

## ***Interactive comment on “How to use mixed precision in Ocean Models” by Oriol Tintó Prims et al.***

**Oriol Tintó Prims et al.**

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We thank the consideration that the referee had for our work and the valuable comments that helped improve the quality of our manuscript. Answers for the questions follow this lines, and the specific suggestions to improve the text have been adopted.

**Referee:** There is one weakness of the presentation at the moment: Results for model simulations that are using the reduced precision configuration are not presented. If these are not shown, the reader will assume that the results are not so great but I think that this is actually not the case. Can you add some figures showing results when using the reduced precision configurations? E.g. mean fields for long term simulations and differences for short term simulations in comparison to differences

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that are caused by a change of the timestep?

**Answer:** The reason to leave the results without a figure was that the maps are virtually identical and the differences are not perceptible. Figure 1 and Figure 2 attached to this document show the sea surface temperature mean during the first month of simulation for the reference case and the loose case. It can be seen that there are no perceptible differences. A paragraph has been added to the discussion section 3.1.4 trying to empathize this.+

**Referee:** The English should be revised and improved throughout the paper (see some detailed comments below but there are more problems in the text).

**Answer:** There has been an effort to improve the quality of the text, all the mistakes pointed out by the referee have been solved and a general revision of the text has been performed.

**Referee:** One of the main problems for a precision reduction in ocean models is that conservation laws may get violated (mass and tracers). Can you comment on that? Or quantify mass loss/gain when running the reduced precision configurations?

**Answer:** The conservation of mass and tracers in our experiments has not been studied. It is in fact a good idea to consider conservation laws to be used as accuracy tests as well. Defining an accuracy test to ensure that conservation laws are fulfilled will prevent that any variable that might negatively affect conservation is set to reduced precision.

**Referee:** The constraints that come in via the exponent are not very well discussed.

**Answer:** I have added clarifications regarding this point in two different sections of the code: when we first talk about the reduced precision emulator in the introduction and when we talk about the possibility of using half-precision for ROMS simulations in section 3.2 .

**Referee:** You may want to cite this paper: Düben et al. 2017: "A study of reduced nu-

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merical precision to make superparameterization more competitive using a hardware emulator in the OpenIFS model".It performs a precision analysis per parameter for the CRM used in superparametrisation similar to the one performed in this paper. It is also arguing that the parameter uncertainty that is found via an automated precision analysis could be used to develop stochastic parametrisation schemes. This may also add to an interesting discussion in this paper.?

**Answer:** A cite to this manuscript has been included in the introduction.

**Referee:** I do not understand IQR and how it is used.

**Answer:** Interquartile Range is a measure of statistical dispersion of the values of a sample. In the manuscript, it is used in the NEMO cases to normalize the RMSD minimizing the effects of outlier values. At first, it was considered because it would make it easier to combine errors from variables of different magnitudes, although in the case presented in this manuscript it might be unnecessary.

**Referee:** Why do you not present the results for the tight evaluation? The light cray is not visible in my printout.

**Answer:** The tight case was included to demonstrate that the method can work imposing different constrains. Showing the impact estimates for the tight case can mislead the reader to think that the potential reduction of memory usage is lower that what it really is. This same information has been included in the manuscript. The Figure 1 has been modified to make the two colors distinguishable in black and white.

**Referee:** For NEMO: Maybe I have missed this information: Do you state how many of the variables are actually used and how many are not used in standard simulations? You should also state the accuracy score when you run simulations with the combined precision reductions for the tight and loose precision configuration.

**Answer:** From more than 3500 variables declared through the code, our specific configuration only uses 942. These are identified during a simulation and a file that

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shows which variables were actually used is generated. This information has been included in the manuscript (section 3.1.3). Our experience using the method with NEMO tells us that with a large number of variables, the final accuracy score ends up being just below the limit established. This has been empathized in the manuscript.

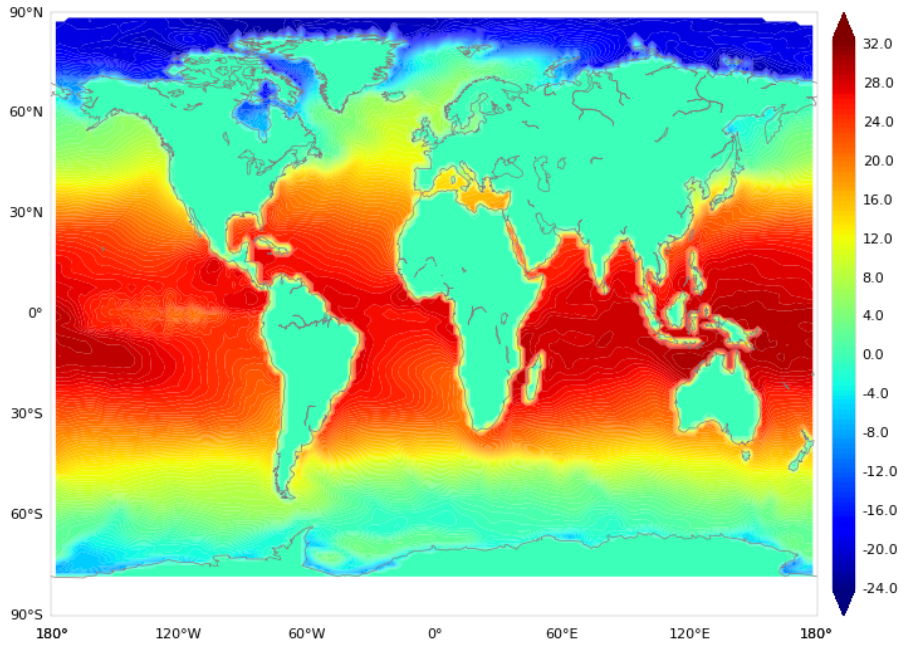
**Referee:** "AD and TL should be better targets" 4DVar experts tend to disagree with this statement since the forward TL and the backward AD need to fit to each other to guarantee convergence of the assimilation. Reduced precision can destroy this. You may want to discuss this less optimistically.

**Answer:** TL and AD models that are typically used in 4D-Var systems involve many approximations (e.g. different resolutions to the NL model, reduced physics, more stable numerics, etc) - nonetheless they provide useful gradient information. We see reduced precision as simply another level of approximation. As long as the TL and AD models are consistent (i.e. the AD will be the transpose of the TL to within the chosen precision), the numerical precision can be reduced. The referee was right pointing out that our previous explanation could seem too optimistic and it was clarified in the manuscript.

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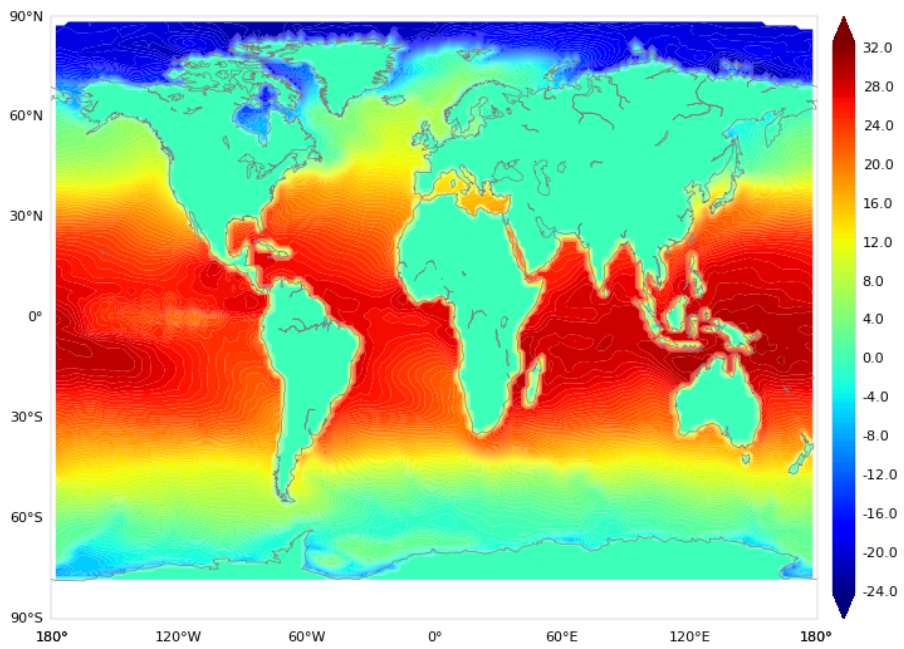
Interactive comment on Geosci. Model Dev. Discuss., <https://doi.org/10.5194/gmd-2019-20>, 2019.

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**Fig. 1.** Monthly mean sea-surface temperature in the first month of the reference simulation.

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**Fig. 2.** Monthly mean sea-surface temperature in the first month of the loose case simulation.

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We are thankful for the referee's positive feedback and the valuable comments that helped to improve the quality of the manuscript. Specific answers for the major comments follow this lines. The minor comments have been addressed and the corrections are included in the manuscript.

**Referee:** Overall assessing quality of simulations using RMS (or similar as used here) is a good approach. However it is useful to pair this with some representative map plots (or other data representation) which can give the readers a sense for the locations and scales of the errors. I would recommend the authors introduce these figures, particularly for the NEMO section.

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**Answer:** We have added a paragraph in section 3.1.3 explaining how the magnitude of the differences is below the thresholds defined and therefore inappreciable in a regular plot.

**Referee:** The authors reference multiple simulations for the NEMO runs. Could they clarify when they use multiple initial conditions and how sensitive the tests are to the initial conditions.

**Answer:** As it is explained in section 2.3, we were using different initial conditions to double-check the results. During the analysis, whenever an experiment was positively evaluated with the first set of initial conditions, it was re-evaluated with a second set of initial conditions to increase the confidence on the results. It has been clarified in the text.

**Referee:** The paper is hindered by its length, there are many points where too many words are used to communicate the necessary information. Cutting space can be a challenging task but the final product will be a paper where readers can easily digest all the information that the authors wish to communicate. Ideally the authors would run through the text and ask themselves whether there is a more concise way of communicating each point or whether the information needs to be communicated. I have highlighted just a few examples in my minor points below.

**Answer:** The authors have done an effort to reduce the length of the document. This included rephrasing several parts all along the document and the reviewed manuscript is three pages shorter. We believe that the quality of the document has improved and many parts have been simplified.

**Referee:** P7:S2.2 Designing accuracy tests. What is the purpose of this section? This question is more thoroughly discussed in the model-specific sections. I would advise removing this section.

**Answer:** Being able to determine if a result is accurate or not is a basic requirement for the analysis. The purpose of this section is to show a simple example that tries

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to illustrate that not only the actual results but also how we evaluate them will impact the method outputs. We consider that it is important to keep it in the manuscript but however we shortened it.

**Referee:** P8:L3-7 Unsure of the purpose of this example. Suggest removing.

**Answer:** The example was provided because in a previous review it was considered useful to show a simple case in which a result of an arithmetic operation was wrong only when both variables involved were using reduced precision. We consider it illustrative for audience without an extensive experience in the field.

**Referee:** P9:L15 Do you have a citation for this?

**Answer:** This affirmation is based in our own experiments but the results have not been published.

**Referee:** How are the quartiles defined? Over space?

**Answer:** For each output variable and for each time-step the quartiles are computed using the data of the full spatial domain.

**Referee:** \* How does the ratio of RMSD and IQR vary as a function of time generally? Are failed simulations more likely to exceed the threshold for early/late times?

**Answer:** Since the simulations with reduced precision start with the same initial conditions than the reference, the RMSD at the beginning is very small and grows with time. The specific trajectories depend on the output variable analyzed, the variables which precision is being reduced and other casuistic. There is interesting information that can be learned from the results of a precision analysis, for instance the specific impact of each variable that is determined to require double-precision. These kind of analyses, however, go beyond the scope of this manuscript and might be part of future work.

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Interactive comment on Geosci. Model Dev. Discuss., <https://doi.org/10.5194/gmd-2019-20>, 2019.

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We thank the editor to help us to adjust to the journal requirements. From the points exposed, we would like to do the following remarks.

- The contributions of the manuscript go beyond an individual model. If it is required to specify in the title which models have been explored in the document, the final title would be: *"How to use mixed precision in Ocean Models: exploring potential reduction of numerical precision in NEMO 4.0 and ROMS 3.6"*
- There has been a misunderstanding. Although we used the RPE tool. It is not the main contribution of the paper. There are few tools that have been devel-

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oped and already appear in the code availability section. These tools are publicly accessible, as well as the other sources cited.

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# How to use mixed precision in Ocean Models: exploring a potential reduction of numerical precision in NEMO 4.0 and ROMS 3.6

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**Abstract.** Mixed-precision approaches can provide substantial speed-ups for both computing- and memory-bound codes with little effort. Most scientific codes have overengineered the numerical precision leading to a situation where models are using more resources than required without knowing where they are required and where they are not. Consequently, it is possible to improve computational performance by establishing a more appropriate choice of precision. The only input that is needed is a method to determine which real variables can be represented with fewer bits without affecting the accuracy of the results. This paper presents a novel method that enables modern and legacy codes to benefit from a reduction of precision of certain variables without sacrificing accuracy. It consists of a simple idea: we reduce the precision of a group of variables and measure how it affects the outputs. Then we can evaluate the level of precision that they truly need. Modifying and recompiling the code for each case that has to be evaluated would require a prohibitive amount of effort. Instead, the method presented in this paper relies on the use of a tool called Reduced Precision Emulator (RPE) that can significantly streamline the process. Using the RPE and a list of parameters containing the precisions that will be used for each real variable in the code, it is possible within a single binary to emulate the effect on the outputs of a specific choice of precision. When we are able to emulate the effects of reduced precision, we can proceed with the design of the tests that will give us knowledge of the sensitivity of the model variables regarding their numerical precision. The number of possible combinations is prohibitively large and therefore impossible to explore. The alternative of performing a screening of the variables individually can give a certain insight about the required precision of variables, but on the other hand other complex interactions that involve several variables may remain hidden. Instead, we use a divide-and-conquer algorithm that identifies the parts that require high precision and establishes a set of variables that can. This method has been tested using two state-of-the-art ocean models, NEMO and ROMS, with very promising results. Obtaining this information is crucial to build an actual mixed precision version of the code in the next phase that will bring the promised performance benefits.

## 1 Introduction

Global warming and climate change are a great challenge for human kind, and given the social (e.g. Kniveton et al., 2012 regarding climate refugees), economic (e.g. Whiteman G, Hope C, 2013 regarding the trillion dollar problem) and environmental threat (e.g. Bellard et al., 2012 regarding mass extinctions) that it poses, any effort to understand and fight them fall short. A better knowledge and greater capacity to forecast how the climate will evolve can be a game changing achievement, since it could help to justify ambitious policies that adapt for future scenarios (Oreskes et al., 2010). The Earth System can be seen as an amalgamation of many parts: the atmosphere, the hydrosphere, the cryosphere, the land surface and the biosphere. All these elements are extremely rich in phenomena, and are open and inter-related. Fluxes of mass, heat and momentum interchange in ways that are virtually endless, some of which are poorly or not known. The magnitude and complexity of these systems make it difficult for scientists to observe and understand them fully. For this reason, the birth of computational science was a turning point, leading to the development of Earth System Models (ESMs) that allowed the execution of experiments that were impossible until then. ESMs, despite being incomplete, inaccurate and uncertain, have been a framework where possible to build upon knowledge, and have become crucial tools (Hegerl and Zwiers, 2011). Since their inception, the capability to mimic the climate system has increased, and with it the capacity to perform useful forecasts (Bauer et al., 2015). The main developments that have led to this improvement in model skill are the enhancement of the physical parameterizations, the use of ensemble forecasts, the improvement of the model initialization and increases in resolution (Bauer et al., 2015). Most of these contribute to a higher computational cost (see Randall et al., 2007). For this reason, these developments are only possible with an increasing availability of computing power, a situation that will continue in the future. The motivation to make models efficient is twofold. Firstly, developments that are considered crucial to increase the skill of the models require more computational power. This is not just a matter of having a larger machine since some of the issues that emerge are not trivial and require additional developments (Dennis and Loft, 2011). Secondly, the huge investment in computational resources that is necessary to perform simulations with ESMs implies that investing time in optimizing them will be of value.

One research field that has gained momentum in recent years and that can improve model performance is the use of mixed precision algorithms. Until not so long ago, the speed of most computations was constrained by how fast a CPU could perform operations, with the speed of the memory being fast enough to provide more data than the processor could process. In addition CPUs were designed in a way that they could virtually perform operations at the same speed no matter whether they were operating with 32-bit or 64-bit floating point representations. Therefore, the only benefit of using less precision was to reduce the memory requirements and the computational performance was not so much a motivation. Mainly two factors have changed that scenario. First, the CPU speed increased at a faster rate than memory speed meaning that at some point many codes that were CPU-bound before would become memory-bound, with the memory-bandwidth being insufficient to feed all the data that the processor can process. Second, vector operations doubled the number of floating point operations per cycle that could be performed when the number of bits of the representation is halved. For this reason, the use of smaller representations can now provide performance benefits that justify the effort of optimizing the numerical precision (Baboulin et al., 2009), and while this



is true with the actual hardware, the expected potential is even bigger in future architectures that will include not only 64-bit and 32-bit but also 16-bit arithmetic.

*We are now in a situation where ESMs, as computer codes of other domains, need to use computational resources efficiently and where mixed-precision approaches emerge as a potential solution to help improve efficiency.*

5 The main risk of reducing the precision is falling short, since using less precision than needed can lead to numerical errors that make model results inaccurate or simply wrong. The precision required depends on many factors, so what is needed is a method to identify which variables can effectively use less precision without compromising the quality of the simulations and which ones cannot. If the precision can be reduced, in many situations it is because the precision has been over engineered. One example is the precision used to represent the input data provided to ESMs. The precision of the physical observations  
10 is limited by the instruments used to collect them. In the case of sea surface temperature measurements from Earth orbiting satellites, this precision to a few tenths of a degree. 64-bit representations are often used when 16-bit could potentially be enough.

Recent work has demonstrated the potential benefits that mixed-precision approaches can provide to many different kinds of codes, since it is possible to achieve substantial speed-ups for both computing- and memory-bound codes requiring little effort  
15 with respect to the code (Baboulin et al., 2009). The spectrum of studies goes from explicit code manipulation in very specific algorithms to automatic modification of binaries of any kind of code. Some studies have focused on the use and development of mixed-precision algorithms to obtain performance benefits without compromising the accuracy of the results (Baboulin et al., 2009 and Haidar et al., 2018). There are also several automatic mixed-precision exploration tools (Graillat et al., 2016 Lam et al., 2012) that have been mainly tested on small benchmarks, usually C++ codes. These kinds of studies inspired Earth  
20 Science groups working with ESMs that are willing to improve their computational performance to make bigger and more ambitious experiments possible (Váňa et al., 2017, Düben et al., 2014, Düben et al., 2017, Düben et al., 2017 and Thornes, 2016). Inspired by previous work, we propose a method that automatically explores the precision required for the real variables used in state-of-the-art ESMs.

The method emerged while trying to explore how to achieve simulations as similar as possible to the standard double precision simulations whilst reducing the precision of some of the variables used. Our work extends the research aforementioned  
25 to achieve mixed precision implementations for full-scale models. To do so we rely on the Reduced Precision Emulator (RPE) (Dawson and Düben, 2017), that mimics the effects of using an arbitrary number of significant bits to represent the real variables in a code and measure the impact of a specific reduced precision configuration in the output produced by the model. Minimizing the user intervention by automating all the tedious intermediate processes allows an analysis of models that would  
30 have otherwise required too much manpower. Although the tool is very convenient for exploring the impact of the bits used to represent the mantissa of the floating point numbers, the effect of changing the number of bits devoted to represent the exponent is not explored.

To test the methodology, this work includes two case studies. These cases correspond to two different ocean models that are widely used worldwide: NEMO and ROMS. With these models we demonstrate how the methodology can be used with  
35 different applications, thus demonstrating its potential.

## 2 Method

In this section we will demonstrate how we can establish which real variables written in a Fortran code can effectively use less precision than the *de facto* 64-bits. The reader will find an explanation as to why and how we developed this method, with the specific steps of the methodology detailed below. The basic idea behind the method is to perform simulations with a Fortran model using a custom set of precisions and directly assess the outputs to see if the results are accurate enough. To do so we use the RPE tool, a Fortran library that allows us to simulate the result of a floating point operation given that the variables are using a specific number of significand bits. This can be integrated into an actual code to mimic the possible consequences of using reduced precision in certain variables. The advantage of the tool is the flexibility that it offers once implemented into the code, allowing us to easily test any given combination of precisions. The main drawback is the considerable overhead added to the simulations, increasing its cost.

The objective of the method is to find a set of precisions that minimizes the numerical resources used while keeping the accuracy of the results. A set of precisions is a specific combination of the precisions assigned to each variable, with  $52^n$  being the number of possible sets, where  $n$  is the number of real variables used in the code and 52 the number of bits used to describe the significand in a double-precision representation. This number makes it prohibitively expensive to explore all combinations. For any real-world code, this holds true even when not considering all possible values between 0 and 52 but just considering double-precision (64-bits), single-precision (32-bits) and half-precision (16-bits), where the number of possible sets is still  $3^n$ .

A feasible alternative is to perform a screening of the variables individually. The idea is to simply perform  $n$  simulations to observe what happens when all the variables are retained at high precision except the one that is being tested. While it is true that this approach can give an insight about the precision needed by a particular variable, it has some drawbacks. This approach can possibly miss most of the variables that require high precision, however it may not reveal many issues regarding more complex interactions between more than one variable. Additionally, building a complete set of variables from the tests performed on individual variables is not trivial at all i.e. a set which consists of variables that, as individuals, can use lower precision may not behave as such when combined and produce inaccurate results.

Another alternative is a divide-and-conquer algorithm that identifies the sections of the code that cannot handle reduced precision and builds a complete set of variables that can. Starting from a variable set that contains all the real variables that we want to analyze, the approach consists of evaluating what happens when the set uses reduced precision. If the results become inaccurate, we proceed to split the set in two parts which are evaluated individually. The process is recursive and ideally a binary search is performed until the sets that are evaluated contain only a single variable. If a set containing a single variable ends up being inaccurate, this variable is kept in high precision in the preceding sets when they are re-evaluated. The advantage of this approach is that it is cheaper to find all the variables that can individually compromise the results, and in addition it is easier to rebuild a complete set assimilating the results of the simulations of subsets that gave an accurate result.

Nevertheless, there are some elements that prevent this approach from working properly. The non-linearity of most of the Earth science codes implies that the differences between two simulations performed using different numerical precisions will not be constant. In many cases two accurate subsets resulted in an inaccurate set when combined. To increase the confidence in

the results, we propose to re-evaluate the sets whose results are accurate with different initial conditions. This method is similar to the ensemble simulation used in ESMs (Palmer et al. 2005), which tries to assess the uncertainty of the simulation outcomes by taking into consideration the uncertainty in the model inputs. The method remains the same adding an extra simulation initialized with different initial conditions for the sets that show accurate results. According to our results, an ensemble of only two members was required to solve most of the issues related with combinations of accurate subsets resulting in inaccurate sets.

The steps of the methodology, which are discussed in the next subsections, consist of:

- Implementing the emulator into the code, completing all the necessary actions to obtain a code that uses the emulator in which it is possible to select the precision of each real variable through a list of parameters.
- Establishing a test that will determine if the results of a simulation are accurate enough.
- Performing a precision analysis by launching the necessary tests to obtain a set of variables that can effectively use reduced precision passing the accuracy test.

## 2.1 Implementing the emulator

The RPE is a Fortran library that allows the user to emulate floating point arithmetic using a specific number of significant bits. It has the capability to emulate the use of arbitrary reduced floating-point precision. Its development was motivated by the need to explore mixed-precision approaches in large numerical models that demand more computational power, with weather and climate fields in mind, making the tool highly suitable for our purpose. The emulator is open source, can be accessed through github, has documentation available and a reference paper by Dawson and Düben (2017) with more detailed information.

Although the use of the emulator facilitates the testing of different precision configurations without recompiling, in large codes like ESMs the implementation of the emulator can carry more work than expected. The length of the code, the large development time, the quantity of different developers and the lack of a rigid style guide can end up with a large number of exceptions that make it harder to fully automate the emulator implementation, requiring the user to solve the emerging issues.

Our implementation of the emulator has two different parts:

1. Replacing the declaration of the real variables with the custom type `rpe_var`.
2. Introducing a method of selecting the precision of the variables without requiring recompilation of the code.

### 2.1.1 Replace variable declarations

To use the emulator, the user has to replace the declarations of the real variables with the custom type defined in the emulator library (see Dawson and Düben, 2017). Even though the idea is quite simple, the practical process in a complex and large state-of-the-art ESM can present several minor issues that can add up to a considerable amount of work. This is a list of some of the specific issues that can be found implementing the emulator:

- All the real variables that were initialized at declaration time need to be initialized providing a derived type variable instead of a real, which requires modification of all these declarations.
  - When a hard-coded real is used as a routine argument where the routine is expecting an rpe\_var variable, it is necessary to cast this hard-coded variable into a rpe\_var type variable.
- 5 (i.e. "call routine(*var*, 1.0, *var2*, 0.1)" has to be "call routine(*var*, rpe\_var(1.0), *var2*, rpe\_var(0.1))" )
- Although it is possible to adapt the RPE library to include intrinsic functions (i.e. max,min) that can use rpe\_var variables as arguments, there is still a problem when mixing rpe variables and real variables. The problem can be overcome converting all the variables to the same type.
  - When there is a call to an external library (i.e. netcdf, mpi), the arguments cannot be rpe\_var and must be reals.
- 10
- Read and write statements that expect a real variable cannot deal with rpe\_var variables.
  - Several other minor issues (pointer assignments, type conversions, used modules,...)

In codes with hundreds/thousands of variables this task can represent months/years of work, and for this reason it is worthwhile to automate the whole process. When all the issues are solved the model should be able to compile and run.

### 2.1.2 Selecting the precision

- 15 To specify at runtime the precision of each individual variable, the method that we use is to create a new Fortran module which includes an array of integers containing the precision value of each one of the real variables of the model. The values of this array will be read and assigned at the beginning of the simulation. After implementing the emulator into a code, one should be able to launch simulations specifying individually the number of significant bits used for each variable and obtain outputs, having completed the most arduous part of the proposed methodology.

### 20 2.2 Designing the accuracy tests

Once we are able to launch simulations, we must define how we will verify the results, the kind of experiment that we want to perform, and define a True/False test to perform on the outputs.

To define a test to verify results, we must define a function that can be applied to simulation output and determine if the outputs are correct.

- 25 To give an example, consider a simulation whose only output is a single scalar value, then we can consider that a given test is accurate if the output and reference match to a certain number of significant figures. Using the value of  $\pi$  as a reference, we can consider that a given simulation is accurate enough if the difference between the reference and the value obtained is smaller than a given threshold, i.e. the results coincide up to a specific number of significant figures. For example, a result accurate to 6 significant figures would pass if the required condition was to coincide with 4 significant figures, but would fail if it had to
- 30 coincide with 10.

## 2.3 Performing the analysis

We propose a recursive divide and conquer algorithm with few slight modifications. For a given set of variables, we generate a list of parameters that set these variables to use reduced precision and we launch a simulation. When the simulation is completed, we proceed to apply the accuracy test described in section 2.2. If the simulation with the specific set passes the test we consider it safe to reduce the precision of this set. If this is not the case, the purpose of the algorithm is to identify which part of the set is responsible for the inaccuracy: we proceed by sub-dividing the set and evaluating its parts separately until we have identified one of the variables that needs to preserve higher precision. The sets that yield inaccurate results require information from the subsets after these have been evaluated to be modified and reevaluated.

This initial approach has some drawbacks: On one hand, the effect of reducing the precision of a set of variables can not be directly deduced from what happens to its individual parts. The simplest case where this can happen is when we deal with two variables that appear in the same arithmetic operation: using the same logic as the actual processors, the emulator performs intermediate operations using the largest precision between the variables involved, so it may happen that having any of the two variables in higher precision will give an accurate enough result but not when both of the variables use reduced precision.

To illustrate this let's consider the following example: having two variables  $x$  and  $y$ , with  $x = 2^6$  and  $y = 2^{-6}$ , if we compute the sum  $z = x + y$  in real number arithmetic, the result is  $z = 64.015625$ . Both  $x$  and  $y$  can be perfectly represented using a 10-bit significand, but it is not the case for  $z$  that requires more numerical precision. Following the processor logic, if either  $x$  or  $y$  use a 52-bit significand, the computation of  $z$  will be done using 52 bits leading to a correct result, but if both variables are using 10 bits, the computation will be done using 10 bits and will yield a wrong result ( $z = 2^6$ ).

On the other hand, numerical error in most algorithms has a stochastic component which, combined with the non-linearity of these kind of models, can mean that a specific set of variables give accurate results under certain conditions, but gives inaccurate results under different conditions.

For these two reasons we added an extra test into our workflow that consists in assessing the results with different initial conditions whenever the first evaluation result in a positive outcome. While we cannot be sure that performing only a single re-evaluation will be enough, it can be sufficient for the most sensitive cases.

Another slight modification that we added to the initial approach is the definition of stricter thresholds for smaller subsets, to prevent the possibility of errors accumulating in bigger sets.

The entire algorithm is described in the pseudo-code presented in Appendix 1, that also contains the instructions that any given set has to follow in order to learn which elements of the set can use reduced precision.

## 3 Study cases

In this section we will present a proof of concept of the method using two state-of-the-art models, NEMO and ROMS. For each one of the two models we carried out two different experiments. With NEMO, we performed two analyses using different accuracy tests having as target to run using single-precision (23-bit significand). With ROMS, we performed two analyses

with the same accuracy tests but having two different reduced precision targets, single and half precision (23-bit and 10-bit significand). The section is divided in three parts, one part for each model and finally a discussion of the results.

### 3.1 NEMO

NEMO (Nucleus for European Modelling of the Ocean) is a state-of-the-art modelling framework of ocean related engines.

5 The physical core engines for the different parts of the model are the OPA engine for the ocean, LIM for the sea-ice and TOP-PISCES for biogeochemistry (Madec 2008, Rousset et al. 2015 and Aumont et al. 2015). The range of applications includes oceanographic research, operational oceanography, seasonal forecast and (paleo)climate studies.

Previous performance analyses of NEMO have shown that the most time-consuming routine was not even responsible for 20% of the total computation time (Tintó Prims et al., 2018). For this reason, any effort to improve the computational performance of the model cannot target a single region of the code but something that has to be applied along all the sections.

As explained in section 1, previous publications have demonstrated the positive impact that the use of mixed precision approaches can have on the performance of scientific models. Previous experiences in reducing the working precision of NEMO from 64-bit to 32-bit demonstrated a significant change in the results, indicating that blindly reducing the precision in the entire code was not an option.

15 To make the outcome of this work relevant for the modeling community, the analysis has been performed using the version 4.0b of the code that at the time of writing is the latest version available. The configuration used was an ocean-only simulation using the ORCA2 grid (about 220 km resolution near the equator) and the objective of the analysis is to identify which set of variables can effectively use 32-bit floating point representations instead of the 64-bit standard while keeping the difference with the reference below a chosen threshold.

#### 20 3.1.1 Emulator implementation

We have developed a tool (see code availability section) that not only modifies the source code to implement the emulator solving all the issues mentioned in the methods section, but also creates a database with information about the sources, including its modules, routines, functions, variables and their relations. This database will have several uses afterwards, since it can be used to generate the list of precisions assigned to each variable and to process the results of the analysis afterwards.

25 The code largely relies on MPI and netCDF. Since there is no special interest in analyzing these routines, a simple solution is to keep them unmodified. The selection of the source files that should not be modified requires user expertise. After that the tool handles all the necessary workarounds to ensure that the proper variable type is passed as routine arguments.

#### 3.1.2 Designing the accuracy tests

Our approach was to define a metric to evaluate how similar two simulations are, and define a threshold above which we will consider simulations inaccurate.

The metric used to evaluate the similarity between two simulation outputs is the Root Mean Square Deviation divided by the Interquartile Range. It is computed for each time step and the maximum value is retained.

$$RMSD(t) = \sqrt{\frac{\sum_{i=1}^{i_{max}} \sum_{j=1}^{j_{max}} \sum_{k=1}^{k_{max}} (ref_{i,j,k}(t) - x_{i,j,k}(t))^2}{i_{max} \cdot j_{max} \cdot k_{max}}} \quad (1)$$

where  $i, j, k$  are the spatial axis indices,  $t$  is the time index,  $ref_{i,j,k}(t)$  is the value of the reference simulation at a given point  $i, j, k$  and a given time  $t$  and  $x_{i,j,k}(t)$  the value of simulation that is being evaluated at the same point  $i, j, k$  and a given time  $t$ .

$$IQR(t) = Q3(t) - Q1(t) \quad (2)$$

where  $Q3$  and  $Q1$  are the values of the third quartile and first quartile respectively, and  $t$  is the time index.

So the final metric will be the accuracy score:

$$AccuracyScore = \max_{\forall t} \left( \frac{RMSD(t)}{IQR(t)} \right) \quad (3)$$

The final accuracy test can thus be defined as:

$$AccuracyTest(AccuracyScore, threshold) = \begin{cases} \text{True} & \text{if } AccuracyScore < threshold \\ \text{False} & \text{if } AccuracyScore \geq threshold \end{cases} \quad (4)$$

To be able to use the test defined above we need a reference simulation and to establish the thresholds. To obtain the reference simulation, first we have to define what we want to compare and the kind of test. For this analysis, we are using as a reference a 64-bit real variables version of the code. The runs consisted of 10-day simulations that produced daily outputs of the 3D temperature field, the 3D salinity field, and the column integrated heat and salt content. Temperature and salinity were selected because these are the two active tracers that appear in the model equations. Reference simulations were launched for each different initial condition that was used later in the analysis.

In order to define some meaningful thresholds, we performed a simulation using a halved time-step to compute the accuracy score against the reference simulation, to use this value as a first guess to define our thresholds (see Table 1). To show how defining different thresholds leads to different results and to emphasize how with this method is possible to keep arbitrarily small output differences, two different thresholds were defined (see Table 1). The first of the two thresholds is defined to be one thousand times smaller than the differences obtained using a halved time-step. The second is defined to be only ten times smaller. We will refer these cases as the tight case and the loose case respectively.

### 3.1.3 Executing the tests

To execute the tests, we implemented the rules described in the methodology section developing a python workflow manager capable of handling the dynamic workflow by creating the simulation scripts, launching them on a remote platform, then checking the status and the adequacy of the results.

Variable	Accuracy Score half-time step (AS)	Thresholds tight case (AS $\times 10^{-3}$ )	Thresholds loose case (AS $\times 10^{-1}$ )
Temperature (3D field)	$1.49 \times 10^{-3}$	$1.49 \times 10^{-6}$	$1.49 \times 10^{-4}$
Salinity (3D field)	$6.41 \times 10^{-3}$	$6.41 \times 10^{-6}$	$6.41 \times 10^{-4}$
Heat Content (2D field)	$2.74 \times 10^{-3}$	$2.74 \times 10^{-6}$	$2.74 \times 10^{-4}$
Salt Content (2D field)	$5.47 \times 10^{-6}$	$5.47 \times 10^{-9}$	$5.47 \times 10^{-7}$

**Table 1.** Accuracy score of the simulation performed using a time-step shorter than the reference and the different thresholds used for the different variables in the tight and loose cases. The thresholds for the tight case are defined multiplying the accuracy score of the half-time step simulations by  $10^{-3}$  and the thresholds for the loose case are defined multiplying the accuracy score of the half-time step by  $10^{-1}$ .

Processor	2 sockets Intel Xeon Platinum 8160 CPU with 24 cores each @ 2.10GHz for a total of 48 cores per node
Memory	L1d 32K; L1i cache 32K; L2 cache 1024K; L3 cache 33792K 96 GB of main memory 1.880 GB/core
Network	100 Gbit/s Intel Omni-Path HFI Silicon 100 Series PCI-E adapter 10 Gbit Ethernet
Local Storage	200 GB local SSD available as temporary storage during jobs

**Table 2.** Marenostrum 4 node specifications

To perform tests, the Marenostrum 4 supercomputer has been used (see table 2), with each individual simulation taking about 8 minutes 30 seconds on a single node.

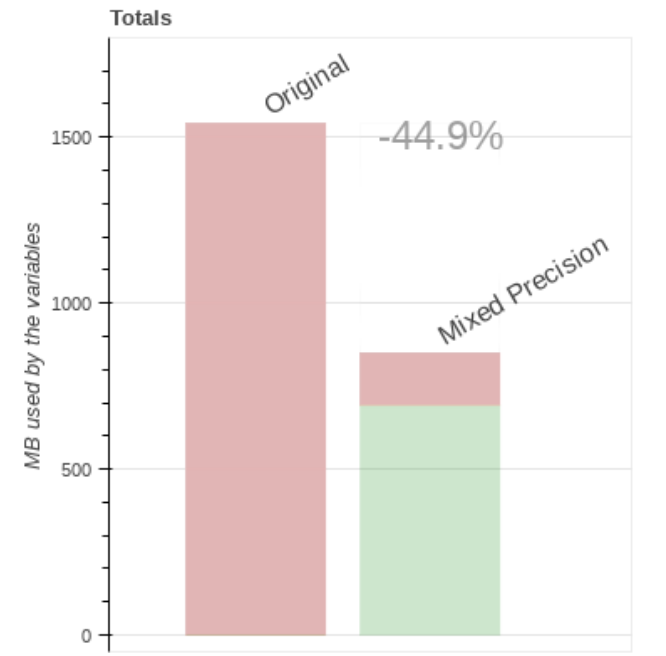


During the implementation of the emulator, the declarations of more than 3500 real variables were replaced with emulator variables. These variables can be scalars or arrays of up to 5 dimensions. They can be global variables or just temporary variables used only in a single line of code inside a subroutine. In a large code like NEMO there are usually parts of the code that are either used or not depending on the specific parameters employed. For this reason even when more than 3500 variables were identified, using our specific configuration only 942 are used. The variables that are used are identified during the runtime. Given that considering the unused variables for the analysis would be useless and dangerous (as incorrect conclusions could be drawn about which precision is needed) those are simply omitted from the analysis. The initial set used to start the analysis will therefore be the set containing the 942 variables that are actually used during our specific case.

### 3.1.4 Discussion

Starting with the evaluation of the initial set containing all the variables, the results show that a global reduction of the precision changes the results beyond what is acceptable. After running the full analysis for both cases we can see that the results differ. On one hand the tight case shows that 652 variables (69.2%) could use single-precision and on the other hand in the loose case the obtained solution contained 902 variables (95.8%), keeping only 40 variables in higher precision. As expected, defining looser thresholds allows the use of lower-precision in a larger portion of the variables. Table 3 presents the results split by arrays'





**Figure 1.** Estimation of the memory usage impact in an ORCA2 configuration using the set obtained with the loose accuracy test. The estimation has been performed using the dimensions of the variables and the size of the domain. In red (darker) we have the memory that is occupied by variables in double precision (100% in the original case), in light green the proportion of the memory occupied by variables in single precision, the difference between the original case and the loose case implies a potential 44.9% decrease in memory usage.

dimension. Also, the tighter case required more tests, with 1442 simulations required to arrive to the solution (consuming 204.3 node-hours), while the loose case required only 321 (consuming 45.5 node-hours).

The method ensures that the differences between the reduced-precision simulations performed with the final variable sets and the reference are below the determined thresholds. Since the thresholds for the two presented cases are so small, it means that the differences between the results are essentially negligible and would not be noticeable in a regular plot of the temperature, salinity, heat content or salt content.

The Figure 1 shows the expected impact in the memory usage when using the set obtained with the loose accuracy test. Since the results produced by both cases are so close to the reference simulation, Figure 1 only demonstrates the loose case since we anticipate that a mixed-precision implementation that is accepted by the scientific community would be more similar to the loose case.

### 3.2 ROMS

The Regional Ocean Model System (ROMS) is a free-surface, hydrostatic, primitive equation ocean model that uses stretched, terrain-following coordinates on the vertical and orthogonal curvilinear coordinates on the horizontal. It contains a variety of

Dimension	Total variables	Tight case		Loose case	
		n	%	n	%
0	374	304	81.3	366	97.9
1	32	23	71.9	32	100.0
2	322	216	67.1	307	95.3
3	200	105	52.5	190	95.0
4	13	3	23.1	6	46.2
5	1	1	100.0	1	100.0
TOTAL	942	652	69.2	902	95.8

**Table 3.** The table presents the total number of variables that were included in the analysis split by the dimension of the arrays (0 for scalars). Also, the number of variables that can safely use single-precision for the two cases discussed in section 3.1 (tight and loose) and the percentage of the total variables that this represents. Using tight constrains 69.2 % of the variables can use single-precision, although only 52.5 % of the 3D variables are responsible for the most memory usage. Using loose conditions, 95.8% of the variables can use single-precision, including 95% of the 3D variables.

features including high-order advection schemes; accurate pressure gradient algorithms; several subgrid-scale parameterizations; atmospheric, oceanic, and benthic boundary layers, biological modules, radiation boundary conditions, and data assimilation (<http://www.myroms.org>).

The experiments performed with ROMS were done applying the primal form of incremental strong constraint 4D-Var (4DVAR) [Moore et al. 2011](#). The configuration used is the U.S. west coast at 1/3 degree horizontal, referred to as WC13, a standard model test case. It has 30 km horizontal resolution, and 30 levels on the vertical (<http://www.myroms.org>). This configuration was selected because a 4DVAR ROMS has a large community of users, there is an easy-to-follow tutorial to set-up the configuration and involves linear models that make this an interesting choice to expand the results obtained in Section 3.1.

To perform this analysis, we set up the tutorial available online that performs a I4DVAR data assimilation cycle that spans the period 3-6 January, 2004. The observations assimilated into the model are satellite sea surface temperature, satellite sea surface height in the form of a gridded product from Aviso, and hydrographic observations of temperature and salinity collected from Argo floats and during the GLOBEC/LTOP and CalCOFI cruises off the coast of Oregon and southern California, respectively.

With the I4DVAR version of ROMS, most of the computational time is spent inside the data assimilation “inner loops”, within the adjoint and tangent linear sub-models (AD and TL respectively). To give some numbers, in a simulation with the WC13 configuration, 35% of the time is spent in the TL model and 50% in the AD model while the time spent in the nonlinear model is below 14%. It was felt that since the TL and AD models are used to compute an approximation gradient of the I4DVAR cost function, further approximations in the gradient resulting from lower precision will probably be not so detrimental leading to our starting hypothesis that the AD and TL models are better targets than the nonlinear model. However, for this hypothesis to be true the AD needs to keep being the transpose of the TL to within a chosen precision, otherwise it might prevent the

convergence of the algorithm. For this reason, we are trying to minimize the precision used in these regions of the code. In this case, the target reduced precision is not limited to single-precision (23-bit significand) but also the half-precision is explored (10-bit significand).

5 It is important to remark that in our experiments the number of bits used to represent the exponent of the variables is 11 (the same number as used in double-precision), no matter which number of bits is used for the significand. In practice, it means that to ensure that it is possible to reduce the precision to half-precision we would need to ensure that the values do not exceed the range that can be represented with a smaller exponent. However, the results are still interesting because we can learn the potential use of reduced number of bits for the significand.

### 3.2.1 Emulator Implementation

10 One aspect that made this exercise different from that of NEMO in terms of implementing the emulator was that the interest was focused on specific regions of the code, i.e. the parts related to the tangent linear model and the adjoint model.

### 3.2.2 Designing the tests

When running a data assimilation experiment, the objective is to obtain a coherent state of the ocean that minimizes the difference between the model and the observations. Through different forward-backward iterations using the TL and AD  
15 models, the model should converge to a state where the cost function (function that describes the difference between the model state and the observations) is minimum. We can consider that a simulation is accurate enough if the model converges to the same result as the double-precision reference. Through the different iterations, the solution should converge to a minimum. To set a threshold for the accuracy of the simulations, we can look at the difference between the last two inner-loop iterations. In the reference simulation the value of this difference computed as a cost function defined in the model is is of  $1.77 \times 10^{-1}$   
20 . Defining a threshold 10 times smaller ( $1.77 \times 10^{-2}$ ) ensures that the impact of reducing the precision will be smaller than changing the number of inner iterations performed.

### 3.2.3 Executing the tests

For ROMS, we use the same workflow manager developed for NEMO, simply using different templates for launching simulations and evaluating the results.

### 25 3.2.4 Discussion

As in the case with NEMO, we first performed the reference executions for all the different initial conditions, using 64-bit precision.

The parts selected for the analysis contain 1556 real variable declarations, of which 1144 are actually used in our case. Starting with this initial set and trying to use a 23-bit significand, the results showed that in fact all the variables can use  
30 reduced precision at once while still obtaining accurate results.

Dimension	Total variables	23-bits		10-bits	
		n	%	n	%
0	326	326	100.0	277	85.0
1	82	82	100.0	71	86.6
2	450	450	100.0	385	85.6
3	173	173	100.0	135	78.0
4	78	78	100.0	44	56.4
5	31	31	100.0	9	29.0
6	4	4	100.0	2	50.0
40	2	2	100.0	2	100.0
TOTAL	1146	1146	100.0	925	80.7

**Table 4.** The table presents the total number of variables that were included in the ROMS analysis split by the dimension of the arrays (0 for scalars). Also, the number of variables that can safely use reduced-precision for the two cases discussed in section 3.2 (single and half precision ) and the percentage of the total variables that they represent. The single-precision case was trivial since all the variables considered can use single-precision while keeping the accuracy. For the half-precision case, 80.7% of the variables could use half-precision, although the proportion of variables that can use reduced precision becomes less as the dimension increases.

This suggests that this model and in particular this specific configuration are suitable for a more drastic reduction of the numerical precision. To test that, we proceeded with a new analysis using a 10-bit significand. The first simulation of the analysis crashed, not providing any output and showing that it is not possible to reduce the precision to 10-bit overall. Using the analysis to find where this precision can be used, the results show that a 80.7% of the variables can use 10-bit instead of 52. Looking to the effects produced by the variables that were not able to use 10-bit precision we could see that only a single variable was preventing the model from completing the simulations, even though many others were introducing too many numerical errors. In Table 4 the results are presented split by dimension.

### 3.3 Common discussion

From the two exercises shown in section 3 we can draw several conclusions. The most important is that the method can provide a set of variables that can use reduced numerical precision preserving the accuracy of the results, as it was observed in the four cases explored (two different accuracy tests for NEMO and two target precisions for ROMS). The results in the four cases showed that the potential to reduce the numerical precision is considerable even in the most constrained cases (i.e. NEMO tight). In the NEMO case, the analysis covers the full model, while the ROMS case was focused only on a part of the model, demonstrating the versatility of the method. It has also been shown that it is possible to achieve results that are arbitrarily close to the reference, while requiring more exact results will have the cost of leaving more parts of the code in higher precision.

## 4 Conclusions

Previous works suggested that the generalized use of double precision for Earth Science modelling is a case of over-engineering and that for this reason adapting the computational models to use the smallest numerical precision that is essential would compensate in terms of improvement in performance. However, an improper reduction can lead to accuracy losses that may make the results unreliable. In this manuscript we presented a method that was designed to solve this problem by finding which variables can use a lower level of precision without degrading the accuracy of the results.

The method was thought and designed to be applied to computational ocean models coded in Fortran. It relies on the Reduced Precision Emulator tool that was created to help understand the effect of reduced precision within numerical simulations, it allows us to simulate the results that would be produced in case of performing the arithmetic operations in reduced precision, using a custom number of significant bits for each floating point variable. The proposed analysis algorithm finds which variables need to be kept in double precision and which ones can use reduced precision without impacting the accuracy of the results.

The method has been tested with two widely used state-of-the-art ocean models, NEMO and ROMS. The experiences with the two models pursued different objectives. With NEMO, the analysis covered all the routines and variables used within the ocean-only simulation, the target precision was 32-bits and we explored how the selection of a specific accuracy tests changes which variables can safely use reduced precision. However with ROMS, the analysis covered only the variables belonging to the adjoin and tangent linear models, using a single accuracy test and examining how the method can be used to discover the viability of using numerical precisions below 32-bits.

The results presented in this work allows us to draw some conclusions. It is shown that both models can use reduced precision for large portions of the code proving the feasibility of mixed precision approaches, and the method described is able to find these. The method can also provide a configuration that can be arbitrarily close to the double-precision reference, where the amount of variables that can use reduced-precision will depend on how strict the imposed conditions are.

Users might want to follow the method presented here to build a version of the model that can benefit from the reduction of the precision and can be used by the whole community without concerns.

*Code and data availability.* Releases of the Reduced Precision Emulator library are available at <https://github.com/aopp-pred/rpe> (last accessed in January 2019). The tool developed to automatically implement RPE can be found at <https://earth.bsc.es/gitlab/otinto/AutoRPE>. The workflow manager used to manage the analysis simulations can be found in <https://earth.bsc.es/gitlab/otinto/AutoRPE>. The source code of NEMO model and the input data used for the experiments referred in this work can be found in [www.nemo-ocean.eu](http://www.nemo-ocean.eu) (last accessed in January 2019). The source code of the ROMS model can be found in [www.myroms.org](http://www.myroms.org), can be freely accessed under registration. The details and input data used for the experiments involving ROMS can be found in [www.myroms.org/wiki/I4DVAR\\_Tutorial](http://www.myroms.org/wiki/I4DVAR_Tutorial) (last accessed in January 2019).

*Author contributions.* Oriol Tintó Prims led the design of the method, the experiments and the writing of the manuscript, Mario C. Acosta supervised all the process and had a main role in the writing of the manuscript, Andrew M. Moore participated in the design of the experiments involving ROMS and the writing of the manuscript, Miguel Castrillo was involved in the discussion and design of the method and the experiments and participated in the writing of the manuscript, Kim Serradell, Ana Cortés and Francisco J. Doblas-Reyes participated in the  
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## Appendix A

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**Algorithm 1** The analysis algorithm describes the actions that have to be taken in a given set that has a given status. Using that framework, the list of possible statuses is: **Pending**: the set is ready to be evaluated, **Running**: the set is being evaluated, **Asserting**: the set had a successful evaluation and it is ready to be reevaluated using a different configuration, **Suspended**: the set had an unsuccessful evaluation and now it is waiting for the results of its child subsets, **Failed**: the set had a unsuccessful evaluation and can not be further divided.

---

```
if STATUS is PENDING then
  submit job
  set STATUS to RUNNING
else if STATUS is RUNNING then
  Check job status in remote machine
  if SIMULATION was SUCCESSFUL then
    Assert results and set STATUS to ASSERTING
  else
    if the set can be divided then
      Create and submit sub-sets and set STATUS to SUSPENDED
    else
      Set STATUS to FAILED
    end if
  end if
else if STATUS is ASSERTING then
  Check assertion job status in remote machine
  if job status is COMPLETED then
    Check results:
    if results are successful then
      Set STATUS to SUCCESS
    else
      if set can be divided then
        Create and submit sub-sets and set STATUS to SUSPENDED
      else
        Set STATUS to FAILED
      end if
    end if
  end if
else if STATUS is SUSPENDED then
  Check subsets STATUS
  if subsets are [FAILED or SUCCESS] then
    if Both subsets FAILED then
      Set STATUS to FAILED
    else
      Integrate subset information and set STATUS to PENDING
    end if
  end if
end if
```

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