

# DecTree v1.0 - Chemistry speedup in reactive transport simulations: purely data-driven and physics-based surrogates

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**Abstract.** The computational costs associated with coupled reactive transport simulations are mostly due to the chemical subsystem: replacing it with a pre-trained statistical surrogate is a promising strategy to achieve decisive speedups at the price of small accuracy losses and thus to extend the scale of problems which can be handled. We introduce a hierarchical coupling scheme in which “full physics”, equation-based geochemical simulations are partially replaced by surrogates. Errors on mass balance resulting from multivariate surrogate predictions effectively assess the accuracy of multivariate regressions at runtime: inaccurate surrogate predictions are rejected and the more expensive equation-based simulations are run instead. Gradient boosting regressors such as xgboost, not requiring data standardization and being able to handle Tweedie distributions, proved to be a suitable emulator. Finally, we devise a surrogate approach based on geochemical knowledge, which overcomes the issue of robustness when encountering previously unseen data, and which can serve as basis for further development of hybrid physics-AI modelling.

## 1 Introduction

Coupled reactive transport simulations (~~Steeffel et al., 2005, 2015~~) (Steeffel et al., 2005, 2015) are very expensive, effectively hampering their wide applications. While hydrodynamic simulations on finely resolved spatial discretisations, containing millions of grid elements, are routinely run on common workstations, the order of magnitude of the computationally affordable reactive transport simulations on the same hardware decreases by a factor of ten to a hundred as soon as chemical reactions are coupled in (~~De Lucia et al., 2015; Jatnieks et al., 2016; De Lucia et al., 2017; Leal et al., 2020; Prasianakis et al., 2020~~) (De Lucia et al., 2020). This usually requires oversimplifications of the subsurface domain, reduced to 2D or very coarse 3D, and of the geochemical complexity as well.

In the classical *operator splitting* such as Sequential Non-Iterative Approach (SNIA), the three interacting physical processes hydrodynamic flow, solutes transport and chemical interactions between solute species and rock forming minerals are solved sequentially. Chemistry usually represents the bottleneck for coupled simulations ~~with up to, taking up easily 90% of computational time~~ (~~De Lucia and Kühn, 2013; De Lucia et al., 2015; Leal et al., 2020~~) with up to, taking up easily 90% of compute time, but much higher

percentages of over 99 % are frequent (Steeffel et al., 2015; He et al., 2015; De Lucia et al., 2015; Huang et al., 2018; Leal et al., 2020).

25 The numerical model for geochemical speciation and reactions requires in general the integration of one stiff differential-algebraic system of equations per grid element per simulation time step. Parallelisation is thus required to tackle large spatial discretisations, which is why many modern codes are developed to run on high performance computing (HPC) clusters with many thousand of CPUs (Hammond et al., 2014; Beisman et al., 2015; Steffel, 2019). However, ~~parallelisation alone still is not sufficient to ensure numerical convergence of the simulations, a problem~~ the problem of difficult numerical convergence

30 for the geochemical sub-process, routinely encountered by many practitioners, ~~is not solved by parallelisation~~. Furthermore, large uncertainties affect the phenomenological model itself ~~(i. e., reaction kinetics spanning~~ Kinetics rates in natural media span over orders of magnitude ~~;~~ consistent activity model for concentrated solutions (Marty et al., 2015); activity models for the brines usually encountered in the subsurface ~~;~~ lack parametrization for higher temperature, salinity or for many elements (Dethlefsen et al., 2011; Appelo et al., 2013; Moog et al., 2015; Miron et al., 2019); and even larger uncertainties concern the

35 parametrisation of the subsurface, regarding ~~the spatial heterogeneity of rocks~~ for example the heterogeneity of rock mineralogy, which is mostly unknown and hence often disregarded ~~(De Lucia et al., 2011). It thus may~~ (Nissan and Berkowitz, 2019). It may thus appear unjustified to allocate large computational resources to solve very expensive, yet still actually oversimplified or uncertain problems. Removing the computational cost associated with reactive transport modelling is thus of paramount importance to ensure its wide application on a range of otherwise practically unfeasible problems (Prommer et al., 2019).

40 The much desired speedup of this class of numerical models has been the focus of intensive research in the last few years. Among the proposed solutions, Jatnieks et al. (2016) suggests to replace the “full physics” numerical models of the geochemical subsystem with emulators or surrogates, employed at runtime during the coupled simulations. A surrogate in this sense is a statistical multivariate regressors which has to be trained in advance on a set of pre-calculated “full physics” solutions of the geochemical model at hand, spanning the whole parameter range expected for the simulations. Since the regressors are much

45 quicker to compute than the setup and integration of a differential algebraic system of equations (DAE), this promises a significant speedup and has thus found resonance in the scientific community ~~(e.g., De Lucia et al., 2017; Laloy and Jacques, 2019; Guérillot and~~ However, all approximations and especially purely data-driven surrogates introduce accuracy losses into the coupled simulations. These must be kept low in order to generate meaningful simulation results. Ultimately, replacing a fully fledged geochemical simulator with surrogate equals to trading computational time for accuracy of the simulations. Due to the non-linear

50 nature of geochemical sub-processes, even small errors in surrogate predictions propagate in successive iterations so that diverging trajectories for the coupled models originate from only few time-steps, leading to unphysical results. Mass and charge imbalances, i.e., “creation” of matter, happen to be the most common source of unphysicality in our early tests. It is thus of paramount importance to obtain highly accurate surrogates, which in turn may require very large and densely sampled training datasets and training times.

55 ~~Any regression algorithm can be employed to replace the “full physics” equation-based geochemical model.~~ The thriving developments in data science and machine learning in the recent years have produced many different and efficiently implemented regressors readily available and usable in high-level programming languages such as python or R. Among the most known ones there are gaussian processes, support vector machines, artificial neural networks and decision-tree based algorithms such

as random forest or gradient boosting. Most of these algorithms are “black boxes”, which non-linearly relate many output variables to many input variables. Their overall accuracy can be statistically assessed by measuring their performances on the training dataset or on a subset of the available training data left out for the specific purpose of testing the models. In any case these training and/or test datasets must be obtained ~~beforehands~~ beforehand computing an appropriate number of points with the “full physics” model. Geochemistry is usually largely multivariate, meaning that many input and many output variables are passed to and from the geochemical subsystem at each time step. In general, different regressors may capture each output variable in better fashion depending on many factors (e.g., the problem at hand, where variables display different non-linear behaviors; the sampling density of training dataset, which may be biased). ~~For this reason, we argue that the most sensible choice for a surrogate modelling framework is that of multiple multivariate regression: one multivariate regressor – making use of many or all inputs as predictors – is trained independently for each distinct output variable, while the choice of regressor may vary from variable to variable.~~ With algorithms such as Artificial Neural Networks (ANN) it is possible to train one single network ~~, and hence~~ and hence in practice one single surrogate ~~, for all model for all output~~ variables at once. ~~However, ANN~~ While ANN in particular usually require long CPU times for training and quite large training datasets:-

~~In praxis, the CPU-time, the user interactions and the overall skills required for optimally training complex regressors cannot be underestimated and may prove overwhelming for a geoscientist. The whole process of~~ they offer large speedups when used for predictions (Jatnieks et al., 2016; Prasianakis et al., 2020) and furthermore they can efficiently leverage GPUs (Graphic Processing Units) for even larger acceleration. It is however difficult to achieve the required accuracy simultaneously for all output variables (Kelp et al., 2020). For this reason, we focus on a more flexible approach, multiple multivariate regression: one distinct multivariate regressor - i.e., making use of many or all inputs as predictors - is trained independently for each distinct output variable. This approach allows using different specialized models from variable to variable, including different regression methods altogether, but also data preprocessing and hyperparameter tuning, required by most advanced ~~machine learning algorithms, while being an active area of development and research, is still hardly fully automatable while not necessarily requiring larger computing resources.~~

This work showcases and analyses two different approaches for surrogate geochemical modelling in reactive transport simulations. The first is completely data-driven, disregarding any possible knowledge about the ongoing process. In the second approach, we derive a surrogate which exploits the actual equations solved by the full physics representation of chemistry. Both are applied and evaluated on the same 1D benchmark implemented in a simple reactive transport framework. Our implementation of coupled reactive transport includes a hierarchical submodel coupling strategy, which is advantageous when different accuracy levels for the predictions of one sub-process are available.

## 2 Methods: simulation environment and benchmark problem

~~All the~~ The versioned R code used for ~~running the reactive transport simulations, generating the datasets and training of~~ surrogates is included in DecTree v.1.0 model setup and evaluation is referenced in section “code availability”. It is based on version v0.0.4 of the RedModRphree package for the R environment (R Core Team, 2020), ~~making which is also~~

referenced in section “code availability”. It makes use of the geochemical simulator PHREEQC (Appelo et al., 2013). ~~The above mentioned package RedModRphree~~ supersedes the in-house developed R-PHREEQC interface Rphree (<https://rphree.r-forge.r-project.org/>, De Lucia and Kühn, 2013). ~~See section code availability for more details.~~

95 The benchmarks and the performance measurements refer to computations run on a recent desktop workstation equipped with Intel Xeon W-2133 CPU with clock at 3.60 GHz and DDR4 RAM at 2.666 GHz under Linux kernel 5.9.14 and R version 4.0.3. If not otherwise specified, only one CPU core is employed for all computational tasks. Since chemistry in an operator-splitting approach the simulation of geochemical sub-process is inherently an embarassing parallel task, the embarassing parallel task, in which at each time step one geochemical simulation per grid element is required, completely independent on the neighbours, the speedup achieved on a single CPU as in this work will transfer ~~—given large enough simulation grids making up for the overhead—on parallel computations~~ on parallel computations in which each CPU is assigned a comparable number of grid elements, up to the overhead required to dispatch and collect the results in a parallel environment.

## 2.1 Numerical simulation of flow and transport

We consider a stationary, fully-saturated, incompressible, isothermal 1D Darcy flow in a homogeneous medium. Transport is restricted to pure advection and the feedback of mineral precipitation and dissolution on porosity and permeability is also disregarded; the fluid density is ~~also~~ considered constant. Advection is numerically computed via a *forward Euler* explicit resolution scheme:

$$C_i(x, t + 1) = C_i(x, t) - u \cdot \Delta t \frac{C_i(x, t) - C_i(x - 1, t)}{\Delta x} \quad (1)$$

where  $u$  is the module of Darcy velocity,  $C_i(x, t)$  the volumetric concentration (molality) of the  $i$ -th solute species at the point  $x$  and time  $t$ , and  $\Delta x$  the size of a grid element. For this scheme, the Courant-Friedrichs-Lewy stability condition (CFL) imposes that the Courant number  $\nu$  be less than or equal to 1:

$$\nu = \frac{u \cdot \Delta t}{\Delta x} \leq 1 \quad (2)$$

For Courant numbers less than 1, numerical dispersion arises; the scheme is unstable for  $\nu > 1$ . The only both stable and precise solution for advection is with  $\nu = 1$ . Thus, the CFL condition is very limiting in  $\Delta t$ : a factor two refinement in the spatial discretisation corresponds to a factor two decrease in  $\Delta t$ , thus ~~obtaining double required~~ requiring twice the coupling iterations. Note that ~~equation 1 is not written in terms of porosity~~ porosity is not considered in equation 1, so that effectively the Darcy velocity is assumed equal to the fluid flux seepage velocity or, alternatively, porosity is equal to unity. This assumption does not have any impact on the calculations ~~besides the initial scaling of the system.~~ beside the volumetric scaling that has to be considered for the minerals. In the code the mineral amounts are always treated as mol per kg of solvent.

120 The implemented advection relies on transport of total elemental concentrations instead of the actual dissolved species, an allowable simplification since all solutes are subjected to the ~~very~~ same advection equation (Parkhurst and Wissmeier, 2015). ~~Special attention needs to be paid to~~ Total dissolved O, H and solution charge should be included among the state variables and thus transported, but since this problem is redox-insensitive, we can disregard charge imbalance and only transport pH instead of H and O, disregarding changes in water mass. pH ~~which~~ is defined in terms of activity of protons:

125  $\text{pH} = -\log_{10} ([\text{H}^+])$

and is hence not additive. ~~Assuming~~ If we further assume that the activity coefficient ~~for protons is of protons stays~~ constant throughout the simulation, the activity  $[\text{H}^+]$  can be actually transported~~instead of pH. Charge imbalance and redox potential (pe) can be safely disregarded for this redox-insensitive model, with absolutely insignificant errors when compared to the~~. The resulting simplified advective model shows negligible deviations from the results of the same problem simulated ~~, e.g.,~~

130 with PHREEQC’s ADVECTION keyword (not shown).

## 2.2 The chemical benchmark

The chemical benchmark used throughout this work is inspired by Engesgaard and Kipp (1992) and is well known, with many variants, in the reactive transport community (e.g., Shao et al., 2009; Leal et al., 2020). It was chosen since it has been studied by many different authors and it is challenging enough from a computational point of view.

135 At the inlet of a column, conventionally on the left side in the pictures throughout this work, a 0.001 molal magnesium chloride ( $\text{MgCl}_2$ ) solution is injected into a porous medium whose initial solution is at thermodynamic equilibrium with calcite. With the movement of the reactive front, calcite starts to dissolve and dolomite is transiently precipitated. Kinetic control is imposed on all mineral reactions following a Lasaga rate expression from Palandri and Kharaka (2004), limited to only neutral and  $\text{H}^+$  mechanisms (parameters are summarised in Table 1) and constant reactive surfaces, hence independent on the actual  
140 amounts of minerals. Precipitation rate - relevant only for dolomite - is set equal to the rate of dissolution. Temperature is set for simplicity at constant  $25^\circ\text{C}$  in disregard to actual physical meaningfulness of the model concerning dolomite precipitation (Möller and De Lucia, 2020). Detailed initial and boundary conditions are summarized in Table 2. To achieve a complete

**Table 1.** Parameters for kinetic control for dissolution and precipitation of calcite and dolomite.  $k$  is given in  $\text{mol m}^{-2} \text{s}^{-1}$ ,  $E_a$  in  $\text{kJ mol}^{-1}$  and reactive surface in  $\text{m}^2/\text{kg}_{\text{H}_2\text{O}}$ .

Mineral	$\text{H}^+$ mechanism			Neutral mechanism		
	log $k$	$E_a$	$\text{H}^+$ order	log $k$	$E_a$	reactive surface
calcite	-0.30	14.4	1	-5.81	23.5	3.20
dolomite	-3.19	36.1	0.5	-7.53	52.2	0.32

description of the chemical system at any time, seven input variables are required: pH, C, Ca, Mg, Cl, calcite and dolomite - those can be considered ~~, with an abuse of language, state variables, in the sense that since~~ they constitute the necessary  
145 and sufficient inputs of the geochemical subsystem, and all reactions only depend on them. The outcome of the “full physics” calculations is completely defined (at least with the simplifications discussed above) by four distinct quantities: the amounts of reaction affecting the two minerals calcite (i) and dolomite (ii) in the given time step, from which the changes in solutes Ca, Mg and C can be backcalculated; Cl (iii), which is actually non-reactive; and pH (iv). In a completely process-agnostic, data-driven

**Table 2.** Initial (IC) and boundary (BC) conditions for the benchmark problem.

	<b>C</b> molal	<b>Ca</b> molal	<b>Cl</b> molal	<b>Mg</b> molal	<b>pH</b> -	<b>calcite</b> mol	<b>dolomite</b> mol
<b>IC</b>	$1.2279 \cdot 10^{-4}$	$1.2279 \cdot 10^{-4}$	0.00	0.00	9.91	$2.07 \cdot 10^{-3}$	0.00
<b>BC</b>	0.00	0.00	$0.2 \cdot 10^{-2}$	$0.1 \cdot 10^{-2}$	7		

framework, however, the relationships between minerals and aqueous concentrations are disregarded, and the output of the  
150 chemical subsystem is expressed solely in terms of the input variables.

### 2.3 Reference simulations and training data

For the remainder of this work, the geochemical benchmark described above is solved on a 1D column of length 0.5 m, with  
constant fluid velocity of  $u = 9.375 \cdot 10^{-6}$  m/s. The domain is discretised with grid refinements ranging between 50 and 500  
grid elements. Higher refinements have a double effect: on one side larger grids obviously increase the overall computational  
155 load, and in particular for chemistry; on the other side, given the restriction of the implemented forward Euler explicit ad-  
vection scheme, the time stepping required for the coupled simulations in order to be free of numerical dispersion decreases  
accordingly. Smaller time steps decrease the computational load for geochemistry for each iteration, since they require shorter  
time integrations, but also require more coupled iterations to reach the same simulation time. More iterations mean also that  
there are more chances for errors introduced by surrogates to further propagate into the simulations in both space and time. In  
160 presence of significant overhead due to, e.g., data passing between different softwares or the setup of geochemical simulations,  
the advantage due to shorter time steps vanishes. However, these aspects become more relevant in the context of parallelisation  
of geochemistry and are not addressed in the present work.

All coupled simulations, both reference (full physics) and with surrogates, are run with constant time step either honouring  
the CFL condition with  $\nu = 1$ , and thus free of numerical dispersion, or, when assessing how the speedup scales with larger  
165 grids, a fixed time step small enough for the CFL condition (eq. 2) to be satisfied for every discretisation. As previously noted,  
the resulting simulations will be affected by grid-dependent numerical dispersion, which we do not account for in the present  
work. This makes the results incomparable in terms of transport across grids. However, since the focus is on the acceleration  
of geochemistry through pre-computed surrogates, this is an acceptable simplification.

The comparison between the reference simulations, obtained by coupling of transport with the PHREEQC simulator, and  
170 those obtained with surrogates is based on an error measure composed as the geometric mean of the relative RMSEs of each  
variable  $i$ , using the variable's maximum at a given time step as norm:

$$\text{Error}_t = \exp \left\{ \frac{1}{m} \sum_i^m \ln \frac{\sqrt{\frac{1}{n} \sum_j^n (\text{ref}_{i,j} - \text{pred}_{i,j})^2}}{\max_t(\text{pred}_i)} \right\} \quad (3)$$

where  $m$  is the number of variables to compare,  $n$  the grid dimension and  $t$  the particular time step where the error is computed.

175 In this work the datasets used for training the surrogates are obtained directly by storing all calls to the full physics simulator and its responses in the reference coupled reactive transport simulations, possibly limited to a given simulation time. This way of proceeding is considered more practical than, e.g., an a priori sampling of a given parameter space, where the bounds of the parameter space are defined by the ranges of the input/output variables occurring in the reference coupled simulations. This strategy mimics the problem of wanting to train a surrogates directly at runtime during the coupled simulations. Furthermore, an a priori, statistical sampling of parameter space, in absence of restrictions based on the physical relationships between the  
180 variables, would include unphysical and irrelevant input combinations. By employing only the input/outputs tables actually required by the full physics simulations, this issue is automatically solved; however, the resulting datasets will be in general skewed, multimodal and highly inhomogeneously distributed within the parameter space, with highly dense samples in some regions and even larger empty ones.

## 2.4 Hierarchical coupling of chemistry

185 In this work we consider only a Sequential Non-Iterative Approach (SNIA) coupling scheme, meaning that the sub-processes flow, transport and chemistry are solved numerically one after another before advancing to the next simulation step. For sake of simplicity, we let the CFL condition (2) for advection dictate the allowable time step for the coupled simulations.

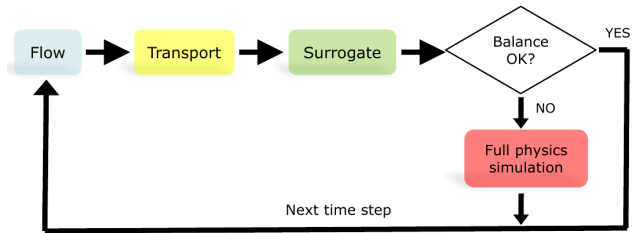
Replacing the time-consuming, equation-based numerical simulator for geochemistry with an approximated but quick surrogate introduces inaccuracies into the coupled simulations. These may quickly propagate in space and time during the coupled  
190 simulations and lead to ultimately incongruent and unusable results.

A way to mitigate error propagation, and thus to reduce the accuracy required of the surrogates, is represented by a *hierarchy of models* used to compute chemistry at each time step during the coupled simulations. The idea is to first ask the surrogate for predictions, then identify unphysical or implausible ones, and finally run the full physics chemical simulator for the rejected ones. This way, the surrogate can be tuned to capture with good accuracy the bulk of the training data, and no particular  
195 attention needs to be paid to the most difficult “corner cases”. For the highly non-linear systems usually encountered in geochemistry, this is of great advantage. In practice, however, there still is need to have a reliable and cheap error estimation of surrogate predictions at runtime.

It is important to understand that the criteria employed to accept or reject the surrogate predictions depend strictly on the architecture of the multivariate surrogate and on the actual regression method used. Methods such as kriging offer error ~~models;~~  
200 ~~based, e.g., variances based~~ on the distance of the ~~estimated-target estimation~~ point from the ~~nearest-training-data-data used for estimation, for a given variogram model~~. However, in the general case, any error estimation requires first the training and then the evaluation at runtime of a second “hidden” model. Both steps can be time-consuming; furthermore, in the general case one can only guarantee that the error is *expected* - in a probabilistic sense - to be lower than a given threshold.

In a completely data-driven surrogate approach, where each of the output variables is independently approximated by a  
205 different multivariate regressor, checking mass conservation is a very inexpensive way to estimate the reliability of a given surrogate prediction, since it only requires the evaluation of linear combinations across predictors and predictions. Other con-

straints may be added, suited to the chemical problem at hand, such as charge balance. However we only use mass balance in the present work. Figure 1 illustrates this simple hierarchical coupling schematically. For the chemical benchmark of sec-



**Figure 1.** Schematic view of hierarchical sequential non iterative coupling. The decision whether to accept or not the predictions of a multiple multivariate surrogate is based on computing the mass balances for the three elements forming dolomite and calcite before and after reaction, and computing their mean absolute error. If this error exceeds a given threshold, the more expensive equation based geochemical simulator is run instead.

tion 2.2, three mass balance equations can be written, one for each element C, Ca and Mg, accounting for the stoichiometry of the minerals’ brute formulas. If a surrogate prediction exceeds a given, predetermined, tolerance on the Mean Absolute Error of the balance equations, that particular prediction is rejected and a more expensive full physics simulation is run instead.

The same procedure is repeated in all coupling iterations for the whole grid, irrespective of previous calls to PHREEQC. Note that calling the numerical simulator only ensures that the results are plausible, i.e., they are guaranteed to honour mass balance at the end of the iteration, but they do not dampen the overall errors w.r.t. a reference simulation if some inaccuracies are already present in the inputs.

This approach moderates the need for extremely accurate regressions, especially in instances of non-linear behaviour of the chemical models, for example when a mineral precipitates for the first time or when it is completely depleted, which are hard things for regressors to capture. However, the number of rejected simulations must be low to produce relevant speedups; it is effectively a trade-off between the accuracy of the surrogates (and efforts and time which goes into their training and complexity) and the speedup achieved in coupled simulations.

### 3 Fully data-driven approach

The first approach is a completely general one, fully data-driven and thus process-agnostic: it can be employed for any kind of numerical model or process which can be expressed in form of input and output tables. In our case, the tables produced by the geochemical sub-process during the reference coupled simulations are used to train seven multiple multivariate regressors, one for each output.

The reference simulations, and hence the dataset for training the surrogate, are fully coupled simulations on grid 50, 100 and 200 with a fixed time step of 210 s, run until 33600 s or else 161 total coupling iterations. The time step is chosen for resulting in  $\nu = 1$  in the largest grid. As previously noted, these simulations are then not comparable among themselves due



to ~~significant numerical dispersion~~ the introduction of numerical dispersion in the lower resolution grids; however, from the  
230 point of view of geochemical processes, this strategy has the advantage of spreading the ~~“perturbations” due to transport of~~  
~~the results of geochemistry in the previous time step~~ sampling of the parameter space for the chemical sub-process, while  
eliminating the time step as free variable. In this setting, one single trained surrogate can be employed on all grids and time  
steps.

Instead of the usual random split of the dataset in train and test subsets, ~~ecostumary~~ customary in the machine learning com-  
235 munity, we retained only the data resulting from the first 101 iterations for training the surrogates, and evaluated the resulting  
reactive transport simulations until iteration 161, where the geochemical surrogate is faced with 60 iterations on unseen or  
“out of sample” geochemical data. The training dataset comprises tables with 13959 unique rows or input combinations. All  
simulations, the reference and those with surrogates, are run on a single CPU core. No further filtering, i.e., elimination of  
data points very near to each other, has been performed. The data do not display clear collinearity, which is expected being  
240 geochemistry a non-linear process.

The choice of the regressor for each output is actually arbitrary, and nothing forbids to have different regressors for each  
variables, or even different regressors in different regions of parameter space of each variable. Without going into details on all  
kinds of algorithms that we tested, we found that decision-tree based methods such as Random Forest and their recent gradient  
boosting evolutions appear the most flexible and successful for our purposes. Their edge can in our opinion be resumed by: (1)  
245 implicit feature selection by construction, meaning that the algorithm automatically recognizes which input variables are most  
important for the estimation of the output. Note that co-linearity is usually not an issue for geochemical simulations; (2) no  
need for standardisation (e.g., centering, scaling) of both inputs and outputs, which helps preserving the physical meaning of  
variables; (3) ~~ability to deal with any probability distributions~~; (4) fairly quick to train with sensible hyperparameter defaults;  
~~(5) extremely efficient implementations available, although they are slower to evaluate than neural networks~~; (4) robustness,  
250 since they revert to mean value when evaluating points outside of training data.

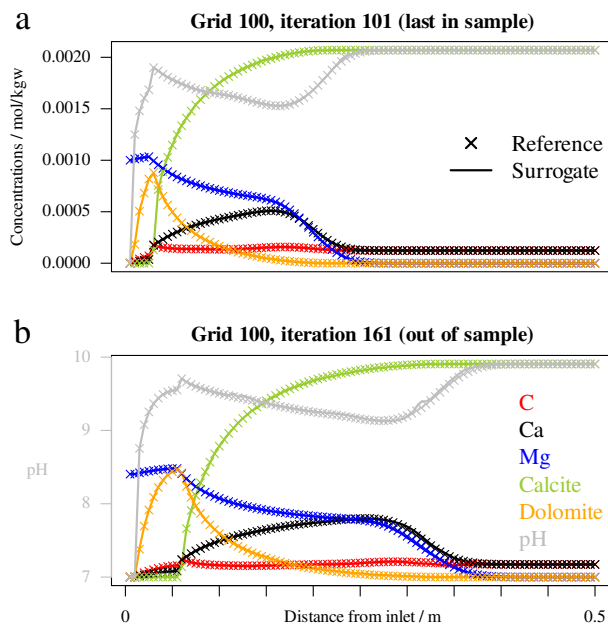
The points number (2)-(4) cannot be overlooked. Data normalisation or standardisation techniques, also called “preprocess-  
ing” in machine learning lingo, are redundant with decision-tree based algorithms, whereas they have a significant impact on  
results and training efficiency with other regressors such as Support Vector Machines and Artificial Neural Networks. The  
distributions displayed by the variables in the geochemical data are extremely variable and cannot be assumed uniform, gaus-  
255 sian or lognormal in general. We found out that the Tweedie distribution is suited to reproduce many of the variables in the  
training dataset. The Tweedie distribution is a special case of exponential dispersion models introduced by Tweedie (1984) and  
thoroughly described by Jørgensen (1987), which finds application in many actuarial and signal processing processes (Hassine  
et al., 2017). A Random Variable  $Y$  is a Tweedie distribution of parameter  $p$  if  $Y \geq 0$ ,  $E[Y] = \mu$  and  $Var(Y) = \sigma^2 \mu^p$ . This  
means that it is a *family* depending on  $p$ : gaussian if  $p = 0$ , Poisson if  $p = 1$ , gamma if  $p = 2$  and inverse gaussian if  $p = 3$ . The  
260 interesting case, which is normally referred to when using the term “Tweedie”, is when  $1 \leq p \leq 2$ . This distribution represents  
positive variables with *positive mass at zero*: meaning that this distribution preserves the “physical meaning” of zero. It’s intu-  
itively an important property when modelling solute concentrations and mineral abundances: the geochemical system solved  
by the full physics simulator is radically different when, e.g., a mineral is present or not.

Extreme gradient boosting `xgboost` (Chen and Guestrin, 2016) is a decision-tree based algorithm which enjoys an enormous success in the machine learning community in recent years. It has out-of-the-box the capability to perform regression of Tweedie variables and it is extremely efficient in both training and prediction. The package has support for GPU computing but we did not use it in the present work. Using the target Tweedie regression with fixed  $p = 1.2$ , max tree depth of 20, the default  $\eta = 0.3$  and 1000 boosting iterations with early stopping at 50, all results in the dataset are reproduced with great accuracy and the training itself takes around 20 seconds for all seven outputs on our workstation, using four `CPU` cores. Contrary to the ~~expectation, the accuracy of the predictions is largely enhanced if the labels (i.e., the output table) are sealed before training.~~ We used the max value of each label divided by expectation and specific statements in the software package, we found that scaling - not recentering - the labels by their maximum value divided by  $1 \cdot 10^{-5}$  as scale  $10^{-5}$ , thus spreading the range of the scaled outputs from 0 to  $10^5$ , greatly improves the accuracy. We did not pursue a more in-depth analysis about this issue, since it probably depends on this specific software, or with the small values of the labels for our geochemical problem. The default evaluation metric when performing Tweedie regression is the Root Mean Squared Log Error:

$$\text{rmsle} = \sqrt{\frac{1}{N} [\ln(\text{pred} + 1) - \ln(\text{label} + 1)]^2} \quad (4)$$

In the previous section it was claimed that in the framework of hierarchical coupling there is no practical need to further refine the regressions. This could be achieved by hyperparameter tuning and by using a different and more adapted probability distribution for each label including proper fitting of parameter  $p$  for the Tweedie variables. While this would be of course beneficial, we proceed now by plugging such a rough surrogate into the reactive transport simulations. The coupled simulations with surrogates are performed on the three grids for 161 iterations, setting the tolerance on mass balance to  $10^{-5}$ ,  $10^{-6}$  and only relying on the surrogate, meaning with no call to PHREEQC even if a large mass balance error is detected.

In Figure 2 are exemplarily displayed the variables profiles for grid 100 and tolerance  $10^{-6}$  at two different time steps, iteration 101, which is the last one within the training dataset, and at the end of the simulation time, after 60 coupling iterations in “unseen territory” for the surrogates. The accuracy of the surrogate simulations is excellent for the 101st iteration, but by iteration 161, while still acceptable, some discrepancies start to show. The number of rejected surrogate responses at each time step does not remain constant during the simulations, but increases steadily. An overview of all the simulations is given in Figure 3 (top frame). The more stringent mass balance tolerance of  $10^{-6}$  (solid lines) rejects obviously many more simulations which goes hand in hand with the excellent accuracy of the results (Figure 3, bottom panel; error measured with formula of equation 3 excluding pH). It was expected, and it is demonstrated by the evaluation, that starting with the first “out of sample” time step the accuracy of the surrogates significantly drops, which triggers a steep increase of rejected predictions and conversely of calls to PHREEQC. The hierarchical coupling ensures that the errors in the surrogate simulations do not follow the same steep increase, but from this moment on there is a loss of computational efficiency, visible in the simulations with tolerance  $10^{-6}$ , which makes the whole surrogate predictions actually useless in terms of speedup even before making them so inaccurate to be useless. It is also apparent from the error panel in Figure 3 (bottom) that errors introduced in the coupled simulations at early time steps propagate through the rest of the simulations, so that the overall discrepancy between reference and surrogate simulations also steadily increases. Note that this “diverging behavior” also tends to bring the geochemistry

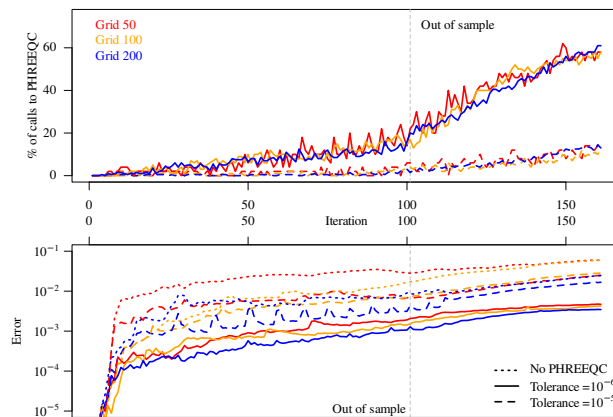


**Figure 2.** Profiles of total concentrations, pH and minerals for reference and hierarchical coupling 1D simulations with tolerance on mass balance error set to  $10^{-6}$ , for grid 100. The ~~top row displays axes are annotated in these figures: all aqueous and mineral concentrations are given in terms of mol per kg of solvent, while pH in its adimensional units.~~ (a) here ist shown the last in sample time step; (b) the ~~bottom the~~ last simulated time step, after 60 iterations for which the surrogate was out of sample.

“out of sample”, in the sense of seen vs. unseen geochemical data, since the training data only comprises “physical” input combinations but, due to the introduced inaccuracies, we are asking the surrogate more and more predictions based on slightly  
 300 “unphysical” input combinations. Having highly accurate surrogates, hence, would be beneficial also in this regard.

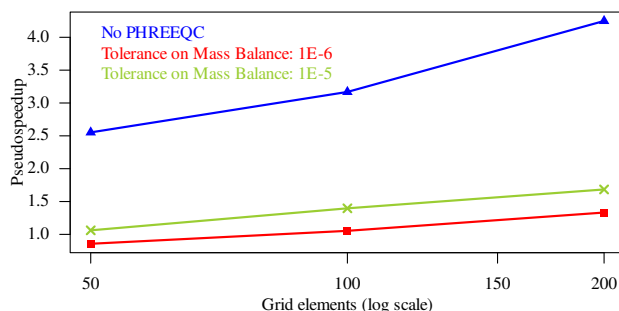
It is difficult to discriminate “a priori” between acceptable and unacceptable simulation results based on a threshold of an error measure such as that of eq. 3, which can be roughly interpreted as “mean percentage error”. This is also a point where in our opinion further research is needed. Relying on the visualisation of the surrogate simulation results and reference, we can summarize that the tolerance on mass balance of  $10^{-6}$  (solid lines in Figure 3) produces accurate coupled simulations, excellent  
 305 accuracy within the time steps of the training data and good accuracy after the 60 out of sample iterations. The tolerance of  $10^{-5}$  as well as the simulations based solely on surrogates produce acceptable accuracy in sample but unusable and rapidly diverging results out of sample. For the given chemical problem, the  $10^{-6}$  tolerance on mass balance could be relaxed, whereas the  $10^{-5}$  is too optimistic. The optimal value, at least for the considered time steps, lies between these two values.

The overall speedup - in terms of total wall clock time of the coupled simulations, thus including also CPU time used  
 310 for advection and all the overheads, although both much less computationally intensive than chemistry, and therefore termed pseudo speedup - with respect to the reference simulations is summarized in Figure 4. Here the whole 161 iterations, also all the out of sample ones are considered. Pseudo speedup increases with grid size as expected. The accurate  $10^{-6}$  simulations



**Figure 3.** Purely data-driven approach: evaluation of calls to full physics simulator for the runs with hierarchical coupling for the three discretisations à 50, 100 and 200 elements, and of overall discrepancy between surrogate simulations and reference. When the surrogate enters the region of “unseen data”, its accuracy degrades significantly, which causes loss of efficiency rather than accuracy.

are not accelerated on grid 50 (pseudo speedup of 0.86), but they reach 1.33 on the 200 grid. The surrogate-only speedup



**Figure 4.** Overall pseudo speedup (total wall clock time) after 161 iterations for coupled simulations with hierarchical coupling and only relying on the surrogate.

starts at around 2.6 for the 50 grid and reaches 4.2 for the 200 grid, ~~and that can be taken as a measure of achievable speedup, in projection, by using extremely accurate surrogates.~~ Considering only the first 101 iterations, the  $10^{-6}$  simulations would achieve speedup slightly larger than one already on the 50 elements grid, and be well over 2 on the 200 grid. ~~Extrapolating to grids with  $10^5$  or  $10^6$  elements, speedups in the order of 25-50 are achievable for this chemical problem. The speedup will arguably increase even further in presence of more complex chemistry.~~

#### 4 Surrogates based on geochemical knowledge

320 The above presented fully data-driven approach disregards any domain knowledge or known physical relationships between variables besides those which are picked up automatically by the multivariate algorithms operating on the input/outputs in the training data.

We start [this a second](#) approach by considering the actual “true” degrees of freedom for the geochemical problem, which is fully described by seven inputs and four outputs:  $\Delta\text{calcite}$ ,  $\Delta\text{dolomite}$ , Cl and pH. This means that we will have to calculate  
325 back the changes in concentrations for C, Ca and Mg, risking a quicker propagation of errors if the reaction rates of the minerals are incorrectly predicted, [but honouring by construction the mass balance](#).

The reference simulations for this part are run with  $\nu = 1$  and thus without numerical dispersion on four different grids: 50, 100, 200 and 500 elements respectively. This implies that the simulation on grid 500 has ten times more coupling iterations than the 50 grid, or in other terms, that the allowable time step in grid 500 is a tenth of that for grid 50.

330 A common way to facilitate the task of the regressors by “injecting” physical knowledge into the learning task of the algorithms is to perform *feature engineering*: this simply means computing new variables defined by non-linear functions of the original ones, which may give further insights regarding multivariate dependencies, hidden conditions or relevant subsets of the original data.

For any geochemical problem involving dissolution or precipitation of minerals, each mineral’s saturation ratio (SR) or  
335 its logarithm SI (Saturation Index) discriminates the direction of the reaction. If  $\text{SR} > 1$  (and thus  $\text{SI} > 0$ ) the mineral is oversaturated and precipitates; it is undersaturated and dissolves if  $\text{SR} < 1$  ( $\text{SI} < 0$ );  $\text{SR} = 1$  ( $\text{SI} = 0$ ) implies local thermodynamic equilibrium. Writing the reaction of calcite dissolution:



The Law of Mass Action (LMA) relates, at equilibrium, the activities of the species present in the equation. We conventionally  
340 indicate activity with square brackets. For eq. 5, the LMA reads:

$$\begin{aligned} K_{\text{Cc}}^{\text{eq}} &= \frac{[\text{Ca}^{+2}]_{\text{eq}} \cdot [\text{HCO}_3^-]_{\text{eq}}}{[\text{H}^+]_{\text{eq}}} \\ &= \frac{\text{Ca}_{\text{eq}}^{+2} \cdot \text{HCO}_3^-_{\text{eq}}}{[\text{H}^+]_{\text{eq}}} \cdot \gamma_{\text{Ca}^{+2}} \gamma_{\text{HCO}_3^-} \end{aligned} \quad (6)$$

where  $\gamma$  stands for the activity coefficient of subscripted aqueous species. The solubility product  $K_{\text{Cc}}^{\text{eq}}$  at equilibrium, tabulated in thermodynamic databases, is a function of temperature and pressure and defines the saturation ratio:

$$345 \text{ SR}_{\text{Cc}} = \frac{1}{K_{\text{Cc}}^{\text{eq}}} \frac{\text{Ca}^{+2} \cdot \text{HCO}_3^-}{[\text{H}^+]} \cdot \gamma_{\text{Ca}^{+2}} \gamma_{\text{HCO}_3^-} \quad (7)$$

The estimation of the saturation ratio of equation 7 using the elemental concentrations available in our training data is the first, natural feature engineering [tentative we can try](#). Hereby, a few assumptions must be made.

Using total elemental concentrations as proxy for species activities implies neglecting the actual speciation to estimate the ion activity products, but also the difference between concentration and activity - “true” activity  $[\text{H}^+]$  is known from the pH-[7](#)

350 **but also not relying on.** For the chemical problem at hand, as it will be shown, it is a viable approximation, but it will not be in presence of strong gradients of ionic strength or in general for more complex or concentrated systems. An exception to this simplification is required for dissolved carbon due to the well known buffer. In this case, given that the whole model is at pH between 7 to 10, we may assume that two single species dominate the dissolved carbon speciation:  $\text{CO}_3^{-2}$  and  $\text{HCO}_3^-$ . The relationship between the activities of those two species is always kept at equilibrium in the PHREEQC models and thus, up to the “perturbation” due to transport, also in our dataset. This relationship is expressed by the reaction and the corresponding law of mass action written in eq. 8:



The closure equation, expressing the approximation of total carbon concentration as the sum of two species, gives us the second equation for the two unknowns:

$$360 \quad C = \text{HCO}_3^- + \text{CO}_3^{-2} \quad (9)$$

Combining eq. 8 and 9 we get the estimation of dissolved bicarbonate (the wide tilde indicates that it is an estimation) from the variables total carbon and pH comprised in our dataset and an externally calculated thermodynamic constant:

$$\widetilde{\text{HCO}_3} := \frac{C \cdot [\text{H}^+]}{K_{\text{carb}}^{\text{eq}} + [\text{H}^+]} \quad (10)$$

Now we can approximate the theoretical calcite saturation ratio  $\widetilde{\text{SR}}_{\text{Cc}}^{\text{theor}}$  with the formula:

$$365 \quad \widetilde{\text{SR}}_{\text{Cc}}^{\text{theor}} := \frac{\text{Ca} \cdot \widetilde{\text{HCO}_3}}{[\text{H}^+] \cdot K_{\text{Cc}}^{\text{eq}}} = \frac{\text{Ca} \cdot C}{K_{\text{Cc}}^{\text{eq}} (K_{\text{carb}}^{\text{eq}} + [\text{H}^+])} \quad (11)$$

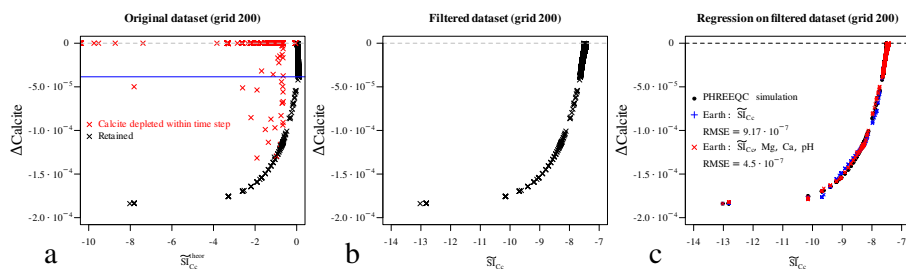
The two thermodynamic quantities (at 25 °C and atmospheric pressure)  $K_{\text{carb}}^{\text{eq}} = 10^{-10.3288}$  and  $K_{\text{Cc}}^{\text{eq}} = 10^{-2.00135}$  were computed with the CHNOSZ package for the R environment (Dick, 2019), but may also be derived with simple algebraic calculations from, i.e., the same PHREEQC database employed in the reactive transport simulations.

Do these two newly defined variables, or “engineered features”, bicarbonate and calcite saturation ratio, actually help to better understand and characterize our dataset? This can be simply assessed by plotting the  $\Delta_{\text{calcite}}$  against the logarithm of  $\widetilde{\text{SR}}_{\text{Cc}}^{\text{theor}}$ , which is the  $\widetilde{\text{SI}}_{\text{Cc}}^{\text{theor}}$  (Figure 5a, leftmost panel, dataset from the reference simulations on grid 200, which will be used from now on to illustrate the analysis since it contains enough data points) in the data. While many points remarkably lie on a smooth curve (colored in black), many others are scattered throughout the graph (in red). It is easy to observe that those red points are either on the trivial  $\Delta_{\text{calcite}}=0$  line, implying that calcite is undersaturated but not present in the system so nothing happens, or else the reaction did not reach the amount which could have been expected based on its initial undersaturation simply because calcite has been completely depleted during the timestep. All the red points correspond in **facts** **fact** to simulations with calcite=0 in the labels (results) dataset. The retained black points, however, belong to timesteps where the dissolution of calcite is limited by kinetics and not by its initial amount, and can be thus used to estimate the reaction rate.

Figure 5a also displays a problem with the defined  $\widetilde{SR}_{Cc}^{theor}$  : its relationship is not bijective with the  $\Delta calcite$ . This means  
 380 that we should proceed now to split the data in two different regions above and under the cusp (signalled by the blue horizontal line). However, just simply dropping the denominator of equation 11 solves this problem to a large extent:

$$\widetilde{SR}_{Cc} := Ca \cdot C \quad (12)$$

The center panel of Figure 5b shows the scatter plot of  $\Delta calcite$  versus the simplified  $\widetilde{SI}_{Cc}$ . All points lie now on a smooth curve, and the relation between the two variables is indeed quite perfectly bijective, with the exception of points very close  
 385 to the  $\Delta calcite=0$  line, where they are more scattered; but since those points also correspond to the smallest amounts of reactions, we can deem this as successful approximation. Note that dropping the denominator in the definition of  $\widetilde{SR}_{Cc}$  also means that this feature does not reach one at equilibrium (and  $\widetilde{SI}_{Cc}$  zero), which is clear observing the range of the x-axis in panels a and b of Figure 5. This has however no practical consequence for this problem: calcite is always undersaturated or at equilibrium in the benchmark, and we just defined a simple feature which is in bijective relationship with the amount of  
 390 “true” dissolution in the data. While it could be possible to derive an analytical functional dependency between the observed amount of dissolved calcite and the estimated  $\widetilde{SI}_{Cc}$ , for example manipulating the kinetic law, we opted to use a regressor instead. The good bijectivity between the two variables means that we should be able to regress the first using only the second. In the rightmost panel of Figure 5c are plotted in blue the *in sample* predictions of a Multivariate Adaptive Regression Spline model (MARS) (Friedman, 1991, 1993), computed through the `earth` R package (Milborrow, 2018), based only on  $\widetilde{SI}_{Cc}$ .  
 395 The accuracy is already acceptable indeed; however including further predictors from the already available features, in this case pH, Ca and Mg, a better regression (in red) is achieved, improving the RMSE of more than factor two.



**Figure 5.** (a) Scatter plot of  $\Delta calcite$  vs estimated  $\widetilde{SI}_{Cc}^{theor}$ . The datapoints in red cannot be used to estimate the reaction rate from the dataset since calcite is depleted within the simulation time step. Furthermore, the retained points are not in bijective relationship with the  $\Delta calcite$ , with the blue horizontal line separating two regions where bijectivity is given. (b)  $\Delta calcite$  versus the simplified  $\widetilde{SI}_{Cc}$ : bijectivity is achieved. (c) A MARS regressor is computed for the retained data points, based solely on the estimated  $\widetilde{SI}_{Cc}$  (in blue) and using also other predictors to ameliorate the multivariate regression.

Before moving forward, two considerations are important. First, the red points of Figure 5a should not be used when trying to estimate the rate of calcite dissolution, since they result from a steep and “hidden” non-linearity or discontinuity in the

underlying model. This is a typical example of data potentially leading to overfitting in a machine-learning sense. Secondly,  
 400 this “filter” does not need to be applied at runtime during coupled reactive transport simulations: it suffices to estimate correctly  
 the reaction rate given the initial state and then ensure that calcite does not reach negative values.

More interesting and more demanding is the case of dolomite, which firstly precipitates and then re-dissolves in the bench-  
 mark simulations. In a completely analogous manner as above we define its saturation ratio  $\widetilde{SR}_{Dol}$  as:

$$\widetilde{SR}_{Dol} = \frac{Mg \cdot Ca \cdot C^2}{[H^+]^2 \cdot K_{Dol}^{eq}} \quad (13)$$

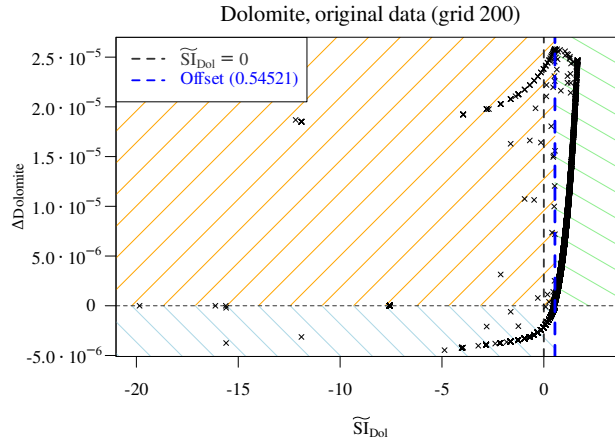
405 thus using the total elemental dissolved concentration of C and with  $K_{Dol}^{eq} = 10^{3.647}$  resulting from the reaction:



The theoretical value of  $K_{Dol}^{eq} = 10^{3.647}$  used for calculation of  $\widetilde{SI}_{Dol}$  does not discriminate the initially undersaturated from the  
 oversaturated samples (dashed vertical black line in Figure 6). The “offset” which would serve us for a correct discrimination is  
 nothing else than the maximum value of  $\widetilde{SR}_{Dol}$  restricted to the region where  $\Delta_{dolomite} \leq 0$ . We correspondingly update  
 410 the definition of  $\widetilde{SR}_{Dol}$ :

$$\widetilde{SR}_{Dol} = \frac{Mg \cdot Ca \cdot C^2}{[H^+]^2 \cdot K_{Dol}^{eq}} - \max(\widetilde{SR}_{Dol} | \Delta_{dolomite} \leq 0) \quad (15)$$

Now we are guaranteed that the vertical line  $\widetilde{SR}_{Dol}=1$  (or equivalently,  $\widetilde{SI}_{Dol}=0$ , plotted with a dashed blue line in Figure 6)



**Figure 6.** Scatter plot of  $\Delta_{dolomite}$  vs estimated  $\widetilde{SI}_{Dol}$ . The theoretical  $\widetilde{SI}_{Dol}=0$  does not discriminate the initially undersaturated from the  
 oversaturated samples (dashed vertical black line), and must be corrected with an apparent offset (blue dashed line). The plot identifies three  
 distinct regions in parameter space: initially supersaturated and precipitating dolomite (top right, green shading); initially undersaturated  
 and dissolving (bottom left, blue shading); and points where dolomite is initially undersaturated but ends up precipitating (top left, orange  
 shading).

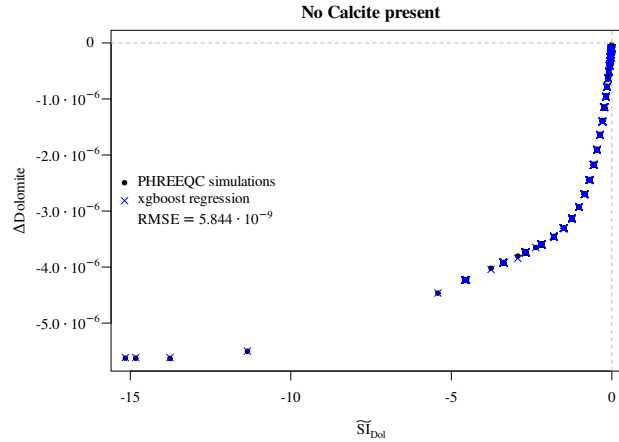
divides correctly the parameter space in four distinct quadrants. Note that this offset emerges from the actual considered data,



and depends on the perturbation of the concentrations due to transport and thus, in our simple advective scheme, on the grid  
 415 resolution through the time step. It follows that a different offset is expected for the other grids, and a different learning for  
 each grid is necessary.

The green shaded, top right quadrant points to dolomite precipitation in initially supersaturated samples; the bottom left,  
 blue shaded contains solutions initially undersaturated w.r.t. dolomite and, if present, dissolving; the top left, orange shaded  
 quadrant is the most problematic: dolomite is initially undersaturated but, presumably due to the concurring dissolution of  
 420 calcite, it becomes supersaturated during the time step and hence precipitates.

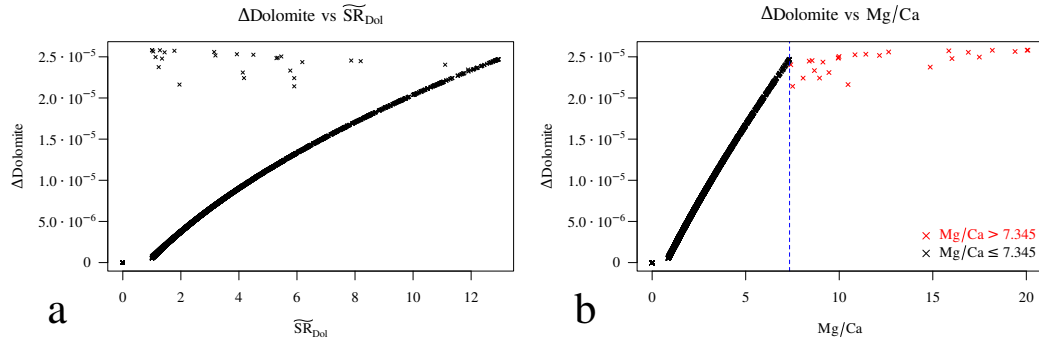
First of all, we note that the initial presence of calcite is a perfect proxy for  $\tilde{SI}_{Dol}$ . If calcite is initially present in points  
 reached by the reactive magnesium chloride solution, then dolomite precipitates. When calcite is completely depleted, then  
 dolomite starts dissolving again. The dissolution of dolomite in absence of calcite follows the same logic as the dissolution  
 of calcite above: a few points are scattered inbetween the line  $\Delta dolomite=0$  and the envelope of points lying on a well  
 425 defined curve. These scattered points are again those where dolomite is depleted within the time step, so they are excluded. For  
 the remaining points, an xgboost regressor based on the predictors  $\tilde{SI}_{Dol}$ , pH, C, Cl, Mg and dolomite achieves an excellent  
 accuracy (Figure 7) in reproducing the observed  $\Delta dolomite$ . The top right quadrant of Figure 6, corresponding to the case of



**Figure 7.** Regression of  $\Delta dolomite$  vs estimated  $\tilde{SI}_{Dol}$  for the cases where no calcite is initially present. The multivariate regressor makes  
 use of the predictors  $\tilde{SI}_{Dol}$ , pH, C, Cl, Mg and dolomite.

dolomite precipitating while calcite is dissolving, cannot be explained based only on the estimated  $\tilde{SI}_{Dol}$  since their relationship  
 is not surjective (Figure 8a). Here again we can use a piece of domain knowledge to engineer a new feature to move forward.  
 430 The Mg/Ca ratio is often used to study the thermodynamics of dissolution of calcite and precipitation of dolomite (Möller and  
 De Lucia, 2020). Effectively, the occurring overall reaction which transforms calcite into dolomite reads:



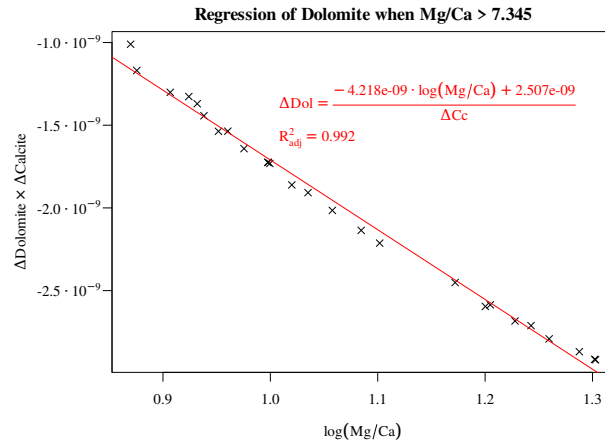


**Figure 8.** Precipitation of dolomite in presence of calcite. **(a)** the relationship between  $\Delta_{\text{dolomite}}$  and its saturation ratio is not surjective. **(b)** The Mg/Ca ratio perfectly discriminates two distinct regions in parameter space.

By applying the law of mass action to reaction 16, it is apparent that its equilibrium constant is a function of the Mg/Ca ratio (of its inverse in the form of equation 16). Plotting the  $\Delta_{\text{dolomite}}$  versus the initial Mg/Ca ratio, a particular ratio of 7.345 discriminates between two distinct regions for this reaction. Incidentally, this splitting value corresponds to the highest observed  $\widetilde{SR}_{Dol}$  in the training data; again, as previously noted for the offset on the estimated saturation index, this numerical value depends on the considered grid and time step. On the left hand region we observe a smooth, quasi-linear dependency of the amount of precipitated dolomite on initial Mg/Ca. This is a simple bijective relationship where we can apply a simple monovariate regression. The amount of precipitated dolomite is accurately predicted by a MARS regressor using the sole Mg/Ca as predictor.

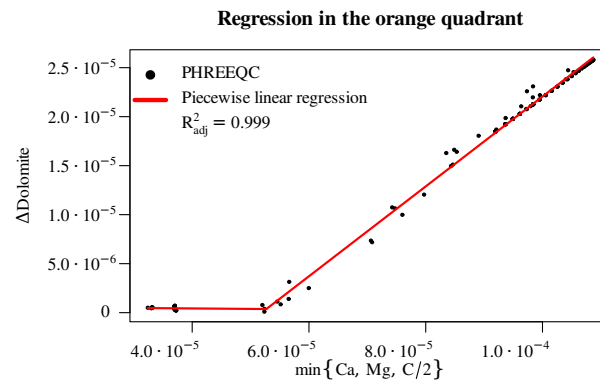
The region on the right of the splitting ratio can be best understood considering the fact that the precipitation of dolomite is limited, in this region, by a concurrent amount of calcite dissolution. The full physics chemical solver finds iteratively the correct amounts of calcite dissolution and dolomite precipitation while honoring both the kinetic laws and all the other conditions for a geochemical DAE system (mass action equations, electroneutrality, positive concentrations, activity coefficients, ...). We cannot reproduce such articulate and “interdependent” behavior without knowing the actual amount of dissolved calcite: we are forced here to employ the previously estimated  $\Delta_{\text{calcite}}$  as a “new feature” to estimate of the amount of dolomite precipitation, albeit limited to this particular region of the parameter space. A surprisingly simple expression, fortunately, captures this relationship quite accurately (Figure 9). This implies of course that during coupled simulations first the  $\Delta_{\text{calcite}}$  must be computed, and relying on this value, the  $\Delta_{\text{dolomite}}$  can be further estimated.

The last parameter space region which is left to consider is the orange-shaded, topleft quadrant of Figure 6. Here, although dolomite is undersaturated at the beginning of the time step, it still precipitates in the end, following the concurrent dissolution of calcite which changes its saturation state. Since however we already calculated the  $\Delta_{\text{calcite}}$ , we can update the concentrations of dissolved Ca and C of corresponding amounts. One of these two concentrations, together with that of Mg, will constitute a limiting factor for the precipitation of dolomite. Hence, plotting the  $\Delta_{\text{dolomite}}$  against the minimum value of these three concentrations at each point (C must be divided by two for the stoichiometry of dolomite), we obtain a piecewise-



**Figure 9.** Regression of  $\Delta$ dolomite in the right hand region of Figure 8b.

linear relationship with limited non-linear effects. A very simple regression is hence sufficient to capture the bulk of the “true model behavior” for all these data points (Figure 10). Now the behavior of calcite and dolomite is fully understood and we dis-



**Figure 10.** Piecewise-linear regression for the orange-shaded, top left quadrant of figure 6 based on the limiting elemental concentration after having considered calcite dissolution.

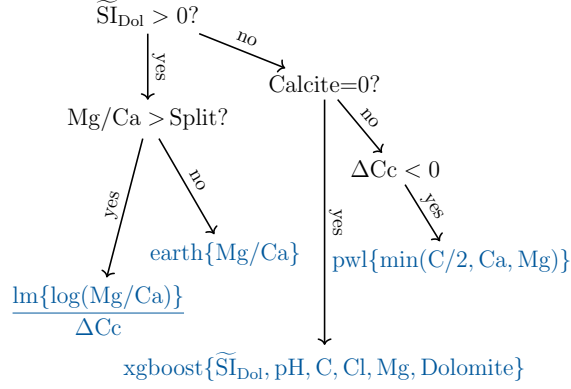
pose of a surrogate for both of them. Among the remaining output variables, only pH needs to be regressed: Cl is non-reactive, meaning that the surrogate is the identity function. For pH, while it could be possible to derive a simplified regression informed with geochemical knowledge, we chose for simplicity to use the xgboost regressor.

Summarizing, we effectively designed a *decision tree*, based on domain knowledge, which enabled us to make sense of the “true” data, to perform physically meaningful feature engineering and ultimately to define a surrogate model “translated” to the data domain (Figure 11). The training of this decision tree surrogate consists merely in computing the engineered features,

### 1. $\Delta\text{Calcite}$

$\text{earth}\{\widetilde{\text{SI}}_{\text{Cc}}, \text{Ca}, \text{Mg}, \text{pH}\}$

### 2. $\Delta\text{Dolomite}$



### 3. pH

$\text{xgboost}\{\text{all inputs}\}$

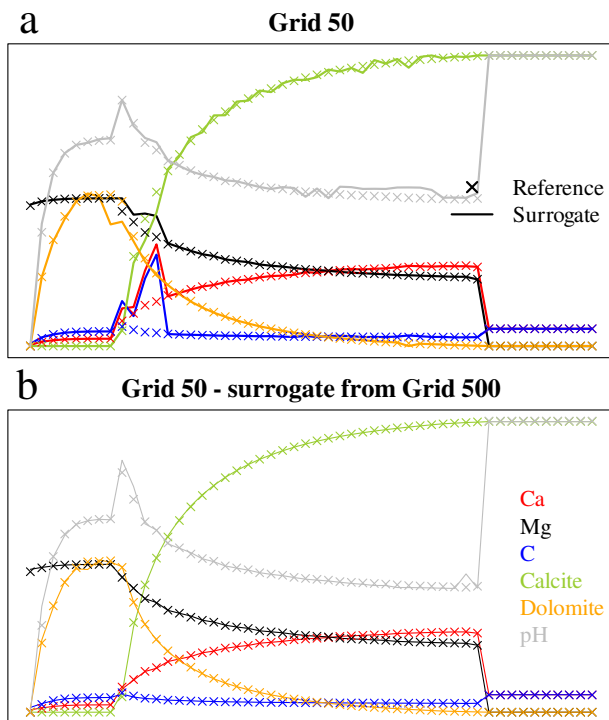
**Figure 11.** Decision tree for the surrogate based on physical interpretation of the training dataset. The engineered features are used as splits and as predictors for different regressions depending on the region of parameter space. The abbreviations “lm” and “pwl” stand respectively for “linear model” and for “piecewise-linear” regression.

finding the apparent offset for the  $\widetilde{\text{SI}}_{\text{Dol}}$ , the split value for the Mg/Ca ratio, and performing six distinct regressions on data  
 465 subsets, of which three are monivariate and two use less predictors than the corresponding completely data-driven counterpart.  
 All of them, excluding pH, only use a subset of the original training dataset. On our workstation, this operation takes few  
 seconds. The resulting surrogate is valid for the  $\Delta t$  of the corresponding training data.

To evaluate the performance of this surrogate approach, a decision tree is trained separately for each grid (and hence  $\Delta t$ )  
 using the reference timesteps until 42000 seconds, whereas the coupled simulations are prolonged to 60000 s, so that at least  
 470 30 % of the simulation time is computed on unseen geochemical data.

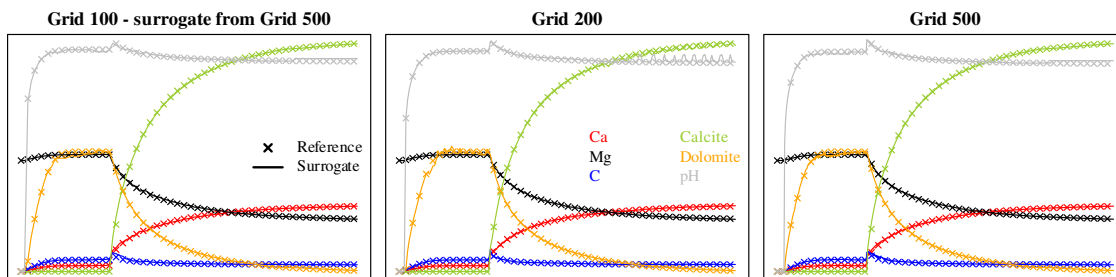
The top panel of Figure 12 shows the results of the coupled simulation for grid 50 using the surrogate trained on the same  
 data, at the end of the iterations used for training. Discrepancies with respect to the reference full physics simulation are already  
 evident. The problem here is that the training dataset is too small and the time step too large for the decision tree surrogate  
 to be accurate. However, nothing forbids to perform “inner iterations” for the chemistry using a surrogate trained on a finer  
 475 grid, which directly corresponds to smaller  $\Delta t$ . For grid 50 ( $\Delta t=1066$  s) we can hence use the surrogate trained on grid 500  
 ( $\Delta t=106.6$  s) just calling it 10 times within each coupling iterations. The bottom panel of Figure 12 displays the corresponding

results. The same problem affects the grid 100, which also requires the surrogate trained on grid 500, reiterated 5 times in this



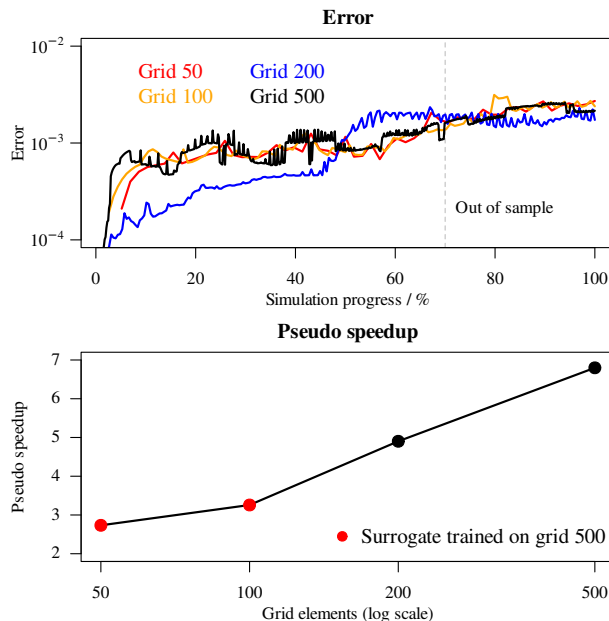
**Figure 12.** Comparison of variables profiles for coupled simulations using the decision tree approach versus the references, at the end of the timesteps used for training for grid 50 (41 coupled iterations). The axes are the same as in Figure 2. (a) decision tree trained on the data from reference grid 50 ( $\Delta t=1066$  s). (b) surrogate simulations using decision tree trained on grid 500 ( $\Delta t=106.6$  s), repeated 10 times for each coupling time step.

case. The grids 200 and 500 are fine with ~~the~~their own reference data, as can be seen in Figure 13, this time displaying the end of simulation time at 60000 s.



**Figure 13.** Variable profiles after 60000 s (simulation time) for grids 100, 200 and 500. The axes are the same as in Figure 2.

480 In Figure 14 are summarised the errors of the surrogates simulations (top panel) and the overall pseudo speedup after 60000 s (bottom panel). While inaccuracies are indeed introduced in the coupled simulations by the decision tree surrogate, crossing the “out of sample” boundary does not provoke a steep increase in error. Even if the overall error is slightly larger than the corresponding purely data-driven simulations with  $10^{-6}$  tolerance, the physics-based approach has the major advantage of being much more robust when encountering unseen data. Moreover, since no calls to PHREEQC are issued at all during these  
 485 simulations, the performance of the coupled simulations is not going to degrade during the simulation time. The physics-based surrogates achieve large pseudo speedups, starting with 2.7 for the grid 50 and reaching 6.8 for the 500 grid (Figure 14, bottom panel).



**Figure 14.** Top: errors of surrogate simulations w.r.t. references. Bottom: overall pseudo speedup after 60000 s.

Note that the decision tree approach has been implemented in pure high-level R language (up to the calls to the regressors `xgboost` and `earth`, which are implemented in low-level languages such as C/C++) and is not optimized. A better imple-  
 490 mentation would further improve its performance, especially in the case where repeated calls to the surrogate are performed at each coupled iteration.

## 5 Discussion and future work

The results presented in this work devise some strategies which can be ~~successfully~~ exploited to speedup reactive transport sim-  
 ulations. The simplifications concerning the transport and the coupling itself (~~stationary flow; in the present work are obviously~~  
 495 ~~severe: stationary, incompressible and isothermal flow; regular, homogeneous grids;~~ pure advection with dispersive full explicit

forward Euler scheme ~~no feedback of chemistry and constant time stepping~~ pertain to hydrodynamics. From the point of view of chemistry, the lack of feedback on porosity and permeability~~the initially homogeneous mediumkinetic rate~~, the kinetic rates not depending on reactive surfaces ~~are obviously severe, but most of them should only marginally affect the validity of the benchmarks concerning the achievable speedup of geochemistry in a broad class of problems~~ and the presence of only

500 two reacting minerals. However, while it is still to be assessed how both surrogate approaches will perform once removing these limitations, a number of real world problems already fall in the complexity class captured by the benchmarks in this work, for example the modelling of laboratory flow-through reactive transport experiments, which are usually performed in controlled, simplified settings aimed at evaluating kinetic rates or the permeability evolution following from mineral reactions (Poonoosamy et al., 2020).

505 A fully data-driven approach, combined with a hierarchical coupling in which full physics simulations are performed only if surrogate predictions are found implausible, is feasible and promises significant speedups for large scale problems. The main advantage of this approach is that the same “code infrastructure” can be used to replace any physical process, not limited to geochemistry: it is completely general, and it could be implemented in any multiphysics toolbox to be used for any co-simulated process. The hierarchy of models for process co-simulation is a vast research field on itself. This idea has to our

510 knowledge never been implemented specifically for reactive transport, but has been proposed, e.g., for particular problem settings in fluid dynamics and elastomechanics (Altmann, 2013; Altmann and Heiland, 2015) and in the broader context of theoretical model reduction and error control (Domschke et al., 2011). This is however a fertile interdisciplinary research task and it is not difficult to foresee that significant progress in this area will soon be required to facilitate and fully leverage the powerful machine learning algorithms already available, in order to speedup any complex, multiscale numerical simulations.

515 The coupling hierarchy implemented in this work ~~is obviously extremely simple and~~ cannot be directly compared with the above cited works, since it is merely based on a *a posteriori* evaluation of plausibility of geochemical simulations. Furthermore, it exploits redundant regressions, which is suboptimal, albeit practical: in effects, regressing more variables than strictly necessary is not much different than regressing the true independent variables and their error models. Since the surrogate predictions are so cheap compared to the full physics, it would be only slightly beneficial to first interrogate the error model and then go

520 directly to the full physics instead of computing at once the whole surrogate predictions and check it afterwards. Nevertheless, several improvements can be implemented with respect to the hierarchy presented in this work. The first would be to add charge balance to the error check at runtime. For different classes of chemical processes, other criteria may be required. For example check on mass action laws can be implemented for models requiring explicit speciation, like in the simulations of radionuclide diffusion and sorption in storage formations. Another one would be to actually eliminate one or more redundant regression

525 and base the error check on the accordance between the overlapping one. As an example, one could regress the  $\Delta$ dolomite,  $\Delta$ calcite and  $\Delta$ Ca, limiting in practice the mass balance check to one element.

In our opinion there is no point in discussing if there is one most suitable or most efficient regression algorithm. This largely depends on the problem at hand and on the skills of the modeller. While we rather focused on gradient boosting decision-tree regressors for the reasons briefly discussed in section 3, a consistent number of authors successfully applied

530 artificial neural networks to a variety of geochemical problems and coupled simulations (Laloy and Jacques, 2019; Guérillot

and Bruyelle, 2020; Prasianakis et al., 2020). ~~We would like to point out that transforming~~ Transforming geochemistry - as any other physical process - in a pure machine learning problem requires on one hand skills that are usually difficult for the geoscientists to acquire, and on the other it fatally overlooks domain knowledge that can be used to improve at least the learning task, which will directly result in accurate and robust predictions, as we demonstrated in section 4. Feature engineering based on known physical relationships and equations should be part of any machine learning workflow anyway; building experience in this matter, devising suitable strategies for a broad class of geochemical problems is in our opinion much more profitable than trying to tune overly complex “black box” models of general applicability. ~~The~~ Nevertheless, the popularization of high-level programming interfaces to generate and train such models, specifically addressing hyperparameter tuning with methods such as grid search, randomized and Bayesian optimization, mitigates the difficulty that a domain scientist faces when dealing with these problems.

A purely data-driven approach has its own rights and applications. As already noted, it is a completely process-agnostic approach which can be implemented in any simulator for any process. However, in absence of physical knowledge *within* the surrogate, the training data must cover beforehand all the processes and the scenarios happening in the coupled simulations. On-demand training and successive incremental update of the surrogates at runtime during the coupled simulations would mitigate this issue. This would require a careful choice of the regressors, since not all of them have this capability, and possibly a sophisticated load balance distribution within the simulator, likely viable only in the context of massive parallel computing. In perspective, however, this is a feature that in our opinion should be implemented in the numerical simulators. A second issue, related to the first, is that a data-driven surrogate trained on a specific chemical problem (intending here initial conditions, concentration of the injected solutions, mineral abundances, time steps...), is not automatically transferable to different problem settings, even when for example only a single kinetic constant is varied. Again, shaping the surrogate following the physical process to be simulated seem here the most straightforward way to overcome this issue, at least partially. One would ~~dispose of partial~~ in fact dispose of regressions in specific parameter space regions which could be parametrically varied following changes in underlying ~~parameters-variables~~. A typical example would be the temperature effect on kinetics, where the law is of Lasaga type: assuming negligible influence of temperature on mineral’s equilibrium constant and solutes activities, a surrogate expressing the reaction rate at 25 °Celsius can be transformed to another temperature by just multiplying it by a factor derived from the Arrhenius term in the original kinetic law.

It remains to be assessed if and how it is possible to generalize and automate the physics-based surrogate approach devised in section 4 on geochemical problems of higher complexity, i.e., with many minerals reacting. No claim of optimality is made about the actual choice of engineered features we made for this chemical benchmark: different features could possibly explain the data even more simply, and thus the chemical process. The important part is the principle: identify relationships ~~as-bijective~~ as possible-as bijective as possible between input and output parameters, compartmentalized in separated regions of parameter space, using features derived by the governing equations. An automation of feature engineering based on stoichiometry of the ~~minerals-considered reactions~~ is a straightforward extension, since it can be achieved by simply parsing the thermodynamic ~~databases~~database. An automatic application of the approach starting with a large number of engineered features may originate



565 forests of trees much like the well known random forest or gradient boosting algorithms, but specialised in geochemical models:  
a true hybrid physics-AI model.

Also, the regressors which constitute the leaves of the decision tree of Figure 11 are completely arbitrary and were selected based on our own experience. A more in-depth breakdown of the relationships between variables, for example analytical expressions derived directly from the kinetic law, could reduce most or all regressions to simple statistical linear models, which  
570 would even further increase the interpretability of the surrogate.

In this work fixed time stepping was used for all coupled simulations. A partial extension to variable time stepping has been devised with the “inner iteration” approach demonstrated with the physics-informed decision tree surrogate: one can recursively call a surrogate on itself, trained on fixed “training  $\Delta t$ ” until reaching the “required  $\Delta t$ ”. This is obviously valid only for multiples of the “training  $\Delta t$ ”; for non-multiples, some further (non-linear!) interpolation between the inner iterations  
575 nearest to the required time step is required. A more flexible and general approach would be treating the time step as a free, independent and non-negative variable. However, this would require even larger training datasets and hence training times. Assessing an optimal approach for variable time stepping remains high priority for future work.

At the moment no conclusive statement can be made about the general applicability of any surrogate approach to complex settings usually encountered in the praxis, and on the achievable overall speedup - they are strictly problem and implementation-dependent  
580 to cover them in a general way.

From inhomogeneous, irregular grids with transient flow regimes, to highly variable initial spatial distribution of mineralogy and sharp gradients in ionic strengths, these are all factors making the learning task more difficult, either because regression of many more variables (e.g., ionic strength or even activity coefficients) becomes necessary, or because much more data are needed in order to obtain coverage of parameter space of higher dimensionality. Embedding domain knowledge into the  
585 surrogate seems the most natural way in order to counter this increase in difficulty. For the second issue, the generation of training data, we believe that the sampling strategy of parameter space used for training should be further optimized. In the simple approach presented in this work - also justified by the fact that we deal with small grids - all the data from the reference simulations were considered, with the only filtering being the removal of duplicated data points. In these datasets many points are concentrated near to others while other regions of parameter space are underrepresented. In problems of  
590 increasing complexity and higher dimensionality it becomes paramount to include only data with high informative content in the training dataset to speedup the learning phase. Note that if the training data are taken from reference, “true” coupled simulations, we are guaranteed that the sampling is always physically plausible - this is not the case if we build the training dataset by pre-computing geochemistry for example on a regularly sampled grid covering the whole parameter space. This approach can include physically unfeasible parameter combinations, which may introduce bias into the surrogate.

## 595 6 Conclusions

Employing surrogates to replace computationally intensive geochemical calculations is a viable strategy to speedup reactive transport simulations. A hierarchical coupling of geochemical sub-processes, allowing to recur to “full physics” simulations

when surrogate predictions are not accurate enough is advantageous to mitigate the inevitable inaccuracies introduced by the approximated surrogate solutions. In the case of purely data-driven surrogates, which are a completely general approach not limited to geochemistry, regressors operate exclusively on input/output data oblivious to known relationships. Here, redundant information content can be employed effectively to obtain cheap estimation of plausibility of surrogate predictions at runtime, by checking the errors on mass balance. This estimation works well at least for the presented geochemical benchmark. Our tests show consistent advantage of decision-tree based regression algorithms, especially belonging to the gradient boosting family.

Feature engineering based on domain knowledge, i.e., the actual governing equations for the chemical problem as solved by the full physics simulator, can be used to construct a surrogate approach in which the learning task is enormously reduced. The strategy consists in partitioning the parameter space based on the engineered features, and looking for bijective relationships within each region. This approach reduces both the number of distinct required multivariate predictions and the dimension of training dataset upon which each regressor must operate. Algorithmically it can be represented by a decision tree, and proved both accurate and robust, being equipped to handle unseen data and less sensible to sparse training dataset, since it embeds and exploits knowledge about the modelled process. Further research is required in order to generalize it and to automate it ~~for~~ , to deal with more complex chemical problems, as well as ~~for-adapting-to~~ adapt it to specific needs such as sensitivity and uncertainty analysis.

Both approaches constitute non-mutually-exclusive valid strategies in the arsenal of modellers dealing with overwhelmingly CPU-expensive reactive transport simulations, required by present day challenges in subsurface utilisation. In particular, we are persuaded that hybrid AI-physics models will offer the decisive computational advantage needed to overcome current limitations of classical equation-based numerical modelling.

*Code availability.* DecTree v1.0 is a model experiment setup and evaluated in the R environment. All the code used in the present work is available under LGPL v2.1 license at Zenodo with DOI 10.5281/zenodo.4569573 (<https://doi.org/10.5281/zenodo.4569573>)

DecTree depends on the RedModRphree package v0.0.4, equally available at Zenodo with DOI 10.5281/zenodo.4569516 (<https://doi.org/10.5281/zenodo.4569516>).

*Author contributions.* MDL shaped the research, performed analyses, programming and wrote the manuscript. MK helped providing funding, shaping the research, and revised the manuscript.

*Competing interests.* The authors have no conflict of interests.

625 *Acknowledgements.* The authors gratefully acknowledge the Helmholtz Association of German Research Centers - Initiative and Networking Fund for the funding in the framework of the project “*Reduced Complexity Models* – Explore advanced data science techniques to create models of reduced complexity” - reference number ZT-I-0010.

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