

1 **Response to Reviewer:**
2 **Title: Using wavelet transform and dynamic time warping to identify the limitations of**
3 **the CNN model as an air quality forecasting system**
4 **Author(s): Ebrahim Eslami et al.**
5 **MS No.: gmd-2019-346**
6 **MS Type: Model evaluation paper**
7 **Iteration: Minor Revision**

8
9 **Responses to the comments of Referee:**

10 We would like to thank the reviewer for his/her time and effort in reviewing this manuscript. Please
11 find below our responses.

12
13 *Referee:*

14 *In this paper, Eslami et al. present a method based on wavelet transform and dynamic time*
15 *warping (DTW) to characterize the quality of a machine-learning (ML) algorithm (convolutional*
16 *neural network, CNN) for air quality forecasting (AQF). Using the example of two AQF*
17 *applications, they show how wavelet transform and DTW can provide new insights into the*
18 *strengths and weaknesses of the CNN model.*

19 *Better understanding the potential and limitations of ML algorithms for AQF applications is a*
20 *topic that is rapidly gaining importance given the explosion of ML applications in this area. This*
21 *paper makes a valuable contribution to this discussion by presenting a powerful analytical tool*
22 *that can effectively highlight conditions under which the employed ML algorithm fails to produce*
23 *satisfactory results. As such, the manuscript is highly suitable for publication in GMD. However,*
24 *in its current form there are still some issues regarding the main message of the paper and how*
25 *wavelet transform and DTW can be used to improve error characterization of ML applications.*
26 *For instance, the authors simultaneously say that the tested CNN models have ‘significant*
27 *limitations’ and ‘show promising accuracy’, and generally seem to switch between the view that*
28 *the ML model is either ‘bad’ or ‘good’. In reality, the CNN models – like chemical transport*
29 *models – perform very well under some conditions and poorly under others. One of the powerful*
30 *elements of the discussed statistical analysis tools is that they offer a method to identify these*
31 *conditions and thus help the model developers better understand the strengths and limitations of*
32 *the ML algorithms. This information also helps identify how the ML model might be improved,*
33 *which is very powerful. The authors should stress this more clearly.*

34 *Another point that needs more discussion is the time dimension. The used CNN models seem to*
35 *use snapshots of time-series data as inputs (rather than a window of the time-series) and are thus*
36 *not designed to learn temporal relationships. This should be stated more clearly, as it means that*
37 *the wavelet transform and DTW offer an assessment of a feature that is not directly optimized by*
38 *the ML algorithm (which is a good thing).*

39

40 **Response:**

41 To respond to your suggestion and comments, the following section was added to the revised
42 manuscript:

43

44 **3.3. Discussion:**

45 Despite the enormous success of the convolutional neural network (CNN) algorithm in
46 numerous applications, certain issues related to its applications in air quality forecasting (AQF)

47 require further analysis and discussion. Our main goal in this paper was to discuss some of these
48 issues is a few practical applications. To discuss these issues analytically, we used wavelet
49 transform and dynamic time warping (DTW) as powerful mathematical tools for time-series
50 analysis and models. Based on the findings that were presented in the paper, these tools are
51 beneficial not only in understanding the issues with machine learning models but also in fine-
52 tuning them to improve their performances with a scientific point of view. Awareness of the
53 limitations in CNN models will enable scientists to develop more accurate regional or local air
54 quality forecasting systems by identifying the affecting factors in high concentration episodes.

55 Based on our findings in the base studies presenting the aforementioned CNN models, in
56 both cases, the CNN model shows reasonable accuracy for ozone prediction, 24 hours in advance,
57 in two geographical locations (the United States and South Korea). However, similar to other data-
58 driven prediction tools, in a CNN model, the out-of-sample prediction error is almost always
59 greater than the in-sample prediction error. Thus, since both CNN models were designed as a real-
60 time air quality prediction models, the prediction error is inevitable, even though (i) both models
61 were configured for optimum performance (based on the input or training samples), and (ii) in
62 development of both models, cross-validation processes were followed to mitigate any systematic
63 biases. However, the underperformance of the CNN model was dependent on several factors,
64 including modeling configuration (e.g., the depth of CNN model), arrangements of input variables
65 (e.g., number of previous days as inputs), the day of the week (e.g., weekdays versus weekends),
66 the hour of the day (e.g., daytime versus nighttime) (see Eslami et al. (2019a, 2019b, 2019c), Choi
67 et al. (2019), Sayeed et al. (2020), and Lops et al. (2019), and the discussion within).

68 Here, we discussed the general limitations of the CNN model in two common applications:
69 (i) a real-time AQF model, and (ii) a post-processing tool in a dynamical AQF model (i.e., CMAQ).
70 These examples are fundamentally different in terms of execution, one being a raw predictor
71 (statistical approach) while the other being a post-processor (hybrid approach). Since both models
72 are commonly being used as a real-time air quality prediction system, we discussed their issues
73 individually to explain certain issues that one may encounter in executing either of them. Thus, it
74 will provide both machine learning researchers and atmospheric scientists with multiple candidate
75 models and analytical tools to develop any specific model of their choice.

76 For one case (raw prediction model), we used the wavelet transform to determine the
77 reasons behind the poor performance of CNN during the nighttime, cold months, and high ozone
78 episodes. We find that when fine wavelet modes (hourly and daily) were relatively weak or when
79 coarse wavelet modes (weekly) were strong, the CNN model produced less accurate forecasts.
80 Since the CNN model has used only one previous day of air quality and meteorological parameters,
81 neither the coarse patterns (e.g., weekly) were used as a prediction feature, nor any connection
82 between different time-series windows (as is revealed in a wavelet transform analysis) was
83 considered. Thus, the wavelet transform can be helpful as a complementary tool in filling these
84 gaps in a CNN prediction model development. It should be noted that long short-term memory
85 (LSTM) model can potentially incorporate some of the aforementioned time-dependencies (e.g.,
86 bi-daily or weekly). However, the focus of this study is to address such a limitation in a CNN
87 model as the choice of the ML model.

88 For the other case (post-processing model), we used the DTW distance analysis to compare
89 post-processed results with their CMAQ counterparts (as a base model). For those CMAQ results
90 with a consistent DTW distance from the observation, the post-processing approach properly
91 addressed the CMAQ modeling bias with predicted IOAs exceeding 0.85. When the DTW distance
92 of CMAQ-vs-observation is irregular, the post-processing approach is unlikely to perform

93 satisfactorily. Even though the CMAQ-CNN model has included several chemical components
94 and meteorological variables as its inputs, there was no input feature representing CMAQ's own
95 accuracy. By comparing a history of CMAQ results in different geographical locations with
96 available observation data, the DTW can provide an 'irregularity' index as an additional input
97 feature.

98
99
100 **Response:**
101 To respond to your suggestion and comments, the following modifications were made in the
102 manuscript:

103
104 *Referee:*
105 *Minor comments:*
106 *- Page 4, line 100: 'general inability of the machine learning model' seems a bit too harsh.*
107 *I suggest to rephrase this.*

108
109 Response: "general inability" has been changed to "certain limitations."
110
111 *- Page 5, line 124. Should be Figure 1, not Figure 3.*

112
113 Response: Thanks. The figure citation in the text has been changed.
114
115 *- Page 6, line 201: Please provide the definition of index of agreement*

116
117 Response: The following statement has been added to the manuscript.
118 Note that IOA is a standardized measure of the degree of model prediction error and varies between
119 0 and 1. The agreement value of 1 indicates a perfect match, and 0 indicates no agreement at all.
120
121 *- Page 6, line 213: I'd be careful with the statement that NOx and VOC emissions are*
122 *constant in time. These emissions have large diurnal and seasonal cycles.*

123
124 Response: Thanks for a good point. The following modification has been made in the
125 manuscript.
126 Compared with meteorological variables, emission sources from volatile organic compounds
127 (VOCs) and NOx are experiencing less variability in time. Thus, meteorological variables play an
128 important role in governing the variation of the ozone at different times throughout the year
129
130 *- Page 7, line 251ff: maybe worth mentioning here the potential of long short-term*
131 *memory (LSTM) algorithms to incorporate time dependency in the training?*

132
133 Response: The following statement has been added to the manuscript in 4th paragraph in the newly
134 added Discussion section (Section 3.3, lines 476-479).
135 It should be noted that long short-term memory (LSTM) model can potentially incorporate some
136 of the aforementioned time-dependencies (e.g., bi-daily or weekly). However, the focus of this
137 study in addressing such a limitation in a CNN model as the choice of the ML model.

138 **Using wavelet transform and dynamic time warping to identify the limitations**
139 **of the CNN model as an air quality forecasting system**

140

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143

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145 **Abstract:**

146 As the deep learning algorithm has become a popular data analytic technique, atmospheric
147 scientists should have a balanced perception of its strengths and limitations so that they can provide a
148 powerful analysis of complex data with well-established procedures. Despite the enormous success of the
149 algorithm in numerous applications, certain issues related to its applications in air quality forecasting (AQF)
150 require further analysis and discussion. This study addresses significant limitations of an advanced deep
151 learning algorithm, the convolutional neural network (CNN), in two common applications: (i) a real-time
152 AQF model, and (ii) a post-processing tool in a dynamical AQF model, the Community Multi-scale Air
153 Quality Model (CMAQ). In both cases, the CNN model shows promising accuracy for ozone prediction 24
154 hours in advance in both the United States and South Korea (with an overall index of agreement exceeding
155 0.8). For the first case, we use the wavelet transform to determine the reasons behind the poor performance
156 of CNN during the nighttime, cold months, and high ozone episodes. We find that when fine wavelet modes
157 (hourly and daily) are relatively weak or when coarse wavelet modes (weekly) are strong, the CNN model
158 produces less accurate forecasts. For the second case, we use the dynamic time warping (DTW) distance
159 analysis to compare post-processed results with their CMAQ counterparts (as a base model). For CMAQ
160 results that show a consistent DTW distance from the observation, the post-processing approach properly
161 addresses the modeling bias with predicted IOAs exceeding 0.85. When the DTW distance of CMAQ-vs-
162 observation is irregular, the post-processing approach is unlikely to perform satisfactorily. Awareness of
163 the limitations in CNN models will enable scientists to develop more accurate regional or local air quality
164 forecasting systems by identifying the affecting factors in high concentration episodes.

165

166 **Keywords:** machine learning, neural networks, atmospheric chemistry, air quality modeling.

167 1. Introduction:

168 Currently, atmospheric scientists have shown significant interest in applying machine learning
169 (ML) algorithms in their field, specifically for air quality forecasting, remote sensing data retrieval, and
170 hurricane tracking. ML is a technique used for developing data-driven algorithms that learn to mimic human
171 behavior on the basis of a prior example or experience. It is a tool that allows systems to more effectively
172 deal with knowledge-intensive problems in complex domains, which occurs via learning that involves
173 gathering information from a training dataset and using a certain logic to purposefully detect a pattern of
174 behavior. The fundamental goal of ML models is to apply the detected patterns to make generalizations
175 beyond the examples in the training set.

176 Generalizations stemming from ML models provide a scope of improvement in a number of
177 physical applications. Evidence of the growing interest in applying ML is the rapid increase in the number
178 of scientific publications in this area, illustrated in Fig. S1. However, the focus of these studies was the
179 general performance of the model ML models compared to that of conventional statistical models rather
180 than identifying the shortcoming of such models in explaining the uncertainties of prediction models. Such
181 examples can be found in studies by Eslami et al. (2019a, 2019b, 2019c), Choi et al. (2019), Sayeed et al.
182 (2020), and Lops et al. (2019). To achieve more reasonable outcomes, we must first explore the current
183 challenges we face when forecasting ambient air quality and then assess how or even whether ML models
184 can address the challenges to produce more accurate forecasting.

185 To develop a capable air quality forecasting tool, atmospheric scientists often turn to chemical
186 transport models (CTMs) and statistical models, both of which use meteorological parameters and chemical
187 precursors from previous atmospheric conditions to estimate the following conditions. A brief summary of
188 these models appears in Zhang et al. (2012). Although CTMs, with their dynamical implementation of
189 atmospheric chemistry and physics, have shown promise in forecasting, they are too computationally
190 intensive for real-time operational forecasts. Thus, computationally efficient statistical models such as ML
191 have emerged as alternative approaches. Unlike CTMs, however, these models mainly rely on data from a
192 network of monitoring stations that are sparsely distributed and measure a limited number of meteorology
193 and air quality variables (Eslami et al., 2019a). Given the complexity of the formation/depletion of air
194 pollutants such as ozone, this limitation may be vital in predicting extreme events (Eslami et al., 2019b).

195 Another challenge in predicting ozone concentration is the “external” relationships among
196 predictors. For instance, as important meteorological parameters, temperature and solar radiation are
197 synoptic factors, while the wind field is influenced by regional factors such as geography and urbanization.
198 Such conditions particularly affect ozone variability since locally-produced NO₂ emissions under certain
199 meteorological circumstances lead to the formation of ozone that is later transported by the wind and
200 detected by monitoring stations (Pan et al., 2015). Nevertheless, station-specific ML models use such
201 chemical and meteorological variables as a footprint of local conditions.

202 Although local emissions of ozone precursors are the dominant source of ozone, particularly in
203 urban areas, ozone pollution arising from sources outside of a target region, such as background ozone,
204 inevitably degrade local air quality (Camalier et al., 2007). The lack of measurable environmental variables
205 that indicate the potential long-range transport of air pollutants poses an unprecedented challenge for a ML
206 model to estimate ozone concentrations over downwind communities (Eslami et al., 2019a). Because of
207 the nonlinear spatial relationships between neighboring monitoring stations, ML models as operational real-
208 time forecasting systems produce relative uncertainty.

209 A number of studies have proposed solutions addressing the above limitations of ML models.
210 Eslami et al. (2019a) implement a deep convolutional neural network (CNN) (Krizhevsky et al., 2012)

211 model that uses hourly values of several meteorological and air pollution variables to predict hourly ozone
212 concentrations 24 hours in advance. Even though the accuracy of the forecasting system guarantees a
213 reasonable level of accuracy, it fails to address high ozone episodes owing to the infrequent occurrences of
214 such events, which lead to the undertraining of the CNN model. In another study, Eslami et al. (2019b)
215 propose a data ensemble approach that mitigates this issue by regularizing the training dataset toward
216 capturing high ozone episodes. While the authors remove a significant portion of the underprediction biases
217 of the CNN model, its predictions of ozone during the nighttime and on rainy days are unreliable. Sayeed
218 et al. (2020) use historical data covering a longer period within a diverse geographical domain (Texas) to
219 train a similar CNN model. Their results from stations for which fewer measurements are available, while
220 more accurate, are prone to uncertainty. Using the outputs of air quality and meteorological forecast models
221 to map the hourly ozone concentrations at station locations, Choi et al. (2019) train a similar deep CNN
222 model, a spatially generalized model that bias-corrects ozone forecasts of the community multi-scale air
223 quality (CMAQ) model for all monitoring stations in the EPA AirNow network. Even though the model
224 significantly improved CAMQ forecasts, the bias-correction process and the unbalanced CMAQ modeling
225 outputs are unclear.

226 This paper discusses **certain limitations** of the machine learning model using wavelet transform and
227 dynamic time warping (DTW). Wavelet transform is a powerful technique for analyzing the temporal
228 variation of a time-series (Grinsted et al., 2004). Wavelet analysis uses an adjustable resolution to translate
229 time-series data and then decomposes the data into a certain frequency level that cannot be achieved by
230 other conventional methods such as Fourier analysis (Huang et al., 2010). DTW is a nonlinear technique
231 that measures any alignment between two time-series (i.e., model prediction and observation in this study)
232 by warping them to match their similarities (Berndt and Clifford, 1994). By introducing two applications
233 of CNN in the real-time ozone forecasting system, we use these analytical tools to identify the source of
234 the prediction biases of the CNN model. In this paper, we do not describe the forecasting results in detail
235 but instead refer the reader to studies by Eslami et al. (2019a, 2019b), Choi et al. (2019), and Sayeed et al.
236 (2020).

237

238 2. Materials and Methods

239 2.1. Deep convolutional neural networks:

240 The deep CNN model (Krizhevsky et al., 2012) is a common deep learning architecture that has
241 long been used in numerous applications (Deng and Yu, 2014; Schmidhuber, 2015; Goodfellow et al., 2016;
242 Litjens et al., 2017; Chen et al., 2018; Kamilaris and Prenafeta-Boldú, 2018; Higham and Higham, 2019).
243 Unlike other methods, the CNN model is capable of analyzing joint features and attaining greater accuracy
244 on large-scale datasets. Deep CNNs can be trained to approximate smooth, highly nonlinear functions
245 (LeCun et al., 2015), rendering them appropriate for analyzing nonlinear processes in the atmosphere. In
246 addition, feature extraction using deep learning algorithms is more efficient than using other neural network
247 methods, particularly when multiple hidden layers are structured (Krizhevsky et al., 2012).

248 A schematic for the deep CNN used in this paper appears in Fig. 1. The figure shows the input layer
249 of the CNN algorithm, which represents the normalized time series of all input variables. The normalization
250 process prevents a steep cost function and averts one feature from overbearing others. A filter passes
251 through a set of units located in a small neighborhood in the previous convolutional layer. With local
252 receptive fields, neurons can extract the elementary features of inputs that are then combined with those of
253 higher layers. The outputs of such a set of neurons constitute a feature map (see Fig. 3). At each position,

254 various types of units in different feature maps compute various types of features. A sequential
255 implementation of this procedure for each feature map is used for scanning the input data with a single
256 neuron in a local receptive field and storing the states of this neuron at corresponding locations in the feature
257 map. The constrained units in a feature map perform the same operation on different instances in a time
258 series, and several feature maps (with different weight vectors) can comprise one convolutional layer. Thus,
259 multiple features can be extracted in each instance. Once a feature is detected, its exact “location” becomes
260 less important as long as its approximate position relative to the other features is preserved (Krizhevsky et
261 al., 2012; LeCun et al., 2015).

262 CNN uses a kernel of a given size to capture changes in the temporal variation of the input data by
263 sweeping through time series. The various sections of the data are represented by feature maps. An
264 additional layer performs local averaging, called “pooling,” and subsampling reduces the resolution of the
265 feature map and the sensitivity of the output to possible shifts and distortions. This step could potentially
266 discard important information (e.g., sudden ozone peaks) as explained in Sabour et al. (2017). Hence, this
267 study uses the convolution layer without pooling. The feature maps are connected to a fully-connected
268 layer, which helps us to map each feature of multiple inputs to the hourly ozone output (see Fig. 1).

269 Compared to fully-connected multilayer perceptrons (MLPs) and recurrent neural networks (RNN),
270 which have been extensively used as regression models, CNNs are attractive for several reasons. MLPs and
271 RNNs are not explicitly designed to model variance within an estimation that results from a complex
272 interaction between several inputs and outputs. While MLPs of sufficient size could indeed capture
273 invariance, they require large networks with a large training set. Compared to the CNNs proposed in this
274 study, RNNs are challenging to implement and computationally expensive (Eslami et al., 2019a; Sayeed et
275 al., 2020; Lops et al., 2019).

276

277 **2.2. Wavelet transform:**

278 Wavelet transformation decomposes a signal into a scale frequency space, allowing the
279 determination of the relative contributions of each temporal scale present within a signal (Mallet, 1989).
280 Wavelet decompositions are powerful tools for analyzing the variation in signal properties across different
281 resolutions of geophysical variables (Mallet, 1989; Grinsted et al., 2004; Foufoula-Georgiou and Kumar,
282 2014). Using a fully scalable modulated window that shifts along with the signal, the wavelet transform
283 overcomes the inability of the Fourier transform to represent a signal in the time and frequency domain at
284 the same time (see Fig. S2 in the supplementary document). The spectrum is calculated for every position.
285 After repeating the process, each time with a different window size, the results constitute a collection of
286 time-frequency representations of the signal, all with different resolutions. The data are separated into
287 multiresolution components, each of which is studied with a resolution that matches its scale (Aiuzzi et al.,
288 2002). While high-resolution components capture fine-scale features in the signal, low-resolution
289 components capture the coarse-scale features.

290 As wavelet analysis represents any arbitrary (nonlinear) function by a linear combination of a set
291 of wavelets or alternative basis functions, they are highly suitable for use as both an integration kernel for
292 analysis to extract information about the process and a basis for representation or characterization of
293 processes (Kaheil et al., 2008). Figure S3 in the supplementary document shows the hourly ozone time
294 series of a monitoring station in downtown Seoul, South Korea, with a wavelet transform for the year 2017.
295 Here, the wavelet transform exhibits strong power levels associated with period=24 and period=168 in the
296 middle of the year, indicating dominant daily (24 hours) and weekly variation (168 hours).

297

298 **2.3. Dynamic time warping:**

299 To assess the similarity between two time series, DTW expands or contracts a given time series to
300 minimize the difference between the two of them (Berndt and Clifford, 1994). The advantage it has over
301 Euclidean distance, a conventional distance analysis method, is that it highlights when a shift (e.g., a time
302 lag) occurs between two time-steps in two time series (see Fig. S4 in the supplementary document).
303 Euclidean distance takes pairs of data within the time series and compares them. DTW calculates the
304 smallest distance between all points, matching one time-step to many counterpart steps on the linked time
305 series (see Fig. S4). Owing to its nonlinear mapping capability, it is widely used in various domains, from
306 time-series classification (Jeong et al., 2011) to bioinformatics (Giorgino, 2009), health signal processing
307 (Tormene et al., 2009), and speech recognition (Berndt and Clifford, 1994).

308 One benefit of DTW is that it will classify two time series of the same shape as similar even if their
309 absolute values differ or if one time series contains large variability. Figure S5 compares the DTW distance
310 between the observation time series and two prediction models for an ozone monitoring station in Texas.
311 DTW detects the differences between CMAQ estimation and observation with the highest difference in the
312 middle of 2014.

313

314 **3. Results and Discussion**

315 **3.1. Case 1: CNN as a real-time ozone forecasting system**

316 In this case, we used the modeling experience reported in Eslami et al. (2019a). Briefly, the system
317 employs a deep CNN model that uses an hourly variation of seven meteorological and two air quality
318 parameters from the day before as inputs to predict hourly ozone concentrations on the following day for
319 25 monitoring stations in Seoul, South Korea. Figures S7 and S8 show the accuracy of the CNN model
320 (using the index of agreement (IOA)) and the time series comparison of average ozone concentrations
321 between the observation and the CNN prediction, respectively. **Note that IOA is a standardized measure of**
322 **the degree of model prediction error and varies between 0 and 1. The agreement value of 1 indicates a**
323 **perfect match, and 0 indicates no agreement at all.** While the model maintained a proper level of prediction
324 accuracy, it was prone to two main limitations: (i) Its performance at various times of the year varied (see
325 Fig. S6); and (ii) nighttime predictions showed higher relative bias and lower modeling performance than
326 daytime predictions (see Fig. S7). In general, wavelet transform can explain varying, time-dependent
327 modeling performance; nevertheless, the significant difference between modeling performance during the
328 daytime and the nighttime indicates an undertrained CNN model.

329

330 **3.1.1. Time-dependent model performance:**

331 The performance of the CNN model is directly dependent on how well the model understands the
332 relationship between the inputs (meteorology and ozone precursors) and output (ozone concentration).
333 **Compared with meteorological variables, emission sources from volatile organic compounds (VOCs) and**
334 **NO_x are experiencing less variability in time. Thus, meteorological variables play an important role in**
335 **governing the variation of the ozone at different times throughout the year** (Choi, 2014; Pan et al., 2019).
336 Temperature, wind speed, and relative humidity (RH) are among the most important meteorological
337 parameters affecting ozone variation.

338 Figure 2 shows the wavelet power transform of the aforementioned meteorological variables for
339 2017. Since we used an hourly time series to calculate the wavelet powers, both the index and the period
340 are in hours. The figure also locates five time periods, which indicates significant performance variations.
341 From Fig. S6, the CNN model underperformed during weeks 3-9 and 44-51, labeled the “Worst CNN
342 results” in Fig. 2. For weeks 14-22 and 42-44, the CNN model showed the best forecasting results. Between
343 weeks 29 and 33, the CNN model produced significant underestimations, labeled “Large under-prediction”
344 in Fig. 2. The figure shows strong wavelet powers during a 24-hour (daily) period for all variables, the
345 results of strong diurnal variation of these parameters, which are directly or indirectly controlled by sunlight
346 (e.g., temperature, relative humidity, etc.). While the wavelet powers for wind speed were generally larger
347 than RH, the temperature showed lower but more consistent daily modes. This finding is important since
348 the CNN model can more accurately detect specific “patterns” in the temperature than those in the wind
349 speed and RH. Thus, when the daily modes are stronger in temperature, the CNN model likely performs
350 better. In contrast, when the daily modes of the meteorological variables are relatively weak, the CNN
351 model performs poorly (see Fig. 2).

352 The large coarse modes in the wind speed and RH lead to significant over and underestimation of
353 the CNN model. Figure S8 shows the polar frequency (influenced by the wind speed) of the CNN modeling
354 bias in various months. As the figure shows, while southwesterly winds in August 2017 were associated
355 with relatively large underpredictions boosted by pollution transport from the Incheon area, north-
356 northwesterly winds with air coming from less urbanized regions were allied with notable over predictions.

357 Figure S9 compares the CNN model predictions with observational data for the seasons with
358 respect to levels of RH. The figure showed the largest differences in the CNN model predictions (both over
359 and underpredictions) when the level of RH was close to the extreme (very high and very low). This finding
360 was particularly evident for the summer months when the model showed poor performance at capturing
361 high ozone episodes. This finding underscores the importance of coarse models from the wavelet analysis
362 during the warm months. Directly indicating the over or underpredictions by the model through these
363 modes, however, is challenging. For instance, Fig. S10 shows one high ozone episode in July 2017, when
364 the daily ozone peak exceeded 90ppb on two continuous days at most stations. Here, the overprediction of
365 the CNN model was associated with high RH, while the underprediction was linked to low RH, indicating
366 more complexity among the relationships between meteorological factors and ozone formation or depletion.

367 Another reason for the poor performance of the CNN model during the selected time period was
368 the relatively large coarse modes (period > 24 hours). The CNN model received information about only the
369 last day; hence, it was unable to address the bi-daily and weekly trends with the input data. For instance,
370 for time periods with large underpredictions, coarse modes in the wind speed were even larger than the
371 daily modes. Thus, employing a longer history would adequately explain the relationship between wind
372 speed and ozone. In the comparison of the average wavelet powers in various periods (from daily to weekly
373 modes) of CNN predictions and observational data, Fig. 3 shows that the powers for both time series match
374 periods of approximately 24 hours. After 32 hours, however, the wavelet power of the CNN model shrinks
375 to a relatively constant power while that for the observation reaches local extremums at around 3, 5, and 7
376 days.

377 Although wavelet analysis indicates that modes coarser than 24 hours are important components of
378 the ozone time series, their relationship to CNN model accuracy can be complicated. Figure 4 compares
379 wavelet powers for both fine and coarse modes with a correlation coefficient (r) in 25 ozone stations in
380 Seoul. For stations closer to the downtown area (i.e., those with station numbers under 11), the fine modes
381 had fewer wavelet powers than those for stations in less urbanized areas, indicating that the relationship
382 between ozone concentrations with local emissions was evident in the less urbanized areas than it was in

383 the other areas. The coarse modes, however, varied from station-to-station with relatively higher coarse
384 wavelet power for those in less urbanized areas. Nonetheless, no evidence points to a clear relationship
385 between either coarse or fine wavelet modes and the accuracy of the model. Figure 4 shows that the CNN
386 model generally performed better for stations close to downtown Seoul. Because Seoul has only one
387 meteorological station, these stations had access to more realistic weather parameters in their
388 training/prediction process.

389

390 **3.1.2. Low modeling performance during the nighttime:**

391 In their discussion of several air quality forecasting models that incorporated machine learning
392 algorithms, including CNN, deep neural networks, and decision trees, Eslami et al. (2019a) and Eslami et
393 al. (2019b) claimed that the algorithms encounter a significant modeling bias while estimating air quality
394 concentrations during the nighttime. This bias reduced the prediction accuracy of nighttime ozone
395 concentrations, compared to daytime concentrations, by more than 20%. A similar issue is also encountered
396 by CTMs, even those with complex physical and chemical equations that explain the diurnal variation of
397 ozone concentrations.

398 One reason for this modeling bias was likely the result of variation among the meteorological
399 inputs during the nighttime. Although their absolute values were generally higher they were during the
400 daytime, the relative frequency of variation was more pronounced during the nighttime, causing a
401 discontinuity in the learning process of the CNN model. Since both daytime and nighttime hours were
402 inputs, the CNN model minimized the cost function that contained “normalized” errors during both daytime
403 and nighttime hours (the cost function was the mean squared errors or 24-hour ozone predictions at each
404 step). Generally, there are more daytime hours than nighttime hours (see Fig. S11). Also, the accumulation
405 of NO₂ concentrations for these extreme cases was mainly due to stagnant atmospheric conditions with
406 wind speeds close to their yearly minimum values (see Fig. S12a for scatter plots with levels of wind
407 speeds). As a result, the CNN model was vulnerable to characteristic bias in nighttime ozone estimations.
408 As a customized cost function could be a potential solution to this limitation, it requires further
409 investigation.

410 The performance of the CNN model in predicting nighttime ozone concentrations also suffered
411 because of the misinterpretation of extreme conditions of the input parameters. Figure 5 shows scatter plots
412 that compare CNN predictions and observations by the levels of two important ozone precursors (NO₂
413 concentrations) and meteorological variables (RH%) separated into daytime and nighttime. The NO₂
414 concentration was generally higher during the nighttime when the ozone concentration was near zero for
415 extreme NO₂ values because of conditions amenable to ozone depletion with the absence of sunlight.
416 Unable to capture this relationship, however, the CNN model overestimated these cases (See Fig. 5a).

417 In contrast to the above-mentioned overestimated events, Fig. 5b shows an underestimation of
418 nighttime ozone when the level of RH% was generally high, primarily during warm days. A similar pattern
419 occurred when the surface pressure was accounted for (Fig. S12b). Such underestimated events occurred
420 for two reasons. One is that high (or low) levels of RH% and surface pressure generally occur at about the
421 same time during the early morning (or late afternoon) when the planetary boundary layer (PBL) is at its
422 lowest (or highest) level during the day. In these extreme conditions, the earlier sunrise (or later sunset)
423 during the summer months established a condition that elevated ozone concentrations. As these events
424 normally occurred only during short periods of time, the CNN model was not sufficiently trained to capture
425 these relationships.

426

427 **3.2. Case 2: CNN as a post-processing tool in a real-time ozone forecasting system:**

428 In this case, a generalized bias-correction CNN model introduced by Choi et al. (2019) was used.
429 Their model is a computationally efficient deep learning-based model that produces more reliable numerical
430 results. The authors used a deep CNN model to map ozone precursors from CMAQ and meteorological
431 parameters from the weather research and forecasting (WRF) model (as input variables) to observe hourly
432 ozone concentrations at a monitoring station (as a target). Their model, the CMAQ-CNN model,
433 significantly improves the performance of the CMAQ model in both accuracy and bias. Figures S13 shows
434 the statistical improvements (in correlation, root mean squared error, and standard deviation) of the CMAQ-
435 CNN model over the CMAQ model (as a base model) in different months. Figure S14 compares the daily
436 maximum ozone estimated by CMAQ and CMAQ-CNN in 48 states for which the CMAQ-CNN
437 significantly moderated the over predictions of the CMAQ.

438 It was clear that the likelihood of the CMAQ-CNN model producing accurate results was strongly
439 associated with the quality of CMAQ forecasts; when CMAQ forecasted hourly ozone concentrations with
440 a station-specific yearly IOA of more than 0.5, the IOA of the CMAQ-CNN model was more than 0.8 for
441 most cases. The probability of such accuracy was generally unrelated to that of the CMAQ model. For
442 instance, the CMAQ-CNN model was unable a reach the yearly IOA=0.8 even though the CMAQ IOA was
443 more than 0.7 (e.g., EPA #101 Tennessee: CMAQ IOA=0.7; CMAQ-CNN IOA=0.78). In some cases,
444 however, the yearly IOA following the post-processing approach was less than 0.7 (e.g., EPA #1011
445 California: CMAQ-CNN IOA=0.63). Here, we used the distance analysis from DTW to explain (i) why
446 CMAQ-CNN produced satisfactory results at some stations but not others, and (ii) why it performed poorly
447 at some stations.

448

449 **3.2.1. Satisfactory post-processing scenarios:**

450 Figure 6 shows the time-series of CMAQ, CMAQ-CNN, and observed daily ozone concentrations
451 at three EPA stations. These stations were selected because the IOA accuracy of the CMAQ-CNN model
452 was either more than 0.9 (Fig. 6a and 6b) or 20% more than that of CMAQ (Fig. 6c). Figure 7 compares
453 the DTW distance analysis of CMAQ and CMAQ-CNN for the same stations. These are three typical cases
454 of satisfactory improvement by the CMAQ-CNN post-processing approach:

455 Figures 6-7(a): Observed ozone concentrations in this California location were higher at the beginning of
456 the ozone season, followed by relatively steady values ranging between 20-40ppb. After
457 May, however, CMAQ significantly overestimated daily ozone concentrations. The
458 overestimation was more pronounced at the end of the ozone season, resulting in an
459 overall IOA accuracy of 0.73. The DTW distance analysis showed a consistent distance
460 between CMAQ predictions and observed values. Because of this consistency, the
461 CMAQ-CNN model recognized the bias trends in CMAQ, boosting its prediction
462 accuracy by 0.17, even though the large distance from the CMAQ predictions (mean
463 distance=0.52) mirrored a relatively significant overestimation in the CMAQ-CNN post-
464 processed results.

465 Figures 6-7(b): Here, the trend in ozone concentrations followed a U-shaped curve in the ozone season
466 because of strong summer winds coming from the large bodies of water near Florida (the
467 North Atlantic Ocean and the Gulf of Mexico). For this station, CMAQ accurately
468 predicted this trend throughout the ozone season with a relatively constant bias from July
469 to September. As a result, the overall accuracy of the IOA was 0.84 for the CMAQ

470 prediction. The CMAQ was also consistent with the DTW analysis, with two distance
471 gaps in July and September (at the beginning and the end of the CMAQ overestimation
472 period). The CMAQ-CNN model, recognizing the adequate performance of the base
473 model in its post-processing algorithm, further improved the IOA accuracy of CMAQ by
474 around 10%.

475 Figures 6-7(c): The trend of observed ozone showed a steady decrease in this northeastern state because
476 of the significantly cooler summer and fall months. This trend, along with the fewer ozone
477 emission sources surrounding this station, resulted in the formation of less ozone during
478 the ozone season. The CMAQ model overestimated ozone concentrations by more than
479 50% during most of the season with a relatively large mean DTW distance (0.62). The
480 CMAQ-CNN model was able to address this issue because of the consistency of the bias
481 trend in CMAQ predictions (see left panel for DTW distance). Thus, overall, the accuracy
482 of IOA improved by 0.2.

483 The satisfactory post-processing results using the CMAQ-CNN model were mainly characterized
484 by the regularity of the bias trend in CMAQ as the base model for training the CNN model. As shown by
485 the DTW distance analysis, when the DTW distance of CMAQ predictions from observed values was
486 consistent throughout the ozone season, the CNN model was able to improve the CMAQ results to a reliable
487 level (IOA>0.8). To test this hypothesis, we used the CMAQ-CNN post-processing approach in typical
488 unsatisfactory scenarios.

489

490 3.2.2. Unsatisfactory post-processing scenarios:

491 Figure 8 compares the time series of ozone observations with the CMAQ and CMAQ-CNN models
492 at three selected EPA stations. For all of these stations, the CMAQ-CNN model failed to reach a reliable
493 IOA accuracy level of 0.8, while the accuracy of the CMAQ model improved. Figure 9 represents the DTW
494 distance analysis of the two models and the ozone observation for the same stations. Unsatisfactory
495 improvement by the CMAQ-CNN model occurred in the following three cases:

496 Figures 8-9(a): The ozone trend in this station fluctuated throughout the ozone season with frequent
497 spikes in May, July, and October, primarily the result of biomass burning (Choi et al.,
498 2016). While the CMAQ model predicted ozone concentrations with a relatively small
499 bias (IOA=0.7), the bias trend varied from time to time—that is, trends of under and over
500 predictions changed frequently. A footprint of these trends, that is, changes in the path of
501 the distance trend, is evident in the DTW analysis. This inconsistency was mirrored in the
502 equivalent DTW analysis for the CMAQ-CNN model by a consistent distance trend,
503 resulting in an unsatisfactory IOA accuracy level (IOA=0.78) with an increased mean
504 DTW distance (0.89 compared to 0.74 for the CMAQ time series).

505 Figures 8-9(b): The trend in this California location was a relatively constant concentration of ozone
506 generally ranging between 10-30ppb. The CMAQ model significantly overpredicted
507 ozone concentrations throughout the entire time period, mostly the result of the proximity
508 of this station to the Pacific Ocean (San Diego County), which controls the variation in
509 the daily ozone concentration (Pan et al., 2017). The DTW distance analysis shows a
510 significant yet steady spike in the distance between CMAQ and the observation. Thus,
511 even though the CMAQ-CNN significantly improved the accuracy of the CMAQ model
512 (IOA=0.63 compared to CMAQ IOA=0.44), the large distance accounted for the
513 underperformance of the post-processing approach. That also mirrored the consistent
514 distance in the CMAQ-CNN distance trend (see the right panel).

515 Figures 8-9(c): In this station, the ozone concentration followed an infrequent trend with lows and highs
516 spread indiscriminately across the ozone season, the result of several factors affecting air

517 pollution in this region, including biomass burning, a strong frontal system, and other
518 conditions. As a result, the CMAQ model underperformed with substantial overestimation
519 during most of the time period (IOA=0.55). In addition, the bias of the CMAQ model did
520 not follow as clear a trend as the DTW distance analysis. The CMAQ-CNN model
521 improved the prediction results by more than 10% with a reduced DTW distance (0.27 vs.
522 0.35 for the CMAQ time series). Nevertheless, the varying ozone trend accompanying the
523 inconsistency in the prediction bias trend resulted in the low overall accuracy of the IOA
524 of the CMAQ-CNN for this station (IOA=0.67).

525 Unlike the satisfactory cases, the unsatisfactory post-processing results using the CMAQ-CNN
526 model stemmed from the inconsistency in the bias trend found by the DTW distance analysis. Another
527 influential factor was the variability of observed ozone concentrations. Because of the frequent variation in
528 the observational data, it was more complicated to train the CMAQ-CNN model so that it addressed the
529 bias in the CMAQ model. The geographical location of a station was also an important factor in the
530 improvement level of the post-processing approach. Proximity to the large body of water and/or sources
531 from biomass burning during the ozone season were among the influential geographical features. Also, as
532 Figs. 8-9 show, the DTW distances of the CMAQ-CNN predictions from the observed ones followed a
533 consistent trend. Therefore, the information in Figs. 6-7 indicate that a secondary post-processing model
534 might be a possible solution to boosting prediction accuracy.

535

536 **3.3. Discussion:**

537 Despite the enormous success of the convolutional neural network (CNN) algorithm in numerous
538 applications, certain issues related to its applications in air quality forecasting (AQF) require further
539 analysis and discussion. Our main goal in this paper was to discuss some of these issues in a few practical
540 applications. To discuss these issues analytically, we used wavelet transform and dynamic time warping
541 (DTW) as powerful mathematical tools for time-series analysis and models. Based on the findings that were
542 presented in the paper, these tools are extremely helpful not only in understanding the issues with machine
543 learning models but also in fine-tuning them to improve their performances with a scientific point of view.
544 Awareness of the limitations in CNN models will enable scientists to develop more accurate regional or
545 local air quality forecasting systems by identifying the affecting factors in high concentration episodes.

546 Based on our findings in the base studies presenting the aforementioned CNN models, in both
547 cases, the CNN model shows reasonable accuracy for ozone prediction, 24 hours in advance, in two
548 geographical locations (the United States and South Korea). However, similar to other data-driven
549 prediction tools, in a CNN model, the out-of-sample prediction error is almost always greater than the in-
550 sample prediction error. Thus, since both CNN models were designed as a real-time air quality prediction
551 models, the prediction error is inevitable, even though (i) both models were configured for optimum
552 performance (based on the input or training samples), and (ii) in development of both models, cross-
553 validation processes were followed to mitigate any systematic biases. However, the underperformance of
554 the CNN model was dependent on several factors, including modeling configuration (e.g., the depth of
555 CNN model), arrangements of input variables (e.g., number of previous days as inputs), the day of the week
556 (e.g., weekdays versus weekends), the hour of the day (e.g., daytime versus nighttime) (see Eslami et al.
557 (2019a, 2019b, 2019c), Choi et al. (2019), Sayeed et al. (2020), and Lops et al. (2019), and the discussion
558 within).

559 Here, we discussed the general limitations of the CNN model in two common applications: (i) a
560 real-time AQF model, and (ii) a post-processing tool in a dynamical AQF model (i.e., CMAQ). These
561 examples are fundamentally different in terms of execution, one being a raw predictor (statistical approach)

562 while the other being a post-processor (hybrid approach). Since both models are commonly used as a real-
563 time air quality prediction system, we discussed their issues individually to explain specific issues that one
564 may encounter in executing either of them. Thus, it will provide both machine learning researchers and
565 atmospheric scientists with multiple candidate models and analytical tools to develop any specific model
566 of their choice.

567 For one case (raw prediction model), we used the wavelet transform to determine the reasons behind
568 the poor performance of CNN during the nighttime, cold months, and high ozone episodes. We find that
569 when fine wavelet modes (hourly and daily) were relatively weak or when coarse wavelet modes (weekly)
570 were strong, the CNN model produced less accurate forecasts. Since the CNN model has used only one
571 precious day of air quality and meteorological parameters, neither the coarse patterns (e.g., weekly) were
572 used as a prediction feature, nor any connection between different time-series windows (as is revealed in a
573 wavelet transform analysis) was considered. Thus, the wavelet transform can be helpful as a complementary
574 tool in filling these gaps in a CNN prediction model development. It should be noted that long short-term
575 memory (LSTM) model can potentially incorporate some of the aforementioned time-dependencies (e.g.,
576 bi-daily or weekly). However, the focus of this study is to address such a limitation in a CNN model as a
577 choice of the ML model.

578 For the other case (post-processing model), we used the DTW distance analysis to compare post-
579 processed results with their CMAQ counterparts (as a base model). For those CMAQ results with a
580 consistent DTW distance from the observation, the post-processing approach properly addressed the
581 CMAQ modeling bias with predicted IOAs exceeding 0.85. When the DTW distance of CMAQ-vs-
582 observation is irregular, the post-processing approach is unlikely to perform satisfactorily. Even though the
583 CMAQ-CNN model has included several chemical components and meteorological variables as its inputs,
584 there was no input feature representing CMAQ's own accuracy. By comparing a history of CMAQ results
585 in different geographical locations with available observation data, the DTW can provide an 'irregularity'
586 index as an additional input feature.

587 4. Conclusion:

588 Various applications of deep learning algorithms, particularly convolutional neural networks, have
589 universally been applied in the field of atmospheric sciences, especially in air quality forecasting systems.
590 Although such applications supported easy-to-use, computationally-efficient frameworks and flexible
591 capabilities appeared to generate accurate prediction results, the risk of exaggerated expectations may be a
592 cause for concern. In an effort to elucidate both the advantages and limitations of deep learning models in
593 air quality forecasting (AQF) systems, this paper addressed several common issues raised by the use of
594 these models.

595 To explore the limitation, we chose two applications of two similar CNN models. (i) CNN as an
596 independent real-time AQF; and (ii) CNN as a post-processing model of a state-of-the-art dynamical model,
597 the Community Multi-scale Air Quality Model (CMAQ). For both cases, the CNN model resulted in an
598 acceptable 24-hour in advance, hourly ozone concentration prediction with an index of agreement (IOA) of
599 more than 0.8 for two networks of monitoring stations in South Korea and the United States. We selected
600 two powerful statistical data analytic techniques—wavelet transform and dynamic time warping (DTW)—
601 to identify the limitations of the proposed models in both cases. By applying these techniques, researchers
602 find discrepancies in the input data and their temporal trends and thus gain awareness of the limitations of
603 deep learning models.

604 When the CNN model was used as a real-time AQF system in South Korea, it underperformed
605 during both cold months and high ozone episodes. In these scenarios, we found that the fine wavelet modes
606 (daily and hourly) were relatively weaker than they were in other conditions. Also, when the coarse modes
607 were strong, the predictions of the CNN model were fraught with a large number of errors. We also found
608 that the model underperformed during the nighttime hours, the results of an undertrained model and extreme
609 values of the input parameters during the nighttime.

610 For the post-processing CNN model, the level of improvement depended on the DTW distance of
611 the CMAQ model to the observations. When the calculated distance followed a consistent trend, the post-
612 processing model was able to address the bias of CMAQ, independent from its accuracy level or error range.
613 When such consistency was absent or when observed ozone varied frequently, however, the errors in the
614 CMAQ model were mirrored in the results of the post-processing model.

615 Given this discussion of the limitations of deep learning models, we suggest that researchers
616 configure their deep learning models based on temporal trends within the input parameters, geographical
617 locations, and variation frequency of target pollutants. To predict ambient hourly ozone concentrations, we
618 have restricted our discussions to a multi-output regression problem in supervised settings. While our study
619 approach might be valid for other supervised algorithms, we leave a detailed study of other supervised
620 methods for future work.

621

622 **Code availability.** The code for the algorithm development, evaluation, and statistical analysis is freely
623 available for non-commercial research purposes by contacting the corresponding author.

624

625 **Supplement.** The supplementary document related to this article is available.

626

627 **Author contribution.** E.E., Y.C, Y.L., A.S., and A.K.S. contributed to the design and implementation of
628 the research, to the analysis of the results. E.E. took the lead in writing the manuscript with inputs from
629 Y.C, Y.L., A.S., and A.K.S.. Y.C. supervised the project. E.E. and A.S. prepared the modeling input data
630 and optimized the python codes. All authors discussed the results and commented on the manuscript and
631 contributed to the final version of the manuscript.

632

633 **Competing interest.** The authors declare no competing financial and/or non-financial interests in relation
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635

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