# BioRT-Flux-PIHM v1.0: a watershed biogeochemical reactive transport model

Wei Zhi[1], Yuning Shi[2], Hang Wen[1], Leila Saberi[3], Gene-Hua Crystal Ng[3], ~~Li Li[1,*]~~Kayalvizhi Sadayappan[1], Devon Kerins[1], Bryn Stewart[1], Li Li[1,*]

[1] Department of Civil and Environmental Engineering, The Pennsylvania State University, State College, PA 16802, USA

[2] Department of Ecosystem Science and Management, The Pennsylvania State University, State College, PA 16802, USA

[3] Department of Earth and Environmental Sciences, University of Minnesota, Twin Cities, MN 55455, USA

[*] Correspondence to lili@engr.psu.edu

## Abstract

Watersheds are the fundamental Earth surface functioning unit that connects the land to aquatic systems. ~~Existing~~Many watershed-scale models ~~typically have physics-based~~represent hydrological processes but often lack the representation of ~~hydrology process but often lack mechanism-based,~~ multi-component reactive transport processes that are relevant to soil and aquatic biogeochemical reactions. The lack of mechanism-based representation of reaction thermodynamics and kinetics~~. This lack of~~ at the watershed ~~reactive transport models~~scale has limited our ability to understand and predict solute export and water quality, particularly under changing climate and anthropogenic conditions. Here we present a recently developed BioRT-Flux-PIHM (~~BFP~~BioRT hereafter) v1.0, a watershed-scale biogeochemical reactive transport model. Augmenting the previously developed RT-Flux-PIHM that integrates land-surface interactions, surface hydrology, and abiotic geochemical reactions (Bao et al., 2017, WRR), the new development enables the simulation of 1) biotic processes including plant uptake, soil respiration, and ~~microbe-~~microbially mediated ~~biogeochemical~~ reactions ~~that are relevant to the~~such as carbon decomposition and nutrient transformation ~~of organic matter that involve carbon, nitrogen, and phosphorus~~; and 2) shallow and deep water partitioning to represent surface, shallow groundwater, and deep groundwater interactions**.** The reactive transport part of the code has been verified against the widely used reactive transport code CrunchTope. BioRT-Flux-PIHM v1.0 has recently been applied to understand reactive transport processes in multiple watersheds ~~across different~~under diverse climate, vegetation, and ~~geology~~geological conditions. This paper briefly introduces the governing equations and model structure ~~of the code.~~with a focus on new model developments. It also ~~demonstrates examples~~ showcases one hydrology example that ~~simulate~~simulates shallow and deep water interactions, and two biogeochemical ~~reactive transport~~ examples relevant to nitrate and dissolved organic carbon (DOC). These examples ~~were~~are illustrated in two simulation modes of varying complexity. One is the spatially ~~implicit mode~~lumped mode (i.e., two land cells connected by one river segment) that focuses on processes and average behavior of a watershed. Another is ~~in a~~the spatially ~~explicit~~distributed mode (i.e., hundreds of cells) that includes details of topography, land cover, and soil property conditions. The spatially ~~explicit~~distributed

mode can be used to understand the impacts of spatial structure and identify hot spots of biogeochemical reactions.

## 1. Introduction

Watersheds are the fundamental Earth surface units that receive and process water, mass, and energy ~~(Li, 2019).~~(Li, 2019;Li et al., 2020;Ranalli and Macalady, 2010;Hubbard et al., 2018;Seyfried et al., 2018). Watershed processes include land~~-~~surface interactions that regulate evapotranspiration and discharge, and water partitioning between shallow soil lateral flow going into streams versus downward flow and recharge into the deeper subsurface (Edwards et al., 2015) (Figure 1). Complex biogeochemical interactions also occur ~~between~~among soil, water, roots, and ~~microbe~~microbes, dictating ~~the $CO_2$~~gas effluxes (e.g., $CO_2$) via soil respiration, export of ~~soil~~solute products derived from chemical weathering and ~~biotransformation, and nutrient cycling (Fatichi et al., 2019;van der Velde et al., 2010).~~biogeochemical transformation (Fatichi et al., 2019;van der Velde et al., 2010;Grathwohl et al., 2013).

These hydrological and biogeochemical processes determine how ~~Earth~~land surface responds to external forcings such as hydroclimatic drivers and human perturbations ~~(van der Velde et al., 2014;Miller et al., 2020;Han et al., 2019;Steimke et al., 2018).~~(van der Velde et al., 2014;Miller et al., 2020;Han et al., 2019;Steimke et al., 2018). Understanding these processes ~~remain~~remains challenging due to the complex coupling of land surface processes, hydrology, and biogeochemical reactions ~~(Kirchner, 2003).~~(Kirchner, 2003). An example is the concentration-discharge (C-Q) relationships of solutes at stream and river outlets. These relationships encode the integrated signature of ~~Earth~~land surface ~~response~~responses to changes in hydrological conditions~~.~~ (Brooks et al., 2015;Zhi et al., 2020;Zhi and Li, 2020). Similar C-Q relationships have been observed for some solutes ~~–~~across watersheds under diverse ~~geology~~geological and ~~climate~~climatic conditions ~~(Godsey et al., 2009;Basu et al., 2010;Moatar et al., 2017;Zarnetske et al., 2018),~~(Godsey et al., 2009;Basu et al., 2010;Moatar et al., 2017;Zarnetske et al., 2018;Godsey et al., 2019), whereas different solutes have shown contrasting patterns in the same watershed ~~(Miller et al., 2017;Herndon et al., 2015;Zhi et al., 2019;Musolff et al., 2015).~~(Miller et al., 2017;Herndon et al., 2015;Zhi et al., 2019;Musolff et al., 2015). A general theory that can explain contrasting C-Q observations (e.g., flushing vs. dilution behaviors) under diverse watershed characteristics and forcing

conditions remains elusive. The lack of understanding of mechanisms ~~that govern~~governing hydrological and biogeochemical interactions presents major roadblocks for forecasting water quality ~~such that~~, including water issues such as eutrophication that persist worldwide.

One of the challenges ~~along these lines~~to answering questions relevant to water quality and biogeochemical reactions is the lack of modeling tools that mechanistically link hydrological and biogeochemical processes at the watershed scale. Model development has been advancing ~~primarily~~separately within the disciplinary boundaries of hydrology and biogeochemistry ~~(Li, 2019). Hydrology models that~~(Li, 2019). Hydrologic models focus on solving for water storage and fluxes at the watershed scale and beyond ~~(Fatichi et al., 2016), and reactive~~(Fatichi et al., 2016). Reactive transport models (RTMs) ~~that center on aqueous and solid concentration changes arising from~~have traditionally centered on transport and multi-component biogeochemical reactions typically in ~~"closed"~~ groundwater systems ~~without much~~, which often have limited interactions with ~~"open" watersheds directly receiving precipitation and sunlight (Steefel et al., 2015;Li et al., 2017b;Mayer et al., 2002;MacQuarrie and Mayer, 2005). This comes along with a history of hydrologists often trained as physicists studying fluid mechanics, and biogeochemists typically grow up as geologists, chemists, or~~climate and other surficial watershed processes (Steefel et al., 2015;Li et al., 2017b;Mayer et al., 2002). Biogeochemical reactions in shallow soils that are often driven by environmental ~~engineers~~factors such as soil temperature and moisture cannot be well simulated in these models.

~~Recent works have shown some integration across these two lines. Examples include HSPF (Hydrological Simulation Program – FORTRAN) (Filoso et al., 2004;Laroche et al., 1996), SWAT (Soil & Water Assessment Tool) (Gassman et al., 2007;Lam et al., 2010;Moriasi et al., 2013;Neitsch et al., 2011), CATHY (Catchment Hydrology) (Gatel et al., 2019;Scudeler et al., 2016), PAWS (Process-based Adaptive Watershed Simulator) (Niu and Phanikumar, 2015;Qiu et al., 2019). These models have relatively crude representations of solute leaching out of element bulk mass as part of the solute export. These models do not represent kinetics and thermodynamics of multi-component biogeochemical reactions typically done in reactive transport models (RTMs).~~

~~In filling in this model development need, recently we developed the watershed reactive transport code RT-Flux-PIHM that integrates kinetics and thermodynamics of multi-component geochemical reactions with the land-surface and hydrology model Flux-PIHM (Bao et al., 2017). The geochemical reactions in RT-Flux-PIHM are abiotic, including mineral dissolution and precipitation, aqueous and surface complexation, and ion exchange reactions.~~

~~This manuscript introduces BioRT-Flux-PIHM (BFP~~Previous modeling works has shown some integration across these two lines. For example, SWAT (Soil & Water Assessment Tool) (Gassman et al., 2007;Lam et al., 2010;Moriasi et al., 2013;Neitsch et al., 2011) includes a version that couples with the groundwater model MODFLOW and simulates surface water and groundwater quality in RT3D (Bailey et al., 2017; Ochoa et al., 2020). CATHY (Catchment Hydrology) includes processes of pesticide decay (Gatel et al., 2019;Scudeler et al., 2016). Some other hydrological models, including Hydrologiska Byråns Vattenbalansavdelning (HBV) and the Hydrological Predictions for the Environment (HYPE), also have modules that simulate processes relevant to nutrients and contaminants (Lindström et al., 2005;Lindström et al., 2010). While many of these models can simulate reaction processes such leaching of nutrients from agriculture lands (Lindström et al., 2005;Lindström et al., 2010;Bailey et al., 2017), most of them do not explicitly solve the multi-component reactive transport equations. In other words, they have relatively crude representations of solute leaching out of element bulk mass as part of the solute export but do not represent kinetics and thermodynamics of multi-component biogeochemical reactions typically included in reactive transport models (RTMs). They also do not simulate processes such as chemical weathering. As an example, nutrient leaching is often calculated based on empirical equations without explicitly solving reactive transport equations. Reaction rates are often represented using first-order decay (Gatel et al., 2019), assuming reaction rate constants do not change with time and environmental conditions. However, biogeochemical processes including carbon decomposition and nutrient cycling are highly variable in space and time, depending on local environments such as substrate availability, soil temperature, and soil moisture (Li et al., 2017a;Suseela et al., 2012;HARTLEY et al., 2007). In filling in this model need, recently we augmented our watershed model RT-Flux-

PIHM (Bao et al., 2017) with new developments of microbially mediated reactions, which allows us to model the interactions between biogeochemical reactions and environmental factors that are driven by land surface and hydrological processes.

This manuscript introduces BioRT-Flux-PIHM (BioRT hereafter) v1.0, augmented based on RT-Flux-PIHM with two new additions. One is the capability of simulating biotic processes including plant uptake of nutrients, soil respiration, and ~~microbe-~~microbially mediated reactions in the soil. ~~These soil processes~~ Examples include the ~~transformation of fresh and old organic matter, for example,~~ soil respiration that produces $CO_2$ and carbon decomposition that generates dissolved organic carbon (DOC), and other nutrient ~~cyclings~~ transformation processes such as nitrification and denitrification. The other is the introduction of ~~a~~an optional deeper layer below the shallow soil that enables the simulation of interactions of deep water and shallow soil water flow (Figure 1). Here the deep water is loosely defined as the water beyond the soil zone, typically in less weathered, fractured subsurface that harbors ~~the~~ relatively old and slow-moving groundwater contributing to streams. This contrasts ~~the~~with shallow water in highly permeable soils. Mounting evidence in recent years has shown that ~~the~~ deeper water beyond the shallow soil interacts with streams, ~~brings~~introduces water with distinct chemistry, sustains base flow in dry times, and buffers climate variability ~~(Gurdak, 2017;Green, 2016;Taylor et al., 2013;Condon et al., 2013;Anyah et al., 2008;Maxwell et al., 2011;Gleeson et al., 2015). They are therefore~~(Gurdak, 2017;Green, 2016;Taylor et al., 2013;Condon et al., 2013;Anyah et al., 2008;Maxwell et al., 2011;Gleeson et al., 2015). Stream chemistry often reflects the distinct chemistry from the shallow soil and deeper groundwater zones, i.e., the so called Shallow and Deep Hypothesis (Zhi et al., 2019;Zhi and Li, 2020). Deeper groundwater is thus a fundamental component of the hydrologic cycle and water budget. The groundwater-surface water interactions can also modulate land-atmospheric energy exchanges and soil moisture dynamics~~.~~ (Keune et al., 2016;Martínez-de la Torre and Miguez-Macho, 2019). Including the deep water component ~~therefore~~thus enables the simulation of such interactions and the dynamics of water quality.

This paper introduces new developments in the ~~governing equations,~~BioRT model ~~structure and capabilities of BFP. The biogeochemical reactive transport~~. The code has been verified against the widely used reactive transport code CrunchTope (Supporting Information~~).~~., SI). This paper briefly overviews water and energy related processes incorporated in the model. Readers are referred to previous publications for more details of processes such as evapotranspiration (ET), hydrological flow, and abiotic reactions (Shi et al., 2013;Bao et al., 2017;Li et al., 2017a;Qu and Duffy, 2007). We showcase ~~the model using two examples~~ three examples that illustrate the new model capabilities and the simulation of ~~varying complexity: one~~biogeochemical reactions. The first hydrological example shows the surface water and groundwater interactions. This second example focuses on nitrate ~~processes run~~transformation and transport in a spatially ~~implicit~~lumped mode~~; another on~~. The third example examines the production and ~~transport~~export of ~~dissolved organic carbon (~~DOC~~) in a spatially explicit mode~~ with the representation of spatial details. The source code and the examples shown here are hosted ~~in~~on the ~~Github page~~GitHub website (https://github.com/PSUmodeling/BioRT-Flux-PIHM).

## 2. Model ~~description~~overview

~~BioRT-Flux-PIHM integrates different processes in three modules (Figure 1). The Flux module is for land-surface interaction processes including surface energy balance, solar radiation, and evapotranspiration (ET) (Shi et al., 2013). The hydrology module PIHM simulates water processes including precipitation, interception, infiltration, recharge, surface runoff, subsurface lateral flow, and deep water flow (Qu and Duffy, 2007). The BioRT module is for multi-component biogeochemical reactive transport processes including microbe-mediated redox reactions (e.g., carbon decomposition and nutrient transformation), ion exchange, aqueous and surface complexation, and mineral dissolution and precipitation.~~

BioRT-Flux-PIHM integrates three modules (Figure 1). The Flux module is for land-surface processes including surface energy balance, solar radiation, and ET (Shi et al., 2013). The hydrology module PIHM simulates water processes including precipitation,

interception, infiltration, recharge, surface runoff, subsurface lateral flow, and deep water flow (Qu and Duffy, 2007). The BioRT module simulates solute transport, bio-relevant processes such as plant uptake of nutrients from water, and multi-component reactions. The reaction processes can include soil respiration, microbially mediated redox reactions (e.g., soil respiration, carbon decomposition and nutrient transformation), ion exchange, aqueous and surface complexation, and mineral dissolution and precipitation. Note that geochemical reactions in our previous RT-Flux-PIHM are abiotic (Bao et al., 2017), including mineral dissolution and precipitation, aqueous and surface complexation, and ion exchange reactions.

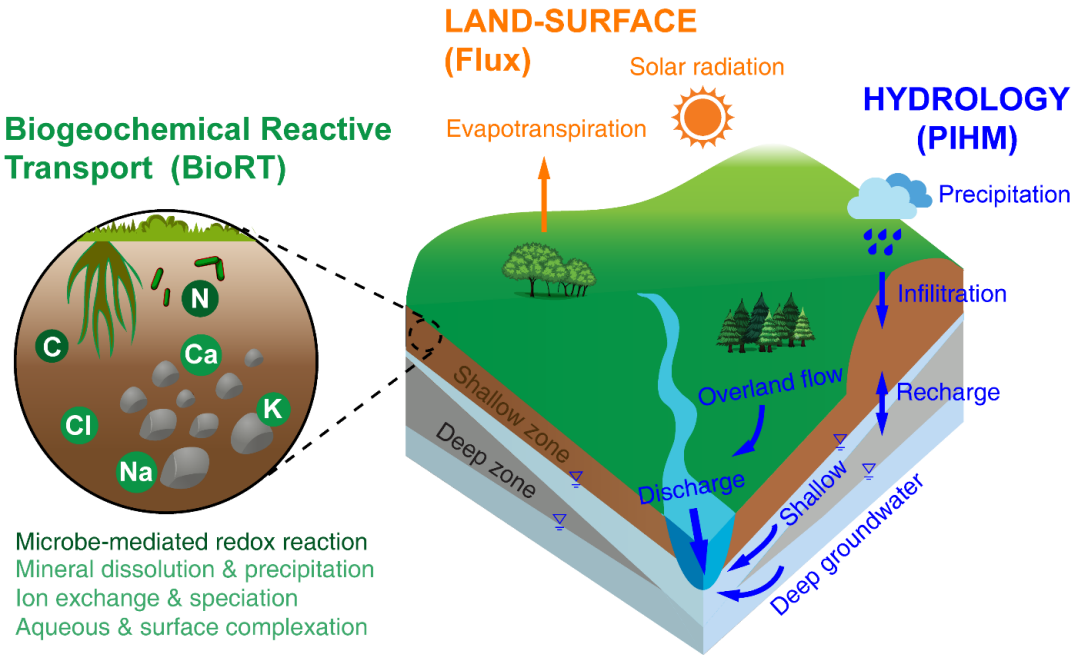



**Figure 1.** A conceptual diagram for processes at the watershed scale. This includes land surface ~~land~~ interactions such as energy balance, solar radiation, evapotranspiration (e.g., evaporation, transpiration, and snow sublimation); hydrological processes partitioning water between surface runoff, shallow soil water ~~lateral flow~~, and deeper water entering the stream~~; and soil~~. Soil biogeochemical reactions ~~including~~include abiotic reactions (e.g., mineral dissolution and precipitation, ion exchange, surface complexations), and biotic processes such as soil respiration, plant uptake of nutrients, and other microbe-mediated reactions such as ~~the~~ transformation of carbon and nitrogen. These processes are represented in three modules: ~~the~~The Flux module for land-surface ~~interaction processes~~interactions, the PIHM module for catchment hydrology ~~processes~~, and the recently augmented BioRT module for ~~soil~~ biogeochemical ~~reaction processes~~reactions. Conceptually the shallow ~~water~~ zone ~~includes~~is the shallow ~~subsurface such as~~ soil and weathered zone that are more conductive to water flow (e.g., soil lateral flow or

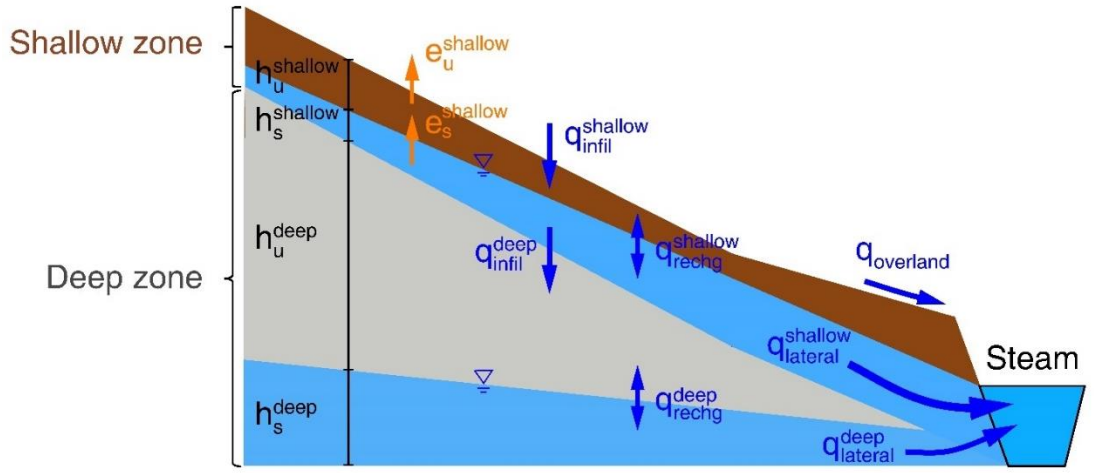
interflow). The deep zone refers to the less weathered~~, fractured~~ zone that often harbors the relatively old and slow flowing ~~water that contributes to stream flow.~~groundwater. Reactions can occur in both shallow and deep zones. For the BioRT, the light and dark greens refer to abiotic and biological reactions, respectively.

The land surface and hydrology modules ~~are coupled to~~ solve for soil temperature and water storage, from which water fluxes can be quantified for surface runoff, shallow and deep water fluxes. The BioRT module uses the calculated soil temperature, water storage, and water fluxes to simulate advection, diffusion~~ / /~~dispersion, and biogeochemical reactions in both shallow and deep zones~~.~~ (see governing equations in later sections). The reactions can be ~~kinetics-~~kinetically controlled (e.g., microbial redox reaction) or ~~thermodynamically~~ equilibrium-controlled (e.g., ion exchange, surface complexation (sorption), and aqueous complexation). Users can define the ~~type~~types of reactions to be included and the form of reaction kinetics in ~~the~~ input files. The output of BioRT includes the spatial distribution and time series of aqueous and solid concentrations ~~in shallow and deep zones and in stream water~~, from which we can also infer reaction rates.

The simulation domain ~~can be discretized into~~is structured as prismatic grids based on topography. Each grid is partitioned into surface and shallow and deep subsurface layers. The surface layer calculates water flow above ground (surface runoff). The shallow ~~subsurface~~zone is loosely defined as the highly permeable subsurface that ~~are most conductive to water flow,~~is contrasting to the deep zone that is broadly defined as the lower permeability zone beyond the shallow zone. In many places, this shallow zone is the soil zone that is most conductive to water flow (e.g., soil lateral flow) and is ~~very~~ responsive to hydroclimatic ~~forcing~~forcings. The deep subsurface zone is the less weathered~~, fractured~~ layer that harbors the relatively ~~old~~older and ~~slow~~slower flowing ground water that contributes to stream flow. Note that these definitions differ from those in the hydrology community, which often ~~refer~~refers to the shallow soil water flow or lumped shallow soil as groundwater, in a way that distinguishes it from the surface runoff ~~(Winter et al., 1998;Dingman, 2015;Todd and Mays, 2005). As illustrated in Figure 1, both shallow~~ (Winter et al., 1998;Dingman, 2015;Todd and Mays, 2005). These shallow and

deep ~~zone~~waters often have ~~unsaturated~~distinct solid and ~~saturated layers, enabling the simulation~~water chemistry, and are dominant at different time of the ~~"two water tables" (Brantley et al., 2017). These transient water tables~~year, as have been observed ~~in~~and inferred in many catchments and watersheds (Brantley et al., 2018;Zhi et al., 2019;Zhi and Li, 2020;Li et al., 2020;Sullivan et al., 2016). Despite the model complexity, the model is flexible for taking inputs from online data portals or local measurements and it can accommodate low data availability (see the following section of ~~Shale Hills, Garner Run, and Cole Farm (Li et al., 2018;Brantley et al., 2018).~~5 for data need and domain setup). The model is developed as a research tool to understand coupled watershed processes rather than as a policy model to guide management.

## 3. Governing equations and processes



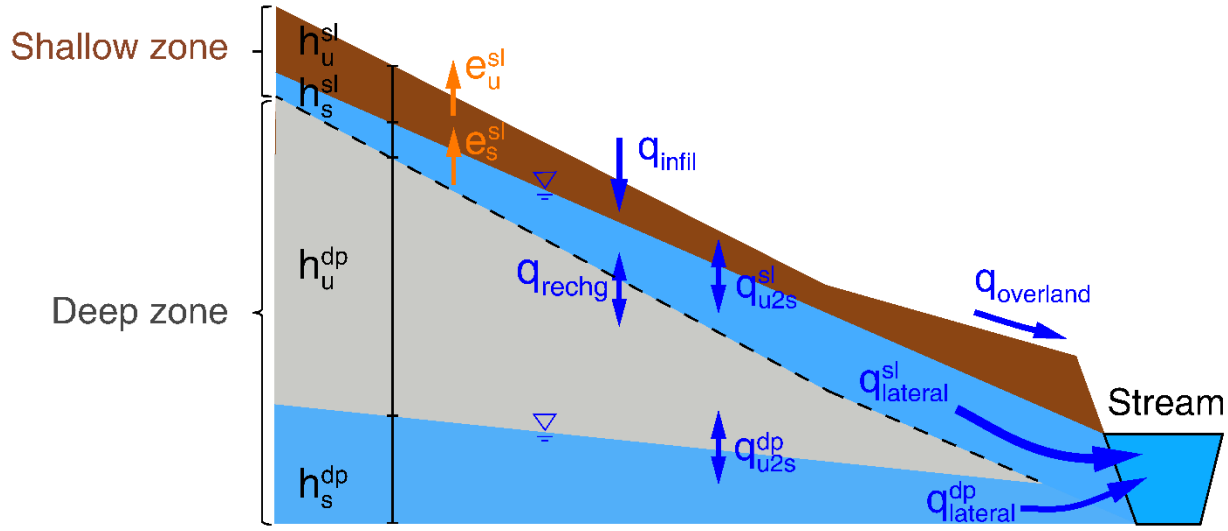



**Figure 2.** Hillslope view of the shallow and deep zones and relevant water flows. The symbol of "h", "e", and "q" denotes water ~~head,~~storage [m], evapotranspiration~~,~~ [m/s], and water flow~~,~~ [m/s], respectively. The superscript letter "sl" and "dp" refer to shallow and deep zone, respectively. The subscript ~~letter~~letters "u" and "s" ~~refers~~refer to unsaturated and saturated layer, respectively. Detailed equations are listed in the following sections. The terms "infil", "u2s", and "recharge' refer to infiltration, unsaturated to saturated zones, and recharge.

### 3.1 ~~The water~~Water equations ~~in~~

The original Flux-PIHM simulates surface runoff and a lumped subsurface flux into streams without distinguishing shallow ~~and deep~~soil water flow and deeper groundwater flow. In working with stream water chemistry data, we realized that a lumped subsurface flow cannot describe the dynamics of stream chemistry, as the shallow soil water and deeper groundwater have distinct chemistry and are dominant at different times of the year (Zhi et al., 2019; Zhi and Li, 2020). We therefore added an optional deeper groundwater zone in the code to simulate the deeper water that interacts with streams. Each prismatic element now has three zones in the vertical direction: surface (or above ground), shallow and deep zones in the subsurface.

~~As shown in Figure 2, in~~In each prismatic element $i$, the shallow zone ~~has~~includes unsaturated and saturated water storages~~.~~. The unsaturated zone receives water from the surface via infiltration and ~~interactions between the two storages~~only flows vertically to the saturated zone. The saturated zone flows both vertically to the deep zone

(recharge) and laterally to neighboring grids $j$ or the stream (lateral). The code solves the following equations for the shallow zone:

$$\theta^{shallow}\frac{dh_u^{shallow}}{dt} = q_{infil}^{shallow} - q_{rechg}^{shallow} - e_u^{shallow} \quad (1)$$

$$\theta^{shallow}\frac{dh_s^{shallow}}{dt} = q_{rechg}^{shallow} - q_{infil}^{deep} - e_s^{shallow} + \sum_{ij}^{1} q_{lateral\_ij}^{shallow} \quad (2)$$

$$\theta_i^{sl}\frac{dh_{i,u}^{sl}}{dt} = q_{i,inf} - q_{i,u2s}^{sl} - e_{i,u}^{sl} \quad (1)$$

$$\theta_i^{sl}\frac{dh_{i,s}^{sl}}{dt} = q_{i,u2s}^{sl} - q_{i,rechg} - e_{i,s}^{sl} + \sum_{1}^{N_{ij}} q_{ij}^{sl} \quad (2)$$

Where $h_u^{shallow}$ and $h_s^{shallow}\theta_i^{sl}$ [m$^3$ pore space/m$^3$ total volume] is the shallow zone porosity in the element $i$; $h_{i,u}^{sl}$ and $h_{i,s}^{sl}$ [m] are the unsaturated and saturated water storage in the shallow zone, respectively; $\theta^{shallow}$ is the shallow zone porosity; $q_{infil}^{shallow}$ and $q_{infil}^{deep}$. Note that the storages $h$ here are the shallow and deep essentially the height of soil column with equivalent saturated water, not the height of the pure water (100% volume) column. That is why porosity is in the equation. For saturation zones, this height is needed to quantify the depths of water tables and determines the direction of water flow between neighboring grids. The $q_{i,inf}$ [m/s] is the infiltration rate from the surface to the shallow zone and from the shallow to the deep zone, respectively; $q_{rechg}^{shallow}$ and $q_{rechg}^{deep}$ are the recharge ; $q_{i,u2s}^{sl}$ [m/s] is the vertical flow from the unsaturated layer to the saturated layer in the shallow and deep zones, respectively; $e_u^{shallow}$zone; $q_{i,rechg}$ [m/s] is the recharge rate from the shallow zone to the deep zone; $e_{i,u}^{sl}$ and $e_s^{shallow}e_{i,s}^{sl}$ [m/s] are shallow evapotranspiration (ET) from the unsaturated and saturated layer (Shi, 2012),in the shallow zone, respectively; $q_{lateral\_ij}^{shallow}$ is the shallow normalized$q_{ij}^{sl}$ [m/s] are the lateral fluxflows in the shallow saturated layer frombetween the element $i$ toand its neighbor element $j$ ($\leq 3$).; $N_{ij}$ ($\leq 3$) is the number of neighbor elements $j$. For a prismatic element $i$, a boundary cell could have one or two neighbors; a non-boundary cell has three neighbors. The ET is calculated by the Penman potential evaporation scheme and

detailed equations can be found in Shi (2012). A similar set of water equations for the deep zone are in the SI (Eqn. S1 and S2).

Infiltration and ~~recharge~~vertical fluxes from the unsaturated to the saturated layer in the shallow zone ~~for the elements $i$ are calculated using~~are based on the Richards equation, in which hydraulic water head $H$ (i.e., the summation of water storage $h$ and elevation head $z$) and hydraulic conductivity $K$ are used to determine the fluxes in each element $i$:

~~$$q_{infil}^{shallow} = AK_{infil}^{shallow} \frac{H_{sur} - H_{u}^{shallow}}{D_{inf}} \quad (3)$$~~

~~$$q_{rechg}^{shallow} = AK_{effV}^{shallow} \frac{H_{u}^{shallow} - H_{s}^{shallow}}{0.5D_{shallow}} \quad (4)$$~~

$$q_{i,inf} = K_{i,inf} \frac{H_{i,sur} - H_{i,u}^{sl}}{d_{i,inf}} \quad (3)$$

$$q_{i,u2s}^{sl} = K_{i,V}^{sl} \frac{H_{i,u}^{sl} - H_{i,s}^{sl}}{0.5d_i^{sl}} \quad (4)$$

Where ~~$A$ is the element area in the vertical direction; $D_{inf}$~~$d_{i,inf}$ and ~~$D_{shallow}$~~$d_i^{sl}$ [m] are the thickness of infiltration ~~(0.1 m)~~layer and shallow ~~layer~~zone depth for the elements $i$, respectively; ~~$K_{infil}^{shallow}$ and $K_{effV}^{shallow}$ are the infiltration and effective~~ $K_{i,inf}$ [m/s] is the hydraulic conductivity ~~in the vertical direction in the shallow zone, respectively;~~of the infiltration layer, the top 0.1 m of the subsurface and is considered to have different conductivity from the rest of subsurface; $K_{i,V}^{sl}$ [m/s] is the hydraulic conductivity in the vertical direction (i.e., weighted average of macropore $K_{i,macV}$ and soil matrix $K_{i,satV}$, Eqn. S7); ~~$H_{sur}$~~$H_{i,sur}$ [m] is the surface hydraulic water head (= ~~$h_{sur}$~~$h_{i,sur}$ + ~~$z_{sur}$~~$z_{i,sur}$ ); ~~$H_{u}^{shallow}$~~$H_{i,u}^{sl}$ and ~~$H_{s}^{shallow}$~~$H_{i,s}^{sl}$ [m] are the shallow hydraulic water ~~head~~heads in the unsaturated and saturated layer, respectively. ~~Shallow~~The lateral flow in the shallow saturated layer is calculated using Darcy's law:

~~$$q_{lateral\_ij}^{shallow} = A_{ij} K_{effH\_ij}^{shallow} \frac{(H_{s}^{shallow})_i - (H_{s}^{shallow})_j}{D_{ij}} \quad (5)$$~~

$$q_{ij}^{sl} = K_{ij}^{sl} \frac{H_{i,s}^{sl} - H_{j,s}^{sl}}{d_{ij}} \quad (5)$$

Where ~~$A_{ij}$ is the projection area of the saturated layer between elements $i$ and $j$; $D_{ij}$ is the~~ $d_{ij}$ [m] is the distance between the centers of elements $i$ and $j$; ~~$K_{effH\_ij}^{shallow}$~~ $K_{ij}^{sl}$ [m/s] is the harmonic mean of shallow ~~effective~~ hydraulic conductivity in the horizontal direction ~~$(K_{effH}^{shallow})$~~ between elements $i$ $(K_{i,H}^{sl})$ and $j$ ~~.~~ $(K_{j,H}^{sl})$. The interaction between the shallow saturated zone and stream channel also follows ~~the~~ Eq. (Eqn. 5~~), where~~ , except that the adjacent head is replaced by the level of the channel water.

Similar to the shallow zone, hydrological equations in the deep zone ~~in each element $i$ can have unsaturated and saturated storages, with unsaturated-saturated flow within $i$.~~ are detailed in the SI (Eqn. S1 – S8).

$$\theta^{deep} \frac{dh_u^{deep}}{dt} = q_{infil}^{deep} - q_{rechg}^{deep} \quad (6)$$

$$\theta^{deep} \frac{dh_s^{deep}}{dt} = q_{rechg}^{deep} + \sum_{j}^{1} q_{lateral\_ij}^{deep} \quad (7)$$

~~Where $h_u^{deep}$ and $h_s^{deep}$ are the unsaturated and saturated storages in the deep zone, respectively; $\theta^{deep}$ is the deep zone porosity; $q_{rechg}^{deep}$ is the deep recharge flux from the unsaturated layer to the saturated layer; $q_{lateral\_ij}^{deep}$ is the deep normalized lateral flux from element $i$ to its neighbor $j$ ($\leq 3$).~~

~~Deep lateral flow is calculated using Darcy's law:~~

$$q_{lateral\_ij}^{deep} = A_{ij} K_{effH\_ij}^{deep} \frac{(H_s^{deep})_i - (H_s^{deep})_j}{D_{ij}} \quad (8)$$

~~Where $H_s^{deep}$ is the deep hydraulic water head; $K_{effH\_ij}^{deep}$ is the harmonic mean of the deep effective hydraulic conductivity in the horizontal direction ($K_{effH}^{deep}$) between elements $i$ and $j$.~~

~~Deep infiltration and recharge fluxes are similarly calculated using the Richards equation as in the shallow zone:~~

$$q_{infil}^{deep} = AK_{infil}^{deep} \frac{H_s^{shallow} - H_u^{deep}}{0.5\left[H_s^{shallow} + \left(D^{deep} - H_s^{deep}\right)\right]} \quad (9)$$

$$q_{rechg}^{deep} = AK_{effV}^{deep} \frac{H_u^{deep} - H_s^{deep}}{0.5D^{deep}} \quad (10)$$

Where $K_{infil}^{deep}$ is the hydraulic conductivity of infiltration from the shallow zone to the deep zone; $D^{deep}$ is the thickness of the deep zone; $K_{effV}^{deep}$ is the effective hydraulic conductivity in the vertical direction of the deep zone.

The deep groundwater can also come from regional groundwater aquifers, which can set up as an influx from the boundary of the domain. Deep groundwater interacts with river channel via the shallow zone. When the level of deep groundwater is higher than the depth to the deep zone, i.e., the shallow transient groundwater and the deep groundwater are connected, the deep groundwater can flow into the transient saturated layer in the shallow zone:

$$q_{infil}^{deep} = -AK_{satV}^{deep} \quad (11)$$

Where $K_{satV}^{deep}$ is the saturated hydraulic conductivity in the vertical direction of the deep zone.

**Macropores.** Macropores, including roots and soil cracks are omnipresent in soils. Macropore flows can be simulated in the model to account for rapid water flows in the shallow zone (Shi et al., 2013). Macropore properties include depth ($D_{mac}$) and macropore vertical and horizontal area fraction ($f_{macV}$ and $f_{macH}$), and vertical and horizontal hydraulic conductivity ($K_{macV}^{shallow}$ and $K_{macH}^{shallow}$). The macropore depth differs from the rooting depth, which specifies the maximum depth of transpiration. By default $K_{macV}^{shallow}$ and $K_{macH}^{shallow}$ are 100 and 1,000 times of the infiltration hydraulic conductivity ($K_{infil}^{shallow}$) and shallow horizontal hydraulic conductivity ($K_{satH}^{shallow}$), respectively, and can be changed during calibration. Taking both soil and macropore properties into account, the effective hydraulic conductivity of the subsurface is calculated as the weighted average of the macropore and the shallow soil matrix within the macropore depth (Eq. (12) and (13)).

$$K_{effV}^{shallow} = f_{macH}K_{macV}^{shallow} + (1 - f_{macH})K_{satV}^{shallow} \quad (12)$$

$$K_{effH}^{shallow} = f_{macV} K_{macH}^{shallow} + (1 - f_{macV}) K_{satH}^{shallow} \quad (13)$$

### 3.2 Biogeochemical reactiveReactive transport equations

The governing advection dispersion reaction (ADR) equation for an arbitrary solute *m* in grid *i* is as follows (Bao et al., 2017), i.e., the change of solute mass (i.e., the left term in Eqn. 6) is driven by dispersive transport, advective transport, and reactions (i.e., the 1st, 2nd, and 3rd right-hand side terms, respectively):

$$V_i \frac{d(S_{w,i}\theta_i C_{m,i})}{dt} = \sum_{j=N_{i,1}}^{N_{i,x}} \left( A_{ij} D_{ij} \frac{C_{m,j} - C_{m,i}}{l_{ij}} - q_{ij} C_{m,j} \right) + R_{m,i} \quad (14$$

$$\frac{d(S_{w,i}\theta_i C_{m,i})}{dt} = \sum_{1}^{N_{ij}} \left( A_{ij} D_{ij} \frac{C_{m,j} - C_{m,i}}{d_{ij}} - q_{ij} A_{ij} C_{m,j} \right) + R_{m,i}, \qquad m = 1, \dots, nm \quad (6)$$

Where $V_i$ is the[$m^3$ total volume of grid *i* (solid + liquid)] is the total volume), $m^3$ of element *i*; $S_{w,i}$ [$m^3$ water/$m^3$ pore space] is soil water saturation, $m^3$ water/$m^3$ pore space; $\theta_i$ is porosity, [$m^3$ pore space/$m^3$ total volume] is porosity; $C_{m,i}$ [mol/$m^3$ water] is the aqueous concentration of species *m*, mol/$m^3$ water;; $N_{ij}$ is the number of fluxes from neighbor element *j* for element *i*, $N_{i,x}$ is the index of elements sharing surfaces; the value of $xN_{ij}$ is 2 for the unsaturated zone (infiltration, recharge) with only vertical flows and 45 for the saturated zone (recharge pluswith flux from (or to) the unsaturated zone, from (or to) the deeper zone, and fluxes between *i* and three neighbor elements *j* in lateral flow directions), respectively for non-boundary grids; $A_{ij}$ [$m^2$] is the interfacegrid area ($m^2$) shared by *i* and its neighbor grid *j*; $D_{ij}$ [$m^2$/s] is the combinedhydrodynamic dispersion/ coefficient (i.e., sum of mechanical dispersion and effective diffusion coefficient ($m^2$/s) normal to the shared surface $A_{ij}$; $l_{ij}d_{ij}$ [m] is the distance between the center of *i* and its neighbor elements *j*; $q_{ij}$ [m/s] is the flow rate across $A_{ij}$, $m^3$/s;; $R_m R_{m,i}$ [mol/s] is the total rate of kinetically controlled reactions in element *i* that involve species *m*, mol/s; *nm* is the total number of independent primary species to be solved for reactive transport equations.

Various types of

## 3.3 Biogeochemical processes and reaction ~~occur~~kinetics

### 3.3.1 Biogeochemical processes

Here we discuss some representative biogeochemical processes that involve plants and microbes that can be included in BioRT. BioRT differs from general water quality models that often primarily target a few contaminants (e.g., N, P, metals). The framework of the ~~subsurface (Fatichi et al., 2019).~~code is flexible and the users can define their reactions and solutes of interests in the input files. For abiotic reactions such as mineral dissolution and surface complexation or ion exchange, readers are referred to an earlier paper (Bao et al. (2017). Generally speaking, shallow soils compared to deep soils contain more weathered materials and soil organic matters (~~OM~~SOM) including roots, leaves, and ~~microbe. In contrast, deeper zones are less weathered and contain much less organic matter. SOM can decompose~~ microbes. SOM can be decomposed partially into organic molecules that dissolve in water ~~(Wieder et al., 2015),~~(Wieder et al., 2015), i.e., DOC, or ~~oxidize~~it can be oxidized completely into $CO_2$ that is released back to the atmosphere as a gas ~~or~~(Davidson, 2006) or surface water in the form of dissolved inorganic carbon (DIC). With coexisting ~~divalent~~ cations (e.g., Ca, Mg), DIC can ~~also~~often precipitate and become carbonate minerals~~. Hence soil C decomposition can release $CO_2$ back into the atmosphere and changes $CO_2$ level (Davidson, 2006), or releases DOC and DOM to surface water. These processes occur in soils and also as dissolved carbon transport laterally to streams.~~ (e.g., $CaCO_3$).

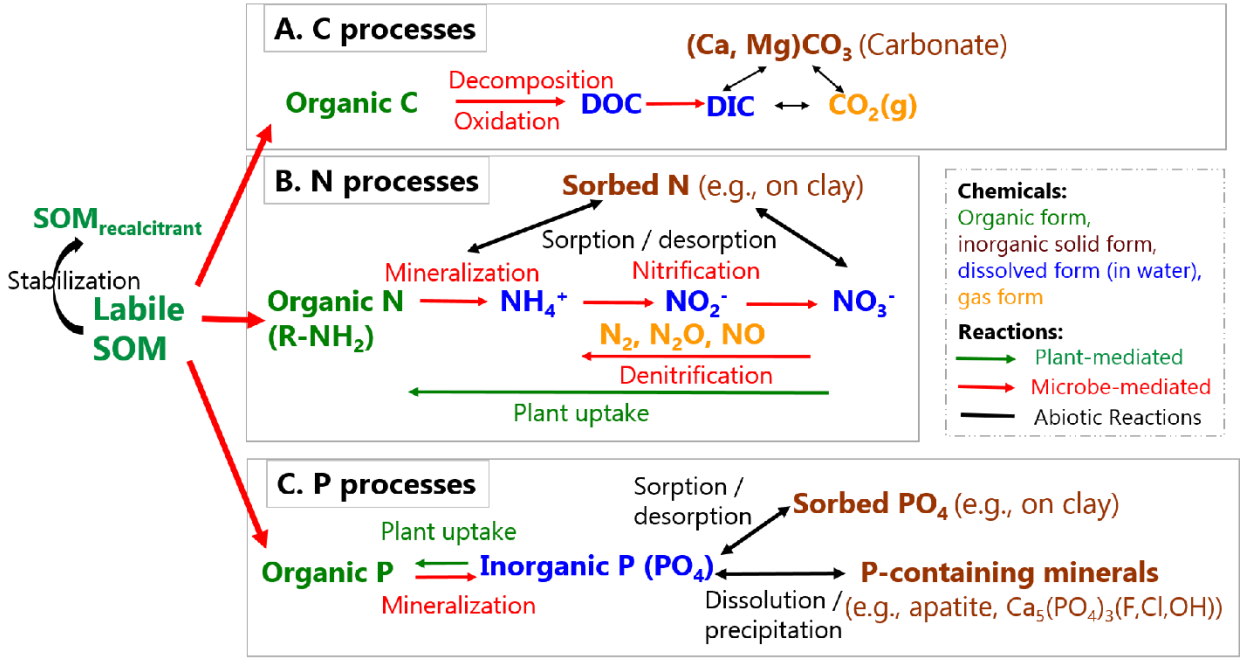



**Figure 3.** ~~Various types of biotic and abiotic reactions relevant to the transformation of soil organic matter (SOM). It can become stabilized through sorption on clay and separation from reactants. It can also decompose into inorganic forms, transitioning between different phases (adopted from Li (2019),~~Biotic and abiotic reactions relevant to the transformation of soil organic matter (SOM). It can become stabilized through sorption on clay and separation from reactants. Labile OM can decompose into inorganic forms, releasing C, N, and P that further transform between different forms (adopted from Li (2019), permission with Mineralogical Society of America).

~~Shown in Figure 3, SOM~~OM decomposition releases organic nitrogen (R-$NH_2$), which can further react to become ~~ammonia,~~$NH_4^+$, and other nitrogen forms ~~in between~~ ($N_2$, $N_2O$, NO, ~~$N_2O_3$ ($NO_2^-$),~~ $NO_2$~~). Some of the gaseous forms emit~~) (Figure 3). The gases can be emitted back to the atmosphere ~~(Saha et al., 2017;Maavara et al., 2018).~~(Saha et al., 2017;Maavara et al., 2018). Denitrification requires anoxic conditions and ~~does not occur as much~~ occurs less commonly in shallow soils owing to the pervasive presence of $O_2$ ~~(Sebestyen et al., 2019);~~(Sebestyen et al., 2019); it can become ~~prevalent however~~important under ~~extremely~~ wet conditions and in $O_2$-depleted groundwater systems. ~~In soils,~~ Phosphorous (P) can be in an organic form (e.g., leaves), sorbed ~~(~~on fine soil particles~~),~~ dissolved in water, or in solid forms as P-containing minerals ~~(Figure 3). The transformation between different forms~~ . Transformation of nutrients occurs through various bio-mediated or abiotic reactions. ~~The most abundant~~A representative P-containing mineral in the Earth´s crust is apatite $Ca_5(PO_4)_3(F, Cl, OH)$. Once liberated via

rock dissolution, P is mostly biologically assimilated and locked in ~~organisms. It is barely soluble so it binds~~organic forms. These organic forms have very low solubility, allowing them to bind on and ~~transports~~be transported together with soil particles in the form of orthophosphate or pyro-diphosphate. Overall, these reactions are a combination of biotic and abiotic reactions.

~~BioRT can simulate biotic reactions including microbe-mediated reactions~~

### 3.3.2 Reaction kinetics in natural soils

**Rate dependence on temperature and soil moisture.** Reactions such as soil respiration and plant uptake~~, in addition to the abiotic reactions such as mineral dissolution and surface complexation or ion exchange that have been introduced by Bao et al. (2017). Here we focus on the discussion of a few representative microbe-mediated reactions.~~

~~**Microbe-mediated reaction kinetics.** SOM is often conceptualized and modeled as pools with different decomposition rates and turnover times (Ostle et al., 2009;Thornton et al., 2009). An extensively used three-pool model includes a readily degradable (labile) pool with residence times less than five years; a slowly degrading pool with residence times of decades; and a relatively stable pool, with residence times between $10^3$ – $10^5$ years (Trumbore et al., 1995;Trumbore, 1993;Marin-Spiotta et al., 2009). The kinetics of microbe-mediated reactions can be described by the general dual Monod rate law, reflecting the need for both electron donor and acceptor in these reactions (Monod, 1949):~~

$$r = \mu_{max} C_{C_5H_7O_2N} \frac{C_D}{K_{m,D} + C_D} \frac{C_A}{K_{m,A} + C_A} \quad (15)$$

~~Here $\mu_{max}$ is the rate constant (mol/time/microbe cell), $C_{C_5H_7O_2N}$ is the concentration of microorganisms (microbe cells/L$^3$), $C_D$ and $C_A$ are the concentrations of electron donor and acceptor (mol/L$^3$), respectively. The $K_{m,D}$ and $K_{m,A}$ are the half-saturation coefficients of the electron donor and acceptors (mol/m$^3$), respectively; they are the concentrations at which half of the maximum rates are reached for the electron donor and acceptor, respectively. If an electron donor or acceptor is not limiting, it means that $C_D \gg K_{m,D}$ or~~

~~$C_A \gg K_{m,A}$, so that the term $\frac{C_D}{K_{m,D}+C_D}$ or $\frac{C_A}{K_{m,A}+C_A}$ is essentially 1, lending to a rate that only depends~~ typically depend on ~~the abundance of microorganisms or one of the chemicals.~~

~~In natural subsurface where multiple electron acceptors coexist, the biogeochemical redox ladder dictates the sequence of redox reactions. That is, aerobic oxidation occurs before denitrification, which in turn occurs before iron reduction. Inhibition terms are used to account for the sequence of redox reactions as follows:~~

$$r = \mu_{max} C_{C_5H_7O_2N} \frac{C_D}{K_{m,D}+C_D} \frac{C_A}{K_{m,A}+C_A} \frac{K_{I,H}}{K_{I,H}+C_H} \quad (16)$$

~~Here $K_{I,H}$ is the inhibition coefficient for the inhibiting chemical $H$. The inhibition term is 1 (not inhibiting) only when $C_H \ll K_{I,H}$. In a system where oxygen and nitrate coexist, which is common in agriculture lands, aerobic oxidation occurs first before denitrification. The denitrification rates can be represented by:~~

$$r_{NO_3^-} = \mu_{max} C_{C_5H_7O_2N} \frac{C_D}{K_{m,D}+C_D} \frac{C_{NO_3^-}}{K_{m,A}+C_{NO_3^-}} \frac{K_{I,O_2}}{K_{I,O_2}+C_{O_2}} \quad (17)$$

~~Here $C_{NO_3^-}$ is the concentration of nitrate, $K_{I,O_2}$ is the inhibition coefficient of $O_2$, or the $O_2$ concentration at which it inhibits the reduction of nitrate. This rate law ensures that denitrification kicks in substantially only when $O_2$ is depleted to $C_{O_2} \ll K_{I,O_2}$, such that the term $\frac{K_{I,O_2}}{K_{I,O_2}+C_{O_2}}$ approaches 1.0. If there exists an electron acceptor that is lower in the redox ladder than nitrate, multiple inhibition terms are needed.~~ environmental conditions (temperature or soil moisture). For example, ~~for iron oxide, we write the following:~~

$$r_{Fe(OH)_3} = \mu_{max} C_{C_5H_7O_2N} \frac{C_D}{K_{m,D}+C_D} \frac{C_{Fe(OH)_3}}{K_{m,Fe(OH)_3}+C_{Fe(OH)_3}} \frac{K_{I,O_2}}{K_{I,O_2}+C_{O_2}} \frac{K_{I,NO_3^-}}{K_{I,NO_3^-}+C_{NO_3^-}} \quad (18)$$

~~Here $K_{I,NO_3^-}$ is the $NO_3^-$ concentration above which it inhibits iron reduction. The additional nitrate inhibition term means that iron reduction occurs at significant rates only when both oxygen and nitrate are low compared to their corresponding inhibition coefficients.~~

~~**Rates in natural soils.** The dual-Monod and inhibition terms are important under conditions where electron donors and acceptors are limited. In shallow soil, $O_2$ is~~

~~prevalent except under wet conditions with little pore space for air. Anoxic conditions can also develop in local environments such as dead-end pores where water is saturated for a long time and not easily flows out. Under conditions~~ in shallow oxic soils where organic carbon and $O_2$ are often abundant, the ~~SOM~~ rate law ~~is~~for carbon decomposition can be simplified to the following form assuming microorganism concentrations are relatively constant~~:~~.

$$~~r_{SOM} = \mu_{max} A f~~ r = kAf(T)f(S_w)f(Z_w) \quad ~~(19~~(7)$$

Where the reaction rate ~~$r_{SOM}$ ($r$~~ [mol ~~/t) now~~/s] depends on ~~$\mu_{max}$ (~~rate constant $k$ [mol/m$^2$/~~t),~~s], the ~~lumped~~ surface area $A$ ~~(m$^2$) as an approximation of~~[m$^2$] is a lumped parameter that quantitatively represents SOM content and biomass abundance, ~~and~~ $f(T)$ and $f(S_w)$ ~~and $f(S_w)$~~ describe ~~its~~the temperature and soil moisture dependence, respectively, $f(Z_w)$ can be included to account for the depth distribution of SOM (Seibert et al., 2009), and $Z_w$ [m] is the water table depth. An example for the depth distribution is $f(Z_w) = \exp\left(-\frac{Z_w}{b_m}\right)$~~. For~~(Weiler and McDonnell, 2006;Ottoy et al., 2016;Bai et al., 2016), with $b_m$ as the depth coefficient describing the gradient of SOM content over depth. Users can choose to include either one or all of these dependences in input or database files.

The temperature dependence~~,~~ follows a $Q_{10}$-based form ~~(Friedlingstein et al., 2006;Hararuk et al., 2015) is commonly used:~~ (Friedlingstein et al., 2006;Hararuk et al., 2015) as follows:

$$f(T) = Q_{10}^{|T-20|/10}~~,~~ \quad (8),$$

where $Q_{10}$ is the relative increase in reaction rates when temperature increases by 10 °C ~~(Davidson and Janssens, 2006). The $f(S_w)$ accounts for the nonlinear~~(Davidson and Janssens, 2006). Values of $Q_{10}$ (Figure 4a) can vary from 1.0 to 3.0, depending on climatic conditions, substrate availability, and ecosystem type (e.g., grassland, forest) (Davidson et al., 2006;Liu et al., 2017). The mean values are in the range of 1.4 to 2.5 (Zhou et al., 2009;Bracho et al., 2016). The $Q_{10}$ value can be specified in the input file. The soil moisture dependence ~~of~~ function $f(S_w)$ is coded based on the following form:

$$\begin{cases} (\frac{S_w}{S_{w,c}})^n, S_w \le S_{w,c} \\ (\frac{1-S_w}{1-S_{w,c}})^n, S_w > S_{w,c} \end{cases} \quad (9)$$

Here $S_{w,c}$ [0 to 1] is the critical soil moisture at which rates ~~on soil moisture. A simple form of $f(S_w) = (S_w)^{\varepsilon}$ where $\varepsilon$ is the saturation~~ are highest, and $n$ is the exponent ~~(a~~reflecting the dependence of rates on soil moisture. A typical ~~$\varepsilon$ value is 2,~~$n$ value is 2 (Yan et al., 2018) with a range between 1.~~5 and 2.5) is~~ 2 and 3.0 (Hamamoto et al., 2010), depending on soil structure and texture. As shown in Figure 4b, the form indicates an intermediate critical soil moisture $S_{w,c}$ at which $f(S_w)$ reaches its maximum. When $S_w$ is below this value, $f(S_w)$ increases with $S_w$; when $S_w$ is above this value, $f(S_w)$ decreases with $S_w$ behavior (Figure 4b) (Yan et al., 2018). Under the extreme conditions of $S_{w,c}$ equals to 0 or 1, $f(S_w)$ monotonically increase or decrease (Figure 4c). The two parameters, $S_{w,c}$ and $n$, determines the shape of the curve. They can be specified in input or database files. One can also choose not to have temperature or soil moisture dependence by choosing parameters that would lead to the value of exponent being zero.

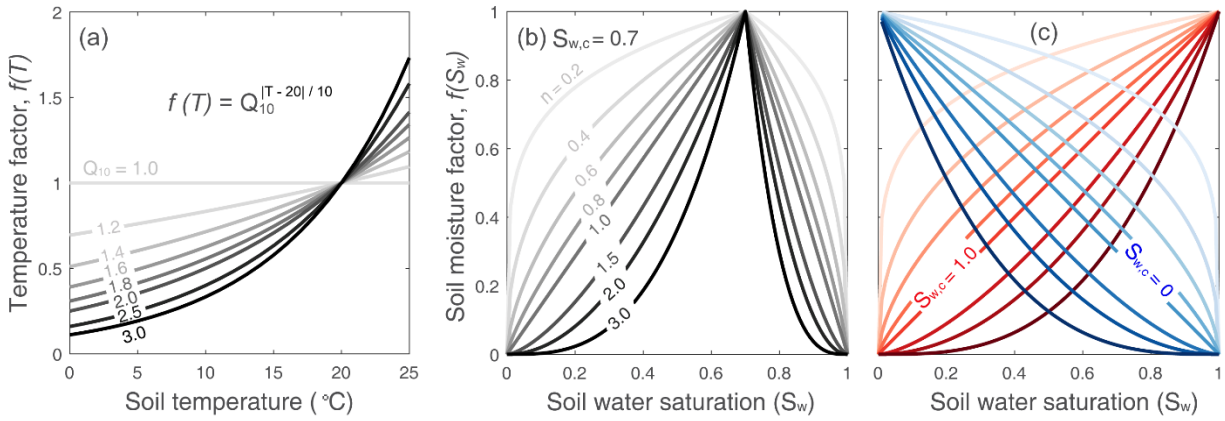



**Figure 4**. (a) Function form of soil temperature dependence and (b, c) soil moisture dependence for reaction rates. The temperature factor $f(T)$ is a function of the $Q_{10}$ (defined by users) and soil temperature. The soil moisture factor $f(S_w)$ is a function of two user-defined parameters $S_{w,c}$ and $n$ and soil water saturation $S_w$. The soil moisture function can represent three types of behaviors: the threshold behavior (b, $0 < S_{w,c} < 1$), increase behavior (red in (c), $S_{w,c} = 1$), and decrease behavior (blue in (c), $S_{w,c} = 0$). Values of $n$ = 1 leads to a linear threshold dependence of $S_w$ while $n < 1$ and $n > 1$ lead to concave and convex dependences, respectively.

**Rate dependence on substrates: Monod kinetics and biogeochemical redox ladder.** Deeper groundwater aquifers often ~~used. More~~experience anoxic conditions that lead to processes such as denitrification or methanogenesis. This can also happen in wetlands or wet soils. The rates of microbe-mediated redox reactions depend not only on temperature and soil moisture as discussed above, they also depend on concentrations of electron donors and non-oxygen electron acceptors (e.g., nitrate, iron oxides, sulfate) that are often limited under anoxic conditions (Bao et al., 2014;Li, 2019). The order of the redox reactions often follows the biogeochemical redox ladder, which is based on how much microbe can harvest energy by reducing different types of electron acceptors. Monod reaction rate laws are often used for quantifying rates of these redox conditions. These rate laws are detailed in the section S2 of Supporting Information and also in Li (2019). Users can combine these Monod rate laws and the temperature and soil moisture dependence described above, if needed.

### 3.4 Plant related processes: root uptake of nitrate as an example

Nitrate uptake by plants is intrinsically complex and remains poorly understood (Devienne-Barret et al., 2000;Crawford and Glass, 1998;Hachiya and Sakakibara, 2016). A variety of plant uptake models exists with varying degrees of complexity (Neitsch et al., 2011;Fisher et al., 2010;Cai et al., 2016). These models are mostly based on plant growth module or supply and demand approach that often requires detailed phenological and plant attributes such as growth cycle, root age and biomass, nitrate availability, phosphorous stress, and carbon allocation, in addition to local climate conditions such as temperature and soil moisture (Neitsch et al., 2011;Porporato et al., 2003;Dunbabin et al., 2002;Buysse et al., 1996;Fisher et al., 2010). Without detailed information, we can assume a simple and operational approach (Eqn. 13 and 14). In the Example 2 that we show later, for example, we modeled nitrate uptake with dependence on $NO_3^-$ concentration, soil temperature and moisture, and rooting density (McMurtrie et al., 2012;Yan et al., 2012;Buljovcic and Engels, 2001).

$$r_{uptake} = k_{uptake} C_{NO_3^-} f(T) f(S_w) f_{root}(d_w) \quad (13)$$

$f_{root}(d_w)$ =~~forms of $f(S_w)$ considering both water limitation under dry conditions and $O_2$ limitation under wet conditions have been proposed (Yan et al., 2018).~~$\exp((-d_w + \delta) / \lambda)$ (14)

Where $k_{uptake}$ [L/s] is the nitrate uptake rate, $f_{root}(d_w)$ is the normalized rooting density term in the range of 0 to 1 as a function of water depth to the groundwater ($d_w$). The rooting term (Eqn. 14) was exponentially fitted ($\delta = 0.013, \lambda = 0.20$) based on field measurements of root distribution along depth (Hasenmueller et al., 2017). It ~~has also been suggested that the decomposition depends strongly on the depth distribution of SOM (Seibert et al., 2009), which is sometime accounted with an additional depth function:~~is common to observe root density decrease exponentially in forests (López et al., 2001). Other form of user-tailored plant uptake rate law can be added if needed.

~~$r_{SOM} = \mu_{max} A f(T) f(S_w) f(Z_w)$ (20)~~

~~where $Z_w$ is the water table depth (m). An example is $f(Z_w) = \exp\left(-\frac{Z_w}{b_m}\right)$ (Weiler and McDonnell, 2006;Ottoy et al., 2016;Bai et al., 2016). Here $b_m$ is the declining coefficient describing the gradient of SOM content over depth.~~

## 4.~~-~~ Numerical scheme and model verification

~~**Numerical scheme.** The local system of differential equations for water storages [e.g., Eq. (1), (2), (6), and (7)] on each control volume are combined into a global system of ordinary differential equations (ODEs) and solved in CVODE, a numerical ODE solver in the SUite of Nonlinear and Differential / ALgebraic equation Solvers (SUNDIALS) (Hindmarsh et al., 2005). CVODE is a numerically efficient solver for ODE systems. It uses the backward difference formula (BDF) with adaptive time steps and method order varying between 1 and 5. At each iteration step, the solver evaluates the local error, which is required to satisfy convergence tolerance conditions set by the users. The internal time step is reduced and the method order is adjusted in response to the stiffness of ODEs if the non-convergence occurred. For example, the solver time steps become smaller after heavy precipitation events to address the rapid change of surface and subsurface water storages. The adaptive time stepping and order adjustment scheme make CVODE an~~

~~accurate and stable solver.~~

~~**Model verification.** The BioRT module had been verified against CrunchTope under a variety of transport and reaction conditions at a range of reaction complexity levels (Supporting Information, Figure S1 – S7). CrunchTope is a widely used subsurface reactive transport model (Steefel and Lasaga, 1994;Steefel et al., 2015), and is often used as a benchmark to verify other reactive transport models. Verification is~~The system of differential equations for the water storages (e.g., Eqn. 1 and 2, and Eqn. S1 and S2) are assembled into a global system of ordinary differential equations (ODEs) and solved in CVODE (short for C-language Variable-coefficients ODE solver, https://computing.llnl.gov/projects/sundials/cvode), a numerical ODE solver in the SUite of Nonlinear and Differential / ALgebraic equation Solvers (SUNDIALS) (Hindmarsh et al., 2005). In BioRT, the transport step is first solved with water by the preconditioned Krylov (iterative) method and the Generalized Minimal Residual Method (Saad and Schultz, 1986). In the following reaction step, all primary species in each finite volume are assembled in a local matrix and then solved iteratively by the Crank-Nicolson and Newton-Raphson method in CVODE (Bao et al., 2017).

**Model verification.** The BioRT module had been verified against CrunchTope under different transport and reaction conditions (Figures S1 – S7 in SI). CrunchTope is a widely used subsurface reactive transport model (Steefel and Lasaga, 1994;Steefel et al., 2015), and is often used as a benchmark to verify other reactive transport models. Verification was performed under simplified hydrological conditions with 1-D column and constant flow rates such that it focuses on ~~biogeochemical reactive transport processes such as~~ advection, diffusion, dispersion, and biogeochemical reactions. Specifically, three cases of soil phosphorus, carbon, and nitrogen were verified for temporal evolution and spatial pattern of relevant solute concentrations ~~(Figure S1 – S7).~~. The ~~soil~~ phosphorus case~~,~~ ~~which~~ that involves ~~geochemically kinetic and thermodynamic processes (i.e.,~~kinetics-controlled apatite dissolution and thermodynamics-controlled phosphorous speciation~~),~~ was first tested for solution accuracy of the bulk code that was inherited from the original RT-Flux-PIHM. Soil carbon and nitrogen processes that involve ~~microbially~~ microbe-

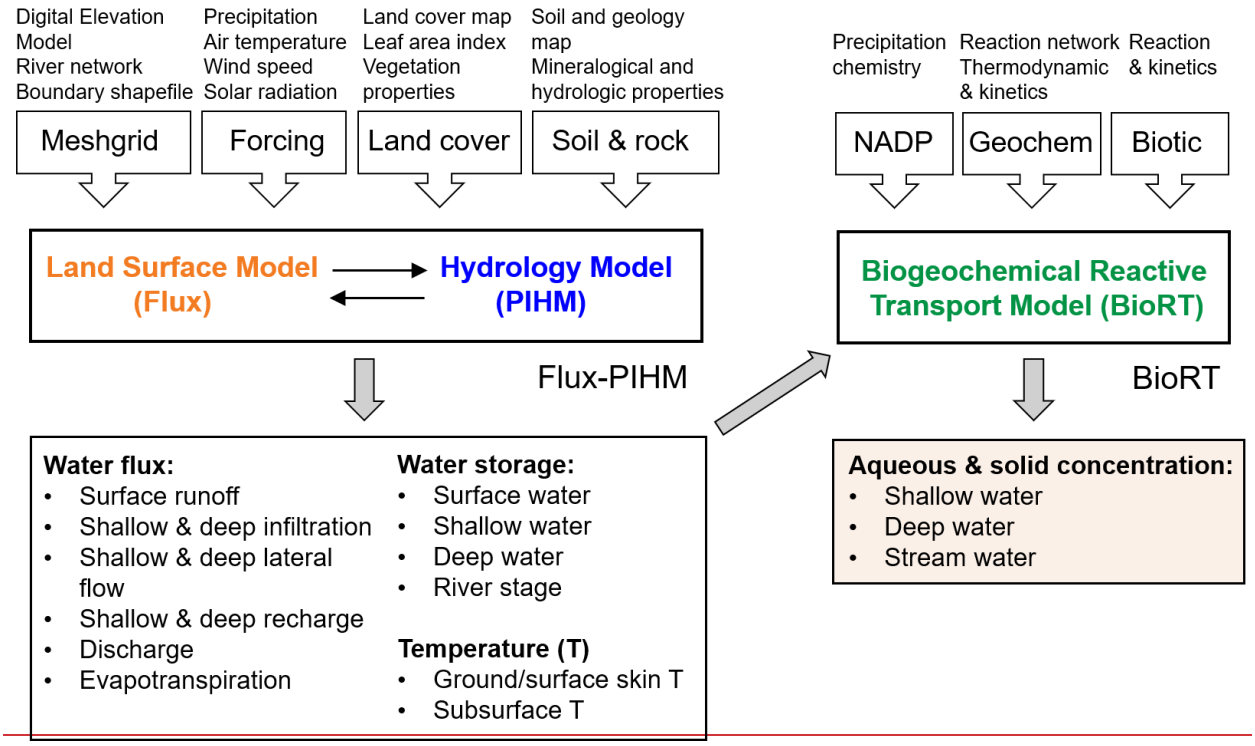
driven processes, such as soil carbon decomposition and mineralization, nitrification and denitrification, were further verified for solution accuracy of the augmented BioRT module.

## ~~4 Model setup and data needs~~

### ~~4.1~~5. Model structure, data needs, and ~~input/output~~

~~Flux-PIHM sets up the~~ **domain** ~~based on watershed characteristics including topography, hydrography, land cover, and shallow and deep zone properties (Figure 4). It~~ **setup**

**Model structure.** The model takes ~~in~~ meteorological forcing time series as input and solves for water storages and soil temperature~~. BioRT takes~~, along with other hydrologic and land surface states and fluxes (Figure 5). BioRT reads in the model output of water and temperature from Flux-PIHM, and ~~drives~~solves the ~~simulation for~~ biogeochemical reactive transport equations. At the time scale of months to years that are typical for BioRT-Flux-PIHM simulations, ~~the alteration~~alterations in solid phase properties ~~due to reactions is~~, including, porosity, permeability, and reactive surface area, are considered negligible ~~and does not change~~such that hydrological parameters~~.~~ remain constant with time.




~~**Figure 4.**~~***Data needs.*** *The code sets up the model domain based on watershed characteristics including topography, land cover, and shallow and deep zone properties (Figure 5). When the model is used in a spatially distributed form,* ~~Model structure, input, and output of BioRT-Flux-PIHM. The Flux-PIHM takes in watershed characteristics including topography (digital elevation model, DEM), land cover, shallow and deep zone properties, and meteorological forcing and then solves for water storage and fluxes, and ground and soil temperature. Water- and temperature-related information from Flux-PIHM with additional inputs such as precipitation chemistry and shallow and deep water chemistry and biogeochemical kinetics parameters are then provided for~~ *the* ~~BioRT module, which eventually outputs aqueous and solid concentration for the shallow and deep zone, and stream water. NADP stands for the National Atmospheric Deposition Program.~~

~~Most~~ model ~~inputs such as~~domain can be set up using elevation, land cover, soil and geology ~~map can be obtained~~maps supplied by the user or from the data portal of Geospatial Data Gateway (https://datagateway.nrcs.usda.gov). The meteorological forcing data can be downloaded from the North American Land Data Assimilation Systems Phase 2 (NLDAS-2, https://ldas.gsfc.nasa.gov/nldas/v2/forcing). The vegetation forcing, i.e., Leaf Area Index (LAI), ~~The meteorological forcing data can be downloaded from the North American Land Data Assimilation Systems Phase 2 (NLDAS-2,~~

~~https://ldas.gsfc.nasa.gov/nldas/v2/forcing). The vegetation forcing, i.e., Leaf Area Index (LAI), is~~can be obtained from ~~the~~ MODIS (Moderate Resolution Imaging Spectroradiometer~~ (~~, https://modis.gsfc.nasa.gov/data). Other vegetation properties associated with land cover (e.g., ~~Other vegetation properties associated with land cover (e.g.,~~ shading fraction, rooting depth) ~~are~~can be adopted from, for example, the Noah vegetation parameter table embedded in the Weather Research and Forecasting model (WRF; Skamarock and Klemp (2019)). Local measurements from meteorological stations and field campaigns (e.g., land cover, soil, geology) can also be used in the model. ~~Skamarock and Klemp (2019)). Local measurements from meteorological stations and field campaigns (e.g., land cover, soil, geology) can also be used in the model.~~ Another data source ~~for the model input~~ is the HydroTerre (http://www.hydroterre.psu.edu/), where users can obtain geospatial data (~~Leonard and Duffy, 2013). The form of microbial reaction rate laws, when it includes full Monod form, or only with~~ e.g., elevation, land cover, geology, soil) (Leonard and Duffy, 2013). Initial water and solid phase chemistry can be based on measurements or general knowledge of the simulated sites. The form of reaction rate laws, including the Monod form, temperature and soil moisture dependence, can be defined in the input files~~. Additional inputs include initial water and solid phase chemistry, description of solutes and biogeochemical reactions, and kinetics and~~ and calibrated to reproduce field data. Reaction thermodynamics ~~of reactions~~, mostly equilibrium constants, are from ~~a~~the geochemical database EQ3/6 by default (Wolery, 1992). These reaction parameters can be modified when necessary. The model outputs include aqueous and solid concentrations of shallow and deep zone and stream water.

~~. The model outputs include aqueous and solid concentrations of shallow and deep zone and stream water.~~

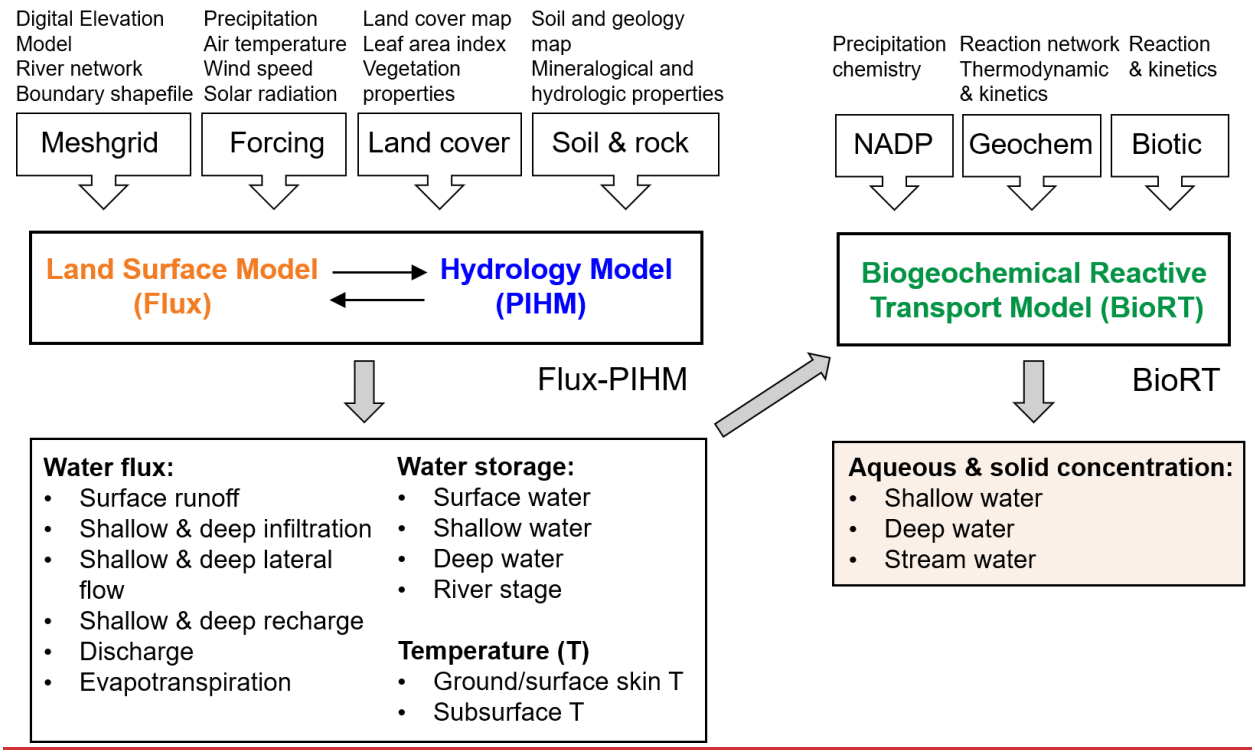
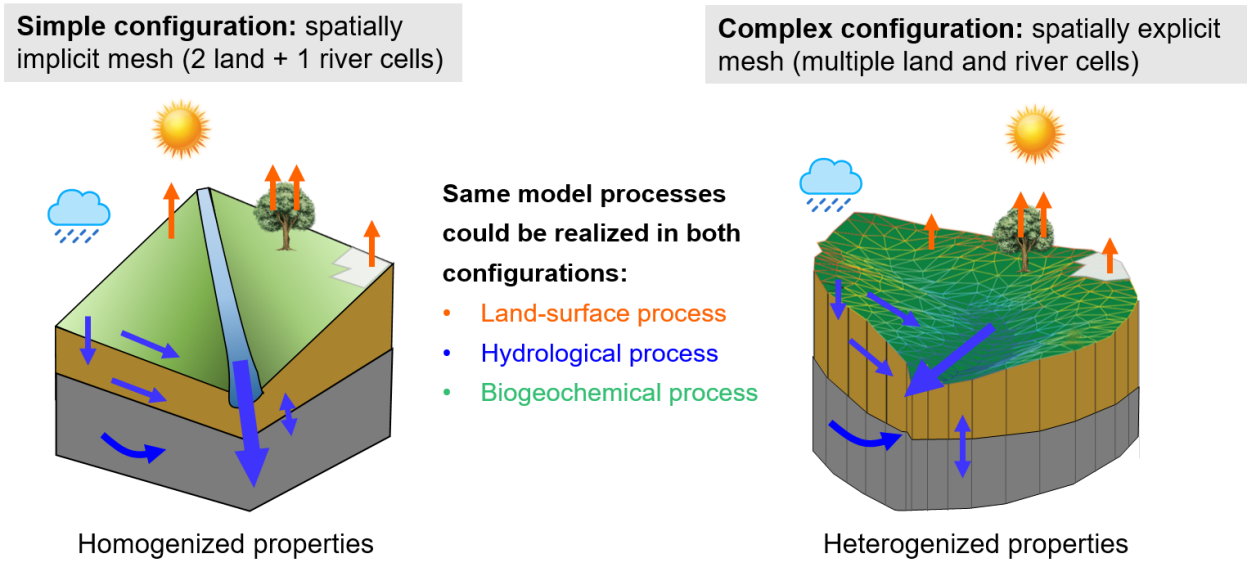



**Figure 5.** Model structure, input, and output of BioRT-Flux-PIHM. The Flux-PIHM takes in watershed characteristics including topography (digital elevation model, DEM), land cover, shallow and deep zone properties, and meteorological forcing

## ~~4.2 Model setup: from simple, spatially implicit to complex, spatially explicit domains~~

~~The model domain can be set up using PIHM-GIS (http://www.pihm.psu.edu/pihmgis_home.html), a standalone GIS interface for watershed delineation, domain decomposition, and parameter assignment (Bhatt et al., 2014). The domain can be set up at different spatial resolutions with a different number of grids. A simple domain can be set up with only two land grids representing two sides of a watershed connected by one river cell (Figure 5). This setup uses averaged properties without considering spatial details. This type of model setup requires less spatial data, is computationally inexpensive, and is relatively easy to set up. It can be used to assess the average dynamics of the water and solute dynamics and focus on the interactions among processes without concerning spatial details. It can also be used as a relatively easy starter for educational purposes before students jump into complex domains. Alternatively, a complex domain can be set up using many grids with explicit~~

~~representation of spatial details. It requires much more data and is computationally expensive but can be used to identify "hot spots" of biogeochemical reactions.~~




~~**Figure 5.** Two extreme model domain setups: a simple domain with two land cells representing two hillslopes connected by one river cell, versus a complex domain with hundreds of land cells. An intermediate number of grids can also set up the domain, depending on watershed heterogeneity, data availability, and desired spatial resolution.~~

~~5~~time series and solves for water storage, and ground and soil temperature. BioRT takes in water- and temperature-related information from Flux-PIHM with additional inputs such as precipitation chemistry and shallow and deep water chemistry and biogeochemical kinetics parameters, and solve for aqueous and solid concentrations in the shallow and deep zone, and stream water. NADP stands for the National Atmospheric Deposition Program. This paper focuses on the BioRT component. The land-surface, hydrological processes, and abiotic reactive transport processes have been described in previous papers (Bao et al., 2017;Shi et al., 2013). Discussions on how air temperature and ET influence stream chemistry can be found in Li (2019).

**Domain set up: from simple, spatially lumped to complex, spatially distributed domains**. The domain can be set up at different spatial resolutions with different numbers of grids. A simple domain can be set up with only two land grids representing two sides of a watershed connected by one river cell. This setup uses averaged properties without needs for larger spatial data. Alternatively, a complex domain can be set up using many grids with explicit representation of spatial details. The model domain can be set up using

PIHM-GIS (http://www.pihm.psu.edu/pihmgis_home.html), a standalone GIS interface for watershed delineation, domain decomposition, and parameter assignment (Bhatt et al., 2014). It requires much more data and can be computationally expensive but can be used to identify "hot spots" of biogeochemical reactions within a watershed. The same model processes (e.g., hydrology, reaction network) can be setup in both spatial configurations. Auto-calibration is not built into the model, but a global calibration coefficient approach is used to reduce parameter dimension and facilitate manual calibration. A typical model application requires 20 to 30 hydrological parameters to be calibrated. These parameters include land surface parameters (e.g., canopy resistance, surface albedo), soil and geology parameters (e.g., hydraulic conductivity, porosity, Van Genuchten, macropore properties) (Shi et al., 2013). Reaction-related parameters (e.g., reaction rate constant, mineral surface area, $Q_{10}$, $S_{w,c}$, and n) are additionally needed for calibration, the number of which depends on the numbers of reactions involved in a particular system.

## 6. Model applications

The original RT-Flux-PIHM has been applied to understand ~~the~~ processes related to the geogenic solutes of Cl and Mg at the Shale Hills watershed and for ~~geogenic~~ Na ~~at the~~in a watershed on Volcán Chimborazo ~~watershed~~in the Ecuadorian Andes (Table 1). The new BioRT-Flux-PIHM has been demonstrated for understanding the dynamics of DOC~~, and~~ nitrate~~, and Na~~ at Shale Hills and Coal Creek. This section ~~presents some new model features using two~~ will present one hydrology and two biogeochemical examples~~: one with a simple, spatially implicit domain, and another with a complex, spatially explicit domain.~~ in the Susquehanna Shale Hills Critical Zone Observatory (SSHCZO), a small headwater watershed in central Pennsylvania, USA. The mean annual precipitation is approximately 1,070 mm and the mean annual temperature is 10 °C (Brantley et al., 2018). Soil carbon storage and respiration and nitrogen budget and fluxes have been studied in detail (Andrews et al., 2011;Hasenmueller et al., 2015;Shi et al., 2018;Hodges et al., 2019;Weitzman and Kaye, 2018). Modeling work has been conducted to understand hydrological dynamics (Shi et al., 2013;Xiao et al., 2019), transport of the non-reactive tracer Cl, and the weathering-derived solute Mg (Bao et al., 2017;Li et al., 2017a).

**Table 1.** Existing Model applications ~~with different biogeochemical reactions~~of BioRT-Flux-PIHM

| Watershed (location) | Size ($km^2$) | Model domain | Modeled solutes | ~~Reaction network~~ ~~(~~Kinetic ~~-~~Reactions (rate ~~law~~laws: 1, TST; 2, Monod based; 3, plant uptake ~~rate~~) | Reference |
|---|---|---|---|---|---|
| Shale Hills (PA, USA) | 0.08 | ~~Complex (535 grids)~~Spatially distributed | Cl, Mg | • Chlorite dissolution[1]<br>• Illite dissolution[1]<br>• Carbonate dissolution & precipitation[1]<br>• Cation exchange | Bao et al., 2017; Li et al., 2017 |
| | | ~~Complex (535 grids)~~Spatially distributed | DOC | • SOC decomposition[2]<br>• DOC sorption | Wen et al., 2020 |
| | | ~~Simple (2 grids)~~Spatially lumped | $NO_3^-$ | • Soil N leaching[2]<br>• Denitrification[2]<br>• Plant ~~nitrate~~ uptake[3] | This work |
| Coal Creek (CO, USA) | 53 | ~~Simple (2 grids)~~Spatially lumped | DOC, Na | • SOC decomposition[2]<br>• DOC sorption<br>• Albite dissolution[1] | Zhi et al., 2019 |
| Volcán Chimborazo (Ecuador) | | ~~Complex (160 grids)~~Spatially distributed | Cl, Na, Ca, Mg, $SiO_2$ | • Albite dissolution[1]<br>• Diopside dissolution[1] | ~~Leila et al., 2020 (under review)~~Saberi et al. (under review) |

Note: Transition State Theory (TST) is a classic kinetic rate law for mineral dissolution and precipitation ~~(Brantley et al., 2008); Monod based~~(Brantley et al., 2008) (Eqn. S15); Monod rate law with environmental dependency (i.e., soil temperature and soil moisture) is widely used for ~~microbial~~microbially driven reactions~~; plant nitrate uptake depends on nitrate availability, environmental dependency, and rooting depth.~~. Monod ~~-~~-based and plant nitrate uptake rate law are detailed in the following section of ~~5.1.1~~6.2. SOC stands for soil organic carbon.

~~Here we present two examples of different processes in the Susquehanna Shale Hills Critical Zone Observatory (SSHCZO), a small headwater watershed (0.08 km$^2$) in central Pennsylvania, USA. The mean annual precipitation is approximately 1,070 mm and the mean annual temperature is 10 °C. Extensive field measurements have been conducted to characterize the topography, vegetation, and bedrock and soil properties (Brantley et al., 2018). Soil carbon storage and respiration and nitrogen budget and fluxes have been detailed studied (Andrews et al., 2011;Hasenmueller et al., 2015;Shi et al., 2018;Hodges et al., 2019;Weitzman and Kaye, 2018). Modeling work has also been conducted to understand hydrological dynamics (Shi et al., 2013), transport of a non-reactive tracer Cl and the soil and rock weathering Cl and Mg (Bao et al., 2017;Li et al., 2017a).~~

## ~~5.1 Hydrology Example: Shallow and deep water interactions~~

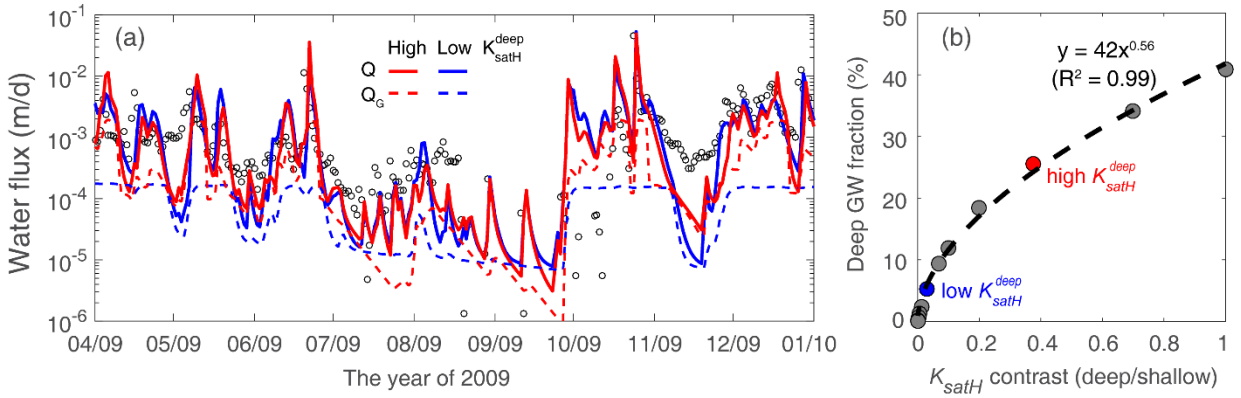
## 6.1 Example 1: Shallow and deep water interactions

The model was set up using the spatially lumped mode with two land grids and one river grid~~, represented~~ characterized by ~~the averaged~~average land cover, soil and rock properties based on previous work ~~(Shi et al., 2013;Kuntz et al., 2011). Specifically, the model~~ (Shi et al., 2013;Kuntz et al., 2011). The model assumed a Weikert soil, the dominant soil type at Shale Hills ~~(Shi et al., 2013).~~(Shi et al., 2013). The porosity of the deep zone was set to ~~1/10~~a tenth of the shallow soil porosity based on measurements of the ~~deep subsurface (Brantley et al., 2018;Kuntz et al., 2011). Stream discharge and ET observations were used to calibrate hydrological parameters (Figure S9). Groundwater ($Q_G$) from the deep layer was constrained by previous work (Li et al., 2017a) and the nitrate concentration-discharge (C-Q) observations. Important land surface and hydrological parameters are summarized in Table S7.~~

~~**Water budget.** The model reproduced the seasonal dynamics of discharge and ET (Figure S9), with daily Nash-Sutcliffe efficiency (NSE) of 0.56 and 0.66, respectively. Precipitation occurs throughout the year while the discharge was responsive to a few big storm events in spring and fall. The ET peaked during the summer due to higher solar~~

radiation and higher temperature while declined in the fall and winter. The runoff ratio was 0.46, suggesting 46% of precipitation was discharged through the stream while the remaining 54% contributed to ET. A breakdown analysis suggests at the annual scale, the shallow lateral flow ($Q_L$, 87% of Q) dominated discharge, followed by the deeper groundwater flow ($Q_G$, 9.3%), and the surface runoff ($Q_S$, 4.2%). The $Q_G$ was essential in maintaining discharge during dry time, especially in the summer.

**Controls of deep water.** aquifer (Brantley et al., 2018;Kuntz et al., 2011). In a headwater watershedcatchment like Shale Hills where the deep groundwater is most likely sourced from recharge, the deep groundwater contribution to the stream wascan be primarily controlled by the hydraulic conductivity ($K_{satH}$) contrast between the deep and shallow zonezones (i.e., $K_{satH}^{deep}/K_{satH}^{dp}$ / $K_{satH}^{shallow}$). Because$K_{satH}^{sl}$). This is because the $K_{satH}$ contrast determineddetermines the partitioning of infiltrating water between the shallow lateral flow and the downward recharge to the deep zone and then deep groundwater flow. Two cases of high (red) and low (blue) $K_{satH}^{deep}K_{satH}^{dp}$ were set up to showcase the control of $K_{satH}$ contrast control on deep groundwater (Figure 6a). By changing the deep zone $K_{satH}^{deep}K_{satH}^{dp}$ from 2.6 to 0.22 (m/d), about 38% and 3.1% of the shallow zone $K_{satH}^{shallow}$,the annual deep groundwater ($Q_G$) contribution to discharge (Q) decreased from 26% to 5.2%, respectively. It is also noticeablealthough the total discharge is negligible. This indicates that there was minimal change between discharge (i.e., solid lines in Figure 6a) as the deep zone $K_{satH}^{deep}$ does not affect shallow water partitioning for infiltrating water and discharge. This new hydrology feature enables the exploration of the interaction between deep groundwater and surface water. These features can be used to understand watersheds of different subsurface structures and with deep water the changing $K_{satH}^{dp}$ mostly from changes the portioning between the shallow soil lateral flow and recharge. In addition, they can be used to explore large watersheds of higher stream order with a large proportion of deep water coming from nearby regional aquifers., whereas total infiltration and discharge remain very similar.




836

837 **Figure 6.** (a) Hydraulic conductivity ($K_{satH}$) contrast control on deep groundwater ($Q_G$). The cases
838 of high ($K_{satH}^{dp} = 2.6\ m/d$, red) and low ~~(~~conductivity ($K_{satH}^{dp} = 0.22\ m/d$, blue) ~~$K_{satH}^{deep}$~~ led to 26%
839 and 5.2% of annual $Q_G$ contribution to discharge (Q), respectively. (b) Deep groundwater fraction
840 as a function of $K_{satH}$ ~~–~~contrast between the deep and shallow zone. The $K_{satH}$ contrast was
841 limited to 1 in the figure as most watersheds exhibit a smaller $K_{satH}$ in the deep zone than in the
842 shallow zone. The two red and blue dots correspond to the two cases in left panel.

843

844 ~~A series of similar~~Several additional cases were further tested to ~~generate~~examine
845 the relationship between deep groundwater fraction (%) of discharge and $K_{satH}$ contrast
846 ~~(~~. Figure 6b~~). Results show~~ shows that the deep groundwater fraction ~~exponentially~~
847 ~~increased~~rapidly increases with the increasing ~~$K_{satH}$ contrast,~~ratio of $K_{satH}^{dp}$ / $K_{satH}^{sl}$,
848 reaching a limit ~~at~~ when $K_{satH}$ contrast is sufficiently high. ~~The results also suggest that~~
849 ~~the maximum~~The deep groundwater contribution to the stream ~~was limited to~~ reaches ~
850 40% ~~as most watersheds exhibit smaller $K_{satH}^{deep}$ than $K_{satH}^{shallow}$. The fitting function (dashed~~
851 ~~line) could be a useful predictor to quantify deep~~when the $K_{satH}^{dp}$ and $K_{satH}^{sl}$ are equal. In
852 natural systems, we do see places, for example, karst formations, where groundwater
853 ~~contribution at headwater watersheds given measured deep and shallow~~
854 ~~hydraulic~~contributes to more than 40% (Hartmann et al., 2014;Husic, 2018). These places
855 may have higher deeper conductivity~~.~~ than shallow soils due to the development of highly
856 conductive conduits.

857

858 ~~5~~6.2 ~~Reactive Transport~~ Example ~~1: Understanding nitrate~~ 2: Nitrate dynamics
859 ~~using~~in a spatially implicit domain

This example focuses on nitrate~~, which is the~~ ($NO_3^-$), a dominant dissolved N form in water ~~and has relatively~~ with abundant measurements ~~from 2008 to 2010~~ (https://criticalzone.org/shale-hills/data/datasets/) ~~(Weitzman and Kaye, 2018). Based on their~~(Weitzman and Kaye, 2018). The N processes at Shale Hills include atmospheric N deposition, soil N leaching, stream export, denitrification, and plant uptake (Figure 7). Based on field measurements, the atmospheric deposition ~~was~~at the site is the dominant N input and N export via discharge ~~was~~is only a small fraction (2.5%) of atmospheric N input~~. Most~~ , indicating most deposited N ~~was either~~is tightly cycled by plants or lost to the atmosphere via denitrification ~~or uptaken by trees. The model at Shale Hills watershed included atmospheric N deposition, soil N leaching, stream export, denitrification, and plant uptake (Figure 7).~~ .

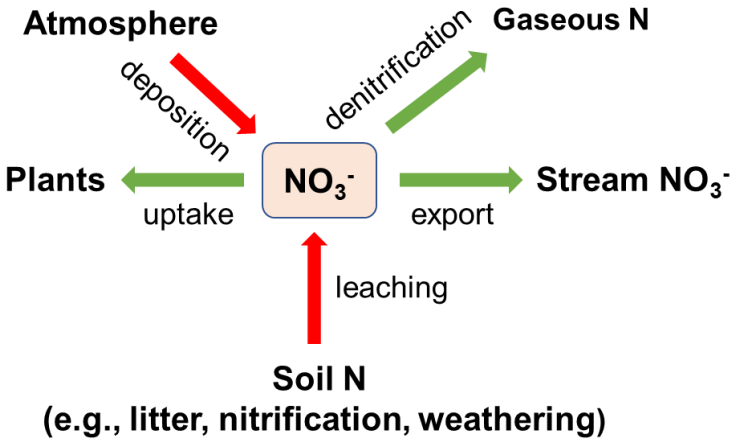



**Figure 7.** Modeled nitrogen processes ~~at Shale Hills.~~in Example 2. Atmospheric N deposition ~~was~~is the major N ~~sources (top red arrows);~~input; denitrification and plant uptake ~~were~~are the major N loss and sink ~~(green arrows).~~ Export ~~from~~via discharge ~~removes nitrate but it was a relatively~~ only occupies a small ~~one~~fraction.

The soil N leaching process was represented using a lumped reaction that generates $NO_3^-$. Conceptually this could represent the total rates of reactions including the decomposition of soil organic matter (SOM), nitrification, and rock weathering that generates $NO_3^-$. Its rate was assumed to depend on soil temperature and moisture and follows the equation $r_{leach} = kAf(T)f(S_w)$, where $r_{leach}$ [mol/s] is the leaching rate, $k$ = $10^{-9.7}$ [mol/m$^2$/s] is the leaching rate constant (Regnier and Steefel, 1999), and $A$ [m$^2$] is the surface area that represents the contact area between substrates and N transforming

microbe, and $f(T)$ and $f(S_w)$ are soil temperature (Eqn. 8) and soil moisture (Eqn. 9) functions, respectively. The surface area was calculated based on SOM volume fraction [$m^3/m^3$], specific surface area (SSA, [$m^2/g$]), substrate density [$g/cm^3$], and element volume [$m^3$]. Denitrification converts $NO_3^-$ to $N_2$ gas under anaerobic conditions. Here this process was modeled by the Monod rate law with DOC as the electron donor (Di Capua et al., 2019), $NO_3^-$ as the electron acceptor, and with an inhibition term $f(O_2)$ (Eqn. S13). The reaction rate: $r_{denitrification} = kA\frac{C_{DOC}}{K_{m,DOC}+C_{DOC}}\frac{C_{NO_3^-}}{K_{m,NO_3^-}+C_{NO_3^-}}f(O_2)f(T)f(S_w)$, where $k$ = $10^{-10}$ [$mol/m^2/s$] is the denitrification rate constant (Regnier and Steefel, 1999), half-saturation constants $K_{m,DOC} = 15\ [uM]$ and $K_{m,NO_3^-} = 45\ [uM]$ (Regnier and Steefel, 1999;Billen, 1977). For soil N leaching and denitrification, the SSA were respectively tuned as $1.6 \times 10^{-6}$ and $7.5 \times 10^{-5}$ [$m^2/g$] to reproduce observed stream nitrate dynamics. The calibrated values were orders of magnitude lower than the lab measured SSA of natural materials (e.g., SOM, 0.6 ~ 2 $m^2/g$) (Rutherford et al., 1992;Chiou et al., 1990). Such discrepancies between calibrated effective reactive surface area (i.e., ~~The soil N leaching process was a lumped reaction that generates $NO_3^-$ source, including the decomposition of soil organic matter (SOM), nitrification, and rock weathering. Its rate was assumed to depend on soil temperature and moisture:~~

~~$$r_{leach} = kAf(T)f(S_w) \quad (21)$$~~

~~Here $r_{leach}$ is the leaching rate (mol/s), $k$ is the rate constant ($mol/m^2/s$), and the surface area $A$ ($m^2$) is a lumped parameter representing the effective contact area between substrates and N transforming microbe. It was calculated based on SOM volume fraction ($m^3/m^3$), specific surface area (SSA, $m^2/g$), substrate density ($g/cm^3$), and element volume ($m^3$).~~

~~The denitrification process converts $NO_3^-$ to $N_2$ gas under anaerobic conditions. This process can be modeled by the Monod rate law with nitrate as the electron acceptor substrate ($K_{m,NO_3^-} = 45\ uM$ (Regnier and Steefel, 1999;Billen, 1977)) and with inhibition from $O_2$ (Eq. (22)). Under conditions where $O_2$ concentration is not explicitly modeled (this work), the $O_2$ inhibitory term can be replaced by a function of soil moisture (Eq. (24)). This is based on field evidence that denitrification typically occurs when soil moisture is greater~~

than 0.6 and increases with increasing soil moisture (Brady et al., 2008). Equation (24) says that under relatively drier conditions ($S_w < 0.6$), there is sufficient $O_2$ that denitrification does not occur; under wet conditions ($S_w \geq 0.6$), the $O_2$ becomes limiting such that denitrification can occur.

$$r_{denitrification} = kA\left(\frac{C_{NO_3}}{K_{m,NO_3} + C_{NO_3}}\right) f(O_2) f(T) f(S_w) \quad (22)$$

$$f(O_2) = \frac{K_{I,O_2}}{K_{I,O_2} + C_{O_2}} \quad (23), \text{ when } O_2 \text{ is explicitly modelled}$$

$$f(O_2) = \frac{0\ (S_w < 0.6)}{(S_w - 0.6) * 2.5\ (S_w \geq 0.6)} \quad (24), \text{ when } O_2 \text{ is not explicitly modelled}$$

Nitrate uptake by plants is intrinsically complex and not yet completely understood (Devienne-Barret et al., 2000;Crawford and Glass, 1998;Hachiya and Sakakibara, 2016). A variety of plant uptake models exists in literature with varying levels of complexity (Neitsch et al., 2011;Fisher et al., 2010;Cai et al., 2016). These models are mostly based on plant growth module or supply and demand approach that often requires detailed phenological and plant attributes such as growth cycle, root age and biomass, nitrate availability, phosphorous stress, and carbon allocation, in addition to local climate conditions such as temperature and soil moisture (Neitsch et al., 2011;Porporato et al., 2003;Dunbabin et al., 2002;Buysse et al., 1996;Fisher et al., 2010). Without all the detailed information, here we assumed a simple and operational approach to model nitrate uptake with dependence on $NO_3^-$ concentration, soil temperature and moisture, and rooting density (Eq. (25), (26)). More detailed, user-tailored plant uptake rate law can be added if needed.

$r_{uptake}$ =solid-water contact area) and lab measured absolute surface area are consistent with other observations in literature (Li et al., 2014;Heidari et al., 2017). The uptake rate constant was calibrated by constraining the partitioning of N transformation flux between denitrification and plant uptake by the ratio of 1:5, a value estimated from field measurements of gaseous N outputs (3.53 kg-N/ha/yr) and plant N uptake (18.3 kg-N/ha/yr) (Weitzman and Kaye, 2018). The uptake rate constant in the deep zone (> 2 m

in depth) was considered negligible (Weitzman and Kaye, 2018;Hasenmueller et al., 2017). Groundwater nitrate was initialized as 0.43 mg/L, the average of measured groundwater concentration during 2009 - 2010.

$$k_{uptake} C_{NO_3^-} f(T) f(S_w) f_{root}(d_w) \quad (25)$$

$$f_{root}(d_w) = \exp((-d_w + r)/s) \quad (26)$$

Where $k_{uptake}$ is the nitrate uptake rate (L/s), $f_{root}(d_w)$ is a normalized rooting density term in the range of 0 to 1 as a function of water depth to the groundwater ($d_w$). The rooting term (Eq. (26)) was exponentially fitted ($r = 0.0132, s = 0.202$) based on field measurements of root distribution along depth (Figure S8) (Hasenmueller et al., 2017). The exponentially declining root function is generally to be the case in forested watersheds but can be tailored to agricultural watersheds when field data are available.

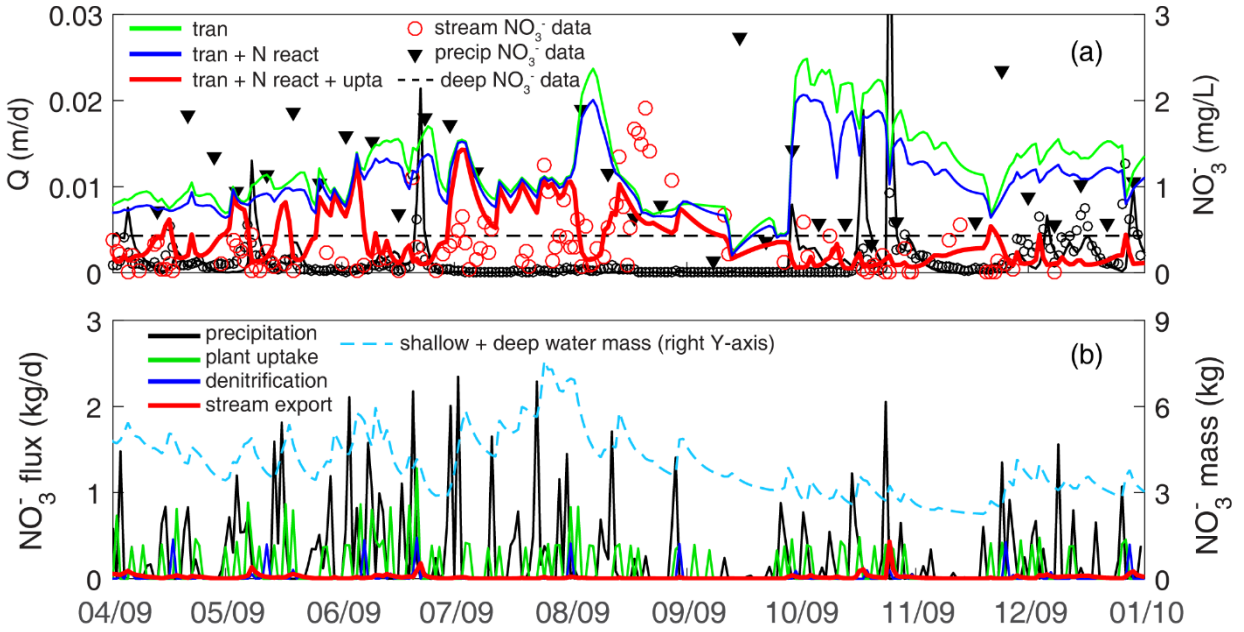
For microbial soil N leaching and denitrification, reaction rate constant $k$ was specified (Regnier and Steefel, 1999) and the lumped surface area $A$ ($m^2$, = specific surface area $m^2/g \times$ g of mass) was turned to reproduce stream nitrate dynamics and its C-Q pattern (Table S8). The calibrated effective specific surface area (SSA) were orders of magnitude lower than the lab measured SSA of natural materials (e.g., SOM, 0.6 ~ 2 $m^2/g$) (Rutherford et al., 1992;Chiou et al., 1990). Such discrepancies between calibrated effective reactive surface area (i.e., solid-water contact area) and lab measured absolute surface area are consistent with other observations (Li et al., 2014;Heidari et al., 2017). The nitrate uptake rate constant $k_{uptake}$ was calibrated to constrain the partitioning of N transformation flux between denitrification and plant uptake by the ratio of 1:5, a value estimated from field measurements of gaseous N outputs (3.53 kg-N/ha/yr) and plant N uptake (18.3 kg-N/ha/yr) (Weitzman and Kaye, 2018). We assumed that the nitrate uptake rate $k_{uptake}$ of the deep zone (> 2 m in depth) was 1/1000 of that in the shallow zone, based on the observations that the rooting density exponentially decrease with depth (Weitzman and Kaye, 2018;Hasenmueller et al., 2017). Groundwater nitrate was initialized as 0.43 mg/L, the average of measured groundwater concentration during 2009-2010.

**Temporal nitrate dynamics.** Three cases were set up to understand and quantify the effects of different processes in determining ~~the~~ nitrate dynamics (Figure ~~8~~8a). The *transport-only* case (~~green~~dashed line, *tran*) ~~only has N~~simulates nitrate input from precipitation (at 1.4 ± 0.96 mg/L, based on the 2009 data of NADP PA42 site) and N transport but without any reactions. It overestimated stream nitrate data (0.33 ± 0.39 mg/L) throughout the year. The *transport + N reactions* case (~~blue~~gray line, *tran + N react*) has ~~the~~ denitrification and soil N leaching processes but not plant uptake. ~~It~~ These two reactions lowered the nitrate concentration~~, suggesting their relative minor role~~ slightly, as these two processes compensate each other in ~~controlling N.~~adding and removing nitrate from water. The *transport + N reactions + uptake* case (~~red~~thick black line, *tran + N react + upta)* have all processes. It significantly lowered the nitrate concentration, especially in April-May and October-December. ~~There were some overestimated short nitrate~~Nitrate peaks from May to July, exhibiting comparable levels of high precipitation nitrate concentration (Figure ~~8a~~8b). It is noticeable that the three cases ~~(i.e., *transport-only*, *transport + N reactions*, *transport + N reactions + uptake*)~~ almost overlapped ~~(i.e., minimal difference)~~ at these overestimated short nitrate peaks, suggesting ~~the~~ nitrate-rich precipitation ~~was~~may not be routed into the subsurface where denitrification and plant uptake could occur~~ and lower the nitrate concentration. In short, hydrology controlled stream nitrate dynamics by partitioning the nitrate-rich precipitation into surface runoff, shallow lateral flow, and deep groundwater. Nitrate reactions primarily controlled stream concentration via the subsurface flow flowpath where the nitrate-rich precipitation undergone significant nitrate loss and sink, as denitrification and plant uptake only occurred to remove nitrate in the subsurface but not in surface water.~~.

~~Comparing the three outfluxes (Figure 8b), nitrate export via discharge (red) was negligible compared to denitrification (blue) and plant uptake (green). At the annual scale, stream nitrate export only accounted for 9.5% outfluxes, whereas denitrification and plant uptake took up 15% and 75% of precipitated $NO_3^-$, respectively. At Shale Hills, rock N leaching (weathering) is calculated up to 10% of N precipitation.~~

Although precipitation ~~source occurred primarily~~ from April to August ~~(~~accounted for 70% of the total simulation period~~),~~, larger storm events in October contributed more to the export. Deeper groundwater had higher nitrate concentration than shallow water,

because most plant uptake occurred in the shallow zone. The nitrate fluxes into the deeper zone however only contributed 26% of stream nitrate export at the annual scale, due to the relatively small groundwater contribution (9.5%) to the stream. Denitrification and plant uptake largely occurred during the wet ~~period, which coincided with the growing season. Denitrification peaks often showed up after major storm events.~~spring period, which is part of the leaf-on season. Denitrification peaks often appeared after major storm events. Comparing the three outfluxes (Figure 8c), nitrate export via discharge (red) was negligible compared to denitrification (blue) and plant uptake (green). At the annual scale, stream export only accounted for 9.5% outfluxes, whereas denitrification and plant uptake took up 15% and 75% of deposited $NO_3^-$, respectively. In other words, as Nitrate enters this system via precipitation, plant uptake can play a significant role in reducing nitrate level, indicating precipitated nitrate is tightly cycled in the system.



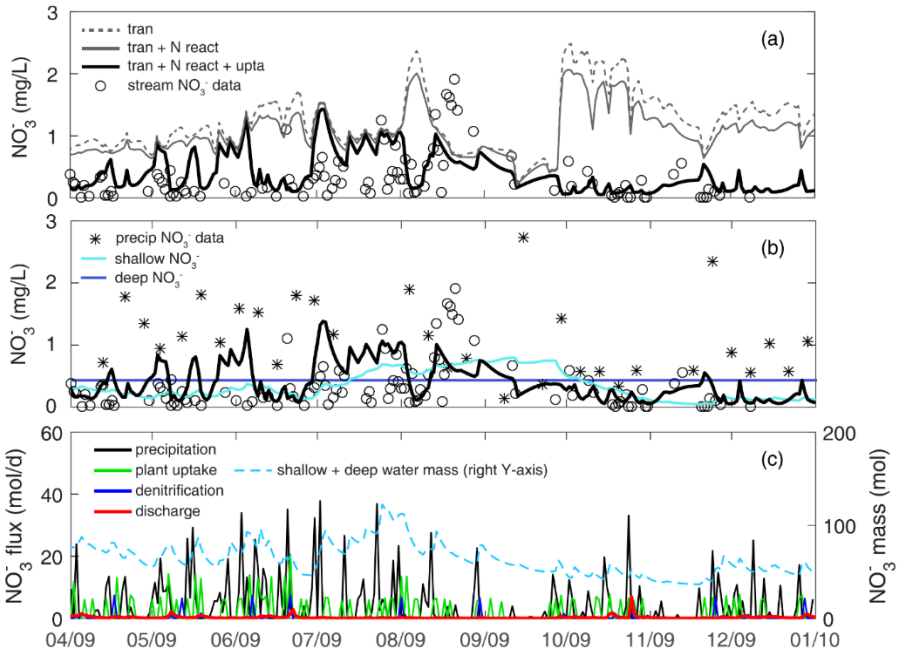
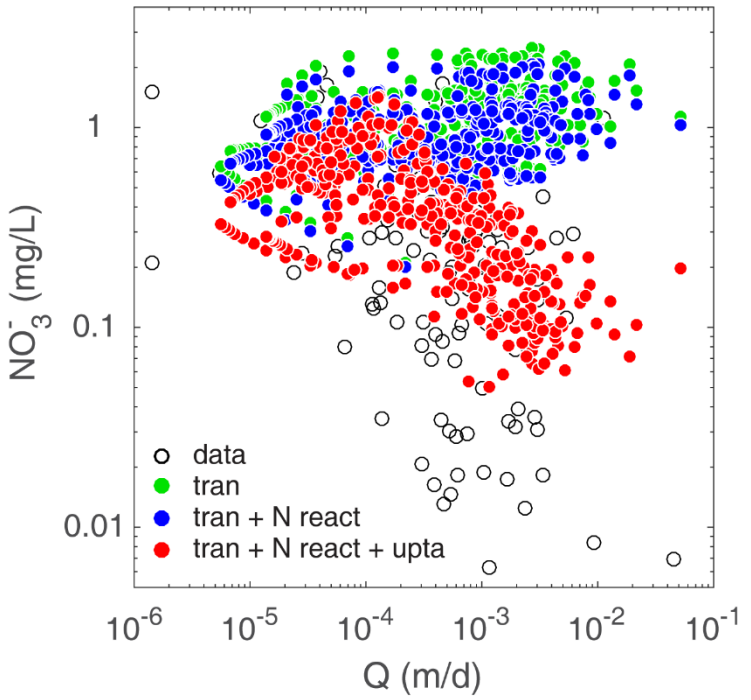



**Figure 8.** Stream nitrate dynamics and fluxes at Shale Hills in Example 2. (a) stream nitrate dynamics in three simulation conditions with different processes: *transport-only* (~~green~~dashed line, *tran*), *transport + N reaction* (~~blue~~gray line, *tran + N react*), *transport + N reaction + plant uptake* (~~red~~thick black line, *tran + N react + upta*), where N reactions include both nitrate leaching and ~~denitrifications~~ denitrification (see Figure ~~8). (a) stream nitrate dynamics;~~7); (b) nitrate concentration in precipitation, shallow and deep water; (c) nitrate fluxes and budget. Note the nitrate leaching was ignored in (b) due to its minimal flux as precipitation N deposition was as the dominant input source ~~(Weitzman and Kaye, 2018).~~(Weitzman and Kaye, 2018).

~~**C-Q patterns.** C-Q plots from the three cases showed distinct patterns (Figure 9). Specifically, the *transport-only* (green) and *transport + N reactions* (blue) cases led to chemostatic or slightly flushing patterns while the *transport + N reactions + plant uptake* (red) case showed a dilution pattern similar to field observation. The *transport-only* case showed a slightly flushing pattern because the shallow water had slightly higher nitrate concentration (directly from precipitation without reactions) than deep groundwater. This results in low stream concentrations from deep groundwater at low flow conditions and high stream concentrations from shallow water with higher nitrate at high flow conditions. With limited denitrification capacity (Figure 8a), the *transport + N reactions* case was similar to the *transport-only* case. In comparison, the plant uptake reduced nitrate~~

~~concentration in the shallow zone, to an extent lower than the concentration in the deeper zone, altering the C-Q pattern from primarily chemostatic to dilution (Figure 9).~~




**~~Figure 9.~~** ~~Concentration-discharge (C-Q) relationships under three scenarios that involve different processes: *transport-only* (green, *tran*), *transport + N reactions* (blue, *tran + N react*), *transport + N reactions + plant uptake* (red, *tran + N react + upta*).~~

## ~~5~~6.3 ~~Reactive Transport~~ Example ~~2~~3: DOC production and export in a spatially ~~explicit~~distributed domain

This example showcases the application of BioRT-Flux-PIHM in a spatially ~~explicit~~distributed mode. This work has been documented with full details in ~~Wen et al. (2020).~~Wen et al. (2020). Here we only introduce some key features and capabilities in the spatially ~~explicit~~distributed mode.

~~**Model set-up.** In this example, the~~The Shale Hills catchment was discretized into 535 prismatic land elements and 20 stream segments through PIHMgis based on the topography (Figure ~~10a~~9a). The heterogeneous distributions of soil depth and solid organic carbon within the domain (Figure ~~10b~~9b-c) were interpolated through ordinary kriging based on field surveys ~~(Andrews et al., 2011;Lin, 2006).~~(Andrews et al., 2011;Lin, 2006). Other soil and mineralogy properties such as hydraulic conductivity, van

Genuchten parameters, and ion exchange capacity were ~~also~~ spatially distributed following intensive field measurements ~~across the catchment (Jin and Brantley, 2011;Jin et al., 2010;Shi et al., 2013)~~(Jin and Brantley, 2011;Jin et al., 2010;Shi et al., 2013) (criticalzone.org/shale-hills/data/).

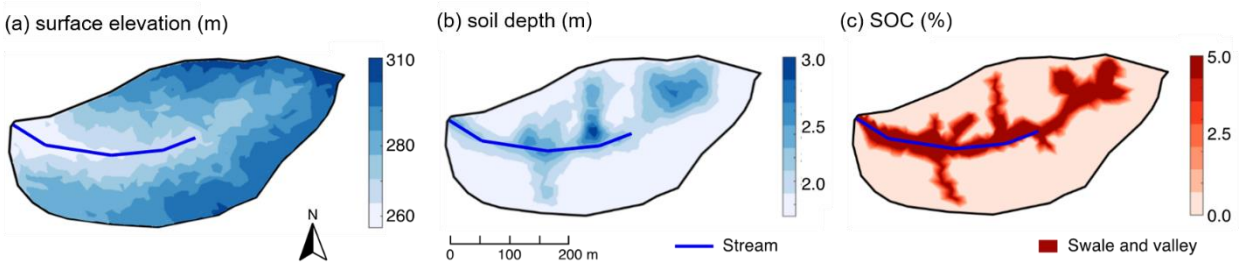



**Figure ~~10~~9**. Attributes of Shale Hills in the spatially ~~explicit~~distributed mode in Example 3: (a) surface elevation, (b) soil depth, and (c) soil organic carbon (SOC). The surface elevation was generated from lidar topographic data (criticalzone.org/shale-hills/data); Soil depths and SOC were interpolated using ordinary kriging based on field surveys ~~(Andrews et al., 2011;Lin, 2006).~~(Andrews et al., 2011;Lin, 2006). The SOC distribution in (c) was further simplified using the high, uniform SOC (5% v/v) in swales and valley soils based on field survey ~~(Andrews et al., 2011).~~(Andrews et al., 2011). Swales and valley floor areas were defined based on surface elevation via field survey and a 10 m resolution digital elevation model ~~(Lin, 2006).~~(Lin, 2006).

~~DOC was produced by the decomposition of soil organic carbon (SOC) via the following reaction:~~

$$SOC(s) \rightarrow DOC \quad (27)$$

~~The produced DOC can sorb on soils via the sorption reaction:~~

$$\equiv X + DOC \leftrightarrow \equiv XDOC \quad (28)$$

~~where $\equiv X$ and $\equiv XDOC$ represent the functional group without and with sorbed DOC, respectively (Rasmussen et al., 2018). For DOC production, with abundant SOC and $O_2$ in shallow soils serving as electron donors and acceptors, Eq. (27) can be simplified into $r_{DOC} = kAf(T)f(S_w)$, where $r_{DOC}$ is the local DOC production rate in individual grids; $k$ is the kinetic rate constant of net DOC production with a value of $10^{-10}$ mol/m$^2$/s (Zhi et al., 2019;Wieder et al., 2014); and $A$ is the lumped "surface area" (m$^2$, = $2.5\times10^{-3}$ m$^2$/g × g of SOC mass) that reflects the effective contact of water with SOC content and biomass (Chiou et al., 1990;Kaiser and Guggenberger, 2003;Zhi et al., 2019). The temperature~~

~~dependence function took the form $f(T) = 2.0^{|T-20|/10}$ while the moisture dependence function followed $f(S_w) = (S_w)^{1.0}$ (Yan et al., 2018;Hamamoto et al., 2010). In DOC sorption, equilibrium constant $K_{eq}$ with a value of $10^{0.2}$ ($= \frac{[\equiv XDOC]}{[\equiv X][DOC]}$) represents the thermodynamic limit of the sorption; The sum of $[\equiv X]$ and $[\equiv XDOC]$ represents the sorption capacity of the soil with a value ranging from $4.0\times10^{-5}$ - $6.0\times10^{-5}$ mol/g soil at Shale Hills (Jin et al., 2010;Li et al., 2017a), depending on the mineralogy.~~

**Temporal and spatial patterns of DOC production and export.** The model outputs followed the general trend of stream DOC ~~data~~measurements (NSE = 0.55 for monthly DOC concentration; Figure ~~11a~~10a), with high values (~15 mg/L) in the dry periods (July-September). The model enabled the identification of spatial patterns and ~~the~~ hot spots of reactions. In May when soil water is relatively abundant, the valley and swales with deeper soils (Figure ~~11b~~10b) generally tended to be wetter compared to the hillslope and ridgetop, and were hydrologically connected to the stream (Figure ~~11b~~10b, c). The distribution of local DOC production rate $r_{DOC}$ and DOC concentration followed that of SOC (Figure ~~11c~~10c) and water content (Figure ~~11b~~10b). Low $r_{DOC}$ in relatively dry planar hillslopes and uplands resulted in low soil water DOC. The average stream DOC (~5 mg/L) reflected soil water DOC in the valley and swales.

In August, the hydrologically-connected zones with high water content shrank to the vicinity of the stream and river bed. With high temperature in summer, $r_{DOC}$ increased by 2-fold from May across the whole catchment while still exhibited the highest values in the SOC-rich regions. Soil water DOC concentration increased by a factor of 2 because the produced DOC was trapped in low soil moisture areas that were not hydrologically connected to the stream. In the north side with low water content (Figure ~~11b~~10b), the soil water DOC (~7 mg/L in average) accumulated more than the south side (~5 mg/L in average). The high shallow water DOC (~10 mg/L) in the stream vicinity dominated the stream DOC in August.

In October, precipitation wetted the catchment again. The hydrologically connected zones expanded beyond swales and the valley to the upland hillslopes (Figure ~~11c~~10c). The increase in hydrological connectivity zones favored the ~~mixture~~mixing of shallow water DOC sourced from upland hillslopes (low DOC), swales, and valley (high

DOC) into stream rather than only from the stream vicinity with high DOC in the dry August, leading to a drop in stream DOC.

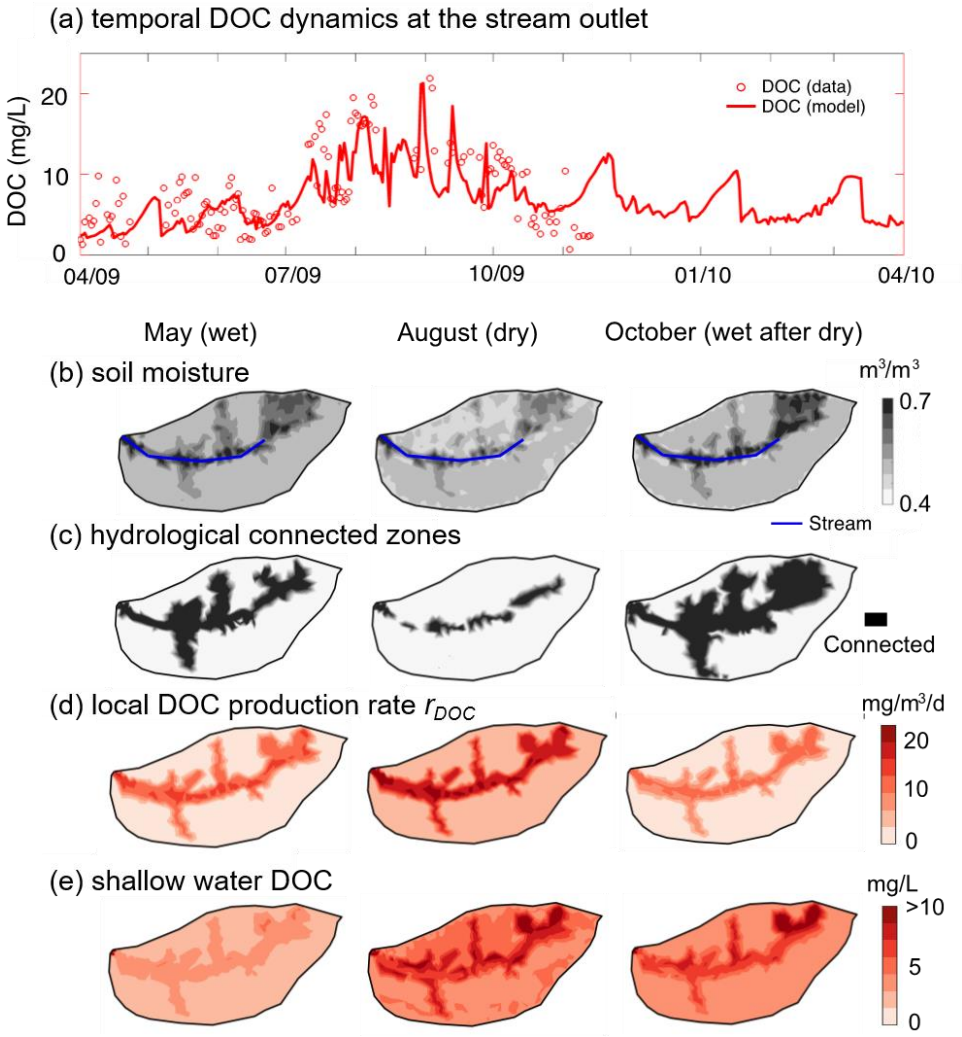



**Figure ~~11~~10**. (a) Temporal dynamics of stream DOC concentration; spatial profiles of (b) shallow soil moisture, (c) hydrologically connected zones, (d) local DOC production rates $r_{DOC}$ and (e) shallow water DOC concentration in May (wet), August (dry), and October (wet after dry) of 2009. The soil DOC and $r_{DOC}$ were high in swales and valley with relatively high shallow water and SOC content. August had the highest shallow water DOC concentration compared to May and October, because most DOC accumulated in zones that are disconnected to the stream.

**C-Q patterns.** The DOC C-Q relationship showed a non-typical pattern with flushing first and transitioning into a dilution pattern, with ~~a general (~~an overall~~)~~ C-Q slope *b* = -0.23 (Figure ~~12~~11). At low discharges (< $1.8\times10^{-4}$ m/d) in the summer dry period, the stream DOC mainly came from the organic-rich swales and valley floor zones with high soil water

DOC (Figure ~~11e~~10e). With discharge increasing in wetter period (i.e., spring and fall), the contribution from planar hillslopes and uplands with lower DOC concentration increased (Figure ~~11e~~10e), leading to the dilution of stream DOC.

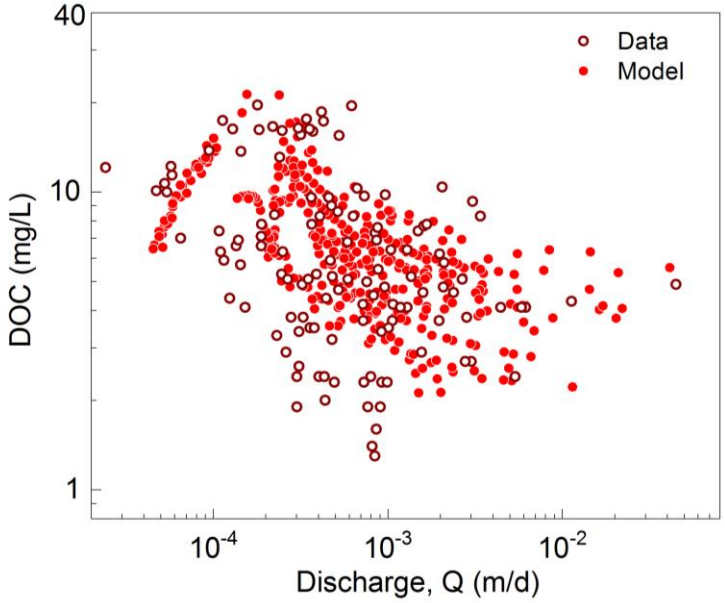



**Figure ~~12~~11**. Relationships of daily discharge (*Q*) with stream DOC concentration. With the increase of *Q*, the stream water first shifted from the dominance of groundwater with low DOC at very low discharge to the predominance of organic-rich soil water from swales and valley at intermediate discharge. As the discharge increases further, the stream water switches to the dominance of high flow with lower DOC water from planar hillslopes and uplands, resulting in a dilution C-Q pattern (modified from Wen et al., ~~(~~2020~~)).~~).

## 7. Discussion

The watershed biogeochemical model BioRT-Flux-PIHM brings the reactive transport modeling capabilities to the watershed scale, enabling the simulation of subsurface shallow and deep flow paths and biogeochemical reactions influenced by hydroclimatic conditions and land-surface interactions. The expanded model capability of simulating bio-mediated processes such as plant uptake, soil respiration, and microbe-mediated redox reactions enables the simulation of carbon and nutrient cycling in the shallow subsurface. The inclusion of the deep groundwater zone allows the exploration of the effects of subsurface structure on hydrological partitioning between shallow soil lateral flow and deep groundwater, and their relationships with stream discharge. Although not shown here, the model can also simulate deeper groundwater coming from

regional aquifers across the outer boundary. This can be particularly useful for watersheds of higher stream orders, where a large proportion of deep water may come from nearby regional aquifers.

The model presented here is complex and process-based. The computational cost of solving a spatially distributed, nonlinear, multi-component reactive transport model is high, posing challenges for the application of ensemble-based uncertainty analysis and model weighting/selection methods (Song et al., 2015). With additional reaction and transport processes, the model includes more functions (such as reaction kinetic rate laws) and parameters (e.g., reaction rate constants, surface area) than hydrological models, which have already been criticized for their complexity, equifinality, uncertainty, and data demands (Beven, 2001, 2006;Kirchner et al., 1996). These issues will persist even though reactive transport models will be constrained by additional chemical data. A major source of uncertainty in these models lies in epistemic uncertainties, i.e., the lack of specific knowledge in forcing data and details of reactivities (e.g., spatial distribution and abundance of reactive materials), on top of uncertainties related to hydrology (Beven, 2000;Beven and Freer, 2001). The model's conceptual foundations also represent a major source of uncertainty.

It is in this spirit of "balancing" the cost and gain that we present both spatial distributed and lumped modes for the BioRT model. Compared to the distributed version, the spatially implicit model~~, the spatial representation enables the exploration on~~ requires less spatial data, is computationally inexpensive, and is relatively easy to set up. It can assess the average dynamics of the water and solute dynamics and focus on the interactions among processes without resolving spatial details. The lumped approach can also accommodate basins with low data availability, and it can be easier for students to learn to use the model. In contrast, spatially explicit representations enable the exploration of the "hot spots" (~~i.~~e.g., swales and riparian zones with high soil water DOC concentrations in Figure ~~11e~~10e) and their contribution to stream chemistry at different times. Spatial heterogeneities in watershed properties (e.g., soil types and depth, lithology, vegetation, biomass, and mineralogy) are ~~omnipresent~~ubiquitous in natural systems. ~~Yet~~However, a general understanding of the linkage between local catchment features and catchment-scale dynamics (e.g., stream concentration dynamics and solute

export pattern) is ~~still~~often lacking. ~~Questions such as~~ We generally do not understand how ~~the heterogeneous features affect~~spatial heterogeneity affects water flow paths, stream water chemistry, and biogeochemical reaction rates ~~remain largely unanswered.~~. The spatially ~~explicit~~distributed model provides a tool to further explore these questions. Ultimately, the choice of the model complexity level depends on the research questions that the model is set to answer. At the end, we all need to balance cost and gain when deciding to use a simple or complex model, striving to be "simple but not simplistic" (Beven and Lane, 2019).

## ~~6~~8. Summary and conclusion

This paper introduces the watershed-scale biogeochemical reactive transport code BioRT (short for BioRT-Flux-PIHM~~. This~~). The code integrates processes of land-surface interactions, surface hydrology, and multi-component biogeochemical reactive transport. The new development enables the simulation of 1) biotic reactions including plant uptake, soil respiration, and microbe-mediated redox reactions ~~and plant uptake~~, and 2) surface water interactions with ~~water~~groundwater from deeper subsurface ~~zones~~that still interacts with streams. BioRT has been verified against the widely used reactive transport code CrunchTope for soil carbon, nitrogen, and phosphorus processes. The BioRT module has been applied to understand carbon, nitrogen, and weathering processes in Shale Hills in ~~central~~ Pennsylvania, Coal Creek in Colorado, and Volcán Chimborazo watershed in Andes in Ecuador. Here we showcase the modeling capability of surface-groundwater interactions~~, transport~~ and reactive transport processes relevant to nitrate and DOC in Shale Hills in two simulation modes. One is in a spatially ~~implicit~~lumped mode using averaged properties and another is in a spatially ~~explicit~~distributed mode with consideration of spatial heterogeneity. Results show that the deep groundwater flow that interacts with the stream is primarily controlled by the hydraulic conductivity contrast between shallow and deep zone. ~~Soil~~ biogeochemical reactions in shallow soil primarily ~~determines~~determine the ~~shallow~~stream water chemistry~~, especially C, N, and biogenic solutes,~~ under high flow conditions. The spatially ~~implicit~~lumped method with two lumped grids can capture the temporal dynamics of average behavior and mass balance; the spatially ~~explicit~~distributed running mode can be used to understand the spatial dynamics

and to identify ~~'~~"hot ~~spots'~~spots" of reactions. The code can be used for biogeochemical reactive transport simulations in watersheds under diverse climate, land cover, and geology conditions.

**Data availability**. Field data (e.g., discharge, stream chemistry) is archived at Shale Hills data portal: http://criticalzone.org/shale-hills/data/datasets/ or maintained at HydroShare: https://www.hydroshare.org/group/147.

**Code availability**. The current model release (BioRT-Flux-PIHM v1.0), including documentation, source code, example data, is available at GitHub repository: https://github.com/PSUmodeling/BioRT-Flux-PIHM.

**Competing interests.** The authors declare that they have no conflict of interest.

**Author contributions.** LL conceived the model idea and oversaw the model development. WZ coded the BioRT module, verified the code against the benchmark reactive transport model CrunchTope, and applied and tested the model at Shale Hills watershed. YS developed the deep groundwater component and integrated the BioRT-Flux-PIHM v1.0 into the MM-PIHM family. WH, LS, KS, DK, BS, and GHCN tested the code during its development and contributed ~~their~~ study cases.

**Acknowledgement.** We acknowledge the funding support from the Department of Energy, Subsurface Biogeochemistry Program DE-SC0020146, National Science Foundation Hydrological Sciences EAR-1758795. LS and GCN were supported by National Science Foundation Grant EAR-1759071. We appreciate data from the Susquehanna Shale Hills Critical Zone Observatory (SSHCZO) supported by National Science Foundation Grant EAR – 0725019 (C. Duffy), EAR – 1239285 (S. Brantley), and EAR – 1331726 (S. Brantley). Data were collected in Penn State's Stone Valley Forest, which is funded by the Penn State College of Agriculture Sciences, Department of Ecosystem Science and Management, and managed by the staff of the Forestlands Management Office.

1239

## References


Andrews, D. M., Lin, H., Zhu, Q., Jin, L., and Brantley, S. L.: Hot spots and hot moments of dissolved organic carbon export and soil organic carbon storage in the Shale Hills catchment, Vadose Zone Journal, 10, 943-954, 2011.

Anyah, R. O., Weaver, C. P., Miguez‐Macho, G., Fan, Y., and Robock, A.: Incorporating water table dynamics in climate modeling: 3. Simulated groundwater influence on coupled land‐atmosphere variability, Journal of Geophysical Research: Atmospheres, 113, 2008.

Bai, J., Zhang, G., Zhao, Q., Lu, Q., Jia, J., Cui, B., and Liu, X.: Depth-distribution patterns and control of soil organic carbon in coastal salt marshes with different plant covers, Sci Rep-Uk, 6, 34835, 10.1038/srep34835, 2016.

Bao, C., Li, L., Shi, Y., and Duffy, C.: Understanding watershed hydrogeochemistry: 1. Development of RT‐Flux‐PIHM, Water Resources Research, 53, 2328-2345, 2017.

Basu, N. B., Destouni, G., Jawitz, J. W., Thompson, S. E., Loukinova, N. V., Darracq, A., Zanardo, S., Yaeger, M., Sivapalan, M., Rinaldo, A., and Rao, P. S. C.: Nutrient loads exported from managed catchments reveal emergent biogeochemical stationarity, Geophys. Res. Lett., 37, 10.1029/2010GL045168, 2010.

Bhatt, G., Kumar, M., and Duffy, C. J.: A tightly coupled GIS and distributed hydrologic modeling framework, Environmental Modelling & Software, 62, 70-84, 10.1016/j.envsoft.2014.08.003, 2014.

Billen, G.: Etude écologique des transformations de l'azote dans les sédiments marins, 1977.

Brady, N. C., Weil, R. R., and Weil, R. R.: The nature and properties of soils, Prentice Hall Upper Saddle River, NJ, 2008.

Brantley, S. L., Kubicki, J. D., and White, A. F.: Kinetics of water-rock interaction, 2008.

Brantley, S. L., Lebedeva, M. I., Balashov, V. N., Singha, K., Sullivan, P. L., and Stinchcomb, G.: Toward a conceptual model relating chemical reaction fronts to water flow paths in hills, Geomorphology, 277, 100-117, 2017.

Brantley, S. L., White, T., West, N., Williams, J. Z., Forsythe, B., Shapich, D., Kaye, J., Lin, H., Shi, Y. N., Kaye, M., Herndon, E., Davis, K. J., He, Y., Eissenstat, D., Weitzman, J., DiBiase, R., Li, L., Reed, W., Brubaker, K., and Gu, X.: Susquehanna Shale Hills Critical Zone Observatory: Shale Hills in the Context of Shaver's Creek Watershed, Vadose Zone Journal, 17, 1-19, ARTN 180092, 10.2136/vzj2018.04.0092, 2018.

Buysse, J., Smolders, E., and Merckx, R.: Modelling the uptake of nitrate by a growing plant with an adjustable root nitrate uptake capacity, Plant and Soil, 181, 19-23, 1996.

Cai, X., Yang, Z.-L., Fisher, J., Zhang, X., Barlage, M., and Chen, F.: Integration of nitrogen dynamics into the Noah-MP land surface model v1. 1 for climate and environmental predictions, Geoscientific Model Development (Online), 9, 2016.

Chiou, C. T., Lee, J. F., and Boyd, S. A.: The surface area of soil organic matter, Environmental Science & Technology, 24, 1164-1166, 1990.

Condon, L. E., Maxwell, R. M., and Gangopadhyay, S.: The impact of subsurface conceptualization on land energy fluxes, Advances in Water Resources, 60, 188-203, 10.1016/j.advwatres.2013.08.001, 2013.

Crawford, N. M., and Glass, A. D.: Molecular and physiological aspects of nitrate uptake in plants, Trends in plant science, 3, 389-395, 1998.

Davidson, E. A., and Janssens, I. A.: Temperature sensitivity of soil carbon decomposition and feedbacks to climate change, Nature, 440, 165-173, 10.1038/nature04514, 2006.

Davidson, E. A., Janssens, I.A.: Temperature sensitivity of soil carbon decomposition and feedbacks to climate change, Nature, 440, 165-173, 2006.

Devienne-Barret, F., Justes, E., Machet, J., and Mary, B.: Integrated control of nitrate uptake by crop growth rate and soil nitrate availability under field conditions, Annals of Botany, 86, 995-1005, 2000.

Dingman, S. L.: Physical hydrology, Waveland press, 2015.

Dunbabin, V. M., Diggle, A. J., Rengel, Z., and Van Hugten, R.: Modelling the interactions between water and nutrient uptake and root growth, Plant and Soil, 239, 19-38, 2002.

Fatichi, S., Vivoni, E. R., Ogden, F. L., Ivanov, V. Y., Mirus, B., Gochis, D., Downer, C. W., Camporese, M., Davison, J. H., Ebel, B., Jones, N., Kim, J., Mascaro, G., Niswonger, R., Restrepo, P., Rigon, R., Shen, C., Sulis, M., and Tarboton, D.: An overview of current applications, challenges, and future trends in distributed process-based models in hydrology, Journal of Hydrology, 537, 45-60, 10.1016/j.jhydrol.2016.03.026, 2016.

Fatichi, S., Manzoni, S., Or, D., and Paschalis, A.: A Mechanistic Model of Microbially Mediated Soil Biogeochemical Processes: A Reality Check, Global Biogeochemical Cycles, 33, 620-648, 10.1029/2018gb006077, 2019.

Filoso, S., Vallino, J., Hopkinson, C., Rastetter, E., and Claessens, L.: Modeling nitrogen transport in the Ipswich River Basin, Massachusetts, using a hydrological simulation program in FORTRAN (HSPF) 1, JAWRA Journal of the American Water Resources Association, 40, 1365-1384, 2004.

Fisher, J., Sitch, S., Malhi, Y., Fisher, R., Huntingford, C., and Tan, S. Y.: Carbon cost of plant nitrogen acquisition: A mechanistic, globally applicable model of plant nitrogen uptake, retranslocation, and fixation, Global Biogeochemical Cycles, 24, 2010.

Friedlingstein, P., Cox, P., Betts, R., Bopp, L., von Bloh, W., Brovkin, V., Cadule, P., Doney, S., Eby, M., and Fung, I.: Climate–carbon cycle feedback analysis: results from the C4MIP model intercomparison, Journal of climate, 19, 3337-3353, 2006.

Gassman, P. W., Reyes, M. R., Green, C. H., and Arnold, J. G.: The soil and water assessment tool: Historical development, applications, and future research directions, T Asabe, 50, 1211-1250, 2007.

Gatel, L., Lauvernet, C., Carluer, N., Weill, S., Tournebize, J., and Paniconi, C.: Global evaluation and sensitivity analysis of a physically based flow and reactive transport model on a laboratory experiment, Environmental Modelling & Software, 113, 73-83, 10.1016/j.envsoft.2018.12.006, 2019.

Gleeson, T., Befus, K. M., Jasechko, S., Luijendijk, E., and Cardenas, M. B.: The global volume and distribution of modern groundwater, Nature Geoscience, 9, 161, 10.1038/ngeo2590 https://www.nature.com/articles/ngeo2590#supplementary-information, 2015.

Godsey, S. E., Kirchner, J. W., and Clow, D. W.: Concentration–discharge relationships reflect chemostatic characteristics of US catchments, Hydrol. Process., 23, 1844-1864, 10.1002/hyp.7315, 2009.

Green, T. R.: Linking climate change and groundwater, in: Integrated groundwater management, Springer, Cham, 97-141, 2016.

Gurdak, J. J.: Groundwater: Climate-induced pumping, Nature Geoscience, 10, 71, 2017.

Hachiya, T., and Sakakibara, H.: Interactions between nitrate and ammonium in their uptake, allocation, assimilation, and signaling in plants, Journal of Experimental Botany, 68, 2501-2512, 10.1093/jxb/erw449, 2016.

Hamamoto, S., Moldrup, P., Kawamoto, K., and Komatsu, T.: Excluded‐volume expansion of Archie's law for gas and solute diffusivities and electrical and thermal conductivities in variably saturated porous media, Water Resources Research, 46, 2010.

Han, B., Benner, S. G., and Flores, A. N.: Including Variability across Climate Change Projections in Assessing Impacts on Water Resources in an Intensively Managed Landscape, Water, 11, 286, 2019.

Hararuk, O., Smith, M. J., and Luo, Y.: Microbial models with data-driven parameters predict stronger soil carbon responses to climate change, Glob. Chang. Biol., 21, 2439-2453, 10.1111/gcb.12827, 2015.

Hasenmueller, E. A., Jin, L., Stinchcomb, G. E., Lin, H., Brantley, S. L., and Kaye, J. P.: Topographic controls on the depth distribution of soil CO2 in a small temperate watershed, Applied Geochemistry, 63, 58-69, 2015.

Hasenmueller, E. A., Gu, X., Weitzman, J. N., Adams, T. S., Stinchcomb, G. E., Eissenstat, D. M., Drohan, P. J., Brantley, S. L., and Kaye, J. P.: Weathering of rock to regolith: The activity of deep roots in bedrock fractures, Geoderma, 300, 11-31, 2017.

Heidari, P., Li, L., Jin, L., Williams, J. Z., and Brantley, S. L.: A reactive transport model for Marcellus shale weathering, Geochimica et Cosmochimica Acta, 217, 421-440, 2017.

Herndon, E. M., Dere, A. L., Sullivan, P. L., Norris, D., Reynolds, B., and Brantley, S. L.: Landscape heterogeneity drives contrasting concentration–discharge relationships in shale headwater catchments, Hydrology and earth system sciences, 19, 3333-3347, 2015.

Hindmarsh, A. C., Brown, P. N., Grant, K. E., Lee, S. L., Serban, R., Shumaker, D. E., and Woodward, C. S.: SUNDIALS: Suite of nonlinear and differential/algebraic equation solvers, ACM Transactions on Mathematical Software (TOMS), 31, 363-396, 2005.

Hodges, C., Kim, H., Brantley, S. L., and Kaye, J.: Soil CO 2 and O 2 Concentrations Illuminate the Relative Importance of Weathering and Respiration to Seasonal Soil Gas Fluctuations, Soil Science Society of America Journal, 83, 1167-1180, 2019.

Jin, L., and Brantley, S. L.: Soil chemistry and shale weathering on a hillslope influenced by convergent hydrologic flow regime at the Susquehanna/Shale Hills Critical Zone Observatory, Applied Geochemistry, 26, Supplement, S51-S56, 10.1016/j.apgeochem.2011.03.027, 2011.

Jin, L. X., Ravella, R., Ketchum, B., Bierman, P. R., Heaney, P., White, T., and Brantley, S. L.: Mineral weathering and elemental transport during hillslope evolution at the Susquehanna/Shale Hills Critical Zone Observatory, Geochim Cosmochim Ac, 74, 3669-3691, 10.1016/j.gca.2010.03.036, 2010.

Kaiser, K., and Guggenberger, G.: Mineral surfaces and soil organic matter, European Journal of Soil Science, 54, 219-236, 10.1046/j.1365-2389.2003.00544.x, 2003.

Kirchner, J. W.: A double paradox in catchment hydrology and geochemistry, Hydrol. Process., 17, 871-874, 10.1002/hyp.5108, 2003.

Kuntz, B. W., Rubin, S., Berkowitz, B., and Singha, K.: Quantifying Solute Transport at the Shale Hills Critical Zone Observatory, Vadose Zone Journal, 10, 843-857, 10.2136/vzj2010.0130, 2011.

Lam, Q. D., Schmalz, B., and Fohrer, N.: Modelling point and diffuse source pollution of nitrate in a rural lowland catchment using the SWAT model, Agricultural Water Management, 97, 317-325, 10.1016/j.agwat.2009.10.004, 2010.

Laroche, A. M., Gallichand, J., Lagacé, R., and Pesant, A.: Simulating atrazine transport with HSPF in an agricultural watershed, Journal of Environmental Engineering, 122, 622-630, 1996.

Leonard, L., and Duffy, C. J.: Essential terrestrial variable data workflows for distributed water resources modeling, Environmental modelling & software, 50, 85-96, 2013.

Li, L., Salehikhoo, F., Brantley, S. L., and Heidari, P.: Spatial zonation limits magnesite dissolution in porous media, Geochimica et Cosmochimica Acta, 126, 555-573, 10.1016/j.gca.2013.10.051, 2014.

Li, L., Bao, C., Sullivan, P. L., Brantley, S., Shi, Y., and Duffy, C.: Understanding watershed hydrogeochemistry: 2. Synchronized hydrological and geochemical processes drive stream chemostatic behavior, Water Resources Research, 53, 2346-2367, 2017a.

Li, L., Maher, K., Navarre-Sitchler, A., Druhan, J., Meile, C., Lawrence, C., Moore, J., Perdrial, J., Sullivan, P., Thompson, A., Jin, L., Bolton, E. W., Brantley, S. L., Dietrich, W. E., Mayer, K. U., Steefel, C. I., Valocchi, A., Zachara, J., Kocar, B., McIntosh, J., Tutolo, B. M., Kumar, M., Sonnenthal, E., Bao, C., and Beisman, J.: Expanding the role of reactive transport models in critical zone processes, Earth-Science Reviews, 165, 280-301, 10.1016/j.earscirev.2016.09.001, 2017b.

Li, L., DiBiase, R. A., Del Vecchio, J., Marcon, V., Hoagland, B., Xiao, D., Wayman, C., Tang, Q., He, Y., Silverhart, P., Szink, I., Forsythe, B., Williams, J. Z., Shapich, D., Mount, G. J., Kaye, J., Guo, L., Lin, H., Eissenstat, D., Dere, A., Brubaker, K., Kaye, M., Davis, K. J., Russo, T., and Brantley, S. L.: The Effect of Lithology and Agriculture at the Susquehanna Shale Hills Critical Zone Observatory, Vadose Zone Journal, 17, 10.2136/vzj2018.03.0063, 2018.

Li, L.: Watershed reactive transport, Reviews in Mineralogy and Geochemistry, 85, 381-418, 2019.

Lin, H.: Temporal stability of soil moisture spatial pattern and subsurface preferential flow pathways in the shale hills catchment, Vadose Zone J, 5, 317-340, 10.2136/vzj2005.0058, 2006.

Maavara, T., Lauerwald, R., Laruelle, G. G., Akbarzadeh, Z., Bouskill, N. J., Van Cappellen, P., and Regnier, P.: Nitrous oxide emissions from inland waters: Are IPCC estimates too high?, Global Change Biology, 0, doi:10.1111/gcb.14504, 2018.

MacQuarrie, K. T. B., and Mayer, K. U.: Reactive transport modeling in fractured rock: A state-of-the-science review, Earth-Science Reviews, 72, 189-227, 10.1016/j.earscirev.2005.07.003, 2005.

Marin-Spiotta, E., Silver, W. L., Swanston, C. W., and Ostertag, R.: Soil organic matter dynamics during 80 years of reforestation of tropical pastures, Global Change Biology, 15, 1584-1597, 10.1111/j.1365-2486.2008.01805.x, 2009.

Maxwell, R. M., Lundquist, J. K., Mirocha, J. D., Smith, S. G., Woodward, C. S., and Tompson, A. F.: Development of a coupled groundwater–atmosphere model, Monthly Weather Review, 139, 96-116, 2011.

Mayer, K. U., Frind, E. O., and Blowes, D. W.: Multicomponent reactive transport modeling in variably saturated porous media using a generalized formulation for kinetically controlled reactions, Water Resources Research, 38, 13-11-13-21, 10.1029/2001wr000862, 2002.

Miller, M. P., Tesoriero, A. J., Hood, K., Terziotti, S., and Wolock, D. M.: Estimating Discharge and Nonpoint Source Nitrate Loading to Streams From Three End-Member Pathways Using High-Frequency Water Quality Data, Water Resources Research, 53, 10201-10216, 10.1002/2017wr021654, 2017.

Miller, M. P., Capel, P. D., García, A. M., and Ator, S. W.: Response of Nitrogen Loading to the Chesapeake Bay to Source Reduction and Land Use Change Scenarios: A SPARROW ‐ Informed Analysis, JAWRA Journal of the American Water Resources Association, 56, 100-112, 2020.

Moatar, F., Abbott, B. W., Minaudo, C., Curie, F., and Pinay, G.: Elemental properties, hydrology, and biology interact to shape concentration ‐ discharge curves for carbon, nutrients, sediment, and major ions, Water Resources Research, 53, 1270-1287, 2017.

Monod, J.: The growth of bacterial cultures, Annual review of microbiology, 3, 371-394, 1949.

Moriasi, D. N., Gowda, P. H., Arnold, J. G., Mulla, D. J., Ale, S., and Steiner, J. L.: Modeling the impact of nitrogen fertilizer application and tile drain configuration on nitrate leaching using SWAT, Agricultural Water Management, 130, 36-43, 10.1016/j.agwat.2013.08.003, 2013.

Musolff, A., Schmidt, C., Selle, B., and Fleckenstein, J. H.: Catchment controls on solute export, Adv. Water Resour., 86, 133-146, 10.1016/j.advwatres.2015.09.026, 2015.

Neitsch, S. L., Arnold, J. G., Kiniry, J. R., and Williams, J. R.: Soil and water assessment tool theoretical documentation version 2009, Texas Water Resources Institute, 2011.

Niu, J., and Phanikumar, M. S.: Modeling watershed-scale solute transport using an integrated, process-based hydrologic model with applications to bacterial fate and transport, Journal of Hydrology, 529, 35-48, 10.1016/j.jhydrol.2015.07.013, 2015.

Ostle, N. J., Smith, P., Fisher, R., Woodward, F. I., Fisher, J. B., Smith, J. U., Galbraith, D., Levy, P., Meir, P., McNamara, N. P., and Bardgett, R. D.: Integrating plant–soil interactions into global carbon cycle models, Journal of Ecology, 97, 851-863, 10.1111/j.1365-2745.2009.01547.x, 2009.

Ottoy, S., Elsen, A., Van De Vreken, P., Gobin, A., Merckx, R., Hermy, M., and Van Orshoven, J.: An exponential change decline function to estimate soil organic carbon stocks and their changes from topsoil measurements, European Journal of Soil Science, 67, 816-826, 2016.

Porporato, A., D'odorico, P., Laio, F., and Rodriguez-Iturbe, I.: Hydrologic controls on soil carbon and nitrogen cycles. I. Modeling scheme, Advances in water resources, 26, 45-58, 2003.

Qiu, H., Niu, J., and Hu, B. X.: Quantifying the integrated water and carbon cycle in a data-limited karst basin using a process-based hydrologic model, Environmental Earth Sciences, 78, 328, 2019.

Qu, Y., and Duffy, C. J.: A semidiscrete finite volume formulation for multiprocess watershed simulation, Water Resour. Res., 43, W08419, 10.1029/2006wr005752, 2007.

Rasmussen, C., Heckman, K., Wieder, W. R., Keiluweit, M., Lawrence, C. R., Berhe, A. A., Blankinship, J. C., Crow, S. E., Druhan, J. L., Hicks Pries, C. E., Marin-Spiotta, E., Plante, A. F., Schädel, C., Schimel, J. P., Sierra, C. A., Thompson, A., and Wagai, R.: Beyond clay: towards an improved set of variables for predicting soil organic matter content, Biogeochemistry, 137, 297-306, 10.1007/s10533-018-0424-3, 2018.

Regnier, P., and Steefel, C. I.: A high resolution estimate of the inorganic nitrogen flux from the Scheldt estuary to the coastal North Sea during a nitrogen-limited algal bloom, spring 1995, Geochimica et Cosmochimica Acta, 63, 1359-1374, 10.1016/s0016-7037(99)00034-4, 1999.

Rutherford, D. W., Chiou, C. T., and Kile, D. E.: Influence of soil organic matter composition on the partition of organic compounds, Environmental science & technology, 26, 336-340, 1992.

Saha, D., Rau, B. M., Kaye, J. P., Montes, F., Adler, P. R., and Kemanian, A. R.: Landscape control of nitrous oxide emissions during the transition from conservation reserve program to perennial grasses for bioenergy, GCB Bioenergy, 9, 783-795, 10.1111/gcbb.12395, 2017.

Scudeler, C., Pangle, L., Pasetto, D., Niu, G.-Y., Volkmann, T., Paniconi, C., Putti, M., and Troch, P.: Multiresponse modeling of variably saturated flow and isotope tracer transport for a hillslope experiment at the Landscape Evolution Observatory, Hydrology and Earth System Sciences, 20, 4061-4078, 2016.

Sebestyen, S. D., Ross, D. S., Shanley, J. B., Elliott, E. M., Kendall, C., Campbell, J. L., Dail, D. B., Fernandez, I. J., Goodale, C. L., and Lawrence, G. B.: Unprocessed Atmospheric Nitrate in Waters of the Northern Forest Region in the US and Canada, Environmental science & technology, 53, 3620-3633, 2019.

Seibert, J., Grabs, T., Köhler, S., Laudon, H., Winterdahl, M., and Bishop, K.: Linking soil- and stream-water chemistry based on a Riparian Flow-Concentration Integration Model, Hydrol. Earth Syst. Sci., 13, 2287-2297, 10.5194/hess-13-2287-2009, 2009.

Shi, Y.: Development of a land surface hydrologic modeling and data assimilation system for the study of subsurface-land surface interaction, 2012.

Shi, Y., Davis, K. J., Duffy, C. J., and Yu, X.: Development of a coupled land surface hydrologic model and evaluation at a critical zone observatory, Journal of Hydrometeorology, 14, 1401-1420, 2013.

Shi, Y., Eissenstat, D. M., He, Y., and Davis, K. J.: Using a spatially-distributed hydrologic biogeochemistry model with a nitrogen transport module to study the spatial variation of carbon processes in a Critical Zone Observatory, Ecological Modelling, 380, 8-21, 2018.

Skamarock, W., and Klemp, J.: A Description of the Advanced Research WRF Model Version 4. Ncar Technical Notes, No, NCAR/TN-556+ STR, 2019.

Steefel, C., Appelo, C., Arora, B., Jacques, D., Kalbacher, T., Kolditz, O., Lagneau, V., Lichtner, P., Mayer, K. U., and Meeussen, J.: Reactive transport codes for subsurface environmental simulation, Computational Geosciences, 19, 445-478, 2015.

Steefel, C. I., and Lasaga, A. C.: A coupled model for transport of multiple chemical species and kinetic precipitation/dissolution reactions with application to reactive flow in single phase hydrothermal systems, American Journal of science, 294, 529-592, 1994.

Steimke, A. L., Han, B., Brandt, J. S., and Flores, A. N.: Climate change and curtailment: Evaluating water management practices in the context of changing runoff regimes in a snowmelt-dominated basin, Water, 10, 1490, 2018.

Taylor, R. G., Scanlon, B., Döll, P., Rodell, M., Van Beek, R., Wada, Y., Longuevergne, L., Leblanc, M., Famiglietti, J. S., and Edmunds, M.: Ground water and climate change, Nature climate change, 3, 322, 2013.

Thornton, P. E., Doney, S. C., Lindsay, K., Moore, J. K., Mahowald, N., Randerson, J. T., Fung, I., Lamarque, J. F., Feddema, J. J., and Lee, Y. H.: Carbon-nitrogen interactions regulate climate-carbon cycle feedbacks: results from an atmosphere-ocean general circulation model, Biogeosciences, 6, 2099-2120, 10.5194/bg-6-2099-2009, 2009.

Todd, D. K., and Mays, L. W.: Groundwater Hydrology, Welly Inte, 2005.

Trumbore, S. E.: Comparison of carbon dynamics in tropical and temperate soils using radiocarbon measurements, Global Biogeochemical Cycles, 7, 275-290, 10.1029/93GB00468, 1993.

van der Velde, Y., de Rooij, G. H., Rozemeijer, J. C., van Geer, F. C., and Broers, H. P.: Nitrate response of a lowland catchment: On the relation between stream concentration and travel time distribution dynamics, Water Resources Research, 46, 10.1029/2010wr009105, 2010.

van der Velde, Y., Vercauteren, N., Jaramillo, F., Dekker, S. C., Destouni, G., and Lyon, S. W.: Exploring hydroclimatic change disparity via the Budyko framework, Hydrological Processes, 28, 4110-4118, 10.1002/hyp.9949, 2014.

Weiler, M., and McDonnell, J. R. J.: Testing nutrient flushing hypotheses at the hillslope scale: A virtual experiment approach, J. Hydrol., 319, 339-356, 10.1016/j.jhydrol.2005.06.040, 2006.

Weitzman, J. N., and Kaye, J. P.: Nitrogen Budget and Topographic Controls on Nitrous Oxide in a Shale - Based Watershed, Journal of Geophysical Research: Biogeosciences, 123, 1888-1908, 2018.

Wen, H., Perdrial, J., Bernal, S., Abbott, B. W., Dupas, R., Godsey, S. E., Harpold, A., Rizzo, D., Underwood, K., and Adler, T.: Temperature controls production but hydrology controls export of dissolved organic carbon at the catchment scale, 24, 945-966, 2020.

Wieder, W. R., Grandy, A. S., Kallenbach, C. M., and Bonan, G. B.: Integrating microbial physiology and physio-chemical principles in soils with the MIcrobial-MIneral Carbon Stabilization (MIMICS) model, Biogeosciences, 11, 3899-3917, 10.5194/bg-11-3899-2014, 2014.

Wieder, W. R., Allison, S. D., Davidson, E. A., Georgiou, K., Hararuk, O., He, Y., Hopkins, F., Luo, Y., Smith, M. J., and Sulman, B.: Explicitly representing soil microbial processes in Earth system models, Global Biogeochemical Cycles, 29, 1782-1800, 2015.

Winter, T., Harvey, J., Franke, O., and Alley, W.: Natural processes of ground-water and surface-water interaction, Ground Water and Surface Water: A Single Resource, US Geological Survey Circular, 1139, 2-50, 1998.

Yan, Z. F., Bond-Lamberty, B., Todd-Brown, K. E., Bailey, V. L., Li, S. L., Liu, C. Q., and Liu, C. X.: A moisture function of soil heterotrophic respiration that incorporates microscale processes, Nature Communications, 9, 10.1038/s41467-018-04971-6, 2018.

Zarnetske, J. P., Bouda, M., Abbott, B. W., Saiers, J., and Raymond, P. A.: Generality of hydrologic transport limitation of watershed organic carbon flux across ecoregions of the United States, Geophysical Research Letters, 45, 11,702-711,711, 2018.

Zhi, W., Li, L., Dong, W. M., Brown, W., Kaye, J., Steefel, C., and Williams, K. H.: Distinct Source Water Chemistry Shapes Contrasting Concentration-Discharge Patterns, Water Resources Research, 55, 4233-4251, 10.1029/2018wr024257, 2019.Andrews, D. M., Lin, H., Zhu, Q., Jin, L., and Brantley, S. L.: Hot spots and hot moments of dissolved organic carbon export and soil organic carbon storage in the Shale Hills catchment, Vadose Zone Journal, 10, 943-954, 2011.

Anyah, R. O., Weaver, C. P., Miguez - Macho, G., Fan, Y., and Robock, A.: Incorporating water table dynamics in climate modeling: 3. Simulated groundwater influence on coupled land - atmosphere variability, Journal of Geophysical Research: Atmospheres, 113, 2008.

Bai, J., Zhang, G., Zhao, Q., Lu, Q., Jia, J., Cui, B., and Liu, X.: Depth-distribution patterns and control of soil organic carbon in coastal salt marshes with different plant covers, Sci Rep-Uk, 6, 34835, 10.1038/srep34835, 2016.
Bailey, R., Rathjens, H., Bieger, K., Chaubey, I., and Arnold, J.: SWATMOD-Prep: Graphical User Interface for Preparing Coupled SWAT-MODFLOW Simulations, JAWRA Journal of the American Water Resources Association, 53, 400-410, https://doi.org/10.1111/1752-1688.12502, 2017.
Bao, C., Wu, H., Li, L., Newcomer, D., Long, P. E., and Williams, K. H.: Uranium Bioreduction Rates across Scales: Biogeochemical Hot Moments and Hot Spots during a Biostimulation Experiment at Rifle, Colorado, Environmental Science & Technology, 48, 10116-10127, 10.1021/es501060d, 2014.
Bao, C., Li, L., Shi, Y., and Duffy, C.: Understanding watershed hydrogeochemistry: 1. Development of RT‐Flux‐PIHM, Water Resources Research, 53, 2328-2345, 2017.
Basu, N. B., Destouni, G., Jawitz, J. W., Thompson, S. E., Loukinova, N. V., Darracq, A., Zanardo, S., Yaeger, M., Sivapalan, M., Rinaldo, A., and Rao, P. S. C.: Nutrient loads exported from managed catchments reveal emergent biogeochemical stationarity, Geophys. Res. Lett., 37, 10.1029/2010GL045168, 2010.
Beven, K.: How far can we go in distributed hydrological modelling?, Hydrol. Earth Syst. Sci., 5, 1-12, 10.5194/hess-5-1-2001, 2001.
Beven, K., and Freer, J.: Equifinality, data assimilation, and uncertainty estimation in mechanistic modelling of complex environmental systems using the GLUE methodology, Journal of Hydrology, 249, 11-29, 10.1016/s0022-1694(01)00421-8, 2001.
Beven, K.: A manifesto for the equifinality thesis, Journal of Hydrology, 320, 18-36, 10.1016/j.jhydrol.2005.07.007, 2006.
Beven, K., and Lane, S.: Invalidation of Models and Fitness-for-Purpose: A Rejectionist Approach, in: Computer Simulation Validation: Fundamental Concepts, Methodological Frameworks, and Philosophical Perspectives, edited by: Beisbart, C., and Saam, N. J., Springer International Publishing, Cham, 145-171, 2019.
Beven, K. J.: Uniqueness of place and process representations in hydrological modelling, Hydrol. Earth Syst. Sci., 4, 203-213, 10.5194/hess-4-203-2000, 2000.
Bhatt, G., Kumar, M., and Duffy, C. J.: A tightly coupled GIS and distributed hydrologic modeling framework, Environmental Modelling & Software, 62, 70-84, http://dx.doi.org/10.1016/j.envsoft.2014.08.003, 2014.
Billen, G.: Etude écologique des transformations de l'azote dans les sédiments marins, 1977.
Bracho, R., Natali, S., Pegoraro, E., Crummer, K. G., Schädel, C., Celis, G., Hale, L., Wu, L., Yin, H., and Tiedje, J. M.: Temperature sensitivity of organic matter decomposition of permafrost-region soils during laboratory incubations, Soil Biology and Biochemistry, 97, 1-14, 2016.
Brantley, S. L., Kubicki, J. D., and White, A. F.: Kinetics of water-rock interaction, 2008.
Brantley, S. L., White, T., West, N., Williams, J. Z., Forsythe, B., Shapich, D., Kaye, J., Lin, H., Shi, Y. N., Kaye, M., Herndon, E., Davis, K. J., He, Y., Eissenstat, D., Weitzman, J., DiBiase, R., Li, L., Reed, W., Brubaker, K., and Gu, X.: Susquehanna Shale Hills Critical Zone Observatory: Shale Hills in the Context of Shaver's Creek Watershed, Vadose Zone Journal, 17, 1-19, ARTN 180092
10.2136/vzj2018.04.0092, 2018.
Brooks, P. D., Chorover, J., Fan, Y., Godsey, S. E., Maxwell, R. M., McNamara, J. P., and Tague, C.: Hydrological partitioning in the critical zone: Recent advances and opportunities for developing transferable understanding of water cycle dynamics, Water Resources Research, 51, 6973-6987, https://doi.org/10.1002/2015WR017039, 2015.
Buljovcic, Z., and Engels, C.: Nitrate uptake ability by maize roots during and after drought stress, Plant and Soil, 229, 125-135, 2001.

Buysse, J., Smolders, E., and Merckx, R.: Modelling the uptake of nitrate by a growing plant with an adjustable root nitrate uptake capacity, Plant and Soil, 181, 19-23, 1996.
Cai, X., Yang, Z.-L., Fisher, J., Zhang, X., Barlage, M., and Chen, F.: Integration of nitrogen dynamics into the Noah-MP land surface model v1. 1 for climate and environmental predictions, Geoscientific Model Development (Online), 9, 2016.
Chiou, C. T., Lee, J. F., and Boyd, S. A.: The surface area of soil organic matter, Environmental Science & Technology, 24, 1164-1166, 1990.
Condon, L. E., Maxwell, R. M., and Gangopadhyay, S.: The impact of subsurface conceptualization on land energy fluxes, Advances in Water Resources, 60, 188-203, https://doi.org/10.1016/j.advwatres.2013.08.001, 2013.
Crawford, N. M., and Glass, A. D.: Molecular and physiological aspects of nitrate uptake in plants, Trends in plant science, 3, 389-395, 1998.
Davidson, E. A., and Janssens, I. A.: Temperature sensitivity of soil carbon decomposition and feedbacks to climate change, Nature, 440, 165-173, 10.1038/nature04514, 2006.
Davidson, E. A., Janssens, I. A., and Luo, Y.: On the variability of respiration in terrestrial ecosystems: moving beyond Q10, Global Change Biology, 12, 154-164, 2006.
Davidson, E. A., Janssens, I.A.: Temperature sensitivity of soil carbon decomposition and feedbacks to climate change, Nature, 440, 165-173, 2006.
Devienne-Barret, F., Justes, E., Machet, J., and Mary, B.: Integrated control of nitrate uptake by crop growth rate and soil nitrate availability under field conditions, Annals of Botany, 86, 995-1005, 2000.
Di Capua, F., Pirozzi, F., Lens, P. N. L., and Esposito, G.: Electron donors for autotrophic denitrification, Chemical Engineering Journal, 362, 922-937, https://doi.org/10.1016/j.cej.2019.01.069, 2019.
Dingman, S. L.: Physical hydrology, Waveland press, 2015.
Dunbabin, V. M., Diggle, A. J., Rengel, Z., and Van Hugten, R.: Modelling the interactions between water and nutrient uptake and root growth, Plant and Soil, 239, 19-38, 2002.
Edwards, P. J., Williard, K. W. J., and Schoonover, J. E.: Fundamentals of Watershed Hydrology, Journal of Contemporary Water Research & Education, 154, 3-20, 10.1111/j.1936-704X.2015.03185.x, 2015.
Fatichi, S., Vivoni, E. R., Ogden, F. L., Ivanov, V. Y., Mirus, B., Gochis, D., Downer, C. W., Camporese, M., Davison, J. H., Ebel, B., Jones, N., Kim, J., Mascaro, G., Niswonger, R., Restrepo, P., Rigon, R., Shen, C., Sulis, M., and Tarboton, D.: An overview of current applications, challenges, and future trends in distributed process-based models in hydrology, Journal of Hydrology, 537, 45-60, https://doi.org/10.1016/j.jhydrol.2016.03.026, 2016.
Fatichi, S., Manzoni, S., Or, D., and Paschalis, A.: A Mechanistic Model of Microbially Mediated Soil Biogeochemical Processes: A Reality Check, Global Biogeochemical Cycles, 33, 620-648, 10.1029/2018gb006077, 2019.
Fisher, J., Sitch, S., Malhi, Y., Fisher, R., Huntingford, C., and Tan, S. Y.: Carbon cost of plant nitrogen acquisition: A mechanistic, globally applicable model of plant nitrogen uptake, retranslocation, and fixation, Global Biogeochemical Cycles, 24, 2010.
Friedlingstein, P., Cox, P., Betts, R., Bopp, L., von Bloh, W., Brovkin, V., Cadule, P., Doney, S., Eby, M., and Fung, I.: Climate–carbon cycle feedback analysis: results from the C4MIP model intercomparison, Journal of climate, 19, 3337-3353, 2006.
Gassman, P. W., Reyes, M. R., Green, C. H., and Arnold, J. G.: The soil and water assessment tool: Historical development, applications, and future research directions, T Asabe, 50, 1211-1250, 2007.
Gatel, L., Lauvernet, C., Carluer, N., Weill, S., Tournebize, J., and Paniconi, C.: Global evaluation and sensitivity analysis of a physically based flow and reactive transport model on a laboratory experiment, Environmental Modelling & Software, 113, 73-83, https://doi.org/10.1016/j.envsoft.2018.12.006, 2019.
Gleeson, T., Befus, K. M., Jasechko, S., Luijendijk, E., and Cardenas, M. B.: The global volume and distribution of modern groundwater, Nature Geoscience, 9, 161, 10.1038/ngeo2590

https://www.nature.com/articles/ngeo2590#supplementary-information, 2015.
Godsey, S. E., Kirchner, J. W., and Clow, D. W.: Concentration–discharge relationships reflect chemostatic characteristics of US catchments, Hydrol. Process., 23, 1844-1864, 10.1002/hyp.7315, 2009.
Godsey, S. E., Hartmann, J., and Kirchner, J. W.: Catchment chemostasis revisited: Water quality responds differently to variations in weather and climate, Hydrological Processes, 33, 3056-3069, https://doi.org/10.1002/hyp.13554, 2019.
Grathwohl, P., Rügner, H., Wöhling, T., Osenbrück, K., Schwientek, M., Gayler, S., Wollschläger, U., Selle, B., Pause, M., and Delfs, J.-O.: Catchments as reactors: a comprehensive approach for water fluxes and solute turnover, Environmental earth sciences, 69, 317-333, 2013.
Green, T. R.: Linking climate change and groundwater, in: Integrated groundwater management, Springer, Cham, 97-141, 2016.
Gurdak, J. J.: Groundwater: Climate-induced pumping, Nature Geoscience, 10, 71, 2017.
Hachiya, T., and Sakakibara, H.: Interactions between nitrate and ammonium in their uptake, allocation, assimilation, and signaling in plants, Journal of Experimental Botany, 68, 2501-2512, 10.1093/jxb/erw449, 2016.
Hamamoto, S., Moldrup, P., Kawamoto, K., and Komatsu, T.: Excluded‐volume expansion of Archie's law for gas and solute diffusivities and electrical and thermal conductivities in variably saturated porous media, Water Resources Research, 46, 2010.
Han, B., Benner, S. G., and Flores, A. N.: Including Variability across Climate Change Projections in Assessing Impacts on Water Resources in an Intensively Managed Landscape, Water, 11, 286, 2019.
Hararuk, O., Smith, M. J., and Luo, Y.: Microbial models with data-driven parameters predict stronger soil carbon responses to climate change, Glob. Chang. Biol., 21, 2439-2453, 10.1111/gcb.12827, 2015.
HARTLEY, I. P., HEINEMEYER, A., and INESON, P.: Effects of three years of soil warming and shading on the rate of soil respiration: substrate availability and not thermal acclimation mediates observed response, Global Change Biology, 13, 1761-1770, https://doi.org/10.1111/j.1365-2486.2007.01373.x, 2007.
Hartmann, J., Lauerwald, R., and Moosdorf, N.: A brief overview of the GLObal RIver CHemistry Database, GLORICH, Procedia Earth and Planetary Science, 10, 23-27, 2014.
Hasenmueller, E. A., Jin, L., Stinchcomb, G. E., Lin, H., Brantley, S. L., and Kaye, J. P.: Topographic controls on the depth distribution of soil CO2 in a small temperate watershed, Applied Geochemistry, 63, 58-69, 2015.
Hasenmueller, E. A., Gu, X., Weitzman, J. N., Adams, T. S., Stinchcomb, G. E., Eissenstat, D. M., Drohan, P. J., Brantley, S. L., and Kaye, J. P.: Weathering of rock to regolith: The activity of deep roots in bedrock fractures, Geoderma, 300, 11-31, 2017.
Heidari, P., Li, L., Jin, L., Williams, J. Z., and Brantley, S. L.: A reactive transport model for Marcellus shale weathering, Geochimica et Cosmochimica Acta, 217, 421-440, 2017.
Herndon, E. M., Dere, A. L., Sullivan, P. L., Norris, D., Reynolds, B., and Brantley, S. L.: Landscape heterogeneity drives contrasting concentration–discharge relationships in shale headwater catchments, Hydrology and earth system sciences, 19, 3333-3347, 2015.
Hindmarsh, A. C., Brown, P. N., Grant, K. E., Lee, S. L., Serban, R., Shumaker, D. E., and Woodward, C. S.: SUNDIALS: Suite of nonlinear and differential/algebraic equation solvers, ACM Transactions on Mathematical Software (TOMS), 31, 363-396, 2005.
Hodges, C., Kim, H., Brantley, S. L., and Kaye, J.: Soil CO 2 and O 2 Concentrations Illuminate the Relative Importance of Weathering and Respiration to Seasonal Soil Gas Fluctuations, Soil Science Society of America Journal, 83, 1167-1180, 2019.
Hubbard, S. S., Williams, K. H., Agarwal, D., Banfield, J., Beller, H., Bouskill, N., Brodie, E., Carroll, R., Dafflon, B., and Dwivedi, D.: The East River, Colorado, Watershed: A mountainous community testbed for improving predictive understanding of multiscale hydrological–biogeochemical dynamics, Vadose Zone Journal, 17, 2018.

Husic, A.: Numerical modeling and isotope tracers to investigate karst biogeochemistry and transport processes, 2018.
Jin, L., and Brantley, S. L.: Soil chemistry and shale weathering on a hillslope influenced by convergent hydrologic flow regime at the Susquehanna/Shale Hills Critical Zone Observatory, Applied Geochemistry, 26, Supplement, S51-S56, http://dx.doi.org/10.1016/j.apgeochem.2011.03.027, 2011.
Jin, L. X., Ravella, R., Ketchum, B., Bierman, P. R., Heaney, P., White, T., and Brantley, S. L.: Mineral weathering and elemental transport during hillslope evolution at the Susquehanna/Shale Hills Critical Zone Observatory, Geochim Cosmochim Ac, 74, 3669-3691, 10.1016/j.gca.2010.03.036, 2010.
Keune, J., Gasper, F., Goergen, K., Hense, A., Shrestha, P., Sulis, M., and Kollet, S.: Studying the influence of groundwater representations on land surface-atmosphere feedbacks during the European heat wave in 2003, Journal of Geophysical Research: Atmospheres, 121, 13,301-313,325, https://doi.org/10.1002/2016JD025426, 2016.
Kirchner, J. W., Hooper, R. P., Kendall, C., Neal, C., and Leavesley, G.: Testing and validating environmental models, Science of the Total Environment, 183, 33-47, 10.1016/0048-9697(95)04971-1, 1996.
Kirchner, J. W.: A double paradox in catchment hydrology and geochemistry, Hydrol. Process., 17, 871-874, 10.1002/hyp.5108, 2003.
Kuntz, B. W., Rubin, S., Berkowitz, B., and Singha, K.: Quantifying Solute Transport at the Shale Hills Critical Zone Observatory, Vadose Zone Journal, 10, 843-857, 10.2136/vzj2010.0130, 2011.
Lam, Q. D., Schmalz, B., and Fohrer, N.: Modelling point and diffuse source pollution of nitrate in a rural lowland catchment using the SWAT model, Agricultural Water Management, 97, 317-325, https://doi.org/10.1016/j.agwat.2009.10.004, 2010.
Leonard, L., and Duffy, C. J.: Essential terrestrial variable data workflows for distributed water resources modeling, Environmental modelling & software, 50, 85-96, 2013.
Li, L., Salehikhoo, F., Brantley, S. L., and Heidari, P.: Spatial zonation limits magnesite dissolution in porous media, Geochimica et Cosmochimica Acta, 126, 555-573, 10.1016/j.gca.2013.10.051, 2014.
Li, L., Bao, C., Sullivan, P. L., Brantley, S., Shi, Y., and Duffy, C.: Understanding watershed hydrogeochemistry: 2. Synchronized hydrological and geochemical processes drive stream chemostatic behavior, Water Resources Research, 53, 2346-2367, 2017a.
Li, L., Maher, K., Navarre-Sitchler, A., Druhan, J., Meile, C., Lawrence, C., Moore, J., Perdrial, J., Sullivan, P., Thompson, A., Jin, L., Bolton, E. W., Brantley, S. L., Dietrich, W. E., Mayer, K. U., Steefel, C. I., Valocchi, A., Zachara, J., Kocar, B., McIntosh, J., Tutolo, B. M., Kumar, M., Sonnenthal, E., Bao, C., and Beisman, J.: Expanding the role of reactive transport models in critical zone processes, Earth-Science Reviews, 165, 280-301, http://dx.doi.org/10.1016/j.earscirev.2016.09.001, 2017b.
Li, L.: Watershed reactive transport, Reviews in Mineralogy and Geochemistry, 85, 381-418, 2019.
Li, L., Sullivan, P. L., Benettin, P., Cirpka, O. A., Bishop, K., Brantley, S. L., Knapp, J. L. A., Meerveld, I., Rinaldo, A., Seibert, J., Wen, H., and Kirchner, J. W.: Toward catchment hydro‐biogeochemical theories, WIREs Water, 10.1002/wat2.1495, 2020.
Lin, H.: Temporal stability of soil moisture spatial pattern and subsurface preferential flow pathways in the shale hills catchment, Vadose Zone J, 5, 317-340, 10.2136/vzj2005.0058, 2006.
Lindström, G., Rosberg, J., and Arheimer, B.: Parameter Precision in the HBV-NP Model and Impacts on Nitrogen Scenario Simulations in the Rönneå River, Southern Sweden, AMBIO: A Journal of the Human Environment, 34, 533-537, 535, 2005.
Lindström, G., Pers, C., Rosberg, J., Strömqvist, J., and Arheimer, B.: Development and testing of the HYPE (Hydrological Predictions for the Environment) water quality model for different spatial scales, Hydrology Research, 41, 295-319, 10.2166/nh.2010.007, 2010.
Liu, Y., Wang, C., He, N., Wen, X., Gao, Y., Li, S., Niu, S., Butterbach‐Bahl, K., Luo, Y., and Yu, G.: A global synthesis of the rate and temperature sensitivity of soil nitrogen mineralization: latitudinal patterns and mechanisms, Global change biology, 23, 455-464, 2017.

López, B., Sabaté, S., and Gracia, C.: Vertical distribution of fine root density, length density, area index and mean diameter in a Quercus ilex forest, Tree Physiology, 21, 555-560, 2001.
Maavara, T., Lauerwald, R., Laruelle, G. G., Akbarzadeh, Z., Bouskill, N. J., Van Cappellen, P., and Regnier, P.: Nitrous oxide emissions from inland waters: Are IPCC estimates too high?, Global Change Biology, 0, doi:10.1111/gcb.14504, 2018.
Martínez-de la Torre, A., and Miguez-Macho, G.: Groundwater influence on soil moisture memory and land–atmosphere fluxes in the Iberian Peninsula, Hydrology and Earth System Sciences, 23, 4909-4932, 2019.
Maxwell, R. M., Lundquist, J. K., Mirocha, J. D., Smith, S. G., Woodward, C. S., and Tompson, A. F.: Development of a coupled groundwater–atmosphere model, Monthly Weather Review, 139, 96-116, 2011.
Mayer, K. U., Frind, E. O., and Blowes, D. W.: Multicomponent reactive transport modeling in variably saturated porous media using a generalized formulation for kinetically controlled reactions, Water Resources Research, 38, 13-11-13-21, 10.1029/2001wr000862, 2002.
McMurtrie, R. E., Iversen, C. M., Dewar, R. C., Medlyn, B. E., Näsholm, T., Pepper, D. A., and Norby, R. J.: Plant root distributions and nitrogen uptake predicted by a hypothesis of optimal root foraging, Ecology and Evolution, 2, 1235-1250, 2012.
Miller, M. P., Tesoriero, A. J., Hood, K., Terziotti, S., and Wolock, D. M.: Estimating Discharge and Nonpoint Source Nitrate Loading to Streams From Three End-Member Pathways Using High-Frequency Water Quality Data, Water Resources Research, 53, 10201-10216, 10.1002/2017wr021654, 2017.
Miller, M. P., Capel, P. D., García, A. M., and Ator, S. W.: Response of Nitrogen Loading to the Chesapeake Bay to Source Reduction and Land Use Change Scenarios: A SPARROW ‐ Informed Analysis, JAWRA Journal of the American Water Resources Association, 56, 100-112, 2020.
Moatar, F., Abbott, B. W., Minaudo, C., Curie, F., and Pinay, G.: Elemental properties, hydrology, and biology interact to shape concentration ‐ discharge curves for carbon, nutrients, sediment, and major ions, Water Resources Research, 53, 1270-1287, 2017.
Moriasi, D. N., Gowda, P. H., Arnold, J. G., Mulla, D. J., Ale, S., and Steiner, J. L.: Modeling the impact of nitrogen fertilizer application and tile drain configuration on nitrate leaching using SWAT, Agricultural Water Management, 130, 36-43, https://doi.org/10.1016/j.agwat.2013.08.003, 2013.
Musolff, A., Schmidt, C., Selle, B., and Fleckenstein, J. H.: Catchment controls on solute export, Adv. Water Resour., 86, 133-146, 10.1016/j.advwatres.2015.09.026, 2015.
Neitsch, S. L., Arnold, J. G., Kiniry, J. R., and Williams, J. R.: Soil and water assessment tool theoretical documentation version 2009, Texas Water Resources Institute, 2011.
Ottoy, S., Elsen, A., Van De Vreken, P., Gobin, A., Merckx, R., Hermy, M., and Van Orshoven, J.: An exponential change decline function to estimate soil organic carbon stocks and their changes from topsoil measurements, European Journal of Soil Science, 67, 816-826, 2016.
Porporato, A., D'odorico, P., Laio, F., and Rodriguez-Iturbe, I.: Hydrologic controls on soil carbon and nitrogen cycles. I. Modeling scheme, Advances in water resources, 26, 45-58, 2003.
Qu, Y., and Duffy, C. J.: A semidiscrete finite volume formulation for multiprocess watershed simulation, Water Resources Research, 43, W08419, 2007.
Ranalli, A. J., and Macalady, D. L.: The importance of the riparian zone and in-stream processes in nitrate attenuation in undisturbed and agricultural watersheds – A review of the scientific literature, Journal of Hydrology, 389, 406-415, https://doi.org/10.1016/j.jhydrol.2010.05.045, 2010.
Regnier, P., and Steefel, C. I.: A high resolution estimate of the inorganic nitrogen flux from the Scheldt estuary to the coastal North Sea during a nitrogen-limited algal bloom, spring 1995, Geochimica et Cosmochimica Acta, 63, 1359-1374, 10.1016/s0016-7037(99)00034-4, 1999.
Rutherford, D. W., Chiou, C. T., and Kile, D. E.: Influence of soil organic matter composition on the partition of organic compounds, Environmental science & technology, 26, 336-340, 1992.

Saad, Y., and Schultz, M. H.: GMRES: A generalized minimal residual algorithm for solving nonsymmetric linear systems, SIAM Journal on scientific and statistical computing, 7, 856-869, 1986.
Saberi, L., Ng, G.-H. C., Nelson, L., Zhi, W., li, L., La Frenierre, J., and Johnstone, M.: Spatiotemporal Drivers of Hydrochemical Variability in a Tropical Glacierized Watershed in the Andes, under review.
Saha, D., Rau, B. M., Kaye, J. P., Montes, F., Adler, P. R., and Kemanian, A. R.: Landscape control of nitrous oxide emissions during the transition from conservation reserve program to perennial grasses for bioenergy, GCB Bioenergy, 9, 783-795, doi:10.1111/gcbb.12395, 2017.
Scudeler, C., Pangle, L., Pasetto, D., Niu, G.-Y., Volkmann, T., Paniconi, C., Putti, M., and Troch, P.: Multiresponse modeling of variably saturated flow and isotope tracer transport for a hillslope experiment at the Landscape Evolution Observatory, Hydrology and Earth System Sciences, 20, 4061-4078, 2016.
Sebestyen, S. D., Ross, D. S., Shanley, J. B., Elliott, E. M., Kendall, C., Campbell, J. L., Dail, D. B., Fernandez, I. J., Goodale, C. L., and Lawrence, G. B.: Unprocessed Atmospheric Nitrate in Waters of the Northern Forest Region in the US and Canada, Environmental science & technology, 53, 3620-3633, 2019.
Seibert, J., Grabs, T., Köhler, S., Laudon, H., Winterdahl, M., and Bishop, K.: Linking soil- and stream-water chemistry based on a Riparian Flow-Concentration Integration Model, Hydrol. Earth Syst. Sci., 13, 2287-2297, 10.5194/hess-13-2287-2009, 2009.
Seyfried, M., Lohse, K., Marks, D., Flerchinger, G., Pierson, F., and Holbrook, W. S.: Reynolds Creek Experimental Watershed and Critical Zone Observatory, Vadose Zone Journal, 17, 180129, 10.2136/vzj2018.07.0129, 2018.
Shi, Y.: Development of a land surface hydrologic modeling and data assimilation system for the study of subsurface-land surface interaction, 2012.
Shi, Y., Davis, K. J., Duffy, C. J., and Yu, X.: Development of a coupled land surface hydrologic model and evaluation at a critical zone observatory, Journal of Hydrometeorology, 14, 1401-1420, 2013.
Shi, Y., Eissenstat, D. M., He, Y., and Davis, K. J.: Using a spatially-distributed hydrologic biogeochemistry model with a nitrogen transport module to study the spatial variation of carbon processes in a Critical Zone Observatory, Ecological Modelling, 380, 8-21, 2018.
Skamarock, W., and Klemp, J.: A Description of the Advanced Research WRF Model Version 4. Ncar Technical Notes, No, NCAR/TN-556+ STR, 2019.
Song, X., Zhang, J., Zhan, C., Xuan, Y., Ye, M., and Xu, C.: Global sensitivity analysis in hydrological modeling: Review of concepts, methods, theoretical framework, and applications, Journal of hydrology, 523, 739-757, 2015.
Steefel, C., Appelo, C., Arora, B., Jacques, D., Kalbacher, T., Kolditz, O., Lagneau, V., Lichtner, P., Mayer, K. U., and Meeussen, J.: Reactive transport codes for subsurface environmental simulation, Computational Geosciences, 19, 445-478, 2015.
Steefel, C. I., and Lasaga, A. C.: A coupled model for transport of multiple chemical species and kinetic precipitation/dissolution reactions with application to reactive flow in single phase hydrothermal systems, American Journal of science, 294, 529-592, 1994.
Steimke, A. L., Han, B., Brandt, J. S., and Flores, A. N.: Climate change and curtailment: Evaluating water management practices in the context of changing runoff regimes in a snowmelt-dominated basin, Water, 10, 1490, 2018.
Sullivan, P. L., Hynek, S. A., Gu, X., Singha, K., White, T., West, N., Kim, H., Clarke, B., Kirby, E., Duffy, C., and Brantley, S. L.: Oxidative dissolution under the channel leads geomorphological evolution at the Shale Hills catchment, American Journal of Science, 316, 981-1026, 10.2475/10.2016.02, 2016.
Suseela, V., Conant, R. T., Wallenstein, M. D., and Dukes, J. S.: Effects of soil moisture on the temperature sensitivity of heterotrophic respiration vary seasonally in an old‐field climate change experiment, Global Change Biology, 18, 336-348, 2012.

Taylor, R. G., Scanlon, B., Döll, P., Rodell, M., Van Beek, R., Wada, Y., Longuevergne, L., Leblanc, M., Famiglietti, J. S., and Edmunds, M.: Ground water and climate change, Nature climate change, 3, 322, 2013.
Todd, D. K., and Mays, L. W.: Groundwater Hydrology, Welly Inte, 2005.
van der Velde, Y., de Rooij, G. H., Rozemeijer, J. C., van Geer, F. C., and Broers, H. P.: Nitrate response of a lowland catchment: On the relation between stream concentration and travel time distribution dynamics, Water Resources Research, 46, 10.1029/2010wr009105, 2010.
van der Velde, Y., Vercauteren, N., Jaramillo, F., Dekker, S. C., Destouni, G., and Lyon, S. W.: Exploring hydroclimatic change disparity via the Budyko framework, Hydrological Processes, 28, 4110-4118, 10.1002/hyp.9949, 2014.
Weiler, M., and McDonnell, J. R. J.: Testing nutrient flushing hypotheses at the hillslope scale: A virtual experiment approach, J. Hydrol., 319, 339-356, 10.1016/j.jhydrol.2005.06.040, 2006.
Weitzman, J. N., and Kaye, J. P.: Nitrogen Budget and Topographic Controls on Nitrous Oxide in a Shale‐Based Watershed, Journal of Geophysical Research: Biogeosciences, 123, 1888-1908, 2018.
Wen, H., Perdrial, J., Bernal, S., Abbott, B. W., Dupas, R., Godsey, S. E., Harpold, A., Rizzo, D., Underwood, K., and Adler, T.: Temperature controls production but hydrology controls export of dissolved organic carbon at the catchment scale, 24, 945-966, 2020.
Wieder, W. R., Allison, S. D., Davidson, E. A., Georgiou, K., Hararuk, O., He, Y., Hopkins, F., Luo, Y., Smith, M. J., and Sulman, B.: Explicitly representing soil microbial processes in Earth system models, Global Biogeochemical Cycles, 29, 1782-1800, 2015.
Winter, T., Harvey, J., Franke, O., and Alley, W.: Natural processes of ground-water and surface-water interaction, Ground Water and Surface Water: A Single Resource, US Geological Survey Circular, 1139, 2-50, 1998.
Wolery, T. J.: EQ3/6, a software package for geochemical modeling of aqueous systems: package overview and installation guide (version 7.0), 1992.
Xiao, D., Shi, Y., Brantley, S. L., Forsythe, B., DiBiase, R., Davis, K., and Li, L.: Streamflow Generation From Catchments of Contrasting Lithologies: The Role of Soil Properties, Topography, and Catchment Size, Water Resources Research, n/a, 10.1029/2018wr023736, 2019.
Yan, Q., Duan, Z., Mao, J., Li, X., and Dong, F.: Effects of root-zone temperature and N, P, and K supplies on nutrient uptake of cucumber (Cucumis sativus L.) seedlings in hydroponics, Soil Science and Plant Nutrition, 58, 707-717, 2012.
Yan, Z., Bond-Lamberty, B., Todd-Brown, K. E., Bailey, V. L., Li, S., Liu, C., and Liu, C.: A moisture function of soil heterotrophic respiration that incorporates microscale processes, Nat Commun, 9, 2562, 10.1038/s41467-018-04971-6, 2018.
Zarnetske, J. P., Bouda, M., Abbott, B. W., Saiers, J., and Raymond, P. A.: Generality of hydrologic transport limitation of watershed organic carbon flux across ecoregions of the United States, Geophysical Research Letters, 45, 11,702-711,711, 2018.
Zhi, W., Li, L., Dong, W., Brown, W., Kaye, J., Steefel, C., and Williams, K. H.: Distinct Source Water Chemistry Shapes Contrasting Concentration-Discharge Patterns, Water Resources Research, 55, 4233-4251, 10.1029/2018wr024257, 2019.
Zhi, W., and Li, L.: The Shallow and Deep Hypothesis: Subsurface Vertical Chemical Contrasts Shape Nitrate Export Patterns from Different Land Uses, Environmental Science & Technology, 54, 11915-11928, 10.1021/acs.est.0c01340, 2020.
Zhi, W., Williams, K. H., Carroll, R. W. H., Brown, W., Dong, W., Kerins, D., and Li, L.: Significant stream chemistry response to temperature variations in a high-elevation mountain watershed, Communications Earth & Environment, 1, 10.1038/s43247-020-00039-w, 2020.

Zhou, T., Shi, P., Hui, D., and Luo, Y.: Global pattern of temperature sensitivity of soil heterotrophic respiration (Q10) and its implications for carbon - climate feedback, Journal of Geophysical Research: Biogeosciences, 114, 2009.