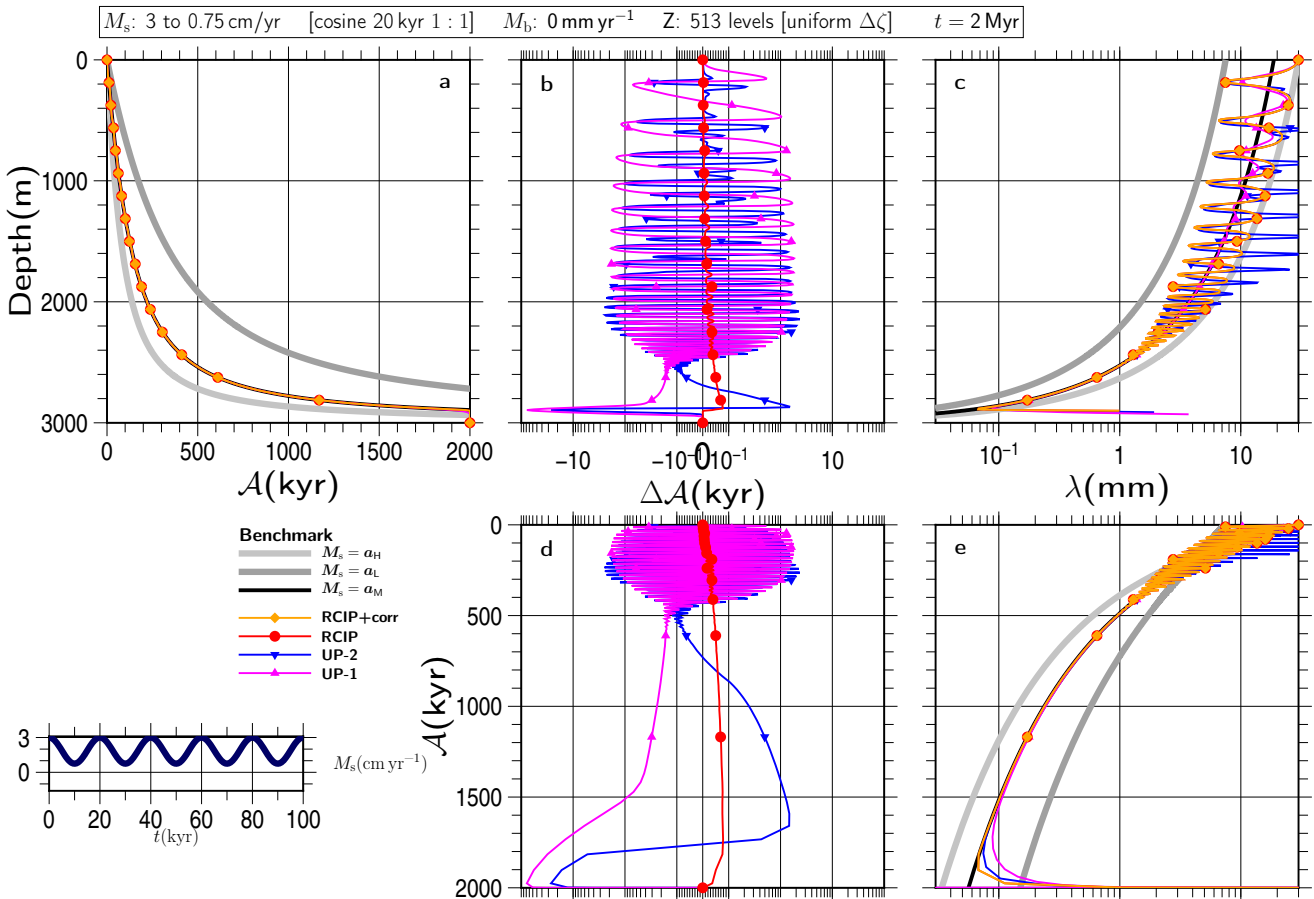
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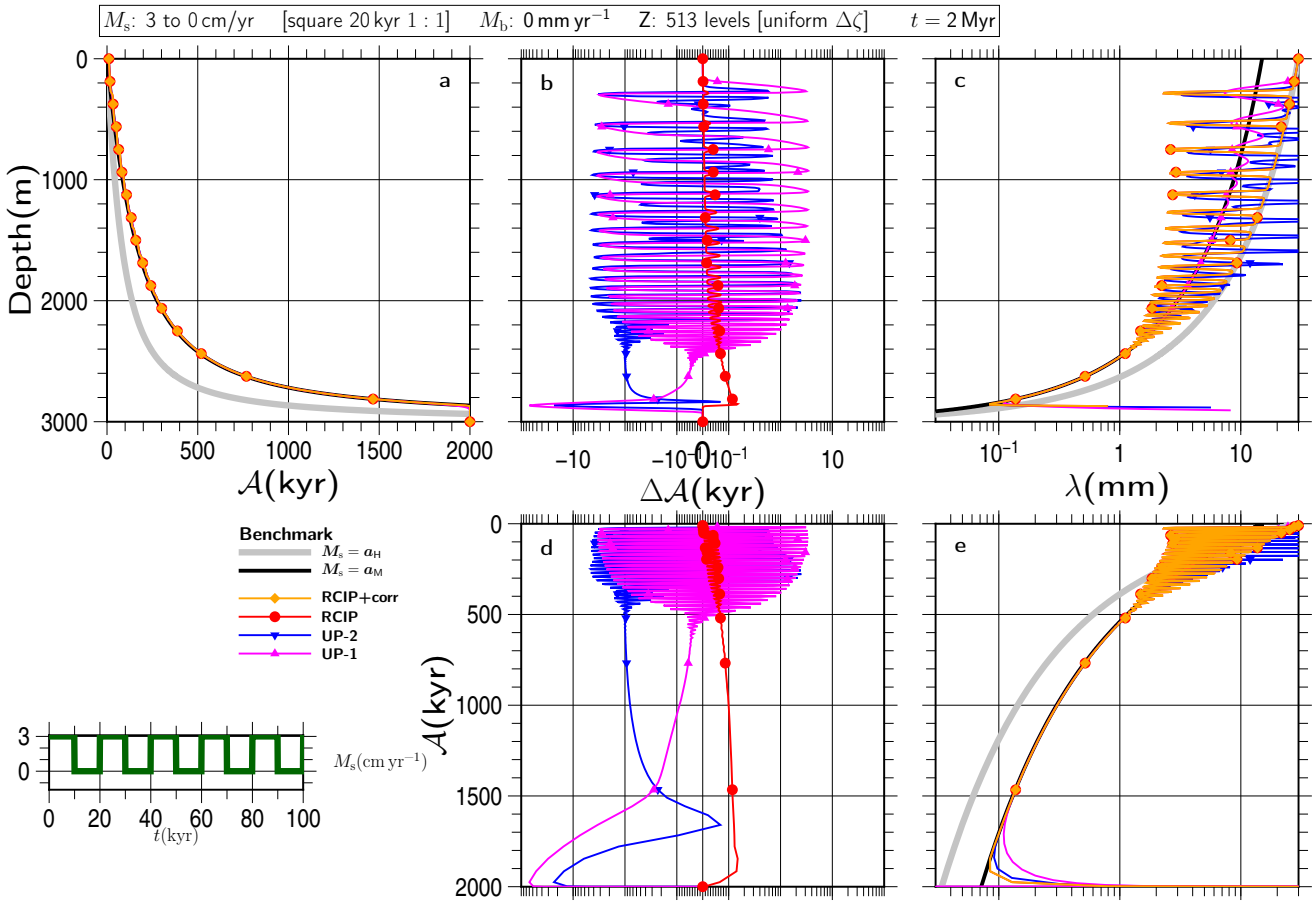
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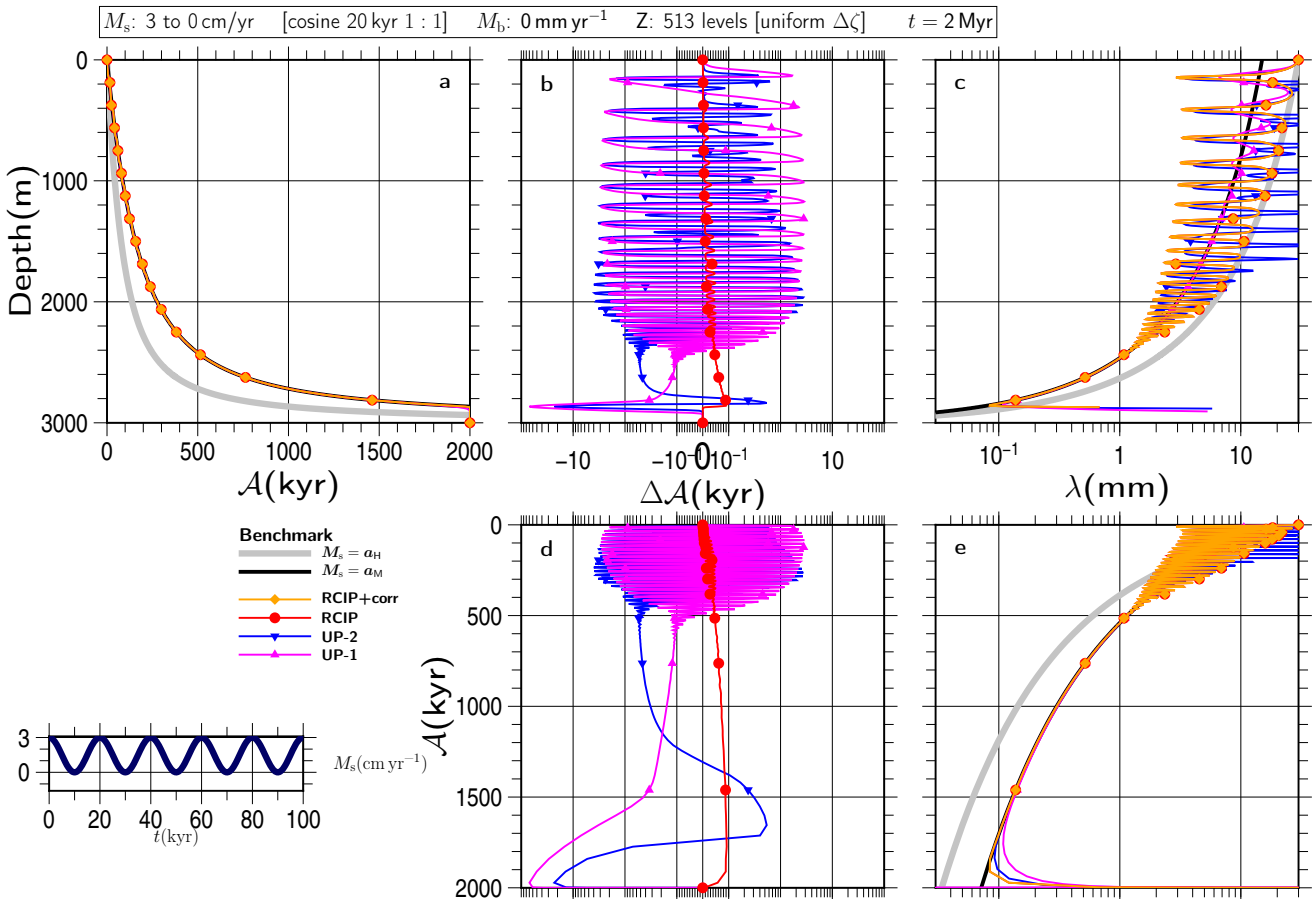
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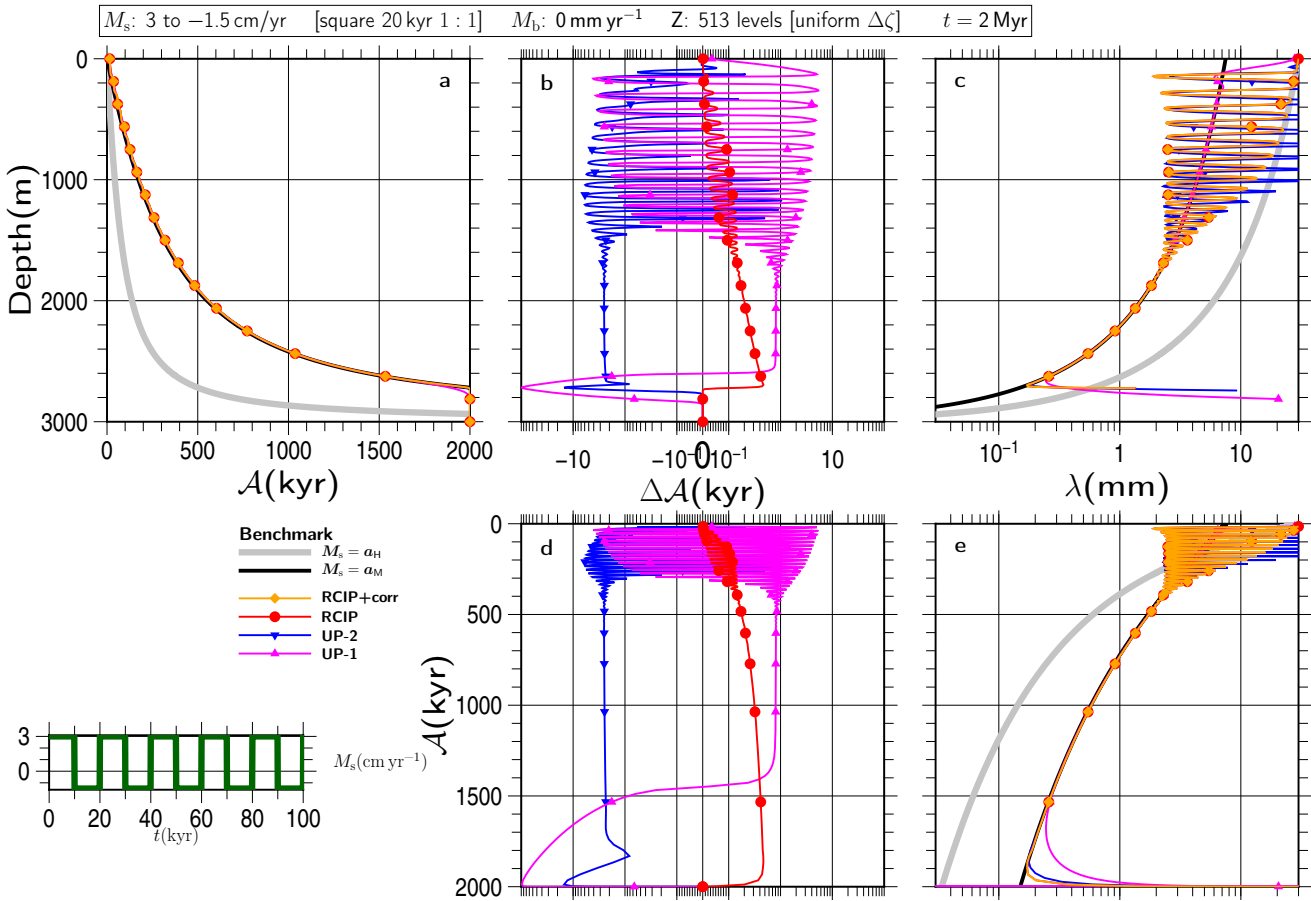
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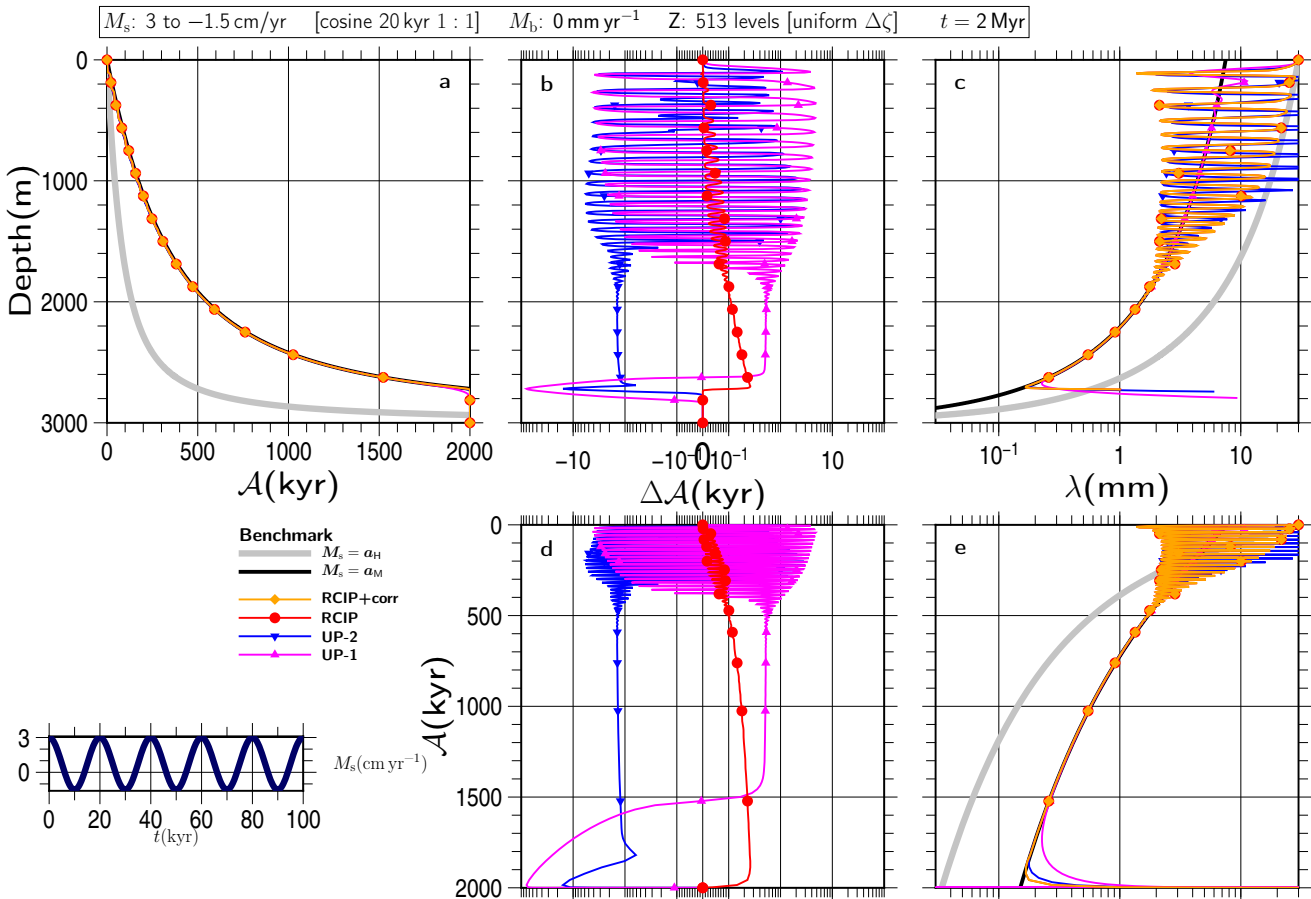
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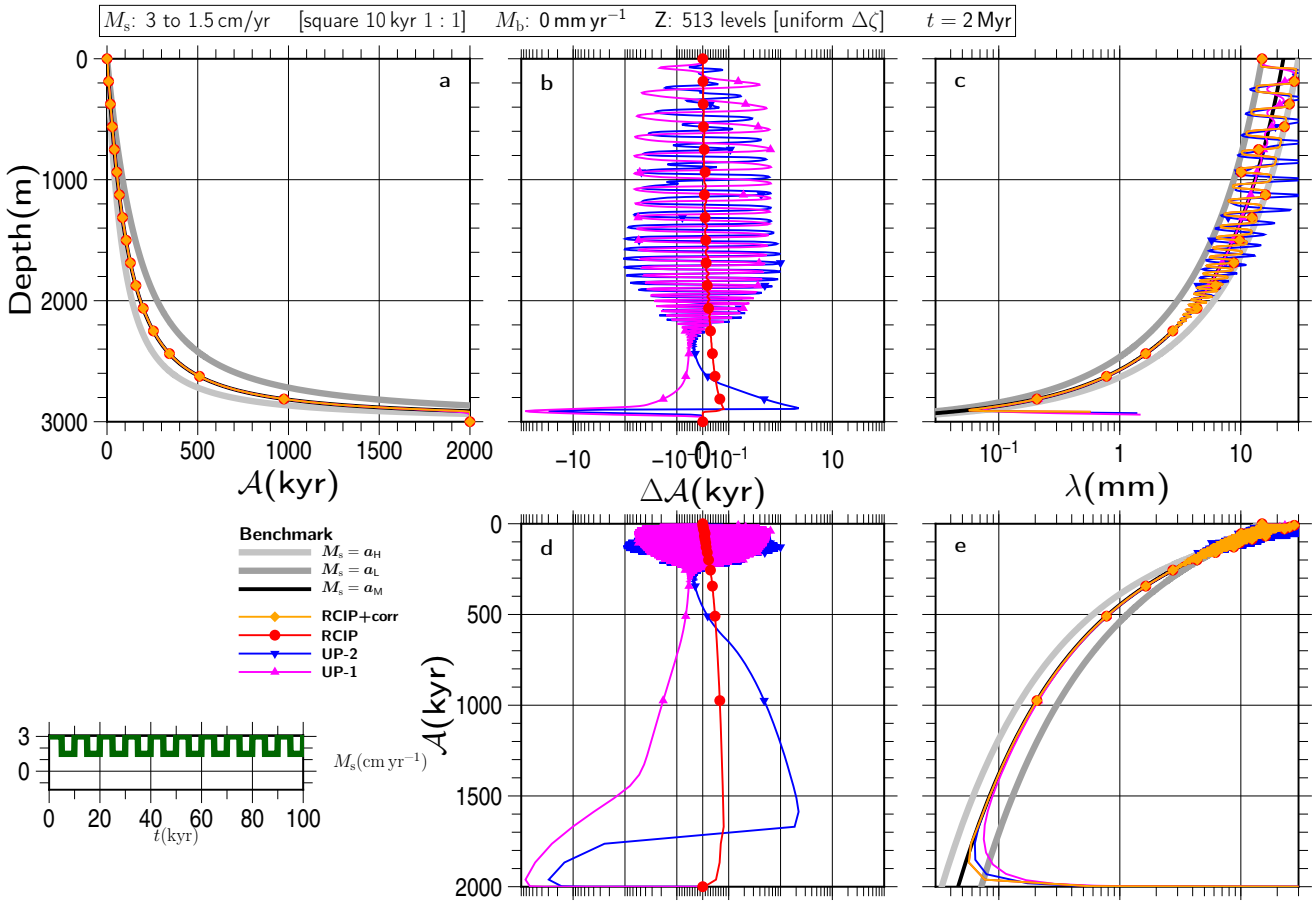
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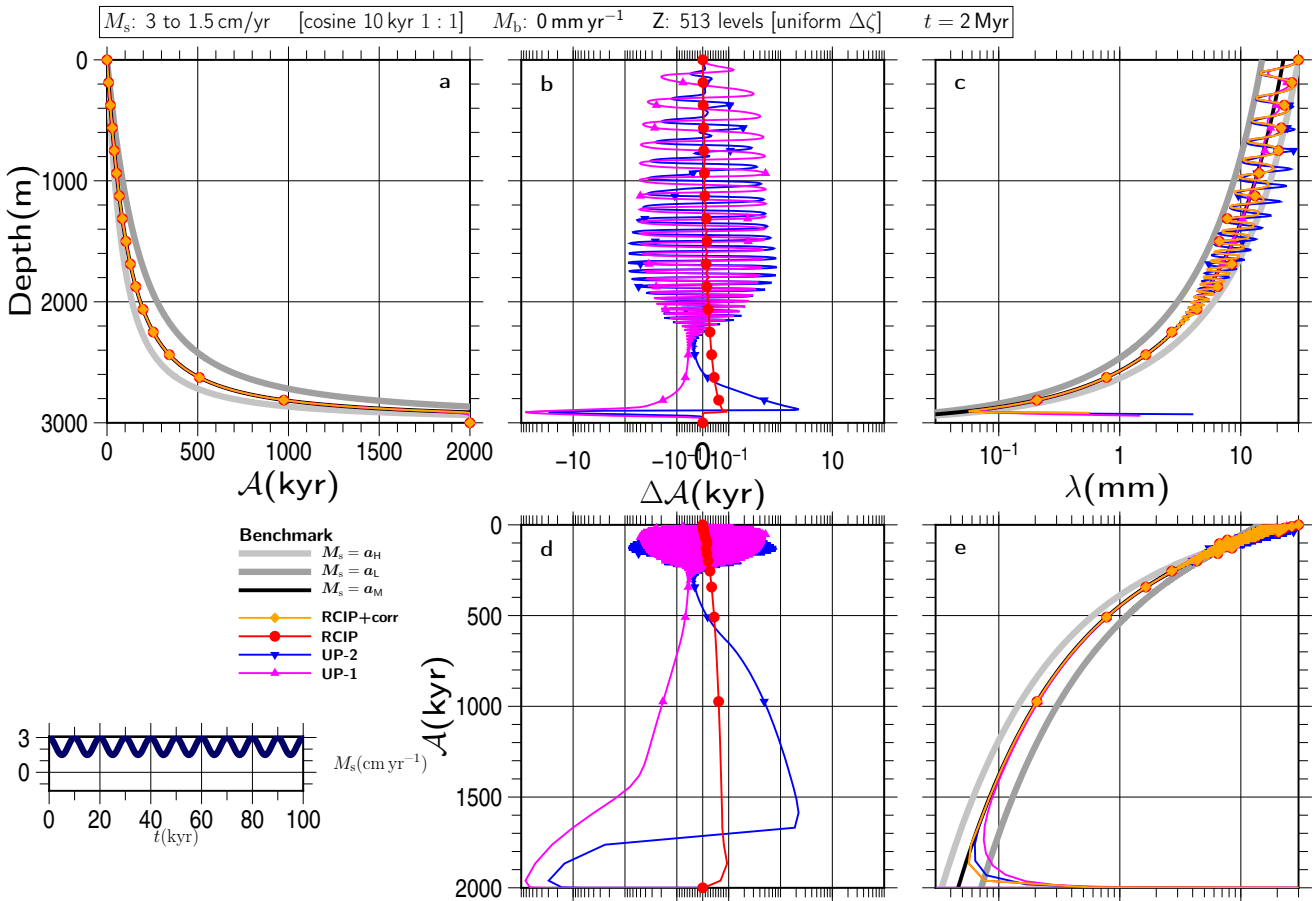
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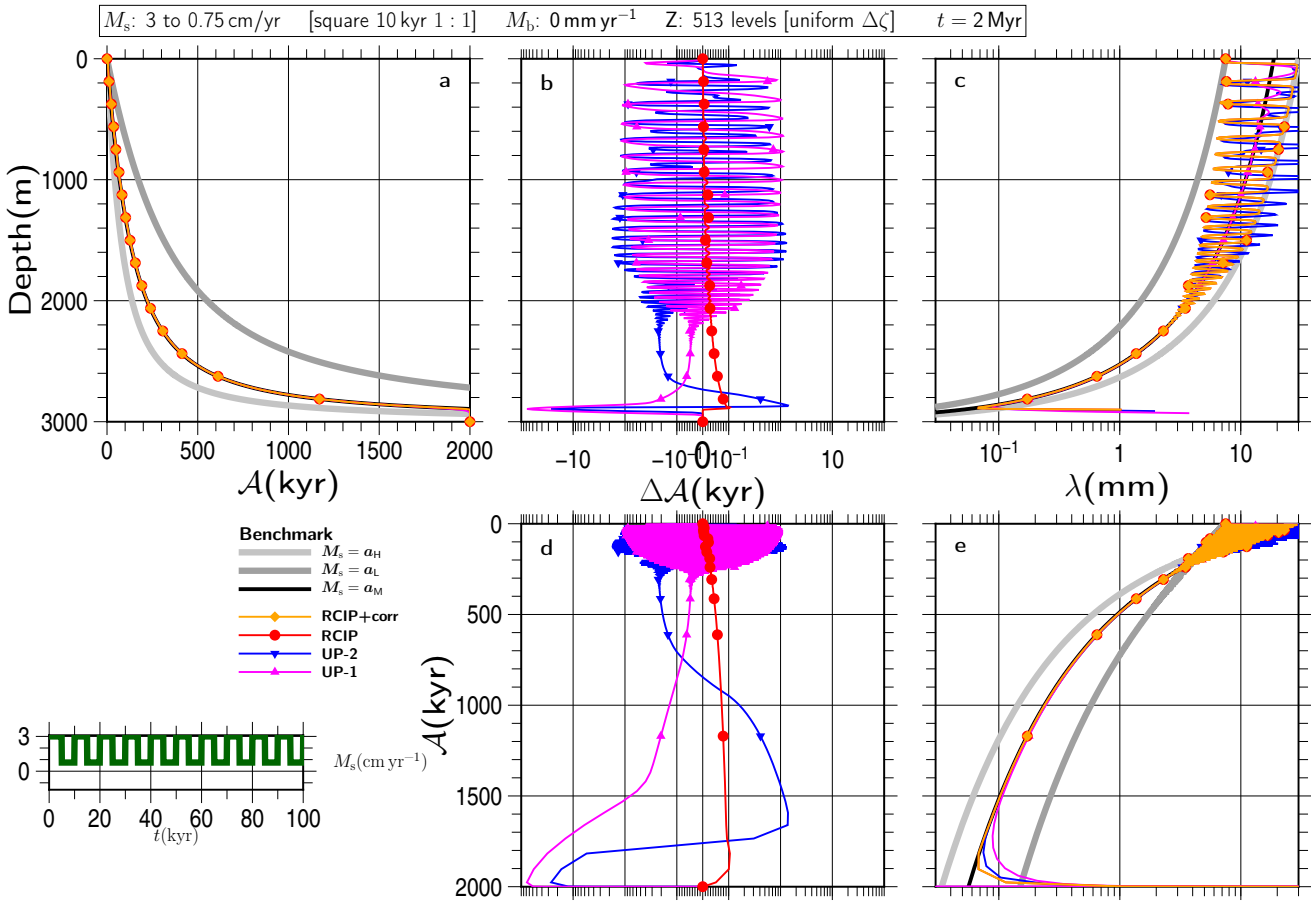
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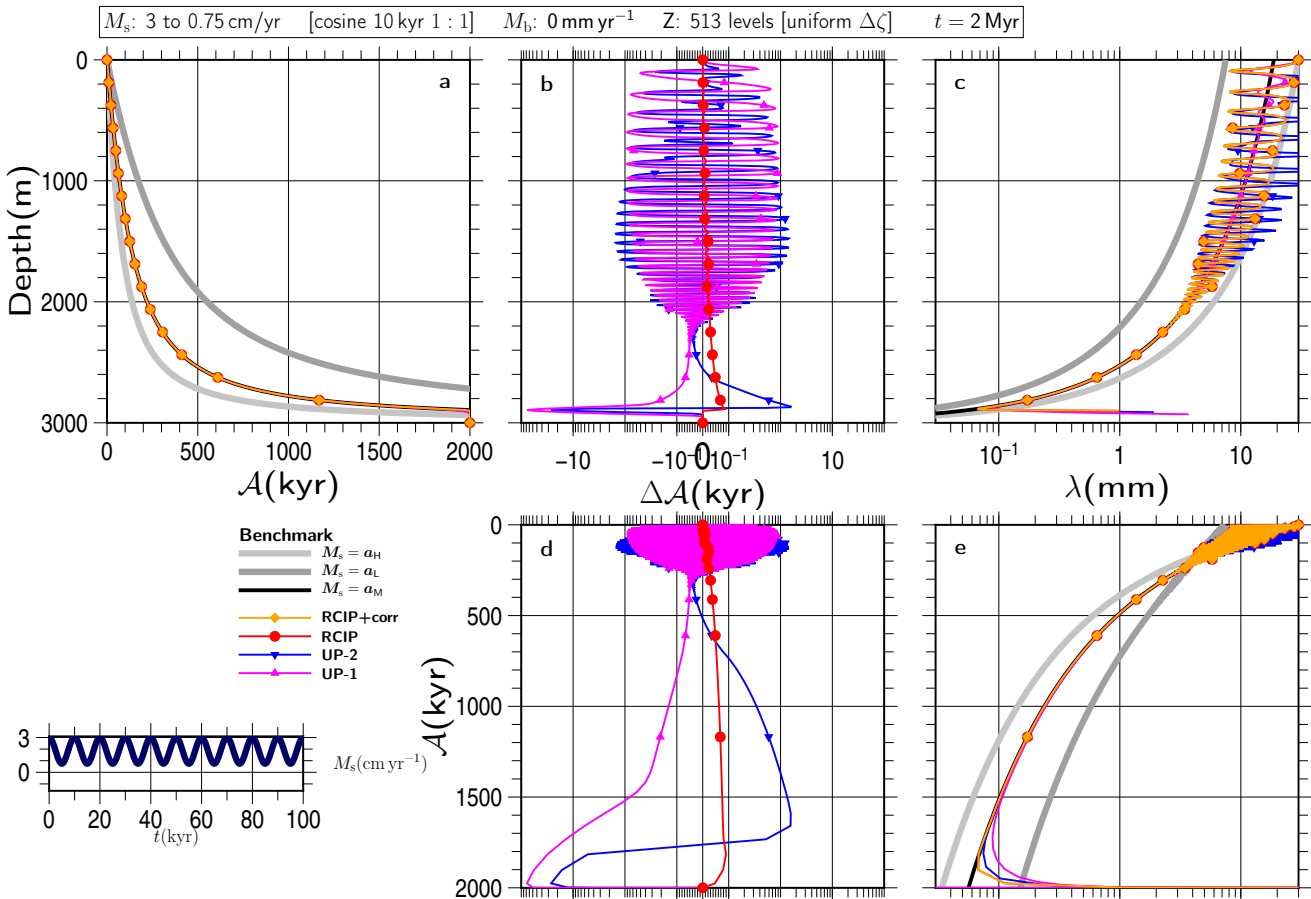
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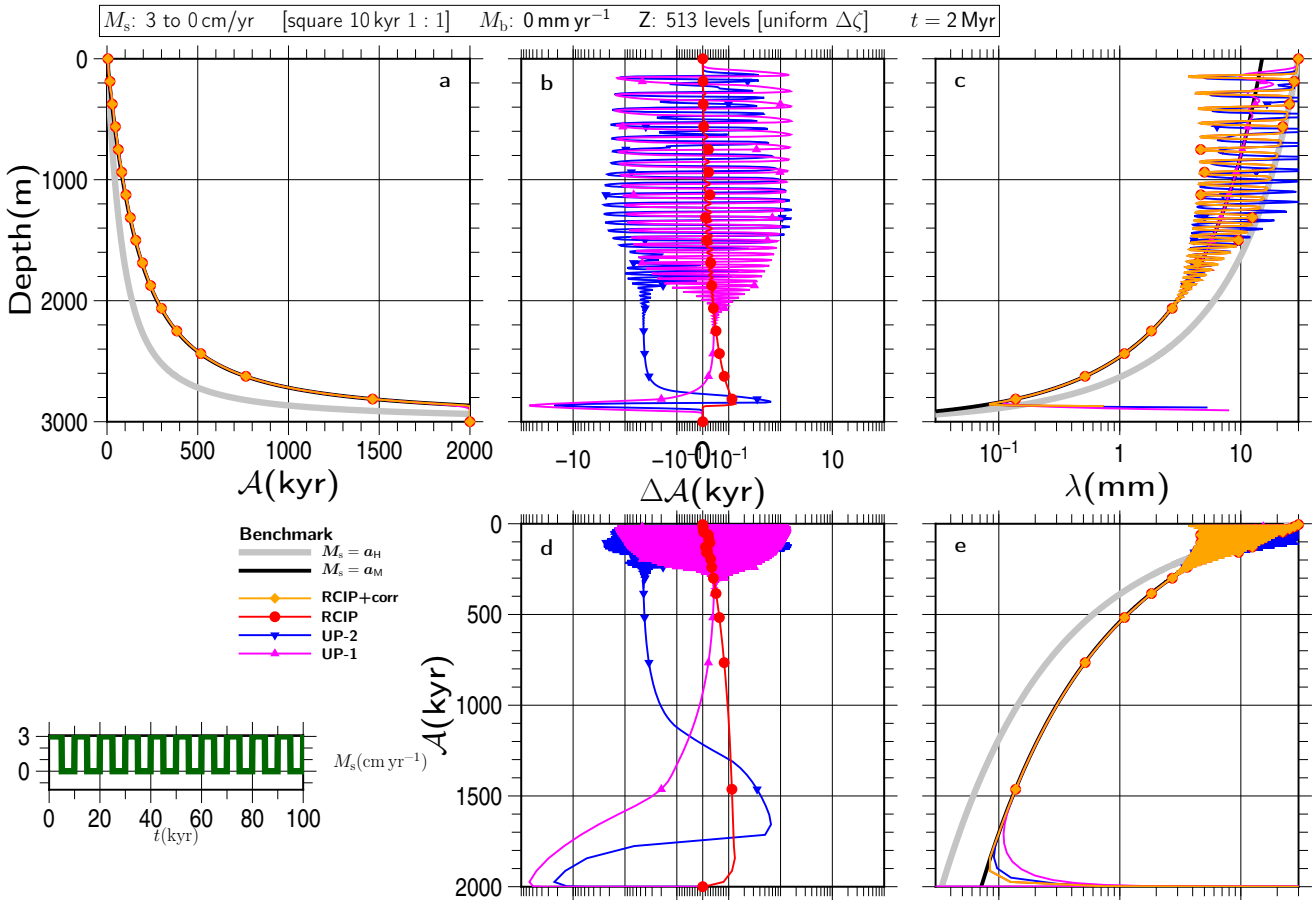
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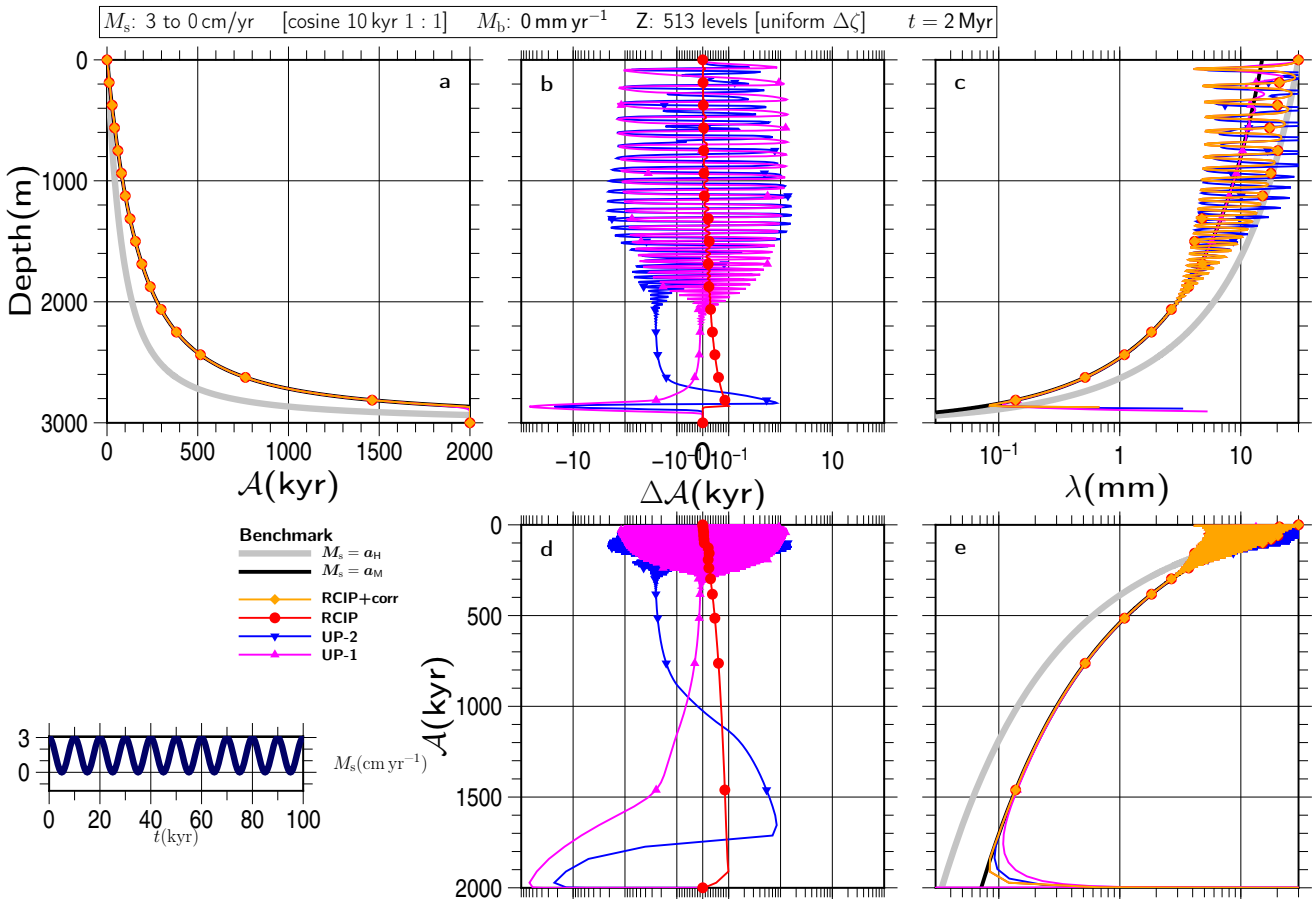
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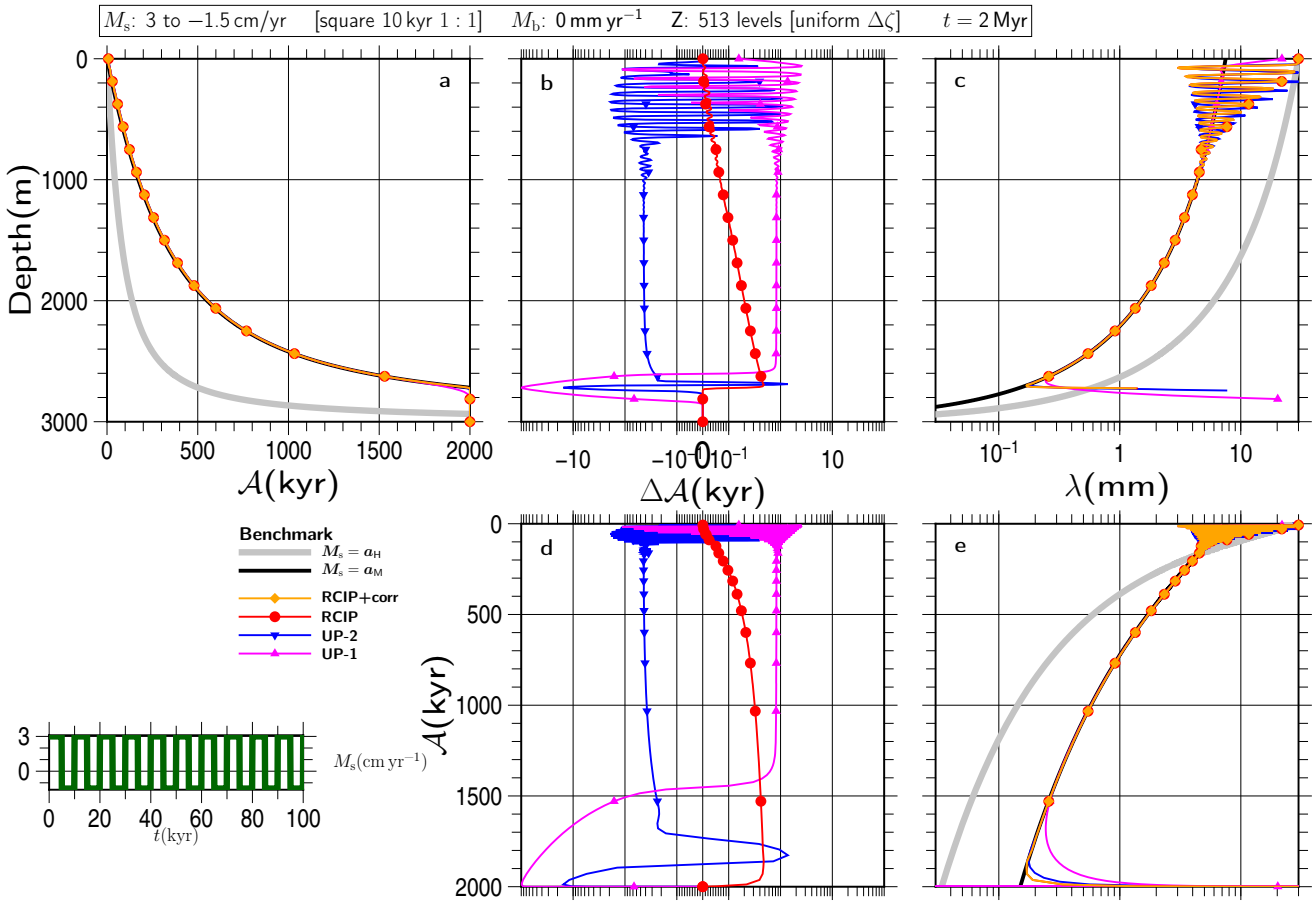
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Figure S94:

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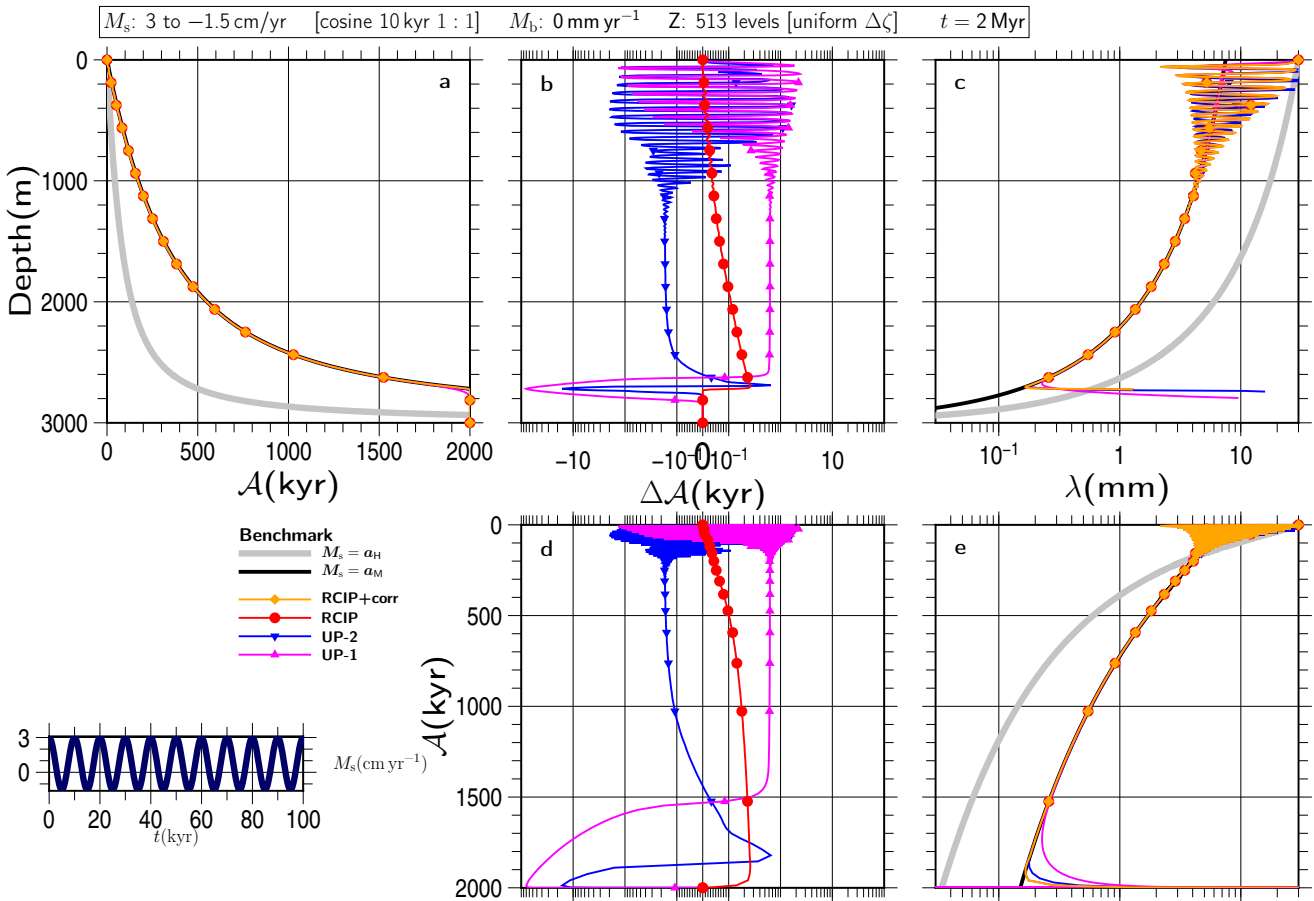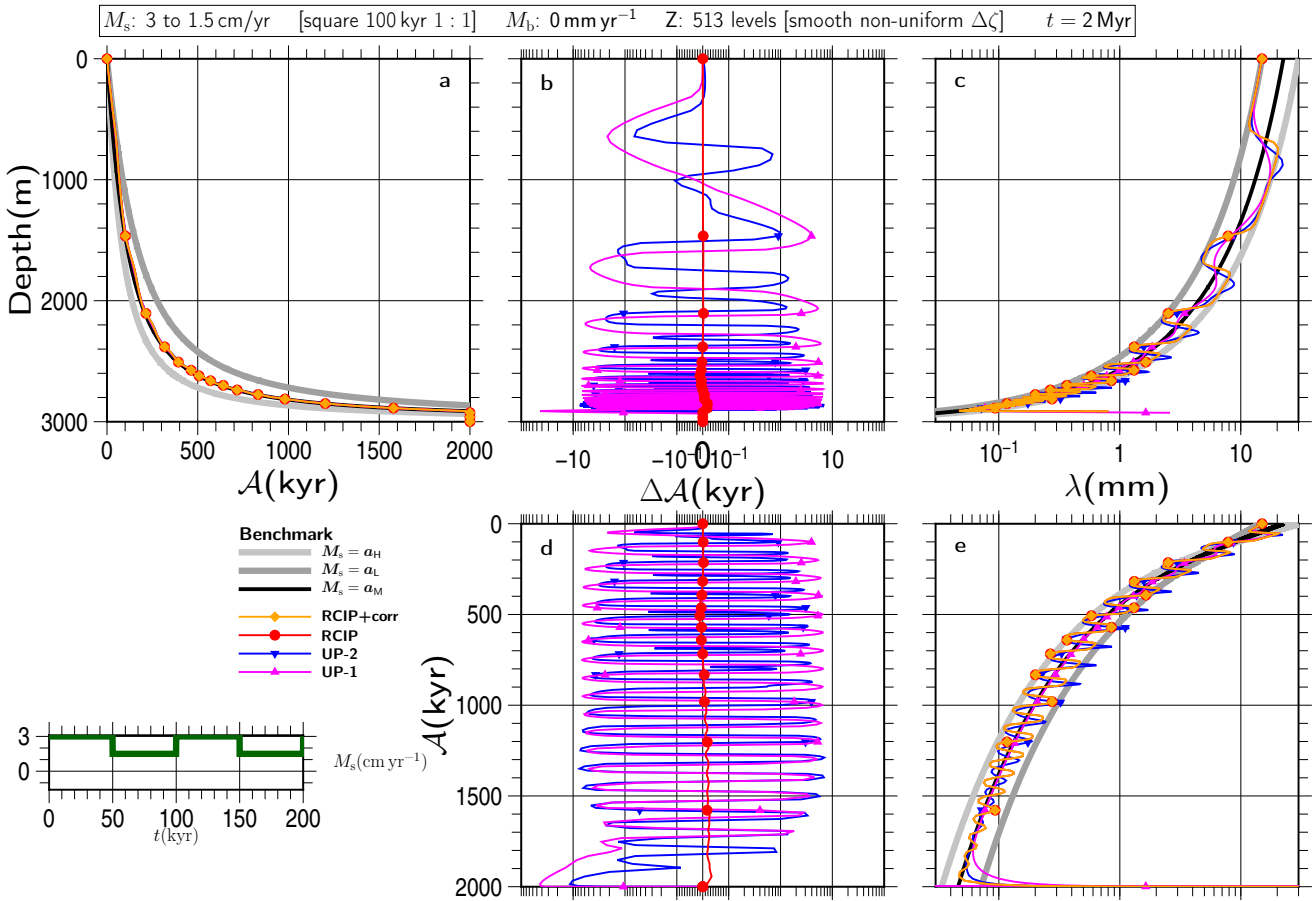
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Figure S96:

49
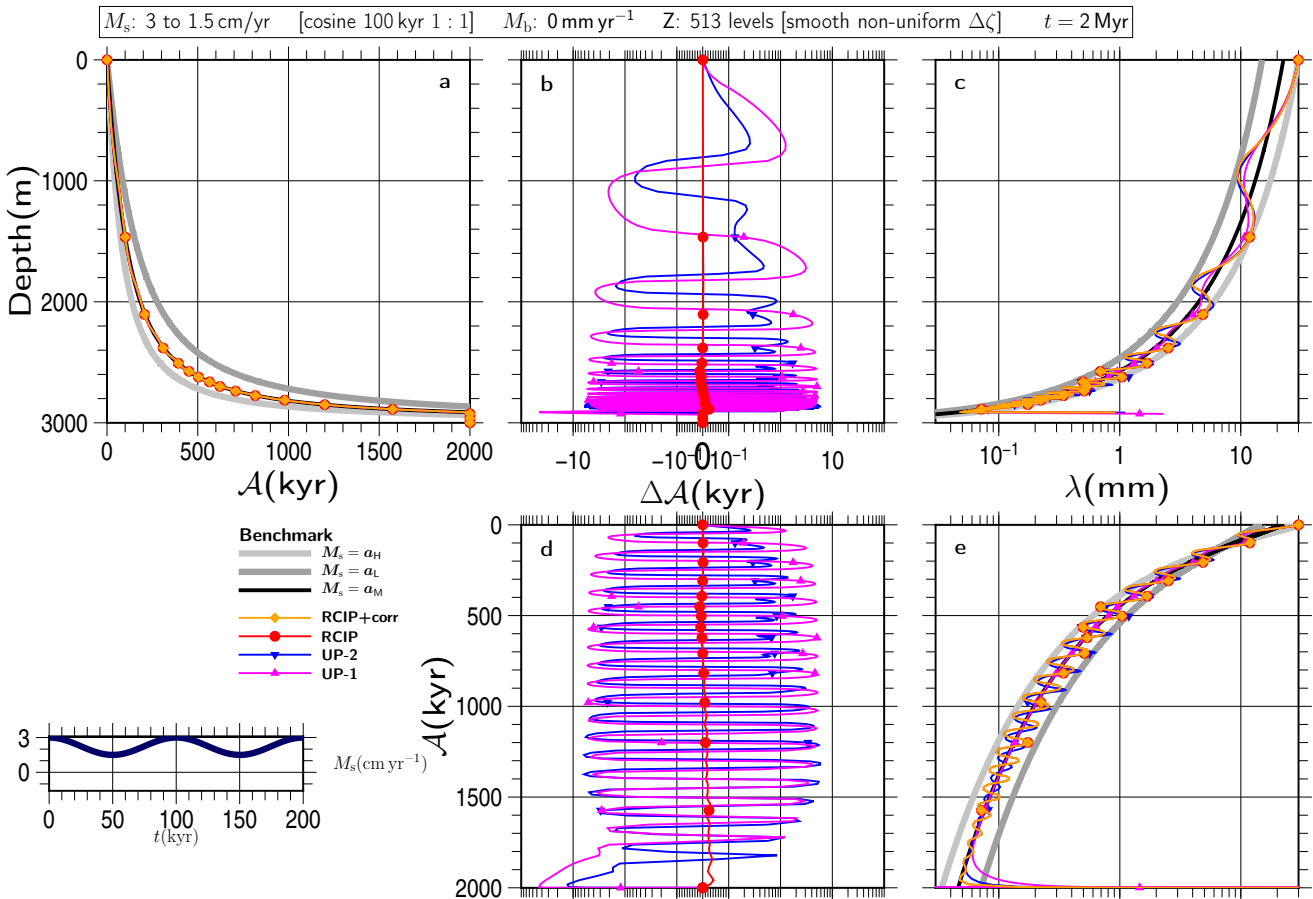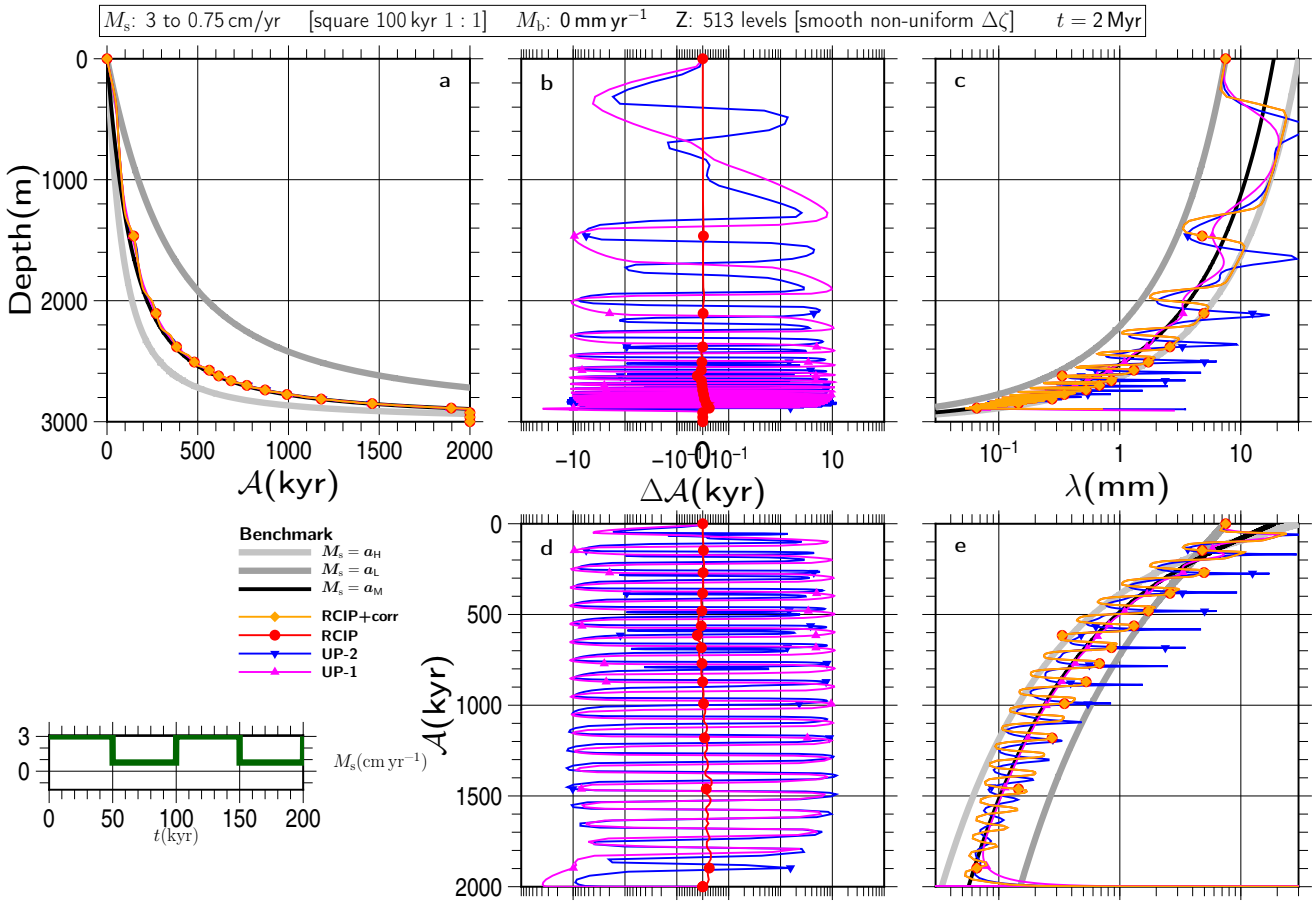
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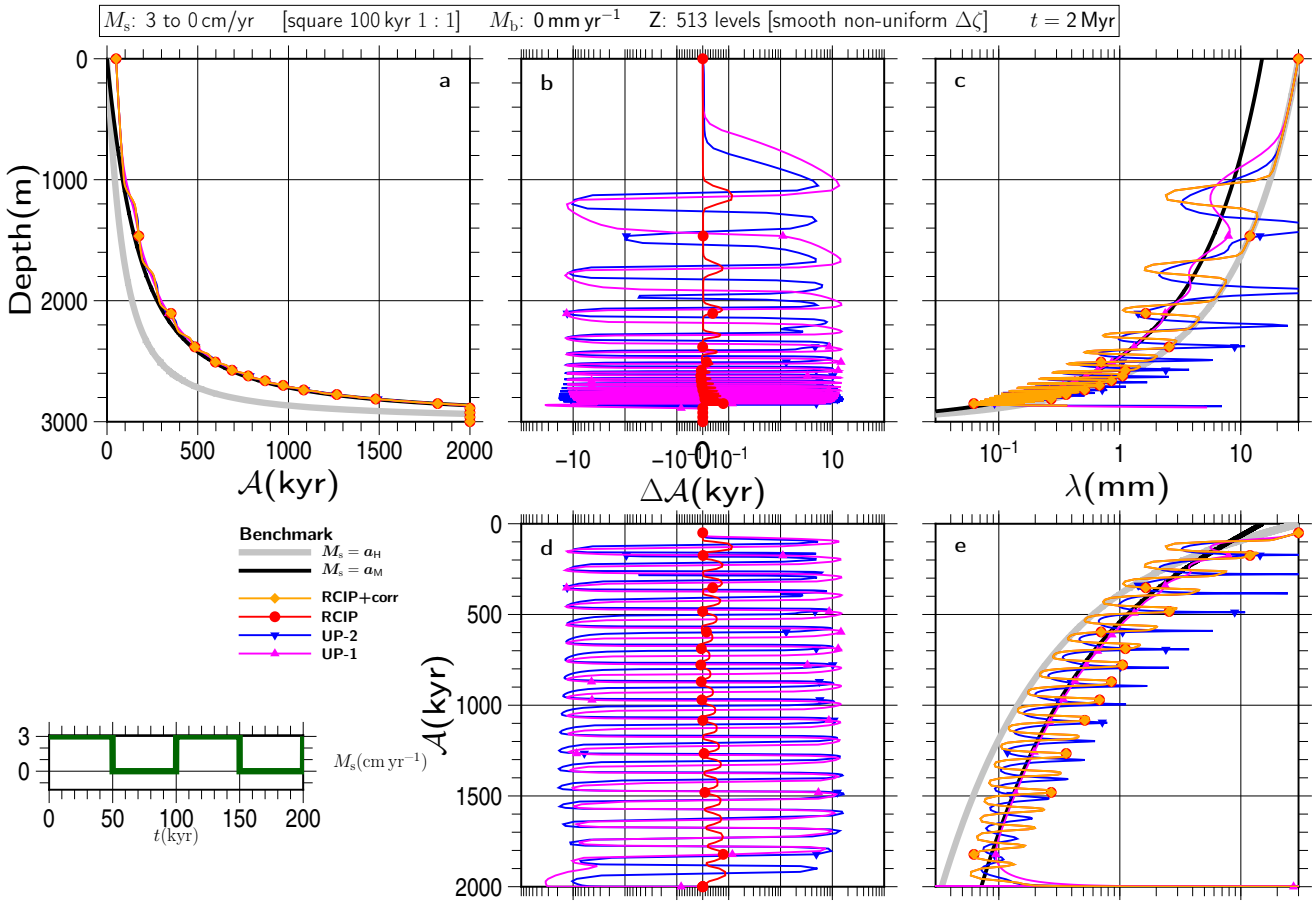
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Figure S100:

51
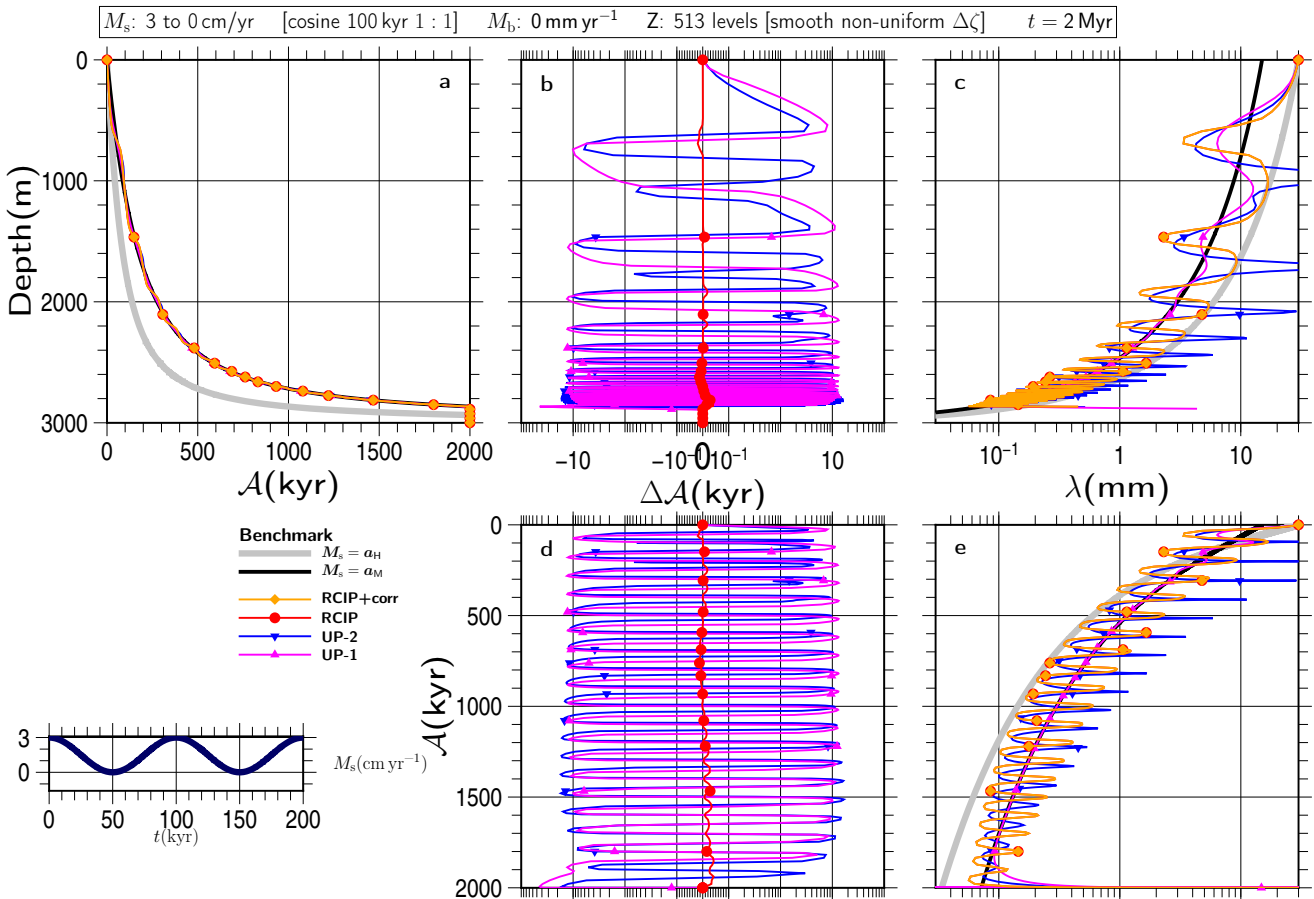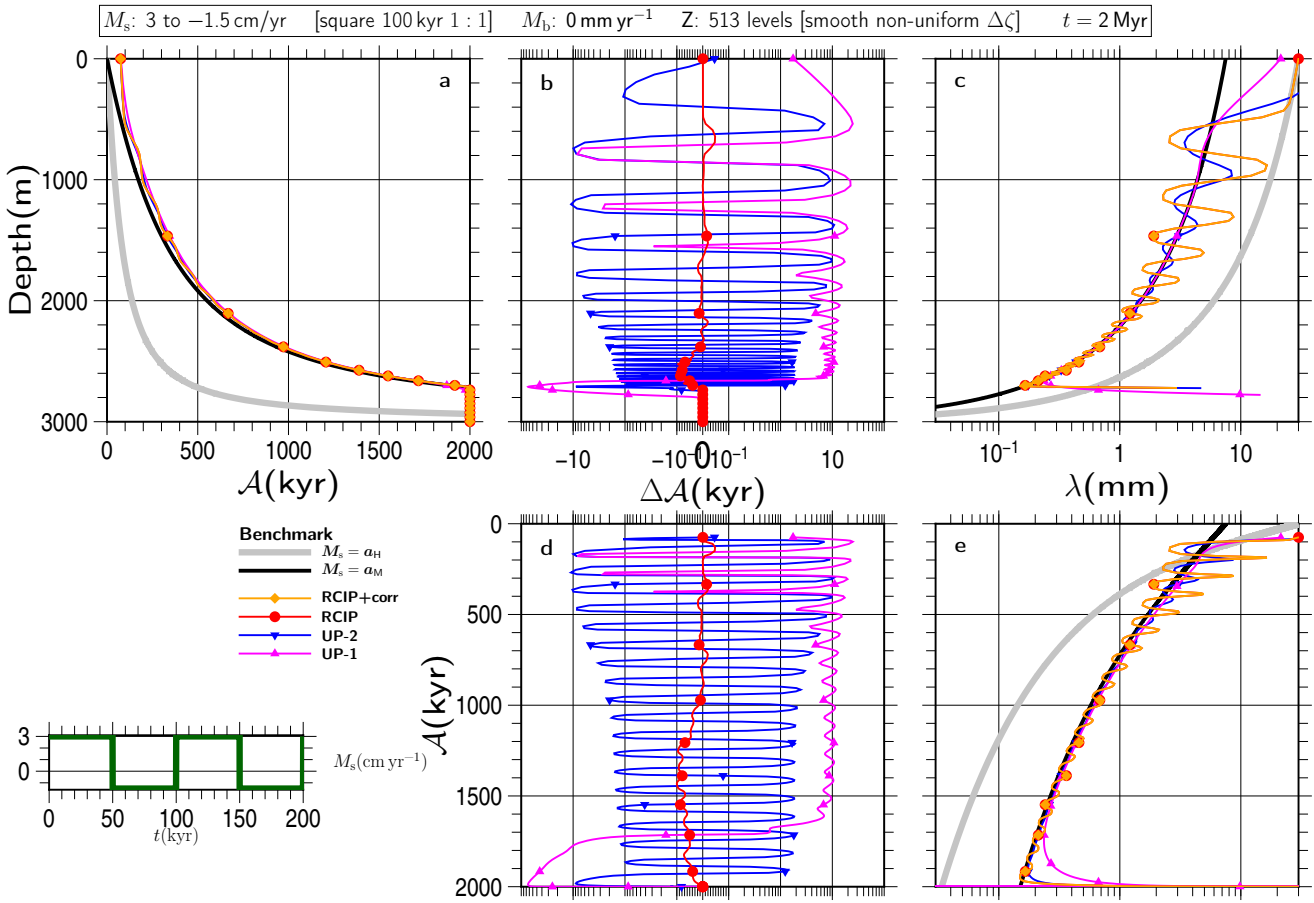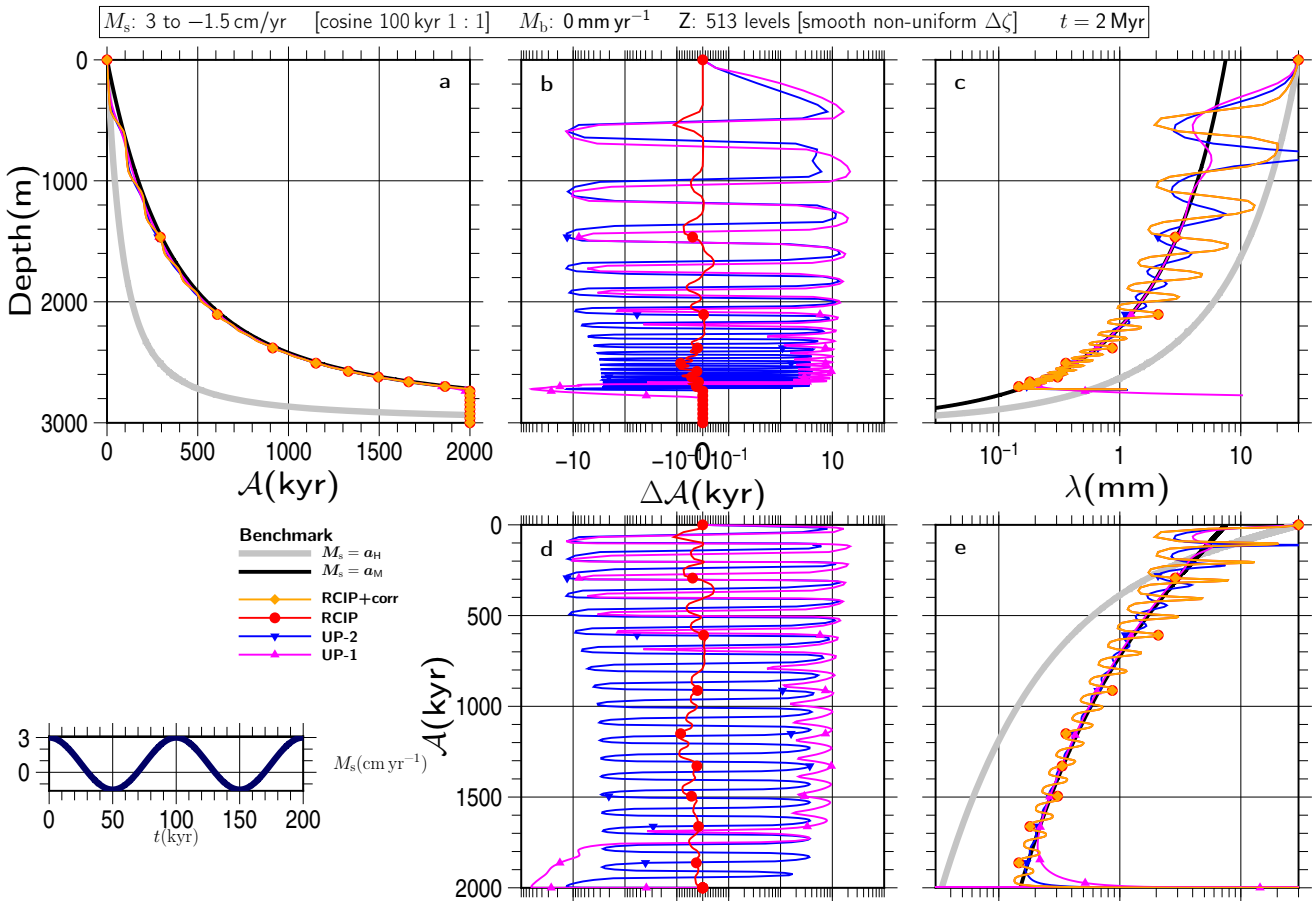
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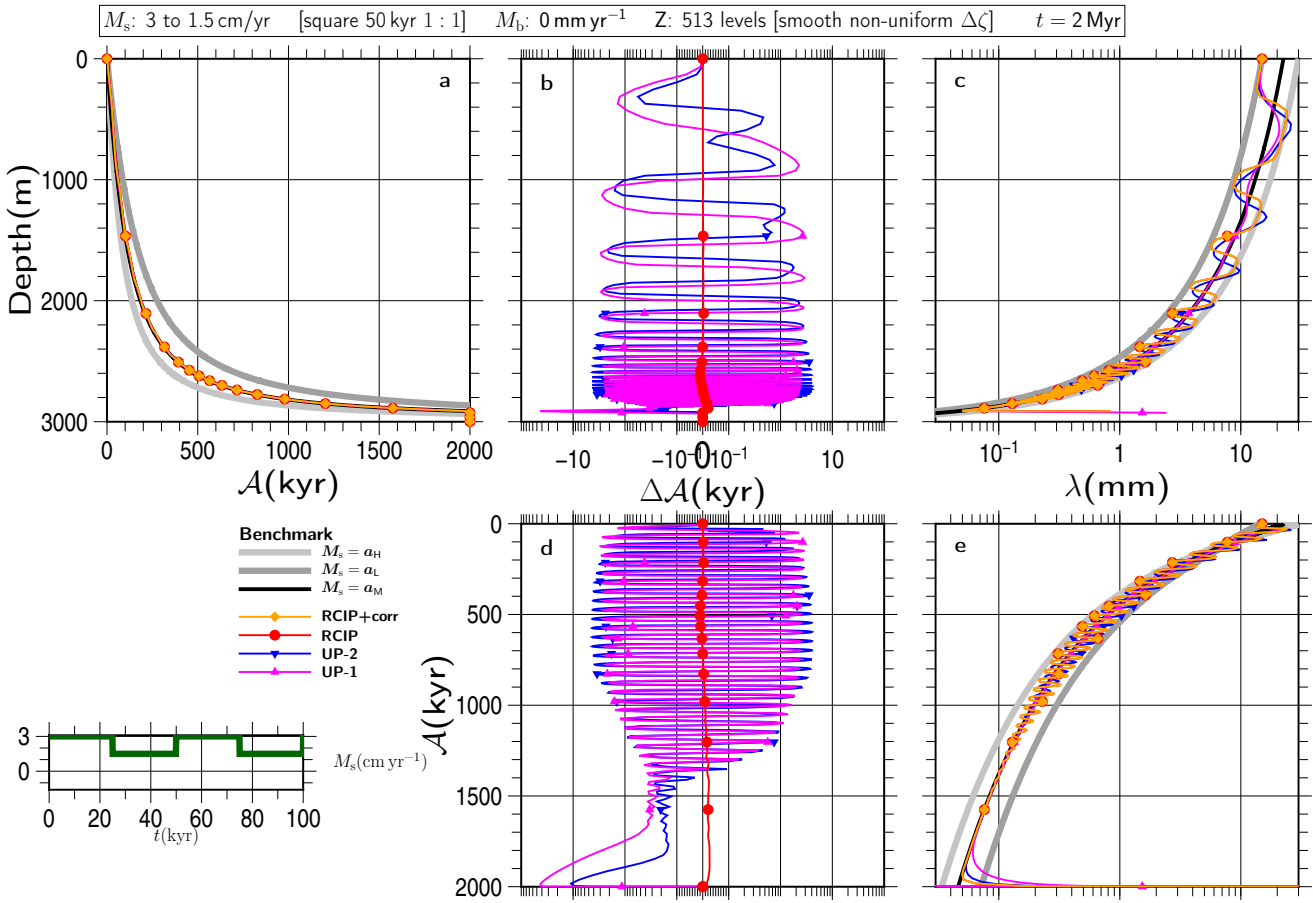
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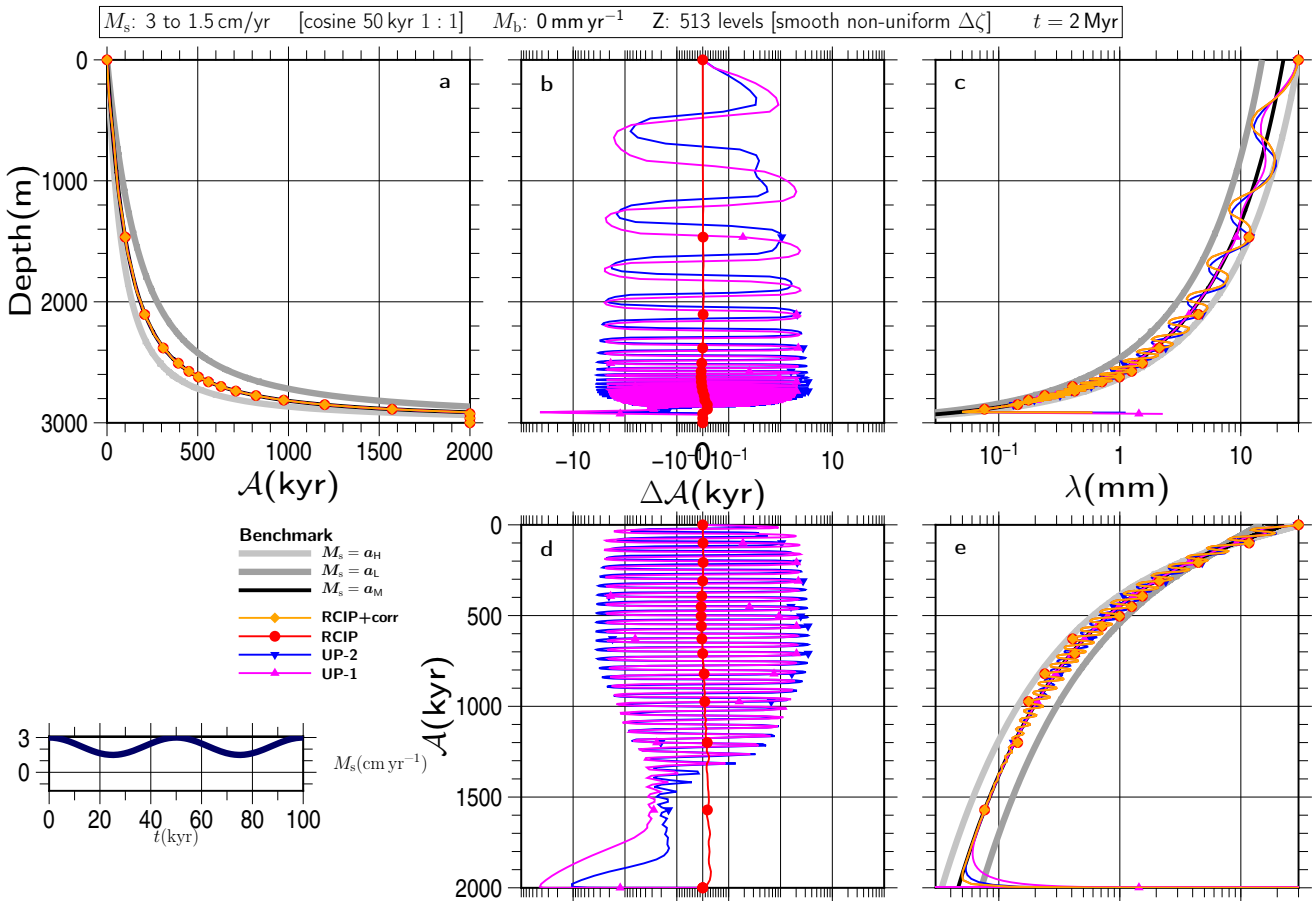
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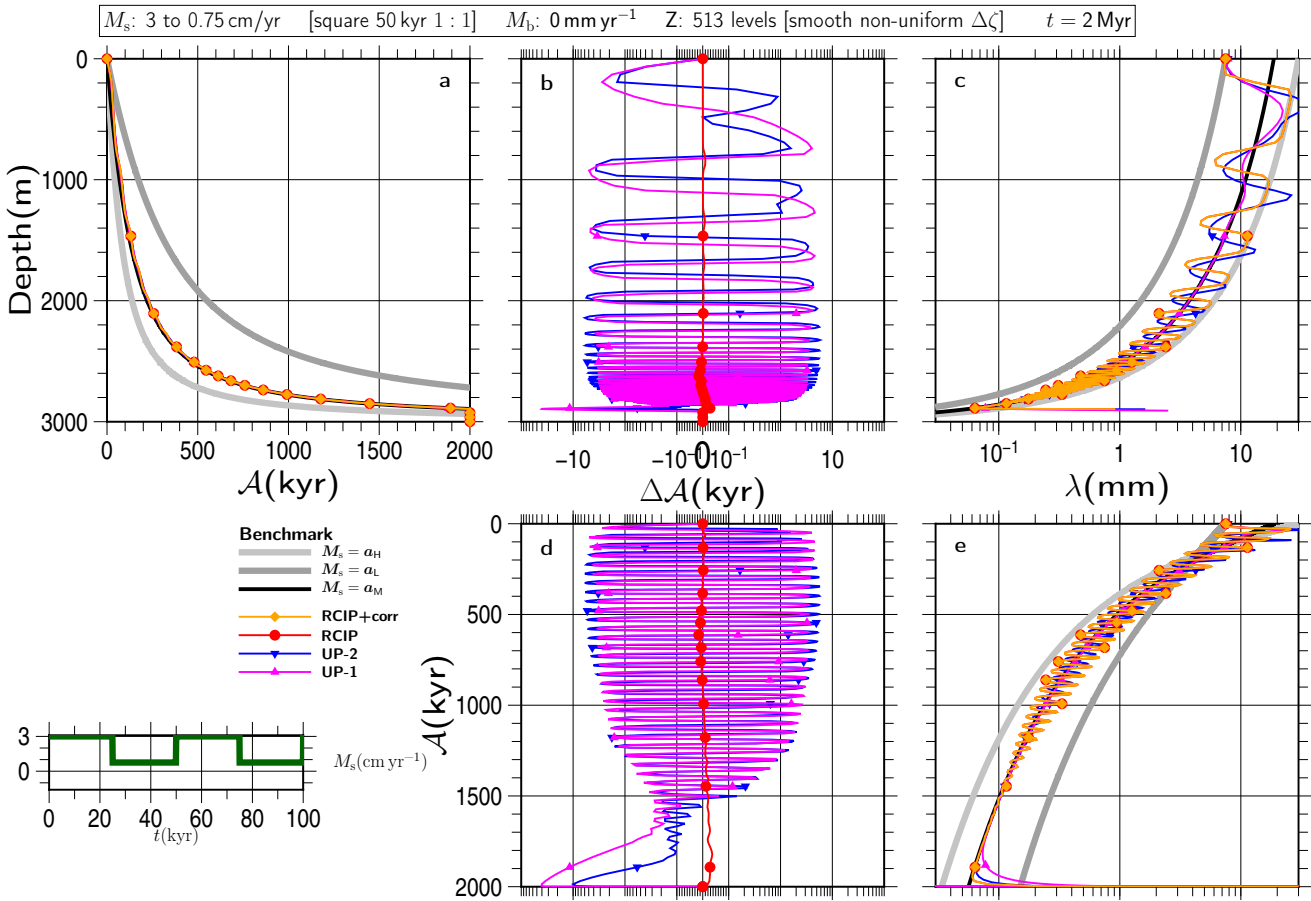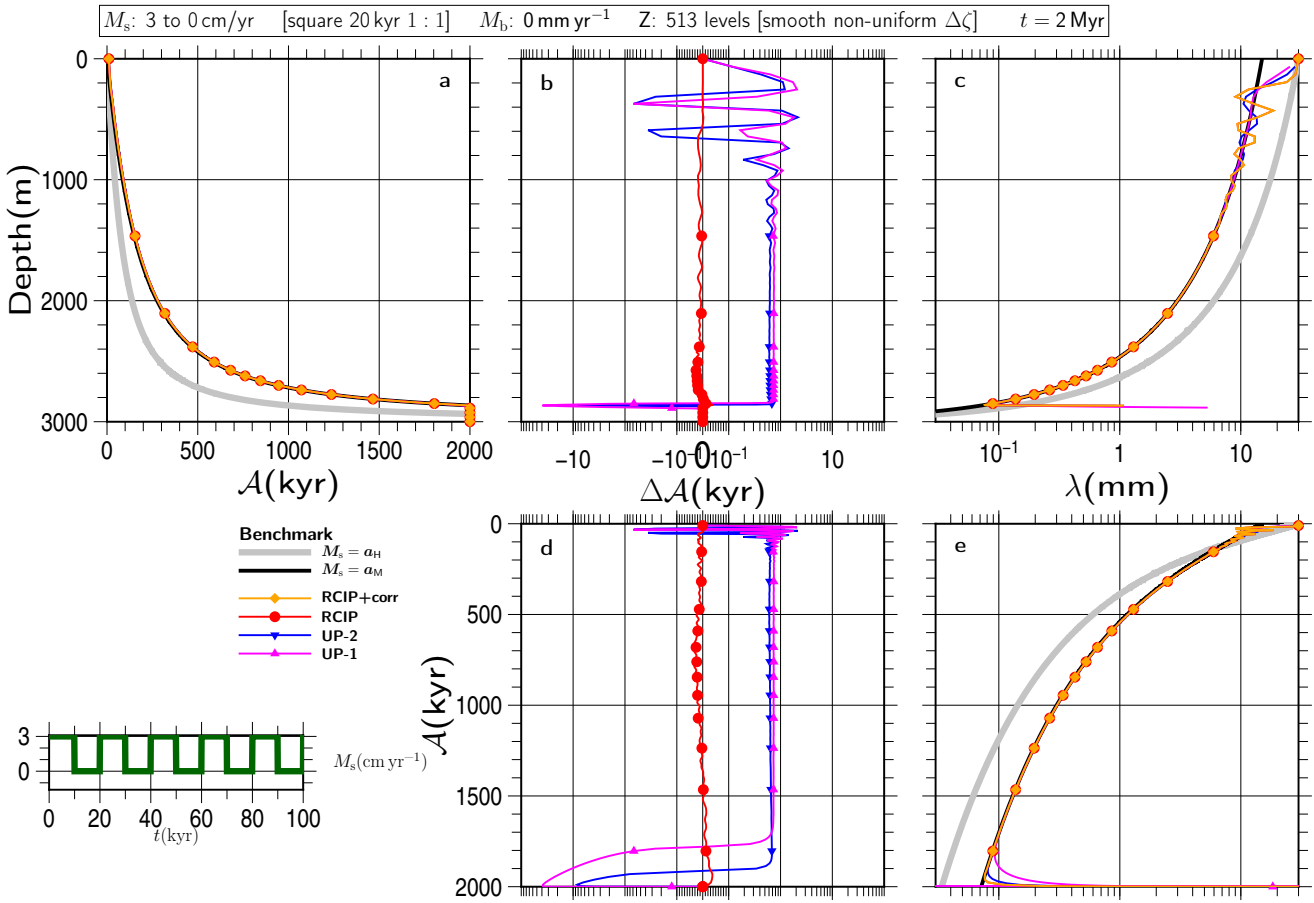
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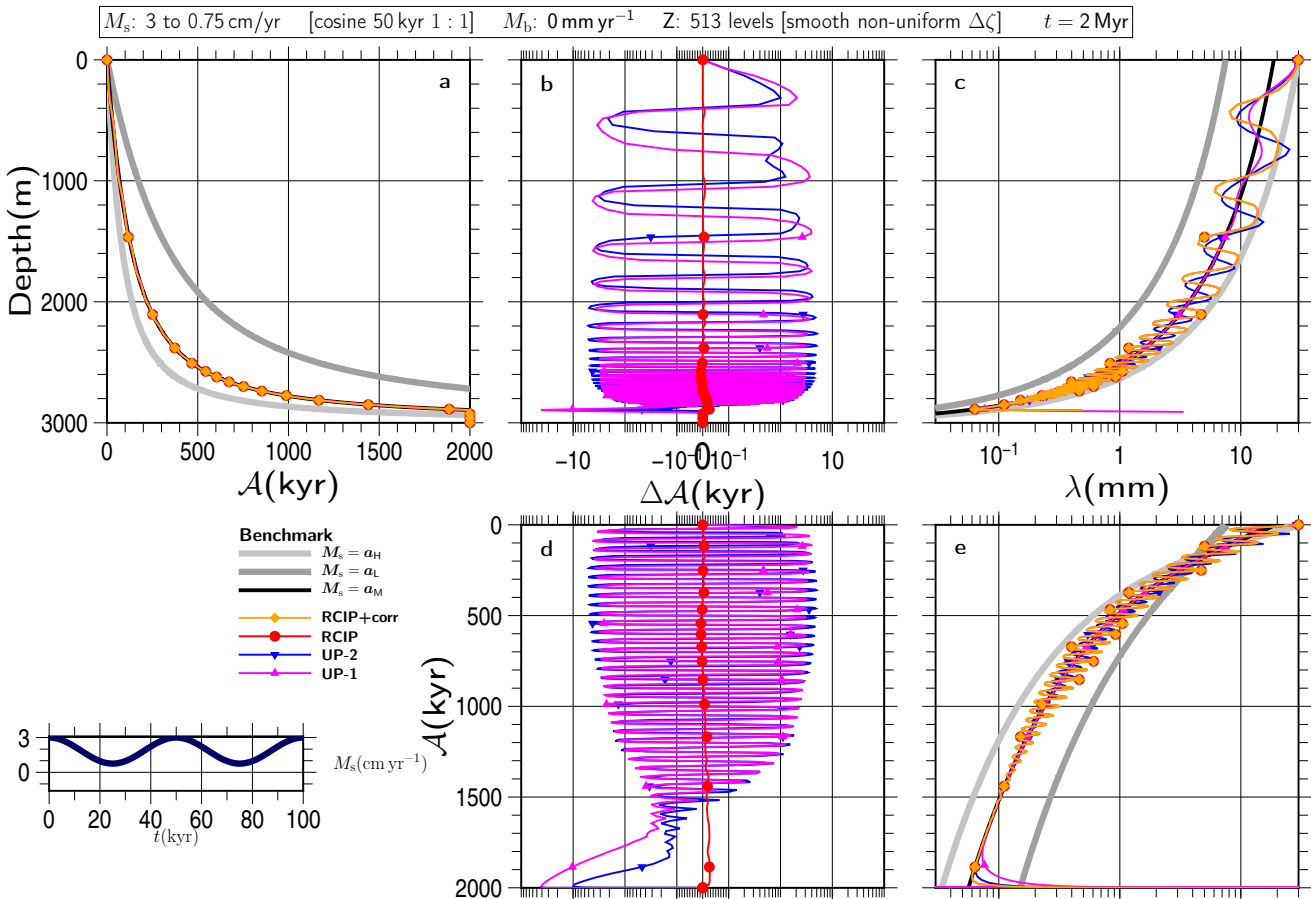
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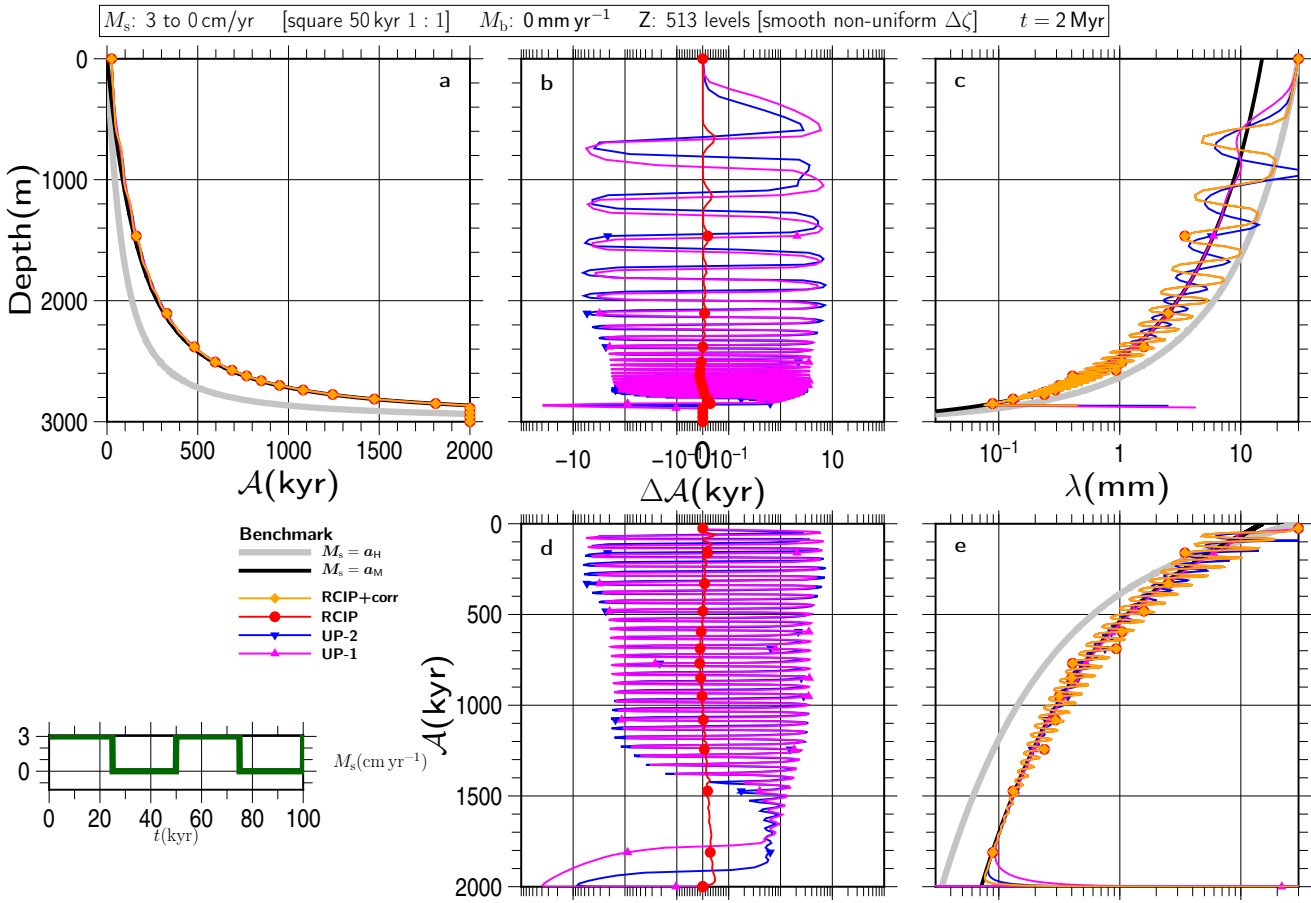
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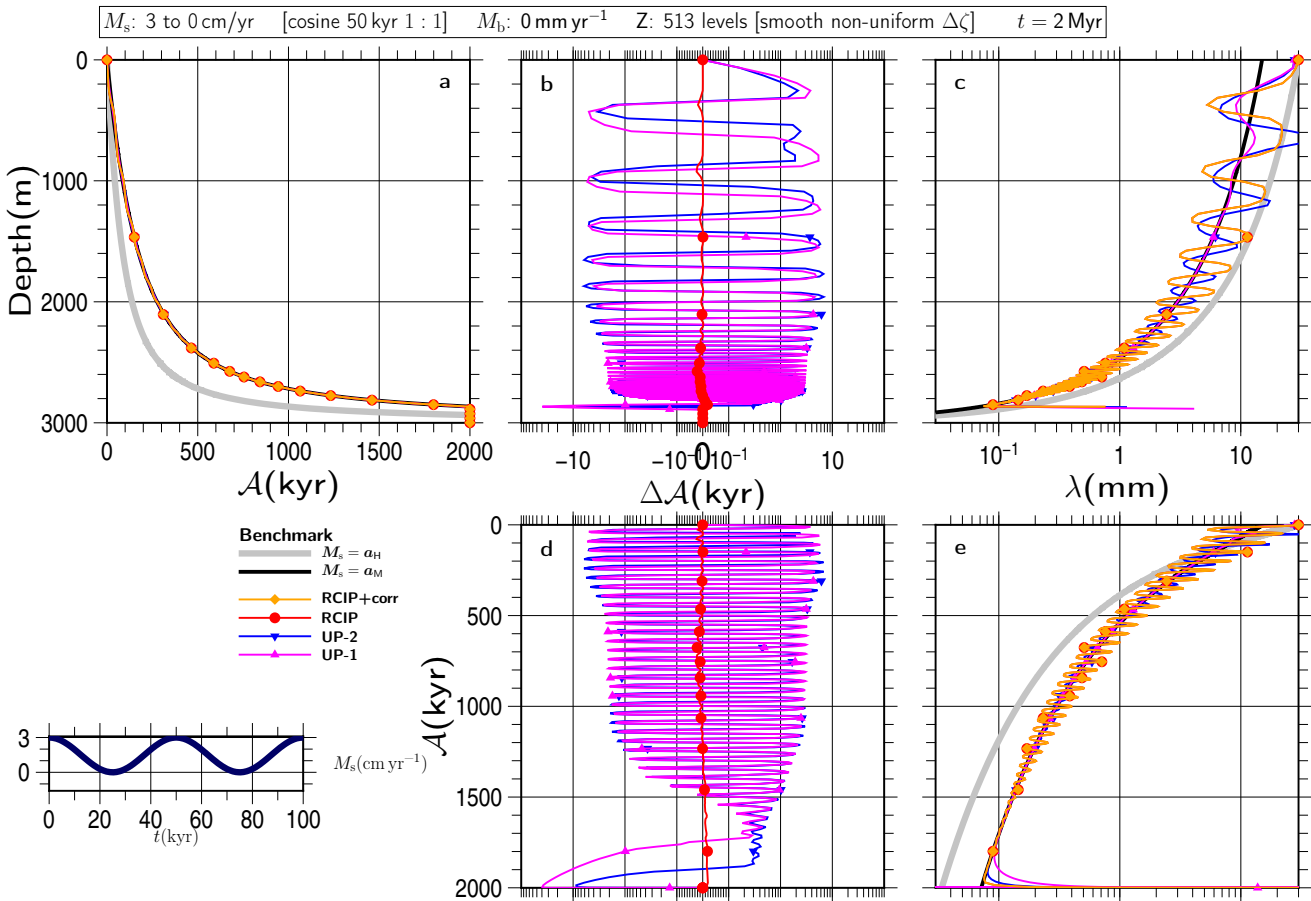
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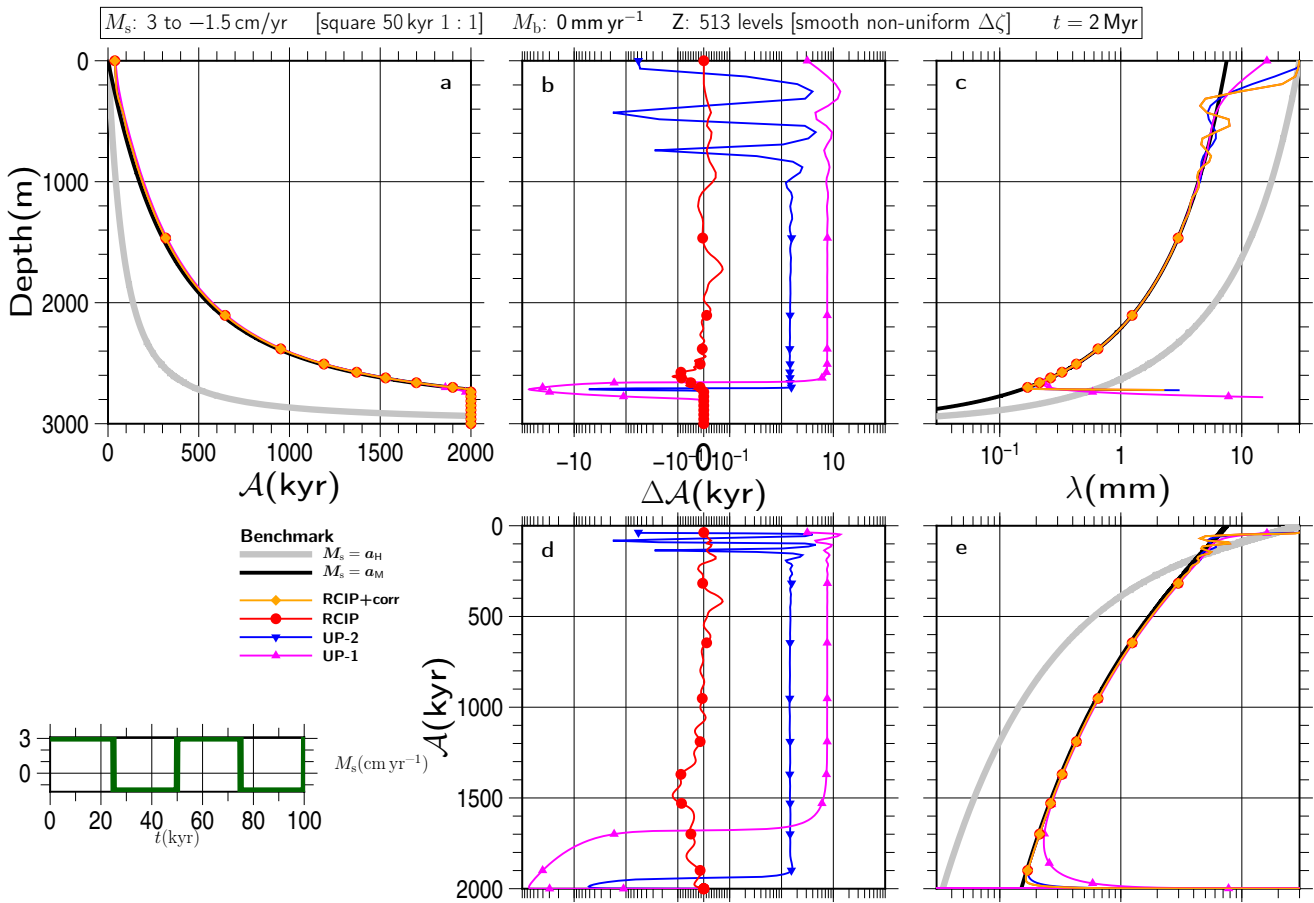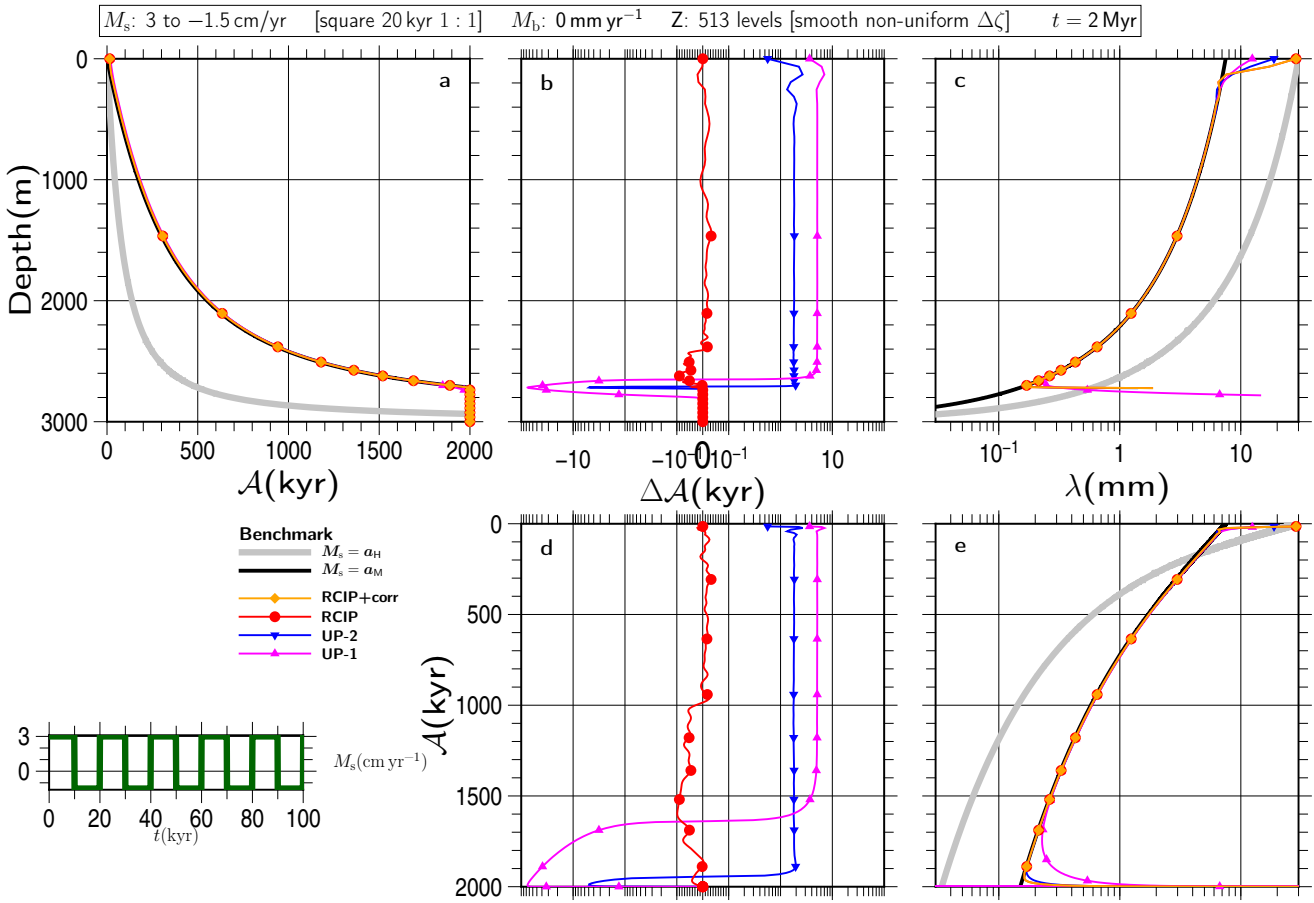
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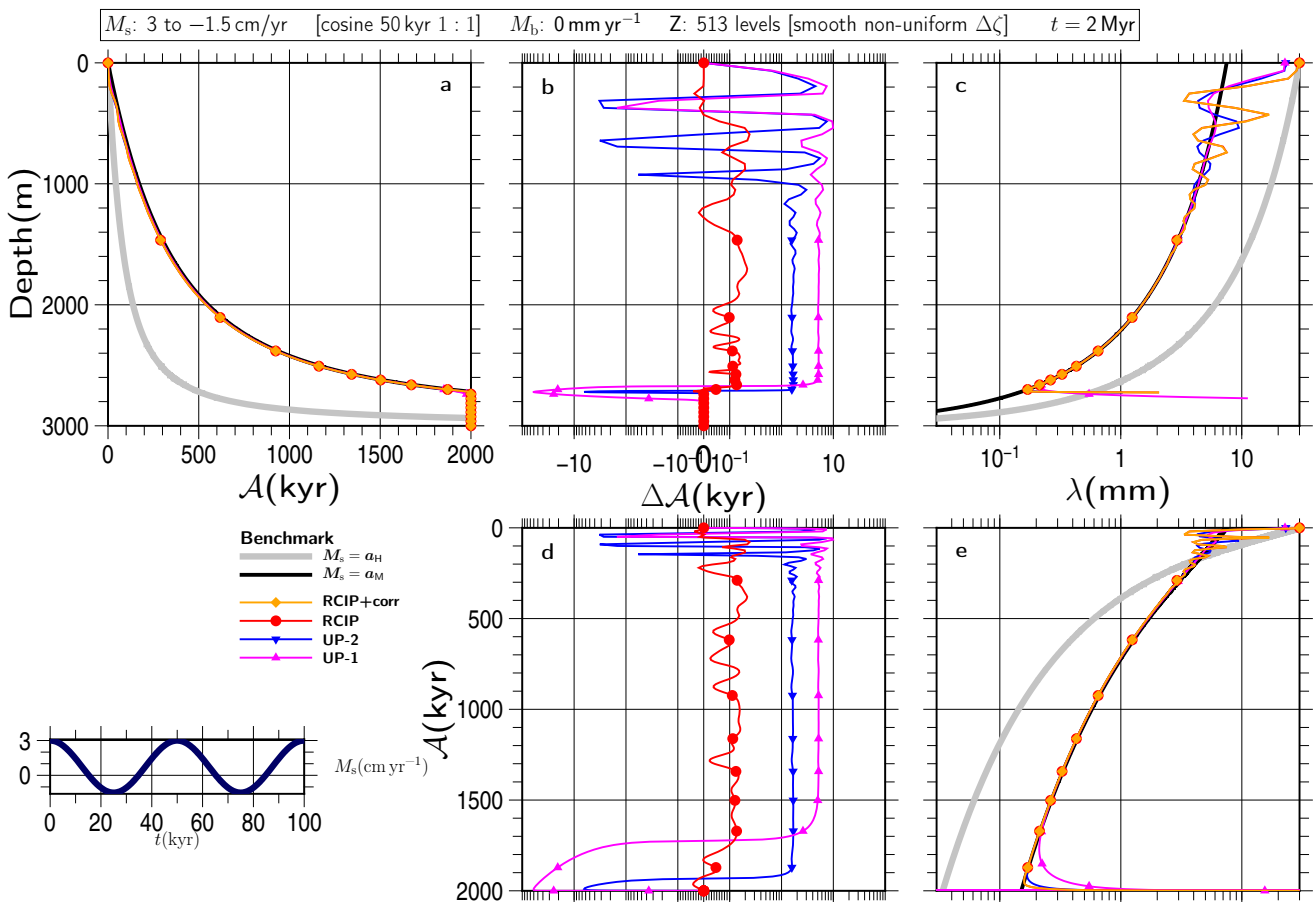
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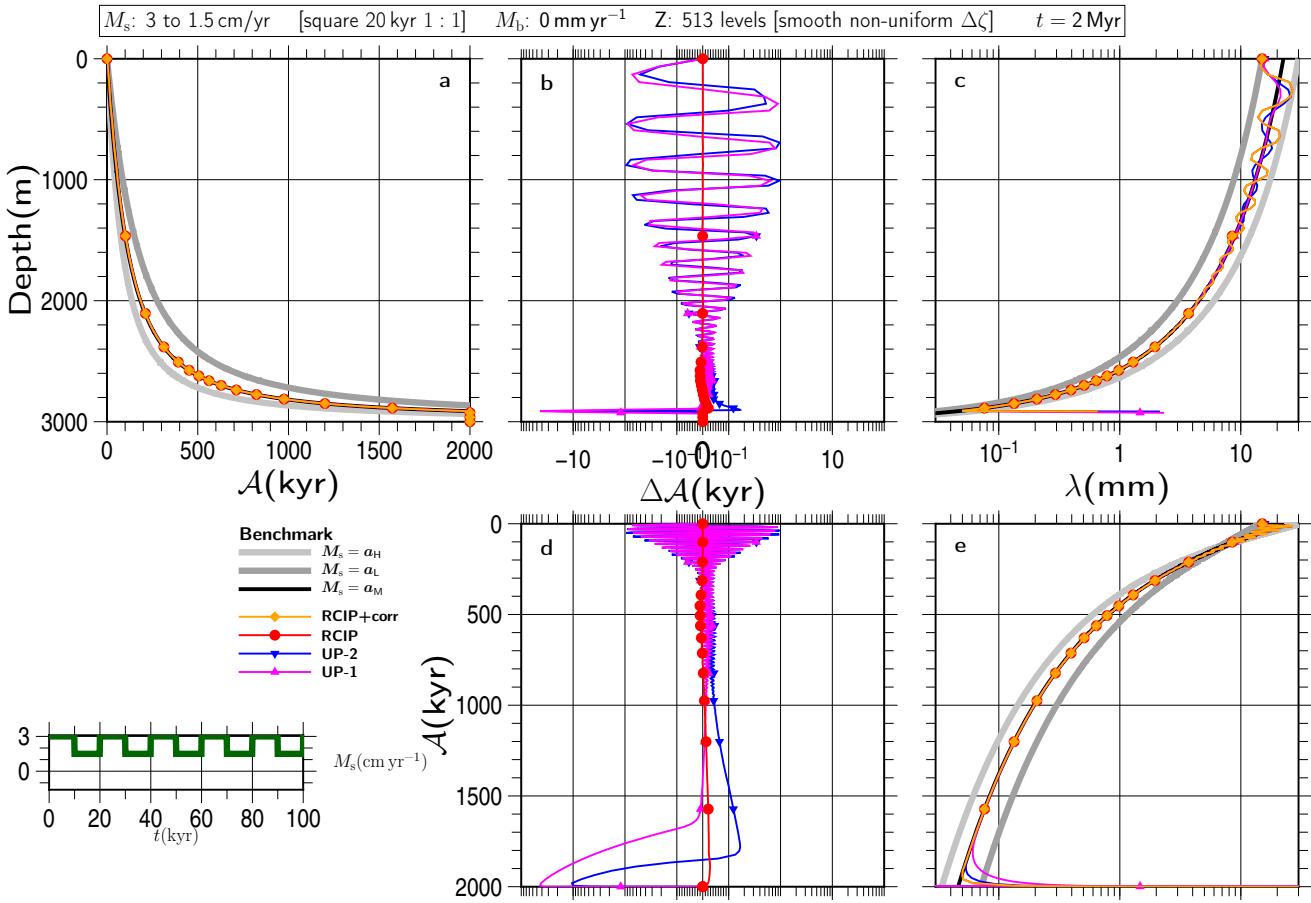
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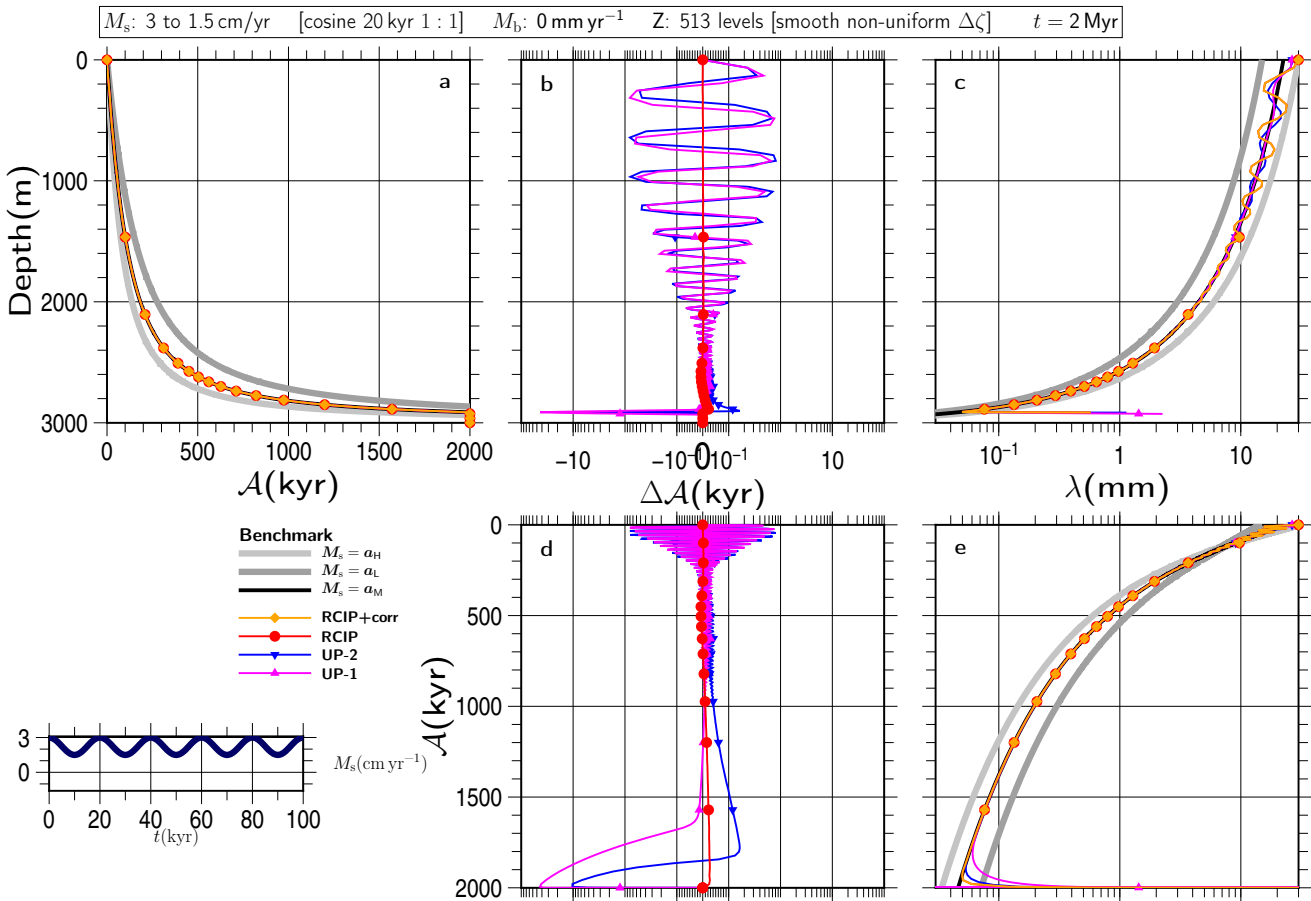
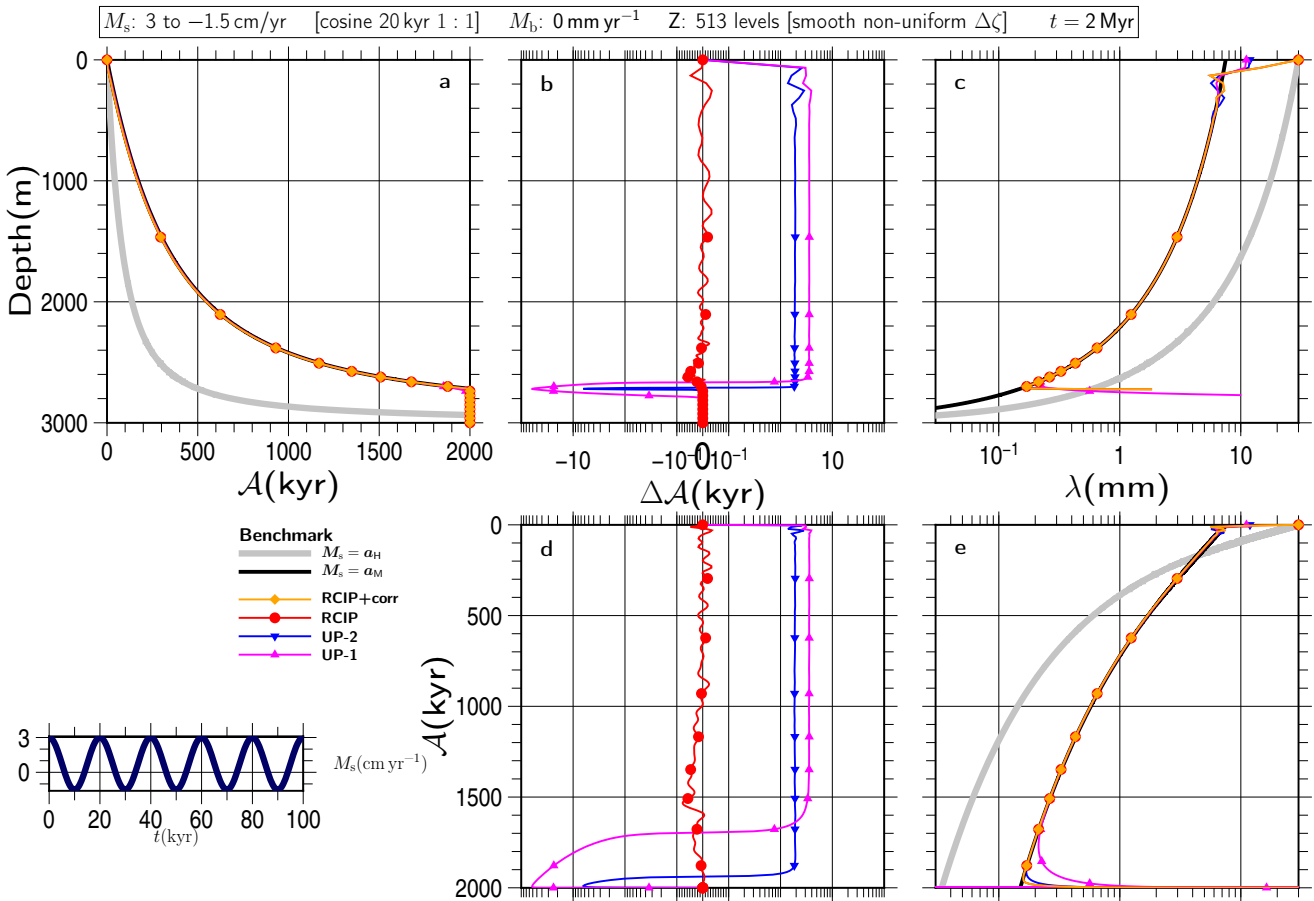Figure S112:
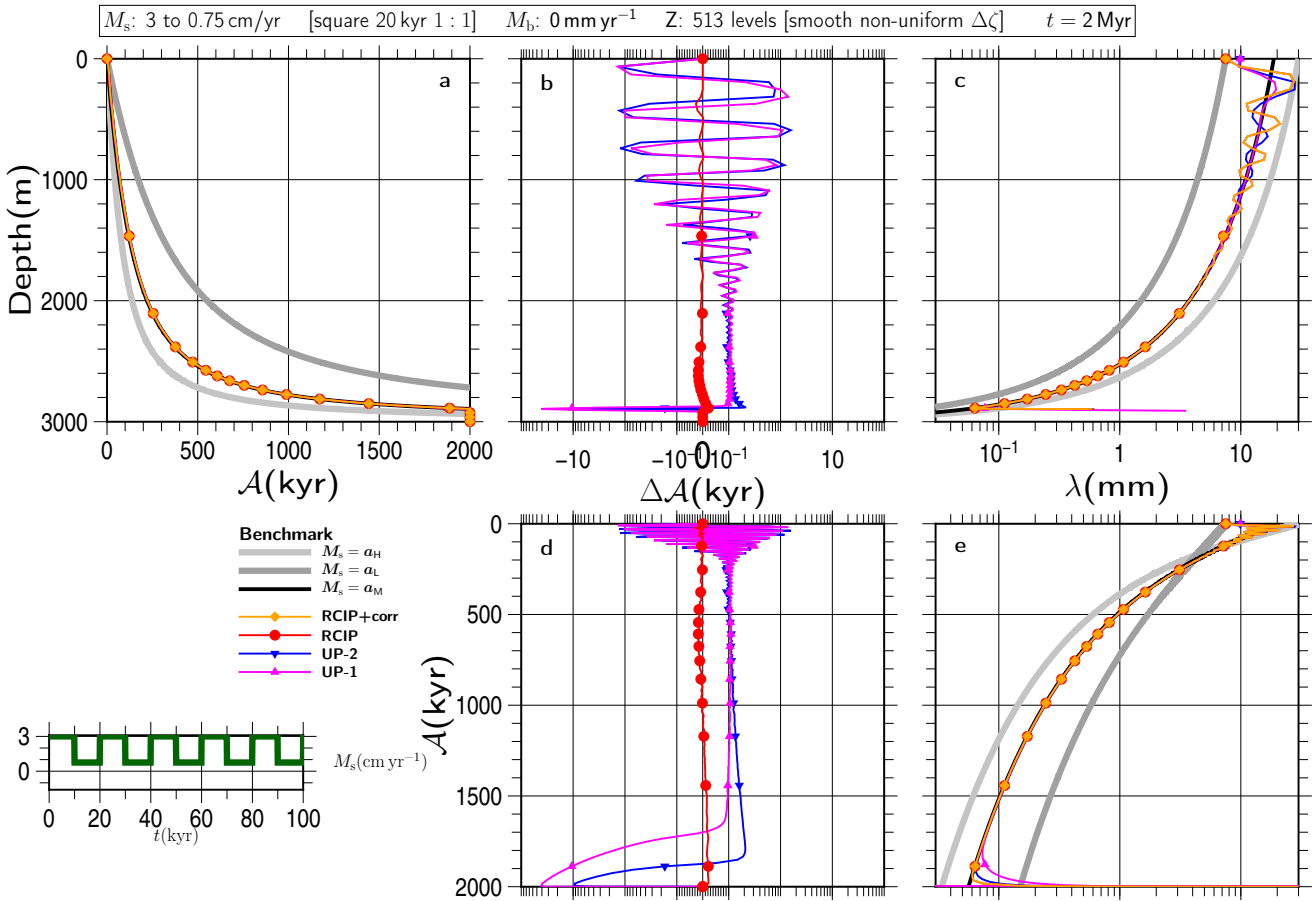
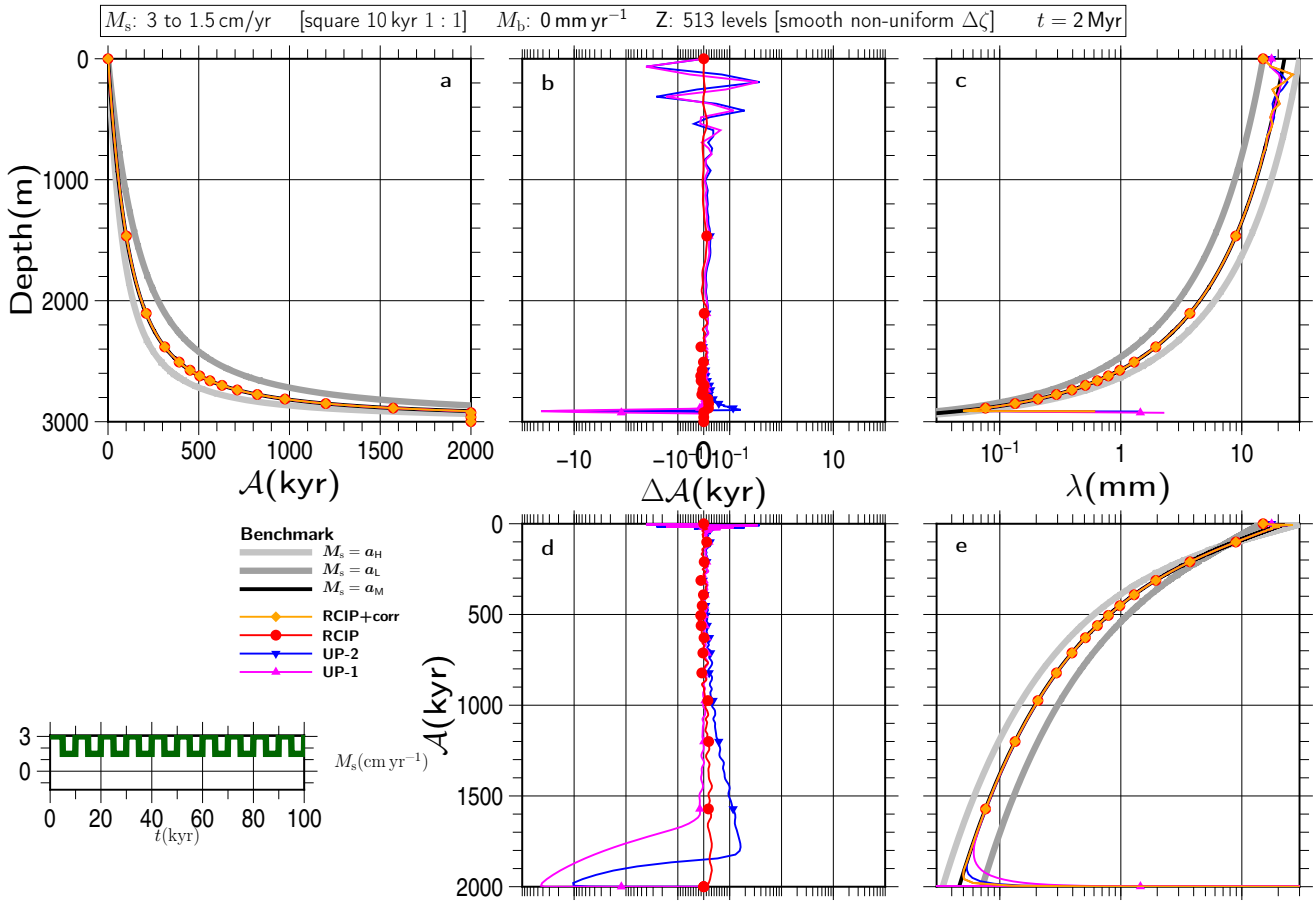Figure S113:
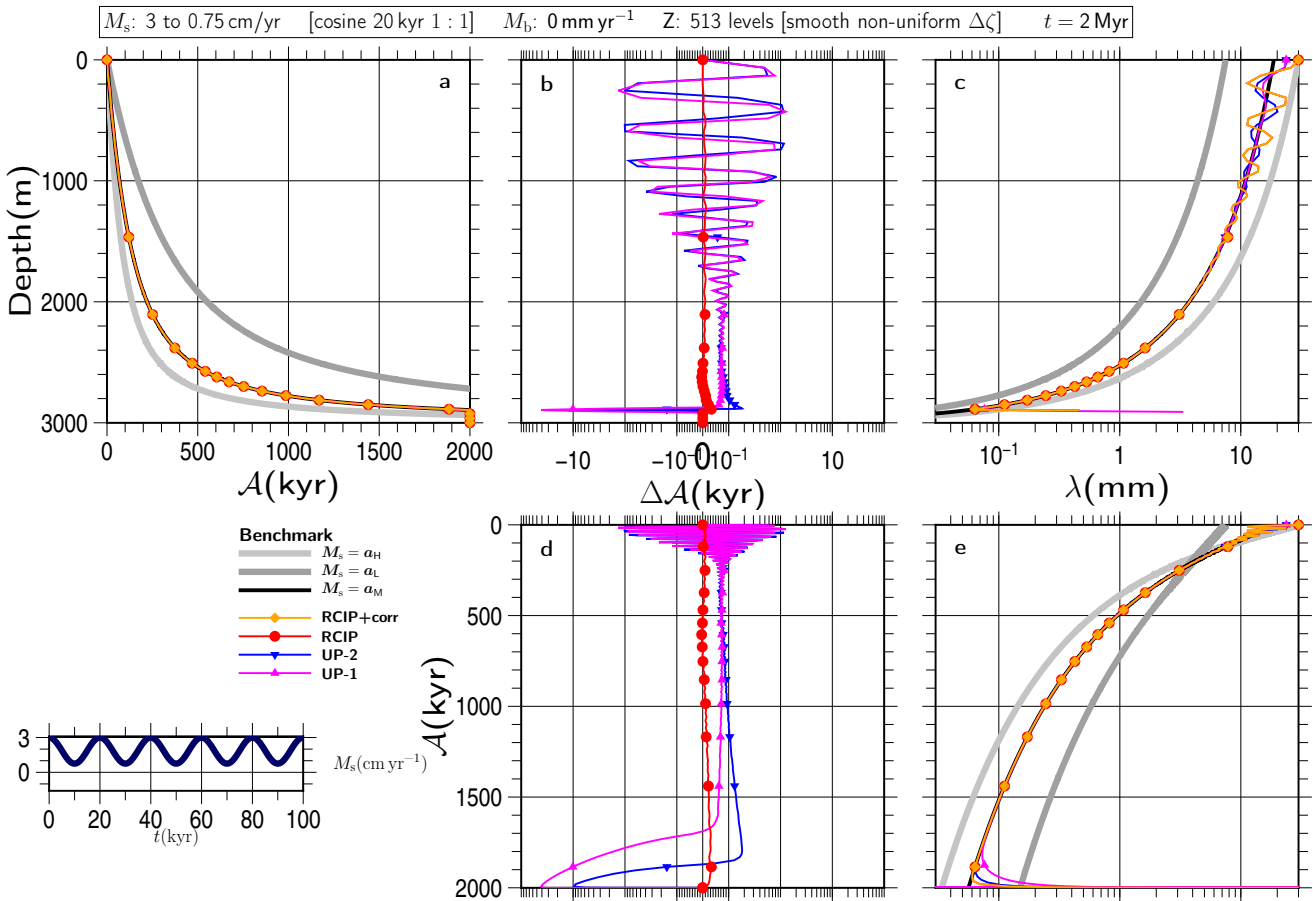
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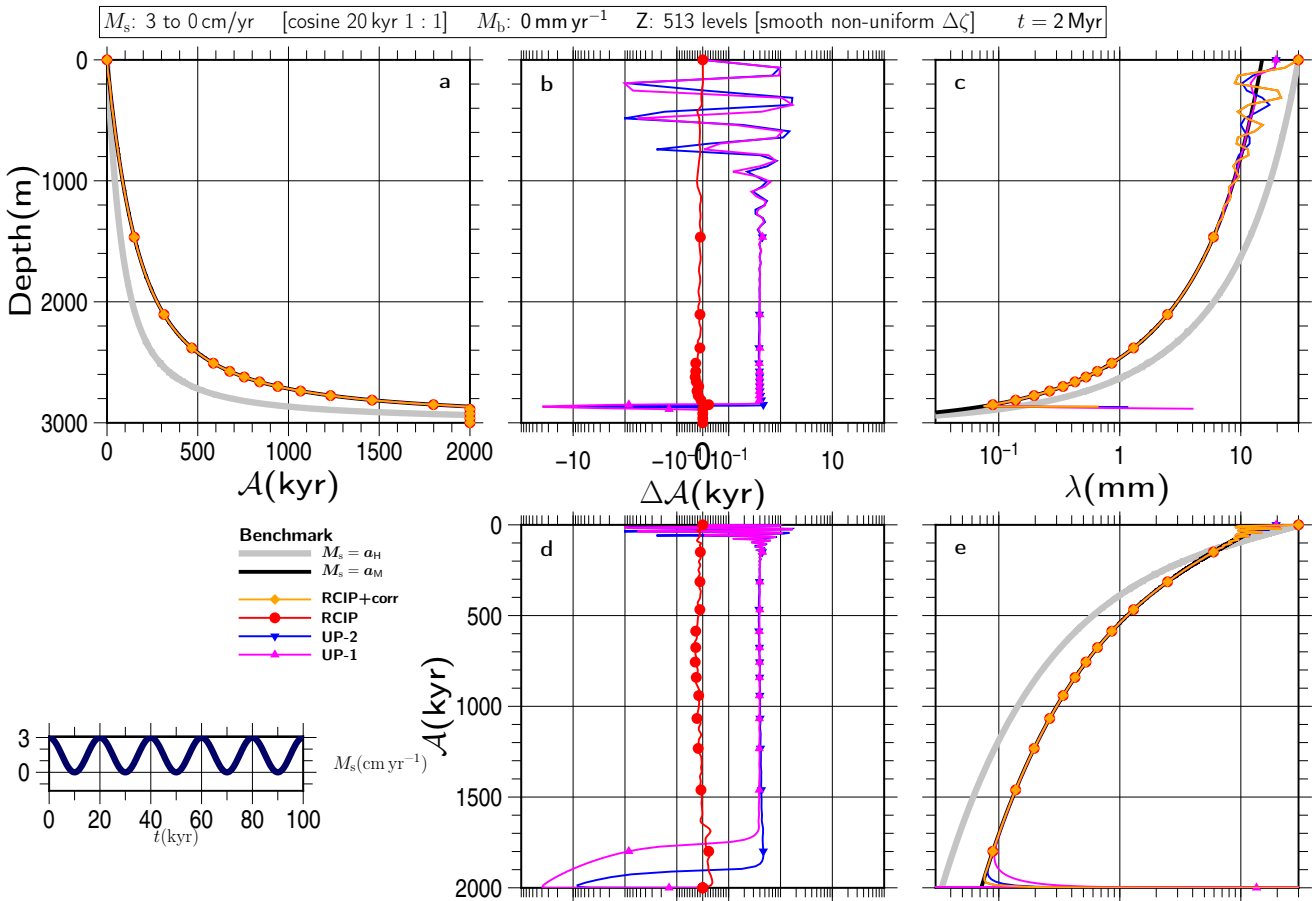
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Figure S117:

Figure S118:

Figure S119:
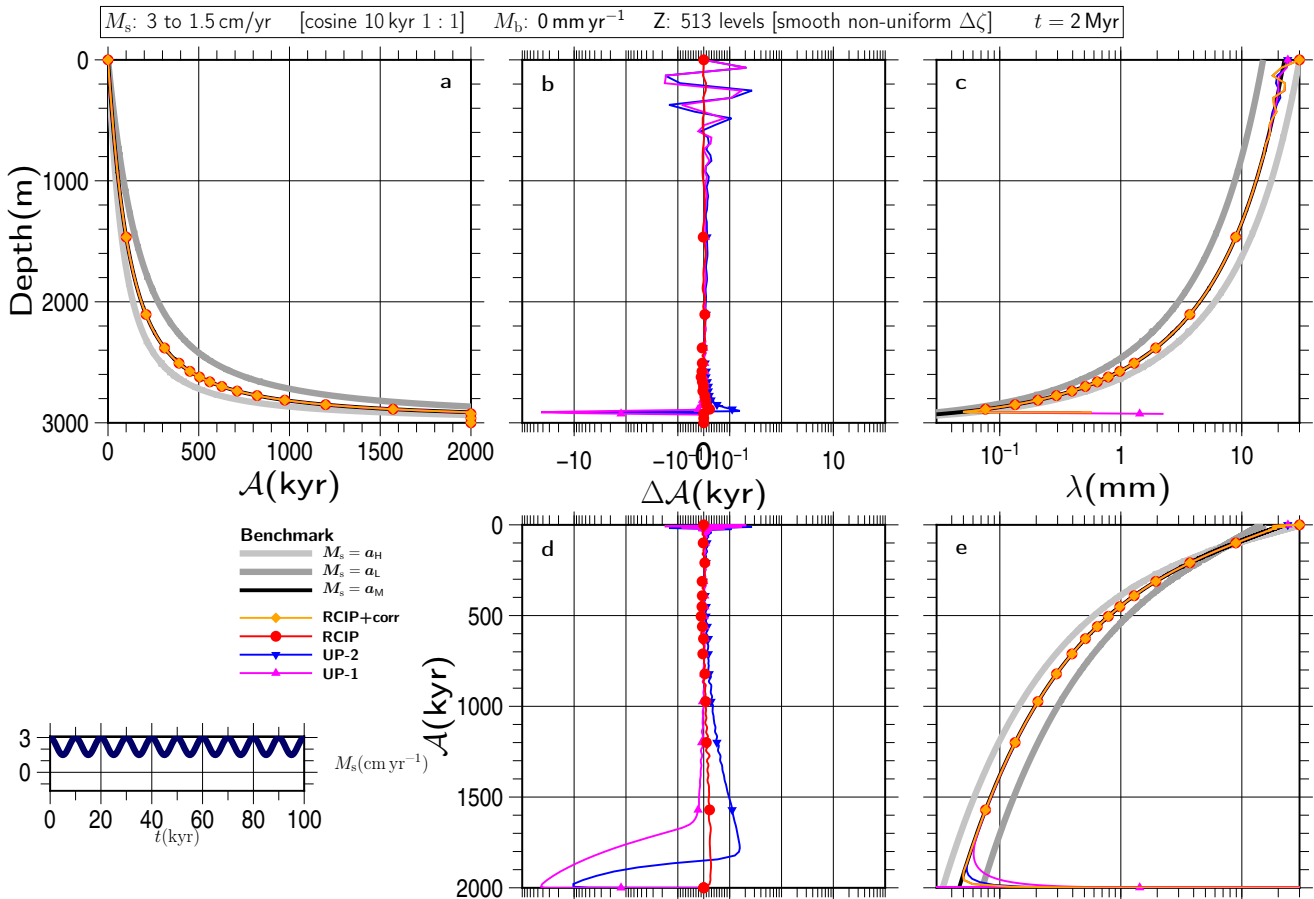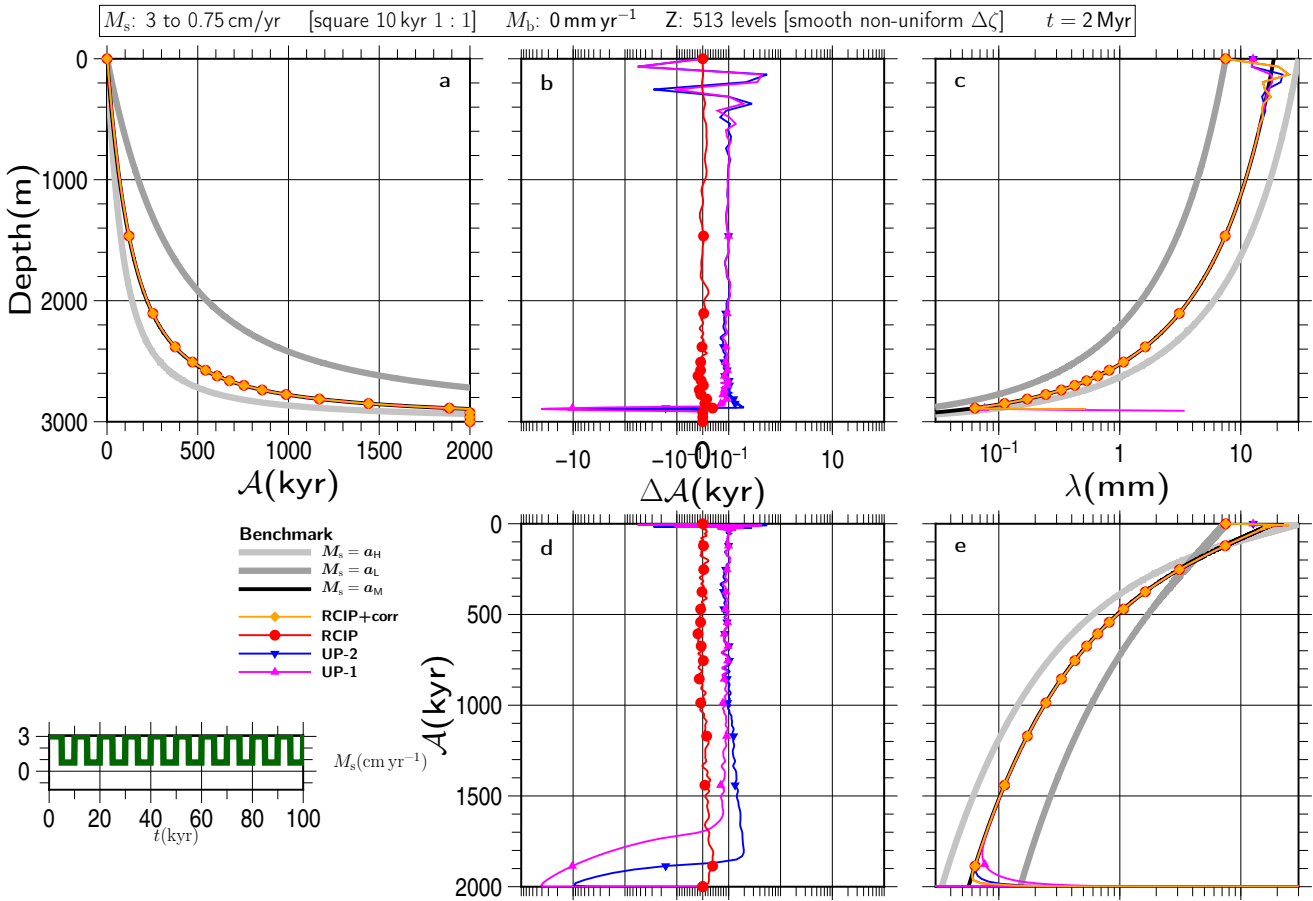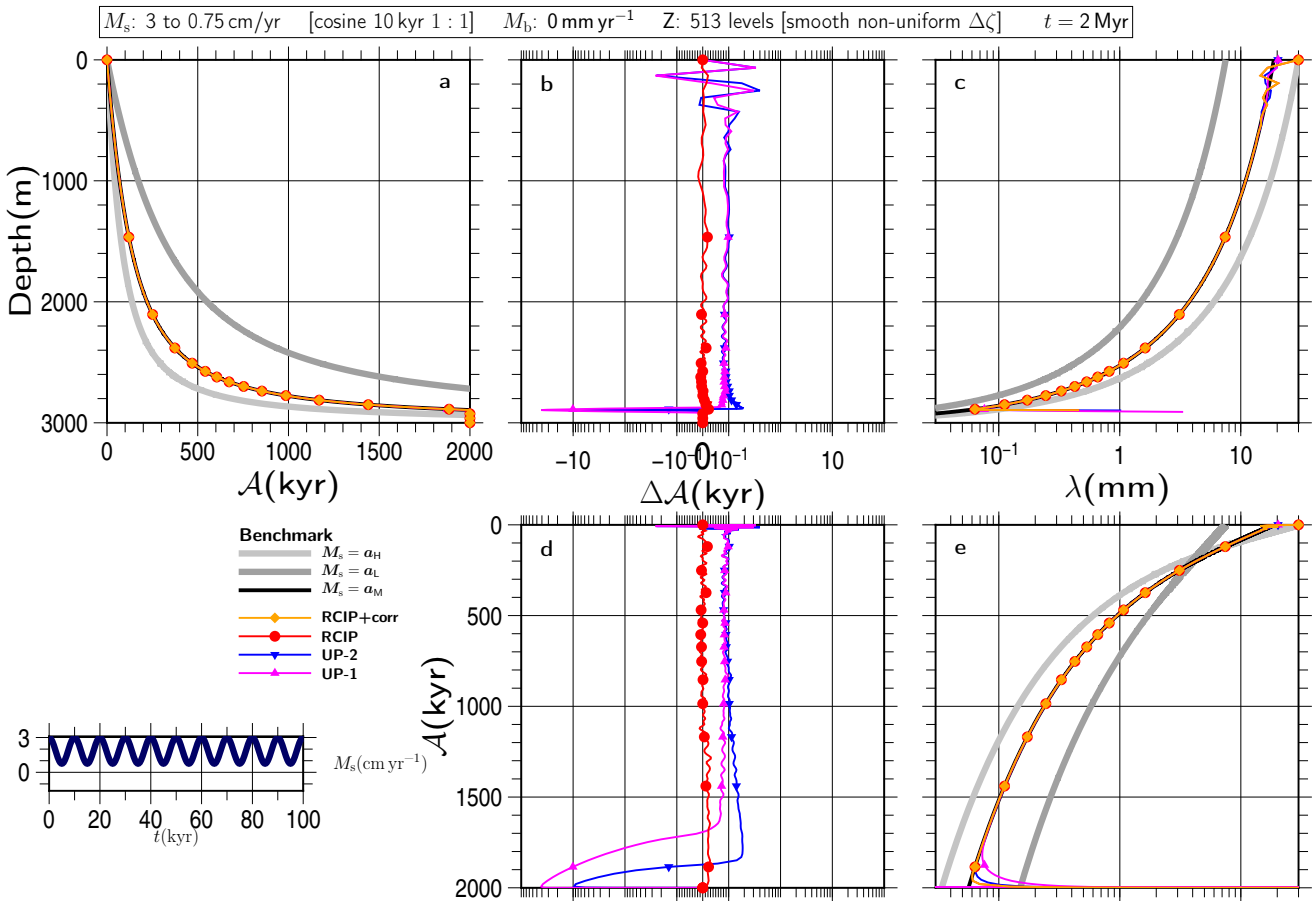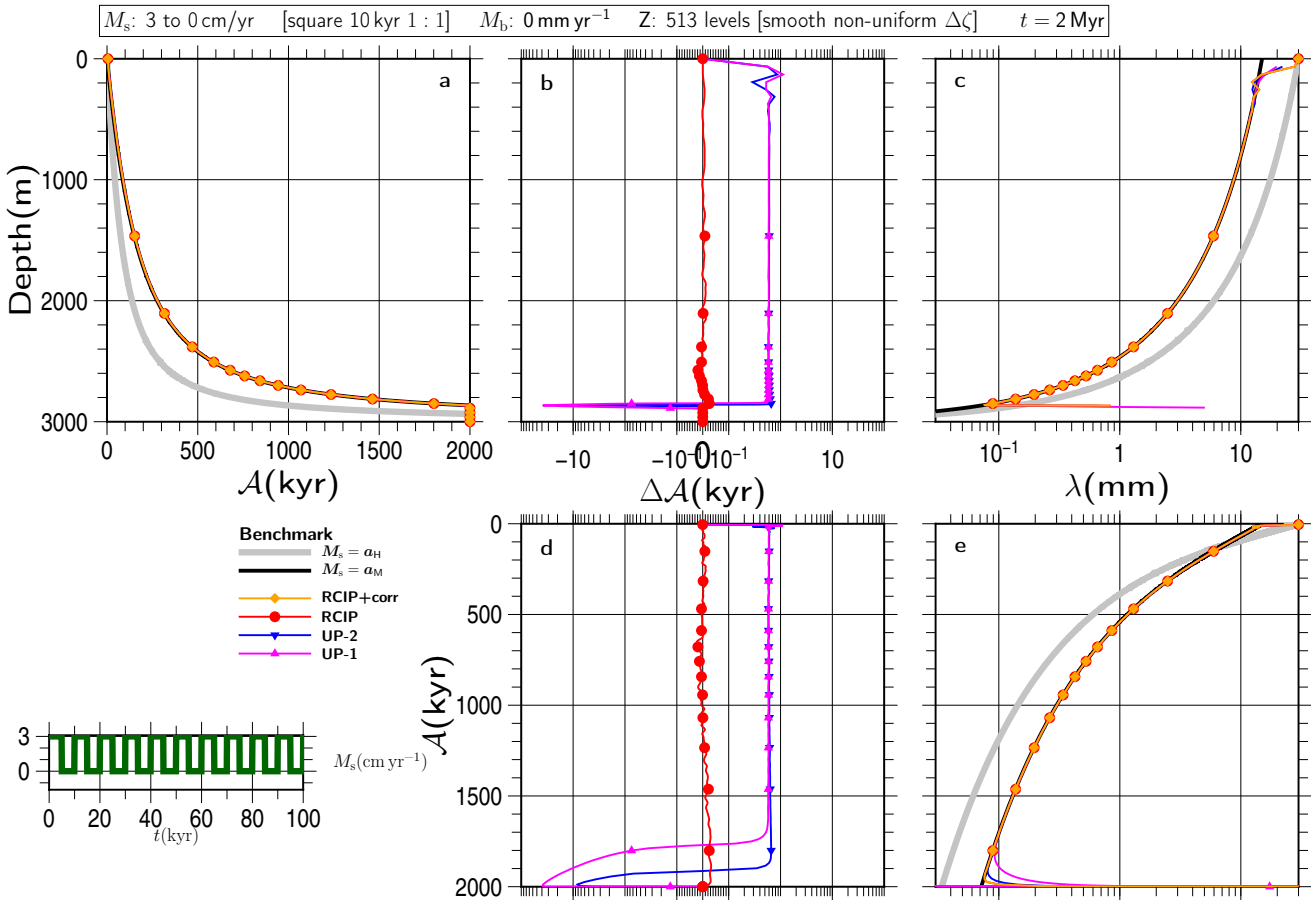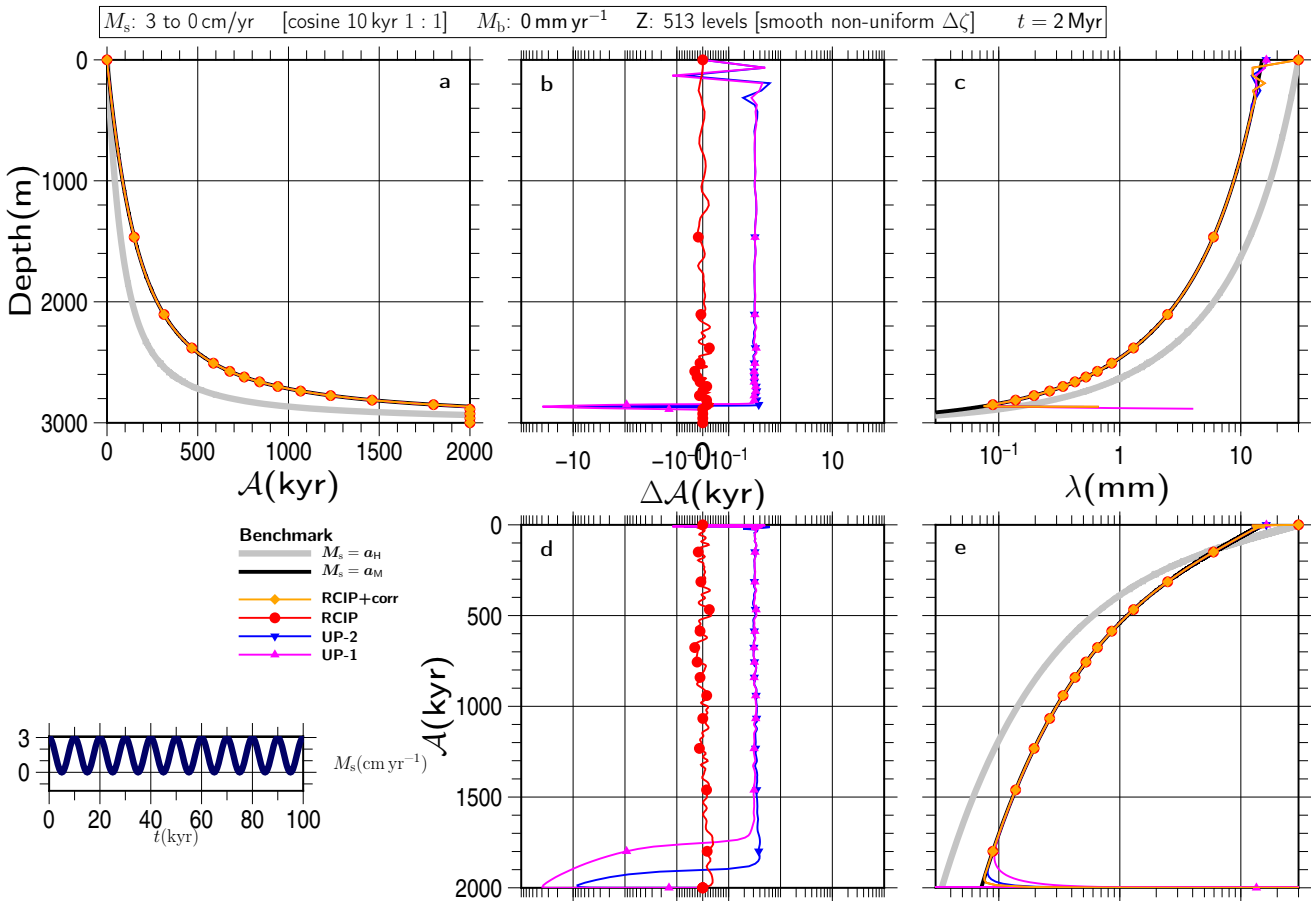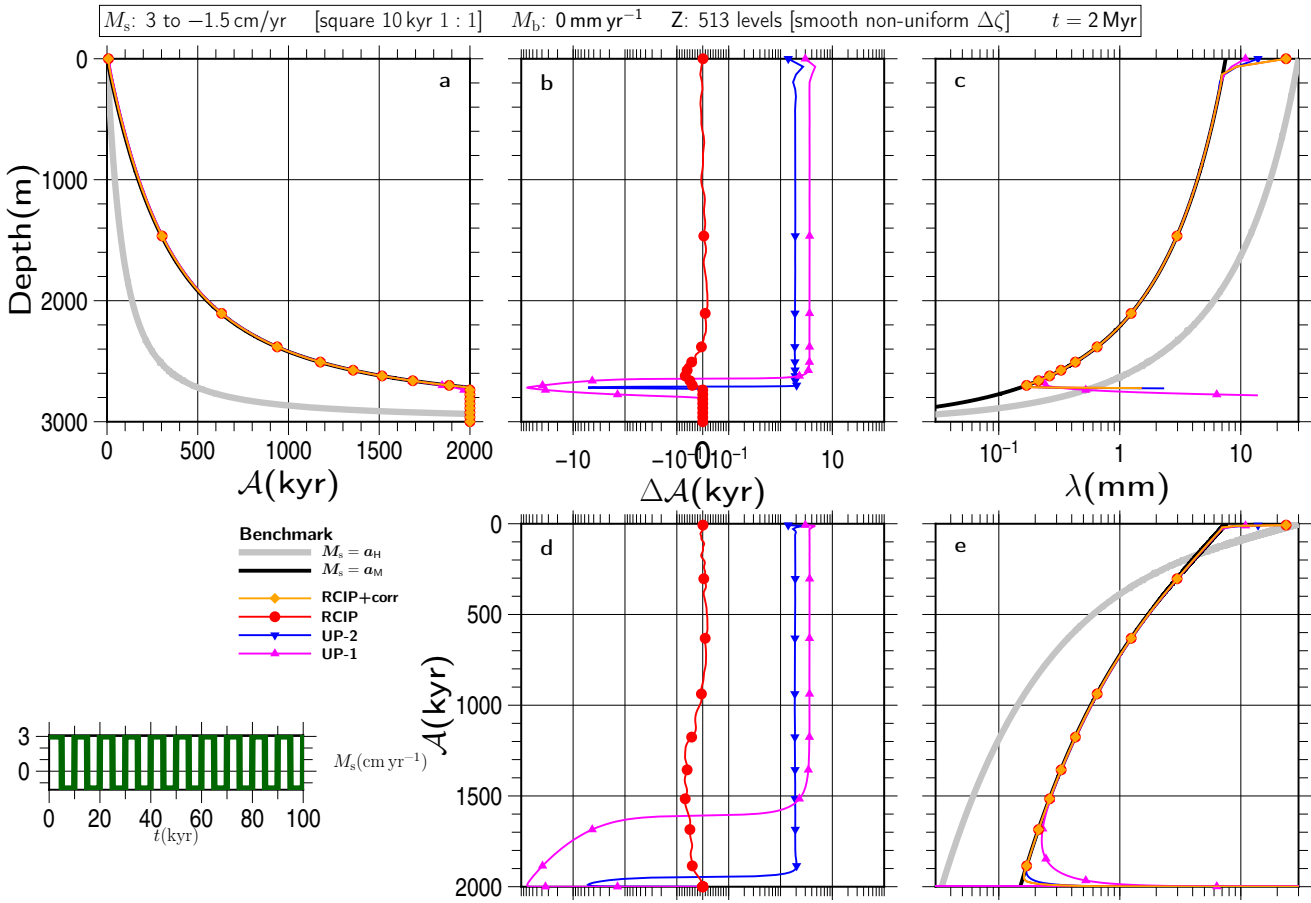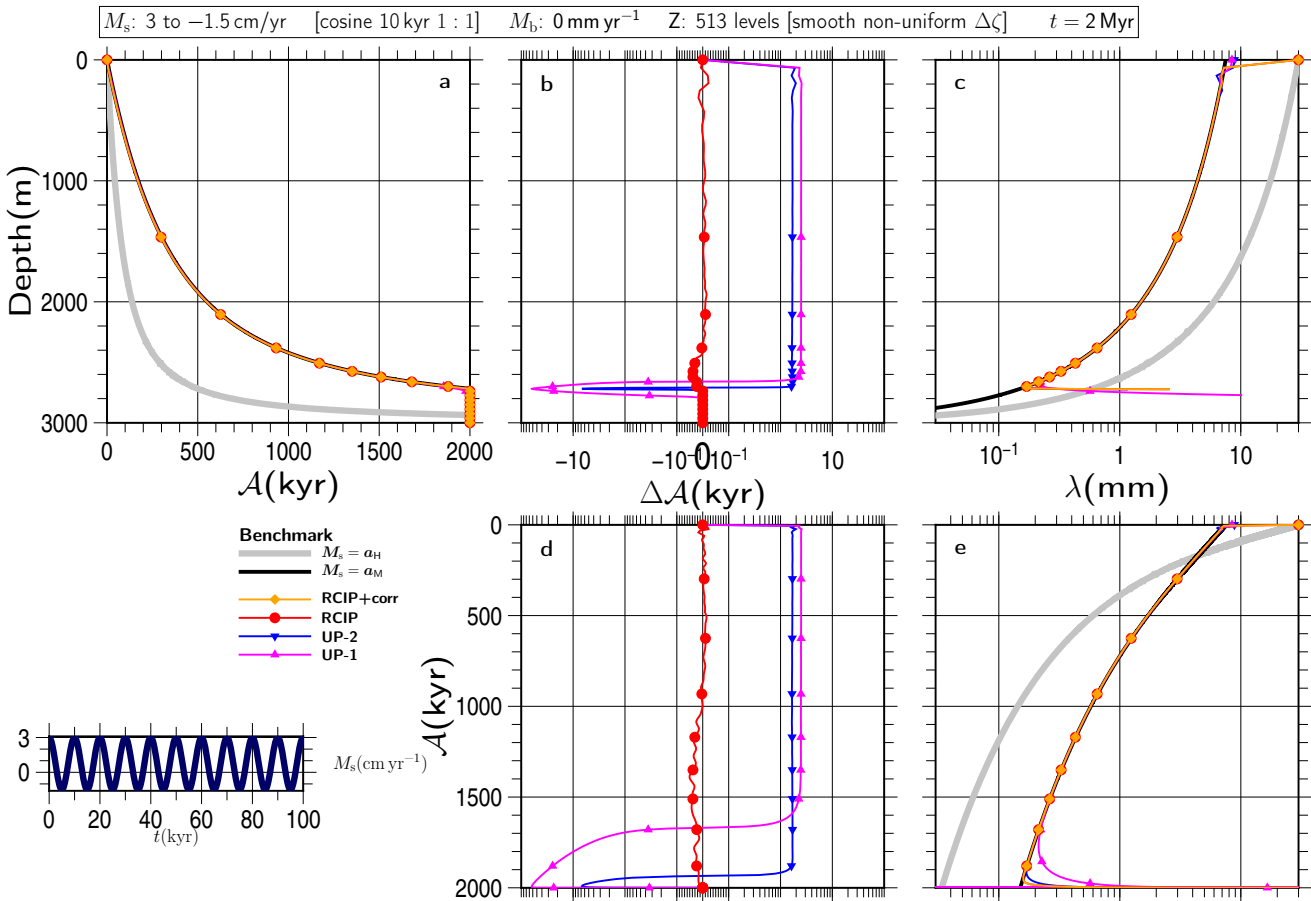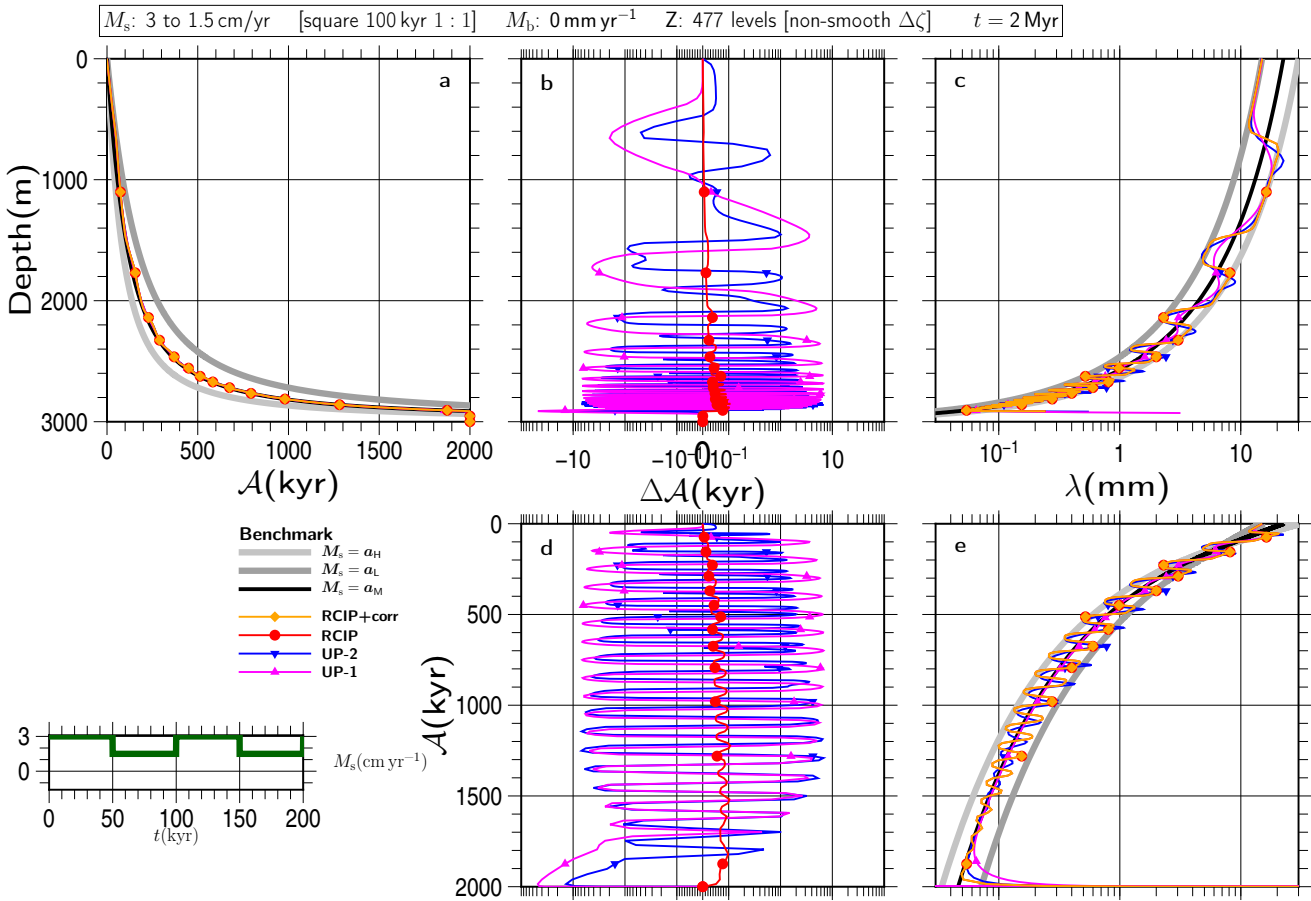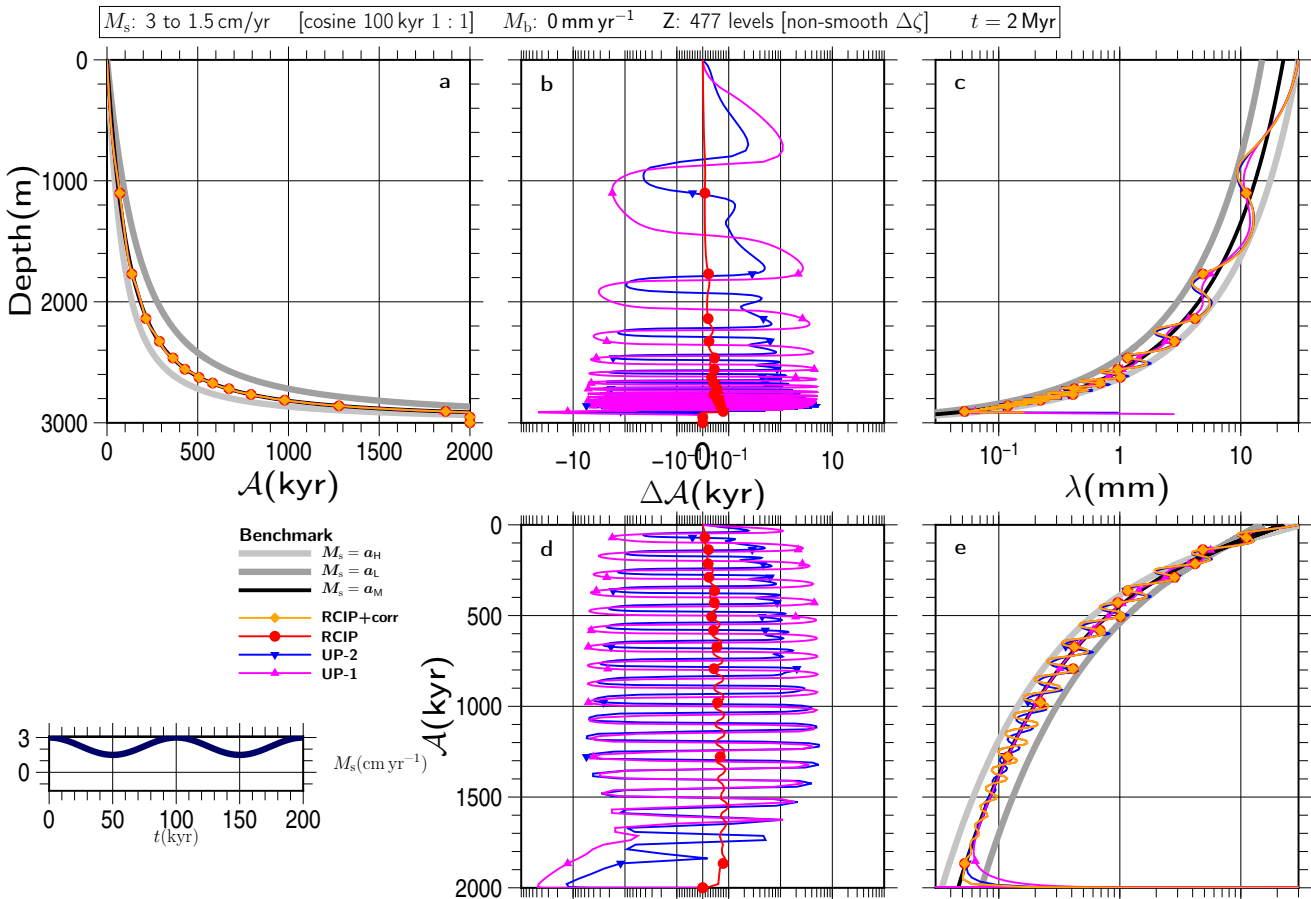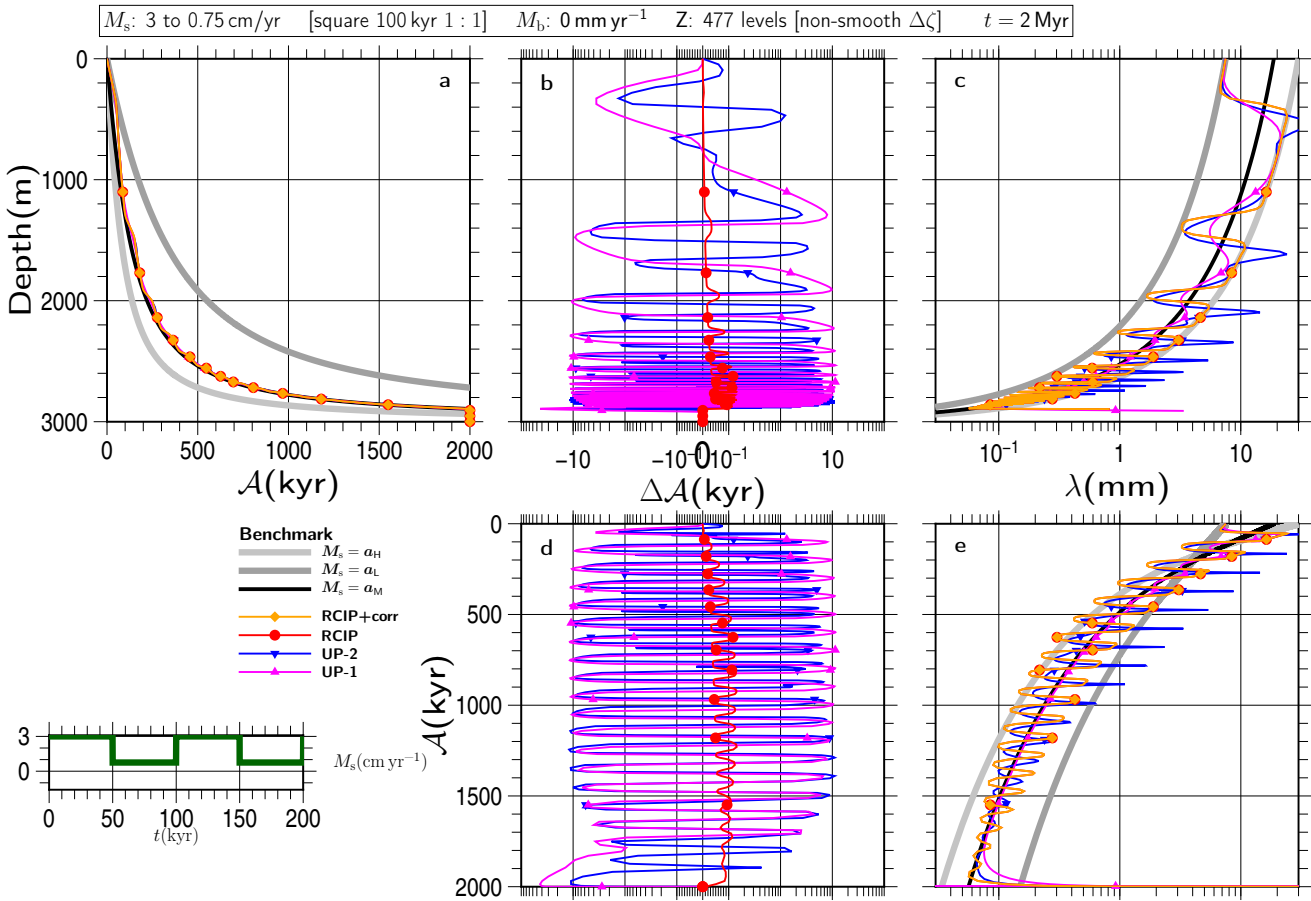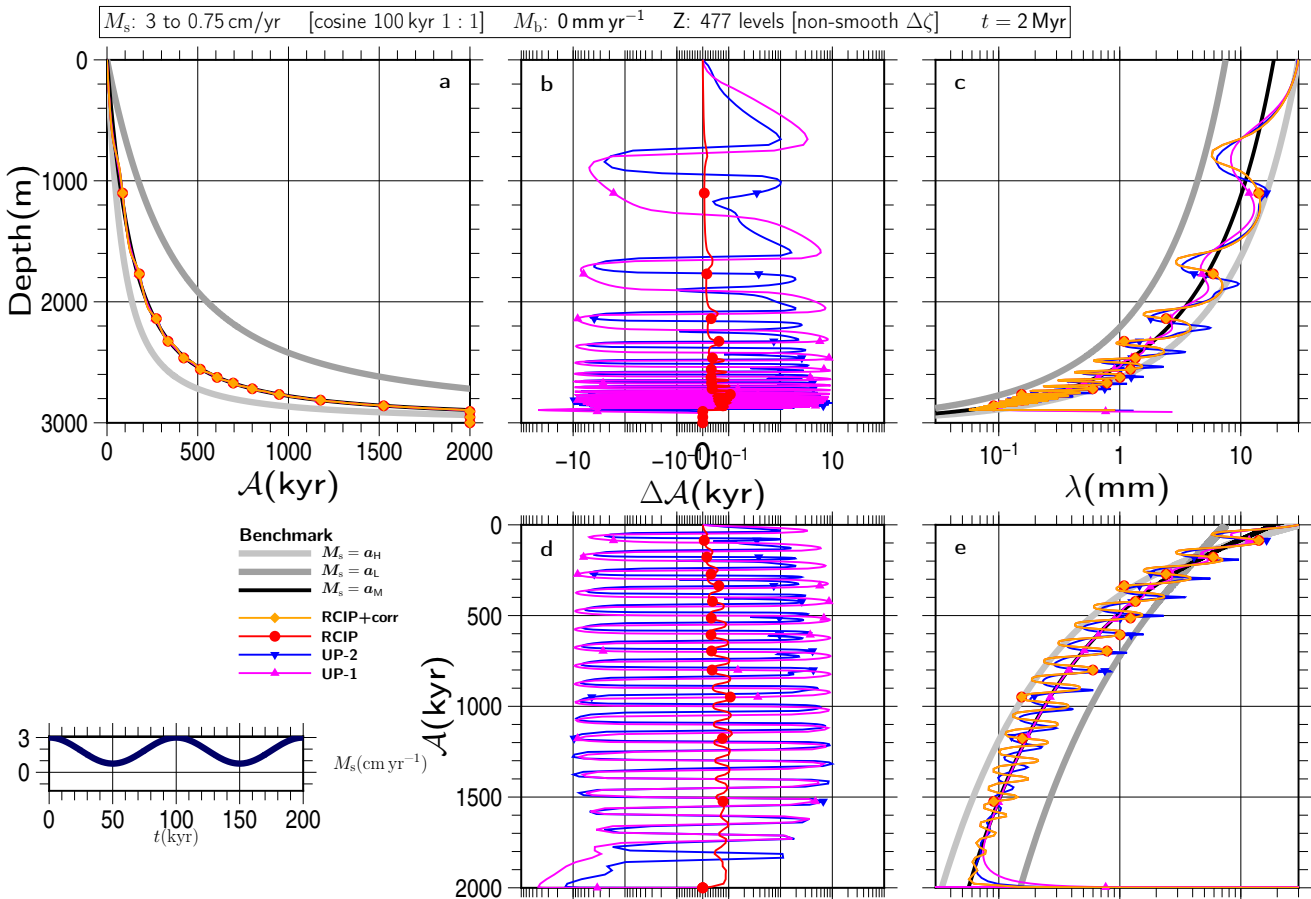

Figure S120:

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M_s: 3 to 0.75 cm/yr   [square 10 kyr 1 : 1] M_b: 0 mm yr^{-1} Z: 513 levels [smooth non-uniform $\Delta\zeta$] $t = 2\,\text{Myr}$

Benchmark
$M_\text{s} = a_\text{H}$
$M_\text{s} = a_\text{L}$
$M_\text{s} = a_\text{M}$
RCIP+corr
RCIP
UP-2
UP-1

Figure S121:

M_s: 3 to 0.75 cm/yr   [cosine 10 kyr 1 : 1] M_b: 0 mm yr^{-1} Z: 513 levels [smooth non-uniform $\Delta\zeta$] $t = 2\,\text{Myr}$

Benchmark
$M_\text{s} = a_\text{H}$
$M_\text{s} = a_\text{L}$
$M_\text{s} = a_\text{M}$
RCIP+corr
RCIP
UP-2
UP-1

Figure S122:

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Figure S123:

Figure S124:

63

Figure S125:

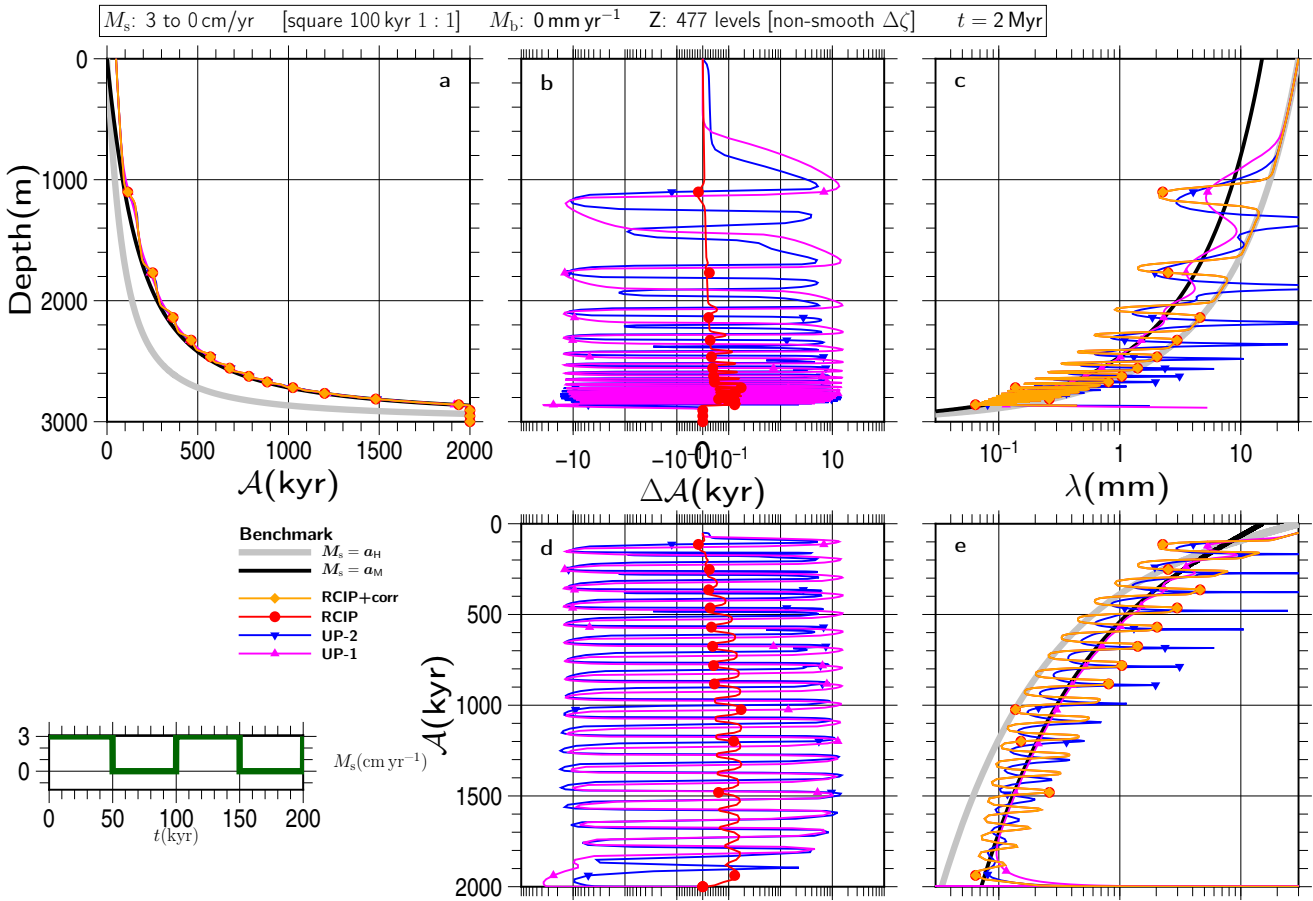Figure S126:
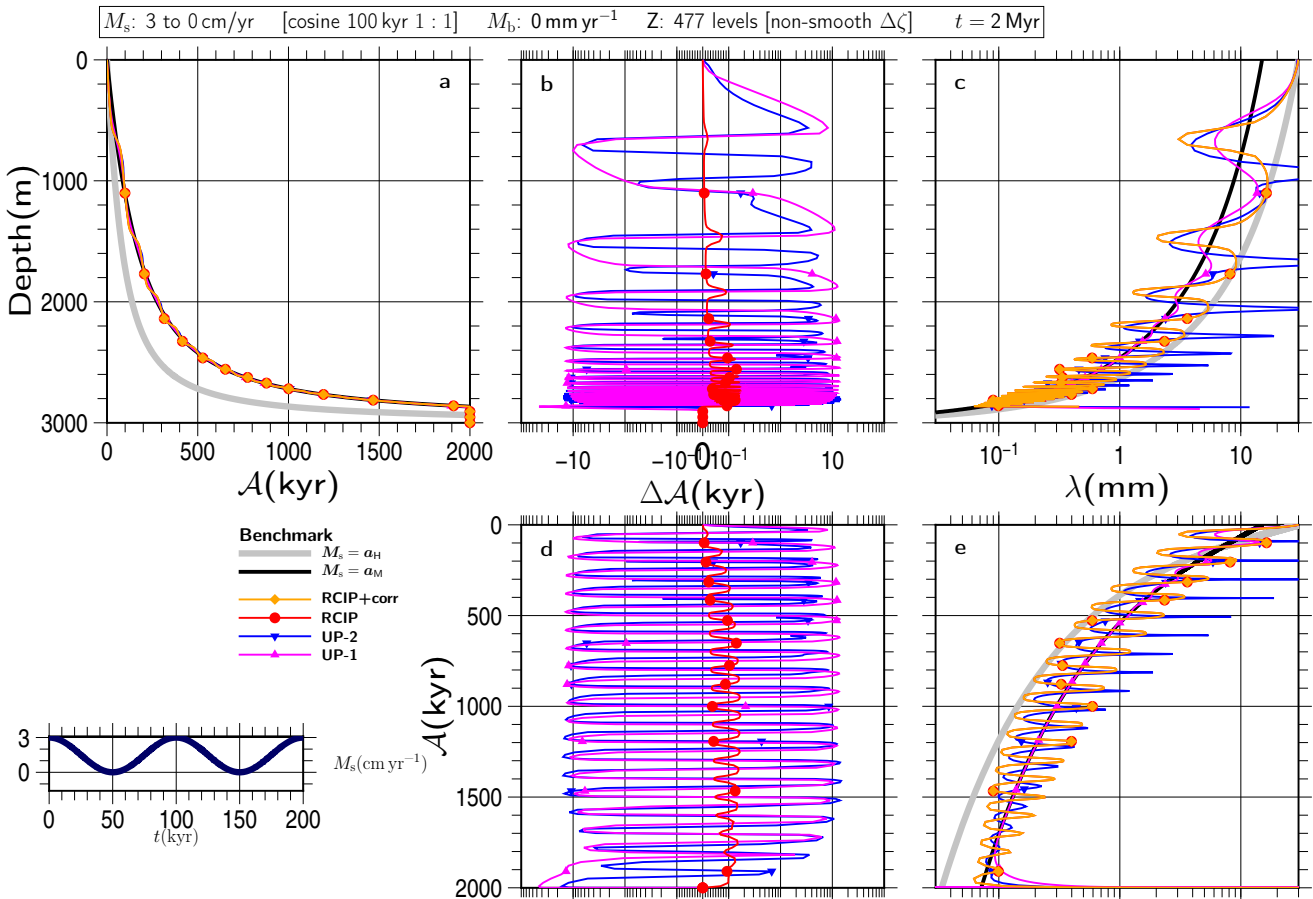
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Figure S127:

Figure S128:

Figure S129:

Figure S130:

Figure S131:

Figure S132:
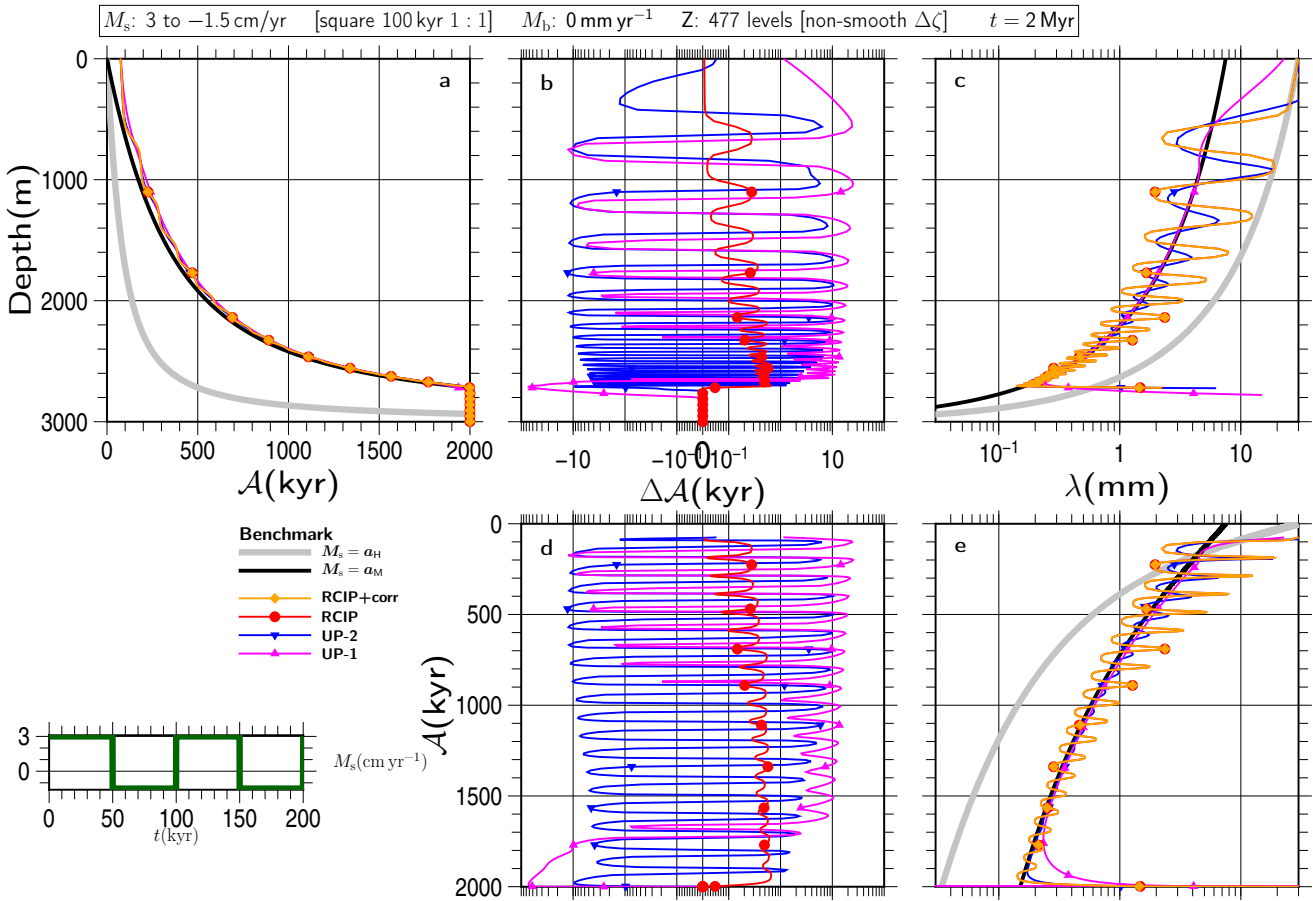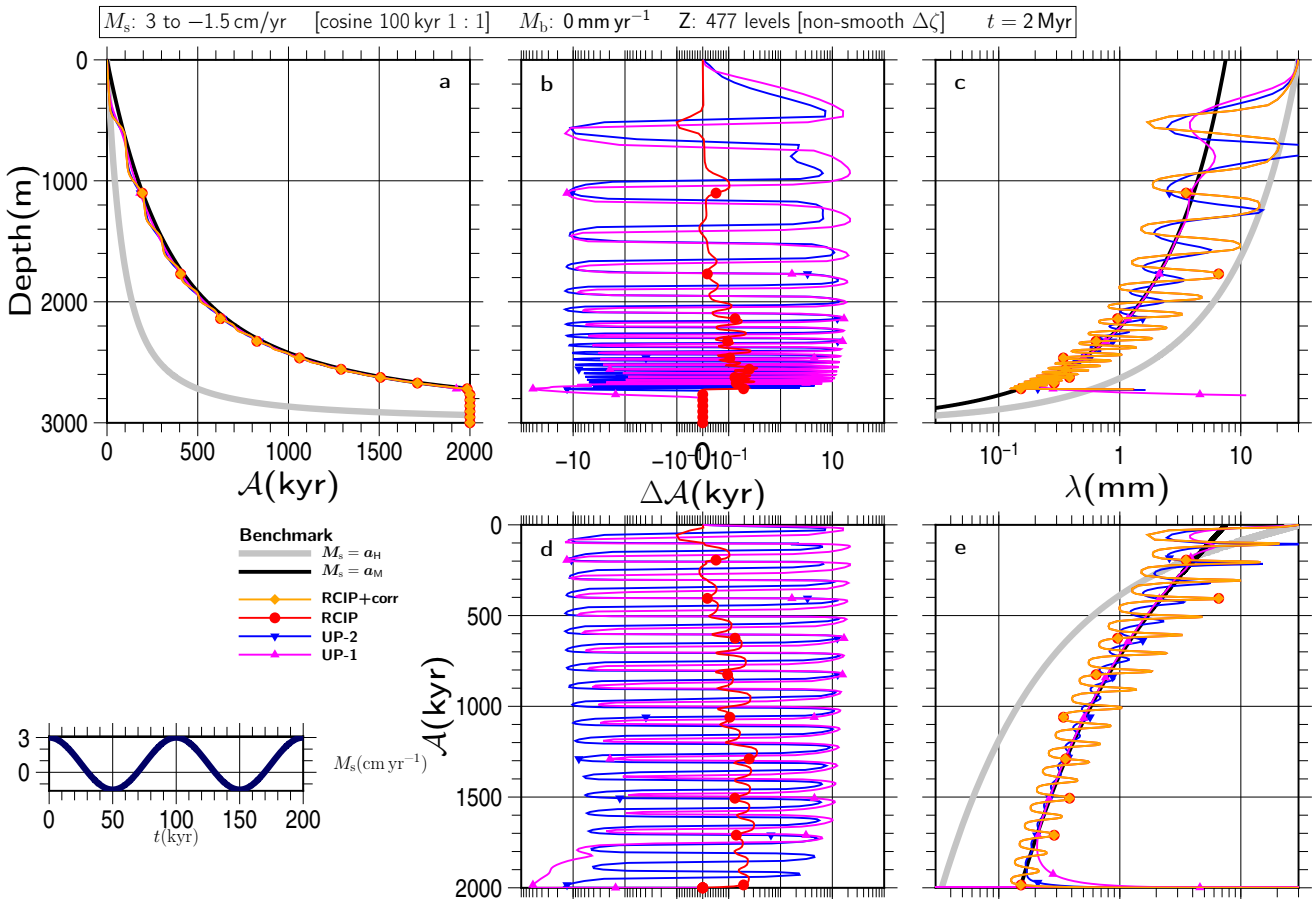
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Figure S134:
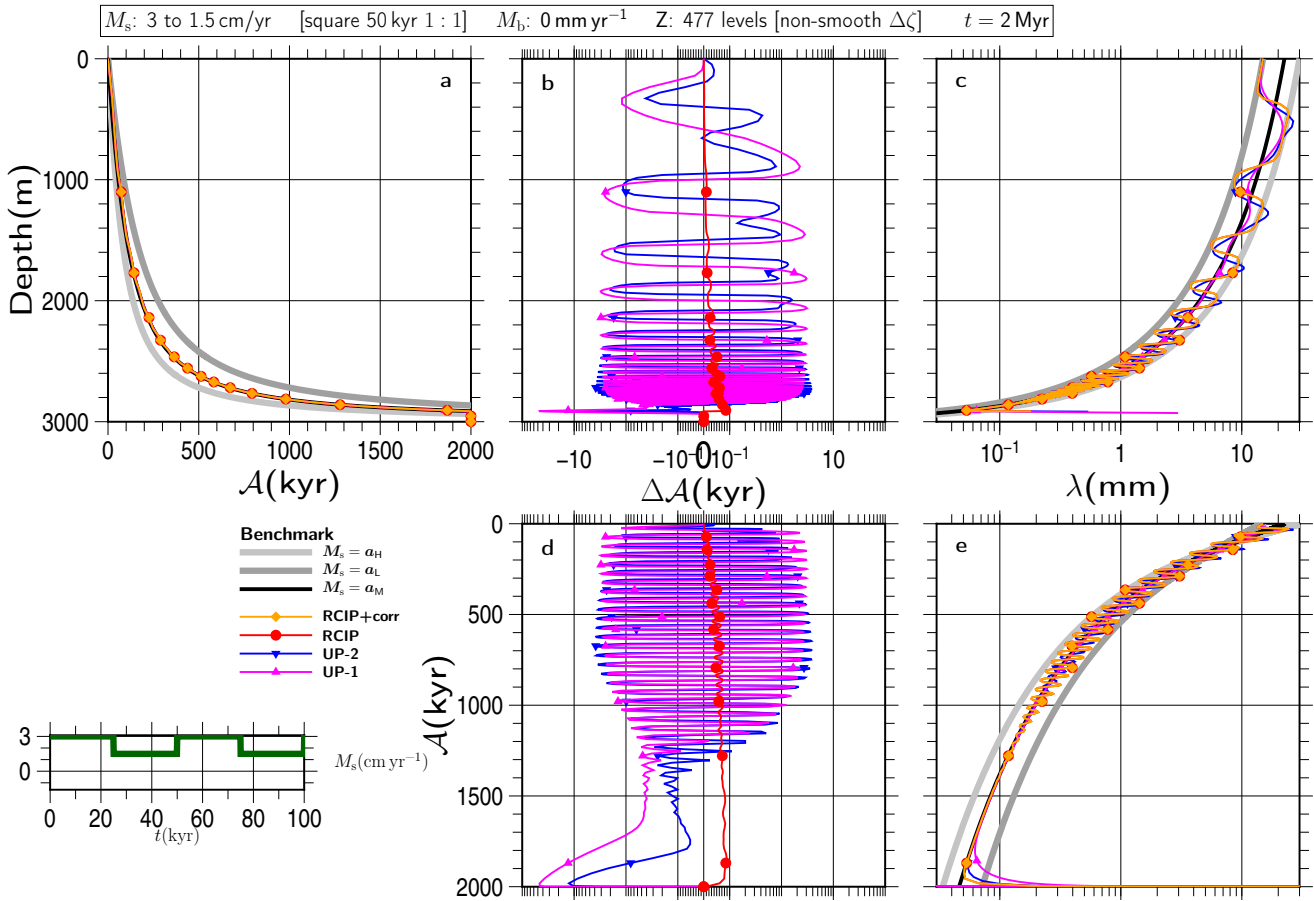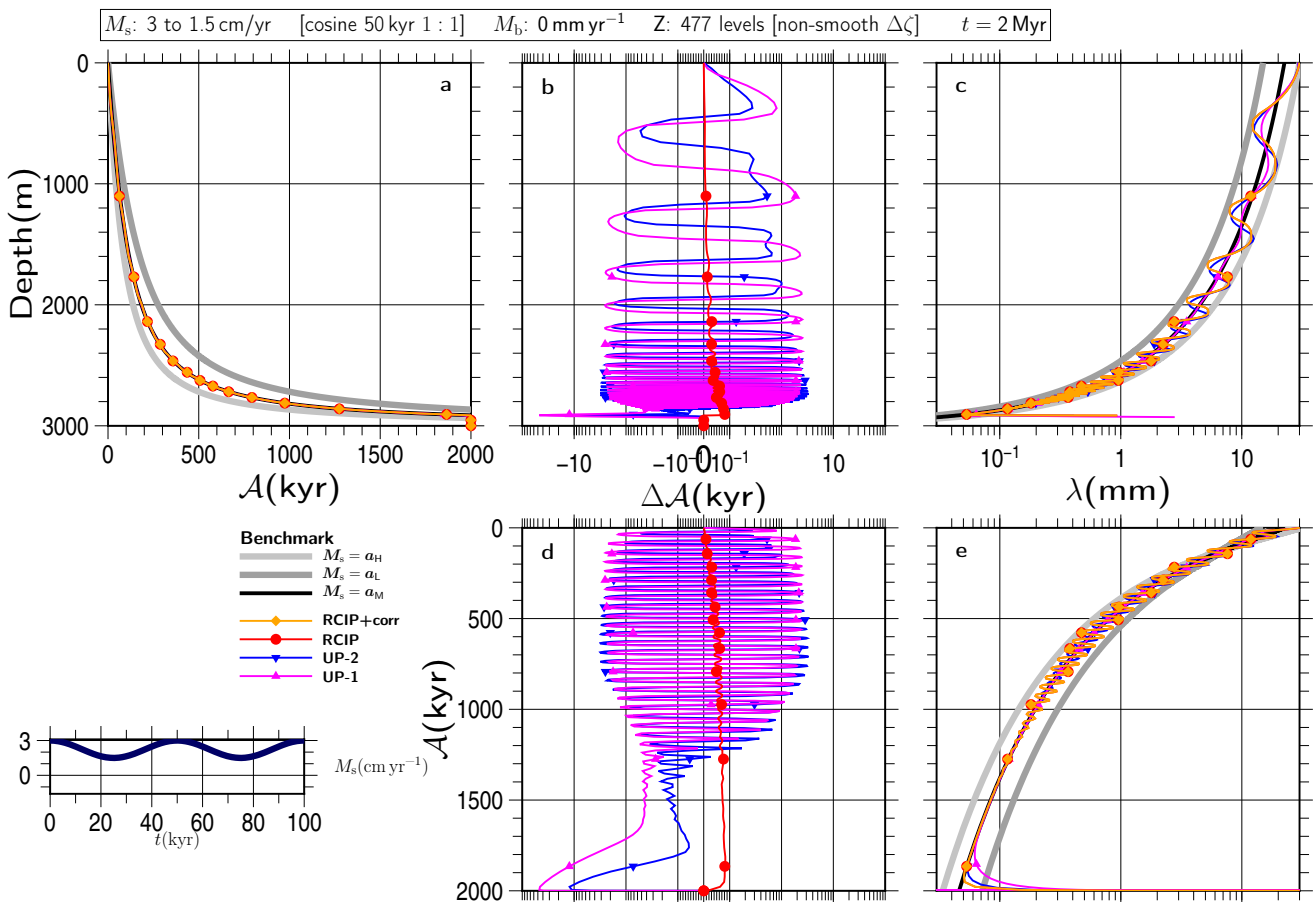
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Figure S136:
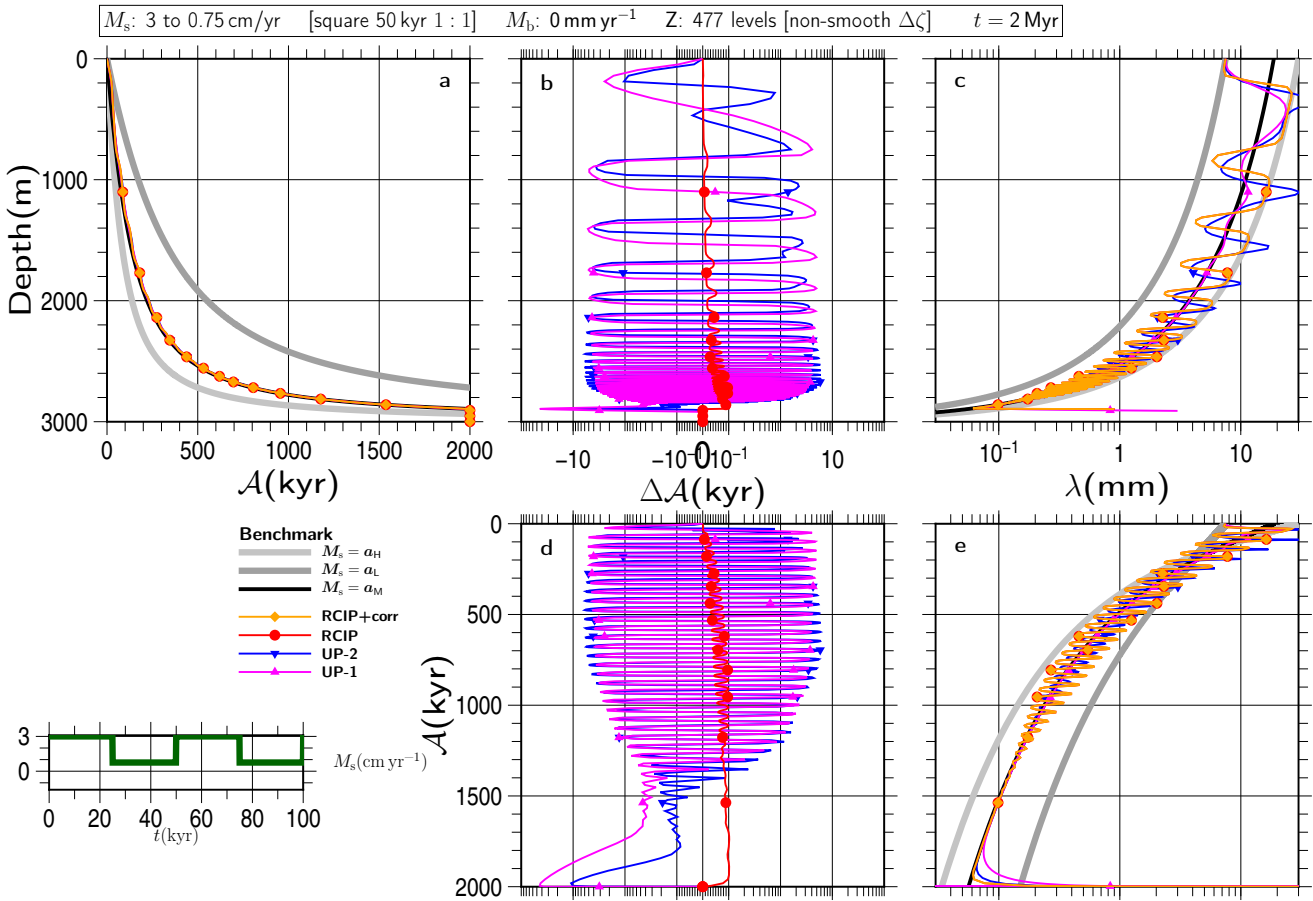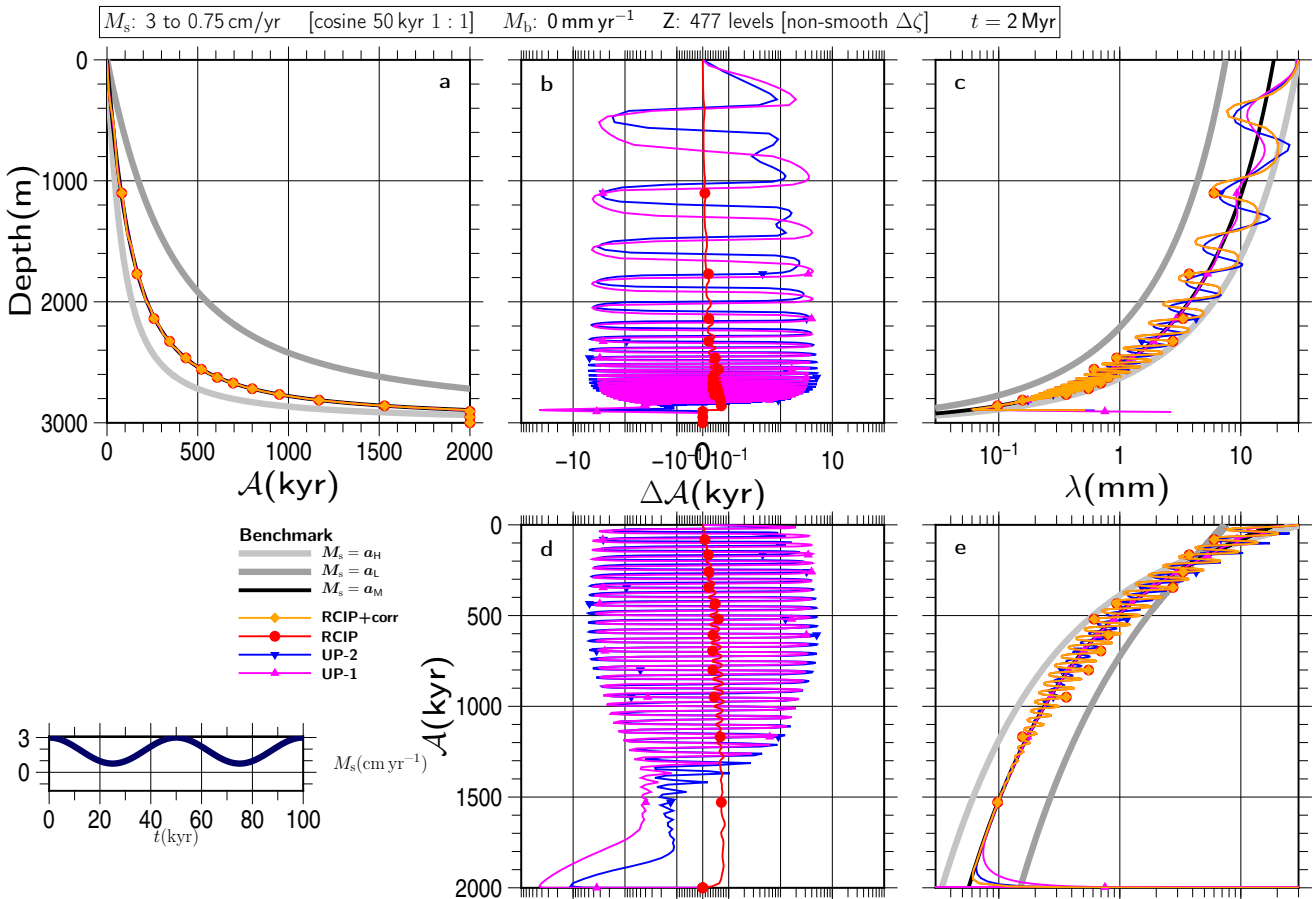
Figure S137:

Figure S138:
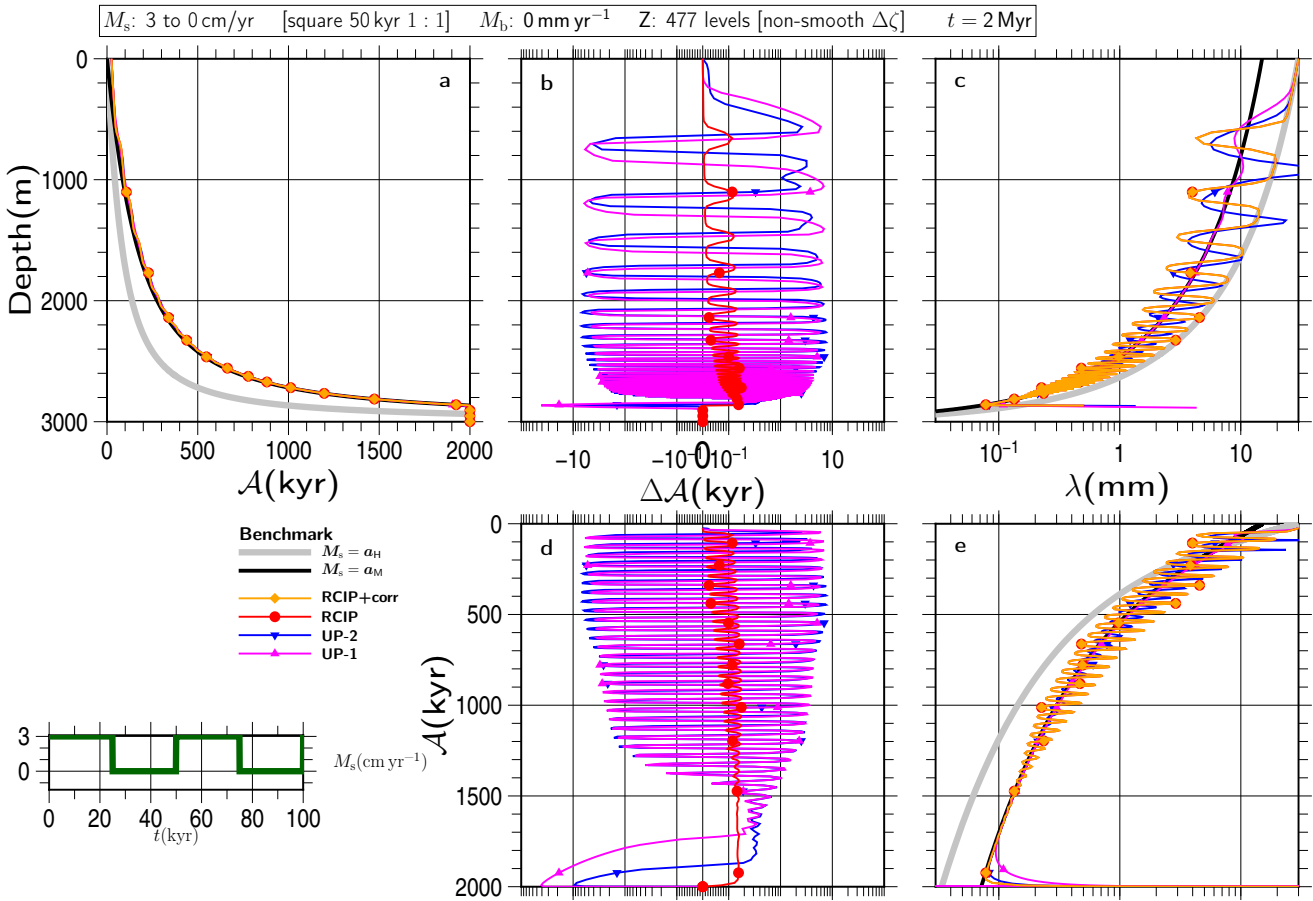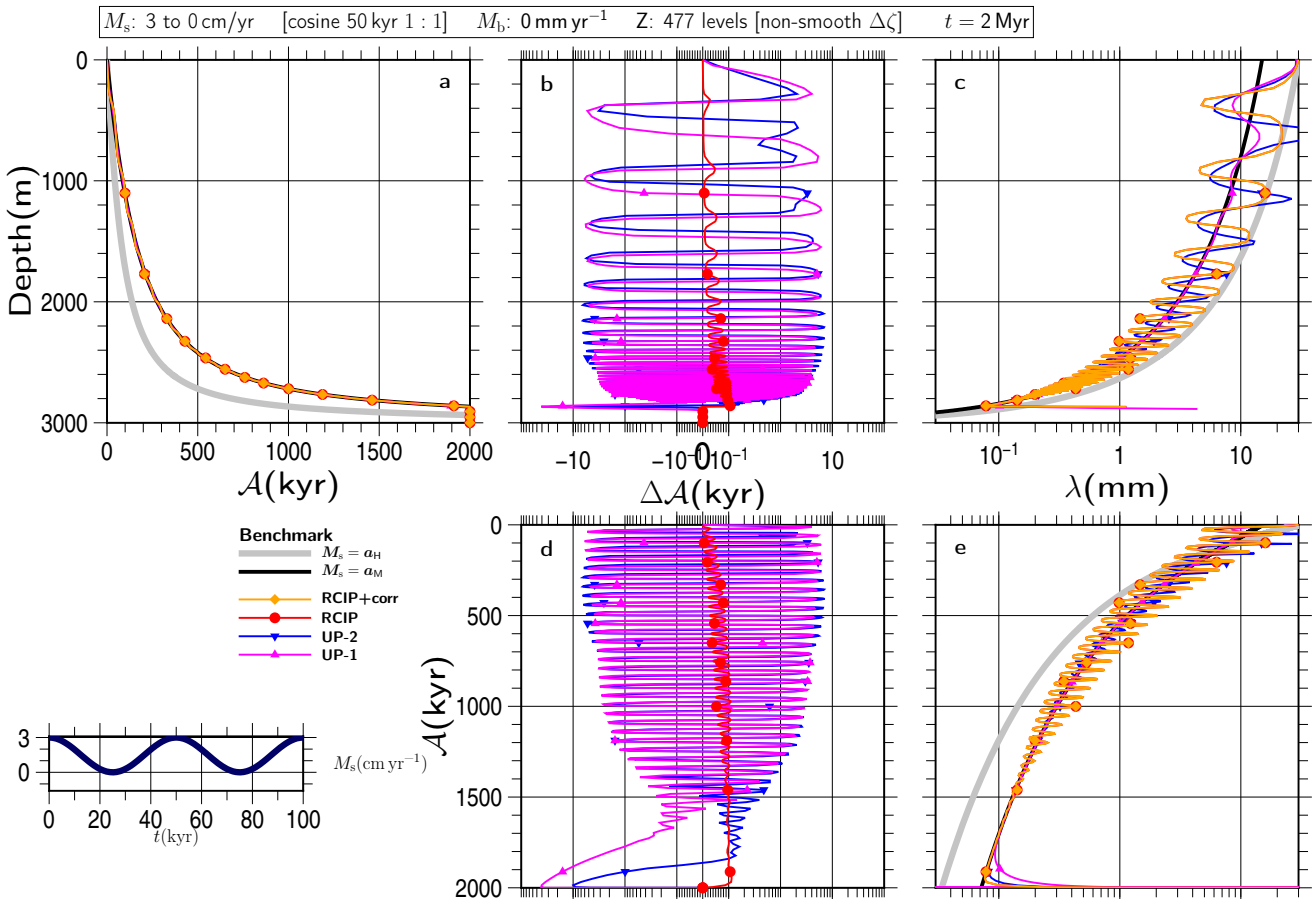
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Figure S140:
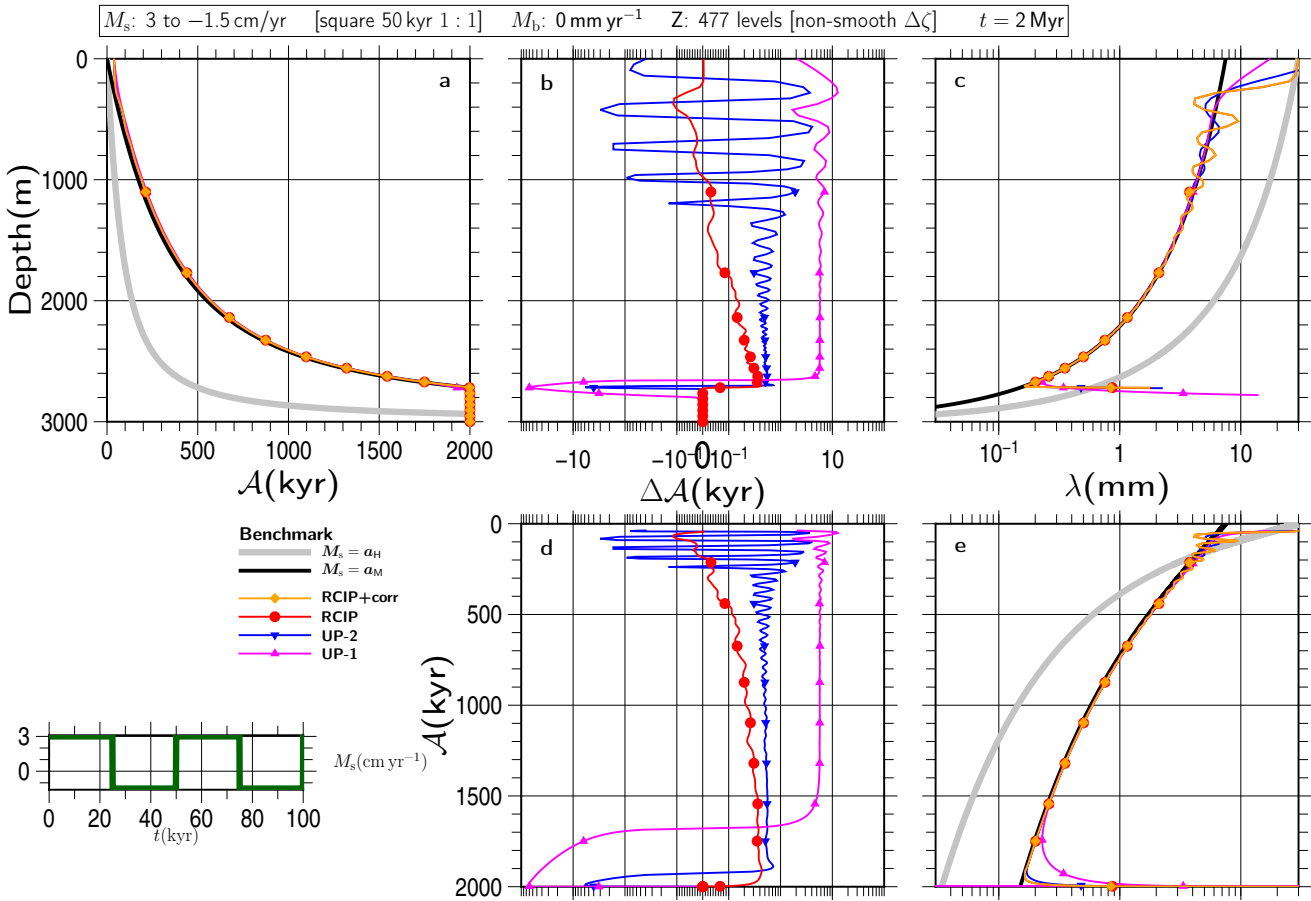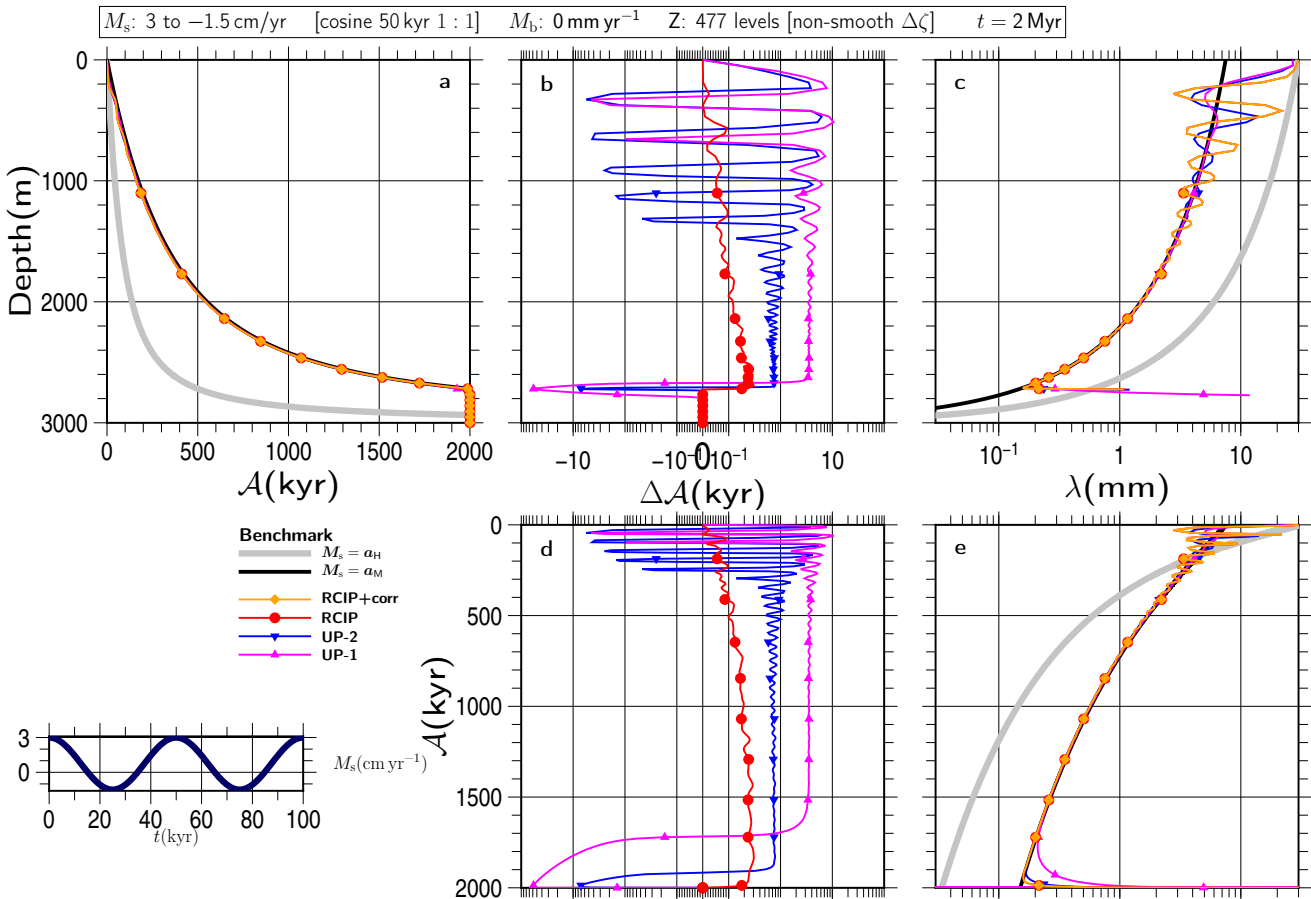
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Figure S142:
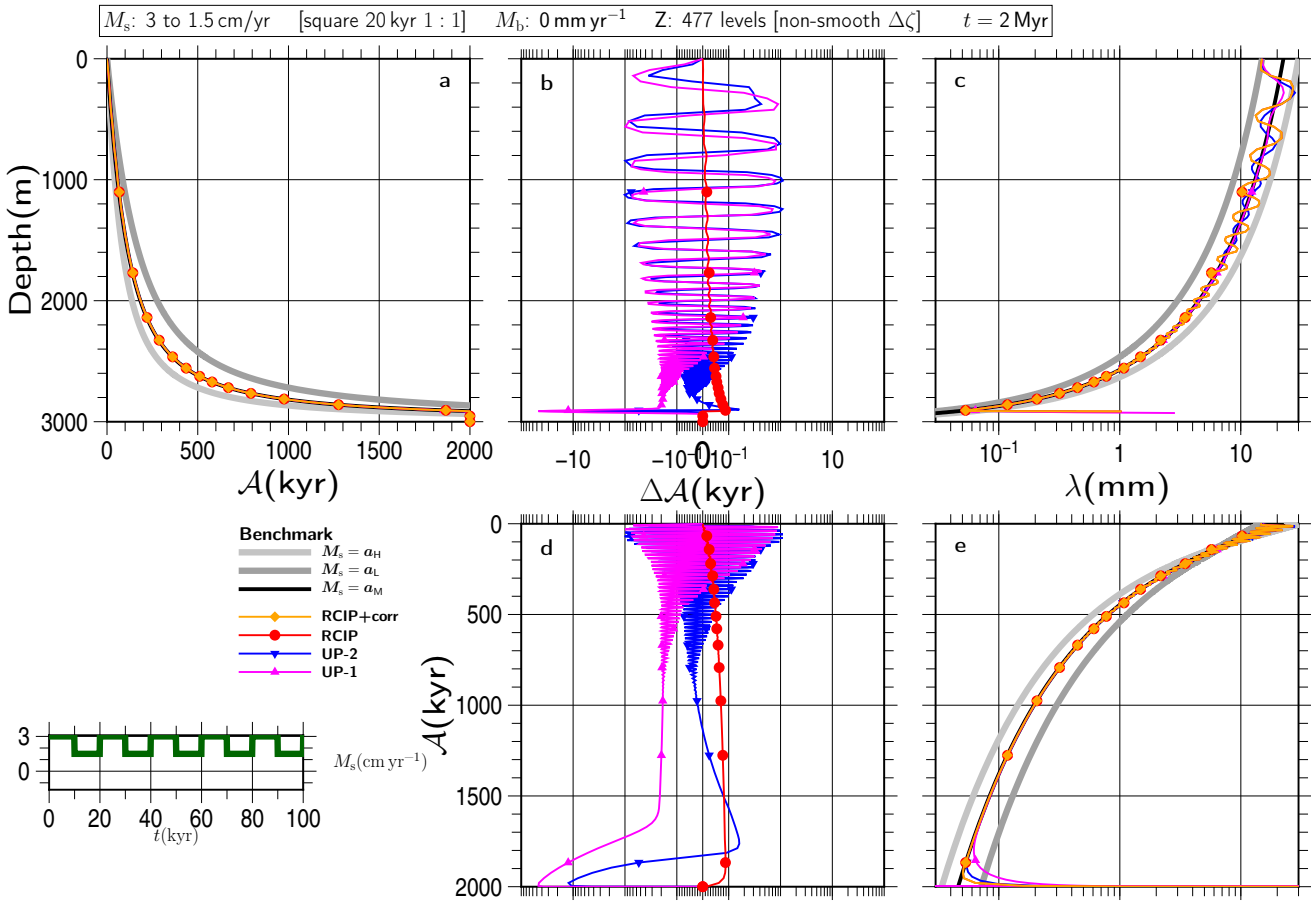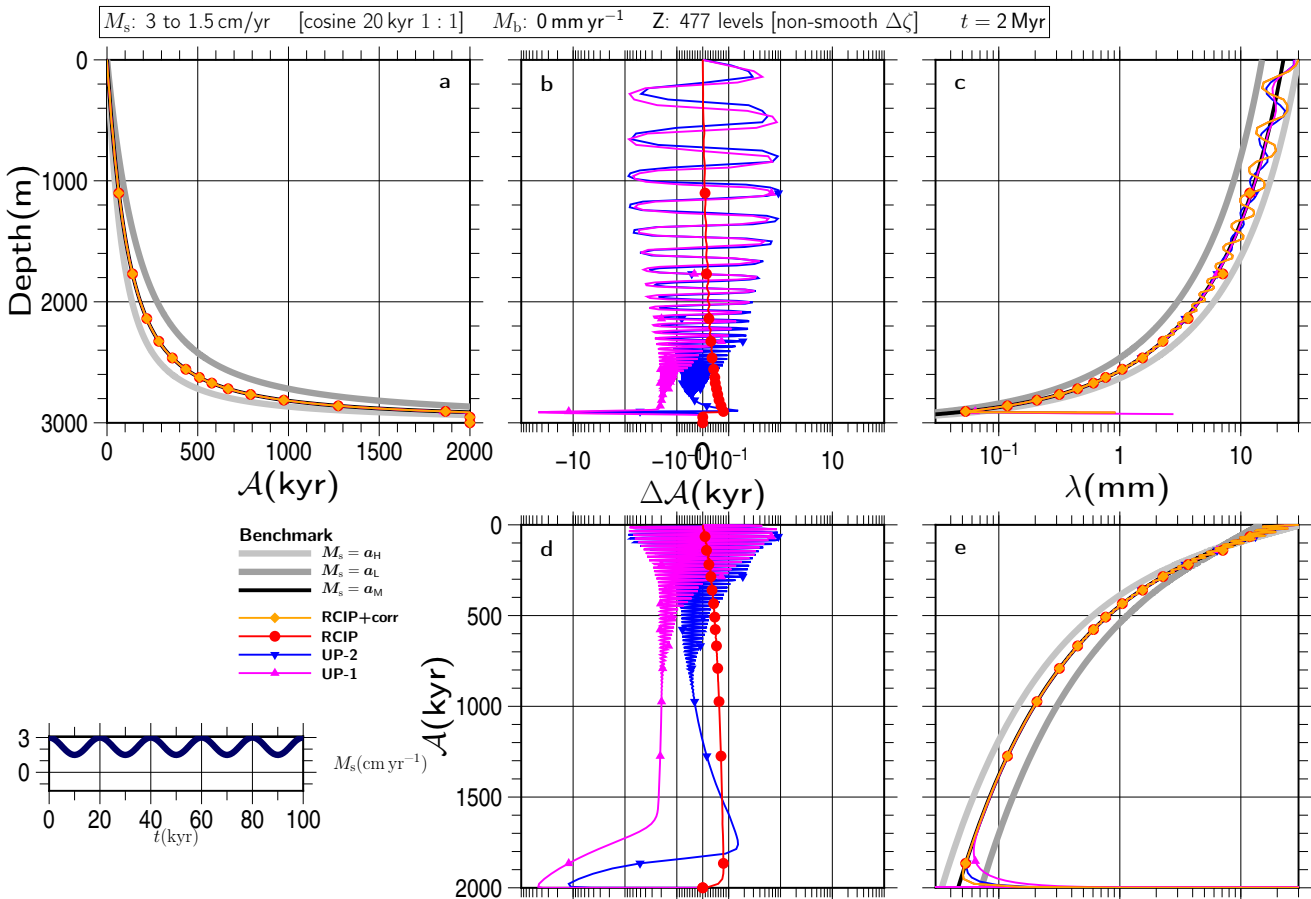
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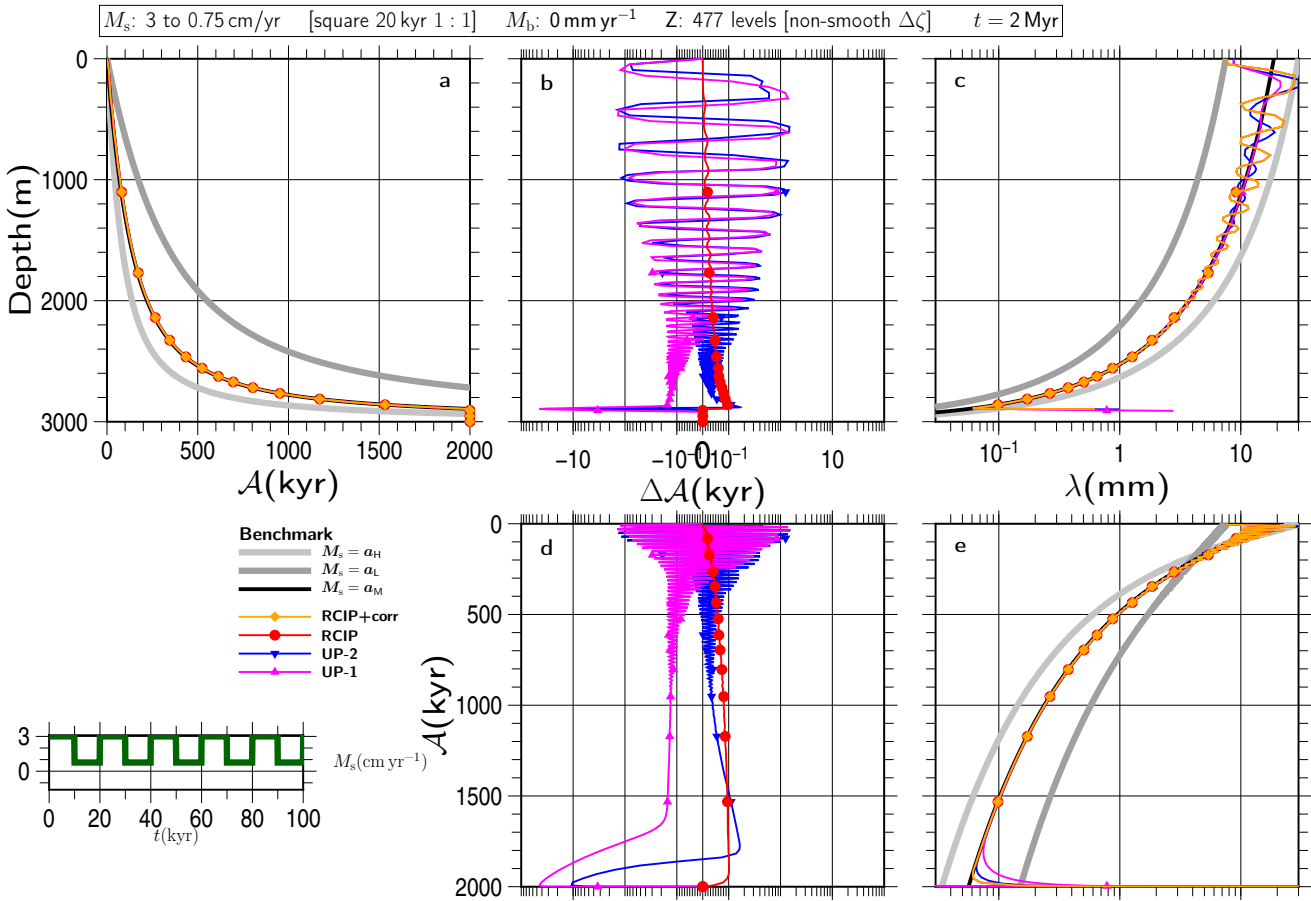
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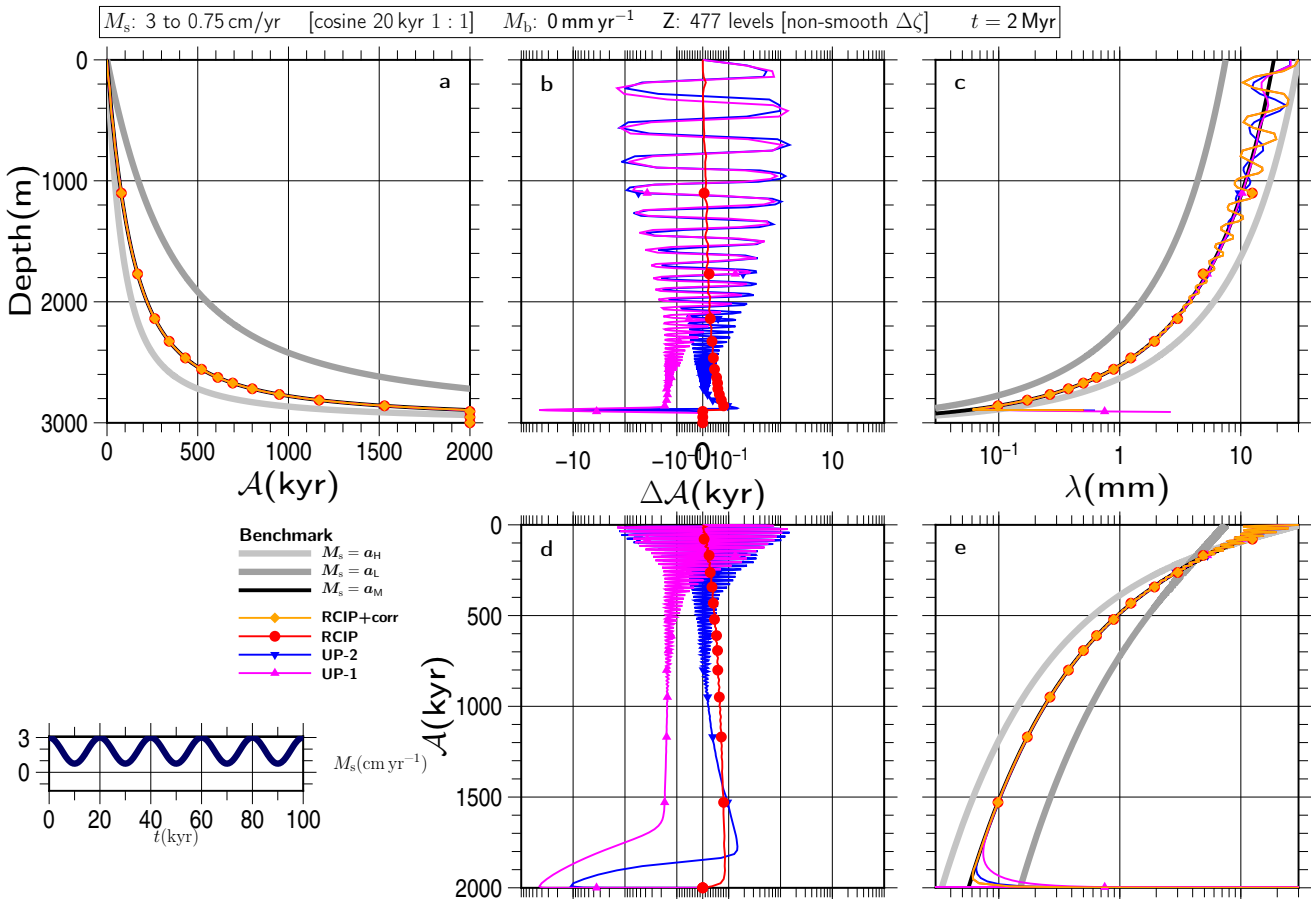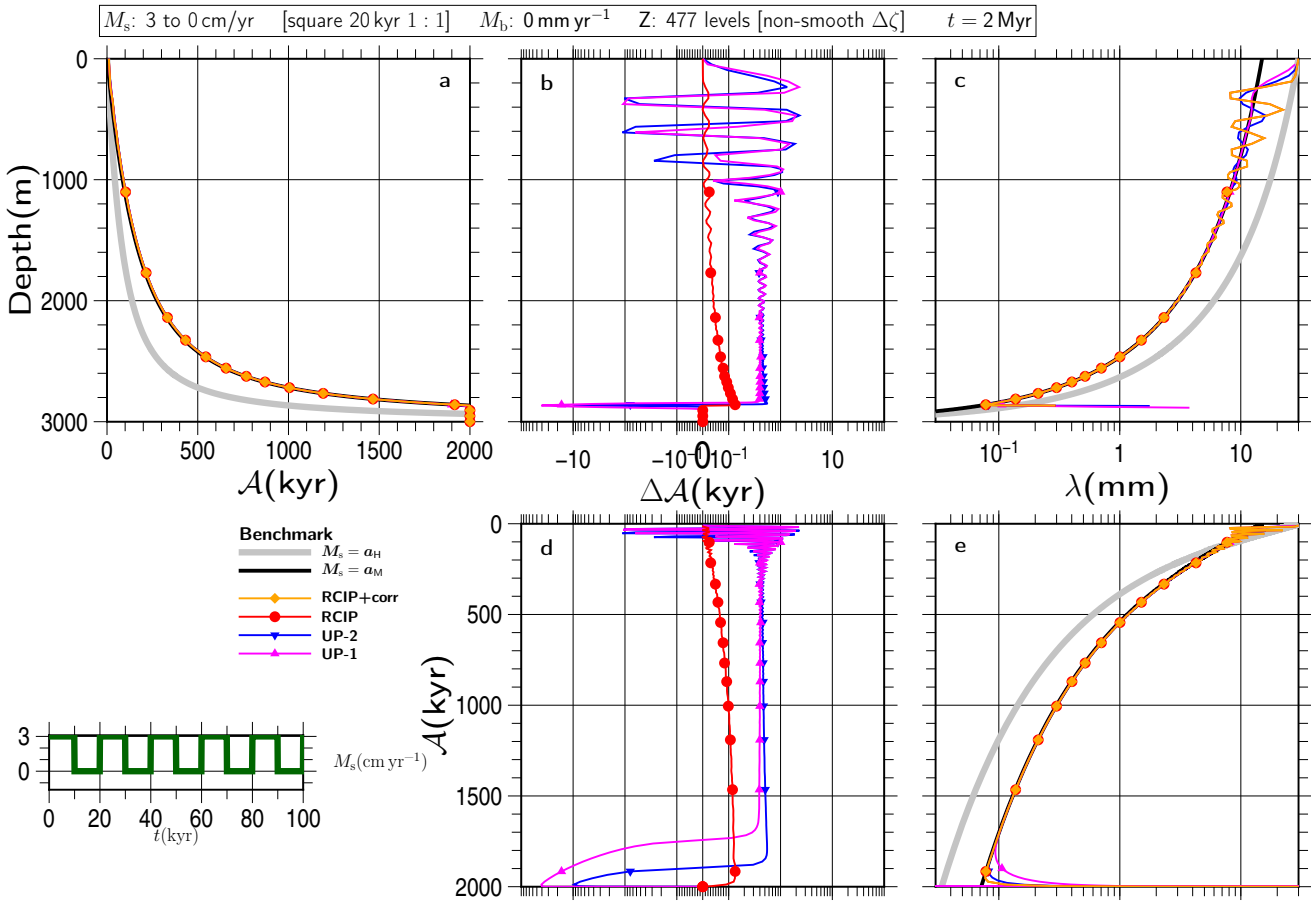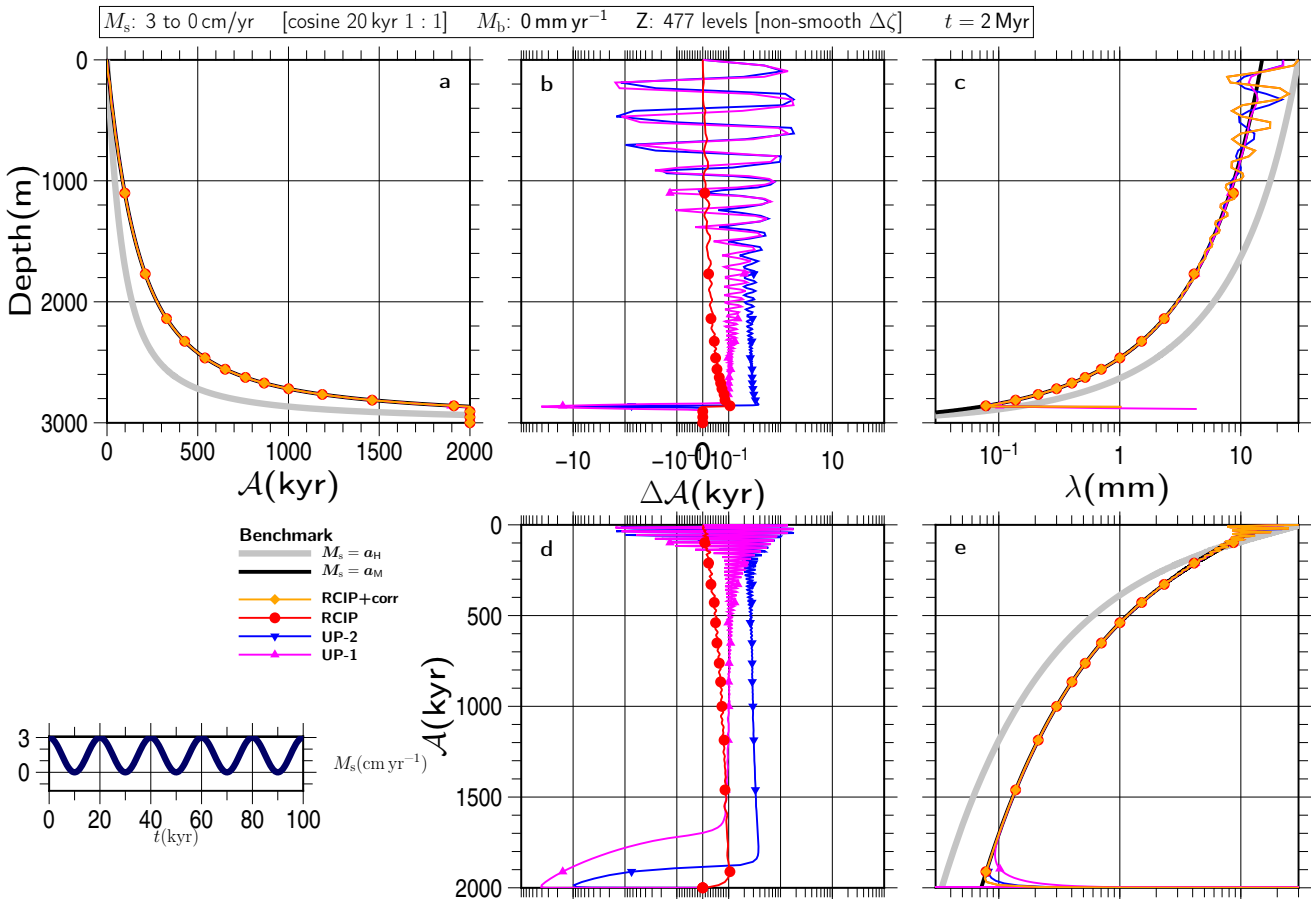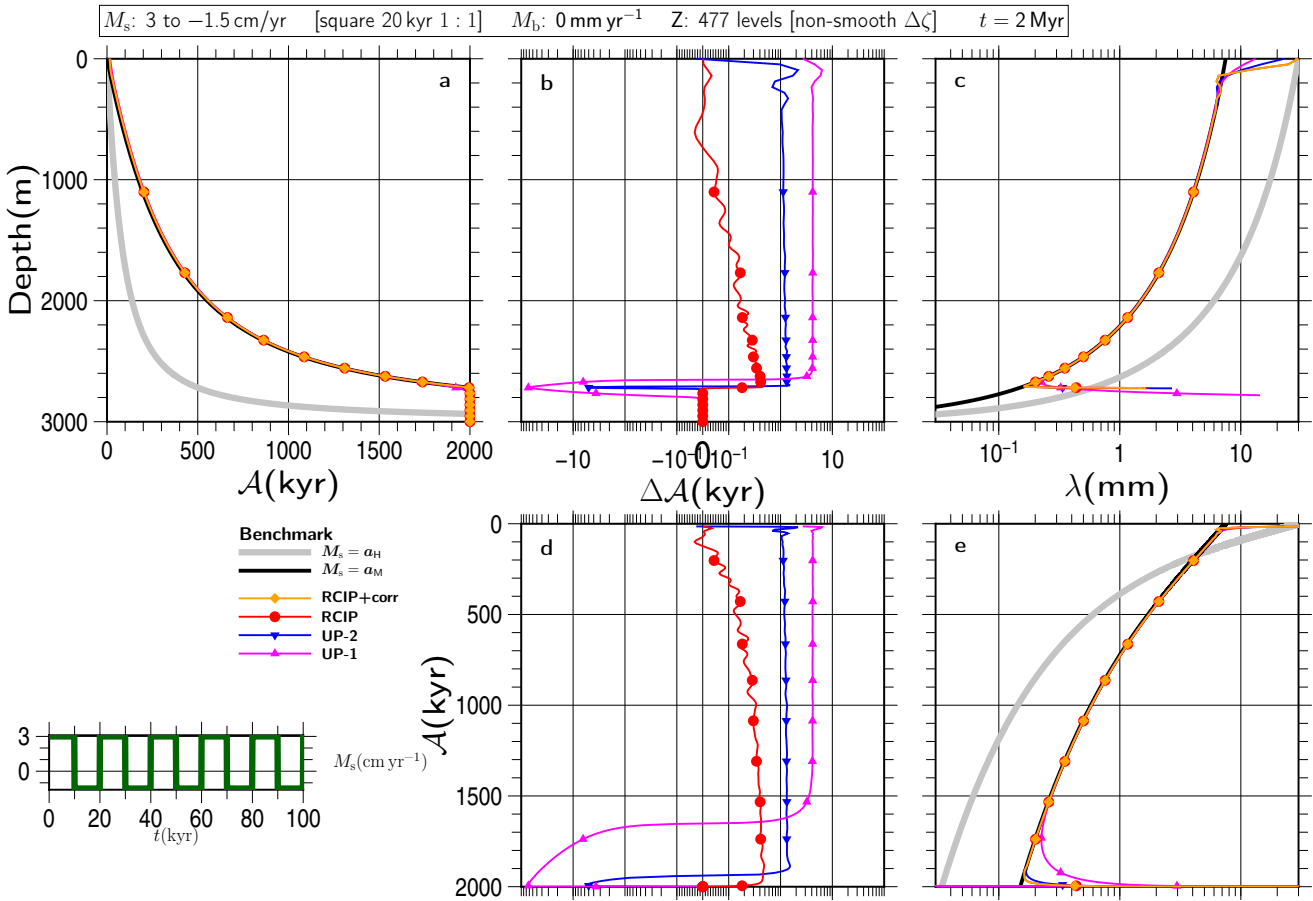

Figure S146:

Figure S147:

Figure S148:

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Figure S149:

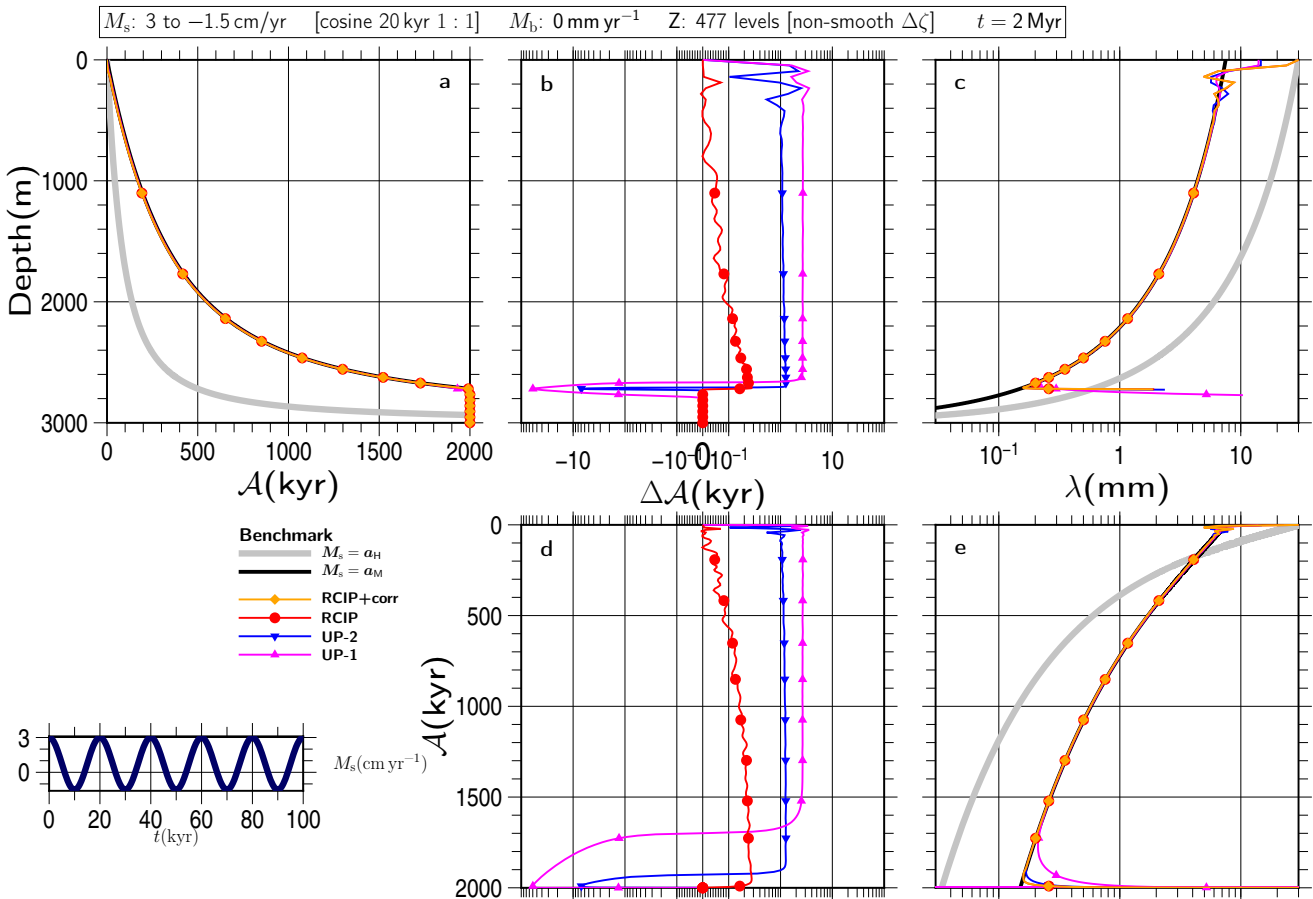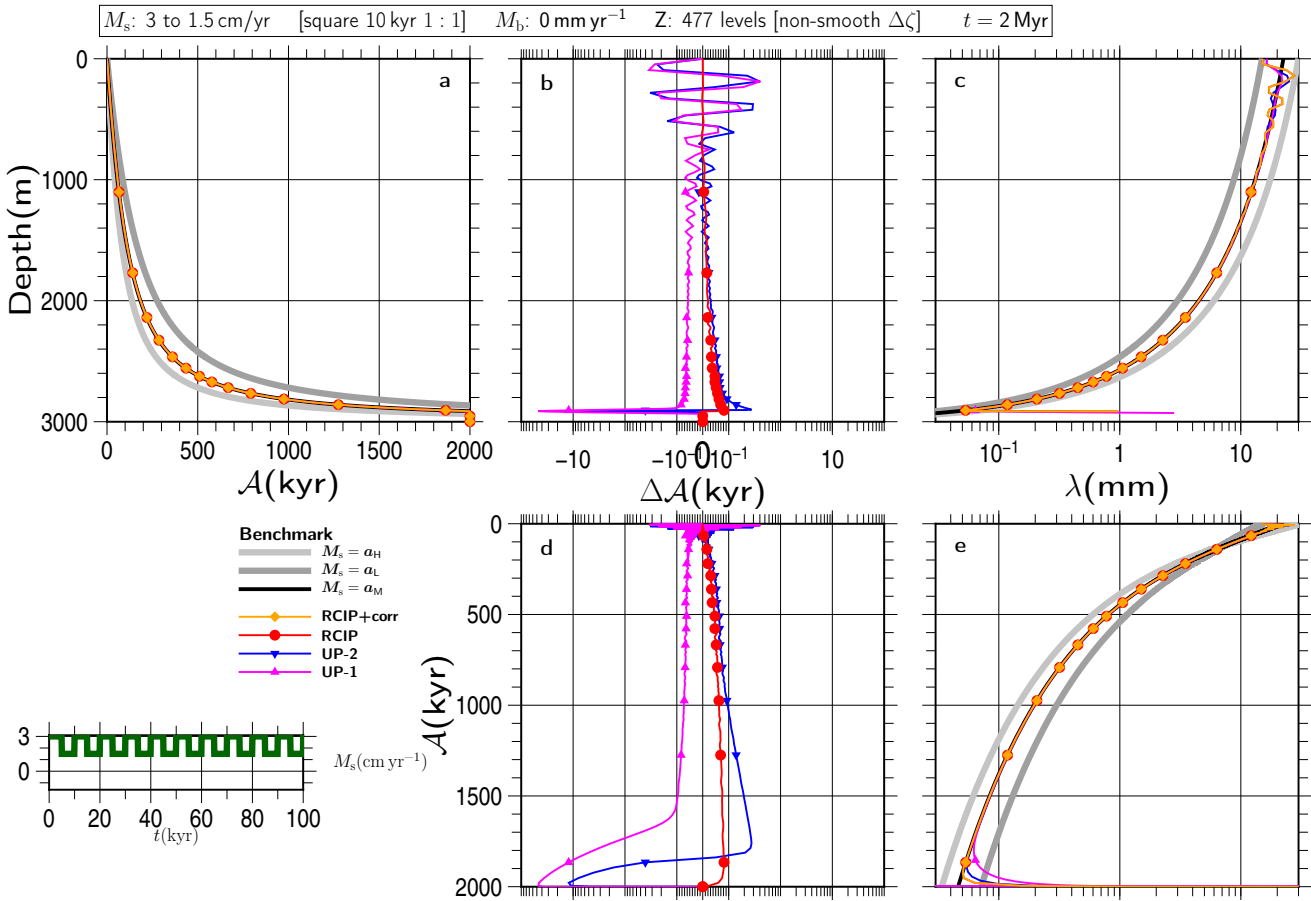Figure S150:

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Figure S151:
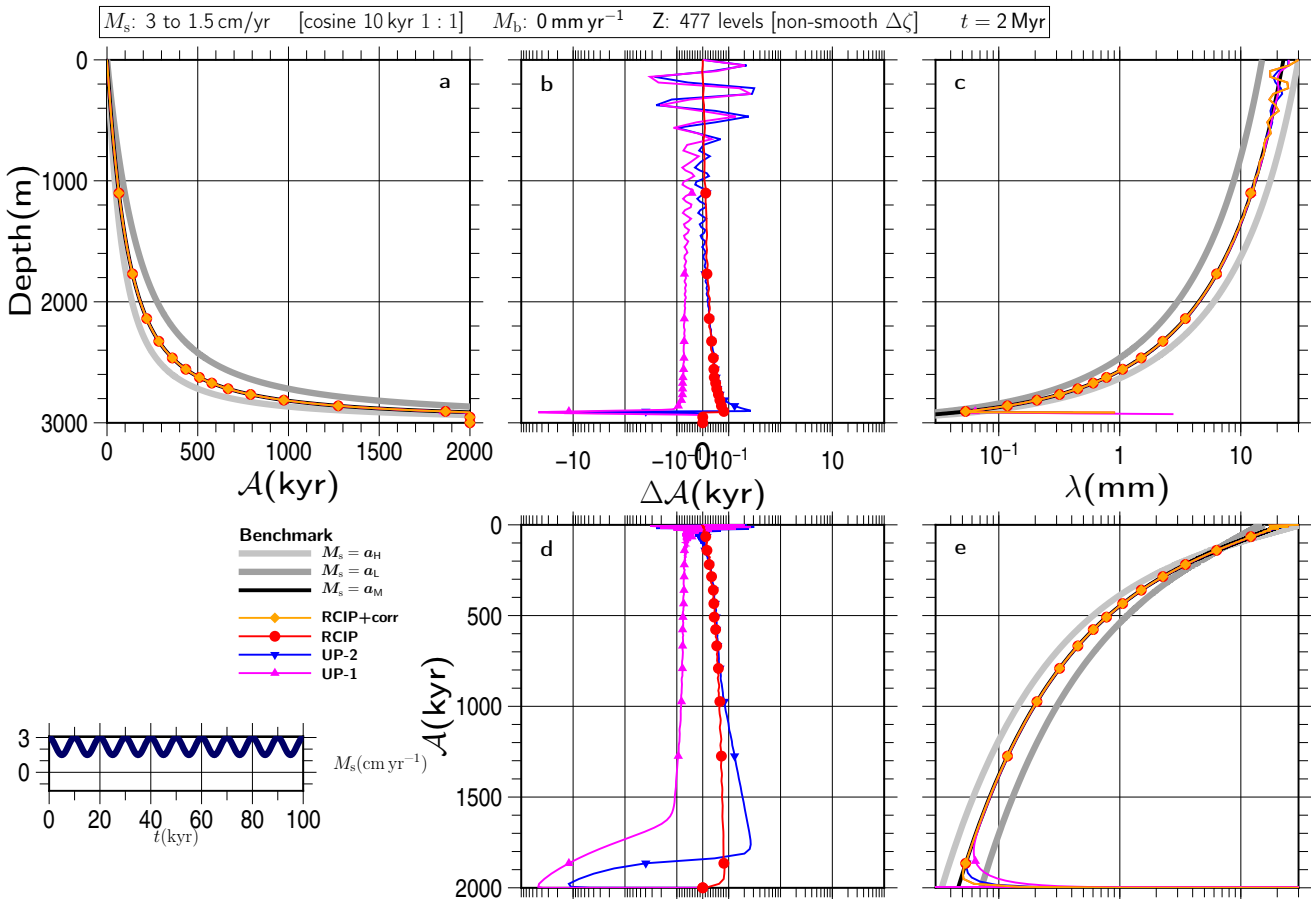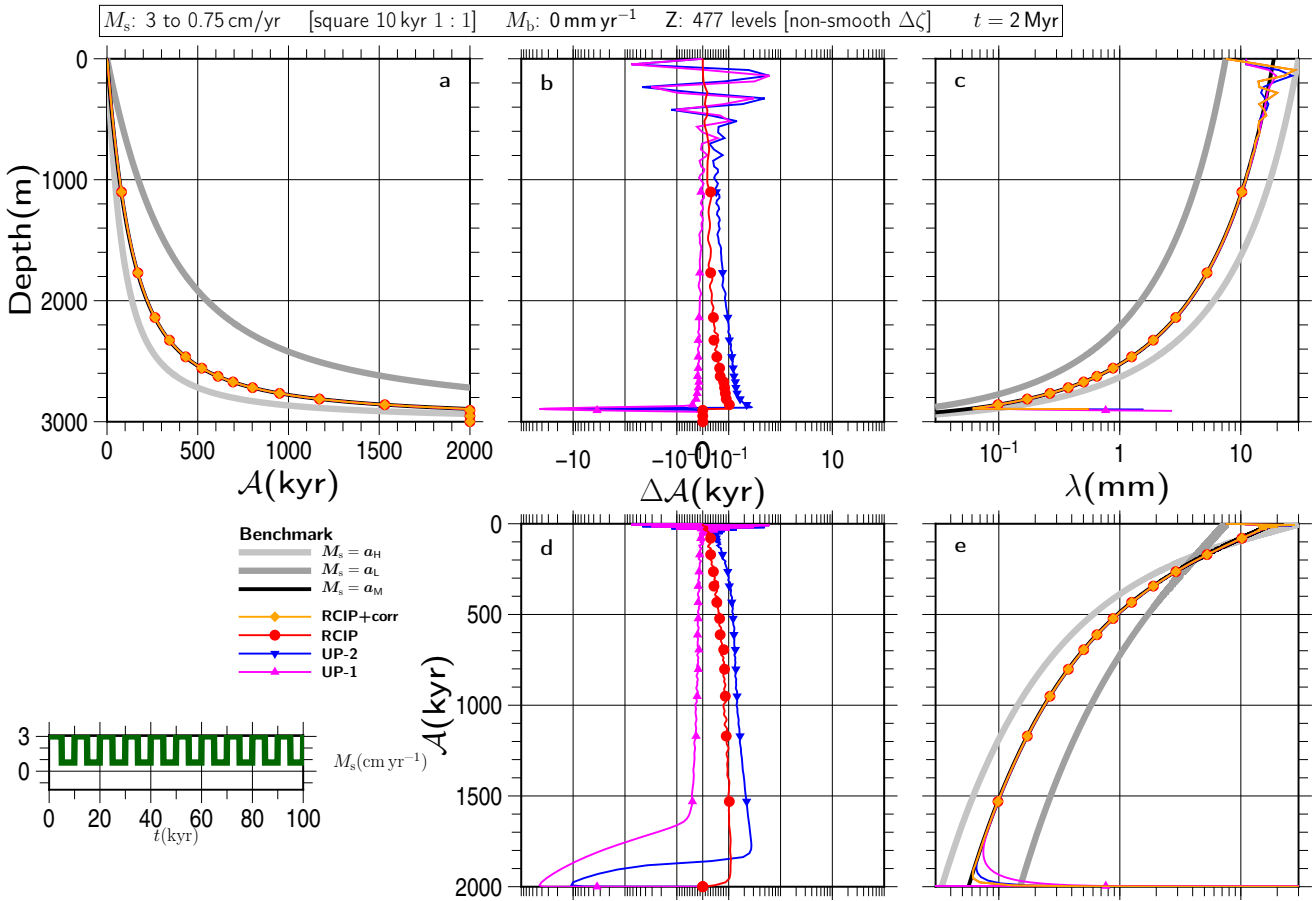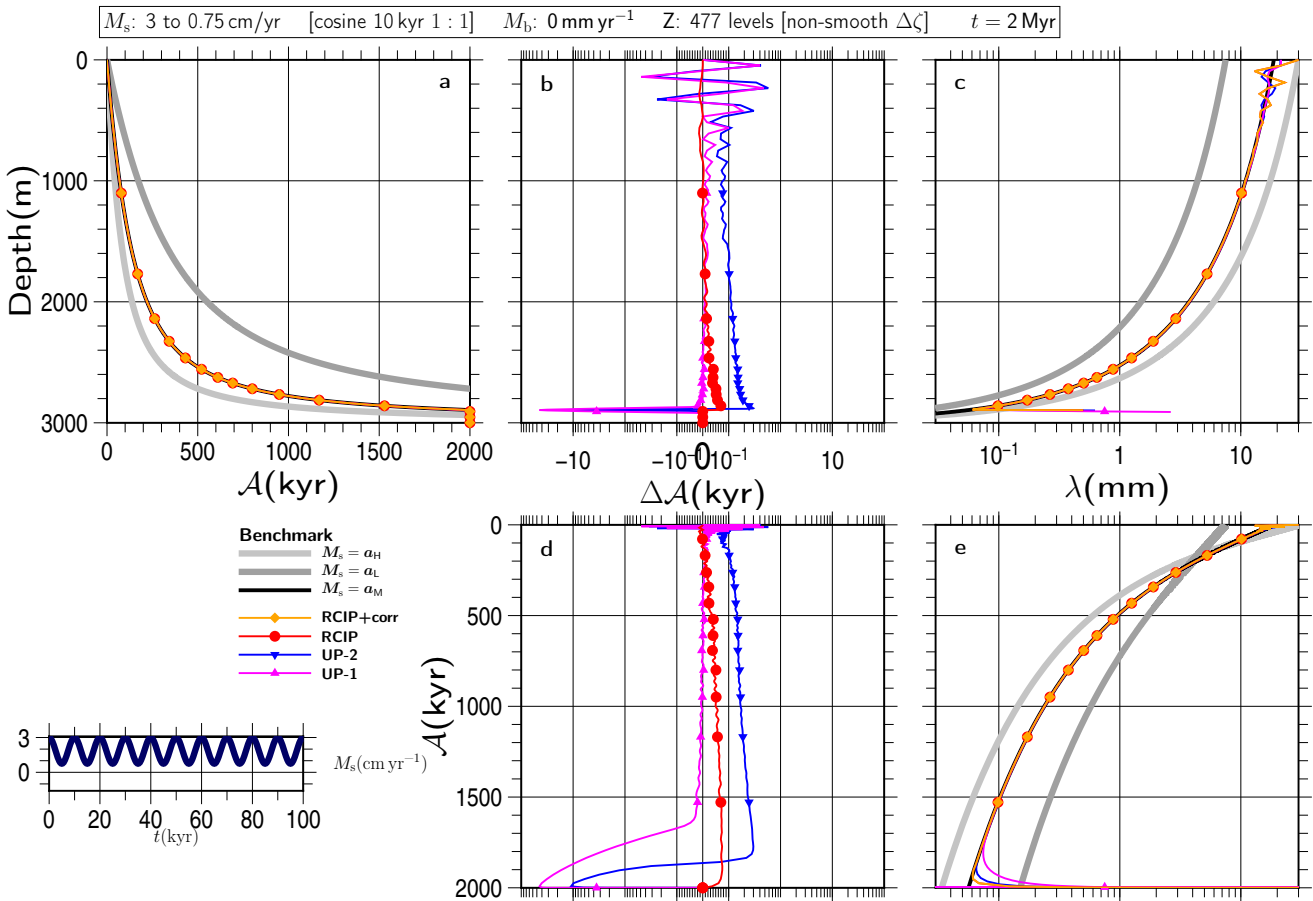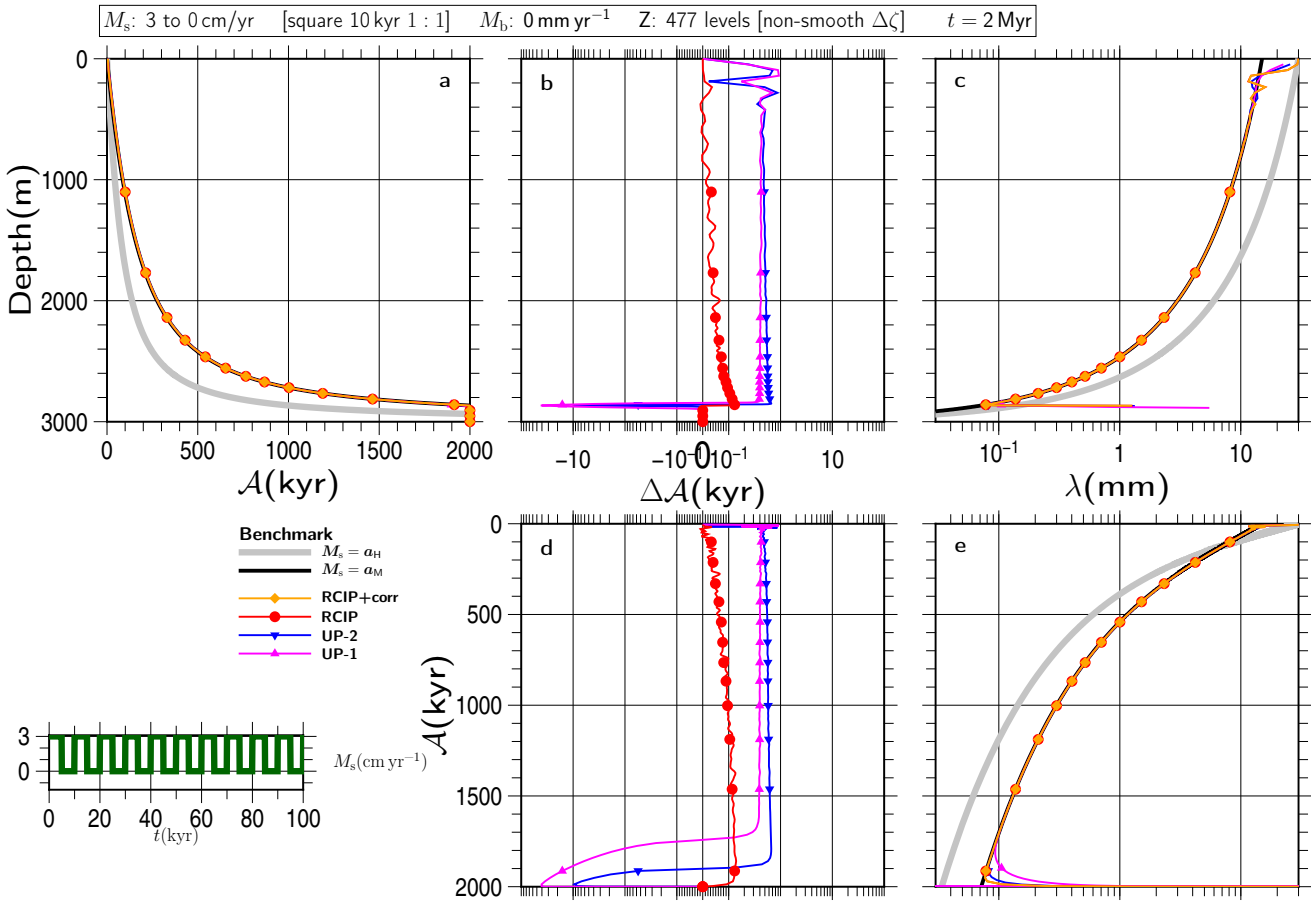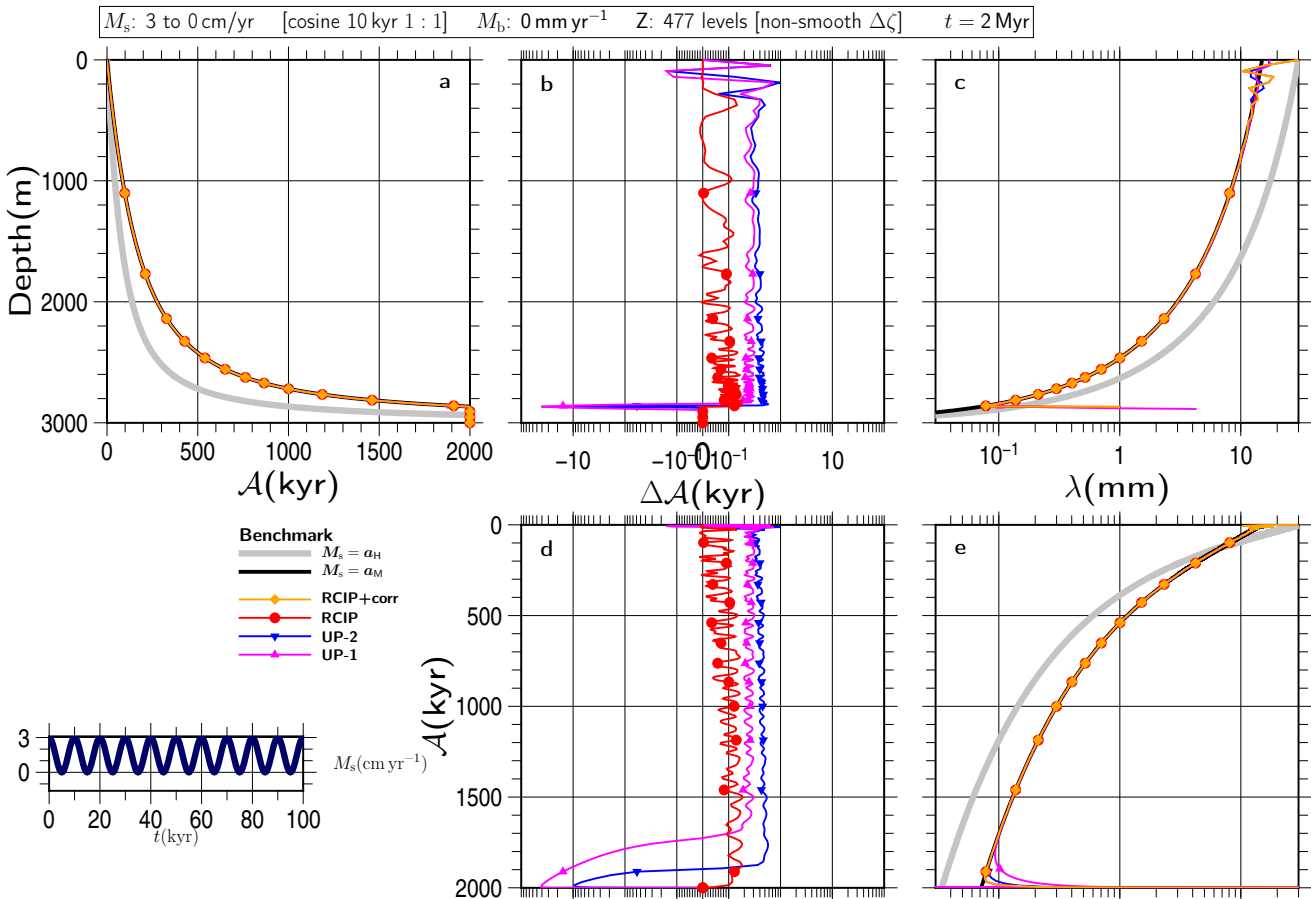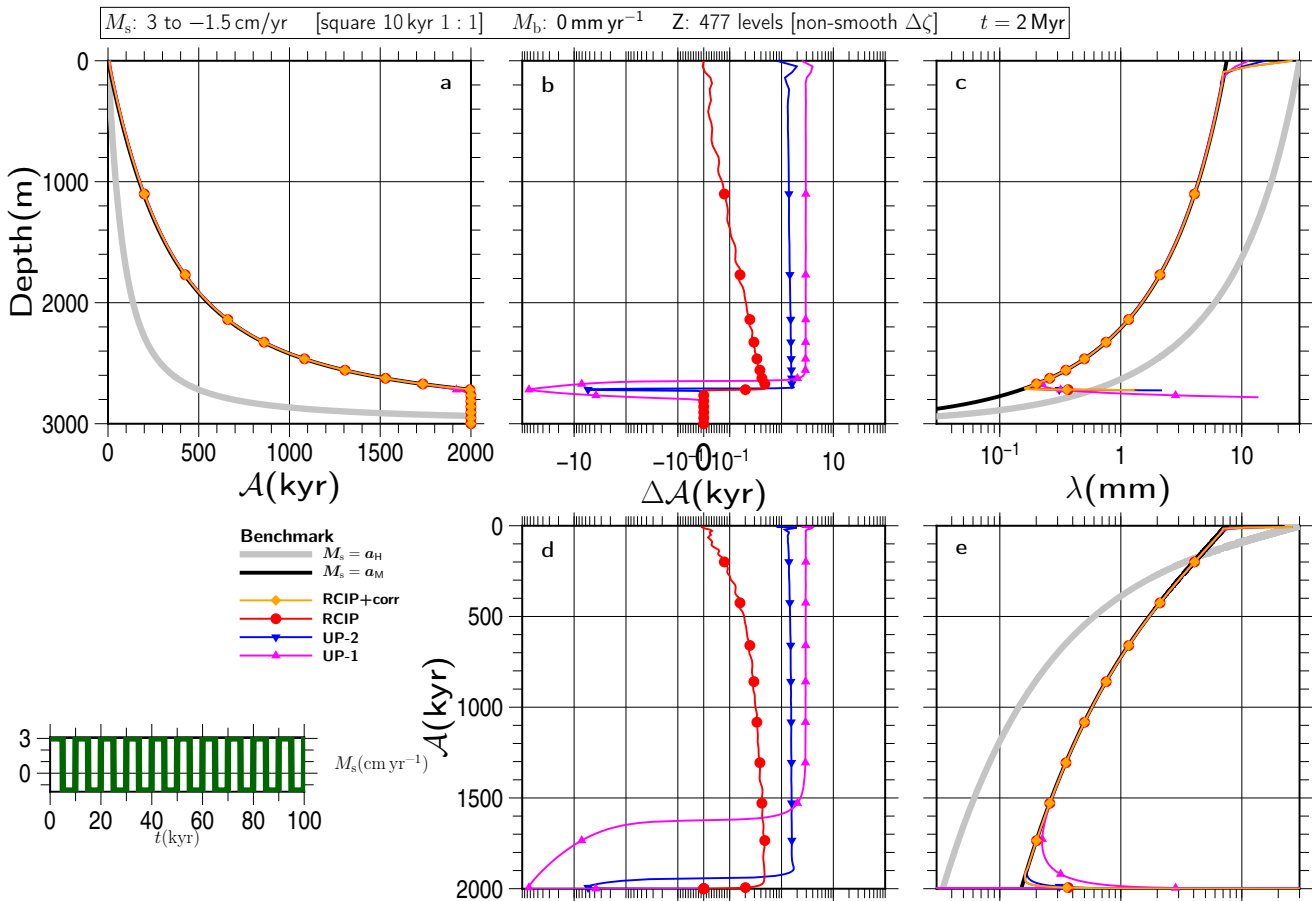
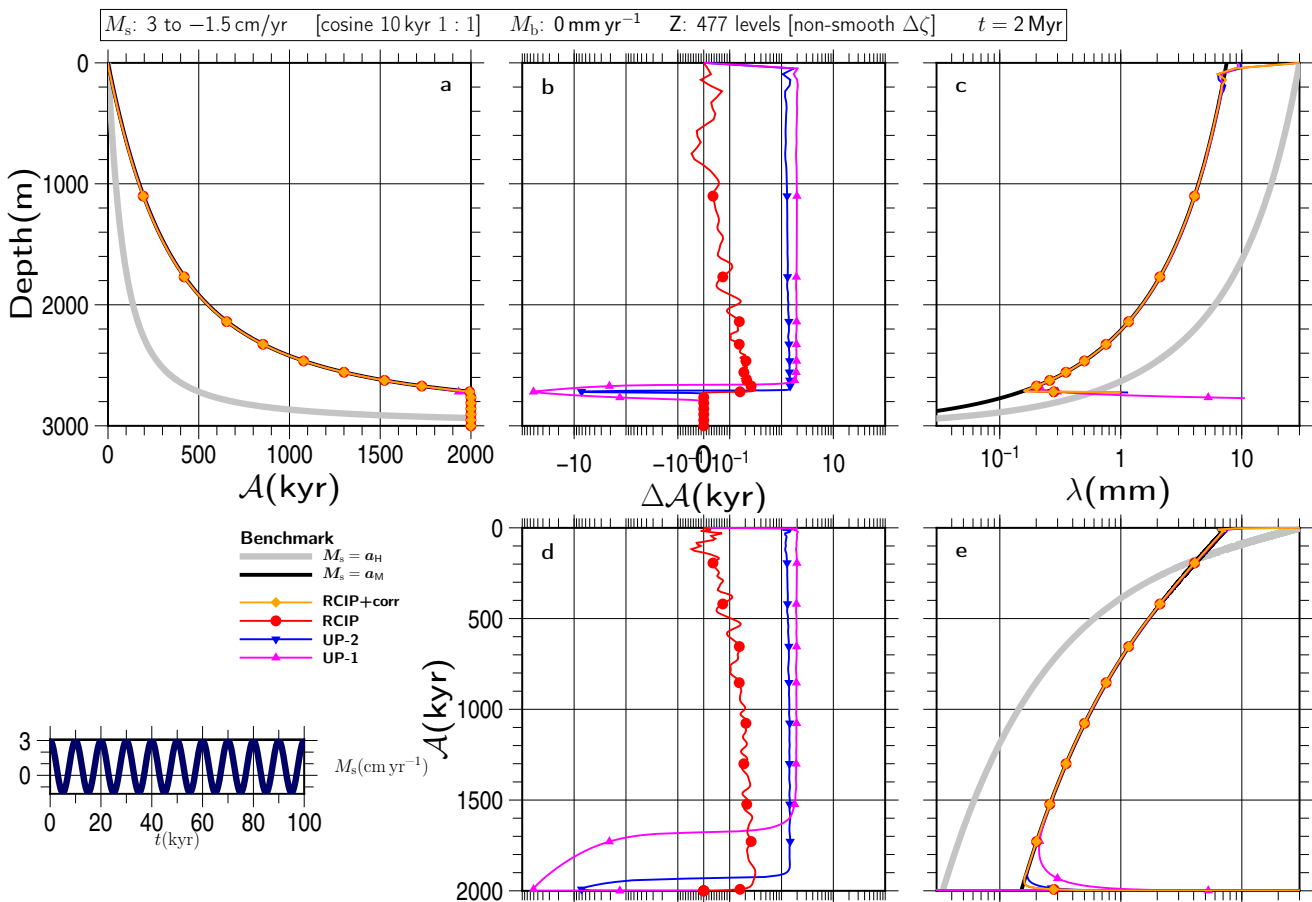Figure S152:

Figure S153:

Figure S154:

Figure S155:

Figure S156:

Figure S157:

Figure S158: