

Figure S1. Seasonal (summer-*left* and winter-*right*) zonal means of ice crystal number concentration (ICNC, $[L^{-1}]$) for the default simulation KL+LD and the relative percentage changes of BN+LD, KL+BN, and BN+BN with respect to it (i.e. $(experiment - DEF)/|DEF| \cdot 100$), computed where $ICNC^{DEF} \ge 1 L^{-1}$. The isolines at 273 K and 238 K and the tropopause (dotted line) are seasonal means.



Figure S2. Annual means of vertically integrated ice crystal number concentration $(ICNC_{burden}, [10^8 \text{ m}^{-2}])$ for the default simulation and the relative percentage changes of BN+LD, KL+BN, and BN+BN with respect to it (i.e. $(experiment - DEF)/|DEF| \cdot 100$), computed where $ICNC_{burden}^{DEF} \ge 10^8 \text{ m}^{-2}$.



Figure S3. Relative percentage changes of annual means of ice water content $(IWC, [mg kg^{-1}])$ at 200 hPa (cirrus regime) and 600 hPa (mixed-phase regime) for BN+LD, KL+BN, and BN+BN with respect to the default simulation (i.e. $(experiment - DEF)/|DEF| \cdot 100$), computed where $IWC^{DEF} \ge 0.1 \text{ mg kg}^{-1}$.



Figure S4. Annual zonal means of vertically integrated number concentration of cloud droplets $(CDNC_{burden}, [10^{10} \text{ m}^{-2}])$ and ice crystals $(ICNC_{burden}, [10^{10} \text{ m}^{-2}])$, non-precipitable liquid water path $(LWP, [gm^{-2}])$ and ice water path $(IWP, [gm^{-2}])$ averaged over the whole grid-boxes, shortwave and longwave cloud radiative effects $(SCRE, LCRE, [Wm^{-2}])$, total cloud cover (TCC, [%]). Colored lines refer to the experiments: KL+LD (blue), BN+LD (green), KL+BN (light blue) and BN+BN (red). Black lines refer to satellite observations.

cloud_param	4	cloud scheme	Lohmann et al., 2010
ncdnc	3	CDNC scheme	UAF
nicnc	3	ICNC - cirrus regime	BN09
limm_BN09	Т	ICNC - mixed phase regime	BN09
lcover	F	cloud cover calculation	Sundqvist
l_cdnc_calc	Т	CDNC parameterisation calculations	
i_cdnc_calc	7	CDNC parameterisation calculation	UAF
i_cdnc_cpl	7	CDNC parameterisation feedback	UAF
aer_stream	'gmxe_gp'	aerosol model for cdnc coupling	GMXe

Figure S5. Setup of cloud.nml for the simulation BN+BN. The first two columns show the parameter names and the corresponding values selected for BN+BN, respectively. The third column describes the meaning of the parameters. The forth column indicates the meaning of the values in the second column.