

1 **Optimizing a dynamic fossil fuel CO₂ emission model with**
2 **CTDAS (v1.0) for an urban area using atmospheric**
3 **observations of CO₂, CO, NO_x, and SO₂**

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11 **Abstract.** We present a modelling framework for fossil fuel CO₂ emissions in an urban environment, which allows
12 constraints from emission inventories to be combined with atmospheric observations of CO₂ and its co-emitted
13 species CO, NO_x, and SO₂. Rather than a static assignment of average emission rates to each unit-area of the urban
14 domain, the fossil fuel emissions we use are dynamic: they vary in time and space in relation to data that describe
15 or approximate the activity within a sector, such as traffic density, power demand, 2m temperature (as proxy for
16 heating demand), and sunlight and wind speed (as proxies for renewable energy supply). Through inverse
17 modelling, we optimize the relationships between these activity data and the resulting emissions of all species
18 within the dynamic fossil fuel emission model, based on atmospheric mole fraction observations. The advantage
19 of this novel approach is that the optimized parameters (emission factors and emission ratios, N=44) in this
20 dynamic emission model (a) vary much less over space and time, (b) allow a physical interpretation of mean and
21 uncertainty, and (c) have better defined uncertainties and covariance structure. This makes them more suited to
22 extrapolate, optimize, and interpret than the gridded emissions themselves. The merits of this approach are
23 investigated using a pseudo-observation-based ensemble Kalman filter inversion setup for the Dutch Rijnmond
24 area at 1x1 km resolution.

25 We find that the fossil fuel emission model approximates the gridded emissions well (annual mean differences <
26 2 %, hourly temporal $r^2 = 0.21-0.95$), while reported errors on the underlying parameters allow a full covariance
27 structure to be created readily. Propagating this error structure into atmospheric mole fractions shows a strong
28 dominance of a few large sectors and a few dominant uncertainties, most notably the emission ratios of the various
29 gases considered. If these are either sufficiently well-known a-priori, or well-constrained from a dense observation
30 network, we find that including observations of co-emitted species improves our ability to estimate emissions per
31 sector relative to using CO₂ mole fractions only. Nevertheless, the total CO₂ emissions can be well-constrained
32 with CO₂ as only tracer in the inversion. Because some sectors are sampled only sparsely over a day, we find that
33 propagating solutions from day-to-day leads to largest uncertainty reduction and smallest CO₂ residuals over the
34 14 consecutive days considered. Although we can technically estimate the temporal distribution of some emission
35 categories like shipping separate from their total magnitude, the controlling parameters are difficult to distinguish.
36 Overall, we conclude that our new system looks promising for application in verification studies, provided that
37 reliable urban atmospheric transport fields and reasonable a-priori emission ratios for CO₂ and its co-emitted
38 species can be produced.

39 **1 Introduction**

40 Within the 2015 Paris Agreement, 195 nations agreed with a climate action plan in which each nation sets its own
41 targets for carbon emission reductions and reports all efforts regularly to the UNFCCC (UNFCCC, 2015). An
42 important role in reaching emission reduction targets is laid out for cities, which emit a large portion of the global
43 fossil fuel CO₂ emissions (about 70 % according to the International Energy Agency (IEA, 2008)). The Paris
44 Agreement also states that parties should strengthen their cooperation, also with respect to the sharing of
45 information and good practices. Within this context it becomes increasingly important to map fossil fuel emissions
46 and to quantify emission trends, both at the country- and city-level.

47 Most country-level greenhouse gas emission estimates reported to the UNFCCC are currently based on annual
48 fuel consumption data (bottom-up method), and are often spatiotemporally disaggregated using activity data and
49 proxies to create spatially explicit emission inventories (Kuenen et al., 2014; Hutchins et al., 2017). Although the
50 annual national estimates are reasonably accurate (estimated uncertainty for developed countries is less than 8 %
51 for CO₂ (Monni et al., 2004; Fauser et al., 2011; Andres et al., 2014)), their uncertainty increases rapidly when
52 disaggregating them towards finer spatiotemporal resolutions (Ciais et al., 2010; Nassar et al., 2013; Andres et al.,
53 2016). A method to improve emission estimates is using transport models in combination with independent
54 observations of atmospheric mole fractions (Palmer et al., 2018), called data assimilation (DA) or inverse
55 modelling (a top-down method). Recently, efforts have been made to apply DA techniques to the urban
56 environment (McKain et al., 2012; Brioude et al., 2013; Lauvaux et al., 2013; Bréon et al., 2015; Boon et al., 2016;
57 Lauvaux et al., 2016; Staufner et al., 2016; Brophy et al., 2018), but several challenges and unexploited opportunities
58 remain.

59 First, urban DA studies have tried to constrain the total fossil fuel flux to validate bottom-up CO₂ inventories, often
60 without considering the underlying emission process that caused the mismatch between observed and modelled
61 concentrations. As one of very few exceptions, Lauvaux et al. (2013) used the CO:CO₂ concentration ratio to
62 conclude that the emission reduction in Davos during the World Economic Forum 2012 was likely related to
63 reduced traffic emissions, but without a quantification. However, emission reduction policies usually target
64 specific source sectors. Therefore, an increase in fossil fuel emissions from one source sector can cause the total
65 CO₂ emissions to appear stable, although a policy targeting another source sector can be effective in itself. To
66 monitor the effect of each measure independently it becomes essential to attribute changes in the total CO₂
67 emissions to these policies and thus to specific source sectors. It is, therefore, not sufficient to constrain the total
68 CO₂ flux, but we need to differentiate the total CO₂ signal into signals from the different source sectors. One way
69 to accomplish this is by using additional measurements of co-emitted species and isotopes. Such measurements
70 have previously been used in modelling studies to differentiate between biogenic and anthropogenic emissions or
71 between fuel types (Djuricin et al., 2010; LaFranchi et al., 2013; Lopez et al., 2013; Turnbull et al., 2015; Fischer
72 et al., 2017; Super et al., 2017b; Brophy et al., 2018; Graven et al., 2018), but also to separate between different
73 fossil fuel sources (Lindenmaier et al., 2014; Super et al., 2017a; Nathan et al., 2018).

74 Second, for urban DA the fine scales (less than 1km and less than 1 hour) need to be resolved, therefore putting a
75 higher demand on the atmospheric transport models. For example, Boon et al. (2016) mentioned that sources with
76 a small spatial extent (point sources) are not correctly represented on a 2x2 km² grid, while these sources have a
77 significant impact on the locally observed mole fractions. Concurrently, we have previously shown that a plume
78 model improves the representation of sources with a limited spatial extent. Moreover, we found that the description

79 of short-term variations in the wind direction by the Eulerian WRF model in the vicinity of an urban area is poor
80 (Super et al., 2017a).

81 Third, the prior emissions also need to have a higher resolution for urban-scale studies to resolve the dominant
82 spatiotemporal variations. Previous studies have often used high-resolution emission maps developed specifically
83 for that region, using local data as much as possible (Zhou and Gurney, 2011; Bréon et al., 2015; Boon et al., 2016;
84 Lauvaux et al., 2016; Rao et al., 2017; Gurney et al., 2019). Yet such emission maps are only available for a few
85 data-rich regions. For other regions, continental or global emission maps (such as MACC or EDGAR) can be used
86 if downscaling is applied to reach the high resolution required for urban-scale inversions. For example, the
87 temporal downscaling can be done using typical daily, weekly and monthly profiles for each source sector (Denier
88 van der Gon et al., 2011), which are based on activity data (e.g. traffic counts) averaged over several years and/or
89 a large region. Spatial downscaling often involves proxies like population density. This spatiotemporal
90 downscaling introduces a large additional uncertainty due to uncertainties in the proxies. For example, Hogue et
91 al. (2016) have found an uncertainty of 150 % in the $1 \times 1^\circ$ fossil fuel CO₂ emissions for the US, whereas Ciais et
92 al. (2010) estimated the uncertainty of regional European emissions at 100 km resolution to be about 50 %.
93 Quantification of the uncertainty at an even higher resolution for urban applications has so far been limited (Andres
94 et al., 2016; Super et al., 2020), also for most local inventories, while a correct definition of the prior error
95 covariance matrix for an inversion is important to get reliable output (Chevallier et al., 2006; Boschetti et al.,
96 2018). This currently complicates the application of DA studies to urban areas.

97 Here, we describe the development of an urban-scale DA framework (based on the CarbonTracker Data
98 Assimilation Shell (CTDAS) (Van der Laan-Luijkx et al., 2017)) which uses a dynamic fossil fuel emission model
99 as a prior and optimizes the parameters of this model. The fossil fuel emission model uses a wide range of
100 (statistical) data to calculate CO₂ emissions per source sector at high spatiotemporal resolution (1×1 km² and
101 hourly). The emission model is more dynamic than a regular emission inventory in the sense that its formulation
102 allows emissions to change as a function of rapidly varying conditions in the emission landscape, such as the
103 outside temperature, the traffic density, or availability of wind and solar radiation for sustainable power generation.
104 Using such information enables the calculation of dynamic emissions without a two-year lag, as opposed to the
105 construction of a static emission map based on statistical downscaling. Moreover, the emission model can supply
106 spatiotemporal emission uncertainties and error correlations between source sectors, based on the estimated
107 uncertainty of its model parameters. Since many of these parameters are also used in bottom-up accounting of
108 emissions, their uncertainty is often better established than the uncertainty in the total emissions themselves.
109 Finally, we use the emission model to calculate emissions of other co-emitted species (CO, NO_x and SO₂) from
110 the CO₂ emissions using source sector specific emission ratios. These co-emitted species are included in the DA
111 system to facilitate source attribution, which is possible due to the distinct emission ratios of different source
112 sectors. The overall aim of this study is to explore how our fossil fuel emission model and additional tracers can
113 be used to overcome the known limitations in anthropogenic CO₂ inverse modelling described above. The research
114 questions are:

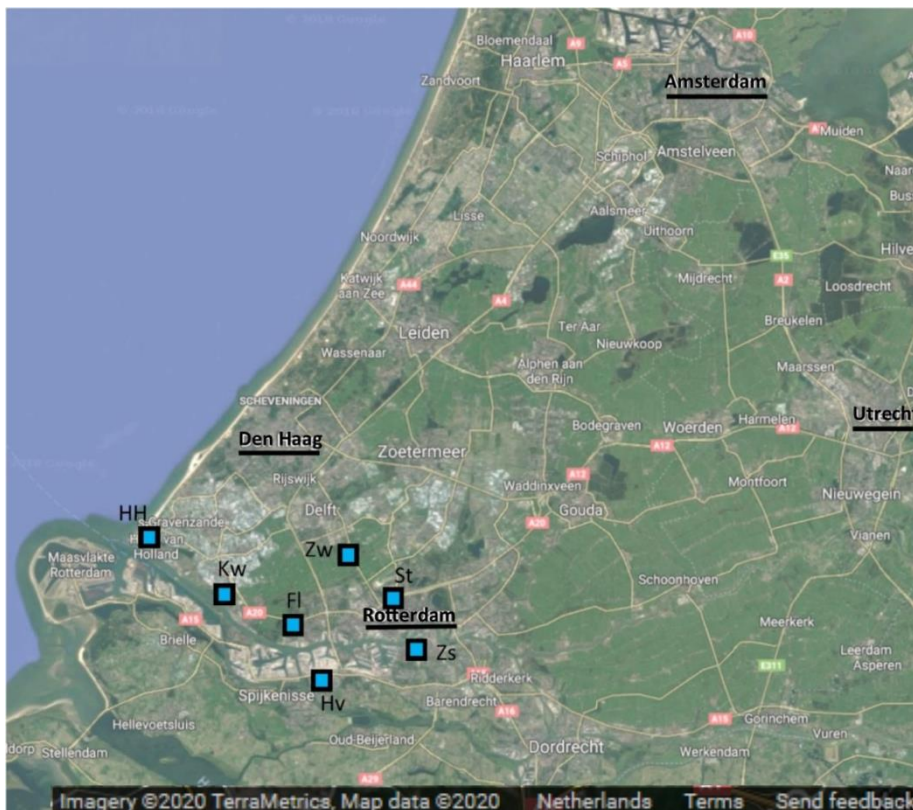
- 115 1. Can our dynamic fossil fuel emission model represent the spatiotemporal structure of a high-resolution
116 emission inventory, and what does it add to that on small scales?
- 117 2. Is the addition of co-emitted species beneficial for the attribution of CO₂ signals to specific source sectors,
118 and which observations help most in that effort?

119 3. Does the prior error covariance structure that we build with the dynamic emissions model help the
120 optimization, and what can we learn from the posterior error covariance estimate?

121 In the inverse modelling part of this study we use observing system simulation experiments (OSSEs, experiments
122 using pseudo-observations), applied to the urban-industrial complex of Rotterdam (Netherlands). This choice
123 allows us to test our new approach, while with real observations the errors in non-fossil and background fluxes,
124 model structure, and model transport will likely dominate the results (Tolk et al., 2008; Super et al., 2017a; He et
125 al., 2018) and reduce the ability to evaluate the methodology. First, we give an overview of the dynamic fossil fuel
126 emission model and demonstrate its applicability to the domain, followed by an introduction to the DA system
127 components and the model settings. Then we discuss the different experiments in which we start with the
128 comparison of different network configurations, one with only CO₂ and one including co-emitted species to
129 examine the ability to attribute CO₂ emissions to specific source sectors, and different state vectors. Another
130 experiment is used to examine the importance of propagating posterior parameters values and covariances. Finally,
131 we address the effect of cross-correlations.

132 2 Methods

133 2.1 The dynamic emission model



134 Figure 1. Map of the domain covered (Randstad area, the Netherlands) within this study, including major cities
135 Amsterdam, Rotterdam, The Hague, and Utrecht (underlined). The squares show the locations of the measurement
136 sites within the urban network configuration. The area of this domain is approximately 77x88 km. Source: ©Google
137 Maps.
138

139 Although generally applicable, the dynamic emission model is initially developed for the Netherlands and focused
140 on Rotterdam (Fig. 1). This is one of the major cities in the Netherlands (about 625,000 inhabitants) with the
141 largest sea port of Europe to its west. It is located in a larger urbanized area (Randstad, about 7 million inhabitants)

142 with The Hague, Amsterdam and Utrecht being other major cities. A large area to the southwest of The Hague is
 143 used for glasshouse horticulture producing vegetables and flowers. The Rotterdam area is characterized by a
 144 complex mixture of residential and industrial activities and therefore we distinguish five source sectors and a total
 145 of ten sub-sectors to construct its emissions (see Table 1). Note that, for simplicity, only the largest source sectors
 146 are included, which are responsible for >95 % of the CO₂ emissions in the area. Moreover, a further subdivision
 147 of industrial activities is neglected because of two reasons: 1) the lack of data for each subsector and 2) the inability
 148 to separate between those activities with atmospheric measurements because of their spatial clustering. The main
 149 goal is to get a reasonable first estimate of the emission landscape using readily available data.

150 **Table 1. Overview of source sectors and subsectors distinguished in the dynamic emission model, including their short**
 151 **name used in the figures, whether they are represented as point or area sources, and their approximate contribution to**
 152 **the total CO₂ emission in Rotterdam (Netherlands PRTR, 2014). Crosses indicate which emission factors (EF), and**
 153 **tracer ratios of CO, NO_x or SO₂ (R_{CO}, R_{NO_x}, R_{SO₂}) are part of the state vector and circles indicate whether they are**
 154 **also part of the short state vector (see Sect. 2.3).**

Source sector	Subsector	Short name	Source type	Contribution	EF	R _{CO}	R _{NO_x}	R _{SO₂}
Power plants	Gas-fired power plants	1A	Point	37 %	XO	X	X	
	Coal-fired power plants	1B			XO	X	X	X
Non-industrial combustion	Households	2A	Area	15 %	XO	XO	X	X
	Glasshouses	2B			XO	X	X	
Industry		3	Point	39 %	XO	XO	XO	XO
Road traffic	Cars	7A	Area	6 %	XO	XO	XO	
	Heavy duty vehicles	7B			XO	XO	XO	
Shipping	Ocean shipping	8A	Area	3 %	XO	X	XO	XO
	Inland shipping	8B			XO	X	XO	XO
	Recreational shipping	8C						

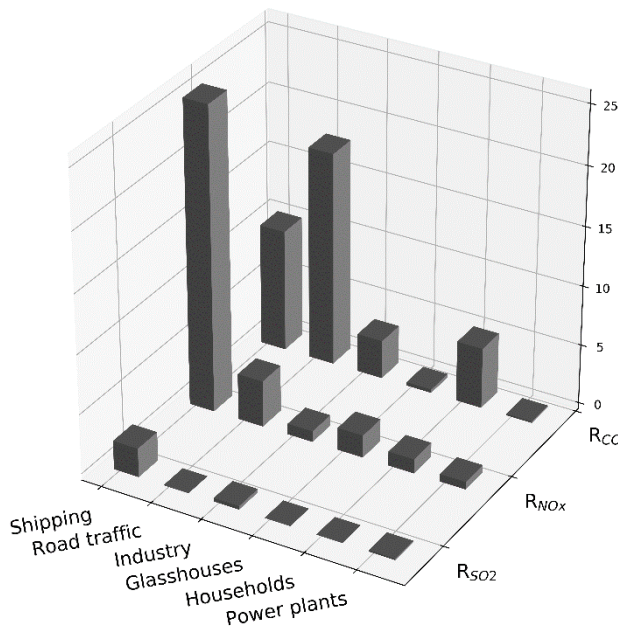
155 The ultimate goal is to develop an emission model that assimilates high-resolution activity data, such as traffic
 156 data, in near real-time. A truly dynamic emission model is not dependent on pre-calculated annual emissions and
 157 spatial or temporal downscaling, but directly uses activity data to calculate emissions for that specific moment.
 158 However, the development of a dynamic emission model still requires a lot of research. Here, we make a first step
 159 by mainly illustrating the potential of using high-resolution activity data to better represent temporal variations.
 160 In this work, the emissions are calculated in four steps. First, the annual, national emission is calculated per sector
 161 using reported annual activity data and CO₂ emission factors. Second, we apply temporal disaggregation to hourly
 162 emissions using time profiles based on a combination of default temporal profiles, and environmental conditions.
 163 Third, we downscale the national totals to 1x1 km² resolution using statistical data, such as population density.
 164 Finally, our approach also allows uncertainties to be described in detail based on parameters in Eq. (2).

166 2.1.1 Step 1: Sectorial total emission calculations

167 Total annual emissions (F_X in kg yr^{-1}) per sector and species ($X=\text{CO}_2, \text{CO}, \text{NO}_x, \text{SO}_2$) are calculated as a function
 168 of the economic activity and an emission factor (adapted from Raupach et al. (2007)):

$$169 \quad F_X = A \left(\frac{E}{A} \right) \left(\frac{F_{\text{CO}_2}}{E} \right) R_X \quad (1)$$

170 where A is the amount of activity (which often has the unit € when GDP or industrial productivity is used as proxy)
 171 and E is the primary energy consumption (petajoule (PJ)). R_X is the emission ratio needed to calculate emissions
 172 of co-emitted species X from the CO_2 emissions (kg kg^{-1}), which is specific for each economic sector (R_{CO_2} is
 173 always 1, others are illustrated in Fig. 2). In this equation the term F_{CO_2}/E is the CO_2 emission factor (EF), i.e. the
 174 amount of CO_2 emitted per amount of energy consumed. The term E/A can be seen as a measure of energy
 175 efficiency, in which technological development plays an important role (Nakicenovic et al., 2000).



176 **Figure 2. Emission ratios of $\text{CO}:\text{CO}_2$ (R_{CO}), $\text{NO}_x:\text{CO}_2$ (R_{NO_x}) and $\text{SO}_2:\text{CO}_2$ (R_{SO_2}) for specific source sectors based on**
 177 **the Dutch Pollution Release and Transfer Register (Netherlands PRTR, 2014). Units are in ppb ppm^{-1} . A value of 10 on**
 178 **the y-axis thus implies that for each 1000 moles of CO_2 , 10 moles of the auxiliary tracer is emitted.**
 179

180 The information needed in Eq. (1) comes from various inventories and national information sources. For example,
 181 changes in annual activity can be approximated based on national statistics such as the GDP (Gross Domestic
 182 Product), which can be a proxy for industrial activity. Or A can be based on environmental data such as the annual
 183 degree day sum based on the outside temperature, as proxy for the need for household heating in a particular year.
 184 These proxies for A are known globally, which is why we use Eq. (1) instead of directly using energy consumption
 185 data (E). For local studies more specific activity data could be used, for example vehicle kilometres driven as a
 186 predictor for road traffic emissions. The second term in Eq. (1) (E/A , the energy efficiency) can be estimated from
 187 activity data and energy consumption statistics, such as available from the International Energy Agency or data
 188 from national statistics agencies. Even if E is not directly available for a country, an estimate can be made based
 189 on a country with a comparable level of development and climatology. Note that this term can show a large trend
 190 in case of technological development. The last terms in Eq. (1) (F/E and R_x , the emission factors) are the most
 191 uncertain ones, because the emission factor is dependent on the fuel mix and the energy efficiency, which itself
 192 can vary with environmental conditions (e.g. a cold engine on a winter day burns less efficiently). It can therefore
 193 differ significantly between countries. Emission factor values that are generally valid can be gathered from the

194 Intergovernmental Panel on Climate Change (IPCC) or the European Environmental Agency (EEA), while
195 country-specific values are typically less easily accessible. For our study area, we have access to both EEA data,
196 as well as to Netherlands-specific numbers and even to Rijnmond-specific values (Netherlands PRTR, 2014) . See
197 Appendix A for a full overview of the data used.

198 **2.1.2 Step 2: Temporal profiles and parameterizing activity**

199 The second step is to disaggregate the annual emissions to hourly emissions by calculating time profiles, such that
200 Eq. (1) becomes "dynamic":

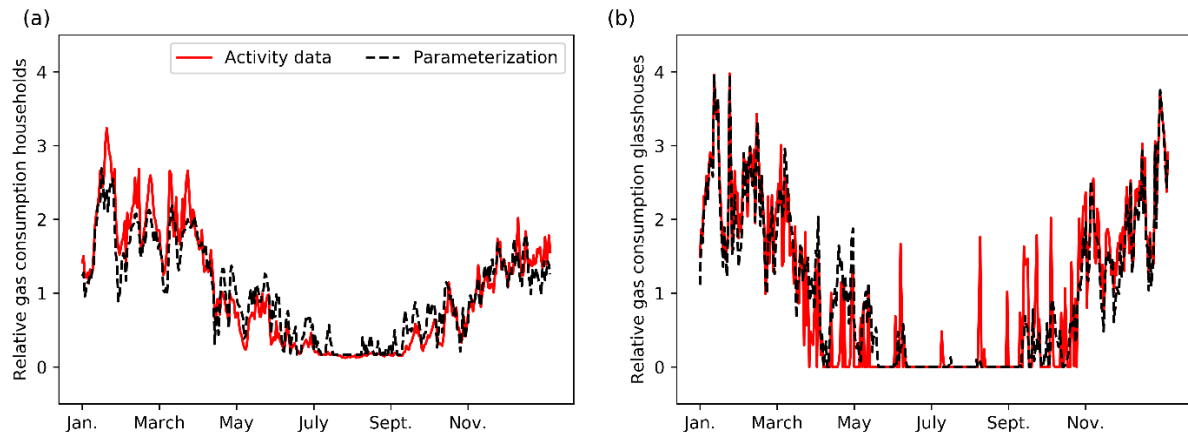
$$201 \quad F_{X,t} = A \left(\frac{E}{A} \right) \left(\frac{F_{CO_2,t}}{E} \right) R_X T_t \quad (2)$$

202 where T_t is the hourly time factor and F is in kg h⁻¹ (hence the subscript t). Averaged over a year the value of T_t is
203 1.0, so that it only alters the temporal evolution and not the total emissions. Energy use is often specifically linked
204 to an activity (A in Eq. (1) and Eq. (2)) on which temporal information is more readily available than on the
205 resulting emissions. Therefore, T_t can be calculated in two ways: 1) by directly using temporally explicit activity
206 data or 2) by parameterizing temporal variations from environmental and/or economic conditions. When activity
207 data is available the first option is preferable. However, in data-sparse regions the second option might be
208 necessary to implement, which is still an improvement compared to long-term average profiles as commonly used
209 as we will discuss next for several sectors represented in our emission model. Appendix B provides an overview
210 of the data that is used per sector.

211 Non-industrial combustion is dominated by households' natural gas consumption to heat houses, for cooking, and
212 for warm water supply. A Dutch energy provider has a dataset publicly available from about 80 smart meters for
213 the year 2013 with hourly gas consumption (Liander, 2018). It clearly shows a seasonal cycle, but also more small-
214 term variations (daily data are shown in Fig. 3). We also see higher gas consumption in the beginning of the year,
215 where the first three months of 2013 had some long, cold spells.

216 The use of energy for household heating is connected to the outside temperature. Previous studies have therefore
217 used the concept of heating degree days to describe the temporal variability in emissions from households (Mues
218 et al., 2014; Terrenoire et al., 2015). This method weighs all daily mean temperatures below a certain temperature
219 threshold (here 18°C, as suggested by Mues et al. (2014)) and assigns emissions to these days accordingly. Besides
220 heating, gas consumption is related to warm water supply and cooking, which is largely independent of the outside
221 temperature. Therefore, a constant offset is assumed of 20%, similar to Mues et al. (2014). More details can be
222 found in Appendix B.

223 We compared the heating degree day method using observed temperature data from the Royal Netherlands
224 Meteorological Institute (KNMI) with gas consumption data on a daily basis (Fig. 3). The degree day function
225 follows the gas consumption data very well, including the higher consumption at the start of the year, reaching an
226 R² of 0.90 (N=365). The gas consumption of consumers also has a diurnal pattern with peaks in the early morning
227 and late afternoon. Therefore, a diurnal profile can be estimated based on typical working hours, for which we
228 used profiles from Denier van der Gon et al. (2011). For hourly data R² is 0.80 (N=8760, not shown).



229
 230 **Figure 3. Daily time profiles for households (a) and glasshouses (b). Solid red lines are based on true activity data,**
 231 **whereas dashed black lines are parameterizations based on the degree day function.**

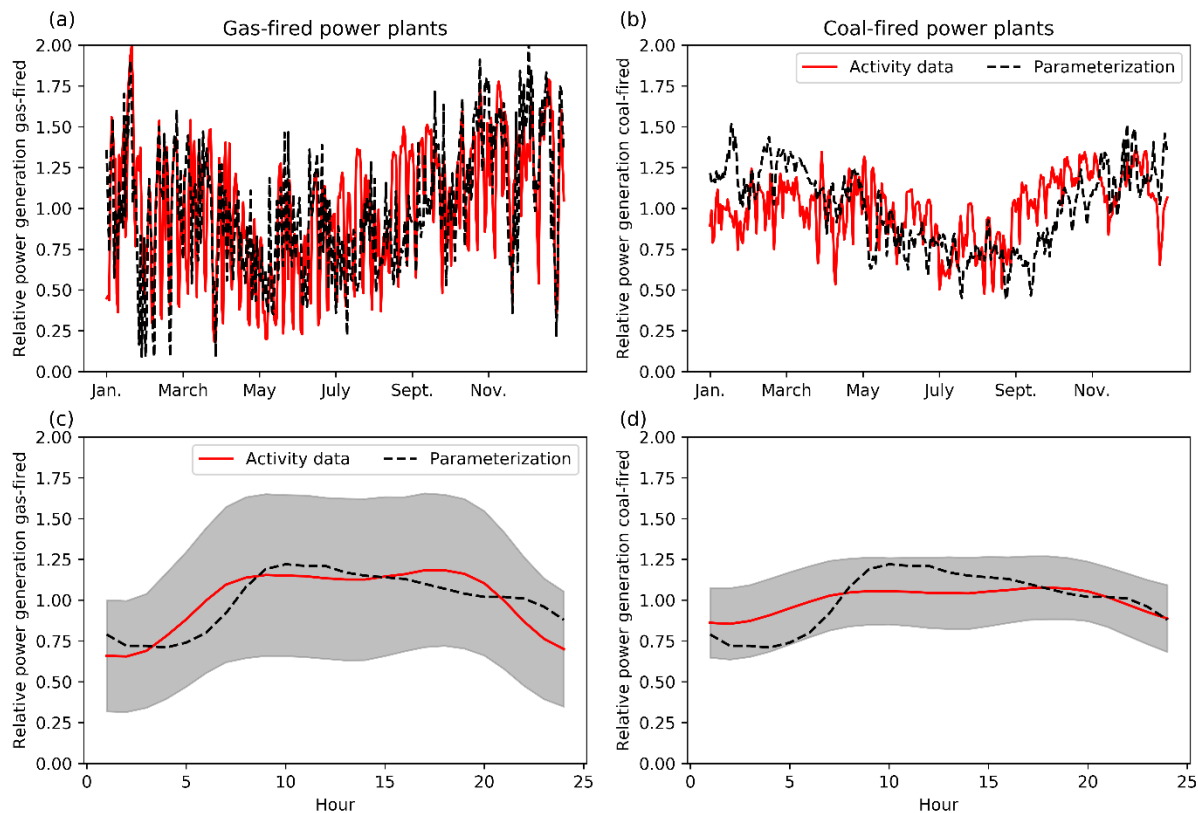
232 For the energy consumption of glasshouses there is no true activity data available. Instead, we use modelled daily
 233 energy consumption for a typical Dutch glasshouse cultivating tomatoes (courtesy of Bas Knoll, TNO) as the
 234 ‘truth’ (activity data). This time profile is calculated for typical meteorological conditions, such that the order of
 235 magnitude and the peaks are representative for an average year. There is almost no energy consumption during the
 236 summer, which indicates that there is no constant offset. So, we use the heating degree day function with no
 237 constant offset to determine the time factors. Moreover, we use a lower temperature threshold of 15 °C to get a
 238 better fit with the observed energy consumption. During summer several days show a peak in the relative gas
 239 consumption, suggesting that the average temperature has dropped below the threshold. The estimated function
 240 compares well with the activity data (Fig. 3) with an R^2 of 0.85 ($N=365$). The diurnal cycle of glasshouse emissions
 241 is likely to be different from that of household emissions. Yet we lack data to establish a diurnal cycle. We therefore
 242 use the same diurnal profile as for households, although this is likely to be incorrect.

243 Power plants can use different fuels such as hard coal, natural gas or biomass. In the Netherlands coal-fired and
 244 gas-fired power plants account for 80–85 % of the total energy production. The remainder comes mainly from
 245 wind energy (5–6 %) and biomass burning (5–6 %). Power generation data are reported by the European Network
 246 of Transmission System Operators for Electricity (ENTSO-E), which has detailed data available for the whole of
 247 Europe (Hirth et al., 2018). Coal-fired power plants are currently the main source of energy and their generation
 248 is relatively stable compared to other sources. It does, however, show a seasonal cycle with less energy production
 249 during the summer months. Gas-fired power plants have a larger temporal variability as they are mainly used as
 250 back-up for peak hours, depending also on the amount of renewable energy that is available.

251 We use the degree day function to estimate the time profiles of both coal- and gas-fired power plants. Linear
 252 regression analysis shows that the coal-fired power generation is correlated with degree days ($R^2 = 0.17$). In this
 253 case we use a large constant offset of 80 % and a threshold of 25 °C which were chosen to best match the actual
 254 power generation data. The offset is much larger than for households because there is always a basic energy
 255 demand from the industry. In contrast, the gas-fired power plants are (negatively) correlated with the wind speed
 256 ($R^2 = 0.13$) and incoming solar radiation ($R^2 = 0.10$), which may indicate a higher need for gas-fired power
 257 generation in the absence of renewable sources. Therefore, we replace the temperature in the degree day function
 258 with the multiplication of wind speed (threshold of 10 m s^{-1}) and incoming solar radiation (threshold of 150 J cm^{-2}).
 259 A constant offset of 10 % is assumed.

260 The diurnal cycles for power plants can be based on socio-economic factors. For example, the energy demand
 261 peaks early in the morning when people get ready to go to work and at the end of the afternoon when they get
 262 home. We find this pattern in the actual power generation data, with coal-fired power plants being less variable
 263 during the day than gas-fired power plants. The fixed profile from the European MACC-III emission inventory
 264 (Denier van der Gon et al., 2011; Kuenen et al., 2014) matches reasonably well with gas-fired power plant profiles,
 265 but it is less applicable for coal-fired power plants (Fig. 4). Overall, the estimated profiles for gas-fired power
 266 plants (daily/hourly data) have an R^2 of 0.31/0.32 ($N=366/8784$) when compared to the activity data. For coal-
 267 fired power plants this is 0.17/0.21 ($N=366/8784$).

268 The constant offset of 80% for coal-fired power plants is mainly caused by the energy demand of the industry and
 269 other semi-continuous processes. Taking into account seasonal variations in these processes could improve the
 270 timing of coal-fired power plant activities, probably increasing the power generation in winter relative to the
 271 summer holiday period. Moreover, the renewable energy supply is probably better modelled when taking into
 272 account a larger domain, since the energy supply is not just local. With a better prediction of the amount of
 273 renewables we could improve the timing of the gas-fired power plant emissions, which mostly function as a back-
 274 up for renewable energy.



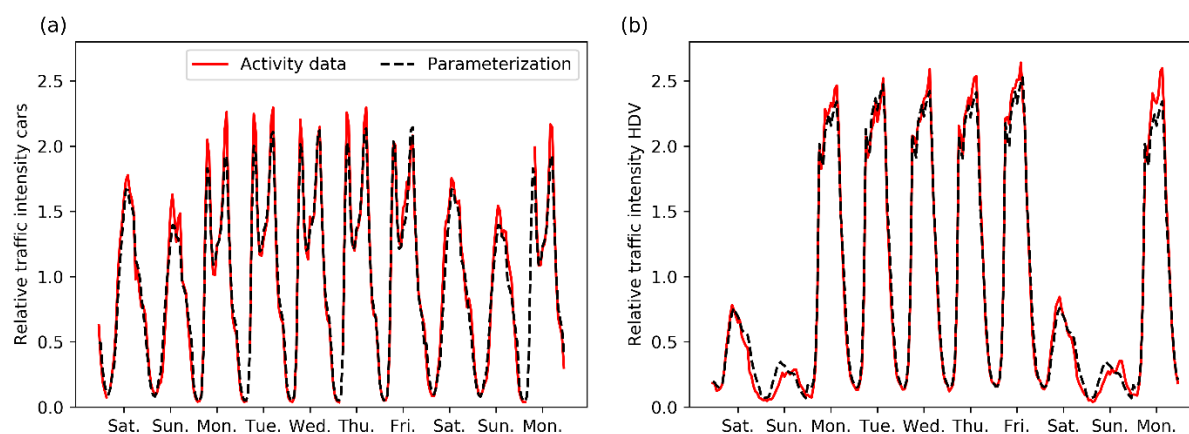
275
 276 **Figure 4. (top row) Daily time profiles for gas-fired (a) and coal-fired (b) power plants. Solid red lines are based on true**
 277 **activity data, whereas dashed black lines are parameterizations based on observed temperature (coal) and wind**
 278 **speed/radiation (gas). (bottom row) Average diurnal cycle for gas-fired (c) and coal-fired (d) power plants. Solid red**
 279 **lines are based on true activity data, whereas dashed black lines are fixed profiles from the MACC inventory (Denier**
 280 **van der Gon et al., 2011; Kuenen et al., 2014). Shading gives the 1σ variability of the diurnal cycle based on activity**
 281 **data.**

282 The industrial sector consists of a wide range of activities, of which some are semi-continuous and only interrupted
 283 by maintenance stops while others follow working hours. This makes it very difficult to predict the temporal
 284 variability, especially for the overall sector. Since the largest CO_2 emissions are related to refineries and heavy

285 industry we will focus on these activities. We find a seasonal cycle in the reported industrial activity, with a small
286 decline during the summer and Christmas holidays. However, the variations are very small (max. 1 %). Therefore,
287 we assume constant emissions.

288 Road transport emissions can vary between different road and vehicle types (Mues et al., 2014), but are also
289 strongly dependent on environmental, socio-economic and driving conditions (such as the amount of stops, free-
290 flow versus stagnant conditions, and engine temperature). Traffic count data are often used to create average time
291 profiles for road traffic emissions, although with traffic counts we are unable to account for environmental and
292 driving conditions. Traffic counts for the Netherlands are made available by the Nationale Databank
293 Wegverkeersgegevens (NDW) and similar data is available in many developed countries. We differentiate between
294 two vehicle types (passenger cars + motorcycles (hereafter referred to as cars) and light duty + heavy duty vehicles
295 (hereafter referred to as HDV)) and three road types (highway, main road, urban road). We selected all available
296 locations for 2014 within or close to Rotterdam that distinguish 3-5 vehicle lengths and filtered for a minimum
297 data coverage of 75 %. This leaves us with 25 highway, 6 main road and 13 urban road locations. From this data
298 we make average time profiles (daily, weekly and monthly) per road and vehicle type, as is often done to
299 disaggregate road traffic emissions. Note that this method excludes any spatial variations (e.g. highways leading
300 towards the city vs. the beach), except for differentiating between road types.

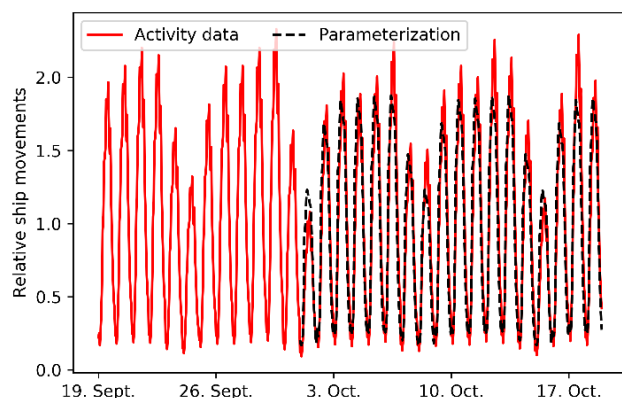
301 Generally, HDV show a larger spread due to the low counts during the weekend (Fig. 5). Car counts on weekdays
302 show a morning and evening rush hour and they go down in between. In contrast, HDV counts peak throughout
303 the day and only go down after the evening rush hour. Moreover, the diurnal cycles are different during the
304 weekend than on weekdays. These patterns can be explained from socio-economic factors. Current time profiles
305 are often based on cars and are unable to correctly represent the temporal variability of HDV. This also affects the
306 spatial distribution of emissions and therefore we create average diurnal, weekly and seasonal profiles separately
307 for cars and HDV, for different road types and considering the day of the week. The comparison of true traffic
308 counts and averaged traffic counts results in R^2 values between 0.83 and 0.95 for hourly data for the whole year
309 (N between 2665 and 6471 because of gaps in the traffic count data).



310
311 **Figure 5. Time profiles of passenger cars (a) and heavy-duty vehicles (b) road transport on highways for ten randomly**
312 **chosen days in March. Solid red lines are based on true activity data, whereas dashed black lines are parameterizations**
313 **based on averaged traffic counts for Rotterdam.**

314 Shipping emissions are dependent on the type of fuel used and whether ships apply slow-steaming. Additionally,
315 during loading and unloading ships still emit CO₂ and other pollutants, even though they are not moving. Such
316 information is currently not available, so instead we use information about the arrival and departure of ships in the

317 port of Rotterdam to make a time series of ship movements. Note that this only applies to large vessels that
 318 transport goods and passengers and that the time profile will look different for recreational shipping. However,
 319 large ships account for approximately 80 % of the total shipping emissions in the area of interest. Since we lack
 320 information about other type of shipping movements, we will only account for large ships in the time profiles.
 321 We collected ship movements for one month (daily data) and an average diurnal profile. The diurnal cycle shows
 322 a peak throughout the day, which corresponds well with the HDV road transport emission patterns on highways.
 323 The reason for this is that HDV road transport is related to shipping movements, as HDV takes care of part of the
 324 good transport further inland after the goods have arrived by ship. We also find a clear weekly pattern with less
 325 ship movements during the weekend, although the decrease is less than for HDV road transport. This is likely
 326 because large ships, such as entering the port of Rotterdam, continue travelling during the weekend. Therefore,
 327 the weekly pattern resembles more that of car road transport on highways. Thus, we can estimate ship movements
 328 by using the temporal profiles of HDV and cars on highways. This method is specifically tested for Rotterdam and
 329 different patterns might be visible elsewhere. We also use HDV patterns for the seasonal variability, and final
 330 parameterized and reported activity in this method reach an R^2 value of 0.89 for a period of 18 days with hourly
 331 data (N=432) as shown in Fig 6.



332
 333 **Figure 6. Daily time profiles for shipping. Solid red line is based on true activity data, whereas dashed black line is a**
 334 **parameterization based on traffic counts of heavy-duty vehicles (diurnal cycle) and cars (day-to-day variations) on**
 335 **highways.**

336 2.1.3 Step 3: Spatial disaggregation.

337 National total sectorial emissions need to be distributed into spatially explicit emissions for our study domain. The
 338 spatial disaggregation of emissions has already received attention from inventory builders. Existing emission
 339 inventories can be used to describe the spatial disaggregation, if available for the region at high resolution.
 340 Therefore, no extra effort is put in the spatial disaggregation and the spatial patterns from the Dutch Emission
 341 Registration have been adopted (Netherlands PRTR, 2014).

342 In absence of a high-resolution inventory, simple default proxies for the spatial distribution can be used, such as
 343 population density (e.g. Gridded Population of the World (GPW)) and the presence of roads or waterways (e.g.
 344 OpenStreetMap). Generally, these proxies are also used by inventory builders, but are often updated to take into
 345 account local circumstances. For example, main roads and urban roads are busiest in densely populated areas and
 346 we can assume emissions on main and urban roads are correlated with population density. Highways are used for
 347 transport between cities and therefore emissions take place outside densely populated areas as well. Nevertheless,
 348 highway transport is usually to and from densely populated areas, such that most emissions will take place close
 349 to cities. We can therefore relate these emissions with the population density in the area of interest (in this case

350 Rijnmond) relative to the rest of the country, which places the same amount of the country-level emissions in our
351 case study domain as the gridded inventory. Additionally, the location of large power plants or industrial plants is
352 often known (for example from E-PRTR (Pollutant Release and Transfer Register)), which can be used directly.
353 Although such information allows us to possibly construct a detailed fossil fuel model in data-sparse regions in
354 the future, in this study we focus first on the more easily implementable and less-developed parameterization of
355 temporal activity in different sectors (step 2) to assess whether this approach is promising enough for future
356 extension.

357 **2.1.4 Step 4: Uncertainty analysis**

358 The emission model we have constructed in steps 1–3 contains several parameters per source sector: activity,
359 emission factor, spatial proxy and time profile. For the analysis we only consider the emission factors and time
360 profiles, as we assume activity data and the spatial distribution to be (a) well-known for our study area, and (b)
361 mostly unobservable from the network of only 7 sites which is used here to evaluate our approach (see Sect. 2.2.3).
362 Although the spatial distribution is actually a large source of uncertainty, we aim at optimizing parameter values
363 that are valid for the entire case study area and for simplicity we ignore the spatially variable uncertainties.
364 Nevertheless, it is possible to incorporate spatial uncertainties in this methodology as well, as illustrated by Super
365 et al. (2020).

366 As input for step 1 in the dynamic emission model we use generalized parameters which we take from the IPCC,
367 EEA and other organizations. These databases also provide an uncertainty range, which we use in a final step to
368 create a covariance matrix. The covariance matrix describes the Gaussian uncertainty of these parameters (diagonal
369 values) and error correlations between parameters (off-diagonal values). From the covariance matrix we create an
370 ensemble of parameters (N=500) that represents their joint distributions, and we use them to calculate an ensemble
371 of emissions. In this Monte Carlo simulation, we transform some Gaussian parameters into log-normal
372 distributions to account for non-negativity, or to account for distributions with a very long tail (mainly emission
373 ratios, which can become high in specific cases where no emission reduction measures are taken). Appendix A
374 summarizes the used parameter values and uncertainties (including the shape of the distributions) and shows an
375 example of the covariance matrix. This method is a first step towards a better quantification of parameter
376 uncertainties and error correlations and additional effort has already been made to improve this method (Super et
377 al., 2020).

378 In a final step, we select the most important parameters which are either very uncertain or have a large impact on
379 the total emissions. This leaves us with the 44 parameters that we optimize in a set of data assimilation experiments,
380 described next. In Sect. 3.1 we report uncertainties in % (1σ) for normal distributions (CO_2) or as a 90 %
381 confidence interval (CI) for lognormal distribution (co-emitted species).

382 **2.2 Data assimilation to estimate fossil fuel sources**

383 The goal of data assimilation is to find a state at which the system is in optimal agreement with observations. In
384 this work, the observations we want to explore are the mole fractions of CO_2 and its co-emitted species while the
385 state of the system is the underlying spatiotemporal distribution of fossil fuel emissions. Such configurations are
386 sometimes referred to as “FFDAS” (fossil fuel data assimilation systems) applications, with a number of examples
387 in recent literature (Rayner et al., 2010; Asefi-Najafabady et al., 2014; Basu et al., 2016; Graven et al., 2018).

388 Given the sparsity of approaches explored so far, the dynamic emission model with its parameter driven emissions
 389 we present here could lend itself well for application in an FFDAS, and this is what we explore through a set of
 390 experiments with our own data assimilation methodology.

391 In this study we use the CarbonTracker Data Assimilation Shell (CTDAS) (v1.0) described in detail in Van der
 392 Laan-Luijkx et al. (2017). Briefly, the CTDAS system is a flexible implementation of a square-root Ensemble
 393 Kalman Filter (Whitaker and Hamill, 2002), which also allows lagged windows (i.e. smoothing instead of
 394 filtering). The Ensemble Kalman Filter optimizes the cost function for unknown variables in the state vector x
 395 using information from observations (\mathbf{y}^0 with covariance \mathbf{R}) and a prior estimate of the state vector (\mathbf{x}^b with
 396 covariance \mathbf{P}).

$$397 \quad J(\mathbf{x}) = (\mathbf{y}^0 - \mathcal{H}(\mathbf{x}))^T \mathbf{R}^{-1} (\mathbf{y}^0 - \mathcal{H}(\mathbf{x})) + (\mathbf{x} - \mathbf{x}^b)^T \mathbf{P}^{-1} (\mathbf{x} - \mathbf{x}^b) \quad (7)$$

398 In this function, \mathcal{H} is the observation operator that returns simulated mole fractions given the state vector. \mathbf{R} and
 399 \mathbf{P} determine how much weight is given to the observations and prior estimate, respectively.

400 The optimized state vector (indicated with superscript a , whereas b refers to the prior estimates) which minimizes
 401 the cost function is

$$402 \quad \mathbf{x}^a = \mathbf{x}_t^b + \mathbf{K}(\mathbf{y}_t^0 - \mathcal{H}(\mathbf{x}_t^b)) \quad (8)$$

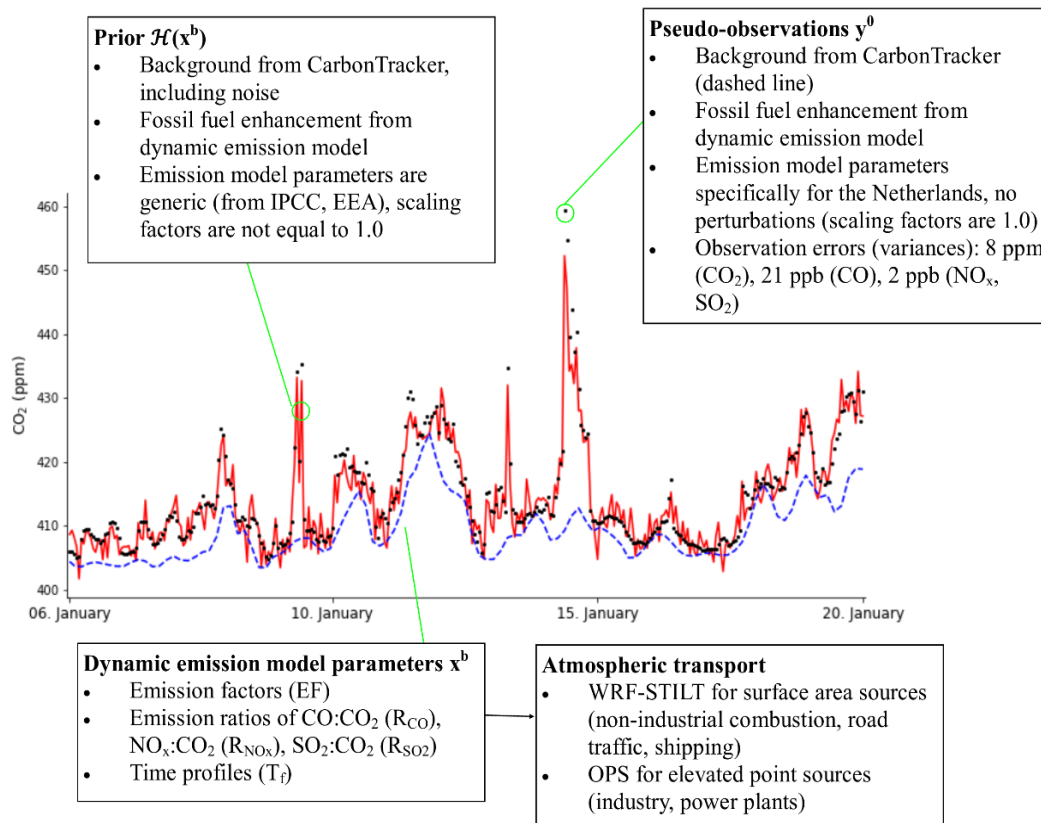
403 and its covariance is

$$404 \quad \mathbf{P}_t^a = (\mathbf{I} - \mathbf{K}\mathbf{H})\mathbf{P}_t^b \quad (9)$$

405 Here, \mathbf{H} is the linearized observation operator and \mathbf{K} is the Kalman gain matrix:

$$406 \quad \mathbf{K} = (\mathbf{P}_t^b \mathbf{H}^T)(\mathbf{H}\mathbf{P}_t^b \mathbf{H}^T + \mathbf{R})^{-1} \quad (10)$$

407 The solutions of Eq. (8) and Eq. (9) are calculated as in Peters et al. (2005) using an ensemble of 80 members. The
 408 choice for the ensemble size was based on the typical dimensions of our inverse problem, which has $N=1960$
 409 observations and $M=44$ unknowns for the base run.



410
 411 **Figure 7. Time series of pseudo-observations and prior CO₂ mole fractions and a summary of how these time series**
 412 **were created.**

413 We have adapted CTDAS for smaller scale studies by replacing the typical observation operator \mathcal{H} , which is the
 414 global TM5 transport model (Huijnen et al., 2010), with a combination of WRF-STILT footprints and the OPS
 415 plume model, building on the methods described in Super et al., (2017a) and He et al. (2018). Moreover, we have
 416 added our emission model to the observation operator so that we can sample its parameter distribution in
 417 atmospheric mole fraction space. More details about the individual parts of this system are provided below and
 418 are summarized in Fig. 7.

419 2.2.1 Observation operator

420 The observation operator translates the 44 parameters in the emission model first into emissions (through Eq. (1)
 421 and Eq. (2)) and then into atmospheric mole fractions. The transport modelling consists of two parts. The first part,
 422 the Weather Research and Forecasting-Stochastic Time-Inverted Lagrangian Transport (WRF-STILT, (Nehrkorn
 423 et al., 2010) model, is used for surface emissions that are representative of large areas (i.e., not a point source).
 424 STILT is a Lagrangian particle dispersion model that describes the footprint of a single measurement by dispersing
 425 particles back in time (Gerbig et al., 2003; Lin et al., 2003). With this footprint the surface influence of emissions
 426 on a single observation can be described. An advantage of this method is that it allows the pre-calculation of linear
 427 atmospheric transport, which makes this part of the observation operator less computationally demanding than
 428 running an ensemble of a full atmospheric transport model (like WRF with chemistry). The total domain covered
 429 with WRF-STILT is 77 x 88 km (Fig. 1) and includes most of the Randstad.

430 The second part of the transport modelling is a plume model. In a previous study we have shown that point source
 431 (stack) emissions should be modelled with a plume model to better represent the limited dimensions of the stack

432 plume (Super et al., 2017a). Similarly, Vogel et al. (2013) have shown that the surface influence calculated by
433 STILT can lead to large model errors for stack emissions. Therefore, we include the OPS (Operational Priority
434 Substances, short-term version) plume model in our framework to model the transport and dispersion of stack
435 emissions (Van Jaarsveld, 2004; Sauter et al., 2016). OPS provides hourly concentrations at pre-defined receptor
436 points, which represent our measurement sites. We apply the OPS model only to point source emissions within
437 the Rijnmond area, as we found in a previous study that a plume model only has an added value less than 10–15
438 km downwind from the stack (Super et al., 2017a). Point sources at more than 10–15 km from the observation site
439 can be sufficiently represented with a Eulerian model. The OPS model input includes detailed information about
440 the exact stack height and heat content of the plume. For more details on WRF-STILT and OPS see Appendix C.
441 In addition to the fossil fuel contribution we also include background mole fractions for CO₂ and CO. NO_x and
442 SO₂ are short-lived and therefore the variations in the background are relatively small compared to the fossil fuel
443 signals. The CO₂ background is taken from the 3-D mole fractions of CarbonTracker Europe (Peters et al., 2010)
444 and also accounts for biogenic fluxes. The resolution of these CO₂ fields is 1x1° and we select the grid box that is
445 situated over Rotterdam. The 3-hourly data are linearly interpolated to get hourly background mole fractions that
446 are added to the fossil fuel signals calculated by the transport models. We use the strong wintertime correlation
447 between CO₂ and CO mole fractions ($r = 0.73$) to calculate CO background conditions from the CO₂ background.
448 This is not very accurate, but for the purpose of this OSSE it provides us with a decent estimate of the variability
449 in background mole fractions.

450 2.2.2 State vector

451 We populated the state vector with a selection of the most important parameters of the emission model, based on
452 their impact on the total emission uncertainty described in the results (Sect. 3.1). However, we hypothesize that
453 emission model parameters that are not part of the state vector are nevertheless uncertain and may affect the results.
454 Therefore, we include a total of 44 scaling factors in our state vector (x^b), and each scaling factor is linearly related
455 to a parameter from the emission model. The uncertainty in these parameters (covariance matrix P) is derived from
456 the Monte Carlo simulations described in Sect. 2.1, with the spread in the emission model parameter values
457 provided by the same databases of the IPCC and EEA. These uncertainty values can also be found in Appendix A.
458 For this study we selected an arbitrary two-week period in January 2014 (6–20 January). Note that during the
459 summer the importance of source sectors might be different, e.g. there will be less heating from households.
460 Nevertheless, this period is sufficient to test the applicability of our DA system. We loop over the 14 days in our
461 study period, resulting in one posterior state vector for each day. We initialize our state vector for every new day
462 using the posterior values and posterior uncertainties from the previous day. Because the footprints we generated
463 extend backwards for six hours, the state vector for each day is effectively only constrained by the observations
464 from that same day, and hence we did not use a Kalman-smoother approach in this work in contrast to other
465 CTDAS applications.

466 Although this is a data-rich region, we use generic values for the prior emission model parameters which we take
467 from the IPCC, EEA and other organisations (Appendix A). These values are typically valid for a large region
468 (e.g. Europe) and not necessarily the best estimate for our regional case study. The reason that we use these values
469 is that they can provide a first estimate of the emissions in data-scarce regions where inverse modelling might add

470 most to our knowledge. With this set-up we can examine how well we can constrain the true emissions starting
471 with this generic, and widely available, information.

472 One major challenge in this study is to attribute the mismatch between the observed and modelled mole fractions
473 to a specific sector, as a CO₂ observation alone provides no details on the origin of the CO₂. Therefore, we include
474 three tracers (CO, NO_x and SO₂) that are co-emitted with CO₂ during fossil fuel combustion in a ratio (referred to
475 as R_{CO}, R_{NO_x} and R_{SO₂}) that is specific for each source sector (Fig. 2). Their (pseudo-)observations can inform us
476 about the source of the mismatch, but through their emission ratio to CO₂ they also constrain the magnitude of
477 CO₂ emissions in the emission model. The ratios R_{CO}, R_{NO_x} and R_{SO₂} used for this conversion to CO₂ emissions is
478 not fixed: for each of the co-emitted species we included them in the state vector. This recognizes that emission
479 ratios are highly variable and uncertain but play an important role in source attribution.

480 **2.2.3 Pseudo-observations**

481 In this work we create observing system simulation experiments (OSSEs), which use pseudo-observations instead
482 of true observations. The advantage of using pseudo-observations is that we can accurately examine the abilities
483 of our new approach without having to account yet for (often dominant) atmospheric transport errors. This
484 approach represents an ideal situation with relatively few sources of error compared to a study using real
485 observations, which makes it useful to study the potential of this new system to optimize emission model
486 parameters.

487 The pseudo-observations used to optimize the emission model parameters are created using the same observation
488 operator as described above. The emission model is used to create realistic emissions with a high spatiotemporal
489 resolution. Yet in contrast to the prior, we use specific local (Dutch) values for the emission model parameters.
490 These parameters are considered to be the truth and are therefore not scaled (scaling factors are 1.0). We found
491 that these local parameter values are always within the uncertainty range of the general (prior) values, so that the
492 true solution is part of the distribution explored within the prior. This is confirmed in an experiment with a small
493 model-data mismatch and no noise on the background, which reproduces the true parameters very well (not
494 shown).

495 The resulting emissions are used in combination with the background mole fractions and transport calculated by
496 WRF-STILT and the OPS model to create pseudo-observations at the locations shown in Fig. 1. For the pseudo-
497 observations the original background time series are used, whereas in the inversion random noise is added to the
498 background mole fractions with a standard deviation of 2 ppm for CO₂. We assume no contribution from biogenic
499 CO₂ to the excess CO₂ over the background, which means that any biogenic contribution to CO₂ within our
500 footprint is the same as in the inflow from outside our domain, thus cancelling in the subtraction of the background
501 CO₂. An error in biogenic fluxes is therefore attributed to the fossil fuel emissions, which represents a typical case
502 where biogenic and fossil fuel signals are hard to distinguish from each other and from the background. Biogenic
503 fluxes can be significant, even in urban areas, and therefore add significant uncertainty to the fossil fuel flux
504 estimates (Fischer et al., 2017; Sargent et al., 2018).

505 One simulated time series is illustrated in Fig. 7. The monitoring network consists of seven sites that are scattered
506 over the city of Rotterdam and the port. All sites exist in the national CO₂ or air quality measurement networks,
507 although not all species used in the inversion are observed at all locations. We only use the daytime (12–16 h LT)
508 observations to constrain our emissions, resulting in a total of 1960 observations. This is normally done to favour

509 well-mixed conditions when simulated transport is more reliable, and we want to mimic this limitation. We assume
 510 all instruments have an inlet at 10m above ground level. In reality this is lower for several sites, but during the
 511 well-mixed daytime conditions the difference is minimal. Representing atmospheric transport around in-city sites
 512 can be very challenging and therefore the use of elevated sites or a transport model that can represent transport in
 513 complex terrain in more detail is recommended when true observations are used.

514 The covariance matrix \mathbf{R} describes the observation error. It accounts for errors related to instrumentation, but also
 515 representativeness errors due to model transport, interpolation, and parameterization used in the emission model.
 516 Although in principle such errors can be excluded in an OSSE, we prefer to use realistic estimates of these errors
 517 to allow for the random errors that we applied to the prescribed boundary inflow, as well as to account for
 518 parameters in the emission model that are not optimized even though they contained uncertainty in the pseudo-
 519 data creation. We base the \mathbf{R} matrix on the calculated errors in the background and atmospheric transport and
 520 variability caused by parameters that are not part of the state vector from the uncertainty analysis, and we end up
 521 with variances of 2.5 ppm (CO₂), 8 ppb (CO), 3 ppb (NO_x) and 1 ppb (SO₂).

522 2.3 Data Assimilation Experiments

523 We perform various experiments to examine the sensitivity of the system to different set-ups and sources of error.
 524 The experiments are discussed here, and the detailed set-up of the inversions is summarized in Table 2. The base
 525 run is labelled “Base”.

526 1) State vector definition: We start with a comparison of two different state vectors. For this purpose, we compare
 527 the base run with an inversion (Short_state) which only includes the 21 most important parameters as identified in
 528 the sensitivity analysis. This test allows us to examine the impact of erroneous, non-optimized emission model
 529 parameters on the emission estimates. The results are discussed in Sect. 3.2.

530 2) Source attribution: Next we compare two monitoring network configurations which differ in the number of
 531 tracers used. We perform an inversion with CO₂ as the only tracer (CO₂_only) and one with the full range of tracers
 532 (Base) to assess the added value of including co-emitted species for source attribution. These tests address the
 533 question whether co-emitted species can be used for source attribution. The results are discussed in Sect. 3.2.

534 3) Propagation: The third experiment is used to examine the effect of propagation of posterior values and
 535 uncertainties on the final emission estimates. We compare the base run to a run that has no propagation
 536 (No_propagation and CO₂_only_no_propagation) but instead starts from the same prior mean and uncertainty on
 537 each of our 14 days considered. The runs without would allow the parameter values to change over time. The
 538 results are discussed in Sect. 3.3.

539 **Table 2. Overview of the inversions: which tracers are included, the length of the state vector and whether posterior**
 540 **values and uncertainties are propagated.**

Inversion name	Tracers	State vector length (per day)	Propagation to the next day
Base	All	44	Yes
Short_state	All	21	Yes
No_propagation	All	44	No
CO ₂ _only	CO ₂	44	Yes
CO ₂ _only_no_propagation	CO ₂	44	No

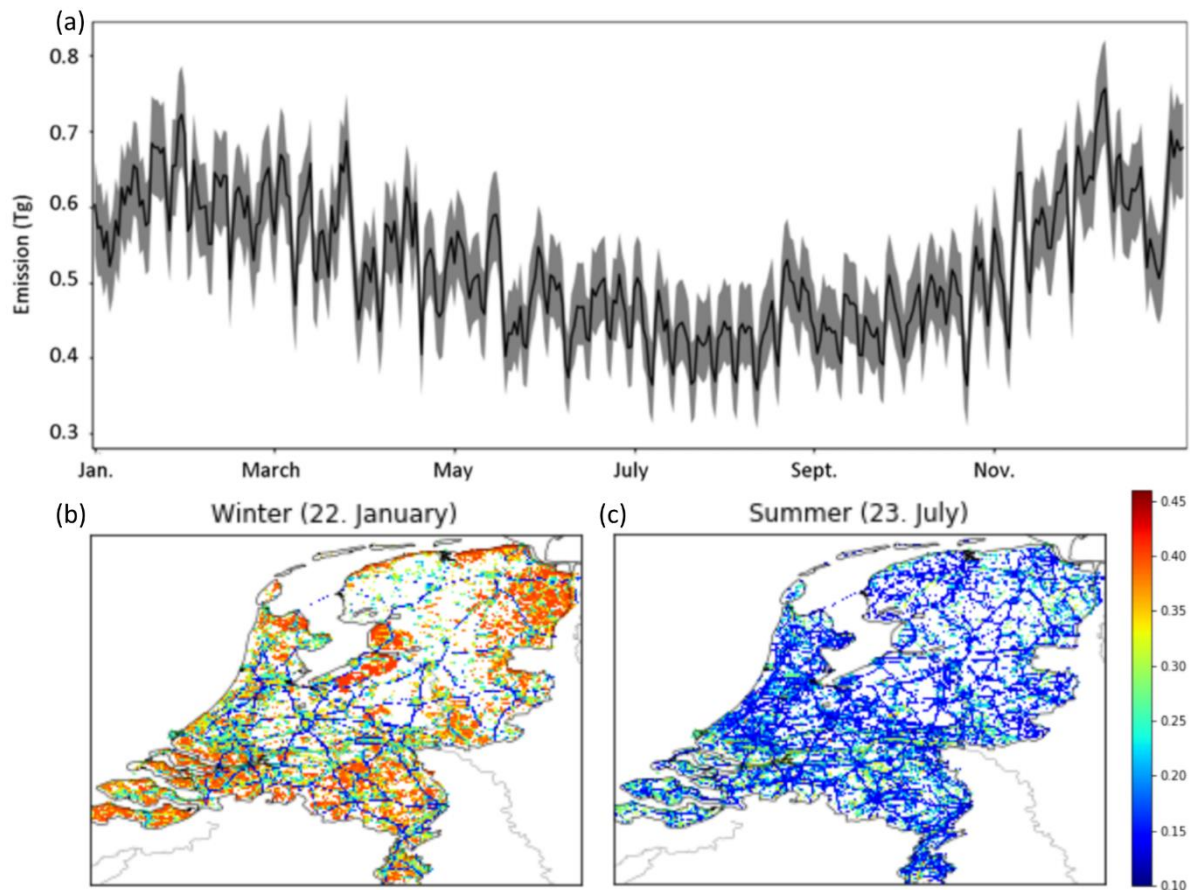
541 **3 Results**

542 Before demonstrating the use of our dynamic emission model in an inverse framework, we demonstrate its
543 application as a simple but versatile method to generate hourly gridded emissions for multiple species with full
544 covariances.

545 **3.1 Dynamic emissions and their uncertainty**

546 The total annual emission of CO₂ for the Netherlands calculated with the dynamic emission model is 180 Tg CO₂
547 with an uncertainty of 15 % (1-sigma Gaussian based on 500 members of a Monte Carlo simulation). This matches
548 the total of the Dutch national emission inventory for 2014 by design (step 1), but the uncertainty on the latter was
549 estimated with a similar Monte Carlo simulation to be only 1 % for CO₂ in 2004 (Ramírez et al., 2006). This
550 smaller uncertainty is fully due to the use of country-specific emission factors with a much smaller range than we
551 derived from the IEA and IPCC inventories. Spatial disaggregation (step 2) does not affect the uncertainty of the
552 domain aggregated annual fluxes, and the time profiles (step 3) have no impact on the annual total emissions. For
553 CO, NO_x and SO₂ the uncertainties in the emission model are much larger, with medians (CI's) of 6.5×10^8
554 $(1.3 \times 10^8 - 6.8 \times 10^9)$ kg CO yr⁻¹, 5.0×10^8 $(1.2 \times 10^8 - 5.1 \times 10^9)$ kg NO_x yr⁻¹, and 1.3×10^8 $(5.1 \times 10^6 - 2.2 \times 10^{10})$ kg SO₂ yr⁻¹.
555 These ranges result from uncertainties in the assumed ratios of their release per unit of CO₂ emitted.

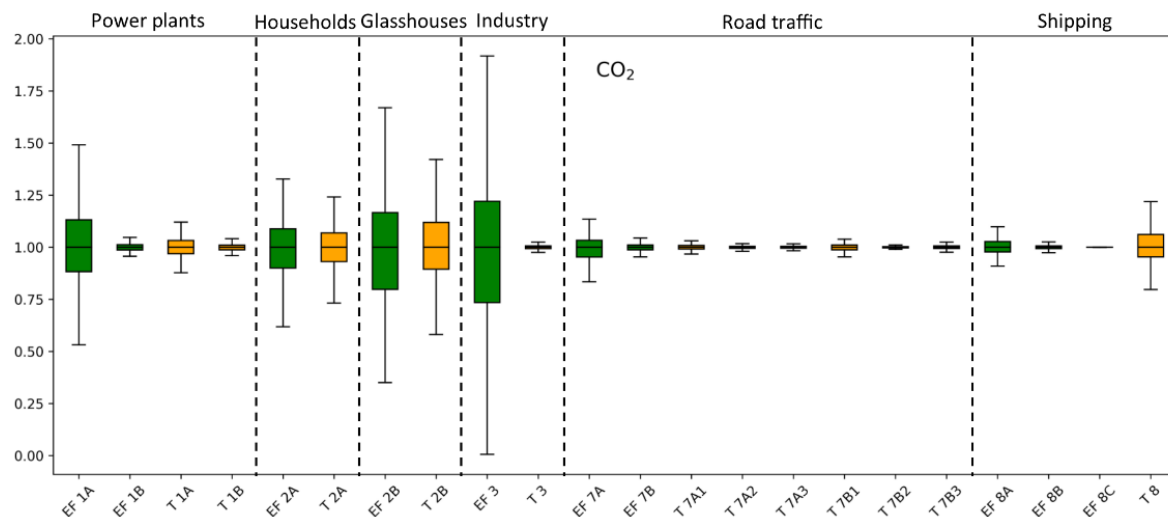
556 At the sub-annual time scale, time profiles have an impact on the uncertainties as well. The daily emissions of the
557 Netherlands depend on the day and the season (Fig. 8) and range from 0.36 to 0.76 Tg CO₂ day⁻¹. The time series
558 shows a seasonal cycle with lower emissions during the summer. There is a clear weekly cycle with reduced
559 emissions during the weekend. The uncertainty in the total daily emission varies between 8 and 15 %, which is
560 similar to or lower than the uncertainty in the annual total emissions. The explanation for these relatively low
561 uncertainties is that many uncertainties are temporally uncorrelated and their impacts on individual days partially
562 cancel out. Moreover, the largest sectors (coal-fired power plants and industry) already have a large uncertainty
563 and adding more uncertainty through the time profiles has little impact. Nevertheless, the uncertainties introduced
564 through the time profiles cause an uncertainty in daily CO₂ emissions of about 7 %, if the other uncertainties are
565 excluded from the analyses.



566

567 **Figure 8. (a) Time series of daily CO₂ emissions (in Tg CO₂ day⁻¹) and their uncertainty. Given is the interquartile range**
 568 **(shaded area) and the median (line) from the ensemble. (b and c) Map of annual mean relative uncertainty of emissions**
 569 **for the top 25 % pixels with the largest emissions, during a winter month (dominated by household gas- and electricity**
 570 **use) and a summer month (electricity and road-traffic dominated).**

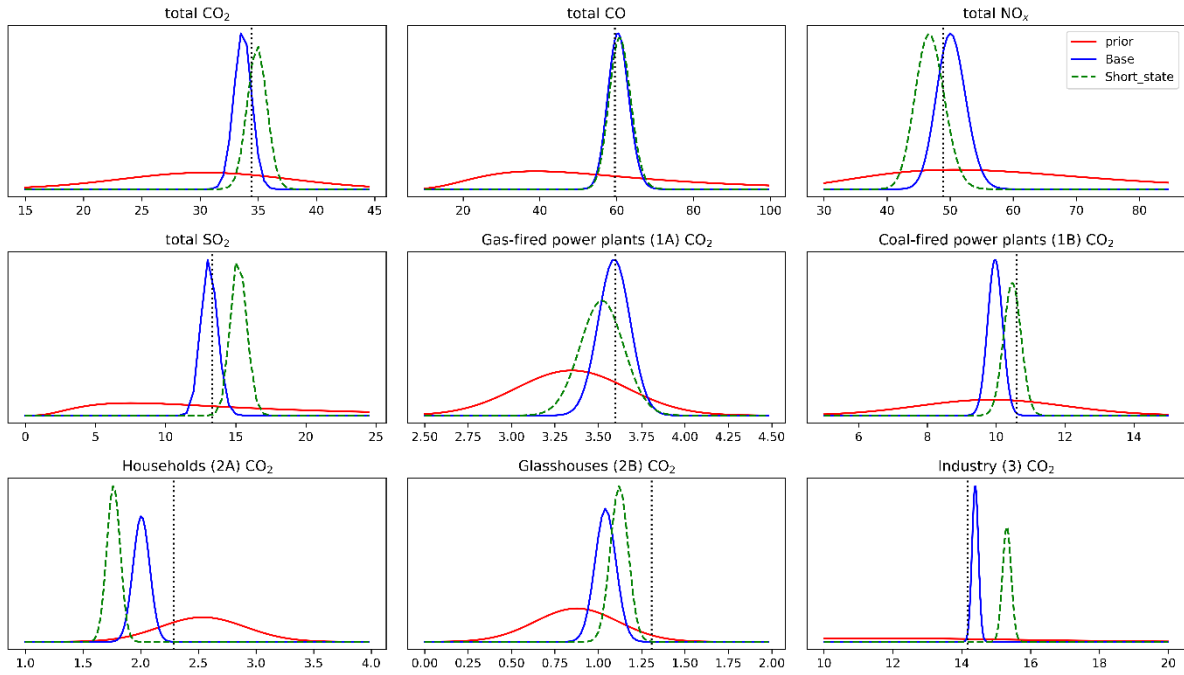
571 Differences in the relative contribution of different sectors are evident when looking at the map of uncertainties
 572 across the Netherlands (Fig. 8), reflecting both the most uncertain parameters, but also the dominant source sectors.
 573 Winter emissions for example are dominated by household gas-usage, while industrial and traffic emissions give
 574 rise to uncertainty year-round at a 10–30 % level. We further identified the most important parameters per source
 575 sector with a Monte Carlo simulation per source sector (Fig. 9). Results shows that the road traffic and shipping
 576 sectors contain the smallest relative uncertainties, although the time profile for shipping causes an uncertainty of
 577 about 7 % in the total shipping emissions. The industrial emissions are most uncertain, and this is almost
 578 exclusively due to the emission factor, which causes an uncertainty of 41 % in the total industrial emissions.
 579 Similarly, the power plant emissions have a large relative uncertainty due to the uncertain emission factor of coal-
 580 fired power plants (19 %). Also, for households and glasshouses the emission factor is uncertain (14 % and 26 %, respectively),
 581 but here the time profiles also have a large impact (10 % and 16 %, respectively).



582
 583 **Figure 9. Box plots showing the uncertainty in the CO₂ emissions from power plants (1A+1B), households (2A),**
 584 **glasshouses (2B), industry (3), road traffic (7A+7B) and shipping (8A+8B+8C) caused by individual parameters**
 585 **affecting that sector. Uncertainty is represented as the spread in daily (normalized) emissions from each ensemble**
 586 **member (N=500) for a randomly chosen day. EF refers to an emission factor (green bars) and T to a time profile (orange**
 587 **bars). (Sub)sectors are indicated with their short names as summarized in Table 1. Note that the time profiles of road**
 588 **traffic emissions are specified per road type (1 = highway, 2 = main road, 3 = urban road). Minor parameters that have**
 589 **very small impacts on CO₂ emissions are not shown here (23 out of 44).**

590 3.2 Optimizing dynamic emissions

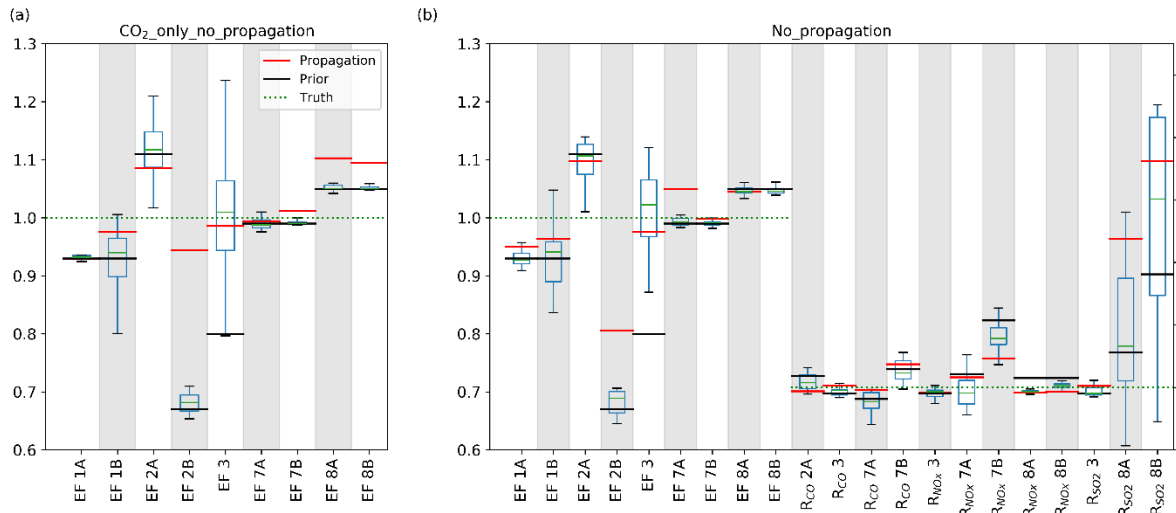
591 In the base inverse modelling setup, our system is able to improve the mean estimate and reduce the uncertainty
 592 on total CO₂, CO, NO_x, and SO₂ emissions. Figure 10 shows the probability density function of these estimated
 593 total emissions, compared to the prior (using parameters derived from IPCC/EEA) and the truth (created with
 594 country-specific parameter values). Interestingly, the posterior result deteriorates slightly when using a shortened
 595 state vector in which 11 parameters of “minor” influence (such as the SO₂:CO₂ ratio of household emissions) are
 596 not optimized from their incorrect prior. This is caused by sporadic atmospheric signals that are dominated by
 597 household emissions, even if these emissions only contribute a small fraction to the total emissions. These signals
 598 are then used to update the emission factor, while the emission ratios are also incorrect.



599 **Figure 10. Probability density functions of emissions per species or per source category (for CO₂) in units of Tg (CO₂)**
 600 **or Gg (CO, NO_x, SO₂).** The truth is shown as a vertical dotted line, typically well-matched by the mean of the posterior
 601 **in blue.** Using a shortened state vector (green dashed line) deteriorates the total non-CO₂ emissions substantially and
 602 **leads to misattribution of CO₂ emissions in minor categories such as 2A (households).**
 603

604 With CO₂ as the only tracer in the inversion we find that we can still estimate total CO₂ emissions (truth-minus-
 605 optimized = 0.03 Tg CO₂ yr⁻¹), but we lose the capacity to attribute emissions to specific sectors. Instead, mainly
 606 the emission factor of the largest single source being industry (EF3) is optimized. We illustrate this in Fig. 11,
 607 using the No_propagation run. The large spread across the 14 individual days indicates that the emission factor
 608 jumps around within a large prior uncertainty distribution and is not well-constrained on each day. Some of the
 609 other emission factors show almost no deviation from the prior and little variability. Given the constraints posed
 610 by CO₂ observations alone, and the limited number of parameters that change the simulated CO₂, optimizing EF3
 611 improves the results at the lowest costs. Introducing the co-emitted species allows the system to identify the source
 612 of a residual, and attribute it to the right parameters if sufficient sensitivity is present. This is especially true for
 613 those sectors that have relatively small emissions and/or uncertainties, like 2B and 1A. This is corroborated by the
 614 posterior covariance matrices (See Appendix D) which show a reduction in parameter correlations for those
 615 parameters (i.e., a better mathematical separation of the estimates) when all tracers are included in the estimate.
 616 For other parameters the median values are further from the truth than the prior (e.g. for R_{SO2} 8), which indicates
 617 that there is too little sensitivity to these parameters.

618

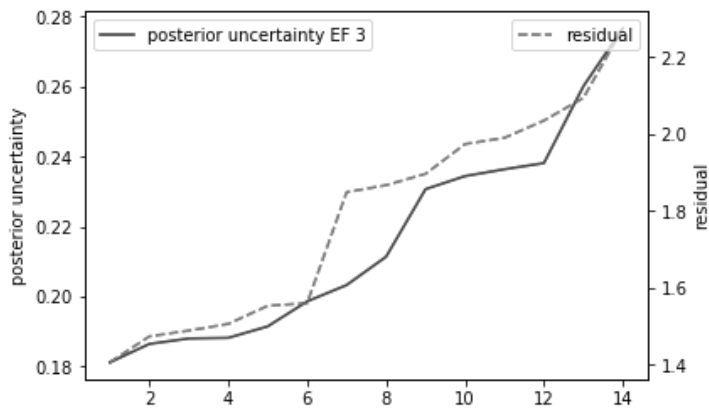


619

620 **Figure 11. Spread (Q1-Q3) and median values of the parameter scaling factors for the fourteen individual days included**
 621 **in the CO₂_only_no_propagation (a) and No_propagation (b) inversions, and final value of the CO₂_only (left) and base**
 622 **(right) inversion (red lines). The prior values are indicated by the black lines and the truth is indicated with the green**
 623 **dotted lines (value of 1.0). The left y-axis is for the emission factors, the right y-axis for the tracer ratios. The inversion**
 624 **with all tracers shows more variability in the emission factors and larger deviations from the prior values.**

625 3.3 Localization and propagation of information

626 Propagating information on parameter values from one day to the next is often better than using the median of
 627 individual days' estimates as illustrated by the red lines in Fig. 11. Nevertheless, the sporadic detection of plumes
 628 with specific signatures suggests that a form of selection or localization of the strongest signals could reduce noise
 629 and improve the estimate for the No_propagation run. We therefore ranked the 14 daily independent parameter
 630 estimates based on their relative posterior uncertainty and the residuals in an attempt to find the most trustworthy
 631 parameter values. This ranking is done per parameter, so the best estimate of different parameters can be related
 632 to different days. The increase in residual (same for all parameters) and posterior uncertainty (of the industrial
 633 emission factor) is shown in Fig. 12, where the 3–5 highest ranked days have similar characteristics after which
 634 the reliability decreases. On the lower ranked days, atmospheric signals from that particular source sector are too
 635 small (or even absent) to update the parameters related to that source sector. A similar pattern is found for the other
 636 parameters (not shown), with 2–5 days of high sensitivity out of 14.



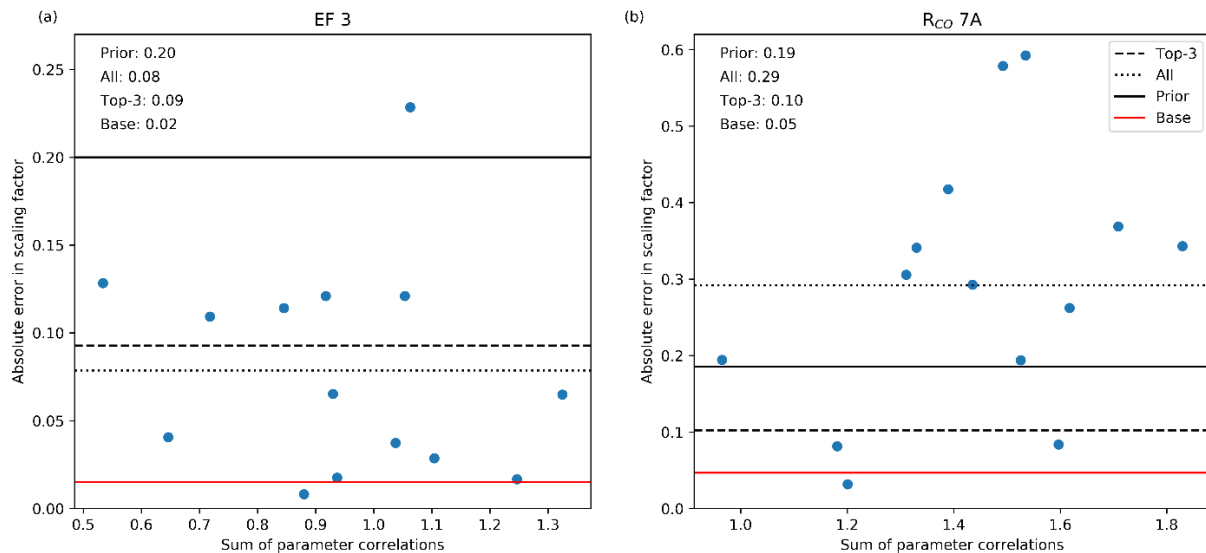
637

638 **Figure 12. Increase in posterior uncertainty (1 σ of unitless scaling factor) in the industrial emission factor (EF 3) and**
 639 **absolute mean residual of CO₂ (in ppm) from highest- to lowest-ranked days.**

640

641 When we use the top-3 averaged parameter values to calculate emissions we find for most sectors that the emission
 642 estimate is similar to the base run, albeit with a larger uncertainty, while for a few specific sectors results
 643 deteriorate. This suggests that selecting for strong signals can dampen spurious noise, but still does not improve
 644 on the base run that includes full propagation of the covariances, hence carrying information on parameter
 645 correlations that is partially lost in the No_propagation run.

646 From the posterior covariance matrices we can confirm our selection of “good” days, as these typically show
 647 relatively weak correlations between parameters. For the industrial sector (emission factor, R_{NO_x} , R_{SO_2}) these are
 648 typically weak on most days, and indeed the mean over the entire period already gives a robust estimate of the true
 649 parameter value (Fig. 13). The parameters with the strongest correlations are R_{CO} of households and road traffic,
 650 and their mean values tend to be dominated by a few outliers. Selecting days on which the posterior parameter
 651 correlations are weak (i.e. the atmospheric signal clearly contains information about this specific parameter) results
 652 in a large improvement compared to the prior or a 14-day average. Moreover, these results show a similar or better
 653 performance as the top-3 selection based on Fig. 12 (0.08 for EF3 and 0.18 for R_{CO} 7A, not shown), and are closer
 654 to the base run.



655
 656 **Figure 13. Scatter plot of the absolute error in the scaling factor of the industrial emission factor (EF 3) and R_{CO} of road**
 657 **traffic (7A) against the sum of the parameter correlations of the same parameters. The correlation coefficients are -0.17**
 658 **and 0.37 respectively. The horizontal lines give the average absolute error in the scaling factor for the prior (full black**
 659 **line), if all 14 days are averaged (dotted line), and based on the 3 days with the smallest parameter correlations (dashed**
 660 **line) and the result for the base run (full red line). The values are also given.**

661 4 Discussion

662 4.1 Optimizing the dynamic emission model

663 The dynamic emission model has the advantage over static emission fields that its parameters are optimized, giving
 664 more detailed physical meaning to the results. To reduce the size of the problem, the state vector can be populated
 665 with those parameters that are most important and/or uncertain. However, we find that other uncertain parameters
 666 that are not part of the state vector can still significantly affect the optimization. Therefore, the size of the state
 667 vector should be considered carefully when applying this method. How to best determine the size of the state
 668 vector requires further work, possibly using some objective criterion to select for a dynamic model with an optimal
 669 information content (Akaike, 1974). Moreover, we performed an experiment to establish the possibility to optimize

670 the time profiles as part of the state vector. Although we found small improvements for some sectors, it appears to
671 be difficult to differentiate between the different variables in Eq. (2) that have a linear relationship based purely
672 on the observations. Therefore, the results are not shown and optimizing the temporal dynamics of the emission
673 model requires further work. In a future study the uncertainty caused by spatial disaggregation should also be
674 included, as well as the possibility to reduce this uncertainty using higher-resolution satellite observations
675 (Kuhlmann et al., 2019).

676 Additionally, we identified the base run as the simplest method to get good estimates, but we do note that our
677 current propagation scheme does not yet include error growth. That means that eventually the ensemble will
678 converge on a parameter value and discard incoming observational evidence, unless the covariance is inflated to
679 allow new updates. Examples of such a covariance inflation scheme are ample in literature and in principle not
680 difficult to include, but were not yet considered in this work as the time periods covered were still short. An
681 example related to this work is to use weather system characteristics to determine a correlation length for
682 household emissions.

683 Finally, we have demonstrated that tracers are suitable for source attribution. Several previous studies have used
684 co-emitted species as tracer for fossil fuel CO₂ by taking advantage of the specific emission ratio characteristics
685 of each source sector (Lauvaux et al., 2013; Lindenmaier et al., 2014; Turnbull et al., 2015) and came to similar
686 conclusions. Nevertheless, the uncertainty in emission ratios remains a source of error and therefore the
687 optimization of emission ratios with our system is a promising step forward. Using co-emitted species to identify
688 the total fossil fuel contribution to the observed CO₂ signal is more difficult (Turnbull et al., 2006). The reason for
689 this is that there is a large variability in emission ratios between sectors. This makes it difficult to establish an
690 average emission ratio for an urban area, because it depends strongly on the relative contribution of each source
691 sector and may vary over time.

692 **4.2 Radiocarbon and background definition**

693 Therefore, a nice addition to this inversion system would be the inclusion of radiocarbon measurements. The
694 radiocarbon isotope (¹⁴CO₂) can be used to simulate fossil fuel CO₂ records and has been applied successfully in
695 several inverse modelling studies (Turnbull et al., 2006; Levin and Karstens, 2007; Miller et al., 2012; Turnbull et
696 al., 2015; Basu et al., 2016; Wang et al., 2018). The radiocarbon measurements could be used directly in the
697 inversion (as we did with the co-emitted species) or be used to define a fossil fuel CO₂ record in advance (Fischer
698 et al., 2017; Graven et al., 2018). Our urban network detects average fossil fuel CO₂ signals of about 5 ppm with
699 peaks up to 50 ppm. This would result in $\Delta^{14}\text{C}$ signals (the ratio of ¹⁴CO₂ to ¹²CO₂) of around 13 up to 130 per
700 mille, which are certainly detectable with current techniques. However, observations of carbon isotopes are
701 expensive and currently not widely available, so their applicability is still limited. Besides $\Delta^{14}\text{C}$ other isotope
702 signatures and tracers can also provide additional information. For example, ¹³CO₂ and O₂/N₂ can give insight in
703 the dominant sources and sinks or fuel types (Lopez et al., 2013; Van der Laan et al., 2014) and as such be an
704 indicator for the transition from fossil fuels to biofuels. They might also help to separate between the stack
705 emissions of industry and coal- and gas-fired power plants.

706 An additional advantage of including the radiocarbon isotope is that the uncertainty in the background CO₂ can be
707 excluded, i.e. only the fossil fuel record is considered. Here, we choose to ignore the uncertainty in the background,
708 except in the definition of the covariance matrix R , and attribute all tracer residuals to the fossil fuel emissions.

709 Yet an incorrect definition of the background causes a large bias in the optimized emissions (Göckede et al., 2010).
710 There are also several other methods to deal with the non-fossil fuel related CO₂ signals. First, the uncertain
711 background can be added to the state vector and be optimized in the inversion. For example, He et al. (2018) have
712 shown that high-altitude aircraft observations are suitable to improve regional biosphere flux estimates by
713 correcting the bias in boundary conditions. Second, a mole fraction gradient over the area of interest can be
714 calculated using an upwind and downwind site such that the boundary inflow plays no role anymore (Turnbull et
715 al., 2015). This method was shown to reduce the impact of boundary inflow, but only when the wind direction is
716 more or less perpendicular to the gradient (Bréon et al., 2015; Stauffer et al., 2016). Therefore, this method limits
717 the amount of useful measurements.

718 **4.3 Error correlations**

719 The emission model also allows us to study the correlations between model parameters, therefore giving more
720 insight in how information can be used in the system and which parameters are more challenging to separate.
721 Previously, Boschetti et al. (2018) have used the presence of error correlations between emissions of different
722 species and found that this reduces the posterior uncertainties for all species. They even show that the uncertainty
723 reduction increases with the correlation and that an incorrect definition of the error correlations may cause a
724 systematic bias in the posterior emission estimate. However, error correlations are only beneficial if the
725 atmospheric observations can distinguish between the correlated parameters. If this is not the case the presence of
726 parameter correlations can result in poorly constrained parameters and/or large posterior uncertainties. This is
727 especially true when parameters are sensitive to parameter correlations, as we show for R_{CO} of road traffic.

728 An important question is then why some emission model parameters are more sensitive to the presence of
729 parameter correlations than others. One hypothesis is that parameters with a lower prior uncertainty are more
730 sensitive to the presence of parameter correlations. The idea behind this is that if we reduce the diagonal value
731 (uncertainty) by a factor of 4 the off-diagonal value (parameter correlation) reduces by a factor of 2. This means
732 that the parameter correlation is relatively stronger if the uncertainty is lower (Boschetti et al., 2018). This
733 hypothesis cannot be confirmed by our results, as we only find a correlation of -0.27 between the prior uncertainty
734 and the sensitivity to parameter correlations (defined as the correlation between the posterior uncertainty and the
735 sum of the parameter correlations). The main difficulty here is that not all parameters can be discerned with the
736 observed atmospheric signals. Although we included the additional co-emitted tracers for source attribution, the
737 emission ratios have a large uncertainty and the system can have difficulties assigning residuals to either the
738 emission ratio or the emission factor. Yet if we calculate an average sensitivity and total posterior uncertainty per
739 sector (by combining the emission factor and emission ratios per sector) we find a correlation coefficient of -0.82.
740 This suggests that this hypothesis might indeed be correct and source sectors with larger parameter uncertainties
741 are less sensitive to the presence of parameter correlations.

742 **4.4 Atmospheric transport model errors**

743 In addition to the experiments described in Sect. 2.3 we conducted an experiment that focused on the role of
744 transport model errors by using observed meteorology to drive the OPS model in the inversion. Like many authors
745 before us (McKain et al., 2012; Brioude et al., 2013; Lauvaux et al., 2013; Bréon et al., 2015; Boon et al., 2016)
746 we found a large impact on the performance of our system and once again confirmed the need for accurate transport

747 models. This experiment is not further shown in this work because of its redundancy with previous conclusions.
748 Nevertheless, we performed this experiment to examine whether transport errors are important when the state
749 vector consists of parameters that are valid for the entire domain. Random errors, such as errors in the wind
750 direction, are unlikely to affect the optimized emissions much when averaged over a longer time period and
751 domain. This was shown by Deng et al. (2017), who found little variation in the average CO₂ emission for
752 Indianapolis using different configurations of WRF to calculate the transport. However, they did find an impact
753 on the spatial distribution of the emissions. This becomes important when optimizing a specific source sector that
754 is clustered in one place, such as the glasshouses. We found that the glasshouse sector is only correctly optimized
755 with a specific wind direction. If the modelled wind direction is wrong the residuals would thus not be attributed
756 to the glasshouse sector as it is not in the modelled footprint of the measurement site. As such, we conclude that
757 the footprint definition has an impact on the optimized parameters, despite that the parameters have no spatial
758 distribution. Similarly, Broquet et al. (2018) mention that the location and structure of a simulated urban plume
759 might differ significantly from the true plume characteristics due to errors in the simulated wind speed and wind
760 direction.

761 Systematic errors, whether in the modelled transport or in the observations, are more difficult to solve as they do
762 not cancel out when simulating a longer period, and this can lead to biased emission estimates (Meirink et al.,
763 2008; Su et al., 2011). Several methods have been suggested to overcome problems with an incorrect description
764 of atmospheric transport, such as using an ensemble of atmospheric transport model simulations (Angevine et al.,
765 2014) or the assimilation of meteorological observations (Lauvaux et al., 2013). The latter showed lower biases in
766 buoyancy and mean horizontal wind speed. Another method that is often used is the selection of well-mixed
767 afternoon hours to exclude stable conditions under which pollutant dispersion is often poorly represented (Lauvaux
768 et al., 2013; Bréon et al., 2015; Boon et al., 2016). Such data selection however leads to a bias in the estimated
769 emissions when the diurnal cycle is not correctly accounted for (Super et al., 2020).

770 Here, we also applied a daytime selection criterion to mimic this situation. However, we found that night time
771 hours could be very useful to constrain our emissions. In our DA system we use residual fossil fuel enhancements
772 over a background (prior - true mole fraction enhancement) to constrain the fossil fuel fluxes. The larger the
773 residual, the more information can be gained from it since the impact of the observation error (R matrix) is
774 relatively small. If, for example, the industrial emission factor is underestimated by 10 %, the residual industrial
775 enhancement (given a linear relationship between the emission factor and the total emission from this sector) will
776 be 10 % of the pseudo-observed mole fraction. This means that a large signal from the industry is needed to reach
777 a residual that is larger than the observation error (σ is 1.6 ppm for CO₂). Looking at the time series of pseudo-
778 observations we find that such large signals mostly occur during night time or in the early morning. Therefore, the
779 inversion could benefit strongly from an improved description of night time boundary layers and stable conditions,
780 so that the large night time enhancements can be used to constrain the fossil fuel fluxes.

781 **5 Conclusions**

782 The aim of this study was to examine how well our DA system can quantify urban CO₂ emissions per source
783 sector. Since the prior consists of a dynamic fossil fuel emission model the model parameters are optimized rather
784 than the emissions themselves. The parameters are related to specific source sectors and to attribute residuals to
785 these sectors measurements of additional tracers (CO, NO_x and SO₂) are included in the inversions. We tested this

786 system to examine its ability to overcome some major limitations in current urban-scale inversions: source
787 attribution, definition of the prior and its uncertainties, and the sensitivity to errors in atmospheric transport.

788 We find that inverse modelling at the urban scale is feasible when the observations contain a lot of information
789 about the different source sectors. Based on this work we can conclude:

- 790 1. A dynamic fossil fuel emission model can be useful to create a prior in data-sparse regions or to make
791 use of local data to increase the spatiotemporal representation, while allowing to constrain physically
792 relevant parameters in more detail.
- 793 2. When only CO₂ mole fractions are used in the inversion the total CO₂ emissions are well-constrained, but
794 additional tracers are an important addition to the inversion framework in order to discern the information
795 belonging to specific source sectors and emission model parameters. However, even more tracers might
796 be needed to fully capture the heterogeneity of the emission landscape.
- 797 3. The prior error covariance structure based on the emission model provides useful insight in how
798 parameters interact and what is needed to separate them.

799 Nevertheless, several challenges remain. Transport modelling at this small scale needs to be improved to be able
800 to use real urban observations, as under current conditions the transport error strongly dominates the results.
801 Especially improving the description of night time boundary layers could be beneficial, because large atmospheric
802 signals mostly occur during this period. For the future, additional advances need to be made to include satellite
803 observations in the inverse modelling framework. The advantage of satellite data is that it covers data-sparse
804 regions and with a larger view it can differentiate between the urban dome with high pollution levels and the
805 cleaner rural areas, which is a nice addition to in situ measurements.

806 **Code and data availability**

807 CTDAS (v1.0) (Van der Laan-Luijkx et al., 2017) is released under a GNU-GPL3.0 license and forms the basis of
808 the system described in this paper. Minor changes have been made to include the dynamic emission model. Revised
809 code and the additional module used to describe the dynamic emission model and the creation of pseudo-
810 observations is included as Supplement, as is a script used for the emission uncertainty analysis (Monte Carlo
811 simulation). Input data for the dynamic emission model are taken from open, online databases and are summarized
812 in Appendix A, including their data sources. Example input files for CTDAS and the OPS model are also included
813 as Supplement.

814 **Appendix A: Emission model input data and uncertainties**815 **Table A1. Overview of all parameters in the dynamic emission model, their unit, function type, expected value and**
816 **uncertainty (range).**

Parameter	(Sub)sector	Unit	Function type	Expected value	Uncertainty
Emission factor^(a)	Coal-fired power plants ^(c)	kg PJ ⁻¹	Normal	1.01E8	23 %
	Gas-fired power plants ^(c)	kg PJ ⁻¹	normal	5.61E7	10 %
	Households ^(c)	kg PJ ⁻¹	normal	5.89E7	14 %
	Glasshouses ^(c)	kg PJ ⁻¹	normal	5.61E7	25 %
	Industry ^(d)	kg PJ ⁻¹	normal	7.66E7	40 %
	Road traffic cars ^(e)	kg PJ ⁻¹	normal	7.24E7	10 %
	Road traffic HDV ^(e)	kg PJ ⁻¹	normal	7.33E7	5 %
	Ocean shipping ^(f)	kg PJ ⁻¹	normal	7.76E7	5 %
	Inland shipping ^(f)	kg PJ ⁻¹	normal	7.30E7	5 %
	Recreational shipping ^(f)	kg PJ ⁻¹	normal	7.10E7	5 %
Emission ratio CO:CO₂	Coal-fired power plants ^(c)	kg kg ⁻¹	lognormal	1.29E-4	8.7E-7–2.9E-4
	Gas-fired power plants ^(c)	kg kg ⁻¹	lognormal	8.47E-4	3.4E-4–2.5E-3
	Households ^(c)	kg kg ⁻¹	lognormal	3.88E-3	8.3E-4–9.6E-3
	Glasshouses ^(c)	kg kg ⁻¹	lognormal	5.40E-4	3.1E-5–7.7E-4
	Industry ^(d)	kg kg ⁻¹	normal	2.06E-3	40 %
	Road traffic cars ^(e)	kg kg ⁻¹	lognormal	1.32E-2	8.0E-5–6.5E-2
	Road traffic HDV ^(e)	kg kg ⁻¹	lognormal	2.22E-3	9.3E-5–1.3E-2
	Ocean shipping ^(f)	kg kg ⁻¹	normal	2.32E-3	30 %
	Inland shipping ^(f)	kg kg ⁻¹	normal	3.42E-3	30 %
	Recreational shipping ^(f)	kg kg ⁻¹	normal	2.96E-1	30 %
Emission ratio NO_x:CO₂	Coal-fired power plants ^(c)	kg kg ⁻¹	lognormal	5.94E-4	3.0E-4–9.4E-4
	Gas-fired power plants ^(c)	kg kg ⁻¹	lognormal	2.00E-3	2.6E-4–3.7E-3
	Households ^(c)	kg kg ⁻¹	lognormal	1.50E-3	4.8E-4–3.3E-3
	Glasshouses ^(c)	kg kg ⁻¹	lognormal	1.63E-3	5.0E-4–3.5E-3
	Industry ^(d)	kg kg ⁻¹	normal	6.56E-4	40 %
	Road traffic cars ^(e)	kg kg ⁻¹	lognormal	1.76E-3	9.0E-5–7.5E-3
	Road traffic HDV ^(e)	kg kg ⁻¹	lognormal	1.11E-2	3.3E-4–3.7E-2

	Ocean shipping ^(f)	kg kg ⁻¹	normal	2.32E-2	30 %	
	Inland shipping ^(f)	kg kg ⁻¹	normal	1.37E-2	30 %	
	Recreational shipping ^(f)	kg kg ⁻¹	normal	1.97E-3	30 %	
Emission ratio SO₂:CO₂	Coal-fired power plants ^(e)	kg kg ⁻¹	lognormal	1.66E-4	2.9E-5–4.4E-4	
	Gas-fired power plants ^(e)	kg kg ⁻¹	lognormal	5.01E-6	2.9E-6–7.2E-6	
	Households ^(e)	kg kg ⁻¹	lognormal	2.21E-5	1.4E-5–6.7E-5	
	Glasshouses ^(e)	kg kg ⁻¹	lognormal	8.91E-6	5.2E-6–1.3E-5	
	Industry ^(d)	kg kg ⁻¹	normal	4.28E-4	40 %	
	Road traffic cars ^(g)	kg kg ⁻¹	normal	1.01E-6	100 %	
	Road traffic HDV ^(g)	kg kg ⁻¹	normal	8.16E-7	100 %	
	Ocean shipping ^(f)	kg kg ⁻¹	lognormal	6.18E-3	3.3E-4–2.0E-2	
	Inland shipping ^(f)	kg kg ⁻¹	lognormal	6.57E-3	3.5E-4–3.0E-2	
	Recreational shipping ^(f)	kg kg ⁻¹	lognormal	3.14E-4	1.1E-4–7.0E-4	
Hourly time factor^(h)	Coal-fired power plants	-	normal	1	28 %	
	Gas-fired power plants	-	normal	1	43 %	
	Industry	-	normal	1	5 %	
	Households	-	normal	1	43 %	
	Glasshouses	-	normal	1	74 %	
	Road traffic cars highway	-	normal	1	18 %	
	Road traffic cars main road	-	normal	1	18 %	
	Road traffic cars urban road	-	normal	1	18 %	
	Road traffic HDV highway	-	normal	1	41 %	
	Road traffic HDV main road	-	normal	1	18 %	
	Road traffic HDV urban road	-	normal	1	48 %	
	Total shipping	-	normal	1	31 %	
	Energy consumption per activity data⁽ⁱ⁾	Total power plants	PJ/mln €	-	8.22E-4	-
		Households	PJ/dd ^(b)	-	0.199	-
Glasshouses		PJ/dd ^(b)	-	0.061	-	
Industry		PJ/mln €	-	7.05E-4	-	
Road traffic cars		PJ/mln €	-	3.98E-4	-	

	Road traffic HDV	PJ/mln €	-	2.01E-4	-
	Total shipping	PJ/mln €	-	1.51E-4	-
Fraction of total energy consumption per subsector^(d)	Total power plants: coal	-	-	0.62	-
	Total power plants: gas	-	-	0.38	-
	Road traffic cars: highway	-	-	0.47	-
	Road traffic cars: main road	-	-	0.28	-
	Road traffic cars: urban road	-	-	0.25	-
	Road traffic HDV: highway	-	-	0.56	-
	Road traffic HDV: main road	-	-	0.24	-
	Road traffic HDV: urban road	-	-	0.20	-
	Total shipping: ocean	-	-	0.79	-
	Total shipping: inland	-	-	0.20	-
	Total shipping: recreational	-	-	0.01	-

817 ^(a) Emission factor for coal-fired and gas-fired power plants include uncertainty due to variations in fuel type, including burning
818 of biomass (5 % uncertainty). For households assume 8 % wood combustion based on CO₂ emission values (*Vernieuwd*
819 *emissiemodel houtkachels*, by B.I. Jansen (TNO, 2016)), the remainder is natural gas (with 10 % uncertainty). For glasshouses
820 assume only natural gas combustion, including 20 % additional uncertainty due to use of cogeneration plants. For road traffic
821 cars assume 69 % gasoline, 29 % diesel and 2 % LPG (with 5 % uncertainty); for road traffic HDV assume 100 % diesel.

822 ^(b) dd = degree day

823 ^(c) Expected value and uncertainty based on IPCC Emission Factor Database (EFDB) using 2006 IPCC guidelines

824 ^(d) Expected value based on Netherlands PRTR (emission) and Statistics Netherlands (energy consumption); uncertainty based
825 on expert judgement

826 ^(e) Expected value and uncertainty based on the EMEP/EEA air pollutant emission inventory guidebook 2016

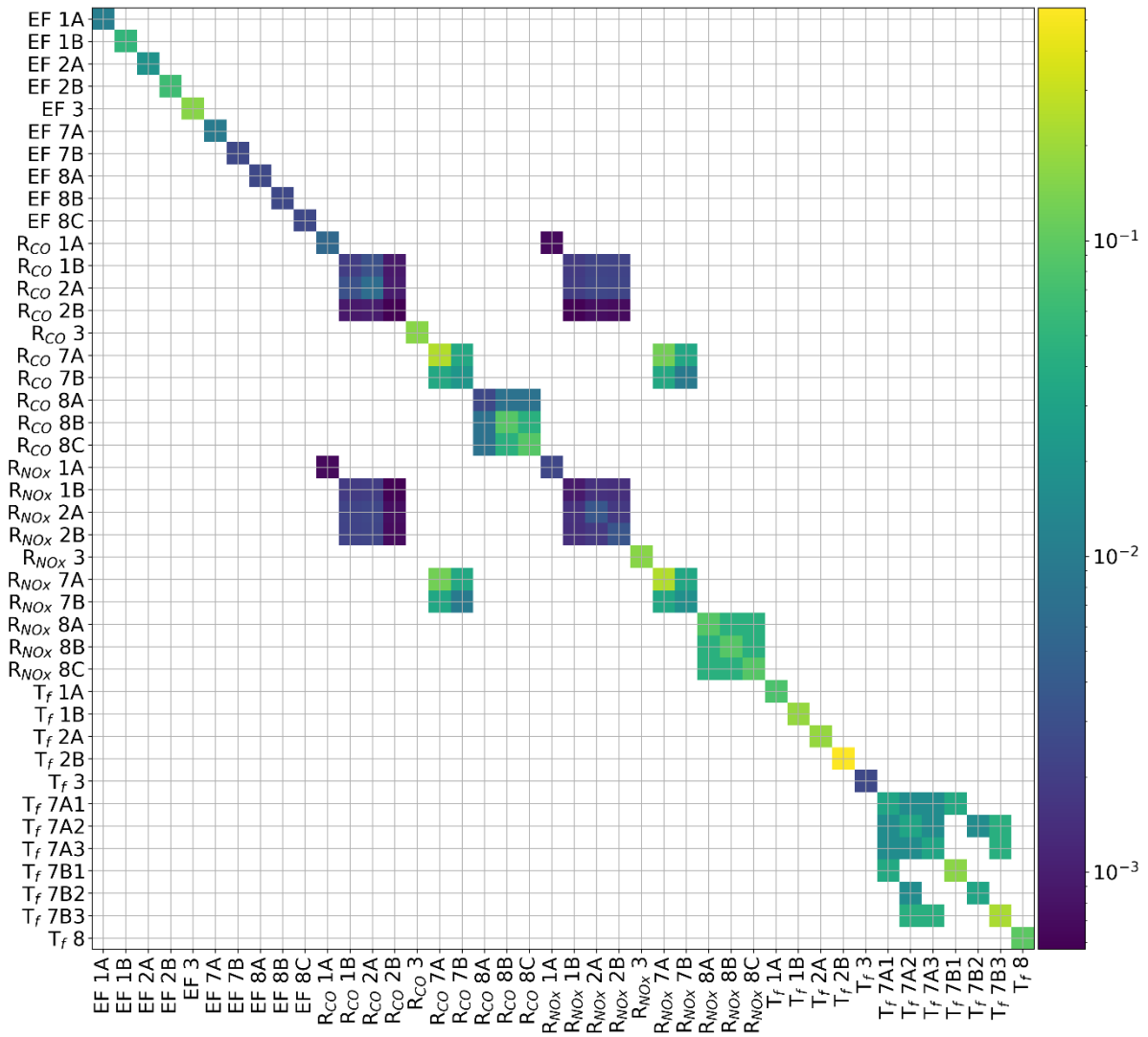
827 ^(f) Expected value and uncertainty based on *CO₂, CH₄, and N₂O emissions from transportation-water-borne navigation*, by Paul
828 Jun, Michael Gillenwater, and Wiley Barbour (Good Practice Guidance and Uncertainty Management in National Greenhouse
829 Gas Inventories)

830 ^(g) Expected value based on Air Pollutant Emission Factor Library (Finish Environment Institute); uncertainty based on expert
831 judgement

832 ^(h) Uncertainties based on comparison activity data-based time profiles and estimated time profiles from environmental/socio-
833 economic factors (Denier van der Gon et al., 2011)

834 ⁽ⁱ⁾ Expected value based on data from Statistics Netherlands (energy consumption, GDP (663008 mln € in 2014)) and Royal
835 Netherlands Meteorological Institute (degree day sum (2313.95 for households, 1443.63 for glasshouses))

836 ^(j) Expected value based on Netherlands PRTR



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840

Figure A1. Covariance matrix for all parameters in the emission model. For all covariances we assume a correlation coefficient of 0.5. (Sub)sectors are indicated with their short names as summarized in Table 1. Note that the time profiles of road traffic emissions are specified per road type (1 = highway, 2 = main road, 3 = urban road).

841 **Appendix B: Temporal profiles**

842 **Table B1. Overview of the data used to create the temporal profiles presented in Sect. 2.1.2. The activity data represents**
 843 **the actual and the parameterizations are based on environmental variables or other proxies.**

Source sector	Subsector	Parameterization	Activity data
Power plants	Gas-fired power plants	Wind speed, solar radiation Threshold: 10 m s ⁻¹ , 150 J cm ⁻² f: 0.1	Power generation
	Coal-fired power plants	Temperature Threshold: 25°C f: 0.8	Power generation
Non-industrial combustion	Households	Temperature Threshold: 18°C f: 0.2	Gas consumption from smart meters
	Glasshouses	Temperature Threshold: 15°C f: 0	Modelled energy consumption
Industry		None (fixed profile)	
Road traffic	Cars	Average traffic counts	Traffic counts
	Heavy duty vehicles	Average traffic counts	Traffic counts
Shipping	Ocean shipping	None (fixed profile)	
	Inland shipping	Traffic counts	Shipping movements
	Recreational shipping	None (fixed profile)	

844
 845 The daily time factor of gas combustion for households may be described in terms of two components. First, gas
 846 is used for warm water supply and cooking, which is relatively fixed. Second, gas is used for heating, which is
 847 strongly temperature dependent. The second component has previously been described using the degree day
 848 concept, from which the daily time factor can be defined as:

$$849 \quad T_t = H/\bar{D} \quad (B1)$$

850 where H is the heating degree day factor ($H = \max(T_{threshold} - \overline{T_{2m}}, 0)$) based on the daily mean outside temperature
 851 at 2 m and a threshold temperature below which heating takes place. \bar{D} is the annual average heating degree day
 852 ($\bar{D} = \frac{1}{N} \sum_{j=1}^N H$). However, gas consumption related to warm water supply and cooking is largely independent of
 853 the outside temperature and therefore a constant offset is included in the heating degree day factor:

$$854 \quad H_f = H + f \cdot \bar{D} \quad (B2)$$

855 where f is the constant offset, which is assigned equally to all days The time factor can now be defined as:

$$856 \quad T_t = H_f/\overline{D_f} \quad (B3)$$

857 where the average heating degree day accounted for the constant offset $\overline{D_f} = (1 + f)\bar{D}$.

858 The Eq. B3 is used for households and coal-fired power plants, whereas for glasshouses no constant offset is
859 assumed and so Eq. B1 is applied. For gas-fired power plants Eq. B3 is used, but the temperature is replaced with
860 average wind speed and solar radiation to match its function as back-up for renewable energy supply:

$$861 \quad H = \max(10 - \bar{u}, 0) \cdot \max(150 - \bar{R}, 0) \quad (\text{B4})$$

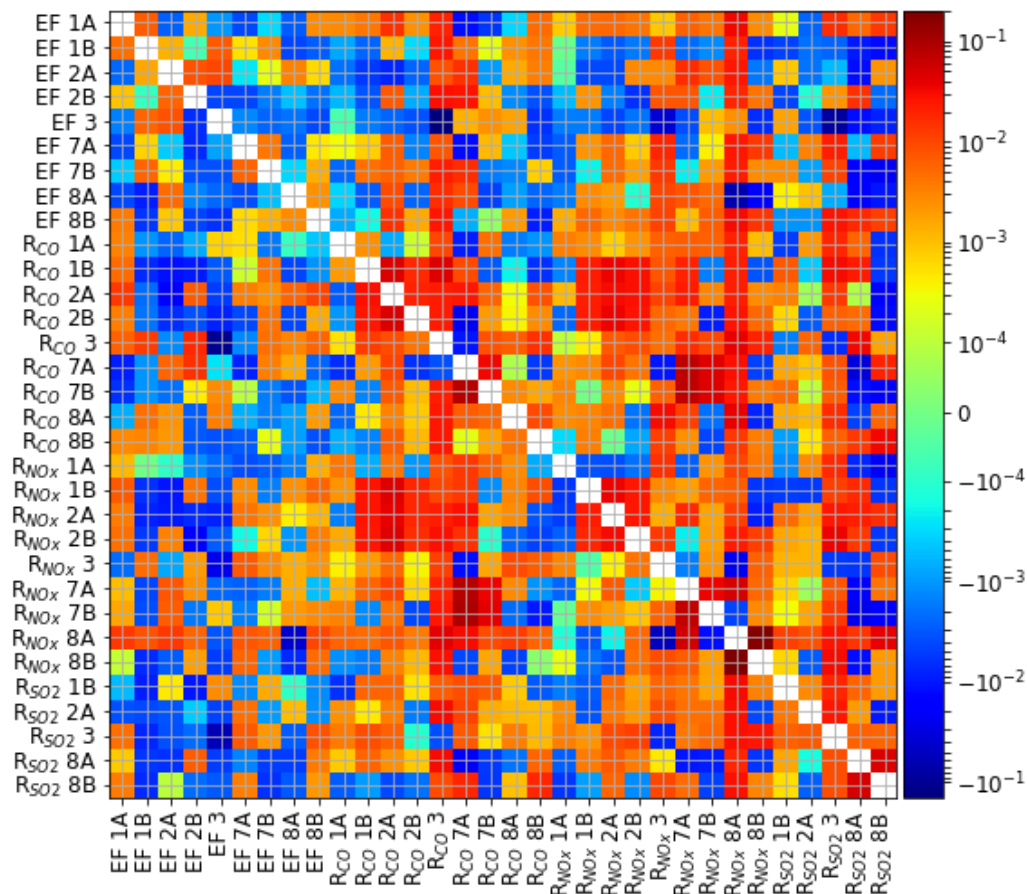
862 where u is the wind speed (m s^{-1}) and R the incoming solar radiation ($\text{J cm}^{-2} \text{hr}^{-1}$).

863 **Appendix C: Observation operator**

864 To generate a footprint with the WRF-STILT model, 75 particles are released at the observation site at the start of
865 the back-trajectory and followed back in time. Given that the variability in hourly observations at an urban location
866 is dominated by local signals, we construct back-trajectories spanning 6 hours. This is based on the domain size,
867 which could be covered within 6 hours for typical wind speeds of 4 m s^{-1} . Within this time frame emissions can
868 become well-mixed throughout the boundary layer under normal daytime mixing conditions, such that emissions
869 outside this range can be represented by a boundary inflow. Footprints are generated for each hour within the back-
870 trajectory to account for hourly variations in the emissions. We drive STILT with meteorology from the WRF
871 model (v3.5.1). The WRF model was set up with two nested domains (15×15 and $3 \times 3 \text{ km}^2$ horizontal resolution)
872 and the STILT footprints have a $1 \times 1 \text{ km}^2$ resolution over the entire domain.

873 The OPS plume model keeps track of a plume trajectory, considering time-varying transport over longer distances
874 (e.g. changes in wind direction and dispersion). If for a time step a specific plume affects the receptor, a Gaussian
875 plume formulation is used to calculate the mole fraction caused by that source based on the true travel distance
876 along the trajectory. We drive the model with the same WRF meteorology as STILT. Only primary meteorological
877 variables (temperature, relative humidity, wind direction, wind speed, precipitation, global radiation) are
878 prescribed, secondary variables (e.g. boundary layer height, friction velocity) are calculated by OPS itself and can
879 differ from WRF. Similar to the WRF-STILT model, we assume an influence time of 6 hours on our observations.
880 However, in this case we run the OPS model forward from -6 hours to the time of observation.

881 **Appendix D**



882
 883 **Figure D1.** Matrix showing the difference in correlation coefficient (r) between the `CO2_only_no_propagation` and
 884 `No_propagation` run averaged for all 14 days, where positive differences indicate reduced parameter correlations when
 885 all tracers are included (`No_propagation`). (Sub)sectors are indicated with their short names as summarized in Table 1.
 886 For some parameters a strong reduction in parameter correlations is shown, indicating that with all tracers that
 887 parameter can be more easily separated from others, for example the emission factors of industry and coal-fired power
 888 plants (EF3 and EF1B).

889 **Author contribution**

890 The initial ideas are developed by WP, IS, HACDvdG and MKvdM. IS and SNCD developed the dynamic
 891 emission model. IS and WP are responsible for setting up the inverse modelling experiments and prepared the
 892 manuscript with contributions from all co-authors.

893 **Competing interests**

894 The authors declare that they have no conflict of interest.

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