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HydroMix v1.0: a new Bayesian mixing framework for attributing uncertain hydrological 1 2 sources

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9

10 Abstract

11 Tracers have been used for over half a century in hydrology to quantify water sources with 12 the help of mixing models. In this paper, we build on classic Bayesian methods to quantify 13 uncertainty in mixing ratios. Such methods infer the probability density function (pdf) of the 14 mixing ratios by formulating pdfs for the source and target concentrations and inferring the 15 underlying mixing ratios via Monte Carlo sampling. However, collected hydrological samples are rarely abundant enough to robustly fit a pdf to the sources. Our approach, called 16 17 HydroMix, solves the linear mixing problem in a Bayesian inference framework where the 18 likelihood is formulated for the error between observed and modelled target variables, which 19 corresponds to the parameter inference set-up commonly used in hydrological models. To 20 address small sample sizes, every combination of source samples is mixed with every target 21 tracer concentration. Using a series of synthetic case studies, we evaluate the performance of 22 HydroMix. We then use HydroMix to show that snowmelt accounts for 60-62% of 23 groundwater recharge in a Swiss Alpine catchment (Vallon de Nant), despite snowfall only 24 accounting for 40-45% of the annual precipitation. Using this example, we then demonstrate 25 the flexibility of this approach to account for uncertainties in source characterization due to 26 different hydrological processes. We also address an important bias in mixing models that 27 arises when there is a large divergence between the number of collected source samples and 28 their flux magnitudes. HydroMix can account for this bias by using composite likelihood 29 functions that effectively weights the relative magnitude of source fluxes. The primary 30 application target of this framework is hydrology, but it is by no means limited to this field.

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33 Keywords: stable water isotopes; hydrograph separation; isotopic lapse rate; rain; snow;

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Introduction 1 1

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3 Most water resources are a mixture of different water sources that have travelled via distinct 4 flow paths in the landscape (e.g. streams, lakes, groundwater). A key challenge in hydrology 5 is to infer source contributions to understand the flow paths to a given water body using a 6 source attribution technique. A classic example is the two-component hydrograph separation 7 model to quantify the proportion of groundwater and rainfall in streamflow, often referred to 8 as "pre-event" water vs "event" water (Brewer et al., 2011; Burns et al., 2001; Buttle et al., 9 1995; Dusek and Vogel, 2018; Joerin et al., 2002; Klaus and McDonnell, 2013; Lopes et al., 10 2018; Schmieder et al., 2016; W. et al., 2009). Other examples include estimating the 11 proportional contribution of rainfall and snowmelt to groundwater recharge (Beria et al., 12 2018; Earman et al., 2006; Jasechko et al., 2014, 2017; Jasechko and Taylor, 2015; Jeelani et 13 al., 2010; Kohfahl et al., 2008; O'Driscoll et al., 2005; Rose, 2003; Winograd et al., 1998), fog 14 to the amount of throughfall (Scholl et al., 2011, 2002; Uehara and Kume, 2012), and soil 15 moisture (at varying depths) and groundwater to vegetation water use (Dawson and 16 Ehleringer, 1991; Ehleringer and Dawson, 1992; Evaristo et al., 2016, 2017; Evaristo and 17 McDonnell, 2017; Rothfuss and Javaux, 2017; Vargas et al., 2017; Zhao et al., 2016).

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19 The primary goal of such attribution in hydrology is to infer the contribution of different 20 sources to a target water body, where the tracer can be an observable compound like a dye, 21 or a conservative solute, or even a proxy for chemical composition such as electrical 22 conductivity. The key requirement is that the concentration of the tracer is distinguishable 23 between different sources. The sources are then assumed to linearly mix in the target water 24 body as follows:

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 $\rho_1 S_1^{k} + \rho_2 S_2^{k} + \dots + \rho_n S_n^{k} = Y^k.$

where γ^{k} is the concentration of the k^{th} tracer in the target mixture, S_{k}^{k} is the concentration 28 29 of the k^{th} tracer in source *i*. ρ_i (*i*=1, ..., *n*) are the fractions of all sources in the mixture, with $\sum_{i=1}^{n} \rho_i = 1$. The system of the *n* linear equations can be solved if the number of tracers is *n*-30 31 1, leading to a system of *n* equations and *n* unknown variables.

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33 The stable isotope composition of hydrogen and oxygen in water (subsequently referred to as 34 'stable isotopes of water') are used as tracers in hydrology. Other commonly used tracers include electrical conductivity (Hoeg et al., 2000; Laudon and Slaymaker, 1997; Lopes et al., 35 36 2018; Pellerin et al., 2007; Weijs et al., 2013) and conservative geochemical solutes such as 37 chloride and silica (Rice and Hornberger, 1998; Wels et al., 1991).

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39 Classically, Eq. (1) is solved by assigning an average tracer concentration to each source, 40 estimated typically from time or space-averages of observed field data (Maule et al., 1994; 41 Winograd et al., 1998). Alternatively, Bayesian mixing models can be used, which explicitly 42 acknowledge the variability of source tracer concentrations estimated from observed samples 43 (Barbeta and Peñuelas, 2017; Blake et al., 2018). Rather than a single estimate of source 44 contributions, Bayesian approaches yield full probability density functions (pdfs) of the 45 fraction of different sources in the target mixture (Parnell et al., 2010; Stock et al., 2018), 46 hereafter referred to as 'mixing ratios'.

47





1 Bayesian mixing was first developed in ecology to estimate the proportion of different food 2 sources to animal diets (Parnell et al., 2010; Stock et al., 2018). Hydrological applications of such models are still rare (Blake et al., 2018; Evaristo et al., 2016, 2017; Oerter et al., 2019). In 3 4 a Bayesian mixing model, a statistical distribution is fitted to both the measured source tracer 5 concentrations, and to the measured tracer concentrations from the target (e.g. river, groundwater, vegetation). The distribution of the mixing ratios is then inferred via Bayesian 6 7 inference as follows: Random samples are drawn from the source distributions and from a 8 given prior distribution of the mixing ratios. Based on these samples, the target tracer 9 concentrations are calculated according to Eq. (1). The likelihood of a given (drawn) set of 10 mixing ratios is calculated by comparing the modelled target tracer concentrations with their 11 observed values. With recent advances in probabilistic programming languages like Stan 12 (Carpenter et al., 2017), this has become a relatively simple task. 13 14 However, the key limitation with the above approach is that the source compositions are 15 assumed to come from standard statistical distributions. Typically, the sources are assumed 16 to be drawn from Gaussian distributions, which can be fully characterized by the mean and 17 variance of the data available for each source (Stock et al., 2018). This limits both the potential 18 applicability and the insight that can be gained from tracer information in hydrology because: 19 20 1) The mean and variance may not accurately reflect the statistical properties of the 21 source composition. 22 2) If there is a large amount of information on the source composition, the mean and 23 variance may be an unnecessary simplification of its variability. 24 3) If the source compositions have a low number of samples, then the mean and variance 25 estimates may be poorly constrained. 26 27 An additional complication in hydrology comes from the fact that observed point-scale 28 samples do not necessarily capture the tracer concentrations in the actual sources, which are 29 spatially distributed and whose contribution can be temporally variable depending on the 30 state of the catchment (Harman, 2015). For instance, if we were to characterize the 31 contribution of snowmelt to groundwater, we need to capture (1) the temporal evolution of 32 the isotopic ratio of snowmelt, which strongly varies in space (Beria et al., 2018; Earman et al., 33 2006), and (2) the temporal evolution of the area actually covered by snow. This spatially and 34 temporally distributed nature of the sources can be hard to account for in both the analytical 35 and the Bayesian mixing approaches. 36 To overcome the above limitations, we present a new mixing approach for hydrological 37 38 applications, called HydroMix. This approach does not require a parametric description of 39 observed source or target tracer concentrations. Instead, HydroMix formulates the linear 40 mixing problem in a Bayesian inference framework similar to hydrological rainfall-runoff 41 models (Kavetski et al., 2006a), where the mixing ratios of the different sources are treated as 42 model parameters. Thereby, HydroMix explicitly uses the whole dataset of observed source 43 tracer concentrations instead of reducing it to its few statistical moments. An advantage of 44 this approach is that additional model parameters can be incorporated in the framework to

describe how the source tracer concentrations might be modified according to specifichydrologic processes that can be decided and explored by the user.



2



1 In this paper, we first describe the theoretical details of HydroMix for a simple case study with 2 two sources, one mixture and one tracer (Section 2). Section 3 presents synthetic and real-3 world case studies that demonstrate the accuracy, robustness and flexibility of HydroMix. In 4 the synthetic case study, we use a conceptual hydrologic model to simulate tracer 5 concentrations. We also introduce a composite likelihood function that accounts for the magnitude of the different sources. The results of these applications are presented in Section 6 7 4 before summarizing the main outcomes, applicability, and limitations of HydroMix in Section 8 5.

9 2 Model description and implementation

11 This section details the general modeling approach underlying HydroMix for a system with 12 two sources and one tracer. This is followed by a detailed discussion on the choice of the 13 parameter inference approach used.

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15 2.1 Linear mixing model with non-concomitant observed data

For a system with two sources that combine linearly to form a mixture, the mixing model canbe formulated as:

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$$\rho S_1(t) + (1 - \rho)S_2(t) = Y(t + \tau),$$

20

where $S_1(t)$ is the concentration of tracer in source 1 at timestep t, $S_2(t)$ is the concentration 21 22 of tracer in source 2 at timestep t, $Y(t + \tau)$ is the concentration of the mixture (i.e. the tracer 23 concentration in the target) at timestep $t + \tau$, ρ is the mixing ratio and τ is the time delay 24 between the time when source enters the system and the time when it is observed in the 25 mixture. As an example, for a case where the two sources are snowmelt and rainfall and the 26 mixture is groundwater, ρ represents the proportional groundwater recharged from 27 snowmelt and τ represents the average time lag for rain and snowmelt to reach the 28 groundwater once they enter into the soil.

29

The two parameters in this system, the mixing ratio (ρ) and the time delay (τ), can be inferred via classical Bayesian parameter inference which is widely used in hydrology (Kavetski et al., 2006a, 2006b; Schaefli and Kavetski, 2017). This implies taking an observed timeseries of the target (e.g. the tracer concentration in groundwater) and building a vector of model residuals:

where \tilde{Y}_t represents the observed mixture concentration and \hat{Y}_t represents the simulated mixture concentration. However, in real environmental systems like that of groundwater recharge from rainfall and snowmelt, there are four major difficulties which can prevent the inference of ρ and τ from the observed data.

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42 i. ρ and τ strongly vary in time depending on catchment conditions such as soil moisture 43 (Benettin et al., 2017; Harman, 2015)

44 ii.Long time series of the tracer concentration in both the sources and mixture are rare.

45 iii. The effect of seasonality in precipitation can make the inference of τ very difficult in case the 46 goal is to understand the intra-annual recharge dynamics.



4



1 iv.The tracer concentration in the different sources are generally measured at point scales

- 2 whereas the tracer concentration in the target integrates inputs over the entire source area.
- 3 Section 3.5 introduces such an example and proposes a solution in these cases.

5 Our practical solution to limitation ii) is to assume that tracer concentrations in the two 6 sources are functions of observable point processes:

7
8
$$S_i(t) = f_i(P_i(t)),$$

9

14

where the function f_i represents the transformation from the point to the catchment scale for source *i*. Limitation iii) can be relaxed by assuming a long enough timestep (eg: long term groundwater recharge dynamics) or a short enough timestep (eg: event based hydrograph separation (Klaus and McDonnell, 2013)) such that we can neglect τ and write Eq. (2) as:

15
$$\rho S'_1(\Delta t) + (1 - \rho)S'_2(\Delta t) = Y'(\Delta t),$$
 5

16 17 where the ' signifies time-integrated processes. The space- and time-integrated processes S_i 18 are not directly observable. We thus need to make the simplifying assumption that any 19 observed point-scale tracer concentration p_i in a given source *i* (e.g., the isotopic ratio of 20 snowmelt) represents a sample of the space- and time-integrated processes S_i . This 21 assumption is in fact implicitly underlying most of the existing hydrological mixing models 22 where point samples are used to characterize a spatial process and where the time reference 23 of the samples is discarded.

24

By utilizing all the available measurements $\{p'_1\}_{i=1..n}$ and $\{p'_2\}_{j=1..m}$ of the two sources in the above model, with n samples of source 1 and m samples of source 2, we can build $n \times m$ predictions and compare them with the q observed samples of the target as:

$$29 \quad \varepsilon_{ij}^k = \tilde{Y}_{obs}^k - \hat{Y}_{ij}, \tag{6}$$

30

28

where \tilde{Y}_{obs}^k is the *k*-th observed target concentration out of a total number of *q* target concentrations.

33

Assuming that the residuals can be described with a Gaussian error model with a mean of zero and constant variance σ ,

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37
$$\varepsilon \sim N(0,\sigma),$$
 7

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39 we can compute the likelihood function of the residuals as the joint probability of all the 40 residuals:

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42
$$L_j(\tilde{Y}_{obs}|S_1, S_2, \theta) = \prod_{k=1}^q \prod_{j=1}^m \prod_{i=1}^n (2\pi\sigma^2)^{-0.5} \exp(-\frac{1}{2} \frac{(\tilde{Y}_{obs}^k - \hat{Y}_{ij})^2}{\sigma^2}),$$
 8

44 where θ represents all the model parameters. The above Gaussian error model could in 45 principle be replaced with any other stochastic process. However, the Gaussian error model





has been shown to be relatively robust in this kind of an application (Schaefli and Kavetski,
 2017).

3

4 In the case of linear mixing between two sources, the two model parameters considered at 5 this stage are the mixing ratio ρ and the error variance σ . The error variance can either be 6 computed from the observed residuals or be treated as a model parameter (Kuczera and 7 Parent, 1998; Schaefli et al., 2007). For the examples shown in this paper, the error variance 8 is computed from the residuals.

9

10 In order to avoid numerical problems, we use the log-likelihood form of Eq. (8):

11

12
$$\log L_j(\tilde{Y}_{obs}|S_1, S_2, \theta) = \sum_{k=1}^q \sum_{j=1}^m \sum_{i=1}^n -0.5 \left[2\pi\sigma^2 + \frac{\left(\tilde{Y}_{obs}^k - \hat{Y}_{ij}\right)^2}{\sigma^2} \right) \right].$$
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14 2.2 Parameter inference in a Bayesian framework

Following the general Bayes' equation, the posterior distribution of the model parameterscan be written as:

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19
$$p(\theta|S_1, S_2, \tilde{Y}) = \frac{p(\tilde{Y}|\theta, S_1, S_2)p(\theta)}{p(\tilde{Y}|S_1, S_2)},$$
 10

20

where $p(\theta)$ is the prior distribution of the model parameters and $p(\tilde{Y}|\theta, S_1, S_2)$ is the likelihood function. The denominator of Eq. (10) can generally not be computed as that would require integration over the whole parameter space which is computationally expensive, which is why Eq. (10) is reduced to:

25

26
$$p(\boldsymbol{\theta}|S_1, S_2, \tilde{Y}) \propto p(\tilde{Y}|\boldsymbol{\theta}, S_1, S_2)p(\boldsymbol{\theta}).$$
 11
27

28 Two methods are traditionally used in hydrology to infer the posterior distribution from Eq. 29 (11), Markov Chain Monte Carlo (MCMC) sampling and importance sampling. In the case of 30 MCMC sampling, a common approach is the Metropolis algorithm (Kuczera and Parent, 1998; Schaefli et al., 2007; Vrugt et al., 2003). This method is suited when the overall computational 31 32 cost for inferring the posterior distribution is high, either because of a large number of model 33 parameters or a computationally intensive model. In importance sampling, the posterior 34 distribution is obtained from weighted samples drawn from the so-called importance 35 distribution. For typical multivariate hydrological problems, the only possible choices for the importance distribution are either uniform sampling over a hypercube or sampling from an 36 37 over-dispersed multi-normal distribution (Kuczera and Parent, 1998). A stochastic process is defined as over-dispersed when the variance of the underlying distribution is greater than its 38 39 mean (Inouye et al., 2017). The sampling distributions in such cases have large variance, 40 allowing sufficient sampling over the entire parameter range. 41

Given the low number of model parameters in HydroMix, we infer the posterior distribution by random Monte Carlo sampling. The prior distribution of the mixing ratio is assumed to be

44 uniform between 0 and 1. With the uniform prior assumption, the posterior distribution is





dependent only on the likelihood function. In order to compute the posterior distribution, only
 model runs with the highest likelihood score, corresponding to the top 5 percentile of the
 model runs, are retained. This also highlights the key difference between MCMC and
 importance sampling.

5

The prior distribution of additional model parameters (if applicable) are discussed in the
corresponding case study section. The error model variance is not jointly inferred with other
model parameters but calculated for each sample parameter set from the residuals according
to Eq. (6).

10

11 3 Case studies

12

We provide a comprehensive overview of the performance of HydroMix based on a set of 13 14 synthetic case studies (case studies 3.1 and 3.2) and a real-world application to demonstrate 15 the practical relevance for hydrologic applications (case studies 3.4 and 3.5). The first case 16 study demonstrates the ability of HydroMix to converge on the correct posterior distribution 17 for synthetically generated data. The second case study uses a synthetic dataset of rain, snow 18 and groundwater isotopic ratios using a conceptual hydrologic model, and compares the 19 results of HydroMix to the actual mixing ratios assumed to generate the data set. It then 20 weights the sources samples and evaluates the effect of weighting on the mixing ratio. In the 21 third and fourth case studies, HydroMix is applied to observed tracer data from an Alpine 22 catchment in the Swiss Alps to infer source mixing ratios and an additional parameter (isotopic 23 lapse rate).

24

26

25 3.1 Mixing using Gaussian distributions

In this example, sources S_1 and S_2 are drawn from two Gaussian distributions with different means (μ_1, μ_2) and standard deviations (σ_1, σ_2) and combined to form the mixture Y with a constant mixing ratio ρ :

30 31

$$\rho S_1 + (1 - \rho) S_2 = Y.$$

32

Assuming the two distributions are independent, the resultant mixture is normally distributedwith mean and variance defined as:

35 36

37

$$Y \sim N(\rho\mu_1 + (1-\rho)\mu_2, \ \rho^2 \sigma_1^2 + \ (1-\rho)^2 \sigma_2^2).$$
13

A given number of samples are drawn from the distributions of S_1 and S_2 and of the mixture Y. The posterior distribution of the mixing ratio, $p(\rho | \tilde{S_1}, \tilde{S_2}, \tilde{Y})$, is then inferred using HydroMix for i) a case where the two source distributions are well identifiable, and ii) a case where the distributions have a large overlap. Different values of mixing ratios are tested, with ratios varying from 0.05 to 0.95 in steps of 0.05.

43

The sensitivity of HydroMix to the number of samples drawn from S_1 , S_2 and Y, along with the time to convergence is assessed based on the sum of the absolute error between the estimated mixing ratio $\hat{\rho}$ and its true value ρ .





2 3.2 Mixing with a time series generated using a hydrologic model

4 In this case study, we build a conceptual hydrologic model where groundwater is assumed to 5 be recharged directly from rainfall and snowmelt. Stable isotopes of water in deuterium (δ^2 H) 6 is used to see how the isotopic ratio in groundwater evolves under different assumptions of 7 rain and snow recharge efficiencies.

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9 Synthetic time series are generated for precipitation, isotopic ratio in precipitation and air 10 temperature at a daily timestep. For generating the precipitation time series, the time 11 between two successive precipitation events is assumed to be a Poisson process with the 12 precipitation intensity following an exponential distribution (Botter et al., 2007; Rodriguez-13 Iturbe et al., 1999). Time series of air temperature and of isotopic ratios in precipitation are 14 obtained by generating an uncorrelated Gaussian process with the mean following a sine 15 function (to emulate a seasonal signal) and with constant variance (Allen et al., 2018; Parton and Logan, 1981). The separation of precipitation into rainfall (P_r) and snowfall (P_s) is done 16 17 based on a temperature threshold approach (Harpold et al., 2017), where the fraction of 18 rainfall $f_r(t)$ at time step t is computed as a function of air temperature T(t): 19

20
$$f_r(t) = \begin{cases} 0 \text{ if } T(t) < T_L \\ \frac{T(t) - T_L}{T_H - T_L} \text{ if } T_L \le T(t) \le T_H \\ 1 T(t) > T_H, \end{cases}$$
 14

21

22 where T_L and T_H are the lower and upper threshold bounds. In this case study, T_L and T_H are 23 set to -1 °C and +1 °C. The evolution of the snow water equivalent (SWE) in the snowpack (h_s) 24 is computed as: 25

26
$$\frac{dh_s(t)}{dt} = P_s(t) - M_s(t),$$
 15

27

28 where M_s is the magnitude of snowmelt, computed using a degree-day approach as proposed 29 by Schaefli et al., (2014):

30
31
$$M_s = \begin{cases} a_s(T(t) - T_m), & \text{if } T(t) > T_m \\ 0 & \text{otherwise} \end{cases}$$
16
32

33 where a_s is the degree-day factor (set here to 2.5 mm/°C/day) and T_m is the threshold 34 temperature at which snow starts to melt (set to 0 °C). The snowpack is assumed to be fully 35 mixed, and the isotopic ratio of snowpack is computed as:

37
$$\frac{d(h_{s}(t)C_{s}(t))}{dt} = C_{p}(t)P_{s}(t) - C_{s}(t)M_{s}(t),$$
38 17

39 where C_s is the isotopic ratio of snowpack and C_p is the isotopic ratio of precipitation. The 40 amount of groundwater recharge (R) is the sum of groundwater recharged from rainfall and 41 snowmelt:

42

 $R(t) = R_r P_r(t) + R_s M_s(t),$





18

where
$$R_r$$
 and R_s are the rainfall and snowmelt recharge efficiencies. Recharge efficiency is
defined as the fraction of rainfall or snowmelt that reaches groundwater and is assumed to be
a constant value. The groundwater storage is assumed to be fully mixed, and the isotopic ratio
of groundwater is computed as:

8
$$\frac{d(G(t)C_g(t))}{dt} = R_r C_p(t) P_r(t) + R_s C_s(t) M_s(t) - C_g(t) Q(t),$$
 19

where C_g is the isotopic ratio in groundwater, G is the volume of groundwater and Q is the 10 amount of groundwater outflow to the stream defined as: 11

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13
$$Q(t) = k(G(t) - G_C),$$
 20

15 where k is the recession coefficient and G_{c} is a constant groundwater storage that does not interact with the stream (added here to avoid zero flow). This formulation follows the linear 16 17 groundwater reservoir assumption used in numerous hydrological modeling frameworks 18 (Beven, 2011). The volume of the groundwater storage is computed as: 19

20
$$\frac{dG(t)}{dt} = R(t) - Q(t).$$
 21

21 22 The model is run for a period of 100 years, allowing the system to reach a long term steady 23 state. Only the last 2 years of the model runs are used to obtain the time series of isotopic 24 ratios in rainfall, snowmelt and groundwater. These years are then used to estimate the 25 mixing ratio of snowmelt in groundwater, which is the fraction of groundwater recharged from 26 snowmelt. Rainfall and snowmelt samples are the two sources and groundwater samples 27 represent the mixture. For the HydroMix application, all the rainfall and snowmelt samples 28 are used, whereas for groundwater, only one isotopic ratio per month is used (randomly 29 sampled). The mixing ratios inferred using HydroMix are compared to the actual recharge ratio 30 obtained from the hydrologic model as:

31
32
$$R_s^a = \frac{\sum_t R_s M_s(t)}{\sum_t R(t)}$$
, 22
33

33

34 where R_s^a represents the proportion of groundwater recharge derived from snowmelt, 35 summed over all the time steps. The numerical implementation of the evolution of isotopic 36 ratio in snowpack and groundwater are given in the Appendix.

37

38 3.3 Weighting mixing ratios in the hydrologic model

39 40 In Section 3.2, rainfall and snowmelt samples are not weighted by the magnitude of their 41 fluxes while computing the mixing ratios with HydroMix. As all rainfall and snowmelt samples 42 are used, the weights are implicitly determined by the number of rainfall and snowmelt 43 events, instead of their magnitudes. This is a general problem in all mixing approaches and 44 has not been adequately acknowledged in the literature. Ignoring the weights may lead to 45 biased mixing estimates if the proportional contribution of one of the components (e.g.:





1 rainfall or snowmelt) is low, but the number of samples obtained to represent that component 2 is proportionally much higher (Varin et al., 2011). For example, in a given catchment, the 3 amount of total snowfall maybe a small proportion of the annual precipitation, but the 4 number of days when snowmelt occurs maybe comparable to the total number of rainfall days 5 in a year. If this is not specified a priori, HydroMix may overestimate the proportion of groundwater being recharged from snowmelt. To account for this, we introduce a weighting 6 7 factor in the likelihood function originally formulated in Eq. (8), to make a new composite 8 likelihood (Varin et al., 2011):

9

10
$$L_j(\tilde{Y}_{obs}|S_1, S_2, \theta) = \prod_{k=1}^q \prod_{j=1}^m \prod_{i=1}^n \left[(2\pi\sigma^2)^{-0.5} \exp(-\frac{1}{2} \frac{(\tilde{Y}_{obs}^k - \hat{Y}_{ij})^2}{\sigma^2}) \right]^{w_i w_j}$$
, 23

11

where *i* and *j* correspond to snowmelt and rainfall samples, and the weights w_i and w_j reflect the proportion of snowmelt and rainfall contributing to groundwater recharge (Vasdekis et al., 2014), where w_i is expressed as:

15
16
$$w_i = \frac{R_i S_i}{\sum_{i=1}^n R_i S_i}$$
, 24

17

where R_i is the magnitude and S_i is the isotopic ratio of the *i*th snowmelt event. Rain weights (w_j) are also expressed similarly to Eq. (24). The obtained mixing ratio estimates are then compared with the unweighted estimates (in Section 3.2) to see if weighting by magnitude makes a significant difference.

22

23 3.4 Real case study: Snow ratio in groundwater in Vallon de Nant

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The objective of this case study is to infer the proportional contributions of snow versus rainfall to the groundwater of an Alpine headwater catchment, Vallon de Nant (Switzerland), using stable water isotopes.

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29 3.4.1 Catchment description

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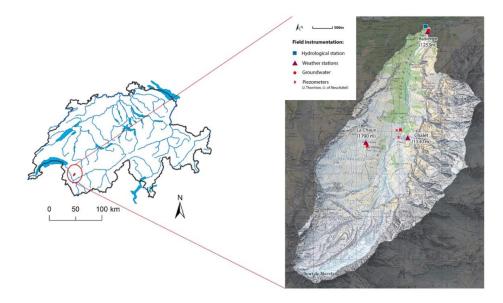
31 Vallon de Nant is a 13.4km² catchment located in the Vaud Alps in South-West of Switzerland 32 (Figure 1), with elevation ranging from 1253 m to 3051 m asl. Steep slopes form a major part 33 of the catchment with a mean catchment slope of around 36° (Thornton et al., 2018). At lower 34 elevations, a dense forest dominated by Picea abies covers 14% of the catchment area. At 35 around 1500 m asl., there is an active pasture area with scattered trees and an open forest 36 dominated by Larix decidua. Additional species scattered throughout the catchment include 37 Pinus sp., Alnus sp. and Acer pseudoplatanus. Alpine meadows cover most of the higher 38 elevation land surfaces. Despite the relatively low elevation, there is a small glacier with an 39 extended moraine that cover 4.4% and 10.1% of the catchment area. A large part (28% of 40 catchment area) of the hillslopes are composed of steep rock walls. At lower to mid-41 elevations, talus slopes account for about 6% of the catchment area. 42

Vallon de Nant has a typical Alpine climate, with around 1900 mm of annual precipitation and
 a mean air temperature of 1.8 °C (Michelon, 2017). For this paper, long term climate statistics
 are computed using MeteoSwiss gridded precipitation and air temperature dataset from





- 1 1961-2015 (Isotta et al., 2013; MeteoSwiss, 2016, 2017). Applying a simple temperature
- 2 threshold (0 and 1 °C) to observed precipitation indicates that on average, 40-45% of the total
- 3 precipitation falls as snow in the catchment. There is a small degree of seasonality in
- 4 precipitation, with higher precipitation between June to August, and lower precipitation in the
- 5 months of September and October.



6 7

Figure 1. Map showing Vallon de Nant along with the locations of meteorologic and hydrologic
observations and the frequent sampling sites. Composite samples of precipitation were
collected at the weather stations. Groundwater samples were collected at the groundwater
monitoring points and the installed piezometers. The groundwater piezometers were installed
by James Thornton from University of Neuchâtel (Thornton et al., 2018).

13

14 3.4.2 Data collection

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Vallon de Nant has been extensively monitored since February 2016. Water samples are collected from streamflow, rain, snowpacks and groundwater at different elevations, which are then analyzed for the isotopic ratios in deuterium (δ^2 H) and oxygen-18 (δ^{18} O). Due to logistical constraints, snowmelt water is not collected, thus snowpack samples are used as a proxy for snowmelt. A summary of the isotopic data is shown in Table 1.

21

Table 1. Summary of the isotopic data (δ^{2} H and δ^{18} O) collected in Vallon de Nant between February 2016 to July 2017

| Sample name | Number of samples | Lowest elevation | Highest elevation |
|--------------------|-------------------|------------------|-------------------|
| Rainfall | 32 | 1253 | 1773 |
| Top snowpack layer | 80 | 1241 | 2455 |
| Groundwater | 22 | 1253 | 1779 |





1 3.4.3 Model implementation

2

HydroMix is used to estimate the proportion of snow recharging groundwater (subsequently
referred to as 'snow recharge coefficient'). In order to obtain a pdf of the snow recharge
coefficient, isotopic ratios in all the water samples from rain, snowpack and groundwater are
used. A uniform prior distribution is assigned to the snow recharge coefficient, which varies
between 0 and 1, representing the entire range of possible values. Groundwater isotopic ratio
is estimated using Eq. (12).

9

10 3.5 Introduction of an additional model parameter

11

12 In any mixing analysis, it may be useful or desirable for users to specify an additional model 13 parameter that is able to modify the tracer concentrations based on their process 14 understanding of the system. In the case of Alpine catchments with large elevation gradients, 15 stable isotopes in precipitation often exhibit a systematic trend with elevation, becoming 16 more depleted in heavier isotopes with increasing elevation. This is also known as the 'isotopic 17 lapse rate' (Beria et al., 2018). In typical field campaigns, because of logistical challenges, 18 precipitation samples are collected only at a few points in a catchment, with often fewer 19 precipitation samples at high elevations. This leads to oversampling at lower elevations, and 20 under sampling at higher elevations, which can bias mixing estimates. This has been found 21 specially relevant for hydrograph separation in forested catchments (Cayuela et al., 2019). To 22 allow a process compensation for this, an additional lapse rate factor is introduced in which 23 each observed point scale sample (observed at a given elevation) is corrected to a reference 24 elevation as follows:

25 26

$$ar{r} = rac{\sum_{j=1}^{k} [lpha(e_j - e) + r] a_j}{\sum_{j=1}^{k} a_j},$$

27

where r is the isotopic ratio in precipitation collected at elevation e, \bar{r} is the catchment averaged isotopic ratio in precipitation, α is the isotopic lapse rate factor, and e_j is the elevation of the *j*-th elevation band where the catchment is divided into *k* elevation bands. These bands are obtained by constructing a hypsometric curve of the catchment (Strahler, 1952).

33

34 The lapse rate factor is allowed to modify both rainfall and snowpack isotopic ratios to obtain 35 a catchment averaged isotopic ratio, which is then used in the mixing model. Using this 36 formulation of an isotopic lapse rate makes the following implicit assumptions: (1) 37 precipitation storms on aggregate move from the lower part of the catchment to the upper 38 part of the catchment thus creating a lapse rate effect, and (2) precipitation falls uniformly 39 over the catchment. It is important to note that the isotopic lapse rate is different from the 40 precipitation lapse rate, i.e., the rate of change of precipitation with elevation is different from 41 the rate of change of precipitation isotopic ratio with elevation.

42

The prior distribution of the isotopic lapse rate is specified based on isotopic data collected across Switzerland under the Global Network of Isotopes in Precipitation (GNIP) program (IAEA/WMO, 2018). Using the monthly isotopic values collected in between 1966 and 2014,





1 average lapse rate values are obtained for both δ^2 H and δ^{18} O. These were (-)1.94 ‰/100m for 2 δ^2 H, and (-)0.27 ‰/100m for δ^{18} O (Beria et al., 2018).

3

4 A uniform prior distribution is assigned to the isotopic lapse rate parameter, with the lower 5 bound specified as three times the Swiss lapse rate for both $\delta^2 H$ and $\delta^{18} O$. The observed isotopic lapse rate data from Switzerland suggests average lapse rates are weakly negative; 6 7 however, positive lapse rates can a priori not be excluded for the case study catchment. 8 Accordingly, we do not specify an upper lapse rate bound of zero but set it as three times the 9 Swiss lapse rate (Table 2). In the case of Vallon de Nant, the elevation ranges from 1253 m to 10 3051 m asl. For computing the Swiss lapse rate, the elevation range over which the monthly 11 precipitation samples were collected was 300 m to 2000 m asl.

12

13 Table 2. Prior distribution of the different model parameters as specified to HydroMix

14

| Variable | Prior distribution | Lower bound | Upper bound |
|---------------------------------------|--------------------|----------------|----------------|
| Snow recharge coefficient | Uniform | 0 | 1 |
| Isotopic lapse rate in $\delta^2 H$ | Uniform | (-)5.82 ‰/100m | (+)5.82 ‰/100m |
| Isotopic lapse rate in $\delta^{18}O$ | Uniform | (-)0.81 ‰/100m | (+)0.81 ‰/100m |

15 4 Results

16

17 The results for the different case studies are discussed in the sections below.

18

19 4.1 Mixing with normal distributions

20

The mean and standard deviations used to generate the low and high variance source distributions for the synthetic case studies are summarized in Table 3. We randomly generated 40 samples from each of the two source distributions and from the target distribution, and varied the mixing ratios between 0.05 and 0.95 in 0.05 increments. However, it should be noted that HydroMix permits using different number of samples for the sources and the mixture.

27

28 For the low variance case, the posterior distributions obtained with HydroMix with 1000 29 Monte Carlo (MC) simulations reproduce closely the theoretical mean of the mixing ratios 30 used to generate the synthetic data (Figure 2). However, for the high variance case, the 31 posterior distributions do not capture the true underlying mixing ratios. This is partly due to 32 the poor identifiability of the sources (given that their distributions are highly overlapping), 33 and partly due to the small sample size of 40. Interestingly, the model performance improves 34 slightly with an increasing number of samples (Figure 3a) but markedly with an increase in the number of MC runs (Figure 3b). The performance is measured here in terms of the absolute 35 36 error between the posterior mixing ratio mean and the true mean, summed over all tested 37 ratios from 0.05 to 0.95

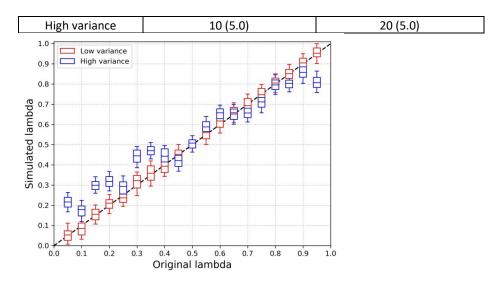
38

39 Table 3. Mean and variance of the two sources S₁ and S₂ drawn from Normal distribution

| Dataset | S ₁ mean (standard deviation) | S ₂ mean (standard deviation) |
|--------------|--|--|
| Low variance | 10 (0.5) | 20 (0.5) |







1 2

Figure 2. Scatterplot showing boxplots of the mixing ratio (ρ) values inferred using HydroMix for the low and high variance synthetic case of Table 3. The boxplots shows the median value,

4 with the box extending from 25th to 75th percentile values. The number of Monte Carlo runs

5 is 1000 and the boxplot represents the top 10 percentile values of the mixing ratio.

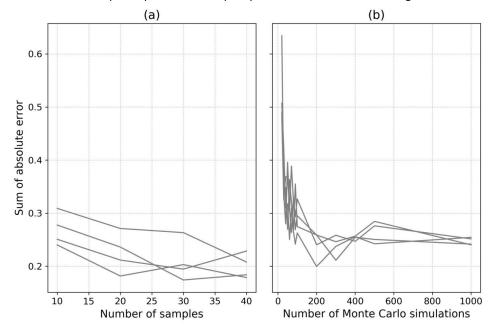


Figure 3. Performance of HydroMix in terms of the absolute error between the posterior mixing ratio mean and the true mean, summed over all tested ratios plotted as a function of (a) number of samples drawn for the two sources (100 Monte Carlo simulations) and (b) number of MC simulations for sample size 10. The four lines in the plot correspond to four different random seeds that were used to initialize HydroMix. The underlying dataset used is the low variance dataset shown in Table 3.





2 4.2 Contribution of rain and snow to groundwater recharge using a hydrologic model3

4 The parameters used to generate daily precipitation, air temperature and precipitation 5 isotopic ratios for a run time of 100 years are shown in Table 4. The static volume of 6 groundwater that does not interact directly with the stream, G_c is set to 1000 mm. Figure 4 7 shows the resulting variation in the isotopic ratio of groundwater over the entire 100 year 8 period, showing the system achieves a steady state condition after ~15 years of simulation.

9

1

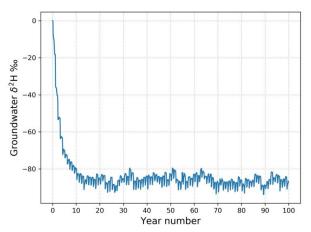
10 Table 4. Parameters used to generate time series of precipitation, air temperature and

11 isotopic ratios in precipitation. μ represents the mean, A is the amplitude and ϕ the time lag

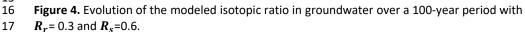
of the underlying sine function. For the precipitation process, μ is the mean intensity on days with precipitation. The resulting mean winter length (air temp. below 0°C) is 119.5 days.

| Variable | Parameter values |
|------------------------------|---|
| Precipitation | # events/year = 30, μ = 33.45 mm/day |
| Air temperature | μ = 4 °C, A = 8 °C, ϕ = - $\pi/2$ |
| Precipitation isotopic ratio | μ = (-80) ‰, A = 40 ‰, ϕ = - $\pi/2$ |

14



15



18

19 The mixing ratio is estimated with HydroMix using: (1) samples of the isotopic ratio in snowfall, 20 and (2) samples of the isotopic ratio in snowmelt. The two sample distributions differ, as 21 shown in Figure 5, where the variability of the isotopic ratio is lower in snowmelt when 22 compared to snowfall. In the model at hand, this reduction is obtained because of mixing 23 occurring within the snowpack, leading to homogenization, thus reducing the variability in the 24 isotopic ratio of snowmelt. In field data, such a reduction in variability is also generally 25 observed (Beria et al., 2018), as a result of the homogenization as modelled here and from 26 more complex snow physical processes, which lie beyond the scope of this study.





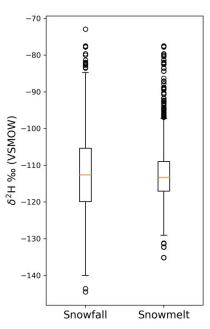


Figure 5. Boxplot showing the variability in the isotopic ratio of snowfall and snowmelt as
simulated by the hydrologic model. The boxplot extends from 25th to 75th percentile value,
with the median value depicted by the orange line. The whiskers extend up to 1.5 times of the
interquartile range. The black circles are the outliers.

6

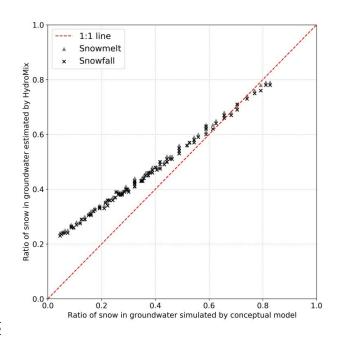
7 The mixing ratios inferred with HydroMix are very similar regardless of whether snowfall or 8 snowmelt is used across the entire range of recharge efficiencies (Figure 6). This provides 9 confidence in the use of snowfall samples as a proxy for snowmelt when estimating mixing 10 ratios. However, it is clear from Figure 6 that an important bias emerges between the 11 estimated mixing ratio from HydroMix and the actual mixing ratio known from the hydrologic 12 model, especially for high and low mixing ratios.

13

This bias can be expected to emerge where the source contributions are not weighted according to their fluxes, which to our knowledge has not been explicitly addressed in the hydrological literature. As already discussed in Section 3.3, the absence of sample weighting typically induces a bias when there is a large divergence between the amount of samples taken over a certain period (e.g. one year) to characterize a source, and the magnitude of source flux over that period (e.g. 40 snow and 10 rain samples taken to characterize the two sources, where snow only accounts for a very small portion (e.g. 10%) of the annual precipitation).







1 2

> Figure 6. Ratios of snow in groundwater estimated with HydroMix plotted against ratios obtained from the hydrologic model for the last two years of simulation. Also shown are the separate results obtained by using samples of either snowmelt or snowfall. The full range of ratios is obtained by varying rainfall and snowmelt recharge efficiencies from 0.05 to 0.95. The number of rainfall, snowfall and snowmelt days are 39, 24 and 107 in the last two years of simulation.

9 10

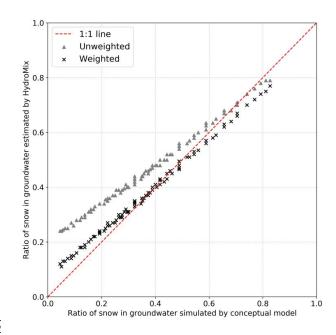
4.3 Effect of weights on estimates of mixing ratios using a hydrologic model

11

After taking into account the magnitude of rainfall and snowmelt events in the composite likelihood function of Eq. (23), it is clear that much of the un-weighted biases can be removed (Figure 7). The most significant improvement is seen at very low mixing ratios where the divergence between the conceptual model and the mixing model estimates error reduces by almost 50%. In this study, we have used a relatively simple normalization based weighting function (Eq. (24)). Testing other weighting functions which have been proposed in the past (Vasdekis et al., 2014) is certainly possible, and is left for future research.







1 2

> Figure 7. Ratios of snow in groundwater estimated using HydroMix plotted against ratios obtained from the hydrologic model, for both weighted and unweighted mixing scenarios. The full range of ratios is obtained by varying rainfall and snowmelt recharge efficiencies from 0.05 to 0.95. The number of rainfall, snowfall and snowmelt days are 39, 24 and 107 in the last two years of simulation.

8

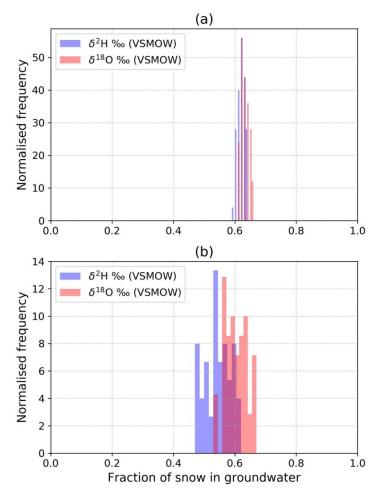
9 4.4 Inferring fraction of snow recharging groundwater in a small Alpine catchment10 along with an additional model parameter

11

12 Using the dataset from an Alpine catchment (Vallon de Nant, Switzerland), HydroMix 13 estimates that 60-62% of the groundwater is recharged from snowmelt (using unweighted approach), with the full posterior distributions shown in Figure 8a. This estimate is consistent 14 15 for both the isotopic tracers (δ^{2} H and δ^{18} O), which are often used interchangeably in the 16 hydrologic literature (Gat, 1996). Comparing this recharge estimate to the proportion of total 17 precipitation that falls as snow (around 40-45%, see Section 3.4.1), suggests that snowmelt is 18 more effective at reaching the aquifer than an equivalent amount of rainfall falling at a 19 different period of the year. Similar results have been obtained in a number of previous 20 studies across the temperate and mountainous regions of the world (see Table 1 in the work 21 of Beria et al., (2018) for a summary).







1 2 **Figure 8.** Histogram showing the fraction of snow recharging groundwater in Vallon de Nant 3 using the isotopic ratios in δ^{2} H and δ^{18} O (a) without correcting for lapse rate and (b) after 4 correcting for lapse rate.

5

6 As can be seen from Figure 8a, the estimated distribution of snow ratio in groundwater is very 7 narrow. This can be explained by the fact that we assume that the collected precipitation 8 samples represent the variability actually occurring in the catchment. To overcome this 9 limitation, we infer an additional parameter called the isotopic lapse rate that accounts for 10 the spatial heterogeneity in terms of catchment elevation. As shown in Figure 9, the posterior distributions of the isotopic lapse rate (for both δ^2 H and δ^{18} O) largely overlap with the spatially 11 12 averaged isotopic lapse rate as estimated from precipitation isotopes across Switzerland. The 13 overlap with the average Swiss isotope lapse rate suggests our inferred lapse rates are reasonable, with the spread in the estimates likely reflecting the temporal variation in the 14 15 catchment specific isotope lapse rate that can develop from a wide range of moderating 16 factors (e.g. air masses contributing precipitation without traversing the full elevation range of the catchment due to varying trajectories). The Swiss lapse rate is constructed as a long 17





term spatial average, whereas the inferred isotopic lapse rate in Vallon de Nant is constructed from the temporal variations in the isotopic ratios. This makes the comparison more informative than definitive. In any case, these results demonstrate that it is relatively straightforward to jointly infer multiple parameters within the HydroMix modeling framework provided users have a mechanistic basis for their interpretation.

6

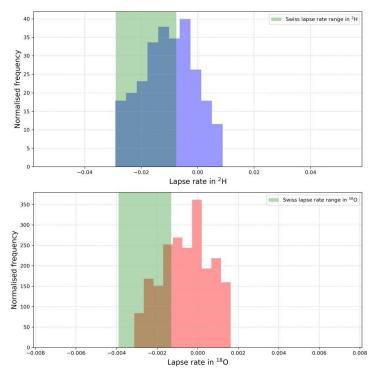
However, an important consequence of additional parameter inference without providing
additional data or constraints is an increase in the degree of freedom, which can then increase

additional data or constraints is an increase in the degree of freedom, which can then increase
 the uncertainty on source contributions. This effect is seen in Figure 8b, especially in contrast

10 with the previous result in Figure 8a, where the median mixing ratios of the posterior

distributions remain similar (~0.6), but the spread increase drastically, from 0.005 to 0.2.

12



13

Figure 9. Histogram showing the posterior distribution of the isotope lapse rate parameter in δ^2 H and δ^{18} O. The green region shows the confidence bounds (significant at α =0.01) of lapse rate computed over Switzerland by using inverse variance weighted regression. Limits of the prior distribution of the isotopic lapse rates correspond to limits of the x-axis. The slope of the isotopic ratio when plotted against elevation for the Swiss-wide data is shown in Figure 3 of Beria et al. (2018).

20

21 5 Limitations and opportunities

22

As with all linear mixing models, the quality of the underlying data determines the accuracy and utility of the results. If the tracer compositions of the different sources are not sufficiently





- 1 distinct, the uncertainty in the estimated mixing ratios will become very large. This means that
- 2 if either the underlying data quality is poor, or the source contribution dynamics are not well
- 3 conceptualized, then the uncertainty in the mixing ratios will be too high to be useful.
- 4

5 In cases where a large number of source samples are available, the computational 6 requirements of HydroMix outweigh the benefit from using it. These are likely cases where 7 the statistical distribution of the source tracer composition is well understood, therefore 8 fitting a probability density curve to the source and target samples, and then inferring the 9 distribution of the mixing ratio using a probabilistic programming approach is more 10 appropriate (Carpenter et al., 2017; Parnell et al., 2010; Stock et al., 2018).

11

Finally, it is noteworthy that adding additional parameters to characterize the source tracer composition increases the degree of freedom of the model, which implies that adding such parameters leads to an increase in the uncertainty of the source contribution estimates unless new information, i.e. new observed data, is added to the model. This means that users who are interested in incorporating additional modification processes by adding parameters should ideally provide additional tracer data able to constrain this process.

18

19 For consistency and simplicity, the case studies and synthetic hydrological examples provided 20 here focused on the contribution of rain and snow in recharging groundwater. However, it is 21 important to emphasize that the opportunities to implement HydroMix extend to all cases 22 where mixing contributions are of interest, and where it is difficult to build extensive 23 databases of source tracer compositions. Such examples include quantifying the amount of 24 "pre-event" vs. "event water" in streamflow, where "pre-event water" refers to groundwater 25 and "event water" refers to rainfall or snowmelt. Another interesting use case might be to 26 quantify the proportion of streamflow coming from the different source areas in a catchment, 27 to capture the spatial dynamics of streamflow. Other uses include quantifying the amount of 28 fog contributing to throughfall, the proportion of glacial melt vs. snowmelt flowing into a 29 stream, the amount of vegetation water use from soil moisture at different depths vs 30 groundwater, the interaction between surface water and groundwater at the hyporheic zone, 31 sediment fingerprinting in fluvial systems, etc. In all of these cases, understanding source 32 water contributions, both spatially and temporally, will improve the physical understanding of 33 the system.

34

35 6 Conclusions

36

37 We develop a new Bayesian modeling framework for the application of tracers in mixing 38 models. The primary application target of this framework is hydrology, but it is by no means 39 limited to this field. HydroMix formulates the linear mixing problem in a Bayesian inference 40 framework that infers the model parameters based on differences between observed and 41 modelled tracer concentrations in the target mixture, using all possible combinations between 42 all source and target concentration samples. For data scarce environments, this represents an 43 advance over existing probabilistic mixing models that compute mixing ratios based on the 44 formulation of probability distribution functions for the source and target tracer 45 concentrations. HydroMix also makes the inclusion of additional model parameters to account

Geoscientific 🤤 Model Development



1 for source modification processes straightforward. Examples include known spatial or 2 temporal tracer variations (e.g. isotopic lapse rates or evaporative enrichment).

3

4 An evaluation of HydroMix with data from different synthetic and field case studies leads to 5 the following conclusions:

6

8

9

11

12

7 1. HydroMix gives reliable results for mixing applications with small sample sizes. As expected, the variance in source tracer composition and the ensuing composition overlap determines the uncertainty in the mixing ratio estimates. The uncertainty in 10 mixing ratio estimates increases with increasing variance in source tracer compositions. Mixing ratio estimates improve (in terms of lower error) with increasing number of source samples.

- 13 2.As revealed by our synthetic case study with a conceptual hydrological model, at low 14 source contributions (i.e. < 20%), a strong divergence between the actual and 15 estimated mixing ratios emerges. This arises if HydroMix assigns equal weights to all 16 source samples proportionally oversampling the less abundant source, which then leads to significant biases in mixing estimates. This problem is inherent to all mixing 17 18 approaches, and to our knowledge has not been adequately addressed in the 19 literature.
- 20 3. The use of composite likelihoods to weight samples by their amounts can significantly 21 reduce the bias in the mixing estimates. At low source proportions, the estimated 22 mixing ratio improves by more than 50% after accounting for the amount of all the 23 sources. We show this using a simple normalization based weighting function. Future 24 studies should explore the usage of different weighting functions that have been 25 proposed in the past (Vasdekis et al., 2014).
- 26 4.A synthetic application of HydroMix to understand the amount of snowmelt induced 27 groundwater recharge, revealed that using snowfall isotopic ratio instead of snowmelt 28 isotopic ratio leads to similar mixing ratio estimates. This is particularly useful in high 29 mountainous catchments, where sampling snowmelt is logistically difficult.
- 30 5. A real case application of HydroMix in a Swiss Alpine catchment (Vallon de Nant) showed 31 a clear winter bias in groundwater recharge. About 60-62% of the groundwater is 32 recharged from snowmelt (unweighted mixing approach), when snowfall only 33 accounts for 40-45% of the total annual precipitation. This has also been previously 34 suggested elsewhere in the European Alps (Cervi et al., 2015; Penna et al., 2014, 2017; 35 Zappa et al., 2015).
- 36

37 To conclude, HydroMix provides a Bayesian approach to mixing model problems in hydrology 38 that takes full advantage of small sample sizes. Future work will show the full potential of this 39 approach in hydrology as well as other environmental modelling applications.

- 40
- Appendix 41 7
- 42

43 The equations below show the numerical implementation of the evolution of isotopic ratios

- 44 in snowpack and groundwater at a daily timestep.
- 45

Geoscientific Model Development Discussions



$$\begin{array}{l} 1 \quad C_{s}(t) = \frac{C_{s}(t-1)h_{s}(t-1)+C_{p}(t)P_{s}(t)-C_{s}(t-1)M_{s}(t)}{h_{s}(t-1)+P_{s}(t)-M_{s}(t)} \\ 2 \\ 3 \quad C_{g}(t) = \frac{C_{g}(t-1)G(t-1)+C_{p}(t)R_{r}P_{r}(t)+C_{s}(t)R_{s}M_{s}(t)-C_{g}(t-1)Q(t)}{G(t-1)+R_{r}P_{r}(t)+R_{s}M_{s}(t)-Q(t)} \end{array}$$

4

5 Author contributions

The paper was written by HB with contributions from all co-authors. HB and BS formulated
the conceptual underpinnings of HydroMix. JRL helped in framing the statistical and
hydrological tests to evaluate HydroMix. AM and NCC helped in compiling data used for model
evaluation and provided critical feedback during model validation.

10

11 Code and data availability

The model code is implemented in python 2.7 and available on GitHub at the following link <u>https://github.com/harshberia93/HydroMix</u>. The synthetically generated time series used in Sections 4.1, 4.2 and 4.3, along with the hypsometric curve for Vallon de Nant used in Section 4.4 are available with the model code on GitHub. The isotope data used in Section 4.4 will be made available on request.

17

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21 formulation of the Bayesian mixing model.

22





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