

1 The authors would like to thank the editor and reviewers for their considerate feed-
2 back on our manuscript. We have taken care for all remarks and address them in the
3 following responses point-by-point.

4 **Reviewer #1**

5 Major Comments:

6 1. The ECHAM model uses the conventional lat/long geometry. The global trans-
7 port schemes FFSL and CISL have special strategy for the cross-polar advection
8 (restricting the λ -directional Courant number less than 1). The AMR invariably
9 makes transport algorithms more complex around the polar regions, but there
10 is no discussion how the authors addressed the cross-polar transport for their
11 implementation. Authors should discuss this issue in the revision.

12 **Answer:** Thank you for pointing out the issue and we hope we understand the
13 reviewer correctly.

14 ECHAM6 restricts Courant number in the θ direction to avoid parallelization
15 problems. The semi-Lagrangian scheme is not restricted by Courant number.
16 However, it is restricted by the deformational Courant number, which measures
17 whether the wind trajectory crosses.

18 We provide a paragraph for the treatment of poles in Section 2.3 (line 194, re-
19 vised manuscript). The text there reads as follows:

20 The staggering of the velocity means that $v \cos \theta = 0$ at poles. Hence, the cross
21 pole advection is controlled by the velocity u in the λ direction restricted by
22 the *deformational Courant number*, $|\frac{\partial u \Delta t}{a \cos \theta \partial \lambda}|$, which is less restrictive than the
23 Courant number. When the deformational Courant number is less than one,
24 trajectories do not cross, which ensures the stability of the semi-Lagrangian
25 scheme. This restriction holds on adaptive meshes and we disable mesh refine-
26 ment in the case that interpolated wind would lead to trajectory crossing. We
27 will also discuss the restriction of the deformational Courant number on mesh
28 refinement in Section 2.4.

29 In Section 2.4, we provide information that we do not refine meshes if interpo-
30 lated wind on high resolution mesh leads to trajectory crossing.

31 2. The time traces of normalized standard errors for the solid-body rotation test
32 should be produced for the uniform high-resolution grid vs. AMR grid of your
33 choice (Fig.8). The error behavior (particularly L-infinity) will be interesting.

34 **Answer:** Thank you for the suggestion. We put the time evolution of numerical
35 error for the solid body rotation in Fig. 12 and added a paragraph for discussion
36 (line 431, revised manuscript).

37 Minor comments:

38 1. The lower panel of Fig.8 is virtually useless! The tracer fields over the polar
39 regions are obscured by the AMR grids. You could plot the grid and the fields
40 side- by-side for better clarity. Please consider this issue with the Fig.22 too,
41 where you could plot it bigger.

42 **Answer:** We take the reviewer's suggestion and modified Fig. 8.

43 We change the colormap, enlarge the figure and reduce the size of the mesh of
44 Fig. 22 (now 23). We also have Fig. 23 (now 24) as a zoom-in for the details of
45 our results.

46 We hope it solves the problem.

47 2. Please cite the paper bt St. Cyr et al., A Comparison of Two Shallow-Water
48 Models with Nonconforming Adaptive Grids, 2008, Monthly Weather Review
49 136(6). They have used FFSL/AMR scheme.

50 **Answer:** Thank you for listing it. This reference is added in the introduction.
51 (line 59, revised manuscript)

52 **Reviewer #2**

53 **Summary:**

54 1. The manuscript describes how an existing transport algorithm can be augmented
55 with an adaptive mesh refinement (AMR) approach. In particular, the Flux-Form
56 Semi-Lagrangian (FFSL) transport scheme of the model ECHAM6-HAMMOZ
57 has been modified without changing the underlying spectral transform dynamical
58 core of ECHAM. This allows the newly developed FFSL AMR transport scheme
59 to resolve a tracer mixing ratio with higher resolution in regions of interests while
60 utilizing interpolated wind information from ECHAM's coarser resolution Gaus-
61 sian grid. Currently, the better resolved AMR tracer distribution is not commu-
62 nicated back (only one-way coupling) to the dynamical core. However, two-way
63 coupling will become important for any future practical applications of the code.
64 The manuscript describes the algorithmic changes of the existing FFSL transport
65 scheme and provides assessments of the AMR transport algorithms via idealized
66 tracer transport test cases. These idealized test cases seem to utilize a standalone
67 AMR model that is not connected to ECHAM. In addition, a dust transport ex-
68 ample with parameterized sources and sinks is presented that mimics a more
69 realistic flow situation with ECHAM. However, the dust example leaves it open
70 what the 'correct' solution is since even the non-adapted control simulations at
71 the resolutions T31 and T63 have almost no resemblance (no convergence). This
72 makes it rather impossible to judge whether AMR provides any benefits in this
73 more realistic example. It also raises the question how AMR would be used for
74 multiple tracers that most likely all need to be refined in different areas (e.g. will
75 each tracer have its own AMR grid?). Add a comment about such aspects.

76 Overall, the research is very interesting and should be published (after revisions).
77 However, the manuscript contains various mathematical errors in the equations

78 (e.g. quantities with different physical units are used in sums, incorrect equations
79 for the PPM subgrid distribution). This raises the question whether these are
80 typos or whether the implementation is also incorrect. The manuscript also needs
81 some additional explanations of the algorithm as detailed below. For example,
82 it is unclear whether/how time-averaged winds are computed which are a key
83 component of the original FFSL algorithm by Lin and Rood (1996). I also would
84 like to see the cosine bell transport test in its most challenging configuration,
85 which is the transport of the tracer at the 45° angle to the equator. This will
86 more clearly assess the 2D transport characteristics of the chosen dimensionally-
87 split AMR approach. Currently, the cosine bell is only tested for pure north-
88 south or west-east flows in a 1D manner which leads to high convergence rates
89 (between 2nd and 3rd order). I assume that the convergence rate will drop to first
90 order for a 2D flow, and that the cosine bell will suffer from rather severe shape
91 deformations. This will provide a more holistic assessment of the pros and cons
92 of the dimensionally-split approach.

93 **Answer:** Thank you for the reviewer's comments.

94 We have added a comment on the resemblance (or rather dissimilarity) between
95 T31 and T63 in Section 4.3.2.

96 These simulations show an important fact of multi-physics simulations: there ex-
97 ist subgrid-scale parameterizations that inhibit convergence in a classical mathe-
98 matical sense. The differences between *T31* and *T63* horizontal resolution sim-
99 ulations are not caused by increased resolution in the dynamical core, but also
100 and predominantly by the necessary change in parameterizations due to the in-
101 creased resolution. In particular, Gläser et al. (2012) showed that the dust emis-
102 sion scheme is sensitive to different horizontal resolutions. The observed dust
103 mixing ratio is affected also by wet and dry deposition, which itself is affected
104 by cloud and convection parameterizations. These results indicate that we can-
105 not use a high-resolution simulation as a converged state quasi reference solution.
106 Our analysis of accuracy will therefore be more subtle.

107 Since we will add AMR only to the tracer transport, our comparison will be
108 focused on differences in filamentation of tracer clouds as well as resolution of
109 sharp gradients. Our scheme cannot compensate for insufficient scale-awareness
110 of the parameterization and we will rely on the given parameterization schemes.

111 Further details can also be found in our reply to point 36 in the detailed com-
112 ments.

113 We corrected the mistakes in the equations that were due to the intention to
114 simplify our nomenclature (which we obviously failed). We assure the reviewer
115 that these mistakes do not affect our implementations.

116 Since the moving vortices test case rotates around the globe in a 45° angle, we
117 omitted the solid body rotation at this angle. However, we follow the suggestion
118 and present a 45° solid body rotation figure as well. The discussion of the results
119 is also in the revised manuscript.

120 Detailed comments:

- 121 1. The abstract (line 10) states that the AMR data structure is introduced, but this
122 description is missing in the manuscript. Add this information.
- 123 **Answer:** Apologies for the unclarity. We rephrased the abstract. The AMR data
124 structure was introduced in our 2018 paper. So, we added a short description in
125 Section 2.5 (line 263, revised manuscript) and point to the earlier publication.
126 This is reflected by stating that we utilize the data structure (rather than claiming
127 that we introduce it here).
- 128 2. Line 48-49: be more specific what is meant by 'spectral' method since there are
129 many variants. Here, the spectral transform method is meant. Use 'the FFSL
130 scheme' in line 49 to make this sentence clearer.
- 131 **Answer:** Thank you for the suggestion. We changed our text to 'spectral trans-
132 form method' and rephrased the sentence (line 47, revised manuscript).
- 133 3. Line 66: sentence starting with 'By' is not a sentence, rephrase
- 134 **Answer:** We corrected it.
- 135 4. Line 68: An important component of the original FFSL scheme by Lin and Rood
136 (1996) is the use of limiters to avoid numerical oscillations and negative tracer
137 mixing ratios. Later in the manuscript, it is stated that limiters are not used.
138 Please provide insight whether/how such unwanted characteristics in the AMR
139 algorithm are avoided without any limiters.
- 140 **Answer:** We clarified in Section 2 (line 230, revised manuscript) and Section 3
141 (line 335, revised manuscript) that we do not use limiters in the idealized tests,
142 where numerical oscillations are of minor physical importance, but an important
143 diagnostic observable; and adopt limiters in the realistic tests (dust transport)
144 (line 632, revised manuscript).
- 145 5. Line 69: How is the AMR tracer transport discretized in the vertical direction
146 (e.g. vertical remaps). This is important for the dust example (could be included
147 in this section).
- 148 **Answer:** We provide a very short description of the vertical transport in the
149 introduction (line 68, revised manuscript) where we refer to the original paper
150 by Lin and Rood (1996) for the vertical tracer transport. Further details are
151 shown in Section 4.2.1.
- 152 6. Line 104: A more precise explanation is that c is a dimensionless tracer mixing
153 ratio. The phrase 'concentration' implies a physical unit.
- 154 **Answer:** Thank you for pointing this out. We changed the term 'concentra-
155 tion' to 'mixing ratio' throughout the manuscript. This correction goes along the
156 corrections made for the equations.
- 157 7. Eqs. (4)-(7): Unit mismatches in equations and incorrect definition of the ad-
158 vective operators in Eq. (5). In Eq. (4) F is defined as a flux difference with
159 units $kg/(m^3s)$ and is then added to the air density (with units of kg/m^3) in Eqs.

160 (6) and (7). There is no notion of the computation of a time-averaged (time in-
161 tegrated) flux as in Lin and Rood (1996) which is a major error/omission. In
162 addition, the advective operators (Eq. (5)) use wrong math notation. The diver-
163 gence of the scalar u does not exist (also wrong in line 122), and even if u was
164 meant to symbolize the horizontal velocity vector $\vec{v} = \begin{pmatrix} u \\ v \end{pmatrix}$ the equations are
165 still incorrect. As before, a unit mismatch is present in the two terms on the right
166 hand sides (RHS) of Eq. (5). In addition, only $\rho \frac{\partial u}{\partial x}$ contributes to the definition
167 of the advective operator in the x direction, and only $\rho \frac{\partial v}{\partial y}$ can be used in the y di-
168 rection. This should be expressed in spherical geometry. Do these errors impact
169 the implementation?

170 **Answer:** Our apologies for the inaccurate presentation of the equations. We
171 corrected the issue and we can assure the reviewer that these are mistakes in the
172 presentation while implementation is not affected by these mistakes.

173 8. Line 142: typo, should read 'accounts for'

174 **Answer:** Thank you. We corrected it.

175 9. Line 153: the use of the phrase 'could' is confusing. Do you mean 'would'? Is
176 there a condition if case 'could' was intentional?

177 **Answer:** Using 'would' is appropriate. We changed this.

178 10. Line 170: the definition of x is incorrect. ' x ' needs to represent a normalized
179 coordinate that varies between $-1/2$ and $+1/2$ and cannot be defined as the longi-
180 tude (varying between $0 - 2\pi$) or the sine of the latitude. Correct the definition
181 of x .

182 **Answer:** Thank you for pointing it out. Here the definition of ' x ' is simply the
183 length of a single cell in any dimension in the dimensionally split scheme. We
184 now describe the 1-D CISL in the reference coordinate x between $-1/2$ and $+1/2$
185 in a pure 1-D manner and we hope it is clearer.

186 11. Eqs. (11) and (12): More explanations are needed to clarify the computations
187 of the departure points. How is u_a computed? At which spatial positions are u
188 and v assessed? Is there any grid staggering? Are the velocities time-centered or
189 time extrapolated? If yes, how is this accomplished? u and v are typically not
190 constant along long trajectories. Please comment on the specifics. Are iterations
191 needed to compute the trajectories for the semi-Lagrangian transport?

192 **Answer:** We improved Eqs. (11) and (12). We now use $u_{i+\frac{1}{2}}$ instead of u_a and
193 explicitly describe the velocity in cell edges like in Arakawa C-staggering.

194 We also clarify the use of the first-order Euler scheme for computing departure
195 points. The velocity is viewed as constant along the trajectory. We expect that
196 using a higher-order time-stepping can lead to better accuracy. However, the
197 AMR scheme is compared with the original scheme in ECHAM6 and we decide
198 to follow the algorithmic design there.

- 199 12. Fig. 3: add labels that show the $i+1/2$ and $i-1/2$ positions.
200 **Answer:** Thanks for the suggestion. We added that.
- 201 13. Line 190, Eq. (14): it seems as if ΔA needs a subscript. Correct.
202 **Answer:** Thanks for pointing that out. We corrected it.
- 203 14. Eq. (15): incorrect equations for the PPM subgrid distributions. The middle
204 term on the RHS needs to be linear (just x and not x^2 in the upper equation. In
205 the lower equation, the same math error exists for the linear terms. In addition,
206 the normalized coordinates instead of λ and μ need to be used (see point 10).
207 The explanations of PPM also become somewhat sloppy here since Colella and
208 Woodward (1984) do not use the a and b notation for the coefficients and the
209 reader will be guessing how to find the information. An easier way is to point to
210 Carpenter et al. (1990). However, I suggest adding the precise definition of the a
211 and b coefficient, and also come back to the point whether/how (if any) limiters
212 are used for the subgrid distribution.
213 **Answer:** Thank you for the kind suggestion. We clarified that the equation is
214 given in a reference coordinate and cited Carpenter et al. (1990). We also added
215 the definition of a and b with a short description of the limiters, which are used
216 in the dust simulations (line 230, revised manuscript).
- 217 15. Eq. (16): Unit mismatch between symbols F and ρ . The ρ in line 217 misses
218 the superscript $n + 1$.
219 **Answer:** Thanks for pointing it out. This is corrected.
- 220 16. Section 2.4: is it correct that only the wind is interpolated/updated at each time
221 step whereas the AMR tracer distribution is kept from time step to time step?
222 How close to the pole can the refinement go, e.g. just one grid spacing north/south
223 of the poles as suggested later in Fig. 15? It would be helpful to remind the reader
224 in section 2, that the AMR tracer is never averaged back to the Gaussian grid and
225 thereby does not influence the dynamical core computations. Is my understand-
226 ing correct, that the tracers are still also computed on a coarser Gaussian grid in
227 addition to the AMR transport? It seems to be a must for quantities like moisture
228 tracers in real applications.
229 **Answer:**
230 The reviewer's understanding is correct and thanks for the suggestion. We added
231 one paragraph in Section 2.4, stating that the tracer distribution in the AMR
232 model is not affected by the tracer distribution in the coarse-resolution model.
233 The coarse-resolution model runs independently from the AMR method. We
234 also give a clearer explanation regarding the refinement from the poles.
- 235 17. Section 2.5: What is the allowable refinement ratio, e.g. just 1:2? Be clearer
236 what the 'refinement of intermediate steps' means. It is still not clear, even after
237 reading section 3.1. Where exactly are the additional refinement regions for
238 intermediate steps?

- 239 **Answer:** We added a sentence in Section 2.5: "The data structure allows drastic
 240 spatial resolution changes. However, to alleviate numerical oscillations due to
 241 sudden spatial resolution variation, we restrict our simulations to a 1:2 refinement
 242 ratio such that it is locally quasi-uniform. In our idealized tests, we present
 243 results with up to two refinement levels."
- 244 We added text to indicate the exact position of intermediate steps, γ and β , in
 245 the schematic illustration in Fig 1 and point to the Equation 6 to denote the
 246 intermediate step.
- 247 18. Section 2: add some comments about the AMR data structure. Is this an AMR
 248 application that can currently only run on 1 CPU?
- 249 **Answer:** In Section 2.5 we added a summary of the AMR data structure and
 250 clarify that our current implementation is serial but the data structure does indeed
 251 allow for parallelization (line 263, revised manuscript).
- 252 19. Section 3 and 4: add the time step information for all test cases.
- 253 **Answer:** We added time step information for all tests in Section 3 and 4.
- 254 20. Section 3.2.1: add the assessment of the most challenging 45° rotation angle
 255 which exposes the characteristics of the 2D transport. Does the cosine bell test
 256 use analytically initialized wind speeds on the AMR grid (which are analytically
 257 updated when the grid moves) or interpolated winds from a coarser (Gaussian?)
 258 grid? Are these simulations embedded in ECHAM or run with a standalone
 259 version of the AMR code? They seem to be standalone applications since no
 260 reference is made to Gaussian grid resolutions, correct?
- 261 **Answer:** Thank you for your suggestion. We added the 45° using the solid body
 262 rotation test case in Section 3.2.1. On the other hand, the moving vortices test
 263 case rotates in 45° in Section 3.2.3.
- 264 In each subsection, we now provide information whether the wind is analytically
 265 initialized. In Section 3.1, 3.2.1, 3.2.2, the wind is always assigned analytically.
- 266 In the beginning of Section 3, we provide information that the idealized tests use
 267 standalone code, which is then incorporated into ECHAM6. The code always
 268 uses a Gaussian grid.
- 269 21. Line 370: cosbell should read cosine bell
- 270 **Answer:** Thanks for the advice. We changed all cosbell to cosine bell in the
 271 manuscript.
- 272 22. Section 3.2.2: provide information on the wind initialization for this test case
 273 (analytical or interpolated).
- 274 **Answer:** The wind is given analytically for the solid body rotation and the
 275 divergent wind test cases. We provide the information in corresponding sections.
- 276 23. Fig. 14: Why does the curve in the right figure start with a mass variation of
 277 4×10^{-12} instead of 0?

278 **Answer:** We addressed this question in the manuscript. The main reason is that,
279 the plot is normalized by the time-averaged mass. The initial mass is a bit higher
280 than the mean value of the mass.

281 24. Fig. 15: it seems as if the refinement criterion was inadequate (too sensitive)
282 since almost the complete domain is refined at day 12. This is especially true in
283 regions with very little tracer variations. Why was this example chosen instead
284 of a more tailored refinement criterion that focuses the AMR grid on the spirals?

285 **Answer:** We provide a detailed explanation for the result of excessive refinement
286 and our choice of refinement criterion in Section 3.2.3:

287 We use the same gradient-based criterion with different thresholds for all ideal-
288 ized test cases. This avoids focusing on the choice of the refinement criterion
289 in this study and focuses on the effect of AMR in the transport module of an
290 existing model. We expect that the choice of a refinement criterion requires fur-
291 ther investigations, especially in operational settings, to maximize computational
292 efficiency and accuracy.

293 The large refinement area in Figure 15 (Fig. 17 in the revised manuscript) is a
294 result of the gradient-based refinement criterion, which is sensitive to the conver-
295 gence of grid cell sizes towards the poles. The less tailored refinement criterion
296 still shows improved efficiency for the idealized test cases.

297 25. Line 442: what is meant by 'uniform refinement'? Do you mean uniform resolu-
298 tion? There seems to be a contradiction in lines 443 and 444. Line 443 states that
299 experiment 3 uses a wind interpolation. Line 444 refers to an exact (analytical?)
300 wind field for experiment 3. Please clarify.

301 **Answer:** Thank you for spotting this mistake. We clarify the meaning of uniform
302 refinement and corrected the mistake in the description in Section 3.2.3.

303 26. Section 4.1: Comment on the vertical transport of the tracer. How is it handled?

304 **Answer:** We reuse the vertical transport/remapping subroutine of the original
305 ECHAM6 model. A short description of the equation is given in Section 4.2.1
306 of the revised manuscript and readers are referred to the relevant literature for
307 details:

308 Jöckel, P., von Kuhlmann, R., Lawrence, M. G., Steil, B., Brenninkmeijer, C. A.,
309 Crutzen, P. J., Rasch, P. J., and Eaton, B.: On a fundamental problem in imple-
310 menting flux-form advection schemes for tracer transport in 3-dimensional gen-
311 eral circulation and chemistry transport models, Quarterly Journal of the Royal
312 Meteorological Society, 127, 1035–1052, 2001.

313 27. Line 530: typo, needs to read the tendency of the 'tracer density', not tracer
314 concentration.

315 **Answer:** Thanks for the advice. We corrected the term.

28. Eq. (23) and lines 536-539: Does the phrase 'hybrid' refer to a hybrid sigma-
pressure η coordinate? Eq. (23) is not valid for the such a hybrid system and

also does not require the definition of p in line 553. Does the divergence operator imply a 3D divergence or horizontal divergence? The \mathbf{u} vector is undefined (2D or 3D). In a hybrid sigma-pressure system η the tracer transport equation (here written with the symbol q for the tracer mixing ratio) is

$$\frac{\partial}{\partial t} \left(\frac{\partial p}{\partial \eta} q \right) + \nabla \cdot \left(\frac{\partial p}{\partial \eta} q \vec{u} \right) + \frac{\partial}{\partial \eta} \left(\dot{\eta} \frac{\partial p}{\partial \eta} q \right) = 0$$

316 The vertical pressure derivative stands for a pseudo density, velocity vector sym-
 317 bolizes the horizontal velocity vector, and the vertical velocity is $\dot{\eta}$. Please clar-
 318 ify and correct Eq. (23) as needed. Do you refer to a pure σ vertical coordinate
 319 (not hybrid) and if yes, is this the default in ECHAM? The phrase 'the hybrid
 320 coordinate prescribes a vertical pressure distribution' is confusing. Clarify and
 321 rephrase.

322 **Answer:** Thank you for correcting this mistake. The original equation was not
 323 for the hybrid coordinate. We now provide more information on the implemen-
 324 tation of the transport scheme in the η -coordinate in Section 4.2.1.

325 29. Line 544: since no limiters are used comment on the presence of under- and
 326 overshoots, and negative tracer values.

327 **Answer:** Apologies for the unclear sentence. We rephrase the sentence and we
 328 hope it is clear that limiters are not used in the idealized tests but are used in the
 329 dust simulations (line 632, revised manuscript).

330 30. Line 584: what is the position of the model top for the 31-level setup?

331 **Answer:** Added the pressure level at the model top, i.e., $10hPa$.

332 31. Line 590: typo, should read October 1 to October 31

333 **Answer:** Thanks, we corrected it.

334 32. Line 597: provide approximate grid resolutions for T31 and T63 (in degrees or
 335 km).

336 **Answer:** Thanks for the suggestion. We added it.

337 33. Section 4.3.3: The chosen refinement/coarsening thresholds stated in line 562
 338 seem to be inadequate (way to small/sensitive) for the dust simulations. All
 339 the dust figures show color bars with labels between 0.00001-0.00071, which
 340 are orders of magnitude bigger than the AMR criterion. Explain the motivation
 341 for the small AMR thresholds. They will refine areas that are irrelevant. For
 342 example, Fig. 22 (left) shows large refinement areas where there is no obvious
 343 presence of the tracer. The light yellow color scheme is also very difficult to see
 344 on top of the white background. I suggest adjusting the color scheme for all dust
 345 simulations to improve the clarity/readability of the figures.

346 Line 635 suggests a motivation for a small threshold, but why was it enough to
 347 e.g. go with a threshold like 10^{-6} instead of the chosen 10^{-11} ? Provide more
 348 insight.

349 **Answer:** We apologize for the confusing units here for the refinement criterion.
350 Although the refinement criterion is not the purpose of our work, our refinement
351 criterion does not deviate too much away from the plots. The plots use a unit
352 of $mgkg^{-1}$ while the refinement criterion is $10^{-11}kgkg^{-1}$. We now provide a
353 refinement criterion based on the same unit as plots for $10^{-5}mgkg^{-1}$ and we
354 hope it clarifies the concern.

355 We follow the advice to change the color bar of all dust figures and hope it
356 improves the clarity.

357 We also discussed the cause for the large refinement region:

358 We also observe large refined regions in Figure 23. The size of the refined regions
359 is a result of the thresholds used in the refinement criterion. Further optimiza-
360 tion of refinement criteria could potentially alleviate this in future applications.
361 However, a more important reason is that the mesh is refined only horizontally.
362 So, even if a significant amount of tracer concentration is only present in a lower
363 (or higher) level of the atmosphere, the refinement is performed on all levels.
364 Finally, another reason for such large refined regions is that four different dust
365 tracers share the same adaptive mesh. Using different adaptive meshes can be
366 desirable when the number of tracers is high but it can affect the reuse of the
367 departure point computations. One of the benefits of multi-tracer efficiency in
368 the semi-Lagrangian scheme arises from the capability to reuse departure points
369 of trajectories. As a compromise, putting tracers into groups sharing the same
370 (adaptive) mesh may achieve a better balance between individual adaptivity of
371 meshes and the multi-tracer efficiency in semi-Lagrangian schemes.

372 We note that even with the non-optimal refinement criterion the one-way cou-
373 pled dust simulation on an adaptive mesh requires on average 9062 cells over
374 the 30 days simulation, while the uniformly high-resolution transport mesh re-
375 quires 17280 cells. This difference highlights the potential efficiency gain from
376 adaptive mesh refinement.

377 34. Page 32: Fig. 21 can be deleted. The left column of Fig. 21 is a repetition of the
378 data in Fig. 20 (left column) and the right column is indistinguishable (by eye)
379 from the left column. It is sufficient to state this in one sentence.

380 **Answer:** As suggested, we removed Fig. 21 from the manuscript.

381 35. Fig. 22: incorrect figure caption

382 **Answer:** Thanks for pointing out. It is indeed unclear. We changed the text
383 here.

384 36. Section 4.3.3: The dust example is problematic since there is no reference solu-
385 tion (T31 and T63 simulations differ greatly). Was the uniform-resolution dust
386 simulation also conducted at higher resolutions like T127 to understand this bet-
387 ter? If there is no trusted uniform resolution reference solution, it is unclear how
388 to judge any AMR simulation and to see the added value. For example, I cannot
389 see the AMR improvements in Fig. 23 (right) since they have no resemblance

390 with the T63 simulation (Fig. 20 right) in the refined patch. This assumes that
391 T63 is the 'more correct' simulation. Make this clearer in the discussion.

392 **Answer:** We understand reviewer's concerns for the dust simulations and we
393 made some text changes and hope it can clarify these concerns.

394 In Section 4.3.2, we added:

395 These simulations show an important fact of multi-physics simulations: there ex-
396 ist subgrid-scale parameterizations that inhibit convergence in a classical mathe-
397 matical sense. The differences between $T31$ and $T63$ horizontal resolution sim-
398 ulations are not caused by increased resolution in the dynamical core, but also
399 and predominantly by the necessary change in parameterizations due to the in-
400 creased resolution. In particular, Gläser et al. (2012) showed that the dust emis-
401 sion scheme is sensitive to different horizontal resolutions. The observed dust
402 mixing ratio is affected also by wet and dry deposition, which itself is affected
403 by cloud and convection parameterizations. These results indicate that we can-
404 not use a high-resolution simulation as a converged state quasi reference solution.
405 Our analysis of accuracy will therefore be more subtle.

406 Since we will add AMR only to the tracer transport, our comparison will be
407 focused on differences in filamentation of tracer clouds as well as resolution of
408 sharp gradients. Our scheme cannot compensate for insufficient scale-awareness
409 of the parameterization and we will rely on the given parameterization schemes.

410 In Section 4.3.3, we added:

411 There are multiple sources for uncertainties in low-resolution simulations. The
412 coarse initial condition and boundary condition can lead to less accurate results
413 while the coarse resolution dynamical core and parameterizations cannot resolve
414 the finer features of the atmosphere.

415 The results from our idealized tests in Section 3 show that, using AMR in the
416 tracer transport module can effectively reduce the numerical error of the tracer
417 transport process. Using an interpolated wind field with a coarse resolution initial
418 condition can still improve the numerical accuracy of passive tracer transport
419 schemes. It is promising that we can treat one source of error by using AMR in
420 coarse resolution climate simulations.

421 Since we observed in the previous paragraph that uniform refinement of the
422 whole atmosphere model does not yield a converged solution, usable as a ref-
423 erence, we adopt the following approach. We will use a dust transport scheme
424 run on a uniform high resolution $T63$ grid, coupled to a coarse $T31$ dynamical
425 core with corresponding low-resolution parameterizations. This solution, shown
426 in the left panel of Figure 23, will serve as a reference for our adaptive mesh
427 simulations.

428 37. Line 667: without any 2-way interaction, the practical value of the AMR tracer
429 transport is limited. It would be good to highlight the current study as a first step
430 towards to full functionality of the AMR approach.

431 **Answer:** Thank you for your suggestion. We added corresponding remarks in
432 the discussion.

433 **References**

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435 sensitivity to the spectral resolution and the dust emission scheme, *Atmospheric*
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