HydroMix v1.0: a new Bayesian mixing framework for attributing uncertain hydrological sources

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11 Abstract

12 Tracers have been used for over half a century in hydrology to quantify water sources with 13 the help of mixing models. In this paper, we build on classic Bayesian methods to quantify 14 uncertainty in mixing ratios. Such methods infer the probability density function (pdf) of the 15 mixing ratios by formulating pdfs for the source and target concentrations and inferring the 16 underlying mixing ratios via Monte Carlo sampling. However, collected hydrological samples 17 are rarely abundant enough to robustly fit a pdf to the source concentrations. Our approach, 18 called HydroMix, solves the linear mixing problem in a Bayesian inference framework where 19 the likelihood is formulated for the error between observed and modelled target variables, 20 which corresponds to the parameter inference set-up commonly used in hydrological models. 21 To address small sample sizes, every combination of source samples is mixed with every target 22 tracer concentration. Using a series of synthetic case studies, we evaluate the performance of 23 HydroMix using a Markov Chain Monte Carlo sampler. We then use HydroMix to show that 24 snowmelt accounts for around 61% of groundwater recharge in a Swiss Alpine catchment 25 (Vallon de Nant), despite snowfall only accounting for 40-45% of the annual precipitation. 26 Using this example, we then demonstrate the flexibility of this approach to account for 27 uncertainties in source characterization due to different hydrological processes. We also 28 address an important bias in mixing models that arises when there is a large divergence 29 between the number of collected source samples and their flux magnitudes. HydroMix can 30 account for this bias by using composite likelihood functions that effectively weight the 31 relative magnitude of source fluxes. The primary application target of this framework is 32 hydrology, but it is by no means limited to this field.

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35 Keywords: Markov Chain Monte Carlo; stable water isotopes; hydrograph separation; isotopic

- 36 lapse rate; rain; snow;
- 37 38

1 1 Introduction

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3 Most water resources are a mixture of different water sources that have travelled via distinct 4 flow paths in the landscape (e.g. streams, lakes, groundwater). A key challenge in hydrology 5 is to infer source contributions to understand the flow paths to a given water body using a 6 source attribution technique. A classic example is the two-component hydrograph separation 7 model to quantify the proportion of groundwater and rainfall in streamflow, often referred to as "pre-event" water vs "event" water (Burns et al., 2001; Klaus and McDonnell, 2013; 8 9 Schmieder et al., 2016). Other examples include estimating the proportional contribution of 10 rainfall and snowmelt to groundwater recharge (Beria et al., 2018; Jasechko et al., 2017; 11 Jeelani et al., 2010), fog to the amount of throughfall (Scholl et al., 2011, 2002; Uehara and 12 Kume, 2012), and soil moisture (at varying depths) and groundwater to vegetation water use 13 (Ehleringer and Dawson, 1992; Evaristo et al., 2017; Rothfuss and Javaux, 2017).

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15 The primary goal of such attribution in hydrology is to infer the contribution of different 16 sources to a target water body, where the tracer can be an observable compound like a dye, 17 or a conservative solute, or even a proxy for chemical composition such as electrical 18 conductivity. The key requirement is that the concentration of the tracer is distinguishable 19 between different sources. The stable isotope composition of hydrogen and oxygen in water 20 (subsequently referred to as 'stable isotopes of water') are used as tracers in hydrology. Other 21 commonly used tracers include electrical conductivity (Hoeg et al., 2000; Laudon and 22 Slaymaker, 1997; Lopes et al., 2018; Pellerin et al., 2007; Weijs et al., 2013) and conservative 23 geochemical solutes such as chloride and silica (Rice and Hornberger, 1998; Wels et al., 1991). 24

25 Classically, attribution analysis is done by assigning an average tracer concentration to each 26 source, estimated typically from time or space-averages of observed field data (Maule et al., 27 1994; Winograd et al., 1998), and then solving a series of linear equations. In order to express 28 uncertainty in the attribution analysis, a tracer-based hydrograph separation approach was 29 first proposed in the work of Genereux, (1998) and has subsequently been used in many 30 studies (Genereux et al., 2002; Koutsouris and Lyon, 2018; Zhu et al., 2019). Bayesian mixing 31 approaches offer a useful alternative to classic hydrograph separation, as Bayesian 32 approaches explicitly acknowledge the temporal variability of source tracer concentrations 33 estimated from observed samples (Barbeta and Peñuelas, 2017; Blake et al., 2018). Rather 34 than a single estimate of source contributions, Bayesian approaches yield full probability 35 density functions (pdfs) of the fraction of different sources in the target mixture (Parnell et al., 36 2010; Stock et al., 2018), hereafter referred to as 'mixing ratios'.

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38 Bayesian mixing was first developed in ecology to estimate the proportion of different food 39 sources to animal diets (Parnell et al., 2010; Stock et al., 2018). Hydrological applications of 40 such models are still rare (Blake et al., 2018; Evaristo et al., 2016, 2017; Oerter et al., 2019). In 41 a Bayesian mixing model, a statistical distribution is fitted to both the measured source tracer 42 concentrations, and to the measured tracer concentrations from the target (e.g. river, 43 groundwater, vegetation). The distribution of the mixing ratios is then inferred via Bayesian 44 inference. With recent advances in probabilistic programming languages like Stan (Carpenter 45 et al., 2017), Bayesian inference has become a relatively simple task.

1 However, the key limitation with the above approach is that the source compositions are 2 assumed to come from standard statistical distributions. Typically, the sources are assumed 3 to be drawn from Gaussian distributions, which can be fully characterized by the mean and 4 variance of the data available for each source (Stock et al., 2018). This limits both the potential 5 applicability and the insights that can be gained from tracer information in hydrology because 6 the sample mean and variance may not accurately reflect the statistical properties of the 7 actual source composition and the Gaussian approach represents an unnecessary 8 simplification in cases where a large amount of information on source composition is 9 available.

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11 An additional complication in hydrology comes from the fact that observed point-scale 12 samples do not necessarily capture the tracer concentrations in the actual sources, which are 13 distributed heterogeneously in space and whose contribution can be temporally variable 14 depending on the state of the catchment (Harman, 2015). For instance, if we were to 15 characterize the contribution of snowmelt to groundwater, we would need to capture (1) the 16 temporal evolution of the isotopic ratio of snowmelt, which strongly varies in space (Beria et 17 al., 2018; Earman et al., 2006), and (2) the temporal evolution of the area actually covered by 18 snow. This spatially and temporally distributed nature of the sources can be hard to account 19 for in both the analytical and the Bayesian mixing approaches.

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21 To overcome the limitations of source heterogeneity and the previously discussed restriction 22 to Gaussian distributions, we present a new mixing approach for hydrological applications, 23 called HydroMix. This approach does not require a parametric description of observed source 24 or target tracer concentrations. Instead, HydroMix formulates the linear mixing problem in a 25 Bayesian inference framework similar to hydrological rainfall-runoff models (Kavetski et al., 26 2006a), where the mixing ratios of the different sources are treated as model parameters. 27 Multiple model parameters can be inferred in such a setup allowing parameterization of 28 additional hydrologic processes that can modify source tracer concentrations (shown in 29 Section 3.5). A more detailed account of the advantages and limitations of this new approach 30 is given in Section 5.

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32 In this paper, we first describe the theoretical details of HydroMix for a simple case study with two sources, one mixture and one tracer (Section 2). Section 3 presents synthetic and real-33 34 world case studies that demonstrate the accuracy, robustness and flexibility of HydroMix. In 35 the synthetic case study, we use a conceptual hydrologic model to simulate tracer 36 concentrations. We also introduce a composite likelihood function that accounts for the 37 magnitude of the different sources. The real-world case study applies HydroMix in a highelevation headwater catchment in Switzerland. The results of these applications are 38 39 presented in Section 4 before summarizing the main outcomes, applicability, and limitations 40 of HydroMix in Section 5.

41 2 Model description and implementation

43 A system with *n* sources mixing linearly in a target water body can be written as:

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45 $\rho_1 S_1^k + \rho_2 S_2^k + \dots + \rho_n S_n^k = Y^k$,

- 1 where Y^k is the concentration of the k^{th} tracer in the target mixture, S_i^k is the concentration 2 of the k^{th} tracer in source *i*. ρ_i (*i*=1, ..., *n*) are the fractions of all sources in the mixture, with 3 $\sum_{i=1}^{n} \rho_i = 1$, corresponding to the aggregation of different sources in the mixture. In order to 4 solve this system of linear equations, "*n*-1" different tracers are required.
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Section 2.1 details the general modeling approach for a simplified system with two sources
and one tracer. This is followed by a detailed discussion on the choice of the parameter
inference approach used.

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10 2.1 Linear mixing model with non-concomitant observed data

For a system with two sources that combine linearly to form a mixture, the mixing model canbe formulated as:

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$$\rho S_1(t - \tau_1) + (1 - \rho)S_2(t - \tau_2) = Y(t),$$
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16 where $S_1(t - \tau_1)$ is the tracer concentration in source 1 at timestep $t - \tau_1$, $S_2(t - \tau_2)$ is the tracer concentration in source 2 at timestep $t - \tau_2$, Y(t) is the concentration of the mixture 17 18 (i.e. the tracer concentration in the target) at timestep t, ρ is the mixing ratio and τ_i is the 19 time delay between the time when source *i* enters the system and the time when it is observed 20 in the mixture. As an example, for a case where the two sources are snowmelt and rainfall and 21 the mixture is groundwater, ρ represents the proportional groundwater recharged from 22 snowmelt and τ represents the average time lag for rain or snowmelt to reach groundwater 23 once they enter into the soil. In other words, the time lag (τ) stands for any delay caused by 24 tracer transport from the source to the output; we assume that the source components are 25 conservative in nature.

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The two parameters in this system, the mixing ratio (ρ) and the time delay (τ), can be inferred via classical Bayesian parameter inference which is widely used in hydrology (Kavetski et al., 2006a, 2006b; Schaefli and Kavetski, 2017). This implies taking an observed timeseries of the target (e.g. the tracer concentration in groundwater) and building a vector of model residuals:

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$$\begin{array}{ll} \mathbf{32} & \varepsilon_t = \tilde{Y}_t - \hat{Y}_t,\\ \mathbf{33} & \end{array}$$

34 where \tilde{Y}_t represents the observed mixture concentration and \hat{Y}_t represents the simulated 35 mixture concentration. However, in real environmental systems like that of groundwater 36 recharge from rainfall and snowmelt, there are four major difficulties which can prevent the 37 inference of ρ and τ from the observed data.

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39 i. ρ and τ strongly vary in time depending on catchment conditions such as soil moisture (as 40 previously discussed in the context of the 'inverse storage effect' (Benettin et al., 2017; 41 Harman, 2015)).

42 ii.Long time series of the tracer concentration in both the sources and mixture are rare.

43 iii. The effect of seasonality in precipitation can make the inference of τ very difficult in case the 44 goal is to understand intra-annual recharge dynamics.

45 iv.The tracer concentration in the different sources are generally measured at point scales
46 whereas the tracer concentration in the target integrates inputs over the entire source area.
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Our practical solution to limitation iv) is to assume that tracer concentrations in the two
 sources are functions of observable point processes:

$$\begin{array}{l} 4 \quad S_i(t) = f_i(P_i(t)), \\ 5 \end{array}$$

6 where the function f_i represents the transformation from the point to the catchment scale for 7 source *i*. Limitation iii) can be relaxed by assuming a long enough timestep (eg: long term 8 groundwater recharge dynamics), where the observed samples are samples from the long 9 term (>> 1 year) source and target compositions. This allows to replace the timestep 't' and 10 't+ τ ' with Δt and write Eq. (2) as:

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 $\rho S_1'(\Delta t) + (1 - \rho)S_2'(\Delta t) = Y'(\Delta t),$ 5

14 where the ' signifies the new time-integrated variables. Now, any observed point-scale tracer 15 concentration p_i in a given source *i* or in the output (e.g., the isotopic ratio of snowmelt) can 16 be assumed to represent a sample from a stationary process (from S'_1 or S'_2 or Y'). This 17 assumption is in fact implicitly underlying most of the existing hydrological mixing models 18 where point samples are used to characterize a spatial process and where the time reference 19 of the samples is discarded.

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By utilizing all the available measurements $\{p'_1\}_{i=1..n}$ and $\{p'_2\}_{j=1..m}$ of the two sources in the above model, with n samples of source 1 and m samples of source 2, we can build $n \times m$ predictions and compare them with the q observed samples of the target as:

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$$\varepsilon_{ij}^k = \tilde{Y}_{obs}^k - \hat{Y}_{ij},$$

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where \tilde{Y}_{obs}^{k} is the *k*-th observed target concentration out of a total number of *q* target concentrations.

Assuming that the residuals can be described with a Gaussian error model with a mean of zero and constant variance σ^2 ,

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$$\varepsilon \sim N(0, \sigma^2),$$

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we can compute the likelihood function of the residuals as the joint probability of all theresiduals:

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$$L_j(\tilde{Y}_{obs}|P_1, P_2, \theta) = \prod_{k=1}^q \prod_{j=1}^m \prod_{i=1}^n (2\pi\sigma^2)^{-0.5} \exp\left(-\frac{1}{2} \frac{(\tilde{Y}_{obs}^k - \hat{Y}_{ij})^2}{\sigma^2}\right),$$
 8
39

40 where θ represents all the model parameters and P_i (*i*=1,2) is the observed point process (see 41 Eq. 4). The above Gaussian error model could in principle be replaced with any other stochastic 42 process. However, the Gaussian error model has been shown to be relatively robust in this 43 kind of an application (Lyon, 2013; Schaefli and Kavetski, 2017).

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45 In the case of linear mixing between two sources, the two model parameters considered at 46 this stage are the mixing ratio ρ and the error variance σ^2 . The error variance can either be

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computed from the observed residuals or be treated as a model parameter (Kuczera and
Parent, 1998; Schaefli et al., 2007). For the examples shown in this paper, the error variance
is computed from the residuals.

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In order to avoid numerical problems, we use the log-likelihood form of Eq. (8):

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$$\log L_j(\tilde{Y}_{obs}|P_1, P_2, \theta) = \sum_{k=1}^q \sum_{j=1}^m \sum_{i=1}^n -0.5 \left[\log (2\pi\sigma^2) + \frac{\left(\tilde{Y}_{obs}^k - \hat{Y}_{ij}\right)^2}{\sigma^2} \right].$$
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9 2.2 Parameter inference in a Bayesian framework

Following the general Bayes' equation, the posterior distribution of the model parameterscan be written as:

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$$p(\theta|P_1, P_2, \tilde{Y}) = \frac{p(\tilde{Y}|\theta, P_1, P_2)p(\theta)}{p(\tilde{Y}|P_1, P_2)},$$
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16 where $p(\theta)$ is the prior distribution of the model parameters and $p(\tilde{Y}|\theta, P_1, P_2)$ is the 17 likelihood function. The denominator of Eq. (10) can generally not be computed as that would 18 require integration over the whole parameter space which is computationally expensive, 19 which is why Eq. (10) is reduced to:

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 $p(\boldsymbol{\theta}|P_1, P_2, \tilde{Y}) \propto p(\tilde{Y}|\boldsymbol{\theta}, P_1, P_2)p(\boldsymbol{\theta}).$ 11

23 Two methods are traditionally used in hydrology to sample from the posterior distribution 24 from Eq. (11), Markov Chain Monte Carlo (MCMC) sampling (Hastings, 1970; Metropolis and 25 Ulam, 1949) and importance sampling (Glynn and Iglehart, 1989; Neal, 2001). In the case of 26 MCMC sampling, a common approach is the Metropolis algorithm (Kuczera and Parent, 1998; 27 Schaefli et al., 2007; Vrugt et al., 2003). In importance sampling, the posterior distribution is 28 obtained from weighted samples drawn from the so-called importance distribution. For 29 typical multivariate hydrological problems, the only possible choices for the importance 30 distribution are either uniform sampling over a hypercube or sampling from an over-dispersed 31 multi-normal distribution (Kuczera and Parent, 1998). A stochastic process is defined as over-32 dispersed when the variance of the underlying distribution is greater than its mean (Inouye et 33 al., 2017). The sampling distributions in such cases have large variance, allowing sufficient 34 sampling over the entire parameter range.

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36 We implement a MCMC sampling algorithm using a Metropolis-Hastings (Hastings, 1970) 37 criterion to infer the posterior distribution of the mixing ratio. For the synthetic case study 38 (Section 3.1), we setup 10 parallel MCMC chains to monitor convergence according to the 39 classical Gelman-Rubin convergence criterion (Gelman and Rubin, 1992). Each chain is 40 initiated by assigning a uniform prior distribution for the mixing ratio, where the mixing ratio 41 varies between 0 and 1. For the subsequent case studies, we use importance sampling for the 42 sake of simplicity. The prior distribution of additional model parameters (if applicable) are 43 discussed in the corresponding case study section. Apart from the prior distribution of the 44 model parameters, HydroMix requires tracer concentration of the different sources and of the 1 mixture. The error model variance is not jointly inferred with other model parameters but 2 calculated for each sample parameter set from the residuals according to Eq. (6).

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4 3 Case studies

We provide a comprehensive overview of the performance of HydroMix based on a set of 6 7 synthetic case studies (case studies 3.1 and 3.2) and a real-world application to demonstrate 8 the practical relevance for hydrologic applications (case studies 3.4 and 3.5). The first case 9 study demonstrates the ability of HydroMix to converge on the correct posterior distribution 10 for synthetically generated data. The second case study uses a synthetic dataset of rain, snow 11 and groundwater isotopic ratios using a conceptual hydrologic model, and compares the 12 results of HydroMix to the actual mixing ratios assumed to generate the data set. It then 13 weights the sources samples and evaluates the effect of weighting on the mixing ratio (case 14 study 3.3). In the last two case studies, HydroMix is applied to observed tracer data from an 15 Alpine catchment in the Swiss Alps to infer source mixing ratios and an additional parameter 16 (isotopic lapse rate).

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3.1 Mixing using Gaussian distributions

In this example, source concentrations S_1 and S_2 are drawn from two Gaussian distributions with different means (μ_1, μ_2) and standard deviations (σ_1, σ_2) and combined to form the mixture Y with a constant mixing ratio ρ :

24 $\rho S_1 + (1 - \rho)S_2 = Y.$

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Assuming the two distributions are independent, the resultant mixture is normally distributed with mean (μ_y) and variance (σ_y^2) defined as:

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 $\mu_y = \rho \mu_1 + (1 - \rho) \mu_2; \ \sigma_y^2 = \rho^2 \sigma_1^2 + (1 - \rho)^2 \sigma_2^2.$ 13

A given number of samples are drawn from the distributions of S_1 and S_2 and of the mixture Y. The posterior distribution of the mixing ratio, $p(\rho | \tilde{S_1}, \tilde{S_2}, \tilde{Y})$, is then inferred using HydroMix for i) a case where the two source distributions are well identifiable, and ii) a case where the distributions have a large overlap. Different values of mixing ratios are tested, with ratios varying from 0.05 to 0.95 in steps of 0.05.

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The sensitivity of HydroMix to the number of samples drawn from S_1 , S_2 and Y, along with the time to convergence is assessed based on the sum of the absolute error between the estimated mixing ratio $\hat{\rho}$ and its true value ρ .

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41 3.2 Mixing with a time series generated using a hydrologic model

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43 In this case study, we build a conceptual hydrologic model where groundwater is assumed to 44 be recharged directly from rainfall and snowmelt. Stable isotopes of deuterium (δ^2 H) is used

1 to see how the isotopic ratio in groundwater evolves under different assumptions of rain and

- 2 snow recharge efficiencies.
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4 Synthetic time series are generated for precipitation, isotopic ratio in precipitation and air 5 temperature at a daily timestep. For generating the precipitation time series, the time 6 between two successive precipitation events is assumed to be a Poisson process with the 7 precipitation intensity following an exponential distribution (Botter et al., 2007; Rodriguez-8 Iturbe et al., 1999). Time series of air temperature and of isotopic ratios in precipitation are 9 obtained by generating an uncorrelated Gaussian process with the mean following a sine 10 function (to emulate a seasonal signal) and with constant variance (Allen et al., 2018; Parton 11 and Logan, 1981). The separation of precipitation into rainfall (P_r) and snowfall (P_s) is done 12 based on a temperature threshold approach (Harpold et al., 2017a), where the fraction of 13 rainfall $f_r(t)$ at time step t is computed as a function of air temperature T(t):

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$$f_r(t) = \begin{cases} 0 \text{ if } T(t) < T_L \\ \frac{T(t) - T_L}{T_H - T_L} & \text{if } T_L \le T(t) \le T_H \\ 1 & T(t) > T_H, \end{cases}$$

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17 where T_L and T_H are the lower and upper threshold bounds. A double air temperature 18 threshold approach has been shown to be more accurate than a single temperature threshold 19 (Harder and Pomeroy, 2014; Harpold et al., 2017a, 2017b). In this case study, T_L and T_H are 20 set to -1 °C and +1 °C. The evolution of the snow water equivalent (SWE) in the snowpack (h_s) 21 is computed as:

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$$\frac{dh_s(t)}{dt} = P_s(t) - M_s(t),$$
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where M_s is the magnitude of snowmelt, computed using a degree-day approach as proposed by Schaefli et al., (2014):

28
$$M_s = \begin{cases} a_s(T(t) - T_m), & \text{if } T(t) > T_m \\ 0 & \text{otherwise} \end{cases}$$
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30 where a_s is the degree-day factor (set here to 2.5 mm/°C/day) and T_m is the threshold 31 temperature at which snow starts to melt (set to 0 °C). Enhanced heat exchange processes 32 happening during rain-on-snow events are not explicitly considered as this lies beyond the 33 scope of this paper. The snowpack is assumed to be fully mixed, and the isotopic ratio of 34 snowpack is computed as:

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$$\frac{d(h_s(t)C_s(t))}{dt} = C_p(t)P_s(t) - C_s(t)M_s(t),$$
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where C_s is the isotopic ratio of snowpack and C_p is the isotopic ratio of precipitation. The amount of groundwater recharge (R) is the sum of groundwater recharged from rainfall and snowmelt:

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$$R(t) = R_r P_r(t) + R_s M_s(t),$$
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where R_r and R_s are the rainfall and snowmelt recharge efficiencies. Recharge efficiency is defined as the fraction of rainfall or snowmelt that reaches groundwater and is assumed to be a constant value. The groundwater storage is assumed to be fully mixed, and the isotopic ratio of groundwater is computed as:

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$$\frac{d(G(t)C_g(t))}{dt} = R_r C_p(t) P_r(t) + R_s C_s(t) M_s(t) - C_g(t) Q(t),$$
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8 where C_g is the isotopic ratio in groundwater, G is the volume of groundwater and Q is the 9 amount of groundwater outflow to the stream defined as:

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 $Q(t) = k(G(t) - G_C),$ 20

where k is the recession coefficient and G_C is a constant groundwater storage that does not interact with the stream (added here to avoid zero storage and thus very small outflow). This formulation follows the linear groundwater reservoir assumption used in numerous hydrological modeling frameworks (Beven, 2011). The volume of the groundwater storage is computed as:

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$$\frac{dG(t)}{dt} = R(t) - Q(t).$$
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The model is run for a period of 100 years, allowing the system to reach a long term steady state. The parameters used to generate daily precipitation, air temperature and precipitation isotopic ratios are shown in Table 4. The number of yearly precipitation events is set to 30. The snow accumulation and the degree-day snowmelt models are then used to compute the number of snowfall days and of snowmelt events. The static volume of groundwater that does not interact directly with the stream, *G_c*, is set to 1000 mm.

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28 Only the last 2 years of the model runs are used to obtain the time series of isotopic ratios in 29 rainfall, snowmelt and groundwater. These years are then used to estimate the mixing ratio of snowmelt in groundwater, which is the fraction of groundwater recharged from snowmelt. 30 31 Rainfall and snowmelt samples are the two sources and groundwater samples represent the 32 mixture. For the HydroMix application, all the modeled rainfall and snowmelt samples 33 generated using the hydrologic model are used, whereas for groundwater, only one isotopic 34 ratio per month is used (randomly sampled). The mixing ratios inferred using HydroMix are 35 compared to the actual recharge ratio obtained from the hydrologic model as: 36

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$$R_s^a = \frac{\sum_t R_s M_s(t)}{\sum_t R(t)}$$
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where R_s^a represents the proportion of groundwater recharge derived from snowmelt, summed over all the time steps. The numerical implementation of the evolution of isotopic ratio in snowpack and groundwater are given in the Appendix.

- 42
- 43 3.3 Weighting mixing ratios in the hydrologic model
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1 In Section 3.2, rainfall and snowmelt samples are not weighted by the magnitude of their 2 fluxes while computing the mixing ratios with HydroMix. As all rainfall and snowmelt samples 3 are used, the weights are implicitly determined by the number of rainfall and snowmelt 4 events, instead of their magnitudes. This is a general problem in all mixing approaches and 5 has not been adequately acknowledged in the literature. Ignoring the weights may lead to 6 biased mixing estimates if the proportional contribution of one of the components (e.g.: 7 rainfall or snowmelt) is low, but the number of samples obtained to represent that component 8 is proportionally much higher (Varin et al., 2011). For example, in a given catchment, the 9 amount of total snowfall maybe a small proportion of the annual precipitation, but the 10 number of days when snowmelt occurs maybe comparable to the total number of rainfall days 11 in a year. If this is not specified a priori, HydroMix may overestimate the proportion of 12 groundwater being recharged from snowmelt. To account for this, we introduce a weighting 13 factor in the likelihood function originally formulated in Eq. (8), to make a new composite 14 likelihood (Varin et al., 2011):

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$$L_j(\tilde{Y}_{obs}|P_1, P_2, \boldsymbol{\theta}) = \prod_{k=1}^q \prod_{j=1}^m \prod_{i=1}^n \left[(2\pi\sigma^2)^{-0.5} \exp\left(-\frac{1}{2} \frac{(\tilde{Y}_{obs}^k - \hat{Y}_{ij})^2}{\sigma^2}\right) \right]^{w_i w_j},$$
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where *i* and *j* correspond to snowmelt and rainfall samples, and the weights w_i and w_j reflect the proportion of snowmelt and rainfall contributing to groundwater recharge (Vasdekis et al., 2014), where w_i is expressed as:

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$$w_i = \frac{R_i S_i}{\sum_{i=1}^n R_i S_i}$$
, 24

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where R_i is the snowmelt magnitude and S_i is the isotopic ratio of the *i*th snowmelt event. Rain weights (w_j) are also expressed similarly to Eq. (24). The obtained mixing ratio estimates are then compared with the unweighted estimates (in Section 3.2) to see if weighting by magnitude makes a significant difference.

- 29 3.4 Real case study: Snow ratio in groundwater in Vallon de Nant
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The objective of this case study is to infer the proportional contributions of snow versus
rainfall to the groundwater of an Alpine headwater catchment, Vallon de Nant (Switzerland),
using stable water isotopes.

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35 3.4.1 Catchment description

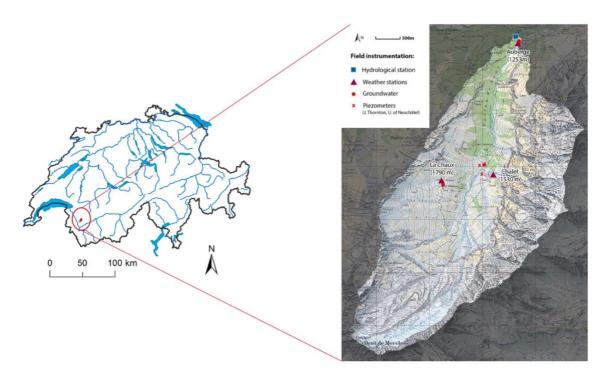
36

Vallon de Nant is a 13.4km² catchment located in the Vaud Alps in South-West of Switzerland 37 38 (Figure 1), with elevation ranging from 1253 m to 3051 m asl. Steep slopes form a major part 39 of the catchment with a mean catchment slope of around 36° (Thornton et al., 2018). At lower 40 elevations, a dense forest dominated by Picea abies covers 14% of the catchment area. At 41 around 1500 m asl., there is an active pasture area with scattered trees and an open forest 42 dominated by Larix decidua. Additional species scattered throughout the catchment include 43 Pinus sp., Alnus sp. and Acer pseudoplatanus. Alpine meadows cover most of the higher 44 elevation land surfaces. Despite the relatively low elevation, there is a small glacier on its 45 South-western tip, which covers around 4.4% of the catchment area, below which an extended moraine occupies 10.1% of the catchment area. A large part (28% of catchment
area) of the hillslopes are composed of steep rock walls. At lower to mid-elevations, talus
slopes account for about 6% of the catchment area.

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5 Vallon de Nant has a typical Alpine climate, with around 1900 mm of annual precipitation and

- a mean air temperature of 1.8 °C (Michelon, 2017). For this paper, long term climate statistics
 are computed using MeteoSwiss gridded precipitation and air temperature dataset from
- 8 1961-2015 (Isotta et al., 2013; MeteoSwiss, 2016, 2017). Applying a simple temperature
- 9 threshold (0 and 1 °C) to observed precipitation indicates that on average, 40-45% of the total
- 10 precipitation falls as snow in the catchment. There is a small degree of seasonality in
- 11 precipitation, with higher precipitation between June to August, and lower precipitation in the
- 12 months of September and October.



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Figure 1. Map showing Vallon de Nant along with the locations of meteorologic and hydrologic observations and the frequent sampling sites. Composite samples of precipitation were collected at the weather stations. Groundwater samples were collected at the groundwater monitoring points and the installed piezometers. The groundwater piezometers were installed by James Thornton from University of Neuchâtel (Thornton et al., 2018).

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21 3.4.2 Data collection

22

Vallon de Nant has been extensively monitored since February 2016. Water samples are collected from streamflow, rain, snowpacks and groundwater at different elevations, which are then analyzed for the isotopic ratios in deuterium (δ^2 H) and oxygen-18 (δ^{18} O). Vallon de Nant is remotely located with very limited winter access, frequently experiencing winter avalanches. Due to these logistical constraints, snowmelt lysimeters or passive capillary samplers could not be setup to sample snowmelt water; accordingly, grab snowpack samples are used here as a proxy for snowmelt. A summary of the isotopic data is shown in Table 1.

Table 1. Summary of the isotopic data (δ^2 H and δ^{18} O) collected in Vallon de Nant between

3 February 2016 to July 2017

4

Sample name	Number of samples	Lowest elevation	Highest elevation
Rainfall	32	1253	1773
Top snowpack layer	80	1241	2455
Groundwater	22	1253	1779

5

6 3.4.3 Model implementation

7

8 HydroMix is used to estimate the proportion of snow recharging groundwater (subsequently 9 referred to as 'snow recharge coefficient'). In order to obtain a pdf of the snow recharge 10 coefficient, isotopic ratios in all the water samples from rain, snowpack and groundwater are 11 used. A uniform prior distribution is assigned to the snow recharge coefficient, which varies 12 between 0 and 1, representing the entire range of possible values.

13

14 3.5 Introduction of an additional model parameter

15

16 In any mixing analysis, it may be useful or desirable for users to specify an additional model 17 parameter that is able to modify the tracer concentrations based on their process 18 understanding of the system. In the case of Alpine catchments with large elevation gradients, 19 stable isotopes in precipitation often exhibit a systematic trend with elevation, becoming 20 more depleted in heavier isotopes with increasing elevation. This is also known as the 'isotopic 21 lapse rate' (Dansgaard, 1964; Friedman et al., 1964). In typical field campaigns, because of 22 logistical challenges, precipitation samples are collected only at a few points in a catchment, 23 with often fewer precipitation samples at high elevations. This leads to oversampling at lower 24 elevations, and under sampling at higher elevations, which can bias mixing estimates. This has 25 been found specially relevant for hydrograph separation in forested catchments (Cayuela et 26 al., 2019). To allow a process compensation for this, an additional lapse rate factor is 27 introduced in which each observed point scale sample (observed at a given elevation) is 28 corrected to a reference elevation as follows:

29

30
$$\bar{r} = \frac{\sum_{j=1}^{k} [\alpha(e_j - e_j)]}{\sum_{j=1}^{k} a_j}$$

 $+r]a_j$

31

where r is the isotopic ratio in precipitation collected at elevation e, \bar{r} is the catchment averaged isotopic ratio in precipitation, α is the isotopic lapse rate factor, e_j is the elevation of the *j*-th elevation band, and a_j is the catchment area under the *j*-th elevation band, where the catchment is divided into k elevation bands. These bands are obtained by constructing a hypsometric curve of the catchment (Strahler, 1952).

37

The lapse rate factor is allowed to modify both rainfall and snowpack isotopic ratios to obtain a catchment averaged isotopic ratio, which is then used in the mixing model. Using this formulation of an isotopic lapse rate makes the following implicit assumptions: (1) precipitation storms on aggregate move from the lower part of the catchment to the upper part of the catchment thus creating a lapse rate effect, and (2) precipitation falls uniformly

over the catchment. It is important to note that the isotopic lapse rate is different from the
precipitation lapse rate, i.e., the rate of change of precipitation with elevation is different from
the rate of change of precipitation isotopic ratio with elevation.

4

5 It is important to note that precipitation isotopic ratio is not only a function of elevation, but 6 also depends on other factors such as the source of moisture origin, cloud condensation 7 temperature, secondary evaporation, etc. Similarly, a strong spatial variability exists in the 8 isotopic ratio of snowmelt water, depending on catchment aspect, snow metamorphism, wind 9 distribution, etc. This case study is a mere demonstration that HydroMix allows inference of 10 additional parameters that can account for various physical processes that may modify 11 isotopic ratios.

12

13 The prior distribution of the isotopic lapse rate is specified based on isotopic data collected 14 across Switzerland under the Global Network of Isotopes in Precipitation (GNIP) program 15 (IAEA/WMO, 2018). Using the monthly isotopic values collected in between 1966 and 2014, 16 average lapse rate values are obtained for both δ^2 H and δ^{18} O. These were (-)1.94 ‰/100m for

17 δ^{2} H, and (-)0.27 ‰/100m for δ^{18} O (Beria et al., 2018).

18

19 A uniform prior distribution is assigned to the isotopic lapse rate parameter, with the lower 20 bound specified as three times the Swiss lapse rate for both $\delta^2 H$ and $\delta^{18} O$. The observed 21 isotopic lapse rate data from Switzerland suggests average lapse rates are weakly negative; 22 however, positive lapse rates can a priori not be excluded for the case study catchment. 23 Accordingly, we do not specify an upper lapse rate bound of zero but set it as three times the 24 Swiss lapse rate (Table 2). In the case of Vallon de Nant, the elevation ranges from 1253 m to 25 3051 m asl. For computing the Swiss lapse rate, the elevation range over which the monthly 26 precipitation samples were collected was 300 m to 2000 m asl. This difference in elevation 27 ranges between Vallon de Nant and the GNIP network should be kept in mind during 28 interpretation of results.

29

30 **Table 2.** Prior distribution of the different model parameters as specified to HydroMix

31

Variable	Prior distribution	Lower bound	Upper bound
Snow recharge coefficient	Uniform	0	1
Isotopic lapse rate in $\delta^2 H$	Uniform	(-)5.82 ‰/100m	(+)5.82 ‰/100m
Isotopic lapse rate in δ^{18} O	Uniform	(-)0.81 ‰/100m	(+)0.81 ‰/100m

- 32 4 Results
- 33

34 The results for the different case studies are discussed in the sections below.

35

36 4.1 Mixing with normal distributions

37

The mean and standard deviations used to generate the low and high variance source distributions for the synthetic case studies are summarized in Table 3. We randomly generated 100 samples from each of the two source distributions and from the target distribution, and varied the mixing ratios between 0.05 and 0.95 in 0.05 increments. It should be noted that

42 HydroMix permits using different number of samples for the sources and for the mixture.

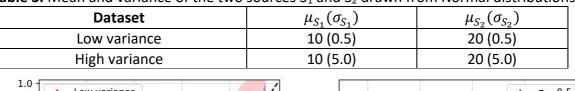
2 For the low variance case, the mixing ratio inferred with HydroMix with 1000 MCMC 3 simulations reproduce closely the theoretical mean of the mixing ratios used to generate the 4 synthetic data (Figure 2a). However, for the high variance case, the inferred mixing ratios do 5 not match the true underlying mixing ratios, especially for low and high mixing ratios. This is 6 partly due to the poor identifiability of the sources (given that their distributions are highly 7 overlapping), and partly due to the relatively small sample size of 100. The inferred mean 8 should reproduce the theoretical mean with increasing sample size and we clearly see this for 9 the low variance case in Figure 2b, where the model performance markedly improves with 10 increasing number of samples. The performance is measured here in terms of the absolute 11 error between the posterior mixing ratio mean and the true mean, summed and averaged 12 over all tested ratios from 0.05 to 0.95. We did not perform inferences for sample sizes larger 13 than 100 as the computational requirement increases exponentially with increasing sample 14 sizes.

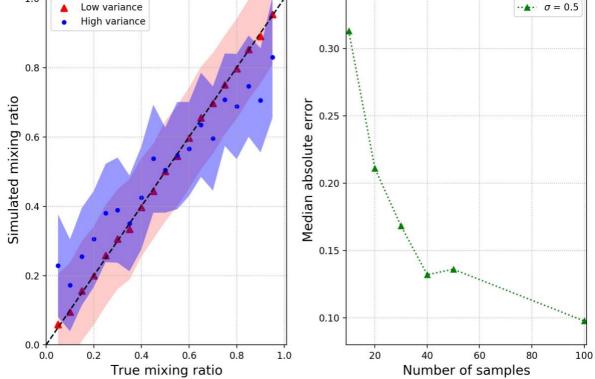
15

The model converges fairly quickly for the low variance case after ~100 runs as shown in Figure
3(a). The obtained model residuals have zero mean and are approximatively normally
distributed as revealed by quantile-quantile plots (not shown), in line with the assumption of

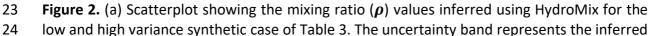
19 an unbiased normally distributed error model, as stated in Eq. 7.

- 20
- 21 Table 3. Mean and variance of the two sources S₁ and S₂ drawn from Normal distributions

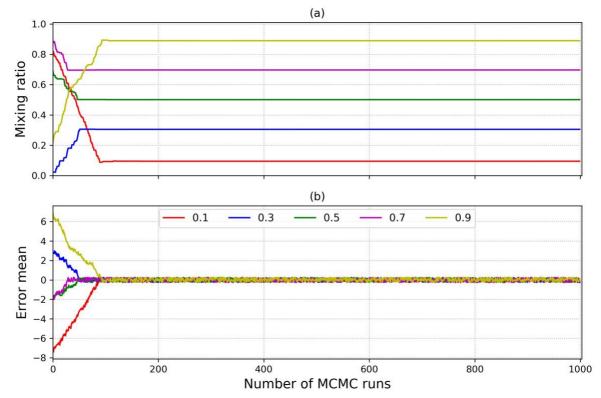








- 1 mixing ratio ± error standard deviation obtained from Eq. 13. The number of source and target
- 2 samples are 100. (b) Performance of HydroMix in terms of the absolute error between the
- 3 posterior mixing ratio mean and the true mean for the low variance dataset, over all tested
- 4 ratios plotted as a function of the number of samples drawn for the two sources.



5 6 Figure 3. Diagnostic plots showing the convergence characteristics of MCMC chains for five 7 different mixing ratios for the low variance dataset (shown in Table 3). Subplots (a) and (b) 8 show variations in the inferred mixing ratio and the error mean with increasing MCMC runs. 9

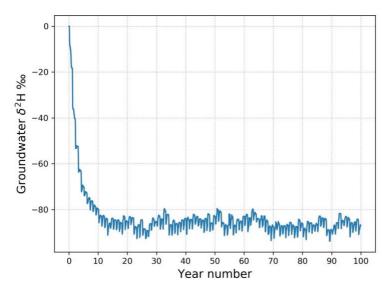
4.2 Contribution of rain and snow to groundwater recharge using a hydrologic model 11

12 Figure 4 shows the variation in the isotopic ratio of groundwater over the entire 100 year 13 period, showing the system achieves a steady state condition after ~15 years of simulation. 14 The mixing ratio is estimated with HydroMix using: (1) samples of the isotopic ratio in snowfall, 15 and (2) samples of the isotopic ratio in snowmelt. The two sample distributions differ, as 16 shown in Figure 5, where the variability of the isotopic ratio is lower in snowmelt when 17 compared to snowfall. In the model at hand, this reduction is obtained because of mixing 18 occurring within the snowpack, leading to homogenization, thus reducing the variability in the 19 isotopic ratio of snowmelt. In field data, such a reduction in variability is also generally 20 observed (Beria et al., 2018), as a result of the homogenization as modelled here and from 21 more complex snow physical processes, which lie beyond the scope of this study.

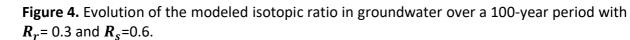
22 23

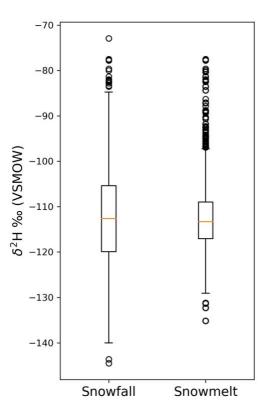
24 Table 4. Parameters used to generate time series of precipitation, air temperature and 25 isotopic ratios in precipitation. μ represents the mean, A is the amplitude and ϕ the time lag 26 of the underlying sine function. For the precipitation process, μ is the mean intensity on days 27 with precipitation. The resulting mean winter length (air temp. below 0°C) is 119.5 days.

Variable	Parameter values
Precipitation	# events/year = 30, μ = 33.45 mm/day
Air temperature	μ = 4 °C, A = 8 °C, ϕ = - $\pi/2$
Precipitation isotopic ratio	μ = (-80) ‰, A = 40 ‰, ϕ = - $\pi/2$









7

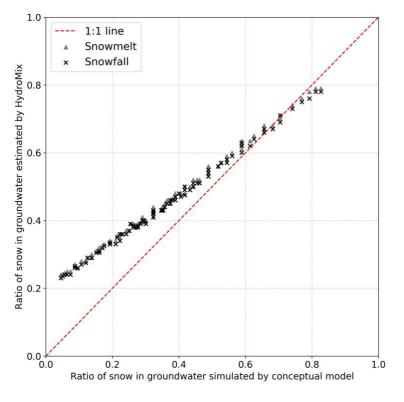
Figure 5. Boxplot showing the variability in the isotopic ratio of snowfall and snowmelt as simulated by the hydrologic model. The boxplot extends from 25th to 75th percentile value, with the median value depicted by the orange line. The whiskers extend up to 1.5 times of the interquartile range. The black circles are the outliers.

The mixing ratios inferred with HydroMix are very similar regardless of whether snowfall or snowmelt is used across the entire range of recharge efficiencies (Figure 6). This provides confidence in the use of snowfall samples as a proxy for snowmelt when estimating mixing ratios. However, it is clear from Figure 6 that an important bias emerges between the estimated mixing ratio from HydroMix and the actual mixing ratio known from the hydrologic model, especially for low mixing ratios.

8

9 This bias can be expected to emerge where the source contributions are not weighted 10 according to their fluxes, which to our knowledge has not been explicitly addressed in the 11 hydrological literature. As already discussed in Section 3.3, the absence of sample weighting 12 typically induces a bias when there is a large divergence between the number of samples taken 13 over a certain period (e.g. one year) to characterize a source, and the magnitude of source 14 flux over that period (e.g. 40 snow and 10 rain samples taken to characterize the two sources, 15 where snow only accounts for a very small portion (e.g. 10%) of the annual precipitation).

16



17 18

Figure 6. Ratios of snow in groundwater estimated with HydroMix plotted against ratios obtained from the hydrologic model for the last two years of simulation. Also shown are the separate results obtained by using samples of either snowmelt or snowfall. The full range of ratios is obtained by varying rainfall and snowmelt recharge efficiencies from 0.05 to 0.95. The number of rainfall, snowfall and snowmelt days are 39, 24 and 107 in the last two years of simulation.

25

27

26 4.3 Effect of weights on estimates of mixing ratios using a hydrologic model

After taking into account the magnitude of rainfall and snowmelt events in the composite likelihood function of Eq. (23), it is clear that much of the un-weighted biases can be removed 1 (Figure 7). The most significant improvement is seen at very low mixing ratios where the 2 divergence between the conceptual model and the mixing model estimates error reduces by 3 almost 50%. In this study, we have used a relatively simple normalization based weighting 4 function (Eq. (25)). Testing other weighting functions which have been proposed in the past 5 (Vasdekis et al., 2014) is left for future research.

- 1.0 1:1 line Unweighted Ă Weighted Ratio of snow in groundwater estimated by HydroMix 0.8 0.6 0.4 0.2 0.0 / 0.0 0.4 0.8 1.0 0.2 0.6 Ratio of snow in groundwater simulated by conceptual model
- 7 8

6

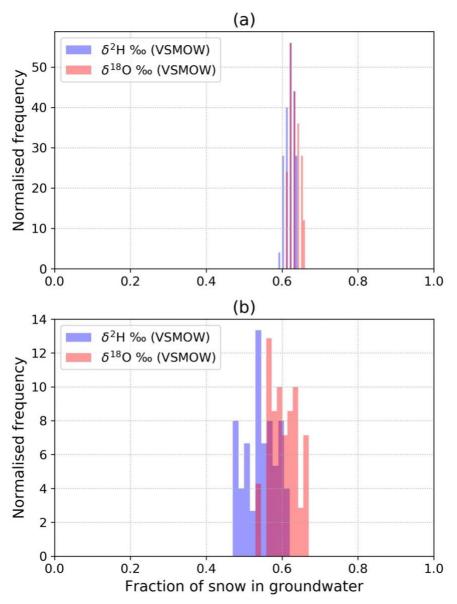
Figure 7. Ratios of snow in groundwater estimated using HydroMix plotted against ratios
 obtained from the hydrologic model, for both weighted and unweighted mixing scenarios. The
 full range of ratios is obtained by varying rainfall and snowmelt recharge efficiencies from 0.05
 to 0.95. The number of rainfall, snowfall and snowmelt days are 39, 24 and 107 in the last two
 years of simulation.

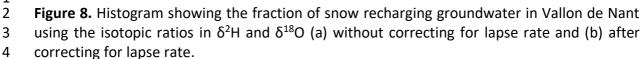
14

4.4 Inferring fraction of snow recharging groundwater in a small Alpine catchmentalong with an additional model parameter

17

18 Using the dataset from an Alpine catchment (Vallon de Nant, Switzerland), HydroMix 19 estimates that 60-62% of the groundwater is recharged from snowmelt (using unweighted 20 approach), with the full posterior distributions shown in Figure 8a. This estimate is consistent for both the isotopic tracers (δ^2 H and δ^{18} O), which are often used interchangeably in the 21 22 hydrologic literature (Gat, 1996). Comparing this recharge estimate to the proportion of total 23 precipitation that falls as snow (around 40-45%, see Section 3.4.1), suggests that snowmelt is 24 more effective at reaching the aquifer than an equivalent amount of rainfall falling at a 25 different period of the year. Similar results have been obtained in a number of previous 26 studies across the temperate and mountainous regions of the world (see Table 1 in the work 27 of Beria et al., (2018) for a summary).





5

6 As can be seen from Figure 8a, the estimated distribution of snow ratio in groundwater is very 7 narrow. This can be explained by the fact that we assume that the collected precipitation 8 samples represent the variability actually occurring in the catchment. To overcome this 9 limitation, we infer an additional parameter called the isotopic lapse rate that accounts for 10 the spatial heterogeneity in terms of catchment elevation. As shown in Figure 9, the posterior 11 distributions of the isotopic lapse rate (for both δ^2 H and δ^{18} O) largely overlap with the spatially 12 averaged isotopic lapse rate as estimated from precipitation isotopes across Switzerland. The 13 overlap with the average Swiss isotope lapse rate suggests our inferred lapse rates are 14 reasonable, with the spread in the estimates likely reflecting the temporal variation in the 15 catchment specific isotope lapse rate that can develop from a wide range of moderating 16 factors (e.g. air masses contributing precipitation without traversing the full elevation range 17 of the catchment due to varying trajectories). The Swiss lapse rate is constructed as a long

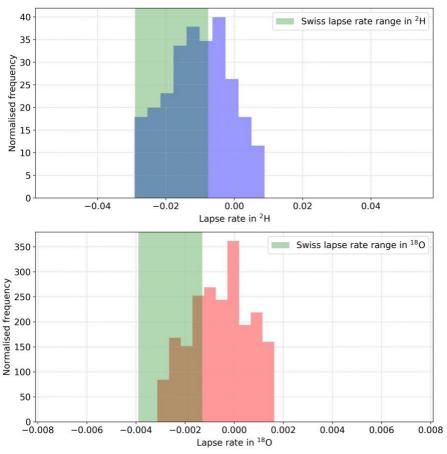
term spatial average, whereas the inferred isotopic lapse rate in Vallon de Nant is constructed from the temporal variations in the isotopic ratios. These results demonstrate that it is relatively straightforward to jointly infer multiple parameters within the HydroMix modeling framework.

5

However, an important consequence of additional parameter inference without providing
 additional data or constraints is an increase in the degree of freedom, which can then increase

8 the uncertainty on source contributions. This effect is seen in Figure 8b, especially in contrast

- 9 with the previous result in Figure 8a, where the median mixing ratios of the posterior
- 10 distributions remain similar (~0.6), but the spread increase drastically, from 0.005 to 0.2.
- 11



12

Figure 9. Histogram showing the posterior distribution of the isotope lapse rate parameter in δ^2 H and δ^{18} O. The green region shows the confidence bounds (significant at α =0.01) of lapse rate computed over Switzerland by using inverse variance weighted regression. Limits of the prior distribution of the isotopic lapse rates correspond to limits of the x-axis. The slope of the isotopic ratio when plotted against elevation for the Swiss-wide data is shown in Figure 3 of Beria et al. (2018).

19

20 5 Limitations and opportunities

21

As with all linear mixing models, the quality of the underlying data determines the accuracy and utility of the results. If the tracer compositions of the different sources are not sufficiently distinct the uncertainty in the estimated mixing ratios will become your large. This means that

24 distinct, the uncertainty in the estimated mixing ratios will become very large. This means that

if either the underlying data quality is poor, or the source contribution dynamics are not well
 conceptualized, then the uncertainty in the mixing ratios will be too high to be useful.

3

4 In cases where a large number of source samples are available, the computational 5 requirements of HydroMix outweigh the benefit from using it. These are likely cases where 6 the statistical distribution of the source tracer composition is well understood, therefore 7 fitting a probability density curve to the source and target samples, and then inferring the 8 distribution of the mixing ratio using a probabilistic programming approach is more 9 appropriate (Carpenter et al., 2017; Parnell et al., 2010; Stock et al., 2018). Also HydroMix 10 might not be an appropriate method in instances where fitting statistical distributions to 11 source and target compositions reflect *a priori* knowledge of the system.

12

13 A key difference between HydroMix and other Bayesian mixing approaches is that HydroMix 14 parameterizes the error function whereas other Bayesian approaches parameterize the 15 statistical distribution of source and mixture compositions. Parameterizing source 16 compositions require large sample sizes, which is seldom the case in tracer hydrology. Error 17 parameterization offers a useful alternative and can be also verified against the posterior error 18 distribution. In the case studies demonstrated in this paper, a normally-distributed error 19 model was found to be appropriate. However, error models other than Gaussian can be used 20 by formulating the respective likelihood function.

21

22 HydroMix builds the model residuals by comparing all the observed source samples with all 23 the observed samples of the target mixture, assuming that all available source and target 24 samples are independent. Interestingly, the assumption of independence holds even if the 25 source and target samples are taken at the same time, since the target samples result from 26 water that has travelled for a certain amount of time in the catchment, and hence is not 27 related to the water entering the catchment. However, if a system has instantaneous mixing, 28 then the source and target samples taken at the same moment of time will necessarily be 29 strongly correlated. In such cases, the assumption of independent samples would not make 30 sense and the method might give spurious results.

31

Finally, it is noteworthy that adding additional parameters to characterize the source tracer composition increases the degree of freedom of the model, which implies that adding such parameters leads to an increase in the uncertainty of the source contribution estimates unless new information, i.e. new observed data, is added to the model. This means that users who are interested in incorporating additional modification processes by adding parameters should ideally provide additional tracer data able to constrain this process, subject to tracer data being available.

39

40 For consistency and simplicity, the case studies and synthetic hydrological examples provided 41 here focused on the contribution of rain and snow in recharging groundwater. However, it is 42 important to emphasize that the opportunities to implement HydroMix extend to all cases 43 where mixing contributions are of interest, and where it is difficult to build extensive 44 databases of source tracer compositions. Such examples include quantifying the amount of 45 "pre-event" vs. "event water" in streamflow, where "pre-event water" refers to groundwater 46 and "event water" refers to rainfall or snowmelt. Another interesting use case might be to 47 quantify the proportion of streamflow coming from the different source areas in a catchment, to capture the spatial dynamics of streamflow. Other uses include quantifying the amount of fog contributing to throughfall, the proportion of glacial melt vs. snowmelt flowing into a stream, the amount of vegetation water use from soil moisture at different depths vs groundwater, the interaction between surface water and groundwater at the hyporheic zone (Leslie et al., 2017), sediment fingerprinting to quantify the spatial origin of river sediments, etc. In all of these cases, understanding source water contributions, both spatially and temporally, will improve the physical understanding of the system.

8

9 6 Conclusions

10

11 We develop a new Bayesian modeling framework for the application of tracers in mixing 12 models. The primary application target of this framework is hydrology, but it is by no means 13 limited to this field. HydroMix formulates the linear mixing problem in a Bayesian inference 14 framework that infers the model parameters using a Metropolis-Hastings based MCMC 15 sampling algorithm, based on differences between observed and modelled tracer 16 concentrations in the target mixture, using all possible combinations between all source and target concentration samples. This is especially useful in data scarce environments where 17 18 fitting probability distribution functions is not feasible. HydroMix also makes the inclusion of 19 additional model parameters to account for source modification processes straightforward. 20 Examples include known spatial or temporal tracer variations (e.g. isotopic lapse rates or 21 evaporative enrichment).

22

An evaluation of HydroMix with data from different synthetic and field case studies leads tothe following conclusions:

- 25
- 1. HydroMix gives reliable results for mixing applications with small sample sizes (< 20-30 samples). As expected, the variance in source tracer composition and the ensuing composition overlap determines the bias in the mixing ratio estimates. The bias in mixing ratio estimates increases with increasing variance in source tracer compositions. Mixing ratio estimates improve (in terms of lower error) with increasing number of source samples.
- 2. As revealed by our synthetic case study with a conceptual hydrological model, at low
 source contributions (i.e. < 20%), a strong divergence between the actual and
 estimated mixing ratios emerges. This arises if HydroMix assigns equal weights to all
 source samples proportionally oversampling the less abundant source, which then
 leads to significant biases in mixing estimates. This problem is inherent to all mixing
 approaches, and to our knowledge has not been adequately addressed in the
 literature.
- 3. The use of composite likelihoods to weight samples by their amounts can significantly
 reduce the bias in the mixing estimates. At low source proportions, the estimated
 mixing ratio improves by more than 50% after accounting for the amount of all the
 sources. We show this using a simple normalization based weighting function. Future
 studies should explore the usage of different weighting functions that have been
 proposed in the past (Vasdekis et al., 2014).
- 4.A synthetic application of HydroMix to understand the amount of snowmelt induced
 groundwater recharge, revealed that using snowfall isotopic ratio instead of snowmelt

isotopic ratio leads to similar mixing ratio estimates. This is particularly useful in high
 mountainous catchments, where sampling snowmelt is logistically difficult.

5. A real case application of HydroMix in a Swiss Alpine catchment (Vallon de Nant) showed a clear winter bias in groundwater recharge. About 60-62% of the groundwater is recharged from snowmelt (unweighted mixing approach), when snowfall only accounts for 40-45% of the total annual precipitation. This has also been previously suggested elsewhere in the European Alps (Cervi et al., 2015; Penna et al., 2014, 2017; Zappa et al., 2015).

8 9

3

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To conclude, HydroMix provides a Bayesian approach to mixing model problems in hydrology
 that takes full advantage of small sample sizes. Future work will show the full potential of this
 approach in hydrology as well as other environmental modelling applications.

13

14 7 Appendix

15

The equations below show the numerical implementation of the evolution of isotopic ratios
in snowpack, isotopic ratios in groundwater, and groundwater storage at a daily timestep.

19
$$C_s(t) = \frac{C_s(t-1)h_s(t-1)+C_p(t)P_s(t)-C_s(t-1)M_s(t)}{h_s(t-1)+P_s(t)-M_s(t)}$$
 26

21
$$C_g(t) = \frac{C_g(t-1)G(t-1) + C_p(t)R_rP_r(t) + C_s(t)R_sM_s(t) - C_g(t-1)Q(t)}{G(t-1) + R_rP_r(t) + R_sM_s(t) - Q(t)}$$
27

 $G(t) = G(t - 1) + R_r P_r(t) + R_s M_s(t) - k(G(t) - G_c)$

24 25

26 Author contributions

The paper was written by HB with contributions from all co-authors. HB and BS formulated the conceptual underpinnings of HydroMix. JRL helped in framing the statistical and hydrological tests to evaluate HydroMix. AM and NCC helped in compiling data used for model evaluation and provided critical feedback during model validation.

31

32 Code and data availability

33 The model code is implemented in python 2.7 and can be downloaded along with the

- dataset from Zenodo at <u>http://doi.org/10.5281/zenodo.3475429</u>. The most recent version of
- 35 the model code is available on GitHub at
- 36 <u>https://github.com/harshberia93/HydroMix/tree/20191007_GMD</u>.
- 37

38 **Competing interests**

- 39 The authors declare that they have no conflict of interest.
- 40

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