

Response letter to Reviewer 1

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1 Summary

1 This paper presents a study of the impact of three increasingly realistic parameterizations of the ice-ocean turbulent heat flux (ice-bath, 2-equation, 3-equation) on the seasonality of Arctic sea ice (thickness and concentration) and the climate system in general, using four different models with increasing level of complexity (SIM, CICE, MPIOM, COSMOS). In the ice-bath
5 model, the top ocean grid cell is simply fixed at freezing temperature. The 2-equation and 3-equation models have a linear dependency on the friction velocity and the temperature difference between ocean mixed layer and its interface with the ice. Their difference lies in the definition of the interface temperature: the freezing temperature of the top grid cell of the ocean or the freezing temperature of the water at the interface which depends on the ice bottom melting rate. Results show that the simulation of the seasonal cycle in sea ice thickness and concentration improves with the complexity of the model. Results also
10 show that the spatial distribution of sea surface temperature is insensitive to the treatment of the ice-ocean turbulent heat flux in winter and summer, except at the ice edge in summer for the 3-equation model. In the Arctic Ocean, the 3-equation model leads to cooler deep waters and saltier waters over the whole column. This results in a stronger NAO and AMOC. Based on these results, the authors argue for the importance of a realistic parameterization of ice-ocean heat exchange.

The paper presents an insightful and detailed analysis of the impact of different treatment of the ice-ocean turbulent fluxes on
15 Arctic climate simulation. The introduction, however, lacks details about the relevance of the study and how it fits in the context of previous studies, as well as with the presentation of the three parameterizations. The paper is generally well organized and clear but it should be proof-read for English grammar – particularly after the Introduction section. We recommend that the paper be accepted for publication after the comments below have been addressed.

Dear Reviewer,

20 **Thank you very much for your constructive comments. In the following, we present our point-to-point responses. Our answers to your comments are written in bold.**

Thanks again for your time and efforts.

Best, Xiaoxu

2 Major comments

25 a Abstract: "...a similar turbulent heat-flux parameterization as (2) but with the temperature at the ice-ocean interface depending on ice-ablation rate". The general reader will not appreciate this sentence early in the paper, i.e. before having read the rest of the paper. An explicit reference to the three-equation model should be included here.

We now take direct reference to the three-equation model as follows:

30 *These three parameterizations are (1) an ice-bath assumption with the ocean temperature fixed at the freezing temperature; (2) a 2-equation turbulent heat-flux parameterization with ice-ocean heat exchange depending linearly on the temperature difference between the underlying ocean and the ice-ocean interface whose temperature is kept at the freezing point of the sea water; and (3) a 3-equation turbulent heat-flux approach in which the ice-ocean heat flux depends on the temperature difference between the underlying ocean and the ice-ocean interface whose temperature is calculated based on the local salinity set by the ice-ablation rate.*

35 b Abstract: The abstract should report on all key results. As it stands, only results from Model (3) are reported and one wonders why option (1) and (2) were considered in the first place if they don't deserve a line in the abstract.

We referred to the most realistic parameterization (3) as our reference/control simulation, therefore we compared the simulation results of (1) and (2) to (3). Based on the reviewer's comment, in our abstract we now include a discussion of the differences between (1) and (2), so the reader can obtain a more detailed overview of our key results.

40 **The following texts can also be found in the revised manuscript at line 7-16.**

Based on model simulations with the standalone sea-ice model CICE, the ice-ocean model MPIOM and the climate model COSMOS, we find that compared to the most complex parameterization (3), the approaches (1) and (2) result in thinner Arctic sea ice, cooler water beneath high-concentration ice and warmer water towards the ice edge, and a lower salinity in the Arctic Ocean mixed layer. In particular, parameterisation (1) results in the smallest sea ice thickness among the 3 parameterizations, as in this parameterisation all potential heat in the underlying ocean is used for the melting of the sea ice above. For the same reason, the upper ocean layer of the central Arctic is cooler when using parameterisation (1) compared to (2) and (3). Finally, in the fully coupled climate model COSMOS, parameterisations (1) and (2) result in a fairly similar oceanic or atmospheric circulation. In contrast, the most realistic parameterization (3) leads to an enhanced Atlantic meridional overturning circulation (AMOC), a more positive North Atlantic Oscillation (NAO) mode and a weakened Aleutian Low.

c 119, Introduction: The same Schmidt et al., 2004 reference is used for the simplest parameterization (fixed To_{cn}) and also for the most complex parameterization (3-eqs model). This is confusing. The contribution of Schmidt et al. is the system of 3-eqs to solve for the interface temperature, not the fixed To_{cn} at freezing point. Another (earlier) reference should be used for the fixed To_{cn} parameterization.

55 **We now generically refer to a discussion of all three approaches in Holland, 1999; Jenkins, 2001; Notz et al., 2003 and Schmidt et al., 2004 as follows:**

60 "A number of approaches exist for the calculation of the oceanic heat flux F_{oce} (c.f. Holland and Jenkins, 1999; Jenkins et al., 2001; Notz et al., 2003; Schmidt et al., 2004). For the simplest parameterization, the ice–ocean system is simply treated as an ice bath: The temperature of the uppermost ocean grid cells is fixed at its freezing temperature, and any excess energy that enters these grid cells via advection, convection, or heat exchange with the atmosphere is instantaneously applied to the ice through lateral and bottom melting. "

d The authors should describe how their work fits in with the existing literature in both the Introduction and Discussion. Tsamados et al., 2015 examines similar questions. How do the results of this study compare with those of Tsamados et al? What is learned from this study that was not known before?

65 **In introduction we add (line 92-105):**

70 *Exploring the behavior of different parameterizations describing ice-ocean heat flux has been an important topic in model studies. Significant differences can generally exist between melt rates calculated with the 3-equation approach and less realistic approaches (c.f. Notz et al., 2003; Tsamados et al., 2015), as only the 3-equation approach allows for heat fluxes that are directed from the interface into the water and therefore allows for a realistic limitation of melt rates through the formation of a fresh water layer underneath the ice. In a recent study the sensitivity of sea ice simulation to the approaches introduced in McPhee (1992) and Notz et al. (2003) have been examined using a stand-alone sea ice model CICE (Tsamados et al., 2015). CICE uses a simple thermodynamic slab ocean with fixed mixed layer depth and sea water salinity. Thus, the realistic effect of oceanic processes can not be represented. For example the sea ice over the Southern Ocean is severely overestimated by CICE due to a lack of warming effect from the Antarctic deep water. Therefore it is necessary to also investigate the ice-ocean heat flux formulations in a more complex system, including an interactive ocean or even the atmosphere. Based on this motivation, in the present study, we examine how different physical realism that is represented by the three discussed parameterizations impact the resulting ice cover, large-scale oceanic circulation, and atmosphere properties in different numerical models ranging from an idealized columnar model, a stand-alone sea ice model, an ice-ocean coupled model, to a most complex climate system model.*

80 **In discussion we add (line 400-409):**

85 *Note that our results are in good agreement with a previous study using CICE (Tsamados et al., 2015) that found in August stronger basal -melting of Arctic sea ice, decreased Arctic Ocean salinity, cooling of sea water in the central Arctic and warming of sea water at the ice edge in the 2-equation experiments compared to the 3-equation approach. However, in their study the effects are more pronounced, possibly because we used different model versions of CICE and different parameters for the ice-ocean heat flux formulations, one example is the value for R, which is 50 in Tsamados et al. (2015) and 35 in our case. In addition, different atmospheric forcings were used in our studies.*

In contrast to their and other previous studies, in our study we do not only use a stand-alone sea-ice model but also analyse a coupled ice-ocean model and an earth-system model. These allow us to examine the effect of various oceanic heat-flux formulations on the deep ocean and the atmospheric circulation as well as their impact on sea-ice properties.

90 e The background provided in the introduction is well written. However, the overall motivation for the study and its relevance to the field is not clearly stated. A discussion of how different climate models currently simulate ice-ocean heat fluxes would go a long way in addressing this point. This is stated at the end of the paper. It should also be stated earlier in the paper.

95 **One motivation of our study is to test the 3 heat-flux formulations in sea ice models. Another motivation, as our response to your last comment, arise from the fact that most former studies used stand-alone sea ice models, there is a lack of investigation on the oceanic and atmospheric responses, here we refer to our response to comment d.**

Besides, according to the reviewer's comment, we further add in the introduction the following content (line 106-109):
Another motivation of our study is to help improve the formulation describing ice-ocean heat flux in various models. For example in the 4th version of CICE, only ice-bath and 2-equation assumptions could be applied. In MPIOM and COSMOS, the ice-bath approach is used, which can lead to an overestimation of oceanic heat flux into sea ice. In our study
100 *we implemented the more realistic 3-equation parameterization into all the models mentioned above.*

f The presentation of results from the ice-bath parameterization should be motivated given that the authors states that it is "incompatible with observations" (1.24)?

105 **Yes, since this parameterization is incompatible with observations but still used in MPIOM and COSMOS, we would like to improve the heat-flux formulation in the two models. We have included this point in the introduction (the same as our response to your last comment) (line 106-109):**

Another motivation of our study is to help improve the formulation describing ice-ocean heat flux in various models. For example in the 4th version of CICE, only ice-bath and 2-equation assumptions could be applied. In MPIOM and COSMOS, the ice-bath approach is used, which can lead to an overestimation of oceanic heat flux into sea ice. In our study we implemented the more realistic 3-equation parameterization into all the models mentioned above.

110 g 1.45. The introduction should include a discussion of the different ways of calculating the ice-ocean heat flux for all three methods. This is only clarified in section 2. This should also come earlier in the paper, in section 1.

According to the reviewer's comment, we have merged section2 into section1. Here we refer to the Introduction part in the updated manuscript.

115 h 1.170: Ideally, the experiments would be done with the same GCM, subsequently removing components to reduce the level of complexity. As it stands now, the CICE model has an ITD, when the GCM(COSMOS) does not. The same comment applies for the forcing that changes between models. This would facilitates the comparison of simulations with different model components. As it stands now, we are left wondering how much of the difference in behavior between models is due to the different model components and forcing rather than the ice-ocean turbulent flux parameterization. GCMs typically has this functionality. If COSMOS does not have this capability, it should be acknowledged, and this caveat should be mentioned.

120 **Thanks for the nice comment. The model COSMOS consists of the atmospheric module ECHAM5 and the ice-ocean module MPIOM, therefore, the ice-ocean model MPIOM used in our study is actually part of COSMOS. In this case, we are using the same GCM (COSMOS) and removing the atmosphere part to reduce the level of complexity (from**

coupled ECHAM5-MPIOM to ocean-only MPIOM). But in MPIOM it is not possible to separate the ocean from the sea ice. Therefore we choose another stand-alone sea ice model CICE.

125 So the only thing to be discussed here is the different components/forcings/configurations used in CICE and MPIOM. Therefore we add the following in the discussion section (line 429-436):

It should be noted that CICE is in many aspects different from the sea ice component in MPIOM: 1) CICE uses the multi-layer approach with a sub-grid scale ice-thickness distribution (Bitz and Lipscomb, 1999), while MPIOM uses zero-layer thermodynamics following Semtner Jr (1976). 2) A submodel of ice dynamics based on an elastic-viscous-plastic rheology (Hunke and Dukowicz, 1997; Hunke, 2001) is used in CICE, and in MPIOM viscous-plastic dynamics following Hibler III (1979) is applied. 3) Different spatial resolutions are used in CICE (1°) and MPIOM (3°). 4) CICE is forced by monthly-mean climatological data from National Center for Atmospheric Research (NCAR), while MPIOM experiments are forced by daily fields from the climatological OMIP data set (Röske, 2006). Therefore, the different model behavior between CICE and MPIOM can to a certain extent be explained by the different model configurations.

135 i Section 2, 192-110: The discussion of the methods, the caveats related to each method, and how each method relate to previous studies should be streamlined. References should appear in parentheses for clarity and text that does not pertain to the Heat Flux Parameterisations should appear in other sections (e.g. Discussion).

Thanks. According to the comment, we have made several modifications to the manuscript:

1). For the original 196-97, we put the references in a clearer way:

140 *Laboratory experiments imply $35 \leq R \leq 70$ (Owen and Thomson, 1963; Yaglom and Kader, 1974; Notz et al., 2003).*

2). For the original 198-99, we remove the text into a new section of "Experimental design"

3). For the original 1104-111, we simplified the texts and also remove it to "Experimental design" section (189-195):

For each model, we perform separate simulations based on the three ice-ocean heat flux formulations (see table 1). We assume that the 3-equation approach with $R = 35$ describes reality more realistically, and hence use this simulation as our reference. In our idealized 1-D model, we also use $R = 70$ to test the model sensitivity with respect to this parameter. For a given value of R , we calculate α_h to satisfy the requirement described in McPhee et al. (1999). This results in a turbulent heat exchange coefficient $\alpha_h = 0.0095$ for $R = 35$ and $\alpha_h = 0.0135$ for $R = 70$. In SIM and CICE the mixed-layer salinity has a constant value of 34 g/kg. In MPIOM and COSMOS the salinity of the sea water evolves dynamically in response to oceanic or atmospheric processes.

150 j 1.206. The temperature at the interface for SIM-icebath is described here; yet it is not used in ice-bath. Are T_f and $T_{interface}$ from Equ. (2) and (3) for the ice-bath and 2-equation parameterizations (respectively) always the same? Does T_f for the ice-bath parameterization also depend on salinity? If so, that would also make it a "2 equations" problem. The differences between each "temperatures" in all three parameterizations should be described more clearly. A table with the formulas and temperatures used in each method would help clarify this issue.

155 **Yes, for ice-bath and 2-equation, the ice-ocean interface temperature is equal to the freezing temperature T_f . T_f in ice-bath also depend on salinity of sea water, but as the the sea water salinity in SIM and CICE is fixed at 34 psu, T_f is**

therefore always kept at -1.84 C. According to the comment, we now extend our table 1, in order to show the Tinterface and Tf in each experiment. We refer to Table 1 in our revised paper.

k 1.99 Why is the sensitivity of the model to the parameter R tested given that “R=35 best describes reality”?

160 **Because laboratory experiments imply $35 \leq R \leq 70$ (Owen and Thomson, 1963; Yaglom and Kader, 1974; Notz et al., 2003). The value of $R \approx 35$, as suggested by McPhee et al. (2008) is more consistent with the laboratory result ($35 \leq R \leq 70$), as compare to what Sirevaag (2009) found from an analysis of field data ($R \approx 33$).**

l Section 4.1: This is where the authors examine the sensitivity of the choices described in Section 2 using an idealized model. A more detailed discussion of these results (along with additional figures) should be included in this section.

165 **We use our 1-D model to conduct a series of sensitivity studies to test the response of ice-ocean heat flux to the choices of mixed layer depth or friction velocity. We also add one figure here for the SIM model.**

The following texts can also be found in the revised manuscript at line 239-248.

170 *To quantify the different response of the simulated sea-ice cover for a larger range of forcing conditions, we carried out a series of sensitivity studies. For each of these, we varied one of the forcing parameters and analysed the difference in annual mean ice thickness between SIM-3eq35 and SIM-icebath.*

We find that in our simplified setup, differences in ice thickness between SIM-3eq35 and SIM-icebath increases with mixed layer depth. This is due to the fact that the same amount of heat input from the atmosphere causes a smaller temperature change for a deeper mixed layer. According to equation (3), such smaller temperature change then causes a smaller heat flux to the ice bottom (Fig.2).

175 *In addition, we find that the anomaly in sea ice thickness generally decreases with friction velocity. This is related to the fact that for larger friction velocities, more heat is transported to the ice-ocean interface in the 3-equation setup (Fig.2), which enhances sea-ice ablation. While in icebath assumption the ocean-to-ice heat flux is independent of the friction velocity.*

m Section 5: One question that keeps coming up in the readers mind while reading the results section is: did the model
180 become more realistic as a result including a more realistic ice-ocean heat flux? Sometimes, especially in complex models, fixing one thing can often expose other problems, perhaps related to model tuning. With respect to this, the authors might consider describing how the results using the most realistic ice-ocean flux parameterization compare with observations. Sea ice thickness is tricky to measure, but Labe et al., 2018 could be a good start (They compare CESM, which uses CICE, to PIOMAS data). For the ocean surface, a qualitative comparison could be made to Peralta-Ferriz and Woodgate 2015, which is
185 a nice study looking pan-Arctic ocean observations over the past 30 years.

**Thanks for the suggestion. We agree that a more realistic parameterization might not improve the model results. The results of COSMOS in terms of sea ice properties have been validated in Notz et al. (2013), which showed an overestimation of Arctic sea ice thickness in COSMOS (i.e., ECHAM5/MPIOM) as compared to the PIOMAS for both winter and summer. Therefore our implementation of the 3-equation approach increases such model bias. We now
190 discuss this point in the last section of the updated paper (line 437-443).**

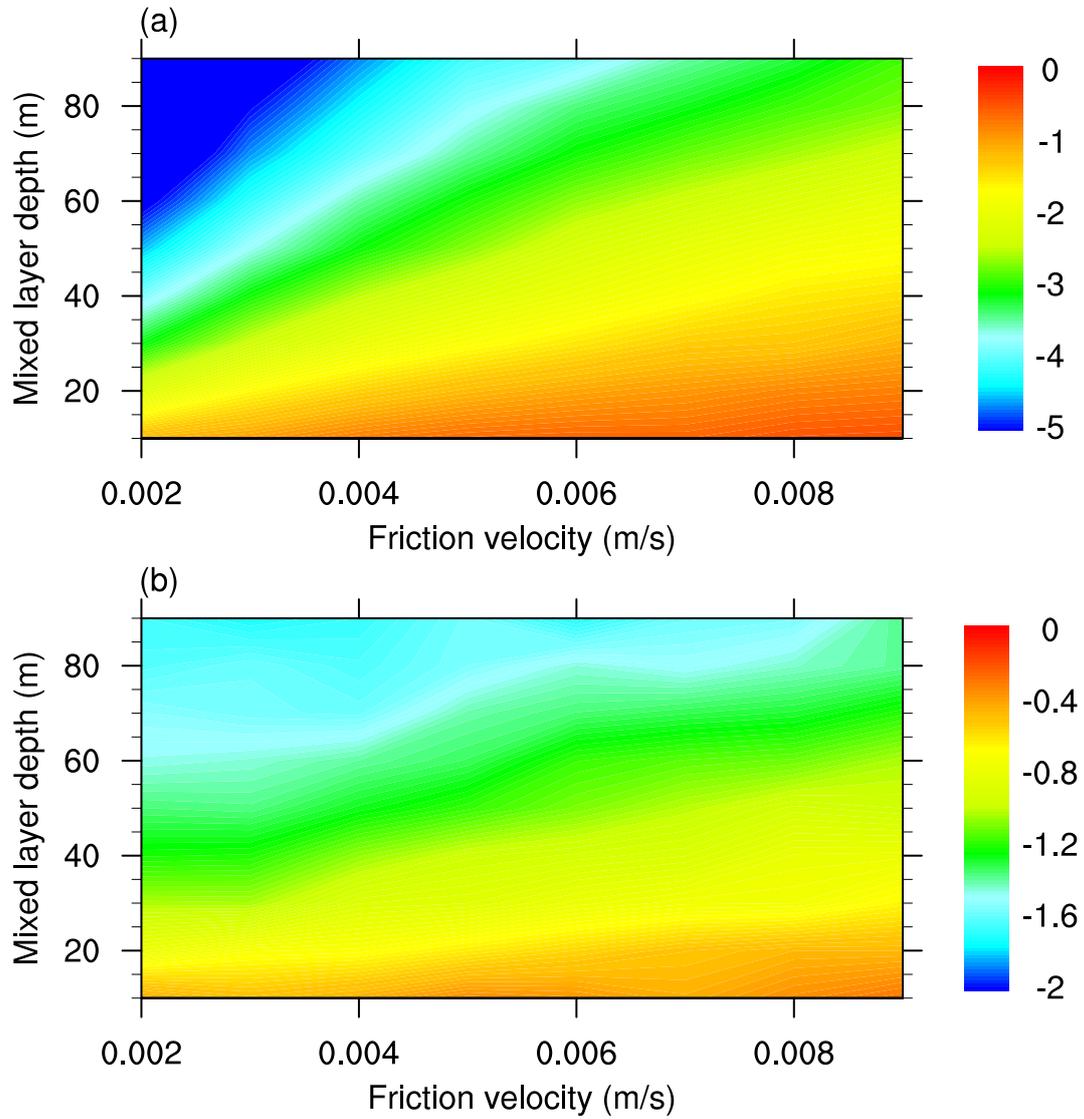


Figure 1. Anomalies of ocean-to-ice heat flux in SIM for (a) 3-equation minus icebath, and (b) 3-equation minus 2-equation, for different choices of mixed layer depth and friction velocity. Units are W/m^2 .

A detailed comparison of the simulations carried out here with observational data is beyond the scope of our study. However, we note that the sea ice thickness simulated by COSMOS have been evaluated by Notz et al. (2013), who found an overestimation of Arctic sea-ice thickness in ECHAM5/MPIOM (i.e., COSMOS) with the ice-bath formulation compared to the reanalysis from the Pan-Arctic Ice-Ocean Modeling and Assimilation System (PIOMAS) in both winter and summer.

195 *Improving the formulation of the ice–ocean heat flux by applying the 3-equation approach causes thicker ice and hence further increases this particular model bias. This indicates that the simplified heat flux parameterisation partly compensates for other errors in the coupled model setup.*

n 1218 and lines below. 1.218 should read “difference in annual mean ice thickness increases with friction velocity”. The same form should be used for 1220 and other instances that appear below: e.g. “. . .the larger the deeper our mixed layer is”.

200 The same comment for “mixed-layer and atmospheric temperature”, and again for “ice concentration and ice thickness”.Line 225: Do not word “explicable” should not be used in this context. Use instead: “This is explained by the fact that..”

Thanks. We have corrected all the grammar errors mentioned here in the revised version.

3 Minor comments

a 1.9, abstract. “The most realistic representation”. This is vague. It should reference parameterization (1), (2) or (3) above.

205 **We now reference parameterization (1), (2) or (3) . (see line 13)**

b 1.49-51. grammatical errors.

We have correct it: "*This becomes particularly important when large amounts of meltwater accumulate underneath sea ice during summer.*" (see line 74-75)

c 1.53-57. This sentence should be broken into more than one sentence for clarity.

210 **We have separated the long sentence into several sentences (line 110-114):**

" Section 2 introduces various models that we use for our purposes: 1) A conceptual 1-dimensional model allows us to examine a wide parameter range. 2) The Los Alamos Sea Ice Model (CICE) allows us to determine changes of sea ice in a modern sea-ice model. 3) The Max-Planck-Institute Global Ocean/Sea-Ice Model (MPIOM) can be used for examining the impact of the parameterizations on the large-scale ocean circulation. 4) The fully coupled climate model COSMOS can

215 *further help us to look at the atmospheric response to the described parameterizations. "*

d 1.71. Tmix is defined as the ocean temperature. The vertical level (e.g. first layer) should be stated since the temperature is not constant in the mixed layer of CICE.

CICE has only a slab-ocean, so there is only one fixed-depth mixed layer.

e 1.80. The freezing-point equation for seawater should be written explicitly.

220 **According to the comment, now we add a new equation describing the relationship between salinity and freezing point of sea water (Eq 4 at line 61 of the revised paper).**

f 1.100. typo: salt and heat are transported almost equally efficiently.

Thanks, we have corrected the typo in the updated version.

g Section 3: There are several instances where numbers appear in the text or within equations without references. The
225 references should be added.

**Thanks for the comment. For the bulk formulae we add the references for the Stefan-Boltzman constant and also
for the thermal conductivity of sea ice. The equations for the idealized seasonal variation in various fluxes and surface
albedo are based on approximation from observations. For this we provide the references in which the approximation
had been made. We also provide the references for the observational seasonal variation in surface albedo, and monthly
230 fluxes (we refer to section 2.1 in the revised paper).**

h 1.121. T_s is the ICE surface temperature. This should be defined. T_{bot} should also be defined.

**T_s was defined right before the equation (line 125). Now we add the definition of T_{bot} in the updated manuscript
(line 128).**

i 1.116. The acronym MPIOM should be defined when it first appear.

235 **Now the acronym MPIOM is defined in the introduction:**

*" 3) The Max-Planck-Institute Global Ocean/Sea-Ice Model (MPIOM) can be used for examining the impact of the
parameterizations on the large-scale ocean circulation."*

j 1.127: A reference for k_i should be given. Is this measurement really precise up to two decimal places?

We re-run the SIM experiments with a new $k_i=2.03$ (line 130-132).

240 ***For simplicity, we assume that the thermal conductivity of sea ice k_i is constant and set $k_i = 2.03 \text{ W/(m} \cdot \text{K)}$ according to
the seminal 1-D thermodynamic sea-ice model of Maykut and Untersteiner (1971).***

k 1.130 The Notz et al. and Maykut and Untersteiner references should appear above on line 129, i.e. before F_{sw} and F_{other} is
introduced.

We have moved the references before the equations (line 136-137).

245 l (5), 1.130, 1.131, 1.135. The number in the equations should be replaced by symbols; the "x" should be removed and the
numerical values should appear in the text, for the sake of clarity: (eg. 5.67×10^{-8} would be σ)

According to the comment, we have improved our representation of equations (line 125-142):

***The model consists of a simple zero-layer sea-ice model, where the surface temperature T_s is determined by balancing
atmospheric fluxes and the conductive heat flux through the ice according to***

$$-(1 - \alpha)F_{sw} - F_{other} + \epsilon\sigma T_s^4 = -k_i \frac{T_s - T_{bot}}{h}. \quad (1)$$

250 ***Here, α is the albedo of the ice surface, F_{sw} is the short-wave flux, $\epsilon = 0.95$ the infrared emissivity, $\sigma = 5.67 \times 10^{-8}$
the Stefan-Boltzman constant, T_{bot} the temperature at the ice-ocean interface, and F_{other} is the sum of sensible heat flux,***

latent heat flux and downward longwave radiation flux. $(1 - \alpha)F_{sw} + F_{other}$ represents the heat input to the surface of the ice, and $\epsilon\sigma T_s^4$ the upward longwave radiation flux from the ice surface. For simplicity, we assume that the thermal conductivity of sea ice k_i is constant and set $k_i = 2.03 \text{ W/(m} \cdot \text{K)}$ according to the 1-D thermodynamic sea-ice model of Maykut and Untersteiner (1971). During melting periods, the surface temperature is fixed at the bulk freezing temperature of the ice and the excess heat is used to melt ice at the surface. We assume the sea ice in our idealized model to be very fresh, using a freezing temperature of 0°C . At the ice bottom, the model calculates the change in ice thickness by balancing the conductive heat flux and the oceanic heat flux according to Eq. (??).

The seasonal variation of the atmospheric fluxes F_{sw} and F_{other} are prescribed according to the fits provided by Notz (2005), approximating the monthly-mean observational data compiled by Maykut and Untersteiner (1971). These fits are:

$$F_{sw} = A_1 \exp\left[B\left(\frac{d - C_1}{D_1}\right)^2\right] + E_1 \quad (2)$$

$$F_{other} = A_2 \exp\left[B\left(\frac{d - C_2}{D_2}\right)^2\right] + E_2 \quad (3)$$

where $A_1=19.5$, $A_2=117.8$, $B=-0.5$, $C_1=164.1$, $C_2=206$, $D_1=47.9$, $D_2=53.1$, $E_1=16.1$, $E_2=179.1$, and d is the number of the day in the year. The seasonal variation in surface albedo is calculated as

$$\alpha = \frac{F}{1 + \left(\frac{d - G}{H}\right)^2} + I \quad (4)$$

where F , G , H and I have the values of -0.431 , 207 , 44.5 and 0.914 , respectively. This equation is a fit to measurements obtained during the Surface Heat Budget of the Arctic Ocean (SHEBA) campaign (Perovich et al., 1999).

m l.126. The bulk freezing temperature of the ice should be defined.

We assume the sea ice in our idealized model is very fresh (Si=0 psu) and thus have a freezing temperature of 0 degree. Now we have added this point in the text (line 133-134).

n l.130. Numbers should be added for equations that appear after (5).

270 We have labelled the three equations as (6), (7), and (8).

o l.147: “the so-called CCSM3 set-up”. This is not a commonly know term. The set-up should simply be defined. There are a lot of acronyms in the paper that are used and not defined. Acronyms should be defined when they first appear.

Thanks. According to the comment, we now give full definitions for all the acronyms when they first appear in the paper, such as:

275 National Center for Atmospheric Research (NCAR)
 Ocean Model Intercomparison Project (OMIP)
 Surface Heat Budget of the Arctic Ocean (SHEBA)
 The Los Alamos Sea Ice Model (CICE)

The Max-Planck-Institute Global Ocean/Sea-Ice Model (MPIOM)

280 p 1.153 Is the mixed-layer salinity held constant in all the models? This would have an impact on the freezing temperature, and therefore on the heat flux parameterizations. This should be discussed (though not necessarily in the methods section).

In SIM and CICE the mixed-layer salinity is held constant (34 psu). But in MPIOM and COSMOS the salinity is treated as a passive tracer thus can be changed due to oceanic or atmospheric processes. Now we have clarified this point in the updated version.

285 q 1.154 What climatological dataset is being referred to exactly? The reference to the dataset should be included here. The time period over which the climatology was calculated should also be stated.

We now add in the paper (line 196-201):

As atmospheric forcing, we use for our conceptual 1-D model equations (7) to (9), For CICE, we use the National Center for Atmospheric Research (NCAR) monthly-mean climatological data with $1^\circ \times 1^\circ$ resolution Kalnay et al. (1996). Input fields contain monthly climatological sea-surface temperature, sea-surface salinity, the depth of ocean mixed layer, surface wind speeds, 10 m air temperature, humidity and radiation for the time period of 1984-2007. For MPIOM, we use a GR30 (about 3°) horizontal resolution and 40 uneven vertical layers, forced by daily heat, freshwater and momentum fluxes as given by the climatological Ocean Model Intercomparison Project (OMIP) forcing (Röske, 2006).

r 1.166: The ice distribution parameter must be described. The paper should be stand-alone.

295 **We now updated the texts (line 170-173):**

The change in sea ice thickness and concentration can be calculated via two main ice distribution parameters as outlined by Notz et al. (2013), the first one is a so-called lead closing parameter which describes how quickly the sea ice concentration increases during new ice formation processes, and the other describes the change in ice-thickness distribution during melting.

300 s 1.188, 1.193: "We start with" is used twice.

We have rephrased the second sentence.

t 1.191: "which is set to either 35 or 70". This is redundant as the simulations are listed above.

For simplifying the text we have removed those words from the manuscript.

u 1.192: "no more changes from one year to the next." What were the initial changes?

305 **The initial ice thickness is 0.5 m in our idealized setup, which then changes with time due to the forcings applied. After several simulation years, the model finally ran into equilibrium. Since it is a simple 1-D model, there is no interannual variability in the final years. We found that after the simulation is in equilibrium, there are no changes from one year to the next.**

v 1.202: Why is the mixed-layer warming more slowly in SIM-2eq and 3eq? Is it that the ice cover is lost earlier when the sun is higher over the horizon? This should be stated.

310

Because in SIM-icebath the sea ice melts completely, so all the heat flux on ocean could directly lead to warming of sea water, while in in SIM-2eq and SIM-3eq, there are still remaining sea ice, so the heat flux is firstly used for melting of the sea ice.

Now we make this point clearer in the updated manuscript (line 224-228):

315 *" Once the ice in SIM-icebath is melted completely, the ocean temperature rises rapidly and quickly exceeds that in SIM-2eq and SIM-3eq. This can be explained by two facts: 1) in SIM-2eq and SIM-3eq, the sea ice reflects most of the incoming shortwave radiation, and 2) in SIM-2eq and SIM-3eq the heat flux absorbed by open water is primarily used for sea-ice melting, while in SIM-icebath no more sea ice exists such that the entire heat flux into the ocean causes a warming of the sea water. "*

320 w 1.208: The word "faster" should be used instead of "stronger" when describing "ice melt".

We have changed the term to "faster".

x Section 4.2: This subsection consists of a single paragraph that is approximately one page long. It should be broken into several paragraphs for clarity.

Thanks for the comment. We have divided it into 5 paragraphs. We refer to section 4.2 in our revised paper.

325 y 1.240. The student's t-test should be more clearly described. Is it testing that the results from two different parameterizations are significantly different?

Yes. We have clarified this in the revised paper (line 264-266).

z Figures: Units and labels should be included on all figures. Fig.1. Units are missing. Fig.3-4. A larger font size for longitudes and the colorbars should be used. Fig.6-7. Units are missing for depth on the y axis. Fig.6-7. The seabed should appear in grey or a different color to differentiate it from zero in the water. Table 1: The parameter R should be defined/included in the Table caption. Currently, it is only defined later on 1.192

330 **According to the comment, we have updated the figures in the revised manuscript.**

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Response letter to Reviewer 2

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Review of Sensitivity of Northern Hemisphere climate to ice-ocean interface heat flux parameterizations by Shi et al

This paper presents the impact of various ice-ocean heat flux parameterization on several aspects of the climate of the Northern Hemisphere within four models of increasing complexity. The paper is clearly laid out. I find the analysis ambitious and interesting but would need some clarifications to be satisfied of its robustness and significance. I am also curious as to the chosen focus on this process (among so many others). I suggest major corrections (see below) before the paper can be accepted for publication.

Dear Reviewer,

Thanks so much for your constructive comments. In the following we present our point-to-point responses. Our answers to your comments are written in bold.

10 **Thanks again for your time and efforts.**

Best, Xiaoxu

1 General comments:

1) The fixed depth mixed layer model in the 1D and stand-alone models is a clear simplification that could affect the key results. For example a thinner mixed layer warms up more under fragmented ice in summer and I expect this to really influence your conclusions. Please discuss and provide additional information.

We agree with the reviewer. The prescribed ocean mixed layer depth in the 1-D and stand-alone sea ice models is a simplification. This is why we also used ice-ocean model and earth system model to perform the sensitivity experiments. In this revision, we also used the 1-D model to conduct a series of sensitivity studies to test the response of ice-ocean heat flux to the choices of mixed layer depth or friction velocity.

20 **The following texts can also be found in the revised manuscript at line 238-248.**

To quantify the different response of the simulated sea-ice cover for a larger range of forcing conditions, we carried out a series of sensitivity studies. For each of these, we varied one of the forcing parameters and analysed the difference in annual mean ice-ocean heat flux between SIM-3eq35 and SIM-icebath.

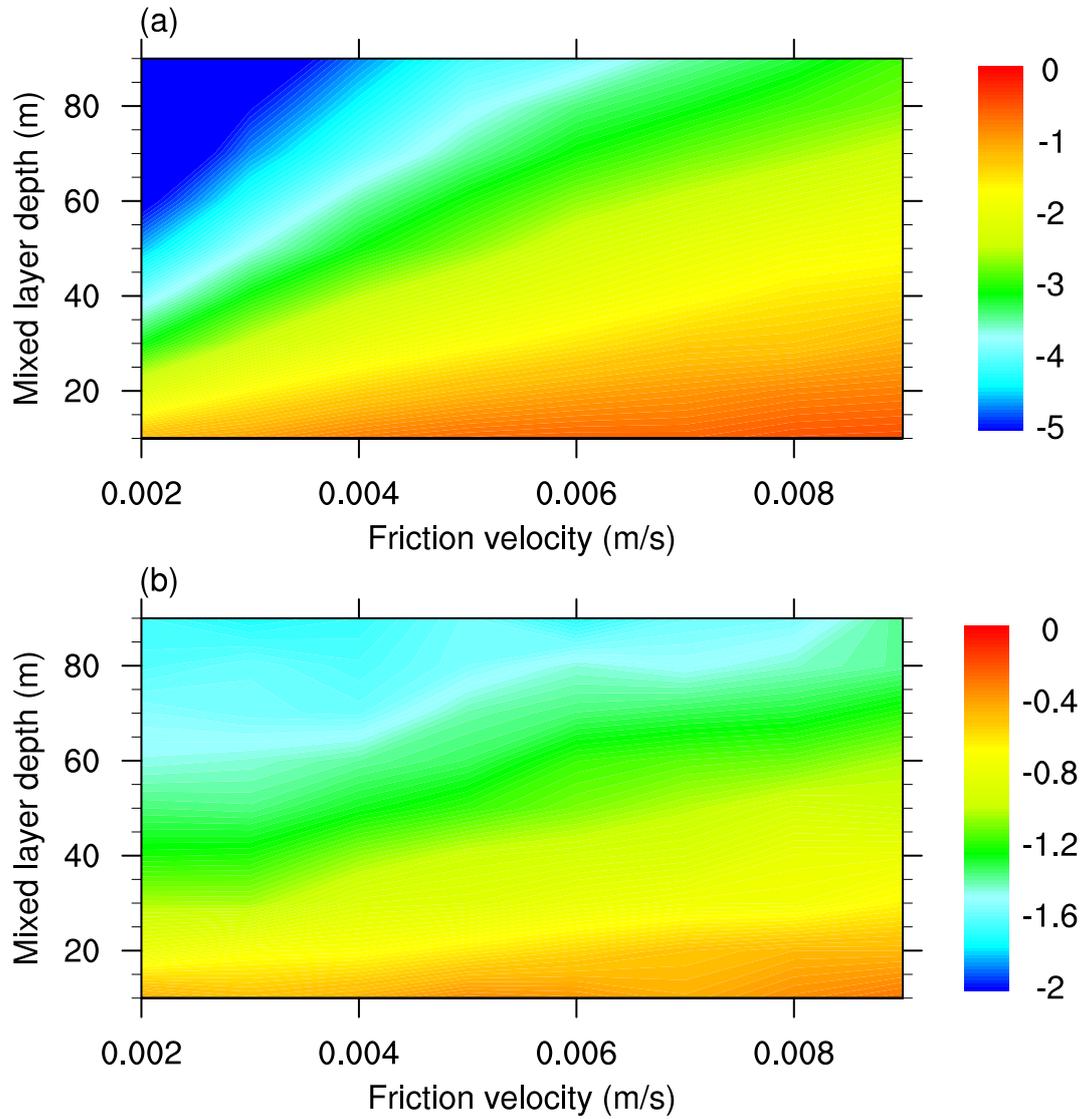


Figure 1. Anomalies of ocean-to-ice heat flux in SIM for (a) 3-equation minus icebath, and (b) 3-equation minus 2-equation, for different choices of mixed layer depth and friction velocity. Units are W/m^2 .

25 *We find that in our simplified setup, differences in ice thickness between SIM-3eq35 and SIM-icebath increase with mixed layer depth. This is due to the fact that the same amount of heat input causes a smaller temperature change for a deeper mixed layer. According to equation 3, a smaller temperature change then leads to a smaller change in heat flux to the ice bottom (Fig. 1).*

30 *In addition, we find that the anomaly in sea ice thickness generally decreases with friction velocity. This is related to the fact that for larger friction velocity, more heat is transported to the ice-ocean interface in the 3-equation setup (Fig. 1), which enhances sea-ice melt.*

2) I would like clarification on how the ice-bath model can be implemented in the ice-ocean coupled models.

In ice-ocean models, in all grid cells covered by sea ice, one usually simply resets the temperature of the sea water in the uppermost grid cell to its freezing point. All excess heat released during this adjustment is used to ablate sea ice.

35 *Now we clarify it in more detail in the revised manuscript (line 173-178): "In its standard setup, MPIOM uses an ice-bath parameterization to calculate the heat flux between the ocean and the ice. Wherever covered by sea ice, the temperature of sea water in the uppermost grid cell is kept at its freezing point. All heat entering the uppermost grid cells either from the atmosphere or from the deeper oceanic grid cell is instantaneously transported into the sea-ice cover, maintaining the temperature of the uppermost oceanic layer at the freezing point. In the present study, this formulation is either used directly, or replaced by the 2-equation or the 3-equation parameterization."*

40 3) Elaborate on the mechanisms that explain the weakening of the THC.

The weakening of the AMOC in the ice-bath and 2eq as compared to 3eq35 is mainly affected by the NAO changes. In the revised paper, we added a section to describe the relationship between NAO and AMOC (line 357-380):

45 *In this section, the mechanism explaining the weakening AMOC in COSMOS-icebath and COSMOS-2eq as compared to COSMOS-3eq35 is explored. It has long been recognized that the NAO variability has an important influence on the AMOC (Curry et al., 1998; Delworth and Zeng, 2016). Variations in the NAO have been hypothesized to play a role in AMOC variations by modifying air-sea fluxes of heat, water, and momentum. A similar relationship between NAO and the AMOC has been reported also for past climate conditions (Shi and Lohmann, 2016; Shi et al., 2020). Here in Fig.11 we show the results from a composite analysis between the NAO index and the anomalies in mixed layer depth based on COSMOS-3eq35. It is calculated by averaging March mixed layer depth anomalies (departure from the mean state) during years when the NAO index exceeds one standard deviation.*

55 *The convective activities in the Labrador Sea and the Greenland-Iceland-Norwegian (GIN) Seas are shown to have important contributions to the production and transport of North Atlantic deep water (Fig.11a). For comparison we also show the distribution of mixed layer depth in MPIOM-3eq35 in Fig. S3, which indicates a different location of main deep water convection site in our ice-ocean coupled model: the northeastern North Atlantic. The results from the composite analysis shown in Fig.11b indicate that the anomalous NAO pattern can lead to significant changes in the ocean circulation. We find that the intensity of the Labrador Sea convection is characterized by variations that appear to be synchronized*

with variabilities in the NAO. Therefore, the weakening of AMOC in our simplified setups compared to the most realistic approach can be attributed to the simulated anomalous negative NAO phase.

60 *The NAO affects the sea water convection mainly via modifying the surface heat fluxes which leads to anomalies in the spatial and vertical density gradient. Fig.12a shows the composite map between surface heat flux anomalies and the NAO index. During the positive phase of NAO, more heat than usual is removed from the ocean to the atmosphere at the western Atlantic, in particular the Labrador Sea. Such pattern is in good agreement with the NAO-relative heat flux anomalies derived from the European Centre for Medium-Range Weather Forecasts (ECMWF) interim reanalysis (Delworth and Zeng, 2016). The enhanced removal of heat favors an increase in the surface density and thereby strengthens deep water*
65 *formation. On the other hand, the NAO also affects the net precipitation over North Atlantic Ocean. As illustrated in Fig.12b, relatively drier condition could occur over Labrador Sea and Irminger Sea during positive NAO years. .*

4) How does the mixed layer look like in the ice-ocean coupled models (i.e. depth,...)

Following this comment, we now show the mixed layer depth of MPIOM in the Supplementary Fig. S3.

In the revised paper we added (line 365-368):

70 *" The convective activities in the Labrador Sea and the Greenland-Iceland-Norwegian (GIN) Seas are shown to have important contributions to the production and transport of North Atlantic deep water (Fig. ??a). For comparison we also show the distribution of mixed layer depth in MPIOM-3eq35 in Fig. S3, which indicates a different location of main deep water convection site in our ice-ocean coupled model: the northeastern North Atlantic. "*

5) Scales on figures are chosen to essentially show the sign but not so much the magnitude of the differences (i.e, one can
75 tell where ice is thicker or thinner but not by how much). Is that to hide the large differences that cannot be easily explained between model setups?

The blue-red color-bar was chosen as it represent clearly the sign of the changes. In the revised version we have chosen a different color-bar so the magnitude of the anomalies can be more easily read. Here we refer to the figures in the updated manuscript.

80 6) If the mixed layer temperature is so critical in controlling the temperature of the deep waters then it is all the more important to give a convincing description of its evolution and realism

Following the reviewer's comment, we now plot the anomalies of mixed layer temperature, as seen in Fig. 2 and Fig. 3 in the present response letter. We find the patterns are very similar to the SST anomalies as shown in the manuscript. As the sea water in the mixed layer is well mixed, it is not surprising that the mixed layer temperature anomalies mimic
85 that of the SST.

7) A comparison with Tsamados et al (2015) would be useful especially as the author of this study found a small impact of the 3eq BC. Discuss

Thanks for the comment, now we mention the study by Tsamados et al (2015) in the introduction and discuss it in the discussion section:

90 In introduction (line 92-105):

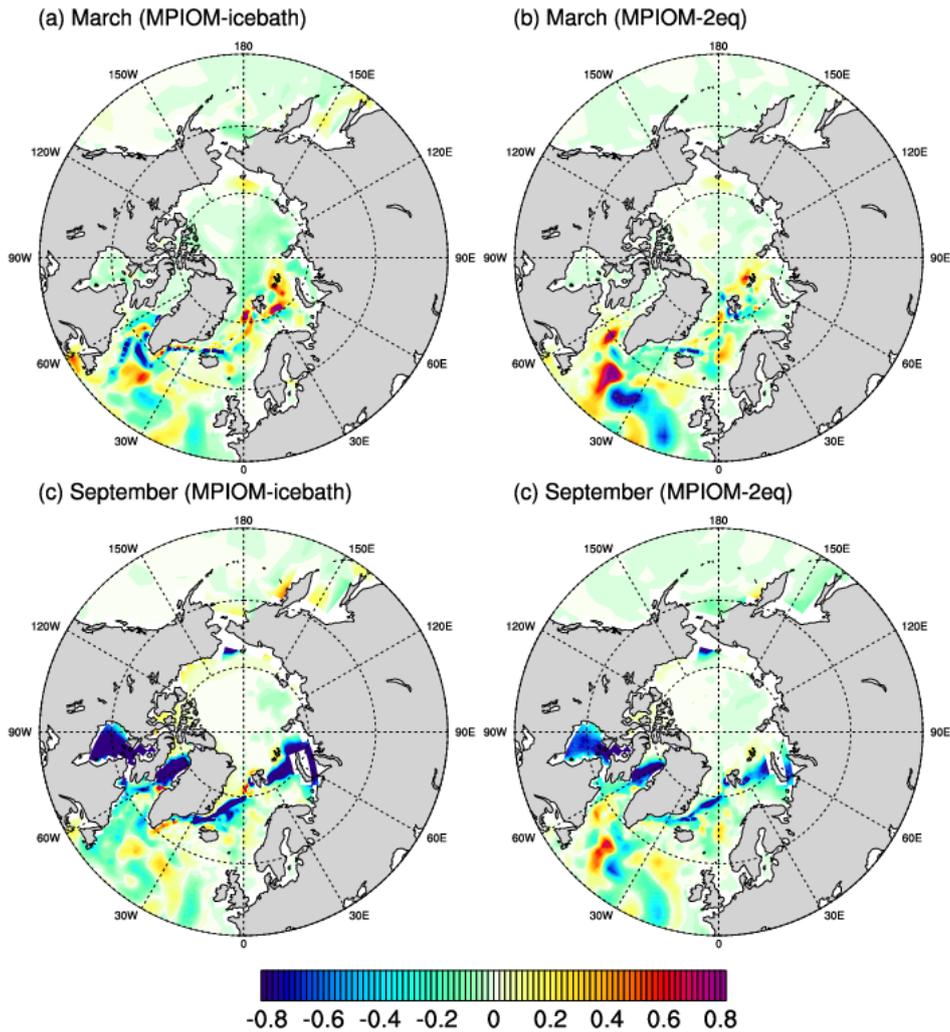


Figure 2. Anomalies of mixed layer temperature for (a) MPIOM-3eq35 minus MPIOM-icebath in March, (b) MPIOM-3eq35 minus MPIOM-2eq in March, (c) MPIOM-3eq35 minus MPIOM-icebath in September, and (d) MPIOM-3eq35 minus MPIOM-2eq in September. Units: K.

Exploring the behavior of different parameterizations describing ice-ocean heat flux has been an important topic in model studies. Significant differences can generally exist between melt rates calculated with the 3-equation approach and less realistic approaches (c.f. Notz et al., 2003; Tsamados et al., 2015), as only the 3-equation approach allows for heat fluxes that are directed from the interface into the water and therefore allows for a realistic limitation of melt rates through the formation of a fresh water layer underneath the ice. In a recent study the sensitivity of sea ice simulation to the approaches

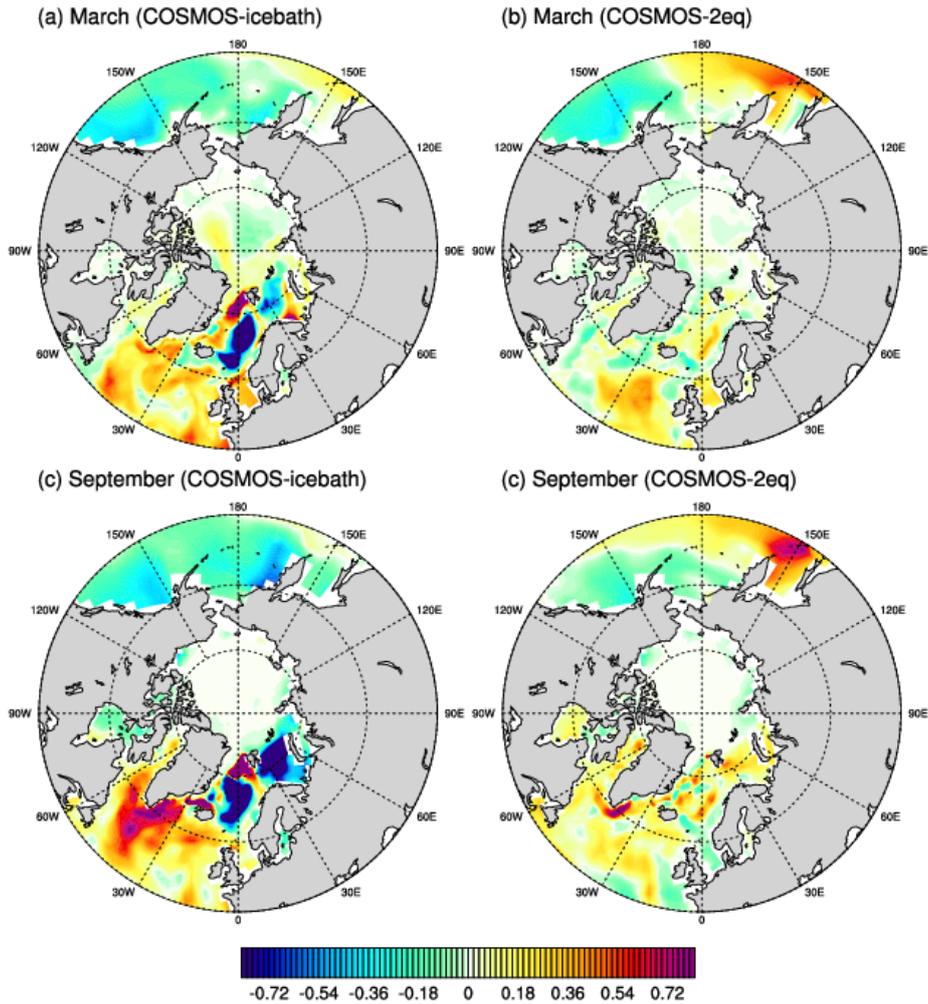


Figure 3. As in Fig. 2 but for COSMOS.

introduced in McPhee (1992) and Notz et al. (2003) have been examined using a stand-alone sea ice model CICE (Tsamados et al., 2015). CICE uses a simple thermodynamic slab ocean with fixed mixed layer depth and sea water salinity. Thus, the realistic effect of oceanic processes can not be represented. For example the sea ice over the Southern Ocean is severely overestimated by CICE due to a lack of warming effect from the Antarctic deep water. Therefore it is necessary to also investigate the ice-ocean heat flux formulations in a more complex system, including an interactive ocean or even the atmosphere. Based on this motivation, in the present study, we examine how different physical realism that is represented by the three discussed parameterizations impact the resulting ice cover, large-scale oceanic circulation, and atmosphere

properties in different numerical models ranging from an idealized columnar model, a stand-alone sea ice model, an ice-ocean coupled model, to a most complex climate system model.

105 **In the discussion we add (line 400-406):**

Note that our results are in good agreement with a previous study using CICE (Tsamados et al., 2015) that found in August stronger basal -melting of Arctic sea ice, decreased Arctic Ocean salinity, cooling of sea water in the central Arctic and warming of sea water at the ice edge in the 2-equation experiments compared to the 3-equation approach. However, in their study the effects are more pronounced, possibly because we used different model versions of CICE and different
110 *parameters for the ice-ocean heat flux formulations, one example is the value for R, which is 50 in Tsamados et al. (2015) and 35 in our case. In addition, different atmospheric forcings were used in the two studies.*

8) Is the most advanced thicker because of the reduced (even reversed) summer fluxes from the ocean to the ice? Again why is this results not so marked in Tsamados et al(2015)

Thanks for the comment. In fig.6 and fig.9 of Tsamados et al(2015), we can see that our results regarding the bottom
115 **melt and thickness of sea ice are identical. Both our studies indicate reduced sea ice when using the 2-eq rather than the 3-eq approach. This is due to a larger bottom melt rate in the 2-eq experiment. From fig.9 of Tsamados et al(2015), we see that the anomaly of summer sea ice thickness in 2-eq as compared to 3-eq is up to -0.25 m, while in our study the maximum change is -0.1 m (Fig. 2d in the manuscript). Therefore actually Tsamados et al(2015) shows a stronger change than our study does. Another thing to be noted is that Tsamados et al(2015) and our study use different values**
120 **for the exchange coefficients for salinity and heat, which is R=50 in Tsamados et al(2015), while we have R=35. Now we discuss this point in the discussion (line 400-406):**

Note that our results are in good agreement with a previous study using CICE (Tsamados et al., 2015) that found in August stronger basal -melting of Arctic sea ice, decreased Arctic Ocean salinity, cooling of sea water in the central Arctic and warming of sea water at the ice edge in the 2-equation experiments compared to the 3-equation approach. However,
125 *in their study the effects are more pronounced, possibly because we used different model versions of CICE and different parameters for the ice-ocean heat flux formulations, one example is the value for R, which is 50 in Tsamados et al. (2015) and 35 in our case. In addition, different atmospheric forcings were used in our studies.*

9) I am really uncertain as to the significance of the impacts found on the ocean and atmosphere. How does this compare to internal variability within the models? I have heard in the past Notz state that sea ice physics does not play a significant role in
130 the climate response (I might be misquoting and apologies if I do) but how do these finding square with this view? 10) Are the results presented reproducible. What if you analysed another 10 years or 100 years period?

Thanks, here we answer comments 9 and 10 together, as they both point to the significance of our results. We agree that showing the robustness of the results is crucial. To examine the significance of our results, we have performed a Student t-test which takes the internal variability into consideration. In the anomaly plots, we marked the areas with
135 **significant level higher than 95 percent with black dots. As seen from those figures, our main results are beyond the internal variability of the climate. For the sea level pressure pattern, no statistical significant changes are found, as the**

SLP variability is very large. Therefore we analyzed another 100 years of the simulation, and found consistent pattern as in the last 100 model years. These give us the confidence in the robustness of our results. (Note from Dirk Notz: I often say that in my view, in current models one primarily needs to improve the atmospheric/oceanic forcing in order to improve the simulation of the sea ice cover. In the opposite direction, things are less clear cut as indicated by the debate on the impact of sea-ice loss on Mid-Latitude weather patterns. However, also here in my view the impact of sea ice on atmospheric processes is small compared to internal variability, consistent with what we find here. For the ocean, I don't think I ever intended to say that the role of sea ice is negligible or the like, primarily because of its impact on watermass-transformation.)

11) I wonder why you do not use the same setup to analyse several other sea ice processes (albedo, melt pond, form drag, as per the recipe of Tsamados et al 2015 etc....). Is it too good to be true?

We agree with the reviewer that there are many other interesting processes/parameters that deserve being examined. However, the focus of this study is the impacts of different parameterizations of ice-ocean heat exchange on simulated ice thickness, ice concentration, and water masses in a hierarchy of models, 1D sea ice model, basin-scale stand-alone sea ice model, ice-ocean coupled model, and fully coupled model.

Our work started in the year 2011, therefore most of the simulations were performed before the publication of Tsamados et al (2015). We used a super long time to put everything together into a complete paper. The initial idea of our work is based on my interest on the 3-eq heat flux parameterization as described in Notz et al (2003), that is why I came to Germany and work with Prof. Notz on the topic. We are also interested in applying various approaches describing various processes (albedo effect, lateral melting, top melting, form drag...) into various models. This could be our next step.

12) Not clear how the prescribed atmospheric forcing subdues the impact on AMOC. Please elaborate.

The AMOC consists of wind-driven circulation (WDC) and thermohaline circulation (THC). The atmospheric process over North Atlantic plays an important role on determining the AMOC state. One of the key elements controlling the atmospheric circulation over the North Atlantic is NAO. As discussed in our paper (as well as many other papers), the positive phase of NAO leads to stronger deep mixing at the North Atlantic subpolar regions. But in ice-ocean model, as the atmosphere are prescribed, there is no difference in the atmospheric state between different experiments. Therefore, the change of AMOC in the MPIOM simulations can only be affected by thermohaline state, while in COSMOS runs both atmospheric and thermohaline conditions play a role.

We have discussed this point in the discussion section (line 416-420).

"As indicated in the present paper and many other studies (Curry et al., 1998; Latif et al., 2006; Sun et al., 2015), the AMOC is closely related to the atmospheric processes over North Atlantic Ocean. One of the key elements controlling the atmospheric circulation over the North Atlantic is the NAO. As the atmospheric forcings are prescribed in MPIOM, there is no difference in the atmospheric state among the MPIOM experiments. Therefore, the prescribed atmospheric forcing largely limits the air-sea interaction feedback."

2 Specific comments:

P1 L18 expand on motivation and justification

We now expand our motivation and justification in the end of introduction (line 92-105):

175 *Exploring the behavior of different parameterizations describing ice-ocean heat flux has been an important topic in model studies. Significant differences can generally exist between melt rates calculated with the 3-equation approach and less realistic approaches (c.f. Notz et al., 2003; Tsamados et al., 2015), as only the 3-equation approach allows for heat fluxes that are directed from the interface into the water and therefore allows for a realistic limitation of melt rates through the formation of a fresh water layer underneath the ice. In a recent study the sensitivity of sea ice simulation to the approaches introduced in McPhee (1992) and Notz et al. (2003) have been examined using a stand-alone sea ice model CICE (Tsamados*
180 *et al., 2015). CICE uses a simple thermodynamic slab ocean with fixed mixed layer depth and sea water salinity. Thus, the realistic effect of oceanic processes can not be represented. For example the sea ice over the Southern Ocean is severely overestimated by CICE due to a lack of warming effect from the Antarctic deep water. Therefore it is necessary to also investigate the ice-ocean heat flux formulations in a more complex system, including an interactive ocean or even the atmosphere. Based on this motivation, in the present study, we examine how different physical realism that is represented*
185 *by the three discussed parameterizations impact the resulting ice cover, large-scale oceanic circulation, and atmosphere properties in different numerical models ranging from an idealized columnar model, a stand-alone sea ice model, an ice-ocean coupled model, to a most complex climate system model.*

P1 L20 clarify this paragraph. Which freezing temperature...

We mean the freezing point of the uppermost cell itself. Here we improved the texts:

190 *The temperature of the uppermost ocean grid cells is fixed at its freezing temperature.*

P1 L27 Here is a good place to expand on the analogy and differences between momentum and heat transfer and write the equations and if need be criticise what is missing in either of them. At the moment it is too vague. For example what do you ‘differs from the exchange of momentum’ in what way?

At line 42-47:

195 *These measurements demonstrate that in particular during melting, the exchange of scalar quantities such as heat and salt differs significantly from the exchange of momentum. The reason for this lies in the fact that, unlike ice-ocean momentum flux, heat and mass transfer are strongly affected by a thin sublayer controlled by molecular processes (McPhee et al., 1987). Consistent with laboratory studies of heat transfer over hydraulically rough surfaces (Yaglom and Kader, 1974), the heat exchange is hence not only determined by turbulent processes but also by diffusion through this molecular sublayer.*

200 P2 L42 a local phase

Thanks for the correction. We have modified the text.

P2 L50 , Tsamados et al (2015)

We have added the reference.

P4 L85 together with the freezing equation(1)

205 **We have modified the text accordingly.**

P4 L 91 2003) and as implemented in CICE by Tsamados et al (2015)

Thanks for providing the reference, we are glad to cite Tsamados et al (2015) in our revised paper.

P5 L137 fixed mixed layer depth?

Yes. Our SIM is a simple 1-D sea ice model with a fixed-depth mixed layer.

210 P6 L141 version? Expand + maybe

We used the 4.0 version, we now clarify this point in the paper (line 146-151):

We use the 4.0 version of the stand-alone sea ice model CICE to investigate the sensitivity of sea ice to the three ice-ocean heat flux parameterizations in a modern sea-ice model. The model consists of a multi-layer energy-conserving thermodynamic sub-model (Bitz and Lipscomb, 1999) with a sub-grid scale ice-thickness distribution, and a submodel of ice dynamics

215 *based on an elastic-viscous-plastic rheology (Hunke and Dukowicz, 1997; Hunke, 2001) that uses incremental remapping for ice advection (Lipscomb and Hunke, 2004). A detailed model description is given in Hunke and Lipscomb (2010).*

P6 L150 again default mixed layer of fixed depth. Not realistic, this affects your Tmix and hence your results. P6L153 same issue with salinity should change with mixed layer depth

We agree, in an ice-ocean model like the MPIOM the salinity changes with ocean depth, and the depth of the mixed

220 **layer is not fixed. What is described here is the stand-alone sea ice model CICE. It has only one ocean layer (a slab-ocean), and in its standard setup, 34 psu is used for the ocean salinity. That is one of the reasons why we also tested the 3 parameterizations in more complex models such as MPIOM and COSMOS. This is also a highlighting point of our study, as most previous studies on testing sea ice parameterizations were only based on stand-alone sea ice models.**

We talked about this point in the introduction section (line 97-101): "CICE uses a simple thermodynamic slab ocean

225 **with fixed mixed layer depth and sea water salinity. Thus, the realistic effect of oceanic processes can not be represented. For example the sea ice over the Southern Ocean is severely overestimated by CICE due to a lack of warming effect from the Antarctic deep water. Therefore it is necessary to also investigate the ice-ocean heat flux formulations in a more complex system, including an interactive ocean or even the atmosphere."**

P6 L160 expand

230 **Thanks for the suggestion, we now expand the description for MPIOM (line 162-165):**

MPIOM is based on the primitive equations with representation of thermodynamic processes (Marsland et al., 2003). The orthogonal curvilinear grid is applied in MPIOM with the north pole located over Greenland. The relevant terms of the surface heat balance are parameterized according to bulk formulae for turbulent fluxes (Oberhuber, 1993), and radiant fluxes (Berliand, 1952).

235 P6 L165 The repartition? Rephrase slightly

We improved the text to let it be more understandable (line 170-173):

240 *The change in sea ice thickness and concentration can be calculated via two main ice distribution parameters as outlined by Notz et al. (2013), the first one is a so-called lead closing parameter which describes how quickly the sea ice concentration increases during new ice formation processes, and the other describes the change in ice-thickness distribution during melting. "*

P6 L169 wouldn't it better to have it at 1 deg and run for 100 years? Or is that needed for equilibration?

For ice-ocean model, a equilibrium-state requires a stable AMOC, which normally needs a simulation time of several centuries. That's why we run both MPIOM and COSMOS for 1,000 years.

245 **Regarding the spatial resolution, we choose GR30 to be consistent with COSMOS, as in COSMOS the standard setup of spatial resolution is GR30. This also helps us to save computing resources.**

P8 L187 and ice concentration P8 L210 more slowly P10 L221 a smaller...for a deeper... P10 L226 are larger...

Thanks, we have corrected the above mentioned grammar errors.

P10 L238 I am surprised that you needed a 90 years spin-up for a stand-alone sea ice model.

250 **We let all models run at least 100 simulation years, although the stand-alone sea ice model reach the equilibrium in a few years of integration. For more complex models we run the simulations for 1,000 years.**

P13 L257 what do you mean by far-field? Mixed layer? Also typo...at the interface

Sorry for the confusion. We mean "the uppermost ocean layer". We have corrected this as well as the typo.

P13 L268 I am not clear on how you can obtain an ice bath situation in the ice-ocean coupled models

MPIOM and COSMOS originally uses the ice-bath assumption.

255 **Now we clarify it in more detail in the revised manuscript (line 173-177): " In its standard setup, MPIOM uses an ice-bath parameterization to calculate the heat flux between the ocean and the ice. Wherever covered by sea ice, the temperature of sea water at the uppermost grid cell is kept at its freezing point. All heat, coming from above atmosphere or deeper ocean, will then be instantaneously transported to sea ice, thus keeping the first-layer temperature unchanged. In the present study, this formulation is either used directly or replaced by the 2-equation or the 3-equation parameterization."**

260 P13 L269 how significant is this cooling in COSMOS? How does it compare to model internal variability for example?

To test the significance level of the anomalies, we performed Student t-test. In the revised plots, the areas with significant changes (significance level > 95%) are marked with dots. As shown in figure 4i-k, the cooling of the North Atlantic in COSMOS is significant (marked with black dots), and thus the anomalies are beyond the internal variability. However, in Fig.4l, the cooling over North Atlantic in September between 2eq and 3eq35 is not statistically significant.

265 Fig5 why don't you show CICE?

CICE is a stand-alone sea ice model which includes only a slab ocean mixed-layer parameterization, but the salinity of the ocean is kept constantly at 34 psu. That is why it is not necessary to show the salinity change for CICE. The salinity anomaly should be 0 everywhere in CICE.

P13 L274 doesn't less ice mean more growth in winter(negative feedback) and hence more brine release?

270 According to the reviewer's comment, I think we shall use "larger melting rate" rather than "reduction in sea ice thickness" here, as the salinity of the sea water responds to the change of sea ice, instead of the absolute value of sea ice.

Now we have corrected this point in the manuscript (line 298-301).

275 *"In regions in which the ice-bath approach or the 2-equation approach cause an increased heat flux to the ice underside, and hence a larger melting rate of sea ice in summer as well as a smaller growth rate in winter, the ocean is generally less salty in these simulations with a simplified parameterization of ice-ocean heat exchange than in the simulations with the full 3-equation parameterization."*

P13 L280 the small differences between COSMOS-2eq and COSMOS-3eq35 indicates that once mixed layer allowed to evolve impact of this parameterisation is small?

Regarding the small differences in COSMOS, we have discussed in the discussion section (line 421-428):

280 *"Our study indicates a less pronounced sea-ice response to ice-ocean interface heat flux parameterizations in the fully coupled climate model COSMOS than in the ice-ocean model MPIOM (compare Fig.3e-h with Fig.3i-l). This is because the change of the AMOC has a dampening effect on the simulated sea ice anomalies. The strengthening of the AMOC in COSMOS-3eq can lead to a warming over the Northern Hemisphere, especially over the North Atlantic and the Arctic. This hypothesized link between the AMOC and Northern Hemisphere mean surface climate has been documented in an abundance of studies (e.g., Schlesinger and Ramankutty, 1994; Rühlemann et al., 2004; Dima and Lohmann, 2007; Parker et al., 2007). The AMOC-induced warming helps to reduce the sea ice mass over the Arctic and North Atlantic subpolar regions. Indeed, the sea ice across the Greenland Sea and Baffin Bay are found to be thinnest in COSMOS-3eq."*

P13 L278 I don't get this explanation

290 Interestingly, the opposite sign is observed in the Barents sea and its adjacent regions (Fig.6e-f), despite the larger melt rates in the ice-bath scheme. This is likely due to sea ice dynamic processes. The interannual variability of sea ice volume in the Barents sea and its adjacent regions is mainly determined by variations in sea ice import from the Central Arctic, rather than the local thermodynamic change of sea ice (Koenigk et al., 2009). Since less Arctic sea ice is simulated in COSMOS-icebath, less sea ice volume is transported to the subpolar regions in the experiment with ice-bath parameterization. However, it is just a speculation. The sea ice dynamic process in our simulations needs further investigation. Therefore in our revised paper, we removed this part and we will have a more detailed analysis on the sea ice dynamics in the future.

P17 L288 where are these regions of deep water formation?

Thanks, we mean the marginal ice zone. We now corrected the texts (line 311-313):

"This warming in the simulations with the least realistic parameterization of ice-ocean heat exchange reflects its earlier ice loss in the marginal ice zone."

300 P17 L289 I am not sure I follow why thinner means fresher mixed layer. The system rapidly equilibrates to a thinner state and then no reason to have fresher ML

Thanks for the comment. We agree on that. At the same time, the system also equilibrates to a state with more summer ablation of sea ice. This effect dominates the change in salinity. So it is the change in the melting rate rather

than the sea ice thickness that leads to sea water freshening. Now we have corrected this in the updated manuscript
305 (line 314-316):

"As the simplified parameterizations both lead to faster melting rate of sea ice at the Arctic Ocean in summer, and less growing rate of sea ice in winter, as compared to the most realistic approach, one would expect a freshening of the ocean mixed layer and the deep water mass that originates from such fresher surface source water."

P17 L293 could it be because these results are coincidental

310 **The anomalies are statistically significant as they pass 95% significance level based on Student's t-test. On the other hand, the anomaly patterns from ice-bath and 2-eq experiments are identical, only with different magnitudes.**

Fig S2 caption -> departure from

Thanks, we have corrected the typo in the revised version.

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Sensitivity of Northern Hemisphere climate to ice-ocean interface heat flux parameterizations

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Abstract. We investigate the impact of three different parameterizations of ice-ocean heat exchange on modeled ~~ice thickness~~, ~~ice-sea-ice thickness~~, ~~sea-ice~~ concentration, and water masses. These three parameterizations are (1) an ice-bath assumption with the ocean temperature fixed at the freezing temperature; (2) a 2-equation turbulent heat-flux parameterization with ice-ocean heat exchange depending linearly on the temperature difference between the ~~mixed-layer underlying ocean~~ and the ice-ocean interface, ~~whose temperature is kept at the freezing point of the sea water~~; and (3) a ~~similar 3-equation~~ turbulent heat-flux ~~parameterization as (2) but with the temperature at the~~ approach in which the ice-ocean heat flux depends on the temperature difference between the underlying ocean and the ice-ocean interface ~~depending on whose temperature is calculated based on the local salinity set by the~~ ice-ablation rate. Based on model simulations with the standalone sea-ice model CICE, the ice-ocean model MPIOM and the climate model COSMOS, we find that compared to the most complex parameterization (3) ~~leads (in comparison to the other two parameterizations) to a thicker modeled~~, the approaches (1) and (2) result in thinner Arctic sea ice, ~~warmer-cooler~~ water beneath high-concentration ice and ~~cooler-warmer~~ water towards the ice edge, and ~~higher~~ a lower salinity in the Arctic Ocean mixed layer. In particular, parameterisation (1) results in the smallest sea ice thickness among the 3 parameterizations, as in this parameterisation all potential heat in the underlying ocean is used for the melting of the sea ice above. For the same reason, the upper ocean layer of the central Arctic is cooler when using parameterisation (1) compared to (2) and (3). Finally, in the fully coupled climate model COSMOS, parameterisations (1) and (2) result in a fairly similar oceanic or atmospheric circulation. In contrast, the most realistic parameterization (3) leads to an enhanced Atlantic meridional overturning circulation (AMOC), a more positive North Atlantic Oscillation (NAO) mode and a weakened Aleutian Low.

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20 1 Introduction

The growth and decay rate \dot{h} of sea ice at the ice–ocean interface are is determined by the local imbalance between imbalance of the conductive heat flux within into the ice and the oceanic heat flux from below F_{oce} from underneath the ice. Hence,

$$\rho_i L \dot{h}(t) = k_i \frac{\partial T}{\partial z} \Big|_{ice} + F_{oce}, \quad (1)$$

where ρ_i is the density of the ice, L is the latent heat of fusion, k_i is thermal conductivity of the ice, T is temperature and z is the vertical coordinate. Some simple sea-ice models assume that sea ice has no heat capacity and does not absorb solar radiation. In these so-called zero-layer models, the temperature gradient is constant and simply given as the temperature difference between the ice surface and the ice bottom, divided by ice thickness (Semtner Jr, 1976). In more advanced sea-ice models, the ice consists of several layers and the conductive heat flux into the lower most grid cell is explicitly calculated.

Because the temperature at the ice–ocean interface is determined by phase equilibrium, any imbalance between the two fluxes is not compensated by changes in the local temperature as is the case at the ice surface, but instead by ice growth or ablation. This makes the evolution of sea ice thickness very sensitive to small changes in oceanic heat flux (e.g. Maykut and Untersteiner, 1971). Thus/Therefore, a realistic parameterization of flux exchanges at the ice-ocean interface F_{oce} is important for simulating sea ice and its climate feedback.

A number of approaches exist for the calculation of the oceanic heat flux F_{oce} (c.f. Holland and Jenkins, 1999; Jenkins et al., 2001; Notz). For the simplest parameterization, the ice–ocean system is simply treated as an ice bath (e.f. Schmidt et al., 2004): The temperature of the uppermost ocean grid cells is fixed at the its freezing temperature, and any excess energy that enters these grid cells via advection, convection, or heat exchange with the atmosphere is instantaneously applied to the ice through lateral and bottom melting. Such/Hence, the oceanic heat flux is given as

$$F_{oce} = \frac{\rho_w c_w (T_{mix} - T_f) h_{mix}}{\delta t}, \quad (2)$$

where T_{mix} is ocean temperature, T_f is the salinity-dependent freezing temperature, ρ_w is the density of the sea water and c_w the specific heat capacity, all determined for the uppermost oceanic grid cell with vertical extent h_{mix} . δt is the time step.

The ice-bath parameterization is consistent with turbulence models that treat the flux of heat and salt as analogous to momentum flux (Josberger, 1983; Mellor et al., 1986), which results in very efficient transfer whenever the ice is in motion relative to the underlying water. However, the ice-bath paradigm is incompatible with observations (i.e., the 1984 Marginal Ice Zone Experiment (MIZEX)), which clearly indicate that an ice-covered mixed layer can store significant amounts of heat (i.e., remain above freezing) for extended periods of time (McPhee, 1986; MCPhee et al., 1987; Perovich and Maykut, 1990). These measurements demonstrate that in particular during melting, the exchange of scalar quantities such as heat and salt differs significantly from the exchange of momentum. The reason for this lies in the fact that, unlike ice-ocean momentum flux, heat and mass transfer are strongly affected by a thin sublayer controlled by molecular processes (McPhee et al., 1987). Consistent with laboratory studies of heat transfer over hydraulically rough surfaces (Yaglom and Kader, 1974), the heat exchange is hence not only determined by turbulent processes but also by diffusion through this molecular sublayer.

50 The fact that the oceanic temperature can be significantly higher than the freezing temperature even underneath a dense
ice cover cannot be represented in numerical models that employ an ice-bath assumption. More advanced formulations of
ice–ocean heat exchange are therefore based on bulk formula, where the ice–ocean heat exchange depends linearly on the
temperature difference between the mixed layer and the ice–ocean interface. Early models used a constant diffusion term as the
proportionality constant (Røed, 1984), while more advanced formulations made the heat exchange depend on friction velocity
55 as well (McPhee, 1992):

$$F_{oce} = -\rho_w c_w \alpha_h u_* (T_{mix} - T_{interface}), \quad (3)$$

where u_* is friction velocity and α_h is a turbulent heat exchange coefficient (McPhee et al., 2008). A number of different
formulations exist for the calculation of the interfacial temperature. Following Schmidt et al. (2004), these can be differentiated
between a 1-equation approach, a 2-equation approach and, most realistically, a 3-equation approach. In the 1-equation
approach, $T_{interface}$ is simply set to a constant value. We will not consider this approach any further here. In the more realistic
60 2-equation approach, $T_{interface}$ is set to the freezing temperature of the sea water in the upper-most ocean grid cell. Hence, in
addition to Eq. (3), the freezing-point relationship of seawater is also required, which is the second equation of the 2-equation
approach:

$$T_{interface} = -0.054 \cdot S_{interface} \quad (4)$$

For such more advanced formulations, measurements show proportionality between heat flux and temperature difference
times friction velocity across a large range of Reynolds numbers (e.g., Fig. 6.5 in MCPhee, 2008). These formulations form the
65 basis of many modern sea-ice models (e.g. Hunke and Lipscomb, 2010).

These formulations, despite being physically much more realistic than the crude ice-bath assumption, often suffer from the
fact that the temperature at the ice–ocean interface is simply set as the freezing temperature of the underlying sea water. In
reality, however, the interfacial temperature is determined by a local phase equilibrium, and in particular during periods of
high ablation rates, the local salinity at the interface can be significantly lower than the salinity of the sea water underneath.
70 The interfacial temperature can be significantly higher than the freezing temperature of the underlying sea water. Therefore,
one extension of the turbulent parameterizations of ice–ocean heat exchange lies in the explicit calculation of the tempera-
ture at the ice–ocean interface based on local salinity (Jenkins et al., 2001; Notz et al., 2003; Schmidt et al., 2004). Such
formulations then allow for the explicit calculation of heat and salt fluxes, and give a more realistic estimate of ice–ocean
heat exchange. In particular, these formulations allow for the ice–ocean interface to be warmer than the underlying sea water,
75 which allows for heat fluxes from the interface into the underlying ocean. This becomes ~~in particular important whenever~~
~~particularly important when~~ large amounts of meltwater accumulate underneath sea ice during summer (Notz et al., 2003)
(Notz et al., 2003; Tsamados et al., 2015).

~~In this study, we examine how different physical realism that is represented by the three discussed parameterizations impact
the resulting ice cover, large-scale oceanic circulation, and atmosphere properties in numerical models. The paper is organized~~

80 as follows. Section 2 describes the parameterizations in details. Section 3 introduces various models that we use for our
 purposes, including a conceptual 1-dimensional model that allows us to examine a wide parameter range, the standalone sea-ice
 model CICE that allows us to determine changes of sea ice in a modern sea-ice model, the ocean-sea-ice model MPIOM, which
 allows us to examine the impact of the parameterizations on the large-scale ocean circulation, and the fully coupled climate
 model COSMOS, which further helps us to look at the atmospheric response to the described parameterizations. Section 4
 85 describes results from sensitivity studies with using the various models. We discuss and summarize our main findings in
 section 5.

2 Heat flux parameterizations

The growth and decay rate \dot{h} of sea ice at the ice-ocean interface is determined by the imbalance of the conductive heat flux
 into the ice and the oceanic heat flux F_{oce} from underneath the ice. Hence,

$$90 \quad \rho_i L \dot{h}(t) = k_i \frac{\partial T}{\partial z} \Big|_{ice} + F_{oce},$$

where ρ_i is the density of the ice, L is the latent heat of fusion, k_i is thermal conductivity of the ice, T is temperature and z is the
 vertical coordinate. Some simple sea-ice models assume that sea ice has no heat capacity and does not absorb solar radiation. In
 these so-called zero-layer models, the temperature gradient is constant and simply given as the temperature difference between
 the ice surface and the ice bottom, divided by ice thickness (Semtner Jr, 1976). In more advanced sea-ice models, the ice
 95 consists of several layers and the conductive heat flux into the lower most grid-cell is explicitly calculated.

As discussed in the introduction, a number of approaches exist for the calculation of the oceanic heat flux F_{oce} . For the
 simplest, the ice-bath assumption, the temperature of the uppermost oceanic grid-cell is kept at the freezing temperature.
 Hence, the oceanic heat flux is given as

$$F_{oce} = \frac{\rho_w c_w (T_{mix} - T_f) h_{mix}}{\delta t},$$

100 where T_{mix} is ocean temperature, T_f is the salinity-dependent freezing temperature, ρ_w is the density of the sea water and c_w
 the specific heat capacity, all determined for the uppermost oceanic grid-cell with vertical extent h_{mix} . δt is the time step.

In more realistic formulations, the heat flux is determined from a bulk equation based on friction velocity and temperature
 difference between the mixed layer and the ice-ocean interface according to

$$F_{oce} = -\rho_w c_w \alpha_h u_* (T_{mix} - T_{interface}),$$

105 where u_* is friction velocity and α_h is a turbulent heat exchange coefficient (McPhee et al., 2008). A number of different
 formulations exist for the calculation of the interfacial temperature. Following Schmidt et al. (2004), these can be differentiated
 between a 1-equation approach, a 2-equation approach and, most realistically, a [In this most realistic](#) 3-equation approach. In
 the 1-equation approach, $T_{interface}$ is simply set to a constant value. We will not consider this approach any further here. In

the more realistic 2-equation approach, $T_{interface}$ is set to the set to the freezing temperature of the sea water in the upper-most ocean grid cell. Hence, in addition to Eq. (3), the freezing point relationship of seawater is also required, which is the second equation of the 2-equation approach. In the most realistic 3-equation approach, $T_{interface}$ is set to the freezing temperature of the water water that exists directly at the interface. The salinity of this water is explicitly calculated from a salinity-balance equation

$$(S_{interface} - S_{ice})\dot{h}(t) = \alpha_s u_* (S_{mix} - S_{interface}). \quad (5)$$

Here, $S_{interface}$ is the salinity directly at the interface, which decreases during melting through the addition of fresher melt water of sea ice with salinity S_{ice} . Salt is exchanged with the underlying water (with salinity S_{mix}) through turbulent exchange, with a salt exchange coefficient α_s . Together with the freezing point relationship equation 1 of sea water, Equations (3) and (5) form the three equations of the 3-equation approach. These three equations can be solved to calculate the three unknowns \dot{h} , $S_{interface}$ and $T_{interface}$.

~~As mentioned before, only the 3-equation approach allows for heat fluxes that are directed from the interface into the water. In addition, only the 3-equation approach allows for a realistic limitation of melt rates through the formation of a fresh water layer underneath the ice. For these reasons, significant differences can generally exist between melt rates calculated with the 3-equation approach and less realistic approaches (c.f. Notz et al., 2003).~~

Quantitatively, a value of $0.005 < \alpha_h < 0.006$ has been found to give good agreement between measured and calculated heat fluxes for a large spread of Rayleigh numbers (McPhee, 2008; MCPhee et al., 2008). More uncertainty exists regarding the most appropriate values for the turbulent exchange coefficients α_h and α_s for the 3-equation approach. Their ratio $R = \alpha_h/\alpha_s$ depends on the molecular diffusivities for heat and salt as well as on the roughness of the boundary (McPhee et al., 1987; MCPhee, 2008). Laboratory experiments ~~by Owen and Thomson (1963) and Yaglom and Kader (1974)~~ imply $35 \leq R \leq 70$ ~~(Notz et al., 2003)~~ (Owen and Thomson, 1963; Yaglom and Kader, 1974; Notz et al., 2003). Sirevaag (2009) found from an analysis of field data, $R \approx 33$, while MCPhee et al. (2008) suggest a value of $R \approx 35$. ~~Here we assume that the 3-equation approach with $R = 35$ best describes reality and then perform model simulations based on this approach as our reference.~~

During freezing conditions, salt and heat are transported almost equally ~~effieient~~ efficiently (McPhee et al., 2008). This is because during freezing conditions, the water column is statically unstable owing to the salt release from growing sea ice. Hence, during freezing conditions, $R \approx 1$ (McPhee et al., 2008), and the 2-equation approach can be used without much loss in accuracy. Best agreement with observational data is then found for $\alpha_h = 0.0057$.

~~In testing the impact of the various parameterizations on modeled sea ice and ocean circulation, we therefore take the following approach: for the~~ Exploring the behavior of different parameterizations describing ice-ocean heat flux has been an important topic in model studies. Significant differences can generally exist between melt rates calculated with the 3-equation approach and less realistic approaches (c.f. Notz et al., 2003; Tsamados et al., 2015), as only the 3-equation approach allows for heat fluxes that are directed from the interface into the water and therefore allows for a realistic limitation of melt rates through the formation of a fresh water layer underneath the ice. In a recent study the sensitivity of sea ice simulation to the approaches introduced in MCPhee (1992) and Notz et al. (2003) have been examined using a stand-alone sea ice model CICE

(Tsamados et al., 2015). CICE uses a simple thermodynamic slab ocean with fixed mixed layer depth and sea water salinity. Thus, the realistic effect of oceanic processes can not be represented. For example the sea ice over the Southern Ocean is severely overestimated by CICE due to a lack of warming effect from the Antarctic deep water. Therefore it is necessary to also investigate the ice-ocean heat flux formulations in a more complex system, including an interactive ocean or even the atmosphere. Based on this motivation, in the present study, we examine how different physical realism that is represented by the three discussed parameterizations impact the resulting ice cover, large-scale oceanic circulation, and atmosphere properties in different numerical models ranging from an idealized columnar model, a stand-alone sea ice model, an ice-ocean coupled model, to a most complex climate system model.

Another motivation of our study is to help improve the formulation describing ice-ocean heat flux in various models. For example in the 4th version of CICE, only ice-bath parameterization, we simply incorporate Eq. (2). For the and 2-equation approach, we use Eq. (3) with $\alpha_h = 0.006$ and the freezing-point relationship for seawater. For the assumptions could be applied. In MPIOM and COSMOS, the ice-bath approach is used, which can lead to an overestimation of oceanic heat flux into sea ice. In our study we implemented the more realistic 3-equation approach, we differentiate between freezing and melting conditions. During melting, we use the full 3-equation approach with $R = 35$ as our reference. In an idealized 1-D model used in our study, $R = 70$ is also applied to test the sensitivity with respect to this parameter. For a certain value of R , we calculate α_h to satisfy the requirement described in McPhee et al. (1999). $R = 35$ is associated with a turbulent heat exchange coefficient of $\alpha_h = 0.0095$; and $R = 70$ with $\alpha_h = 0.0135$. During freezing, we fall back to the 2-equation approach. parameterization into all the models mentioned above.

The paper is organized as follows. Section 2 introduces various models that we use for our purposes: 1) A conceptual 1-dimensional model allows us to examine a wide parameter range. 2) The Los Alamos Sea Ice Model (CICE) allows us to determine changes of sea ice in a modern sea-ice model. 3) The Max-Planck-Institute Global Ocean/Sea-Ice Model (MPIOM) can be used for examining the impact of the parameterizations on the large-scale ocean circulation. 4) The fully coupled climate model COSMOS can further help us to look at the atmospheric response to the described parameterizations. Section 3 gives an overview of our experiment configuration. Section 4 describes results from sensitivity studies with using the various models. We discuss and summarize our main findings in section 5.

2 Models

We will now briefly introduce the four different models that we use to analyse the different response to oceanic heat-flux parameterizations based on the ice-bath assumption, the 2-equation approach and the 3-equation approach. We start with a description of our idealized columnar model with simple sea ice thermodynamics, then move to the stand-alone sea ice model CICE, and finally describe the ice-ocean-ice-ocean model MPIOM and a fully coupled model COSMOS, which consists of the oceanic component MPIOM the fully coupled ice-ocean-atmosphere model COSMOS.

2.1 Idealized 1-D model

We use a one-dimensional columnar sea-ice model coupled to a simple ocean mixed layer to carry out sensitivity studies and to investigate the impact of the three formulations for ice–ocean heat exchange in an idealised setup.

The model consists of a simple zero-layer sea-ice model, where the surface temperature T_s is determined by balancing atmospheric fluxes and the conductive heat flux through the ice according to

$$-(1-\alpha)F_{sw} - F_{other} + 0.95 \cdot 5.67 \times 10^{-8} T_s^4 = -k_i \frac{T_s - T_{bot}}{h}. \quad (6)$$

Here, α is the albedo of the ice surface, F_{sw} is the short-wave flux, $\epsilon = 0.95$ the infrared emissivity, $\sigma = 5.67 \times 10^{-8}$ the Stefan-Boltzman constant, T_{bot} the temperature at the ice-ocean interface, and F_{other} is the sum of sensible heat flux, latent heat flux and downward longwave radiation flux. $(1-\alpha)F_{sw} + F_{other}$ represents the heat input to the ocean, and $0.95 \times 5.67 \times 10^{-8} T_s^4$ the upward longwave radiation flux from the oceanice surface. For simplicity, we assume that the thermal conductivity of sea ice k_i is constant and set $k_i = 2.22$ W/(m·K) according to the 1-D thermodynamic sea-ice model of Maykut and Untersteiner (1971). During melting periods, the surface temperature is fixed at the bulk freezing temperature of the ice and the excess heat is used to melt ice at the surface. We assume the sea ice in our idealized model to be very fresh, using a freezing temperature of 0 °C. At the ice bottom, the model calculates the change in ice thickness by balancing the conductive heat flux and the oceanic heat flux according to Eq. (1).

The seasonal variation of the atmospheric fluxes F_{sw} and F_{other} are prescribed according to

$$F_{sw} = 19.5 \times \exp\left[-0.5 \times \left(\frac{d-164.1}{47.9}\right)^2\right] \times 16.1$$

the fits provided by Notz (2005), approximating the monthly-mean observational data compiled by Maykut and Untersteiner (1971)

These fits are:

$$F_{sw} = A_1 \exp\left[B\left(\frac{d-C_1}{D_1}\right)^2\right] \quad (7)$$

$$F_{other} = 117.8 \times \exp\left[-0.5 \times \left(\frac{d-206}{53.1}\right)^2\right] \times 179.1,$$

$$F_{other} = A_2 \exp\left[B\left(\frac{d-C_2}{D_2}\right)^2\right] + E \quad (8)$$

where

where $A_1=314$, $A_2=117.8$, $B=-0.5$, $C_1=164.1$, $C_2=206$, $D_1=47.9$, $D_2=53.1$, $E=179.1$, and d is the number of the day in the year. Following Notz (2005), these two equations are a fit to the monthly-mean data compiled by Maykut and Untersteiner (1971)

The seasonal variation in surface albedo is calculated as

$$\alpha = \frac{-0.431}{1 + \left(\frac{d-207}{44.5}\right)^2} + 0.914,$$

$$\alpha = \frac{F}{1 + \left(\frac{d-G}{H}\right)^2} + I \quad (9)$$

which where F , G , H and I have the values of -0.431, 207, 44.5 and 0.914, respectively. This equation is a fit to measurements obtained during the [SHEBA Surface Heat Budget of the Arctic Ocean \(SHEBA\)](#) campaign (Perovich et al., 1999).

200 The model is coupled to an idealised oceanic mixed layer of depth h_{mix} , which can store and release heat. The coupling between the mixed layer ocean and the sea ice via the oceanic heat flux F_{oce} is given by the three parameterizations as described before.

2.2 CICE

~~We use the stand-alone sea ice model CICE to~~ To investigate the sensitivity of sea ice to the three ice-ocean heat flux parameterizations in a modern sea-ice model, [we use version 4.0 of the stand-alone sea ice model CICE](#). The model consists of a multi-layer energy-conserving thermodynamic sub-model (Bitz and Lipscomb, 1999) with a sub-grid scale ice-thickness distribution, and a submodel of ice dynamics based on an elastic-viscous-plastic rheology (Hunke and Dukowicz, 1997; Hunke, 2001) that uses incremental remapping for ice advection (Lipscomb and Hunke, 2004). A detailed model description is given in Hunke and Lipscomb (2010).

210 The surface temperature of the ice is calculated by balancing incoming fluxes from the atmosphere with outgoing longwave fluxes and the conductive heat flux in the ice. For the albedo, we here use the standard [setup of The Community Climate System Model version 3 \(CCSM3\)](#), ~~so-called CCSM3-setup~~, where the (spectral) albedo is calculated explicitly based on snow and ice temperature and thickness (see Hunke and Lipscomb (2010) for details). A bulk sea ice salinity of 4 psu is implemented.

We run CICE in standalone mode, coupled to the mixed-layer ocean that forms part of the CICE package. The heat flux between this mixed-layer ocean and the sea ice is in the standard form of CICE described by the 2-equation approach with $\alpha_h = 0.006$. This formulation is here either used directly or replaced by the ice-bath formulation or the 3-equation formulation as described before. The salinity of the mixed-layer [in SIM and CICE](#) is kept at 34 g/kg.

~~We force CICE with the National Center for Atmospheric Research (NCAR) monthly-mean climatological data with $1^\circ \times 1^\circ$ resolution. Input fields consist of monthly climatological sea-surface temperature, sea-surface salinity, the depth of ocean mixed layer, surface wind speeds, 10-m air temperature, humidity and radiation.~~

2.3 MPIOM

To examine the interaction of changes in the sea-ice model with large-scale ocean circulation, we use the ocean general circulation model MPIOM (Max-Planck Institute Ocean Model). MPIOM is based on the primitive equations with representation of thermodynamic processes ~~—A detailed description is given by Marsland et al. (2003)—~~ [\(Marsland et al., 2003\)](#). [The orthogonal curvilinear grid is applied in MPIOM with the north pole located over Greenland. The relevant terms of the surface heat balance are parameterized according to bulk formulae for turbulent fluxes \(Oberhuber, 1993\), and radiant fluxes \(Berliand, 1952\).](#)

The sea-ice component of MPIOM uses zero-layer thermodynamics following Semtner Jr (1976) and viscous-plastic dynamics following Hibler III (1979). It does not allow for a sub-grid ice-thickness distribution. The sea-ice state within a certain grid cell is hence fully described by ice concentration C and ice thickness h . The surface heat balance is solved separately for the ice covered and ice free part of every grid cell. Any ice that is formed through heat loss from the ice-free part is merged with the existing ice to form a new ice thickness and ice concentration. The ~~distribution between thickening and a change in ice concentration is described by a distribution parameter~~ change in sea ice thickness and concentration can be calculated via two main ice distribution parameters as outlined by Notz et al. (2013):-

, the first one being a so-called lead closing parameter that describes how quickly the sea ice concentration increases during new ice formation processes, and the other describing the change in the ice-thickness distribution during melting. In its standard setup, MPIOM uses an ice-bath parameterization to calculate the heat flux between the ocean and the ice. ~~This~~ Wherever covered by sea ice, the temperature of sea water in the uppermost grid cell is kept at its freezing point. All heat entering the uppermost grid cells either from the atmosphere or from the deeper oceanic grid cell is instantaneously transported into the sea-ice cover, maintaining the temperature of the uppermost oceanic layer at the freezing point. In the present study, this formulation is either used directly, or replaced by the 2-equation or the 3-equation parameterization ~~as described before.~~

~~We run MPIOM with GR30 (about 3°) horizontal resolution and 40 uneven vertical layers, forced by daily heat, freshwater and momentum fluxes as given by the climatological OMIP forcing (Röske, 2006).~~

2.4 COSMOS

The comprehensive climate model COSMOS (ECHAM5-MPIOM), developed by the Max Planck Institute for Meteorology, is used in the present study to further investigate the atmospheric response to the three ice-ocean heat flux parameterizations. The atmosphere component ECHAM5 solves the primitive equations for the general circulation of the atmosphere on a sphere (Roeckner et al., 2003). It ~~applies is formulated on a~~ Gaussian grid for the horizontal transport schemes and on a hybrid sigma-pressure grid for the vertical ~~between the surface and 0 hPa~~ coordinate. The OASIS3 coupler (Valcke, 2013) is used for the coupling between the ocean and the atmosphere components. ~~For each~~ Once per simulated day, solar and non-solar heat fluxes, hydrological variables, and horizontal wind stress are ~~sent provided~~ from the atmosphere through OASIS3 to the ocean ~~through OASIS3~~. At the same time, the ocean ~~transfers sea ice and sea surface~~ provides its sea-ice coverage and the sea-surface temperature to the atmosphere.

~~The~~

3 Experimental design

For each model, we perform separate simulations based on the three ice-ocean heat flux formulations (see table 1). We assume that the 3-equation approach with $R = 35$ describes reality more realistically, and hence use this simulation as our reference. In our idealized 1-D model, we also use $R = 70$ to test the model sensitivity with respect to this parameter. For a given value of R , we calculate α_h to satisfy the requirement described in McPhee et al. (1999). This results in a turbulent heat exchange

coefficient $\alpha_h = 0.0095$ for $R = 35$ and $\alpha_h = 0.0135$ for $R = 70$. In SIM and CICE the mixed-layer salinity has a constant value of 34 g/kg. In MPIOM and COSMOS the salinity of the sea water evolves dynamically in response to oceanic or atmospheric processes.

As atmospheric forcing, we use for our conceptual 1-D model equations (7) to (9). For CICE, we use the National Center for Atmospheric Research (NCAR) monthly-mean climatological data with $1^\circ \times 1^\circ$ resolution Kalnay et al. (1996). Input fields contain monthly climatological sea-surface temperature, sea-surface salinity, the depth of ocean mixed layer, surface wind speeds, 10 m air temperature, humidity and radiation for the time period of 1984-2007. For MPIOM, we use a GR30 (about 3°) horizontal resolution and 40 uneven vertical layers, forced by daily heat, freshwater and momentum fluxes as given by the climatological Ocean Model Intercomparison Project (OMIP) forcing (Röske, 2006).

For the coupled model COSMOS, the configuration of the ice-ocean component MPIOM is the same as ~~that of the ice-ocean model MPIOM used in our study~~ we use for the stand-alone version of this model. The atmospheric module ECHAM5 ~~was is~~ used at T31 resolution (3.75°) with 19 vertical levels ~~between the surface and 0 hPa~~. The coupled model was initialized from a ~~previous~~ pre-industrial simulation and integrated with the ~~boundary conditions, involving the~~ solar constant, Earth's orbital parameters and greenhouse ~~gases, fixed at~~ gas forcing all fixed at their 1950 CE ~~values~~. All simulations were run sufficiently long to reach quasi-equilibrium.

4 Results

We now turn to a description of the simulated responses of sea ice, ocean and atmosphere to the three different parameterizations. Table 1 presents the list of our experiments.

3.1 Influence of u_* , h_{mix} and the ice concentration

4 Results

We now turn to a description of the simulated responses of sea ice, ocean and atmosphere to the three different parameterizations.

4.1 Influence of u_* , h_{mix} and ice concentration

We start with a number of sensitivity experiments with our simple 1-D model that were carried out to understand the underlying relationship between simulated ice thickness and the three different parameterizations. We ~~carried out~~ performed four different simulations with our simple model, which in the following are called SIM-icebath, SIM-2eq, SIM-3eq35 and SIM-3eq70, where for the 3-equation setup the last number denotes the value of $R = \alpha_h/\alpha_s$, ~~which is set to either 35 or 70~~. We run the simulations until the ice reaches its equilibrium thickness, with no more changes from one year to the next.

~~We start with examining a standard simulation with~~ In our standard SIM simulations we applied $u_* = 0.002$ m/s, a sea-ice concentration $C = 85\%$, an albedo of sea water $\alpha_{oce} = 0.1$ and a mixed-layer depth $h_{mix} = 40$ m. The sea ice salinity is kept

Table 1. List of experiments, note that $R = \alpha_h/\alpha_s$, denoting the ratio between turbulent exchange coefficients for heat (α_h) and salt (α_s).

Name	Parameterization			length (model year)
		<u>$T_{interface}$</u>	<u>T_f</u>	
SIM-icebath	Ice bath	<u>same as T_f</u>	<u>$-1.84^\circ C$</u>	100
SIM-2eq	2-equation	<u>same as T_f</u>	<u>$-1.84^\circ C$</u>	100
SIM-3eq35	3-equation, with R=35	<u>from Eq. (1), Eq. (3), Eq. (5)</u>	<u>$-1.84^\circ C$</u>	100
SIM-3eq70	3-equation, with R=70	<u>from Eq. (1), Eq. (3), Eq. (5)</u>	<u>$-1.84^\circ C$</u>	100
CICE-icebath	Ice bath	<u>same as T_f</u>	<u>$-1.84^\circ C$</u>	100
CICE-2eq	2-equation	<u>same as T_f</u>	<u>$-1.84^\circ C$</u>	100
CICE-3eq35	3-equation, with R=35	<u>from Eq. (1), Eq. (3), Eq. (5)</u>	<u>$-1.84^\circ C$</u>	100
MPIOM-icebath	Ice bath	<u>same as T_f</u>	<u>freezing point of the uppermost cell</u>	1000
MPIOM-2eq	2-equation	<u>same as T_f</u>	<u>freezing point of the uppermost cell</u>	1000
MPIOM-3eq35	3-equation, with R=35	<u>from Eq. (1), Eq. (3), Eq. (5)</u>	<u>freezing point of the uppermost cell</u>	1000
COSMOS-icebath	Ice bath	<u>same as T_f</u>	<u>freezing point of the uppermost cell</u>	1000
COSMOS-2eq	2-equation	<u>same as T_f</u>	<u>freezing point of the uppermost cell</u>	1000
COSMOS-3eq35	3-equation, with R=35	<u>from Eq. (1), Eq. (3), Eq. (5)</u>	<u>freezing point of the uppermost cell</u>	1000

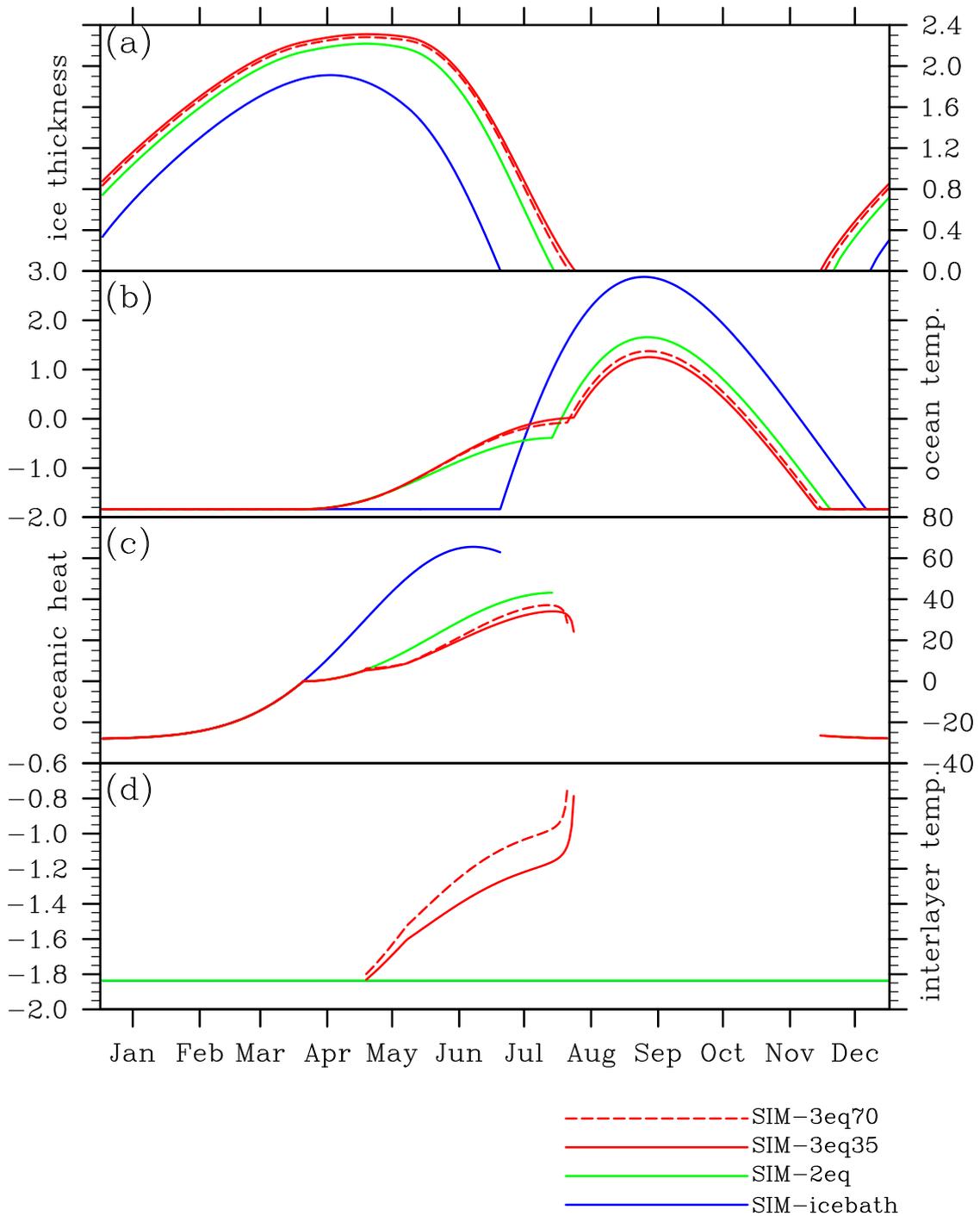


Figure 1. Time series of (a) sea-ice thickness (units: m), (b) ocean temperature (units: $^{\circ}\text{C}$), (c) ocean-to-ice heat flux (units: W/m^2) and (d) ice-ocean interface temperature (units: $^{\circ}\text{C}$) in the experiments SIM-icebath, SIM-2eq, SIM-3eq35 and SIM-3eq70 with friction velocity at 0.002 and ice concentration at 75%. The model is run into equilibrium.

at 0. In winter, when the ocean loses energy to the atmosphere through the open-water part of the grid cell, the simulated heat
290 loss from the ocean is identical in the four setups (Fig. 1c), since their open-water part is identical and the ocean is constantly
at its freezing temperature (Fig. 1b). Hence, any heat that is extracted from the mixed layer directly causes ice growth, which
explains the very similar accretion rates of the sea ice (Fig. 1a). Major differences between the simulations arise as soon as
the net heat flux becomes positive and begins to heat the ocean. All energy that enters the ocean is then directly used to melt
the ice in SIM-icebath, while some of the heat is stored in the ocean in SIM-2eq and SIM-3eq. Hence, ice in SIM-2eq and
295 SIM-3eq melts slower than the ice in SIM-icebath, and the ocean remains warmer throughout spring (Fig. 1b). Once the ice in
SIM-icebath is melted completely, the ocean temperature rises rapidly and quickly exceeds that in SIM-2eq and SIM-3eq. This
can be explained by two facts: 1) in SIM-2eq and SIM-3eq, the sea ice reflects most of the incoming shortwave radiation, and
2) in SIM-2eq and SIM-3eq the heat flux absorbed by open water is primarily used for sea-ice melting, while in SIM-icebath
no more sea ice exists such that the entire heat flux into the ocean causes a warming of the sea water. The slower melting of the
300 ice in SIM-2eq and SIM-3eq and the resulting lower heat storage in the ocean throughout summer results in an earlier onset of
sea-ice formation during autumn.

For SIM-icebath and SIM-2eq, the temperature at the ice-ocean interface is constant at the freezing point of the sea-water,
which for our choice of $S_{seawater} = 34$ g/kg is around -1.84 °C. For SIM-3eq, the interface temperature can be significantly
above this value, as the interface freshens through the melting of the comparably fresh sea ice (Fig. 1d).

305 Comparing SIM-2eq, SIM-3eq35 and SIM-3eq70, we find that the ice thins earlier and stronger-faster in SIM-2eq, because
the ocean heat flux between the ocean and the ice is amplified in this setup owing to the constantly cold interfacial temperature.
Accordingly, the oceanic temperature increases slower-more slowly throughout spring in SIM-2eq. In SIM-3eq70, the transport
of salt to the interface is lower than in SIM-3eq35. Hence, the interface remains fresher and warmer throughout summer. Dispite
Despite the warmer interface, stronger heat fluxes and slightly faster ablation of the ice are simulated, mainly resulting from a
310 higher turbulent heat exchange coefficient α_h , which is 0.0095 in SIM-3eq35 and 0.0135 in SIM-3eq70.

To quantify the different response of the simulated sea-ice cover for a larger range of forcing conditions, we carried out
a series of sensitivity studies. For each of these, we varied one of the forcing parameters and analysed the difference in
annual mean ice thickness-ice-ocean heat flux between SIM-3eq35 and SIM-icebath. Regarding friction-velocity, we find that
differences in resulting ice thickness are the larger the smaller the friction velocity is. This is related to the fact that for lower
315 friction velocities, less heat is transported to the ice-ocean interface in the 3-equation setup, which slows down sea-ice ablation.

Regarding oceanic mixed-layer depth, we We find that in our simplified setup, differences in ice thickness between SIM-
3eq35 and SIM-icebath are the larger the deeper our mixed layer is increase with mixed layer depth. This is due to the fact that
the same amount of heat input from the atmosphere causes the smaller a temperature change the deeper the mixed layer is causes
320 a smaller temperature change for a deeper mixed layer. According to equation (3), such a smaller temperature change then
causes a smaller leads to a smaller change in heat flux to the ice bottom throughout summer. In SIM-icebath, in contrast, the
ice-ocean heat flux is identical to the net flux between the air and the open water, and hence independent of the depth of the
oceanic mixed layer (Fig. 2).

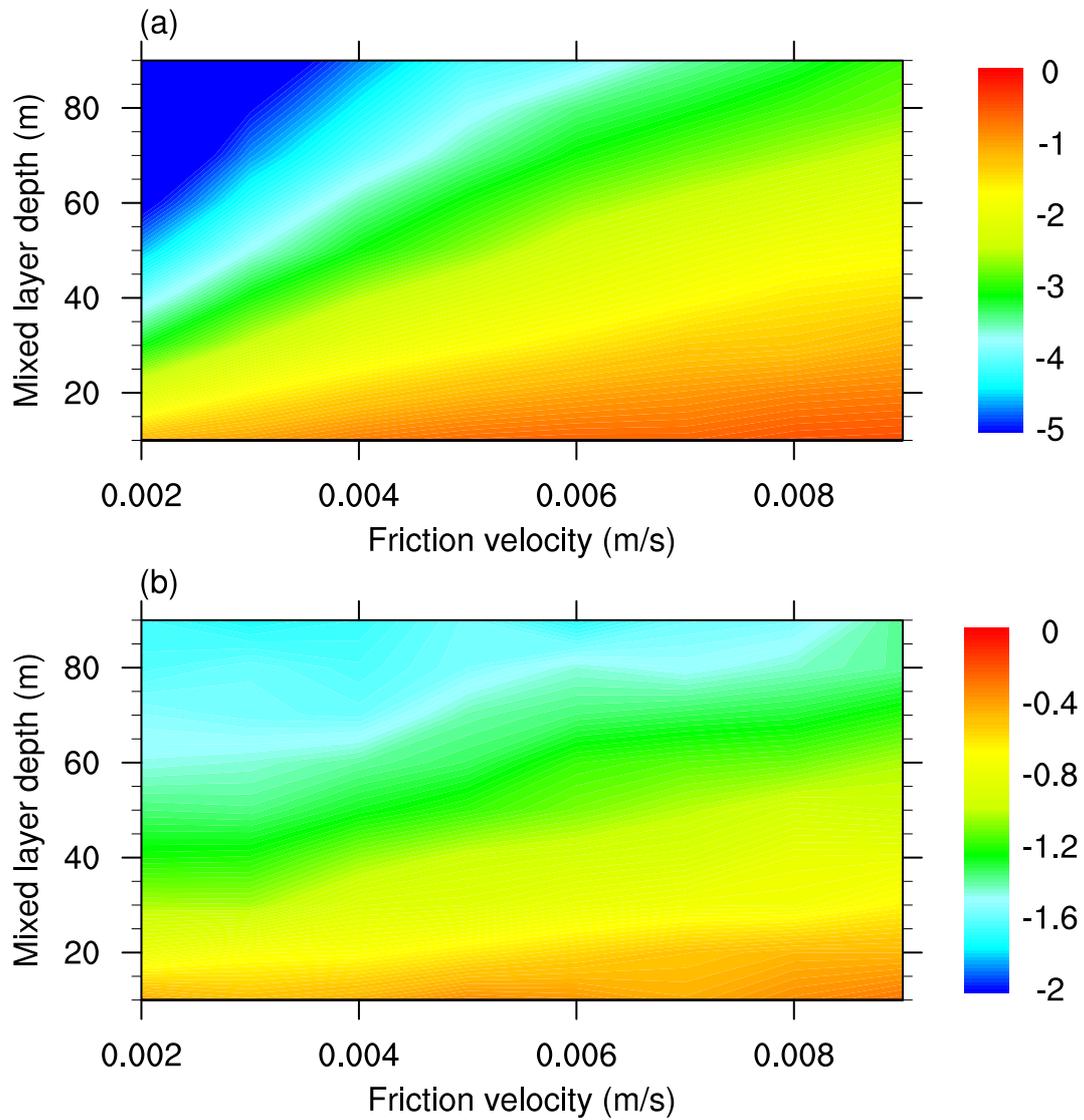


Figure 2. Anomalies of ocean-to-ice heat flux in SIM for (a) 3-equation minus ice bath, and (b) 3-equation minus 2-equation, for different choices of mixed layer depth and friction velocity. Units are W/m^2 .

325 In addition, we find that the difference in sea-ice thickness generally decreases with friction velocity. This is related to the
fact that for larger friction velocity, more heat is transported to the ice-ocean interface in the 3-equation setup (Fig. 2), which
enhances sea-ice melt.

Finally, regarding sea-ice concentration, we find in our simplified setup that differences in ice thickness between SIM-3eq35
and SIM-icebath are ~~the larger the lower the ice concentration is~~ larger for a smaller ice concentration. This is ~~explicable by~~
related to the fact that the residual energy, which mainly comes from the net incoming heat flux through open water, is all ~~given~~
330 ~~to used for ablating~~ sea ice in SIM-icebath, while in SIM-3eq35 only a fraction of ~~it the heat~~ is used for ice ablation. Lower ice
concentration ~~, namely, larger open water, amplifies the residual energy and therefore~~ enhances the energy by the open water
and therefore also the difference in the amount of heat transferred to ~~sea ice~~ the ice cover.

4.2 Ice thickness

Having understood some of the qualitative impact of the different parameterizations, we can now turn to an analysis of their
335 impact in the more realistic setting provided by CICE, MPIOM and COSMOS. In these models $R = 35$ is applied in the full
3-equation approach. The presented results focus on the Arctic Ocean, as we ~~find only minor response of the~~ only find a small
response of Southern Ocean properties to the change of ice-ocean heat flux parameterizations ~~espeeially in in particular in~~
MPIOM and COSMOS; furthermore, the stand-alone ~~sea ice~~ sea-ice model CICE simulates an unrealistic distribution of sea
ice in warm months in the Southern Ocean, as it fails to capture the heat release from the relatively deep mixed layer.

340 We let all models run until the modeled ice cover ~~(as well as the deep ocean temperatures in the cases of and, in~~ MPIOM
and COSMOS) ~~reaches~~, the deep ocean temperatures reach quasi-equilibrium. ~~In detail~~ More concretely, we performed CICE
experiments for 100 model years, with the last 10 years representing its quasi-equilibrium state. For MPIOM and COSMOS,
1000-model-year experiments were conducted, and data from the last 100 model years were used for analysis. ~~Signifiancee~~
~~level~~ The significance level of any differences between the individual simulations was calculated by performing Student's t-
345 test which ~~considers the~~ is used to examine if results from two different parameterizations are significantly different. For the
Student's t-test, the interannual variances of the last 100 simulation years (10 years in the case of CICE) ~~. Doing so, we find a~~
~~similar response in ice thickness~~ are considered.

We find that the ice thickness responds similarly to the different parameterizations as in the simple, one-dimensional
model: Everything else unchanged, ~~the ice-bath parameterization leads~~ compared to the 3-equation approach the ice-bath
350 parameterization leads to thinner ice throughout the Arctic Ocean, both in winter and summer (Fig. 3). The change is similar
but less pronounced in the simulations based on the 2-equation parameterization. The most significant changes occur in the
marginal ice zone where sea-ice concentration is lowest, again consistent with the results from the one-dimensional model. In
the Arctic, the change in March thickness is generally less pronounced than the change in September thickness. This is due to
the fact that the air-to-ocean heat flux tends to be negative (the ocean loses heat to the air) in March, and both the temperature
355 of the water and the temperature at the ice-ocean interface are maintained at the freezing point. Hence, in all parameterizations,
the extracted heat is directly transferred into sea-ice formation. In September, in contrast, the ocean can maintain a temperature

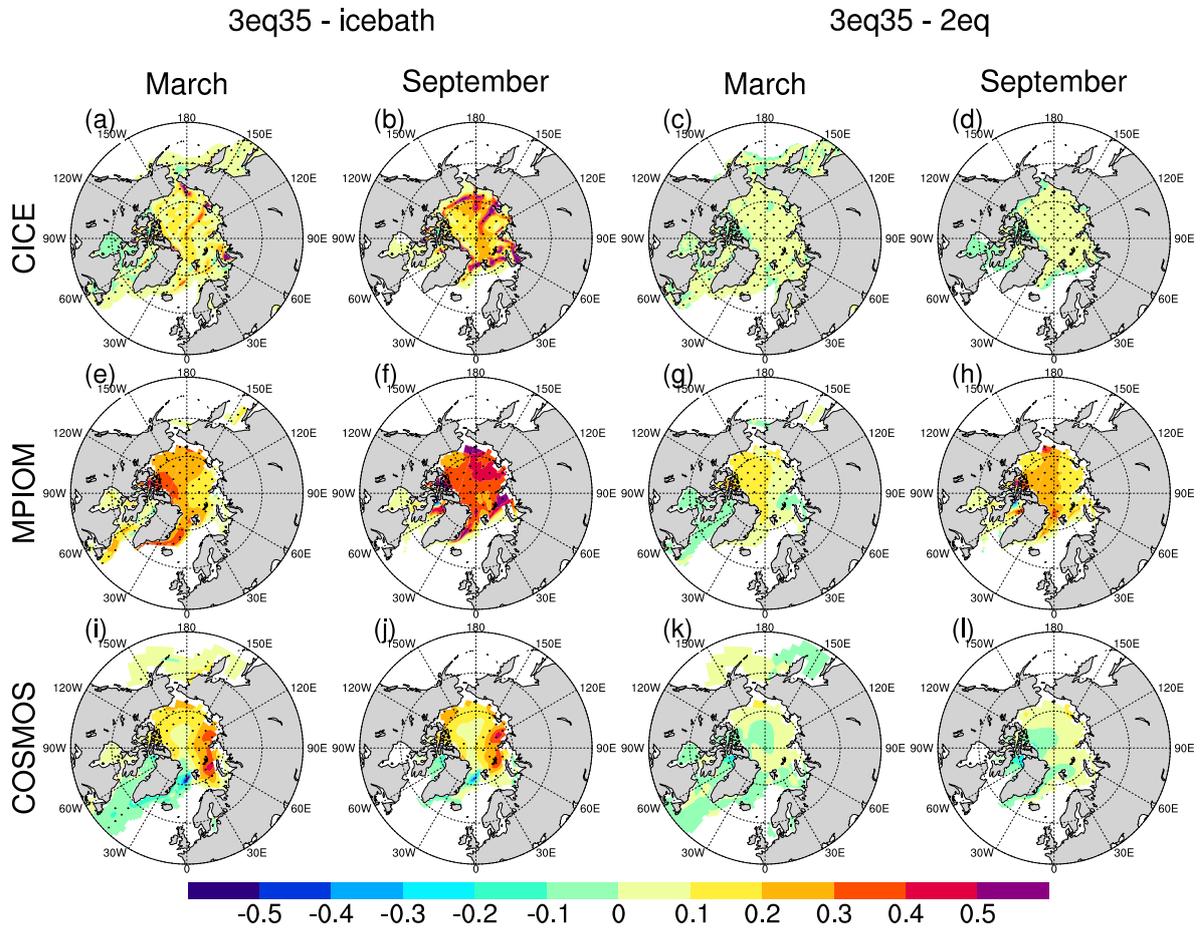


Figure 3. The difference in the Arctic sea-ice thickness for (a) CICE-3eq35 – CICE-icebath in March, (b) CICE-3eq35 – CICE-icebath in September, (c) CICE-3eq35 – CICE-2eq in March, (d) CICE-3eq35 – CICE-2eq in September, (e) MPIOM-3eq35 – MPIOM-icebath in March, (f) MPIOM-3eq35 – MPIOM-icebath in September, (g) MPIOM-3eq35 – MPIOM-2eq in March, (h) MPIOM-3eq35 – MPIOM-2eq in September, (i) COSMOS-3eq35 – COSMOS-icebath in March, (j) COSMOS-3eq35 – COSMOS-icebath in September, (k) COSMOS-3eq35 – COSMOS-2eq in March, and (l) COSMOS-3eq35 – COSMOS-2eq in September. The marked area has a significance level of greater than 95% based on Student’s t-test. Units: m.

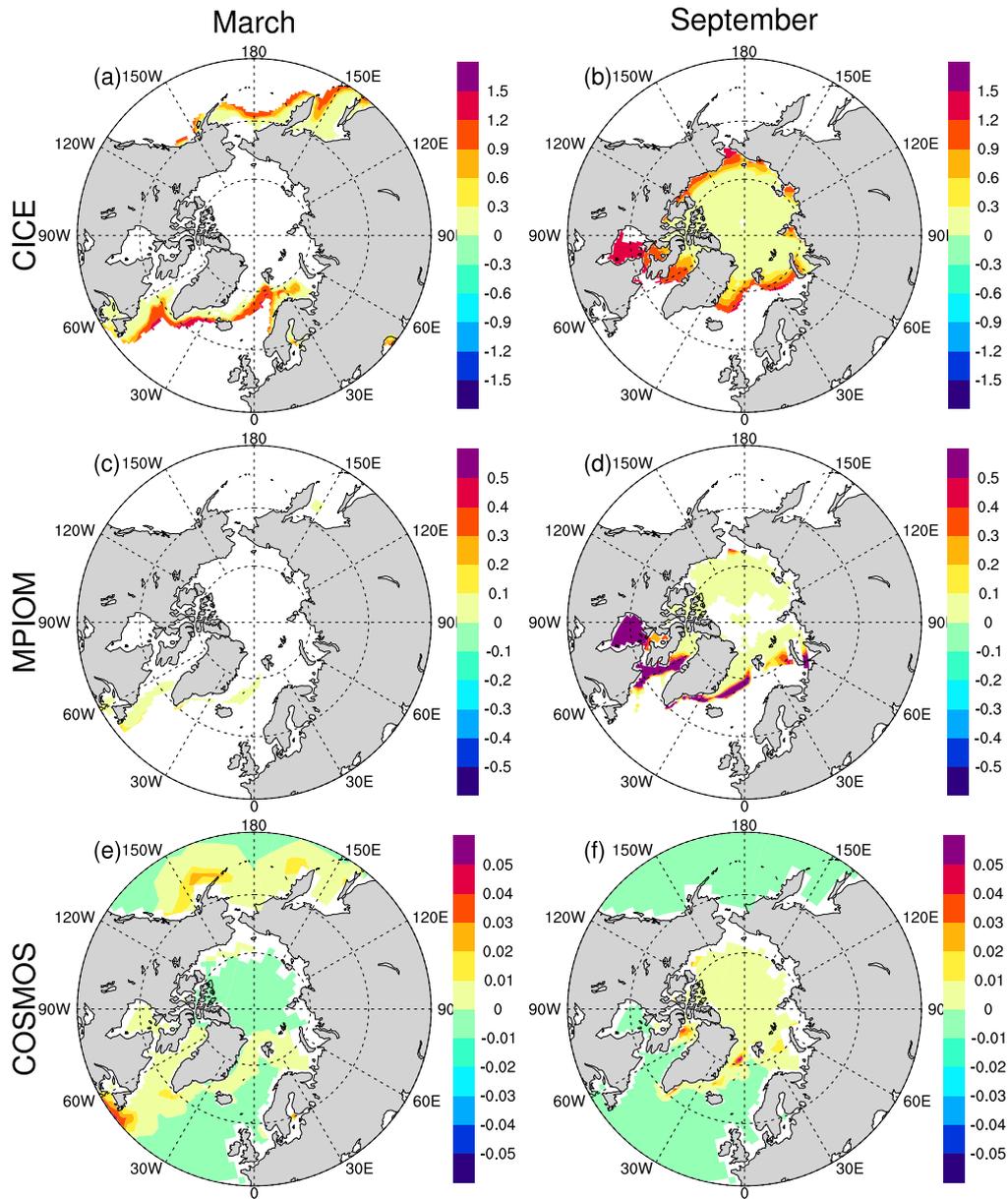


Figure 4. The anomaly of the Arctic ice-ocean interface temperature in (a-b) CICE-3eq35, (c-d) MPIOM-3eq35, and (e-f) COSMOS-3eq35 relative to freezing point of the far-field ocean (about -1.8°). The left column is for March and the right column for September. Units: K.

above the freezing temperature in the 2-equation or 3-equation approach but not in the ice-bath approach. Hence, as in the simple 1-D model, differences between the different parameterizations are more pronounced during summer.

360 In addition, sea-ice concentration is high throughout March, which reduces the direct interaction of atmospheric heat fluxes with the ocean. As discussed in the previous subsection, this limits differences between the different parameterizations during winter time. Finally, the ice thins somewhat less in winter because of dynamical effects: the thinner ice is more mobile and more prone to ridging, which fosters the formation of areas with open water. In these areas, significant amounts of new ice can form, which dampens some of the thermodynamic thinning of the ice pack. ~~Among-~~

365 ~~In summer, among~~ the three parameterizations, only the 3-equation approach can ~~obtain a result in an ice-ocean-interface~~ temperature above the freezing point of the ~~far-field-ocean-at-the-the-interface-between-the-ice-and-the-salt-water~~ uppermost ocean layer (Fig. 4), which ~~can slow down-reduces~~ the ocean-to-ice heat flux. This is due to the fact that the ice-ocean interface is usually very fresh owing to the ablation of the ice bottom. When the temperature of the interface exceeds that of the mixed layer, a reversed heat flux from the ice to the ocean can occur.

4.3 Upper ocean temperature and salinity

370 We now move on to analyse how the described changes in sea ice impact upper ocean temperature and salinity. We find for the Arctic Ocean that the ice-bath parameterization and the 2-equation approach result in almost the same temperature distribution during winter as the more realistic 3-equation approach in CICE and MPIOM (Fig. 5a,c,e,g). During summer, however, the ice-bath approach causes warmer water to persist around the ice edge in CICE (Fig. 5b). This is caused by the fact that here the ice melts earlier than in the 3-equation approach, which then allows the ocean to absorb heat more efficiently. The same is found in 375 MPIOM in the areas of Hudson Bay, Baffin-Bay and Norwegian Sea and Barents Sea (Fig. 5f,h). The most intriguing feature found in COSMOS is a significant cooling across the North Atlantic Ocean in the ice-bath and 2-equation parameterizations compared to the 3-equation approach (Fig. 5i-l). Such cooling is a consequence of weakened thermohaline circulation which tends to bring relatively warmer water from the lower latitudes (~~illustrated in see~~ Section 4.4).

380 Because brine is released from sea-ice-sea ice during its formation and growth, the changes in ice thickness between different parameterizations should trigger changes in upper ocean salinity. Indeed, we find such changes to occur (Fig. 6): In regions in which the ice-bath approach or the 2-equation approach cause an increased heat flux to the ice underside, and hence a ~~reduction in ice thickness~~ larger melting rate of sea ice in summer as well as a smaller growth rate in winter, the ocean is generally less salty in ~~these the~~ simulations with a simplified parameterization of ice-ocean heat exchange than in the simulations with the full 3-equation parameterization. Interestingly, the opposite sign is observed in ~~coastal regions of the Arctic Ocean in~~ 385 ~~COSMOS-icebath, both in winter and summer~~ the Barents sea and its adjacent regions (Fig. 6e-f), despite the larger melt rates ~~of the simplified scheme. This is explicable by the fact that less ice mass is accumulated at the coastal areas in the experiment with in the~~ ice-bath ~~parameterization, thus less brine can be released during ice ablation periods~~ scheme. The North Atlantic Ocean experiences a pronounced freshening in the ice-bath approach in COSMOS (Fig. 6e-f), which lowers the efficiency of deep-water formation. No significant ~~change differences~~ in upper ocean salinity ~~is revealed-are found~~ between experiments 390 COSMOS-2eq and COSMOS-3eq35 (Fig. 6g-h).

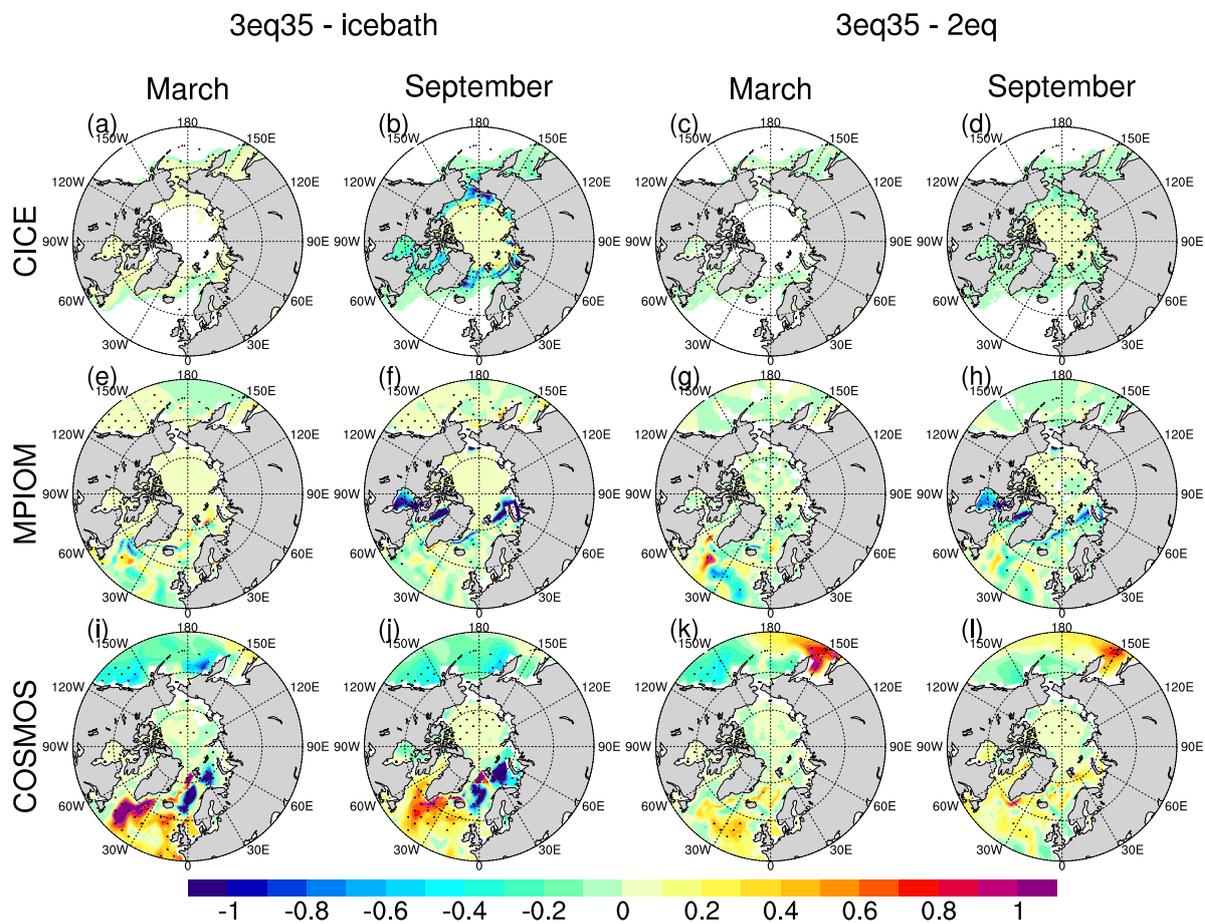


Figure 5. As in Fig. 3, but for the sea surface temperature. Units: K.

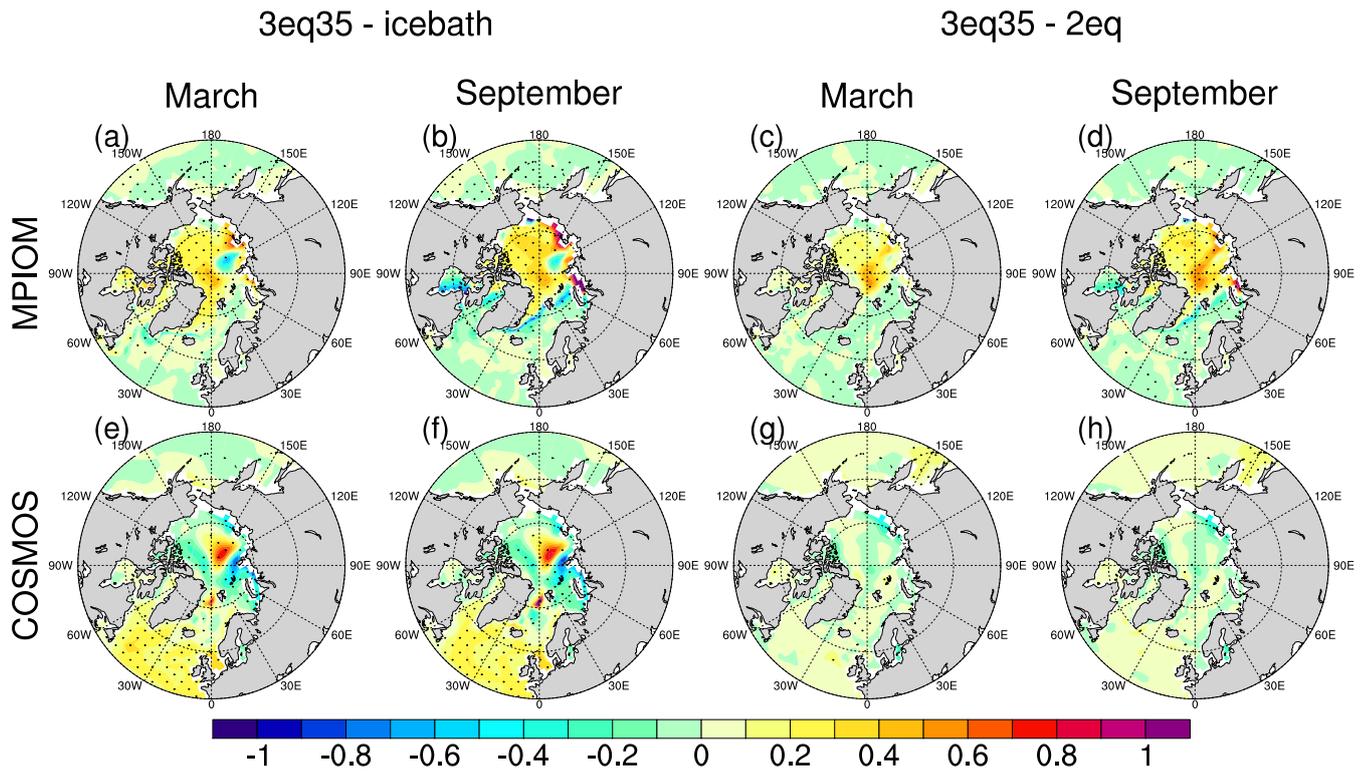


Figure 6. As in Fig. 3e-l, but for the sea surface salinity. Units: g/kg.

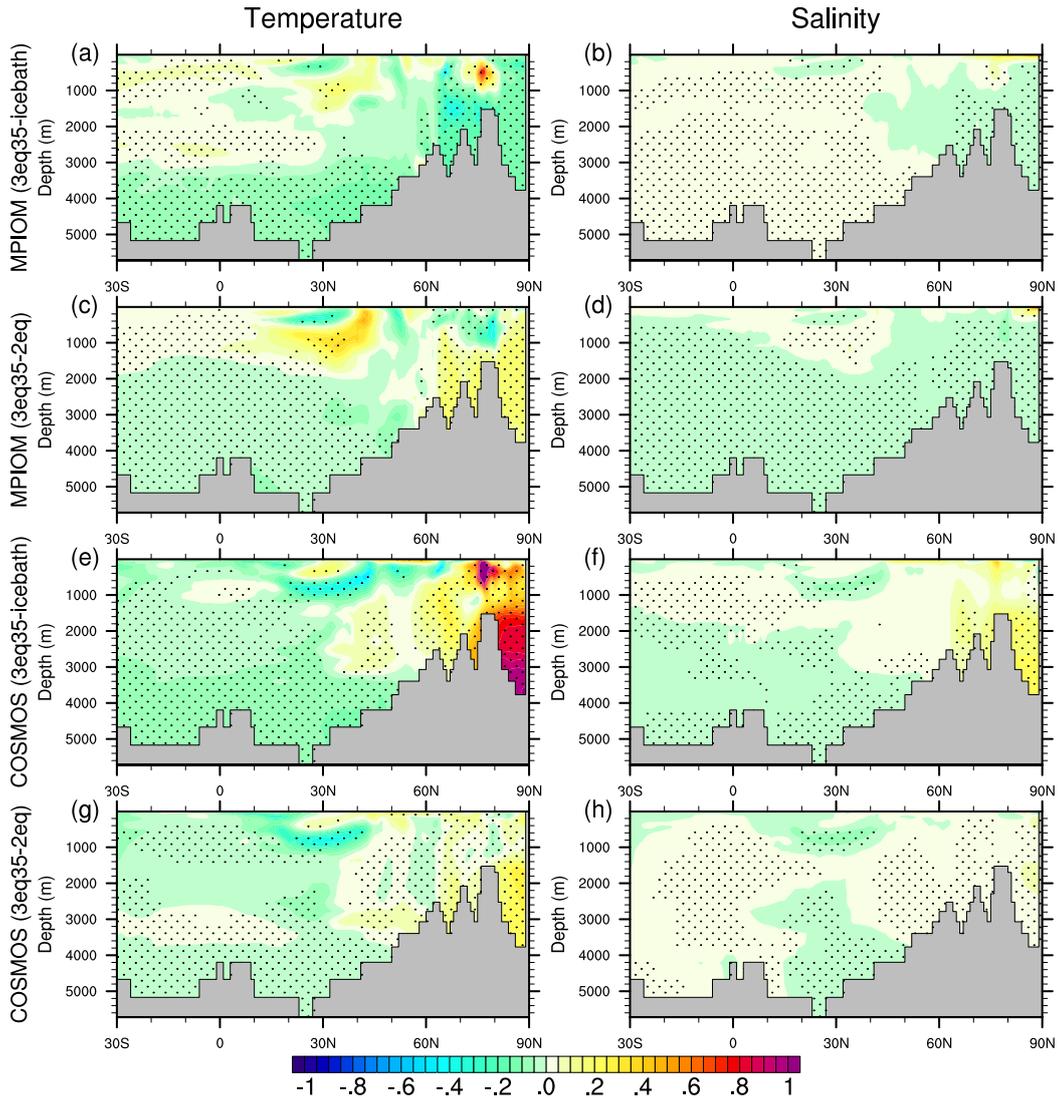


Figure 7. Anomalies in temperature and salinity vertical profile across the North Atlantic section ($-80-0^{\circ}\text{W}$) (a,b) MPIOM-3eq35 – MPIOM-icebath, (c,d) MPI-3eq35 – MPI-2eq, (e,f) COSMOS-3eq35 – COSMOS-icebath, and (g,h) COSMOS-3eq35 – COSMOS-2eq. The left column is for temperature and the right column for salinity. Units: K and g/kg.

4.4 Thermohaline structure of the ocean

We now turn to the large-scale changes in the thermohaline structure of the ocean. We find that compared to the more realistic 3-equation approach, the ice-bath and 2-equation approaches lead to significant cooling of the ocean’s deep water masses (Fig. 7c,e,g). This behaviour is due to the fact that the heat flux out of the ocean is slowed down in the 3-equation approach,

Table 2. AMOC index

Experiment	AMOC index	NP index
MPIOM-icebath	20.1	-
MPIOM-2eq	20.2	-
MPIOM-3eq35	20.2	-
COSMOS-icebath	16.6	1017.5
COSMOS-2eq	16.8	1017.4
COSMOS-3eq35	17.6	1017.9

395 ~~therefore~~. Hence, more heat can be stored in the mixed layer and further ~~advects to~~ advected into the deep ocean. However, the opposite ~~sign is observed is found~~ in experiment MPIOM-icebath, which results in a pronounced warming in the deep water masses by up to 0.5 °C (Fig. 7a). This warming in the simulations with the least realistic parameterization of ice–ocean heat exchange reflects ~~its is caused by the~~ earlier ice loss in ~~areas of deep-water formation~~ the marginal ice zone, which causes enhanced surface warming of the water there.

400 As the simplified parameterizations both lead to ~~thinner sea ice throughout~~ faster melting of sea ice in the Arctic Ocean in summer, and less growth in winter, as compared to the most realistic approach, one would expect a freshening of the ocean mixed layer and the deep water mass that originates from such fresher surface source water. ~~Indeed~~ However, we find that such freshening in MPIOM occurs only within the Arctic upper ocean between depths of 0 and 100 m (Fig. 7b,d). In COSMOS, the freshening extends to the bottom of the Arctic Ocean (Fig. 7f,h). ~~Such~~ This different model behaviour is currently not
405 understood.

The Atlantic meridional overturning circulation (AMOC) streamfunction—~~—~~, defined as the zonally integrated transport over the Atlantic basin, shows a weakening over 40–60°N, 0–3000 m depth in MPIOM-icebath and MPIOM-2eq compared to MPIOM-3eq35. In COSMOS, a pronounced weakening of AMOC is obtained south of 60°N. The AMOC index, i.e. the maximum value of the AMOC streamfunction over the region of 800–2000 m depth, 20–90°N is found to be 20.2 Sv and 17.6 Sv
410 ~~($1\text{ Sv} = 10^6\text{ m}^3/\text{s}$)~~ in MPIOM-3eq35 and COSMOS-3eq35, respectively (Table 2). The latter is consistent with the estimates of global circulation from hydrographic data (15 ± 3 Sv) (Ganachaud and Wunsch, 2000). Compared to the corresponding 3-equation approach, the strength of the AMOC decreases by 1 Sv and 0.8 Sv in COSMOS-icebath and COSMOS-2eq respectively (Table 2). In COSMOS-icebath, the reduced sea surface salinity in the Atlantic section (Fig. 6e-f, Fig. 7f) lowers the efficiency of deep-water formation, resulting in a weakening of the AMOC (Fig. 8c). A similar but less pronounced pattern is
415 obtained by COSMOS-2eq (Fig. 7h). No significant anomaly in the AMOC index is found in MPIOM (Table 2).

4.5 ~~Atmosphere~~ Atmospheric responses

We now finally turn to investigate how the sea ice changes affect the atmospheric properties in the fully coupled model COSMOS.

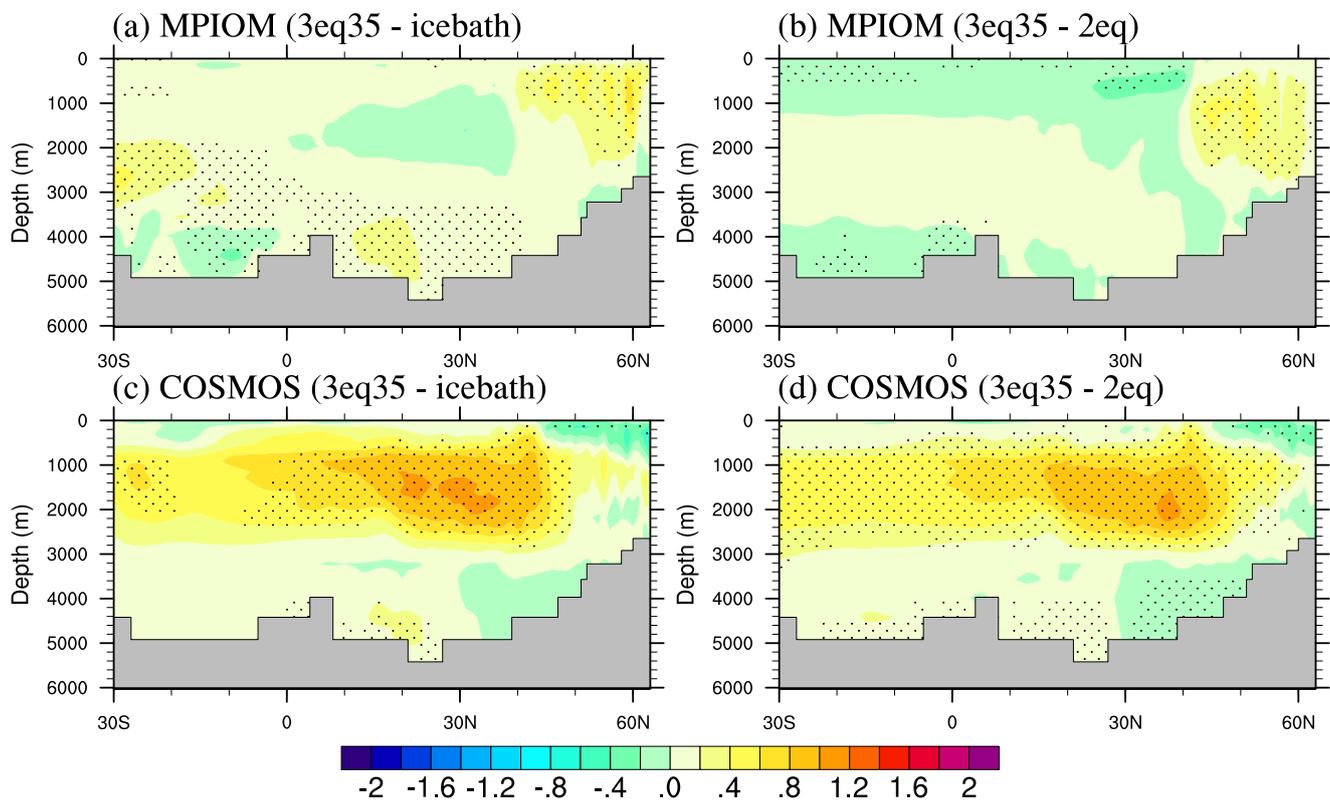


Figure 8. Anomalies in AMOC (a) MPIOM-3eq35 – MPIOM-icebath, (b) MPI-3eq35 – MPI-2eq, (c) COSMOS-3eq35 – COSMOS-icebath, and (d) COSMOS-3eq35 – COSMOS-2eq. Units: Sv.

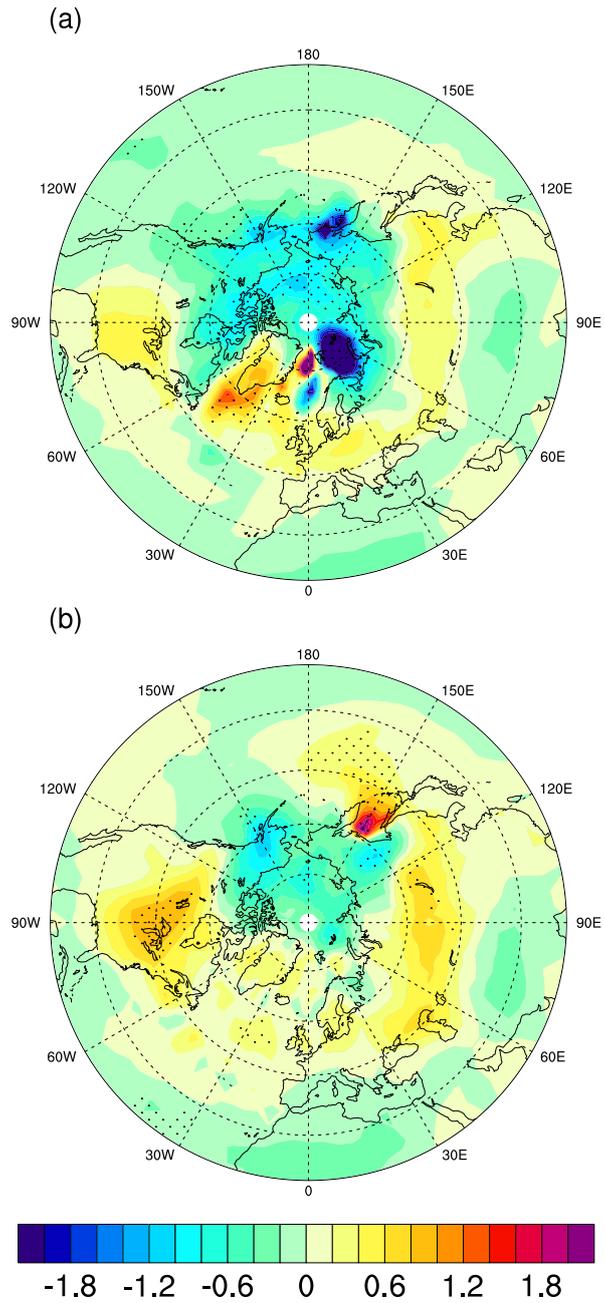


Figure 9. Anomalies in surface air temperature (a) COSMOS-3eq35 – COSMOS-icebath, and (b) COSMOS-3eq35 – COSMOS-2eq. Units: K.

The response in surface air temperature, as shown in Fig. 9, indicates a general warming over the Arctic Ocean and its adjacent continents in the COSMOS-icebath and COSMOS-2eq compared to COSMOS-3eq35; ~~while the opposite sign a~~ cooling can be found for the Greenland Sea, Nordic Sea, North Atlantic Ocean, southeastern North America, and mid-latitude Eurasia. There are various reasons responsible for these changes: 1) Reduced Arctic sea ice mass in the ice-bath and 2-equation approaches lead to a decrease in the surface albedo, resulting in more heat flux absorbed by the surface. 2) The decline of AMOC in experiments COSMOS-icebath and COSMOS-2eq weakens the northward heat transport from lower latitudes to North Atlantic regions. 3) The atmospheric circulation also plays a role, which is discussed in the following.

Fig. 10 depicts the responses in boreal winter sea level pressure (SLP). Compared to the most realistic parameterization, the simplified approaches illustrate a more negative North Atlantic Oscillation (NAO) mode, with positive SLP anomalies over the Greenland and Nordic seas and negative anomalies over the North Atlantic subtropical zone. SLP anomalies in another time window show similar pattern (Fig. S1), indicating the robustness of the NAO- signal in the simplified approaches, even though the significance level does not exceed 95%. Composite analysis shows that a positive NAO mode leads to a warming over much of Europe and far downstream as the winter-time enhanced westerly flow across the North Atlantic moves relatively warm and moist maritime air to that region (Fig. S2a). Another notable feature is the cooling and warming over North Africa and North America respectively, which is associated with the stronger clockwise flow around the subtropical Atlantic high-pressure center. These described patterns are consistent with the modeled surface air temperature response over Northern Hemisphere continents (Fig. 9).

~~The anomalous NAO pattern can also lead to significant changes in the ocean circulation. The convective activities in the Labrador Sea and the Greenland-Iceland-Norwegian (GIN) Seas are shown to have important contributions to the production and transport of North Atlantic deep water (Fig. S3a), and therefore drive the North Atlantic thermohaline circulation. We find that the intensity of the the Labrador Sea convection is characterized by variations that appear to be synchronized with variabilities in the NAO (Fig. S3b). Therefore, the weakening of AMOC in our simplified setups compared to the most realistic approach can be attributed to the simulated anomalous negative NAO phase.~~

Another intriguing pattern in the atmosphere is an anomalous negative SLP over the North Pacific Ocean in the simplified parameterizations compared to the most realistic approach. Here we calculate the North Pacific (NP) index as the area-weighted SLP over the region of 30-65°N, 160°E-140°W during boreal winter (Trenberth and Hurrell, 1994). The NP index in COSMOS-3eq35 is shown to be 0.4-0.5 hPa higher than its counterparts (Table 2). A high NP index leads to a warming over southern North America and ~~the~~ northern Eurasia, as well as a cooling over northern North America (Fig. S2b), resembling the pattern of the surface air temperature anomalies (Fig. 9). Therefore, the response of the surface air temperature in the simplified parameterizations can be attributed to the combined effect of the weakened AMOC and NAO, and the enhanced Aleutian Low.

4.6 Air-sea interaction

In this section the mechanism explaining the weakening AMOC in COSMOS-icebath and COSMOS-2eq as compared to COSMOS-3eq35 is explored. It has long been recognized that the NAO variability has an important influence on the AMOC (Curry et al., 1998; Delworth and Zeng, 2016). Variations in the NAO have been hypothesized to play a role in AMOC variations

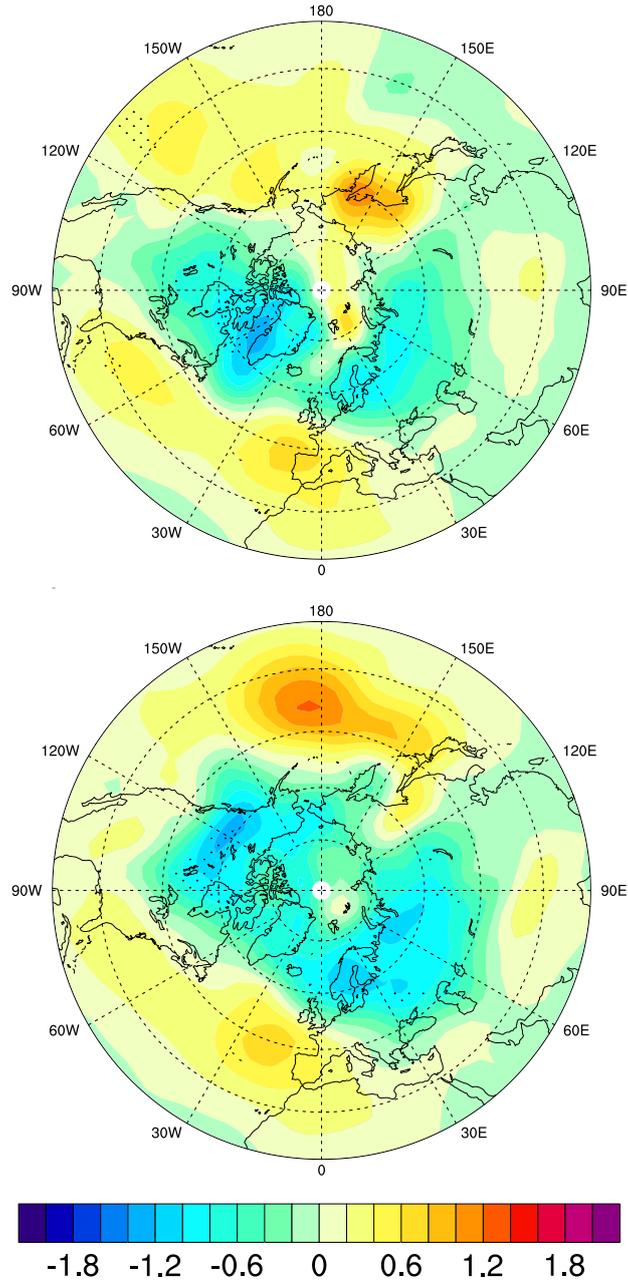


Figure 10. Anomalies in boreal winter sea level pressure (a) COSMOS-3eq35 – COSMOS-icebath, and (b) COSMOS-3eq35 – COSMOS-2eq. Units: hPa.

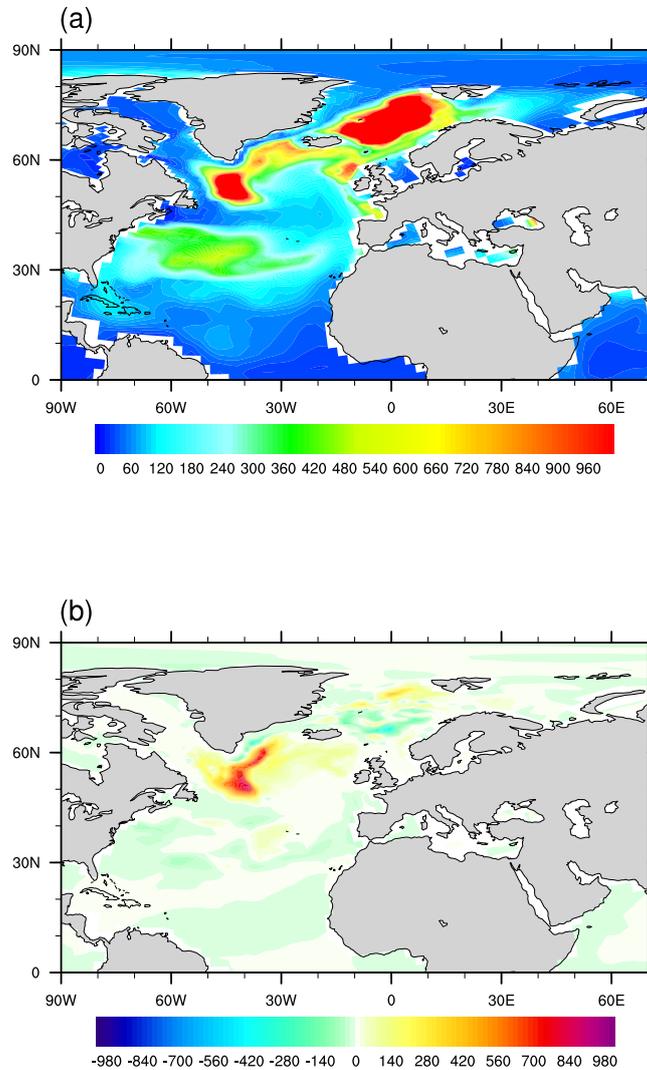


Figure 11. (a) Distribution of March mixed layer depth in COSMOS-3eq35. (b) Composite map of mixed layer depth and NAO index for COSMOS-3eq35. It is calculated by averaging March mixed layer depth anomalies (departure from the mean state) during years when the NAO index exceeds one standard deviation. Units are m.

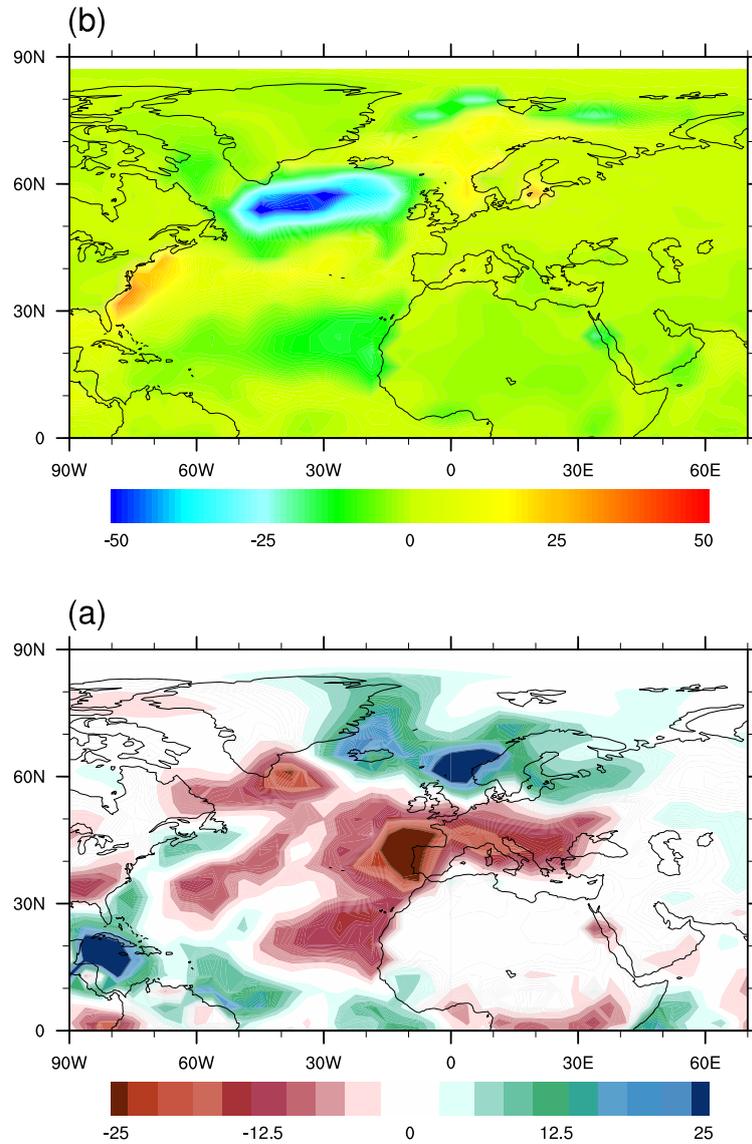


Figure 12. Composite map of (a) surface heat flux and (b) net precipitation and NAO index for COSMOS-3eq35. It is calculated by averaging winter anomalies of (a) surface heat flux and (b) net precipitation (departure from the mean state) during years when the NAO index exceeds one standard deviation. Units are W/m^2 and m.

by modifying air-sea fluxes of heat, water, and momentum. A similar relationship between NAO and the AMOC has been reported also for past climate conditions (Shi and Lohmann, 2016; Shi et al., 2020). Here in Fig. 11 we show the results from a composite analysis between the NAO index and the anomalies in mixed layer depth based on COSMOS-3eq35. It is calculated by averaging March mixed layer depth anomalies (departure from the mean state) during years when the NAO index exceeds one standard deviation.

The convective activities in the Labrador Sea and the Greenland-Iceland-Norwegian (GIN) Seas are shown to have important contributions to the production and transport of North Atlantic deep water (Fig. 11a). For comparison we also show the distribution of mixed layer depth in MPIOM-3eq35 in Fig. S3, which indicates a different location of main deep water convection site in our ice-ocean coupled model: the northeastern North Atlantic. The results from the composite analysis shown in Fig. 11b indicate that the anomalous NAO pattern can lead to significant changes in the ocean circulation. We find that the intensity of the Labrador Sea convection is characterized by variations that appear to be synchronized with variabilities in the NAO. Therefore, the weakening of AMOC in our simplified setups compared to the most realistic approach can be attributed to the simulated anomalous negative NAO phase.

The NAO affects the sea water convection mainly via modifying the surface heat fluxes which leads to anomalies in the spatial and vertical density gradient. Fig. 12a shows the composite map between surface heat flux anomalies and the NAO index. During the positive phase of NAO, more heat than usual is removed from the ocean to the atmosphere at the western Atlantic, in particular the Labrador Sea. Such pattern is in good agreement with the NAO-relative heat flux anomalies derived from the European Centre for Medium-Range Weather Forecasts (ECMWF) interim reanalysis (Delworth and Zeng, 2016). The enhanced removal of heat favors an increase in the surface density and thereby strengthens deep water formation. On the other hand, the NAO also affects the net precipitation over North Atlantic Ocean. As illustrated in Fig. 12b, relatively drier condition could occur over Labrador Sea and Irminger Sea during positive NAO years.

5 Discussion and conclusion

In the present study, we perform 1-D simulations with an idealized columnar model (SIM), as well as global simulations with a stand-alone sea ice model (CICE), an ice-ocean coupled model (MPIOM), and a fully coupled climate model COSMOS, to analyze the sensitivity of modeled climate to ice-ocean interface heat flux parameterizations. This is achieved by implementing into the models: 1) a simple ice-bath assumption with the ocean temperature fixed at the freezing temperature, 2) a more realistic bulk 2-equation with freezing temperature kept at the ice-ocean interface and the ocean being allowed to be warmer than freezing point (McPhee, 1992) and 3) a most advanced double diffusional transport (3-equation) approach with the temperature at the ice-ocean interface being calculated based on the melting rate of the ice bottom (Notz et al., 2003).

The conclusions drawn from these models in terms of sea ice properties are quite similar with each other: The thinnest ice is observed in the ice-bath simulations, as no residual heat is allowed to remain in ~~water, therefore the the ocean and the~~ sea water beneath sea ice is constantly at its freezing point. The 2-equation experiments simulate ~~a relatively~~ thicker sea ice, because some of the heat is stored in the ocean rather than used for ~~ice growth~~ ablating the ice. The simulated sea ice by the 3-equation

approach has the largest thickness, as the temperature at the ice-ocean interface can exceed the freezing point of the far-field ocean, ~~thus causing the heat flux out of the ocean can be slowed from the ocean to be reduced~~ or even reversed. The ~~ice-marginal marginal ice~~ areas are found to be highly sensitive to the choice of ice-ocean heat flux parameterizations. ~~Furthermore~~In particular, the sea water temperature in the ~~ice-marginal-marginal ice~~ zones is largely determined by the onset/retreat of the sea ice.

As a result of the brine release during sea ice formation, the Arctic Ocean is most ~~and-least~~ salty in the 3-equation experiment and least salty in the ice-bath experiment respectively; the same is found in the deep water masses due to their coupling with the surface source water. The thermohaline instability obtained from such salinity profile is responsible for a strengthening of the Atlantic meridional overturning circulation (AMOC) in the coupled simulation with the 3-equation approach. Note that our results are in good agreement with a previous study using CICE (Tsamados et al., 2015) that found in August stronger basal-melting of Arctic sea ice, decreased Arctic Ocean salinity, cooling of sea water in the central Arctic and warming of sea water at the ice edge in the 2-equation experiments compared to the 3-equation approach. However, in their study the effects are more pronounced, possibly because we used different model versions of CICE and different parameters for the ice-ocean heat flux formulations, one example is the value for R, which is 50 in Tsamados et al. (2015) and 35 in our case. In addition, different atmospheric forcings were used in the two studies.

In contrast to their and other previous studies, in our study we do not only use a stand-alone sea-ice model but also analyse a coupled ice-ocean model and an earth-system model. These allow us to examine the effect of various oceanic heat-flux formulations on the deep ocean and the atmospheric circulation as well as their impact on sea-ice properties. In our study, COSMOS reveals intensification in both the AMOC and NAO when the most advanced ice-ocean heat flux parameterization is applied. It has long been recognized that the NAO variability has an important influence on deep convection in the North Atlantic subpolar regions (Curry et al., 1998). Ocean observations and model simulations show that the changes in the thermohaline circulation during the last century have been driven by low-frequency variations in the NAO via changes in Labrador Sea convection (Latif et al., 2006). More recently, a delayed oscillator model as well as a climate model suggest that the NAO forces the AMOC on a 60-year cycle (Sun et al., 2015). The strengthening in-of the AMOC, obtained in our COSMOS-3eq experiment, is likely due to the combined effect of increased thermohaline instability and the anomalous NAO+ mode. In contrast, no obvious response of the AMOC can be found in the MPIOM experiments (Table 2). ~~This is due to the fact that MPIOM uses prescribed atmospheric forcings which~~ As indicated in the present paper and many other studies (Curry et al., 1998; Latif et al., 2006; Sun et al., 2015), the AMOC is closely related to the atmospheric processes over North Atlantic Ocean. One of the key elements controlling the atmospheric circulation over the North Atlantic is the NAO. As the atmospheric forcings are prescribed in MPIOM, there is no difference in the atmospheric state among the MPIOM experiments. Therefore, the prescribed atmospheric forcing largely limits the air-sea interaction feedback.

Our study indicates a less pronounced sea-ice response to ice-ocean interface heat flux parameterizations in the fully coupled climate model COSMOS than in the ice-ocean model MPIOM (compare Fig. 3e-h with Fig. 3i-l). This is because the change of the AMOC has a ~~damping dampening~~ effect on the simulated sea ice anomalies. The strengthening of the AMOC in COSMOS-3eq can lead to a warming over the Northern Hemisphere, especially over the North Atlantic and the Arctic. This hypothesized

link between [the](#) AMOC and Northern Hemisphere mean surface climate has been documented in an abundance of studies (e.g., Schlesinger and Ramankutty, 1994; Rühlemann et al., 2004; Dima and Lohmann, 2007; Parker et al., 2007). The AMOC-induced warming helps to reduce the sea ice mass over the Arctic and North Atlantic subpolar regions. Indeed, the sea ice across the Greenland Sea and Baffin Bay are found to be thinnest in COSMOS-3eq.

525 [It should be noted that CICE is in many aspects different from the sea ice component in MPIOM: 1\) CICE uses the multi-layer approach with a sub-grid scale ice-thickness distribution \(Bitz and Lipscomb, 1999\), while MPIOM uses zero-layer thermodynamics following Semtner Jr \(1976\). 2\) A submodel of ice dynamics based on an elastic-viscous-plastic rheology \(Hunke and Dukowicz, 1997; Hunke, 2001\) is used in CICE, while in MPIOM viscous-plastic dynamics following Hibler III \(1979\) are used. 3\) Different spatial resolutions are used in CICE \(1°\) and MPIOM \(3°\). 4\) CICE is forced by monthly-mean climatological data from National Center for Atmospheric Research \(NCAR\), while the MPIOM experiments are forced by daily fields from the climatological OMIP data set \(Röske, 2006\). Therefore, the different model behavior between CICE and MPIOM can to a certain extent be explained by the different model configurations.](#)

530 [A detailed comparison of the simulations carried out here with observational data is beyond the scope of our study. However, we note that the sea ice thickness simulated by COSMOS have been evaluated by Notz et al. \(2013\), who found an overestimation of Arctic sea-ice thickness in ECHAM5/MPIOM \(i.e., COSMOS\) with the ice-bath formulation compared to the reanalysis from the Pan-Arctic Ice-Ocean Modeling and Assimilation System \(PIOMAS\) in both winter and summer. Improving the formulation of the ice-ocean heat flux by applying the 3-equation approach causes thicker ice and hence further increases this particular model bias. This indicates that the simplified heat flux parameterisation partly compensates for other errors in the coupled model setup.](#)

540 In the present paper, we exclude the responses of the Southern Ocean, as ~~they are found to be these are~~ much less pronounced than those of the Arctic Ocean. Another reason lies on the over-estimation of the Southern Ocean sea ice extent by the stand-alone sea ice model CICE due to a lack of represented warm deep water.

545 ~~The presented study gives us~~ [Our study provides](#) a better understanding of the ~~importance-impact~~ of a realistic representation of ice-ocean heat flux processes in large scale-climate models, including their effect on sea ice, ocean circulation, and the atmosphere. We find that substantial, large scale climate metrics can emerge from the different parameterization, highlighting the importance of a careful evaluation of their impact in climate-model simulations.

Code and data availability. The source code, data as well as scripts for plotting the figures in this manuscript can be downloaded from "<https://gitlab.awi.de/xshi/ice-ocean-heat-flux>". A snapshot of this repository has been submitted to Zenodo with a granted doi number of 10.5281/zenodo.4160368.

550 *Author contributions.* D. Notz, J. Liu and X. Shi developed the original idea for this study. X. Shi and H. Yang contribute to the code modification and model simulation under the supervision of J. Liu (for CICE), D. Notz (for SIM and MPIOM), and G. Lohmann (for COSMOS). All authors contributed to the data analysis, discussion and paper writing.

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