

# The Sailor diagram. A new diagram for the verification of two-dimensional vector data from multiple models.

Jon Sáenz<sup>1,2</sup>, Sheila Carreno-Madinabeitia<sup>3</sup>, Ganix Esnaola<sup>4,2</sup>, Santos J. González-Rojí<sup>5,6</sup>, Gabriel Ibarra-Berastegi<sup>7,2</sup>, and Alain Ulazia<sup>8</sup>

<sup>1</sup>Dept. Applied Physics II, Universidad del País Vasco/Euskal Herriko Unibertsitatea (UPV/EHU), Barrio Sarriena s./n., 48940-Leioa, Spain

<sup>2</sup>Joint Research Unit BEGIK, Instituto Español de Oceanografía (IEO)-Universidad del País Vasco/Euskal Herriko Unibertsitatea (UPV/EHU), Plentziako Itsas Estazioa, Areatza Pasealekua, 48620-Plentzia, Spain

<sup>3</sup>TECNALIA, Basque Research and Technology Alliance (BRTA), Parque Tecnológico de Álava, Albert Einstein 28, E-01510 Vitoria-Gasteiz, Spain

<sup>4</sup>Nuclear Engineering and Fluid Mechanics Dept., Gipuzkoako Ingeniaritza Eskola, Europa Plaza 1, 20018-Donostia, Spain

<sup>5</sup>Oeschger Centre for Climate Change Research, University of Bern, 3010 Bern, Switzerland

<sup>6</sup>Climate and Environmental Physics, University of Bern, 3010 Bern, Switzerland

<sup>7</sup>Nuclear Engineering and Fluid Mechanics Dept., Escuela de Ingeniería de Bilbao, Plaza Ingeniero Torres Quevedo 1, 48013-Bilbao, Spain

<sup>8</sup>Nuclear Engineering and Fluid Mechanics Dept., Gipuzkoako Ingeniaritza Eskola, Otaola etorbidea 29, 20600-Eibar, Spain

**Correspondence:** Jon Sáenz (jon.saenz@ehu.eus)

**Abstract.** A new diagram is proposed for the verification of vector quantities generated by multiple models against a set of observations. It has been designed with the idea behind the Taylor diagram of providing a diagram which allows an easy comparison of simulations by multiple models against a reference dataset. However, the Sailor diagram extends this ability to two dimensional quantities such as currents, wind, horizontal fluxes of water vapour or other geophysical variables by adding features which allow to evaluate directional properties of the data as well. The diagram is based on the analysis of the two-dimensional structure of the mean squared error matrix between model and observations. This matrix is separated in a part corresponding to the bias and the relative rotation of the two orthogonal directions (empirical orthogonal functions) which best describe the vector data. We test the performance of this new diagram to identify the differences amongst the reference dataset and a series of model outputs by using some synthetic datasets and real-world examples with time-series of variables such as wind, current and vertically integrated moisture transport. An alternative setup for spatially varying time-fixed fields is shown in the last examples, where the spatial average of surface wind in the Northern and Southern Hemispheres according to different reanalyses and realizations from ensembles of CMIP5 models are compared. The Sailor diagrams presented here show that it is a tool which helps in identifying errors due to the bias or the orientation of the simulated vector time series or fields. The R implementation of the diagram presented together with this paper allows also to easily retrieve the individual diagnostics of the different components of the mean squared error and additional diagnostics which can be presented in tabular form.

## 1 Introduction

It has been long time since visual tools were recognized as an easy way to analyse different properties of datasets. This appreciation is at the root of simple and effective visualizations for exploratory data analysis such as the well-known Hovmöller diagram (Hovmöller, 1949) and the Box Plot (McGill et al., 1978). A visual tool for presenting temperature anomalies has also been recently recognized as a very effective way of presenting information regarding the evolution of climate to general audiences (Hawkins et al., 2019). Visual tools are very helpful in the scientific inquiry, see, for instance Peircean diagrammatic thinking (Dörfler, 2005). Furthermore, the visualization via diagrammatic representations does not constitute only a way of interpretation. Peircean theory of signs and other studies on scientific creative thinking show that diagrams, together with analogy or extreme thinking, also constitute a way of reasoning and knowledge generation (Dörfler, 2005; Ulazia, 2016).

Visual representation of data allows a fast and intuitive interpretation of many of their characteristics. This has led to the development of many special types of diagrams, particularly in the field of model verification. These diagrams present different measures of forecast quality as in the case of the well known Relative Operating Characteristic curve (Wilks, 2006) or a combination of Success Ratio and Probability of Detection (Roebber, 2009) to name a few.

Boer and Lambert (2001) designed a diagram based on second-order space-time differences between model simulations and observations as a tool to diagnose the performance of climate models. Their diagram was based on simple quantities such as mean square differences, variances and Pearson's correlation coefficient between observations and model runs. They used the analytical relationship between the standard deviation of the datasets, their common correlation coefficient and the squared difference between the datasets. They also showed that the diagram could be used for the evaluation of model ensembles.

Following a similar reasoning, Taylor (2001) presented a diagram which has become a well known and popular tool for the evaluation of model simulations against observed data (in general, a *reference* dataset). In the so-called Taylor diagram, the horizontal axis represents the standard deviation of the reference dataset, the radial distance represents the standard deviation ratio of the forecast against the reference and the angular distance from the  $X$  axis is related to the correlation coefficient between the reference dataset (also referred to as observations) and every model run. The distance from the point assigned to a model in the diagram to the point representing the reference dataset is related to the centered root mean squared error. In the Taylor diagram, every model tested is represented by a point in the diagram and visual inspection allows to easily determine which points are closer (i.e. present lower error) to observations. This approach works for any number of models and, therefore, comparing models using the Taylor diagram is in general faster and easier than using an equivalent table listing the different error measures. This explains the success of the diagram, as shown by the fact that the paper describing it has been cited more than 2300 times at the time of writing this contribution. This diagram is a tool that helps in the fast diagnose of the relative merits of the models. Aspects such as under or overestimated variance, incorrect phasing of the seasonal cycle and many others are reflected in the relative position of the points characterizing a model in the diagram. The diagram is flexible enough so that it can be extended to ensembles of models. More specific developments such as incorporating bootstrap techniques for the

50 estimation of confidence intervals can be easily done (González-Rojí et al., 2018; Ulazia et al., 2017) and stress the idea of flexibility associated to the Taylor diagram. Finally, since observed data also suffer from errors, an estimation of the relevance of these observational errors in different datasets can also be achieved by checking alternative measured datasets against the same reference as if they were models too (Fernández et al., 2007). Thus, the dispersion amongst observational datasets yields an estimate of the uncertainty of the observations (González-Rojí et al., 2019).

55 Pearson's correlation coefficient between two scalars plays a fundamental role in the design of Taylor's diagram, but there does not exist a single universally accepted definition of the correlation coefficient in two dimensions. Jupp and Mardia (1980) recognized that any multivariate definition of a correlation coefficient equivalent to Pearson's one must be invariant to rotation, be close to zero for independent datasets, smaller or equal than a constant and equal to that constant only if the datasets are related to each other by means of a function. Since they based their definition on these properties, they found that the sum  
60 of the squared canonical correlations was a potential definition of the squared correlation coefficient that met the previous requisites. In a previous paper, Cramer (1974) defined the two-dimensional correlation coefficient by means of the product of the canonical correlations. In this case, a low canonical correlation yields a low correlation coefficient because of the use of the product.

Stephens (1979) defined two versions of correlation between vectors by means of functions which satisfy the requirement  
65 that two perfectly correlated vector sets can be related by means of an orthogonal transformation. In this case, the vectors are assumed to share a common center and to be unit vectors, so that this measure cannot be used to identify biases between datasets or different standard deviations. In any case, the author correctly asserted that invariance to rotation does not lead to a unique definition of correlation coefficient for multivariate datasets.

Robert et al. (1985) presented an interesting review of different alternatives to compute the correlation coefficient for vector  
70 quantities. They recognized that two approaches to the problem exist. The first one is based on the use of canonical correlations between multivariate datasets. In the second approach, the definition of a two-dimensional correlation coefficient for vector datasets is based on functions which satisfy some desirable properties, such as the invariance of the correlation to the rotation of the original datasets or the existence of a limit constant for linearly related vectors as earlier suggested by Jupp and Mardia (1980).

75 Despite these many previous studies, it is a fact that up to day, several alternative versions of correlation coefficients between vectors exist. The fact that the definition of a two-dimensional correlation coefficient must satisfy the properties mentioned before was also followed by Crosby et al. (1993), who presented an in-depth review of previous definitions in oceanography and meteorology such as Kundu (1976). Crosby et al. (1993) also stated different possible definitions of the correlation coefficient. Amongst them, they proposed a definition similar to the one used by Jupp and Mardia (1980). This definition was later applied  
80 to real marine and atmospheric data sets by Breaker et al. (1994) and Cosoli et al. (2008), for instance.

However, the diagram designed by Taylor (2001) for scalar variables, is being used by modellers when comparing vectorial quantities of model output with observations. For example, Lee et al. (2013) presented a comparison of CMIP3, CMIP5, reanalysis and satellite-based estimations of wind stress by means of the average of the Taylor diagrams for the zonal and meridional components of the wind stress as a way to apply Taylor diagrams for vector quantities. A different strategy is

85 followed, for instance, in Jiménez et al. (2010). In this case, the behaviour of several models for the zonal and meridional components is not the same in terms of the identification of the model rankings. The best model for the zonal component in terms of its Taylor diagram is not the best one for the meridional component (see their Figure 6). This is a typical problem which arises when using the Taylor diagram with vector data, as also shown in a study about currents measured by means of an HF-Radar (Lorente et al., 2015). It also appears in the evaluation of global climate models using zonal and meridional  
90 components of wind speed (Martin et al., 2011) or in an analysis of moisture fluxes (Ibarra-Berastegi et al., 2011). A last example appears when wind stress components are analyzed (Chaudhuri et al., 2013). A different alternative which allows the use of the Taylor diagram for verification of wind estimations against observations is to use it as a tool to verify the magnitude of the wind (Ulazia et al., 2016, 2017; Rabanal et al., 2019). However, even in this case, the results are limited, since the information regarding errors in the direction of the vectors is lost.

95 In a recent paper, Xu et al. (2016) proposed a new method to overcome the deficiencies of the Taylor diagram for vector datasets and produced a new type of diagram visually equal to the original Taylor diagram, but which can be used for vector quantities. It is constructed on the basis of pattern similarities of vector observations and model runs and they call it Vector Field Evaluation (VFE) diagram. It is constructed from both components of the vectors which appear in the vector datasets that are used for the verification. In order to arrive to the same structure of the Taylor diagram, the authors apply some normalizations  
100 to the original two-dimensional vector quantities.

However, in the original paper by Crosby et al. (1993), the authors show that two dimensional fields showing a perfect correlation according to their definition do not have to be simple two-dimensional counterparts of what we expect in the one-dimensional case (see their Figure 3). Thus, we have decided to follow a new approximation which does not lead to the common Taylor diagram used for scalars, but gives more information about the structure of the two-dimensional errors between vector  
105 quantities involved in the verification of a vector quantity derived from a model with its observational counterpart (reference dataset). This is the rationale which leads us to base our definition in a full use of the two-dimensional structure of the mean squared error (MSE) between both vectorial datasets. This does not allow us to reduce our diagram to the well-known Taylor diagram used for scalars, as the one produced by Xu et al. (2016). However, we hope that our diagram will be considered a valuable contribution to the set of techniques used for the evaluation of models, as it visually explores other properties of  
110 the error between the vector datasets, such as the relative rotation of the major axes of variability and the underestimation (or overestimation) along each principal axis of the covariance matrix. It is the authors' need to find a solution to problems found in the past when using the Taylor diagram for vector quantities that inspired this proposal. The Sailor diagram provides a full analysis of the two-dimensional covariance matrix of the observed and simulated vector fields and, at the same time, it yields exact numerical estimations of the RMSE between those vector fields. Additional diagnostics presented in this contribution  
115 such as the relative rotation of the principal axes can be obtained following our methodology. Thus, this contribution provides a useful tool for the verification of simulated vector fields.

We propose the name Sailor diagram as a joke due to the fact that it is a diagram which can be used for winds and currents (properties of geophysical fluid dynamics that sailors need to know about) and because this name is very similar to the original

Taylor diagram. Thus, the name can be derived from the original Taylor just by changing two letters in the word (two letters  
120 equal the number of dimensions used in the diagram) following the idea behind Lewis Carroll's games with words.

Section 2 presents the datasets that we have used as examples of application of our Sailor diagram. Section 3 explains the methodology that we follow to build the two-dimensional diagram. Results are included in Section 4, followed by some concluding remarks in Section 5.

## 2 Data

125 In order to show that the diagram that we propose is of general interest and can be applied in different studies involving vector magnitudes, we have selected some examples ranging from evident variables (wind or ocean currents) to additional postprocessed quantities such as vertically integrated moisture transports.

### 2.1 Wind data

The first wind dataset that will be used in this paper corresponds to a one-year long dataset of hourly wind (zonal and meridional  
130 components) from ERA5 reanalysis at the point  $38^{\circ}$  N,  $12^{\circ}$  W, in front of Los Angeles and we will refer to it as reference (Ref) onwards. In order to produce synthetic models which are affected by individual sources of error, we have prepared a perturbed version of this dataset which we refer to as MOD1 in which we have just added a constant bias of  $(4.8, -6.8)$  m s<sup>-1</sup>. In order to address a second source of error, a change in the simulated direction, we have applied a rotation of  $30^{\circ}$  counterclockwise to the original dataset in order to produce MOD2. The rotation produces a change in the principal axes of the distribution of zonal  
135 and meridional wind and a new bias too, since it rotates the original averaged wind. A third source of error (lack of temporal correlation) is addressed by resampling (without repetition) the original Ref dataset to produce MOD3, which is characterized by perfect mean wind (no bias) and direction of major and minor axes of the distribution of wind but no correlation of wind events. A final synthetic dataset (MOD4) is produced by scaling the wind distribution with a constant factor (2) so that both the mean and the standard deviations of wind are affected.

140 Next, offshore wind data are also used as our first example of a Sailor diagram constructed with realistic data. The wind dataset (zonal and meridional components) extends from 01/01/2009 to 01/01/2015 and includes five sources (Ulazia et al., 2017). Two Weather Research and Forecasting Model (WRF) simulations around the Iberian Peninsula are used, one with 3DVAR data assimilation every six hours (experiment D) and the second one without data assimilation (experiment N). ERA Interim (ERA-I) data (Dee et al., 2011) were also used to nest the two (N and D) WRF runs and these data are also compared  
145 with observations. Fully assimilated Level 3 wind analysis data from the second version of Cross-Calibrated Multi-Platform (CCMPv2) are also used (Hoffman et al., 2003; Atlas et al., 2011) for the evaluation. The previous sources will be validated against in-situ observations provided by the buoy in Dragonera, near the Balearic Islands, a buoy managed by Spanish State Ports Authority (Puertos del Estado) (P.P.E., 2015).

## 2.2 Ocean currents

150 Three different data sources of ocean surface horizontal vectorial currents are also compared with in-situ data. They cover the Bay of Biscay area and include in-situ observations from a deep-water buoy, remotely sensed surface HF-Radar currents and an ocean modelling product. Observational products, both in-situ buoy (named DONOSTIA buoy) and remotely sensed radar currents, belong to the Basque Meteorological Agency (EUSKALMET) and were obtained from <https://www.euskoos.eus>. They provide hourly data that is punctual in the case of the buoy (approx. location  $43.6^\circ$  N and  $2.0^\circ$  W). In the case of the HF  
155 Radar dataset, it consists of a gridded dataset which covers the corner of the Bay of Biscay (approx. location  $43.5$ - $44.7^\circ$  N and  $3.2$ - $1.3^\circ$  W) with 5 km spatial resolution (Rubio et al., 2011, 2013; Solabarrieta et al., 2014). The ocean modelling product used in this example is the global analysis and forecast product of the Copernicus Marine Environment Monitoring Service (CMEMS), available through their data portal (identifier GLOBAL\_ANALYSIS\_FORECAST\_PHY\_001\_024) (Madec and the NEMO team, 2008; Lellouche et al., 2018).

## 160 2.3 Vertically integrated water vapour transports

Zonal and meridional components of vertically integrated water vapour transport have been calculated or downloaded from different sources. First, observations were obtained from the sounding data for A Coruña (Station ID 08001, longitude  $-8.41^\circ$  E and latitude  $43.36^\circ$  N) with a temporal resolution of 12 hours for the period 2010-2014. Both components of vertically integrated moisture transport from ERAI in the original vertical levels of the ECMWF model were downloaded by means of the  
165 Meteorological Archival and Retrieval System (MARS) repository at ECMWF at the nearest point to A Coruña.

Both moisture transport components were also calculated using the moisture and wind data from the previously mentioned N and D simulations created with the WRF model over the Iberian Peninsula as described by González-Rojí et al. (2018). The components of the moisture transport were calculated at the nearest point in WRF's grid by means of the vertical integration of the specific humidity (Sáenz et al., 2019) and the zonal and meridional winds over the original 51  $\eta$  levels of the WRF model.

## 170 2.4 Verification of spatial vector fields

An important application of the Taylor diagram is the verification of climate models and, as such, it is often used to verify the spatial structure of climate model outputs. In order to show that the Sailor diagram proposed in this paper can also be applied for this purpose, some reanalyses are compared. The original NCEP/NCAR first generation reanalysis (Kalnay et al., 1996) is compared to more modern reanalyses such as MERRA2 (Gelaro et al., 2017), CFSv2 (Saha et al., 2014), ERAI  
175 and ERA5 (Hersbach et al., 2018). In all those cases, we have analyzed the January average of the monthly values covering a common period (2011-2018), regridded by means of bilinear interpolation to the grid corresponding to the NCEP/NCAR reanalysis case ( $2.5^\circ \times 2.5^\circ$ ).

Finally, in terms of the application of the diagram to a typical case in the analysis of climate models, we use time-averaged wind speed over the Southern Hemisphere (1979-2015). This case example uses the time average of surface wind obtained from  
180 ERA5 as the reference dataset. In order to check the behaviour of the diagram when analyzing ensembles of multimodels, we

have also downloaded surface wind fields of the historical forcing experiment from the CMIP5 repository for the same period. The first model ensemble (four realizations) is the IPSL model, developed at the Institute Pierre-Simon Laplace (Dufresne et al., 2013), whilst the second one (three realizations) is the MIROC model (Watanabe et al., 2010). All the models and ERA5 reanalysis gridded fields have been bilinearly interpolated to a common  $1.25^\circ \times 1^\circ$  regular longitude-latitude grid. This example  
 185 is selected to illustrate the way the diagram can be applied for the analysis of ensemble data.

### 3 Methodology

In this section, we present the derivation of the  $2 \times 2$  squared-error matrix that is on the basis of the definition of the diagram that is proposed later. The two dimensional squared error matrix is decomposed in the Empirical Orthogonal Functions (EOFs) corresponding to the covariance matrix defined by the zonal and meridional components of observations (and similarly for  
 190 the covariance matrix defined by each model). Subsection 3.1 describes the decomposition of the matrix  $\mathbf{U}$  corresponding to the reference dataset (observations) in its EOFs. A similar notation will be used later for the decomposition of the matrix  $\mathbf{V}$  corresponding to the zonal and meridional components of every model which is being compared to observations. Later, the expansion of the  $\mathbf{V}$  matrix corresponding to the model is expressed as a rotation from the the EOFs derived from observations (Subsection 3.2).

#### 195 3.1 Decomposition of $\mathbf{U}$ in its EOFs

We consider a time series or spatial field of a two-dimensional vectorial variable such as horizontal wind, vertically integrated moisture transport or horizontal currents, for instance. It has been measured at an observatory or buoy (time series) or it is a time-average over a grid (the case of the evaluation of a climatology derived from climate models). By now, we will consider that we are evaluating a time-series of  $N$  samples, but later we will present results where the  $N$  represents the number of  
 200 grid points where a time-averaged field is defined. Note that in the following presentation,  $\mathbf{U}$  includes the zonal and meridional components of observations and so does  $\mathbf{V}$  for a simulated dataset. The observational dataset is formed by the two-dimensional (zonal and meridional) components of vector measurements  $\mathbf{u}_i$ , with  $i = 1 \dots N$  arranged as rows in an  $N \times 2$  matrix  $\mathbf{U}$ . The average  $\bar{\mathbf{u}}$  of the  $\mathbf{u}_i$  time series will be repeated as constant rows in an  $N \times 2$  matrix  $\bar{\mathbf{U}}$ . The  $\mathbf{U}$  matrix can be expressed by means of the empirical orthogonal functions of the original vector data by using the expression

$$205 \quad \mathbf{U} = \bar{\mathbf{U}} + \mathbf{P}_u^* \boldsymbol{\Sigma}_u \mathbf{E}_u^T = \bar{\mathbf{U}} + \mathbf{P}_u \mathbf{E}_u^T, \quad (1)$$

with  $\mathbf{P}_u^*$  (an  $N \times 2$  matrix) the standardized principal components of the  $\mathbf{U}$  data,  $\boldsymbol{\Sigma}_u$  ( $2 \times 2$  matrix) the standard deviations ( $\sigma_{1u}$  and  $\sigma_{2u}$ ) of the leading and second EOFs of the  $\mathbf{U}$  field,  $\mathbf{E}_u$  ( $2 \times 2$  matrix) the matrix holding the orthogonal rotation-matrix leading to the empirical orthogonal functions of the  $\mathbf{U}$  field arranged as columns and  $\mathbf{P}_u = \mathbf{P}_u^* \boldsymbol{\Sigma}_u$  ( $N \times 2$  matrix) the variance-holding principal components. Please, note that when the standardized principal components  $\mathbf{P}_u^*$  are used, this matrix  
 210 is always multiplied by the corresponding standard deviations, so that no variance is lost in the process. Thus, the anomalies of

wind are computed without any loss of variance as

$$\mathbf{U} - \bar{\mathbf{U}} = \mathbf{P}_u^* \boldsymbol{\Sigma}_u \mathbf{E}_u^T = \mathbf{P}_u \mathbf{E}_u^T \quad (2)$$

and the corresponding principal components

$$\mathbf{P}_u = \mathbf{P}_u^* \boldsymbol{\Sigma}_u = (\mathbf{U} - \bar{\mathbf{U}}) \mathbf{E}_u, \quad (3)$$

215 and their standardized counterparts

$$\mathbf{P}_u^* = (\mathbf{U} - \bar{\mathbf{U}}) \mathbf{E}_u \boldsymbol{\Sigma}_u^{-1}. \quad (4)$$

Unless the wind (current) time series is completely arranged across a straight line (something which is very unlikely in observed vector variables unless the flow is stationary and laminar),  $\boldsymbol{\Sigma}_u$  is a full-rank diagonal matrix:

$$\boldsymbol{\Sigma}_u = \begin{pmatrix} \sigma_{1u} & 0 \\ 0 & \sigma_{2u} \end{pmatrix}, \quad (5)$$

220 with  $\sigma_{1u} > \sigma_{2u}$ . Due to the fact that the rotation matrix is always full rank (in the two-dimensional space spanned by the zonal and meridional components, given enough samples), the  $\mathbf{E}_u$  matrix can also be interpreted geometrically as a rotation matrix expressed as a function of the angle  $\theta_u$  formed by the leading (second) EOF with the zonal (meridional) axis as:

$$\mathbf{E}_u = \begin{pmatrix} \cos \theta_u & -\sin \theta_u \\ \sin \theta_u & \cos \theta_u \end{pmatrix}, \quad (6)$$

The first column of the  $\mathbf{E}_u$  matrix is the first eigenvector of observations in the horizontal plane,  $\mathbf{e}_{u1}$ . Similarly, the second  
225 column of  $\mathbf{E}_u$  corresponds to  $\mathbf{e}_{u2}$ , the second eigenvector of the observational covariance matrix.

The principal components and EOF rotation matrices fulfill the well-known orthogonality properties

$$\mathbf{P}_u \mathbf{P}_u^T = \boldsymbol{\Sigma}_u^2, \quad (7)$$

so do the standardized principal components

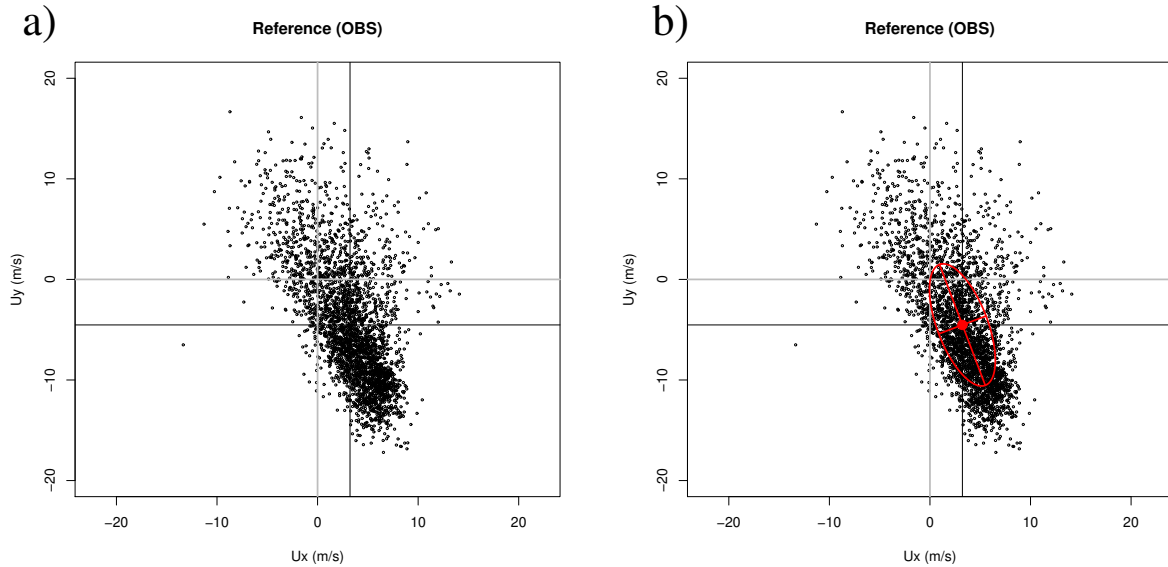
$$\mathbf{P}_u^* \mathbf{P}_u^{*T} = \mathbb{1} \quad (8)$$

230 and eigenvectors (EOFs) in the horizontal plane

$$\mathbf{E}_u \mathbf{E}_u^T = \mathbf{E}_u^T \mathbf{E}_u = \mathbb{1}. \quad (9)$$

Figure 1 (panel a) illustrates in a scatterplot the distribution of measurements of zonal and meridional wind components in the Reference dataset. Panel b in Figure 1 shows the definition of the ellipses centered in the mean of the reference dataset used in the Sailor diagrams by using the semi-major and semi-minor axes as defined by the EOF decomposition of the two-dimensional  
235 covariance matrix of the zonal and meridional components of the original vector field, the directions of the principal axes





**Figure 1.** Scatterplot of wind in dataset Ref (panel a) and its decomposition in terms of the principal axes corresponding to the covariance matrix of the zonal and meridional components (panel b) as defined in Equation (1).

(matrix  $\mathbf{E}_u$ ) and the standard deviations corresponding to the principal components  $\mathbf{P}_u$ . From equations (4) and (8), the quadratic form leading to the ellipses in the diagram can be obtained by applying the Frobenius norm to equation (8) as

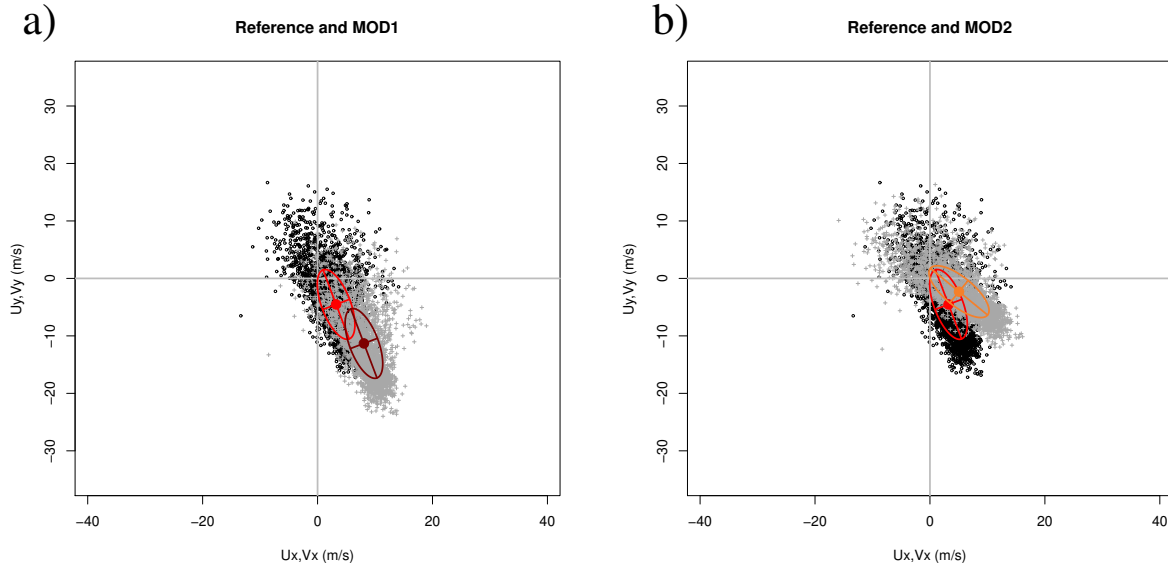
$$\|\mathbf{P}_u^* \mathbf{P}_u^{*T}\|_F = \|(\mathbf{U} - \bar{\mathbf{U}}) \mathbf{E}_u \boldsymbol{\Sigma}_u^{-2} \mathbf{E}_u^T (\mathbf{U} - \bar{\mathbf{U}})^T\|_F = 1. \quad (10)$$

The principal components are combined according to the quadratic form in Equation (10). This shows that the ellipse  
 240 produced from the EOF decomposition of the two-dimensional covariance matrix is a good way to make a simple and clear  
 representation of the original scatterplot. The eccentricity of the ellipse

$$\varepsilon_u = \sqrt{1 - \frac{\sigma_{2u}^2}{\sigma_{1u}^2}} \quad (11)$$

is an interesting indicator for additional diagnostics designed for testing the reliability of rotation angles due to the degeneracy  
 of the eigenvalues.

245 Following similar notation to the one used for the observations ( $\mathbf{U}$  matrix), the time series (or time-averaged constant field  
 over  $N$  points in a grid) of simulated wind (current, wave energy flux, vertically integrated moisture transport ...) at the same  
 observatory (or the closest grid point) formed by the two-dimensional (zonal and meridional components) simulations  $\mathbf{v}_i$ , with  
 $i = 1 \dots N$  will be arranged as rows in an  $N \times 2$  matrix  $\mathbf{V}$ . The average vector from model data  $\bar{\mathbf{v}}$  is arranged as constant rows  
 in an  $N \times 2$  matrix  $\bar{\mathbf{V}}$ . The  $\mathbf{V}$  matrix (and its anomalies) can be expressed as done for observations as in Equations (1) and (2)  
 250 above by means of the empirical orthogonal functions of the two-dimensional covariance matrix from simulated zonal and



**Figure 2.** Scatterplot of wind in datasets Ref (panel a, black circles) and MOD1 (panel a, grey crosses) and their decomposition in terms of the principal axes corresponding to the covariance matrix of the zonal and meridional components of each dataset as defined in Equations (9) and (12). The comparison of the reference dataset (black circles) with model MOD2 (grey crosses) is shown in panel b.

meridional components of wind (current, moisture transport ...) data

$$\mathbf{V} = \bar{\mathbf{V}} + \mathbf{P}_v^* \Sigma_v \mathbf{E}_v^T = \bar{\mathbf{V}} + \mathbf{P}_v \mathbf{E}_v^T \Leftrightarrow \mathbf{V} - \bar{\mathbf{V}} = \mathbf{P}_v^* \Sigma_v \mathbf{E}_v^T = \mathbf{P}_v \mathbf{E}_v^T, \quad (12)$$

with equivalent interpretations and equal ranks for  $\mathbf{P}_v^*$ ,  $\Sigma_v$ ,  $\mathbf{E}_v$  and  $\mathbf{P}_v = \mathbf{P}_v^* \Sigma_v$  as presented before for observations.

### 3.2 Expansion of the matrix $\mathbf{V}$ in the EOFs defined by observations

255 In general, the mean values and EOFs derived from observations ( $\mathbf{U}$ ) and simulations ( $\mathbf{V}$ ) will not be the same. This is shown in Figure 2, with panel a clearly showing a change in the bias between both datasets and a counter-clockwise rotation for the case of panel b, as expected from the way these synthetic datasets were produced. It is clearly seen that in the case of MOD1 the structure of the covariance matrix has not changed, whilst a different orientation (but no scaling of the semi-major and semi-minor axes) appears in the case of MOD2.

260 In order to identify these kind of errors (derived from rotations of the axes), the orthonormal EOFs in the  $\mathbf{E}_v$  matrix can be expressed as the result of a rotation applied to the EOFs derived from the observations (accepting these as *true* EOFs). Thus, the rotation matrix  $\mathbf{R}_{vu}$  is defined by an angle  $\theta_{vu} = \theta_v - \theta_u$  as

$$\mathbf{R}_{vu} = \begin{pmatrix} \cos \theta_{vu} & -\sin \theta_{vu} \\ \sin \theta_{vu} & \cos \theta_{vu} \end{pmatrix}, \quad (13)$$

so that

$$265 \quad \mathbf{E}_v = \mathbf{R}_{vu} \mathbf{E}_u, \quad (14)$$

$$\mathbf{V} = \bar{\mathbf{V}} + \mathbf{P}_v \mathbf{E}_u^T \mathbf{R}_{vu}^T \quad (15)$$

and the corresponding principal components can be expanded as

$$\mathbf{P}_v = (\mathbf{V} - \bar{\mathbf{V}}) \mathbf{R}_{vu} \mathbf{E}_u = \tilde{\mathbf{V}} \mathbf{E}_u, \quad (16)$$

270 with  $\tilde{\mathbf{V}} = (\mathbf{V} - \bar{\mathbf{V}}) \mathbf{R}_{vu}$  representing the model-based  $\mathbf{V}$  anomalies *rotated* to the basis given by the EOFs corresponding to observations.

Since both  $\mathbf{e}_{u1}$  and  $-\mathbf{e}_{u1}$  are solutions of the eigenvalue equation when the diagonalization of the two-dimensional covariance matrix is performed (the same happens with  $\mathbf{e}_{v1}$  and  $-\mathbf{e}_{v1}$  for model data),  $\theta_{vu}$  may take difficult to understand values even for eigenvectors which span similar subspaces. This is due to the fact that both  $\theta_{vu} = 0$  and  $\theta_{vu} = \pi$  refer to eigenvectors that point in perfect directions. In order to provide an easier to interpret diagnostic of the adequacy of the EOFs from observations and model, the absolute value of the congruence coefficient (Cheng et al., 1995) can also be used. It is defined as

$$g_{ii} = |\mathbf{e}_{ui} \cdot \mathbf{e}_{vi}| \quad (17)$$

and measures the agreement between the pairs of EOFs from observations ( $\mathbf{e}_{ui}$ ) and models ( $\mathbf{e}_{vi}$ ). Since this coefficient equals the cosine of the angle between both directions, and since the absolute value is used, the closest its value is to one, the best agreement exists between  $\mathbf{e}_{ui}$  and  $\mathbf{e}_{vi}$ . Due to the orthogonality relationship between the EOFs, only the congruence coefficient for EOF1 is computed, since it is equal to the one computed using EOF2 (matrices  $\mathbf{E}_u$  and  $\mathbf{E}_v$  are orthonormal).

### 3.3 Expansion of the mean-squared error

The  $(2 \times 2)$  matrix that represents the mean squared error between the  $\mathbf{U}$  and  $\mathbf{V}$  datasets is given by

$$\Delta_{uv}^2 = \frac{1}{N} (\mathbf{V} - \mathbf{U})^T (\mathbf{V} - \mathbf{U}) \quad (18)$$

285 and the aggregated scalar mean squared error of both components of the vector dataset is given by its Frobenius norm

$$\varepsilon^2 = \|\Delta_{uv}^2\|_F. \quad (19)$$

Substituting Eq. (1) and Eq. (12) into Eq. (18), it can be shown that

$$\Delta_{uv}^2 = \frac{1}{N} \mathbf{B}_{uv}^2 + \frac{1}{N} (\mathbf{S}_{uv}^T + \mathbf{S}_{uv}) + \frac{1}{N} \mathbf{D}_{uv} = \frac{1}{N} \mathbf{B}_{uv}^2 + \frac{1}{N} \mathbf{C}_{uv} + \frac{1}{N} \mathbf{D}_{uv} \quad (20)$$

with

$$290 \quad \mathbf{B}_{uv}^2 = (\bar{\mathbf{V}} - \bar{\mathbf{U}})^T (\bar{\mathbf{V}} - \bar{\mathbf{U}}), \quad (21)$$

$$\mathbf{S}_{uv} = (\mathbf{E}_v \boldsymbol{\Sigma}_v \mathbf{P}_v^{*T} - \mathbf{E}_u \boldsymbol{\Sigma}_u \mathbf{P}_u^{*T}) (\bar{\mathbf{V}} - \bar{\mathbf{U}}) = (\mathbf{E}_v \mathbf{P}_v^T - \mathbf{E}_u \mathbf{P}_u^T) (\bar{\mathbf{V}} - \bar{\mathbf{U}}) \quad (22)$$

and

$$\mathbf{D}_{uv} = \mathbf{E}_u \boldsymbol{\Sigma}_u^2 \mathbf{E}_u^T + \mathbf{E}_v \boldsymbol{\Sigma}_v^2 \mathbf{E}_v^T - (\mathbf{E}_u \boldsymbol{\Sigma}_u \mathbf{P}_u^{*T} \mathbf{P}_v^* \boldsymbol{\Sigma}_v \mathbf{E}_v^T + \mathbf{E}_v \boldsymbol{\Sigma}_v \mathbf{P}_v^{*T} \mathbf{P}_u^* \boldsymbol{\Sigma}_u \mathbf{E}_u^T) \quad (23)$$

295 which can also be written using non-standardized  $\mathbf{P}_u$  and  $\mathbf{P}_v$  principal components as

$$\mathbf{D}_{uv} = \mathbf{E}_u \boldsymbol{\Sigma}_u^2 \mathbf{E}_u^T + \mathbf{E}_v \boldsymbol{\Sigma}_v^2 \mathbf{E}_v^T - (\mathbf{E}_u \mathbf{P}_u^T \mathbf{P}_v \mathbf{E}_v^T + \mathbf{E}_v \mathbf{P}_v^T \mathbf{P}_u \mathbf{E}_u^T). \quad (24)$$

$\mathbf{B}_{uv}^2$  represents the part of the squared error due to the magnitude of the bias vector (difference of both means) between both vector datasets.

The (symmetric) matrix  $\mathbf{C}_{uv} = \mathbf{S}_{uv}^T + \mathbf{S}_{uv}$  reflects the error due to the projection of the bias into the differences of vector anomalies. Since the bias matrices are constant, the sum of the projections become the sum of anomalies and, as such, they become zero. This interpretation is clear if Eq. (2) and the corresponding one for the model anomalies are substituted into the definition of the matrix  $\mathbf{S}_{uv}$  in Eq. (22), yielding

$$\mathbf{S}_{uv} = ((\mathbf{V} - \bar{\mathbf{V}}) - (\mathbf{U} - \bar{\mathbf{U}}))^T (\bar{\mathbf{V}} - \bar{\mathbf{U}}) = (\mathbf{V} - \mathbf{U})^T (\bar{\mathbf{V}} - \bar{\mathbf{U}}) - (\bar{\mathbf{V}} - \bar{\mathbf{U}})^T (\bar{\mathbf{V}} - \bar{\mathbf{U}}) = 0. \quad (25)$$

Since this matrix is zero,  $\mathbf{C}_{uv}$  will also be zero.

305 Finally, the matrix  $\mathbf{D}_{uv}$  is related to the covariance matrix of anomalies, as also clearly seen if Eq. (2) and the corresponding one for simulated data are substituted into Eq. (24).

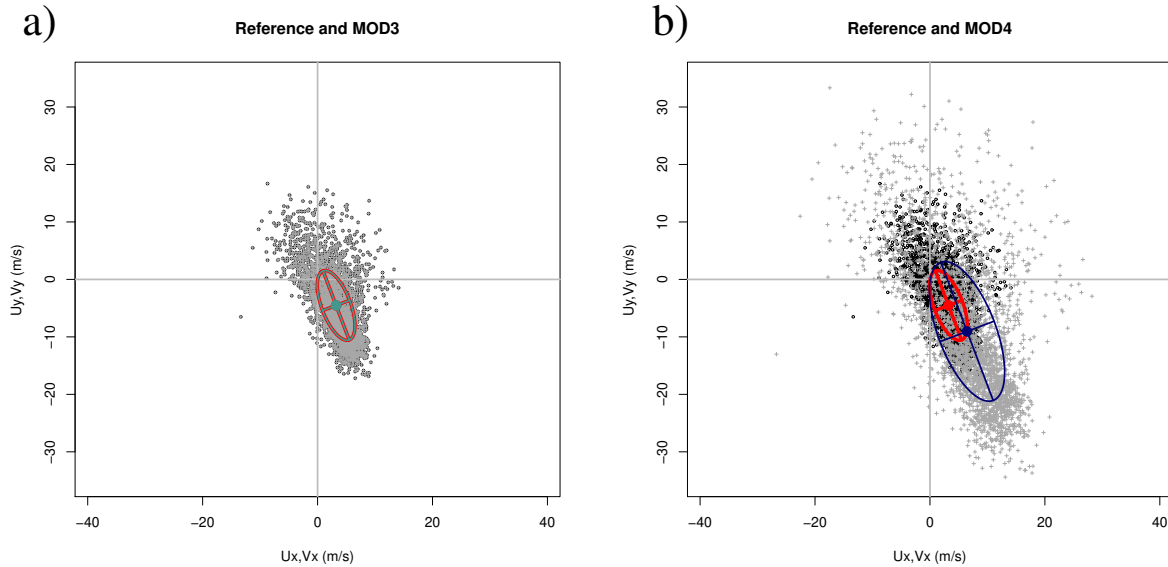
In order to improve the graphical interpretation of the components of the error, the expression of the empirical orthogonal functions of  $\mathbf{V}$  as a rotation of the *true* ones (derived from observations  $\mathbf{U}$ ) is used. Thus, considering Eq. (14), the matrix  $\mathbf{D}_{uv}$  above can be rewritten in terms of the EOFs corresponding to observations as

$$310 \quad \mathbf{D}_{uv} = \mathbf{E}_u \boldsymbol{\Sigma}_u^2 \mathbf{E}_u^T + \mathbf{R}_{vu} \mathbf{E}_u \boldsymbol{\Sigma}_v^2 \mathbf{E}_u^T \mathbf{R}_{vu}^T - (\mathbf{E}_u \mathbf{P}_u^T \mathbf{P}_v \mathbf{E}_u^T \mathbf{R}_{vu}^T + \mathbf{R}_{vu} \mathbf{E}_u \mathbf{P}_v^T \mathbf{P}_u \mathbf{E}_u^T). \quad (26)$$

If  $\boldsymbol{\Gamma}_{vu} = \mathbf{P}_u^T \mathbf{P}_v$  is proportional to the covariance between both datasets' principal components, the above expression can be written as:

$$\mathbf{D}_{uv} = \mathbf{E}_u \boldsymbol{\Sigma}_u^2 \mathbf{E}_u^T + \mathbf{R}_{vu} \mathbf{E}_u \boldsymbol{\Sigma}_v^2 \mathbf{E}_u^T \mathbf{R}_{vu}^T - (\mathbf{E}_u \boldsymbol{\Gamma}_{vu} \mathbf{E}_u^T \mathbf{R}_{vu}^T + \mathbf{R}_{vu} \mathbf{E}_u \boldsymbol{\Gamma}_{vu}^T \mathbf{E}_u^T). \quad (27)$$

The interpretation of this expression is that all the matrices involved in the mean squared error can be expressed in the axes defined by the leading and second EOFs of the  $\mathbf{U}$  (observational) dataset. Thus, using the axes corresponding to the observational dataset  $\mathbf{U}$ , we can produce a diagram which gives us a fast visual impression of the structure of the error in two-dimensional variables the same way the Taylor diagram performs for univariate datasets. Therefore, the diagram presented in this contribution includes not only scalar information in the estimation of the error, but also information regarding the main directions



**Figure 3.** Scatterplot of wind in datasets Ref (panel a, black circles) and MOD3 (panel a, grey crosses) and their decomposition in terms of the principal axes corresponding to the covariance matrix of the zonal and meridional components of each dataset. The comparison of the reference dataset (black circles) with model MOD4 (grey crosses) is shown in panel b.

of variability of the vectors and their differences by means of the characteristics of the ellipses defined by Eq. (16) from the  
 320 different datasets.

Figure 3 presents two interesting cases. The first case, MOD3, is implausible from the point of view of a real model, but it constitutes an interesting case study to analyze the properties of the diagram. In MOD3, a simple random permutation of the original observations has been performed. Thus, there are neither bias nor rotations of the principal axes. From the point of view of the graphical example shown, it seems that the model is perfect, but it is not, due to the lack of temporal correlation  
 325 between model and observations. This is only apparent if the full RMSE is taken into account, as shown by Table 1. Thus, a legend with the RMSE as defined in Eq. (19) must be added to the plot in order to arrive to precise comparison of datasets.

On the other side, panel b in Figure 3 shows that for the scaled dataset (MOD4), the sizes of the major and minor axes of the ellipses allow a fast visual detection of the scaling present in the dataset. The individual components of the error for all the synthetic datasets used in the description of the methodology are also presented in Table 1. The last column shows the full  
 330 RMSE between vector fields. It is apparent from this aggregated estimation of error that it properly evaluates the differences due to the lack of correlation that have been mentioned in the case of MOD3 (no bias and perfect orientation and axes of the ellipses) too. The rotation angle (column  $\theta_{vu}$  in radians) correctly identifies the way the errors have been introduced in the different synthetic models. The same can be said of the different standard deviations (columns  $\sigma_{U_x}$ ,  $\sigma_{U_y}$ ,  $\sigma_{V_x}$  and  $\sigma_{V_y}$ ), which also support the way the ellipses are presented in Figures 1 to 3.

	Model	$\sigma_{U_x}$	$\sigma_{U_y}$	$\sigma_{V_x}$	$\sigma_{V_y}$	$\theta_u$	$\theta_v$	$\theta_{vu}$	$R^2$	bias	RMSE
1	Ref	3.27	6.07			1.93			2.00	0.00	0.00
2	MOD1			3.27	6.07		1.93	-0.00	2.00	8.34	5.56
3	MOD2			5.22	4.51		2.46	0.52	2.00	2.88	8.69
4	MOD3			3.27	6.07		1.93	-0.00	0.00	0.00	1.84
5	MOD4			6.54	12.14		1.93	0.00	2.00	5.56	11.76

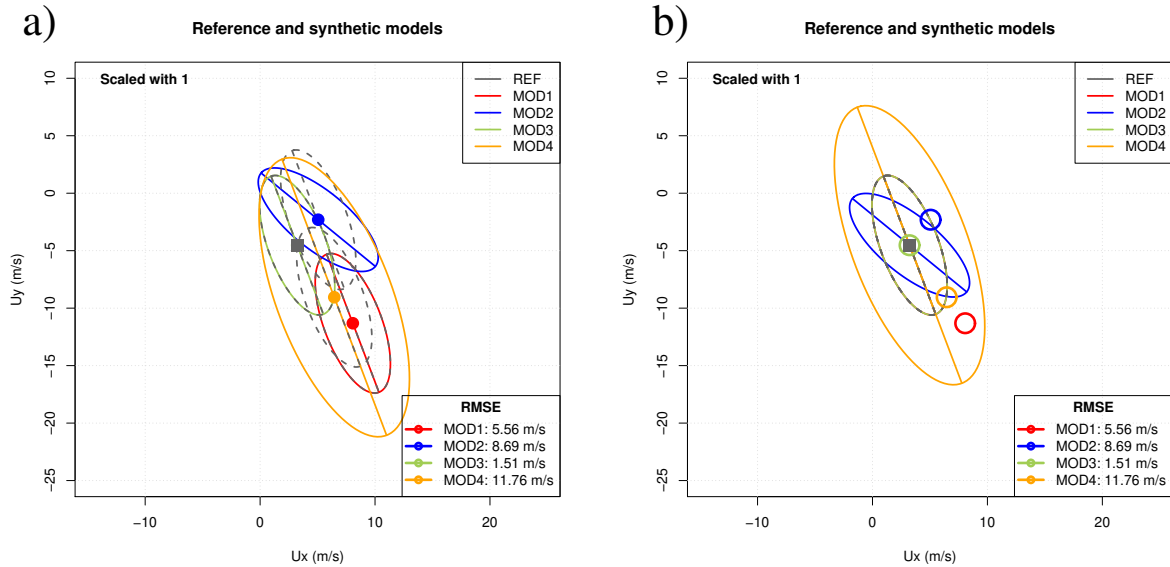
**Table 1.** Individual components of the error for the synthetic datasets used for illustration of the methodology.  $\sigma_x$  and  $\sigma_y$  represent the standard deviations ( $\text{m s}^{-1}$ ) of wind for every dataset (reference or model).  $\theta_u$  and  $\theta_v$  represent the angles (radians) of the semi-major axes of the ellipses calculated from reference and model.  $\theta_{vu}$  (radians) represents the relative rotation of the semi-major axis of the modelled dataset with respect to the observations.  $R^2$  represents the two-dimensional squared correlation coefficient (sum of the squared canonical correlations). |bias| represents the magnitude of the bias ( $\text{m s}^{-1}$ ) and RMSE the root mean squared error ( $\text{m s}^{-1}$ ).

335 The different properties of the synthetic datasets presented so far can be abbreviated in Figure 4, which presents in panels  
a (left) and b (right) uncentered and centered (respectively) versions of the Sailor diagram. In the uncentered version of the  
Sailor diagram, each ellipse, as defined by Eq. (10), is centered in its own average. This allows an easy interpretation of the  
bias term. In order to improve the interpretability of the rotation/scaling parameters of the ellipses (semi-major and semi-minor  
axes and standard deviations), the ellipse corresponding to observations is also drawn in gray centered at the same average of  
340 every model. This way, the rotations and scalings of the vectors produced by models can easily be compared against the ones  
drawn from observations. However, in some cases (depending on the relative values of the bias and the standard deviations), it  
might be more interesting to plot all the ellipses centered at the mean corresponding to the observations and identify the bias  
by means of coloured dots, as shown in the centered version of the diagram (right panel in Figure 4).

An additional reason which supports that the Sailor diagram introduces powerful diagnostics for vector data is properly  
345 shown in Table 1. According to the column which shows the squared correlation coefficient, all models show a perfect match  
( $R^2 = 2$ ) for the two-dimensional correlation coefficient except the one built by randomly resampling the data (MOD3). How-  
ever, Figures 2 and 4 clearly show that the wind data in MOD2 is rotated with respect to the reference dataset. This is  
not detected by  $R^2$  because it yields perfect results by construction when there is a linear relationship between both vector  
datasets (Crosby et al., 1993). However, an analysis based on the full components of the RMSE as the one performed in the  
350 Sailor diagram (Figure 4 and Table 1) clearly highlights these directional problems.

### 3.4 Extension of the methodology to spatial fields

In the case of the analysis of the ability of models to represent the spatial distribution of an averaged field (a typical use of the  
Taylor diagram in climatology, for instance), there is no change needed to the diagram defined so far. Instead of using the  $T$ -  
mode of principal components (covariance matrix defined by temporal covariances), we can just use the  $S$ -mode, in traditional  
355 terminology of principal components (Compagnucci and Richman, 2008). Thus, in the previous description,  $N$  will run along



**Figure 4.** Uncentered (left) and centered (right) versions of the Sailor diagram after placing the ellipses from all the synthetic datasets in the same plot.

the grid points, and the two-dimensional biases and covariances are computed in the spatial domain, but the error analysis is still being performed onto two-dimensional vectors. As an example of this very common case in the application of Taylor's diagram to climatology, we present an example including the comparison of multi-year averages of Northern Hemisphere surface wind vectors. For the case of spatial grids, an external standard area-weighting by means of factors given by  $\sqrt{\cos\phi}$  with  $\phi$  latitude (North et al., 1982) is commonly applied to the data in order to avoid an excessive weight in the results of points in polar latitudes which represent much a lower area in a regular longitude-latitude grid.

### 3.5 Use of the diagram with ensembles of models

As a final example, the use of the diagram with a multimodel ensemble is shown. In this case, the climatologies of surface wind from two models with a different number of realizations are compared with the corresponding climatology from ERA5. As described above, since this is also a comparison of data on a regular longitude-latitude grid, the covariance matrix is also built over the spatial points and the external weights are also applied to avoid an overrepresentation of polar regions in the results.

### 3.6 R package implementing the methodology

The authors have created an R package called `SailOR` which is freely available in the Comprehensive R Archive Network (CRAN). The package has been used to produce the plots presented in section 4, and the code to prepare some of these plots are provided as examples in the manual of the package. Besides producing the diagrams shown as an example in this paper, the

package also computes all the individual terms used in the analysis of the MSE error as described in Section 3. Thus, different aspects of the main principal axes, their relative rotation, the two-dimensional correlation coefficient and the combined RMSE can be readily analyzed for different vector datasets and exported to tables which can be presented in publications.

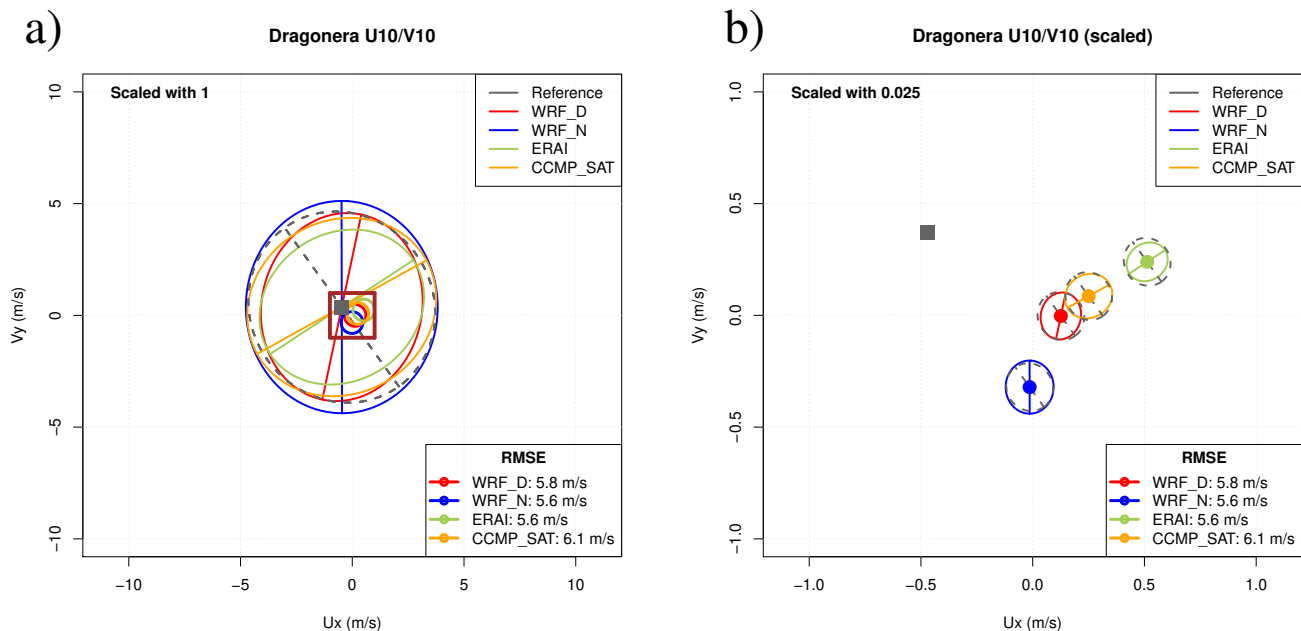
## 4 Use of the elements in the error matrix in the diagram

### 375 4.1 Wind over a Mediterranean location

The first example of a Sailor diagram built using real data is shown in Figure 5 (left). In it, the  $X$  axis represents the zonal component of wind and the  $Y$  axis its meridional component. The mean 2D vector corresponding to each of the datasets is represented by a colored circle, except for the reference dataset, which uses a grey square. The leading EOF of the two-dimensional covariance matrix of zonal and meridional components of every dataset is represented by the direction corresponding to the semi-major axis of the ellipse that is plotted centered at every model's mean value (same colour as the one used to represent the model mean). The second EOF to each model is perpendicular to the previous direction by construction due to the orthonormality constraint in Equation (9). The grey ellipse centered at each model mean represents the EOF from the reference dataset (observations). Thus, the angle between the colored and grey semi-major axes represents the relative rotation ( $\theta_{vu}$ ) between EOFs from observations and simulations. The lengths of the semi-major and semi-minor axes (colour and grey) show the variances explained by each EOF (model and reference) at their principal axes. The comparison of these lengths between coloured and grey ellipses allows to address the question whether the model underestimates or overestimates the variances at each of the principal axes. In this particular example, since the model vs observation biases are much lower than the variance explained by the principal axes defined by the EOFs, the interpretation of this diagram is not very easy. However, it is already showing the main directions of the error matrices, their biases and the position of the reference dataset. The bottom right legend shows the total RMSE error given by Eq. (19) in subsection 3, which takes into account both the contribution from the bias (distance of the points to the reference dataset's mean) and the different orientation and lengths of the major and minor axes (EOFs).

In order to show that different designs optimize the information transmitted by the diagram, in the second diagram prepared using the data from the same example, the ranges of both axes are limited and the ellipses corresponding to the main directions of the error matrix are accordingly scaled by means of a small scale factor (0.025). The brown square in left panel shows the area which is amplified in the right panel and it illustrates the role played by the scale factor, which reduces (or amplifies) the size of the axes of the ellipses, thus making easier to appreciate the relative differences in biases while still making possible to get access to the information relative to the rotation of the principal axes. In the scaled version of the diagram (Figure 5, right) it can be seen that the distance between every coloured point corresponding to a given model to the grey square represents the bias amongst the datasets and they can effectively be visually compared. On the other hand, the grey ellipses and their semiaxes show the main structure of the variability of the reference dataset. This grey ellipse is plotted centered on the point representing the mean of every model, where the EOFs corresponding to that model are also shown for comparison. Both ellipses (the one corresponding to the model being analyzed and the one corresponding to the reference dataset) are scaled by the same scale factor so that they are not deformed during the scaling process. The use of ellipses and their major and minor

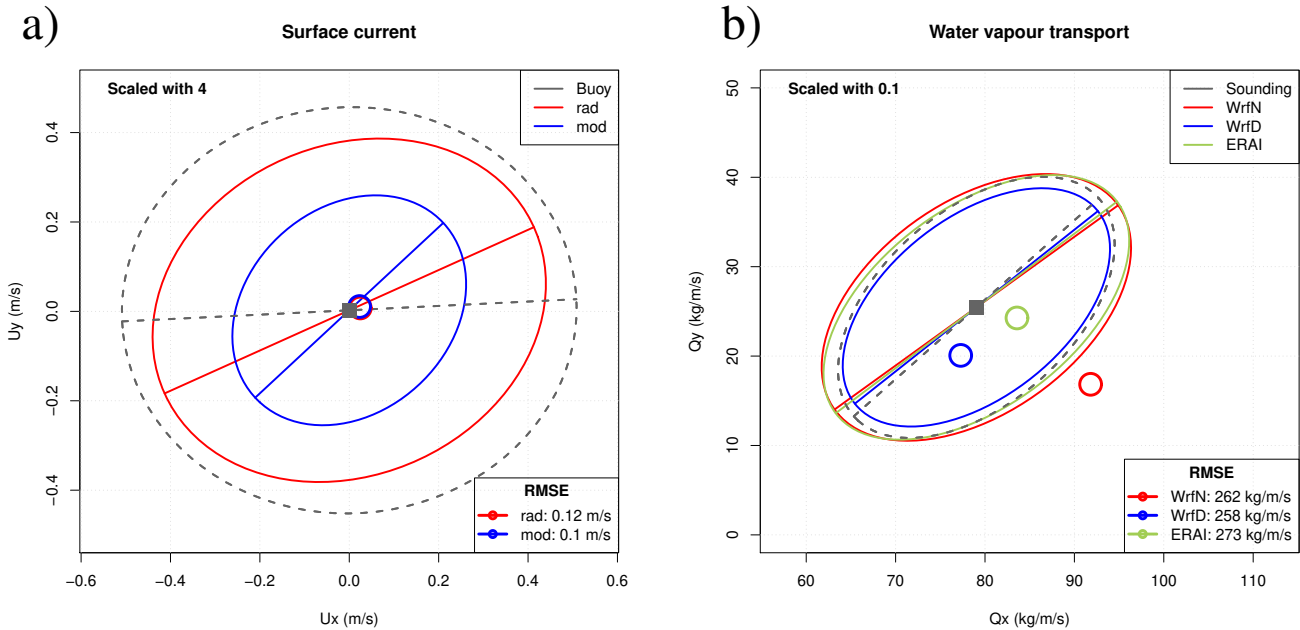




**Figure 5.** Sailor diagram with default parameters (left) and ellipses scaled by a factor 0.025 to improve visibility of the directional error (right) for the wind observed and simulated in Dragonera (buoy in the Mediterranean).

axes easily allows to compare the main directions of variability of the observed (grey) and modelled (colored) winds. It shows  
 405 that the ones corresponding to the WRF model are the closest ones to observations. It can be seen that both WRF simulations  
 show a smaller rotation of their major axes with respect to the one from observations. The model EOFs are almost orthogonal  
 from the ones in observations for the case of ERAI or CCMPv2 (CCMP\_SAT in legend). The bottom right legend, in any case,  
 presents the real RMSE error without scaling its value.

In this particular case, it might seem sensible to think that the fact that the variances of the major and minor axes are very close  
 410 points to a weakness of the diagram since, in that case, the determination of the angle of the axes will be arbitrary. However,  
 it has to be considered that the final index of agreement would still be the RMSE, which does not depend on the eigenvectors  
 of the covariance matrix. Thus, the results in terms of direction might not be very reliable in case that the eigenvalues are  
 degenerated, but the RMSE is not affected by this problem. Thus, the use of the eccentricity of the ellipses (provided as an  
 output in our R package) can be useful to diagnose those cases (in which eccentricity is very low) that make estimations of  
 415 relative rotations difficult. For a more precise determination of the reliability of the rotation angle, a bootstrap analysis of the  
 rotation angles can also be conducted, if needed, since the evaluation of the angles is independent of the production of the  
 diagram.



**Figure 6.** Sailor diagram representing the structure of errors between HF radar estimations of currents (rad) and model results (mod) with variances corresponding to EOFs scaled with scale factor of 4 (left). Sailor diagram derived from vertically integrated water vapour transport (right) scaled with a factor of 0.1.

## 4.2 Surface current in the Bay of Biscay

Figure 6 (left) shows an alternative version of the Sailor diagram. In this particular case, the bias is relatively low. Thus, in order to ease the interpretation of the structure of the errors, the ellipses representing the first and second EOFs are drawn on top of the point corresponding to observations. The fact that the bias is small is only affecting the part of the RMSE derived from term  $B_{uv}^2$  in Eq. (20). As in the previous case, they are scaled (four times larger) in order to improve their visibility. It is clear that the relevant part in terms of the errors of models versus observations is not the bias, but the way the variability is represented, instead. The HF-Radar data's leading EOF (observational data, actually) is closer to the one from in-situ observations, as could be expected, since both cases represent observational (in-situ versus remote) estimations of currents. As in the previous case, the legend at the bottom right shows unscaled total RMSE errors. In this case, the ellipses clearly show not only the difference in the orientation of the EOFs, but also the underestimation of the variability present both in radar data, but especially in the case of model data.

## 4.3 Vertically integrated water vapour transport

The Sailor diagram for the vertically integrated water vapour transport can be seen in Figure 6 (right). In this case, the errors associated to the bias are smaller than the error associated to the covariance. However, since the errors in the anomalies are not

very large, the visibility of the diagram has been increased by plotting all of the ellipses on top of the observational point. This way, the errors in direction can be easily identified. For clarity, the ellipses are again scaled with a scale factor of 0.1. It can be seen that the estimation of the EOFs is closer for the case of the simulation with data assimilation, both in direction and, particularly, in the case of the amount of variance represented, since WRF N and ERAI slightly overestimate the water vapour fluxes.

A selection of the tabular results corresponding to the RMSE between observed and modelled vertically integrated water vapour transport are presented in Table 2. Different aspects of the main principal axes such as their semi-major and semi-minor axes, their relative rotation, the two-dimensional correlation coefficient and the combined RMSE can be readily analyzed for the water vapour transport vectors.

	Model	$\sigma_x$	$\sigma_y$	$R^2$	$ \bar{\mathbf{U}} - \bar{\mathbf{V}} $	RMSE	$\varepsilon$	$g_{11}$
1	OBS	183.45	107.83	2.00	0.00	0.00	0.81	1.00
2	WRF N	195.53	118.21	1.57	15.41	261.98	0.80	0.99
3	WRF D	173.47	100.19	1.94	5.65	257.53	0.82	1.00
4	ERA1	196.99	111.18	1.92	4.69	272.94	0.83	1.00

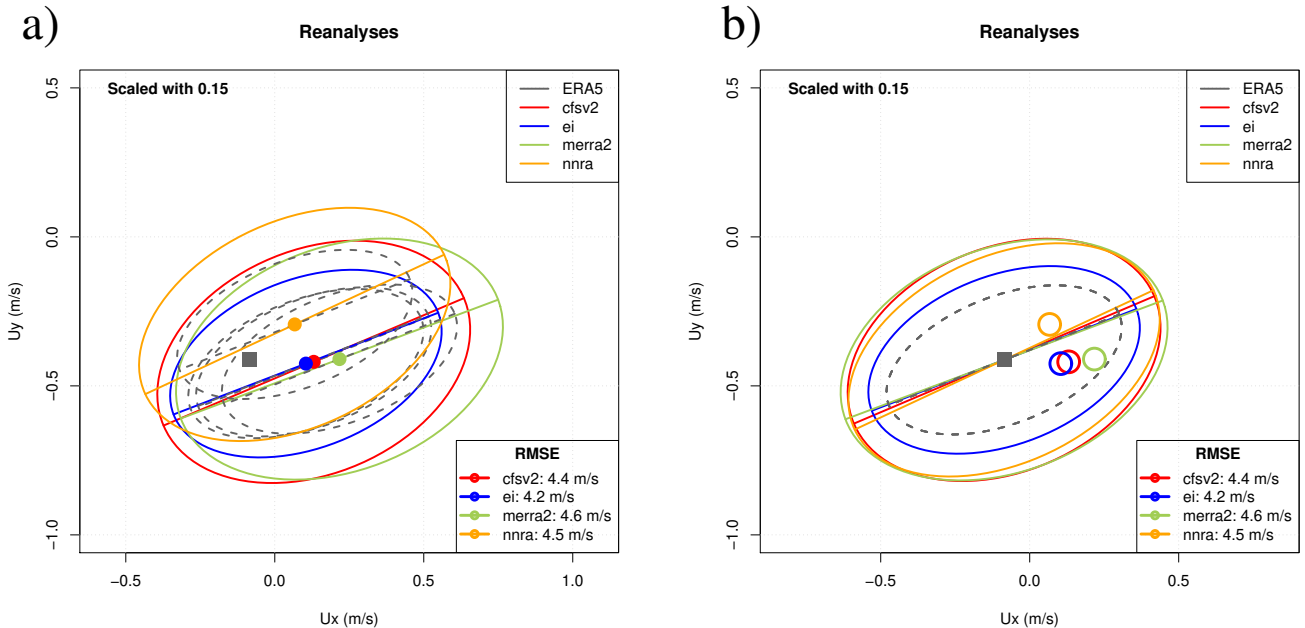
**Table 2.** Agreement of simulations by different models with observed vertically integrated water vapour transport from soundings.  $\sigma_x$  and  $\sigma_y$  represent the semi-major and semi-minor axes of the ellipses ( $\text{kg m}^{-1} \text{s}^{-1}$ ). The  $R^2$  column represents the value of the two-dimensional correlation coefficient following Crosby et al. (1993) ( $R^2 = 2$  for a perfect model, instead of 1 for the one-dimensional counterpart). The differences between the datasets described by the bias  $|\bar{\mathbf{U}} - \bar{\mathbf{V}}|$  ( $\text{kg m}^{-1} \text{s}^{-1}$ ) and total root mean squared error ( $\text{kg m}^{-1} \text{s}^{-1}$ ) are also shown. Finally, the eccentricity of the ellipses ( $\varepsilon$ ) and the congruence coefficient  $g_{11}$  of the EOF1 of every model with the one derived from observations are also shown. The congruence coefficient  $g_{11}$  represents the absolute value of the cosine of the relative rotation of model ellipses with respect to the observational one (Section 3.2).

440

#### 4.4 Spatial distribution of seasonally-averaged surface wind

As an example of the potential uses of the Sailor diagram, Figure 7 (left, panel a) represents in an uncentered version of the Sailor diagram the agreement of the January-averaged northern Hemisphere surface wind from different reanalyses using an scale factor of 0.15. On the other side, Figure 7 (right, panel b) shows the agreement of the January-averaged northern Hemisphere surface wind from different reanalyses using an scale factor of 0.15 in a centered version of the Sailor diagram. In these cases, we are assuming that ERA5 corresponds to the "perfect" dataset (observations). This is quite arbitrary, but we are performing this comparison for the sake of showing the ability of the Sailor diagram to evaluate spatial fields, as was done in the initial design of the Taylor diagram. It is clearly shown that the reanalyses produced by the ECMWF (ERA5 and ERAI) show the closest agreement both in terms of the smallest bias and better matching of the corresponding EOFs. The other reanalyses (CFSRv2, MERRA2 and NNRA) group along the same semi-major axis, but they overestimate the variability when compared

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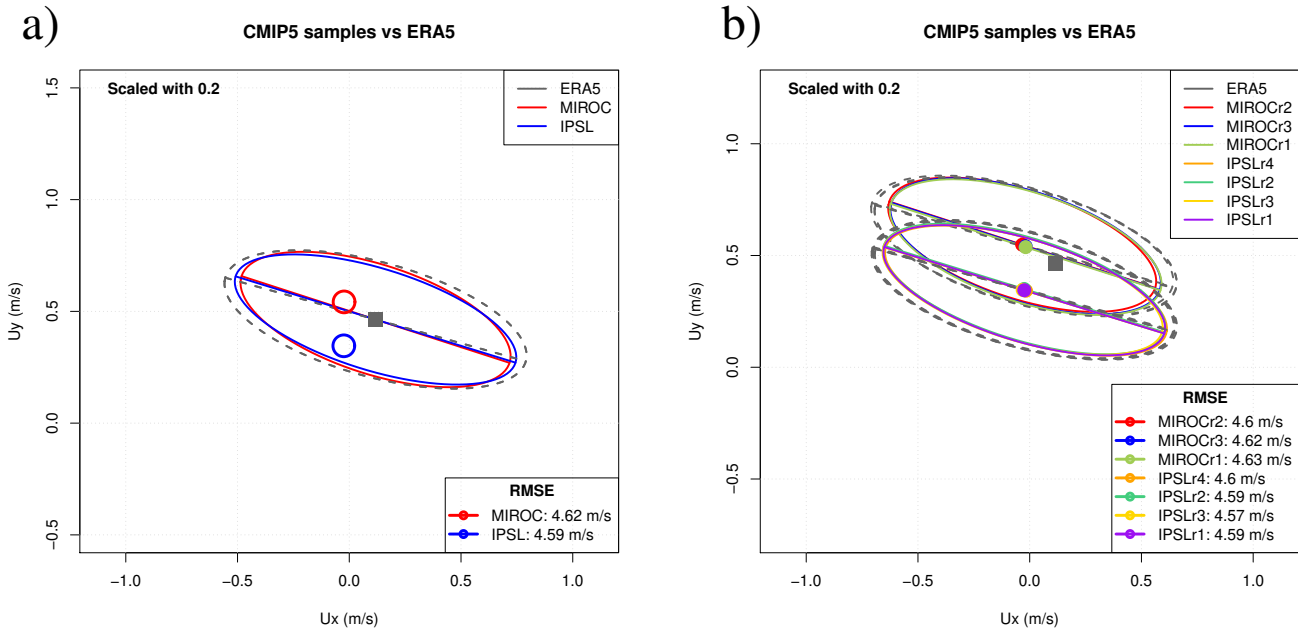
**Figure 7.** Sailor diagram representing the structure of errors in surface wind in January over the Northern Hemisphere for different reanalyses, uncentered version (left, scale factor 0.15) and centered version (right, scale factor 0.15).

with ERA5. In terms of the bias, too, it can be seen that the lowest bias is the one corresponding to ERAI. The easiest way to arrive to a numerically precise overall diagnostic is presented in the legend, where the aggregated RMSE error is shown.

#### 4.5 Application to multimodel ensembles

In this case, we propose to define the average of all the  $M$  ensemble members of every model as the vector  $\bar{\mathbf{V}}$  (Rouquier, 2016).  
 455 On the other side, the principal components and the associated variances and eigenvectors can be estimated from an extended data matrix  $\mathbf{V}_e$  (with dimensions  $NM \times 2$ ), which is built by joining all the realizations together in a single dataset. This means that the observational matrix  $\mathbf{U}$  must also be extended to an  $\mathbf{U}_e$  matrix sized  $NM \times 2$ . This can be done by repeating the observations  $M$  times to produce the  $\mathbf{U}_e$  dataset. This ensures that the algorithm will work because the covariance matrices involved will still be of full rank. However, it has to be considered that, in this case, the number of effective degrees of  
 460 freedom (Bretherton et al., 1999) in both  $\mathbf{U}_e$  and  $\mathbf{V}$  datasets will not be the same. This would also be a problem for different models  $\mathbf{V}_i$  and  $\mathbf{V}_j$ , if the number of members in their ensembles are not the same, such as in the CMIP set of runs, for instance.

As shown in Figure 8 (left), prepared using as scale factor 0.2, the Sailor diagram shows interesting features. The two models studied agree quite well in the simulation of the spatial variability of the field (the EOFs and major/minor axes in the ellipse represent the spatial variability of the field). Both models simulate an underestimation of zonal average winds when compared  
 465 with ERA5. MIROC tends to overestimate the mean meridional circulation and IPSL underestimates it.



**Figure 8.** Sailor diagram representing the agreement between the Southern Hemisphere wind field as simulated by two models from the CMIP5 repository with ERA5 data when the reference dataset is repeated in an extended matrix (left) or when the individual realizations of the ensemble are taken as independent datasets (right).

The second option for ensembles (same scale factor) is shown in Figure 8 (right). It consists in the use of every single realization of the ensemble as a single model. The proposed diagram leads to a neat comparison of the relative performance of the different members of the ensemble. This information might be interesting because of scientific reasons such as that the initialization of the members of the ensemble uses different techniques which need testing, for instance. In the case shown, the conclusion is quite clear: the averaged bias is relatively independent of the realization and the averages corresponding to every model tend to cluster at the same position. These biases are also very low. Besides that, the intra-ensemble variance of properties such as the spatial variability of the field is also quite low, so that the ellipses derived from different realizations in the same model almost overlap. Thus, in the analysis performed here, all the realizations of every model in the ensemble are very close to the reference dataset. The final decision on the use of one approach (Figure 8 left) or the other (Figure 8 right) for the analysis of ensemble integrations is open to the reader, since they can answer different questions, such as whether the intra-variability of the ensemble (in terms of bias and principal directions) is high or low.

## 5 Conclusions

A new diagram for the fast evaluation of the quality of models forecasting two-dimensional vector fields or time series has been presented. As Taylor (2001) properly stated in his seminal paper, a new diagram will only be accepted by users if it helps in the

480 fast and efficient intercomparison of model results against observational datasets. The authors of this paper developed the Sailor  
diagram in order to fill a gap that we detected when comparing two or more vector fields in our own work. In our previous  
papers when we worked with with vector fields (Ibarra-Berastegi et al., 2015, 2016) we solved this problem by duplicating  
the Taylor diagram, one for each component. The Sailor diagram merges the same information and allows a straightforward  
visual comparison while rigorously providing the numeric values of the RMSE. It provides additional diagnostics which allow  
485 a complete analysis of the errors in the simulated directions too.

The authors hope that the results presented so far demonstrate that the Sailor diagram achieves that goal. First, the diagram  
relies on the partition of the two-dimensional MSE in its bias and covariance parts. Those two terms are presented in the diagram  
separately. Thus, those two components of the error can be easily identified for the different datasets. Second, the covariance  
part is decomposed in terms of the corresponding principal components (empirical orthogonal functions). The structure of the  
490 covariance matrix of models and observations can also be effectively compared in the presented diagram, both in terms of the  
length of their semi-axes (fraction of variance) and in the relative rotation of every model against the reference dataset. This  
allows to easily identify in the diagram if the models under or overestimate the variance along any of the main axes and whether  
the main directions of variability in models and observations are relatively rotated or not. Thus, both two-dimensional bias and  
covariance can be visually identified from the diagram.

495 The diagram might provide inaccurate estimations of the relative rotations of the principal axes of the distribution of vector  
components in case both eigenvalues were degenerated and the eigenvectors were affected by substantial sampling uncertainty.  
In any case, a diagnostic produced by the package we provide, the eccentricity of the ellipses, Eq. (10) can be used by the user  
to detect this risk. In any case, even if the eigenvalues were degenerated, the final classification of models is performed in terms  
of the RMSE, which is a measure of error which is not affected by this degeneracy.

500 The diagram is easily customizable in order to increase the ability to identify features of the datasets being verified by means  
of the use of scale factors for the ellipses, by centering all of them in the reference dataset or on top of every model being used.  
Thus, researchers can design a diagram that best suits their needs.

The analysis of ensembles can also be performed by means of the diagram. As shown in subsection 4.5, the diagram can  
accommodate this case by using two different policies. In the first case, all the  $M$  members of the ensemble belonging to a  
505 single model can be mixed in a unique dataset, but this involves repeating the block of observations  $M$  times. This implies  
that the analysis of the results presented in the diagram in this case must consider the different number of effective degrees  
of freedom very carefully and further research should be performed to analyze the impact of this in the application of the  
Sailor diagram to model ensembles. However, in the second case, all the members of the ensemble can also be analyzed as  
independent realizations of the same dataset. This tends to clutter the diagram, but these results are not affected by problems  
510 related to the number of effective degrees of freedom in the different datasets used to build the diagram. However, every  
member of the ensemble can also be treated individually, so that the diagram would represent the intraensemble spread.

As a conclusion, we hope that the diagram presented here, together with an R implementation of it freely available in CRAN  
will ease the verification of vector fields derived from geoscientific models in the future.

*Code and data availability.* The code used to prepare the figures in this paper is described as examples in the manual of the R package `SailoR`, available from CRAN <https://cran.r-project.org/package=SailoR>. The data used to produce these figures are also distributed with the package.

*Author contributions.* JS conceived the idea, most of the mathematical analysis and wrote some parts of the linear algebra code and most of the paper. SCM collaborated in the analysis of the matricial structure of the error and wrote substantial parts of the code, particularly the graphical representation of data. GE collaborated in the preparation and testing of the linear algebra part and provided data for the tests. SJGR prepared the R package distributed with the paper and its documentation. SCM, GIB and AU provided data for the package, performed exhaustive checking of the implementation and helped in the analysis of results. All authors took active part in the writing of the paper.

*Competing interests.* The authors manifest they have no competing interests in the outcome of this paper-edition process.

*Disclaimer.* The code is made publicly available without any warranty.

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530 **References**

- Atlas, R., Hoffman, R. N., Ardizzone, J., Leidner, S. M., Jusem, J. C., Smith, D. K., and Gombos, D.: A cross-calibrated, multiplatform ocean surface wind velocity product for meteorological and oceanographic applications, *Bulletin of the American Meteorological Society*, 92, 157–174, <https://doi.org/10.1175/2010BAMS2946.1>, 2011.
- Boer, G. J. and Lambert, S. J.: Second order space-time climate difference statistics, *Clim. Dyn.*, 17, 213–218, <https://doi.org/10.1007/PL00013735>, 2001.
- 535 Breaker, L. C., Gemmill, W. H., and Crosby, D. S.: The application of a technique for vector correlation to problems in Meteorology and Oceanography, *J. Appl. Meteor.*, 33, 1354–1365, [https://doi.org/10.1175/1520-0450\(1994\)033<1354:TAOATF>2.0.CO;2](https://doi.org/10.1175/1520-0450(1994)033<1354:TAOATF>2.0.CO;2), 1994.
- Bretherton, C. S., Widmann, M., Dymnikov, V. P., Wallace, J. M., and Bladé, I.: The Effective Number of Spatial Degrees of Freedom of a Time-Varying Field, *Journal of Climate*, 12, 1990–2009, [https://doi.org/10.1175/1520-0442\(1999\)012<1990:TENOSD>2.0.CO;2](https://doi.org/10.1175/1520-0442(1999)012<1990:TENOSD>2.0.CO;2), 1999.
- 540 Chaudhuri, A. H., Ponte, R. M., Forget, G., and Heimbach, P.: A Comparison of Atmospheric Reanalysis Surface Products over the Ocean and Implications for Uncertainties in Air–Sea Boundary Forcing, *Journal of Climate*, 26, 153–170, <https://doi.org/10.1175/JCLI-D-12-00090.1>, 2013.
- Cheng, X., Nitsche, G., and Wallace, J. M.: Robustness of Low-Frequency Circulation Patterns Derived from EOF and Rotated EOF Analyses, *Journal of Climate*, 8, 1709–1713, [https://doi.org/10.1175/1520-0442\(1995\)008<1709:ROLFCP>2.0.CO;2](https://doi.org/10.1175/1520-0442(1995)008<1709:ROLFCP>2.0.CO;2), 1995.
- 545 Compagnucci, R. H. and Richman, M. B.: Can principal component analysis provide atmospheric circulation or teleconnection patterns?, *International Journal of Climatology*, 28, 703–726, <https://doi.org/10.1002/joc.1574>, 2008.
- Cosoli, S., Gačić, M., and Mazzoldi, A.: Variability of currents in front of the Venice Lagoon, Northern Adriatic Sea, *Ann. Geophys.*, 26, 731–746, <https://doi.org/10.5194/angeo-26-731-2008>, 2008.
- Cramer, E. M.: A generalization of vector correlation and its relation to canonical correlation, *Multivariate Behavioural Research*, 9, 347–351, [https://doi.org/10.1207/s15327906mbr0903\\_10](https://doi.org/10.1207/s15327906mbr0903_10), 1974.
- 550 Crosby, D. S., Beaker, L. C., and Gemill, W. H.: A proposed definition for vector correlation in Geophysics: Theory and Application, *Journal of Atmos. and Oceanic Technol.*, 10, 355–367, [https://doi.org/10.1175/1520-0426\(1993\)010<0355:APDFVC>2.0.CO;2](https://doi.org/10.1175/1520-0426(1993)010<0355:APDFVC>2.0.CO;2), 1993.
- Dee, D. P., Uppala, S. M., Simmons, A. J., Berrisford, P., Poli, P., Kobayashi, S., Andrae, U., Balmaseda, M. A., Balsamo, G., Bauer, P., Bechtold, P., Beljaars, A. C. M., van de Berg, L., Bidlot, J., Bormann, N., Delsol, C., Dragani, R., Fuentes, M., Geer, A. J., Haimberger, L., Healy, S. B., Hersbach, H., Hólm, E. V., Isaksen, L., Kållberg, P., Köhler, M., Matricardi, M., McNally, A. P., Monge-Sanz, B. M., Morcrette, J.-J., Park, B.-K., Peubey, C., de Rosnay, P., Tavolato, C., Thépaut, J.-N., and Vitart, F.: The ERA-Interim reanalysis: configuration and performance of the data assimilation system, *Quarterly Journal of the Royal Meteorological Society*, 137, 553–597, <https://doi.org/10.1002/qj.828>, 2011.
- Dörfler, W.: Diagrammatic thinking, in: *Activity and sign*, pp. 57–66, Springer, 2005.
- 560 Dufresne, J.-L., Foujols, M.-A., Denvil, S., Caubel, A., Marti, O., Aumont, O., Balkanski, Y., Bekki, S., Bellenger, H., Benschila, R., Bony, S., Bopp, L., Braconnot, P., Brockmann, P., Cadule, P., Cheruy, F., Codron, F., Cozic, A., Cugnet, D., de Noblet, N., Duvel, J.-P., Ethé, C., Fairhead, L., Fichet, T., Flavoni, S., Friedlingstein, P., Grandpeix, J.-Y., Guez, L., Guilyardi, E., Hauglustaine, D., Hourdin, F., Idelkadi, A., Ghattas, J., Jousaume, S., Kageyama, M., Krinner, G., Labetoulle, S., Lahellec, A., Lefebvre, M.-P., Lefevre, F., Levy, C., Li, Z. X., Lloyd, J., Lott, F., Madec, G., Mancip, M., Marchand, M., Masson, S., Meurdesoif, Y., Mignot, J., Musat, I., Parouty, S., Polcher, J., Rio, C., Schulz, M., Swingedouw, D., Szopa, S., Talandier, C., Terray, P., Viovy, N., and Vuichard, N.: Climate change projections using the
- 565



- IPSL-CM5 Earth System Model: from CMIP3 to CMIP5, *Climate Dynamics*, 40, 2123–2165, <https://doi.org/10.1007/s00382-012-1636-1>, 2013.
- Fernández, J., Montávez, J. P., Sáenz, J., González-Rouco, J. F., and Zorita, E.: Sensitivity of the MM5 mesoscale model to physical parameterizations for regional climate studies: Annual cycle, *J. Geophys. Res.*, 112, D04 101, <https://doi.org/10.1029/2005JD006649>, 2007.
- 570 Gelaro, R., McCarty, W., Suárez, M. J., Todling, R. d., Molod, A., Takacs, L., Randles, C. A., Darmenov, A., Bosilovich, M. G., Reichle, R., Wargan, K., Coy, L., Cullather, R., Draper, C., Akella, S., Bucha rd, V., Conaty, A., da Silva, A. M., Gu, W., Kim, G. K., Koster, R., Lucchesi, R., Merkova, D., Nielsen, J. o. E., Partyka, G., Pawson, S., Putman, W., Rienecker, M., Schubert, S. D., Sienkiewicz, M., and Zhao, B.: The Modern-Era Retrospective Analysis for Research and Applications, Version 2 (MERRA-2), *Journal of Climate*, 30, 5419–5454, <https://doi.org/10.1175/JCLI-D-16-0758.1>, 2017.
- 575 González-Rojí, S. J., Sáenz, J., Ibarra-Berastegi, G., and Díaz de Argandoña, J.: Moisture Balance Over the Iberian Peninsula According to a Regional Climate Model: The Impact of 3DVAR Data Assimilation, *Journal of Geophysical Research: Atmospheres*, 123, 708–729, <https://doi.org/10.1002/2017JD027511>, 2018.
- González-Rojí, S. J., Wilby, R. L., Sáenz, J., and Ibarra-Berastegi, G.: Harmonized evaluation of daily precipitation downscaled using SDSM and WRF+WRFDA models over the Iberian Peninsula, *Climate Dynamics*, 53, 1413–1433, <https://doi.org/10.1007/s00382-019-04673-9>,  
580 2019.
- Hawkins, E., Fæhn, T., and Fuglestedt, J.: The climate spiral demonstrates the power of sharing creative ideas, *Bull. of the Amer. Met. Soc.*, 100, 753–756, <https://doi.org/10.1175/BAMS-D-18-0228.1>, 2019.
- Hersbach, H., de Rosnay, P., Bell, B., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Alonso-Balmaseda, M., Balsamo, G., Bechtold, P., Berrisford, P., Bidlot, J.-R., de Boissésou, E., Bonavita, M., Browne, P., Buizza, R., Dahlgren, P., Dee, D., Dragani, R., Diamantakis, M.,  
585 Flemming, J., Forbes, R., Geer, A. J., Haiden, T., Hólm, E., Haimberger, L., Hogan, R., Horányi, A., Janiskova, M., Laloyaux, P., Lopez, P., Munoz-Sabater, J., Peubey, C., Radu, R., Richardson, D., Thépaut, J.-N., Vitart, F., Yang, X., Zsótér, E., and Zuo, H.: Operational global reanalysis: progress, future directions and synergies with NWP, Tech. Rep. 27, ECMWF, <https://doi.org/10.21957/tkic6g3wm>, 2018.
- Hoffman, R. N., Leidner, S. M., Henderson, J. M., Atlas, R., Ardizzone, J. V., and Bloom, S. C.: A Two-Dimensional Variational Analysis Method for NSCAT Ambiguity Removal: Methodology, Sensitivity, and Tuning, *Journal of Atmospheric and Oceanic Technology*, 20,  
590 585–605, [https://doi.org/10.1175/1520-0426\(2003\)20<585:ATDVAM>2.0.CO;2](https://doi.org/10.1175/1520-0426(2003)20<585:ATDVAM>2.0.CO;2), 2003.
- Hovmöller, E.: The trough-and-ridge diagram, *Tellus*, 1, 62–66, <https://doi.org/10.1111/j.2153-3490.1949.tb01260.x>, 1949.
- Ibarra-Berastegi, G., Saénz, J., Ezcurra, A., Elías, A., Diaz Argandoña, J., and Errasti, I.: Downscaling of surface moisture flux and precipitation in the Ebro Valley (Spain) using analogues and analogues followed by random forests and multiple linear regression, *Hydrology and Earth System Sciences*, 15, 1895–1907, <https://doi.org/10.5194/hess-15-1895-2011>, 2011.
- 595 Ibarra-Berastegi, G., Sáenz, J., Esnaola, G., Ezcurra, A., and Ulazia, A.: Short-term forecasting of the wave energy flux: Analogues, random forests, and physics-based models, *Ocean Engineering*, 104, 530–539, <https://doi.org/10.1016/j.oceaneng.2015.05.038>, 2015.
- Ibarra-Berastegi, G., Sáenz, J., Esnaola, G., Ezcurra, A., Ulazia, A., Rojo, N., and Gallastegui, G.: Wave Energy Forecasting at Three Coastal Buoys in the Bay of Biscay, *IEEE Journal of Oceanic Engineering*, 41, 923–929, <https://doi.org/10.1109/JOE.2016.2529400>, 2016.
- Jiménez, P. A., González-Rouco, J. F., García-Bustamante, E., Navarro, J., Montávez, J. P., de Arellano, J. V.-G., Dudhia, J., and Muñoz-Roldán, A.: Surface wind regionalization over complex terrain: Evaluation and analysis of a high-resolution WRF simulation, *J. Appl. Meteorol. and Climatol.*, 49, 268–287, <https://doi.org/10.1175/2009JAMC2175.1>, 2010.
- 600 Jupp, P. E. and Mardia, K. V.: A general correlation coefficient for directional data and related regression problems, *Biometrika*, 67, 163–173, <https://doi.org/10.2307/2335329>, 1980.

- Kalnay, E., Kanamitsu, M., Kistler, R., Collins, W., Deaven, D., Gandin, L., Iredell, M., Saha, S., White, G., Woollen, J., Zhu, Y.,  
605 Leetmaa, A., Reynolds, R., Chelliah, M., Ebisuzaki, W., Higgins, W., Janowiak, J., Mo, K. C., Ropelewski, C., Wang, J., Jenne, R.,  
and Joseph, D.: The NCEP/NCAR 40-year reanalysis project, *Bull. Amer. Meteorol. Soc.*, 77, 437–470, [https://doi.org/10.1175/1520-0477\(1996\)077<0437:TNYRP>2.0.CO;2](https://doi.org/10.1175/1520-0477(1996)077<0437:TNYRP>2.0.CO;2), 1996.
- Kundu, P. K.: Ekman veering observed near the ocean bottom, *J. Phys. Ocean.*, 6, 238–242, [https://doi.org/10.1175/1520-0485\(1976\)006<0238:EVONTO>2.0.CO;2](https://doi.org/10.1175/1520-0485(1976)006<0238:EVONTO>2.0.CO;2), 1976.
- 610 Lee, T., Waliser, D. E., Li, J.-L. F., Landerer, F. W., and Gierach, M. M.: Evaluation of CMIP3 and CMIP5 wind stress climatology using satellite measurements and atmospheric reanalysis products, *J. Climate*, 26, 5810–5826, <https://doi.org/10.1175/JCLI-D-12-00591.1>, 2013.
- Lellouche, J. M., Greiner, E., Galloudec, O. L., Garric, G., Regnier, C., Drevillon, M., Benkiran, M., Testut, C.-E., Bourdalle-Badie, R., Gasparin, F., Hernandez, O., Levier, B., Drillet, Y., Remy, E., and Traon, P.-Y. L.: Recent updates to the Copernicus Marine Service global  
615 ocean monitoring and forecasting real-time 1/12° high-resolution system, *Ocean Sci.*, 14, 1093–1126, <https://doi.org/10.5194/os-14-1093-2018>, 2018.
- Lorente, P., Piedracoba, S., Soto-Navarro, J., and Alvarez-Fanjul, E.: Evaluating the surface circulation in the Ebro delta (northeastern Spain) with quality-controlled high-frequency radar measurements, *Ocean. Sci.*, 11, 921–935, <https://doi.org/10.5194/os-11-921-2015>, 2015.
- Madec, G. and the NEMO team: NEMO ocean engine, Tech. rep., Institut Pierre-Simon Laplace (IPSL), France, 2008.
- 620 Martin, T. H. D. T. G. M., Bellouin, N., Collins, W. J., Culverwell, I. D., Halloran, P. R., Hardiman, S. C., Hinton, T. J., Jones, C. D., McDonald, R. E., McLaren, A. J., O'Connor, F. M., Roberts, M. J., Rodriguez, J. M., Woodward, S., Best, M. J., Brooks, M. E., Brown, A. R., Butchart, N., Dearden, C., Derbyshire, S. H., Dharssi, I., Doutriaux-Boucher, M., Edwards, J. M., Falloon, P. D., Gedney, N., Gray, L. J., Hewitt, H. T., Hobson, M., Huddleston, M. R., Hughes, J., Ineson, S., Ingram, W. J., James, P. M., Johns, T. C., Johnson, C. E., Jones, A., Jones, C. P., Joshi, M. M., Keen, A. B., Liddicoat, S., Lock, A. P., Maidens, A. V., Manners, J. C., Milton, S. F., Rae, J. G. L.,  
625 Ridley, J. K., Sellar, A., Senior, C. A., Totterdell, I. J., Verhoef, A., Vidale, P. L., and Wiltshire, A.: The HadGEM2 family of Met Office Unified Model climate configurations, *Geoscientific Model Development*, 4, 723–757, <https://doi.org/10.5194/gmd-4-723-2011>, 2011.
- McGill, R., Tukey, J. W., and Larsen, W. A.: Variations of Box Plots, *The American Statistician*, 32, 12–16, <https://doi.org/10.2307/2683468>, 1978.
- North, G., Bell, T., Cahalan, R., and Moeng, F.: Sampling Errors in the Estimation of Empirical Orthogonal Functions, *Monthly Weather*  
630 *Review*, 110, 699–706, [https://doi.org/10.1175/1520-0493\(1982\)110<0699:SEITEO>2.0.CO;2](https://doi.org/10.1175/1520-0493(1982)110<0699:SEITEO>2.0.CO;2), 1982.
- P.P.E.: Puertos del Estado: Oceanography: Forecast, real time and climate, Spanish Government: Madrid. Updated 2015-10-11. <http://www.puertos.es/en-us/oceanografia/Pages/portus.aspx>, 2015.
- Rabanal, A., Ulazia, A., Ibarra-Berastegi, G., Sáenz, J., and Elosegui, U.: MIDAS: A Benchmarking Multi-Criteria Method for the Identification of Defective Anemometers in Wind Farms, *Energies*, 12, 28, 2019.
- 635 Robert, P., Cléroux, R., and Ranger, N.: Some results on vector correlation, *Computational Statistics & Data Analysis*, 3, 25–32, [https://doi.org/10.1016/0167-9473\(85\)90055-6](https://doi.org/10.1016/0167-9473(85)90055-6), 1985.
- Roebber, P. J.: Visualizing multiple measures of Forecast Quality, *Wea. and Forecast.*, 24, 601–608, <https://doi.org/10.1175/2008WAF2222159.1>, 2009.
- Rougier, J.: Ensemble averaging and mean squared error, *Journal of Climate*, 29, 8865–8870, <https://doi.org/10.1175/JCLI-D-16-0012.1>,  
640 2016.

- Rubio, A., Reverdin, G., Fontán, A., González, M., and Mader, J.: Mapping near-inertial variability in the SE Bay of Biscay from HF radar data and two offshore moored buoys, *Geophysical Research Letters*, 38, L19 607, <https://doi.org/10.1029/2011GL048783>, 2011.
- Rubio, A., Fontán, A., Lazure, P., González, M., Valencia, V., Ferrer, L., Mader, J., and Hernández, C.: Seasonal to tidal variability of currents and temperature in waters of the continental slope, southeastern Bay of Biscay, *Journal of Marine Systems*, 109-110, S121 –  
645 S133, <https://doi.org/10.1016/j.jmarsys.2012.01.004>, 2013.
- Sáenz, J., González-Rojí, S. J., Carreno-Madinabeitia, S., and Ibarra-Berastegi, G.: Analysis of atmospheric thermodynamics using the R package aiRthermo, *Computers & Geosciences*, 122, 113–119, <https://doi.org/10.1016/j.cageo.2018.10.007>, 2019.
- Saha, S., Moorthi, S., Wu, X., Wang, J., Nadiga, S., Tripp, P., Behringer, D., Hou, Y.-T., Chuang, H.-y., Iredell, M., Ek, M., Meng, J., Yang, R., Mendez, M. P., van den Dool, H., Zhang, Q., Wang, W., Chen, M., and Becker, E.: The NCEP Climate Forecast System Version 2,  
650 *Journal of Climate*, 27, 2185–2208, <https://doi.org/10.1175/JCLI-D-12-00823.1>, 2014.
- Solabarrieta, L., Rubio, A., Castanedo, S., Medina, R., Charria, G., and Hernández, C.: Surface water circulation patterns in the southeastern Bay of Biscay: New evidences from HF radar data, *Continental Shelf Research*, 74, 60–76, <https://doi.org/10.1016/j.csr.2013.11.022>, 2014.
- Stephens, M. A.: Vector correlation, *Biometrika*, 66, 41–48, <https://doi.org/10.2307/2335240>, 1979.
- 655 Taylor, K. E.: Summarizing multiple aspects of model performance in a single diagram, *J. Geophys. Res.*, D7, 7183–7192, <https://doi.org/10.1029/2000JD900719>, 2001.
- Ulazia, A.: Multiple roles for analogies in the genesis of fluid mechanics: How analogies can cooperate with other heuristic strategies, *Foundations of Science*, 21, 543–565, 2016.
- Ulazia, A., Sáenz, J., and Ibarra-Berastegi, G.: Sensitivity to the use of 3DVAR data assimilation in a mesoscale model for  
660 estimating offshore wind energy potential. A case study of the Iberian northern coastline, *Appl. Energy*, 180, 617–627, <https://doi.org/10.1016/j.apenergy.2016.08.033>, 2016.
- Ulazia, A., Sáenz, J., Ibarra-Berastegi, G., González-Rojí, S. J., and Carreno-Madinabeitia, S.: Using 3DVAR data assimilation to measure offshore wind energy potential at different turbine heights in the West Mediterranean, *Applied Energy*, 208, 1232–1245, <https://doi.org/10.1016/j.apenergy.2017.09.030>, 2017.
- 665 Watanabe, M., Suzuki, T., O’ishi, R., Komuro, Y., Watanabe, S., Emori, S., Takemura, T., Chikira, M., Ogura, T., Sekiguchi, M., Takata, K., Yamazaki, D., Yokohata, T., Nozawa, T., Hasumi, H., Tatebe, H., and Kimoto, M.: Improved Climate Simulation by MIROC5: Mean States, Variability, and Climate Sensitivity, *Journal of Climate*, 23, 6312–6335, <https://doi.org/10.1175/2010JCLI3679.1>, 2010.
- Wilks, D. S.: *Statistical Methods in the Atmospheric Sciences*, Academic Press, Burlington, MA, 2 edn., 2006.
- Xu, Z., Hou, Z., Han, Y., and Guo, W.: A diagram for evaluating multiple aspects of model performance in simulating vector fields, *Geosci. Mod. Dev.*, 9, 4365–4380, <https://doi.org/10.5194/gmd-9-4365-2016>, 2016.  
670