

Dear editor and reviewers,

First of all, we would like to express our sincere appreciation to your valuable feedbacks. Your comments are highly insightful and enable us to substantially improve the quality of our manuscript and OpenArray.

In the previous reviews, both reviewers and the editor suffered some issues compiling OpenArray. To ease the installation of OpenArray, we have split it into two packages, a release one for users (<https://github.com/hxmhuang/OpenArray>) and a developing one for project team members (https://github.com/hxmhuang/OpenArray_Dev). The release package includes all the final operator functions and does not require any external libraries (e.g., Python, Boost, Ctags, LLVM, JIT, and Git) other than gcc/g++/gfortran compilers, MPI library, and PnetCDF (shown in the Tab. 1). For the users who are interested in the details of how the C++ code is generated, the developing package can be referred to. The release package enables users to install OpenArray from source through three simple steps (./configure; make; make install). The configure file can detect the environment and generate corresponding Makefile, as many apps do. In addition, we have tested the release package on many platforms, including macOS and quite a few Linux distros (including different versions of Fedora, CentOS, Ubuntu, openSUSE and Debian). We believe the installation should be much easier and the source code is much more robust. The thorough installing guide is given in the updated user manual (<https://github.com/hxmhuang/OpenArray/tree/master/doc>).

Table 1 Dependency of the release package

Type	Source package
Dependency	gcc/g++/gfortran compilers, version 4.9.0 or later. MPI compilers (mpich v3.2.1 or later; openmpi v3.0.0 or later; Parallel Studio XE 2017 or later) PnetCDF, version 1.7.0 or later.
Notes	In the release package, the function of Boost, JIT, LLVM, and Armadillo has been added into OpenArray. In addition, the pre-process which uses Python is removed. Git and Ctags is optional.

Below are our point-to-point responses to all comments.

1 Responses to Dr. Steven J. Phipps

(1) I am afraid, therefore, that I agree with Referee #2 that OpenArray is not yet in a sufficiently robust state for me to allow publication in Geoscientific Model Development.

Ultimately, while your manuscript fulfils the GMD mission of documenting the software, it remains the case that the software described must also be useful to the community.

I have therefore made the decision “Reconsider after major revisions”. Referee #1 has suggested that the text of the manuscript would benefit from proof-reading. Apart from this, I would like to emphasise that the text of the manuscript itself is satisfactory and you should not consider that you need to make changes.

Rather, my reason for returning the manuscript to you at this stage is to allow you to revise the manual and source code of OpenArray, in response to the comments of both referees and in response to my own comments. I hope you can agree that your manuscript will be strengthened considerably if OpenArray is a robust tool that can readily be adopted by the community.

Response:

We sincerely appreciate your efforts installing OpenArray and valuable comments. As described above, we have first minimized the dependencies on the many external libraries for OpenArray users (e.g., Python, Boost, Ctags, LLVM, JIT, and Git). Second we have rebuilt an easy-to-use release package, which enables users to install OpenArray from source by three simple steps (./configure; make; make install). The release package and scripts has been tested on different platforms (including MacOS, openSUSE, Fedora, Ubuntu, Debian, Centos) using different compilers with mpi libraries (e.g., GCC+mpich, GCC+openmpi, Intel Parallel Studio XE). We believe that OpenArray are stable and robust enough to be adopted by the modelling community.

We have revised the manual on GitHub (<https://github.com/hxmhuang/OpenArray/tree/master/doc>) and modified the corresponding sentence in the manuscript. (Lines 653-655):

In the revised manuscript, we changed the sentences “The source codes of OpenArray v1.0 is available at https://github.com/hxmhuang/OpenArray_CXX, and the user manual of OpenArray can be accessed at https://github.com/hxmhuang/OpenArray_CXX/tree/master/doc.” into “The source codes of OpenArray v1.0 is available at <https://github.com/hxmhuang/OpenArray>, and the user manual of OpenArray can be accessed at <https://github.com/hxmhuang/OpenArray/tree/master/doc>.”

In the revised user manual, we added a installing guide for the release version of OpenArray and GOMO. For more details, please refer to the user manual diff.

(2) On my machine, the names of the Intel MPI compilers are mpifort, mpicc and mpi++. The compiler flag to enable OpenMP is also -openmp, rather than -qopenmp. Both of these required me to edit the makefile.

Response:

Thanks for your helpful comments. Using different versions of Intel MPI compilers will vary the compilation instructions and compiler flags. In the Inter compilers version 2017 or later, the names of the Intel MPI compilers are mpiifort, mpiicc, and mpiicpc, and the

compiler flag to enable OpenMP is `-qopenmp`. For the release package, the configure file can detect the environment and generate the Makefile automatically. Therefore, users do not need to modify the makefile.

(3) I had to install the `ctags` package to avoid an error at the precompile stage.

Response:

In the release package, the dependency of OpenArray on `ctags` is removed.

(4) However, I was unable to compile the test case. Firstly, it would be helpful if the instructions could make it clear that you need to be in the `build/` directory, rather than the top-level directory. Nonetheless, the main problem is simply that the model does not compile:

```
mpifort -O0 -w -g -std=c++0x -DBOOST_LOG_DYN_LINK -openmp -D_WITHOUT_LLVM_ -o
manual_main user-manual/oa_main.o \
-lpnetcdf -lboost_program_options -lboost_filesystem -lboost_system -lboost_log -
lboost_log_setup -lboost_thread -ldl -ljit -lgfortran -Wl,-rpath=/lib64/-lstdc++ -L/lib64/ -lpnetcdf
-lboost_program_options -lboost_filesystem -lboost_system -lboost_log -lboost_log_setup -
lboost_thread -ldl -ljit -lgfortran -Wl,-rpath=/lib64/ -lgfortran -L. -lopenarray -lm -ldl -lstdc++ -
lboost_program_options \
-lboost_system -lboost_log -lboost_log_setup -lboost_thread -lpnetcdf -lpnetcdf
```

```
/usr/bin/ld: cannot find -ljit
/usr/bin/ld: cannot find -ljit
collect2: error: ld returned 1 exit status
makefile.intel:146: recipe for target 'manual_main' failed
```

Clearly, there is at least one undocumented dependency on an external library that is causing compilation to fail.

Response:

Thanks for your valuable suggestions. The previous installation instruction is misleading. In the revised version, there is no need to install the JIT library as well as some other apps, since the dependency has been removed.

2 Responses to Dr. David Webb

(1) After some effort (see below) I managed to compile the programs and routines in the top level and in directory 'c-interface'. The compile process then failed in the 'modules' directory:

```
=====
mpicxx -O3 -ffast-math -DBOOST_LOG_DYN_LINK -fopenmp -c -fPIC --std=c++0x -
Werror=return-type -fno-trapping-math -fno-signaling-nans
modules/tree_tool/Simple_Node.cpp -o modules/tree_tool/Simple_Node.o
modules/tree_tool/Simple_Node.cpp: In member function 'void* Simple_node::get_val()':
```

```
modules/tree_tool/Simple_Node.cpp:30:1: error: control reaches end of non-void function
[-Werror=return-type]
}
^
```

cc1plus: some warnings being treated as errors

make: *** [makefile.linux:63: modules/tree_tool/Simple_Node.o] Error 1

=====

Response:

Sorry for the failure in your compiling process. In the User Manual, we recommended installing OpenArray with the below instruction:

make -f makefile.intel oalib_obj.

The makefile *makefile.intel*, rather than *makefile.linux*, should be used here. However, we have simplified the installing process by splitting OpenArray into release and developing packages. The release package does not require external libraries other than gcc/g++/gfortran compilers, MPI library, and PnetCDF. In addition, the release package is easy to use and has been tested on many platforms, including macOS and a few Linux distros (Fedora, CentOS, Ubuntu, openSUSE, and Debian). For more details, please refer to the revised user manual (<https://github.com/hxmhuang/OpenArray/doc/>).

(2) I was conscious last time of the number of additional packages that I had to install before I could compile the programs. One of the problems seemed to be that the authors were use to using scripting packages, for example fypp, which are not usually used by the community running geophysical models. At the same time they were treating gcc, fortran, openmpi and netcdf as being special.

Response:

Thanks for your suggestions. We have removed the dependency of such packages from the release version of OpenArray.

(3) Another oddity was the use of pnetcdf, somewhat outdated, and a lack of specificity about which version of python or openmpi to use.

Response:

Thanks for your suggestions. We used pnetcdf at this moment. In the future version of OpenArray, a climate fast input/output (CFIO) library (Huang et.al, 2014) will be implemented to achieve better efficiency. OpenArray requires Open MPI v3.0.0 or later, as specified in the revised user manual. Python is not needed anymore by the release version.

(4) This time I started with a clean install of opensuse 15.1, the KDE desktop version. The use manual talks of compiling the various subroutine libraries etc, but my experience last time and with other systems is that each library usually requires at least one other library to be compiled and the whole process can take for ever.

Instead modern distributions use packages, installation of one package automatically installing any additional required packages. The authors need to revise their user manual to reflect this.

With opensuse 15.1 I could install packages:

gcc7-7.4.0, gcc7-fortran-7.4.0, gcc7-c++-7.4.0 (+ 12 packages)
openmpi1-gnu-hpd-devel (+13 packages)
pnetcdf (+26 packages)
armadillo-devel

To download from the git repository I also needed git:
git (+ 25 packages)

The system had python3 already installed. But script test.sh needed python. Other packages I found I had to install to get to the compile stage are:

python-base (+ 2 packages)
ctags
lua-luarocks
clang7 (+21 packages)

Additional packages were also installed but unfortunately it is only after installation that I can be sure that the package contains, for example the include file, that is needed. Time taken: parts of 4 days (probably about 10 hours).

Response:

We are very sorry for the problems you met. The release package is improved and robust. The configure file can detect the environment and generate corresponding Makefile, thus saving lots of trouble. We believe the installation of the revised OpenArray is much easier as we have tested on many platforms.

1 **OpenArray v1.0: A Simple Operator Library for the Decoupling of**

2 **Ocean Modelling and Parallel Computing**

3
4 Xiaomeng Huang^{1,2,3}, Xing Huang^{1,3}, Dong Wang^{1,3}, Qi Wu¹, Yi Li³, Shixun Zhang³,
5 Yuwen Chen¹, Mingqing Wang^{1,3}, Yuan Gao¹, Qiang Tang¹, Yue Chen¹, Zheng Fang¹,
6 Zhenya Song^{2,4}, Guangwen Yang^{1,3}

7
8 ¹ Ministry of Education Key Laboratory for Earth System Modeling, Department of
9 Earth System Science, Tsinghua University, Beijing 100084, China

10 ² Laboratory for Regional Oceanography and Numerical Modeling, Qingdao National
11 Laboratory for Marine Science and Technology, Qingdao, 266237, China

12 ³ National Supercomputing Center in Wuxi, Wuxi, 214011, China

13 ⁴ First Institute of Oceanography, Ministry of Natural Resources, Qingdao, 266061,
14 China

15
16 Corresponding author: hxm@tsinghua.edu.cn

17 **Abstract**

18 The rapidly evolving computational techniques are making a large gap between
19 scientific aspiration and code implementation in climate modelling. In this work, we
20 design a simple computing library to bridge the gap and decouple the work of ocean
21 modelling from parallel computing. This library provides twelve basic operators that
22 feature user-friendly interfaces, effective programming and implicit parallelism.
23 Several state-of-art computing techniques, including computing graph and Just-In-Time
24 compiling are employed to parallelize the seemingly serial code and speed up the ocean
25 models. These operator interfaces are designed using native Fortran programming
26 language to smooth the learning curve. We further implement a highly readable and
27 efficient ocean model that contains only 1860 lines of code but achieves a 91% parallel
28 efficiency in strong scaling and 99% parallel efficiency in weak scaling with 4096 Intel
29 CPU cores. This ocean model also exhibits excellent scalability on the heterogeneous

30 Sunway TaihuLight supercomputer. This work presents a promising alternative tool for
31 the development of ocean models.

32

33 **Keywords:** implicit parallelism, operator, ocean modelling, parallel computing

34 **1. Introduction**

35 Many earth system models have been developed in the past several decades to improve
36 the predictive understanding of the earth system (Bonan and Doney, 2018; Collins et
37 al., 2018; Taylor et al., 2012). These models are becoming increasingly complicated,
38 and the amount of code has expanded from a few thousand lines to tens of thousands,
39 or even millions of lines. In terms of software engineering, an increase in code causes
40 the models to be more difficult to develop and maintain.

41

42 The complexity of these models mainly originates from three aspects. First, more model
43 components and physical processes have been embedded into the earth system models,
44 leading to a tenfold increase in the amount of code (e.g., Alexander and Easterbrook,
45 2015). Second, some heterogeneous and advanced computing platforms (e.g.,
46 Lawrence et al., 2018) have been widely used by the climate modelling community,
47 resulting in a fivefold increase in the amount of code (e.g., Xu et al., 2015). Last, most
48 of the model programs need to be rewritten due to the continual development of novel
49 numerical methods and meshes. The promotion of novel numerical methods and
50 technologies produced in the fields of computational mathematics and computer
51 science have been limited in climate science because of the extremely heavy burden
52 caused by program rewriting and migration.

53

54 Over the next few decades, tremendous computing capacities will be accompanied by
55 more heterogeneous architectures which are equipped with two or more kinds of cores
56 or processing elements (Shan, 2006), thus making for a much more sophisticated
57 computing environment for climate modellers than ever before (Bretherton et al., 2012).
58 Clearly, transiting the current earth system models to the next generation of computing
59 environments will be highly challenging and disruptive. Overall, complex codes in
60 earth system models combined with rapidly evolving computational techniques create
61 a very large gap between scientific aspiration and code implementation in the climate
62 modelling community.

63

64 To reduce the complexity of earth system models and bridge this gap, a universal and
65 productive computing library is a promising solution. Through establishing an implicit
66 parallel and platform-independent computing library, the complex models can be
67 simplified and will no longer need explicit parallelism and transiting, thus effectively
68 decoupling the development of ocean models from complicated parallel computing
69 techniques and diverse heterogeneous computing platforms.

70

71 Many efforts have been made to address the complexity of parallel programming for
72 numerical simulations, such as operator overloading, source-to-source translator and
73 domain specific language (DSL). Operator overloading supports the customized data
74 type and provides simple operators and function interfaces to implement the model
75 algorithm. This technique is widely used because the implementation is straightforward
76 and easy to understand (Corliss and Griewank, 1994; Walther et al., 2003). However, it
77 is prone to work inefficiently because overloading execution induces numerous
78 unnecessary intermediate variables, consuming valuable memory bandwidth resources.
79 Using a source-to-source translator offers another solution. As indicated by the name,
80 this method converts one language, which is usually strictly constrained by self-defined
81 rules, to another (Bae et al., 2013; Lidman et al., 2012). It requires tremendous work to
82 develop and maintain a robust source-to-source compiler. Furthermore, DSLs can
83 provide high-level abstraction interfaces that use mathematical notations similar to
84 those used by domain scientists, so that they can write much more concise and more
85 straightforward code. Some outstanding DSLs, such as ATMOL (van Engelen, 2001),
86 ICON DSL (Torres et al., 2013), STELLA (Gysi et al., 2015) and ATLAS (Deconinck
87 et al., 2017), are used by the numerical model community. Although they seem source-
88 to-source technique, DSLs are newly-defined languages and produce executable
89 programs instead of target languages. Therefore the new syntax makes it difficult for
90 the modellers to master the DSLs. In addition, most DSLs are not yet supported by
91 robust compilers due to their relatively short history. Most of the source-to-source

92 translators and DSLs still do not support the rapidly evolving heterogeneous computing
93 platforms, such as the Chinese Sunway TaihuLight supercomputer which is based on
94 the homegrown Sunway heterogeneous many-core processors and located at the
95 National Supercomputing Center in Wuxi.

96

97 Other methods such as COARRAY Fortran and CPP templates provide alternative ways.
98 Using COARRAY Fortran, a modeller has to control the reading and writing operation
99 of each image (Mellor-Crummey et al., 2009). In a sense, one has to manipulate the
100 images in parallel instead of writing serial code. In term of CPP templates, it is usually
101 suitable for small code and difficult for debugging (Porkoláb et al., 2007).

102

103 Inspired by the philosophy of operator overloading, source-to-source translating and
104 DSLs, we integrated the advantages of these three methods into a simple computing
105 library which is called OpenArray. The main contributions of OpenArray are as follows:

- 106 • Easy-to-use. The modellers can write simple operator expressions in Fortran to
107 solve partial differential equations (PDEs). The entire program appears to be
108 serial and the modellers do not need to know any parallel computing techniques.
109 We summarized twelve basic generalized operators to support whole
110 calculations in a particular class of ocean models which use the finite difference
111 method and staggered grid.
- 112 • High efficiency. We adopt some advanced techniques, including intermediate
113 computation graphing, asynchronous communication, kernel fusion, loop
114 optimization, and vectorization, to decrease the consumption of memory
115 bandwidth and improve efficiency. Performance of the programs implemented
116 by OpenArray is similar to the original but manually optimized parallel program.
- 117 • Portability. Currently OpenArray supports both CPU and Sunway platforms.
118 More platforms including GPU will be supported in the future. The complexity
119 of cross-platform migration is moved from the models to OpenArray. The
120 applications based on OpenArray can then be migrated seamlessly to the

121 supported platforms.

122

123 Furthermore, we developed a numerical ocean model based on the Princeton Ocean
124 Model (POM, Blumberg and Mellor, 1987) to test the capability and efficiency of
125 OpenArray. The new model is called the Generalized Operator Model of the Ocean
126 (GOMO). Because the parallel computing details are completely hidden, GOMO
127 consists of only 1860 lines of Fortran code and is more easily understood and
128 maintained than the original POM. Moreover, GOMO exhibits excellent scalability and
129 portability on both central processing unit (CPU) and Sunway platforms.

130

131 The remainder of this paper is organized as follows. Section 2 introduces some concepts
132 and presents the detailed mathematical descriptions of formulating the PDEs into
133 operator expressions. Section 3 describes the detailed design and optimization
134 techniques of OpenArray. The implementation of GOMO is described in section 4.
135 Section 5 evaluates the performances of OpenArray and GOMO. Finally, discussion
136 and conclusion are given in section 6 and 7, respectively.

137

138 **2. Concepts of the Array, Operator, and Abstract Staggered Grid**

139 In this section, we introduce three important concepts in OpenArray: Array, Operator
140 and Abstract Staggered Grid to illustrate the design of OpenArray.

141

142 **2.1 Array**

143 To achieve this simplicity, we designed a derived data type, *Array*, which inspired our
144 project name, OpenArray. The new *Array* data type comprises a series of information,
145 including a 3-dimensional (3D) array to store data, a pointer to the computational grid,
146 a Message Passing Interface (MPI) communicator, the size of the halo region and other
147 information about the data distribution. All the information is used to manipulate the
148 *Array* as an object to simplify the parallel computing. In traditional ocean models,
149 calculations for each grid point and the i , j , and k loops in the horizontal and vertical

150 directions are unavoidable. The advantage of taking the *Array* as an object is the
 151 significant reduction in the number of loop operations in the models, making the code
 152 more intuitive and readable. When using the OpenArray library in a program, one can
 153 use *type(Array)* to declare new variables.

154

155 2.2 Operator

156 To illustrate the concept of an operator, we first take a 2-dimensional (2D) continuous
 157 equation solving sea surface elevation as an example:

$$158 \quad \frac{\partial \eta}{\partial t} + \frac{\partial DU}{\partial x} + \frac{\partial DV}{\partial y} = 0, \quad (1)$$

159 where η is the surface elevation, U and V are the zonal and meridional velocities, and
 160 D is the depth of the fluid column. We choose the finite difference method and staggered
 161 Arakawa C grid scheme, which are adopted by most regional ocean models. In Arakawa
 162 C grid, D is calculated at the centers, U component is calculated at the left and right
 163 side of the variable D , V component is calculated at the lower and upper side of the
 164 variable D (Fig. 1). Variables (D , U , V) located at different positions own different sets
 165 of grid increments. Taking the term $\frac{\partial DU}{\partial x}$ as an example, we firstly apply linear
 166 interpolation to obtain the D 's value at U point represented by $tmpD$. Through a
 167 backward difference to the product of $tmpD$ and U , then the discrete expression of $\frac{\partial DU}{\partial x}$
 168 can be obtained.

$$169 \quad tmpD(i+1,j) = 0.5*(D(i+1,j)+D(i,j))*U(i+1,j), \quad (2)$$

170 and

$$171 \quad \frac{\partial DU}{\partial x} = \frac{tmpD(i+1,j)-tmpD(i,j)}{dx(i,j)^*} = \frac{0.5*(D(i+1,j)+D(i,j))*U(i+1,j)-0.5*(D(i,j)+D(i-1,j))*U(i,j)}{dx(i,j)^*}, \quad (3)$$

172 where $dx(i,j)^* = 0.5*(dx(i,j) + dx(i-1,j))$.

173

174 In this way, the above continuous equation can be discretized into the following form.

$$175 \quad \frac{\eta_{t+1}(i,j)-\eta_{t-1}(i,j)}{2*dt} + \frac{0.5*(D(i+1,j)+D(i,j))*U(i+1,j)-0.5*(D(i,j)+D(i-1,j))*U(i,j)}{dx(i,j)^*} +$$

$$176 \quad \frac{0.5*(D(i,j+1)+D(i,j))*V(i,j+1)-0.5*(D(i,j)+D(i,j-1))*V(i,j)}{dy(i,j)^*} = 0, \quad (4)$$

177 where $dx(i,j)^* = 0.5 * (dx(i,j) + dx(i-1,j))$, $dy(i,j)^* = 0.5 * (dy(i,j) + dy(i,j-1))$,
 178 subscripts η_{t+1} and η_{t-1} denote the surface elevations at the $(t+1)$ time step and $(t-1)$ time
 179 step. To simplify the discrete form, we introduce some notation for the differentiation
 180 (δ_f^x, δ_b^y) and interpolation $(\overline{\overline{}}_f^x, \overline{\overline{}}_b^y)$. The δ and overbar symbols define the
 181 differential operator and average operator. The subscript x or y denotes that the
 182 operation acts in the x or y direction, and the superscript f or b denotes that the
 183 approximation operation is forward or backward.

184

185 Table 1 lists the detailed definitions of the twelve basic operators. The term *var* denotes
 186 a 3D model variable. All twelve operators for the finite difference calculations are
 187 named using three letters in the form [A|D][X|Y|Z][F|B]. The first letter contains two
 188 options, A or D, indicating an average or a differential operator. The second letter
 189 contains three options, X, Y or Z, representing the direction of the operation. The last
 190 letter contains two options, F or B, representing forward or backward operation. The
 191 dx , dy and dz are the distances between two adjacent grid points along the x , y and z
 192 directions.

193 Using the basic operators, Eq. (4) is expressed as:

$$194 \quad \frac{\eta_{t+1} - \eta_{t-1}}{2 * dt} + \delta_f^x (\overline{\overline{D}}_b^x * U) + \delta_f^y (\overline{\overline{D}}_b^y * V) = 0. \quad (5)$$

195 Thus,

$$196 \quad \eta_{t+1} = \eta_{t-1} - 2 * dt * \left(\delta_f^x (\overline{\overline{D}}_b^x * U) + \delta_f^y (\overline{\overline{D}}_b^y * V) \right). \quad (6)$$

197 Then, Eq. (6) can be easily translated into a line of code using operators (the bottom
 198 left panel in Fig. 2). Compared with the pseudo-codes (the right panel), the
 199 corresponding implementation by operators is more straightforward and more
 200 consistent with the equations.

201

202 Next, we will use the operators in shallow water equations, which are more complicated
 203 than those in the previous case. Assuming that the flow is in hydrostatic balance and
 204 that the density and viscosity coefficients are constant, and neglecting the molecular
 205 friction, the shallow water equations are:

$$206 \quad \frac{\partial \eta}{\partial t} + \frac{\partial DU}{\partial x} + \frac{\partial DV}{\partial y} = 0, \quad (7)$$

$$207 \quad \frac{\partial DU}{\partial t} + \frac{\partial DUU}{\partial x} + \frac{\partial DVU}{\partial y} - fVD = -gD \frac{\partial \eta}{\partial x} + \mu D \left(\frac{\partial^2 U}{\partial x^2} + \frac{\partial^2 U}{\partial y^2} \right), \quad (8)$$

$$208 \quad \frac{\partial DV}{\partial t} + \frac{\partial DUV}{\partial x} + \frac{\partial DVV}{\partial y} + fUD = -gD \frac{\partial \eta}{\partial y} + \mu D \left(\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} \right), \quad (9)$$

209 where f is the Coriolis parameter, g is the gravitational acceleration, and μ is the
 210 coefficient of kinematic viscosity. Using the Arakawa C grid and leapfrog time
 211 difference scheme, the discrete forms represented by operators are shown in Eq. (10) ~
 212 Eq. (12).

$$213 \quad \frac{\eta_{t+1} - \eta_{t-1}}{2*dt} + \delta_f^x (\bar{D}_b^x * U) + \delta_f^y (\bar{D}_b^y * V) = 0, \quad (10)$$

$$214 \quad \frac{D_{t+1}U_{t+1} - D_{t-1}U_{t-1}}{2*dt} + \delta_b^x (\overline{D_b^x * U}_f^x * \bar{U}_f^x) + \delta_f^y (\overline{D_b^y * V}_b^x * \bar{U}_b^y) - \overline{f \bar{V}_f^y * D}_b^x = -g *$$

$$215 \quad \bar{D}_b^x * \delta_b^x(\eta) + \mu * \bar{D}_b^x * \left(\delta_b^x (\delta_f^x (U_{t-1})) + \delta_f^y (\delta_b^y (U_{t-1})) \right), \quad (11)$$

$$216 \quad \frac{D_{t+1}V_{t+1} - D_{t-1}V_{t-1}}{2*dt} + \delta_f^x (\overline{D_b^x * U}_b^y * \bar{V}_b^x) + \delta_b^y (\overline{D_b^y * V}_f^y * \bar{V}_f^y) + \overline{f \bar{U}_f^x * D}_b^y = -g *$$

$$217 \quad \bar{D}_b^y * \delta_b^y(\eta) + \mu * \bar{D}_b^y * \left(\delta_f^x (\delta_b^x (V_{t-1})) + \delta_b^y (\delta_f^y (V_{t-1})) \right). \quad (12)$$

218 As the shallow water equations are solved, spatial average and differential operations
 219 are called repeatedly. Implementing these operations is troublesome and thus it is
 220 favourable to abstract these common operations from PDEs and encapsulate them into
 221 user-friendly, platform-independent, and implicit parallel operators. As shown in Fig.
 222 3, we require only 3 lines of code to solve the shallow water equations. This more
 223 realistic case suggests that even more complex PDEs can be constructed and solved by
 224 following this elegant approach.

225

226 **2.3 Abstract staggered grid**

227 Most ocean models are implemented based on the staggered Arakawa grids (Arakawa
 228 and Lamb, 1981; Griffies et al., 2000). The variables in ocean models are allocated at
 229 different grid points. The calculations that use these variables are performed after
 230 several reasonable interpolations or differences. When we call the differential
 231 operations on a staggered grid, the difference value between adjacent points should be
 232 divided by the grid increment to obtain the final result. Setting the correct grid
 233 increment for modellers is troublesome work that is extremely prone to error, especially

234 when the grid is nonuniform. Therefore, we propose an abstract staggered grid to
235 support flexible switching of operator calculations among different staggered grids.
236 When the grid information is provided at the initialization phase of OpenArray, a set of
237 grid increments, including horizontal increments ($dx(i,j)$, $dy(i,j)$) and vertical increment
238 ($dz(k)$), will be combined with each corresponding physical variable through grid
239 binding. Thus, the operators can implicitly set the correct grid increments for different
240 *Array* variables, even if the grid is nonuniform.

241

242 As shown in Fig. 4, the cubes in the (a), (b), (c), and (d) panels are the minimum abstract
243 grid accounting for 1/8 of the volume of the cube in Panel (e). The eight points of each
244 cube are numbered sequentially from 0 to 7, and each point has a set of grid increments,
245 i.e., dx , dy and dz . For example, all the variables of an abstract Arakawa A grid are
246 located at Point 3. For the Arakawa B grid, the horizontal velocity *Array* (U , V) is
247 located at Point 0, the temperature (T), the salinity (S), and the depth (D) are located at
248 Point 3, and the vertical velocity *Array* (W) is located at Point 7. For the Arakawa C
249 grid, *Array* U is located at Point 2 and *Array* V is located at Point 1. In contrast, for the
250 Arakawa D grid, *Array* U is located at Point 1 and *Array* V is located at Point 2.

251

252 When we call the average and differential operators mentioned in Table 1, for example,
253 on the abstract Arakawa C grid, the position of *Array* D is Point 3, and the average AXB
254 operator acting on *Array* D will change the position from Point 3 to Point 1. Since *Array*
255 U is also allocated at Point 1, the operation $AXB(D)*U$ is allowed. In addition, the
256 subsequent differential operator on *Array* $AXB(D)*U$ will change the position of *Array*
257 $DXF(AXB(D)*U)$ from Point 1 to Point 3.

258

259 The jumping rules of different operators are given in Table 2. Due to the design of the
260 abstract staggered grids, the jumping rules for the Arakawa A, B, C, and D grids are
261 fixed. A change in the position of an array is determined only by the direction of a
262 certain operator acting on that array.

263

264 If users change the Arakawa grid type, first the position information of each physical
 265 variable need to be reset (Shown in Fig. 4). Then the discrete form of each equation
 266 needs to be redesigned. We take the Eq. (1) switching from Arakawa C grid to Arakawa
 267 B grid as an example. The positions of the horizontal velocity *Array U* and *Array V* are
 268 changed to Point 0, *Array η* and *Array D* stay the same. The discrete form is changed
 269 from Eq. (4) to Eq. (13), the corresponding implementation by operators is changed
 270 from Eq. (6) to Eq. (14).

$$\begin{aligned}
 271 \quad & \frac{\eta_{t+1}(i,j) - \eta_{t-1}(i,j)}{2*dt} + \frac{0.25*(D(i+1,j)+D(i,j))*(U(i+1,j)+U(i+1,j+1)) - 0.25*(D(i,j)+D(i-1,j))*(U(i,j)+U(i,j+1))}{dx(i,j)*} + \\
 272 \quad & \frac{0.25*(D(i,j+1)+D(i,j))*(V(i,j+1)+V(i+1,j+1)) - 0.25*(D(i,j)+D(i,j-1))*(V(i,j)+V(i+1,j))}{dy(i,j)*} = 0, \\
 273 \quad & \hspace{15em} (13)
 \end{aligned}$$

$$274 \quad \eta_{t+1} = \eta_{t-1} - 2 * dt * \left(\delta_f^x \left(\bar{D}_b^x * \bar{U}_f^y \right) + \delta_f^y \left(\bar{D}_b^y * \bar{V}_f^x \right) \right). \quad (14)$$

275 The position information and jumping rules are used to implicitly check whether the
 276 discrete form of an equation is correct. The grid increments are hidden by all the
 277 differential operators, thus it makes the code simple and clean. In addition, since the
 278 rules are suitable for multiple staggered Arakawa grids, the modellers can flexibly
 279 switch the ocean model between different Arakawa grids. Notably, the users of
 280 OpenArray should input the correct positions of each array in the initialization phase.
 281 The value of the position is an input parameter when declaring an *Array*. An error will
 282 be reported if an operation is performed between misplaced points.

283

284 Although most of the existing ocean models use finite difference or finite volume
 285 methods on structured or semi-structured meshes (e.g., Blumberg and Mellor, 1987;
 286 Shchepetkin and McWilliams, 2005), there are still some ocean models using
 287 unstructured meshes (e.g., Chen et al., 2003; Korn, 2017), and even the spectral element
 288 method (e.g., Levin et al., 2000). In our current work, we design the basic operators
 289 only for finite difference and finite volume methods with structured grids. More
 290 customized operators for the other numerical methods and meshes will be implemented

291 in our future work.

292

293 **3. Design of OpenArray**

294 Through the above operator notations in Table 1, ocean modellers can quickly convert
295 the discrete PDE equations into the corresponding operator expression forms. The main
296 purpose of OpenArray is to make complex parallel programming transparent to the
297 modellers. As illustrated in Fig. 5, we use a computation graph as an intermediate
298 representation, meaning that the operator expression forms written in Fortran will be
299 translated into a computation graph with a particular data structure. In addition,
300 OpenArray will use the intermediate computation graph to analyse the dependency of
301 the distributed data and produce the underlying parallel code. Finally, we use stable and
302 mature compilers, such as the GNU Compiler Collection (GCC), Intel compiler (ICC),
303 and Sunway compiler (SWACC), to generate the executable programs according to
304 different backend platforms. These four steps and some related techniques are described
305 in detail in this section.

306

307 **3.1 Operator expression**

308 Although the basic generalized operators listed in Table 1 are only suitable to execute
309 first-order difference, other high-order difference or even more complicated operations
310 can be combined by these basic operators. For example, a second-order difference
311 operation can be expressed as $\delta_f^x(\delta_b^x(var))$. Supposing the grid distance is uniform,
312 the corresponding discrete form is $[var(i+1,j,k)+var(i-1,j,k) -2* var(i,j,k)] / dx^2$. In
313 addition, the central difference operation can be expressed as $(\delta_f^x(var) + \delta_b^x(var))/2$
314 since the corresponding discrete form is $[var(i+1,j,k)-var(i-1,j,k)] / 2dx$.

315

316 Using these operators to express the discrete PDE equation, the code and formula are
317 very similar. We call this effect “the self-documenting code is the formula”. Fig. 6
318 shows the one-to-one correspondence of each item in the code and the items in the sea
319 surface elevation equation. The code is very easy to program and understand. Clearly,

320 the basic operators and the combined operators greatly simplify the development and
321 maintenance of ocean models. The complicated parallel and optimization techniques
322 are hidden behind these operators. Modellers no longer need to care about details and
323 can escape from the “parallelism swamp”, and can therefore concentrate on the
324 scientific issues.

325

326 **3.2 Intermediate computation graph**

327 Considering the example mentioned in Fig. 6, if one needs to compute the term
328 $DXF(AXB(D)*u)$ with the traditional operator overloading method, one first computes
329 $AXB(D)$ and stores the result into a temporary array (named $tmp1$), and then executes
330 $(tmp1*u)$ and stores the result into a new array, $tmp2$. The last step is to compute
331 $DXF(tmp2)$ and store the result in a new array, $tmp3$. Numerous temporary arrays
332 consume a considerable amount of memory, making the efficiency of operator
333 overloading is poor.

334

335 To solve this problem, we convert an operator expression form into a directed and
336 acyclic graph, which consists of basic data and function nodes, to implement a so-called
337 lazy expression evaluation (Bloss et al., 1988; Reynolds, 1999). Unlike the traditional
338 operator overloading method, we overload all arithmetic functions to generate an
339 intermediate computation graph rather than to obtain the result of each function. This
340 method is widely used in deep learning frameworks, e.g., TensorFlow (Abadi et al.,
341 2016) and Theano (Bastien et al., 2012), to improve computing efficiency. Figure 7
342 shows the procedure of parsing the operator expression form of the sea level elevation
343 equation into a computation graph. The input variables in the square boxes include the
344 sea surface elevation (elb), the zonal velocity (u), the meridional velocity (v) and the
345 depth (D). $dt2$ is a constant equal to $2*dt$. The final output is the sea surface elevation
346 at the next time step (elf). The operators in the round boxes have been overloaded in
347 OpenArray. In summary, all the operators provided by OpenArray are functions for the
348 *Array* calculation, in which the “=” notation is the assignment function, the “-” notation
349 is the subtraction function, the “*” notation is the multiplication function, the “+”

350 notation is the addition function, DXF and DYF are the differential functions, and AXF
351 and AYP are the average functions.

352

353 **3.3 Code generation**

354 Given a computation graph, we design a lightweight engine to generate the
355 corresponding source code (Fig. 8). Each operator node in the computation graph is
356 called a kernel. The sequence of all kernels in a graph is usually fused into a large kernel
357 function. Therefore, the underlying engine schedules and executes the fused kernel once
358 and obtains the final result directly without any auxiliary or temporary variables.
359 Simultaneously, the scheduling overhead of the computation graph and the startup
360 overhead of the basic kernels can be reduced.

361

362 Most of the scientific computational applications are limited by the memory bandwidth
363 and cannot fully exploit the computing power of a processor. Fortunately, kernel fusion
364 is an effective optimization method to improve memory locality. When two kernels
365 need to process some data, their fusion holds shared data in the memory. Prior to the
366 kernel fusion, the computation graph is analysed to find the operator nodes that can be
367 fused, and the analysis results are stored in several subgraphs. Users can access to any
368 individual subgraph by assigning the subgraph to an intermediate variable for
369 diagnostic purposes. After being given a series of subgraphs, the underlying engine
370 dynamically generates the corresponding kernel function in C++ using just-in-time (JIT)
371 compilation techniques (Suganuma and Yasue, 2005). The JIT compiler used in
372 OpenArray can fuse numbers of operators into a large compiled kernel. The benefit of
373 fusing operators is to alleviate memory bandwidth limitations and improve performance
374 compared with executing operators one-by-one. In order to generate a kernel function
375 based on a subgraph, we first add the function header and variable definitions according
376 to the name and type in the *Array* structure. And then we add the loop head through the
377 dimension information. Finally, we perform a depth-first walk on the expression tree to
378 convert data, operators, and assignment nodes into a complete expression including

379 load variables, arithmetic operation, and equal symbol with C++ language.

380

381 Notably, the time to compile a single kernel function is short, but practical applications
382 usually need to be run for thousands of time steps, and the overhead of generating and
383 compiling the kernel functions for the computation graph is extremely high. Therefore,
384 we generate a fusion kernel function only once for each subgraph, and put it into a
385 function pool. Later, when facing the same computation subgraph, we fetch the
386 corresponding fusion kernel function directly from the pool.

387

388 Since the arrays in OpenArray are distributed among different processing units, and the
389 operator needs to use the data in the neighbouring points, in order to ensure the
390 correctness, it is necessary to check the data consistency before fusion. The use of
391 different data splitting methods for distributed arrays can greatly affect computing
392 performance. The current data splitting method in OpenArray is the widely used block-
393 based strategy. Solving PDEs on structured grids often divides the simulated domain
394 into blocks that are distributed to different processing units. However, the differential
395 and average operators always require their neighbouring points to perform array
396 computations. Clearly, ocean modellers have to frequently call corresponding functions
397 to carefully control the communication of the local boundary region.

398

399 Therefore, we implemented a general boundary management module to implicitly
400 maintain and update the local boundary information so that the modellers no longer
401 need to address the message communication. The boundary management module uses
402 asynchronous communication to update and maintain the data of the boundary region,
403 which is useful for simultaneous computing and communication. These procedures of
404 asynchronous communication are implicitly invoked when calling the basic kernel or
405 the fused kernel to ensure that the parallel details are completely transparent to the
406 modellers. For the global boundary conditions of the limited physical domains, the
407 values at the physical border are always set to zero within the operators and operator

408 expressions. In realistic cases, the global boundary conditions are set by a series of
409 functions (e.g., radiation, wall) provided by OpenArray.

410

411 **3.4 Portable program for different backend platforms**

412 With the help of dynamic code generation and JIT compilation technology, OpenArray
413 can be migrated to different backend platforms. Several basic libraries, including Boost
414 C++ libraries and Armadillo library, are required. The JIT compilation module is based
415 on Low-Level-Virtual-Machine (LLVM), thus theoretically the module can only be
416 ported to platforms supporting LLVM. If LLVM is not supported, as on the Sunway
417 platform, one can generate the fusion kernels in advance by running the ocean model
418 on an X86 platform. If the target platform is CPUs with acceleration cards, such as GPU
419 clusters, it is necessary to add control statements in the CPU code, including data
420 transmission, calculation, synchronous and asynchronous statements. In addition, the
421 accelerating solution should involve the selection of the best parameters, for example
422 “blockDim” and “gridDim” on GPU platforms. In short, the code generation module of
423 OpenArray also needs to be refactored to be able to generate codes for different backend
424 platforms. The application based on OpenArray can then be migrated seamlessly to the
425 target platform. Currently, we have designed the corresponding source code generation
426 module for Intel CPU and Sunway processors in OpenArray.

427

428 According to the TOP500 list released in November 2018, the Sunway TaihuLight is
429 ranked third in the world, with a LINPACK benchmark rating of 93 Petaflops provided
430 by Sunway many-core processors (or Sunway CPUs). As shown in Fig. 9, every
431 Sunway CPU includes 260 processing elements (or cores) that are divided into 4 core-
432 groups. Each core-group consists of 64 computing processing elements (CPEs) and a
433 management processing element (MPE) (Qiao et al., 2017). CPEs handle large-scale
434 computing tasks and MPE is responsible for the task scheduling and communication.
435 The relationship between MPE and CPE is like that between CPU and many-core
436 accelerator, except for they are fused into a single Sunway processor sharing a unified

437 memory space. To make the most of the computing resources of the Sunway TaihuLight,
438 we generate kernel functions for the MPE, which is responsible for the thread control,
439 and CPE, which performs the computations. The kernel functions are fully optimized
440 with several code optimization techniques (Pugh, 1991) such as loop tiling, loop
441 aligning, single-instruction multiple-data (SIMD) vectorization, and function inline. In
442 addition, due to the high memory access latency of CPEs, we accelerate data access by
443 providing instructions for direct memory access in the kernel to transfer data between
444 the main memory and local memory (Fu et al., 2017).

445

446 **4. Implementation of GOMO**

447 In this section, we introduce how to implement a numerical ocean model using
448 OpenArray. The most important step is to derive the primitive discrete governing
449 equations in operator expression form, then the following work is completed by
450 OpenArray.

451

452 The fundamental equations of GOMO are derived from POM. GOMO features a
453 bottom-following, free-surface, staggered Arakawa C grid. To effectively evolve the
454 rapid surface fluctuations, GOMO uses the mode-splitting algorithm inherited from
455 POM to address the fast propagating surface gravity waves and slow propagating
456 internal waves in barotropic (external) and baroclinic (internal) modes, respectively.
457 The details of the continuous governing equations, the corresponding operator
458 expression form and the descriptions of all the variables used in GOMO are listed in
459 the Appendix A, Appendix B, and Appendix C, respectively.

460

461 Figure 10 shows the basic flow diagram of GOMO. At the beginning, we initialize
462 OpenArray to make all operators suitable for GOMO. After loading the initial values
463 and the model parameters, the distance information is input into the differential
464 operators through grid binding. In the external mode, the main consumption is
465 computing the 2D sea surface elevation η and column-averaged velocity (Ua, Va). In

466 the internal mode, 3D array computations predominate in order to calculate baroclinic
467 motions (U, V, W), tracers (T, S, ρ), and turbulence closure scheme (q^2, q^2l) (Mellor and
468 Yamada, 1982), where (U, V, W) are the velocity fields in the x, y and σ directions, ($T,$
469 S, ρ) are the potential temperature, the salinity and the density. ($q^2/2, q^2l/2$) are the
470 turbulence kinetic energy and production of turbulence kinetic energy with turbulence
471 length scale.

472

473 When the user dives into the GOMO code, the main time stepping loop in GOMO
474 appears to run on a single processor. However, as described above, implicit parallelism
475 is the most prominent feature of the program using OpenArray. The operators in
476 OpenArray, not only the difference and average operators, but also the “+”, “-”, “*”, “/”
477 and “=” operators in the Fortran code, are all overloaded for the special data structure
478 “Array”. The seemingly serial Fortran code is implicitly converted to parallel C++ code
479 by OpenArray, and the parallelization is hidden from the modellers.

480

481 Because the complicated parallel optimization and tuning processes are decoupled from
482 the ocean modelling, we completely implemented GOMO based on OpenArray in only
483 4 weeks, whereas implementation may take several months or even longer when using
484 the MPI or CUDA library.

485

486 In comparison with the existing POM and its multiple variations, to name a few, Stony
487 Brook Parallel Ocean Model (sbPOM), mpiPOM and POMgpu, GOMO has less code
488 but is more powerful in terms of compatibility. As shown in Table 3, the serial version
489 of POM (POM2k) contains 3521 lines of code. sbPOM and mpiPOM are parallelized
490 using MPI, while POMgpu is based on MPI and CUDA-C. The codes of sbPOM,
491 mpiPOM and POMgpu are extended to 4801, 9680 and 30443 lines. In contrast, the
492 code of GOMO is decreased to 1860 lines. Moreover, GOMO completes the same
493 function as the other approaches while using the least amount of code (Table 4), since
494 the complexity has been transferred to OpenArray, which includes about 11,800 lines

495 of codes.

496

497 In addition, poor portability considerably restricts the use of advanced hardware in
498 oceanography. With the advantages of OpenArray, GOMO is adaptable to different
499 hardware architectures, such as the Sunway processor. The modellers do not need to
500 modify any code when changing platforms, eliminating the heavy burden of
501 transmitting code. As computing platforms become increasingly diverse and complex,
502 GOMO becomes more powerful and attractive than the machine-dependent models.

503

504 **5. Results**

505 In this section, we first evaluate the basic performance of OpenArray using benchmark
506 tests on a single CPU platform. After checking the correctness of GOMO through an
507 ideal seamount test case, we use GOMO to further test the scalability and efficiency of
508 OpenArray.

509

510 **5.1 Benchmark testing**

511 We choose two typical PDEs and their implementations from Rodinia v3.1, which is a
512 benchmark suite for heterogeneous computing (Che et al., 2009), as the original version.
513 For comparison, we re-implement these two PDEs using OpenArray. In addition, we
514 added two other test cases. As shown in Table 5, the 2D continuity equation is used to
515 solve sea surface height, and its continuous form is shown in Eq. (1). The 2D heat
516 diffusion equation is a parabolic PDE that describes the distribution of heat over time
517 in a given region. Hotspot is a thermal simulation used for estimating processor
518 temperature on structured grids (Che et al., 2009; Huang et al., 2006). We tested one
519 2D case (Hotspot2D) and one 3D case (Hotspot3D) of this program. The average
520 runtime for 100 iterations is taken as the performance metric. All tests are executed on
521 a single workstation with an Intel Xeon E5-2650 CPU. The experimental results show
522 that the performance of OpenArray versions is comparable to the original versions.

523

524 **5.2 Validation tests of GOMO**

525 The seamount problem proposed by Beckman and Haidvogel is a widely used ideal test
526 case for regional ocean models (Beckmann and Haidvogel, 1993). It is a stratified
527 Taylor column problem, which simulates the flow over an isolated seamount with a
528 constant salinity and a reference vertical temperature stratification. An eastward
529 horizontal current of 0.1 m/s is added at model initialization. The southern and northern
530 boundaries are closed. If the Rossby number is small, an obvious anticyclonic
531 circulation is trapped by the mount in the deep water.

532

533 Using the seamount test case, we compare GOMO and sbPOM results. The
534 configurations of both models are exactly the same. Figure 11 shows that GOMO and
535 sbPOM both capture the anticyclonic circulation at 3500 metres depth. The shaded plot
536 shows the surface elevation, and the array plot shows the current at 3500 metres. Figure
537 11(a), 11(b), and 11(c) are the results of GOMO, sbPOM, and the difference (GOMO-
538 sbPOM), respectively. The differences in the surface elevation and deep currents
539 between the two models are negligible (Fig. 11(c)).

540

541 **5.3 The weak and strong scalability of GOMO**

542 The seamount test case is used to compare the performance of sbPOM and GOMO in
543 a parallel environment. We use the X86 cluster at National Supercomputing Center in
544 Wuxi of China, which provides 5000 Intel Xeon E5-2650 v2 CPUs for our account at
545 most. Figure 12(a) shows the result of a strong scaling evaluation, in which the model
546 size is fixed at $2048 \times 2048 \times 50$. The dashed line indicates the ideal speedup. For the
547 largest parallelisms with 4096 processes, GOMO and sbPOM achieve 91% and 92%
548 parallel efficiency, respectively. Figure 12(b) shows the weak scalability of sbPOM and
549 GOMO. In the weak scaling test, the model size for each process is fixed at $128 \times 128 \times 50$,
550 and the number of processes is gradually increased from 16 to 4096. Taking the
551 performance of 16 processes as a baseline, we determine that the parallel efficiencies
552 of GOMO and sbPOM using 4096 processes are 99.0% and 99.2%, respectively.

553

554 **5.4 Testing on the Sunway platform**

555 We also test the scalability of GOMO on the Sunway platform. Supposing that the
556 baseline is the runtime of GOMO at 10000 Sunway cores with a grid size of
557 $4096 \times 4096 \times 50$, the parallel efficiency of GOMO can still reach 85% at 150000 cores,
558 as shown in Fig. 13. However, we notice that the scalability declines sharply when the
559 number of cores exceeds 150000. There are two reasons leading to this decline. First,
560 the block size assigned to each core decreases as the number of cores increases, causing
561 more communication during boundary region updating. Second, some processes cannot
562 be accelerated even though more computing resources are available; for example, the
563 time spent on creating the computation graph, generating the fusion kernels, and
564 compiling the JIT cannot be reduced. Even though the fusion-kernel codes are
565 generated and compiled only once at the beginning of a job, it consumes about 2
566 minutes. In a sense, OpenArray performs better when processing large-scale data, and
567 GOMO is more suitable for high-resolution scenarios. In the future, we will further
568 optimize the communication and graph-creating modules to improve the efficiency for
569 large-scale cores.

570

571 **6. Discussion**

572 As we mentioned in Section 1, the advantages of OpenArray are easy-to-use, high
573 efficiency and portability. Using OpenArray, the modellers without any parallel
574 computing skill and experience can write simple operator expressions in Fortran to
575 implement complex ocean models. The ocean models can be run on any CPU and
576 Sunway platforms which have deployed the OpenArray library. We call this effect
577 “write once, run everywhere”. Other similar libraries (e.g., ATMOL, ICON DSL, and
578 STELLA, COARRAY) require the users to manually control the boundary
579 communication and task scheduling to some extent. In contrast, OpenArray implements
580 completely implicit parallelism with user-friendly interfaces and programming
581 languages.

582

583 However, there are still several problems to be solved in the development of OpenArray.
584 The first issue is computational efficiency. Once a variable is in one of the processor
585 registers or in the highest speed cache, it should be used as much as possible before
586 being replaced. In fact, we should never to move variables more than once each
587 timestep. The memory consumption brought by overloading techniques is usually high
588 due to the unnecessary variable moving and unavoidable cache missing. The current
589 efficiency and scalability of GOMO are close to sbPOM, since we have adopted a series
590 of optimization methods, such as memory pool, graph computing, JIT compilation, and
591 vectorization, to alleviate the requirement of memory bandwidth. However, we have to
592 admit that we cannot fully solve the memory bandwidth limited problem at present. We
593 think that time skewing is a cache oblivious algorithm for stencil computations (Frigo
594 and Strumpen, 2005), since it can exploit temporal locality optimally throughout the
595 entire memory hierarchy. In addition, the polyhedral model may be another potential
596 approach, which uses an abstract mathematical representation based on integer
597 polyhedral, to analyze and optimize the memory access pattern of a program.

598

599 The second issue is that the current OpenArray version cannot support customized
600 operators. When modellers try out another higher-order advection or any other
601 numerical scheme, the twelve basic operators provided by OpenArray are not abundant.
602 We consider using a template mechanism to support the customized operators. The
603 rules of operations are defined in a template file, where the calculation form of each
604 customized operator is described by a regular expression. If users want to add a
605 customized operator, they only need to append a regular expression into the template
606 file.

607

608 OpenArray and GOMO will continue to be developed, and the following three key
609 improvements are planned for the following years.

610

611 First, we are developing the GPU version of OpenArray. During the development, the
612 principle is to keep hot data staying in GPU memory or directly swapping between
613 GPUs and avoid returning data to the main CPU memory. NVLink provides high
614 bandwidth and outstanding scalability for GPU-to-CPU or GPU-to-GPU
615 communication, and addresses the interconnect issue for multi-GPU and multi-
616 GPU/CPU systems.

617

618 Second, the data Input/Output is becoming a bottleneck of earth system models as the
619 resolution increases rapidly. At present we encapsulate the PnetCDF library to provide
620 simple I/O interfaces, such as load operation and store operation. A climate fast
621 input/output (CFIO) library (Huang et al., 2014) will be implemented into OpenArray
622 in the next few years. The performance of CFIO is approximately 220% faster than
623 PnetCDF because of the overlapping of I/O and computing. CFIO will be merged into
624 the future version of OpenArray and the performance is expected to be further improved.

625

626 Finally, as most of the ocean models, GOMO also faces the load imbalance issue. We
627 are adding the more effective load balance schemes, including space-filling curve
628 (Dennis, 2007) and curvilinear orthogonal grids, into OpenArray in order to reduce the
629 computational cost on land points.

630

631 OpenArray is a product of collaboration between oceanographers and computer
632 scientists. It plays an important role to simplify the porting work on the Sunway
633 TaihuLight supercomputer. We believe that OpenArray and GOMO will continue to be
634 maintained and upgraded. We aim to promote it to the model community as a
635 development tool for future numerical models.

636

637 **7. Conclusion**

638 In this paper, we design a simple computing library (OpenArray) to decouple ocean
639 modelling and parallel computing. OpenArray provides twelve basic operators that are

640 abstracted from PDEs and extended to ocean model governing equations. These
641 operators feature user-friendly interfaces and an implicit parallelization ability.
642 Furthermore, some state-of-art optimization mechanisms, including computation
643 graphing, kernel fusion, dynamic source code generation and JIT compiling, are applied
644 to boost the performance. The experimental results prove that the performance of a
645 program using OpenArray is comparable to that of well-designed programs using
646 Fortran. Based on OpenArray, we implement a numerical ocean model (GOMO) with
647 high productivity, enhanced readability and excellent scalable performance. Moreover,
648 GOMO shows high scalability on both CPU and the Sunway platform. Although more
649 realistic tests are needed, OpenArray may signal the beginning of a new frontier in
650 future ocean modelling through ingesting basic operators and cutting-edge computing
651 techniques.

652

653 *Code availability.* The source codes of OpenArray v1.0 is available at
654 https://github.com/hxmhuang/OpenArray_CXX, and the user manual of OpenArray
655 can be accessed at https://github.com/hxmhuang/OpenArray_CXX/tree/master/doc.
656 GOMO is available at <https://github.com/hxmhuang/GOMO>.

657

658 **Appendix A: Continuous governing equations**

659 The equations governing the baroclinic (internal) mode in GOMO are the 3-
660 dimensional hydrostatic primitive equations.

$$661 \quad \frac{\partial \eta}{\partial t} + \frac{\partial UD}{\partial x} + \frac{\partial VD}{\partial y} + \frac{\partial W}{\partial \sigma} = 0, \quad (\text{A1})$$

$$662 \quad \frac{\partial UD}{\partial t} + \frac{\partial U^2 D}{\partial x} + \frac{\partial UV D}{\partial y} + \frac{\partial UW}{\partial \sigma} - fVD + gD \frac{\partial \eta}{\partial x} = \frac{\partial}{\partial \sigma} \left(\frac{K_M}{D} \frac{\partial U}{\partial \sigma} \right) +$$

$$663 \quad \frac{gD^2}{\rho_0} \frac{\partial}{\partial x} \int_{\sigma}^0 \rho d\sigma' - \frac{gD}{\rho_0} \frac{\partial D}{\partial x} \int_{\sigma}^0 \sigma' \frac{\partial \rho}{\partial \sigma'} d\sigma' + F_u, \quad (\text{A2})$$

$$664 \quad \frac{\partial VD}{\partial t} + \frac{\partial UV D}{\partial x} + \frac{\partial V^2 D}{\partial y} + \frac{\partial VW}{\partial \sigma} + fUD + gD \frac{\partial \eta}{\partial y} = \frac{\partial}{\partial \sigma} \left(\frac{K_M}{D} \frac{\partial V}{\partial \sigma} \right) +$$

$$665 \quad \frac{gD^2}{\rho_0} \frac{\partial}{\partial y} \int_{\sigma}^0 \rho d\sigma' - \frac{gD}{\rho_0} \frac{\partial D}{\partial y} \int_{\sigma}^0 \sigma' \frac{\partial \rho}{\partial \sigma'} d\sigma' + F_v, \quad (\text{A3})$$

$$666 \quad \frac{\partial TD}{\partial t} + \frac{\partial TUD}{\partial x} + \frac{\partial TVD}{\partial y} + \frac{\partial TW}{\partial \sigma} = \frac{\partial}{\partial \sigma} \left(K_H \frac{\partial T}{\partial \sigma} \right) + F_T + \frac{\partial R}{\partial \sigma}, \quad (\text{A4})$$

$$667 \quad \frac{\partial SD}{\partial t} + \frac{\partial SUD}{\partial x} + \frac{\partial SVD}{\partial y} + \frac{\partial SW}{\partial \sigma} = \frac{\partial}{\partial \sigma} \left(K_H \frac{\partial S}{\partial \sigma} \right) + F_S, \quad (\text{A5})$$

$$668 \quad \rho = \rho(T, S, p), \quad (\text{A6})$$

$$669 \quad \frac{\partial q^2 D}{\partial t} + \frac{\partial U q^2 D}{\partial x} + \frac{\partial V q^2 D}{\partial y} + \frac{\partial W q^2}{\partial \sigma} = \frac{\partial}{\partial \sigma} \left(\frac{K_q}{D} \frac{\partial q^2}{\partial \sigma} \right) + \frac{2K_M}{D} \left[\left(\frac{\partial U}{\partial \sigma} \right)^2 + \left(\frac{\partial V}{\partial \sigma} \right)^2 \right] +$$

$$670 \quad \frac{2g}{\rho_0} K_H \frac{\partial \rho}{\partial \sigma} - \frac{2Dq^3}{B_1 l} + F_{q^2}, \quad (\text{A7})$$

$$671 \quad \frac{\partial q^2 l D}{\partial t} + \frac{\partial U q^2 l D}{\partial x} + \frac{\partial V q^2 l D}{\partial y} + \frac{\partial W q^2 l}{\partial \sigma} = \frac{\partial}{\partial \sigma} \left(\frac{K_q}{D} \frac{\partial q^2 l}{\partial \sigma} \right) + E_1 l \left\{ \frac{K_M}{D} \left[\left(\frac{\partial U}{\partial \sigma} \right)^2 + \right. \right.$$

$$672 \quad \left. \left. \left(\frac{\partial V}{\partial \sigma} \right)^2 \right] + \frac{gE_3}{\rho_0} K_H \frac{\partial \rho}{\partial \sigma} \right\} \tilde{W} - \frac{Dq^3}{B_1} + F_{q^2 l}, \quad (\text{A8})$$

673

674 where F_u , F_v , F_{q^2} , and $F_{q^2 l}$ are horizontal kinematic viscosity terms of u , v , q^2 , and
675 $q^2 l$, respectively. F_T and F_S are horizontal diffusion terms of T and S respectively. \tilde{W}
676 is the wall proximity function.

$$677 \quad F_u = \frac{\partial}{\partial x} (2A_M D \frac{\partial U}{\partial x}) + \frac{\partial}{\partial y} \left[A_M D \left(\frac{\partial U}{\partial y} + \frac{\partial V}{\partial x} \right) \right], \quad (\text{A9})$$

$$678 \quad F_v = \frac{\partial}{\partial y} (2A_M D \frac{\partial V}{\partial y}) + \frac{\partial}{\partial x} \left[A_M D \left(\frac{\partial U}{\partial y} + \frac{\partial V}{\partial x} \right) \right], \quad (\text{A10})$$

$$679 \quad F_T = \frac{\partial}{\partial x} (A_H H \frac{\partial T}{\partial x}) + \frac{\partial}{\partial y} (A_H H \frac{\partial T}{\partial y}), \quad (\text{A11})$$

$$680 \quad F_S = \frac{\partial}{\partial x} (A_H H \frac{\partial S}{\partial x}) + \frac{\partial}{\partial y} (A_H H \frac{\partial S}{\partial y}), \quad (\text{A12})$$

$$681 \quad F_{q^2} = \frac{\partial}{\partial x} (A_M H \frac{\partial q^2}{\partial x}) + \frac{\partial}{\partial y} (A_M H \frac{\partial q^2}{\partial y}), \quad (\text{A13})$$

$$682 \quad F_{q^2 l} = \frac{\partial}{\partial x} (A_M H \frac{\partial q^2 l}{\partial x}) + \frac{\partial}{\partial y} (A_M H \frac{\partial q^2 l}{\partial y}), \quad (\text{A14})$$

$$683 \quad \tilde{W} = 1 + \frac{E_2 l}{\kappa} \left(\frac{1}{\eta - z} + \frac{1}{H - z} \right). \quad (\text{A15})$$

684 The equations governing the barotropic (external) mode in GOMO are obtained by
685 vertically integrating the baroclinic equations.

$$686 \quad \frac{\partial \eta}{\partial t} + \frac{\partial U_{AD}}{\partial x} + \frac{\partial V_{AD}}{\partial y} = 0, \quad (\text{A16})$$

$$687 \quad \frac{\partial U_{AD}}{\partial t} + \frac{\partial (U_A)^2 D}{\partial x} + \frac{\partial U_A V_{AD}}{\partial y} - f V_{AD} + g D \frac{\partial \eta}{\partial x} = \tilde{F}_{u_a} - wu(0) +$$

$$688 \quad wu(-1) - \frac{gD}{\rho_0} \int_{-1}^0 \int_{\sigma}^0 \left[D \frac{\partial \rho}{\partial x} - \frac{\partial D}{\partial x} \sigma' \frac{\partial \rho}{\partial \sigma} \right] d\sigma' d\sigma + G_{u_a}, \quad (\text{A17})$$

$$689 \quad \frac{\partial V_{AD}}{\partial t} + \frac{\partial U_A V_{AD}}{\partial y} + \frac{\partial (V_A)^2 D}{\partial y} + f U_{AD} + g D \frac{\partial \eta}{\partial y} = \tilde{F}_{v_a} - wv(0) +$$

$$690 \quad wv(-1) - \frac{gD}{\rho_0} \int_{-1}^0 \int_{\sigma}^0 \left[D \frac{\partial \rho}{\partial y} - \frac{\partial D}{\partial y} \sigma' \frac{\partial \rho}{\partial \sigma} \right] d\sigma' d\sigma + G_{v_a}, \quad (\text{A18})$$

691

692 where \tilde{F}_{u_a} and \tilde{F}_{v_a} are the horizontal kinematic viscosity terms of U_A and V_A
693 respectively. G_{u_a} and G_{v_a} are the dispersion terms of U_A and V_A respectively. The
694 subscript 'A' denotes vertical integration.

695

$$696 \quad \tilde{F}_{u_a} = \frac{\partial}{\partial x} \left[2H(AA_M) \frac{\partial U_A}{\partial x} \right] + \frac{\partial}{\partial y} \left[H(AA_M) \left(\frac{\partial U_A}{\partial y} + \frac{\partial V_A}{\partial x} \right) \right], \quad (\text{A19})$$

$$697 \quad \tilde{F}_{v_a} = \frac{\partial}{\partial y} \left[2H(AA_M) \frac{\partial V_A}{\partial y} \right] + \frac{\partial}{\partial x} \left[H(AA_M) \left(\frac{\partial U_A}{\partial y} + \frac{\partial V_A}{\partial x} \right) \right], \quad (\text{A20})$$

$$698 \quad G_{u_a} = \frac{\partial^2 (U_A)^2 D}{\partial x^2} + \frac{\partial^2 U_A V_A D}{\partial x \partial y} - \tilde{F}_{u_a} - \frac{\partial^2 (U^2)_{AD}}{\partial x^2} - \frac{\partial^2 (UV)_{AD}}{\partial y^2} + (F_u)_A, \quad (\text{A21})$$

$$699 \quad G_{v_a} = \frac{\partial^2 U_A V_A D}{\partial x \partial y} + \frac{\partial^2 (V_A)^2 D}{\partial y^2} - \tilde{F}_{v_a} - \frac{\partial^2 (UV)_{AD}}{\partial x^2} - \frac{\partial^2 (V^2)_{AD}}{\partial y^2} + (F_v)_A, \quad (\text{A22})$$

$$700 \quad U_A = \int_{-1}^0 U d\sigma, \quad (\text{A23})$$

$$701 \quad V_A = \int_{-1}^0 V d\sigma, \quad (\text{A24})$$

$$702 \quad (U^2)_A = \int_{-1}^0 U^2 d\sigma, \quad (\text{A25})$$

$$703 \quad (UV)_A = \int_{-1}^0 UV d\sigma, \quad (\text{A26})$$

$$704 \quad (V^2)_A = \int_{-1}^0 V^2 d\sigma, \quad (\text{A27})$$

$$705 \quad (F_u)_A = \int_{-1}^0 F_u d\sigma, \quad (\text{A28})$$

$$706 \quad (F_v)_A = \int_{-1}^0 F_v d\sigma, \quad (\text{A29})$$

$$707 \quad AA_M = \int_{-1}^0 (A_M) d\sigma. \quad (\text{A30})$$

708

709 **Appendix B: Discrete governing equations**

710 The discrete governing equations of baroclinic (internal) mode expressed by operators
711 are shown as below:

$$712 \quad \frac{\eta^{t+1} - \eta^{t-1}}{2dti} + \delta_f^x (\bar{D}_b^x U) + \delta_f^y (\bar{D}_b^y V) + \delta_f^z (W) = 0, \quad (\text{B1})$$

$$\begin{aligned}
713 \quad & \frac{(\overline{D_b^x U})^{t+1} - (\overline{D_b^x U})^{t-1}}{2dti} + \delta_b^x \left[\overline{(\overline{D_b^x U})_f \overline{U}_f^x} \right] + \delta_f^y \left[\overline{(\overline{D_b^y V})_b \overline{U}_b^y} \right] + \\
714 \quad & \delta_f^z \left(\overline{W_b^x \overline{U}_b^z} - \overline{(\tilde{f} \overline{V}_f^y D)_b} - \overline{(\tilde{f} \overline{V}_f^y D)_b} + g \overline{D_b^x} \delta_b^x(\eta) \right) = \delta_b^z \left[\frac{K_{M_b}^x}{(\overline{D_b^x})^{t+1}} \delta_f^z(U^{t+1}) \right] + \\
715 \quad & \frac{g(\overline{D_b^x})^2}{\rho_0} \int_{\sigma}^0 \left[\delta_b^x(\overline{\rho}_b^z) - \frac{\sigma}{\overline{D_b^x}} \delta_b^x(D) \delta_b^z(\overline{\rho}_b^x) \right] d\sigma' + F_u, \tag{B2}
\end{aligned}$$

$$\begin{aligned}
716 \quad & \frac{(\overline{D_b^y V})^{t+1} - (\overline{D_b^y V})^{t-1}}{2dti} + \delta_f^x \left[\overline{(\overline{D_b^x U})_b \overline{V}_b^x} \right] + \delta_b^y \left[\overline{(\overline{D_b^y V})_f \overline{V}_f^y} \right] + \\
717 \quad & \delta_f^z \left(\overline{W_b^y \overline{V}_b^z} + \overline{(\tilde{f} \overline{U}_f^x D)_b} + \overline{(\tilde{f} \overline{U}_f^x D)_b} + g \overline{D_b^y} \delta_b^y(\eta) \right) = \delta_b^z \left[\frac{K_{M_b}^y}{(\overline{D_b^y})^{t+1}} \delta_f^z(V^{t+1}) \right] + \\
718 \quad & \frac{g(\overline{D_b^y})^2}{\rho_0} \int_{\sigma}^0 \left[\delta_b^y(\overline{\rho}_b^z) - \frac{\sigma}{\overline{D_b^y}} \delta_b^y(D) \delta_b^z(\overline{\rho}_b^y) \right] d\sigma' + F_v, \tag{B3}
\end{aligned}$$

$$\begin{aligned}
719 \quad & \frac{(TD)^{t+1} - (TD)^{t-1}}{2dti} + \delta_f^x(\overline{T}_b^x U \overline{D}_b^x) + \delta_f^y(\overline{T}_b^y V \overline{D}_b^y) + \delta_f^z(\overline{T}_b^z W) = \\
720 \quad & \delta_b^z \left[\frac{K_H}{D^{t+1}} \delta_f^z(T^{t+1}) \right] + F_T + \delta_f^z R, \tag{B4}
\end{aligned}$$

$$\begin{aligned}
721 \quad & \frac{(SD)^{t+1} - (SD)^{t-1}}{2dti} + \delta_f^x(\overline{S}_b^x U \overline{D}_b^x) + \delta_f^y(\overline{S}_b^y V \overline{D}_b^y) + \delta_f^z(\overline{S}_b^z W) = \\
722 \quad & \delta_b^z \left[\frac{K_H}{D^{t+1}} \delta_f^z(S^{t+1}) \right] + F_S, \tag{B5}
\end{aligned}$$

$$723 \quad \rho = \rho(T, S, p), \tag{B6}$$

$$\begin{aligned}
724 \quad & \frac{(q^2 D)^{t+1} - (q^2 D)^{t-1}}{2dti} + \delta_f^x(\overline{U}_b^z q^2 \overline{D}_b^x) + \delta_f^y(\overline{V}_b^z q^2 \overline{D}_b^y) + \\
725 \quad & \delta_f^z(\overline{W} q^2)_b^z = \delta_b^z \left[\frac{K_{q_f}^z}{D^{t+1}} \delta_f^z(q^2)^{t+1} \right] + \frac{2K_M}{D} \left\{ \left[\delta_b^z(\overline{U}_f^x) \right]^2 + \left[\delta_b^z(\overline{V}_f^y) \right]^2 \right\} + \\
726 \quad & \frac{2g}{\rho_0} K_H \delta_b^z(\rho) - \frac{2Dq^3}{B_1 l} + F_{q^2}, \tag{B7}
\end{aligned}$$

$$\begin{aligned}
727 \quad & \frac{(q^2 l D)^{t+1} - (q^2 l D)^{t-1}}{2dti} + \delta_f^x(\overline{U}_b^z q^2 \overline{l}_b^x \overline{D}_b^x) + \delta_f^y(\overline{V}_b^z q^2 \overline{l}_b^y \overline{D}_b^y) + \\
728 \quad & \delta_f^z(\overline{W} q^2 \overline{l})_b^z = \delta_b^z \left[\frac{K_{q_f}^z}{D^{t+1}} \delta_f^z(q^2 l)^{t+1} \right] + l E_1 \frac{K_M}{D} \left\{ \left[\delta_b^z(\overline{U}_f^x) \right]^2 + \left[\delta_b^z(\overline{V}_f^y) \right]^2 \right\} \tilde{W} + \\
729 \quad & \frac{l E_1 E_3 g}{\rho_0} K_H \delta_b^z(\rho) \tilde{W} - \frac{Dq^3}{B_1} + F_{q^2 l}, \tag{B8}
\end{aligned}$$

730

731 where F_u , F_v , F_{q^2} , and $F_{q^2 l}$ are horizontal kinematic viscosity terms of u , v , q^2 , and

732 $q^2 l$, respectively. F_T and F_S are horizontal diffusion terms of T and S respectively.

$$733 \quad F_u = \delta_b^x [2A_M D \delta_f^x (U^{t-1})] + \delta_f^y \left\{ \overline{(\overline{A_M})}_b^x \overline{(\overline{D_b})}_b^y [\delta_b^x (V)^{t-1} + \delta_b^y (U)^{t-1}] \right\}, \quad (\text{B9})$$

$$734 \quad F_v = \delta_b^y [2A_M D \delta_f^y (V^{t-1})] + \delta_f^x \left\{ \overline{(\overline{A_M})}_b^y \overline{(\overline{D_b})}_b^x [\delta_b^x (V)^{t-1} + \delta_b^y (U)^{t-1}] \right\}, \quad (\text{B10})$$

$$735 \quad F_T = \delta_f^x [\overline{A_{H_b}}^x \overline{H_b}^x \delta_b^x (T^{t-1})] + \delta_f^y [\overline{A_{H_b}}^y \overline{H_b}^y \delta_b^y (T^{t-1})], \quad (\text{B11})$$

$$736 \quad F_S = \delta_f^x [\overline{A_{H_b}}^x \overline{H_b}^x \delta_b^x (S^{t-1})] + \delta_f^y [\overline{A_{H_b}}^y \overline{H_b}^y \delta_b^y (S^{t-1})], \quad (\text{B12})$$

$$737 \quad F_{q^2} = \delta_f^x \left[\overline{(\overline{A_M})}_b^x \overline{H_b}^x \delta_b^x (q^2)^{t-1} \right] + \delta_f^y \left[\overline{(\overline{A_M})}_b^y \overline{H_b}^y \delta_b^y (q^2)^{t-1} \right], \quad (\text{B13})$$

$$738 \quad F_{q^2 l} = \delta_f^x \left[\overline{(\overline{A_M})}_b^x \overline{H_b}^x \delta_b^x (q^2 l)^{t-1} \right] + \delta_f^y \left[\overline{(\overline{A_M})}_b^y \overline{H_b}^y \delta_b^y (q^2 l)^{t-1} \right]. \quad (\text{B14})$$

739

740 The discrete governing equations of barotropic (external) mode expressed by operators
741 are shown as below:

$$742 \quad \frac{\eta^{t+1} - \eta^{t-1}}{2dte} + \delta_f^x (\overline{D_b}^x U_A) + \delta_f^y (\overline{D_b}^y V_A) = 0, \quad (\text{B15})$$

$$743 \quad \frac{(\overline{D_b}^x U_A)^{t+1} - (\overline{D_b}^x U_A)^{t-1}}{2dte} + \delta_b^x \left[\overline{(\overline{D_b}^x U_A)}_f^x \overline{(U_A)}_f^x \right] + \delta_f^y \left[\overline{(\overline{D_b}^y V_A)}_b^x \overline{(U_A)}_b^y \right] -$$

$$744 \quad \left[\overline{\tilde{f}_A (V_A)}_f^y D \right]_b^x - \left[\overline{f (V_A)}_f^y D \right]_b^x + g \overline{D_b}^x \delta_b^x (\eta) = \delta_b^x \{ 2(AA_M) D \delta_f^x [(U_A)^{t-1}] \} +$$

$$745 \quad \delta_f^y \left\{ \left[\overline{(\overline{AA_M})}_b^x \right]_b^y \overline{(\overline{D_b})}_b^y [\delta_b^x (V_A) + \delta_b^y (U_A)]^{t-1} \right\} + \phi_x, \quad (\text{B16})$$

$$746 \quad \frac{(\overline{D_b}^y V_A)^{t+1} - (\overline{D_b}^y V_A)^{t-1}}{2dte} + \delta_f^x \left[\overline{(\overline{D_b}^x U_A)}_b^y \overline{(V_A)}_b^x \right] + \delta_b^y \left[\overline{(\overline{D_b}^y V_A)}_f^y \overline{(V_A)}_f^y \right] +$$

$$747 \quad \left[\overline{\tilde{f}_A (U_A)}_f^x D \right]_b^y + \left[\overline{f (U_A)}_f^x D \right]_b^y + g \overline{D_b}^y \delta_b^y (\eta) = \delta_b^y \{ 2(AA_M) D \delta_f^y [(V_A)^{t-1}] \} +$$

$$748 \quad \delta_f^x \left\{ \left[\overline{(\overline{AA_M})}_b^x \right]_b^y \overline{(\overline{D_b})}_b^y [\delta_b^x (V_A) + \delta_b^y (U_A)]^{t-1} \right\} + \phi_y, \quad (\text{B17})$$

749

750 where

$$751 \quad \phi_x = -WU(0) + WU(-1) - \frac{g(\overline{D_b}^x)^2}{\rho_0} \int_{-1}^0 \left\{ \left[\int_{\sigma}^0 \delta_b^x (\overline{\rho})_b^z d\sigma' \right] d\sigma \right\} +$$

$$752 \quad \frac{g\bar{D}_b^x \delta_b^x D}{\rho_0} \int_{-1}^0 \left\{ \left[\int_{\sigma}^0 \bar{\sigma}_b^z \delta_b^z(\bar{\rho}_b^x) \right] d\sigma \right\} + G_x, \quad (\text{B18})$$

$$753 \quad \phi_y = -WV(0) + WV(-1) - \frac{g(\bar{D}_b^y)^2}{\rho_0} \int_{-1}^0 \left\{ \left[\int_{\sigma}^0 \delta_b^y(\bar{\rho})_b^z d\sigma' \right] d\sigma \right\} +$$

$$754 \quad \frac{g\bar{D}_b^y \delta_b^y D}{\rho_0} \int_{-1}^0 \left\{ \left[\int_{\sigma}^0 \bar{\sigma}_b^z \delta_b^z(\bar{\rho}_b^y) \right] d\sigma \right\} + G_y. \quad (\text{B19})$$

755

756

757 **Appendix C: Descriptions of symbols**

758 The description of each symbol in the governing equations is list as below:

759 Table C1. Descriptions of symbols

Symbol	Description
η	Free surface elevation
H	Bottom topography
ua, va	Vertical average velocity in x, y direction, respectively
U, V, W	Velocity in x, y, σ direction, respectively
D	Fluid column depth
f	The Coriolis parameter
g	The gravitational acceleration
ρ_0	Constant density
ρ	Situ density
T	Potential temperature
S	Salinity
R	Surface solar radiation incident
$q^2/2$	Turbulence kinetic energy
l	Turbulence length scale
$q^2l/2$	Production of turbulence kinetic energy and turbulence length scale
dti	Time step of baroclinic mode
dte	Time step of barotropic mode
dx	Grid increment in x direction
dy	Grid increment in y direction
A_M	Horizontal kinematic viscosity
A_H	Horizontal heat diffusivity
K_M	Vertical kinematic viscosity
K_H	Vertical mixing coefficient of heat and salinity
K_q	Vertical mixing coefficient of turbulence kinetic energy

761 *Author contributions.* Xiaomeng Huang led the project of OpenArray and the writing
762 of this paper, DW, QW, SZ and Xing Huang designed OpenArray. Xing Huang, DW,
763 QW, SZ, MW, YG, and QT implemented and tested GOMO. All coauthors contributed
764 to the writing of this paper.

765

766 *Competing interests.* The authors declare that they have no conflict of interest.

767

768 *Acknowledgements.* Xiaomeng Huang is supported by a grant from the State's Key
769 Project of Research and Development Plan (2016YFB0201100) and the National
770 Natural Science Foundation of China (41776010). Xing Huang is supported by a grant
771 from the State's Key Project of Research and Development Plan (2018YFB0505000).
772 Shixun Zhang is supported by a grant from the State's Key Project of Research and
773 Development Plan (2017YFC1502200) and Qingdao National Laboratory for Marine
774 Science and Technology (QNL2016ORP0108). Zhenya Song is supported by
775 National Natural Science Foundation of China (U1806205) and AoShan Talents
776 Cultivation Excellent Scholar Program Supported by Qingdao National Laboratory for
777 Marine Science and Technology (2017ASTCP-ES04).

778

779 **References**

780 Abadi, M., Barham, P., Chen, J., Chen, Z., Davis, A., Dean, J., Devin, M., Ghemawat,
781 S., Irving, G., Isard, M., Kudlur, M., Levenberg, J., Monga, R., Moore, S., Murray,
782 D. G., Steiner, B., Tucker, P., Vasudevan, V., Warden, P., Wicke, M., Yu, Y. and
783 Zheng, X.: TensorFlow: A System for Large-Scale Machine Learning, in 12th
784 {USENIX} Symposium on Operating Systems Design and Implementation ({OSDI}
785 16), pp. 265–283, {USENIX} Association, Savannah, GA. [online] Available from:
786 <https://www.usenix.org/conference/osdi16/technical-sessions/presentation/abadi>,
787 2016.

788 Alexander, K. and Easterbrook, S. M.: The software architecture of climate models: A
789 graphical comparison of CMIP5 and EMICAR5 configurations, *Geosci. Model Dev.*,

790 8(4), 1221–1232, doi:10.5194/gmd-8-1221-2015, 2015.

791 Arakawa, A. and Lamb, V. R.: A Potential Enstrophy and Energy Conserving Scheme
792 for the Shallow Water Equations, *Mon. Weather Rev.*, doi:10.1175/1520-
793 0493(1981)109<0018:APEAEC>2.0.CO;2, 1981.

794 Bae, H., Mustafa, D., Lee, J. W., Aurangzeb, Lin, H., Dave, C., Eigenmann, R. and
795 Midkiff, S. P.: The Cetus source-to-source compiler infrastructure: Overview and
796 evaluation, in *International Journal of Parallel Programming.*, 2013.

797 Bastien, F., Lamblin, P., Pascanu, R., Bergstra, J., Goodfellow, I. J., Bergeron, A.,
798 Bouchard, N., Warde-Farley, D. and Bengio, Y.: Theano: new features and speed
799 improvements, *CoRR*, abs/1211.5 [online] Available from:
800 <http://arxiv.org/abs/1211.5590>, 2012.

801 Beckmann, A. and Haidvogel, D. B.: Numerical simulation of flow around a tall
802 isolated seamount. Part I: problem formulation and model accuracy, *J. Phys.*
803 *Oceanogr.*, 23(8), 1736–1753, doi:10.1175/1520-
804 0485(1993)023<1736:NSOFAA>2.0.CO;2, 1993.

805 Bloss, A., Hudak, P. and Young, J.: Code optimizations for lazy evaluation, *Lisp Symb.*
806 *Comput.*, doi:10.1007/BF01806169, 1988.

807 Blumberg, A. F. and Mellor, G. L.: A description of a three-dimensional coastal ocean
808 circulation model, , (January 1987), 1–16, doi:10.1029/CO004p0001, 1987.

809 Bonan, G. B. and Doney, S. C.: Climate, ecosystems, and planetary futures: The
810 challenge to predict life in Earth system models, *Science* (80-.),
811 doi:10.1126/science.aam8328, 2018.

812 Bretherton, C., Balaji, V. and Delworth, T. et al: A National Strategy for Advancing
813 Climate Modeling, National Academies Press., 2012.

814 Che, S., Boyer, M., Meng, J., Tarjan, D., Sheaffer, J. W., Lee, S. H. and Skadron, K.:
815 Rodinia: A benchmark suite for heterogeneous computing, in *Proceedings of the*
816 *2009 IEEE International Symposium on Workload Characterization, IISWC 2009.*,
817 2009.

818 Chen, C., Liu, H. and Beardsley, R. C.: An unstructured grid, finite-volume, three-

819 dimensional, primitive equations ocean model: Application to coastal ocean and
820 estuaries, *J. Atmos. Ocean. Technol.*, doi:10.1175/1520-
821 0426(2003)020<0159:AUGFVT>2.0.CO;2, 2003.

822 Collins, M., Minobe, S., Barreiro, M., Bordoni, S., Kaspi, Y., Kuwano-Yoshida, A.,
823 Keenlyside, N., Manzini, E., O'Reilly, C. H., Sutton, R., Xie, S. P. and Zolina, O.:
824 Challenges and opportunities for improved understanding of regional climate
825 dynamics, *Nat. Clim. Chang.*, 8(2), 101–108, doi:10.1038/s41558-017-0059-8, 2018.

826 Corliss, G. and Griewank, A.: *Operator Overloading as an Enabling Technology for*
827 *Automatic Differentiation*, 1994.

828 Deconinck, W., Bauer, P., Diamantakis, M., Hamrud, M., Kühnlein, C., Maciel, P.,
829 Mengaldo, G., Quintino, T., Raoult, B., Smolarkiewicz, P. K. and Wedi, N. P.: *Atlas :*
830 *A library for numerical weather prediction and climate modelling*, *Comput. Phys.*
831 *Commun.*, 220, 188–204, doi:10.1016/j.cpc.2017.07.006, 2017.

832 Dennis, J. M.: Inverse space-filling curve partitioning of a global ocean model, *Proc. -*
833 *21st Int. Parallel Distrib. Process. Symp. IPDPS 2007*; *Abstr. CD-ROM*, 1–10,
834 doi:10.1109/IPDPS.2007.370215, 2007.

835 van Engelen, R. a.: *ATMOL: A Domain-Specific Language for Atmospheric Modeling*,
836 *J. Comput. Inf. Technol.*, 9(4), 289–303, doi:10.2498/cit.2001.04.02, 2001.

837 Frigo, M. and Strumpen, V.: Cache oblivious stencil computations, , 361,
838 doi:10.1145/1088149.1088197, 2005.

839 Fu, H., He, C., Chen, B., Yin, Z., Zhang, Z., Zhang, W., Zhang, T., Xue, W., Liu, W.,
840 Yin, W. and others: 18.9-Pflops nonlinear earthquake simulation on Sunway
841 TaihuLight: enabling depiction of 18-Hz and 8-meter scenarios, in *Proceedings of*
842 *the International Conference for High Performance Computing, Networking, Storage*
843 *and Analysis.*, 2017.

844 Griffies, S. M., Böning, C., Bryan, F. O., Chassignet, E. P., Gerdes, R., Hasumi, H.,
845 Hirst, A., Treguier, A.-M. and Webb, D.: Developments in ocean climate modelling,
846 *Ocean Model.*, 2(3–4), 123–192, doi:10.1016/S1463-5003(00)00014-7, 2000.

847 Gysi, T., Osuna, C., Fuhrer, O., Bianco, M. and Schulthess, T. C.: *STELLA: A Domain-*

848 specific Tool for Structured Grid Methods in Weather and Climate Models, Proc. Int.
849 Conf. High Perform. Comput. Networking, Storage Anal. - SC '15, 1–12,
850 doi:10.1145/2807591.2807627, 2015.

851 Huang, W., Ghosh, S., Velusamy, S., Sankaranarayanan, K., Skadron, K. and Stan, M.
852 R.: HotSpot: A compact thermal modeling methodology for early-stage VLSI design,
853 IEEE Trans. Very Large Scale Integr. Syst., doi:10.1109/TVLSI.2006.876103, 2006.

854 Huang, X. M., Wang, W. C., Fu, H. H., Yang, G. W., Wang, B. and Zhang, C.: A fast
855 input/output library for high-resolution climate models, Geosci. Model Dev., 7(1),
856 93–103, doi:10.5194/gmd-7-93-2014, 2014.

857 Korn, P.: Formulation of an unstructured grid model for global ocean dynamics, J.
858 Comput. Phys., 339, 525–552, doi:10.1016/j.jcp.2017.03.009, 2017.

859 Lawrence, B. N., Rezny, M., Budich, R., Bauer, P., Behrens, J., Carter, M., Deconinck,
860 W., Ford, R., Maynard, C., Mullerworth, S., Osuna, C., Porter, A., Serradell, K.,
861 Valcke, S., Wedi, N. and Wilson, S.: Crossing the chasm: How to develop weather
862 and climate models for next generation computers?, Geosci. Model Dev.,
863 doi:10.5194/gmd-11-1799-2018, 2018.

864 Levin, J. G., Iskandarani, M. and Haidvogel, D. B.: A nonconforming spectral element
865 ocean model, Int. J. Numer. Methods Fluids, 34(6), 495–525, doi:10.1002/1097-
866 0363(20001130)34:6<495::AID-FLD68>3.0.CO;2-K, 2000.

867 Lidman, J., Quinlan, D. J., Liao, C. and McKee, S. A.: ROSE::FTTransform - A source-
868 to-source translation framework for exascale fault-tolerance research, Proc. Int. Conf.
869 Dependable Syst. Networks, (June), doi:10.1109/DSNW.2012.6264672, 2012.

870 Mellor-Crummey, J., Adhianto, L., Scherer III, W. N. and Jin, G.: A New Vision for
871 Coarray Fortran, in Proceedings of the Third Conference on Partitioned Global
872 Address Space Programming Models, p. 5:1--5:9, ACM, New York, NY, USA., 2009.

873 Mellor, G. L.: Users guide for a three-dimensional, primitive equation, numerical ocean
874 model (June 2003 version), Prog. Atmos. Ocean. Sci, Princet. Univ., (October), 53,
875 2003.

876 Mellor, G. L. and Yamada, T.: Development of a turbulence closure model for

877 geophysical fluid problems, *Rev. Geophys.*, doi:10.1029/RG020i004p00851, 1982.

878 Porkoláb, Z., Mihalicza, J. and Sipos, Á.: Debugging C++ template metaprograms, ,
879 255, doi:10.1145/1173706.1173746, 2007.

880 Pugh, W.: Uniform Techniques for Loop Optimization, in *Proceedings of the 5th*
881 *International Conference on Supercomputing*, pp. 341–352, ACM, New York, NY,
882 USA., 1991.

883 Qiao, F., Zhao, W., Yin, X., Huang, X., Liu, X., Shu, Q., Wang, G., Song, Z., Li, X.,
884 Liu, H., Yang, G. and Yuan, Y.: A Highly Effective Global Surface Wave Numerical
885 Simulation with Ultra-High Resolution, in *International Conference for High*
886 *Performance Computing, Networking, Storage and Analysis*, SC., 2017.

887 Reynolds, J. C.: *Theories of Programming Languages*, Cambridge University Press,
888 New York, NY, USA., 1999.

889 Shan, A.: Heterogeneous Processing: A Strategy for Augmenting Moore’s Law, *Linux*
890 *J.*, 2006(142). Available from: <http://dl.acm.org/citation.cfm?id=1119128.1119135>,
891 2006.

892 Shchepetkin, A. F. and McWilliams, J. C.: The regional oceanic modeling system
893 (ROMS): A split-explicit, free-surface, topography-following-coordinate oceanic
894 model, *Ocean Model.*, doi:10.1016/j.ocemod.2004.08.002, 2005.

895 Suganuma, T. and Yasue, T.: Design and evaluation of dynamic optimizations for a
896 Java just-in-time compiler, *ACM Trans. ...*, doi:10.1145/1075382.1075386, 2005.

897 Taylor, K. E., Stouffer, R. J. and Meehl, G. A.: An overview of CMIP5 and the
898 experiment design, *Bull. Am. Meteorol. Soc.*, 93(4), 485–498, doi:10.1175/BAMS-
899 D-11-00094.1, 2012.

900 Torres, R., Linardakis, L., Kunkel, J. and Ludwig, T.: ICON DSL: A Domain-Specific
901 Language for climate modeling, *Sc13.Supercomputing.Org* [online] Available from:
902 <http://sc13.supercomputing.org/sites/default/files/WorkshopsArchive/pdfs/wp127s1>
903 .pdf, 2013.

904 Walther, A., Griewank, A. and Vogel, O.: ADOL-C: Automatic Differentiation Using
905 Operator Overloading in C++, *PAMM*, doi:10.1002/pamm.200310011, 2003.

906 Xu, S., Huang, X., Oey, L. Y., Xu, F., Fu, H., Zhang, Y. and Yang, G.: POM.GPU-v1.0:
907 A GPU-based princeton ocean model, *Geosci. Model Dev.*, doi:10.5194/gmd-8-
908 2815-2015, 2015.
909

910 **Tables**

911 Table 1. Definitions of the twelve basic operators

Notations	Discrete Form	Basic Operator
\overline{var}_f^x	$[var(i,j,k) + var(i+1,j,k)] / 2$	AXF
\overline{var}_b^x	$[var(i,j,k) + var(i-1,j,k)] / 2$	AXB
\overline{var}_f^y	$[var(i,j,k) + var(i,j+1,k)] / 2$	AYF
\overline{var}_b^y	$[var(i,j,k) + var(i,j-1,k)] / 2$	AYB
\overline{var}_f^z	$[var(i,j,k) + var(i,j,k+1)] / 2$	AZF
\overline{var}_b^z	$[var(i,j,k) + var(i,j,k-1)] / 2$	AZB
$\delta_f^x(var)$	$[var(i+1,j,k) - var(i,j,k)] / dx(i,j)$	DXF
$\delta_b^x(var)$	$[var(i,j,k) - var(i-1,j,k)] / dx(i-1,j)$	DXB
$\delta_f^y(var)$	$[var(i,j+1,k) - var(i,j,k)] / dy(i,j)$	DYF
$\delta_b^y(var)$	$[var(i,j,k) - var(i,j-1,k)] / dy(i,j-1)$	DYB
$\delta_f^z(var)$	$[var(i,j,k+1) - var(i,j,k)] / dz(k)$	DZF
$\delta_b^z(var)$	$[var(i,j,k) - var(i,j,k-1)] / dz(k-1)$	DZB

912

913

914

Table 2 The jumping rules of an operator acting on an *Array*

The initial position of <i>var</i>	The position of $[A D]X[F B]$ (<i>var</i>)	The position of $[A D]Y[F B]$ (<i>var</i>)	The position of $[A D]Z[F B]$ (<i>var</i>)
0	1	2	4
1	0	3	5
2	3	0	6
3	2	1	7
4	5	6	0
5	4	7	1
6	7	4	2
7	6	5	3

915

916

917

Table 3. Comparing GOMO with several variations of the POM

Model	Lines of code	Method	Computing Platforms
POM2k	3521	Serial	CPU
sbPOM	4801	MPI	CPU
mpiPOM	9685	MPI	CPU
POMgpu	30443	MPI + CUDA	GPU
GOMO	1860	OpenArray	CPU, Sunway

918

919

920

Table. 4. Comparison of the amount of code for different functions

Functions	Lines of code		
	POM2k	sbPOM	GOMO
Solve for η	16	72	1
Solve for Ua	75	183	11
Solve for Va	75	183	11
Solve for W	36	90	3
Solve for q^2 and q^2l	318	854	162
Solve for T or S	178	234	71
Solve for U	118	230	50
Solve for V	118	230	50

921

922

923

Table 5. Four benchmark tests

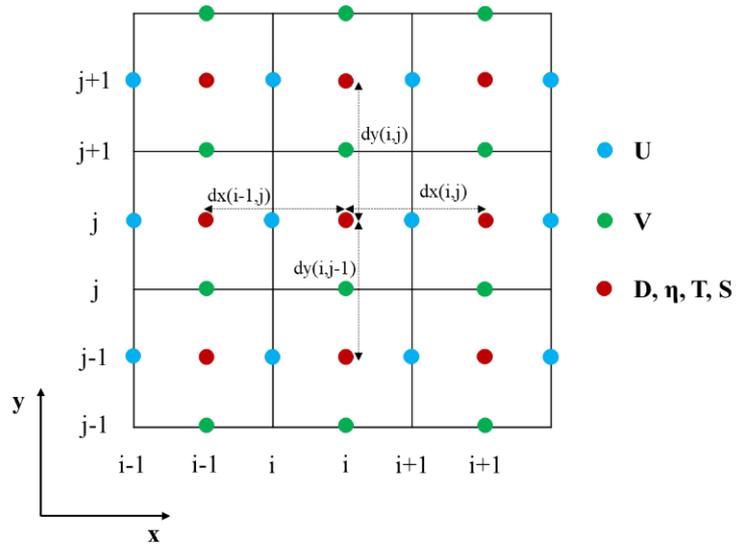
Benchmark	Dimensions	Grid Size	OpenArray version (seconds)	Original version(seconds)
Continuity equation	2D	8192×8192	7.22	7.10
Heat diffusion equation	2D	8192×8192	6.20	6.34
Hotspot2D	2D	8192×8192	11.37	11.21
Hotspot3D	3D	512×512×8	0.96	1.01

924

925

926 **Figures**

927



928

929

930

Figure 1. Arrangement of variables in the staggered Arakawa C grid.

931

\$ 1) 2D continuous equation

$$\eta_{t+1} = \eta_{t-1} - 2 * dt * (\delta_x^2 (\bar{D}_b^x * U) + \delta_y^2 (\bar{D}_b^y * V))$$

\$ 2) The code constructed by operators

$$elf = elb - 2 * dt * (DXF(AXB(D)*U) + DYF(AYB(D)*V))$$

\$ 3) The pseudo-code

```
exchange2d_mpi(u,im,jm)
exchange2d_mpi(v,im,jm)
exchange2d_mpi(D,im,jm)
```

```
do i = 1, im
```

```
do j = 1, jm
```

```
elf(i,j) = elb(i,j) - 2 * dt * ( &
((D(i+1,j)+D(i,j))/2 * u(i+1,j) - (D(i,j)+D(i-1,j))/2 * u(i,j)) / dx(i,j) + &
((D(i,j+1)+D(i,j))/2 * v(i+1,j) - (D(i,j)+D(i,j-1))/2 * v(i,j)) / dy(i,j))
```

932

933 Figure 2. Implementation of Eq. (6) by basic operators. The *elf* and *elb* are the surface

934 elevations at times $(t+1)$ and $(t-1)$ respectively.

935

\$ Equation (8)

$$elf = elb - 2*dt*(DXF(AXB(D)*U) + DYF(AYB(D)*V))$$

\$ Equation (9)

$$Uf = Db*Ub/Df - 2*dt/Df*(DXB(AXF(AXB(D)*U)*AXF(U)) + DYF(AXB(AYB(D)*V)*AYB(U)) - & \\ AXB(f*AYF(V)*D) + g*AXB(D)*DXB(el) - aam*AXB(D)*(DXB(DXF(Ub)) + DYF(DYB(Ub)))))$$

\$ Equation (10)

$$Vf = Db*Vb/Df - 2*dt/Df*(DXF(AYB(AXB(D)*U)*AXB(V)) + DYB(AYF(AYB(D)*V)*AYF(V)) + & \\ AYB(f*AXF(U)*D) + g*AYB(D)*DYB(el) - aam*AYB(D)*(DXF(DXB(Vb)) + DYB(DYF(Vb)))))$$

936

937 Figure 3. Implementation of the shallow water equations by basic operators. *elf*, *el* and

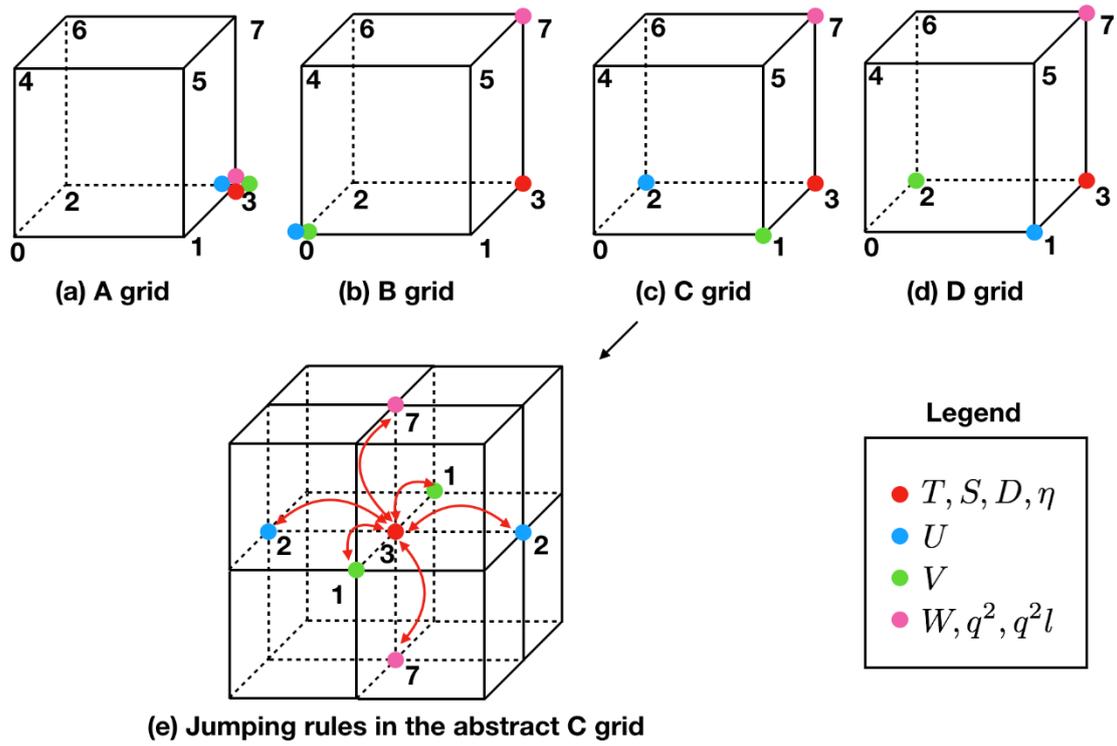
938 *elb* denote sea surface elevations at times $(t+I)$, t and $(t-I)$, respectively. *Uf*, *U* and *Ub*

939 denote the zonal velocity at times $(t+I)$, t and $(t-I)$, respectively. *Vf*, *V* and *Vb* denote

940 the meridional velocity at times $(t+I)$, t and $(t-I)$, respectively. *aam* denotes the

941 viscosity coefficient.

942



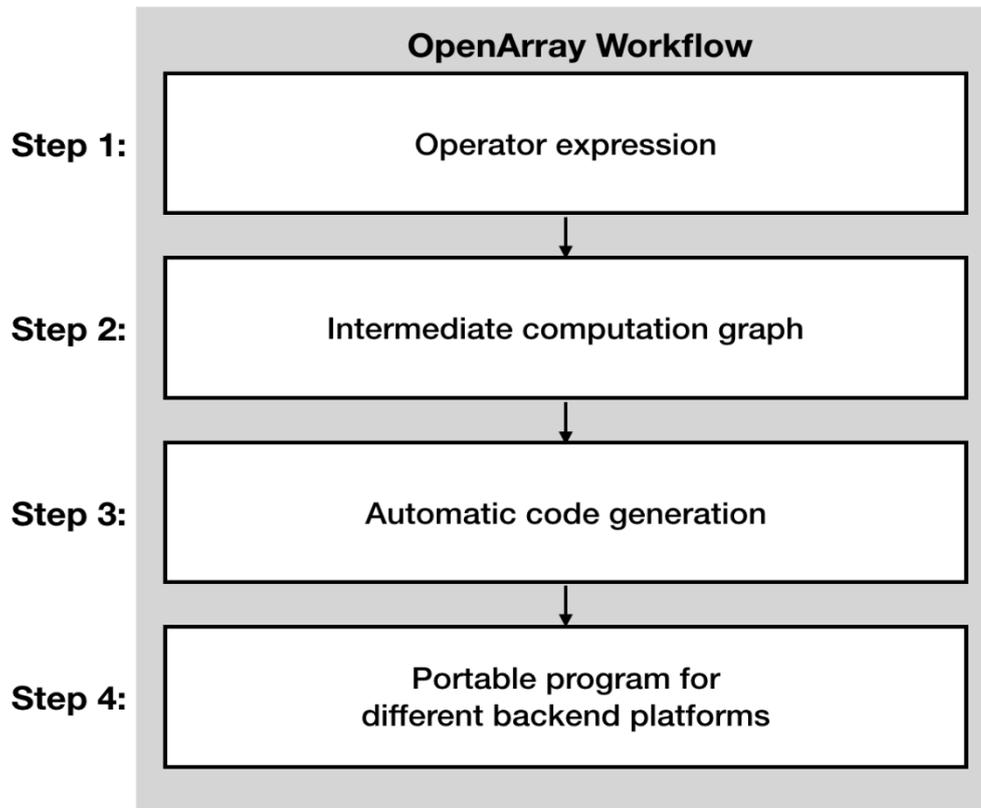
943

944

Figure 4. The schematic diagram of the relative positions of the variables on the abstract staggered grid and the jumping procedures among the grid points.

945

946



947

948

949

Figure 5. The workflow of OpenArray.

Formula	$\eta_{t+1} = \eta_{t-1} - 2 * dt * \left(\delta_f^x(\bar{D}_b^x * U) + \delta_f^y(\bar{D}_b^y * V) \right)$
Code	$elf = elb - dt2 * (DXF(AXB(D)*U) + DYF(AYB(D)*V))$

950

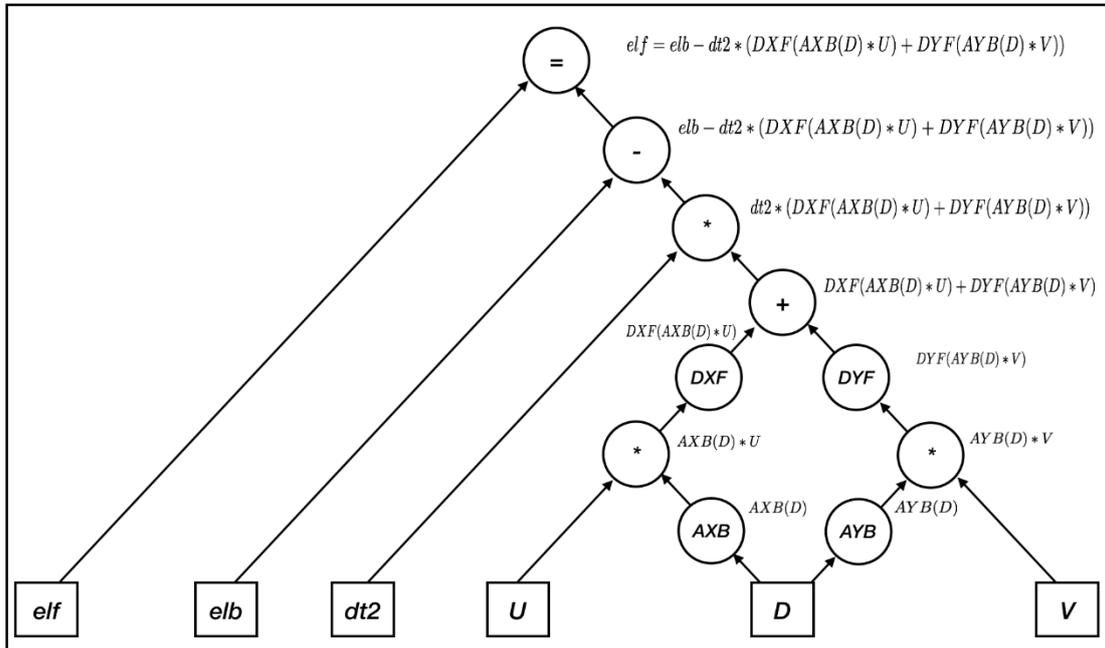
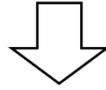
951

952

953

Figure 6. The effect of “The self-documenting code is the formula” illustrated by the sea surface elevation equation.

$$elf = elb - dt2 * (DXF(AXB(D) * U) + DYF(AYB(D) * V))$$



954

955

956

Figure 7. Parsing the operator expression form into the computation graph.

957
958
959

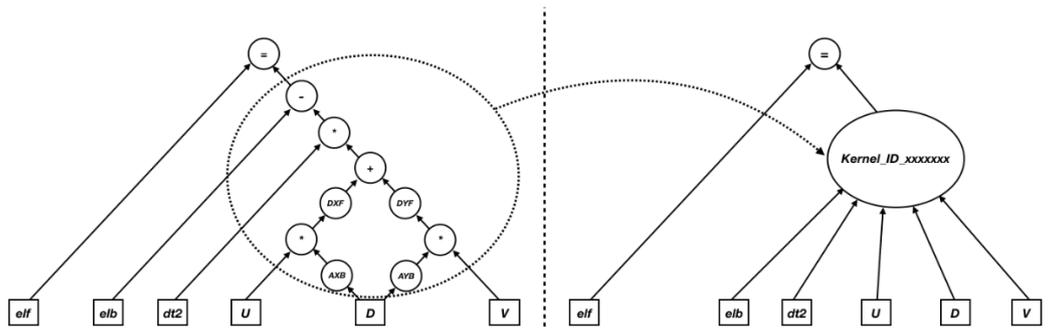
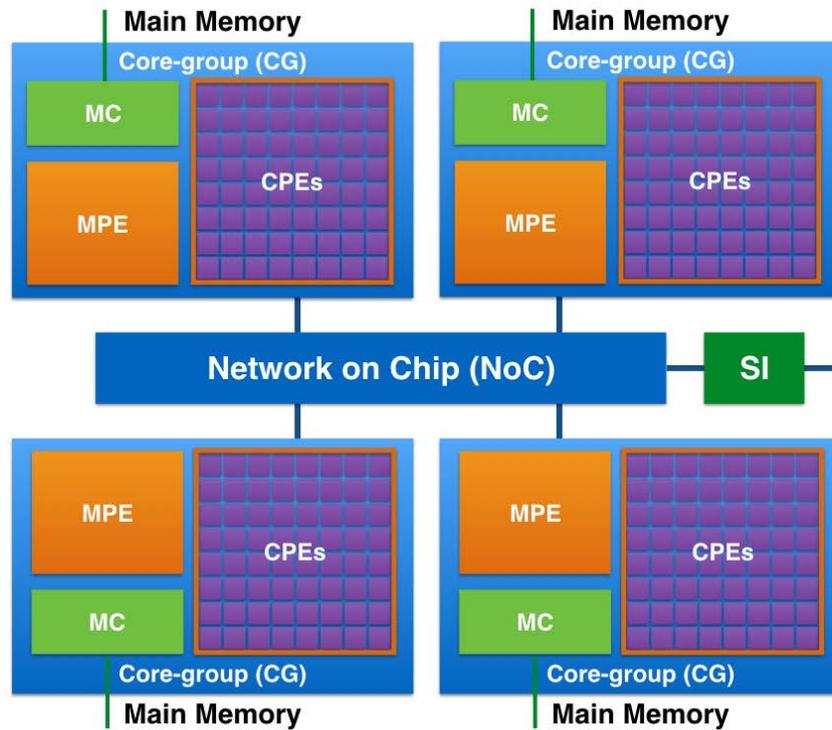


Figure 8. The schematic diagram of kernel fusion.



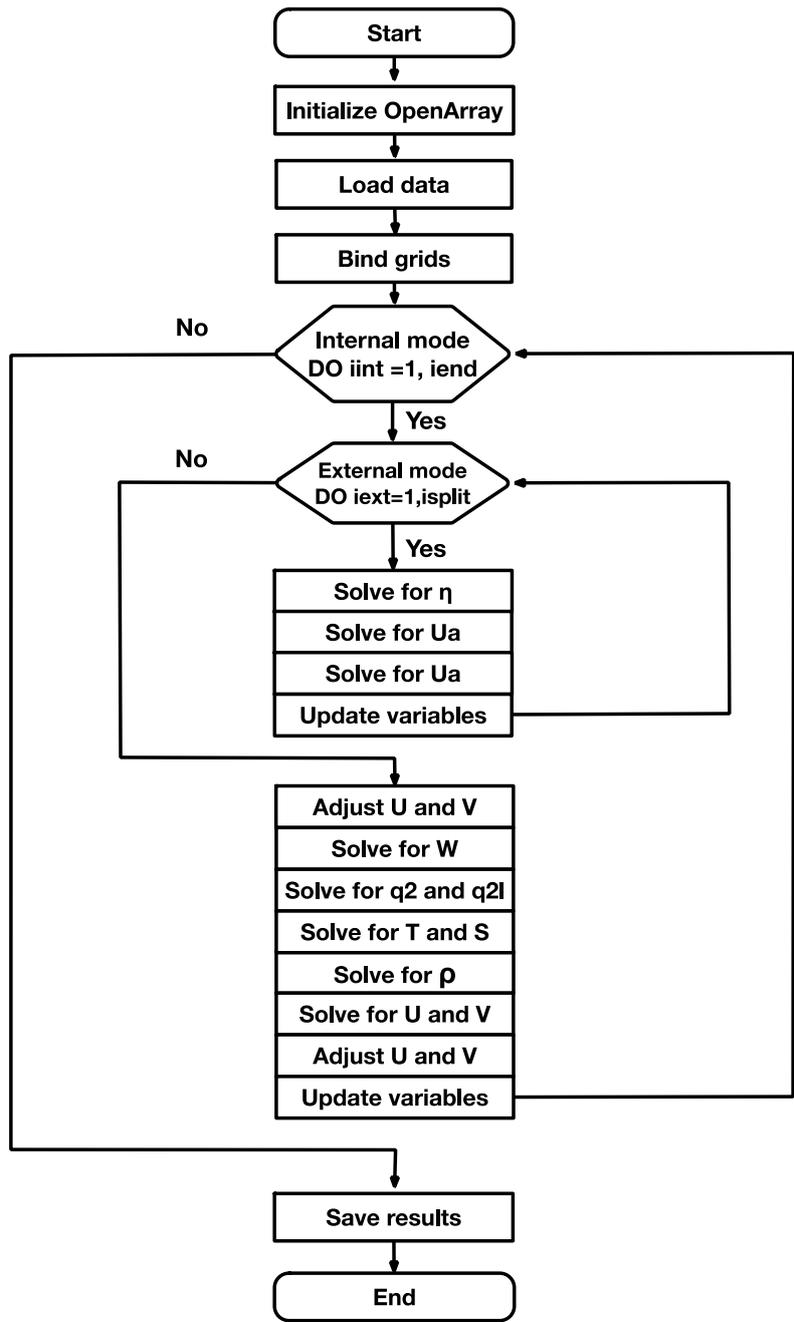
961

962 Figure 9. The MPE-CPEs hybrid architecture of the Sunway processor. Every Sunway
 963 processor includes 4 Core-groups (CGs) connected by the Network on Chip (NoC).

964 Each CG consists of a management processing element (MPE), 64 computing
 965 processing elements (CPEs) and a memory controller (MC). The Sunway processor

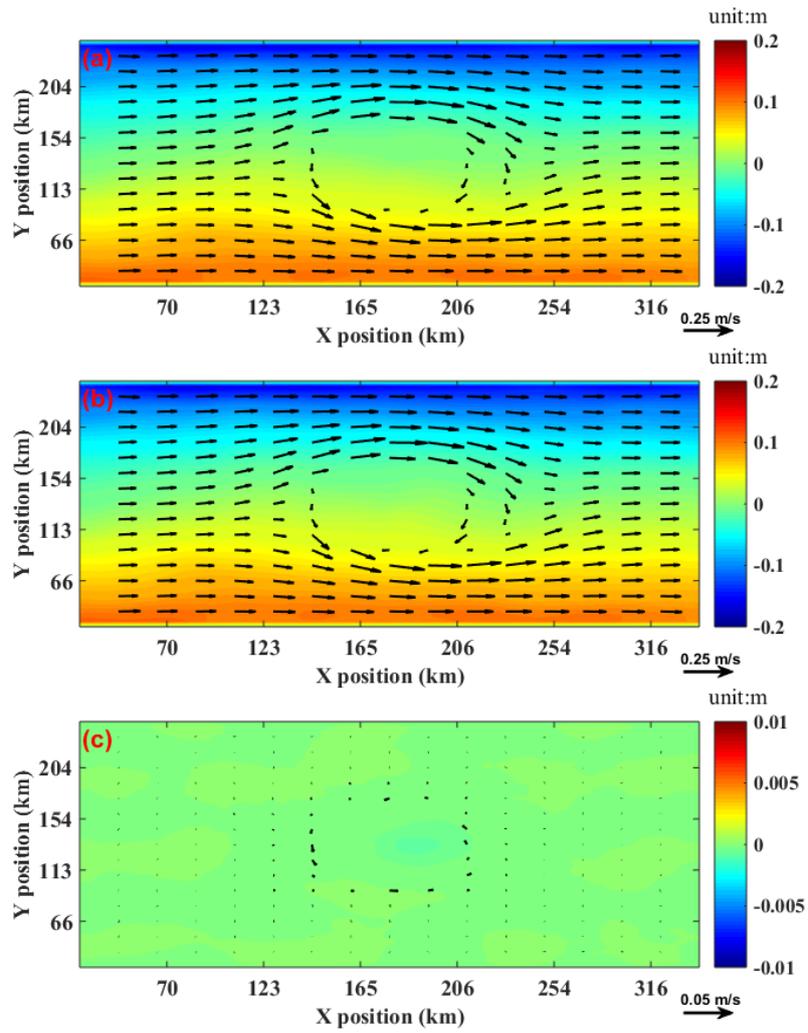
966 uses the system interface (SI) to connect with outside devices.

967



968
969
970

Figure 10. Flow diagram of GOMO



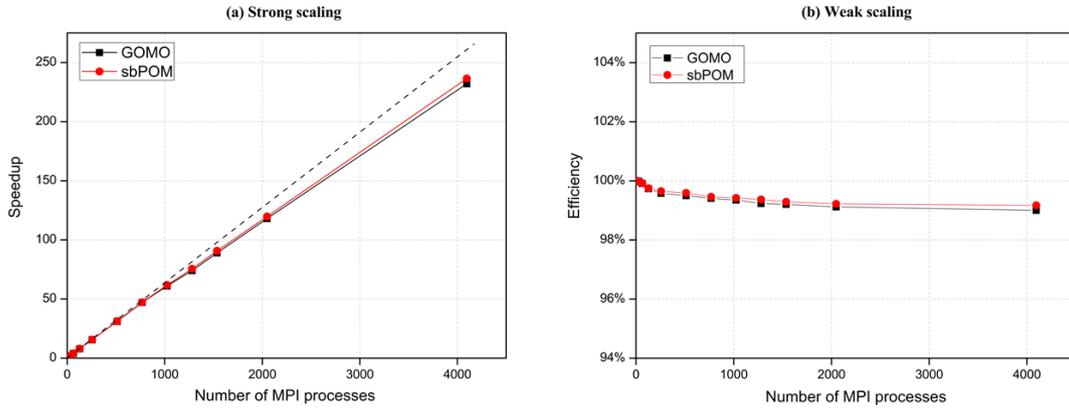
971

972 Figure 11. Comparison of the surface elevation (shaded) and currents at 3500 metres

973 depth (vector) between GOMO and sbPOM on the 4th model day. (a) GOMO, (b)

974 sbPOM, (c) GOMO-sbPOM.

975



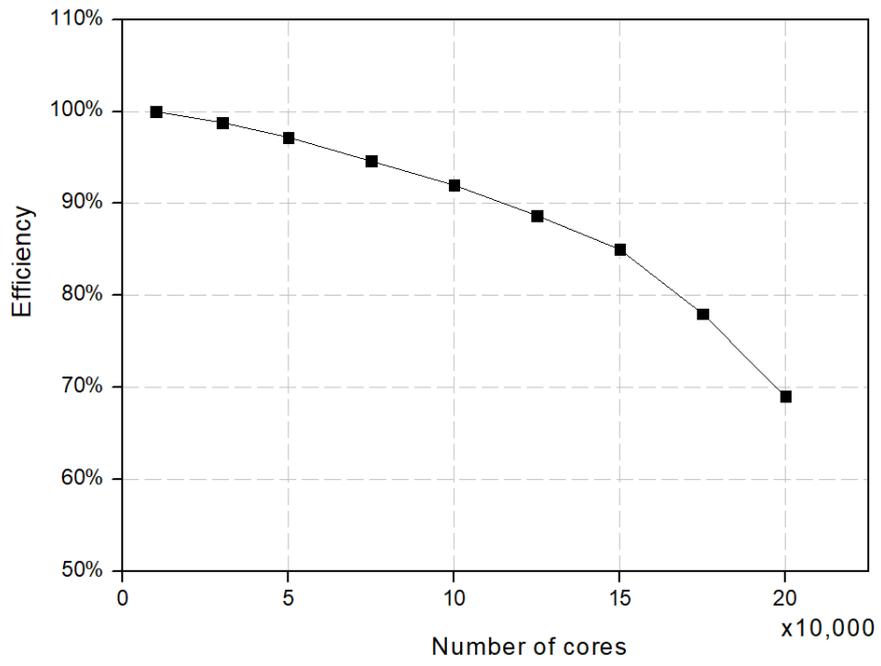
976

977 Figure 12. Performance comparison between sbPOM and GOMO on the X86 cluster.

978 (a) The strong scaling result; vertical axis denotes the speedup relative to 16 processes

979 in a single node. (b) The weak scaling result.

980



981
982
983

Figure 13. Parallel efficiency of GOMO on the Sunway platform.