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2 GTS v1.0: A Macrophysics Scheme for Climate Models Based on a Probability  
3 Density Function  
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29 Short title: Macrophysics for Climate Models

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31 Key points:

32 1) A cloud macrophysics scheme utilizing grid-mean hydrometeor information is  
33 developed and evaluated for climate models.

34 2) The GFS-TaiESM-Sundqvist (GTS) scheme can simulate variations of cloud fraction  
35 associated with relative humidity (RH) in a more consistent way than the default  
36 scheme of CAM5.3.

37 3) Through a better cloud–RH relationship, the GTS scheme helps to better represent  
38 cloud fraction, cloud radiative forcing, and thermodynamic-related climatic fields in  
39 climate simulations.

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42



43 Abstract

44 Cloud macrophysics schemes are unique parameterizations for general circulation  
45 models. We propose an approach based on a probability density function (PDF) that  
46 utilizes cloud condensates and saturation ratios to replace the assumption of critical  
47 relative humidity (RH). We test this approach, called the GFS-TaiESM-Sundqvist (GTS)  
48 scheme, using the macrophysics scheme within the Community Atmospheric Model  
49 version 5.3 (CAM5.3) framework. Via single-column model results, the new approach  
50 reveals a stronger linear relationship between the cloud fraction (CF) and RH when  
51 compared to that of the default CAM5.3 scheme. We also validate the impact of the  
52 GTS scheme on global climate simulations with satellite observations. The simulated  
53 CF is comparable to CloudSat/CALIPSO data. Comparisons of the vertical  
54 distributions of CF and cloud water content (CWC), as functions of large-scale dynamic  
55 and thermodynamic parameters, with the CloudSat/CALIPSO data suggest that the  
56 GTS scheme can closely simulate observations. This is particularly noticeable for  
57 thermodynamic parameters, such as RH, upper-tropospheric temperature, and total  
58 precipitable water, implying that our scheme can simulate variation in CF associated  
59 with RH more reliably than the default scheme. Changes in CF and CWC would affect  
60 climatic fields and large-scale circulation via cloud–radiation interactions. Both  
61 climatological means and annual cycles of many of the GTS-simulated variables are  
62 improved compared with the default scheme, particularly with respect to water vapor  
63 and RH fields. Different PDF shapes in the GTS scheme also significantly affect global  
64 simulations.

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68 1. Introduction

69

70 Global weather and climate models commonly use cloud macrophysics  
71 parameterization to calculate the sub-grid cloud fraction (CF) and/or large-scale cloud  
72 condensate, as well as cloud overlap, which is required in cloud microphysics and  
73 radiation schemes [Slingo, 1987; Sundqvist, 1988; Sundqvist *et al.*, 1989; Smith, 1990;  
74 Tiedtke, 1993; Xu and Randall, 1996; Rasch and Kristjansson, 1998; Jakob and Klein,  
75 2000; Tompkins, 2002; Zhang *et al.*, 2003; Wilson *et al.*, 2008a,b; Chabourea and  
76 Bechtold, 2012; Park *et al.*, 2014; Park *et al.*, 2016]. The largest uncertainty in climate  
77 prediction is associated with clouds and aerosols [Boucher *et al.*, 2013]. The large  
78 number of cloud-related parameterizations in general circulation models (GCM)  
79 contributes to this uncertainty. In recent years, an increasing amount of research has  
80 been devoted to unifying cloud-related parameterizations, for example by incorporating  
81 the planetary boundary layer, shallow and/or deep convections, and stratiform cloud  
82 (cloud macrophysics and/or microphysics) parameterizations, to improve cloud  
83 simulations in large-scale global models [Bogenschutz *et al.*, 2013; Park *et al.*, 2014a,  
84 2014b; Storer *et al.*, 2015].

85 Some of these parameterizations use prognostic approaches to parameterize the CF  
86 [Tiedtke, 1993; Tompkins, 2002; Wilson *et al.*, 2008a, b; Park *et al.*, 2016] while others  
87 use diagnostic approaches [Sundqvist *et al.*, 1989; Smith, 1990; Xu and Randall, 1996;  
88 Zhang *et al.*, 2003; Park *et al.*, 2014]. Most of the diagnostic approaches used in GCM  
89 cloud macrophysical schemes use the critical relative humidity threshold ( $RH_c$ ) to  
90 calculate CF [Slingo, 1987; Sundqvist *et al.*, 1989; Roeckner *et al.*, 1996]. In this type  
91 of parameterization, GCMs frequently use the  $RH_c$  value as a tunable parameter  
92 [Mauritsen *et al.*, 2012; Golaz *et al.*, 2013; Hourdin *et al.*, 2016]. There are some studies  
93 on the verification of global simulations focused on the cloud macrophysical  
94 parameterization [Hogan *et al.*, 2009; Franklin *et al.*, 2012; Qian *et al.*, 2012;  
95 Sotiropoulou *et al.*, 2015]. In addition, many model development studies show the  
96 impact of total water used in CF schemes on global simulations after modifying the  $RH_c$   
97 and/or the probability density function (PDF) [Donner *et al.*, 2011; Neale *et al.*, 2013;  
98 Schmidt *et al.*, 2014]. Some recent studies have attempted to constrain  $RH_c$  from  
99 regional sounding observations and/or satellite retrievals to improve regional and/or  
100 global simulations [Quaas, 2012; Molod, 2012; Lin, 2014].

101 While many variations of the diagnostic Sundqvist CF scheme have been proposed,  
102 most numerical weather prediction models and GCMs use the basic principle proposed  
103 by Sundqvist *et al.* [1989]: the changes in cloud condensate in a grid box are derived  
104 from the budget equation for RH. In the meantime, the amount of additional moisture  
105 from other processes is divided between the cloudy portion and the clear portion



106 according to the proportion of clouds determined using an assumed  $RH_c$ . While changes  
107 have been made to other parts of the Sundqvist scheme, the CF- $RH_c$  relationship still  
108 applies in most Sundqvist-based schemes. As highlighted by Thompkins [2005], the  
109  $RH_c$  value in the Sundqvist scheme can be related to the assumption of uniform  
110 distribution for the total water in an unsaturated grid box such that the distribution width  
111 ( $\delta c$ ) of the situation when a cloud is about to form is given by:

$$112 \quad \delta c = q_s(1 - RH_c), \quad (1)$$

113 where  $q_s$  is the saturated mixing ratio.

114 We re-derived this equation by describing the change in the distribution width  $\delta$  with  
115 grid-mean cloud condensates and saturation ratio using the basic assumption of uniform  
116 distribution from Sundqvist *et al.* [1989] rather than using the  $RH_c$ -derived  $\delta c$ , thereby  
117 eliminating unnecessary use of the  $RH_c$  while retaining the PDF assumption for the  
118 entire scheme. This modified macrophysics scheme is named the GFS-TaiESM-  
119 Sundqvist (GTS) scheme version 1.0 (GTS v1.0). It was first developed for the Global  
120 Forecast System (GFS) model at the National Centers for Environmental Protection  
121 (NCEP) and has been further improved for the Taiwan Earth System Model (TaiESM;  
122 Lee *et al.*, 2020) at the Research Center for Environmental Changes (RCEC), Academia  
123 Sinica. Park *et al.* [2014] discussed a similar approach wherein a triangular PDF was  
124 used to diagnose cloud liquid water as well as the cloud liquid fraction, and suggested  
125 that the PDF width could be computed internally rather than specified, to consistently  
126 diagnose both CF and cloud liquid water as in macrophysics. These authors also  
127 mentioned that such stratus cloud macrophysics could be applied across any horizontal  
128 and vertical resolution of a GCM grid, although they did not formally implement and  
129 test this idea using their scheme. Building upon their ideas, we implemented and tested  
130 this assumption with a triangular PDF in the GTS scheme.

131 In summary, this GTS scheme adopts Sundqvist's assumption regarding the partition  
132 of cloudy and clear regions within a model grid box but uses a variable PDF width once  
133 clouds are formed. It introduces a self-consistent diagnostic calculation of CF. Owing  
134 to their use of an internally computed PDF width, GTS schemes are expected to be able  
135 to better represent the relative variation of CF with RH in GCM grids.

136 A variety of assumptions regarding PDF shape can be adopted in diagnostic  
137 approaches [Sommeria and Deardorff, 1977; Bougeault, 1982; Smith, 1990; Tompkins,  
138 2002]. Some studies have investigated representing cloud condensate and water vapor  
139 in a more statistically accurate way by using more complex types of PDF to represent  
140 parameters such as total water, CF, and updraft vertical velocity [Larson, 2002; Golaz  
141 *et al.*, 2002; Firl, 2013; Bogenschutz *et al.*, 2012; Bogenschutz and Krueger, 2013; Firl  
142 and Randall, 2015]. In this study, we apply and investigate two simple and commonly  
143 used PDF shapes—uniform and triangular—in our parameterization of the GTS



144 macrophysics scheme. Other complex types of PDF assumptions can also be used if  
145 analytical solutions regarding the width of the PDF can be derived.

146 Most of the studies mentioned above estimate the CF via cloud liquid or total cloud  
147 water. Earlier versions of GCMs used a Slingo-type approach to resolve the cloud ice  
148 fraction [Slingo, 1987; Tompkins *et al.*, 2007; Park *et al.*, 2014]. On the other hand, the  
149 current generation of global models participating in the Coupled Model  
150 Intercomparison Project Phase 6 (CMIP6) have alternative approaches for the handling  
151 of CFs associated with ice clouds. In the GTS scheme, the approach to cloud liquid-  
152 water fraction parameterization is extended to the cloud ice fraction as well, wherein  
153 the saturation-mixing ratio ( $q_s$ ) with respect to water is replaced by  $q_s$  with respect to  
154 ice. This provides a consistent treatment for the cloud liquid and cloud ice fractions.  
155 Many studies have argued that the assumption of rapid adjustment between water vapor  
156 and cloud liquid water applied in GCM CF schemes cannot be applied to ice clouds  
157 [Tompkins *et al.*, 2007; Salzmann *et al.*, 2010; Chosson *et al.*, 2014]. In addition, it  
158 would be difficult to represent the CF of mixed-phase clouds using such an assumption  
159 [McCoy *et al.*, 2016]. Applying a diagnostic approach to the cloud ice fraction similar  
160 to that used for the cloud liquid fraction is indeed challenging and may result in a high  
161 level of uncertainty. To investigate this issue, we also conduct a series of sensitivity  
162 tests related to the super-saturation ratio assumption, which is applied when calculating  
163 the cloud ice fraction in the GTS scheme.

164

## 165 2. Descriptions of scheme, model, and simulation setup

166

### 167 2.1 Scheme descriptions

168 Figure 1 illustrates the PDF-based scheme with a uniform PDF and a triangular PDF  
169 of total water substance  $q_t$ . By assuming that the clear region is free of condensates and  
170 that the cloudy region is fully saturated, the cloudy region ( $b$ ) becomes the area where  
171  $q_t$  is larger than the saturation value  $q_s$  (shaded area). The PDF-based scheme  
172 automatically retains consistency between CF and condensates because it is derived  
173 from the same PDF. Here, we used the uniform PDF to demonstrate the relationship  
174 between  $RH_c$  and the width of the PDF. Using a derivation extended from Tompkins  
175 [2005]:

$$176 \quad b = \frac{1}{2\delta} (q_t + \delta - q_s). \quad (2)$$

177 It is evident that, with the uniform PDF:

$$178 \quad \delta_c = q_s(1 - RH_c). \quad (3)$$

179 Therefore,  $RH_c = 1 - \frac{\delta_c}{q_s}$ . Thus, if the width  $\delta$  of the uniform PDF is determined, then



180  $RH_c$  can be determined accordingly. This relation reveals that the  $RH_c$  assumption of  
181 the RH-based scheme actually assumes the width of the uniform PDF to be  $\delta c$  from the  
182 PDF-based scheme. As noticed by Thompkins [2005], the  $RH_c$  used by Sundqvist *et al.*  
183 [1989] for cloud generation can be linked to the statistical cloud scheme with a uniform  
184 distribution. Building upon this finding, we eliminated the assumption of  $RH_c$  by  
185 determining the  $P(q_t)$  with information about  $q_v$  and  $q_L$  provided by the base model.

186 In addition to the application of a PDF-based approach for liquid CF  
187 parameterization, the GTS scheme also uses the same concept for parameterizing the  
188 ice CF ( $b_i$ ) as follows:

$$189 \quad b_i = \frac{1}{2\delta} (\bar{q}_l + \bar{q}_v + \delta - sup * q_{si}), \quad (4)$$

190 where  $\bar{q}_l$ ,  $\bar{q}_v$ , and  $q_{si}$  denote the grid-mean cloud-ice mixing ratio, water-vapor mixing  
191 ratio, and saturation mixing ratio over ice, respectively. In equation (4),  $q_{si}$  is multiplied  
192 by a supersaturation factor ( $sup$ ) to account for the situation in which rapid saturation  
193 adjustment is not reached for cloud ice. In the present version of the GTS scheme,  $sup$   
194 is temporarily assumed to be 1.0. Sensitivity tests regarding  $sup$  will be discussed in  
195 Section 5.6.

196 A more complex PDF can be used for  $P(q_t)$  instead of the uniform distribution in  
197 our derivation. For example, the Community Atmospheric Model version 5.3 (CAM5.3)  
198 macrophysics model adopts a triangular PDF instead of a uniform PDF to represent the  
199 sub-grid distribution of the total water substance [Park *et al.*, 2014]. Mathematically,  
200 the triangular distribution is a more accurate approximation of the Gaussian distribution  
201 than the uniform distribution and it may also be more realistic. Therefore, we followed  
202 the same procedure to diagnose the CF by forming a triangular PDF with  $\bar{q}_l$ ,  $\bar{q}_v$ , and  
203  $\bar{q}_s$  provided. Moreover, by using a triangular PDF, we can obtain results that are more  
204 comparable with the CAM5.3 macrophysics scheme because the same PDF was used.  
205 By considering the PDF width, the CF ( $b$ ) and liquid water content ( $\bar{q}_l$ ) can be written  
206 as follows:

$$207 \quad b = \begin{cases} \frac{1}{2}(1 - s_s)^2 & \text{if } s_s > 0 \\ 1 - \frac{1}{2}(1 - s_s)^2 & \text{if } s_s < 0 \end{cases} \quad (5)$$

208 and:

$$209 \quad \frac{q_L}{\delta} = \begin{cases} \frac{1}{6} - \frac{s_s^2}{2} + \frac{s_s^3}{3} - s_s b \\ \frac{1}{6} - \frac{1}{6}(3s_s^2 - 2s_s^3) - s_s b \end{cases}, \quad (6)$$

210 respectively, where  $s_s = \frac{q_s - \bar{q}_l}{\delta}$ . From these two equations, we can derive the width of  
211 the triangular PDF and calculate the CF ( $b$ ) based on  $q_s$ ,  $q_t$ , and  $q_L$  instead of  $RH_c$ .



212 Notably, the PDF width for the total water substance can only be constrained when the  
213 cloud exists. Therefore, the  $RH_c$  is still required when clouds start to form from a clear  
214 region.

215 In this study, GTS schemes utilizing two different PDF shape assumptions are  
216 evaluated: uniform (hereafter, U\_pdf) and triangular (hereafter, T\_pdf). These two PDF  
217 types are specifically formulated to evaluate the effects of the choice of PDF shape. A  
218 triangular PDF is the default shape used for cloud macrophysics by the Community  
219 Atmospheric Model version 5.3 (CAM5.3; hereafter, the Park scheme). The T\_pdf of  
220 the GTS scheme is numerically similar to that of the Park scheme except for using a  
221 variable width for the triangular PDF once clouds are formed.

222

## 223 2.2 Model description and simulation setup

224 The GTS schemes described in this study were implemented into CAM5.3 in the  
225 Community Earth System Model version 1.2.2 (CESM 1.2.2), which is developed and  
226 maintained by DOE UCAR/NCAR. Physical parameterizations of CAM5.3 include  
227 deep convection, shallow convection, macrophysics, aerosol activation, stratiform  
228 microphysics, wet deposition of aerosols, radiation, a chemistry and aerosol module,  
229 moist turbulence, dry deposition of aerosols, and dynamics. References for the  
230 individual physical parameterizations can be found in the NCAR technical notes [Neale  
231 *et al.*, 2010]. The master equations are solved on a vertical hybrid pressure–sigma  
232 coordinate system (30 vertical levels) using the finite-volume dynamical core option of  
233 CAM5.3.

234 We conducted both the single-column tests and stand-alone global-domain  
235 simulations with CAM5.3 physics. The single-column setup provides the benefit of  
236 understanding the responses of physical schemes under environmental forcing of  
237 different regimes of interest. Here, we adopt the case of Tropical Western Pacific–  
238 International Cloud Experiment (TWP-ICE), which was supported by the ARM  
239 program of the Department of Energy and the Bureau of Meteorology of Australia from  
240 January to February 2006 over Darwin in Northern Australia. Based on the  
241 meteorological conditions, the TWP-ICE period can be divided into four shorter periods:  
242 the active monsoon period (19–25 January), the suppressed monsoon period (26  
243 January to 2 February), the monsoon clear-sky period (3–5 February), and the monsoon  
244 break period (6–13 February, May *et al.* [2008]; Xie *et al.* [2010]). To take advantage  
245 of previous studies of cloud-resolving models and single-column models, we followed  
246 the setup of Franklin *et al.* [2012] to initiate the single-column runs starting on 19  
247 January, 2006, and running for 25 days.

248 Stand-alone CAM5.3 simulations of the CESM model, forced by climatological sea  
249 surface temperature for the year 2000 (*i.e.*, CESM compset: F\_2000\_CAM5), are





250 conducted to demonstrate global results. The horizontal resolution of the CESM global  
251 runs is set at  $2^\circ$ . Individual global simulations are integrated for 12 years, and the output  
252 for the last 10 years is used to calculate climatological means and annual cycles in  
253 global means. Because we made changes largely with respect to CF, we also conducted  
254 corresponding simulations using the satellite-simulator approach to provide CF for a  
255 fair comparison with satellite CF products and typical CESM model output. This was  
256 done using the CFMIP Observation Simulator Package (COSP) built into CESM 1.2.2  
257 [Kay *et al.*, 2012]. In addition to the default monthly outputs, daily outputs of several  
258 selected variables are also written out for more in-depth analysis.

259

260

### 261 3. Observational datasets and offline calculations

262

#### 263 3.1 Observational data

264 Cloud field comparisons are critical for modifications to our system with respect to  
265 cloud macrophysical schemes. Therefore, we use the products from  
266 CloudSat/CALIPSO to provide CF and CWC data for evaluating the modeling  
267 capabilities of the default and modified GTS cloud macrophysical schemes.

268 In addition to cloud observations, observational radiation fluxes from CERES-EBAF  
269 are also used to investigate whether simulations using our system will improve radiation  
270 calculations for both shortwave and longwave radiation flux, as well as their  
271 corresponding cloud radiative forcings. Precipitation data are compared with Global  
272 Precipitation Climatology Project data and several other climatic parameters, *e.g.*, air  
273 temperature, RH, precipitable water, and zonal wind, are evaluated against the  
274 reanalysis data (ERA-Interim).

275 We further evaluate the performance of the three macrophysics schemes by using the  
276 approach of Su *et al.* [2013], which compares CF and CWC sorted by large-scale  
277 dynamical and thermodynamic parameters. The CF products are based on the 2B-  
278 GEOPROF R04 dataset [Marchand *et al.*, 2008], while the CWC data are based on the  
279 2B-CWC-RO R04 dataset [Austin *et al.*, 2009]. The methodology from Li *et al.* [2012]  
280 is used to generate gridded data. Four years of CloudSat/CALIPSO data, from 2007 to  
281 2010, are used to carry out the statistical analyses. These data are used to obtain overall  
282 climatological means to compare to those obtained from model simulations instead of  
283 undergoing rigorous year-to-year comparisons between observations and simulations.  
284 Monthly data from ERA-Interim for the same four years are used to obtain the  
285 dynamical and thermodynamic parameters used in Su *et al.*'s approach. These  
286 parameters include large-scale vertical velocity at 500 mb and RH at several vertical  
287 levels.



288

### 289 3.2 Offline calculation of cloud fraction

290 To evaluate the impact of assumptions of CF distributions for the RH- and PDF-  
291 based schemes, we conducted offline calculations of the CF by using the reanalyzed  
292 temperature, humidity, and condensate data from ERA-Interim. As the differences in  
293 CF characteristics do not change from month to month, the results for July are shown  
294 in Figure 2 as an example. The ERA-Interim reanalysis performed by Dee *et al.* [2011]  
295 using a  $0.75^\circ$  resolution from 1979 to 2012 is used in the calculation. With this offline  
296 approach, we can observe the impacts of these macrophysics assumptions with a  
297 balanced atmospheric state provided by the reanalysis.

298 Overall, the geographical distributions from the two GTS schemes are similar to that  
299 of the ERA-Interim reanalysis shown in Figure 2. In July, high clouds corresponding to  
300 deep convection are shown over South and East Asia where monsoons prevail. The  
301 diagnosed clouds of the GTS scheme have a maximum level of 125 hPa, which is  
302 consistent with those of the ERA-Interim reanalysis, but also have a more extensive  
303 cloud coverage of up to 90%. Below the freezing level at approximately 500 hPa, the  
304 CF diagnosed by the GTS scheme is comparable with that diagnosed by ERA-Interim  
305 reanalysis. The most substantial differences in CF between the GTS scheme and the  
306 ERA-Interim are observed in the mixed-phase clouds, such as the low clouds over the  
307 Southern and Arctic Oceans. Such differences suggest that more complexity in  
308 microphysics assumptions may be needed to describe the large-scale balance of mixed-  
309 phase clouds. The diagnosed CF for the Park macrophysics scheme is also shown in the  
310 right column of Figure 2. We found that the cloud field diagnosed by the Park  
311 macrophysics scheme was considerably different from that diagnosed by ERA-Interim  
312 reanalysis and the GTS schemes. The Park scheme diagnosed overcast high clouds of  
313 100–125 hPa with coverage of up to 100% over the warm pool and Intertropical  
314 Convergence Zone, but very little cloud coverage below 200 hPa, suggesting that the  
315 assumptions of the Park scheme are probably not suitable for large-scale states of the  
316 ERA-Interim reanalysis.

317 However, such a calculation does not account for the feedback of the clouds to the  
318 atmospheric states through condensation or evaporation and cloud radiative heating.  
319 Therefore, we further extended our single-column CAM5.3 experiments to examine the  
320 impact of the cloud PDF assumption.

321

322

### 323 4. Single-column results

324 This section presents the analysis of single-column simulations using the TWP-ICE  
325 field campaign. We focused on the CF fields and humidity fields, and their relation to



326 each other, to see how the  $RH_c$  assumption affects these features through humidity  
327 partitioning. Three sets of model experiments were conducted. In addition to the T\_pdf  
328 of the GTS and Park schemes, we also include the T\_pdf of the GTS scheme with the  
329 Slingo ice CF parameterization. This experiment can help us to interpret the impacts of  
330  $RH_c$  on liquid and ice CFs separately.

331 Figure 3 shows the correlation between CF and RH for the three time periods during  
332 the TWP-ICE. As expected, the correlation coefficients are quite similar for the  
333 individual schemes during the active monsoon period when convective clouds  
334 dominated ( $R = 0.688$ , Park, vs.  $0.698$ , T\_pdf). In contrast, the correlation coefficient  
335 between CF and RH differs during the suppressed monsoon period when stratiform  
336 clouds dominated ( $R = 0.510$ , Park, vs.  $0.728$ , T\_pdf). The correlation coefficient  
337 between CF and RH is approximately 20% higher for the stratiform-cloud-dominated  
338 period when using T\_pdf in the GTS scheme. It is also worth mentioning that, during  
339 the monsoon break period when both convective and stratiform clouds co-exist, the  
340 usage of the GTS scheme can also increase the correlation between CF and RH by 10%  
341 compared to the default Park scheme. The higher correlation coefficient for stratiform-  
342 cloud-dominated areas also suggests that the GTS scheme can somehow better simulate  
343 the variation of CF associated with RH, for which stratiform cloud macrophysics  
344 parameterization normally takes effect in CAM5.3.

345 Comparisons between T\_pdf with the Slingo ice CF and the Park scheme can be used  
346 to examine the role of applying a PDF-based approach in simulating the liquid CF in  
347 the GTS scheme. The use of a PDF-based approach for calculating the liquid CF can  
348 increase the correlation between CF and RH by approximately 13% during the  
349 suppressed monsoon period ( $R = 0.637$ , T\_pdf with Slingo, vs.  $0.51$ , Park). Such an  
350 outcome also suggests that implementing a PDF-based approach for liquid clouds can  
351 lead to more reasonable fluctuations between CF and RH in GCM grids.

352 It turns out that using the PDF-based approach for ice clouds also contributes to the  
353 increased correlation between CF and RH by approximately 10%, as shown in Figure  
354 3 with the T\_pdf scheme ( $R = 0.637$ , T\_pdf with Slingo, vs.  $0.728$ , T\_pdf). Such results  
355 also suggest that extending this PDF-based approach for ice clouds can better simulate  
356 changes in the cloud ice fraction using an RH-based approach rather than an  $RH_c$ -based  
357 approach. Such pair comparisons (*i.e.*, T\_pdf with Slingo cloud ice fraction scheme vs.  
358 T\_pdf and vs. Park) also reveal the important features of the GTS scheme, such as how  
359 variations in both the ice and liquid CF are better correlated with changes in RH of the  
360 GCM grids when compared to that of the default cloud macrophysics scheme.

361 Figure 4 shows scatter plots of RH and CF between 50 and 300 hPa determined from  
362 observations [Xie *et al.*, 2010] and simulated by models run for the suppressed monsoon  
363 period from the TWP-ICE case. It is evident that the relationship between CF and RH



364 appears to be more linear using the  $T_{pdf}$  of the GTS scheme as shown in Figure 4(c)  
365 when compared to the default Park scheme (Figure 4(b)). Moreover, the CF-RH  
366 distributions simulated by the GTS scheme are also closer to those of the observational  
367 results except under more overcast conditions (*i.e.*,  $RH > 70\%$  and  $RH > 110\%$ ). Similar  
368 to the results shown in Figure 3, the role of a PDF-based treatment of CF for the liquid  
369 CF can increase the degree of linearity between CF and RH (Figures 4(b) vs. 4(d)). On  
370 the other hand, by excluding PDF-based treatment for the cloud ice fraction in the GTS  
371 scheme, a more obvious spread in the CF-RH distribution is produced (comparing  
372 Figures 4(c) and 4(d)). In other words, results from the paired comparisons shown in  
373 Figure 4 are consistent with features shown in Figure 3, suggesting that applying a PDF-  
374 based treatment for both liquid and ice CF parameterization can indeed increase the  
375 linearity between CF and RH simulated by GCMs.

376

377

## 378 5. Global-domain results

### 379 5.1 Impacts on cloud fields

#### 380 a. Cloud fraction

381 In Figure 5, total CF simulated by the GTS schemes and the CESM default cloud  
382 macrophysics scheme, obtained from the COSP satellite simulator of the AMWG  
383 package of NCAR CESM, are compared with the total CF in CALIPSO-GOCCP. Both  
384 global mean and root-mean-square error (RMSE) values are improved by applying  
385  $U_{pdf}$  in the GTS scheme. The CF simulation resulting from the use of  $U_{pdf}$  in the  
386 GTS scheme is qualitatively similar to that of CloudSat/CALIPSO, especially over the  
387 mid- and high-latitude regions and for the annual and December-January-February  
388 (DJF) simulations (Figure 6). On the other hand, the results of the Park scheme in the  
389 tropics show clouds at higher altitudes than either  $U_{pdf}$  or  $T_{pdf}$ , in closer agreement  
390 with CloudSat/CALIPSO. Cross-section comparison of the zonal height shows that the  
391 CF simulation using  $U_{pdf}$  and  $T_{pdf}$  in the GTS scheme agrees better with that of  
392 CloudSat/CALIPSO than that produced by Park under most scenarios (globally, within  
393  $60^\circ N$ – $60^\circ S$ , and within  $30^\circ N$ – $30^\circ S$ ), especially for the annual and DJF simulations  
394 (Table 1). In contrast, some scenarios show lower RMSEs when the Park scheme is  
395 used, *e.g.*, for the June-July-August (JJA) season globally, within  $30$ – $90^\circ N$ , and within  
396  $30$ – $90^\circ S$ . Interestingly, when high latitudes are included (*i.e.*,  $30$ – $90^\circ N$  and  $30$ – $90^\circ S$ ),  
397  $U_{pdf}$  still results in the smallest RMSE values, except for during the JJA season.

398 We also compared the annual latitude–longitude distributions of CF at different  
399 specific pressure levels (Figure 7). The use of  $U_{pdf}$  resulted in a CF simulation  
400 relatively similar to that of CloudSat/CALIPSO for mid-level clouds, *i.e.*,  $300$ – $700$  mb,  
401 particularly for the mid- and high latitudes. However, none of the CF parameterizations



402 are able to simulate stratocumulus clouds effectively, as revealed at the 850 and 900 mb  
403 levels. For high clouds, the GTS and Park schemes exhibit observable differences  
404 regarding the maximum CF level. Table 2 summarizes the RMSE values for the  
405 latitude–longitude distribution of CFs at nine specific levels for the three schemes and  
406 CloudSat/CALIPSO for the annual, JJA, and DJF means. For the annual mean, U\_pdf  
407 results in the smallest RMSE at all levels except at 125 mb, for which the Park scheme  
408 yields the smallest RMSE (Table 2). For JJA, the Park scheme is closer to the  
409 observations aloft (100–200 mb) and nearest the surface (900 mb). For DJF, U\_pdf  
410 again performs best at most levels except 100 and 125 mb, for which T\_pdf is slightly  
411 better, while for JJA, U\_pdf is only best for most of the levels below 300 mb. Overall,  
412 U\_pdf in the GTS scheme results in better latitude–longitude CF distributions for 300–  
413 900 mb for the annual, DJF, and JJA means, suggesting improvements in CF simulation  
414 for middle and low clouds.

415 When annual, DJF, and JJA mean vertical CF profiles are averaged over the entire  
416 globe and between 30° N and 30° S, U\_pdf in the GTS scheme can produce a global  
417 simulation close to that of CloudSat/CALIPSO for 200–850 mb (Figure S3). In contrast,  
418 there is a large discrepancy between the simulated and observed CFs over the tropics.  
419 Although the GTS schemes can simulate CF profiles above 100 mb, the height of the  
420 maximum CF is lower than that of CloudSat/CALIPSO. In contrast, the height of the  
421 maximum CF simulated by the Park scheme is similar to that of CloudSat/CALIPSO  
422 but overestimated in CF. As before, when compared with CloudSat/CALIPSO, U\_pdf  
423 in the GTS scheme results in the smallest RMSE and the largest correlation coefficient  
424 of the three schemes, whether or not the lower levels are included except in JJA at 125  
425 mb, for which Park yields the smallest RMSE (Table 3). The reason for excluding the  
426 lower levels from the statistical results is that there may be a bias for low clouds  
427 retrieved by CloudSat due to radar-signal blocking by deep convective clouds.

428 The different degrees of changes for the global and tropical CFs can be attributed to  
429 the relative roles of cumulus parameterizations (both deep and shallow) and stratus  
430 cloud macrophysics/microphysics for the different latitudinal regions. It is expected that  
431 the GTS scheme can alter CF simulations in the mid- and high-latitude areas more than  
432 in the tropics because more stratiform clouds occur in those areas. It is also interesting  
433 to note that, although it is known that more convective clouds exist in the tropics (*i.e.*,  
434 the cumulus parameterization contributes more to the grid CF), the GTS scheme can  
435 also affect the CF simulation over the tropics to some extent. Such different responses  
436 in GCMs can be attributed to the degree of correlation between CF and RH for the  
437 different types of clouds, as shown in the single-column model simulations (Figure 3).  
438 This increase in the correlation coefficient between CF and RH is also evident in the  
439 global simulations shown in Figure 8, where the two selected grids in the tropics are



440 examined. It is clear that the correlation coefficient ( $R^2$ ) is approximately 20% higher  
441 for high clouds when applying T\_pdf or U\_pdf in the GTS scheme rather than using  
442 the default Park scheme ( $R^2 = 0.410$ , Park, vs. 0.652, T\_pdf, vs. 0.646, U\_pdf). An  
443 increase in linearity between CF and RH with regard to high clouds can also be seen  
444 for other latitudinal grids, as shown in Figures S1 and S2, especially for the high  
445 latitudinal grids (Figure S3,  $R^2 = 0.265$ , Park, vs. 0.656, T\_pdf, vs. 0.587, U\_pdf). As  
446 addressed in Section 4, this increase in the correlation coefficient between CF and RH,  
447 also seen in the global simulation results, is contributed by the application of the PDF-  
448 based approach for parameterizing both the liquid and ice CFs in the GTS scheme.

449

#### 450 b. Cloud fraction and cloud water content

451 In Figures 9 and 10, the distributions of CWC and CF as functions of large-scale  
452 vertical velocity at 500 mb ( $\omega_{500}$ ) or mean RH averaged between 300 and 1000 mb  
453 (RH300–1000) are evaluated against CloudSat/CALIPSO observations for 30° N–  
454 30° S and 60° N–60° S. Figures 9 and 10 show that the model simulations are all  
455 qualitatively more similar to each other than to the observations. Further statistical  
456 comparisons are shown in Table 4. It is encouraging to note that, in addition to the slight  
457 improvements in CF for both of these latitudinal ranges, the use of U\_pdf in the GTS  
458 scheme results in a CWC simulation that is more consistent with CloudSat/CALIPSO,  
459 whether it is plotted against  $\omega_{500}$  or RH300–1000. The RMSE and correlation  
460 coefficient (R) values in Table 4 confirm this. For global simulations, using U\_pdf also  
461 results in better agreement with CloudSat/CALIPSO for both CF and CWC when they  
462 are plotted against  $\omega_{500}$ , although for CWC plotted against RH300–1000, the Park  
463 scheme yields the smallest RMSE (Table 4). Overall, these comparisons yield results  
464 that are consistent with the general characteristics of most CMIP5 models, as found by  
465 Su *et al.* [2013]. GCMs in general simulate the distribution of cloud fields better with  
466 respect to a dynamical parameter as opposed to a thermodynamic parameter.

467 It is also worth noting that the use of U\_pdf yields a 20–30% improvement in R when  
468 plotted against RH300–1000 for the two latitudinal ranges, 30° N–30° S and 60° N–  
469 60° S. The observable improvement in a thermodynamic parameter is an indication of  
470 the uniqueness of this GTS scheme, in that it is capable of simulating the variation in  
471 cloud fields relative to that in RH fields. There are also slight improvements in cloud  
472 fields with respect to large-scale dynamical parameters. On the other hand, the Park  
473 scheme results in an approximately 20% improvement in R when plotted against  
474 RH300–1000 for the global domain, suggesting that the default Park scheme still  
475 simulates cloud fields better over the high latitudinal regions. It is thus worth addressing  
476 the likelihood that the different CF and CWC results for the different latitudinal ranges  
477 simulated using the GTS scheme induce cloud–radiation interactions distinct from



478 those simulated in the Park scheme. Such changes in cloud–radiation interactions would  
479 not only modify the thermodynamic fields but also the dynamic fields in the GCMs.  
480 These changes are in turn likely to affect the climate mean state and variability. We  
481 assess and compare these potential effects in the following subsection.

482

## 483 5.2 Effects on annual mean climatology

484 GTS schemes tend to produce smaller RMSE values for most of the global mean  
485 values of the radiation flux, cloud radiative forcing, and CF parameters shown in Table  
486 5, suggesting that the GTS scheme is capable of simulating the variability of these  
487 variables. Furthermore, the assumed U\_pdf shape appears to perform better for  
488 outgoing longwave radiation flux, longwave cloud forcing (LWCF), and CF at various  
489 levels, whereas the T\_pdf assumption is better for simulating net and shortwave  
490 radiation flux at the top of the atmosphere as well as shortwave cloud forcing (SWCF)  
491 (Table 5). On the other hand, the Park scheme is better for simulating clear-sky net  
492 shortwave radiation flux and precipitation. Smaller RMSE values can also be seen for  
493 parameters such as total precipitable water, total-column cloud liquid water, zonal wind  
494 at 200 mb (hereafter, U\_200), and air temperature at 200 mb (hereafter, T\_200) when  
495 U\_pdf of GTS is used. For global annual means, U\_pdf simulates net radiation flux at  
496 the top of the atmosphere, all- and clear-sky outgoing longwave radiation flux, and  
497 precipitable water as well as U\_200 and T\_200 in closer agreement with observations.  
498 In contrast, the Park scheme is better for simulating global mean variables such as net  
499 shortwave radiation flux at the top of the atmosphere, longwave cloud forcing, and  
500 precipitation. T\_pdf simulates SWCF closest to the observational mean.

501 Overall, the averaged RMSE values of the ten parameters are 0.97 and 0.96 for U\_pdf  
502 and T\_pdf, respectively, in the GTS schemes (Figure 11), suggesting that using the GTS  
503 schemes would result in global simulation performances more or less similar to those  
504 from the Park scheme. It is also worth noting that the biases in RH are smallest when  
505 U\_pdf in the GTS scheme is used (Table S1 of the supplementary material). In contrast,  
506 T\_pdf results in the smallest biases for SWCF, sea-level pressure, and ocean rainfall  
507 within 30° N–30° S. On the other hand, the Park scheme produces the smallest biases  
508 regarding mean fields such as LWCF, land rainfall within 30° N–30° S, Pacific surface  
509 stress within 5° N–5° S, zonal wind at 300 mb, and temperature.

510 Comparisons of latitude–height cross-sections of RH and ERA-Interim show that the  
511 GTS schemes tend to simulate RH values smaller than the default scheme does,  
512 especially for high-latitude regions (> 60° N and 60° S), as shown in Figure 12. In  
513 general, in terms of RH, using T\_pdf in the GTS scheme results in better agreement  
514 with ERA-Interim (Table 6). Figure 13 shows that the Park and T\_pdf schemes are  
515 wetter than ERA-Interim almost everywhere and that the uniform scheme is sometimes



516 drier. Table 7(a) further suggests that specific humidity simulated by the GTS schemes  
517 is slightly more consistent with ERA-Interim than the Park scheme. Comparisons of air  
518 temperature show that the three schemes tend to have cold biases almost everywhere.  
519 However, it is interesting to note that the cold biases are reduced to some extent while  
520 using the GTS schemes compared to the default scheme, as is evident in the smaller  
521 values of RMSE shown in Table 7(b). These effects on moisture and temperature are  
522 likely to result in changes in the annual cycle and seasonality of climatic parameters.  
523 Such observable changes in RH, clouds (both CF and CWC), and cloud forcing suggest  
524 that the GTS scheme will simulate cloud macrophysics processes in GCMs quite  
525 differently from the Park scheme, owing to the use of a variable-width PDF that is  
526 determined based on grid-mean information.

527

### 528 5.3 Changes in the annual cycle of climatic variables

529 Figure 14 shows the annual cycle of precipitable water simulated by the three  
530 schemes. The magnitude of precipitable water simulated by the GTS schemes is closer  
531 to the ERA-Interim data than the Park simulation is (Table 8). Interestingly, U\_pdf  
532 results in slightly better agreement with ERA-Interim than T\_pdf for the region 60° N–  
533 60° S. This implies that the GTS scheme would alter the moisture field for both RH and  
534 precipitable water in GCMs. These results are relatively more realistic with respect to  
535 both the moisture field and CF and CWC (Figures 9 and 10) and are likely to yield a  
536 more reasonable cloud–radiation interaction in the GCMs. It is therefore also worth  
537 examining any differences in dynamic fields, for example, in the annual U\_200 cycle,  
538 between the three schemes and the ERA-Interim data (Figure 15). Like the annual cycle  
539 of precipitable water, U\_200 simulated by the GTS schemes is closer to that of ERA-  
540 Interim than that simulated by the Park scheme, as supported by the smaller RMSE  
541 shown in Table 8. Furthermore, the U\_pdf assumption results in a better annual U\_200  
542 cycle than the T\_pdf assumption, especially for 60° N–60° S. This further supports the  
543 argument that this GTS scheme can effectively modulate global simulations, with  
544 respect to both thermodynamic and dynamical climatic variables.

545 Figure 16 displays the global mean annual cycles of several parameters simulated by  
546 the three schemes and the corresponding parameters from observational data. The GTS  
547 scheme simulations of total precipitable water (TMQ) are close to that of ERA-Interim;  
548 indeed, U\_pdf almost exactly reproduces the ERA-Interim TMQ. However, we must  
549 admit that such good agreement of the global mean is partly due to offsetting wet and  
550 dry differences from ERA-Interim. The GTS schemes also produce a more reasonable  
551 global mean annual cycle for outgoing longwave radiation (FLUT). It is probably due  
552 to the reduced CF simulated by the GTS scheme compared to the Park scheme even  
553 though the cloud top heights simulated by GTS are lower than observations in the





554 tropics. Interestingly, for SWCF, T\_pdf yields a simulation closer to the observations  
555 than the other two schemes, which is consistent with the features of the global annual  
556 mean of SWCF shown in Figure 11 and Table S1. However, for LWCF, the annual cycle  
557 simulated by Park is closest to the observations. The U\_pdf of the GTS scheme also  
558 results in improvements in U\_200 and T\_200 (Figure 16). The RMSEs for all of these  
559 comparisons confirm these results (Table 9).

560

#### 561 5.4 Changes in cloud–radiation interactions

562 As mentioned in Section 5.1, usage of the GTS cloud macrophysics schemes would  
563 affect the cloud fields, *i.e.*, CF and CWC. This, in turn, is likely to affect global  
564 simulations with respect to both mean climatology and the annual cycles of many  
565 climatic parameters (as discussed in Sections 5.2 and 5.3) through cloud–radiation  
566 interactions. Figure 17 compares CF, radiation heating rate (*i.e.*, longwave heating rate  
567 plus shortwave heating rate, hereafter QRL+QRS) and temperature trends due to moist  
568 processes (hereafter, DTCOND) for each pair-wise combination of the three schemes.  
569 Qualitatively consistent changes in CF are apparent for the GTS schemes, *e.g.*, an  
570 increase in the highest clouds over the tropics and a decrease below them, a decrease in  
571 150–400 mb clouds over the mid-latitudes, a decrease in 300–700 mb clouds over the  
572 high latitudes, an increase in 300–700 mb clouds over the tropics to mid-latitudes, and  
573 an increase in low clouds over the high-latitude regions. The GTS schemes also yield a  
574 significant increase in CF at atmospheric levels higher than 300 mb over the high-  
575 latitude regions (Figure 17). These changes affect the radiation calculations to some  
576 extent. In addition, CWC is also affected by the GTS schemes (Figures 9 and 10). The  
577 combined effects of the changes in CF and CWC are likely to result in changes in cloud–  
578 radiation interactions. In addition, although there are significant changes in CF at high  
579 atmospheric levels in the high-latitude regions, the combined effect of CF and CWC on  
580 QRL+QRS is quite small, owing to the low CWC values over this region. The changes  
581 in moisture processes, *i.e.*, DTCOND (Figure 17), also suggest that the combined  
582 effects of the changes in the thermodynamic and dynamical fields occur as a result of  
583 changes in cloud–radiation interactions within the GCMs from GTS schemes.

584 The bottom panel in Figure 17 shows the differences in CF, QRL+QRS, and  
585 DTCOND between the two GTS schemes. Relative to T\_pdf, U\_pdf simulates a greater  
586 CF for 300–1000 mb clouds within 60° N–60° S, but a smaller CF for all three cloud  
587 levels for the high-latitude regions. Furthermore, the CWC vertical cross-section also  
588 differs for the two GTS schemes (data not shown for limitations of space). Combining  
589 the changes in CF and CWC, the corresponding changes in QRL+QRS and DTCOND,  
590 particularly the increase of low clouds over the mid-latitude region, are clear with an  
591 obvious decrease of high clouds over the tropical to mid-latitude region.



592 Observable changes in large-scale circulations are likely, given the various changes  
593 in QRL+QRS and DTCOND resulting from applying different cloud macrophysics.  
594 Accordingly, both the mean and variability of the climate simulated by the GCMs differ  
595 among the three schemes, as shown in the previous subsections. These results  
596 emphasize the importance of improving cloud-related parameterization to provide  
597 better simulations of the cloud–radiation interaction within GCMs. Furthermore, as  
598 previously shown, the cloud–radiation interaction is highly sensitive to the assumptions  
599 of the CF parameterization used in the macrophysical scheme in the GCMs, even if  
600 there is only a small change in the CF parameterization. The uniqueness of the GTS  
601 scheme is in its application of a variable PDF width to calculate CF in the default PDF-  
602 based CF scheme of the CESM model. Further systematic experiments are necessary to  
603 improve our understanding of the sensitivity of the GTS scheme, and some are  
604 presented in Section 5.6.

605

606 5.5 Consistent changes in cloud radiative forcing, cloud fraction, and cloud condensates

607 Observable changes in clouds and radiation fluxes after adopting the GTS scheme  
608 were clearly shown in the previous subsections. It is thus worth examining features in  
609 cloud radiative forcings caused by the GTS scheme that produce such changes, as  
610 compared to those of the default Park scheme. Figure 18 shows the difference in total  
611 cloud fraction, SWCF, LWCF, CF, and averaged cloud water contents, as well as the  
612 averaged RH at the three levels i.e., 100–400, 400–700, and 700–1000 mb, derived  
613 from the  $T_{pdf}$  of GTS with the Park results subtracted. One can readily observe that  
614 changes in SWCF (Figure 18(b)) are quite consistent with those for total CF, showing  
615 a decrease in the total CF over the area within 30° N and 30° S with an increase  
616 everywhere else (Figure 18(a)). Such prominent changes in latitudinal distribution of  
617 SWCF can be further related to the changes in the low (Figure 18(e)) and middle (Figure  
618 18(f)) CFs particularly associated with low clouds.

619 On the other hand, changes in the high CF (Figure 18(d)) are also quite consistent  
620 with those in LWCF (Figure 18(c)), showing an overall decrease of high clouds  
621 especially over the tropical convection areas. As expected, changes in cloud water  
622 condensates (Figures 18(g)–(i)) are closely related to changes in the CF at the three  
623 levels except for the middle clouds. Therefore, according to the evidence shown in  
624 Figures 18(a)–(i), it is clear that use of the GTS scheme would cause significant changes  
625 in the spatial distribution of low, middle, and high clouds (both in CF and cloud water  
626 condensates) that would result in corresponding changes in cloud radiative forcings  
627 (both for SWCF and LWCF).

628 Surprisingly, changes in RH at the three levels (Figures 18(j)–(l)) are relatively less  
629 consistent with changes in the CF and condensates, especially for middle and low



630 clouds over the mid- and high-latitude areas. Such results also indicate that there are  
631 complicated factors accounting for changes in RH in the GCMs. We suggest that, in  
632 addition to the active roles of the GTS scheme in redistributing/modulating moisture  
633 between clouds (*i.e.*, cloud liquid or ice) and environment (water vapor) in GCM grids,  
634 thermodynamic and dynamical feedback resulting from cloud–radiation interactions  
635 also contribute to RH changes. At the present stage, we cannot quantify these individual  
636 contributions. More in-depth analysis is needed to unveil the detailed mechanisms of  
637 why GTS schemes tend to produce less low clouds over the tropics while more low  
638 clouds over the mid- and high latitudes compared to the default Park scheme, as well  
639 as observable changes regarding middle and high clouds.

640

#### 641 5.6 Uncertainty in GTS cloud fraction parameterization

##### 642 a. Assumption of PDF shape in the GTS scheme

643 In general, the simulations of CF, RH, and other parameters (*e.g.*, global annual mean  
644 and/or annual cycle) using the T\_pdf scheme that have been discussed and illustrated  
645 thus far have distribution features qualitatively and values quantitatively between those  
646 of the Park and U\_pdf schemes. In other words, the characteristics of the T\_pdf  
647 simulations are a combination of those from both the default Park scheme and the  
648 U\_pdf scheme. This is to be expected because there are fewer differences between the  
649 Park and T\_pdf schemes than between the Park and U\_pdf schemes in terms of cloud  
650 macrophysics parameterization. Since the shape of the PDF is triangular for both the  
651 Park and T\_pdf schemes, the only difference between these two is that T\_pdf has a  
652 variable PDF width that is based on the grid-mean mixing ratio of hydrometeors and  
653 the saturation ratio of the atmospheric environment, rather than the fixed-width function  
654 of  $RH_c$ . Even such a minor difference, however, can have an impact on both the  
655 thermodynamic and dynamical fields in global simulations. Our findings further  
656 suggest that the use of a variable PDF width to determine CF results in some changes  
657 in consistency between the RH and CF fields, as well as in the simulation of SWCF and  
658 net radiation flux at the top of atmosphere. As mentioned in Section 1, a diagnostic  
659 approach to determining the triangular PDF width of the default Park scheme can be  
660 used to refine the Park scheme [Appendix A of Park *et al.*, 2014]. This is effectively the  
661 same as using the GTS scheme with T\_pdf.

662 However, it is also evident that assuming a uniform PDF (*i.e.*, a rectangular shape)  
663 can have a larger effect on global simulations, as seen with our use of U\_pdf. It is  
664 interesting to note that the use of U\_pdf yields a smaller overall RMSE for many  
665 thermodynamic and dynamical fields than does the use of T\_pdf. This implies that a  
666 uniform distribution is probably more appropriate for the 2° horizontal resolution  
667 currently used in global simulations. The scale-dependence of the PDF shape is



668 certainly important to consider, as revealed in our comparisons between T\_pdf and  
669 U\_pdf, but this is beyond the scope of this paper. Furthermore, the possible dependence  
670 of PDF shape on specific cloud systems in different regions should also be examined  
671 using systematic tests and simulation designs.

672

#### 673 b. Uncertainty resulting from cloud-ice fraction parameterization

674 It is worth evaluating the possible uncertainty related to CF for cloud ice because the  
675 saturation adjustment assumption used for cloud liquid may not apply to cloud ice, as  
676 discussed in Section 1. We thus examine the sensitivity of the super-saturation values  
677 for the cloud ice fraction by multiplying by  $q_{si}$ , as shown in equation 4 by the constant  
678  $sup$ . Several values of  $sup$  are assumed for the cloud ice fraction in the GTS schemes  
679 with CF simulated using Slingo's approach to parameterization as used by Park *et al.*  
680 [2014] and are compared with the CloudSat/CALIPSO observational data (Figure S4).  
681 Both GTS schemes are sensitive to the  $sup$  value. For U\_pdf, CF decreases more-or-  
682 less linearly with increasing  $sup$  values, but there is no such clear linearity for T\_pdf,  
683 especially for  $sup$  values of 1.0000–1.0005. Interestingly, changing the  $sup$  value for  
684 the cloud ice fraction affects the cloud liquid fraction results for the scheme. We also  
685 find that the CF profile simulated by U\_pdf when  $sup = 1.0005$  is similar to that  
686 simulated using Slingo's approach to parameterization, especially for middle and low  
687 clouds. Based on these sensitivity tests, it is evident that the  $sup$  value used in the cloud  
688 ice fraction formulae of the GTS scheme can be regarded as a tunable parameter under  
689 the present cloud macrophysics and microphysics framework of the CESM model.  
690 When  $sup = 1.0$  in the GTS scheme with U\_pdf, the results are comparable to  
691 CloudSat/CALIPSO observations, while with T\_pdf, the  $sup$  value can be tuned  
692 between 1.0 and 1.005 to mimic the CloudSat/CALIPSO data (Figure S4). Thus, the  
693 results of GTS schemes are sensitive to the supersaturation threshold and suggest that  
694 it is still quite challenging to produce a reasonable parameterization for the cloud ice  
695 fraction, given the longer time-scales needed for ice clouds to reach saturation  
696 equilibrium.

697

#### 698 6. Conclusions

699 In this paper, we presented a macrophysics parameterization based on a probability  
700 density function (PDF) called the GFS-TaiESM-Sundqvist (GTS) cloud macrophysics  
701 scheme, which is based on Sundqvist's cloud macrophysics concept for global models  
702 and the recent modification of the cloud macrophysics in the NCAR CESM model by  
703 Park *et al.* [2014]. The GTS scheme especially excludes the assumption of a prescribed  
704 critical relative humidity threshold ( $RH_c$ ), which is included in the default cloud  
705 macrophysics schemes, by determining the width of the PDF based on grid



706 hydrometeors and saturation ratio.

707 We first used ERA-Interim reanalysis data to examine offline the validity of the  
708 relationship between cloud fraction (CF) and relative humidity (RH) based on the PDF  
709 assumption. Results showed that the GTS assumption better describes the large-scale  
710 equilibrium between CF and environment conditions. In a single-column model setup,  
711 we noticed several improved characteristics of the CF and humidity in the model  
712 simulation when the *ad hoc*  $RH_c$  assumptions were removed. First, the CF-RH  
713 relationship is more consistent in our modified scheme and an overall increase in  
714 linearity between CF and RH of approximately 20% was observed, especially for  
715 stratiform clouds. Second, according to the pair-wise comparisons shown and discussed  
716 in Figures 3 and 4, the use of PDF-based treatments for parameterizing both liquid and  
717 ice CFs in the GTS schemes contributed to the linear CF-RH relationship.

718 According to our detailed comparisons with observational cloud field data (CF and  
719 cloud water content (CWC)) from CloudSat/CALIPSO, GTS parameterization is able  
720 to simulate changes in CF that are associated with changes in RH in global simulations.  
721 Improvements with respect to the CF of middle clouds, the boreal winter, and mid- and  
722 high latitudes are particularly evident. Furthermore, examination of the vertical  
723 distributions of CF and CWC as a function of large-scale dynamical and  
724 thermodynamic parameters suggests that, compared to the default scheme, simulations  
725 of CF and CWC from the GTS scheme are qualitatively more consistent with the  
726 CloudSat/CALIPSO data. It is particularly encouraging to observe that the GTS scheme  
727 is also capable of substantially increasing the pattern correlation coefficient of CF and  
728 CWC as a function of a large-scale thermodynamic parameter (*i.e.*, RH300–1000).  
729 These effects appear to have a substantial impact on global climate simulations via  
730 cloud–radiation interactions.

731 The fact that CF and CWC simulated by the GTS scheme are temporally and spatially  
732 closer to those of the observational data suggests that not only the climatological mean  
733 but also the annual cycles of many parameters would be better simulated by the GTS  
734 cloud macrophysical scheme. Improvements with respect to thermodynamic fields such  
735 as upper-troposphere and lower-stratosphere temperature, RH, and total precipitable  
736 water were more substantial even than those in the dynamical fields. This was  
737 consistent with our comparisons based on the vertical distribution of CF and CWC as  
738 functions of large-scale dynamical and thermodynamic forcing. Interestingly, the GTS  
739 scheme results in observable changes in the annual cycle of zonal wind at 200 hPa,  
740 which suggests that the modification of thermodynamic fields resulting from changes  
741 in cloud–radiation interactions will, in turn, reciprocally affect the dynamical fields.  
742 Accordingly, it is worth investigating possible changes in large-scale circulation,  
743 monsoon evolution, and short- and long-term climate variability in future research.



744 GTS schemes can simulate spatial distributions of cloud radiative forcings (both for  
745 shortwave and longwave) quite differently compared to the default Park scheme.  
746 Changes in cloud radiative forcings are very consistent with different latitudinal  
747 changes in CF and cloud water condensates at the three cloud levels. The most  
748 important feature of the GTS scheme is that CF is self-consistently determined based  
749 on hydrometeors and the environmental information in the model grid box in the  
750 general circulation model (GCM) simulation. In contrast to the prescribed vertical  
751 profile of  $RH_c$  used in many current GCMs, the width of the PDF in the GTS scheme is  
752 variable and calculated in a diagnostic way. A fixed  $RH_c$  is thus no longer used once  
753 clouds are formed. This feature also potentially makes the GTS scheme a candidate  
754 macrophysics parameterization for use in modern global weather forecasting and  
755 climate prediction models as it better simulates the CF-RH relationship. However,  
756 further efforts are required to develop a more meaningful and physical way to  
757 parameterize the super-saturation ratio assumption applied to the cloud ice fraction in  
758 the GTS scheme, and to investigate why a uniform PDF in the GTS scheme performs  
759 better overall than the triangular PDF.

760  
761

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955 Code availability

956 The codes of the GTS scheme used in this study can be obtained from the following  
957 website:

958 <https://doi.org/10.5281/zenodo.3626654>

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961 Author contributions. HHH is the initiator and primary investigator of the TaiESM  
962 project. CJS developed code and wrote the majority of the paper. YCW also developed  
963 code and wrote part of the paper. WTC helped process CloudSat/CALIPSO satellite  
964 data. HLP and RS helped develop the theoretical basis of the GTS scheme. YHC helped  
965 with the off-line calculations. CAC helped with most of the visualizations.

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968 Competing interests. The authors declare that they have no conflict of interest.

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**Table 1.** Root-mean-square errors (RMSE) for comparisons of latitude–height cross-sections of CF among the three macrophysical schemes (Park: default scheme; T\_pdf: triangular PDF in the GTS scheme; U\_pdf: uniform PDF in the GTS scheme) and observational data from CloudSat/CALIPSO (Figure 6). Comparisons are made of the means for five latitudinal ranges and three periods (JJA: June, July, August; DJF: December, January, February). The smallest RMSE value of the three schemes in each case is bold and underlined.

	Global			60°N~60°S			30°N~30°S			30°N~90°N			30°S~90°S		
	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf
Annual	7.15	8.27	<b><u>6.75</u></b>	5.25	<b><u>4.53</u></b>	4.85	5.84	5.37	<b><u>5.05</u></b>	8.78	10.40	<b><u>8.52</u></b>	6.46	8.29	<b><u>6.18</u></b>
JJA	<b><u>7.40</u></b>	11.30	9.50	6.27	5.64	<b><u>5.61</u></b>	6.03	5.96	<b><u>5.56</u></b>	<b><u>8.91</u></b>	10.60	9.13	<b><u>6.93</u></b>	15.50	12.70
DJF	9.04	9.37	<b><u>6.99</u></b>	5.62	<b><u>5.24</u></b>	5.38	6.29	5.53	<b><u>5.36</u></b>	12.80	13.00	<b><u>10.00</u></b>	6.33	7.85	<b><u>3.82</u></b>

**Table 2.** RMSEs for comparisons between CF at nine pressure levels, as simulated by the three macrophysical schemes (Park, T\_pdf, U\_pdf) and observational data from CloudSat/CALIPSO (Figure 7). The comparisons are made for three periods (JJA: June, July, August; DJF: December, January, February). The smallest RMSE value of the three schemes in each case is bold and underlined.

	Annual			JJA			DJF		
	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf
100 mb	6.07	5.40	<b><u>4.71</u></b>	<b><u>4.85</u></b>	12.70	10.10	7.88	<b><u>3.94</u></b>	4.20
125 mb	<b><u>4.70</u></b>	5.56	4.80	<b><u>6.13</u></b>	12.60	10.10	5.96	<b><u>4.56</u></b>	4.81
200 mb	7.23	8.34	<b><u>6.78</u></b>	<b><u>9.80</u></b>	14.90	11.90	8.64	6.57	<b><u>6.46</u></b>
300 mb	10.80	9.63	<b><u>7.98</u></b>	11.60	12.90	<b><u>10.80</u></b>	12.40	11.70	<b><u>9.06</u></b>
400 mb	11.80	10.50	<b><u>6.93</u></b>	12.40	10.50	<b><u>9.55</u></b>	12.70	13.90	<b><u>8.06</u></b>
500 mb	11.00	11.50	<b><u>7.65</u></b>	11.90	10.60	<b><u>9.28</u></b>	11.70	13.40	<b><u>8.50</u></b>
700 mb	8.64	9.47	<b><u>8.19</u></b>	9.63	10.80	<b><u>9.46</u></b>	10.70	11.10	<b><u>9.41</u></b>
850 mb	14.30	14.20	<b><u>12.00</u></b>	14.80	15.40	<b><u>12.80</u></b>	16.10	15.30	<b><u>13.20</u></b>
900 mb	12.50	15.10	<b><u>12.30</u></b>	<b><u>13.30</u></b>	16.60	13.60	15.10	16.40	<b><u>12.90</u></b>



**Table 3.** RMSEs and correlation coefficients (R, in brackets) for comparisons between the vertical CF profiles simulated by the three macrophysical schemes (Park, T\_pdf, U\_pdf) and observational data from CloudSat/CALIPSO (Figure S3). Comparisons are made for three periods (JJA: June, July, August; DJF: December, January, February) and two latitudinal ranges. The smallest RMSE value of the three schemes in each case is bolded and underlined.

		Global			30°N~30°S		
		Park	T_pdf	U_pdf	Park	T_pdf	U_pdf
Including low levels	Annual	8.03 (0.83)	9.51 (0.86)	<b><u>7.92</u></b> (0.87)	6.15 (0.60)	6.03 (0.53)	<b><u>5.38</u></b> (0.59)
	JJA	<b><u>8.58</u></b> (0.81)	11.52 (0.85)	9.66 (0.85)	6.61 (0.61)	6.06 (0.54)	<b><u>5.87</u></b> (0.62)
	DJF	9.14 (0.81)	10.20 (0.85)	<b><u>7.92</u></b> (0.86)	6.31 (0.59)	6.65 (0.52)	<b><u>5.60</u></b> (0.57)
Excluding low levels	Annual	5.97 (0.91)	6.51 (0.96)	<b><u>5.32</u></b> (0.99)	5.89 (0.63)	5.75 (0.51)	<b><u>5.13</u></b> (0.55)
	JJA	<b><u>6.60</u></b> (0.92)	9.39 (0.97)	7.72 (0.98)	6.13 (0.63)	6.22 (0.49)	<b><u>5.55</u></b> (0.58)
	DJF	6.05 (0.92)	6.76 (0.95)	<b><u>4.85</u></b> (0.99)	6.20 (0.60)	5.93 (0.49)	<b><u>5.45</u></b> (0.52)

**Table 4.** (a) RMSE and (b) R values for comparisons between CF and CWC simulated by the three macrophysical schemes (Park, T\_pdf, and U\_pdf) and plotted against vertical velocity at 500 mb ( $\omega_{500}$ ) or averaged RH for 300–1000 mb (RH300–1000, obtained from the ERA-Interim reanalysis) and observational data from CloudSat/CALIPSO (Figures 9 and 10). The comparisons are made for three latitudinal ranges. The smallest RMSE or largest R value of the three schemes in each case is bolded and underlined.

(a)

RMSE		Global			60°N~60°S			30°N~30°S		
		Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf
OMEGA@500 mb	CWC	11.10	10.90	<b><u>9.83</u></b>	11.40	11.20	<b><u>10.10</u></b>	14.10	13.80	<b><u>12.50</u></b>
	CF	7.65	7.26	<b><u>6.13</u></b>	7.55	7.23	<b><u>6.24</u></b>	8.13	8.07	<b><u>7.21</u></b>
RH@300-1000 mb	CWC	<b><u>8.73</u></b>	9.69	11.60	13.50	15.10	<b><u>11.80</u></b>	19.10	18.00	<b><u>12.00</u></b>
	CF	17.90	18.30	<b><u>13.90</u></b>	15.40	17.30	<b><u>12.70</u></b>	18.80	18.30	<b><u>12.90</u></b>

(b)

R		Global			60°N~60°S			30°N~30°S		
		Park	T_pdf	U_pdf	Park	T_pdf	U_pdf	Park	T_pdf	U_pdf
OMEGA@500 mb	CWC	0.73	0.77	<b><u>0.80</u></b>	0.74	0.77	<b><u>0.80</u></b>	0.60	0.66	<b><u>0.74</u></b>
	CF	0.84	0.85	<b><u>0.89</u></b>	0.85	0.85	<b><u>0.88</u></b>	0.83	0.82	<b><u>0.84</u></b>
RH@300-1000 mb	CWC	<b><u>0.64</u></b>	0.54	0.45	0.44	0.34	<b><u>0.62</u></b>	0.22	0.25	<b><u>0.55</u></b>
	CF	0.31	0.40	<b><u>0.59</u></b>	0.51	0.46	<b><u>0.68</u></b>	0.45	0.45	<b><u>0.66</u></b>



**Table 5.** Global annual means (Mean) and RMSE values for comparisons with the observed values (Obs) for a selection of climatic parameters simulated by the three cloud macrophysical schemes (Park, T\_pdf, and U\_pdf). The smallest RMSE value or closest global mean of the three schemes in each case is bolded and underlined.

Parameters	Obs	Mean (Park)	Mean (T_pdf)	Mean (U_pdf)	RMSE (Park)	RMSE (T_pdf)	RMSE (U_pdf)
RESTOA_CERES-EBAF	0.81	4.18	3.25	<b><u>-1.06</u></b>	12.39	<b><u>10.43</u></b>	11.11
FLUT_CERES-EBAF	239.67	234.97	237.88	<b><u>238.14</u></b>	8.78	6.73	<b><u>6.50</u></b>
FLUTC_CERES-EBAF	265.73	259.06	259.65	<b><u>260.45</u></b>	7.55	7.12	<b><u>6.48</u></b>
FSNTOA_CERES-EBAF	240.48	<b><u>239.15</u></b>	241.14	237.08	13.97	<b><u>11.64</u></b>	12.79
FSNTOAC_CERES-EBAF	287.62	<b><u>291.26</u></b>	291.31	291.70	<b><u>7.08</u></b>	7.09	7.58
LWCF_CERES-EBAF	26.06	<b><u>24.10</u></b>	21.77	22.31	6.78	6.77	<b><u>6.21</u></b>
SWCF_CERES-EBAF	-47.15	-52.11	<b><u>-50.18</u></b>	-54.61	15.98	<b><u>12.90</u></b>	15.43
PRECT_GPCP	2.67	<b><u>2.97</u></b>	3.04	3.14	<b><u>1.09</u></b>	1.10	1.15
PREH2O ERAI	24.25	25.64	24.90	<b><u>24.45</u></b>	2.56	2.05	<b><u>2.03</u></b>
CLDTO_Cloudsat+CALIPSO	66.82	<b><u>64.11</u></b>	70.77	70.09	9.87	11.38	<b><u>9.76</u></b>
CLDHGH_Cloudsat+CALIPSO	40.33	38.17	44.79	<b><u>40.22</u></b>	9.37	9.28	<b><u>8.17</u></b>
CLDMED_Cloudsat+CALIPSO	32.16	27.22	30.41	<b><u>31.26</u></b>	8.03	6.95	<b><u>6.28</u></b>
CLDLOW_Cloudsat+CALIPSO	43.01	<b><u>43.63</u></b>	43.67	46.19	<b><u>12.78</u></b>	18.06	16.17
CLDTOT_CALIPSO GOCCP	67.25	56.43	55.45	<b><u>61.72</u></b>	14.38	15.37	<b><u>10.28</u></b>
CLDHGH_CALIPSO GOCCP	32.04	<b><u>25.57</u></b>	22.48	24.46	<b><u>9.04</u></b>	11.30	10.16
CLDMED_CALIPSO GOCCP	18.09	11.21	14.55	<b><u>18.19</u></b>	8.35	6.34	<b><u>6.02</u></b>
CLDLOW_CALIPSO GOCCP	37.95	33.24	33.16	<b><u>38.41</u></b>	10.63	11.33	<b><u>9.98</u></b>
TGCLDLWP(ocean)	79.87	42.55	40.68	<b><u>48.74</u></b>	40.92	42.37	<b><u>35.16</u></b>
U_200_MERRA	15.45	16.18	15.87	<b><u>15.66</u></b>	2.52	2.11	<b><u>1.94</u></b>
T_200 ERAI	218.82	215.58	215.76	<b><u>216.84</u></b>	4.03	3.37	<b><u>2.13</u></b>

**Table 6.** RMSEs for comparisons between the latitude–height cross-sections of RH simulated by the three macrophysical schemes (Park, T\_pdf, and U\_pdf) and ERA-Interim (Figure 12). The comparisons are made for three periods (JJA: June, July, August; DJF: December, January, February) and two latitudinal ranges. The smallest RMSE value of the three schemes in each case is bolded and underlined.

RH	Park	T_pdf	U_pdf
Annual	11.2	<b><u>6.4</u></b>	9.4
JJA	11.2	<b><u>7.3</u></b>	10.1
DJF	11.8	<b><u>6.9</u></b>	9.7





**Table 7.** RMSEs for comparisons between the latitude–height cross-sections of (a) specific humidity  $q$  and (b) air temperature  $T$  simulated by the three macrophysical schemes (Park, T\_pdf, and U\_pdf) and ERA-Interim (Figure 13). The comparisons are made for three periods (JJA: June, July, August; DJF: December, January, February) and two latitudinal ranges. The smallest RMSE value of the three schemes in each case is bolded and underlined.

(a)

<b>q</b>	<b>Park</b>	<b>T_pdf</b>	<b>U_pdf</b>
<b>Annual</b>	0.29	0.25	<b><u>0.23</u></b>
<b>JJA</b>	0.32	<b><u>0.26</u></b>	0.27
<b>DJF</b>	0.29	0.27	<b><u>0.25</u></b>

(b)

<b>T</b>	<b>Park</b>	<b>T_pdf</b>	<b>U_pdf</b>
<b>Annual</b>	2.62	2.49	<b><u>2.05</u></b>
<b>JJA</b>	2.65	2.43	<b><u>2.24</u></b>
<b>DJF</b>	2.94	2.86	<b><u>2.60</u></b>

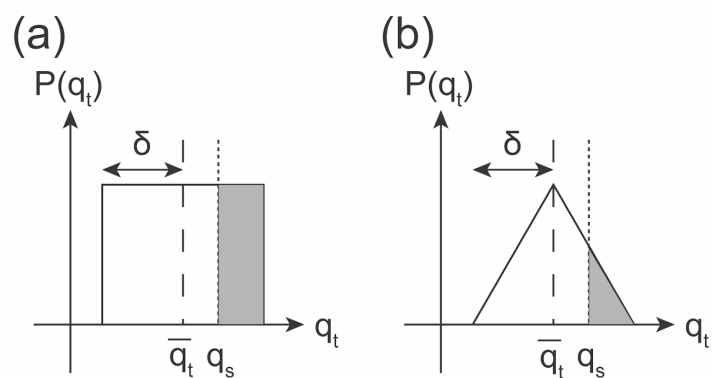
**Table 8.** RMSEs for comparisons between the annual cycles of zonal mean total precipitable water (TMQ) and annual cycles of zonal wind at 200 mb (U200) simulated by the three macrophysical schemes (Park, T\_pdf, and U\_pdf) and ERA-Interim (Figures 14 and 15).

	<b>Park</b>	<b>T_pdf</b>	<b>U_pdf</b>
<b>TMQ</b>	1.44	0.86	<b><u>0.82</u></b>
<b>U200</b>	1.97	1.74	<b><u>1.49</u></b>

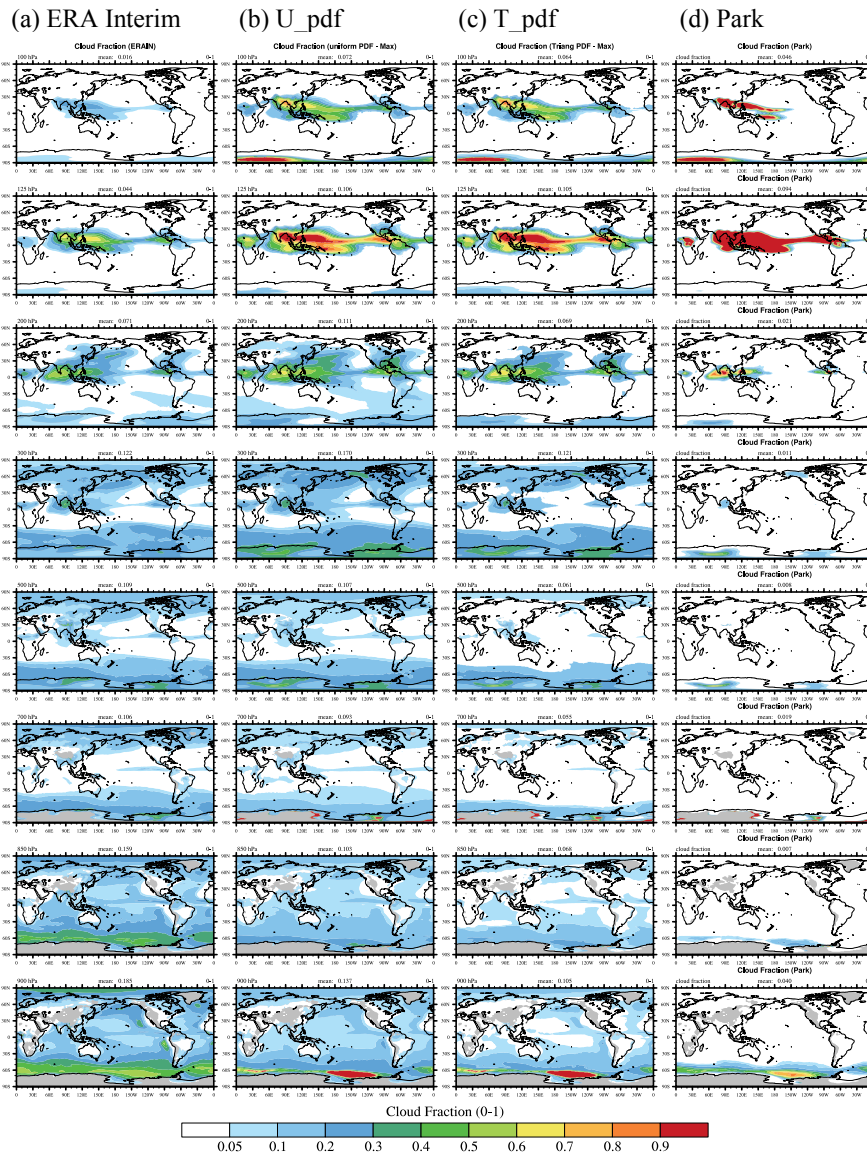


**Table 9.** RMSEs for comparisons between the global mean annual cycles of several parameters simulated by the three macrophysical schemes (Park, T\_pdf, and U\_pdf) and corresponding observational data (Figure 16). The smallest RMSE value of the three schemes in each case is bolded and underlined.

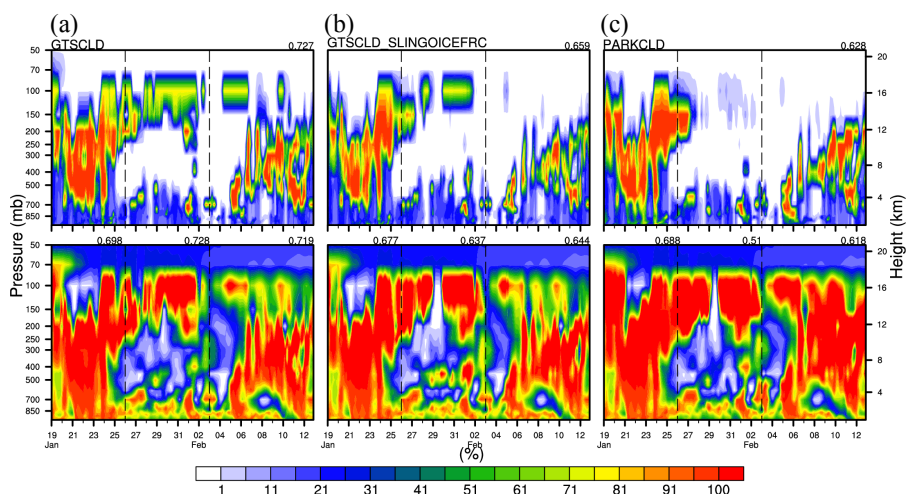
	Park	T_pdf	U_pdf
TMQ	2.08	<b><u>1.70</u></b>	1.74
FLUT	8.15	6.71	<b><u>6.31</u></b>
LWCF	6.18	6.32	<b><u>6.06</u></b>
SWCF	14.00	<b><u>11.80</u></b>	14.00
U_200	2.34	2.04	<b><u>1.70</u></b>
T_200	5.57	4.50	<b><u>2.55</u></b>



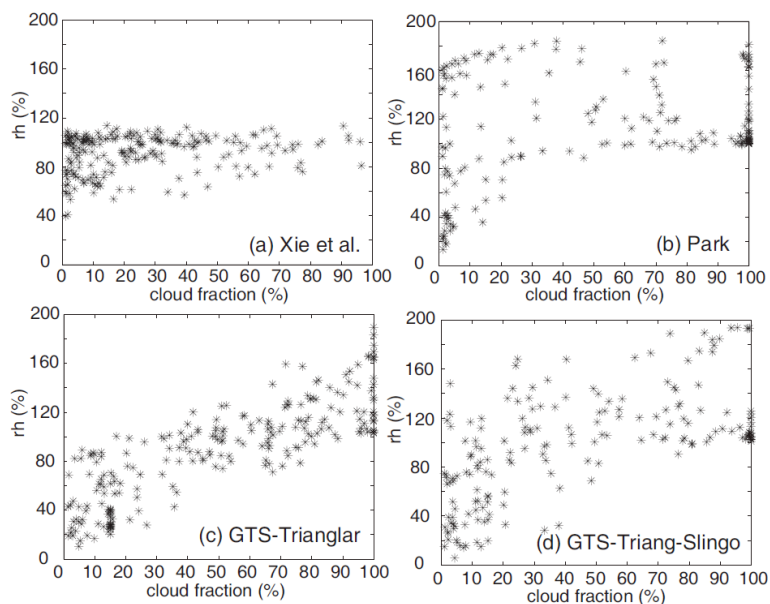
**Figure 1.** Illustration of sub-grid PDF of total water substance  $q_t$  with (a) uniform distribution and (b) triangular distribution. The shaded part shows the saturated cloud fraction,  $\delta$  represents the width of the PDF,  $\bar{q}_t$  denotes the grid-mean value of total water substance, and  $q_s$  represents the saturation mixing ratio as the temperature is assumed to be uniform within the grid.



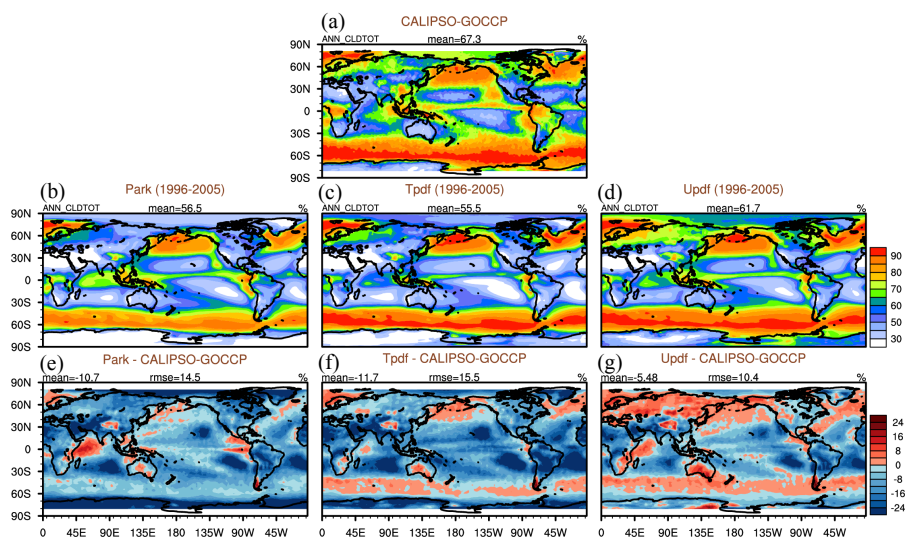
**Figure 2.** Mean cloud fraction in July (a) from the ERA-Interim reanalysis dataset and (b, c, d) diagnosed from cloud fraction schemes, with temperature, moisture, and condensates from the ERA-Interim reanalysis provided. From left to right, these schemes are the (b) U\_pdf, (c) T\_pdf, and (d) Park macrophysics schemes. Cloud distributions from 100 to 900 hPa are plotted from top to bottom.



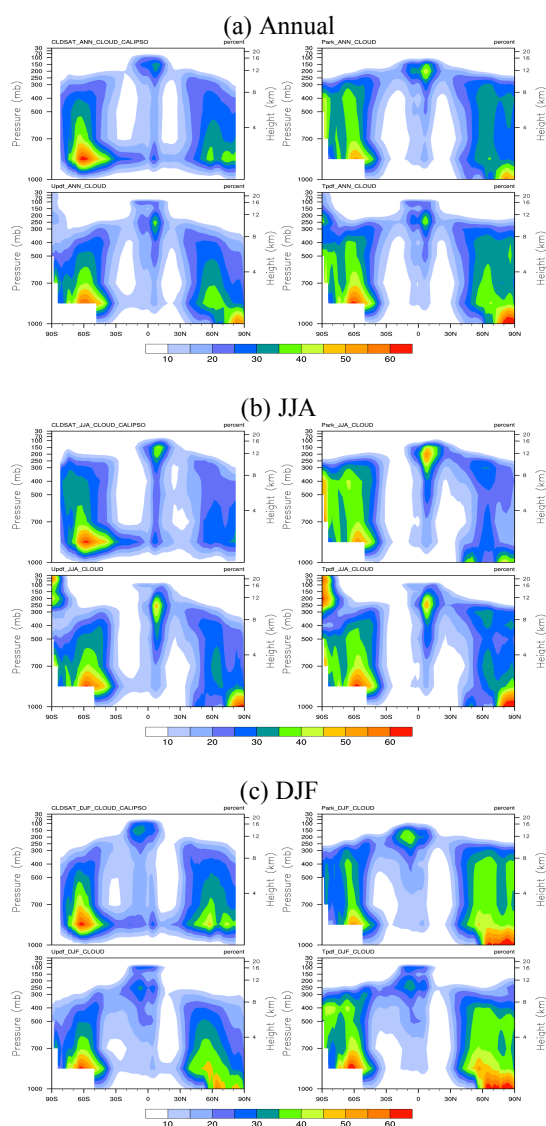
**Figure 3.** Pressure–time cross-sections of cloud fraction (upper row) and relative humidity (lower row) simulated by the three different cloud macrophysical schemes; (a) T\_pdf, (b) T\_pdf with Slingo ice cloud fraction scheme, and (c) the Park scheme during the TWP-ICE field campaign.



**Figure 4.** Scatter plots of high-level (50–300 hPa) relative humidities and cloud fractions during the suppressed monsoon period of the TWP-ICE field campaign (26 January to 2 February, 2006) observed by (a) Xie *et al.* [2010] and simulated by SCAM with the (b) Park of CAM5.3, (c) T\_pdf, and (d) T\_pdf with Slingo ice cloud macrophysics schemes.

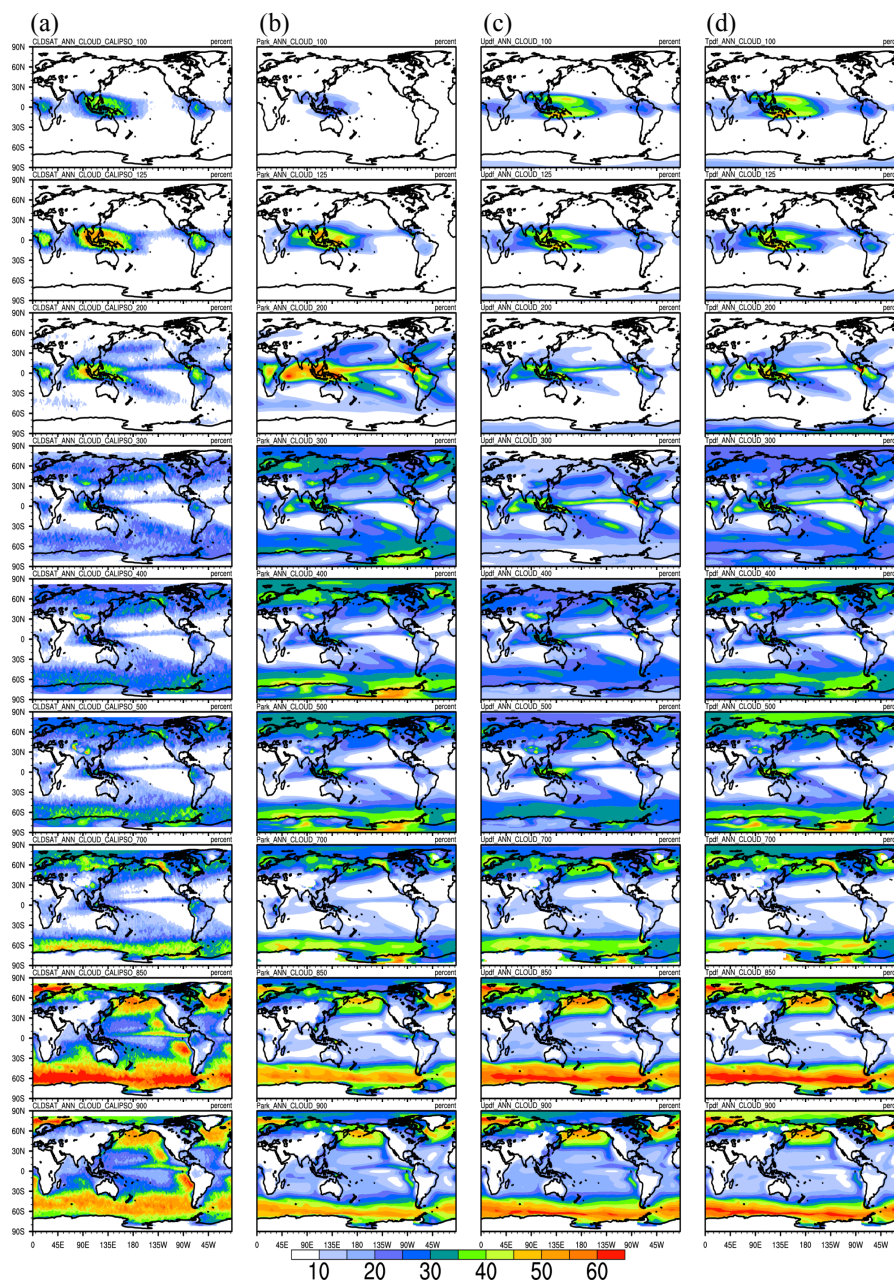


**Figure 5.** Total cloud fraction (CF) from (a) CALIPSO-GOCCP and simulated by the three schemes: (b) the default Park, (c) T\_pdf, and (d) U\_pdf, using the COSP satellite simulator of the NCAR CESM model. Differences between the simulated and observed total CFs derived from (e) the default Park, (f) T\_pdf, and (g) U\_pdf schemes.

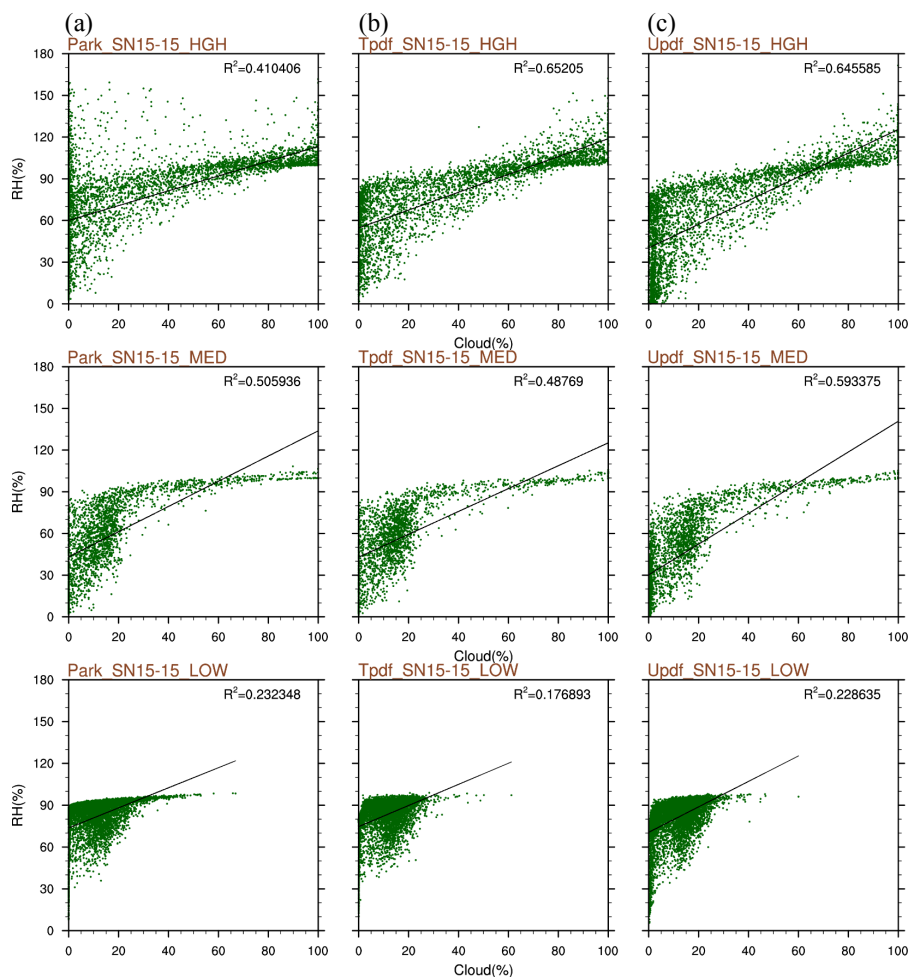


**Figure 6.** Latitude–height cross-sections of (a) annual, (b) June–July–August (JJA), and (c) December–January–February (DJF) mean CFs from CloudSat/CALIPSO data (upper left) and the the Park (upper right), U\_pdf (lower left), and T\_pdf (lower right) schemes.

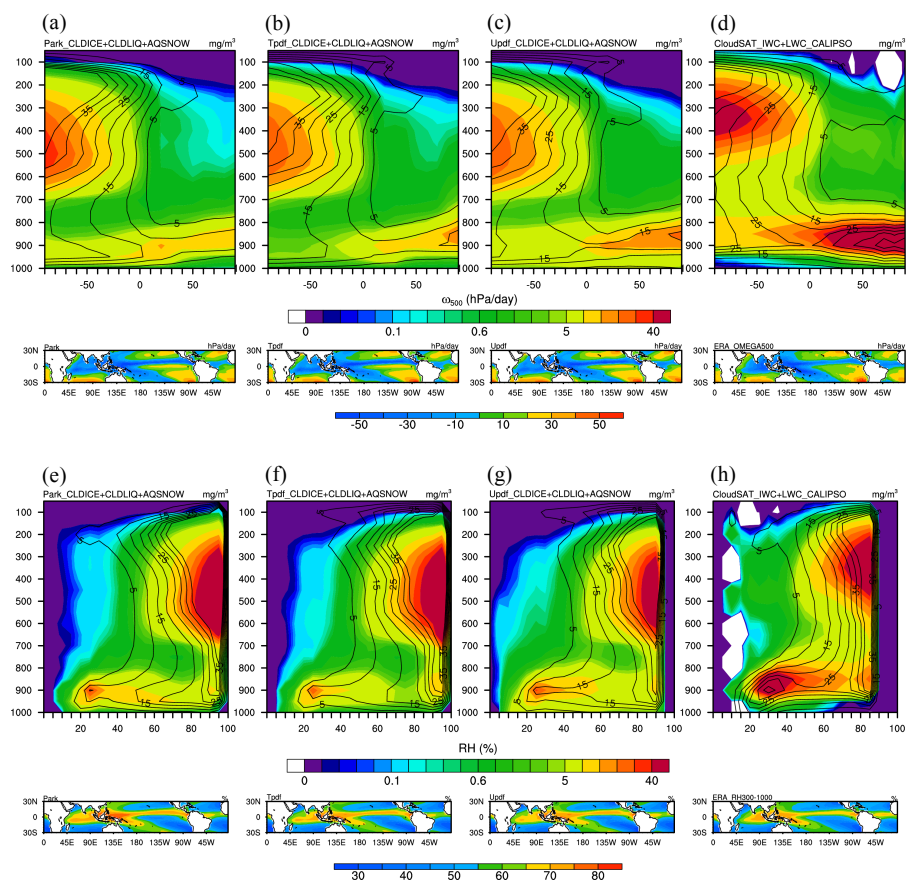




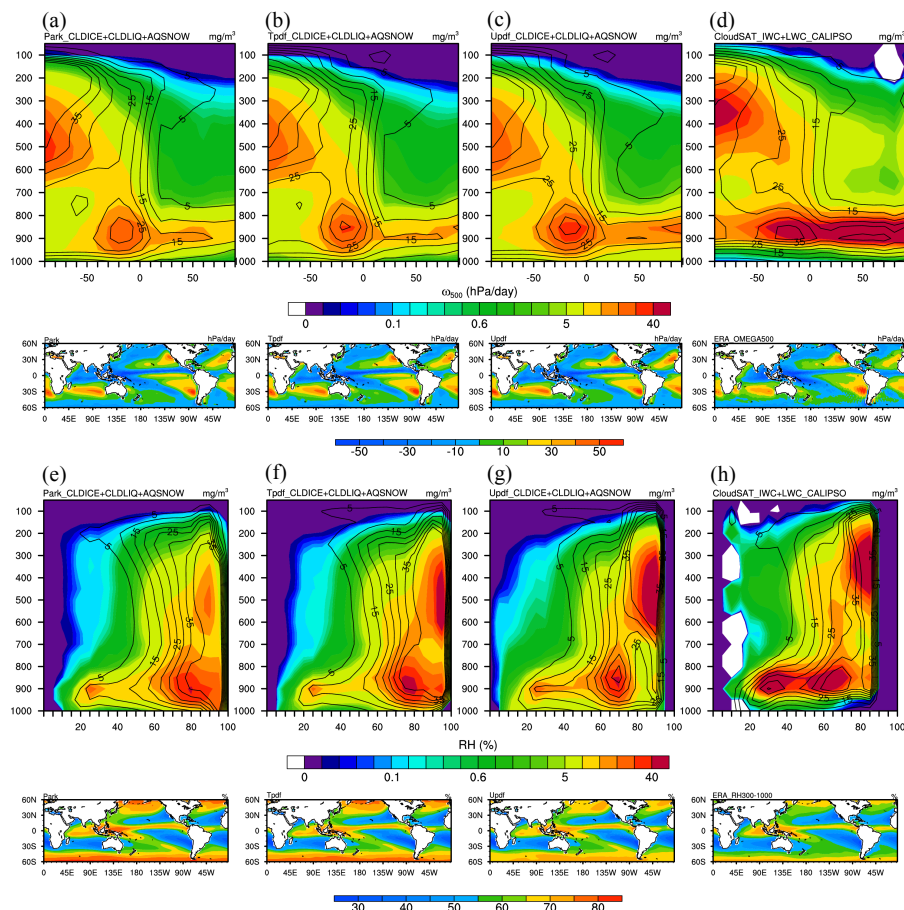
**Figure 7.** CFs at nine pressure levels (one pressure level per row; top to bottom: 100, 125, 200, 300, 400, 500, 700, 850, and 900 mb) from (a) CloudSat/CALIPSO observational data and simulated by (b) the default Park, (c) U\_pdf, and (d) T\_pdf schemes.



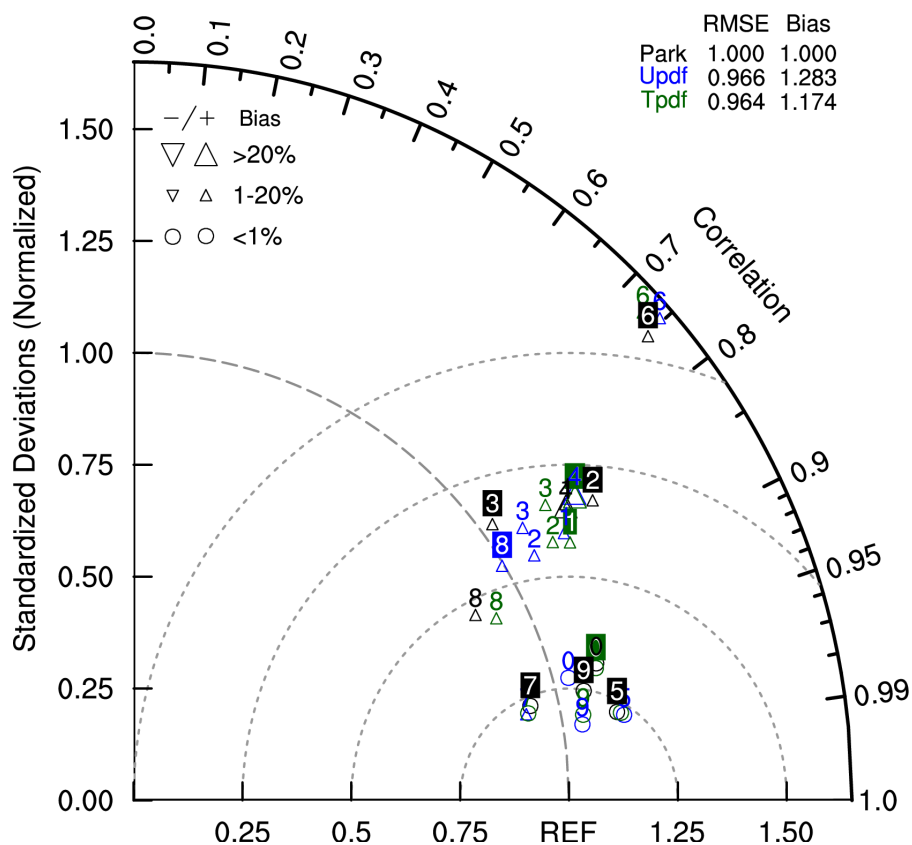
**Figure 8.** CF versus RH at three cloud levels (top to bottom: high, middle, and low clouds) simulated by (a) the default Park, (b) T\_pdf, and (c) U\_pdf schemes. Daily data of the two grid points ((180° E, 15° N) and (180° E, 15° S)) from 1999 to 2000 are used to generate the scatter plots, and linear regression lines with correlation coefficients are also shown.



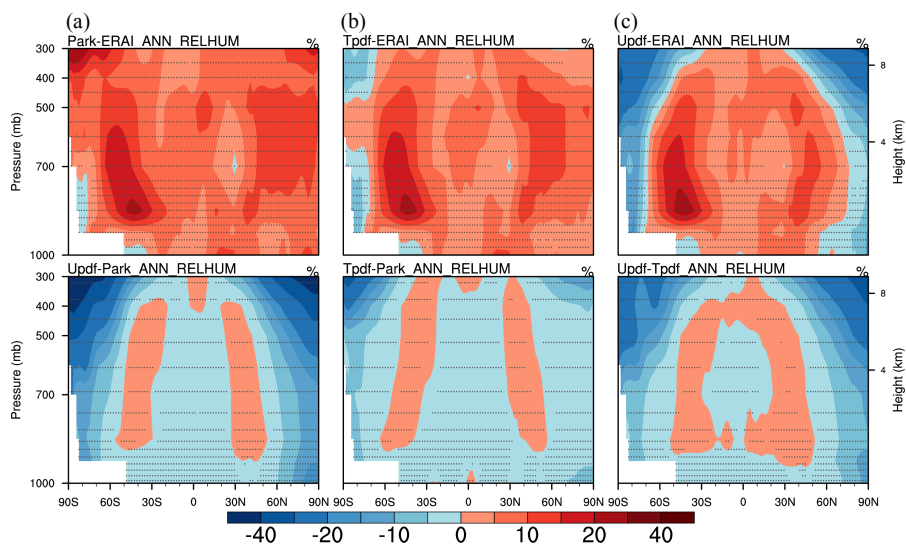
**Figure 9.** Vertical distribution of CF (contour lines) and CWC (colors) as functions of two large-scale parameters: vertical velocity at 500 mb ( $\omega_{500}$ , upper eight panels) and relative humidity averaged between 300 and 1000 mb (RH<sub>300–1000</sub>, lower eight panels) for the latitudinal range 30° N–30° S. Columns present simulations by the (a, e) Park, (b, f) T<sub>pdf</sub>, and (c, g) U<sub>pdf</sub> schemes, and (d, h) observational data from CloudSat/CALIPSO.



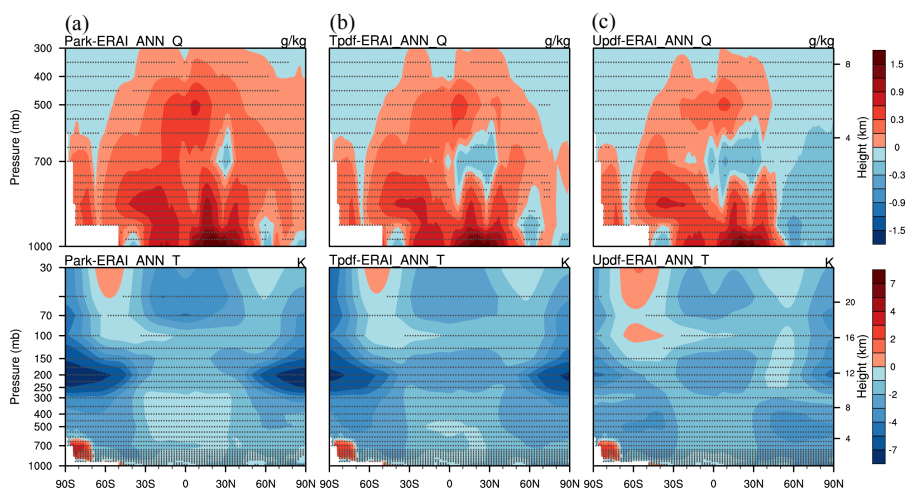
**Figure 10.** Vertical distribution of CF (contour lines) and CWC (colors) as functions of two large-scale parameters:  $\omega_{500}$  (upper eight panels) and RH<sub>300–1000</sub> (lower eight panels) for the latitudinal range 60° N–60° S. Columns present simulations by the (a, e) Park, (b, f) T\_pdf, and (c, g) U\_pdf, and (d, h) observational data from CloudSat/CALIPSO.



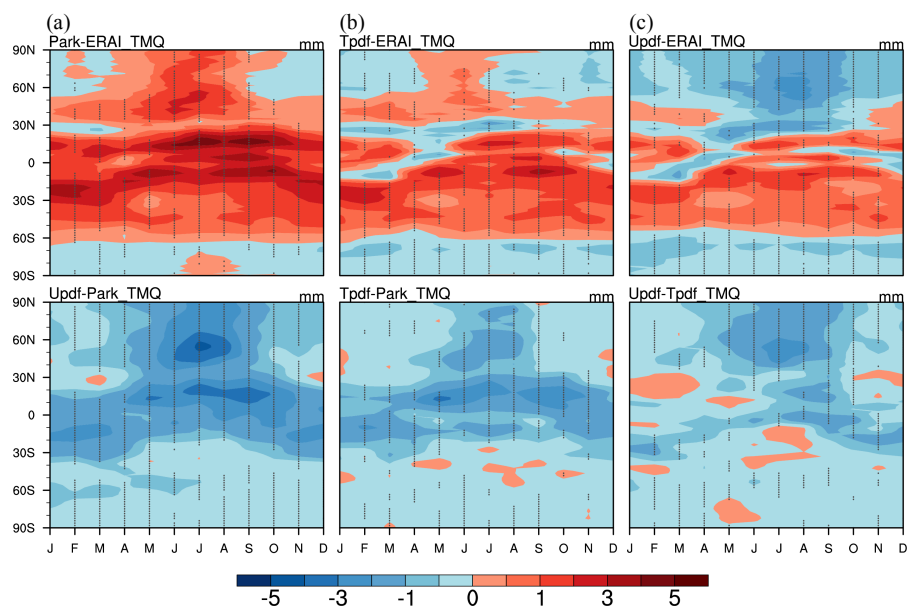
**Figure 11.** Space–time Taylor diagram for the ten climatic parameters simulated by the three macrophysical schemes (Park: black symbols; U<sub>pdf</sub>: green; T<sub>pdf</sub>: blue) and comparisons of these with the corresponding observational data provided by the atmospheric diagnostic package from the NCAR CESM group. The ten climatic parameters are marked from 0 to 9 where 0 denotes sea level pressure; 1 is SW cloud forcing, 2 is LW cloud forcing, 3 is land rainfall, 4 is ocean rainfall, 5 is land 2-m temperature, 6 is Pacific surface stress, 7 is zonal wind at 300 mb, 8 is relative humidity, and 9 is temperature.



**Figure 12.** Upper row: latitude–pressure cross-sections of differences in relative humidity (RH) between the simulations and ERA-Interim from (a) Park, (b) T\_pdf, and (c) U\_pdf schemes. Lower row: differences in RH in pair-wise comparisons of the three cloud macrophysical schemes.

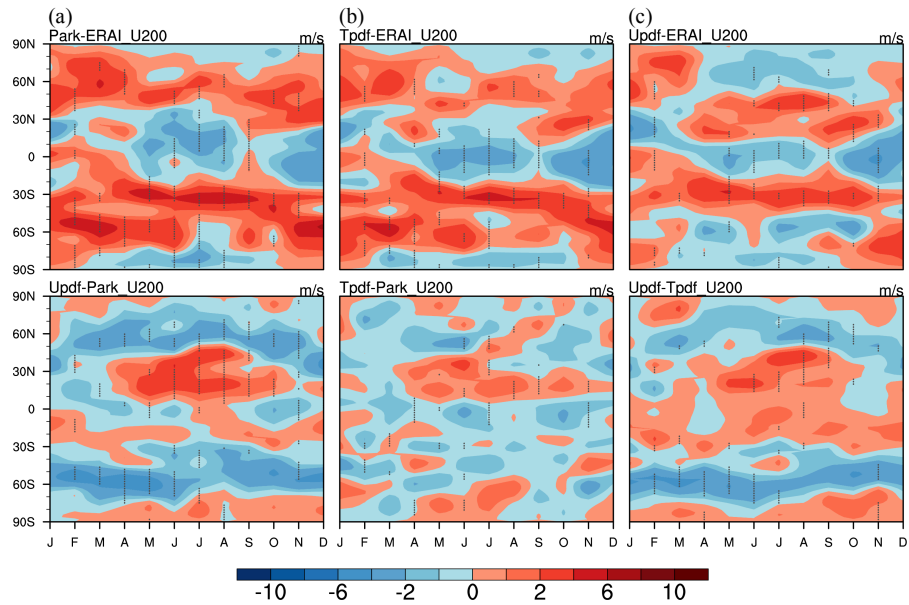


**Figure 13.** Differences in specific humidity (upper row) and air temperature (lower row) between the simulations and ERA-Interim from the (a) Park, (b) T\_pdf, and (c) U\_pdf schemes.

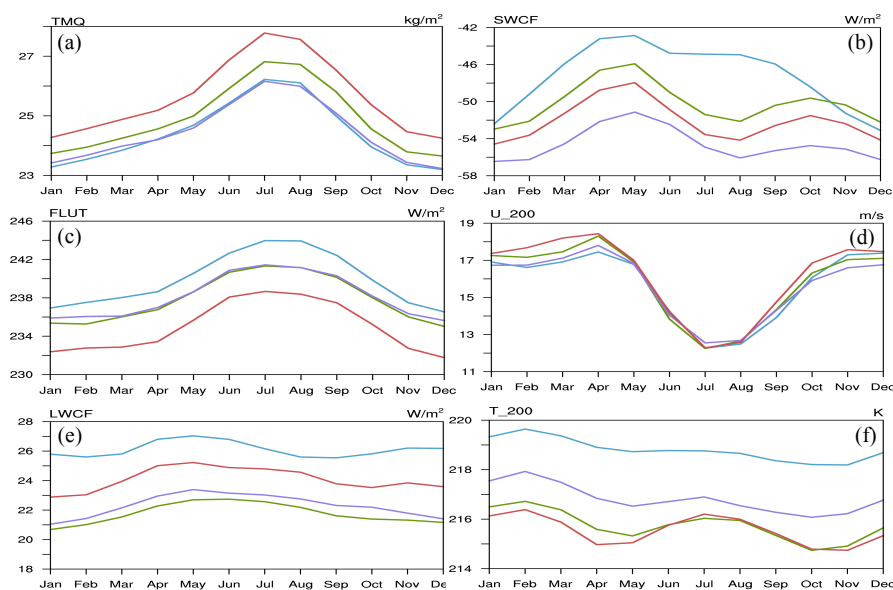


**Figure 14.** Upper row: differences in annual cycles of zonal mean total precipitable water between the three macrophysical schemes and the ERA-Interim data from the (a) Park, (b) T\_pdf, and (c) U\_pdf schemes. Lower row: differences in annual cycles of total precipitable water in pair-wise comparisons of the three cloud macrophysical schemes.

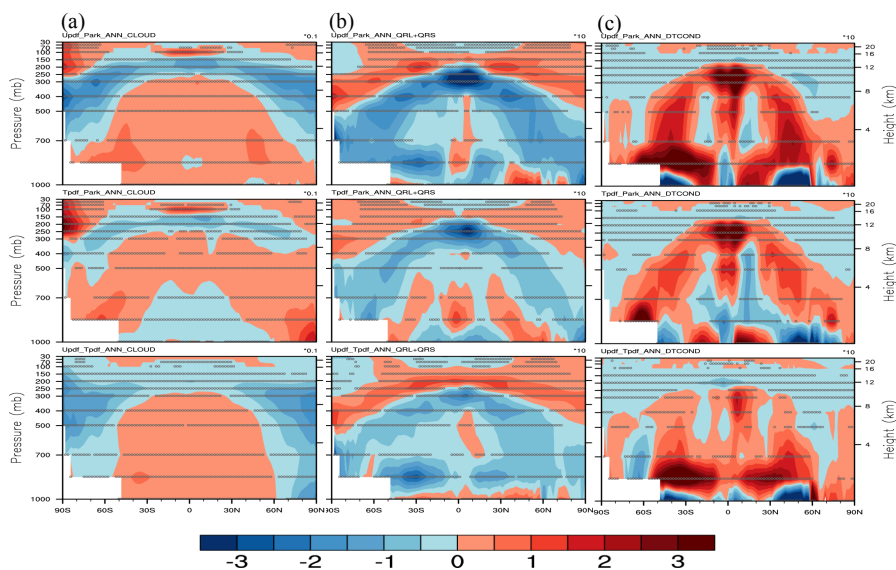




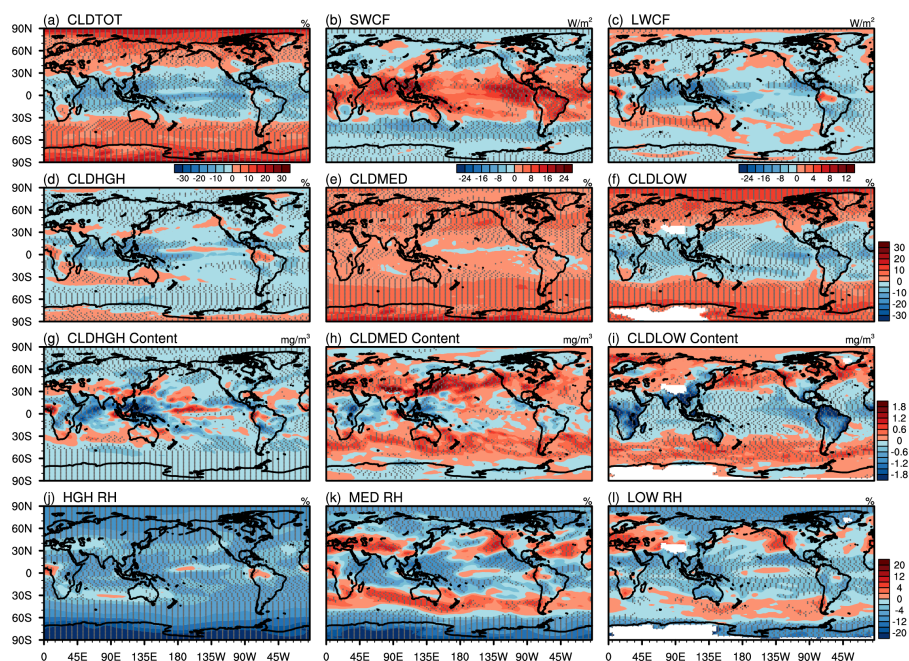
**Figure 15.** Upper row: differences in annual cycles of zonal wind at 200 mb between the three macrophysical schemes and the ERA-Interim data from the (a) Park, (b) T\_pdf, and (c) U\_pdf schemes. Lower row: differences in annual cycles of zonal wind at 200 mb in pair-wise comparisons of the three cloud macrophysical schemes.



**Figure 16.** Global annual cycles of (a) total precipitable water, (b) shortwave cloud forcing, (c) net longwave flux at the top of the model, (d) zonal wind at 200 mb, (e) longwave cloud forcing, and (f) air temperature at 200 mb. Colored lines represent observational data (blue) and simulations by the Park (red), U\_pdf (purple), and T\_pdf (green) schemes.



**Figure 17.** Differences in (a) CF, (b) sum of longwave and shortwave heating rates (QRL+QRS), and (c) temperature trends due to moist processes in the NCAR CESM model (DTCOND) in pair-wise comparisons of the three cloud macrophysical schemes. Upper row: U\_pdf and Park; middle row: T\_pdf and Park; lower row: U\_pdf and T\_pdf. A statistically significant difference with a confidence level of 95% is represented in the panels by an open circle using Student's t-test.



**Figure 18.** Differences in (a) total cloud fraction, (b) short-wave cloud radiative forcing, (c) long-wave cloud radiative forcing, and cloud fraction of (d) high clouds, (e) middle clouds, and (f) low clouds between the  $T\_pdf$  and default Park schemes. (g–i) As for (d–f) but for total cloud water content at the three cloud levels. (j–l) As for (g–i) except for averaged RH at the three cloud levels.