Second review of 'Configuration and Evaluation of a Global Unstructured Mesh Model based on the Variable-Resolution Approach'

I appreciate the updates to the manuscript the authors have made. It is greatly improved over the initial submission, both in terms of the scientific results as well as stylistic presentation. In particular, I think the model solutions look improved in the case of added explicit diffusion (in this case, hyperdiffusion), which also makes the simulations more comparable to other, more mature, variable-resolution (VR) approaches in literature. The more complete analysis of the tropical cyclone (TC) in mesh transition regions is also nice and verifies that the numerics perform adequately in the presence of a 'strong' forcing for weather and climate applications.

I have a few notes listed below that either should be addressed (or at least considered) by the authors, editor, and GMD proof staff before final publication. However, I consider these minor and they do not require additional model simulations or deep analysis (generally clarification, figure modification, etc.), so I recommend publication in GMD following minor revisions.

One note, the authors make reference to 'the initial preprint' quite a few times in addressing changes from the original GMDD submission. While I (and other reviewers) clearly understand what is meant here, it may be worth ensuring that GMD is OK with this presentation, as it will be referencing parts of the original submission not directly included in the final published manuscript that most will directly download/access.

Reply: We thank this reviewer for helpful comments. Considering that the preprint (and its supplement) can be directly downloaded from GMD's website, we keep this usage for the convenience of illustration. In the "code and data" section, we have explicitly stated that "the preprint is available from the online link of this paper". We have slightly revised the latest version. Detailed responses to the Reviewer are given as follows.

Comments on scientific results

• Lines 83-84. '... can capture smoother cloud patterns and smoother mid-level jet structures...' this is a bit ambiguous since 'smoother' could also mean 'lower resolution.' I believe what the authors are trying to say here is that a continuous discretization in a unified VR model does not include explicit (artificial) lateral boundary condition discontinuities one would find in a traditional nested model living inside a global solution (e.g., WRF).

Reply: Thanks for pointing out this. This sentence is modified as "The VR model can capture smoother cloud patterns and smoother mid-level jet structures across the grid refined region...".

• Lines 156-157. These two sentences are a bit vague. I assume by 'generic and flexible' the authors imply that there is an interface/coupling layer that allows one to add parameterizations that are developed in isolation to the model (provided they return tendencies that match what is required by the dynamical core). If these two sentences are to be left in, I would add a bit more clarification.

Reply: We have modified this paragraph:

"GRIST provides a general physics-dynamics coupling interface to incorporate various physics packages. A tailored package can be used as a plugin, and its development can benefit from the broad community resources. One may add a specific physics scheme to an existing physics package, or create an entirely new physics package as long as it is compatible with the current workflow and is scientifically reliable. The surface model (e.g., land or a mixed-layer ocean model), though not used in this study, is coupled in a point-to-point style, and can be shared by different physics configurations. Three physics packages are currently available as basis for continuous research and development. These packages are separate in the sense that they have different physics drivers and data structures. For completeness, we describe them in this section."

• Sections 2.3.1 and 2.3.2. It is worth noting that since different forms of explicit diffusion are applied to both the uniform (UQ) and VR meshes for both Smagorinsky and hyperdiffusion likely lead to some of the differences seen in the comparisons of Figs. 5 and 7 [Jablonowski and Williamson, 2011]. Generally, for VR models diffusion is applied in a way such that the explicit diffusion in the cells in the coarse/fine regions match their UQ counterparts. Far from the transition, the design goal is for the local numerics of a QU/VR pair to be indistinguishable from one another (e.g., Zarzycki et al. [2014], Park et al. [2014]).

While it is not critical to the results here, it needs to be mentioned here that the different choices of diffusion between QU and VR means that a true apples-to-apples comparison is impossible. For example, I suspect one reason for the slightly counterintuitive results in Figs. 5 and 7 (i.e., lines 364-394) is due to addition diffusion in the VR runs, which will slightly increase error relative to an less diffused (and well-posed) UQ simulation of equivalent coarse resolution.

Reply: We agree that this is not "a true apples-to-apples comparison", but this is the best that we can do now. The comparison of error norms ensures that the VR configuration produces overall reasonable error behaviors: increasing the coarse-mesh resolution decreases the global error. Thus, the model can be used for more realistic weather and climate applications. The counterintuitive result (G8X4) is only found for the first few days. We will further think about this question and try to find more confirmative reasons. We have slightly modified the end of the 1st paragraph of Section 2.3.2 as:

"Thus, QU and VR models are applied by different forms of explicit diffusion in this manuscript. Future work may also need to examine the possible impact of hyperdiffusion in a QU model to better isolate its effect."

• Lines 380-388. A counterargument to applying a perturbation in both hemispheres is that the lack of specified baroclinic development in the southern hemisphere allows for large wave number errors associated with grid imprinting to be more overtly realized in the test than it would be in a more complex simulation (e.g., wavenumber 4 imprinting associated with cubed-sphere corners or wavenumber 5 imprinting associated with pentagons in a hexagonal mesh, as in Fig. S3a).

Reply: Indeed, the double-perturbation test makes the imprinting issue less conspicuous. For this part, what we are addressing is not "the imprinting issue does not exist", but that "its impact can be controlled". We believe that it is better to understand and control such impacts in a more realistic environment. In reality, the southern hemisphere is not silent. The consequence of this issue may not be as serious as in a steady state situation. The reduction in the relative error of G8X4 in relative to G7 (Fig. 7 v.s. Fig. 5b) supports this argument. This gives us confidence on the precision of the solver when used in a real-world application.

• Lines 508-515. It is worth noting that the environment in the Reed and Jablonowski TC is conditionally unstable, and therefore some of this noise is almost inevitably going to arise as horizontal gravity waves, etc. induce resolved-scale overturning in the formerly quiescent atmosphere. So while turning up hyperdiffusion can suppress these 'far-field' gridpoint storms, it is unclear whether that is a truly desirable outcome. One could imagine a case where a developer tunes a diffusive operator to eliminate these instabilities, but this results in an overdiffusive configuration for real-world convection in the deep tropics.

Reply: Thanks for pointing out this issue. Indeed, small disturbances are ubiquitous, and they may or may not excite new systems. For this particular case, it depends on the nonlinear feedback between dynamics and physics (for example, certain combination of physics schemes or the physics coupling itself may also remove such systems). We agree that it is not that straightforward to say what is right or wrong. We use the term "highly unrealistic", because we believe that the remote systems should not appear. But any way, the major purpose here is to show the role of explicit diffusion in a VR configuration under full physics-dynamics interaction.

We have slightly modified the first part of Section 5.1 as:

The initial virtual temperature profiles are designed to be conditionally unstable in the troposphere. A small perturbation (either physical or computational) is more likely to excite new storms. Whether these additional signals are realistic depends on the situations.

Considerations regarding figures and tables

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• I would actually move Tables S1 and S2 into the body of the main manuscript and reference accordingly. I referred to these particularly frequently when cross-validating the VR acronyms, and anything that requires more than a single reference probably should be in the primary manuscript. Perhaps Table 1 can be moved to supplemental since it is implicitly referenced in the last two columns of Tables S1/S2.

92 Reply: Tables S1, S2 now become Tables 1 and 2. Table 1 is Table S1 now.

• There are continental outlines in most of the figures, although all simulations are done in the absence of land models (and without any zonal asymmetries). I would add a small disclaimer when describing Fig. 1 or Fig. 3 that all outlines are only showed for spatial reference and do not represent land masses/surface forcing in the simulations.

Reply: We have added the disclaimer below Fig. 1 as: "Throughout this paper, all land-sea outlines are only given for a spatial reference, and do not represent the geographical difference.'

• I would zoom in on the TC in Fig. 13 as the results described in the text are nearly impossible to see.

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Reply: This has been done for Fig. 13.
• Fig. 8 has a small kink in the 28 km contour (towards the southeast quadrant). I actually assume this is due to the small natural imperfections in a spherical tessellation (e.g., pentagons) but it may be worth noting in the manuscript that that contour isn't in error.

103 Reply: This information has been explicitly given in the caption of Fig. 8.

"Note that the small kink in the 28 km contour of (a) (c) simply reflects that the generated mesh occasionally has higher 104 105 local irregularities at some areas.

Typographical errors and grammar

This list is not meant to be exhaustive, but rather, a few obvious catches I noted while reading. 107

- 108 · Line 85, 'Based on a VR configuration... 109
 - Line 110. '... coupling) are in Z20 and Z19.'
- 110 · Line 118. '... that is, using a staggered finite-volume... 111
 - · Line 160. '... study, the suite of Reed and Jablonowski...'
- · Line 174. Splitting is a relatively niche subject, would reference something like Gross et al. [2018] for readers that 112 113 would like additional detail.
- Line 306. '... examine the ability to resolve fine-scale ...' 114
- Lines 336-337. 'For G5B3X4,... 115
 - Line 376. '... or Gaussian grid were predominant.' Line 469. '... looks smooth and...'
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- · Line 530. '... with more realistic weather...' 118

Reply: Thanks for these suggestions. We have corrected them in the main text. We also introduce Gross et al. (2018) to give a reference for splitting. 120

M. Gross, H. Wan, P. J. Rasch, P. M. Caldwell, D. L. Williamson, D. Klocke, C. Jablonowski, D. R. Thatcher, N. Wood, M. Cullen, B. Beare, M. Willett, M. Gross, H. Walt, F.J. Rasen, F. M. Catuwen, D. L. Williamson, D. Ribert, C. Salorinova, A. Zarzycki, K. Sakaguchi, and R. Leung. Physics—Dynamics Coupling in Weather, Climate, and Earth System Models: Challenges and Recent Progress. Mon. Weather Rev., 146(11):3505–3544, Nov 2018. ISSN 0027-0644. doi: 10.1175/MWR-D-17-0345.1.

0644. doi: 10.1175/MWR-D-17-0345.1.

C. Jablonowski and D. L. Williamson. The pros and cons of diffusion, filters and fixers in atmospheric general circulation models. In Numerical techniques for global atmospheric models, pages 381–493. Springer, 2011.

S.-H. Park, J. B. Klemp, and W. C. Skamarock. A comparison of mesh refinement in the global MPAS-A and WRF models using an idealized normal-mode baroclinic wave simulation. Monthly Weather Review, 142(10):3614–3634, 2014.

C. M. Zarzycki, M. N. Levy, C. Jablonowski, J. R. Overfelt, M. A. Taylor, and P. A. Ullrich. Aquaplanet experiments using CAM's variable-resolution nical core. Journal of Climate, 27(14):5481–5503, 2014. doi: 10.1175/JCLI-D-14-00004.1.

Configuration and Evaluation of a Global Unstructured Mesh Atmospheric

Model (GRIST-A20.9) based on the Variable-Resolution Approach

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- 139 Meteorological Administration, Beijing, China

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166 167 region can be well controlled.

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- 141 Correspondence to: Yi Zhang (yizhang@cma.cn or yizhang@cma.gov.cn)

142 Abstract. Targeting a long-term effort towards a variable-resolution (VR) global weather and climate model, this study 143 systematically configures and evaluates an unstructured-mesh atmospheric model based on the multiresolution 144 approach. The model performance is examined from dry dynamics to simple and full physics scenarios. In the dry 145 baroclinic wave test, the VR model reproduces comparable fine-scale structures in the refined regions as a fine-146 resolution quasi-uniform (QU) mesh model. The mesh transition zone does not adversely affect the wave pattern. 147 Regional kinetic energy spectra show that the fine-scale resolving ability improves as the fine resolution increases. 148 Compared to a QU counterpart that has equivalent degrees of freedom, while the VR model tends to increase the global errors, the errors can be reduced when the resolution of the coarse region is increased. The performance over the coarse 149 150 region is generally close to that of a low-resolution QU counterpart. Two multi-region refinement approaches, the 151 hierarchical and polycentric refinement modes, further validate the model performance under the multiresolution refinement. Activating hyperdiffusion for horizontal velocity is helpful with respect to VR modeling. An idealized 152 153 tropical cyclone test is further used to examine its ability to resolve fine-scale structures. In the simple physics 154 environment, the VR model can have the tropical cyclone stably pass the transition zone in various configurations. A 155 series of sensitivity tests examines the model performance in a hierarchical refinement mode. The simulations exhibit 156 $consistency\ even\ when\ the\ VR\ mesh\ is\ slightly\ perturbed\ by\ one\ of\ the\ three\ parameters\ that\ control\ the\ density\ function.$ 157 The tropical cyclone, starting from the 2nd-refinement region and passing through the inner transition zone, gets 158 intensified and covers a smaller area in the refined regions. Such variations are consistent with the behavior that one 159 may observe when uniformly refining the QU mesh. In the full physics environment with a highly variable mesh that 160 reaches sub-10-kilometer resolution, the VR model also produces a reasonable evolution for the tropical cyclone. The explicit diffusion shows its usefulness in terms of suppressing some unrealistic isolated-scale structures that are far 161 162 away from the initial vortex, and does not adversely affect the physically important object. The fine-scale structure is 163 determined mainly by the fine-resolution area, although the systems may have larger differences before they move into

the fine-resolution area. Altogether, this work demonstrates that the multiresolution configuration is a reliable and

economic alternative to high-resolution global modeling. The adverse impact due to mesh transition and the coarse

1. Introduction

Increasing resolution is generally regarded as an effective way to improve global weather and climate modeling (Jung et al. 2012; Wehner et al. 2014; Zhang et al. 2014; Yu et al. 2019). It is apparent that more computational and storage resources are required for higher resolution models. This leads to a major challenge for efficient model development and application. The emergence of the locally refined, variable-resolution (VR) modeling approach offers a complementary route. The term VR is a broad concept. It may be realized with different styles, such as nested regional modeling with multiple grids, abrupt nonconforming mesh division, stretched grids, and the multiresolution approach. The stretched grid (e.g., Hourdin et al. 2006; Harris et al. 2016) and the multiresolution approaches (e.g., Ringler et al. 2011; Guba et al. 2014) are close in terms of their conforming style. They maintain the global modeling configuration while permitting increased resolution for certain regions. The multiresolution approach is usually realized by an unstructured mesh model, such that a more flexible resolution choice can be achieved by considering multiple regions. Such a global-to-regional approach is the VR style that will be investigated in this study.

Numerical weather and climate modeling has shown that the VR approach can preserve the benefits of highresolution applications for certain regions at a lower computational cost, as the total number of grid points can be greatly
reduced (e.g., Sakaguchi et al. 2015; Skamarock et al. 2018; Gettelman et al. 2018). This advantage is especially
valuable for high-resolution modeling that may reach the convection-permitting regime. While the global cloud/stormresolving (a.k.a., convection-permitting/allowing) modeling approach has been widely adopted (e.g., Stevens et al.
2019), it is still expensive and inefficient to frequently run such models for routine model development, research and
application. The VR model provides an efficient testbed for evaluating global model configurations and testing scaleaware physics. It offers flexible resolution configurations that may depend on physical interests. When properly
formulated, it can be an intermediate and transitional step before establishing global convection-permitting modeling.

While the VR approach has shown some benefits, it may potentially suffer from some problems¹. The nonuniform mesh, though it can be gradually refined, hardly decreases the global errors (as compared to its uniform counterpart that has the same degrees of freedom) because the truncation error is controlled mainly by the coarse-resolution region (Weller et al. 2009; Ringler et al. 2011); the numerical convergence rate may also be affected (e.g., Düben and Korn 2014). Mesh refinement also tends to create artificial wave distortion and reflection. This issue is more challenging to the staggered finite-volume methods (Ullrich and Jablonowski 2011), which are widely employed in today's weather and climate models due to their cost-effectiveness. At first glance, this seems to pose some disadvantages. Fortunately, the primary motivation of increasing resolution is to accurately resolve meteorologically important fine-scale structures. This implies that the solutions, in particular at high-wavenumbers, change as the resolution increases. As long as one can maximize the model performance over the refined region, and have good control over the adverse impact due to the non-refined regions, the VR approach based on the staggered finite-volume method is extremely promising. This statement is not intended to diminish the importance of pursuing numerical precision, which is one of several important properties when developing model dynamics. It is hoped that a balanced compromise can be achieved, and thus we can take advantage of this promising approach.

Previous numerical studies have investigated the impact of grid refinement on the solution error in shallow-water models (Ringler et al. 2011; Guba et al. 2014), mainly based on single-region refinement. The impact of the width of the grid transition zone and the densification ratio has been emphasized. On the basis of spherical centroid Voronoi tessellation (SCVT), Ringler et al. (2011) demonstrated that the solution error is controlled primarily by the coarse-resolution region, and suggested that this can help to specify the coarse-mesh resolutions by determining what is an acceptable level of accuracy. They also suspected that the width of the transition zone may lead to increased errors. Liu and Yang (2017) suggested that the width of the transition zone may cause smaller additional errors compared to the

¹ We only consider the issues related to model dynamics in this study.

increase in the densification ratio (for the tests they examined). Within a unified global model, these problems may potentially reduce the performance in the refined region.

In terms of resolving fine-scale fluid structures, the tropical cyclone is a useful testbed, and has been frequently used to examine resolution sensitivity. The global VR approach has been employed to simulate tropical cyclones for cost-effective climate simulations (Zarzycki and Jablonowski 2014). The VR model can capture smoother cloud patterns and smoother mid-level jet structures across the grid refined region, leading to enhanced tropical cyclone activities, compared to a nested model in which boundary forcing may have an adverse influence (Hashimoto et al. 2015). Based on a VR configuration, the Community Atmosphere Model (CAM) with a spectral element core (Taylor 2011) well maintains tropical cyclones crossing the transition zone without discernable wave reflection (Zarzycki et al. 2014).

While these earlier studies have reported the benefits of VR modeling, a proper utilization of this technique is still challenging and deserves ongoing exploration. In this study, we systematically configure and evaluate the Global-to-Regional Integrated forecast SysTem (GRIST) atmosphere model based on the VR approach. GRIST is a new modeling system developed on an unstructured mesh, independent from existing atmospheric models available in the community. Previous studies have described the model formulation, and evaluated its performance in shallow-water model tests (Zhang 2018; Wang et al. 2019), 3D dry dynamical core (dycore² hereafter; Zhang et al. 2019; Z19 hereafter) tests, and multiscale moist-atmosphere tests forced by simple physics (Zhang et al. 2020; Z20 hereafter). These studies considered mainly the quasi-uniform (QU) mesh. The model configuration and performance remain underexplored when local mesh refinement is considered.

In this study, we describe the model configuration for VR modeling. In particular, we will detail the explicit diffusion option, and demonstrate its impact. We then examine the model behavior, to understand its strengths and weaknesses under various mesh-refinement styles. This work is intended to provide a basis for utilizing GRIST-VR for more realistic modeling in future. To achieve these goals, we adopt two idealized initial atmospheric conditions, endorsed by the Dynamical Core Model Intercomparison Project (DCMIP; Ullrich et al. 2017). They drive the model towards some well-expected behaviors, facilitating a basic understanding of VR modeling. The model is forced from zero physics (i.e., pure dynamics) to simple and full physics, so as to represent an increasing degree of complexity.

The remainder of this paper is organized as follows. Section 2 presents the model description and its configuration for VR modeling. Section 3 describes the mesh configuration. Section 4 examines the VR performance in the dry baroclinic wave test. Section 5 investigates the model sensitivity in the tropical cyclone test. Section 6 presents a summary.

2. Model description

2.1 Model framework and dynamics

The model evaluated here is a frozen version of the GRIST-Atmosphere model. A20.9 denotes the version frozen at September 2020. The major descriptions (dynamical framework and component coupling) are in Z20 and Z19. GRIST is formulated on an unstructured mesh, which permits the use of SCVT (Ringler et al. 2008; Jacobsen et al. 2013) that enables VR modeling. A dry-mass-based generalized vertical coordinate is used. It allows flexible switching between the hydrostatic (HDC) and nonhydrostatic (NDC) cores. The moist-atmospheric model exactly conserves the dry air mass to within machine roundoff. The sink of the moist total energy is limited to a quite small value. The flux-form scalar variables are formulated in a layer-averaged manner. The momentum variables are formulated in their primitive forms. A vertically semi-implicit approach is used for solving the acoustic equations in the NDC, with explicit Eulerian vertical advection. The HDC is fully explicit.

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 $^{^2}$ In the context of GRIST, dycore specifically refers to the dry part of the governing equations excluding tracer transport; this should be distinguished from the typical usage of dycore in the literature.

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Thuburn et al. (2009) proposed the key construction of the Coriolis term to achieve desirable mimetic properties. Ringler et al. (2010) formulated a set of spatial operators for the nonlinear shallow-water equations, under the constraints of integral invariant conservation and compatible vorticity dynamics. This approach has been used/examined by the Model for Prediction Across Scales (MPAS; Skamarock et al. 2012; Ringler et al. 2013), ICON-IAP (Icosahedral Nonhydrostatic model at the Institute of Atmospheric Physics, Gassmann 2013) and DYNAMICO (Dubos et al. 2015). GRIST adopts two variations that differ from that in Ringler et al. (2010). Zhang (2018) extended a set of high-order upwind/center flux operators (Skamarock and Gassmann 2011) for approximating the edge-based potential vorticity flux, and demonstrated that both the higher nominal order and implicit upwind damping improve the simulated vorticity field. A pure third-order upwind formulation is used in GRIST. The other variation is a redefinition of the kinetic energy term by blending the original primal-cell value with a reconstructed value from the dual cell (Gassmann 2013). This helps to alleviate the noise associated with the Hollingsworth instability (Hollingsworth et al. 1983) according to earlier OU model tests. A default coefficient of 0.9 is used following Eq. (20) in Z19.

The horizontal discretization is formulated on a hexagonal-C grid, that is, using a staggered finite-volume method.

The C-grid is cost-effective in dealing with the flux-divergence and gradient operators, which constitute the major horizontal computation involved in a full-fledged atmospheric dynamical core. The potentially adverse dispersion issue due to increasing mesh discontinuity in the VR mode (Ullrich and Jablonowski 2011) can be well controlled by: (i) using a smooth and gradual mesh transition (e.g., SCVT); and (ii) using a slight amount of explicit diffusion (as will be discussed). The basic horizontal operators are nominally accurate to the second-order, while the flux operator can be approximated using higher order extensions. GRIST has several options for the flux operator. Among these, a nominal fifth-order upwind formulation can generate the smallest numerical errors (see results in Zhang 2018; Wang et al. 2019), but is not used for our default configuration as it requires three halo layers (the default number is two)3. This formulation is still instrumental in model development, helping to validate that the parallel computing infrastructure (Liu et al. 2020) is working correctly when using different minimum halo layers. The pure upwind formulation of Skamarock and Gassmann (2011) is used for the dycore. When combined with a flux limiter, this scheme can be used for tracer transport (as in Section 5.2). A Two-step Shape-Preserving Advection Scheme (TSPAS; Zhang et al. 2017; Yu 1994) is also a major option for tracer transport (as in Section 5.1). Two-time-level single/multistage forward-in-time integration is used for dycore and tracer transport such that dry air mass and tracer mass are coupled in a consistent manner.

Two initial conditions are used in this study. The baroclinic wave (Jablonowski and Williamson 2006; JW06) examines the adiabatic behaviors in a dry environment. The solution from a high-resolution run can be used as a reference solution. The idealized tropical cyclone is initialized following Reed and Jablonowski (2011). It is available from the DCMIP testing scripts. This test does not support a reference solution. As GRIST uses a dry-mass vertical coordinate, obtaining the moist-atmosphere state requires some special treatment (see Z20 for details). All the simulations use 30 full vertical levels with a top at ~2.25 hPa, basically identical to the default CAM5 setup (e.g., Reed and Jablonowski 2012). Both two tests are short-term deterministic tests (i.e., weather forecasting style), helping to validate the model configuration. Long term climate modeling based on the VR configuration will be reported elsewhere. Also note that, while some studies have pointed out that the vertical resolution should increase with horizontal resolution, we keep it unchanged in this study.

2.2 Model physics

GRIST provides a general physics-dynamics coupling interface to incorporate various physics packages. A tailored package can be used as a plugin, and its development can benefit from the broad community resources. One may add a specific physics scheme to an existing physics package, or create an entirely new physics package as long as it is

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³ Using two halo layers may be possible, but would require a more complicated communication rule than the current one, which is

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 compatible with the current workflow and is scientifically reliable. The surface model (e.g., land or a mixed-layer ocean model), though not used in this study, is coupled in a point-to-point style, and can be shared by different physics configurations. Three physics packages are currently available as basis for continuous research and development. These packages are separate in the sense that they have different physics drivers and data structures. For completeness, we describe them in this section.

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(i) The DCMIP simple physics package. In this study, the suite of Reed and Jablonowski (2012) is used. It contains a large-scale condensation process, a surface flux scheme, and a boundary layer process. The sea surface temperature is 29°C globally. These processes are coupled in a time-splitting manner within the package, and the package is coupled to GRIST in a pure operator-splitting approach (ptend_f2_sudden; see Z20).

- (ii) A climate physics package adopted from CAM5. This package is not used in this study, but the details can be found in Li et al. (2020). It is currently being tuned for the HDC that targets long-term climate modeling, and can also be used for short-term integration in a weather forecast mode (e.g., Zhang et al. 2015).
- (iii) For GRIST-NDC, which is targeted at simulating nonhydrostatic dynamics in a nonhydrostatic regime, a set of parameterization schemes from the Weather Research and Forecast (WRF) model (Powers et al. 2017) has been implemented, and is used in this study. The detailed schemes include: a six-species cloud microphysics scheme (Lin et al. 1983) from WRF version 2.0; the Tiedtke cumulus scheme (Tiedtke 1989) from WRF version 3.7.1; the YSU (Yonsei University) planetary boundary layer scheme (Hong et al. 2006) and a surface scheme from WRF version 2.0; the longwave radiation scheme is the RRTM (Rapid Radiative Transfer Model) from WRF version 2.0 (Mlawer et al. 1997); and the shortwave scheme is a CAM radiation module from WRF version 3.4.1.

The internal coupling of this package is process splitting (see e.g., a review in Gross et al. 2018 for details). All processes start from the dynamics-updated state and send back their respective tendencies to the dynamical model without modifications of the physics state variables. The exception is that microphysics will update the local physics state variables, so the calling sequence still matters. The physics-dynamics coupling uses a hybrid approach that combines the tendency method (ptend_rk) and the operator-splitting approach, as described in Z20. In particular, radiation heating is carried over the internal integration of the dycore as in a tendency method, and other tendencies (microphysics, boundary layer, cumulus) are updated as in a pure operator-splitting approach (ptend_f2_sudden in Z20). We emphasize that this package (including the choice of different schemes and its internal coupling) is still experimental and preliminary. It has not been comprehensively tuned. Ongoing tests, modifications, and additions are required to refine the performance. In this study, it is only intended to evaluate the particular performance of VR modeling and the role of explicit diffusion in a full physics scenario.

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2.3 Time-step choices and explicit diffusion

For a VR model, the time step is theoretically restricted by its fine-resolution region. As emphasized by one reviewer and based on our own experience, some improper VR configurations may lead to higher stability restriction than their equivalent QU counterparts. For example, with regard to the acoustic-mode filter, Klemp et al. (2018) suggested that their original formulation is more problematic in VR applications, and cannot effectively remove the acoustic noise. Uncontrolled acoustic modes may artificially accumulate energy and thus impose a higher stability restriction. For the configurations and tests that we have examined, a suitable configuration of explicit diffusion is mostly relevant to this issue. The details will be given in the following section.

The explicit diffusion tendencies are generated at the largest time interval of each model step (i.e., physics step). They are coupled to model dynamics as in a tendency method (ptend_rk). Z20 showed that the tendency method has a slightly higher stability restriction than the pure operator-splitting approach (ptend_f2_sudden), but it can benefit from the higher accuracy of the time integrator. The tendency method does not require additional data communication. No explicit diffusion is activated for tracer transport in this paper.

2.3.1 Smagorinsky diffusion

Flow-dependent Smagorinsky diffusion (Smagorinsky 1963) is used for velocities and potential temperature, following previous QU model tests. It is activated in all experiments, except the baroclinic wave test at the quasi-uniform G6 resolution. This scheme uses a second-order Laplacian operator multiplied by a flow-dependent eddy viscosity. The eddy viscosity is defined at the edge point. The Smagorinsky diffusion is not very scale selective, but its flow-dependent feature makes it selective in terms of where and how much to diffuse (see e.g., Fig. 9 in Gassmann 2013). The diffusion strength is acceptable overall, as evidenced by the sharp gradient in the QU baroclinic wave test.

In the QU mode, a mean length scale is used for calculating the eddy viscosity. For the VR mode, doing so implies a stronger diffusion (than typically required) for the refinement region. This also leads to a higher stability restriction, especially when the refinement ratio becomes large. In this version, the square of this mean length scale is replaced by the local length product of a pair of crossing edges. In the tropical cyclone test (simple physics), this local approach increases the maximum wind magnitude in the eyewall (as compared to the unscaled version in the preprint), because a smaller amount of diffusion is imposed on the refinement area (see Section 5.1). It also reduces the parametric sensitivity to the Smagorinsky coefficient as found in the preprint. When varying the coefficient, the present version generates more consistent solutions, similar to a QU model. This local scaling approach was used for the VR mode but not for the QU mode.⁴

2.3.2 Hyperdiffusion

The hyperdiffusion option was not used in the initial preprint. Based on some exploration and experiments, we have found that activating scale-selective fourth-order hyperdiffusion for the horizontal velocity shows demonstrable added value for VR modeling. First, in the baroclinic wave test, in the absence of hyperdiffusion, a higher Smagorinsky coefficient (compared to the equivalent QU test) is required to suppress grid-scale noise due to the mesh refinement, which, in turn, restricts the numerical stability. When the hyperdiffusion is activated, we can use a moderate Smagorinsky coefficient that does not challenge the numerical stability, and maintains a quality solution. The DTP (dycore-tracer-physics) splitting mode benefits from this most, because diffusion is called at the step of the model physics. Second, even with a higher coefficient, the Smagorinsky diffusion is inactive over certain regions where weak flow deformation dominates. In the baroclinic wave test, some grid-scale oscillations are more conspicuous over these regions (see preprint). Such noise is due to the mesh transition, and some of it is akin to the Hollingsworth instability. As will be shown, activating a background hyperdiffusion for the horizontal wind successfully removes such noise. The solutions are overall less oscillatory than those in the preprint. Third, in the tropical cyclone tests with full physics, which presents more nonlinear feedback, the hyperdiffusion option is also effective in suppressing some isolated-scale structures. Unlike the minor disturbances that may be generated near the major tropical cyclone in the simple physics test, these systems are far away from the initial vortex, and thus highly unrealistic. For these reasons, the hyperdiffusion option is used for the VR mode, but not for the QU test. Thus, QU and VR models are applied by different forms of explicit diffusion in this manuscript. Future work may also need to examine the possible impact of hyperdiffusion in a QU model to better isolate its effect.

The hyperdiffusion operator is formulated by recursively using the Laplacian operator (see Z19 for details). The diffusion coefficient can be determined in a relatively empirical way. For VR modeling, we adopt the approach documented in Zarzycki et al. (2014) for scaling the coefficient:

$$K_4(\Delta x) = K_4(\Delta x^{ref}) \left(\frac{\Delta x}{\Lambda x^{ref}}\right)^{3.3219};\tag{1}$$

The reference length Δx^{ref} and reference viscosity coefficient $K_4(\Delta x^{ref})$ are empirically determined. This formulation reduces $K_4(\Delta x)$ by a factor of 10 for every halving of resolution. A similar scaling approach is also used

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⁴ To achieve consistency with earlier QU tests.

in MPAS (Skamarock 2016). We typically use the configuration for a G-level resolution that is close to the finest resolution on the mesh. Some typical values for GRIST are documented in Table $\underline{S}1$. These values⁵ are smaller than those in Zarzycki et al. (2014) for the corresponding length scale by a factor of 5. The local grid distance (Δx) is an average distance between the grid point and all its nearest neighbors, that is, a cell-based value. The edge-based value used for hyperdiffusion is an average of two neighboring cell values.

3. Generation of the VR mesh

The properties and generation of the SCVT are detailed in Ringler et al. (2011) and Ju et al. (2011). We focus on two key elements of the SCVT: generators and density function. A spherical Voronoi tessellation is a spatial subdivision of a sphere Ω based on a set of distinct points on Ω . For each point x_i , i=1,...,n, the corresponding Voronoi region V_i , i=1,...,n, is defined by:

$$V_{i} = \{x \in \Omega \mid ||x - x_{i}|| < ||x - x_{j}|| \text{ for } j = 1, ..., n \text{ and } j \neq i\};$$
 (2)

where $\|\cdot\|$ denotes the geodesic distance. Each point x_i is called a generator and its corresponding Voronoi region V_i is called the Voronoi cell. A spherical Voronoi tessellation becomes an SCVT when the generators are also the centroids of the Voronoi cells. In this study, the SCVT mesh is constructed by an iterative process based on Lloyd's algorithm (Du et al. 1999). In particular, a parallel algorithm is used (Jacobsen et al. 2013) to avoid time-consuming serial construction. That said, generating a quality VR SCVT is still nontrivial (but only done once). In our implementation, the iteration stops when two criteria are satisfied: (i) it reaches an empirically determined minimum step; and (ii) the circumcenter of each triangle falls within its shape.

403 3.1 Generators

Three original generators are used in this study:

- (i) Icosahedron bisection. This approach benefits from the excellent uniform properties due to bisections of a regular icosahedron. The mesh resolution is referred to as G-level/Gn, where n denotes the number of bisections. After each bisection, the total grid number is approximately four times greater than the previous one.
- 409 (ii) **Icosahedron bisection with a final-step trisection**. Instead of using recursive bisection, a trisection is used
 410 at the final step, to achieve an intermediate resolution between two neighboring G-level resolutions. This mesh
 411 is referred to as GnB3 (i.e., n bisections plus one trisection). For instance, the resolution of G5B3 (~80 km)
 412 is between that of G6 (~120 km) and that of G7 (~60 km). The number of added primal cells (mainly hexagons)
 413 from G5 to G5B3 is equal to four times the number of dual cells (triangles) in G5.
 - (iii) Spherical uniform random (SUR) set of points. Initial points are created uniformly on the sphere by the Monte Carlo method. In this way, the original generators can be obtained by using an arbitrary number of points, not restricted to a sub-divided icosahedron.

3.2 Density function

By specifying the density function, the SCVT is able to precisely control the distribution of the local resolution.

For any two Voronoi regions indexed by *i* and *j*, the conjecture is:

$$\frac{dx_i}{dx_j} \approx \left[\frac{\rho(x_j)}{\rho(x_i)}\right]^{1/4};\tag{3}$$

where $\rho(x_i)$ is the density function evaluated at x_i , and dx_i measures the local mesh resolution. This relation is valid in a theoretical sense.

A QU mesh can be constructed when the density is one on the sphere, and the Voronoi regions are approximately equivalent to each other. For the VR mesh, the basic density function used in this study is:

⁵ Based on some tests, further halving the coefficient for a given resolution is also acceptable; see Fig. 4.

$$\rho(x_i) = \frac{1}{2(1-\gamma)} \left[\tanh\left(\frac{\beta - \|x_{rc} - x_i\|}{\alpha}\right) + 1 \right] + \gamma; \tag{4}$$

where $\|x_{rc} - x_i\|$ denotes the geodesic distance between the location of the refinement center and each generator. α indicates the width of the transition zone between the fine-resolution and coarse-resolution regions; β defines the coverage radius of the fine-resolution region; γ measures the densification ratio between the finest and coarsest resolutions. A sample X4 mesh based on this density function with $\gamma = (1/4)^4$ is shown in Fig. 1a.

Because the basic density function is fixed to a single-region refinement, we adjust it for multi-region refinement. The multi-region refinement is divided into two styles based on the refinement centers. In the hierarchical refinement way (Fig. 1b), we add a uniform intermediate-resolution region between the inner fine-resolution and the outer coarse-resolution regions (see Fig. 2). This helps to avoid an overly high densification ratio between two neighboring regions. Eq. (4) can be generalized to a form that allows us to control the resolution of the intermediate region:

$$\rho(x_i) = \frac{1}{2(1-\gamma)} \left[\frac{1-\lambda}{1-\gamma} \tanh\left(\frac{\beta_1 - \|x_{rc} - x_i\|}{\alpha_1}\right) + \frac{\lambda - \gamma}{1-\gamma} \tanh\left(\frac{\beta_2 - \|x_{rc} - x_i\|}{\alpha_2}\right) + 1 \right] + \gamma; \tag{5}$$

433 λ is designed to control the resolution of the intermediate-resolution region, also referred to as the 2^{nd} -refinement region

434 (dx_{r_2}) that is located between the 1st-refinement (dx_{r_1}) and the coarse-resolution regions (dx_c) :

$$\frac{dx_{r_1}}{dx_{r_2}} \approx \lambda^{1/4};\tag{6}$$

Generally, $\lambda \in [\gamma, 1]$. The function of γ is similar to that in the previous single-region refinement, except that the fine-

resolution region is referred to as the 1st-refinement region here:

$$\frac{dx_{r_1}}{dx_c} \approx \gamma^{1/4};\tag{7}$$

437 Corresponding to γ , we refer to the meshes that are generated based on λ values of $(1)^4$, $(1/2)^4$, and $(1/3)^4$ as

438 XL1, XL2, and XL3 meshes, since the resolutions of the 1st-refinement and the 2nd-refinement regions vary according

to the inner densification ratios of 1, 2, and 3, respectively. For example, when γ is fixed at X4, the hierarchical meshes

based on G6 are called G6X4L1, G6X4L2, and G6X4L3 meshes.

In a polycentric refinement mode (Fig. 1c), by adding a different refinement center x_{rc2} , the density function of the polycentric refinement mode is defined as:

$$\rho(x_i) = \frac{1}{2(1-\gamma)} \left[\tanh\left(\frac{\beta - \|x_{rc1} - x_i\|}{\alpha}\right) + \tanh\left(\frac{\beta - \|x_{rc2} - x_i\|}{\alpha}\right) + 2 \right] + \gamma; \tag{8}$$

The geodesic distance between the two refinement centers should satisfy $||x_{rc1} - x_{rc2}|| > 2\beta$.

4. Dry-atmosphere simulations

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4.1 Single-region refinement

The dry-atmosphere test examines the pure numerical solution of the model. It does not include the nonlinear interaction between dynamics, moisture transport, and parameterization. Based on the JW06 baroclinic wave test, we first compare the VR and QU simulations. Previous studies that employed this test for a VR model include Gettelman et al. (2018; using the multiresolution approach) and Harris and Lin (2012; using the multi-grid approach), based on different evaluation metrics. The QU grids include G6 (~120 km; 40962 cells), G7 (~60 km; 163842 cells), and G8 (~30 km; 655362 cells). The VR grids examine all three generators: (i) icosahedral bisection (e.g., G6X4), (ii) final-step trisection (G5B3X4), and (iii) spherical uniform random points (SURX4). The minimum iteration number is 300,000 for G6X4, and 1,000,000 for G5B3X4 and SURX4. The refinement center is placed at 35°N, 180°E, with $\alpha = \pi/20$ and $\beta = \pi/6$. The detailed model configuration is given in Table 1. The timestep of the VR model is limited by its fine-resolution region and is set accordingly, although the currently used timesteps do not represent the maximum

We first examine the ability of resolving the fine-scale structures. Figure 3 shows the relative vorticity field at the model level nearest to 850 hPa (level 24) after 10 days. These values have been remapped to the Voronoi cell from the

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raw triangular grid, so as to avoid the aliasing of certain oscillatory patterns. Such patterns (see preprint) actually reflect the mesh shape, and are more conspicuous for coarse resolution. Figure S1 further shows the QU model results interpolated to the regular longitude—latitude grid as a reference. As the resolution increases, the QU models simulate stronger vortices with a clear filament structure (Fig. 3a–3c). The VR model can simulate the smooth structure of the waves in the refined region, as in the high-resolution QU model. In the VR mode, two vortices in the west fall within the fine-resolution region. The structure of the westernmost vortex in G6X4 (Fig. 3d) is close to G7. G5B3X4 and SURX4 (Fig. 3e, 3f) further produce finer scale structures than G6X4, closer to G8. The easternmost wave falls within the transition zone in three VR runs. The variation in the mesh sizes there does not distort the wave pattern, and the fine-scale structure can be improved as the resolution of the transition zone increases (e.g., from G6X4 to G5B3X4). In the SURX4 test, a minor roughness is found on the tails of the vortices. This deficiency is largely due to local mesh irregularities. Compared to the icosahedron-based SCVT generators, the random generators tend to slightly degrade the mesh quality and the simulation performance.

To present a more quantitative evaluation of the momentum field, we examine regional kinetic energy spectra⁶ over the refinement area (red box in Fig. 3). We use the discrete cosine transform to perform this analysis (cf. Denis et al. 2002). The computational procedure is briefly documented in the Appendix. The decomposition is made for relative vorticity and divergence. Fig. 4a–4c show the results from different tests. It is clear that the rotational mode dominates the kinetic energy. The hydrostatic model (Fig. S2) produces similar results to the nonhydrostatic model; thus only the nonhydrostatic core is discussed in the main text.

At the 1st wavenumber, runs with different resolutions show larger discrepancies. This is because this lowest mode absorbs most of the large-scale trend, and corresponds to only a half-cosine wave. Denis et al. (2002) suggested that one may remove this mode if desired, but we keep it here. From the 2nd to the 10th wavenumber, all the curves are consistent overall, suggesting that the well-resolved structures are robust to various tests. The major difference lies in the high wavenumbers. For the VR results, G6X4 is close to G7. This is expected because they have similar resolution over the selected domain (~60 km). For the same reason, G5B3X4 and SURX4 produce better spectral tails than G7 and G6X4, closer to G8. This confirms that increasing the fine resolution of the VR model is able to improve its fine-scale resolving ability. At such high wavenumbers, SURX4 is even closer to G8 as it has slightly higher energy in the tail. However, this actually reflects that SURX4 has slightly more grid-scale oscillations than G5B3X4. Therefore, an examination of kinetic energy spectra should be accompanied by a close look at the real field.

In the context of kinetic energy spectra, it is useful to demonstrate the impact of the hyperviscosity coefficient. For G5B3X4, we vary the reference hyperviscosity coefficient under a fixed reference length (30 km). Note that 2×10^{12} is the default configuration for this test. As shown in Fig. 4d–4f, when using 2×10^{13} , spectra are seriously damped at the high wavenumbers in both the rotational and divergent components. A flat tail is generated. This indicates that the diffusion strength is overly strong for the fine-resolution area. The other four tests generally produce consistent results: reducing the coefficient tends to slightly uplift the tail, that is, increase the kinetic energy. While the lowest coefficient (2×10^{11}) seems to produce a nicer tail than the default run, this, again, reflects the fact that slightly more small-scale oscillations are generated and the solutions are less clean (but still acceptable). Therefore, when tuning a VR model, one should achieve a minimally required hyperviscosity that neither significantly damps the field nor becomes unable to suppress certain grid-scale oscillations. For this test, 2×10^{12} is fairly close to the optimal choice.

Next, we assess the solution errors by first examining the surface pressure field. Its global distribution on day 9 simulated by GRIST-NDC is shown in Fig. S3. The locations and magnitudes of the high- and low-pressure centers are

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⁶ Note that in Z19, due to an incorrect display setting, there is a plotting mistake in the kinetic energy spectra (their Fig. 10): the tick marks of the entire top x-axis (representing wavelength) do not correspond to the actual wavelength of the data. The bottom x-axis is correct

consistent overall in the QU (Fig. S3a–3c) and VR (Fig. S3d–3f) runs. There are some nonzero wave patterns in all VR simulations over the Southern Hemisphere, reflecting that the nonuniform grid structure leads to higher truncation errors. G5B3X4 has smaller wave patterns than G6X4. This is expected as G5B3X4 has a higher resolution than G6X4 there. Moreover, G5B3X4 is also better than SURX4 with regard to these wave patterns. Considering that SURX4 has more mesh cells, this suggests that generators based on a regular icosahedron produce higher mesh quality than random generators, given roughly the same number of iterations.

Figure 5 shows a quantitative comparison. The global l_2 error norm of each test is computed against the highest resolution (G8). The errors of three VR meshes (G6X4, G5B3X4, and SURX4) are higher overall than those of the QU meshes. Note that these errors are also slightly higher than those in the preprint because a larger time step is used in this version (we performed additional tests to check this sensitivity; figure not shown). The nonhydrostatic solver produces slightly smaller errors using three VR meshes, but the overall accuracy of the two solvers is comparable. For three VR meshes, G5B3X4 shows the smallest error, and is generally close to the results of G6 during the first 10 days. G6X4 shows the largest error and SURX4 lies in between them. Again, the fact that SURX4 is less accurate than G5B3X4 implies that random generators are more likely to be trapped into the local area during the iterative procedure of mesh generation, leading to a higher degree of local irregularity.

For GRIST-NDC, we further tested G7X4 and G8X4. As shown (Fig. 5b), G7X4 produces smaller errors overall than G5B3X4, although the difference is small. G8X4 produces higher errors than G7X4 during the first four days. We suspect this is because certain initial imbalance becomes more active in a high-resolution VR configuration. Such imbalance can be caused by the discrete initialization, for example, the continuous properties imposed by the analytic wind field will not be exactly satisfied by the discrete normal velocity, unless the velocity is obtained based on some constraints. After day 5, G8X4 produces smaller errors than G7X4, and the increment in error reduction is close to the difference between G6X4 and G7X4. G8X4 also produces clearly smaller errors than G6 from day 5 to day 12. After day 13, G8X4 has higher errors than G6, although its coarsest resolution is finer than that of G6. These results suggest that the VR models indeed increase the global errors, but the errors can be reduced by increasing the coarse resolution of the mesh. This is not surprising but a reconfirmation of the conclusion in Ringler et al. (2011), using a 3D atmospheric dynamical core.

The JW06 test was originally proposed in the era that models based on a regular latitude—longitude or Gaussian grid were predominant. For a quasi-uniform grid, it is well known that the steady state in the Southern Hemisphere (or in an unperturbed condition) cannot be perfectly maintained due to mesh irregularity (Lauritzen et al. 2010). In a baroclinic environment, such errors will grow exponentially to break the steady state. Because mesh irregularity increases in a VR mode, the inability to maintain the steady state can be further amplified, ultimately contributing to the increased errors.

To reduce the impact of this issue, we add another perturbation over the Southern Hemisphere to excite two wave trains, as was done in some earlier studies (e.g., Gassmann 2013). Figure 6 shows the relative vorticity field on day 10 from three selected tests: G6, G6X4, and G5B3X4. The sign of the relative vorticity in the Southern Hemisphere is flipped to facilitate a visual comparison. The QU model (Fig. 6a) produces a comparable wave train in each hemisphere. The wave trains are not exactly symmetric because the mesh cells are not exactly symmetric across the equator. In the Northern Hemisphere, G6X4 and G5B3X4 (Fig. 6b and 6c) produce similar solutions to Fig. 3d and 3e. In the Southern Hemisphere, the solution of G5B3X4 is closer to that of G6 than G6X4, in terms of wave pattern and magnitude. This is to be expected as G5B3X4 has higher resolution in the Southern Hemisphere. Although G6X4 cannot simulate the structure in the Southern Hemisphere as G5B3X4, no serious problem is found for that region.

Figure 7 presents a quantitative estimation of the solution error. Generally, the magnitude and the growth of the errors are close to those in Fig. 5b. A notable difference is that G8X4 produces smaller relative errors, closer to those

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of G7 from day 8 to day 12. On day 15, G8X4 still shows comparable errors to G6. The error reduction from G6X4 to G7X4 also becomes larger than that in Fig. 5b, when the waves become more developed (e.g., day 8 to 11). This implies that the inability to maintain a steady state in the Southern Hemisphere indeed worsens the error estimation for a VR model.

4.2 Multi-region refinement

To increase the application range of the single-region refinement, two multi-region refinement modes are examined to obtain desired resolutions in multiple regions. This represents a unique aspect of the multiresolution approach. The first way is a hierarchical style with one refinement center. It contains three consecutive uniform sub-regions outside the refinement center: the 1st-refinement region, the 2nd-refinement region, and the coarse-resolution region. The 2nd-refinement region provides an intermediate resolution between the 1st-refinement and coarse-resolution regions. Compared to the single-region refinement, this 2nd-refinement region provides more uniform resolution between the refinement center and the coarse-resolution area.

The symmetrical perturbation test was performed using a G8X4L2 mesh. On day 10, the first wave (the strongest) over the Northern Hemisphere is experiencing a higher gradient of resolution than that over the Southern Hemisphere. The fine-scale structures are well captured by the VR model (Fig. 8a). The second and third waves in the Northern Hemisphere have stronger magnitudes than their equivalents in the Southern Hemisphere. The difference in each wave train generally reflects the differences in the local resolution.

The second way uses a polycentric style with multiple refinement centers. The same double-baroclinic wave trains are generated using a G7X4 mesh, with two refinement centers at 35°N, 180°E and 35°S, 180°E, respectively. On day 10, the model well simulates the fine-scale structures over two selected regions (Fig. 8b). The transitions between the fine and coarse regions are smooth and stable. This refinement mode may provide an effective way to simultaneously improve the simulations over different regions. The wave train in the Southern Hemisphere coincides well with that in the North. Again, they are not exactly identical because the mesh cells are not exactly symmetric across the equator.

In this test case, it is useful to demonstrate the impact of activating the hyperdiffusion option. As shown in Fig. 8c and 8d, when hyperdiffusion is turned off, the simulation results become rather oscillatory. The noise pattern at the tail of the wave is akin to the Hollingsworth instability, and is amplified by a VR model due to mesh transition. The noise is more conspicuous in the 1st-refinement region of G8X4L2, due to higher resolution and rapid mesh transition. Also note that these results are more oscillatory than those in the preprint, because the Smagorinsky diffusion in that version is stronger. As mentioned in Section 2.3, even so, the Smagorinsky option is still inactive over certain regions. Using a background hyperdiffusion is a good complement to this deficiency.

576 5. Moist-atmosphere modeling

5.1 Simple physics

Moist-atmosphere modeling includes the nonlinear interaction of dynamics, moisture transport, and model physics. We use the idealized tropical cyclone test (Reed and Jablonowski 2011) because of its clear resolution sensitivity. This test is useful to examine the VR performance because the solution does not fully converge even at 10 km (Z20). The simulated tropical cyclone is very sensitive to the mesh size. A higher resolution model will produce more intense storms. An initial vortex is placed 10°N, 180°E with no background flow. The tropical cyclone moves northwestward due to beta drift. The initial virtual temperature profiles are designed to be conditionally unstable in the troposphere. A small perturbation (either physical or computational) is more likely to excite new storms. Whether these additional signals are realistic depend on the situations.

Previous studies have shown that model dynamics has a clear impact on the simulations of tropical cyclones. For example, Zhao et al. (2012) showed that increasing the strength of 2D divergence damping in the finite-volume dynamical core (Lin 2004) leads to more occurrences of tropical cyclones. Reed et al. (2015) showed that, in CAM5,

the spectral element core produces stronger tropical cyclones than the finite-volume core, when the parameterization suite remains almost unchanged. For GRIST, a known sensitivity is that different tracer transport options may lead to different wind magnitudes in the eyewall, as the full pressure gradient term is, by design, related to tracer mixing ratios (Z20).

We first examine the model behaviors under a simple-physics environment (Reed and Jablonowski 2012). In the preprint, we compared two representative groups of numerical tests: one group based on the NDC with DTP splitting enabled; and one based on the HDC with no DTP splitting (i.e., dycore, tracer transport, and physics use the same time step). Results from these two groups are consistent overall. The impacts of DTP splitting and hydrostatic/nonhydrostatic options do not generate discernable differences across various VR meshes. This is consistent with the previous QU model tests (Z19; Z20) in that: (i) the nonhydrostatic solver behaves similarly to its hydrostatic counterpart under the hydrostatic regime; and (ii) the DTP splitting does not cause a degeneration in performance when it is properly configured. In this version, which uses an updated configuration, only the NDC is tested. The configuration for the simple physics test is given in Table 2.

We first examine the evolution of the tropical cyclone when it moves across the transition zone in the hierarchical refinement mode. The mesh is fixed at X4, with $\alpha_2 = \pi/36$ and $\beta_2 = \pi/4$. In the control run (G6X4L2; Fig. 9a), $\alpha_1 = \pi/36$, $\lambda = (1/2)^4$, and $\beta_1 = \pi/12$. The 1st-refinement region of this VR mesh has ~40-km resolution. Two cases are used to examine the impact of the mesh distribution. In the first case, we choose to use more rapid resolution changes in the inner transition zone based on the two parameters α_1 and λ . α_1 controls the width of the inner transition zone, and λ represents the densification ratio between the 1st- and 2nd-refinement regions. Either narrowing the width of the transition zone (Fig. 9b) or enlarging the inner densification ratio (Fig. 9c) generates a more abrupt transition zone. The other way is to have the transition zone affect the tropical cyclone at an earlier stage. The initial cyclone is placed closer to or even partly within the transition zone by increasing β_1 (Fig. 9d), a parameter that controls the radius of the 1st-refinement region. The tropical cyclone is initialized at 10°N, 180°E over the 2nd-refinement region, near the transition zone between the 1st-refinement and the 2nd-refinement regions.

On day 10, all four tests well simulate the shape of the tropical cyclone. During its movement from the 2nd-refinement into the 1st-refinement region, the change in the grid size leads to little distortion on the tropical cyclone. Compared to the preprint, two major differences can be found. First, the minor disturbances near the major tropical cyclones almost disappear in this version, because activating hyperdiffuion damps the wind field more effectively. Though it can be damped, this minor disturbance is not that unrealistic because it is near the major cyclone. During the movement, it is possible that the nonlinear feedback can generate new small-scale systems. Similar minor disturbances have also been observed in some models participating in DCMIP2016 (see e.g., https://www.earthsystemcog.org/projects/dcmip-2016/). The other difference is that the maximum wind magnitude in the eyewall is stronger overall in this version. This is due to the locally scaled Smagorinsky formulation, as mentioned in Section 2.3.1

Figure 10 presents the evolution of the tropical cyclone in each test on days 2, 4, 6, and 8. The tropical cyclones in all tests are consistent. No discernable difference is found when they move across the transition. A slightly larger difference is more evident in the early stage (day 2), but such differences diminish as the tropical cyclones move into the refinement center. The relative vorticity field also looks smooth_and-does not show any artifacts (Fig. S4). This indicates that the mesh transition does not create notable problems.

To further examine possible sensitivity, we performed a group of experiments by altering one of the three parameters: α_1 , β_1 , and λ . Figure 11 shows the minimum surface pressure (Fig. 11a–11c) and the maximum wind speed at 850 hPa (Fig. 11e–11f). All these tests use a DTP splitting number 1 : 4 : 8, with a dycore step of 60 s (Table 2). Only one test with the smallest α_1 $\binom{\pi}{90}$ is unstable at this DTP splitting number, so we adjusted it to 1 : 2 : 4 with the same dycore

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step. This suggests that an overly narrow inner transition zone can impose a higher stability restriction. The tropical cyclone rapidly strengthens during the first two days. After day 2, it enters into a moderately developing stage in each experiment. The evolution of intensity is diverse. All the VR runs tend to produce stronger tropical cyclones than G6 or G7, because the fine-resolution area determines the ultimate strength. The tests have run-to-run differences, but they are small overall, showing consistent results and robustness.

Figure 12 shows a further comparison between two VR runs (G6X4L2 and G7X4L2) and two QU runs (G7 and G8). The highest resolution of G6X4L2 and G7X4L2 is slightly higher than that of G7 and G8, respectively (see Table 2). As shown, in each comparison (G6X4L2 vs G7, G7X4L2 vs G8), the VR model produces stronger wind magnitudes in the eyewall and a more compact size featuring a smaller area coverage. The eyewall of the cyclone converges towards its center, almost within 1 degree from the center. The maximum winds develop to higher vertical levels as the local resolution increases. Overall, the difference between the VR and QU tests is attributed to different local resolutions.

In the tropical cyclone test, if an unscaled Smagorinsky eddy viscosity is used (Fig. S5; preprint), the VR model will show a higher parametric sensitivity for the Smagorinsky coefficient than the QU model. The current version has largely reduced such sensitivity, closer to the behavior of the QU model (Fig. S5). This confirms the reasonable behavior of the local length formulation.

5.2 Full physics

The simple physics test, while insightful, is limited in the sense that the physics processes are simplified and do not support enough of the nonlinear feedback typical of a real-world model. A VR model may introduce a higher degree of nonlinear feedback due to mesh refinement. Thus, it is useful to check its behavior given a full parameterization suite. We use a more highly variable mesh: G6B3X16L4. The finest part on this mesh reaches \sim 7–10 km. The refinement center is placed at 35°N, 165°E. The sea surface temperature is identical to that in the simple physics test (29°C uniformly). The starting date is the first day of June. The solar constant is 1370 W.m⁻². The DTP splitting number is 1: 5:10 with a dycore step of 10 s. If activated, the square of the Smagorinsky coefficient is 0.005, and the reference hyperviscosity is 2×10^{10} m⁴.s⁻¹ with a reference length scale of 7000 m.

We first focus on the impact of the explicit diffusion process. Figure 13 shows the tropical cyclones on day 10 from three tests: no explicit diffusion (noDiff), using hyperdiffusion only for the horizontal velocity (hyper), and hyperdiffusion plus Smagorinsky (hyper+smg). The wind speed is shown at the model level nearest to 850 hPa (level 24). On day 10, the tropical cyclone center just moves into the refinement center (35°N, 165°E). In general, the results in the three tests are consistent. The major difference lies in the eyewall. The noDiff and hyper tests produce slightly higher wind maxima than hyper+smg. This suggests that Smagorinsky diffusion becomes active in the eyewall, diffusing the solutions a little bit more strongly. Except for this minor difference (see the zoomed results), hyper and hyper+smg produce very close solutions.

Explicit diffusion, while it seems to be irrelevant to the performance over the fine-resolution region, plays a more important role in the coarse-resolution region. Due to the globally uniform sea surface temperature, near the South Pole, some isolated systems can be generated in the noDiff test (Fig. 14a). Unlike the possible minor disturbances near the major tropical cyclone in the simple physics test, these systems are not expected there because they are far away from the initial vortex. They are likely to be caused by the nonlinear feedback between dynamics and physics. Only using the Smagorinsky diffusion can suppress them to a certain extent, but not enough due to its flow-dependent nature (Fig. 14b). By further activating the hyperdiffusion option, these systems can be effectively removed (Fig. 14c). This suggests that the explicit diffusion configuration is able to achieve a balance between underdiffusion and overdiffusion.

With this X16 mesh, it is also useful to examine whether a single refinement with a high densification ratio (G6B3X16) tends to create serious problems during the simulation, especially when the tropical cyclone moves across the transition. The refinement center is rotated to 60°N, 165°E. The tropical cyclone will encounter more mesh

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transitions in G6B3X16. The results are shown in Fig. 15. On day 2, the tropical cyclone in G6B3X16L4 is experiencing mesh cells between ~30 km and ~50 km. In G6B3X16, the encountered mesh sizes are above 70 km. Hence, G6B3X16L4 has a stronger and more developed eyewall at this stage. On day 6, the eyewall enters into a region with cell sizes ~25–30 km in G6B3X16L4, and ~50 km in G6B3X16. G6B3X16L4 still has a more compact eyewall, but the difference between the two runs becomes smaller. On day 10, the eyewalls in both tests enter into an area with cell sizes ~20–25 km. At this stage, both cyclone systems show similar maximum wind magnitudes in the eyewall, and exhibit a similar distribution. Clearly, the fine-scale structure is determined mainly by the fine resolution, although two systems can have larger differences before they enter into the fine-resolution area. These results also demonstrate that a single refinement with a high densification ratio, though more challenging, can perform competitively with a more gradually refined mesh when properly configured (e.g., an overly narrow transition is undesirable). The choice of different mesh styles thus demands more numerical modeling experience and depends on the target issue. This needs to be further examined with more realistic weather and climate system.

6. Conclusions

In this study, an atmospheric model formulated on an unstructured mesh has been systematically configured and evaluated in its VR mode. Different mesh-refinement styles have been utilized to evaluate the model performance under increasing degrees of complexity, from dry dynamics to simple and then to full physics. Based on some additional NDC tests with full physics, it is found that the QU and VR models (with the same degrees of freedom) have comparable parallel efficiency, that is, the VR configuration does not cause a degeneration in strong scaling performance. This is to be expected as the domain decomposition does not distinguish between QU and VR grids. Other scaling performance (e.g., whether the speedup ratio can achieve the ideal value by simply reducing the total grid number, with all other things being equal) can be found in Liu et al. (2020). Overall, these results demonstrate that the VR configuration of GRIST is a reliable and economic alternative to high-resolution quasi-uniform modeling. The adverse impact due to the mesh transition and the coarse-resolution area can be well controlled. The major conclusions may be summarized in three aspects.

On the overall performance. Based on the dry baroclinic wave test, all VR styles can well capture the fine-scale wave structures. Such fine-scale resolving capability is supported by analysis of regional kinetic energy spectra, and is further verified in the multi-region refinement mode. In the transition zone, the waves are not adversely affected by the mesh refinement. In the coarse-resolution region, the VR model can also simulate an equivalent distribution of waves to its low-resolution counterpart. A VR model indeed produces greater solution errors compared to its QU counterpart that has the same degrees of freedom. However, the solution error can be reduced when the coarse region increases its resolution. Thus, its impact can be controlled. In the tropical cyclone test, the VR model in simple and full physics can simulate the gradual evolution of the tropical cyclone, showing reasonable resolution sensitivity. Importantly, the simulation of the fine-scale structure is controlled mainly by the fine resolution, although larger differences may exist before the systems move into the refinement area,

On the impact of explicit diffusion. Comparing this version with its earlier version (preprint), the impact of explicit diffusion can be clearly demonstrated. It has been shown that activating scaled hyperdiffusion for the horizontal velocity as background diffusion is helpful in alleviating grid-scale oscillations due to mesh transitions. It also suppresses some highly unrealistic disturbances found in the full physics scenario. When activating hyperdiffusion, it is suggested that a minimally required hyperviscosity should be used, such that it neither significantly damps the field nor becomes unable to suppress undesirable grid-scale disturbances. Using only Smagorinsky diffusion would require higher coefficients to remove oscillations, which, in turn, would restrict the numerical stability. Even so, the Smagorinsky-only configuration is not enough for the VR mode, because it becomes inactive over certain regions that are dominated by weak flow deformation. It is also shown that, in the tropical cyclone test, the scaled Smagorinsky diffusion has much lower

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parametric sensitivity than its unscaled counterpart. In general, the use of explicit diffusion (properly scaled) plays a positive role in the VR configuration, although there were concerns that their own discretization may introduce additional problems. The increased demands of explicit diffusion from the QU to VR configuration is in accordance with increasing mesh discontinuity due to transitions, and thus should not be viewed as a disadvantage.

On the impact of the mesh styles. Different mesh styles are all able to produce fine-scale structures. They maintain solution quality over the mesh transition and the coarse-resolution area. In the dry test, it has been shown that G5B3X4, while it has fewer cells than SURX4, leads to smaller solution errors and less oscillatory solutions. As these two meshes are generated given a similar number of iterations, this *might* suggest that the random generators need more computation to achieve a quality mesh. In general, when generating a VR mesh, we empirically suggest that one would be better to start from a subdivided icosahedron. In the tropical cyclone case, a series of sensitivity tests examined the model performance in a hierarchical refinement style. The solutions exhibit consistency even when the VR mesh is slightly perturbed by one of the three parameters that control the density function. It is suggested that an overly narrow transition zone should be avoided. In the full physics test, G6B3X16L4 and G6B3X16 produce consistent results on day 10, although the simulations at the initial stage (e.g., day 2) exhibit larger differences.

Code and data availability: GRIST is available at https://github.com/grist-dev. A version of the model code, and running and postprocessing scripts for supporting this paper are available at: https://zenodo.org/record/3930643. Version 2 is for this manuscript, and version 1 is for the preprint. The preprint is available from the online link of this paper. The grid data used to enable the tests are located at https://zenodo.org/record/3817060. Public code access is available after authorization, following https://github.com/GRIST-Dev/TermsAndConditions.

Appendix: Regional kinetic energy spectra analysis

The model data are first interpolated to the Gaussian grid. For the QU model, we use the Gaussian grid that is close to the nominal resolution of the icosahedral mesh (T106 for G6, T213 for G7, and T426 for G8). For the VR model, the data are interpolated based on the fine resolution of the mesh (T221 for G6X4, T328 for G5B3X4, and T328 for SURX4). The selected regional domain (red box in Fig. 3) ranges from 150°E to 150°W and from 30°N to 65°N, with two vortices.

We follow the approach documented by Denis et al. (2002) for computing kinetic energy spectra on a selected regional domain. Let $F_{\zeta}(m,n)$ be the discrete cosine transform (DCT) of a 2D relative vorticity field $\zeta(i,j)$ of N_i -by- N_i grid points. The variance array can be computed from the DCT field as:

$$\sigma_{\zeta}^{2}(m,n) = \frac{F_{\zeta}^{2}(m,n)}{N_{i}N_{j}},\tag{A1}$$

where $m = 0, 1, 2, ..., N_i - 1$, $n = 0, 1, 2, ..., N_j - 1$, and $(m, n) \neq (0, 0)$. Each 2D wavenumber pair (m, n) is associated with a wavelength:

$$A = \frac{2\Delta}{\mu},\tag{A2}$$

756 where Δ is the grid spacing. μ is a normalized 2D wavenumber defined as:

$$\mu = \sqrt{\frac{m^2}{N_i^2} + \frac{n^2}{N_j^2}}.$$
 (A3)

- 757 To construct a spectrum, the variance contributions of $F_{\zeta}(m,n)$ needs to be binned by bands of μ . The ranges of μ
- 758 for a given wavelength band are determined as follows:

$$\mu(k) = \frac{k}{\min(N_i, N_j)},\tag{A4}$$

$$\mu(k) + \Delta\mu(k) = \frac{k+1}{\min(N_t N_j)},$$
(A5)

759 where $k = 1, 2, 3, ..., \min(N_i, N_j) - 1$ denotes the wavenumber.

The rotational part of a spectrum as a function of wavenumber k can be obtained by binning each element in the

761 variance array. For a given k, Eqs. (A4) and (A5) are used to calculate the lower and upper bounds. For each variance

762 element, if the corresponding μ satisfies $\mu(k) < \mu < \mu(k) + \Delta \mu(k)$, the variance will be summed to give the

763 spectrum for this k, that is:

$$E_{\zeta}(k) = \frac{1}{2} \sum_{\mu(k)}^{\mu(k) + \Delta\mu(k)} \frac{\sigma_{\zeta}^{2}(m,n)}{k^{2}},\tag{A6}$$

where k is the circular wavenumber: 764

$$R = \frac{\pi}{\Lambda} \mu. \tag{A7}$$

Similarly, the divergent part can be evaluated based on the divergence field: 765

$$E_{D}(k) = \frac{1}{2} \sum_{\mu(k)}^{\mu(k) + \Delta\mu(k)} \frac{\sigma_{D}^{2}(m,n)}{k^{2}}, \tag{A8}$$

where $\sigma_D^2(m,n)$ is the variance array of divergence. The total kinetic energy as a function of wavenumber k is given 766

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$$E(k) = E_{\zeta}(k) + E_{D}(k), \tag{A9}$$

In this study, kinetic energy spectra are displayed as a function of wavelength A and wavenumber k. It should be 768

769 noted that the lowest mode (k = 1) absorbs most of the large-scale trend and can be excluded if needed (cf. Denis et

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 $\textbf{Supplement}: vr_supplement.pdf \ contains \ Table \ S1_and \ Figures \ S1_S5.$ 771

772 Author contribution: Y. Zhou performed the mesh generation, most data analysis, and an initial exploration of VR

modeling, with input and guidance from Y. Zhang. R. Yu supervised Y. Zhou's work, provided impetus and resources,

guided experimental design. J. Li supervised the project of model development. Z. Liu is responsible for parallel

775 computing, and customized the parallel mesh generation software. Y. Zhang designed this study, developed and

maintained the model, performed production runs, and analyzed the simulations. Y. Zhang and Y. Zhou wrote this

776 777 manuscript, with contributions from all authors. All the authors continuously discussed the model development.

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Table 1: Mesh resolution, timesteps, and diffusion coefficients for the dry-atmosphere test.							
Test case	Mesh	Mean/min/max	HDC:	NDC:	Square of	$K_4(\Delta x_{ref})$	Δx_{ref}
		averaged cell	timestep	timestep	Smagorinsky	m^4s^{-1}	m
		distance (km)	<u>(s)</u>	<u>(s)</u>	coefficient (c_s^2)		
Baroclinic wave:	G6 QU	120.17/97.93/121.76	150	150 90 60 40	5	Ξ.	Ε
single	G7 QU	60.09/47.60/60.88	<u>90</u>	<u>90</u>	0.015	Ξ.	Ξ.
perturbation	G8 QU	30.04/23.04/30.54	<u>60</u>	<u>60</u>	0.04	Ξ	Ξ
	G6X4	107.93/42.95/188.08	<u>40</u>	<u>40</u>	0.015	2×10^{12}	30000
	G5B3X4	71.98/27.55/125.74	<u>40</u>	<u>40</u>	0.015	2×10^{12}	30000
	SURX4	68.27/28.34/119.65	<u>40</u>	<u>40</u>	0.015	2×10^{12}	30000
	G7X4	53.96/19.88/93.71	Not tested	<u>40</u>	0.015	1×10^{12}	20000
	G8X4	27.04/9.84/46.85	Not tested	40 40 20	0.015	2×10^{11}	15000
Baroclinic wave:	G6 QU	120.17/97.93/121.76	Not tested	150	E	Ξ.	Ξ.
double	G7 QU	60.09/47.60/60.88	<u>90</u>	<u>90</u>	0.015	Ξ.	Ε
perturbations	G8 QU	30.04/23.04/30.54	<u>60</u>	<u>60</u>	0.04	Ξ.	Ξ.
	G6X4	107.93/42.95/188.08	Not tested	<u>40</u>	0.015	2×10^{12}	30000
	G5B3X4	71.98/27.55/125.74	Not tested	<u>40</u>	0.015	2×10^{12}	30000
	SURX4	68.27/28.34/119.65	Not tested	<u>40</u>	0.015	2×10^{12}	30000
	G7X4	53.96/19.88/93.71	Not tested	<u>40</u>	0.015	1×10^{12}	20000
	G8X4	27.04/9.84/46.85	Not tested	150 90 60 40 40 40 40 20 20	0.015	2×10^{11}	15000
	G8X4L2	28.80/13.14/61.19	Not tested	<u>20</u>	0.015	2×10^{11}	15000
	G7X4- polycentric	53.02/26.63/114.94	Not tested	<u>40</u>	0.015	2×10^{12}	30000

| 删除了: Table 1 A list of typical values of reference length and hyperviscosity coefficient. [1]

Reference length (m) ... [1]

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Table 2: Mesh resolution, timesteps, and diffusion coefficients for the simple-physics test.							
Test case	Mesh	Mean/min/max	NDC: timestep	Square of	$K_4(\Delta x_{ref})$	Δx_{ref}	
		averaged cell distance	<u>(s)</u>	Smagorinsky	m^4s^{-1}	m	
		<u>(km)</u>		coefficient (c_s^2)			
Tropical cyclone:	G6 QU	120.16/97.08/121.83	<u>150-600-1200</u>	Ξ.	Ξ	Ξ	
base test	G7 QU	60.08/47.09/60.92	90-360-720	0.015	Ξ.	Ξ	
	G8 QU	30.04/23.04/30.54	60-240-480	0.015	Ξ.	<u> </u>	
	G6X4L2	113.24/40.23/166.00	60-240-480	0.01	8×10^{12}	40000	
	G7X4L2	56.62/19.71/82.64	30-120-240	0.01	8×10^{11}	20000	
Tropical cyclone:	<u>XL</u> 0						
sensitivity to the	$\alpha_1 \stackrel{\underline{\lambda}\underline{\Omega}}{(\lambda)} \beta_1$						
three parameters	$\frac{\pi}{90}$ 2 $\frac{\pi}{13}$	113.81/39.40/163.52	60-120-240	0.01	8×10^{12}	40000	
of the hierarchical refinement mode	$\frac{\pi}{60}$ 2 $\frac{\pi}{10}$	113.62/39.35/165.12 113.40/39.61/165.68	60-240-480	0.01	8×10^{12}	<u>40000</u>	
(various	$\frac{\frac{60}{\pi}}{45}$ $\frac{2}{12}$	113.24/40.23/166.00	60-240-480	0.01	8×10^{12}	40000	
hierarchical	$\frac{\frac{45}{\pi}}{2}$ $\frac{2}{\pi}$		60-240-480	0.01	8×10^{12}	40000	
refinement meshes based on the	$\frac{\frac{36}{\pi}}{\frac{2}{30}} \frac{2}{\frac{\pi}{10}}$	113.02/40.71/165.23	60-240-480	0.01	8×10^{12}	40000	
G6X4 mesh)	$\frac{\frac{30}{\pi}}{1}$ 1.5 $\frac{\frac{12}{\pi}}{1}$	110.59/44.58/179.62 114.26/37.10/158.05	60-240-480	0.01	8×10^{12}	40000	
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	114.72/36.77/153.26	60-240-480	0.01	8×10^{12}	40000	
	$\frac{\frac{36}{\pi}}{\frac{36}{36}} \frac{3}{\frac{\pi}{12}}$	114.73/36.74/150.61	60-240-480	0.01	8×10^{12}	40000	
	$\frac{\pi}{36}$ 3.5 $\frac{\pi}{12}$		60-240-480	0.01	8×10^{12}	40000	
	$\frac{\pi}{36}$ 2 $\frac{\pi^2}{9}$	111.42/39.30/170.05	60-240-480	0.01	8×10^{12}	40000	
	$\frac{\pi}{36}$ $\frac{2}{36}$ $\frac{5\pi}{36}$	109.65/40.54/177.41 107.82/43.03/186.09	60-240-480	0.01	8×10^{12}	40000	
	$\frac{\pi}{36}$ 2 $\frac{\pi}{6}$	107.02/13.03/100.03	60-240-480	0.01	8×10^{12}	40000	
Tropical cyclone: sensitivity to the	G6 QU	120.16/97.08/121.83	150-600-1200	0.005/0.0075/0. 01/0.015/0.02	=	=	
$\frac{\text{Smagorinsky}}{\text{coefficient }(C_s)}$	G6X4L2	113.24/40.23/166.00	60-240-480	0.005/0.0075/0. 01/0.015/0.02	8×10^{12}	40000	

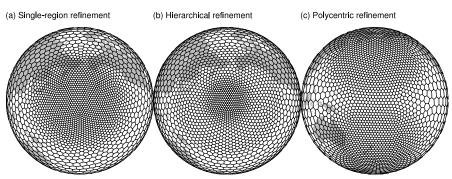


Figure 1: An illustration of the variable-resolution mesh (X4) based on three density functions: (a) single-region refinement, (b) hierarchical refinement, and (c) polycentric refinement. Throughout this paper, all land-sea outlines are only given for a spatial reference, and do not represent the geographical difference.

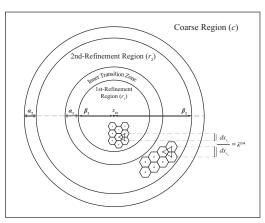


Figure 2: A schematic diagram of the hierarchical refinement mesh, illustrating the function of three parameters of the density function. α_1 and α_2 control the width of the transition zones; λ represents the inner densification ratio between the 1st-refinement and 2nd-refinement resolution regions; β_1 and β_2 control the coverage radius of the 1st-refinement and 2nd-refinement regions.

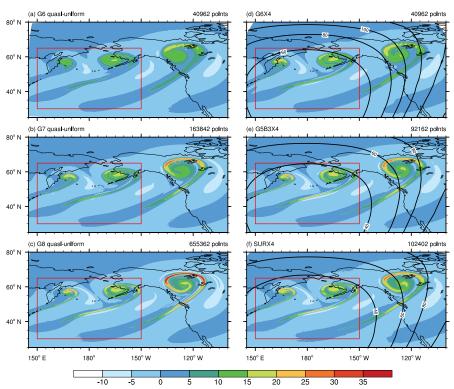


Figure 3: The relative vorticity $(10^{-5} \, s^{-1})$ field at the model level nearest to 850 hPa (level 24) after 10 days. The quasi-uniform (left-hand column) and variable-resolution (right-hand column) results are shown. The contour lines denote the mesh resolution (km). The vorticity is remapped from the raw triangular cell to the Voronoi cell using an area-weighted approach (true for all vorticity values shown in this study). Also see Figure S2 for the remapped QU-model solutions on a regular latitude–longitude grid. The red box denotes the region for regional kinetic energy analysis in Fig. 4. The contour lines denote the smoothed mesh cell sizes (km).

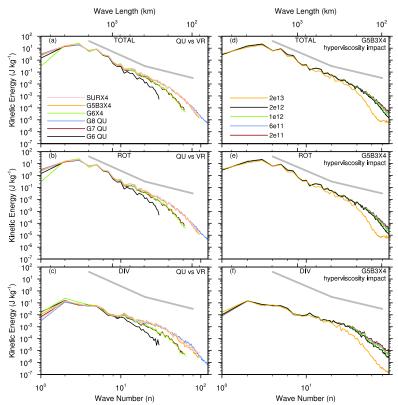


Figure 4: Baroclinic wave: horizontal regional kinetic energy spectra (unit: $J kg^{-1}$) at the model level nearest to 850 hPa on day 10, (a) total kinetic energy, (b) the rotational component, and (c) the divergence component. The results of the nonhydrostatic core are shown here, while the results for the hydrostatic core can be found in Fig. S2. The right-hand column (d)–(f) examines the impact of varying the hyperviscosity coefficient on spectra. The thick gray lines denote the -3 and -5/3 slopes, respectively.

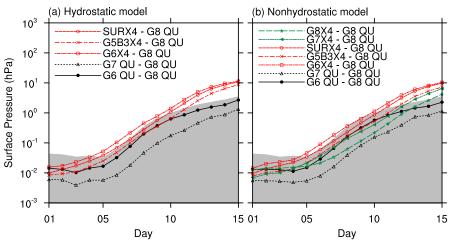


Figure 5: Baroclinic wave test: the l_2 error norms of surface pressure as a function of time for (a) the hydrostatic and (b) the nonhydrostatic dynamical core. The error is computed against the high-resolution quasi-uniform G8 mesh. The gray area denotes the uncertainty in the reference solutions, which selects the maximum l_2 error norms from four curves (HDC and NDC at G7 and G8 as four cases). Details can be found in Jablonowski and Williamson (2006).

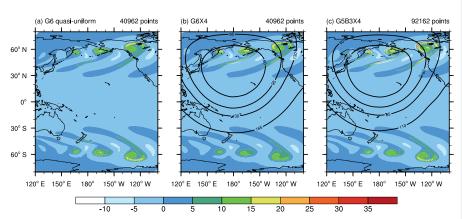


Figure 6: Adding a symmetrical perturbation in the Southern Hemisphere in the baroclinic wave test. The relative vorticity $(10^{-5} \, s^{-1})$ field at the model level nearest to 850 hPa on day 10 is shown for (a) quasi-uniform G6, (b) variable-resolution G6X4, and (c) G5B3X4 meshes. Only the nonhydrostatic core is used. The values in the Southern Hemisphere are substituted by their opposite values. The raw vorticity values on the triangular cell have been remapped to the Voronoi cell. The contour lines denote the smoothed mesh cell sizes (km).

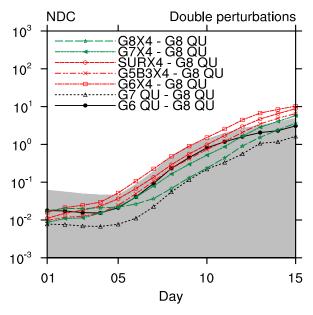


Figure 7 Same as Fig. 5, but for the baroclinic wave test with double perturbations, only for the nonhydrostatic core.

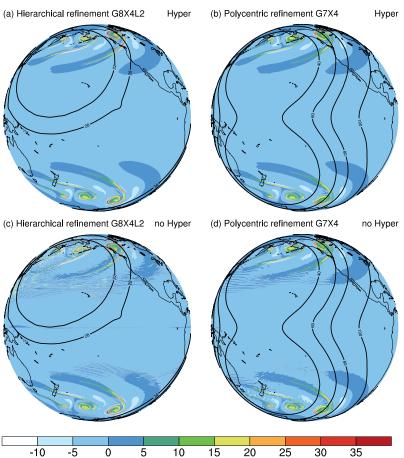


Figure 8: As in Fig. 6, but for two multi-region refinement meshes: (a) a hierarchical refinement style (G8X4L2) and (b) a polycentric refinement mesh based on G7X4. (c) (d) same as (a) (b), but for runs that turn off the hyperdiffusion option. The contour lines denote the smoothed mesh cell sizes (km). Note that the small kink in the 28 km contour of (a) (c) simply reflects that the generated mesh occasionally has higher local irregularities at some areas.

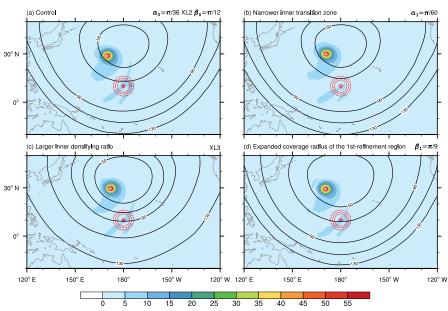


Figure 9: Idealized tropical cyclone test: the horizontal wind speed (m s⁻¹) at 850 hPa after 10 simulation days based on hierarchical refinement meshes with (a) the control, (b) reduced α_1 , and (c) higher λ for more rapid changes in the transition zone, and (d) larger β_1 to make the transition zone affect the tropical cyclone in an earlier stage. The red dashes denote the initial location of the tropical cyclone. The contour lines denote the smoothed mesh cell sizes (km).

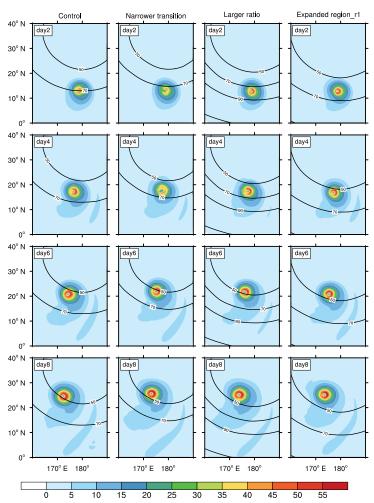


Figure 10: Corresponding to the four cases shown in Fig. 9, the simulation results on days 2, 4, 6, and 8 are shown to examine the movement of the tropical cyclones when they cross the mesh transition.

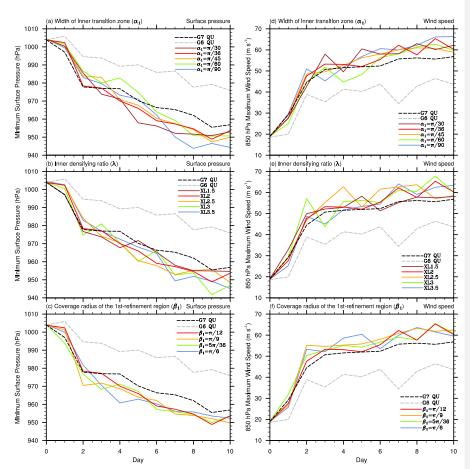


Figure 11 Idealized tropical cyclone test: temporal evolution of minimum surface pressure and maximum horizontal wind speed at 850 hPa based on the quasi-uniform G6 and G7 meshes, and the hierarchical refinement meshes by varying (a, d) α_1 , (b, e) λ , and (c, f) β_1 . When one parameter is altered, the other two parameters are fixed as in the control run ($\alpha_1 = \pi/36$, $\lambda = (1/2)^4$, and $\beta_1 = \pi/12$). The three mesh parameters control the width of the inner transition zone, the inner densification ratio, and the coverage radius of the 1st-refinement region.

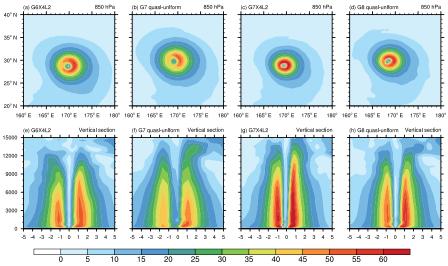
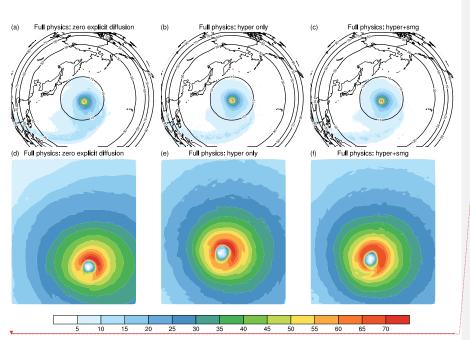
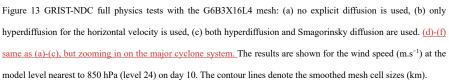
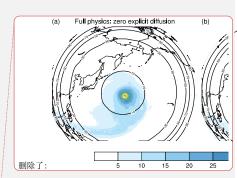


Figure 12: Idealized tropical cyclone test: (a–d) the horizontal wind speed (m s $^{-1}$) at 850 hPa after 10 simulation days based on quasi-uniform and variable-resolution meshes and (e–h) the corresponding vertical cross-section of the wind speed with a meridional range of ± 5 -degrees from the center of the tropical cyclone. The vertical coordinate of the cross-section denotes the height (m).







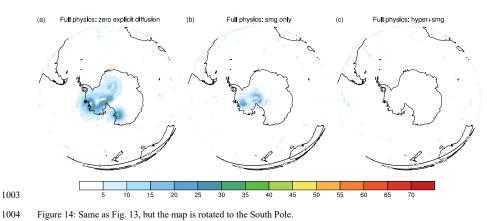


Figure 14: Same as Fig. 13, but the map is rotated to the South Pole.

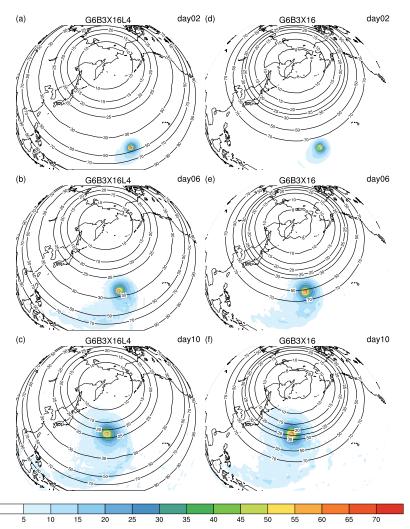


Figure 15: The same tests as in Fig. 13, but the refinement center is rotated to 60° N, 165° E. The left-hand column shows the results on days 2, 6, and 10 on the G6B3X16L4 mesh, the right-hand column shows the corresponding results on the G6B3X16 mesh. The results are shown for the wind speed (m.s⁻¹) at the model level nearest to 850 hPa (level 24).

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