Towards an improved treatment of cloud-radiation interaction in weather and climate models: exploring the potential of the Tripleclouds method for various cloud types using libRadtran 2.0.4

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Abstract. Although the representation of unresolved clouds in radiation schemes of coarse-resolution weather and climate models has progressed noticeably over the past years, a lot of room remains for improvement, as the current picture is by no means complete. The main objective of the present study is to advance the cloud-radiation interaction parameterization, focusing on the issues related to model misrepresentation of cloud horizontal inhomogeneity. This subject is addressed with the state-of-the-art Tripleclouds radiative solver, the fundamental feature of which is the inclusion of the optically thicker and thinner cloud fraction, where the thicker is associated with the presence of convective updraft elements. The research challenge is to optimally set the pair of cloud condensates characterizing the two cloudy regions and the corresponding geometrical split of layer cloudiness. A diverse cloud field data set was collected for the analysis, comprising case studies of stratocumulus, cirrus and cumulonimbus. The primary goal is to assess the validity of global cloud variability estimate along with various condensate distribution assumptions. More sophisticated parameterizations are subsequently explored, optimizing the treatment of overcast as well as extremely heterogeneous cloudiness. The radiative diagnostics including atmospheric heating rate and net surface flux are consistently studied using the Tripleclouds method, evaluated against a three-dimensional radiation computation. The performance of Tripleclouds mostly significantly surpasses the conventional calculation on horizontally homogeneous cloudiness. The effect of horizontal photon transport is further quantified. The overall conclusions are intrinsically different for each particular cloud type, encouraging endeavors to enhance the use of cloud regime dependent methodologies in next-generation atmospheric models. This study highlighting the Tripleclouds potential for three essential cloud types signifies the need for more research examining a broader spectrum of cloud morphologies.

1 Introduction

1.1 General background

The fundamental role of clouds and their interaction with radiation in weather and climate can hardly be overemphasized (e.g., Boucher et al., 2013; Stevens and Bony, 2013; Bony et al., 2015). Clouds are complex phenomena, since they exhibit an immense variety of shapes and sizes (Randall et al., 2003) and highly variable degrees of inhomogeneity (Shonk et al., 2010; Hill et al., 2012, 2015; Boutle et al., 2014). When interacting with solar and thermal radiation, the most common effects are
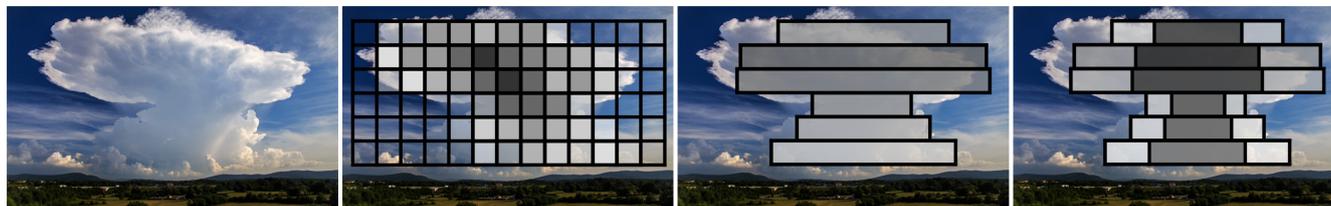
Figure 1. First panel: an explosive storm near Divača, Slovenia (Marko Korošec Weather Photography). Second panel: a representation of such storm in a cloud-resolving model (lighter/darker grey shading denotes smaller/larger optical thickness). Third panel: a traditional storm representation in coarse-resolution weather and climate models. Fourth panel: the state-of-the-art Tripleclouds methodology.

radiatively induced cooling at cloud top and warming at cloud base, which promotes convective instabilities within the cloud

25 (Webster and Stephens, 1980). This radiative destabilization of the cloud layer is impelled primarily by thermal radiation, whereas during daytime solar radiation generally has a stabilizing tendency, albeit the latter strongly depends on solar zenith angle (Črnivec and Mayer, 2019). In the boundary layer, the atmosphere and thereby clouds are directly affected by the Earth's surface, via the transition of heat, moisture and momentum (Baur et al., 2018). The net (difference between downward and upward) surface radiative flux is a crucial component of surface energy budget (Manabe, 1969). Although solar surface flux

30 is customarily markedly larger than its thermal counterpart and thus mostly dominates during daytime (Črnivec and Mayer, 2019), the latter is important at nighttime when solar forcing is absent. All in all, radiatively induced temperature changes in clouds and at the surface are firmly linked to a broad range of atmospheric moist thermodynamic, turbulent and microphysical processes, e.g. formation of precipitation (Harrington et al., 2000; Klinger et al., 2019). A skillful representation of these processes in numerical models as well as of their mutual interplay still poses many grand challenges to atmospheric scientists

35 across the world (Schneider et al., 2017).

The present study aspires to make progress on the treatment of unresolved cloud-radiation interaction in coarse-resolution weather and climate models, often referred to as the general circulation models (GCMs). Despite significant advances in the last few decades, the radiation schemes of GCMs still only crudely represent the interchange between clouds and radiation, being impaired by the poor representation of model cloudiness itself in the first place (Randall et al., 2003). A handy way to tackle

40 these shortcomings is by means of explicit cloud modeling. Over the past decades, large-eddy simulation (LES) and cloud-resolving models (CRMs) (e.g., Klemp and Wilhelmson, 1978; Tao and Simpson, 1993; Khairoutdinov and Randall, 2003; Stevens et al., 2005) have established themselves as a well-acknowledged tool in cloud physics research (Guichard and Couvreaux, 2017). The idea of the so-called superparameterization (Grabowski, 2001, 2003), where a two-dimensional (2-D) CRM is embedded in individual column of a host GCM, has recently been revisited by applying fully three-dimensional (3-D) LES

45 model as a superparameterization, albeit on massively parallel computers (Grabowski, 2016). Short-term global predictions using direct LES/CRM simulations extending up to a few months or even years are beginning to be feasible (Bretherton and Khairoutdinov , 2015). Long-term climate projections utilizing coupled atmosphere-ocean systems in a direct high-resolution mode, however, will not be possible for a next couple of decades even on most powerful supercomputers (Schneider et al.,

2017). Similarly, despite remarkable advancements in numerical weather prediction (NWP), which is burdened by the users'
50   demand for real-time forecasts, global NWP at a subkilometer scale will stay challenging in the near future (Bauer et al., 2015).

Bearing the above-mentioned limitations in mind, the joint scientific effort to improve traditional physical parameterization
schemes, which lie at heart of every weather and climate model, remains intact. To that end, LES and CRM models provide
valuable high-resolution 3-D cloud field data, on which cloud-radiation interplay can be studied either offline (e.g., Jakub
and Mayer, 2015; Klinger and Mayer, 2014, 2016; Černivec and Mayer, 2019, 2020) or interactively (e.g., Jakub and Mayer,
55   2016, 2017; Klinger et al., 2017; Hartmann et al., 2018). In addition, stochastic cloud models (STMs), capable of quickly
generating realistic 3-D cloud structures, were developed by cloud modeling communities worldwide (e.g., model introduced
by Di Giuseppe and Tompkins, 2003a for stratocumulus; Evans and Wiscombe, 2004 for cumulus; Hogan and Kew, 2005
for cirrus). Whereas the disadvantage of stochastic models compared to LES or CRMs might be that interactive studies of
cloud-radiative feedbacks are not possible, our present work is restricted to offline radiative transfer experiments, based on
60   high-resolution cloud field data stemming from diverse LES, CRM and STM models.

A number of studies took advantage of this approach in the past. They often compared offline radiative transfer experiments
performed on a pregenerated well-resolved cloud field (Fig. 1, second panel) including the exact 3-D radiation calculation (such
as SHDOM, Evans, 1998; Monte Carlo technique, Mayer, 2009), the Independent Column Approximation (ICA, Stephens et
al., 1991) and the one-dimensional GCM-type radiation calculation. The latter was carried out on the derived horizontally
65   homogeneous cloud representation, where fractional cloudiness was assumed to overlap vertically in accordance with the
maximum-random rule (Geleyn and Hollingsworth, 1979) − a configuration which persisted in the majority of GCMs for
many decades (Fig. 1, third panel). The disparity between the latter conventional GCM calculation and the 3-D benchmark was
used to assess the overall bias of GCM radiative quantities. The comparison between the ICA and 3-D experiment served to
quantify the portion of the overall bias stemming from neglected horizontal photon transport, whereas the comparison between
70   the conventional GCM configuration and the ICA measured the bias associated with neglected subgrid cloud variability.

In this way the radiative transfer was extensively studied for cumulus (Davies, 1978; Kobayashi, 1988; Welch and Wielicki,
1989), stratocumulus (Cahalan et al., 1994a, b; Cahalan et al., 1995; Zuidema and Evans, 1998; Di Giuseppe and Tompkins,
2003a), cirrus (Fu et al., 2000a; Carlin et al., 2002; Hogan and Kew, 2005; Zhong et al., 2008; Fauchez et al., 2014) as well
as deep convective and anvil clouds (Barker et al., 1999; Fu et al., 2000b; Di Giuseppe and Tompkins, 2003b, 2005; Tompkins
75   and Di Giuseppe, 2003), although some of the earliest work used either very idealized cuboid, single-layered or 2-D clouds.
Moreover, some of these studies assessed solely either the ICA or the subgrid cloud variability bias and therefore did not shed
any light on their relative contribution. Nevertheless, it was commonly found that classic 3-D radiative effects associated with
horizontal photon flow manifest most pronouncedly in areas of notable horizontal gradients of optical properties and are thus
regularly related to cloud side boundaries. But also the in-cloud horizontal variations of optical depth were found to impact
80   3-D radiative transfer and especially the GCM-type approximation. Due to aforementioned reasons, conflicting claims can be
found in the literature regarding the magnitude and sign of these biases. Better understanding of these effects is required to
advance the parameterization of cloud-radiation interaction.

1.2 Focus of this study

The present study aims to reinforce earlier studies by establishing 3-D benchmarks and further exploring the validity of ICA for
85 various cloud types. In particular, we intend to assess the ICA suitability when the GCM resolution refines to the meso-scale
$\mathcal{O}$(10-100 km). Di Giuseppe and Tompkins (2003b), as an illustration, showed that 3-D radiative effects increase as the GCM
resolution approaches the meso-scale. In addition, we strive to investigate more realistic cloud morphologies, as we applied
finer horizontal grid spacing in cloud-generating models compared to the previous research (e.g., Di Giuseppe and Tompkins,
2003b; Hogan and Kew, 2005; Zhong et al., 2008). Furthermore, we aim to consistently analyze atmospheric heating rate and
90 net surface flux, which has received considerably less attention in the previous debates.

The novelty and therefore the prime focus of the current work, however, is the utilization of the state-of-the-art Tripleclouds
(TC) radiative solver for use in coarse-resolution models. The TC method was primarily suggested by Shonk and Hogan (2008)
(henceforth abbreviated to SH08) and operates with two regions in each vertical model layer to represent the cloud: one region
represents the optically thicker part of layer cloudiness, while the other region represents the remaining optically thinner part.
95 The added value of the Tripleclouds scheme compared to its conventional GCM predecessor is thus the capability of accounting
for horizontal cloud heterogeneity in the simplest possible and therefore computationally efficient manner. Following the idea
of SH08, a second cloudy region has recently been incorporated into the broadly used δ-Eddington two-stream method with
maximum-random overlap assumption for partial cloudiness by Črnivec and Mayer (2020). The insertion of a second cloudy
region in the two-stream framework requires an upgrade of vertical overlap rules. This task was accomplished exploiting the
100 core-shell model for convective clouds (Heus and Jonker, 2008; Heiblum et al., 2019), where the convective core characterized
by updraft and condensate loading is positioned in the geometrical centre of the cloud, enclosed by the shell related to down-
drafts and condensate evaporation. In the terminology of radiative transfer, the maximum-random overlap was thus retained
for the entire fractional cloudiness and additionally applied for the optically thicker segment. This extended vertical overlap
formulation implicitly places the optically thicker cloudy region towards the cloud interior in the horizontal plane, whereas the
105 other optically thinner region covers the cloud periphery, as depicted in Fig. 1 (fourth panel).

The primary purpose of the study by Črnivec and Mayer (2020) was to present our implementation of the TC scheme in the
libRadtran radiation package (Emde et al., 2016). Furthermore, the method was at first evaluated on a broken shallow cumulus
cloud field, where it proved to be a significant improvement compared to the conventional GCM approach. Herein, we extend
the work of Črnivec and Mayer (2020) by examining additional case studies of stratocumulus, cirrus and cumulonimbus, since
110 cloud horizontal heterogeneity strongly depends on cloud type (Pincus et al., 1999; Oreopoulos and Cahalan, 2005; Shonk et
al., 2010; Shonk and Hogan, 2010; Hill et al., 2012, 2015; Boutle et al., 2014). These case studies were deliberately chosen in
a way, that cloud vertical arrangement tends towards the assumed maximally-overlapped scenario, thus focusing on radiative
effects associated with cloud horizontal inhomogeneity and eliminating the error arising from the misrepresentation of assumed
vertical overlap as would be expected to occur in conditions with strong vertical wind shear (Naud et al., 2008; Di Giuseppe
115 and Tompkins, 2015).

Once two-stream radiative fluxes had been successfully imposed onto a system of three-region atmospheric layers in accordance with vertical overlap rules, the research challenge is to optimally set the pair of liquid/ice water content (LWC/IWC) characterizing the two cloudy regions and the corresponding geometrical split of layer cloudiness. The answer to the posed scientific question is critically dependent on the characteristic of the underlying subgrid cloud horizontal variability. The latter
120 is conveniently defined by the fractional standard deviation (FSD) of cloud condensate as well as the shape of its distribution. Since this information is generally not available in GCMs, Shonk et al. (2010) estimated a global FSD based upon diverse cloud observational studies. The prime objective of the present study is to assess the validity of the global FSD estimate in the TC radiative solver for three inherently contrasting cloud types in conjunction with various assumptions for condensate distribution, which are commonly applied in cloud modeling (Gaussian, gamma, lognormal). Along the above lines, a further
125 goal of the study is to inspect the actual LWC/IWC distribution based on high-resolution LES/CRM data, as this is the keystone for a well-designed self-consistent TC parameterization. The majority of previous studies examining cloud condensate distribution, namely, adopted cloud data simulated on smaller domains with coarser grid spacing. The final aim of the study is to explore more sophisticated FSD parameterizations, characterizing systematic departures from the global mean. These refined TC configurations refer to distinctive improvements desired in the case of overcast as well as extremely heterogeneous
130 cloudiness. Together with the parent study of Črnivec and Mayer (2020), this work presents the first usage of Tripleclouds to consistently study the cloud-layer heating rate and net surface flux.

The remainder of this paper is structured as follows: the cloud field data and methodology are presented in Sect. 2. The results of the baseline radiation experiments are discussed in Sect. 3. Building upon this discussion, optimized TC realizations are proposed in Sect. 4. Section 5 concludes with a brief summary and outlook.

2 Data and methodology

2.1 Cloud field data

Input data for radiative transfer experiments is a set of 3-D highly-resolved inhomogeneous cloud fields, defined in terms of LWC and IWC distributions. Diverse models employed to generate these cloud fields, together with different resolutions, result in inherently distinctive cloud structures and hence ensure that the three selected cases comprise a wide range of inhomogeneity.
140 In the following, each cloud type is characterized briefly.

2.1.1 Stratocumulus

The stratocumulus cloud was simulated with the University of California, Los Angeles large-eddy simulation (UCLA-LES) model (Stevens et al., 2005). The simulation relates to the Atlantic Stratocumulus Transition Experiment (ASTEX; Albrecht et al., 1995), conducted over the northeast Atlantic Ocean in June 1992. The case study thereby exemplifies a marine boundary
145 layer stratocumulus, exhibiting sporadic convective cells embedded in the stratus layer (Agee et al., 1973; Atkinson and Zhang, 1996; Wood and Hartmann, 2006). Observational studies show, inter alia, that directional and magnitude vertical shear is small
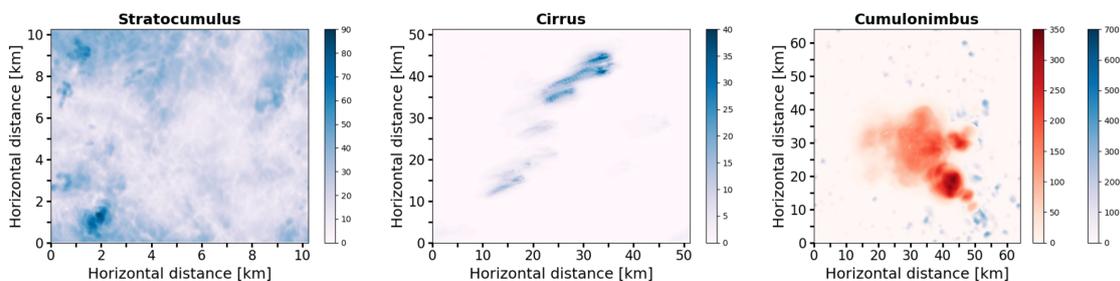
Figure 2. Vertically integrated visible optical thickness of selected cloud field case studies. Note that in case of cumulonimbus, the blue/red shading denotes optical thickness of liquid/ice water content.
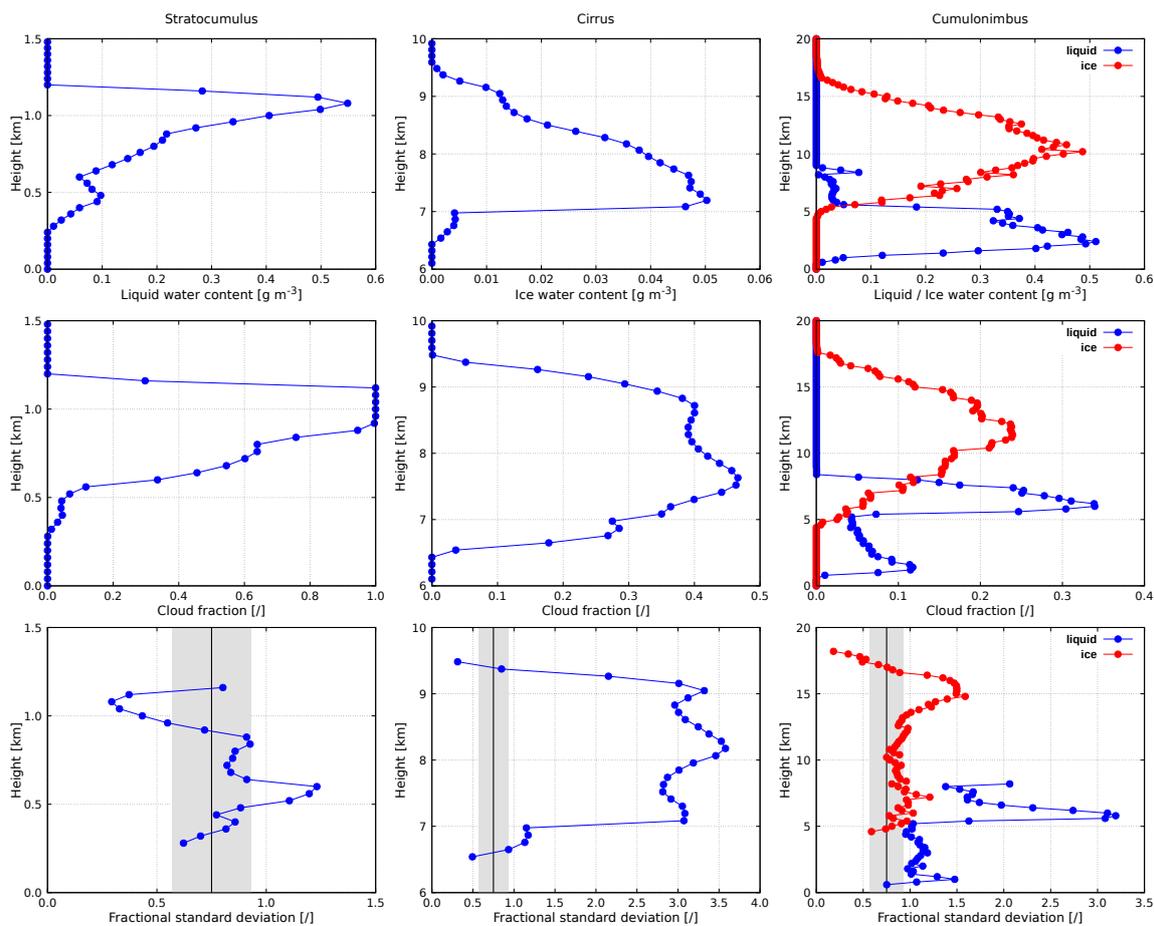
Figure 3. Characterization of selected cloud field case studies in terms of averaged LWC/IWC (top row), cloud fraction (middle row) and fractional standard deviation of LWC/IWC (bottom row), whereby the vertical black line shows the mean global FSD estimate and the grey shaded area denotes its uncertainty.

in mesoscale cellular convection (Agee et al., 1973). The horizontal domain size is 10.24 x 10.24 km^2, with the vertical extent of the domain being 4 km. A constant model grid spacing of 40 m is applied in all three (x-, y-, z-) directions. Figure 2 (left) visualizes the cloud field in terms of vertically integrated optical thickness. Vertical profiles of averaged LWC, cloud fraction

150 (defined by LWC $> 10^{-3}$ g m^{-3}) and FSD are shown on Fig. 3 (left). The overcast stratocumulus scene is topped slightly above 1 km height. The FSD, although roughly centered around the global estimate, strongly depends on the position within the cloud layer: it exhibits a maximum (1.2) in the lowest portion of the cloud layer and a minimum (0.3) in its uppermost radiatively important region.

To gain further insight about the subgrid cloud variability, the theoretical distributions (Gaussian, gamma, lognormal) were
155 fitted to the actual LWC distribution in each vertical layer. The goodness of fit was assessed with the Kolmogorov-Smirnov test. The investigation revealed that the actual LWC distribution throughout the vast majority of the upper portion of the cloud, where radiative effect is maximal, is best approximated with lognormal distribution (best fit in 5/8 of top layers).

2.1.2 Cirrus

The cirrus cloud was generated with the stochastic cloud model Cloudgen of Hogan and Kew (2005), described also in Zhong
160 et al. (2008). The speciality of this 3-D cirrus fractal model is its capability to generate structural features unique to cirrus clouds: realistic fallstreak geometry and shear-induced mixing. The model input parameters are based on the statistics derived from radar observations in southern England (Hogan et al., 2003; Hogan and Illingworth, 2003). We chose the cirrus uncinus case study of June, 24th, 1999, which is the first of the three cases discussed by Hogan and Kew (2005) and subsequently also by Zhong et al. (2008) [1] [2], and was adopted herein as it is the case with smallest vertical wind shear. The horizontal domain size
165 is 51.2 x 51.2 km^2 with a grid spacing of 100 m. The vertical extent of the domain is 7 km using constant vertical grid spacing of 109 m. Figure 2 (middle) visualizes the cloud field in terms of vertically integrated optical thickness. Vertical profiles of averaged IWC, cloud fraction (defined by IWC $> 10^{-3}$ g m^{-3}) and FSD are shown on Fig. 3 (middle). The degree of cloud horizontal heterogeneity is largest in the central part of the cloud layer, with FSD exceeding 3.5. The cirrus layer is thus by far not uniform, rather it exhibits cellular structures ("generating cells"), which would in reality be associated with convective
170 motions. The latter produce higher supersaturations (Heymsfield, 1977) and increase cirrus ice crystal residence time (Mitchell, 1994), which leads to an increased IWC within the cells. The layer IWC of the present cirrus is lognormally distributed, as this is the intrinsic Cloudgen property.

2.1.3 Cumulonimbus

The cumulonimbus cloud was simulated with the Goddard Cumulus Ensemble cloud resolving model (GCE-CRM), described
175 in detail by Tao and Simpson (1993) and more recently by Tao et al. (2003). The simulation relates to the convective event observed on 23 February 1999 during the Tropical Rainfall Measuring Mission (Simpson et al., 1988, 1996) Large-Scale

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[1]The studies of Hogan and Kew (2005) and Zhong et al. (2008) used coarser horizontal grid resolution (1.56 km).

[2]Hogan and Kew (2005) showed that for this particular cirrus case study the maximum-random overlap assumption performs reasonably well in both the solar and thermal spectral range.

Biosphere-Atmosphere (TRMM-LBA) experiment in Amazonia. The horizontal domain size is 64.0 x 64.0 km^2, with the vertical extent of the domain being 23 km, which is sufficient to allow the growth of tropical cirrus anvil. The grid spacing of 250 m is applied in each horizontal direction and 200 m in the vertical direction. The simulation is described by Lang et al.
180   (2007) and briefly by Zinner et al. (2008). Due to light environmental winds (Fig. 2b of Lang et al., 2007), the convection was rather weakly organized.[3] Figure 2 (right) visualizes the cloud field in terms of vertically integrated optical thickness. Vertical profiles of averaged LWC and IWC, the corresponding cloud fraction as well as FSD are shown on Fig. 3 (right). The case study is characterized by three distinct cloud layers: a liquid phase region extending from 0.8 km to 4.4 km consisting of shallow cumuli, a mixed-phase stratiform region located between 4.4 km and 8.2 km, and an ice phase region extending from 8.2 km to
185   17.4 km height, encompassing the cumulonimbus deep convective core and the anvil. Remarkably, the stratiform layer is highly heterogeneous, with the maximum FSD of the liquid phase exceeding 3.2. The maximum FSD in the bottommost cumuliform region as well as in the uppermost anvil region reaches approximately half of this value.

The comparison of theoretical distributions with actual LWC/IWC distributions reveals the following findings: the assumption of gaussianity is void for the present cumulonimbus scenario and in each vertical layer either gamma or lognormal dis-
190   tribution was classified as the best fit. Thus, throughout the majority of the liquid region the actual LWC distribution is best approximated with the gamma distribution (best fit in 58 % of layers). In the mixed-phase region the LWC distribution is best approximated with the lognormal distribution (best fit in 85 % of layers), whereas the IWC distribution is best approximated with the gamma distribution (best fit in 85 % of layers). In the ice region the IWC distribution is best approximated with the gamma distribution within the bottommost 30 % and uppermost 13 % of the region (best fit in all cases), while within the
195   remaining central part the lognormal distribution appears to be the optimal approximation (best fit in 58 % of layers).

2.2   Configuring baseline Tripleclouds experiments

To utilize the TC radiative solver, a pair of LWC/IWC defining the two cloudy regions has to be generated in each vertical layer. We refer solely to the liquid phase in the remainder of this section, since analogous considerations apply to the ice phase. Thus, the LWC values characterizing the optically thin and thick cloudy region are referred to as the LWC^{cn} (Cloud
200   thiN) and LWC^{ck} (Cloud thicK). Based on the analysis of high-resolution cloud radar data, SH08 showed that TC performs well for top-of-the-atmosphere (TOA) radiative fluxes when the LWC^{cn} is chosen to be the value corresponding to the 16th percentile of the observed LWC distribution, whereas the LWC^{ck} is determined under conservation constraints of layer-mean LWC (denoted as $\overline{LWC}$):

$$\overline{LWC} = \frac{LWC^{cn} + LWC^{ck}}{2}. \tag{1}$$

205   This method is referred to as the "lower percentile (LP) method" and utilizes a "split percentile (SP)" of 50, implying that cloudiness in each vertical layer is divided through a median of distribution into two equal parts.

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[3]The fact that the deep convective cloud is practically not sheared, makes it a perfect target to study the performance of our current Tripleclouds implementation, which is not yet capable of representing an arbitrary vertical overlap.

When the TC solver resides in a host GCM model, however, the details about the underlying LWC variability are not known, therefore several assumptions have to be introduced. To obtain the pair (LWC^{cn}, LWC^{ck}) from $\overline{LWC}$, which is indeed available in a GCM, we introduce the so-called $\overline{LWC}$-scaling factors for the optically thin and thick cloudy region, termed s^{cn} and s^{ck}
210 respectively, fulfilling the following relationships:

$$LWC^{cn} = \overline{LWC}s^{cn}, \tag{2}$$

$$LWC^{ck} = \overline{LWC}s^{ck}. \tag{3}$$

Different parameters to define the degree of cloud horizontal inhomogeneity are employed in the existing literature and numeri-
215 cal models (e.g., Cahalan et al., 1994a; Smith and Del Genio, 2001; Carlin et al., 2002; Rossow et al., 2002; Oreopoulos and Cahalan, 2005). A frequently used parameter is the previously mentioned fractional standard deviation (FSD) of LWC, which is simply the standard deviation (σ_{LWC}) divided by the mean ($\overline{LWC}$). The FSD is a convenient measure, since it accounts for a strong correlation between $\overline{LWC}$ and σ_{LWC} (Smith and Del Genio, 2001; Carlin et al., 2002; Hill et al., 2012). Based on a comprehensive review of numerous observational studies encompassing diverse cloud data sets, Shonk et al. (2010) converted
220 various variability measures into a single globally applicable FSD parameter, whose mean value and uncertainty are:

$$FSD = 0.75 \pm 0.18. \tag{4}$$

When TC is employed in a host GCM, moreover, an assumption about the shape of LWC distribution has to be made. To this end, we test three assumptions for subgrid cloud condensate distribution: Gaussian distribution, which traditionally prevailed in many models due to its simplicity, as well as more realistic gamma (supported by Barker et al., 1996; Pincus et al., 1999;
225 Carlin et al., 2002; Rossow et al., 2002) and lognormal distribution (supported by Pincus et al., 1999; Hogan and Illingworth, 2003). For a Gaussian distribution, the 16th percentile (suggested by SH08) is given by:

$$s^{cn} = 1 - FSD, \tag{5}$$

although caution needs to be taken as this expression becomes unphysical for FSD > 1. Similarly, according to Hogan et al. (2019), for a gamma distribution the 16th percentile is approximated by:

230 $$s^{cn} = \exp\left[-FSD - \frac{FSD^2}{2} - \frac{FSD^3}{4}\right]. \tag{6}$$

Finally, according to Hogan et al. (2016), for a lognormal distribution:

$$s^{cn} = \frac{1}{\sqrt{FSD^2+1}} \exp\left[-\sqrt{\ln(FSD^2+1)}\right]. \tag{7}$$

For any FSD value, the s^{cn} defined with Eq. (6) or (7) lies in the range between 0 and 1. The desired conservation of $\overline{LWC}$ implies $s^{ck} = 2 - s^{cn}$, where the layer cloudiness is geometrically halved. The approach outlined above, utilizing any of the
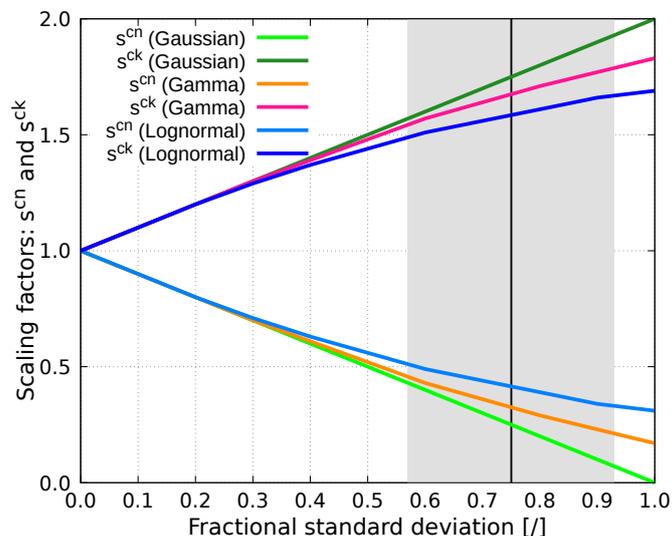
Figure 4. Scaling factors (s^{cn}, s^{ck}) of $\overline{LWC}$ for Gaussian, gamma and lognormal distributions. The black line and the grey area represent mean global FSD and its uncertainty.

selected distributional assumptions to generate the LWC pair, is referred to as the "FSD method" in the remainder of this paper. The resulting $\overline{LWC}$-scaling factors for Gaussian, gamma and lognormal distributions as a function of FSD are shown in Fig. 4. It is apparent that in the region of the global FSD estimate, the pair (LWC^{cn}, LWC^{ck}) exhibits large sensitivity to the assumed form of LWC distribution. This signifies the meaningfulness to pose a question, whether different condensate distribution assumptions significantly affect radiative quantities when global FSD is applied as a proxy for cloud internal variability.

2.3 Setup of radiative transfer calculations

The radiative transfer simulations were carried out with the *libRadtran* software. For consistency, the calculation setup is the same as in Črnivec and Mayer (2020). Here we summarize basic parameter settings and provide additional information regarding the treatment of the ice phase, which was absent in our preceding study. Thus, except for 3-D fields of LWC and IWC as well as the assigned effective radii (parameterized following Bugliaro et al., 2011), all atmospheric conditions are assumed to be horizontally homogeneous and correspond to the US standard atmosphere (Anderson et al., 1986). The domain extends vertically up to a height of 120 km, which is considered to be the TOA. In the lowest portion of the domain where clouds are located we preserved the original high-resolution vertical grid as inherited from the parent cloud model and interpolated the background standard atmospheric conditions onto this grid. It should be reminded that solely LWC and IWC were used as input for radiation calculations to define the cloud fields, while other hydrometeor categories (i.e., precipitation-sized particles, such as rain, snow and graupel) were excluded from the analysis. Optical properties of water droplets (assumed to be spherical) were prescribed following the parameterization of Hu and Stamnes (1993). Optical properties of ice crystals were specified based on the parameterization of Yang et al. (2000), assuming habit of hexagonal columns. Solar zenith angle (SZA) was varied

Table 1. List of radiative transfer experiments.

Experiment description	Abbreviation
Benchmark 3-D Monte Carlo model	3-D
ICA Monte Carlo model	ICA
Conventional GCM radiation scheme	GCM
Tripleclouds solver with LP method	TC(LP)
Tripleclouds solver with FSD method	TC(FSD)

between 0° (overhead Sun), 30° and 60°, whereby downward flux at TOA corresponds to 1365, 1182 and 683 W m^{-2}. At the
surface, the temperature of 288.2 K implies upward flux of 389.5 W m^{-2} according to the Stefan-Boltzmann law. The surface
255   was assumed to have a constant albedo of 0.25 in the solar spectral range, whereas in the thermal spectral range it was assumed
to be black (albedo=0).

Table 1 summarizes the baseline experiments carried out in this study. The benchmark experiment was performed using
the 3-D Monte Carlo radiative model MYSTIC (Mayer, 2009). The horizontal extent of the domain matched that of each
individual cloud field case study. Periodic boundary conditions were applied in the 3-D configuration. In addition, the Monte
260   Carlo experiment in ICA mode was carried out, which is the same as the 3-D experiment, except that periodic boundary
conditions are imposed at each grid column. The 3-D and ICA experiment were both performed on the high-resolution cloud
grid, with the result subsequently horizontally averaged across the domain. The difference between the ICA and 3-D was
used to assess the impact of horizontal photon transport on domain-averaged (GCM-scale) radiative quantities. Whereas the
exact number of traced photons depends on the particular cloud case, it was held sufficiently high, so that the Monte Carlo
265   noise of domain-averaged quantities was kept below 0.1 %. Moreover, we performed a conventional GCM-type calculation
on a layer-averaged fractional cloud. The δ-Eddington two-stream method with maximum-random overlap assumption for
partial cloudiness was recently implemented into *libRadtran* (Črnivec and Mayer, 2019) and was used herein in place of the
conventional GCM scheme. The Tripleclouds solver was employed in conjunction with both the LP and FSD method. In order
to verify (or discard) the validity of the global FSD estimate for heating rates and surface fluxes, we applied its mean value
270   (0.75) in the initial TC experiments together with all three distributional assumptions as outlined in Sect. 2.2.

For each experiment we diagnosed atmospheric heating rate and net surface flux in the solar and thermal part of the spectrum,
as well as their total (integrated) effect. The error is measured by the absolute bias (Eq. 8), relative bias (Eq. 9) and for the
heating rate profile additionally by the cloud-layer RMSE (Eq. 10):

$$\text{absolute bias} = y - x, \tag{8}$$

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$$\text{relative bias} = \left(\frac{y}{x} - 1 \right) \cdot 100\%, \qquad (9)$$

$$\text{cloud-layer RMSE} = \sqrt{\overline{(y-x)^2}}, \qquad (10)$$

where x represents the 3-D benchmark and y represents the biased quantity (outcome of the ICA, GCM or any TC experiment).
280   The cloud-layer RMSE denotes the RMSE evaluated throughout the vertical extent of the cloud layer of each particular cloud field case study.

3   Results and discussion

We present in Sect. 3.1 the atmospheric heating rate for each cloud type, whereas in Sect. 3.2 we discuss the net surface flux in the baseline experiments listed in Table 1.

285   ### 3.1   Atmospheric heating rate

3.1.1   Stratocumulus

Figure 5 (top row) shows the radiative heating rate in the benchmark 3-D experiment for the stratocumulus cloud. There is large absorption of solar radiation in the cloud layer, resulting in the maximum heating rate of about 53, 47 and 27 K day^{-1} at SZA of 0°, 30° and 60°, respectively. The peak heating rates are concentrated in the uppermost part of the cloud layer, since both
290   cloud fraction and LWC increase from cloud base towards cloud top. In the thermal spectral range the cloud layer is subjected to strong cooling, reaching a peak of almost -140 K day^{-1} at the same height where maximum solar heating is attained. These large heating and cooling rates are partially a manifestation of high vertical resolution (Di Giuseppe and Tompkins, 2003a). The total heating rate, a physically relevant quantity during daytime, is dominated by thermal cooling. Thus persistent cloud-top radiative cooling, a typical feature of marine stratocumulus-topped boundary layers (STBLs; Wood, 2012), drives convective
295   instability and controls turbulence within the underlying mixed layer (Randall, 1980; Deardorff, 1981; Stevens et al., 1999), when adequately coupled to a dynamical model. The radiative biases could therefore importantly affect the evolution of the stratocumulus layer itself.

The examination of radiative biases (Fig. 5, bottom row) reveals that these are maximized in the uppermost part of the stratocumulus layer as well. The disparity between the ICA and 3-D is minor: a maximum difference of -0.2 K day^{-1} is
300   observed in the solar spectral range for SZA of 60° (cloud side illumination effect; Jakub and Mayer, 2015, 2016). In the thermal spectral range, the ICA underestimates the amount of 3-D cooling by about 2.5 K day^{-1} in the uppermost grid point of the cloud layer (cloud side cooling effect; Klinger and Mayer, 2014, 2016). These comparatively small ICA biases are attributed to the minor cloud top topography (difference between the nearby local height maximum and minimum; Zuidema
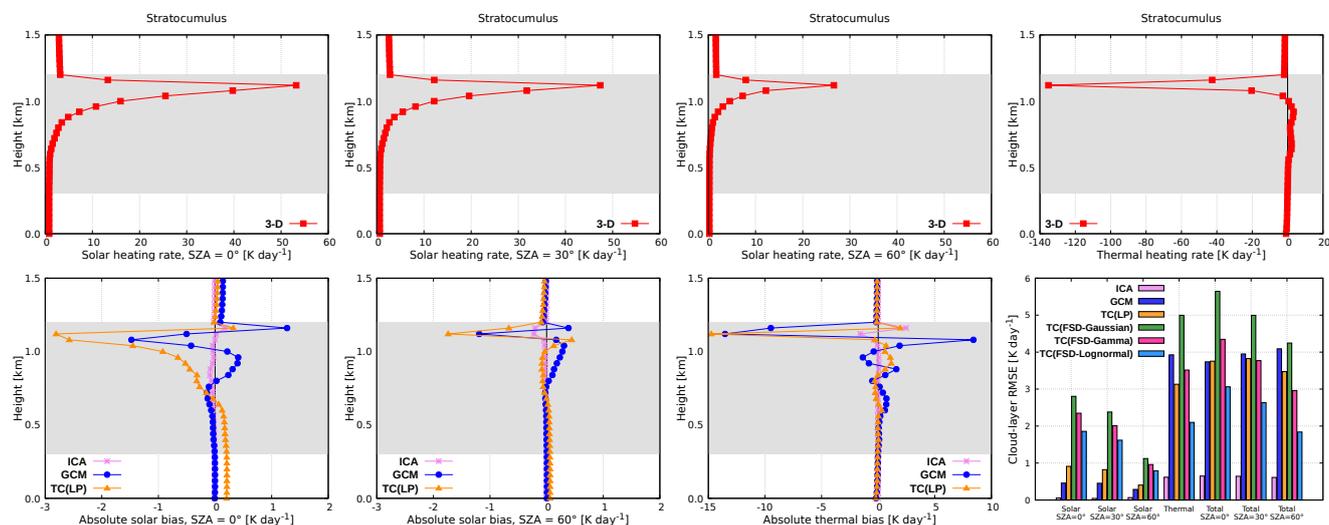
Figure 5. Radiative heating rate for the stratocumulus cloud. The grey-shaded area denotes the cloud layer.

and Evans, 1998) of the present stratocumulus. The radiative transfer, namely, acts to smooth out structures at spatial scales
305 smaller than the photon mean free path, with the latter corresponding to several hundred meters in STBLs (Marshak et al.,
1995).

The GCM bias exhibits a pronounced vertical gradient within the cloud layer: in the uppermost part of the cloud layer the
GCM solar heating rate is too high, while in the region underneath it is too low (at all SZAs). In the thermal spectral range
the opposite is the case, but the bias is quantitatively larger and dominates the daytime bias. Thus the GCM boosts radiatively
310 driven destabilization of the stratocumulus layer during daytime and nighttime, by overestimating cooling at the uppermost
region of the layer (bias of -14 K day^{-1}) and overestimating warming in the region underneath (bias up to 9 K day^{-1}).

In the Triplecloud experiments the solar bias is increased compared to that of the GCM. This is most notable when using
the FSD method, since the global FSD introduces excessive heterogeneity in the radiatively important upper part of the cloud
layer. In the thermal spectral range the TC in most configurations outperforms the conventional GCM. Further, the TC appears
315 to be strongly sensitive to the assumed condensate distribution, highlighting its importance, with the lognormality assumption
performing best. Noteworthy, although the TC with global FSD degrades the solar bias, it is still more accurate than the GCM
during all nighttime and daytime conditions, when LWC lognormality is assumed. In particular, nocturnal cloud-layer RMSE
is reduced from about 3.9 K day^{-1} to only 2.1 K day^{-1}. The largest daytime improvement is observed at SZA of 60°, where
RMSE is reduced from 4.1 K day^{-1} to solely 1.8 K day^{-1}.

320 ### 3.1.2 Cirrus

Figure 6 (top row) shows the radiative heating rate in the benchmark 3-D experiment for the cirrus cloud. The solar absorption
in the ice layer results in a maximum heating rate of about 3.6, 3.3 and 2.2 K day^{-1} at SZA of 0°, 30° and 60°, respectively.
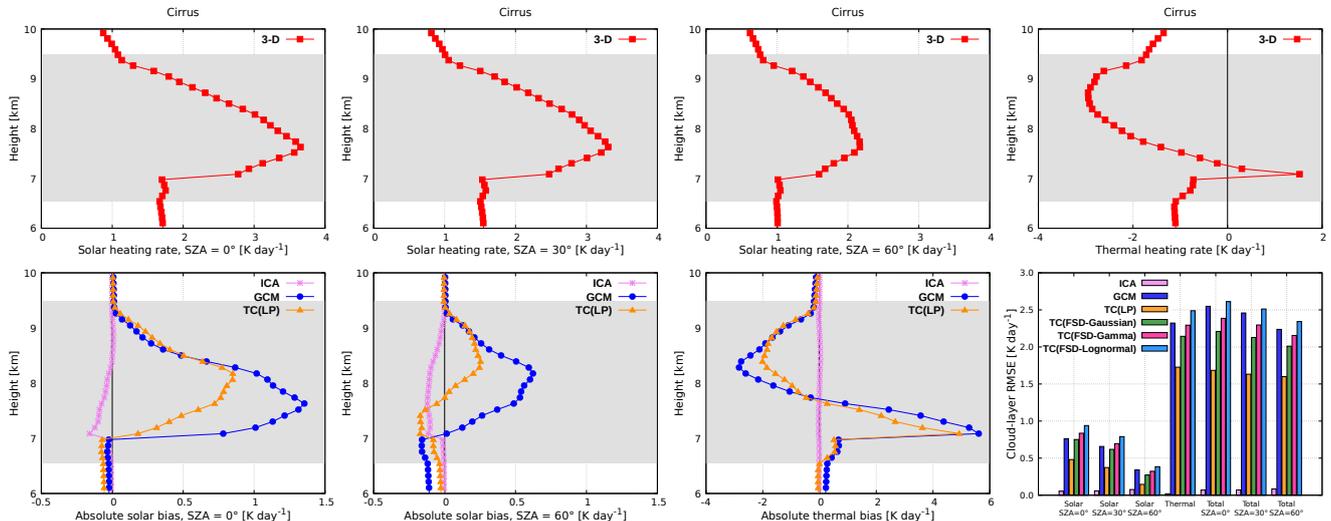
Figure 6. Radiative heating rate for the cirrus cloud. The grey-shaded area denotes the cloud layer.

The height where this maximum heating is reached stays the same for all SZAs and corresponds to the height of maximum cloud fraction (7.6 km). In the thermal spectral range a peak cooling of -2.9 K day^{-1} is attained higher up in the cloud layer

325 (at 8.7 km; effective cloud top; above this height cloud fraction rapidly decreases), followed by a peak warming of 1.5 K day^{-1} located at the height of maximum IWC (7.1 km; effective cloud base; below this height IWC is sharply reduced). In contrast to the stratocumulus, solar heating and thermal cooling observed on the cirrus is more evenly distributed throughout the cloud layer, whereas thermal warming remains confined to a shallow region at cloud base. The daytime heating rate is governed by the stronger thermal effect, although solar heating largely compensates thermal cooling. Compared to the stratocumulus, the

330 heating rate on the cirrus is overall much lower. Nevertheless, it should be kept in mind that the net heating rate in the upper troposphere and lower stratosphere (UTLS) is close to zero (Haigh, 1984), which makes this region highly sensitive to small radiative biases.

The 3-D solar effects (Fig. 6, bottom row) are present at all SZAs and maximized at 60° (cloud side illumination), where the ICA bias of -0.1 K day^{-1} is observed throughout the majority of the cloud layer. In the thermal spectral range the ICA bias

335 is negligible. Similar results were found by Zhong et al. (2008) (recall that the latter investigated the same midlatitude cirrus, although on coarser grid), who also showed that domain-averaged ICA and 3-D heating rates agree within 0.1 K day^{-1} in both the longwave and the shortwave.

In the GCM the solar heating rate is overestimated by up to 1.4, 1.2 and 0.7 K day^{-1} at SZA of 0°, 30° and 60°, respectively. The height where this maximum bias is observed corresponds with the height of maximum benchmark heating. In the thermal

340 spectral range, the GCM bias enhances radiatively driven destabilization of the cirrus layer by an overestimation of top cooling by 2.8 K day^{-1} and a substantial overestimation of base warming (bias exceeding 5.6 K day^{-1}). The thermal GCM bias is in close agreement with that observed by Zhong et al. (2008), whereas the solar GCM bias is by a factor of 2 to 3 smaller. The

latter finding indicates the potential dependence of GCM biases on the initial cloud grid resolution, which could affect the TC experiments as well and has to be more thoroughly examined in the future. The daytime GCM bias profile closely resembles
345 that of its nighttime counterpart, such that the radiatively driven destabilization of the cirrus layer is persistently substantially escalated.

Among the various Tripleclouds experiments, the TC(LP) performs best, reducing the GCM bias in the solar, thermal and total spectral range at all SZAs. Despite that the actual IWC is lognormally distributed, the TC(FSD) performs best with the gaussianity assumption. The latter implies the largest difference between the IWC pair defining the two cloudy regions (Fig. 4),
350 partially accounting for the missing inhomogeneity provided by global FSD. Optimizations for extremely heterogeneous cases will be investigated in the next section.

3.1.3 Cumulonimbus

Figure 7 (top row) shows the radiative heating rate in the benchmark 3-D experiment for the cumulonimbus cloud. There is a strong absorption of solar radiation in the cirrus anvil, reaching a peak value of 4.4, 3.8 and 2.4 K day^{-1} at SZA of 0°, 30°
355 and 60°, respectively. The observed spikes in heating rate are due to the bubbling appearance of the anvil. Underneath the main absorption layer in the upper portion of the anvil, there is a shadowed region with reduced heating rate. A second, although much smaller maximum (partially due to the aforementioned shielding effect of the anvil) of solar heating rate is observed in the mixed-phase stratiform region, followed by a third local maximum in the liquid phase region. In the thermal spectral range, there is a peak cooling of -3.9 K day^{-1} in the upper part of the anvil and a peak warming of 0.7 K day^{-1} at its bottom,
360 driving convective destabilization within the ice layer. Similarly, a peak cooling of -1.8 K day^{-1} is observed at the top of the stratiform layer, followed by a region of locally increased heating rate at its bottom. In the liquid region the thermal profile exhibits many spikes, indicating different cloud top heights of small cumuli where cooling is maximized, followed by a region of locally increased heating rate at the uniform cumulus base height. The daytime heating rate profile is shaped by the stronger thermal radiative effect, although solar heating partially compensates thermal cooling. This solar stabilizing tendency is largest
365 within the anvil and generally decreases with descending Sun. All in all, the three distinct maxima observed throughout the vertical extent of the present deep convective scenario are in accordance with the trimodal structure of tropical clouds (Johnson et al., 1999; Haynes and Stephens, 2007; Su et al., 2008; Fu et al., 2018).

We find that 3-D solar radiative transfer has a nonnegligible effect at all SZAs (Fig. 7, bottom row). In particular, heating rate differences between ICA and 3-D of about -0.5 K day^{-1} (up to -30 %) are observed at SZA of 60° and extend throughout
370 the majority of the ice region. These differences exceed those reported by Di Giuseppe and Tompkins (2003b), which in turn surpass those previously documented by Barker et al. (1999) and Fu et al. (2000b) for solar radiation in deep convective clouds. In the underlying stratiform layer the ICA bias is comparatively small, but it increases again in the bottommost region of shallow cumuli due to their increased side area, where 3-D radiative effects are maximized (Črnivec and Mayer, 2019). A similar picture is identified in the thermal spectral range, where the maximal ICA bias of 0.1 K day^{-1} is observed in the anvil
375 and the cumuliform region, whereas in the stratiform layer the 3-D effect is limited.
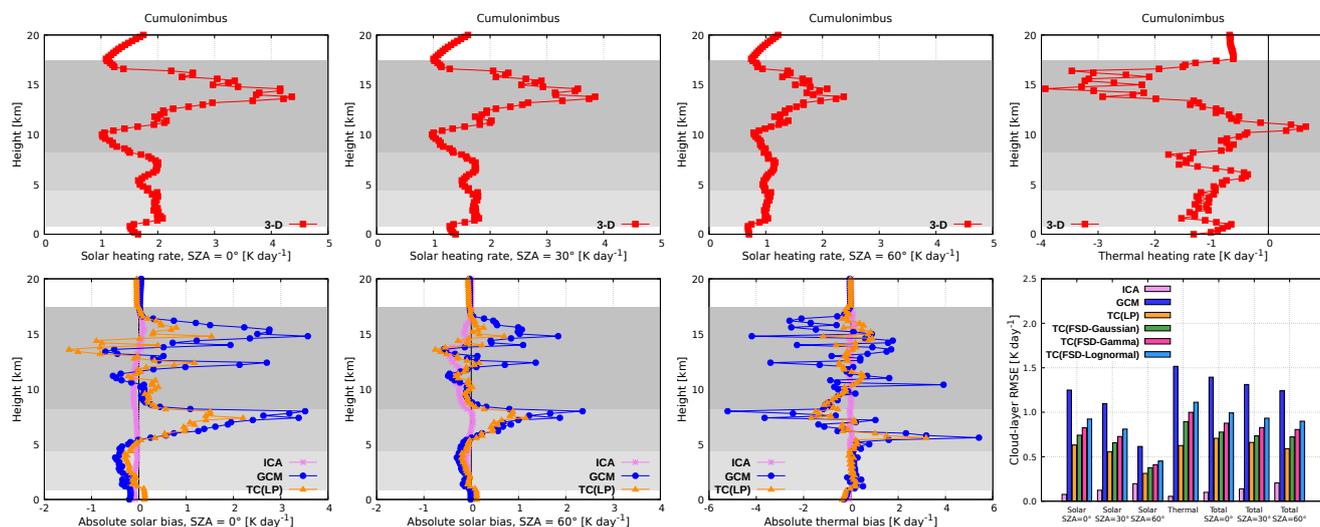
Figure 7. Radiative heating rate for the cumulonimbus cloud. The grey-shaded area denotes the cloud layer. The liquid region is shaded light grey, the mixed-phase region is shaded middle grey and the ice region is shaded dark grey.

In both solar and thermal spectral range the GCM reveals large biases within the anvil portion and even larger biases in the stratiform layer underneath (Fig. 7, bottom row). The latter are as expected a manifestation of considerable horizontal inhomogeneity observed in the stratiform region (recall that its actual FSD is two times larger than that of the anvil), which implies that the horizontally homogeneous cloud assumption is violated more in the stratiform region than in the anvil. If the

380 stratiform layer had not been partially shielded by the anvil, the biases therein would be even larger. For overhead Sun, for example, we observe an overestimation of solar heating by up to 3.6 K day^{-1} in the anvil region and 3.5 K day^{-1} in the stratiform region. Thermal GCM bias of cloud top cooling up to -4.2 K day^{-1} and that of cloud base warming up to 3.9 K day^{-1} is observed within the anvil. Within the stratiform region, thermal cooling is overestimated with a bias of up to -5.2 K day^{-1} and thermal warming is overestimated by 5.4 K day^{-1} in the GCM configuration. This indicates a significant need for

385 proper TC usage when treating deep convection.

All Tripleclouds experiments yield a significant reduction of solar, thermal and total heating rate bias when compared to conventional GCM. The TC(LP) experiment performs best, reducing the cloud-layer RMSE two- to threefold. As an illustration, thermal RMSE of 1.5 K day^{-1} is reduced to solely 0.6 K day^{-1}. Although the actual LWC and IWC are better approximated with either lognormal or gamma distribution, the assumption of gaussianity works best in practice. The reason for this is similar

390 as was for the cirrus case study: the actual FSD of the cumulonimbus is mostly larger than the global estimate. As the assumed gaussianity implies the largest difference between the LWC/IWC pair, it partly accounts for the missing inhomogeneity degree introduced by global FSD. Noteworthy, within the stratiform layer (the liquid phase of which is markedly heterogeneous with FSD similar to that of the cirrus case), TC(FSD) experiments represent a considerable improvement compared to the GCM.

This could be partially due to radiatively important effect of ice within the stratiform mixed-phase region: the actual FSD of
395   ice is in close proximity to the global estimate, thus acting to reduce the overall TC error in this region.

3.2 Net surface flux

3.2.1 Stratocumulus

Figure 8 (top row) shows the net surface flux underneath the stratocumulus. The ICA bias is small during daytime and nighttime,
maximized at overhead Sun (up to -5 W m^{-2} or -2 %). This is essentially attributed to the photon cloud side escape effect
400   (Várnai and Davies, 1999), where preferential forward scattering on cloud droplets increases 3-D surface downward radiation
(Wissmeier et al., 2013). An increased solar absorption in the homogeneous GCM cloudiness implies reduced transmittance
and hence underestimated daytime net surface flux. The bias is largest at overhead Sun (-33 W m^{-2} or -9 %) and decreases
with increasing SZA, whereas at nighttime the GCM bias is minor.

When the TC(LP) is applied, the net flux bias is mostly slightly reduced, whereas in TC(FSD) experiments the bias is
405   increased compared to the conventional GCM, therefore optimizations are tested in Sect. 4.

3.2.2 Cirrus

Figure 8 (middle row) shows the net surface flux underneath the cirrus. The ICA underestimates the 3-D benchmark, primarily
due to the aforementioned cloud side escape, although this phenomenon is less noticeable for optically thin cirrus (bias held
below -3 W m^{-2} or -1 %). The GCM, on the contrary, reveals large biases. Whereas the absolute bias is largest at high Sun
410   (-33 W m^{-2} at SZA of $0°$ and $30°$ during daytime), the relative bias is maximized at SZA of $60°$ on account of strongly
reduced benchmark. Insufficient surface nighttime cooling in the GCM implies a bias of 5.5 W m^{-2} (-6 %).

All Tripleclouds experiments perform better than the GCM. The largest amelioration is observed at nighttime, where the
TC(LP) practically depletes the entire bias, while TC(FSD) experiments generally halve the GCM bias. Nevertheless, alterna-
tive arrangements for better TC utilization are investigated in Sect. 4.

415   ### 3.2.3 Cumulonimbus

Figure 8 (bottom row) shows the net surface flux underneath the cumulonimbus. The 3-D radiative effects at the surface
are by far largest for the cumulonimbus case, which is a consequence of its large aspect ratio. The daytime net flux in the
ICA is underestimated at all SZAs (maximal bias of -45 W m^{-2} or -8 % at overhead Sun), principally due to the cloud
side escape mechanism. The opposing 3-D effect is related to side illumination, where the effective cloud cover (Hinkelman
420   et al., 2007) increases with descending Sun. This casts an elongated shadow, reducing the 3-D net flux, although for the
towering cumulonimbus geometry the side escape dominates also at SZA of $60°$. This extensive role of 3-D radiative transfer
is consistent with the findings of Di Giuseppe and Tompkins (2005), who showed that the solar bias is an asymmetrical function
of cloud cover, with the maximum attained at anvil coverage of $30-40$%. The majority of previous studies on deep convective
systems documented smaller surface ICA bias, mostly due to a vast anvil representative of organized convection. For isolated
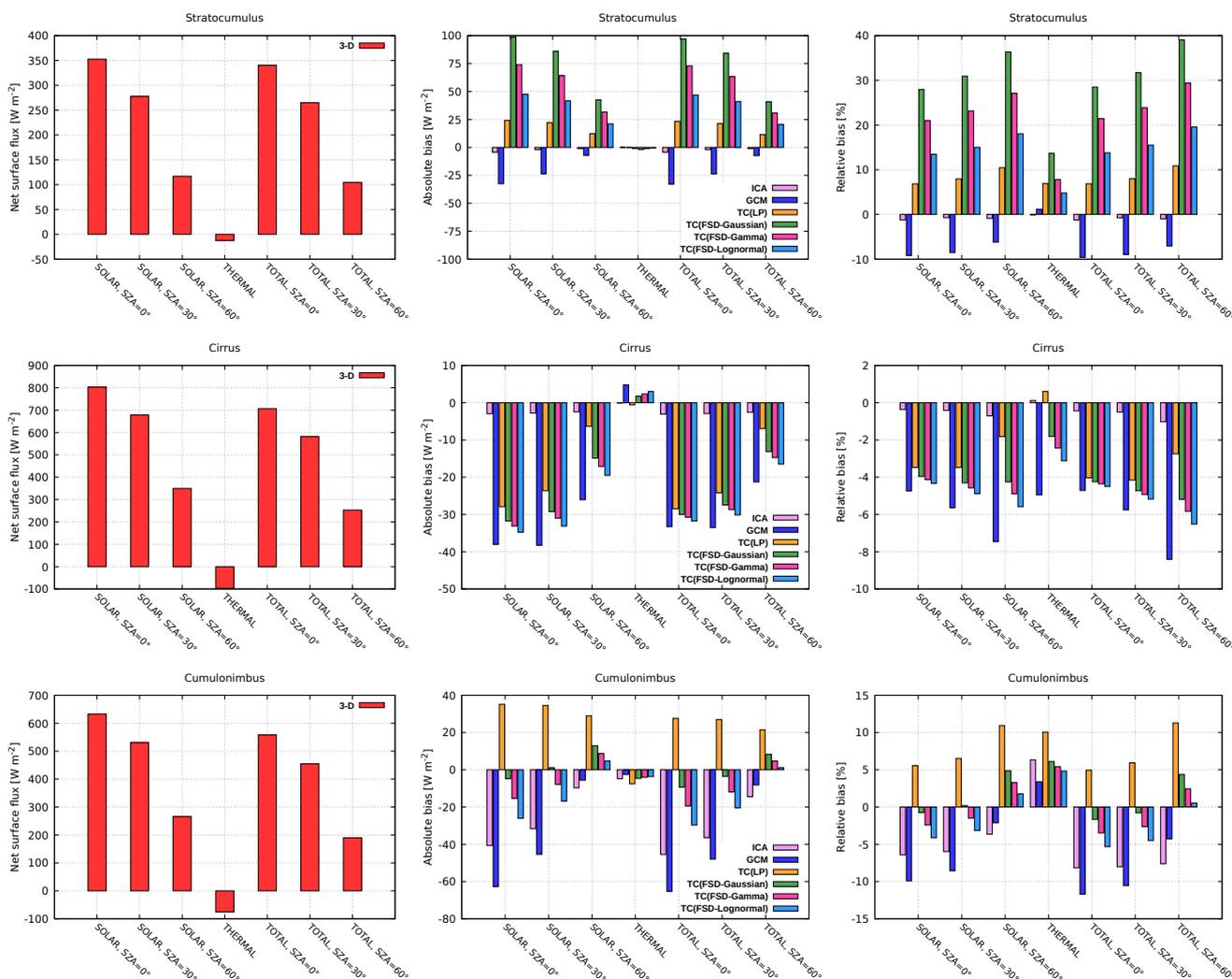
Figure 8. Net surface radiative flux for stratocumulus (top row), cirrus (middle row) and cumulonimbus (bottom row).

thunderstorms or largely unorganized convection, the greater ICA bias as reported herein and previously indicated by Tompkins and Di Giuseppe (2003) is presumably more appropriate. According to Rickenbach and Rutledge (1998) such cases constituted about 50 % of all convective events observed during TOGA-COARE (Webster and Lukas, 1992). The nighttime surface cooling in the ICA is stronger than in the 3-D (bias of -5 W m^{-2} or 6 %), since realistic cloud side emission increases downward radiation at the surface (Schäfer et al., 2016).

All deficiencies of the ICA manifest in the GCM as well. Nevertheless, the daytime GCM bias is even larger (-65 W m^{-2} or -12 % at overhead Sun). The horizontally homogeneous GCM cloud emits a greater radiation amount towards the surface compared to the heterogeneous cloudiness in the ICA, leading to a reduced nighttime bias.

The Tripleclouds method leads to a significantly improved daytime net flux compared to its representation in the GCM, especially in conjunction with the FSD method. In particular, the GCM bias at overhead Sun is reduced by a factor of up to 6. At SZA of 60° the daytime GCM bias is practically entirely depleted as it is reduced by a factor of 8 when TC is applied with the lognormal assumption. The TC slightly degrades nocturnal surface budget compared to the GCM, although for the lognormal assumption this degradation is marginal (relative bias increased by 1 %).

4 Parameter optimizations

In summary, Tripleclouds in its baseline configurations proved to perform well for the apparently most complex deep convective scenario, where it depleted the majority of GCM biases. In the case of stratocumulus and cirrus a refined TC realization is highly desired.

4.1 Optimization for overcast cloud scenarios

It was previously pointed out that in the uppermost overcast part of the stratocumulus, the actual FSD is smaller than the introduced global estimate. This might be partially attributed to the fact that overcast grid boxes do not contain cloud edges, which generally contribute to increased variability. Mixing of cloudy and cloud-free air at the edges of clouds, namely, tends to decrease the mean LWC as well as to increase the spread of LWC, both acting to increase the FSD. A grid box excluding cloud edges will therefore have lower FSD. To that end, we test the parametric FSD relationship proposed by Boutle et al. (2014), denoted as B14, for liquid cloud inhomogeneity, developed based on a rich combination of satellite, in situ and ground-based observations. This parameterization takes into account that variability is generally dependent on grid box size and cloud fraction and exhibits a discontinuity at $C=1$ capturing the aforementioned cloud edge effect. Thus the FSD of liquid phase for a grid box of horizontal size x [km] and cloud fraction C is given by:

$$FSD = \begin{cases} (0.45 - 0.25C)\Phi_c(x,C), & \text{if } C < 1. \\ 0.11\Phi_c(x,C), & \text{if } C = 1. \end{cases} \qquad (11)$$

where:

$$\Phi_c(x,C) = (xC)^{1/3}\big((0.06xC)^{1.5} + 1\big)^{-0.17}.$$

Figure 9 shows the results of the conventional GCM calculation, the Tripleclouds in its baseline lognormal configuration with the global FSD estimate (abbreviated to "G" on the graphs in the remainder of this section), as well as the corresponding refined TC experimentation where the FSD within the stratocumulus layer is parameterized according to B14. The nighttime and daytime cloud-layer RMSE (Fig. 9, left) in the refined TC experiment is generally slightly reduced (except at low Sun) compared to its counterpart in the baseline configuration and remains considerably lower than that in the GCM for all nighttime/daytime conditions. Most importantly, the net surface flux bias (Fig. 9, middle and right), which in the baseline TC setup was even larger than in the conventional GCM, is practically entirely depleted in the refined Tripleclouds venture.
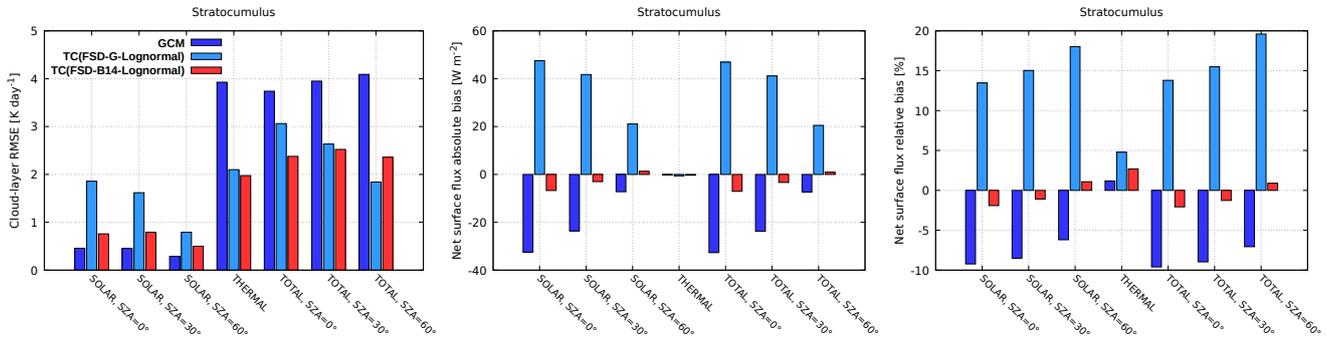
Figure 9. Optimization for stratocumulus (same experiment labeling on all panels).

4.2 Optimization for highly heterogeneous cloud scenarios

The key point worth mentioning when highly heterogeneous scenes as is the cirrus cloud are tackled with the Tripleclouds solver, is that the split percentile (SP) of 50 (geometrically halving layer cloudiness when allocating optically thin and thick

465 portions of the cloud) is not the best choice (Hogan et al., 2019). The examination of IWC distribution in each vertical layer of the present cirrus indeed reveals that these are highly skewed (with a modal value close to zero and a long tail with rarely occurring high IWC). Therefore it seems reasonable to allocate a larger portion of the cloud to the optically thinner region. This concurrently implies increasing the weighting of IWC^{cn} and decreasing the weighting of IWC^{ck}, whereby the latter is shifted to a higher value to conserve the layer mean. In order to discern the optimum geometrical partitioning of the cirrus into two parts,

470 we carried out multiple experiments with global FSD, gradually increasing the SP from 50 to 99 (the limit of 100 coincides to the horizontally homogeneous cloud representation). Further, we aim to assess the advantage of more sophisticated FSD parameterizations. We thus evaluate the parameterization for ice cloud inhomogeneity of Hill et al. (2015) [H15], developed on the basis of CloudSat (Stephens et al., 2002, 2008) data products. All TC experiments presented in this section model the subgrid IWC distribution as lognormal.

475   Figure 10 (top row) shows the cloud-layer RMSE and net surface flux bias using TC with different FSD parameterizations for three selected splitting events, characterized by the SP of 50 (baseline), 75 and 90 (allocating 3/4 and 9/10 of layer cloudiness to the optically thinner region). For comparison the GCM experiment is shown as well. It is apparent that there is a considerable sensitivity to the choice of geometrical splitting, with the most asymmetrical split (matching the SP of 90) performing best in all cases. Noteworthy, at a given splitting event, the experiments where the FSD is parameterized according to H15 mostly

480 lead to degraded results compared to those with global FSD (in particular at best-split scenario with SP of 90). Thus although the parameterization of H15 incorporates height dependence of horizontal variability (via cloud fraction), it underestimates the actual FSD being even smaller than the global estimate (Fig. 10, middle row, left), which brings the aforementioned radiative degradation. Further research oriented towards advanced retrievals of high cloud inhomogeneity is therefore firmly advocated. Vertical profiles of solar and thermal heating rate in TC experiments with global FSD for the aforementioned splitting events
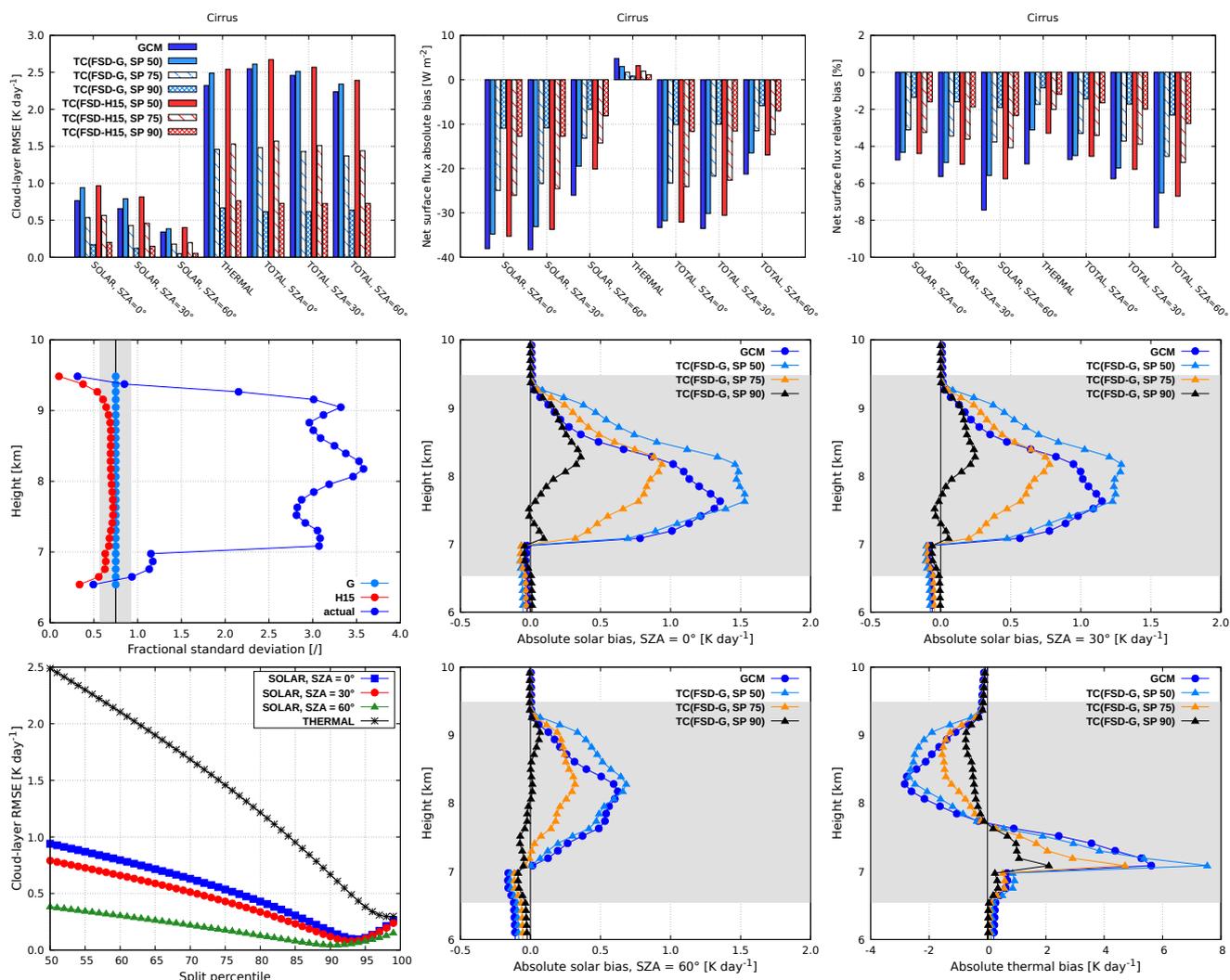
Figure 10. Optimizations for cirrus (subgrid variability is modeled lognormal in all TC experiments shown).

are further compared with the GCM in Fig. 10. For highly asymmetrical splitting, the cloud-radiative bias throughout the
majority of the cirrus layer is significantly reduced.

Figure 10 (bottom left) shows the cloud-layer RMSE of TC experiments with global FSD for the entire range of splitting
events. In the solar part of the spectrum, the optimum SP minimizing the bias indeed lies around 90 (the exact value depends
on SZA). Increasing the SP beyond this optimum value degrades the heating rate in the cirrus layer. In the thermal part,
on the contrary, the RMSE practically monotonically decreases as the SP is increased. Hence, the thermal RMSE exhibits a
minimum when the TC is configured so that the entire layer cloudiness is attributed to the optically thinner region (horizontally
homogeneous cloud representation with an effective IWC equal to IWC^{cn}). This indicates that for extremely heterogeneous
scenes, as is the present cirrus, the radiation scheme employed in a weather or climate model could alternate between the

Tripleclouds in the solar spectral range and the computationally more efficient conventional GCM solver in the thermal spectral

495   range, albeit with scaled IWC (effectively the traditional *scaling factor method*).

5   Summary and conclusions

This study aims to advance the conceptual understanding of radiative transfer in marine stratocumulus, midlatitude cirrus and tropical deep convective clouds. The focus is laid on the issues related to misrepresentation of cloud horizontal inhomogeneity in coarse-resolution weather and climate models, which are tackled with the aid of the Tripleclouds radiative solver. The TC

500   method, primarily introduced by SH08, is an approach accounting for horizontal cloud inhomogeneity by using two regions in each vertical layer to represent the cloud (as opposed to one, which is the convention of traditional cloud models). One of these regions is utilized to represent the optically thicker portion of the cloud, whereas the other region represents the residual optically thinner portion. The challenge is to properly set the pair of liquid/ice water content defining the two cloudy regions and divide the layer cloudiness geometrically in the corresponding two parts. The primary objective of the present

505   work was to evaluate the global FSD estimate together with different assumptions for cloud condensate distribution, which are commonly applied in models. The TC concept was recently integrated in the efficient δ-Eddington two-stream radiation scheme (Črnivec and Mayer, 2020) and was used herein to answer these questions within the scope of the *libRadtran* library. For our study we chose three intrinsically contrasting cloud types generated by different cloud models, which should reflect diverse cloud conditions occurring globally. These high-resolution cloud field data allow to gain important insights about small-scale

510   cloud variability and give the opportunity to compare the actual modeled variability with the global estimate or other existing parameterizations. For each cloud type, various TC experiments were evaluated against a 3-D benchmark calculation. These results were compared with the conventional GCM computation utilizing homogeneous layer cloudiness, which can be viewed as the upper limit for the tolerable TC error. Moreover, the ICA approximation was compared with the 3-D benchmark to quantify the bias related to neglected horizontal photon transport. A systematic investigation of cloud-layer heating rate and

515   net surface flux bias was provided for each selected cloud case.

It was found that in the majority of applications, the ICA is significantly more accurate than the conventional GCM experiment, indicating a large potential for Tripleclouds, which reduces the bias related to unresolved cloud structure, but not to horizontal photon transport. Regarding the optimal TC configuration, which aims to minimize the radiative bias, the exact conclusions drawn depend on each particular cloud type case study. In general, the simplest TC arrangement using a globally

520   constant FSD and geometrically halving the layer cloudiness worked best for the apparently most complex deep convective scenario. In case of stratocumulus and cirrus, an improved TC performance was highly desired. To that end, the second objective of the present study was to assess recent advanced FSD parameterizations, characterizing systematic departures from global mean cloud variability observed for liquid and ice phase. For the stratocumulus, an optimization in terms of a parametric FSD relationship portraying reduced horizontal variability at overcast conditions lead to a substantially improved TC realization.

525   For extremely heterogeneous cirrus, on the other hand, allocating the greater portion to the optically thinner part of the cloud (e.g., approximately 9/10 of layer cloudiness in the solar part of the spectrum), proved to be of crucial importance in the TC

settings, eliminating the vast majority of GCM biases. These findings are in support of cloud regime dependent approaches, which ought to be further boosted to be used in radiation schemes of next-generation atmospheric models. Whereas current GCMs do not explicitly predict cloud meteorological regimes (e.g., whether model cloudiness appears in the form of cumulus
530 or stratocumulus), they have the ability to diagnose cloud type based on temperature and humidity fields (Norris, 1998). An alternative is to consider the physical processes responsible for cloud formation as imprinted in the parameterization schemes activated to generate cloudiness within a model grid box (e.g., shallow convection as opposed to large-scale saturation). We thereby propose that the TC configuration should be adequately adjusted according to cloud type.

The acquired physical understanding of radiative biases, in particular those stemming from neglected cloud horizontal het-
535 erogeneity, for three fundamentally contrasting cloud case studies as highlighted in this work, is a necessary first step for properly setting the TC parameters in its possible future operational usage. A more comprehensive documentation of radiative biases would necessitate the examination of the full parameter space of in-cloud horizontal variability and cloud geometry. As an illustration, Črnivec and Mayer (2019) investigated the 3-D, ICA and NWP-type radiative transfer for an evolving shallow cumulus and showed that the biases depend on the stage of cloud field life cycle. Although Črnivec and Mayer (2019) examined
540 radiative biases at the resolution of regional NWP models, similar problematics is expected at coarser resolution of larger-scale models as well. A natural extension of the present study therefore appears to be the examination of the full ASTEX data set. The transition from solid stratocumulus to trade cumulus or stratocumulus breakup (Albrecht et al., 1995; Bretherton and Wyant, 1997), seems appealing to study with Tripleclouds, since it is often associated with increased horizontal heterogeneity (Wang and Lenschow, 1995; Wood, 2012). Whereas in the current study a single stratocumulus was investigated, the future
545 work should distinguish between clean (marine) and polluted (continental) cases. For the ASTEX field experiment, namely, substantial variations in clear and polluted air masses were reported, which affected both cloud properties and drizzle. These topics will be addressed in a forthcoming study.

Code and data availability.   The radiative transfer package *libRadtran* 2.0.4 is available at https://doi.org/10.5281/zenodo.4262916 under the GNU General Public License v2. The Zenodo repository additionally archives data for the stratocumulus, cirrus and cumulonimbus clouds
550 as well as the MYSTIC benchmark radiation data, which are accessible under Creative Commons Attribution 4.0 International License (CC BY 4.0). The scripts to process the cloud data and to perform the radiative transfer simulations are available at the same repository under CC BY 4.0 as well.

Author contributions.   NC conceived the study, processed the cloud data, performed radiative transfer simulations and evaluated the results. BM upgraded the Tripleclouds implementation within *libRadtran* to include the ice phase cloud processing for the purpose of this research.
555 NC prepared the paper draft, whereby BM provided valuable input for its final version.

Competing interests.   The authors declare that there is no conflict of interest.

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