

Supplementary Materials

Article title: The quasi-equilibrium framework re-visited: analyzing long-term CO₂ enrichment responses in plant-soil models

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The following Supporting Information is available for this article:

Figure S1 Illustration of effect of allocation flexibility on plant response to elevated CO₂ and nitrogen deposition.

Figure S2 Sensitivity test of varying N uptake parameters on CO₂ fertilization effect.

Figure S3 Sensitivity test of varying priming effect parameters on the M-term CO₂ fertilization effect.

Table S1 Relationship of NPP and leaching N rate at different timescales

Table S1 Relationship of NPP ($\text{kg m}^{-2} \text{yr}^{-1}$) and leaching N rate (N_{loss} , $\text{kg m}^{-2} \text{yr}^{-1}$) at different timescales, assuming explicit mineral N pool. VL400 is the very long term timescale under $\text{CO}_2 = 400$ ppm, and M_{800} , L_{800} and VL_{800} are medium, long, and very long term equilibrium point under $\text{CO}_2 = 800$ ppm. Leaching rate is assumed at 0.05 yr^{-1} , which is assumed to be the sum of all N lost from the system (i.e. leaching, denitrification, etc.). Detailed derivations and assumptions provided in Section 3.2 of the manuscript.

Timescale	NPP ($\text{kg m}^{-2} \text{yr}^{-1}$)	N_{loss} ($\text{kg m}^{-2} \text{yr}^{-1}$)
VL400	1.68	0.4
M_{800}	1.79	0.23
L_{800}	1.90	0.395
VL_{800}	1.91	0.4

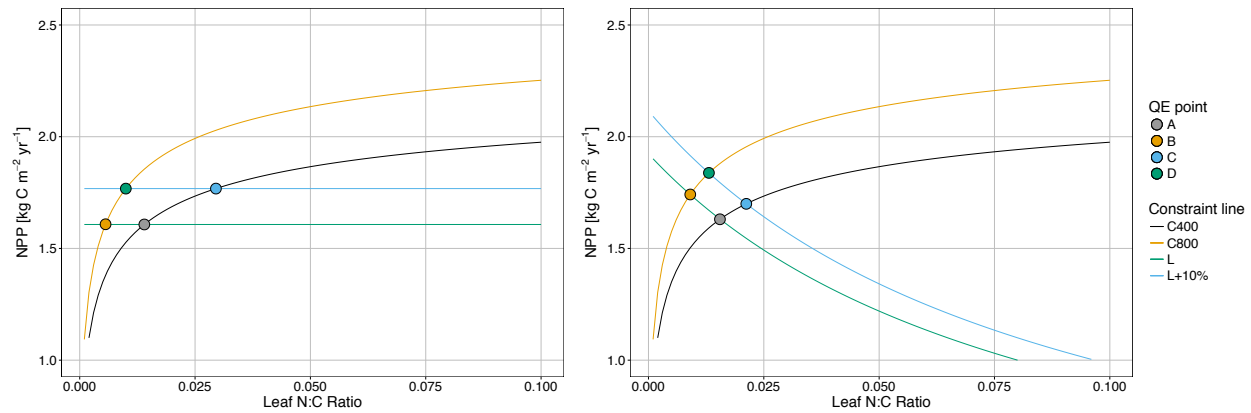


Figure S1 Illustration of effect of allocation flexibility on plant response to elevated CO_2 and nitrogen deposition, with a) as no coupling between allocation of leaf and wood, and b) linear coupling between leaf and wood allocation. No coupling assumes that allocation to wood (a_w) = 0.6, and allocation to leaf (a_f) = 0.2. Linear coupling assumes the same a_f , but $a_w = 3a_f$. The detailed derivations are shown in Medlyn and Dewar (1996). C400 and C800 are the photosynthetic constraint curves at $\text{CO}_2 = 400$ ($a\text{CO}_2$) and 800 ppm ($e\text{CO}_2$), respectively. L and L+10% are the long-term soil recycling constraint under ambient and ambient + 10% nitrogen deposition rate. Point A is the equilibrium point between C400 and L, point B is the equilibrium point between C800 and L, C is equilibrium point between C400 and L+10%, and D is equilibrium point between C800 and L+10%. The graph shows that linear coupling of a_f and a_w resulted in more responsive NPP to $e\text{CO}_2$ even if N deposition does not change, whereas no coupling between a_f and a_w has no effect of CO_2 on production, unless N deposition increases.

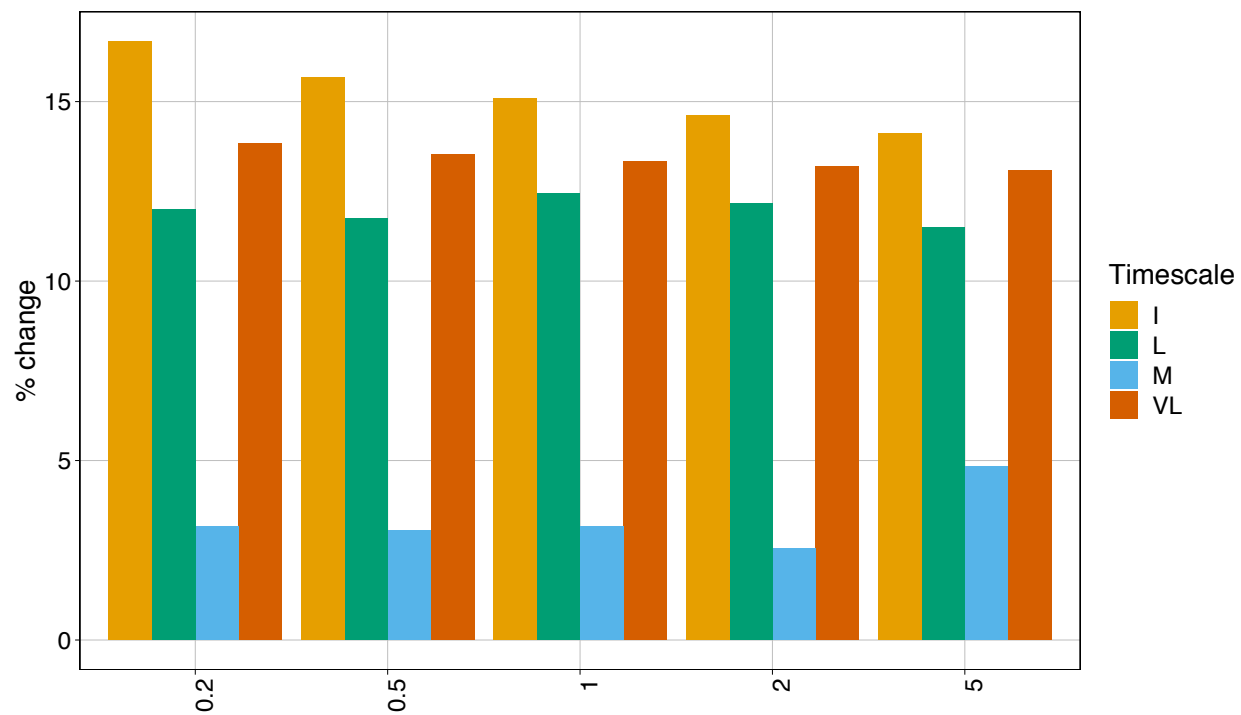


Figure S2 Sensitivity test of varying nitrogen uptake coefficient on the CO₂ fertilization effect (% change) at various equilibrium points. Nitrogen uptake coefficient are 0.2, 0.5, 1, 2 and 5 yr⁻¹. I: instantaneous, M: medium term, L: long term, VL: very long term.

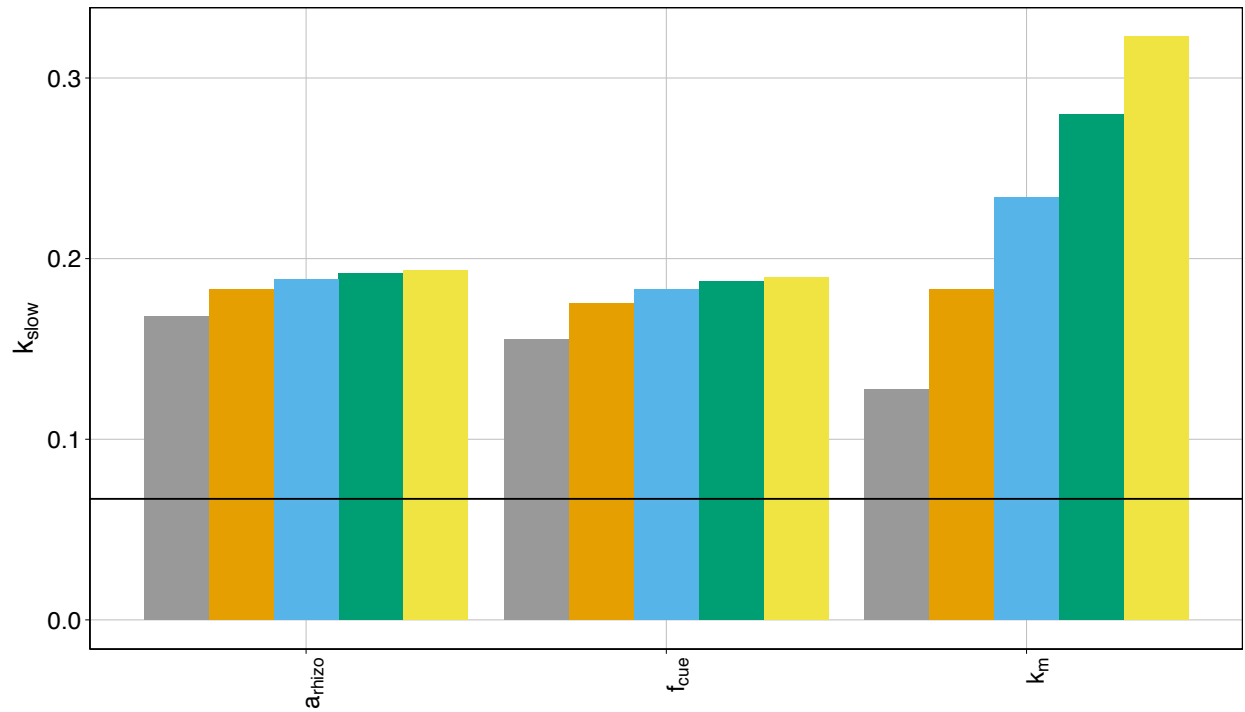


Figure S3 Sensitivity test of varying priming effect parameters on the decomposition rate of slow soil organic matter pool (k_{slow}). Parameters varied are allocation coefficient to rhizosphere (a_{rhizo}), microbial carbon use efficiency (f_{cue}), and scaling factor (k_m). From left to right, value ranges are: 0.1, 0.2, 0.3, 0.4, and 0.5 for a_{rhizo} , 0.1, 0.2, 0.3, 0.4, and 0.5 for f_{cue} , and 1, 2, 3, 4, 5 for k_m . Default values are, Black horizontal line is the existing k_{slow} value, before introducing priming effect.