

1 **Developing a monthly radiative kernel for surface albedo change from satellite**
2 **climatologies of Earth’s shortwave radiation budget: CACK v1.0**

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13 **Abstract**

14 Due to the potential for land use / land cover change (LULCC) to alter surface albedo, there is
15 need within the LULCC science community for simple and transparent tools for predicting
16 radiative forcings (ΔF) from surface albedo changes ($\Delta\alpha_s$). To that end, the radiative kernel
17 technique – developed by the climate modeling community to diagnose internal feedbacks
18 within general circulation models (GCMs) – has been adopted by the LULCC science
19 community as a tool to perform offline ΔF calculations for $\Delta\alpha_s$. However, the codes and
20 data behind the GCM kernels are not readily transparent, and the climatologies of the
21 atmospheric state variables used to derive them vary widely both in time period and duration.
22 Observation-based kernels offer an attractive alternative to GCM-based kernels and could be
23 updated annually at relatively low costs. Here, we present a radiative kernel for surface
24 albedo change founded on a novel, simplified parameterization of shortwave radiative transfer
25 driven with inputs from the Clouds and the Earth’s Radiant Energy System (CERES) Energy

26 Balance and Filled (EBAF) products. When constructed on a 16-year climatology (2001-
27 2016), we find that the CERES-based albedo change kernel – or CACK – agrees remarkably
28 well with the mean kernel of four GCMs (rRMSE = 14%). When the novel parameterization
29 underlying CACK is applied to emulate two of the GCM kernels using their own boundary
30 fluxes as input, we find even greater agreement (mean rRMSE = 7.4%), suggesting that this
31 simple and transparent parameterization represents a credible candidate for a satellite-based
32 alternative to GCM kernels. We document and compute the various sources of uncertainty
33 underlying CACK and include them as part of a more extensive dataset (CACK v1.0) while
34 providing examples showcasing its application.

35 **Keywords:** GCM, radiative forcing, land use change, land cover change, LULCC

36

37 **1. Introduction**

38 Diagnosing changes to the shortwave radiation balance at the top-of-the-atmosphere (TOA)
39 resulting from changes to albedo at the surface ($\Delta\alpha_s$) is an important step in predicting
40 climate change. However, outside the climate science community, many researchers do not
41 have the tools to convert $\Delta\alpha$ to the climate-relevant ΔF measure (Bright, 2015; Jones et al.,
42 2015), which requires a detailed representation of the atmospheric constituents that absorb or
43 scatter solar radiation (e.g. cloud, aerosols, and gases) and a sophisticated radiative transfer
44 code. For single points in space or for small regions, these calculations are typically
45 performed offline – meaning without feedbacks to the atmosphere (e.g., (Randerson et al.,
46 2006))). Large-scale investigations (e.g. Amazonian or pan-boreal LULCC (Bonan et al.,
47 1992; Dickinson and Henderson-Sellers, 1988)) typically prescribe the land surface layer in a
48 GCM with initial and perturbed states, allowing the radiative transfer code to interact with the
49 rest of the model. While this has the benefit of allowing interaction and feedbacks between
50 surface albedo and scattering or absorbing components of the model, such an approach is

51 computationally expensive and thereby restricts the number of LULCC scenarios that can be
52 investigated (Atwood et al., 2016). Consequently, this method does not meet the needs of
53 some modern LULCC studies which may require millions of individual land cover transitions
54 to be evaluated cost effectively (Ghimire et al., 2014; Lutz and Howarth, 2015).

55 Within the LULCC science community, two methods have primarily met the need for
56 efficient ΔF calculations from $\Delta\alpha_s$: simplified parameterizations of atmospheric transfer of
57 shortwave radiation (Bozzi et al., 2015; Bright and Kvalevåg, 2013; Caiazzo et al., 2014;
58 Carrer et al., 2018; Cherubini et al., 2012; Muñoz et al., 2010), and radiative kernels (Ghimire
59 et al., 2014; O'Halloran et al., 2012; Vanderhoof et al., 2013) derived from sophisticated
60 radiative transfer schemes embedded in GCMs (Block and Mauritsen, 2014; Pendergrass et
61 al., 2018; Shell et al., 2008; Soden et al., 2008). Simplified parameterizations of the LULCC
62 science community have not been evaluated comprehensively in space and time. Bright &
63 Kvalevåg (2013) evaluated the shortwave ΔF parameterization of Cherubini *et al.* (2012)
64 when applied at several globally distributed sites on land, finding inconsistencies in
65 performance at individual sites despite good overall cross-site performance. Radiative kernels
66 (Block and Mauritsen, 2014; Pendergrass et al., 2018; Shell et al., 2008; Soden et al., 2008) –
67 while being based on state-of-the-art models of radiative transfer – have the downside of
68 being model-dependent and not readily transparent. While the radiative transfer codes behind
69 them are well-documented, the scattering components (i.e. aerosols, gases, and clouds)
70 affecting transmission have many simplifying parameterizations, vary widely across models,
71 and may contain significant biases (Dolinar et al., 2015; Wang and Su, 2013). An additional
72 downside is that the atmospheric state climatologies used to compute the GCM kernels vary
73 widely in their time periods (i.e., from pre-industrial to the year 2007) and durations (from 1
74 to 1,000 yrs). The application of a state-dependent GCM kernel that is outdated may be
75 undesirable in regions undergoing rapid changes in cloud cover or aerosol optical depth, such

76 as in the northwest United States (Free and Sun, 2014) and in southern and eastern Asia
77 (Srivastava, 2017; Zhao et al., 2018), respectively. An albedo change kernel based on Earth-
78 orbiting satellite products could be updated annually to capture changes in atmospheric state
79 at relatively low costs.

80 The NASA Clouds and the Earth’s Radiant Energy System (CERES) Energy Balance and
81 Filled (EBAF) products (CERES Science Team, 2018a, b), which are based largely on
82 satellite optical remote sensing, provide the monthly mean boundary fluxes and other
83 atmospheric state information (e.g., cloud area fraction, cloud optical depth) that could be
84 used to develop a more empirically-based alternative to the GCM-based kernels. The latest
85 EBAF-TOA Ed4.0 (version 4.0) products have many improvements with respect to the
86 previous version (version 2.8, Loeb et al. 2009), including the use of advanced and more
87 consistent input data, retrieval of cloud properties, and instrument calibration (Kato et al.,
88 2018; Loeb et al., 2017).

89 Here, we present an albedo change kernel based on the CERES EBAF v4 products – or
90 CACK. Underlying CACK is a simplified model of shortwave radiative transfer through a
91 one-layer atmosphere. The model form (or parameterization) is selected after a two-stage
92 performance evaluation of six model candidates: two analytical, one semi-empirical, and
93 three empirical. An initial performance screening is implemented where all six model
94 candidates are driven with a 16-year climatology (January 2001 – December 2016) of
95 monthly all-sky boundary fluxes from CERES, with the resulting kernels benchmarked both
96 qualitatively and quantitatively against the mean of four GCM-based kernels (Block and
97 Mauritsen, 2014; Pendergrass et al., 2018; Shell et al., 2008; Soden et al., 2008). Top model
98 candidates from the initial performance screening are then subjected to an additional
99 performance evaluation where they are applied to emulate two GCM kernels using their own

100 boundary fluxes as input, which eliminates possible biases related to differences in the GCM
 101 representation of clouds or other atmosphere state variables.

102 We start in Section 2 by providing a brief overview of existing approaches applied in LULCC
 103 climate studies for estimating ΔF from $\Delta\alpha$. We then present the six model candidates in
 104 Section 3. Section 4 describes the model evaluation and uncertainty quantification methods,
 105 in addition to two application examples. Results are presented in Section 5, while Section 6
 106 discusses the merits and uncertainties of a CERES-based kernel relative to GCM-based
 107 kernels.

108 **2 Review of existing approaches**

109 Earth's energy balance (at TOA) in an equilibrium state can be written:

$$110 \quad 0 = F = LW_{\uparrow}^{TOA} - (SW_{\downarrow}^{TOA} - SW_{\uparrow}^{TOA}) \quad (1)$$

111 where the equilibrium flux F is a balance between the net solar energy inputs ($SW_{\downarrow}^{TOA} - SW_{\uparrow}^{TOA}$
 112) and thermal energy output (LW_{\uparrow}^{TOA}). Perturbing this balance results in a radiative forcing
 113 ΔF , while perturbing the shortwave component is referred to as a shortwave radiative forcing
 114 and may be written as:

$$115 \quad \Delta F = \Delta(SW_{\downarrow}^{TOA} - SW_{\uparrow}^{TOA}) = \Delta SW_{\downarrow}^{TOA} \left(1 - \frac{SW_{\uparrow}^{TOA}}{SW_{\downarrow}^{TOA}} \right) - SW_{\downarrow}^{TOA} \left(\Delta \frac{SW_{\uparrow}^{TOA}}{SW_{\downarrow}^{TOA}} \right) \quad (2)$$

116 where the shortwave radiative forcing results either from changes to solar energy inputs (
 117 $\Delta SW_{\downarrow}^{TOA}$) or from internal perturbations within the Earth system ($\Delta \frac{SW_{\uparrow}^{TOA}}{SW_{\downarrow}^{TOA}}$). The latter can
 118 be brought about by changes to the reflective properties of Earth's surface which is the focus
 119 of this paper.

120 *a. GCM-based radiative kernels*

121 The radiative kernel technique was developed as a way to assess various climate feedbacks
 122 from climate change simulations across multiple climate models in a computationally efficient
 123 manner (Shell et al., 2008; Soden et al., 2008). A radiative kernel is defined as the differential
 124 response of an outgoing radiation flux at TOA to an incremental change in some climate state
 125 variable -- such as water vapor, air temperature, or surface albedo (Soden et al., 2008). To
 126 generate a radiative kernel for a change in surface albedo with a GCM, the prescribed surface
 127 albedo change is perturbed incrementally by 1%, and the response by the outgoing shortwave
 128 radiation flux at TOA is recorded:

$$129 \quad \Delta SW_{\uparrow}^{TOA} = SW_{\uparrow}^{TOA}(\alpha_s + \Delta\alpha_s) - SW_{\uparrow}^{TOA}(\alpha_s) = \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta\alpha_s \equiv K_{\alpha_s} \Delta\alpha_s \quad (3)$$

130 where SW_{\uparrow}^{TOA} is the outgoing shortwave flux at TOA and K_{α_s} is the radiative kernel (in Wm^{-2})
 131 which can then be used with Eq. (1) to estimate an instantaneous shortwave radiative
 132 forcing (ΔF) at TOA:

$$133 \quad \begin{aligned} F + \Delta F &= LW_{\uparrow}^{TOA} - (SW_{\downarrow}^{TOA} - SW_{\uparrow}^{TOA} + K_{\alpha_s} \Delta\alpha_s) \\ \Delta F &= -K_{\alpha_s} \Delta\alpha_s \end{aligned} \quad (4)$$

134 To the best of our knowledge, four albedo change kernels have been developed based on the
 135 following GCMs: the Community Atmosphere Model version 3, or CAM3 (Shell et al.,
 136 2008), the Community Atmosphere Model version 5, or CAM5 (Pendergrass et al., 2018), the
 137 European Center and Hamburg model version 6, or ECHAM6 (Block and Mauritsen, 2014),
 138 and the Geophysical Fluid Dynamics Laboratory model version AM2p12b, or GFDL (Soden
 139 et al., 2008). These four GCM kernels vary in their vertical and horizontal resolutions, their
 140 parameterizations of shortwave radiative transfer, and their prescribed atmospheric state
 141 climatologies. These differences are summarized in Table 1. Apart from differences in their

142 prescribed atmospheric background states and radiative transfer schemes, a major source of
143 uncertainty in GCM-based kernels is related to the GCM representation of atmospheric liquid
144 water/ice associated with convective clouds; of the four aforementioned GCMs, only CAM5
145 and GFDL attempt to model the effects of convective core ice and liquid in their radiation
146 calculations (Li et al., 2013).

147

148 < Table 1 >

149

150 *b. Single-layer atmosphere models of shortwave radiation transfer*

151 Within the atmospheric science community, various simplified analytical or semi-empirical
152 modeling frameworks have been developed, either to diagnose effective surface and
153 atmospheric optical properties from climate model outputs, or to study the relative
154 contributions of changes to these properties on shortwave flux changes at the top and bottom
155 of the atmosphere (Atwood et al., 2016; Donohoe and Battisti, 2011; Kashimura et al., 2017;
156 Qu and Hall, 2006; Rasool and Schneider, 1971; Taylor et al., 2007; Winton, 2005; Winton,
157 2006). While these frameworks all treat the atmosphere as a single layer, they differ by
158 whether or not the reflection and transmission properties of this layer are assumed to have a
159 directional dependency (Stephens et al., 2015) and by whether or not inputs other than those
160 derived from the boundary fluxes are required (e.g. cloud properties; (Qu and Hall, 2006)).

161 Winton (2005) presented a semi-empirical four-parameter optical model to account for the
162 directional dependency of up- and downwelling shortwave fluxes through the one-layer
163 atmosphere and found good agreement ($rRMSE < 2\%$ globally) when benchmarked to online
164 radiative transfer calculations. Also considering a directional dependency of the atmospheric
165 optical properties, Taylor et al. (2007) presented a two-parameter analytical model where
166 atmospheric absorption was assumed to occur at a level above atmospheric reflection. The

167 analytical model of Donohoe and Battisti (2011) subsequently relaxed the directional
168 dependency assumption and found the atmospheric attenuation of the surface albedo
169 contribution to planetary albedo to be 8% higher than the model of Taylor et al. (2007).
170 Elsewhere, Qu & Hall (2006) developed an analytical framework making use of additional
171 atmospheric properties such as cloud cover fraction, cloud optical thickness, and the clear-sky
172 planetary albedo, which proved highly accurate when model estimates of planetary albedo
173 were evaluated against climate models and satellite-based datasets.

174 *c. Simple empirical parameterizations of the LULCC science community*

175 Two simple empirical parameterizations of shortwave radiative transfer have been widely
176 applied within the LULCC science community for estimating ΔF from $\Delta\alpha_s$ (Bozzi et al.,
177 2015; Caiazzo et al., 2014; Carrer et al., 2018; Cherubini et al., 2012; Lutz et al., 2015;
178 Muñoz et al., 2010). While these parameterizations are also based on a single-layer
179 atmosphere model of shortwave radiative transfer, at the core of these parameterizations is the
180 fundamental assumption that radiative transfer is wholly independent of (or unaffected by)
181 $\Delta\alpha_s$. In other words, they neglect the change in the attenuating effect of multiple reflections
182 between the surface and the atmosphere that accompanies a change to the surface albedo.
183 Nevertheless, due to their simplicity and ease of application they continue to be widely
184 employed in climate research.

185 **3. Kernel model candidates**

186 The six candidate models (or parameterizations) for a CERES-based albedo change kernel
187 (CACK) are presented henceforth. All requisite variables and their derivatives may be
188 obtained directly from the CERES EBAF v4 products (at monthly and $1^\circ \times 1^\circ$ resolution) and
189 are presented in Table 2. To improve readability, temporal and spatial indexing is neglected
190 and all terms presented henceforth in Section 3 denote the monthly pixel means.

191 < Table 2 >

192 *a. Analytical kernels*

193 The first kernel candidate may be analytically-derived from the CERES EBAF all-sky
194 boundary fluxes and their derivatives. The surface contribution to the outgoing shortwave
195 flux at TOA $SW_{\uparrow,SFC}^{TOA}$ can be expressed (Donohoe and Battisti, 2011; Stephens et al., 2015;
196 Winton, 2005) as:

$$197 \quad SW_{\uparrow,SFC}^{TOA} = SW_{\downarrow}^{TOA} \alpha_s \frac{(1-r-a)^2}{(1-r\alpha_s)} \quad (5)$$

198 where r is a single pass atmospheric reflection coefficient, a is a single pass atmospheric
199 absorption coefficient, SW_{\downarrow}^{TOA} is the extraterrestrial (downwelling) shortwave flux at TOA,
200 and α_s is the surface albedo (defined in Table 2). The expression in the denominator of the
201 righthand term represents a fraction attenuated by multiple reflections between the surface
202 and the atmosphere. This model assumes that the atmospheric optical properties r and a are
203 insensitive to the origin and direction of shortwave fluxes – or in other words – that they are
204 isotropic.

205 The single-pass reflectance coefficient is calculated from the system boundary fluxes (Table
206 2) following Winton (2005) and Kashimura *et al.* (2017):

$$207 \quad r = \frac{SW_{\downarrow}^{TOA} SW_{\uparrow}^{TOA} - SW_{\downarrow}^{SFC} SW_{\uparrow}^{SFC}}{SW_{\downarrow}^{TOA 2} - SW_{\uparrow}^{SFC 2}} \quad (6)$$

208 while the single-pass absorption coefficient a is given as:

$$209 \quad a = 1 - r - T(1 - \alpha_s r) \quad (7)$$

210 where T is the clearness index (defined in Table 2). Our interest is in quantifying the $SW_{\uparrow,SFC}^{TOA}$
 211 response to an albedo perturbation at the surface – or the partial derivative of $SW_{\uparrow,SFC}^{TOA}$ with
 212 respect to α in Eq. (5):

$$213 \quad \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s = K_{\alpha_s}^{ISO} \Delta \alpha_s = \frac{SW_{\downarrow}^{TOA} (1-r-a)^2}{(1-r\alpha_s)^2} \Delta \alpha_s \quad (8)$$

214 where $K_{\alpha_s}^{ISO}$ is referred to henceforth as the *Isotropic* kernel.

215 The second analytical kernel is based on the model of Qu and Hall (2006) which makes use of
 216 auxiliary cloud property information commonly provided in satellite-based products of
 217 Earth’s radiation budget – including CERES EBAF – such as cloud cover area fraction, cloud
 218 visible optical depth, and clear-sky planetary albedo. This model links all-sky and clear-sky
 219 effective atmospheric transmissivities of the earth system through a linear coefficient k
 220 relating the logarithm of cloud visible optical depth to the effective all-sky atmospheric
 221 transmissivity:

$$222 \quad k = \frac{(T_{a,CLR}) - (T_a)}{\ln(\tau + 1)} \quad (9)$$

223 where $T_{a,CLR}$ is the clear-sky effective system transmissivity, T_a is the all-sky effective system
 224 transmissivity, and τ is the cloud visible optical depth. This linear coefficient can then be
 225 used together with the cloud cover area fraction to derive a shortwave kernel based on the
 226 model of Qu and Hall (2006) – or $K_{\alpha_s}^{QH06}$:

$$227 \quad \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s = K_{\alpha_s}^{QH06} \Delta \alpha_s = SW_{\downarrow}^{SFC} [(T_a) - kc \ln(\tau + 1)] \Delta \alpha_s \quad (10)$$

228 where c is the cloud cover area fraction.

229 *b. Semi-empirical kernel*

230 The third kernel makes use of three directionally-dependent (anisotropic) bulk optical
 231 properties r_{\uparrow} , t_{\uparrow} , and t_{\downarrow} , where the first is the atmospheric reflectivity to upwelling
 232 shortwave radiation and the latter two are the atmospheric transmission coefficients for
 233 upwelling and downwelling shortwave radiation, respectively (Winton, 2005). It is not
 234 possible to derive r_{\uparrow} analytically from the all-sky boundary fluxes; however, Winton (2005)
 235 provides an empirical formula relating upwelling reflectivity r_{\uparrow} to the ratio of all-sky to clear-
 236 sky fluxes incident at surface:

$$237 \quad r_{\uparrow} = 0.05 + 0.85 \left(1 - \frac{SW_{\downarrow}^{SFC}}{SW_{\downarrow,CLR}^{SFC}} \right) \quad (11)$$

238 where $SW_{\downarrow,CLR}^{SFC}$ is the clear-sky shortwave flux incident at the surface.

239 Knowing r_{\uparrow} , we can then solve for the two remaining optical parameters needed to obtain our
 240 kernel:

$$241 \quad t_{\downarrow} = \frac{SW_{\downarrow}^{SFC} - r_{\uparrow} SW_{\uparrow}^{SFC}}{SW_{\downarrow}^{TOA}} \quad (12)$$

$$242 \quad t_{\uparrow} = T_a - [t_{\downarrow} - t_{\downarrow}(1 - r_{\uparrow}\alpha_s)] \quad (13)$$

243 where T_a is the effective atmospheric transmittance (Table 2) of the earth system.

244 The kernel may now be expressed as:

$$245 \quad \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s = K_{\alpha_s}^{ANISO} \Delta \alpha_s = \frac{SW_{\downarrow}^{TOA} t_{\downarrow} t_{\uparrow}}{(1 - r_{\uparrow} \alpha_s)^2} \Delta \alpha_s \quad (14)$$

246 where $K_{\alpha_s}^{ANISO}$ is henceforth referred to as the *Anisotropic* kernel.

247 *c. Existing empirical parameterizations*

248 Although not referred to as “kernels” in the literature *per se*, we present the simple empirical
 249 parameterizations as such to ensure consistency with previously described notation and
 250 terminology.

251

252 The first candidate parameterization, originally presented in Muñoz *et al.* (2010), makes use
 253 of a local two-way transmittance factor based on the local clearness index:

$$254 \quad \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s \equiv K_{\alpha_s}^{M10} \Delta \alpha_s = SW_{\downarrow}^{TOA} T^2 \Delta \alpha_s \quad (15)$$

255 where SW_{\downarrow}^{TOA} is the local incoming solar flux at TOA, T is the local clearness index, and
 256 $\partial SW_{\uparrow}^{TOA} / \partial \alpha_s$ is the approximated change in the upwelling shortwave flux at TOA due to a
 257 change in the surface albedo.

258 The second candidate parameterization, originally proposed in Cherubini *et al.* (2012), makes
 259 direct use of the solar flux incident at the surface SW_{\downarrow}^{SFC} combined with a one-way
 260 transmission constant k :

$$261 \quad \frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s \equiv K_{\alpha_s}^{C12} \Delta \alpha_s = SW_{\downarrow}^{SFC} k \Delta \alpha_s \quad (16)$$

262 where k is based on the global annual mean share of surface reflected shortwave radiation
 263 exiting a clear-sky (Lacis and Hansen, 1974; Lenton and Vaughan, 2009) and is hence
 264 temporally and spatially invariant. This value – or 0.85 -- is similar to the global mean ratio
 265 of forward-to-total shortwave scattering reported in Iqbal (1983). Bright & Kvalevåg (2013)
 266 evaluated Eq. (16) at several global locations and found large biases for some regions and
 267 months, despite good overall performance globally (rRMSE = 7%; $n = 120$ months).

268 *d. Proposed empirical parameterization*

269 To determine whether the GCM-based kernels could be approximated with sufficient fidelity
 270 using other simpler model formulations based on their own boundary data, we applied
 271 machine learning to identify potential model forms using GCM shortwave boundary fluxes as
 272 input. For the two GCMs kernels in which the GCM's own shortwave boundary fluxes are
 273 also made available (CAM5 and ECHAM6), we used machine learning to minimize the sum
 274 of squared residuals between the four shortwave boundary fluxes (i.e., SW_{\downarrow}^{SFC} , SW_{\downarrow}^{TOA} ,
 275 SW_{\uparrow}^{SFC} , SW_{\uparrow}^{TOA}) and the GCM kernel at the monthly time step. The reference dataset
 276 consisted of a random global sample of 200,000 monthly kernel grid cells at native model
 277 resolution (97% and 32% of all cells for ECHAM6 and CAM5, respectively) of which 50%
 278 were used for training and 50% for validation. Models were identified using a form of genetic
 279 programming known as symbolic regression (Eureqa®; Nutonian Inc.; (Schmidt and Lipson,
 280 2009, 2010)) which searches a wide space of model structures as constrained by user input.
 281 In our case, we allowed the model to include the operators (i.e., addition, subtraction,
 282 multiplication, division, sine, cosine, tangent, exponential, natural logarithm, factorial, power,
 283 square root), but numerical coefficients were forbidden. The model search was allowed to
 284 continue until the percent convergence and maturity metrics exceeded 98% and 50%,
 285 respectively, at which point more than 1×10^{11} formulae had been evaluated. A parsimonious
 286 solution was chosen by minimizing the error metric and model complexity using the Pareto
 287 front (Figure S1 of Supporting Information) (Smits and Kotanchek, 2005). Between CAM5
 288 and ECHAM6, four common model solutions were found (Table S1 of Supporting
 289 Information). The best of these common solutions is subsequently referred to as $K_{\alpha_s}^{BO18}$ and is
 290 given as:

$$\frac{\partial SW_{\uparrow}^{TOA}}{\partial \alpha_s} \Delta \alpha_s = K_{\alpha_s}^{BO18} \Delta \alpha_s = SW_{\downarrow}^{SFC} \sqrt{T} \Delta \alpha_s \quad (17)$$

292

293

294 **4. Kernel model evaluation**

295 *a. Initial candidate screening*

296 The four GCM kernels presented in Section 2.a are employed as benchmarks to initially
297 screen the six simple model candidates introduced from Section 3b to 3d. We compute a
298 skill metric analogous to the “relative error” metric used to evaluate GCMs by Anav et al.
299 (2013) that takes into account error in the spatial pattern between a model and an observation.
300 Because we have no true observational reference, our evaluation instead focuses on the
301 disagreement or deviation between CERES and GCM kernels at the monthly time step. Given
302 interannual climate variability in the earth system, the challenge of comparing the multi-year
303 CERES kernel to a single-year GCM kernel can be partially overcome by averaging the four
304 GCM kernels.

305 Using the multi-GCM mean as the reference, we first compute the absolute deviation $AD_{m,p}^X$
306 as:

$$307 \quad AD_{m,p}^X = \left| CERES_{m,p}^X - \overline{GCM}_{m,p} \right| \quad (18)$$

308 where $CERES_{m,p}^X$ is the kernel for CERES model candidate x in month m and pixel p and
309 $\overline{GCM}_{m,p}$ is the multi-GCM mean of the same pixel and month. $AD_{m,p}^X$ is then normalized to
310 the maximum absolute deviation of all six CERES kernels for the same pixel and month to
311 obtain a normalized absolute deviation, $NAD_{m,p}^X$, which is analogous to the “relative error”
312 metric of Anav et al. (2013) having values ranging between 0 and 1:

$$313 \quad NAD_{m,p}^X = 1 - \frac{AD_{m,p}^X}{\max(AD_{m,p})} \quad (19)$$

314 where $\max(AD_{m,p})$ is the maximum absolute deviation of all six CERES kernels at pixel p
315 and month m .

316 CERES kernel ranking is based on the mean relative absolute deviation in both space and time
317 – or NAD^x :

$$318 \quad NAD^x = \frac{1}{M} \sum_{m=1}^M \frac{1}{P} \sum_{p=1}^P NAD_{m,p}^x \quad (20)$$

319 where M is the total number of months (i.e., 12) and P is the total number of grid cells.

320

321 *b. GCM kernel emulation*

322 In order to eliminate any bias related to differences in the atmospheric state embedded in the
323 GCM kernel input climatologies, we emulate them by applying the top candidate models (as
324 identified from the initial performance screening described in section 4a) using the original
325 GCM boundary fluxes as input. Emulation is only done for two of GCM-based kernels since
326 only two of them have provided the accompanying boundary fluxes needed to do so:
327 ECHAM6 (Block and Mauritsen, 2014) and CAM5 (Pendergrass et al., 2018). Emulation
328 enables a more critical evaluation of the functional form of the candidate models in relation to
329 the more sophisticated radiative transfer schemes employed by ECHAM6 (Stevens et al.,
330 2013) and CAM5 (Hurrell et al., 2013).

331 *c. CACK model uncertainty*

332 Following emulation, monthly GCM kernels are then regressed on the monthly kernels
333 emulated with the leading model candidates. The model that best emulates both GCM kernels
334 – as measured in terms of the mean coefficient of determination (R^2) and mean RMSE – is
335 chosen to represent CACK.

336 Three sources of uncertainty are considered for CACK when based on the CERES boundary
337 flux climatology (i.e., 2001-2016 monthly means): 1) *physical variability* 2) *data uncertainty*;
338 and 3) *model error* (Mahadevan and Sarkar, 2009). The first is related to the interannual
339 variability of Earth’s atmospheric state and boundary radiative fluxes. The second is related
340 to the uncertainty of the CERES EBAF v4 variables used as input to CACK (including
341 measurement error). The third source of uncertainty is the error related to CACK’s model
342 form. CACK’s combined uncertainty for any given pixel and month is estimated as follows,
343 where if CACK or y is some non-linear function of the CERES boundary inputs x_1 and x_2
344 that co-vary in time and space, then the combined uncertainty of y – or $\sigma(y)$ – may be
345 expressed as the sum of the *model error* plus the combined *physical variability* and *data*
346 *uncertainty* associated with x_1 and x_2 summed in quadrature (Breipohl, 1970; Clifford, 1973;
347 Green et al., 2017):

$$348 \quad \sigma(y) \approx \sigma_{ME}(y) + \sqrt{\left(\frac{\partial y}{\partial x_1}\right)^2 [\sigma_{PV}(x_1) + \sigma_{DU}(x_1)]^2 + \left(\frac{\partial y}{\partial x_2}\right)^2 [\sigma_{PV}(x_2) + \sigma_{DU}(x_2)]^2 + \left(2 \frac{\partial y}{\partial x_1} \frac{\partial y}{\partial x_2} \sigma(x_1, x_2)\right)^2} \quad (21)$$

349 where $\sigma_{PV}(x_1)$ and $\sigma_{PV}(x_2)$ are the standard deviations of the 16-yr. climatological record of
350 CERES input variables x_1 and x_2 , respectively, for a given grid cell and month, $\sigma_{DU}(x_1)$ and
351 $\sigma_{DU}(x_2)$ are the absolute uncertainties of CERES input variables x_1 and x_2 , respectively, for
352 a given grid cell and month, $\sigma(x_1, x_2)$ is the covariance within the 16-yr. climatological
353 record between CERES input variables x_1 and x_2 for a given month and grid cell, and σ_{ME} is
354 the monthly grid cell model error. Model error ($\sigma_{ME}(y)$) and data uncertainties ($\sigma_{DU}(x_n)$) for
355 any given grid cell and month are based on the relative RMSE (Supporting Information) and
356 relative uncertainties of CERES boundary terms reported in Kato *et al.* (2018) (cf. Table 8,
357 “Monthly gridded, Ocean + Land”) and Loeb *et al.* (2017) (cf. Table 8, “All-sky, *Terra-Aqua*

358 period”). For the model error, we take the mean relative RMSE of the machine learning
359 model solutions for ECHAM5 and CAM5. For the relative uncertainty of the incoming solar
360 flux at TOA (SW_{\downarrow}^{TOA}), we use the 1% “calibration uncertainty” reported in Loeb *et al.* (2017).

361 If CACK’s intended application is to estimate a temporally-explicit ΔF within the CERES era
362 (i.e., if temporally-explicit rather than the climatological mean CERES boundary fluxes are
363 desired to compute CACK), the uncertainty related to *physical variability* ($\sigma_{PV}(x_n)$) can be
364 dropped from Eq. (21).

365 *d. Climatological CACK example application*

366 To demonstrate CACK’s application when based on monthly CERES EBAF climatology,
367 including the handling of uncertainty, we estimate the annual mean local ΔF from a $\Delta\alpha$
368 scenario associated with hypothetical deforestation in the tropics, where ΔF for a given month
369 is estimated as Eq. (4) where K_{α_s} is the 2001-2016 monthly climatological CACK and $\Delta\alpha$ is
370 the difference in the 2001-2011 monthly climatological mean white-sky surface albedo
371 between “Croplands” (CRO) and “Evergreen broadleaved forests” (EBF) taken from Gao *et al.*
372 *al.* (2014) which is based on International Geosphere-Biosphere Program definitions of land
373 cover classification.

374 The monthly climatological albedo look-up maps of Gao *et al.* (2014) contain their own
375 uncertainties, which we take as the mean absolute difference between the monthly albedos
376 reconstructed using their look-up model and the monthly MODIS retrieval record (c.f. Table 3
377 in Gao *et al.* (2014)).

378 The total estimated uncertainty linked to the annual local (i.e., grid cell) instantaneous ΔF can
379 thus be expressed (in $W\ m^{-2}$) as:

$$380 \quad \sigma(\Delta F) = \frac{1}{12} \sum_{m=1}^{12} |\Delta F_m| \sqrt{\left(\frac{\sigma(K_{\alpha_s,m})}{K_{\alpha_s,m}}\right)^2 + \left(\frac{\sigma(\Delta\alpha_{s,m})}{\Delta\alpha_{s,m}}\right)^2} \quad (22)$$

381 where $\sigma(K_{\alpha_s,m})/K_{\alpha_s,m}$ is the relative grid cell uncertainty of CACK and $\sigma(\Delta\alpha_{s,m})/\Delta\alpha_{s,m}$ is
 382 the relative uncertainty of $\Delta\alpha_s$ in month m defined as:

$$383 \quad \frac{\sigma(\Delta\alpha_{s,m})}{\Delta\alpha_{s,m}} = \sqrt{\left(\frac{\sigma(\alpha_{s,m})}{\alpha_{CRO,m}}\right)^2 + \left(\frac{\sigma(\alpha_{s,m})}{\alpha_{EBF,m}}\right)^2} \quad (23)$$

384 where $\sigma(\alpha_{s,m})$ is the monthly absolute uncertainty of the climatological mean surface albedo
 385 (i.e., of the Gao *et al.* (2014) product).

386 *e. Temporally-explicit CACK application example*

387 Use of a temporally-explicit CACK may be desirable for time-sensitive applications within
 388 the CERES era. This is particularly true for regions experiencing significant changes to the
 389 atmospheric state affecting shortwave radiation transfer. A good example is in southern
 390 Amazonia where tropical deforestation has been linked to changes in cloud cover (Durieux et
 391 al., 2003; Lawrence and Vandecar, 2014; Wright et al., 2017). To exemplify this, we estimate
 392 the annual mean instantaneous ΔF for CERES grid cells in the region having experienced both
 393 significant positive trends in surface albedo and negative trends in cloud area fraction during
 394 the 2001-2016 period. Grid cell trends in surface albedo and cloud area fraction are deemed
 395 significant if the slopes of linear fits obtained from local (i.e., grid cell) ordinary least squares
 396 regressions had p-values ≤ 0.05 . We then apply the slope of the surface albedo trend to
 397 represent the monthly mean interannual $\Delta\alpha$ incurred over the time series together with
 398 CACK updated monthly to estimate the local annual mean instantaneous ΔF at each step in
 399 the series:

$$\Delta F(t) = \sum_{m=1}^{m=12} -K_{\alpha_s, m}(t) \Delta \alpha_s \quad (24)$$

where $K_{\alpha_s, m}(t)$ is the monthly CACK in year t of the time series. ΔF is then averaged across all grid cells in the sample, with the results then compared to the ΔF that is computed for the same grid sample using the time-insensitive CAM5 and ECHAM6 kernels (i.e., $K_{\alpha_s, m} \neq f(t)$). Using the slope of the surface albedo trend as the $\Delta \alpha_s$ for all months and years rather than the actual $\Delta \alpha_{s, m}(t)$ (i.e., $\Delta \alpha_{s, m}(t) = \alpha_{s, m, t} - \alpha_{s, m, t-1}$) yields the same result when averaged over the full time period but allows us to isolate the effect of the changing atmospheric state on calculations of ΔF . We limit the ΔF uncertainty estimate to CACK's uncertainty that includes $\sigma_{DU}(x_n)$ and $\sigma_{ME}(x_n)$ but excludes $\sigma_{PV}(x_n)$.

5. Results

a. Initial performance screening

Seasonally, differences in latitude band means between the CERES kernel candidates and the multi-GCM mean kernels are shown in Figure 1.

413

414 < Figure 1 >

415

416 Qualitatively, starting with December-January-February (*DJF*), $K_{\alpha_s}^{BO18}$ gives the best agreement with $K_{\alpha_s}^{\overline{GCM}}$ with the exception of the zone around 55 – 65°S (-55 – -65°), where

418 $K_{\alpha_s}^{QH06}$ gives slightly better agreement (Fig. 1A). In March-April-May (*MAM*), $K_{\alpha_s}^{BO18}$ appears

419 to give the best overall agreement with the exception of the high Arctic, where $K_{\alpha_s}^{ANISO}$ and

420 $K_{\alpha_s}^{C12}$ give better agreement, and with the exception of the zone around 60 – 65°S (-60 – -65°)

421 where $K_{\alpha_s}^{QH06}$, $K_{\alpha_s}^{ANISO}$, and $K_{\alpha_s}^{C12}$ agree best with $K_{\alpha_s}^{\overline{GCM}}$ (Fig. 1B). The largest spread in

422 disagreement across all six CERES kernels is found in June-July-August (*JJA*; Fig. 1 C) at
 423 northern high latitudes. $K_{\alpha_s}^{BO18}$ appears to agree best both here and elsewhere with the
 424 exception of the zone between $\sim 20 - 35^\circ\text{N}$, where $K_{\alpha_s}^{QH06}$ gives slightly better agreement.
 425 In September-October-November (*SON*), $K_{\alpha_s}^{BO18}$ agrees best with $K_{\alpha_s}^{\overline{GCM}}$ at all latitudes except
 426 the zone between $10 - 25^\circ\text{N}$ and $55 - 65^\circ\text{S}$ where $K_{\alpha_s}^{QH06}$ agrees slightly better.

427 Quantitatively, the proportion of the total variance explained by linear regressions of monthly
 428 $K_{\alpha_s}^{\overline{GCM}}$ on monthly $K_{\alpha_s}^{CERES}$ (i.e., “ R^2 ”) is highest and equal for the CERES kernels based on the
 429 ANISO, QH06, and BO18 models (Fig. 2 B, C, & D). Of these three, $K_{\alpha_s}^{QH06}$ has a y-intercept
 430 (“ B_0 ”) closest to 0 and a slope (“ m ”) of 1, although the root mean squared error (“ $RMSE$ ”) –
 431 an accuracy measure – is slightly better (lower) for $K_{\alpha_s}^{BO18}$. The two CERES kernels with the
 432 lowest R^2 , highest slopes (negative deviations), highest $RMSE$ s, and y-intercepts with the
 433 largest absolute difference from zero – or the worst performing candidates – are those based
 434 on the ISO and M10 models (Fig. 2 A&E).

435

436 < Figure 2 >

437

438 Although the y-intercept deviation from 0 for $K_{\alpha_s}^{C12}$ is relatively low, its $RMSE$ is $\sim 50\%$
 439 higher than that of $K_{\alpha_s}^{QH06}$, $K_{\alpha_s}^{BO18}$, and $K_{\alpha_s}^{ANISO}$ and leads to notable positive deviation from the
 440 multi-GCM mean ($K_{\alpha_s}^{\overline{GCM}}$) judging by its slope of 0.92.

441 Globally, NAD for the QH06, ANISO, and BO18 kernels are far superior to the ISO, M10,
 442 and C12 kernels (Table 3).

443

444 < Table 3 >

445

446 After filtering to remove grid cells for oceans and other water bodies, *NAD* scores for these
447 three kernels decreased; the decrease was smallest for $K_{\alpha_s}^{BO18}$ (-0.03) and largest for $K_{\alpha_s}^{QH06}$ (-
448 0.06). Despite constraining the analysis to land surfaces only, the rank order remained
449 unchanged (Table 3), and $K_{\alpha_s}^{QH06}$, $K_{\alpha_s}^{BO18}$, and $K_{\alpha_s}^{ANISO}$ are subjected to further evaluation.

450 *b. GCM kernel emulation and additional performance evaluation*

451 However, because the QH06 model ($K_{\alpha_s}^{QH06}$) required auxiliary inputs for cloud cover area
452 fraction and cloud optical depth – two atmospheric state variables not provided with the
453 ECHAM6 and CAM5 kernel datasets – it was not possible to emulate these two GCM kernels
454 with $K_{\alpha_s}^{QH06}$. Additional performance evaluation through GCM kernel emulation is therefore
455 restricted to the ANISO and BO18 models.

456 < Figure 3 >

457 Globally, the kernel based on the ANISO model displays larger annual mean biases relative to
458 BO18 when compared to both ECHAM6 and CAM5 kernels (Figure 3). Notable positive
459 biases over land with respect to both ECHAM6 and CAM5 kernels are evident in the northern
460 Andes region of South America, the Tibetan plateau, and the tropical island region comprising
461 Indonesia, Malaysia, and Papua New Guinea (Fig. 3 A & C). Notable negative biases over
462 land with respect to both ECHAM6 and CAM5 kernels are evident over Greenland,
463 Antarctica, northeastern Africa, and the Arabian Peninsula (Fig. 3 A & C).

464 < Figure 4 >

465 Globally, annual biases for BO18 are generally found to be lower than for ANISO and are
466 mostly non-existent in extra-tropical ocean regions (Fig. 3 B & D). Patterns in biases over

467 land are mostly negative with the exception of Saharan Africa where the annual mean bias
468 with respect to both GCMs is positive. For BO18, systematic positive biases – or biases
469 evident with respect to both GCM kernels – appear over eastern tropical and subtropical
470 marine coastal upwelling zones where marine stratocumulus cloud dynamics are difficult for
471 GCMs to resolve (Bretherton et al., 2004; Richter, 2015).

472 < Table 4 >

473 Regression statistics (Figure 4) indicate a greater overall performance for BO18 than for
474 ANISO. RMSEs for monthly kernels emulated with BO18 are 9.0 and 8.2 W m⁻² for CAM5
475 and ECHAM6, respectively – which is ~50-60% of the RMSEs emulated with the ANISO
476 model. Relative to ANISO, the BO18 model also gives a higher R², a slope closer to 1, and a
477 y-intercept closer to zero (Figure 4). The BO18 model (or parameterization) is therefore
478 selected for the CERES albedo change kernel (CACK).

479 Focusing only on the GCM kernels emulated with $K_{\alpha_s}^{BO18}$ henceforth, global mean negative
480 biases are evident in all months (Table 4), with the largest biases (in magnitude) appearing in
481 May (-4.4 W m⁻²) and November (-2.5 W m⁻²) for CAM5 and ECHAM6, respectively. In
482 absolute terms, largest biases of 8.6 W m⁻² and 6.8 W m⁻² appear in June for CAM5 and
483 ECHAM6, respectively. Annually, the mean absolute bias for CAM5 and ECHAM6 is 6.8
484 and 6.1 W m⁻², respectively – a magnitude which seems remarkably low if one compares this
485 to the annual mean disagreement (standard deviation) of 33 W m⁻² across all four GCM
486 kernels (not shown; for seasonal mean standard deviations see Fig. 1).

487 *c. CACK uncertainty*

488 For a kernel based on 2001-2016 monthly mean CERES EBAF climatology, Figure 5
489 illustrates the contribution of the absolute error related to $K_{\alpha_s}^{BO18}$'s model form (Fig. 5 A,

490 annual mean) relative to CACK's total absolute uncertainty (Fig. 5 C, annual mean), which
491 includes the uncertainty surrounding CERES EBAF v4 input variables SW_{\downarrow}^{SFC} and SW_{\downarrow}^{TOA}
492 and their interannual variability (Fig. 5 B, annual mean).

493 < Figure 5 >

494 Total propagated σ_{pv} and σ_{du} far exceeds σ_{me} , is dominated by $\sigma_{du}(SW_{\downarrow}^{SFC})$ and
495 $\sigma_{pv}(SW_{\downarrow}^{SFC})$, and is largest in the Pacific region to the south of the intertropical convergence
496 zone (ITCZ). Over land, the annual σ_{pv} and σ_{du} as well as the annual σ_{total} are generally
497 largest in arid or high altitude regions (Fig. 5 B). However, annual CACK values are also
498 large in these regions reducing the relative uncertainty (Fig. 5 D). The largest relative
499 uncertainties over land (on an annual basis) – which can approach 50% – are found over
500 central Europe, northwestern Asia, southeastern China, Andean Chile, and northwestern N.
501 America (Fig. 5 D).

502 *d. Climatological CACK application*

503 When estimated with a CACK based on monthly CERES EBAF climatology, the annual local
504 ΔF from $\Delta\alpha_s$ linked to hypothetical deforestation in the tropics is negative in most regions,
505 approaching -20 W m^{-2} locally in some regions of the Brazilian Cerrado and south of the
506 Sahel region in Africa (Fig. 6 B). The combined CACK and $\Delta\alpha_s$ uncertainty for these
507 regions can approach $\pm 5 \text{ W m}^{-2}$ annually (Fig. 6 C) in regions like the Brazilian Cerrado and
508 sub-Sahel Africa. Relative to the ΔF magnitude, however, the largest uncertainties (annual)
509 may be found in the subtropical regions of Central America, southern Brazil, southern Asia,
510 and northern Australia, where it can approach 30-40% (Fig. 6 D).

511 *e. Temporally-explicit CACK application*

512 The effect of a decreasing cloud cover and increasing surface albedo trend in southern
513 Amazonia (Fig. 7 B) on shortwave radiative transfer and thus a CACK-based estimate of
514 regional mean annual ΔF emerges in Figure 7 C, where ΔF increases in magnitude by 0.004
515 W m^{-2} from 2002 to 2016. This ΔF trend would otherwise go undetected if a GCM-based
516 kernel were applied to the same surface albedo trend – that is, to a sustained positive
517 interannual monthly albedo change “pulse”. Alternatively, a CACK based on 2001 CERES
518 EBAF inputs (applied with $\Delta\alpha_s$ for 2001-2002) would give slightly higher ΔF estimates
519 relative to those based on ECHAM6 and CAM5 kernels; conversely, a CACK based on 2015
520 CERES EBAF inputs (applied with $\Delta\alpha_s$ for 2015-2016) that would yield lower ΔF estimates
521 relative to those based on the same two GCM-based kernels (Fig. 7 C). Use of temporally-
522 explicit CACK can therefore capture ΔF trends related to a changing atmospheric state that
523 fixed-state GCM kernels are unable to capture.

524 **5. Discussion**

525 Motivated by an increasing abundance of climate impact research focusing on land processes
526 in recent years, we comprehensively evaluated six simplified models (or parameterizations) as
527 candidates for an albedo change kernel based on the CERES EBAF v4 products (Kato et al.,
528 2018; Loeb et al., 2017). Relative to albedo change kernels based on sophisticated radiative
529 transfer schemes embedded in GCMs, a CERES-based albedo change kernel – or CACK –
530 represents a more transparent and empirically-rooted alternative that can be updated
531 frequently at relatively low cost. This allows greater flexibility to meet the needs of research
532 focusing on surface albedo trends within the CERES era in regions currently undergoing rapid
533 changes to atmospheric state as it affects shortwave radiation transfer. Although some
534 modeling groups have provided recent updates to their albedo change kernels using the latest
535 GCM versions (e.g., (Pendergrass et al., 2018)), the atmospheric state conditions used to

536 derive them may still be considered outdated or not in sync with that required for many
537 applications (Table 1).

538 Based on both qualitative and quantitative benchmarking against the mean of four GCM
539 kernels, the novel kernel parameterization obtained from machine learning $K_{\alpha_s}^{BO18}$, together
540 with the two (semi-)analytically derived kernels $K_{\alpha_s}^{QH06}$ and $K_{\alpha_s}^{ANISO}$, proved far superior to the
541 $K_{\alpha_s}^{ISO}$ analytical kernel and to the two additional empirical parameterizations $K_{\alpha_s}^{C12}$ and $K_{\alpha_s}^{M10}$.
542 When subjected to additional performance evaluation, however, we found that $K_{\alpha_s}^{BO18}$ was
543 able to more robustly emulate two GCM kernels (ECHAM6 and CAM5) with exceptionally
544 high agreement, suggesting that $K_{\alpha_s}^{BO18}$ could serve as a suitable candidate for CACK.

545 Relative to the monthly CAM5 and ECHAM6 kernels, the mean absolute monthly emulation
546 “error” of $K_{\alpha_s}^{BO18}$ was found to be 6.8 and 6.1 W m^{-2} , respectively – a magnitude which is only
547 ~20% of the standard deviation found across four GCM kernels (annual mean). CACK’s
548 remarkable simplicity lends support to the idea of using machine learning to explore and
549 detect emergent properties of radiative transfer or other complex, interactive model outputs in
550 future research. The fact that the $K_{\alpha_s}^{BO18}$ parameterization emerged as the best common
551 solution from two independently executed machine learning analyses each employing a
552 random sampling unique to a specific GCM kernel suggests that the $K_{\alpha_s}^{BO18}$ parameterization is
553 robust and insensitive to the underlying GCM representation of shortwave radiative transfer.

554 Despite its stronger empirical foundation over a GCM-based kernel, it is important to
555 recognize CACK’s limitations. Firstly, while CACK has a finer spatial resolution than most
556 GCM kernels, it still represents a spatially averaged response rather than a truly local
557 response; in other words, the state variables used to define the SW_{\uparrow}^{TOA} response are averages

558 tied to the coarse spatial (i.e., $1^\circ \times 1^\circ$) resolution of the CERES EBAF v4 product grids.
559 Secondly, the monthly CERES EBAF-Surface product used to define lower atmospheric
560 boundary conditions is not strictly an observation. The space-borne platform is not able to
561 directly observe surface irradiances, requiring additional satellite-based estimates of cloud and
562 aerosol properties as input to a radiative transfer model (Kato et al., 2012). Although TOA
563 irradiances are applied to constrain the surface irradiances, they remain susceptible to errors
564 in the radiative transfer model inputs. Considering this error as “data uncertainty” increases
565 CACK’s overall uncertainty beyond that which is related to its underlying parameterization or
566 “model error”. The uncertainty of CERES surface shortwave irradiances as well as extensive
567 ground validation and testing are documented in greater detail elsewhere (Kato et al., 2013;
568 Kato et al., 2018; Loeb et al., 2017; Loeb et al., 2009) and may continue to be reduced in
569 future EBAF-Surface versions.

570 *Concluding remarks*

571 To conclude, we developed, evaluated, and proposed a radiative kernel for surface albedo
572 change based on CERES EBAF v4 products – or CACK. Relative to existing kernels based on
573 GCMs, CACK provides a higher spatial resolution, higher transparency alternative that is
574 more amenable to user needs. For LULCC research of the near-past, present day, or near-
575 future periods, application of a CACK whose inputs are based on monthly climatological
576 means of the full CERES EBAF record can better-account for the corresponding interannual
577 variability in Earth’s atmospheric state affecting shortwave radiative transfer. For regions
578 undergoing changes in atmospheric state that are detectable above the normal variability
579 within the CERES era, application of a temporally-explicit CACK can better-account for its
580 influence on ΔF estimates from surface albedo change. CACK’s input flexibility and
581 transparency combined with documented uncertainty make it well-suited to be applied as part

582 of a Monitoring, Reporting, and Verification (MRV) framework for biogeophysical impacts
583 on land, analogous to those which currently exist for land sector greenhouse gas emissions.

584

585 **Code and Dataset Availability**

586 We make both monthly temporally-explicit and monthly climatological mean CACKs for
587 years 2001-2016 available as a complete data product (“CACKv1.0”; (Bright and O’Halloran,
588 2019)) that includes their respective uncertainty layers. A summary of this dataset and
589 associated variables is provided in Table S3 of the Supporting Information. Octave script files
590 for generating monthly CACK and demonstrating its application with user-specified temporal
591 and spatial extents are bundled with the netCDF file.

592

593 **Data Availability**

594 CERES EBAF data are available for download at:
595 <https://ceres.larc.nasa.gov/products.php?product=EBAF-TOA> . The CAM3 kernel is
596 available at: <http://people.oregonstate.edu/~shellk/kernel.html> . The CAM5 kernel is
597 available at: <https://www.earthsystemgrid.org/ac/guest/secure/sso.html> . The ECHAM5
598 kernel is available at: [https://swiftbrowser.dkrz.de/public/dkrz_0c07783a-0bdc-4d5e-9f3b-
599 c1b86fac060d/Radiative_kernels/](https://swiftbrowser.dkrz.de/public/dkrz_0c07783a-0bdc-4d5e-9f3b-c1b86fac060d/Radiative_kernels/) .

600

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842

843 **Table 1.** Attributes of existing GCM kernels, all of which having a monthly temporal
 844 resolution.

Kernel	Base climatology extent	Base climatology period	Shortwave Radiative transfer	Horizontal Resolution	References
ECHAM6	1,000 years	Preindustrial*	RRTM-G	1.88° × 1.88°	(Block and Mauritsen, 2014; Stevens et al., 2013)
CAM3	6 years	1995-2000	δ-Eddington	1.4° × 1.4°	(Collins et al., 2006; Shell et al., 2008)
CAM5	1 year	2006-2007	RRTM-G	0.94° × 1.25°	(Pendergrass et al., 2018)
GFDL	17 years	1979-1995	Exponential sum-fits, 18 bands	2° × 2.5°	(Soden et al., 2008; The GFDL Global Atmospheric Model Development Team, 2004)

845 *Atmospheric CO₂ concentration = 284.7 ppmv; Exact time period unknown

846

847

848 **Table 2.** Definition of CERES input variables and other system optical properties derived
849 from CERES inputs. All variables have a monthly temporal resolution and a spatial
850 resolution of $1^\circ \times 1^\circ$.

CERES EBAF v.4 Shortwave Boundary Fluxes		
SW_{\downarrow}^{TOA}	Downwelling solar flux at top-of-atmosphere	Wm^{-2}
SW_{\downarrow}^{SFC}	Downwelling solar flux at surface	Wm^{-2}
$SW_{\downarrow,CLR}^{SFC}$	Clear-sky downwelling solar flux at surface	Wm^{-2}
SW_{\uparrow}^{TOA}	Upwelling solar flux at top-of-atmosphere	Wm^{-2}
SW_{\uparrow}^{SFC}	Upwelling solar flux at surface	Wm^{-2}
System Optical Properties		
$T = SW_{\downarrow}^{SFC} / SW_{\downarrow}^{TOA}$	Clearness index	unitless
$\alpha_p = SW_{\uparrow}^{TOA} / SW_{\downarrow}^{TOA}$	Planetary albedo	unitless
$\alpha_s = SW_{\uparrow}^{SFC} / SW_{\downarrow}^{SFC}$	Surface albedo	unitless
$A_p = 1 - \alpha_p$	Effective planetary absorption	unitless
$A_s = [SW_{\downarrow}^{SFC} - SW_{\uparrow}^{SFC}] / SW_{\downarrow}^{TOA}$	Effective surface absorption	unitless
$A_a = A_p - A_s$	Effective atmospheric absorption	unitless
$T_a = 1 - A_a$	Effective atmospheric transmission	unitless
$T_{a,CLR} = 1 - A_{a,CLR}$	Clear-sky effective atmospheric transmission	unitless
τ	Cloud visible optical depth	unitless
c	Cloud area fraction	fraction

851

852

853 **Table 3.** Normalized absolute deviation and CERES kernel model candidate ranking.

	Global		Land only		Mean Rank
	<i>NAD</i>	Rank	<i>NAD</i>	Rank	
ISO	0.05	6	0.05	6	6
ANISO	0.64	3	0.59	3	3
C12	0.45	4	0.47	4	4
M10	0.26	5	0.34	5	5
QH06	0.66	2	0.60	2	2
BO18	0.67	1	0.64	1	1

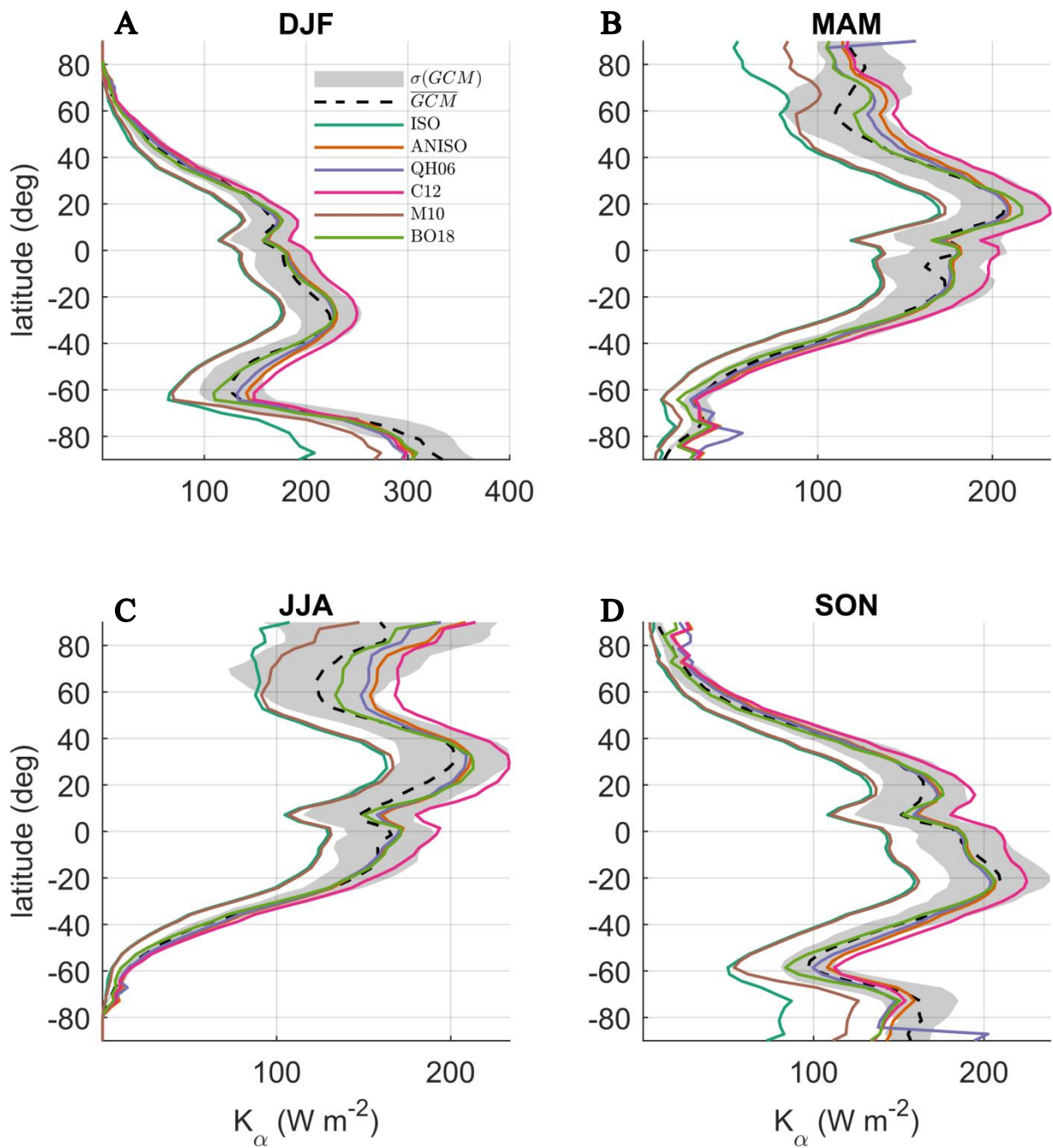
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855

Table 4. Global monthly mean bias (*MB*) and mean absolute bias (*MAB*) for K_{α}^{BO18} emulated with T and SW_{\downarrow}^{SFC} from ECHAM6 and CAM5. For reference, the global mean value of K_{α}^{BO18} is 133 W m^{-2} .

	<i>MB</i> (W m^{-2})												
	Jan.	Feb.	Mar.	Apr.	May	Jun.	Jul.	Aug.	Sep.	Oct.	Nov.	Dec.	Ann.
$K_{\alpha}^{BO18} - K_{\alpha}^{CAM5}$	-2.9	-3.4	-3.3	-3.9	-4.4	-3.8	-3.8	-3.7	-3.4	-3.8	-3.7	-3.3	-3.6
$K_{\alpha}^{BO18} - K_{\alpha}^{ECHAM6}$	-1.9	-2.2	-1.8	-1.9	-2.2	-1.5	-1.1	-1.6	-1.7	-2.5	-2.5	-1.8	-1.9
	<i>MAB</i> (W m^{-2})												
	Jan.	Feb.	Mar.	Apr.	May	Jun.	Jul.	Aug.	Sep.	Oct.	Nov.	Dec.	Ann.
$ K_{\alpha}^{BO18} - K_{\alpha}^{CAM5} $	6.9	5.7	5.2	6.8	7.7	8.6	7.9	6.7	5.6	6.1	6.9	6.9	6.8
$ K_{\alpha}^{BO18} - K_{\alpha}^{ECHAM6} $	6.3	5.7	5.0	5.9	6.7	6.8	6.4	5.8	5.3	5.6	6.4	6.7	6.1

856



857

858 **Figure 1.** Latitudinal (1°) and seasonal means of the multi-GCM mean ($K_\alpha^{\overline{GCM}}$) and CACK

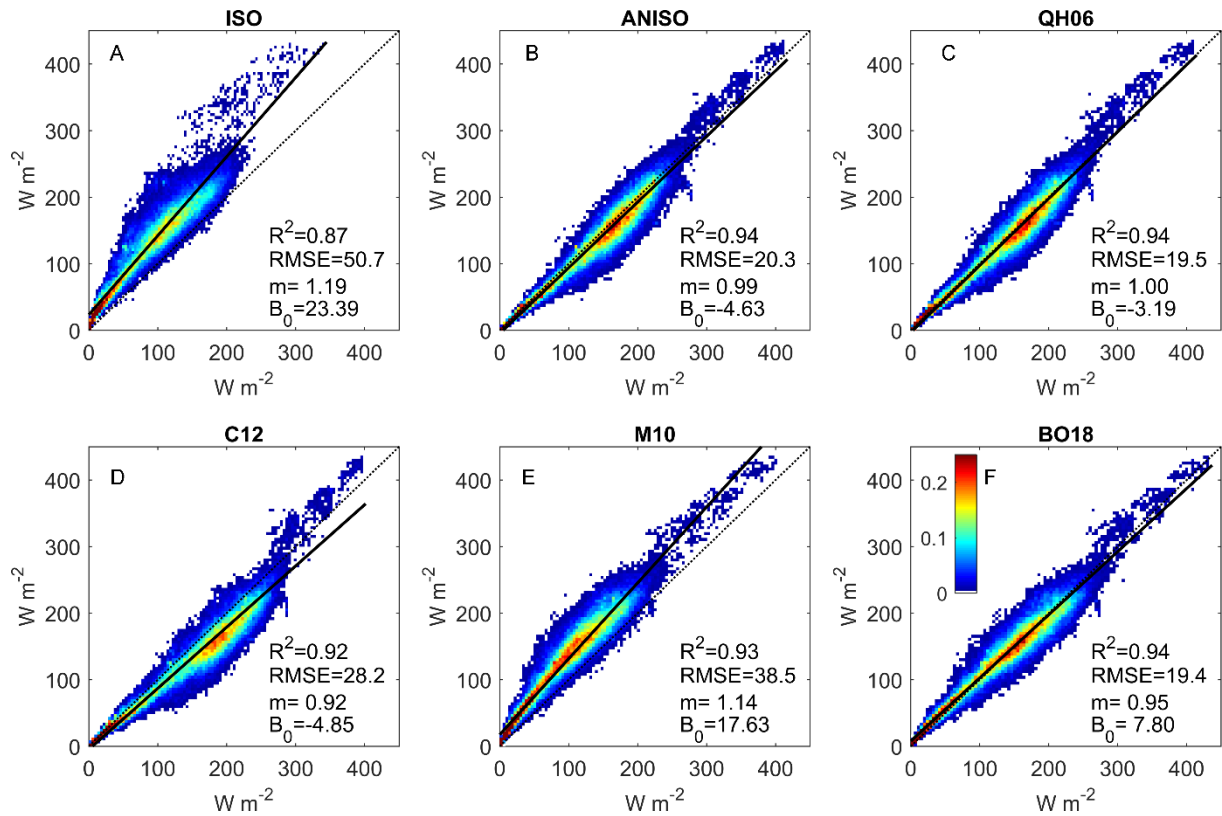
859 model candidates for: A) December-January-February (DJF); B) March-April-May (MAM);

860 C) June-July-August (JJA); D) September-October-November (SON). CACK model

861 candidates refer to those presented in section 3 and not to those of the model selection phase

862 of the machine learning algorithm.

863



864

865 **Figure 2.** A)-F): Scatter-density regressions of global monthly mean $K_{\alpha}^{\overline{GCM}}$ (y-axis) and

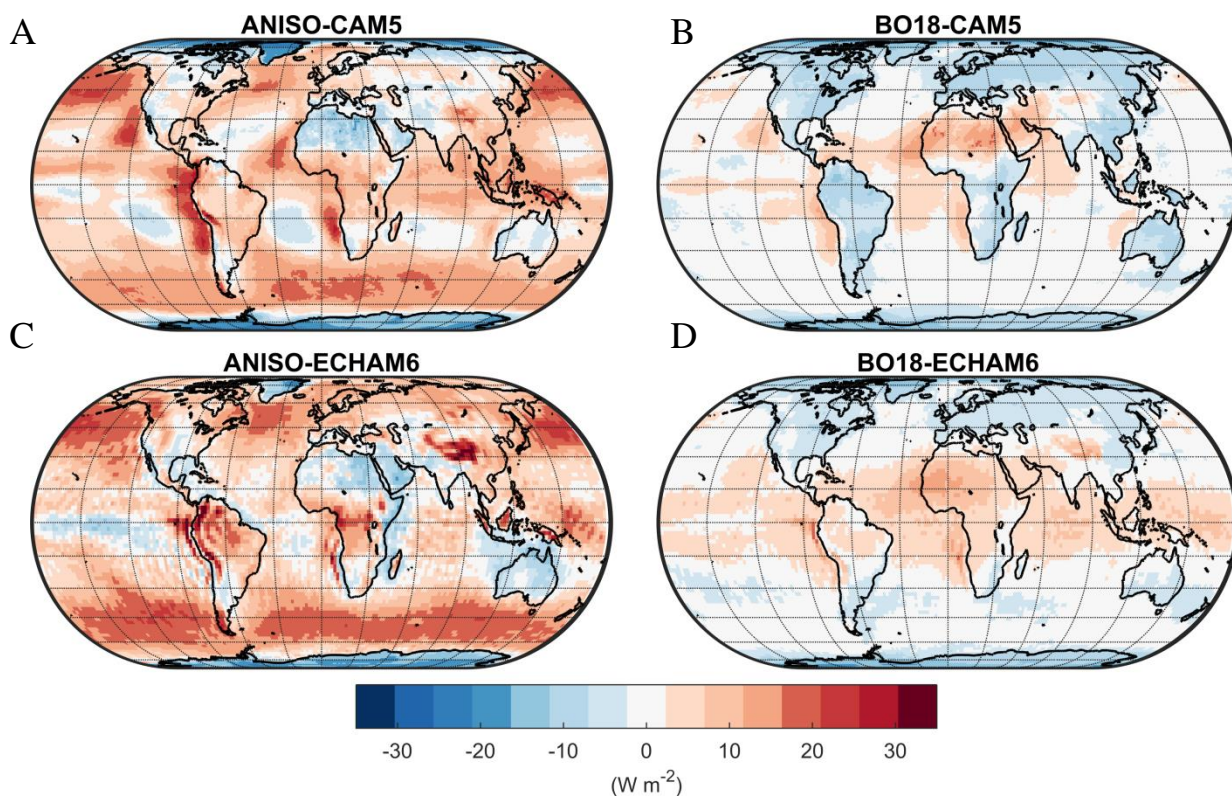
866 K_{α}^{CERES} (x-axis), with the CERES kernel identifier shown at the top of each sub-panel. “ m ” =

867 slope; “ B_0 ” = y-intercept. The color scale indicates the percentage of regression points that

868 fall within an averaging bin, where the x-axis and y-axis have been gridded into 100×100

869 equally-spaced bins to help illustrate the density of overlapping points.

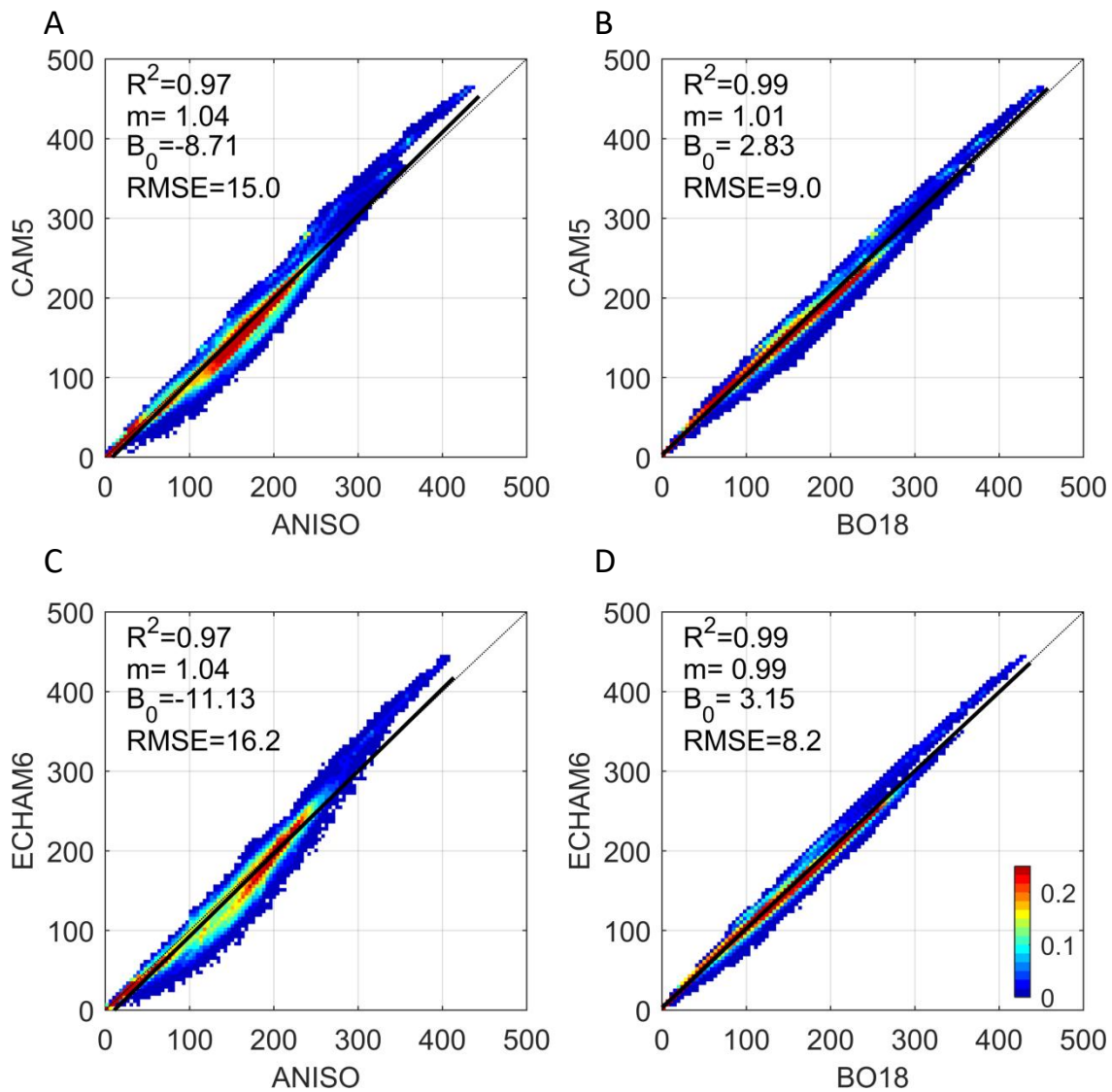
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871

872 **Figure 3.** A) Mean annual bias of the CAM5 albedo change kernel emulated with the ANISO
 873 semi-empirical model; B) Mean annual bias of the CAM5 albedo change kernel emulated
 874 with the BO18 parameterization; C) Mean annual bias of the ECHAM6 albedo change kernel
 875 emulated with the ANISO semi-empirical model; D) Mean annual bias of the ECHAM6
 876 albedo change kernel emulated with the BO18 parameterization

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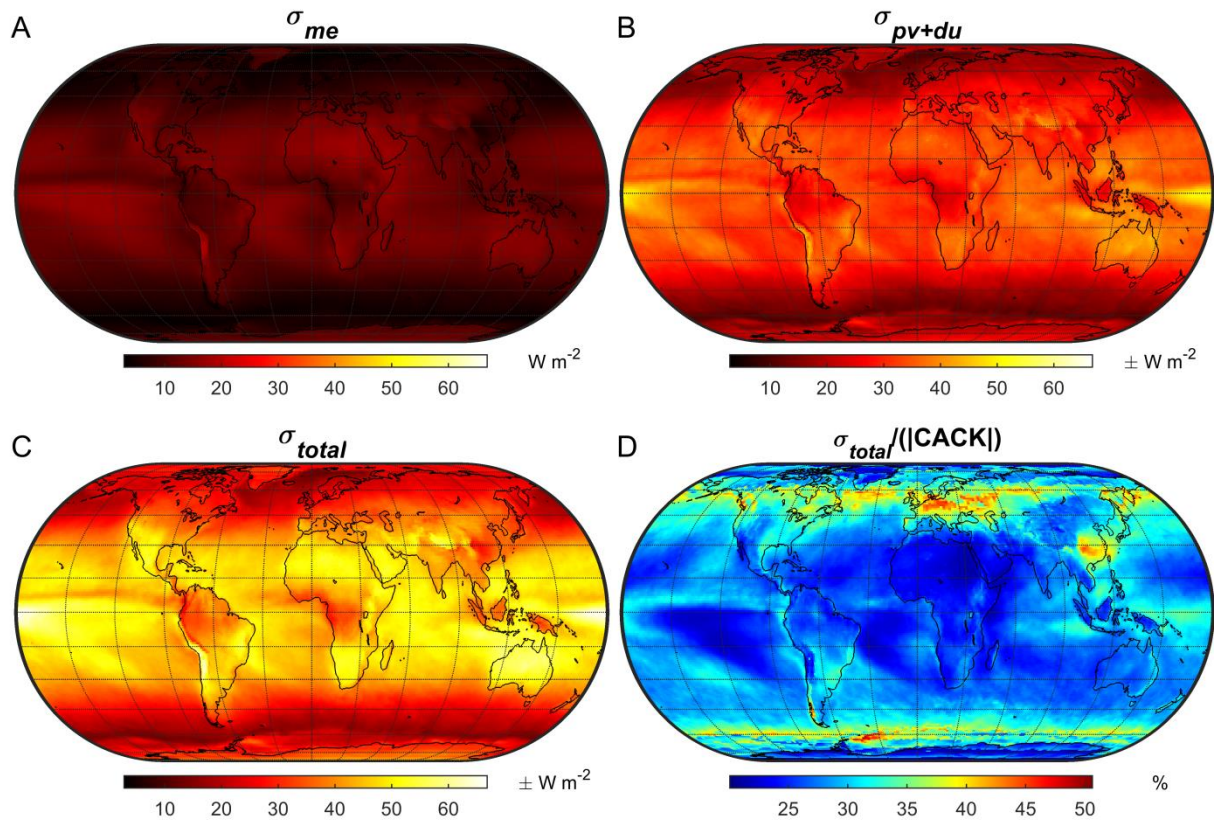


878

879 **Figure 4.** A)-D): Scatter-density regressions of K_{α}^{GCM} (y-axis) and K_{α}^{GCM} emulated with the
 880 ANISO semi-empirical model and BO18 parameterization (x-axis); “ m ” = slope; “ B_0 ” = y-
 881 intercept. See Figure 2 caption for a description of the color scale.

882

883



884

885 **Figure 5.** Annual uncertainty of a CACK based on 2001-2016 monthly mean CERES EBAF

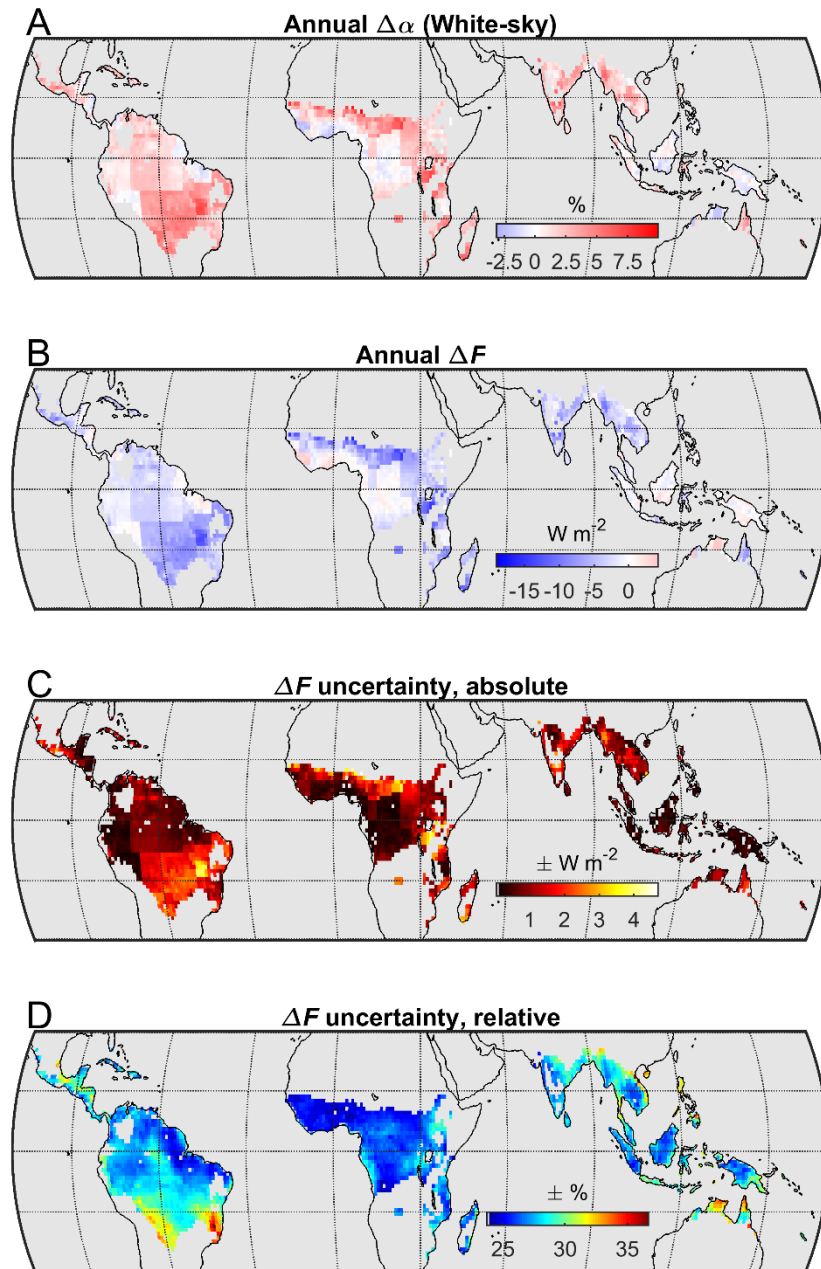
886 v4 climatology: A) The absolute uncertainty related to *model error* (i.e., the $K_{\alpha_s}^{BO18}$

887 parameterization); B) The total propagated absolute uncertainty related to *physical variability*

888 and *data uncertainty* of CACK input variables; C) Total absolute uncertainty; D) Total

889 relative uncertainty.

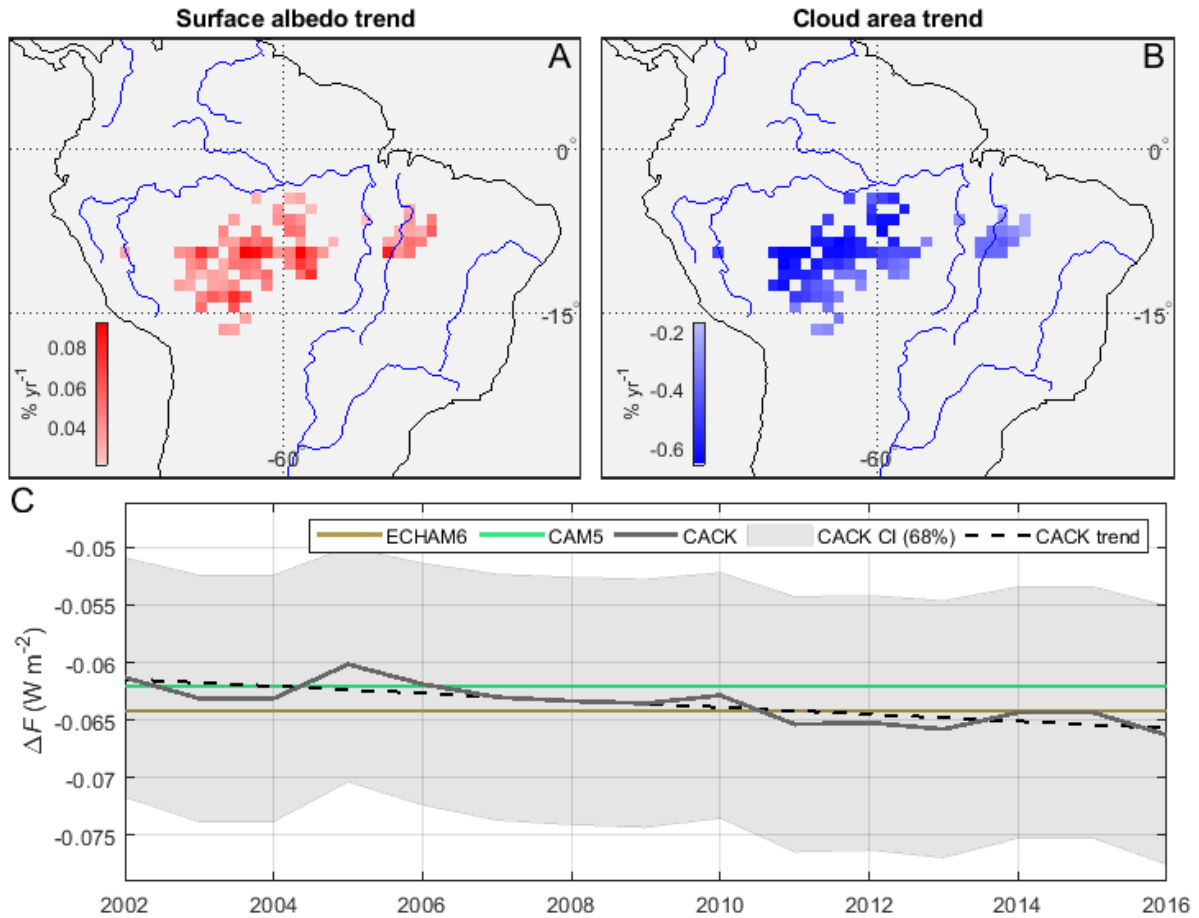
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891

892 **Figure 6.** Example application of a CACK based on the 2001-2016 monthly mean CERES
 893 EBAF v4 climatology to estimate the local annual mean ΔF from a hypothetical land cover
 894 change within a CERES grid cell. A) Annual mean of the climatological (i.e., 2001-2011)
 895 monthly mean difference in white-sky surface albedo between *croplands* and *evergreen*
 896 *broadleaved forests* ($\Delta\alpha_s$) based on the 1° product of Gao *et al.* (2014); B) Annual mean
 897 local (i.e., within grid cell) instantaneous radiative forcing (ΔF) of monthly mean $\Delta\alpha_s$
 898 estimated with CACK; C) Absolute uncertainty (annual mean) of the CACK-based ΔF

899 estimate, including the uncertainty of $\Delta\alpha_s$; D) Relative uncertainty (annual mean) of the
900 CACK-based ΔF estimate.



901

902 **Figure 7.** Example application of a temporally-explicit CACK. A) 2001-2016 statistically
 903 significant positive trends in all-sky *surface albedo* derived from CERES EBAF-Surface v4;

904 B) 2001-2016 statistically significant negative trends in *cloud area* derived from CERES

905 EBAF-TOA v4; C) Mean ΔF from $\Delta\alpha_s$ when estimated with the CACK, ECHAM6, and

906 CAM5 surface albedo change kernels. ΔF is the mean of all grid cells plotted in panel A).

907 The 1σ confidence interval (“CI”) shown for CACK excludes the uncertainty component

908 related to *physical variability*.

909