glmGUI v1.0: an R-based Geographical User Interface and toolbox for GLM (General Lake Model) simulations

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Abstract. Numerical modeling provides the opportunity to quantify the reaction of lakes on alterations in their environment, such as changes in climate or hydrological conditions. The one-dimensional hydrodynamic General Lake Model (GLM) is an open-source software and widely used within the limnological research community. Nevertheless, neither an interface to process the input data and run the model, nor tools for an automatic parameter calibration yet

15 exist. Hence, we developed *glmGUI*, a Geographical User Interface (GUI) including a toolbox for an autocalibration, parameter sensitivity analysis, and several plot options. The tool is provided as a package for the freely available scientific code language R. The model parameters can be analyzed and calibrated for the simulation output variables water temperature and lake level.

The glmGUI package is tested for two sites (Lake Ammersee, Germany, and Lake Baratz, Italy) distinguishing in size,

- 20 mixing regime, hydrology of the catchment area (i.e. the number of inflows and their runoff seasonality), and climatic conditions. A robust simulation of water temperature for both lakes (Ammersee: RMSE = 1.17 °C, Baratz: RMSE = 1.30 °C) is achieved by a quick automatic calibration. The quality of a water temperature simulation can be assessed immediately by means of a difference plot provided by *glmGUI*, which displays the distribution of the spatial (vertical) and temporal deviations. The calibration of the lake level simulations of Lake Ammersee for multiple hydrological
- 25 inputs including also unknown inflows yielded a satisfactory model fit (RMSE = 0.20 m). This shows that GLM can also be used to estimate the water balance of lakes correctly. The tools provided by *glmGUI* enable a less timeconsuming and simplified parameter optimization within the calibration process. Due to this, the free availability and the implementation in a GUI, the presented R package expands the application of GLM to a broader field of lake modeling research and even beyond limnological experts.

1 Introduction

As lakes respond to changes in their environment they are often considered to be "sentinels of change" (Williamson et al., 2009, Hipsey et al., 2017). The investigation of alterations in the physical conditions of lakes, such as water temperature, stratification, water balance, mixing behavior, or ice cover, has a key role in the understanding of the lake

- 5 dynamics. Numerical modeling provides the opportunity of research beyond the analysis of observational monitoring data (Frassl et al., 2016), enabling simulations of periods without in-situ data as well as future conditions of lakes. The development and application of community-based models is of increasing importance in order to find solutions for the future challenges to simulate water body conditions under environmental alterations (e.g. climatic, land use, and agricultural policies, Bruce et al., 2018). The one-dimensional hydrodynamic General Lake Model (GLM) has been
- 10 developed, under the leadership of members of the Global Lake Ecological Observatory Network (GLEON, gleon.org, Hanson et al., 2016), in response to the need of a robust model of lake dynamics (Hipsey et al., 2017), which is applicable for the vast diversity of lakes and reservoirs around the globe. GLM is able to simulate the thermal dynamics of lakes in their temporal and spatial (vertical) characteristics. The model code is open-source and applied in numerous studies to a broad variety of different lakes and research questions (e.g., Bueche et al., 2017; Bucak et al., 2018; Bruce
- 15 et al., 2018; Fenocchi et al., 2018; Robertson et al., 2018; Ladwig et al., 2018; Mi et al., 2018; Fenocchi et al., 2017; Fenocchi et al., 2019). Carey and Gougis (2017) present the usage of GLM beyond the research application incorporated in a teaching tool for students.

Despite the high applicability of GLM a powerful toolbox for automatic calibration, validation and statistical sensitivity analysis is not yet existent. Therefore, we developed an R-based Geographical User Interface (GUI) implemented in the

- 20 new R package *glmGUI* combining an easy handling of GLM simulations, a tool to automatize the calibration process, and visualization options for the input and output data. In general, the maxim of our project was inspired by four aspects:
 - Provision of an open-source tool

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- Provision of a user-friendly tool, which could be used by experts as well as less experienced modelers and limnologists
- Using scripts to adapt the tool, with high acceptance and contribution in the scientific community
- Flexibility for the implementation of different calibration parameters and for the numerical and graphical interpretation of the output results

The R language (https://www.r-project.org) was chosen because it is open-source, flexible and an independent platform

30 (Snortheim et al., 2017). Moreover, the lake modeler community uses already R based packages, i.e. *glmtools* for parameterization or plotting model output (<u>https://github.com/USGS-R/glmtools</u>) and *rLakeAnalyzer* for post-processing and evaluation of the model results (Winslow et al., 2016, <u>https://github.com/GLEON/rLakeAnalyzer</u>).

Changes in the water level of a lake can have strong influences on hydrodynamics, such as thermocline depth and stratification stability and duration, and can also affect lake water quality (Robertson et al., 2018). The appropriate water level reproduction by lake models is essential for a robust simulation of spatial features of thermal dynamics in lakes, especially in shallow lakes with high variations in water stages. Furthermore, an accurate simulation of the lake

5 level ensures the correct representation of hydrological interaction of the lake with its environment in the catchment area. Hence, in addition to the model output water temperature, the lake level is included to be calibrated in the provided automated calibration tool.

In this contribution we present the options included in glmGUI and show the application for two different sites, namely the pre-alpine deep Lake Ammersee, south Germany, and the shallow, Mediterranean Lake Baratz, Sardinia, Italy. The

10 objectives of these two case studies are the calibration of the water temperature and lake level simulations of GLM using the automatic calibration tool.

2 Lake model, software description, and toolbox options

2.1 The hydrodynamic lake model

The GLM is a one-dimensional hydrodynamic model simulating the vertical profiles of temperature, salinity, and density at one spatial point in a lake over time (Frassl et al., 2016; Robertson et al., 2018). It applies the Lagrangian layer structure adapting the thickness and volume of layers with uniform properties from each simulation step (Bueche et al., 2017). The underlying equations and hydrodynamics closures are documented in Hipsey et al. (2014) and Hipsey et al. (2017). The hydrodynamic model can also easily be coupled with the Aquatic Ecodynamics library (AED2) to simulate water quality simulations (Weber et al., 2017; Bruce et al., 2018).

- GLM simulations are based on parameterizations of mixing processes, surface dynamics, and the effect of inflows and outflows. The model performance of simulating the lake thermal dynamics as well as the water balance can be improved by a calibration of lake-specific parameters. The model documentation of Hipsey et al. (2017) includes also a description of the lake specific parameters and the default values for GLM simulations. The model requires meteorological and hydrological input data (see Table A1). Field data of water temperature should be available in a mitchle temperature and metical (accerded depthe) methods.
- 25 suitable temporal and spatial (several depths) resolution to enable a reliable calibration process.

2.2 R package glmGUI

The R package *glmGUI* is a self-written extension in R interacting with the functionality of GLM. It provides two basic application functions - the logical elements of model-fit criteria calculations and graphical user interfaces for data

visualization. The package requires a software version of R of \geq 3.4 and the version of *rLakeAnalyzer* \geq 1.8.3. All required R packages are automatically installed during the first installation of *glmGUI*.

2.3 Graphical User Interface

The Graphical User Interface is constructed as a window based design using functions of the R package gWidgets
(Verzani, 2014), which provides several toolkits for producing user interfaces by creating e.g. labels, buttons, containers, or drop lists. The GUI is organized in a main menu with five sections. Submenus and result messages are opened in separate windows (Fig. 1).



Fig. 1: Window-based structure of glmGUI with examples of the submenu 'Calculate SI-value' and of the result message 10 'Temperature RMSE' created after a model run.

2.3.1 Data pre-processing and model efficiency

The GUI enables either the usage of an existing simulation control file of GLM (glm2.nml) from a selectable workspace (section 1, Fig. 1), or the creation of a new control file using the function nml_template_path() of the R package *GLMr* (<u>https://github.com/GLEON/GLMr</u>). The lake specific parameters and settings are in accordance with the deposited file

of *GLMr* and is due to change with the current GLM version. The input data are automatically listed in section 2 (Fig. 1), if stored at the path as specified in the control file. All included time series of input data can be visualized and tested against missing values (NA). The toolbox includes an option to fill the missing values applying the non-parametric Kalman-filter method (Grewal, 2011) using the R package *imputeTS* (Hyndman and Khandakar, 2007). Several filter

- 5 methods were tested by manually removing values from existing time series of meteorological data and interpolating these missing values. The Kalman smoothing could deliver the best and most constant results for all kinds of the various meteorological data. If selected, an autofill option writes the interpolated values directly to the input file. All parameter settings defined within the control file can be shown and changed by the GUI (section 3, Fig. 1).
- The model simulation can be run (section 5, Fig. 1) and several plot options can be selected to compare the model result with observed field data (section 4, Fig. 1). As lake level variations can have a strong impact on the water temperature distribution within lakes (especially true for shallow waters), the validation of the lake level simulation results is provided within the GUI additionally to the water temperature. The root mean square error (RMSE), which is often applied as model fit criteria in lake modeling studies (e.g. Bueche et al., 2017; Luo et al., 2018; Frassl et al., 2018), can be computed for both model output variables. Additionally, the mean bias error (MBE, average of the lake level
- 15 differences of all time simulated time steps) is calculated for lake level simulations. Both model criteria are calculated for all available observed data points and averaged subsequently.

2.3.2 Plots and output visualization

Plot options are provided by *glmGUI* for the input time series in section 2 (Fig. 1) and for all output variables generated by GLM (csv and netCDF, section 5). This includes simple line plots (e.g. for lake level or evaporation) and contour
plots for parameter varying in lake depth, such as water temperature or density. In addition, two types of contour plots of the vertical profile can be created. First is the visualization of observed and modeled water temperatures in one plot above each other with the option of the measured data as point-overlay to mark where and when field data are available (areas in between are interpolated to draw the plots, Fig. 2). Second plot visualizes the temperature differences between the interpolated measured values and the modeled data. This plot type is a new feature enabling a quick overview on the

- 25 spatial and temporal errors and deviations of the simulation (Fig. 9). The displayed deviations are fixed to 9 classes in the range of the errors between -5 °C to +5 °C and all values beyond these limits are shown in one color (≤ -5 in dark blue and ≥ 5 in red) summarizing and highlighting extreme errors. The spatial reference in both plots is the lake surface, but lake level variations are represented by changes in depth, which become visible at the "bottom" of this plot type. The generation of the contour plots is based on functions provided by *glmtools*. The default settings to scale the color
- 30 bar legend for water temperature plots take into account the range of temperatures and also erroneously the range of



lake depth. This method is adopted in glmGUI, while discarding the consideration of the lake depth, and the temperature range is adjusted explicitly to the plotting method to provide well differentiated color ranges in the legend.

Fig. 2: Example of a contour plot of observed (top) and modelled (below) water temperatures for Lake Ammersee. Black dots mark the availability (time/date and depth) of observed water temperatures.

2.3.4 Sensitivity analysis

To reduce the effort of the model calibration process only sensitive parameters should be included (Luo et al., 2018), which usually are identified applying a sensitivity analysis. It investigates how variations in the output of a numerical model can be attributed to variations of input parameters or factors (Pianosi et al., 2016). The widely used approach after Lenhart et al. (2002) is implemented in the GUI. The Sensitivity Index (SI) is calculated for each selected

5 after Lenhart et al. (2002) is implemented in the GUI. The Sensitivity Index (SI) is calculated for each selected parameter separately, since only one parameter is changed at a time:

$$SI = \frac{(y_1 - y_2)/y_0}{2\Delta x/x_0}$$
(1)

- 10 The parameter with the value x_0 is increased and decreased by Δx . The resulting outputs y_1 and y_2 (either water temperature, lake level or the respective RMSEs) are subtracted and normalized by the output y_0 , which results from using the unchanged parameter value x_0 . Δx can be set to four different values in the GUI (5%, 10%, 20%, 50%). It can be chosen out of four grades of relative changes of a parameter. The sensitivity of the simulation can be analyzed concerning the model output of water temperature or lake level. SI-values can be calculated based on either the 15 respective model output or the RMSE, as also applied by Rigosi et al. (2011).

2.3.4 Autocalibration

Since the GLM uses empirical equations (Hipsey et al., 2017), model parameters can be adjusted during the calibration process to minimize the error between model output and observations (Luo et al., 2018). As an alternative to adjust the parameters manually in the glm2.nml-file, *glmGUI* provides an automatic calibration tool for preselected parameters of

- 20 surface dynamics, mixing parameters, and hydrological and meteorological factors (Table A1). The user can choose out of those parameters that are to be included in the calibration process and define a percentage range, by which the upper and lower limit of every parameter is changed from the value in the glm2.nml-file. The resolution of the increase/decrease of the parameters within the defined limits can be set as well. According to these settings, model runs of GLM are executed with all possible combinations of the selected parameters ("brute-force"). The overall RMSE of
- the lake level or water temperature is calculated and saved for every parameter combination to a csv file, with the "best fit" being indicated.

The automated calibration of the lake level includes also the optimization for the parameter *inflow_factor* for multiple lake inflows. This enables an approximation to the water balance and the reproduction of the lake level, if the contribution of inflows is unknown, which is often the case for groundwater inflows or smaller tributaries.

The runtime of the calibration algorithm (t_cal) increases exponentially with the number of parameters (p) to be calibrated (Eq.(2))

$$t_{cal} = r^p * (t_{GLM} + t_{RMSE}) \tag{2}$$

5 with *r* as the number of tested values for each parameter p and t_GLM , t_RMSE as runtimes of the lake model and the calculation of the output RMSE.

3 Case study Lake Baratz

3.1 Study site

Lake Baratz is located in the northwest of Sardinia (Fig. 3), Italy, and is the only natural lake of the island. The

- 10 elevation of its bottom is 18.6 m a.s.l. and the lake level suffered significant changes in the last two decades with a maximum lake depth of 11 m and a minimum of 3 m (Giadrossich et al., 2015; Niedda et al., 2014). The overflow spillway of the lake is at 32.5 m a.s.l. (Niedda et al., 2014). At this maximum level the lake has a surface of about 0.6 km² and volume of 5.1×10^6 m³ (Giadrossich et al., 2015). As lake-overflow events to the sea were extremely rare in the past century the catchment area can be considered as a closed-basin (Niedda and Pirastru, 2013). The lake watershed
- 15 is about 12 km² with a maximum elevation of 410 m (Pirastru and Niedda, 2013). The only significant tributary is inflowing the lake in the northeast and drains a sub-catchment area of 8.1 km². Due to a very dry summer season the water inflow starts usually in December and ends in May (Giadrossich et al., 2015).

The lake can be classified as eutrophic and the water is brackish. Thermal stratification usually establishes in February or early March and lasts to early autumn (Giadrossich et al., 2015). Lake mixing occurs all throughout winter and thus,

20 it can be classified as a warm monomictic lake.



Fig. 3: a) Lake Baratz and its hydrological catchment area and observation station, b) Observation stations outside of the lake watershed (grey area), c) Contour lines of the lake basin. The blue area indicates the lake surface at a lake level of 8 m (equal to an elevation of 26 m a.s.l) observed in November 2012. Brown lines display dry terrain and cyan isobaths at this lake level.

3.2 Sensitivity analysis and calibration

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The simulation period for Lake Baratz is determined to be 13.07.2011 to 31.12.2016. We assume the light extinction coefficient value $K_w = 0.57 \text{ m}^{-1}$ is representative of the whole study period. Kw is calculated dividing the Secchi-disk constant (in this case the minimum value of 1.44 was taken as it usually ranges between 1.44 and 1.80, Hornung, 2002;

10 Holmes, 1970; Chapra, 2008) by the mean Secchi-disk depth of 2.50 meters (data from June 2016 to June 2017). A similar value can be obtained considering a Secchi-disk average depth of 3 meters (assumed when the lake had a higher water level) and Secchi-disk constant of 1.70 (Poole and Atkins, 1929). A further detailed description on the applied

meteorological and hydrological model input data, the field data, and the data processing can be found in the Appendix A.

The calibration process of the lake level was accomplished without hydrological parameters, as preliminary estimations of the water balance considering the seasonality of the inflow and subsurface outflow already exist (see Appendix

5 A3.3), which are also applied in this study. Thus, the sensitivity analysis was performed considering only the parameters of surface dynamics and the *wind_factor* as wind can have an impact on the lake level due to its influence on evaporation. The options of 10 % increase and the RMSE as measure of deviation were selected.

After Lenhart et al. (2002) only one of four parameters (*cd*) is found to have a negligible sensitivity indicated by a SI-value of below 0.01. The analysis revels a high sensitivity for the parameters *ch* (SI = 0.234, see also Fig. 4) and *ce* (SI = 0.334) and a medium for *wind factor* (SI = 0.089).

- The sensitivity analysis regarding water temperature was conducted for parameters of lake mixing, surface dynamics, and the wind factor with the same options as selected for the lake level. Negligible SI-values of 0.005 and below are found for all considered parameters except for *ce* (SI = 0.232) and *wind_factor* (0.290) with a high sensitivity, and *ch* (0.050) with a sensitivity at the threshold between medium and small (Fig. 4). According to both sensitivity analyses the
- 15 model is calibrated first for the lake level considering these three parameters with medium and high sensitivity. As the model is found to be sensitive in lake level and water temperature simulations for changes in the same parameters, the calibration for water temperature simulations was performed only considering *ce* and *wind_factor* to prevent a decline of the lake level reproduction by the water temperature calibration. Not considering parameter ch is plausible, as its SI value matches only just the threshold to be medium sensitive. In addition, small parameter value ranges of 10 % are
- 20 applied. Within the calibration process a total number of approx. 3000 simulation runs were conducted in 6 autocalibration runs.



Fig. 4: Sensitivity Index after Lenhart et al. (2002) of GLM simulations of Lake Baratz regarding the lake level (blue) and water temperature (cyan). The lower horizontal line (SI = 0.05) marks the threshold between small and medium sensitivity, the upper line (SI = 0.20) between medium and high sensitivity.3.3 Simulation results

The calibration processes for lake level simulations of the lake model reveals the best fit when applying an unchanged parameter value for *ch* and an adjustment of *ce* to 0.001748 and of *wind_factor* to 1.56. The simulated lake level of Lake Baratz shows very good model fit criteria of an average RMSE = 0.11 m and an average MBE = 0.05 m. The seasonal pattern of the lake level, characterized by a strong increase during winter and a drop during summer, is represented well. Additionally, the general decrease of the water stage by about 3 m during the simulation period is simulated correctly, which proves the capability of the model to reproduce the water balance of the lake and its

catchment area.

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Fig. 5: Observed (blue) and simulated (red) lake level of Lake Baratz.

The modeled water temperatures simulated with the adapted lake parameters found by the (auto-)calibration yield an overall average RMSE of 1.30 °C. A period of remarkable deviation of simulated and observed lake level is induced in

- 5 January 2014, which could be attributed to uncertainties in the discharge input data simulated by a hydrological model. The basin in that period of the year is still in an intermediate status of soil moisture. Probably the hydrological model overestimated the discharge on the base of rainfall events in January 2014 which in reality did not produce a significant lake level variation (see Fig. 2 in Giadrossich et al., 2015). However, the observed and simulated lake levels in Fig. 5 have the same trend and the error caused in January is propagated throughout the year.
- 10 The model reproduces stratified and isothermal conditions (Fig. 6). A detailed overview on the temporal and spatial differences between the observed and simulated water temperatures is given in Fig. B1. The simulation can be assessed as a robust fit (Bruce et al., 2018), especially when considering the high degree of thermal dynamics due to the shallow



depth of the lake and an additional enhancement by highly variable lake level (Fig. 6). The results approve also GLM to be applicable for shallow lakes in warm climates with high variety in lake level.

Fig. 6: Observed (top) and simulated (bottom) water temperatures of Lake Baratz.

4 Case study Lake Ammersee

4.1 Study site

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The pre-alpine Lake Ammersee (Fig. 7) has a maximum depth of 83.7 m, a surface area of 46.6 km² and a volume of about 1.8×10^9 km³ (Bueche and Vetter, 2014a). The mixing regime can be classified as dimictic, but also monomictic seasons occur (Bueche, 2016). The trophic status is currently mesotrophic (Vetter and Sousa, 2012).

The lake has a catchment area of about 994 km² and its outflow in the north (Stegen gauge station). The main tributary is River Ammer, which contributes approximately 80% of the total annual discharge to the lake (Bueche and Vetter, 2015). Several other streams and creeks inflow into the lake, but only River Rott and Fischbach have a share of greater than 5 % of the total lake catchment area size (see Fehler! Verweisquelle konnte nicht gefunden werden.7, Suppl.

10 Material). Additionally, groundwater is assumed to inflow the lake, which has not been quantified yet (Bueche and Vetter, 2014b). The mean lake level is 532.9 m a.s.l. and usually varies about 1 m (Bay. LfU, 2018).



Fig. 7: Catchment area (with sub-catchments) of Lake Ammersee. Dots mark the locations of hydrological observation stations (Source DEM: Elevation data from ASTER GDEM, a product of METI and NASA, Source geo-data: Geobasisdaten © Bayerische Vermessungsverwaltung, www.geodaten.bayern.de).

4.2 Sensitivity analysis and calibration

- 5 The simulation period for Lake Ammersee is chosen to be 30.01.2014 to 31.12.2017 starting when reliable field data of the lake station is available consistently (see Supplemental Material, section 2). The initial profile of water temperatures is taken from the observations of that date. No water quality data were available for the simulation period and the salinity values are derived from conductivity measurements of January 2004, when similar thermal conditions of a slight inverse stratification were prevailed and equivalent salinity conditions can be assumed. As the trophic status has
- 10 not changed since 2004 the average value K_W of 0.35 m⁻¹ determined for the period 2004 to 2008 from secchi-disk observations (data surveyed and provided by Bavarian Environment Agency) is used for the GLM simulations in this study.

The calibration of the lake level considers the inflow_factor (i.e. simple factor for the discharge values of the inflows) of the four defined inflows of River Ammer, River Fischbach, groundwater inflow, and the sum of River Rott, River

- 15 Kienbach, and all other unknown inflows. Thus, the adjustment of the representative *inflow_factor* includes the required correction of the available discharge data considering the observations are not taken at the stream inlet to the lake but at an upstream location. This is especially relevant for River Ammer with its gauge at Weilheim (Fig. 7). Meteorological input data are taken by a raft station at the lake center except for precipitation and cloud cover data (see Supplemental Material, section, for a detailed description about the sources of the used meteorological and hydrological input data and
- 20 the processing of the data).

The sensitivity analysis regarding the water temperature (increase: 10%, measure of difference: RMSE) reveals seven parameters with an SI > 0.05 indicating a medium sensitivity (after Lenhart et al., 2002, Table 1). In order to reduce the calculation time of the autocalibration runs, four parameters of high sensitivity with a SI above 0.2 are chosen for this process. In total approx. 50000 simulation runs in 12 autocalibration runs were performed within the calibration process.

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Table 1: Values of SI for Lake Ammersee water temperature simulations.

| Parameter | SI |
|----------------|-------|
| ch | 0.534 |
| coef_mix_shear | 0.484 |
| coef_mix_turb | 0.410 |
| wind_factor | 0.210 |
| cd | 0.126 |
| coef_mix_KH | 0.097 |
| coef_wind_stir | 0.060 |
| ce | 0.034 |
| coef_mix_conv | 0.015 |
| coef_mix_hyp | 0.008 |

4.3 Simulation results

The calibration of the lake level simulation yields its best fit for the combination of the inflow factors for the defined tributaries River Ammer of 1.10, River Fischbach of 0.72, groundwater of 1.07, and Rivers Rott, Kienbach and all other smaller and unknown inflows of 1.01. By using these adapted inflow factors instead of the default value of 1.0, overall RMSE reduced significantly from 1.10 m to 0.20 m, and the MBE from -1.00 m to 0.09 m, and the achieved model fit can be assessed as very satisfactory. The simulation shows periods of general deviations of over 0.20 m up to 0.55 m for some months, but reproduces well the short-term fluctuations (Fig. 8). The remaining errors and differences can be

- 10 ascribed to the uncertainties and lack of data for some inflows as assumptions and estimations for the unknown surface input and the groundwater inflow had to be made. More detailed hydrological data might explain remarkable dates, like during summer, when the trend of simulated and observed lake level changes abruptly. No obvious explanation for these trend shifts could be found, although a detailed investigation of the existing hydrological data was conducted. An impact of a highly complex groundwater inflow system is likely to have a key role in the water balance of the lake,
- 15 which is not considered by the applied input data sufficiently. Furthermore it cannot be ruled out that unknown alterations or errors in the observation setup of the gauges cause these "turning points" as some of them correspond to flood events, which might have implied problems with the measurements. However, it was possible to improve the lake level simulation distinctively considering only the parameter *inflow_factor* for multiple inflows within the calibration process.



Fig. 8: Observed (blue) and simulated (red) lake level of Lake Ammersee.

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Simulated water temperatures reveal an overall RMSE of $1.172 \, ^{\circ}$ C. The highest deviations occur within the metalimnion at a depth between 7 – 18 m (Bueche and Vetter, 2014a) during summer stratification, when the model underestimates the temperature (Fig. 9). This is accompanied by too warm layers in the upper epilimnion in a depth of about 20 m. However, the general seasonal pattern is reproduced adequately and differences during winter are negligible.





Fig. 9: Contour plot of differences between simulated and observed water temperatures of Lake Ammersee.

5 Discussion

The implemented option of an autocalibration in the toolbox enables a less time-consuming and more efficient

- 5 parameter optimization compared to a conventional manual calibration procedure (Luo et al., 2018). The utilization of such automatization techniques is advised for lake modeling studies (Ladwig et al., 2018). Hence, the provided tool can be seen as the centerpeace of the developed GLM Toolbox, which is complemented by the plotting option of differences between observed and simulated water temperatures. This model output visualization enables an immediate overview on the simulated deviations and their spatial distribution without any further post-processing of the model results.
- 10 Although no detailed quantification of the error is possible, this illustration allows a very quick qualitative comparison of different simulation settings. Such visualization option for GLM output has not yet been provided for an open-source software before.

The easy handling and free availability of the GUI expands the reach to potential user of the GLM beyond the limnological research specialists. The used scripting language R is already widespread in limnological (e.g. Winslow et

15 al., 2016), hydrological and environmental research (e.g. Pilz et al., 2017; Gampe et al., 2016), as well as in the field of automation of water management processes (e.g. Erban et al., 2018). Providing the R code as development version (<u>http://doi.org/10.5281/zenodo.2025865</u>) in addition to the R package, enabling the GUI and its tools to be easily customized by users for other specific demands and then again to be shared with the public. Due to the small number of considered parameters in the calibration process of the presented case studies, the efficiency was successfully tested for a realistic effort of time. The visibility of the simulation error provided by the created difference contour plots gives the opportunity to combine the automated calibration easily with expert knowledge. However, the time consumption of an autocalibration run of several days and more for combinations of larger number

5 of parameters and higher intervals might hamper of the calibration efficiency of a solely automatized calibration and can be improved in upcoming versions of the toolbox. At present running the tool on a server in advance or as a "background task" can compensate for this problem.

Further limitations of the toolbox/GUI have to be mentioned and more coding activities should be addressed to minimize the following issues. 1) The contour plots of water temperatures indicate the lake level on the bottom either

- 10 interpolated or in very coarse lake level fluctuation, which does not allow a sufficient derivation of this model output by these plots. For this purpose separated plots of the lake level simulations can be created. 2) The calibration algorithm of the toolbox creates parameter values with a high decimal precision due to the approach of percental alteration. This might pretend a false sensitivity of the model and a too detailed accuracy of the calibration for the respective parameter.
 3) The method of the sensitivity analysis will yield a SI = 0 for any included parameter with the initial value being 0.
- 15 This applies for example to *seepage_rate* as its default value is 0. 4) The applied model version of GLM is dependent of the maintenance on the R package *glmtools*.
 The presented simulations of lake water temperatures have an average overall RMSE of 1.30 °C and 1.17 °C. This is within the range of values obtained by other lake modeling studies applying GLM or other lake 1-D models (Bueche et al., 2017; Ladwig et al., 2018; Robertson et al., 2018; Frassl et al., 2018). This simulation quality was achieved even by
- 20 only a few autocalibration runs showing the effectiveness of the tool. In addition to the visualization options and the calibration tool for water temperature simulations, *glmGUI* enables also a calibration of the lake level to achieve a correct reproduction of the water stage. This is especially important for smaller lakes, for which an incorrect simulation of the lake level can have a significant impact on the water temperature reproduction. Furthermore, as the lake level is the result of the lake-catchment water balance (Vanderkelen et al., 2018),
- 25 the applicability of GLM is enhanced also to hydrological analysis and water balance investigations by this feature. The GLM uses the bulk aerodynamic formula to estimate the latent heat flux and therefore evaporation (Hipsey et al., 2014), which is commonly applied to assess the evaporation rate over open water bodies (Fischer et al., 1979; Hicks, 1972). Including the GLM in the hydrological analysis can therefore improve the accuracy of the modeled evaporation and thus the water balance estimate. In this study, a RMSE for the lake level simulations of 0.11 m (Lake Baratz) and 0.20
- 30 m (Lake Ammersee) is achieved, which is within the range of the GLM performance shown by Weber et al. (2017), and attests a good accordance of the modeled water level with the observed values (Hostetler, 1990).



The GUI is also able to execute simulation runs of GLM coupled with water quality models of ecological lake models (e.g. Aquatic Ecodynamics Modelling Library, AED). Although water quality settings cannot yet be changed using the toolbox, any model generated output can be plotted.

5 Conclusions

- 5 The presented R package *glmGUI* wraps up simulation and processing tools for the GLM. This includes a tool to autocalibrate the model and options of a parameter sensitivity analysis. Both tools can be used to examine the two simulation output variables of water temperature and lake level. Furthermore, *glmGUI* implements several visualizations options for the meteorological and hydrological input data and the model output. After the deployment of other R packages to execute GLM and for model output post-processing and statistical analysis (*rLakeAnalyzer*, *rGLM*,
- 10 *glmtools*) *glmGUI* close the gap of missing tools to simplify and accelerate the calibration process and to extend visualization options.

The tools are tested for two different lakes (deep, dimictic, perennial inflow, and shallow, monomictic, seasonal inflow) located in varying climate zones. Good model results were achieved after a low expenditure of calibration effort. In contrast to many other studies an exhaustive description of the simulation input data and field data (data for Lake

15 Ammersee also provided as example data) is given within this paper (as Supplemetal Material). The GUI includes tools to check the quality of the input data. This comprises the option of a visual detection of errors, missing values and plausibility.

The development of *glmGUI* for the free and open-source programming language R, available on all common platforms (Windows, OS X, Linux), makes it accessible for anyone to use, which contributes to scientific transparency (Winslow

- 20 et al., 2018). The GUI allows a high level of interoperability due to the option of combining with other operating systems. This includes the coupling of GLM with ecological lake models (e.g. Snortheim et al., 2017; Robertson et al., 2018; Weber et al., 2017; Fenocchi et al., 2019), as the toolbox is already applicable for this purpose and can be the basis for establishing of a coupling interface. Furthermore, we designed the software with the aim of a high flexibility for the application of other scenarios, for various study areas or with diverse time steps. An increasing number of lake
- 25 modeling studies are investigating the impact of global change on lakes using as meteorological input data regional climate model output or future scenarios (Fenocchi et al., 2018; Weinberger and Vetter, 2014; Bueche and Vetter, 2015; Ladwig et al., 2018; Pietikäinen et al., 2018; Piccolroaz and Toffolon, 2018). For analyses in these fields of research the presented R package *glmGUI* will be a powerful tool, especially concerning the provided difference contour plots.
- 30 *Code and data availability:* The package and R-code are available at <u>http://doi.org/10.5281/zenodo.2025865</u>. Example data for Lake Ammersee are attached to this paper as a supplementary data. Sources are described in Appendix B.

Author contributions: TB and MV initiated the idea and concept of glmGUI. MW and BP developed the glmGUI package and code. The study sites were suggested by TB and FG. FG and MP operated the raft station and data collection at Lake Baratz. Data pre-processing was conducted by TB with support of MP, FG and BP. Simulations and

analyses have been conducted by TB with support of FG, MP and MV. The manuscript was prepared by TB with 5 contributions of all co-authors.

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Appendix A: Model input data and calibration parameter

| Parameter | Unit | Description |
|----------------------------|-------------------|--|
| Meteorological parameters: | | |
| Air temperature | °C | average air temperature 10 m above the water |
| | | surface |
| Wind speed | ms ⁻¹ | average wind speed 10 m above the water surface |
| Relative Humidity | % | average relative humidity $(0 - 100 \%)$ 10 m above the |
| | | water surface |
| Shortwave radiation | Wm ⁻² | average shortwave radiation |
| Longwave radiation | Wm ⁻² | Longwave radiation input is assumed to be direct |
| | | incident intensity |
| Rainfall | md^{-1} | rainfall depth |
| Cloud cover (optional) | - | Required if no information on longwave radiation available and |
| | | incoming longwave flux is estimated from cloud cover fraction |
| | | data |
| Snowfall (optional) | md^{-1} | snowfall depth |
| Hydrological parameters: | | |
| Inflow discharge | m^3s^{-1} | Average discharge |
| Water temperature | °C | average streamflow water temperature |
| Salinity (optional) | mgl ⁻¹ | streamflow salinity |
| Outflow discharge | m^3s^{-1} | average discharge |

Table A1: Required model input data (after Hipsey et al., 2014).

| Parameter (glm.nml ID) | Description |
|-----------------------------|---|
| Lake Properties | |
| Kw | Extinction coefficient for PAR radiation (unit: m ⁻¹) |
| Surface Dynamics | |
| ch | Bulk aerodynamic coefficient for sensible heat transfer |
| ce | Bulk aerodynamic coefficient for latent heat transfer |
| cd | Bulk aerodynamic coefficient for transfer of momentum |
| Mixing Parameters | |
| coef_mix_conv | Mixing efficiency - convective overturn |
| coef_wind_stir | Mixing efficiency - wind stirring |
| coef_mix_shear | Mixing efficiency - shear production |
| coef_mix_turb | Mixing efficiency - unsteady turbulence (acceleration) |
| coef_mix_KH | Mixing efficiency - Kelvin- Helmholtz turbulent billows |
| coef_mix_hyp | Mixing efficiency of hypolimnetic turbulence |
| Hydrological and meteorolog | cical factors |
| seepage_rate | Rate of seepage from the deepest layer (unit: m day ⁻¹) |
| inflow_factor | Factor for inflow(s) |
| outflow_factor | Factor for outflow |
| Rain_factor | Factor for rainfall |
| wind_factor | Factor for wind speed |

Table A1: List of preselected parameters for autocalibration (after Hipsey et al., 2017).



Fig. B1: Contour plot of differences between simulated and observed water temperatures of Lake Baratz.

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