1 2	Bayesian Inference and Predictive Performance of Soil Respiration Models in the Presence of Model Discrepancy
2 3	of woder Discrepancy
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47 48 49 50	Key Points		
	(1)	Bayesian inference and prediction are useful to evaluate multiple soil respiration models	
51		with different levels of model complexity.	
52	(2)	Data models used in Bayesian inference have substantial impacts on model parameter	
53		distributions and subsequently model predictions.	
54	(3)	Using exponential power distribution and considering heteroscedasticity in data models	
55		improve Bayesian inference and prediction.	
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68	Keywo	ords: Soil respiration, modeling, Bayesian, likelihood function, data model, autocorrelation,	
69	hetero	scedasticity, skew exponential power distribution, cross-validation, scoring rule	
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72 Abstract

Bayesian inference of microbial soil respiration models is often based on the assumptions that the 73 residuals are independent (i.e. no temporal or spatial correlation), identically distributed (i.e. 74 Gaussian noise) and with constant variance (i.e. homoscedastic). In the presence of model 75 discrepancy, since no model is perfect, this study shows that these assumptions are generally 76 invalid in soil respiration modeling such that residuals have high temporal correlation, an 77 increasing variance with increasing magnitude of CO₂ efflux, and non-Gaussian distribution. 78 Relaxing these three assumptions stepwise results in eight data models. Data models are the basis 79 of formulating likelihood functions of Bayesian inference. This study presents a systematic and 80 comprehensive investigation of the impacts of data model selection on Bayesian inference and 81 predictive performance. We use three mechanistic soil respiration models with different levels of 82 model fidelity (i.e. model discrepancy) with respect to number of carbon pools and explicit 83 representations of soil moisture controls on carbon degradation, and accordingly have different 84 levels of model complexity with respect to the number of model parameters. The study shows data 85 models have substantial impacts on Bayesian inference and predictive performance of the soil 86 respiration models such that: (i) the level of complexity of the best model is generally justified by 87 the cross-validation results for different data models; (ii) not accounting for heteroscedasticity and 88 autocorrelation might not necessarily result in biased parameter estimates or predictions, but will 89 definitely underestimate uncertainty; (iii) using a non-Gaussian data model improves the parameter 90 estimates and the predictive performance; and (iv) separate accounting for autocorrelation or joint 91 inversion of correlation and heteroscedasticity can be problematic and requires special treatment. 92 Although the conclusions of this study are empirical, the analysis may provide insights for 93 94 selecting appropriate data models for soil respiration modeling.

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95 1 Introduction

Developing accurate soil respiration models is important for realistic projection of global 96 carbon [C] cycle, as global soils store 2,300Pg carbon, an amount more than 3 times that of the 97 atmosphere (Schmidt et al., 2011) and release 60-75 Pg C/yr, about 7 times more CO₂ to the 98 atmosphere than all human-caused emissions (Le Quéré et al., 2014). The major work on soil 99 respiration modeling has been focused on advancing knowledge about model inputs and 100 calibration data (e.g. Janssens et al., 2003; Peters et al., 2007; Scott et al., 2009; Barron-Gafford et 101 al., 2011; Hilton et al., 2014) and on developing more advanced models for better representing 102 soil microbial processes (e.g. Schimel and Weintraub, 2003; Allison et al., 2010; Davidson et al., 103 2011; Wieder et al., 2013, 2015; Xu et al., 2014; Zhang et al., 2014). Integration of data and 104 models is indispensable for improving predictability of the terrestrial carbon cycle, and statistical 105 106 modeling is a vital tool for the model-data integration (Luo et al., 2011, 2014; Wieder et al., 2015). In addition, use of state-of-the-art statistical methods is necessary to accurately quantify 107 uncertainty in parameters and structures of soil respiration models for improvement and practical 108 109 uses of the models (Katz et al., 2013). A data model that is also known as a residuals model or an error model is used to characterize residuals (i.e., the difference between data and corresponding 110 model simulations). While a large number of data models have been used (e.g. Elshall et al., 2018; 111 Scholz et al., 2018) to our knowledge comprehensive and systematic evaluation of data models for 112 soil respiration modeling has not been reported in literature. 113

The objectives of this study are to evaluate the impacts of data models on Bayesian inference and predictive performance of three mechanistic soil respiration models, and to use the evaluation results to make broader recommendations. The three models were developed by Zhang et al. (2014) to simulate the Birch effect (the peak soil microbial respiration pulses in response to episodic 118 rainfall pulses) at a site scale and a short temporal scale; understanding the Birch effect is important 119 for gaining mechanistic understanding of CO₂ efflux production (Högberg and Read, 2006; Vargas et al., 2011). The models of Zhang et al. (2014) are based on an existing four-carbon pool model, 120 but have additional carbon pools and/or explicit representations of soil moisture controls on carbon 121 degradation and microbial uptake rates. The models were calibrated, and Bayesian model selection 122 was used to select the best model (Zhang et al., 2014). However, this effort was based on a single 123 data model. It is unknown whether the best model still remains the best (in terms of reproducing 124 the both calibration data and the cross-validation data) if a different data model is used. In addition, 125 126 since predictive performance of the models was not evaluated in Zhang et al. (2014), it is unknown whether the best model will give the best predictions. These two questions are addressed in this 127 study by considering eight data models and by evaluating predictive performance in a manner of 128 129 cross-validation. The top two models (also the two most high fidelity models) ranked by Zhang et al. (2014) are considered in this study, and the worst model (also the low fidelity model) is also 130 considered in this study for comparison. We use the terms model fidelity and model discrepancy 131 132 interchangeably. Model fidelity refers to the degree of realism of representing our scientific knowledge with respect to the real world system. That is a high fidelity model has less discrepancy. 133 Evaluating predictive performance for the three models with different degrees of fidelity provides 134 more insights than a single model. 135

Bayesian inference in general uses the Bayes' theorem to update the prior distributions of model parameters to posterior parameter distributions given a likelihood function of data. The mathematical formulation of the (formal and informal) likelihood function requires a probabilistic data model that however is intrinsically unknown due to unknown errors in all model components such as model structures, parameters, and driving forces. Bayesian inference of soil respiration 141 models often adopts the assumption of independent, normally distributed and homoscedastic residuals (e.g. Ahrens et al., 2014; Bagnara et al., 2015, 2018; Barr et al., 2013; Barron-gafford et 142 al., 2014; Braakhekke et al., 2014; Braswell et al., 2015; Correia et al., 2012; Du et al., 2015, 2017; 143 Hararuk et al., 2014; Hashimoto et al., 2011; He et al., 2018; Klemedtsson et al., 2008; Menichetti 144 et al., 2016; Raich et al., 2002; Ren et al., 2013; Richardson and Hollinger, 2005; Steinacher and 145 Joos, 2016; Tucker et al., 2014; Tuomi et al., 2008; Xu et al., 2006; Yeluripati et al., 2009; Yuan 146 et al., 2012, 2016; Zhang et al., 2014; Zhou et al., 2010). These assumptions are conveniently 147 adopted to satisfy the requirement of using an unknown probability model in Bayesian statistics, 148 which is called "a basic dilemma" by (Box and Tiao, 1992). 149

Postulating the data models is always based on assumptions about residual statistics, and the 150 most widely used assumptions are paired as follows: (i) independent vs. correlated residuals, (ii) 151 152 homoscedastic vs. heteroscedastic residuals, and (iii) Gaussian vs. non-Gaussian residuals. For soil respiration modeling few studies have relaxed the non-correlation assumption(e.g. Cable et al., 153 2008, 2011; Li et al., 2016b), the homoscedasticity assumption (e.g. Berryman et al., 2018; Elshall 154 et al., 2018; Ogle et al., 2016; Tucker et al., 2013), and the non-Gaussian and homoscedasticity 155 assumptions (e.g. Elshall et al., 2018; Ishikura et al., 2017; Kim et al., 2014). The recent study of 156 Scholz et al. (2018) relaxed these three assumptions using the generalized likelihood function 157 developed by Schoups and Vrugt (2010). However, few studies have focused on investigating 158 appropriateness and impact of these assumptions for soil respiration modeling, by relaxing the 159 independent residuals assumption (Ricciuto et al., 2011) and the Gaussian residuals assumption 160 (Ricciuto et al., 2011; van Wijk et al., 2008). By relaxing these three assumptions stepwise 161 resulting in eight data models, to our knowledge this is the first study that systematically evaluates 162 163 the impact of data model selection on Bayesian inference and predictive performance of soil

respiration modeling. In addition, to our knowledge this is the first soil respiration modeling studythat investigates the impact of data models in relation to model fidelity.

Relaxing these three assumption results in eight data models, which are shown in details in 166 Section 2. For example, combining the assumptions of independent, homoscedastic, and Gaussian 167 residuals leads to the standard least squares data model. This model is the simplest one among the 168 eight data models, since it requires only one parameter, i.e., the constant variance of the Gaussian 169 distribution. Note that there is a difference between the soil respiration model parameters and the 170 data model parameters. They technically can be jointly estimated, but one arises from assumptions 171 172 about soil respiration processes, and the other from assumptions about the residuals. Relaxing the homoscedastic assumption to heteroscedastic gives the weighted least squares data model. It is 173 more complex because it has extra parameters to account for multiple variances for multiple data. 174 175 Whenever one or combinations of the three assumptions (independence, homoscedasticity, and normality) are relaxed, the resulting data models become more complex and require more 176 parameters. Such systematic evaluation of data models (McInerney et al., 2017; Smith et al. 2010b, 177 2015) is necessary to evaluate appropriateness of residuals assumptions and their impacts on 178 Bayesian inference. 179

The assumptions of heteroscedastic, correlated, and non-Gaussian residuals are accounted for by using the method of Schoups and Vrugt (2010) in the following procedure: (i) the correlation is removed from the residuals by using an autoregressive model; (ii) the resulting residuals are normalized by a linear model of variance; and (iii) the normalized residuals are characterized by using the skew exponential power distribution. The data model parameters (i.e., coefficients of the autoregressive model, the linear variance model, and the skew exponential power distribution) are not specified by users, but estimated together with soil respiration model parameters during the 187 Bayesian inference. The skew exponential power distribution is general in that by adjusting the values of its kurtosis and skewness parameters the distribution can produce other distributions such 188 as the Laplace distribution (van Wijk et al., 2008; Ricciuto et al., 2011) and other distributions 189 through using an exponential model with different kurtosis parameters (Tang and Zhuang, 2009). 190 It is worth pointing out that there exist other methods to account for the three assumptions. Evin 191 et al. (2013) suggested accounting for residual heteroscedasticity before accounting for residual 192 autocorrelation. Lu et al. (2013) developed an iterative two-stage procedure to separately estimate 193 physical model parameters and data model parameters. Evin et al. (2014) developed a similar 194 procedure to first estimate model parameters and then estimate heteroscedasticity and 195 autocorrelation parameters. While this study uses the method of Schoups and Vrugt (2010), 196 exploring other methods is warranted in future studies. 197

198 After investigating the impacts of the data models on Bayesian inference, this study evaluates the impacts of the data models on predictive performance of the three soil respiration models. 199 Using random samples generated during the Bayesian inference, a prediction ensemble is produced 200 201 for each soil respiration model. The ensemble is used to evaluate predictive performance of the models in a stochastic sense by estimating to what extent the models can predict future events. The 202 evaluation in this study is done in a cross-validation manner by splitting the dataset of CO₂ efflux 203 into two parts for Bayesian inference and cross-validation, respectively. The evaluation of 204 predictive performance is important because different data models may give different parameter 205 distributions and accordingly different predictive performance. For example, the study of van Wijk 206 et al. (2008) concluded that the choice of the residual function is crucial to achieve accurate model 207 prediction and parameter estimation. Shi et al. (2014) showed that the posterior parameter 208 209 distributions and predictive performance given by two data models (weighted least square and

210 skew exponential power distribution after removing heteroscedasticity and autocorrelation) are 211 dramatically different, and a definitive conclusion was drawn that one data model is better than the other. The evaluation of predictive analysis is conducted for the following two cases: (1) the 212 prediction ensemble is generated by random samples of the soil respiration models only (i.e. 213 credible interval), and (2) the prediction ensemble is generated by random samples of not only the 214 soil respiration models but also the data models (i.e. predictive interval). The two cases lead to 215 different conclusions about the predictive performance. It is expected that the evaluation of 216 predictive performance conducted in this study can help select the most appropriate data model to 217 achieve optimal model predictions. 218

The remainder of the paper is organized as follows. Section 2 starts with a description of the evolving data models and their corresponding likelihood functions used in Bayesian inference, followed by a brief summary of the three soil respiration models. The results of Bayesian inference are discussed in Section 3 and Section 4, addressing the data model implications on parameter estimation and predictive performance, respectively. Section 5 summarizes the key findings and limitations of this study, and provides recommendations for approaching data model selection.

225 **2** Methodology

This section starts with a description of the eight data models that account for the three pairs of assumptions about residuals in a stepwise manner in Section 2.1. The data models are used to build the likelihood functions used in Section 2.2 for Bayesian inference. The three soil respiration models and observations of CO_2 efflux are described in Sections 2.3 and 2.4, respectively. Metrics for evaluating predictive performance are presented in Section 2.5.

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232 2.1 Data models

This study considers eight evolving data models starting from a data model that assumes independent, homoscedastic, and Gaussian residuals to a data model that relaxes all the three assumptions. The eight data models are based on the generic normalized residual,

236
$$a_t = \frac{\varepsilon_t}{\sigma_t}$$
 $a_t \sim X$, (1)

where $\varepsilon_t = d_t - Y_t$ is the residual (the difference between data d_t and its corresponding model simulation Y_t) at time or location t; σ_t is the standard deviation of the residual; and X is the probability density function (PDF) of a_t . The eight data models are formulated with different forms of ε_t , σ_t , and X. The standard least square (SLS) data model is

241
$$a_t = \frac{\varepsilon_t}{\sigma_0} \qquad a_t \sim N(0,1),$$
 (2)

where $\sigma_t = \sigma_0$ is a constant for all the data (i.e., homoscedasticity), and X is the standard normal 242 distribution, N(0,1). The unknown parameter σ_0 is estimated jointly with unknown physical 243 model parameters. If σ_i is not a constant (i.e., heteroscedastic), SLS becomes the weighted least 244 squared (WLS) data model. While heteroscedasticity can be accounted for through residuals 245 246 transformation (e.g. Thiemann et al., 200; Smith et al., 2010b) or other similar approaches (Gragne et al., 2015), a linear heteroscedastic model $\sigma_t = \sigma_0 + \sigma_1 Y_t$ is assumed here by following the 247 studies of Thyer et al. (2009), Schoups and Vrugt (2010), and Evin et al. (2013, 2014). With the 248 249 linear model, there is no need to estimate σ_t for each data. Instead, σ_t is calculated by estimating only two parameters, σ_0 and σ_1 . The WSL data model is written as 250

251
$$a_t = \frac{\varepsilon_t}{\sigma_0 + \sigma_1 Y_t} \qquad a_t \sim N(0, 1).$$
(3)

The two unknown parameters σ_0 and σ_1 are estimated jointly with unknown physical model parameters. The linear model assigns smaller weight to the data with larger simulation, Y_t . If the simulation is small and $\sigma_0 \gg \sigma_1 Y_t$, the weight becomes constant for all data. Both SLS and WLS assume that a_t is independently and identically distributed.

It is not uncommon that residuals are correlated in space and time, due to propagation of measurement errors (Tiedeman and Green, 2013) and model structure errors (Evin et al., 2014; Kavetski et al., 2013; Lu et al., 2013). The temporal correlation that occurs in the numerical example of this study can be accounted for by using a *p*-order autoregressive model. This leads to the data model of standard least square with autocorrelation (SLS-AC),

261
$$a_t = \frac{\varepsilon_t - \sum_{i=1}^p \phi_i \varepsilon_{t-i}}{\sigma_0} \qquad a_t \sim N(0,1)$$
(4)

where *p* is the order of autocorrelation, and ϕ_i is an autocorrelation coefficient. The unknown ϕ_i and σ_0 are estimated together with unknown model parameters. By extending the concept of correlated residuals to WLS leads to the weight least square with autocorrelation (WLS-AC),

265
$$a_t = \frac{\varepsilon_t - \sum_{i=1}^p \phi_i \varepsilon_{t-1}}{\sigma_0 + \sigma_1 Y_t} \qquad a_t \sim N(0, 1)$$
(5)

266 The unknown parameters of σ_0 , σ_1 , and ϕ_i are estimated jointly with physical model 267 parameters. Equations (2) – (5) assume that the residuals are Gaussian.

The next four data models are similar to the previous four models except that the standard normal distribution of a_t is replaced by the skew exponential power distribution, $SEP(0,1,\xi,\beta)$, with zero mean and unit standard deviation (Schoups and Vrugt, 2010)

271
$$p(a_t | \xi, \beta) = \frac{2\sigma_{\xi}}{\xi + \xi^{-1}} \omega_{\beta} \exp\left[-c_{\beta} |a_{\xi,t}|^{2/(1+\beta)}\right],$$
 (6)

272 where ξ is skewness, β is kurtosis, $a_{\xi,t} = (\mu_{\xi} + \sigma_{\xi}a_t) / \xi^{sign(\mu_{\xi} + \sigma_{\xi}a_t)}$, $\mu_{\xi} = M(\xi - \xi^{-1})$,

273
$$\omega_{\beta} = \frac{\Gamma^{1/2}[3(1+\beta)/2]}{(1+\beta)\Gamma^{3/2}[(1+\beta)/2]} , \qquad \sigma_{\xi} = \sqrt{(1-M^2)(\zeta^2+\zeta^{-2})+2M^2-1} ,$$

274
$$M = \frac{\Gamma[1+\beta]}{\Gamma^{1/2}[3(1+\beta)/2]\Gamma^{1/2}[(1+\beta)/2]}, \text{ and } c_{\beta} = \left(\frac{\Gamma[3(1+\beta)/2]}{\Gamma[(1+\beta)/2]}\right)^{1/(1+\beta)} \text{ are derived variables of } \beta \text{ and}$$

 ξ , and Γ[.] is the gamma function. The kurtosis parameter { $\beta \in \mathbb{R}: -1 \le \beta \le 1$ } determines the peakness of the pdf such that the β values of -1, 0, and 1 give uniform, Gaussian and Laplace distributions, respectively. The skewness parameter { $\xi \in \mathbb{R}: 0.1 \le \xi \le 10$ } determines the skewness of the pdf such that the ξ values of 0.1, 1, and 10 give positively skewed, symmetric, and negatively skewed distributions, respectively. Setting $\beta = 0$ and $\xi = 1$ leads to $\mu_{\xi} = 0$, $\sigma_{\xi} = 1$, $\omega_{\beta} = 1/\sqrt{2\pi}$, $c_{\beta} = 1/2$ and $a_{\xi,t} = a_t$, and the skew exponential power distribution SEP(0,1, $\xi = 1$, $\beta = 0$) becomes the standard normal distribution,

282
$$p(a_t | \xi = 1, \beta = 0) = \frac{1}{\sqrt{2\pi}} \exp\left[-\frac{1}{2}(a_t)^2\right].$$
 (7)

which is the data model of SLS in equation (2).

Replacing
$$a_t \sim N(0,1)$$
 with $a_t \sim SEP(0,1,\xi,\beta)$ in equations (2)–(5) leads to the data models

286
$$a_t = \frac{\varepsilon_t}{\sigma_0}$$
 $a_t \sim SEP(0, 1, \xi, \beta)$ (8)

287
$$a_t = \frac{\varepsilon_t}{\sigma_0 + \sigma_1 Y_t} \qquad a_t \sim SEP(0, 1, \xi, \beta) .$$
(9)

12

288
$$a_{t} = \frac{\varepsilon_{t} - \sum_{i=1}^{p} \phi_{i} \varepsilon_{t-1}}{\sigma_{0}} \qquad a_{t} \sim SEP(0, 1, \xi, \beta)$$
(10)

289
$$a_{t} = \frac{\varepsilon_{t} - \sum_{i=1}^{p} \phi_{i} \varepsilon_{t-1}}{\sigma_{0} + \sigma_{1} Y_{t}} \qquad a_{t} \sim SEP(0, 1, \xi, \beta)$$

$$(11)$$

In comparison with the Gaussian data models, the SEP-based data models have two more parameters (ξ and β) to be estimated jointly with physical model parameters. Data model WSEP-AC, which is known as the generalized likelihood function, is the most commonly used SEP-based data model (e.g. Vrugt and Ter Braak, 2011; Hublart et al., 2016; Scholz et al., 2018). A summary table of the eight data models with corresponding parameters is provided in the supplementary materials.

296 **2.2 Bayesian inference and likelihood functions**

297 Consider a Bayesian inference problem for a nonlinear model, f, used to simulate state 298 variables (e.g., CO₂ efflux), $d = Y(\theta) + \varepsilon$, where d is a vector of data, θ is a vector of model 299 parameters, and ε is a vector of residuals that may include errors in data, model parameters, and 300 model structures. The goal of Bayesian inference is to estimate the posterior distributions, $p(\theta|d)$, 301 of model parameters, θ , given data, d, using Bayes' theorem (Box and Tiao, 1992)

302
$$p(\theta | d) = \frac{p(d | \theta) p(\theta)}{\int p(d | \theta) p(\theta) d\theta}$$
 (12)

where $p(\theta)$ is the prior distribution, and $p(d|\theta)$ is the likelihood function to measure goodness-offit between model simulations, $Y(\theta)$, and data, *d*. The prior distribution can be obtained from data of previous studies (e.g. Elshall and Tsai, 2014) or expert judgment. When prior information is lacking, a common practice is to assume uniform distributions with relatively large parameter ranges so that the prior distributions do not affect the estimation of posterior distributions. The data models above can be used to construct the likelihood functions. For the Gaussian data models given in equations (2) - (5), the corresponding Gaussian likelihood functions are straightforward, and an example is equation (7). For the SEP data models, the corresponding likelihood that is called generalized likelihood function is (Schoups and Vrugt, 2010)

312
$$p(\boldsymbol{d} | \boldsymbol{\theta}) = p(\boldsymbol{\varepsilon}_{t} | \boldsymbol{\theta}) = \prod_{t=1}^{n} \sigma_{t}^{-1} \frac{2\sigma_{\xi}}{\xi + \xi^{-1}} \omega_{\beta} \exp\left(-c_{\beta} \left|a_{\xi,t}\right|^{2/(1+\beta)}\right).$$
(13)

where *n* is the dimension of *d*. The Gaussian likelihood functions are special case of the generalized likelihood functions. For example, by setting $\beta = 0$, $\xi = 1$, $\phi_i = 0$, $\sigma_t = \sigma_0$, $\sigma_{\xi} = 1$, $\mu_{\xi} = 0$, $\omega_{\beta} = 1/\sqrt{2\pi}$, $c_{\beta} = 1/2$, and $a_{\xi,t} = a_t$, equation (13) becomes the likelihood function corresponding to the SLS data model. Replacing $\sigma_t = \sigma_0$ by $\sigma_t = \sigma_0 + \sigma_1 E_t$, equation (13) becomes the likelihood function of the WLS data model.

In this study, the posterior distributions of the data model parameters are jointly estimated with the soil respiration model parameters using the MT-DREAM_(ZS) code (Laloy and Vrugt, 2012). MT-DREAM_(ZS) implements a Markov chain Monte Carlo (MCMC) algorithm by running multiple Markov chains in parallel with adaptive proposal distribution, multiple-try sampling, and sampling from an archive of past states. These state-of-the-art features assist in overcoming common challenges in the sampling space such as multimodality, ill-conditioning, and high dimensionality, and thus allow for accurate exploration of the targeted distributions.

325 2.3 Soil respiration models

Zhang et al. (2014) studied the Birch effect (the peak soil microbial respiration pulses in response to episodic rainfall pulses), and developed five models, evolving from an existing fourcarbon pool model to models with additional carbon pools and/or explicit representations of soil moisture controls on carbon degradation and microbial uptake rates. Three of the five models are

used in this study, and they are dented as 4C, 5C, and 6C. Note that model 4C is model 4C NOSM 330 of Zhang et al. (2014), not their model 4C. Figure 1 is the diagram of model 6C, the most complex 331 one among the five models. The simplest one, model 4C, has four carbon pools, i.e., soil organic 332 carbon (SOC), dissolved organic carbon (DOC), microbial biomass (MIC), and enzymes (ENZ), 333 and does not consider the soil moisture control on carbon degradation and microbial uptake rates. 334 335 Models 5C and 6C have an explicit representation of soil moisture controls on the rates. Based on the dual Arrhenius and Michaelis-Menten kinetics model, the original SOC degradation rate, 336 V_{decom} , is (Davidson et al., 2011; Davidson and Janssens, 2006) 337

$$338 V_{decom} = V_{max} C_{ENZ} \frac{C_{SOC}}{K_m + C_{SOC}} (14)$$

where V_{max} [s⁻¹] is the maximum SOC degradation rate per unit enzyme when the substrates is not limiting, C_{ENZ} [gCm⁻³] is enzyme pool size, C_{SOC} [gCm⁻³] is SOC pool size, and K_m is the halfsaturation for SOC. The original microbial uptake rate, V_{uptake} , is (Davidson et al., 2011; Davidson and Janssens, 2006)

343
$$V_{uptake} = V_{\max_up} C_{MIC} \frac{C_{DOC}}{K_{m_up} + C_{DOC}} \frac{C_{O2}}{K_{m_upO2} + C_{O2}},$$
(15)

where $V_{\max_{up}}$ [s⁻¹] is the maximum DOC uptake rate when the substrates is not limiting, C_{MIC} [gCm⁻³] is the MIC pool size, C_{DOC} [gCm⁻³] is the DOC pool size, C_{O2} [m³m⁻³] is the gas concentration of O₂ in the soil pore, and $K_{m_{up}}$ [gCm⁻³] and $K_{m_{upO2}}$ [m³m⁻³] are the corresponding half-saturation constants for DOC and O₂, respectively. With the explicit representation of soil moisture control, the two rates become (Zhang et al., 2014)

349
$$V_{decom} = V_{max} C_{ENZ} \frac{C_{SOC}}{K_m + C_{SOC}} \left(\frac{\theta}{\theta_s}\right)$$
(16)

350
$$V_{uptake} = V_{max_up} C_{MIC} \frac{C_{DOC}}{K_{m_up} + C_{DOC}} \frac{C_{O2}}{K_{m_upO2} + C_{O2}} \left(\frac{\theta}{\theta_s}\right)$$
 (17)

351 where θ [-] is the volumetric soil moisture, and θ_s [-] is the porosity.

In addition to using the new rate equations, models 5C and 6C have more carbon pools. In model 5C, DOC is split into two sub-pools for wet zone and dry zone of soil pores, and only the wet DOC is used by MIC, as shown in Figure 1. The moisture-controlled microbial uptake rate becomes

356
$$V_{uptake} = V_{\max_up} C_{MIC} \frac{C_{DOC_w}}{K_{m_up} + C_{DOC_w}} \frac{C_{O2}}{K_{m_upO2} + C_{O2}} \left(\frac{\theta}{\theta_s}\right).$$
(18)

where C_{DOC_w} [gCm⁻³] is the DOC pool size in the wet soil pores. Model 6C is more complex in that ENZ is further split into two sub-pools for wet and dry pores, and both the wet and dry ENZ are subject to degradation, as shown in Figure 1. The moisture-controlled SOC degradation rate becomes

361
$$V_{decom} = V_{\max} C_{ENZ_{W}} \frac{C_{SOC}}{K_m + C_{SOC}} \left(\frac{\theta}{\theta_s}\right)$$
(19)

362 for the wet ENZ and

363
$$V_{decom} = V_{\max} C_{ENZ_{-D}} \frac{C_{SOC}}{K_m + C_{SOC}} \left(1 - \frac{\theta}{\theta_s} \right) \varepsilon_D$$
(20)

for the dry ENZ, where C_{ENZ_W} [gCm⁻³] is the wet soil pores enzyme pool size, C_{ENZ_D} [gCm⁻³] is the enzyme pool size in the dry soil pores, and ε_D is the catalysis efficiency of the dry zone enzyme. Due to considering the moisture control and adding more soil pools, model 5C is expected to be significantly better than model 4C for simulating the Birch effect. Since the accumulated ENZ in dry soil is secondary, model 6C is expected to be slightly better than model 5C. In terms of model structural error, model 4C has the largest model structure error, model 5C has significantly
less model structure error, and model 6C has the smallest model structural error. In other words,
model 6C has the highest model fidelity (i.e. lowest model discrepancy) among the three models.
As shown below, the degree of model structural error is reflected in the process of Bayesian
inference and verified by the cross-validation.

374 2.4 Observations and parameter estimation

Figure 2 plots the time series of 17,016 observations of soil moisture and CO₂ efflux used in 375 this study. The observations were obtained during the entire year of 2007, covering a long period 376 377 of dry season prior to monsoon and episodic rainfall events during monsoon. The first two third of this dataset is used for the Bayesian inference, and the last one third is used for cross-validation. 378 The inference and cross-validation periods have both dry and wet periods, as shown in Figure 2. 379 380 The observation site is located within the Santa Rita Experimental Range (SRER, 31.8214°N, 110.8661°W, elevation 1,116 m) outside of Tucson, Arizona (Barron-Gafford et al., 2011; Scott 381 et al., 2009). This savanna site was covered by 22% of perennial grass, forbs and subshrubs and 382 35% of mesquite. The soils are uniformly Comoro loamy sand (77.6% sand, 11.0% clay, and 383 11.4% silt). The half-hourly atmospheric forcing data were collected from measurements through 384 an eddy covariance tower (Scott et al., 2009). This includes downward shortwave, longwave, 385 precipitation, wind, air temperature, humidity, and pressure. Volumetric CO₂ concentration was 386 measured at a half-hourly interval through compact probes. The CO₂ efflux was estimated from 387 the gradient of CO₂ concentration measured at two depths of 2 cm and 10 cm through Fick's first 388 law of diffusion, and the estimates were validated against measurements from a portable CO₂ gas 389 analyzer. 390

The parameters estimated in this study include the parameters of the soil respiration models 391 (4C - 6C) and the parameters of the data models described in Section 2.1. The estimated 392 parameters of models 4C and 5C include the microbial carbon use efficiency (CUE) [g/g], enzyme 393 production rate, k_e [g/m³s], microbial turnover rate, τ_m [1/s], and enzyme turnover rate τ_e [1/s]. 394 Uniform distributions are used as the prior in the Bayesian inference, and the ranges of the four 395 parameters are 0.2 - 1.00, $1 \times 10^{-12} - 1 \times 10^{-7}$, $1 \times 10^{-12} - 1 \times 10^{-5}$ and $1 \times 10^{-11} - 1 \times 10^{-6}$, respectively. 396 The values of other parameters are fixed at the values used in Allison et al. (2010). Model 6C has 397 two more parameters, and they are the catalysis efficiency ε_D [-] and the turnover rate of the dry-398 zone enzymes τ_{en} [1/s]. The prior of the two parameters are uniform distributions with the ranges 399 of 0.2 - 0.8 and $1 \times 10^{-12} - 1 \times 10^{-8}$, respectively. 400

The DREAM-based MCMC simulation is conducted for a total of 24 cases, the combinations of eight data models and three soil respiration models. For each case, the parameter distributions are obtained after drawing a total of 5×10^5 samples using five Markov chains. The Gelman and Rubin (1992) R-statistic is used for convergence diagnostic, and it approaches one in less than 40,000 samples. The initial 50% of the samples are discarded during the burn-in period.

406 **2.5** Metrics for evaluating predictive performance

Three criteria are used to evaluate the predictive performance of the soil respiration models and data models, and they are central mean tendency, dispersion, and reliability. Each criterion is measured by a single metric. In addition, a newly defined metric by (Elshall et al., 2018) is also used for simultaneously measuring the three criteria.

The central mean tendency is measured in this study using the Nash-Sutcliffe model efficiency
(NSME) coefficient (Nash and Sutcliffe, 1970),

413
$$NSME = 1 - \sum_{i=1}^{n} (d_i - \overline{\mathbf{Y}}_i)^2 / \sum_{i=1}^{n} (d_i - \overline{\mathbf{d}})^2,$$
 (21)
18

where *n* is the number of cross-validation data, d_i is the *i*-th data, $\overline{\mathbf{d}}$ is the mean of the data, and $\overline{\mathbf{Y}_i}$ is the mean of the prediction ensemble, \mathbf{Y}_i , for d_i . NSME ranges from $-\infty$ to 1, with *NSME* = 1 corresponding to a perfect match between data and mean prediction, i.e., the ensemble is centered on the data. *NSME* = 0 indicates that the model predictions are as only accurate as the mean of the data, while an efficiency *NSME* < 1 indicates that the mean of data is a better prediction than the mean prediction.

In addition to the central mean tendency, it is also desirable that the ensemble is precise with small dispersion and reliable to cover all the data. This study uses a nonparametric metric for dispersion, and it is the sharpness of a prediction interval (e.g. Smith et al., 2010a)

423
$$Sharpness = 1/n \sum_{i=1}^{n} \left[Max(\mathbf{Y}_i) - Min(\mathbf{Y}_i) \right]$$
(22)

where \mathbf{Y}_i is the prediction ensemble within the 95% prediction interval, the Bayesian credible interval, not the confidence interval used in nonlinear regression (Lu et al., 2013). Smaller values of sharpness indicate better prediction precision. Reliability is measured using predictive coverage. (e.g. Hoeting et al., 1999), which is the percentages of data contained in the prediction interval. Larger predictive coverage values are preferred.

To account for the trade-off between the three metrics, Elshall et al. (2018) defined relative model score (RMS) that simultaneously measure all the three criteria. Scoring rules are commonly used in hydrology to assess predictive performance (e.g., Weijs et al., 2010; Westerberg et al., 2011). RMS is used in this study to measure the relative predictive performance of the combinations of soil respiration models and data models. For combination M_j , RMS is defined as

434
$$RMS(M_j) = \sum_{i=1}^{n} \frac{p(d_i | \mathbf{Y}_{ij}, M_j)}{\sum_{j=1}^{m} p(d_i | \mathbf{Y}_{ij}, M_j)} \times 100$$
 (23)

where *m* is the number of combinations; the ensemble prediction Y_{ij} is similar to Y_i above with 435 index i over time and index j specific to the j-th combination. The density function $p(d_i|Y_{ij})$ can be 436 evaluated by first obtaining the density function $p(Y_{ii})$ of the ensemble prediction Y_{ii} (e.g., by using 437 the kernel density function) and then evaluating $p(d_i|Y_{ii})$ using interpolation methods based on the 438 intersection of Y_{ii} and d_i . More details about evaluating *RMS* can be found in Elshall et al. (2018). 439 This evaluation is based purely on the model predictions, and does not involve any assumptions 440 on the models, their parameters, and likelihood functions. Larger RMS values indicate better 441 overall predictive performance. A figure of our workflow scheme is presented in the 442 supplementary materials. 443

444 **3** Results of Bayesian Inverse Modeling

This section analyzes the residuals of the best realization (with the highest likelihood value) of the MCMC simulation to understand whether the assumptions of the eight data models hold. The impacts of the data models on the posterior parameter distributions are also analyzed.

448 3.1 Residual characterization

Figure 3 shows residual plots for model 6C based on data models SLS and WSEP-AC. SLS is the simplest data model with the assumptions of homoscedastic, independent, and Gaussian residuals, and the WSEP-AC is the most complex one without the assumptions. Model 6C is the most complex model and also the best one as ranked by Zhang et al. (2014) using Bayesian model selection. The variable a_t plotted in Figures 3a-3c and Figures 3d-3f is defined in equations (2) and (11), respectively. Figures 3a – 3c show that all the three residual assumptions are violated when SLS is used, because (i) the residual variance is not constant, but increases as a function of the

simulated CO_2 efflux (Figure 3a); (ii) the autocorrelation function at most lags is beyond the 95% 456 confidence interval (Figure 3b); (iii) the standard normal density function cannot adequately 457 characterize the residuals (Figure 3c). Figures 3d-f show that, after relaxing the three assumptions, 458 the processed residuals, a_t , can be well characterized by WSEP-AC. Figure 3d shows that, after 459 normalizing ε_t with the linear variance ($\sigma_t = 0.034 + 0.099E_t$), the variation of the variance of 460 a_t becomes significantly smaller, although the variance is still not constant. Figure 3e shows that, 461 after removing a first-order autoregressive model from ε_t , a_t becomes less correlated, although the 462 correlation is not fully removed. The two coefficients of the autoregressive model are $\phi_1 = 0.989$ 463 and $\phi_2 = 4.5 \times 10^{-6}$; the small value of ϕ_2 indicates that there is no need to attempt an autoregressive 464 465 model of higher order. Figure 3f shows that a_t follows the SEP distribution with the estimated skewness coefficient of $\xi = 0.933$ and kurtosis coefficient of $\beta = 0.998$. As a summary, Figure 466 467 3 shows that it is important to examine the residuals and to determine whether the selected data model is adequate for charactering the residuals. Although WSEP-AC still cannot perfectly 468 characterize ε_t , it is significantly better than SLS. 469

470 Although the Gaussian assumption used in SLS is violated for model 6C (Figure 3c), this is not generally the case for other data models and soil respiration models. This is shown in Figure 471 4, which presents the quantile-quantile (Q-Q) plot for the eight data models and the three soil 472 respiration models. For SLS, WLS, SLS-AC, and WLS-AC, the theoretical quantiles are based on 473 the standard normal distribution, N(0,1); for SEP, WSEP, SEP-AC, and WSEP-AC, the theoretical 474 quantiles are based on the standard skew exponential power distribution, SEP(0,1,1,0). If the 475 residuals follow the assumed standard distributions, the Q-Q plots fall on the 1:1 lines, marked as 476 the theoretical lines in Figure 4. If the residuals are Gaussian or SEP but not standard, the Q-Q 477 478 plots fall on a straight line but not the 1:1 line. Figures 4a and 4e show that, for all the soil 479 respiration models, the O-O plots of SLS and SEP deviate significantly from the theoretical lines and exhibit fat-tail behaviors, which is an indication of outliers (Thyer et al., 2009). The deviation 480 is reduced after accounting for autocorrelation in SLS-AC and SEP-AC, as shown in Figures 4c 481 and 4g. It is interesting to observe from the two figures that the Q-Q plots of the three models are 482 almost visually identical. The deviation is almost fully removed after accounting for 483 heteroscedasticity in WLS and WSEP in that their corresponding Q-Q plots fall on the 1:1 lines, 484 especially for models 5C and 6C, as shown in Figures 4b and 4f. However, the Q-Q plots start 485 deviating from the 1:1 lines as shown in Figures 4d and 4h, after accounting for both 486 heteroscedasticity and autocorrelation in WLS-AC and WSEP-AC. As a summary, Figure 4 shows 487 that, for the numerical example of this study, either the Gaussian or the SEP distribution is valid if 488 heteroscedasticity is accounted for in the data models. However, accounting for autocorrelation in 489 490 the data models does not help improve the characterization of the residual distributions.

491

3.2 Posterior parameter distributions

While Figures 3 and 4 help understand validity of the three assumptions used in the data 492 models, the impacts of the data models on estimating model parameter distributions must be 493 evaluated separately. This section discusses the impact of the data model selection on parameter 494 estimation with the objective of understanding whether incorrect specification of the data model 495 necessarily leads to biased parameter estimates. Such assessment is not a trivial task for two main 496 reasons. First, microbial soil respiration models aggregate complex natural processes and spatial 497 details into simpler conceptual representations. As a results several model parameters are effective 498 values of several complex natural processes that cannot be actually measured in the field as 499 discussed by Vrugt et al. (2013). In addition, even for model parameter that can be measured in 500 501 the field, since the model structure is imperfect, calibrated parameter values are sometimes beyond

their physically reasonable range, as discussed by Pappenberger and Beven (2006). This is often
undesirable, if we seek to make the models more mechanistically descriptive.

We focus our discussion on carbon use efficiency (CUE) for microbial growth due to two 504 reasons: (1) CUE is a fundamental parameter in microbial soil respiration models, and (2) a 505 physically reasonable range for CUE can estimated. The concept of microbial CUE(Allison et al., 506 2010; Bradford et al., 2008; Manzoni et al., 2012; Wieder et al., 2013) has been used to present 507 fundamental microbial processes in recent microbial enzyme models (Allison et al., 2010; German 508 et al., 2011; Schimel and Weintraub, 2003; Wang et al., 2013). The microbial CUE, which is 509 marked between MIC and CO2 in Figure 1, controls microbial growth, enzyme production and 510 microbial respiration. A physically reasonable range of CUE can be estimated from the physical 511 viewpoint (Tang and Riley, 2014). Sinsabaugh et al. (2013) showed that the thermodynamic 512 513 calculations support a maximum CUE of 0.60 and that previous studies that estimate CUE in terrestrial systems report a mean value of 0.55. Theoretically, there is no lower limit for CUE as it 514 can approach zero, and CUE < 0.1 has been reported for terrestrial ecosystems (e.g., Fernández-515 516 Martínez et al., 2014) and used in modeling studies (Li et al., 2014). Note that, for inverse modeling with MCMC sampling, we did not assume CUE maximum value of 0.6. In other words, for 517 parameter estimation and predictive performance we did not impose the constraint that CUE is less 518 than 0.6. We merely use this CUE maximum value of 0.6 to evaluate whether the posterior CUE 519 parameter samples obtained using different data models and different soil respiration models are 520 within the physically reasonable range of $0 \sim 0.6$. 521

Figure 5 plots the CUE posterior marginal density of the three soil respiration models obtained using the eight data models. The physical range between zero and 0.6 is marked in yellow. Figure 5 shows that the CUE posterior parameter distribution of Model 6C obtained using the data models 525 that does not account for autocorrelation are within the physically reasonable range. For models 4C and 5C, the posterior parameter samples are outside the range for six data models. For model 526 4C, the posterior parameters are within the physical range only for data models SEP and WSEP; 527 for model 5C, the two data models are WLS and WSEP. It is not surprising to find the posterior 528 parameter distribution of models 4C and 5C, which have a certain degree of model structure error, 529 to be out of the physically plausible range. This can be attributed to two reasons. First, the model 530 solution can be biased toward the missing processes in the model structure such as the additional 531 carbon pool in both 4C and 5C or missing the explicit accounting for soil moisture in 4C. Second, 532 533 biased parameter estimation can compensate for model structure inadequacy and other sources of discrepancy in both the physical models and the data models. 534

In addition, it is important to understand how accounting for autocorrelation, heteroscedasticity 535 and non-Gaussian residuals can affect the parameter estimation. First, it is observed in Figure 5e-536 h that biased parameter estimates are outside the physically reasonable range when autocorrelation 537 is explicitly accounted for. This may suggest again that accounting for heteroscedasticity is 538 539 desirable but accounting for autocorrelation is not. A possible reason is that filtering autocorrelation may reduce the residual space such that the transformed residual space cannot 540 correspond to the parameter space of the models. In other words, parameter information may be 541 lost due to filtering out autocorrelation. However, it is not fully understood why this does not occur 542 for the model 6C under data model SLS-AC (Figure 5e), and more research is warranted. Second, 543 unlike accounting for auto-correlation, accounting only for heteroscedasticity (i.e., WLS and 544 WSEP) only amplifies or reduces the variance without affecting the structure of the residual space. 545 Figures 5c-d show that account for heteroscedasticity (i.e. WLS and WSEP) tends to improve the 546 547 parameter estimation in comparison with homoscedastic data models (i.e., SLS and SEP) shown

in Figure 5a-b. Finally, with respect to non-Gaussian residuals, Schoups and Vrugt (2010) suggested that, compared to Gaussian pdf, the peaked pdf of the SEP with a longer tail is useful for making parameter inference robust against outliers. To a certain degree, this can be substantiated by the results in Figure 5a-d, in that SEP and WSEP provide more favorable parameter estimates than SLS and WLS.

Finally, Figure 5a shows that the posterior parameter distributions of SLS are very narrow for the three soil respiration models. The narrow distributions can be attributed to several reasons. Since SEP distribution can have longer tails than Gaussian distribution, this can further increase the samples acceptance ratio from tails resulting in wider distribution (Figure 5b). In addition, accounting for heteroscedasticity will result in wider posterior parameter distribution (Figure 5c) due to accepting higher variances at peak effluxes. Moreover, filtering correlation (Figure 5e-h) increases the entropy, and leads to wider distributions.

560

4.

Results of Predictive Performance

Based on the last one third of the CO₂ efflux observations, a cross-validation test was 561 conducted for the combinations of three soil respiration models and eight data models. For the 562 cross-validation period, the predictive performance is examined using the four statistical metrics 563 that are defined in Section 2.5. The metrics are also calculated for the calibration period. This is 564 not to perform Bayesian model selection given the calibration data, but to better understand the 565 impact of data models on predictive performance of the three soil respiration models. For each 566 calibration and each cross-validation data, a prediction ensemble is generated from the two 567 perspectives of parametric uncertainty only and total uncertainty, as presented in Section 4.1 and 568 4.2, respectively. 569

570

571 4.1 Predictive performance with parametric uncertainty of soil respiration model

In this section the ensemble is generated by running the soil respiration models with the 572 posterior samples (obtained from the Bayesian inference) of the physical model parameters. In 573 other words, the ensemble addresses parametric uncertainty of the soil respiration models only. 574 Considering the relative contribution of parametric uncertainty only will provide insights for 575 modeling approaches that attempt to segregate various sources of uncertainty (e.g., Thyer et al., 576 2009 ; Tsai and Elshall, 2013). The four statistics above (i.e. NSME, sharpness, coverage, and 577 RMS) are calculated for the three soil respiration models and the eight data models. Taking data 578 models SLS and WSEP-AC as an example, Figure 6 plots the data (for the calibration and cross-579 validation periods separately) along with the mean and 95% credible intervals of the prediction 580 ensemble for the three models. 581

Figure 6 shows that the data models affect model simulations for all the models. The statistics, especially RMS, indicate that WSEP-AC has better predictive performance than SLS. This is most visually obvious for model 6C during the cross-validation period after 330 days, as the prediction ensemble of SLS (Figure 6k) cannot cover the observations, whereas the prediction ensemble of WSEP-AC can (Figure 6l). This conclusion that WSEP-AC outperforms SLS agrees with that drawn from Figures 3 and 4.

Figure 7 plots the four statistics for all the soil respiration models and data models. Figures 7a and 7b show the predictive performance with respect to the central mean tendency measured by NSME for both the calibration and cross-validation periods respectively. The results indicate that, under all data models, the low fidelity model 4C over-fits the data and results in biased predictions, in that the NSME values become significantly worse (e.g., from 0.6 to -0.6) from the calibration to the cross-validation period. This is confirmed by the visual inspection of Figures 6a and 6g for data model SLS and of Figures 6b and 6h for data model WSEP-AC. For models 5C and 6C, their
NSME values vary with the data models; and the central mean accuracy is the worst for SLS-AC
that considers only autocorrelation (Figure 6b).

With respect to parametric uncertainty estimation, Figures 7c and 7d show that sharpness generally increases when the three assumptions in the data models are gradually relaxed from SLS to WSEP-AC. This is even more obvious during the validation period. Given that the prediction ensemble does not center on the data, the increasing sharpness is desirable as it improves reliability. This is confirmed by the reliability plots in Figures 7e and 7f. The exceptions are again for SLS-AC and SEP-AC that generally have the lowest coverage.

With respect to the overall predictive performance measured by RMS, the same variation pattern and exception are also observed in the RMS plots in Figures 7g and 7h. This is not surprising because RMS is the metric that can be used to measure all the three criteria (central mean tendency, sharpness, and reliability). Since the prediction ensemble is not centered on the data, the sharpness and reliability are the decisive factors for evaluating the predictive performance.

As a summary, while it is necessary to account for heteroscedasticity in a data model, caution 609 is needed when accounting for autocorrelation in the manner described in Section 2.1. In addition, 610 after comparing the RMS values of the residuals using the Gaussian and SEP distributions, the 611 conclusion is that the SEP distribution outperforms the Gaussian distribution with respect to 612 predictive performance. Finally, uncertainty underestimation is evidenced by the very small 613 predictive coverage. The underestimation of uncertainty for all the physical models with all the 614 data model is not unexpected because only parametric uncertainty is considered in this study. 615 616 Considering the overall predictive uncertainty is the subject of the next section.

617 **4.2** Predictive performance with total uncertainty

The simulated output $\mathbf{Y}(\boldsymbol{\theta}_n)$ is generally not equal to the observed output **d**, and we have a 618 residual term ε due to measurement, input and model structure errors such that $\mathbf{d} = \mathbf{Y}(\boldsymbol{\theta}_p) + \varepsilon$. 619 Accounting for the error term ε can be through separating various error terms. For example, in 620 section 4.1 we obtained uncertainty due to the physical model parameters. Accounting for other 621 sources of uncertainty can be done using a single model approach (e.g. Thyer et al., 2009) or a 622 multi-model approach (e.g. Tsai and Elshall, 2013). Alternatively, we can quantify the uncertainty 623 624 based on total residuals that separates out parametric uncertainty, so the residual error includes errors in measurements, model inputs, and model structures (e.g. Thyer et al., 2009; Schoups and 625 Vrugt, 2010). This lumped approach is based on sampling the residuals model $\varepsilon(\theta_{s})$ with 626 parameters θ_{s} . SLS has one fixed parameter that is the constant variance, and other data models 627 have two to six parameters. Thus in this section the prediction ensemble addresses parametric 628 629 uncertainty of not only the soil respiration models but also the data models. When generating the prediction ensemble in the procedure described by Schoups and Vrugt (2010), an ensemble of 630 residuals is first generated by running the data models with posterior samples of the data model 631 632 parameters for the positive carbon efflux domain; the residual ensemble is then added to the prediction ensemble generated in Section 4.1. 633

We start by a visual assessment of the predictive performance. Figure 8 is similar to Figure 6 with the exception that Figure 8 considers the overall predictive uncertainty (i.e. parametric and output uncertainty), while Figure 6 considers the parametric uncertainty only. Figure 8 reveals a practical observation about accounting for the overall uncertainty through the lumped approach of sampling the data models. For example, Figure 8b shows that, despite the wide prediction interval of model 4C, the model with significant model structure error cannot capture the birch pulse around day 180. It indicates that proper using a data model for model residuals cannot compensatesignificant model structure error.

Figure 9 plots the four statistics (NSME, sharpness, predictive coverage, and RMS) of the three soil respiration models under the eight data models to assess the predictive performance. With respect to central mean tendency, the NSME values in Figures 9a-9b are visually the same as those in Figures 7a-7b, indicating that the central mean accuracy under parametric uncertainty is the same as that under predictive uncertainty.

With respect to uncertainty, the values of sharpness and predictive coverage increase 647 substantially (Figures 9c - 9f). In particular, Figures 9e and 9f show that, except for SLS and SEP, 648 the predictive coverage of the rest of the six data models are close to 100% for all the three soil 649 respiration models, indicating that the prediction intervals cover almost all the data. This is 650 651 demonstrated in Figures 6 for WSEP-AC. Similar to Figures 7c and 7d, Figures 9c and 9d also show a general pattern that the sharpness increases when the three assumptions in the data models 652 are gradually relaxed from SLS to WSEP-AC. The data models that account for autocorrelation 653 are still the exceptions. 654

With respect to the overall predictive performance, the RMS values are largely determined by 655 the mean accuracy and sharpness as the predictive coverage is similar for different data models. 656 Figures 9g and 9h of RMS show that the predictive performance of the four data models that 657 account for autocorrelation is worse than that of the other four data models. This suggests again 658 that one needs to be cautious when building autocorrelation into a data model. This is consistent 659 with the finding of Evin et al. (2013, 2014) that accounting for autocorrelation before accounting 660 for heteroscedasticity or jointly accounting for autocorrelation and heteroscedasticity can result in 661 662 poor predictive performance. In summary, Figures 9g and 9h show for both the calibration and

prediction periods that accounting for heteroscedasticity in WLS and WSEP gives the best overall predictive performance, and accounting for autocorrelation without heteroscedasticity in SLS-AC and SEP-AC gives the worst overall predictive performance. Finally, for the three soil respiration models, RMS shows that model 4C has the worst predictive performance for both the calibration and cross-validation data. Generally speaking, the high fidelity model 6C outperforms model 5C for both the calibration and cross-validation data, which justifies the complexity of model 6C.

To demonstrate the impacts of the data models on predictive performance of the soil respiration 669 models, Figure 10 plots the model simulations and predictions given by model 6C during the 670 calibration and cross-validation periods using all the eight data models. Figure 10 is used to 671 investigate predictive performance characteristics of the different data models. By examining the 672 predictive performance of model 6C, specific predictive performance patterns can be identified. 673 674 Figures 10a – 10d show that SLS and SEP have similar predictive performance with SEP generally having better predictive performance especially during the validation period. Not accounting for 675 heteroscedasticity will underestimate the predication uncertainty (Figure 10b and Figure 10d). This 676 is mainly because the variance of the efflux residuals increases with the magnitude of the carbon 677 effluxes (Figure 3a), and thus assuming constant variance is not representative. Accordingly, 678 accounting for heteroscedasticity using WLS (Figure 10e) or WSEP (Figure 10h) will make the 679 predictions more sensitive to peak carbon effluxes. This will generally improve the predictive 680 coverage on the expense of sharpness and the central mean tendency. While WLS and WSEP have 681 similar predictive performance, WSEP has better central mean tendency and overall predictive 682 performance than WLS. Figures 10i – 10l show that accounting for autocorrelation using SLS-AC 683 and SEP-AC results in wider uncertainty bands and insensitivity to peak carbon effluxes as 684 685 compared to SLS and SEP (Figures 10a-d), which may be due to reduction of information content

of the residuals. This results in deteriorating the sharpness, the central mean tendency and the 686 capturing of peak carbon fluxes, especially during the validation period. Figures 10m - 10p show 687 that accounting for both heteroscedasticity and autocorrelation using WLS-AC and WSEP-AC 688 makes the inference robust against peak carbon effluxes. However, due to the loss of information 689 content, the uncertainty bands are still wider, and uncertainty becomes overestimated especially 690 during validation period as compared to WLS and WSEP (Figures 10e - 10h). The results of 691 Models 4C and 5C, which are not shown here, also show the same prediction patterns with respect 692 to non-Gaussian residuals, heteroscedasticity, and autocorrelation. 693

694 Finally, we observe in Figure 10 that the data models that have good overall predictive performance as measured by RMS during the calibration period will maintain this good predictive 695 performance during the validation period. For model 6C, RMS values for the calibration and 696 697 validation periods are very well correlated with a correlation coefficient of 0.92. However, we note that for models 4C and 5C the overall predictive performances during the calibration and validation 698 periods are not that well correlated as 6C, with correlation coefficients of 0.52 for model 4C and 699 700 0.61 for model 5C. This suggests that model 6C is more robust than 4C and 5C for forecasting and hindcasting. 701

702 4.3 Discussion on handling residual correlation

Accounting for autocorrelation can lead to biased parameter estimation (Figure 5) and poor predictive performance (Figure 10). Auto-correlated residuals may be attributed to model discrepancy, as shown in Lu et al. (2013). The most obvious solution to handle the autocorrelation is to reduce the autocorrelation by improving the soil respiration model. If model improvement is difficult for practical reasons, we can improve the data model to better characterize the autocorrelation. Addressing autocorrelation in a data model is challenging since it involves severalinterlinked factors as follows:

(1) Non-stationarity due to wet-dry periods could be a reason for this problem. By drawing on
similarity from surface hydrology, the study of Ammann et al. (2018) suggests that autocorrelated residuals might be attributed to non-stationarity due to wet-dry periods with halfhourly data. Accounting for non-stationarity could better address the problem of autocorrelated residuals (Ammann et al., 2018; Smith et al., 2010b).

(2) The way of implementing autocorrelation could have an impact. Autocorrelation could be 715 applied to raw residuals directly (e.g., Li et al., 2015), to transformed residuals based on 716 covariance matrix of residuals L(e) (e.g., Lu et al., 2013), or to normalized residuals L(a) (e.g., 717 Schoups and Vrugt, 2010; Evin et al., 2013). Note that e is a vector of transformed residuals, 718 719 while **a** denotes a vector of independent and identically distributed random errors with zero mean and unit standard deviation. The L(e) approach based on covariance matrix of residuals 720 is generally limited to Gaussian data models (e.g. Lu et al., 2013), while the $L(\mathbf{a})$ approach for 721 722 normalized residuals can be readily adopted for non-Gaussian data models.

(3) The autocorrelation model could have an impact. Using an autoregressive model is a popular 723 technique to account for auto-correlated residuals. However, using an autoregressive model 724 with either joint inversion approach (e.g., this study and Schoups and Vrugt, 2010) or 725 sequential approaches (e.g., Evin et al., 2013, 2014; Lu et al., 2013) removes correlation errors 726 through a filter approach, which can lead to a loss of information content. As this may cause 727 overcorrection of prediction especially at surge events, Li et al. (2015) developed a restricted 728 autoregressive model to overcome this adverse effect. Other autocorrelation models include 729 730 moving average model and mixed autoregressive-moving averaging model (Chatfield, 2004).

731 (4) Joint versus sequential inversion for autocorrelation could have an impact. Sequential inversion approaches include two-step procedures (e.g. Evin et al., 2013, 2014; Lu et al., 2013) or the 732 multi-step procedure (Li et al., 2016a). These sequential approach estimates the autoregressive 733 parameters sequentially in a later step after estimating the physical model parameters and other 734 data model parameters. Evin et al. (2013, 2014) used a sequential approach to avoid the 735 interaction between the parameters of the heteroscedasticity model and the autocorrelation 736 model. In addition, the autoregressive model parameters can be deterministically calculated as 737 an internal variables of the data model similar to Lu et al. (2013), and not as calibration 738 parameters (e.g. Schoups and Vrugt; Evin et al. 2013; 2014). While the first step in the 739 sequential approach would avoid the biased parameter estimation (Figure 10a-d), the second 740 step can still lead a poor predicative performance since we are essentially using a filter 741 approach to remove residual correlation. To address this problem, Li et al. (2016) multi-step 742 procedure that is based on Gaussian data model uses restricted autoregressive model. 743 Generally, Ammann et al. (2018) states that the joint inversion is still preferred, and 744 understanding the conditions where accounting for auto-correlation can be achieved remains 745 poorly understood. 746

747 **5.** Conclusions

In parameter estimation and prediction of soil carbon fluxes to the atmosphere, one often assumes that residuals, which include errors in observations, model inputs, parameter estimates, and model structures, are normally distributed, homoscedastic and uncorrelated. We study these assumptions by calibrating three soil respiration models, which have varying degrees of model structure errors. We further explore eight data models that characterize the residuals statistically by starting with the standard least squares (SLS) and skew exponential power (SEP) data models 754 that assume homoscedastic and non-correlated residuals. For these two distributions, we evaluate six other data models that account for heteroscedasticity (WLS and WSEP), autocorrelation (SLS-755 AC and SEP-AC), and joint inversion of heteroscedasticity and autocorrelation (WLS-AC and 756 757 WSEP-AC). To our knowledge this is the first study that provides such detailed analysis for soil reparation inverse modeling. We also use three soil respiration models with different degrees of 758 model fidelity (i.e., model discrepancy) and model complexity (i.e. number of model parameters) 759 to understand the impact of model discrepancy on the calibration results under different data 760 models. We analyze the results with respect to (1) residual characterization, (2) parameter 761 estimation, (3) predictive performance, and (4) impacts of model discrepancy. The main findings 762 of this study are summarized as follows: 763

(1) With respect to residual characterization, residual analysis results suggest that the common 764 765 assumption of not accounting for heteroscedasticity and residual autocorrelation in the data models SLS and SEP results in poor characterization of residuals. Explicit accounting for 766 heteroscedasticity in WLS and WSEP results in significantly improved characterization of the 767 residuals, and the improvement is larger than that obtained by accounting for both 768 heteroscedasticity and autocorrelation in WSL-AC and WSEP-AC. Accounting for 769 autocorrelation only in SLS-AC and SEP-AC does not significantly improve the 770 characterization of the residuals. 771

(2) With respect to parameter estimation, the impacts of the data models are evaluated by focusing
on carbon use efficiency (CUE), which is a central parameter in soil respiration modeling.
Using SLS yields relatively reasonable posterior parameter distributions for CUE, yet very
narrow posterior. The data models SLS-AC, SEP-AC, WLS-AC and WSEP-AC that consider
autocorrelation tend to yield CUE estimates that are physically unreasonable. We speculate

that filtering residual correlation can affect the mapping of the model physics (as implicitly
included in the residuals) into the parameter space, which might result in biased parameter
estimates that are physically unreasonable.

(3) With respect to predictive performance, it is measured by four statistical criteria: central mean 780 tendency, sharpness, coverage, and relative model score for both the calibration and the cross-781 validation periods. Results show that accounting for autocorrelation in SLS-AC, SEP-AC, 782 WLS-AC, and WSEP-AC deteriorates the predicative performance, such that the predictive 783 performance is inferior to that of SLS in terms of the central mean tendency and overall 784 predictive performance (measured by the relative model score), especially during the cross-785 validation period. Results also indicates that using the SEP distribution can potentially improve 786 the predictive performance. The same is true for accounting for heteroscedasticity. Using SEP 787 788 distribution and accounting for heteroscedasticity (i.e. WSEP) can potentially improve the predictive performance. 789

(4) With respect to the impact of model discrepancy, the high fidelity model (6C) gives the best
results with respect to parameter estimation and predictive performance. Model 6C generally
maintains its superior performance under different data models. This justifies the complexity
of model 6C relative to model 5C that has one less carbon pool. Model 4C with the lowest
fidelity maintains its poor performance for different data models, because the model has only
four carbon pools and lacks the explicit representation of soil moisture control.

Based on the empirical findings above, we conclude the following:

797 (1) Not accounting for heteroscedasticity and autocorrelation using a Gaussian or non-Gaussian
 798 data model might not necessarily result in biased parameter estimates or biased predictions

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with respect to central mean tendency, but will definitely underestimate uncertainty resultingin lower overall predictive performance.

801 (2) Using a non-Gaussian data model can improve parameter estimation and predictive
 802 performance with respect to central mean tendency and uncertainty quantification.

803 (3) Accounting for heteroscedasticity improves the uncertainty estimation with respect to
 804 reliability at the cost of having a wider predictive interval.

(4) This study confirms other empirical findings and theoretical analyses (Evin et al., 2013; 2014;
Li et al., 2015, Ammann et al. 2018) that separately accounting for autocorrelation or jointly
accounting for autocorrelation and heteroscedasticity can be problematic. While the reasons
remain poorly understood (Ammann et al., 2018), it might be attributed to non-stationarity due
to wet-dry periods with half-hourly data (Ammann et al., 2013; 2014; Lu et al., 2013; Li et
autocorrelation (e.g., Schoups and Vrugt, 2010, Evin et al., 2013; 2014; Lu et al., 2013; Li et
al., 2015, 2016a; Ammann et al. 2018). Further investigation to address autocorrelation in soil

respiration modeling is warranted in a future study.

The above conclusions are subject to several limitations. First, the conclusions are specific to 813 the soil respiration models developed and validated for semi-arid savannah. Performance 814 variations across different soil respiration models with different levels of complexities is possible. 815 Second, the conclusions are conditioned on the data that were obtained at the half-hour interval 816 over a one-year period. Different conclusions are possible if the data are thinned to daily or weekly 817 scales or data of longer observation periods are used. Third, our study investigates effects of the 818 residual assumptions of formal likelihood functions through direct conditioning of the residuals 819 model parameters, yet this can also be done through other approaches such as residuals 820 821 transformation (Thiemann et al., 2001), autorgressive bias model (Del Giudice et al., 2013),

approximate Bayesian computation (Sadegh and Vrugt, 2013), and data assimilation (Spaaks and
Bouten, 2013). Comparing different methods for accounting the residual assumptions are beyond
the scope of this work. Fourth, this study focuses on formal Bayesian computation using formal
likelihood functions, and comparison with other inference functions such as informal likelihood
functions or approximate Bayesian computation is warranted in a future study.

Based on the aforesaid conclusions and limitations, we recommend to start calibrating soil 827 respiration models with simple SLS or SEP likelihood function. If the residuals characterization is 828 adequate (e.g., Scharnagl et al., 2011), then the underlying assumptions are met. Otherwise, 829 increase complexity of the data model until satisfactory results are obtained in terms of residuals 830 characterization, posterior parameter estimation, and predictive performance. This is similar to the 831 procedure given in Smith et al. (2015). Although the empirical findings of this study provide 832 833 general guidelines for data model selection for soil respiration modeling, more comparative studies are needed to validate and refute the findings of this study. 834

835 Acronyms

836	4C	Four carbon pool model
837	5C	Five carbon pool model
838	6C	Six carbon pool model
839	CUE	Microbial carbon use efficiency
840	DOC	Dissolved organic carbon
841	ENZ	Enzymes
842	MCMC	Markov chain Monte Carlo
843	MIC	Microbial biomass
844	NSME	Nash-Sutcliffe model efficiency
845	PDF	Probability density function
846	RMS	Relative model score
847	SEP	Skew exponential power distribution
848	SEP-AC	Skew exponential power distribution with autocorrelation
849	SLS	Standard least square
850	SLS-AC	Standard least square with autocorrelation
851	SOC	Soil organic carbon
852	WLS	Weighted least squared
853	WLS-AC	Weight least square with autocorrelation

- 854 WSEP Weighted skew exponential power distribution
- 855 WSEP-AC Weighted skew exponential power distribution with autocorrelation
- 856

857 **Code and data availability**

The data and codes and models used to produce this paper are available on contact of the corresponding author at mye@fsu.edu. We cannot publicly share the workflow because MT-DREAM_(ZS) code (Laloy and Vrugt, 2012), which is a main component in the workflow, is in the process of becoming a commercial code.

862 Author contributions

- ASE developed and implemented the code for the eight data models for soil respiration modeling,
- and prepared the manuscript with contribution of all co-authors. MY developed the research idea
- and outline, and supervised the research implementation when ASE was a post-doc at Florida State
- 866 University. GN developed the soil respiration models. GAB collected and processed the eddy-
- 867 covariance data used for model calibration.

868 **Competing interests**

869 The authors declare that they have no conflict of interest.

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- Figure 1. Diagram of model 6C representing the processes of (1) degradation of soil organic carbon 1232 (SOC) to dissolved organic carbon (DOC) through catalysis of enzymes (ENZ) produced by 1233 microbes (MIC), (2) MIC uptake of DOC, and (3) microbial (MIC) respiration to produce CO₂ 1234 1235 (CUE is the carbon use efficiency). SOC degradation and microbial uptake rates are controlled by water saturation (θ / θ_{a}) . The DOC and ENZ pools are split into two subpools, one for the wet zone 1236 and the other for the dry zone of the soil pore space. Microbial uptake of DOC occurs only in the 1237 wet zone, and the uptake rate is linearly related to θ/θ_s . Catalysis through ENZ in the wet zone is 1238 proportional to θ/θ_s , while that in the dry zone is proportional to $1 - \theta/\theta_s$. V_{max} (s⁻¹) is the maximum 1239 rate, and K_m is the half-saturation concentration. 1240
- 1241

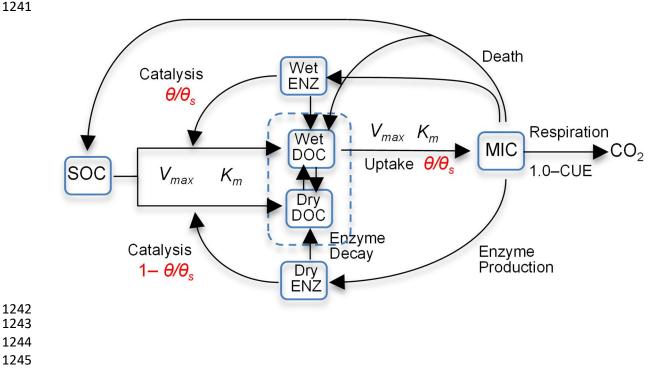


Figure 2. Time series of soil moisture and efflux observations. The dashed line marks the divideof the dataset into calibration and validation periods.

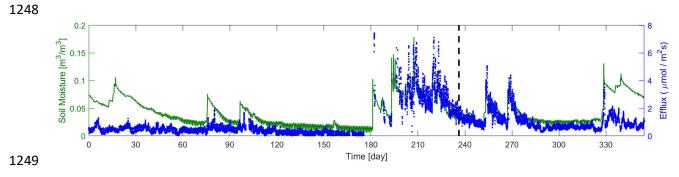
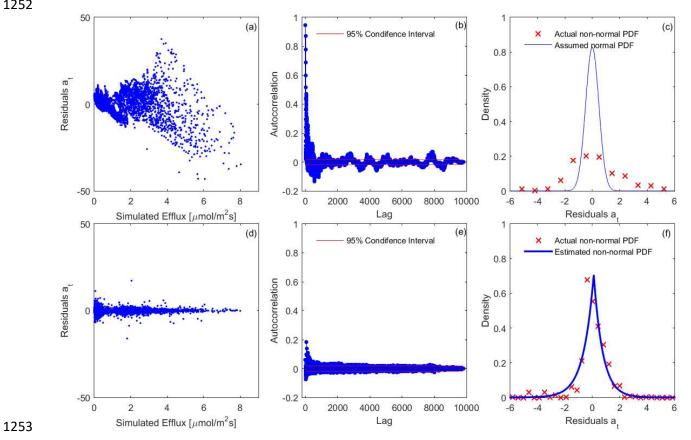
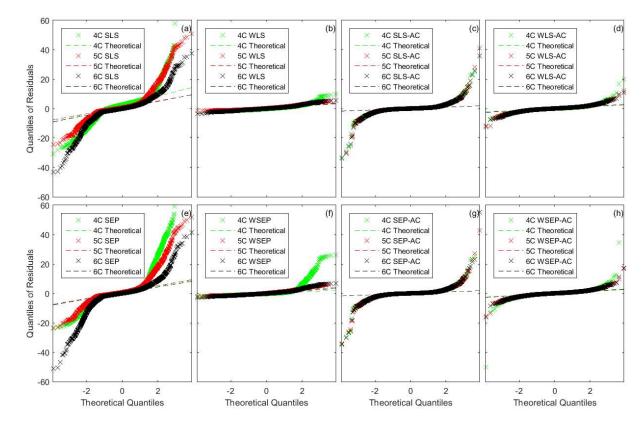


Figure 3. Residual analysis of the best realization (among multiple MCMC realizations) for model
6C using data models (a-c) SLS and (d-f) WSEP-AC.



- Figure 4. Residual quantile-quantile (Q-Q) plots of the best realization (among multiple MCMC
 realizations) for the three soil respiration models and eight data models.



1258 Figure 5. Marginal posterior parameter density of carbon use efficiency (CUE) for the three soil

1259 respiration models and eight data models.

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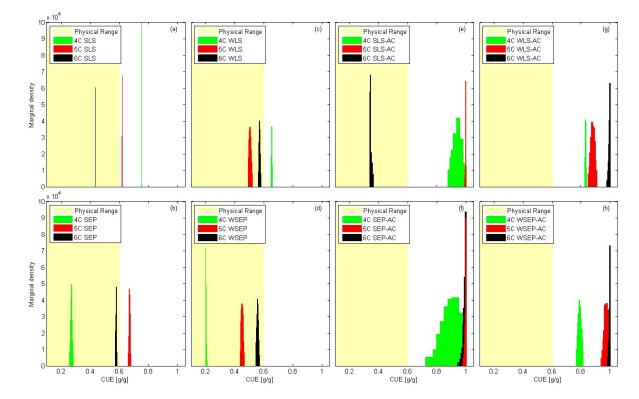


Figure 6. Observation data (blue dots) and mean prediction (green line) and 95% credible intervals (red line) of prediction ensembles for (a)-(f) the calibration period and (g)-(l) the validation period. The plots are for the three soil respiration models using data models SLS and WSEP-AC. *The prediction ensembles are generated to consider parametric uncertainty of the soil respiration models only*.



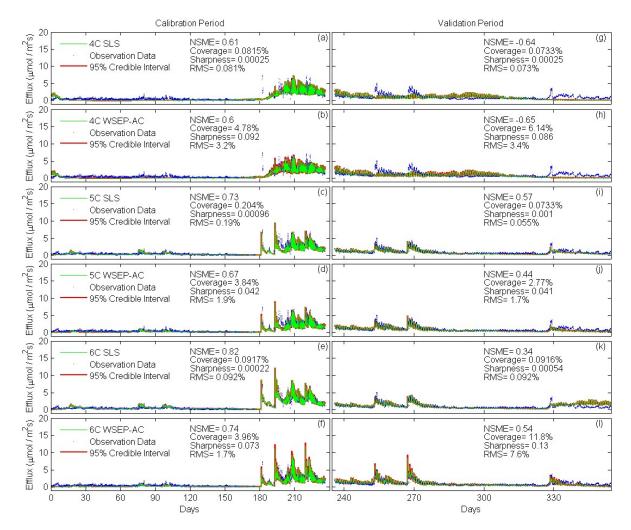


Figure 7. (a-b) Nash-Sutcliffe model efficiency (NSME), (c)-(d) sharpness, (e)-(f) predictive coverage, and (g)-(h) relative model score for measuring predictive performance of the three soil respiration models and the eight data models during the calibration and cross-validation periods. *The statistics are evaluated from the prediction ensembles generated to consider parametric uncertainty of the soil respiration models only.*

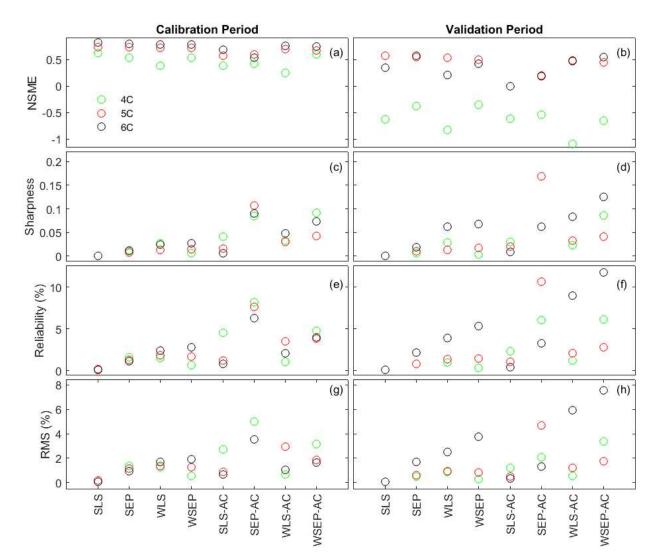


Figure 8. Observation data (blue dots) and mean prediction (green line) and 95% credible intervals
(red line) of prediction ensembles for (a)-(f) the calibration period and (g)-(l) the validation period.
The plots are for the three soil respiration models using data models SLS and WSEP-AC. *The prediction ensembles are generated to consider parametric uncertainty of not only the soil respiration models but also the data models.*



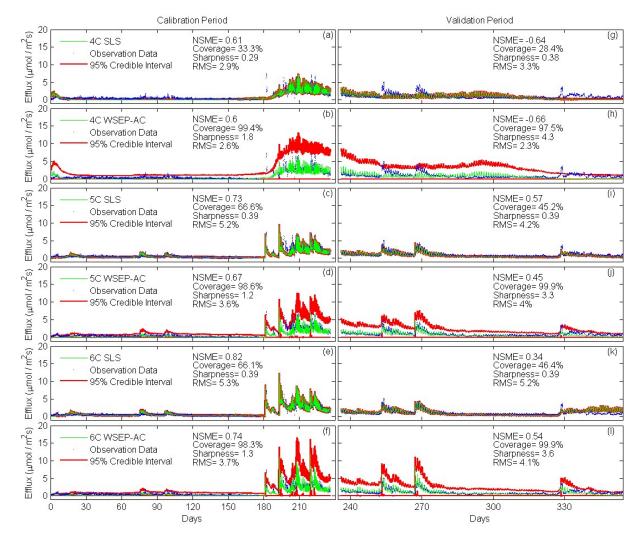


Figure 9. (a-b) Nash-Sutcliffe model efficiency (NSME), (c)-(d) sharpness, (e)-(f) predictive coverage, and (g)-(h) relative model score for measuring predictive performance of the three soil respiration models and the eight data models during the calibration and cross-validation periods. *The statistics are evaluated from the prediction ensembles generated to consider parametric uncertainty of not only the soil respiration models but also the data models*.

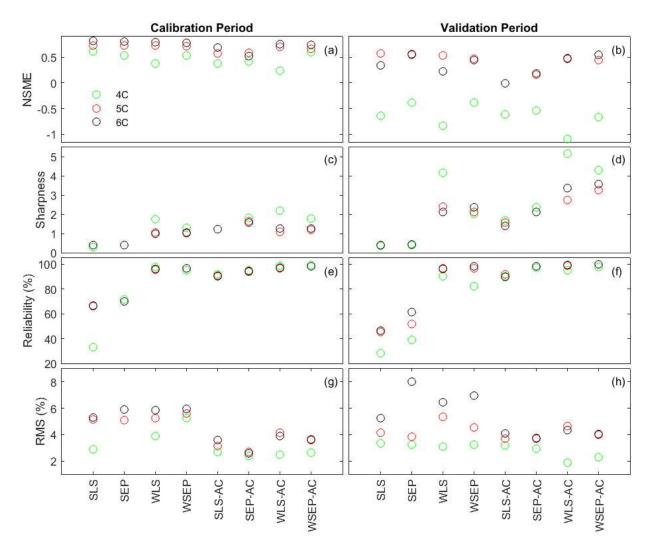


Figure 10. Observation data (blue dots) and mean prediction (green line) and 95% credible intervals (red line) for 6C for the eight likelihood functions during the calibration period (a)-(h) and the validation period (i)-(p). *The prediction ensembles are generated to consider parametric uncertainty of not only the soil respiration models but also the data models*.

