Evaluation of lossless and lossy algorithms for the compression of scientific datasets in NetCDF-4 or HDF5 files

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Abstract. The increasing volume of scientific datasets requires the use of compression to reduce data storage and transmission costs, especially for the oceanographic or meteorological datasets generated by Earth observation mission ground segments. These data are mostly produced in NetCDF files. Indeed, the NetCDF-4/HDF5 file formats are widely
10 used throughout the global scientific community because of the useful features they offer. HDF5 in particular offers a dynamically loaded filter plugin so that users can write compression/decompression filters, for example, and process the data before reading or writing them to disk. This study evaluates lossy and lossless compression/decompression methods through NetCDF-4 and HDF5 tools on analytical and real scientific floating-point datasets. We also introduce the Digit Rounding algorithm, a new relative error-bounded data reduction method inspired by the Bit Grooming algorithm. The Digit Rounding
15 algorithm offers a high compression ratio while keeping a given number of significant digits in the dataset. It achieves a higher compression ratio than the Bit Grooming algorithm with slightly lower compression speed.

1 Introduction

Ground segments processing scientific mission data are facing challenges due to the ever-increasing resolution of on-board instruments and the volume of data to be processed, stored and transmitted. This is the case for oceanographic and
20 meteorological missions, for instance. Earth observation mission ground segments produce very large files mostly in NetCDF format, which is standard in the oceanography field and widely used by the meteorological community. This file format is widely used throughout the global scientific community because of its useful features. The fourth version of the NetCDF library, denoted NetCDF-4/HDF5 (as it is based on the HDF5 layer), offers 'Deflate' and 'Shuffle' algorithms as native compression features. However, the compression ratio achieved does not fully meet ground processing requirements,
25 which are to significantly reduce the storage and dissemination cost as well as the I/O times between two modules in the processing chain.

In response to the ever-increasing volume of data, scientists are keen to compress data. However, they have certain requirements: both compression and decompression have to be fast. Lossy compression is acceptable only if the compression ratios are higher than those of lossless algorithms and if the precision, or data loss, can be controlled. There is a trade-off

between the data volume and the accuracy of the compressed data. Nevertheless, scientists can accept small losses if they remain below the data's noise level. Noise is difficult to compress and of little interest to scientists, so they do not consider data degradation that remains under the noise level as a loss (Baker et al., 2016). In order to increase the compression ratio within the processing chain, 'clipping' methods may be used to degrade the data before compression. These methods increase the compression ratio by removing the least significant digits in the data. Indeed, at some level, these least significant digits may not be scientifically meaningful in datasets corrupted by noise.

This paper studies compression and clipping methods that can be applied to scientific datasets in order to maximize the compression ratio while preserving scientific data content and numerical accuracy. It focuses on methods that can be applied to scientific datasets, i.e. vectors or matrices of floating-point numbers. First, lossless compression algorithms can be applied to any kind of data. The standard is the 'Deflate' algorithm (Deutsch, 1996) native in NetCDF-4/HDF5 libraries. It is widely used in compression tools such as zip, gzip, and zlib libraries, and has become a benchmark for lossless data compression. Recently, alternative lossless compression algorithms have emerged. These include Google Snappy, LZ4 (Collet, 2013) or Zstandard (Collet and Turner, 2016). To achieve faster compression than the Deflate algorithm, none of these algorithms use Huffman coding. Second, preprocessing methods such as Shuffle, available in HDF5, or Bitshuffle (Masui et al., 2015) are used to optimize lossless compression by rearranging the data bytes or bits into a "more compressible" order. Third, some lossy/lossless compression algorithms, such as FPZIP (Lindstrom and Isenburg, 2006), ZFP (Lindstrom, 2014) or Sz (Tao et al, 2017a), are specifically designed for scientific data—and in particular floating-point data—and can control data loss. Fourth, data reduction methods such as Linear Packing (Caron, 2014a), Layer Packing (Silver and Zender, 2017), Bit Shaving (Caron, 2014b), and Bit Grooming (Zender, 2016a) lose some data content without necessarily reducing its volume. Preprocessing methods and lossless compression can then be applied to obtain a higher compression ratio.

This paper focuses on compression methods implemented for NetCDF-4 or HDF5 files. These scientific file formats are widespread among the oceanographic and meteorological communities. HDF5 offers a dynamically loaded filter plugin that allows users to write compression/decompression filters (among others), and to process data before reading or writing them to disk. Consequently, many compression/decompression filters—such as Bitshuffle, Zstandard, LZ4, and Sz—have been implemented by members of the HDF5 user community and are freely available. The NetCDF Operator toolkit (NCO) (Zender, 2016b) also offers some compression features, such as Bit Shaving, Decimal Rounding and Bit Grooming.

The rest of this paper is divided into five sections. Section 2 presents the lossless and lossy compression schemes for scientific floating-point datasets. Section 3 introduces the Digit Rounding algorithm, which is an improvement of the Bit Grooming algorithm that optimizes the number of mantissa bits preserved. Section 4 defines the performance metrics used in this paper. Section 5 describes the performance assessment of a selection of lossless and lossy compression methods on synthetic datasets. It presents the datasets and compression results before making some recommendations. Section 6 provides some compression results obtained with real CFOSAT and SWOT datasets. Finally, section 7 provides our conclusions.

2 Compression algorithms

Compression schemes for scientific floating-point datasets usually entail several steps: data reduction, preprocessing, and lossless coding. These three steps can be chained as illustrated in Fig. 1. The lossless coding step is reversible. It does not degrade the data while reducing its volume. It can be implemented by lossless compression algorithms such as Deflate, Snappy, LZ4 or Zstandard. The preprocessing step is also reversible. It rearranges the data bytes or bits to enhance lossless coding efficiency. It can be implemented by algorithms such as Shuffle or Bitshuffle. The data reduction step is not reversible because it entails data losses. The goal is to remove irrelevant data such as noise or other scientifically meaningless data. Data reduction can reduce data volume, depending on the algorithm used. For instance, the Linear Packing and Sz algorithms reduce data volume, but Bit Shaving and Bit Grooming algorithms do not.

This paper evaluates lossless compression algorithms Deflate, LZ4, and Zstandard; Deflate because it is the benchmark algorithm, LZ4 because it is a widely-used, very-high-speed compressor, and Zstandard because it provides better results than Deflate both in terms of compression ratios and of compression/decompression speeds. The Deflate algorithm uses LZ77 dictionary coding (Ziv and Lempel, 1977) and Huffman entropy coding (Huffman, 1952). Both methods exploit different types of redundancies to enable Deflate to achieve high compression ratios. However, the computational cost of the Huffman coder is high and makes Deflate compression rather slow. LZ4 is a dictionary coding algorithm designed to provide high compression/decompression speeds rather than a high compression ratio. It does this without an entropy coder. Zstandard is a fast lossless compressor offering high compression ratios. It makes use of dictionary coding (repcode modeling) and a finite-state entropy coder (tANS) (Duda, 2013). It offers a compression ratio similar to that of Deflate coupled with high compression/decompression speeds.

This paper also evaluates Shuffle and Bitshuffle. The Shuffle algorithm groups all the data samples' first bytes together, all the second bytes together, etc. In smooth datasets, or datasets with highly correlated consecutive sample values, this rearrangement creates long runs of similar bytes, improving the dataset's compression. Bitshuffle extends the concept of Shuffle to the bit level by grouping together all the data samples' first bits, second bits, etc.

Last, we evaluate the lossy compression algorithms Sz, Decimal Rounding and Bit Grooming. The Sz algorithm predicts data samples using an n-layers prediction model and performs an error-control quantization of the data before variable length encoding. Unpredictable data samples are encoded after a binary representation analysis: the insignificant bits are truncated after computation of the smallest number of mantissa bits required to achieve the specified error bound. The Decimal Rounding algorithm achieves a uniform scalar quantization of the data. The quantization step is a power of 2 pre-computed so as to preserve a specific number of decimal digits. The Bit Grooming algorithm creates a bitmask to degrade the least significant bits of the mantissa of IEEE 754 floating-point data. Given a specified total number of significant digits, nsd, the Bit Grooming algorithm tabulates the number of mantissa bits that has to be preserved to guarantee the specified precision of nsd digits: to guarantee 1-6 digits of precision, Bit Grooming must retain 5, 8, 11, 15, 18, and 21 mantissa bits respectively. The advantage is that the number of mantissa bits that must be preserved is computed very quickly. The disadvantage is that

this computation is not optimal. In many cases, more mantissa bits are preserved than strictly necessary. Table 1 provides an example using the value of π with a specified precision of $nsd = 4$ digits. This table reproduces some of the results from Table 1 in (Zender, 2016a). The Bit Grooming algorithm preserves 15 mantissa bits. Table 1 shows that only 12 bits were actually necessary. Optimizing the number of mantissa bits preserved has a favorable impact on the compression ratios since
5   it allows more bits to be zeroed, thus creating longer sequences of zero bits. In the next section, we propose the Digit Rounding algorithm to overcome this limitation of the Bit Grooming algorithm.

3 The Digit Rounding algorithm

The Digit Rounding algorithm is similar to the Decimal Rounding algorithm in the sense that it computes a quantization factor q, which is a power of 2, in order to set bits to zero in the binary representation of the quantized floating-point value.
10   But it adapts the quantization factor to each sample value. The Digit Rounding algorithm uses uniform scalar quantization with reconstruction at the bin center:

$$\tilde{s}_i = \text{sign}(s_i) \times \left(\left\lfloor \frac{|s_i|}{q_i} \right\rfloor + 0.5 \right) \times q_i \tag{1}$$

where $\tilde{s}_i$ is the quantized value of sample value s_i. The quantization error is bounded by:

$$|s_i - \tilde{s}_i| \leq q_i/2 \tag{2}$$

15   The number of digits d_i before the decimal separator in value s_i is:

$$d_i = \lfloor \log_{10}|s_i| + 1 \rfloor \tag{3}$$

We want to preserve nsd significant digits of sample value s. This is approximately equivalent to having a rounding error of less than half the last tenth digit preserved. The quantization error shall thus be lower than or equal to:

$$|s_i - \tilde{s}_i| \leq 0.5 \times 10^{d_i - nsd} \tag{4}$$

20   This condition guarantees that the Digit Rounding algorithm always preserves a relative error lower than or equal to half the value of the least significant digit. Combining Eq. (2) and Eq. (4), we look for the highest quantization factor q_i such that:

$$q_i/2 \leq 0.5 \times 10^{d_i - nsd} \text{ or } \log_{10}(q_i) \leq d_i - nsd$$

Moreover, in order to lower the computational cost and increase compression efficiency, we seek a quantization factor that is a power of two. This allows bit-masking instead of division, and creates sequences of zero bits:

25    $$q_i = 2^{p_i} \tag{5}$$

We thus look for the greatest integer p_i such that $p_i \leq (d_i - nsd) \log_2 10$. Finally, we take value p_i such that:

$$p_i = \lfloor (d_i - nsd) \log_2 10 \rfloor \tag{6}$$

The log computation in Eq. (3) is the more computationally intensive, but optimization is possible because only the integer part of the result is useful. The optimization consists in computing the number of digits before decimal separator d from
30   binary exponent e_i and mantissa m_i of value s_i, which in binary representation is written:

$$s_i = \text{sign}(s_i) \times 2^{e_i} \times m_i \tag{7}$$

The mantissa m_i is a number between 0.5 and 1. Hence, using Eq. (3) we obtain:

$$d_i = \lfloor \log_{10}(2^{e_i} \times m_i) \rfloor + 1 \text{ or } d_i = \lfloor e_i \log_{10}(2) + \log_{10}(m_i) \rfloor + 1$$

The $\log_{10}(m_i)$ value is tabulated. Only 5 tabulated values are used in our implementation, enough to provide a good precision. The tabulated values v for $\log_{10}(m_i)$ are such that $v \leq \log_{10}(m_i)$. They are provided in the Supplement. Number

5   d_i of significant digits before the decimal separator in sample value s_i is thus approximated with the following equation:

$$d_i \approx \lfloor e_i \log_{10}(2) + v \rfloor + 1 \tag{8}$$

This computation slightly underestimates the values for d_i but provides a more conservative quantization, guaranteeing the specified number of significant digits. The optimization slightly decreases the achievable compression ratios in exchange for a much higher compression speed.

10   The Digit Rounding algorithm is summarized in Fig. 2. We have developed an HDF5 dynamically loaded filter plugin so as to apply the Digit Rounding algorithm to NetCDF-4 or HDF5 datasets. It should be noted that data values rounded by the Digit Rounding algorithm can be read directly: there is no reverse operation to Digit Rounding, and users do not need any software to read the rounded data. Table 2 provides the results of the Digit Rounding algorithm on the value of π with specified precisions nsd varying from 1 to 8 digits. It can be compared to the Bit Grooming results provided in Table 2 in

15   (Zender, 2016a). For a specified precision of $nsd = 4$ digits, the Digit Rounding algorithm preserves 11 bits in the mantissa and sets the 12th bit to 1. Compared to the Bit Grooming algorithm, 3 more bits have been set to 0. Table 3 provides the maximum absolute error obtained with varying nsd values on an artificial dataset composed of 1,000,000 values evenly spaced over the interval [1.0, 2.0]. This is the same artificial dataset used in Table 3 in (Zender, 2016a). It shows that Digit Rounding always preserves a relative error lower than or equal to half the value of the least significant digit, i.e. $|s_i - \tilde{s}_i| \leq$

20   $0.5 \times 10^{d_i - nsd}$. We compare the compression ratio obtained with the Digit Rounding algorithm to that obtained with the Bit Grooming algorithm for the same meteorological data from MERRA re-analysis studied in (Zender, 2016a). Table 4 reports the Bit Grooming results extracted from Table 6 in (Zender, 2016a) and provides the results of the Digit Rounding algorithm. The same lossless compression is employed: Shuffle and Deflate with level 1 compression. From $nsd = 7$ to $nsd = 5$, Digit Rounding and Bit Grooming provide similar compression ratios with a slight advantage for the Bit Grooming

25   algorithm. However, from $nsd = 4$ to $nsd = 1$, the compression ratios obtained with Digit Rounding are clearly better.

The following section first defines the various performance metrics used hereinafter, then studies the performance of various lossless and lossy compression algorithms—including Digit Rounding—when applied to both synthetic and real scientific datasets.

4 Performance metrics

30   One of the features required for lossy scientific data compression is control over the amount of loss, or the accuracy, of the compressed data. Depending on the data, this accuracy can be expressed by an absolute or a relative error bound. The maximum absolute error is defined by $e_{abs}^{max} = \max|\tilde{s}_i - s_i|$ where s_i are the sample values of the original dataset and $\tilde{s}_i$ are

the sample values of the compressed dataset. An absolute error bound specifies the maximum absolute error, e_{abs}, allowed between any sample of the original and compressed data: $e_{abs}^{max} \leq e_{abs}$. The maximum relative error is defined by $e_{rel}^{max} = \max \left| \frac{\tilde{s}_i - s_i}{s_i} \right|$. A relative error bound specifies the maximum relative error, e_{rel}, allowed between any sample of the original and compressed data: $e_{rel}^{max} \leq e_{rel}$. The absolute error bound can be useful for data with a single dynamic range of interest.

5 The relative error bound can be useful for data where both very low and very high values are pertinent.

A near-nearly exhaustive list of metrics for assessing the performance of lossy compression of scientific datasets is provided in (Tao et al., 2017b). For the sake of conciseness, only a few of them are presented in this paper. The following metrics were chosen for this study:

- compression ratio $CR(F)$ to evaluate the reduction in size as a result of the compression. It is defined by the ratio of
10   the original file size over the compressed file size:

$$CR(F) = \frac{filesize(F_{orig})}{filesize(F_{comp})}$$

- compression speed $CS(F)$ and decompression speed $DS(F)$ to evaluate the speed of the compression and decompression. They are defined by the ratio of the original file size over the compression or decompression time:

$$CS(F) = \frac{filesize(F_{orig})}{t_{comp}}$$

$$DS(F) = \frac{filesize(F_{orig})}{t_{decomp}}$$

The compression and decompression speeds are expressed in MB/s. Those reported in this paper were obtained on a Dell T1600 with an Intel Xeon E31225 4-core CPU at 3.1GHz, and a 4GB memory under the RedHat 6.5 (64-bit) OS with

15 compression and decompression run on a single core. Parallel compression has not been considered in this work.

The following metrics were chosen to assess the data degradation of the lossy compression algorithms:

- maximum absolute error e_{abs}^{max} defined previously. It is used to evaluate the maximum error between the original and compressed data;

- mean error $\bar{e}$ to evaluate if any bias is introduced into the compressed data. It is defined as the mean of the
20   pointwise difference between the original and compressed data:

$$\bar{e} = \frac{1}{N} \sum_{i=0}^{N-1} (s_i - \tilde{s}_i)$$

- mean absolute error $\overline{e_{abs}}$ to evaluate the mean data degradation. It is defined as the mean of the pointwise absolute difference between the original and compressed data:

$$\overline{e_{abs}} = \frac{1}{N} \sum_{i=0}^{N-1} |s_i - \tilde{s}_i|$$

- SNR to evaluate the signal to compression error ratio. It is defined by the ratio of the signal level over the root mean square compression error and is expressed in decibels (dB):

$$SNR_{dB} = 20 \log_{10} \left(\frac{\sqrt{\frac{1}{N} \sum_{i=0}^{N-1} s_i^2}}{\sqrt{\frac{1}{N} \sum_{i=0}^{N-1} (s_i - \tilde{s}_i)^2}} \right)$$

These metrics are used in the following sections to evaluate various lossless and lossy compression algorithms, including Digit Rounding.

5 Performance assessment with synthetic data

5.1 Analytical datasets

Synthetic datasets $s1$ and $s3D$ with known statistics were generated in order to test the compression algorithms under variable conditions. Dataset $s1$ is a noisy sinusoid of 1 dimension with a maximum absolute value of 118. The data volume of this dataset is 4MB. Dataset s3D is a noisy sinusoid pulse of 3 dimensions with a maximum absolute value of 145. The data volume of this dataset is 512MB. The Supplement describes these datasets in greater detail.

5.2 Performance assessment of lossless compression methods

The lossless compression algorithms evaluated are Deflate and Zstandard with or without the Shuffle or Bitshuffle preprocessing step. LZ4 is always evaluated with the Bitshuffle preprocessing step because it was imposed in the LZ4 implementation we used. We ran a lossless compression algorithm using the h5repack tool from the HDF5 library, version 1.8.19, Deflate implemented in zlib 1.2.11, Zstandard version 1.3.1 with the corresponding HDF5 filter available on the HDF web portal (http://portal.hdfgroup.org/display/support/Filters), and the implementation of LZ4 and Bitshuffle in python package Bitshuffle-0.3.4. The compression was performed by calling the h5repack tool. The Supplement provides the command lines and options used.

Figures 3 and 4 provide the results obtained for the compression and decompression of dataset $s1$ and dataset $s3D$ respectively. The vertical bars represent the results for different compression levels: from 1 to 9 for Deflate level *dfl_lvl*, from 1 to 22 for Zstandard level *zstd_lvl*, and only one level for LZ4. First, it can be observed that preprocessing steps Shuffle or Bitshuffle have a similarly favorable impact both on the compression ratio and on the compression/decompression speeds. Second, the compression level parameters *dfl_lvl* and *zstd_lvl* have little influence on the compression ratio. However, the compression/decompression speeds decrease as compression levels increase, particularly with Zstandard compression levels. Third, the compression ratios obtained with Deflate and Zstandard are similar, but the compression speeds of Zstandard at low compression levels are far higher, and the decompression speeds of Zstandard are always higher. Fourth, Bitshuffle+LZ4 provides a slightly lower compression ratio than Shuffle+Deflate or Shuffle+Zstandard, with a

compression speeds similar to Shuffle+Deflate or Shuffle+Zstandard at low compression level parameters *dfl_lvl* or *zstd_lvl*. Finally, the compression/decompression speeds obtained with Zstandard and LZ4 for the compression of dataset $s3D$ are much lower than that achieved for the compression of dataset $s1$. Further investigations are required to understand why the compression/decompression speeds are lower, but it might be related to HDF5 chunking.

5   To summarize, these results show that preprocessing by Shuffle or Bitshuffle is very helpful in increasing compression efficiency. They also show that Zstandard can provide higher compression and decompression speeds than Deflate at low compression levels. However, on the $s3D$ dataset, we observed that Zstandard compression and decompression speeds are lower than those obtained with Deflate. Therefore, Deflate and Zstandard are both options to consider for the lossless compression of scientific datasets as long as they follow the Shuffle or Bitshuffle preprocessing step.

10   **5.3 Performance assessment of lossy compression methods**

The lossy compression algorithms evaluated are error-bounded compression algorithms. They can constrain either the maximum absolute error or the maximum relative error, or both. The compression algorithms evaluated are Sz, Decimal Rounding, Bit Grooming and the Digit Rounding algorithm introduced in this paper. The Sz compression algorithm works in both error-bounded modes. Decimal Rounding allows a specific number of decimal digits to be preserved. In this sense, it

15   bounds the maximum absolute error. Bit Grooming allows a specific number of significant digits to be preserved. In this sense, it bounds the maximum relative error. Like the Bit Grooming algorithm, Digit Rounding preserves a specific number of significant digits and bounds the maximum relative error.

We ran Sz version 2.1.1 using the h5repack tool and Sz HDF5 filter plugin, applying the Deflate lossless compression algorithm integrated in the Sz software. We ran the Decimal Rounding and Bit Grooming algorithms using NCO version

20   4.7.9, applying Shuffle and Deflate compression in the call to the NCO tool. Last, we ran the Digit Rounding algorithm using the h5repack tool and custom implantation of the algorithm in an HDF5 plugin filter. The Supplement provides the command lines and options used.

5.3.1 Performance comparison in absolute error-bounded compression mode

This section compares the performance of the absolute error-bounded compression algorithms: Sz and Decimal Rounding.

25   The results reported were obtained by applying Sz configured with the options SZ_BEST_SPEED and Gzip_BEST_SPEED. Shuffle and Deflate with *dflt_lvl* = 1 were applied after Decimal Rounding.

Table 5 compares the results obtained in absolute error-bounded compression mode for $e_{abs} = 0.5$. This corresponds to *dsd* = 0 significant decimal digits preserved, or in other words, a rounding to the nearest integer. Both Sz and Decimal Rounding algorithms respect the specified maximum absolute error value. Moreover, none introduces a statistical bias: the

30   mean absolute errors of both algorithms—not shown in this table—are very close to zero. The errors introduced by these two algorithms are similar. However, it can be seen that Decimal Rounding provided a higher compression ratio than Sz for dataset $s1$. On the other hand, Sz provided a higher compression ratio for dataset $s3D$. Sz may perform better on dataset $s3D$

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because it is smoother than dataset $s1$. Indeed, Sz integrates a prediction step. This prediction might often fail because dataset $s1$ is very noisy. This may explain the lower compression ratio for $s1$ dataset. Decimal Rounding, however, does not make any predictions, which may explain why it achieves a better compression than Sz for dataset $s1$. The lower compression/decompression speeds obtained with Sz on the dataset $s3D$ are not well understood and might be related to HDF5 chunking as previously mentioned.

Figure 5 compares Sz and Bit Grooming algorithms in terms of SNR versus compression ratio. This figure was obtained with the following parameters:

- For the Sz algorithm, the *absErrBound* parameter was successively set to 5e-5, 5e-4, 5e-3, 5e-2, 5e-1, 5;
- For the Decimal Rounding algorithm, the *dsd* parameter was successively set to 4, 3, 2, 1, 0, -1.

For dataset $s1$, Decimal Rounding has a higher SNR than Sz for a given compression ratio. On the contrary, for dataset $s3D$, Sz has a higher SNR than Decimal Rounding for a given compression ratio. Both Sz and Bit Grooming algorithms seem valuable for error-bounded compression.

5.3.2 Performance comparison in relative error-bounded compression mode

This section compares the performance of the relative error-bounded compression algorithms: Sz, Bit Grooming, and Digit Rounding. The results reported were obtained by applying Sz configured with the options SZ_DEFAULT_COMPRESSION and Gzip_BEST_SPEED. Shuffle and Deflate with *dflt_lvl*=1 were applied after the Bit Grooming and Decimal Rounding algorithms.

We first focus on the results obtained with dataset $s1$. The number of significant digits—*nsd* parameter—in the Bit Grooming and Digit Rounding algorithms was set to 3. As the maximum absolute value in the *s1* dataset is 118, the maximum absolute error should be lower than 0.5. In order to be able to compare Sz configured with a relative error bound with those algorithms, we configured the relative error bound to obtain a maximum absolute error of 0.5: the *pw_relBoundRatio* parameter in Sz was set to 0.00424. The results are provided in Table 6. It can be observed that all three algorithms respect the maximum absolute error of 0.5, which corresponds for dataset $s1$ to a relative error of 0.00424. On this dataset, Sz provides higher compression ratio and compression speed than the other two algorithms. Bit Grooming is too conservative. It preserves more mantissa bits than strictly necessary to achieve the required precision. This behavior is illustrated in Table 1 with the value of π. In contrast, Digit Rounding adapts the quantization step to each value of the input dataset. Doing so, it can achieve the required precision while preserving less mantissa bits than Bit Grooming does. This results both in a higher compression ratio but also in higher errors than Bit Grooming. Results obtained for Bit Grooming with *nsd* = 2 are also provided for completeness. With this parameter, Bit Grooming provides slightly higher compression ratio and compression speed than Digit Rounding does.

Figure 6 (left) compares Sz, Bit Grooming, and Digit Rounding algorithms in terms of SNR versus compression ratio. This figure has been obtained with the following parameters:

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- For the Sz algorithm, the *pw_relBoundRatio* parameter was successively set to 4.24e-5, 4.24e-4, 4.24e-3;
- For the Bit Grooming algorithm, the *nsd* parameter was successively set to 6, 5, 4, 3, 2, 1;
- For the Digit Rounding algorithm, the *nsd* parameter was successively set to 6, 5, 4, 3, 2, 1.

All three algorithms provide similar SNR versus compression ratio results, with a slight advantage for the Bit Grooming

5   algorithm. Figure 7 (left) compares the compression ratio obtained as a function of parameter *nsd*, which is the user-specified number of significant digits. Even though *nsd* is not a parameter of the Sz algorithm, we related the *pw_relBoundRatio* to the *nsd* parameters for dataset *s*1 (i.e. *pw_relBoundRatio* = 4.24e^{-nsd}) and plotted the compression ratio obtained with the Sz algorithm on the same figure. It can be seen that, whatever the *nsd* specified by the user, the compression ratios obtained with Digit Rounding are higher than the compression ratio obtained with the Bit Grooming algorithm. It can also be seen that

10   the compressions obtained with the Sz algorithm are even higher.

We now focus on the results obtained with dataset *s3D*. The number of significant digits—*nsd* parameter—in the Bit Grooming and Digit Rounding algorithms was set to 3. As the maximum absolute value in the *s3D* dataset is 145, the *pw_relBoundRatio* parameter in Sz was set to 0.00345. Results are provided in Table 7. It can be observed that all three algorithms comply with the relative error bound specified. However, as previously mentioned, the Bit Grooming algorithm is

15   too conservative. This is why results obtained with *nsd* = 2 are also provided. On this dataset, Sz provides higher compression ratio than the other two algorithms but lower compression speed than Bit Grooming. At *nsd* = 3, Digit Rounding provides slightly higher compression ratio than Bit Grooming but with lower compression speed.

Figure 6 (right) compares Sz, Bit Grooming, and Digit Rounding algorithms in terms of SNR versus compression ratio. This figure has been obtained with the following parameters:

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- For the Sz algorithm, the *pw_relBoundRatio* parameter was successively set to 3.45e-5, 3.45e-4, 3.45e-3;
- For the Bit Grooming algorithm, the *nsd* parameter was successively set to 6, 5, 4, 3, 2, 1;
- For the Digit Rounding algorithm, the *nsd* parameter was successively set to 6, 5, 4, 3, 2, 1.

The Bit Grooming and Digit Rounding algorithms provide similar compression ratios, but even higher compression ratios are obtained with Sz. Figure 7 (right) compares the compression ratio obtained as a function of the *nsd* parameter, which is

25   the user-specified number of significant digits. As for dataset *s*1, we related *pw_relBoundRatio* to the *nsd* parameters for dataset *s3D* (i.e. *pw_relBoundRatio* = 3.45e45^{-nsd}) and plotted the compression ratio obtained with the Sz algorithm on the same figure. Whatever the *nsd* specified by the user, the compression ratios obtained with the Digit Rounding algorithm are higher than the compression ratio obtained with the Bit Grooming algorithm. The compression ratios obtained with Sz are even higher.

30   Those results show that the Digit Rounding algorithm can be competitive with the Bit Grooming and Sz algorithms in relative error-bounded compression mode. It is thus applied to real scientific datasets in the next section.

6 Application to scientific datasets

6.1 Application to a CFOSAT dataset

CFOSAT is a cooperative program between the French and Chinese space agencies (CNES and CNSA respectively). CFOSAT is designed to characterize the ocean surfaces to better model and predict ocean states, and improve knowledge of ocean/atmosphere exchanges. CFOSAT products will help marine and weather forecasting and will also be used to monitor the climate. The CFOSAT satellite will carry two scientific payloads—SCAT, a wind scatterometer; and SWIM, a wave scatterometer—for the joint characterization of ocean surface winds and waves. The SWIM (Surface Wave Investigation and Monitoring) instrument delivered by CNES is dedicated to measuring the directional wave spectrum (density spectrum of wave slopes as a function of direction and wavenumber of the waves). The CFOSAT L1A product contains calibrated and geocoded waveforms.

Currently, the baseline for compression of the CFOSAT L1A product involves a clipping method as a data reduction step, with Shuffle preprocessing and Deflate lossless coding with a compression level *dfl_lvl* of 3. Compression with a clipping method is like compression in an absolute error-bounded mode. It defines the least significant digit (*lsd*) and 'clips' the data to keep only *lsd* decimal digits. The *lsd* is defined specifically for each dataset variable. The full list is provided in the Supplement with all the command lines and parameters used for running the compression methods described in this section. We studied the following compression methods:

- CFOSAT clipping followed by Shuffle and Deflate (*dflt_lvl* = 3): the baseline for the compression of CFOSAT datasets;
- CFOSAT clipping followed by Shuffle and Zstandard (*zstd_lvl* = 2) for higher compression speeds;
- Sz followed by Deflate in the absolute error bounded mode;
- Decimal Rounding followed by Shuffle and Deflate (*dflt_lvl* = 1);
- Bit Grooming (*nsd* = 8) followed by Shuffle and Deflate (*dflt_lvl* = 1);
- Digit Rounding (*nsd* = 8) followed by Shuffle and Deflate (*dflt_lvl* = 1).

We first focused on the *ground_range_5* variable of the CFOSAT L1A product. This variable is an array of 18451×3215 values in double precision. The data volume is 452.58MB (uncompressed). The CFOSAT clipping method defines an *lsd* of 3 for this variable. In absolute error-bounded mode, Decimal Rounding is configured to keep the same number of decimal digits as CFOSAT clipping: *dsd* = .3; Sz is configured with *absErrBound* = 5e-4. In relative error-bounded mode, Bit Grooming and Digit Rounding are configured with *nsd* = 8. The compression results are provided in Table 8. Compared to the CFOSAT baseline compression, Zstandard compression is more than twice faster while offering a similar compression ratio. On this dataset, the use of Sz instead of the CFOSAT Clipping method increases the compression ratio by a factor of 11. Sz prediction step seems to be very efficient on this dataset. Decimal Rounding increases the compression ratio by a factor of 2.5 "only", but provides the fastest decompression. In the relative error-bounded mode, Digit Rounding provides a higher compression ratio than Bit Grooming but lower compression/decompression speeds.

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The results for the compression of the full CFOSAT L1A product of 7.34GB (uncompressed) are provided in Table 9. The maximum absolute error and the mean absolute error are not provided because this dataset contains several variables compressed with different parameters. Compared to the CFOSAT baseline compression, Zstandard increases the compression speed by about 40% while offering a similar compression ratio. It was not possible to apply Sz compression on the full dataset since Sz configuration file has to be modified to adapt the *absErrBound* to the *lsd* defined for each dataset variable. The way around this entails processing each variable one after the other. Sz provides a compression ratio almost 3 times higher than the baseline with faster compression and decompression. Decimal Rounding is configured on a per-variable basis to keep the precision required by the scientists on each variable. It increases the compression ratio by a factor of 1.8 with twice faster compression and decompression compared to the baseline. The compression ratios achieved with Bit Grooming or Digit Rounding in the relative error-bounded mode are lower. This is not the mode targeted for the compression of CFOSAT datasets. The usability of Sz being reduced by the fact that the error bound cannot be easily configured to achieve the precision required variable per variable, our recommendation is to use the Decimal Rounding algorithm. It achieves faster and more effective compression than CFOSAT Clipping method and bounds the absolute errors.

6.2 Application to SWOT datasets

The Surface Water and Ocean Topography Mission (SWOT) is a partnership between NASA and CNES, and continues the long history of altimetry missions with an innovative instrument known as KaRin, which is a Ka band synthetic aperture radar. The launch is foreseen for 2021. SWOT addresses both oceanographic and hydrological communities, accurately measuring the water level of oceans, rivers, and lakes.

SWOT has two processing modes, so two different types of products are generated: high-resolution products dedicated to hydrology, and low-resolution products mostly dedicated to oceanography. The Pixel Cloud product (called L2_HR_PIXC) contains data from the KaRin instrument's high-resolution (HR) mode. It contains information on the pixels that are detected as being over water. This product is generated when the HR mask is turned on. The Pixel Cloud product is organized into sub-orbit tiles for each swath and each pass, and this is an intermediate product between the L1 Single Look Complex products and the L2 lake/river ones. The product granularity is a tile 64 km long in the along-track direction, and it covers either the left or right swath (~60 km wide).

The compression of two different datasets was evaluated:

- A simplified simulated SWOT L2_HR_PIXC pixel cloud product of 460MB (uncompressed);
- A realistic and representative SWOT L2 pixel cloud dataset of 199MB (uncompressed).

The current baseline for the compression of the simplified simulated SWOT L2 pixel cloud product involves Shuffle preprocessing and Deflate lossless coding with a compression level *dfl_lvl* of 4. However, the compression method for the official SWOT L2 pixel cloud product has not yet been defined. A required precision is defined by the scientists as a number of significant digits (*nsd*) for each dataset variable. The full list is provided in the Supplement. We studied the following lossless or relative error bounded compression methods:

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- Shuffle and Deflate (*dflt_lvl* = 4): the current baseline for the compression of SWOT datasets;
- Shuffle and Zstandard (*zstd_lvl* = 2) lossless alternative;
- Sz with Deflate in the relative error bounded mode;
- Bit Grooming followed by Shuffle and Deflate (*dflt_lvl* = 1);
- Digit Rounding followed by Shuffle and Deflate (*dflt_lvl* = 1).

We first focused on the *height* variable of the SWOT L2_HR_PIXC pixel cloud product. This variable is a list of 1,421,888 values in double precision. The data volume is 10.85MB (uncompressed). A precision of 6 significant digits is required for this variable (*nsd* = 6). Sz is configured in the relative error bounded mode with *pw_relBoundRatio* = 5e-6. Bit Grooming and Digit Rounding are configured with *nsd* = 6. The results are provided in Table 10. Compared to the SWOT baseline compression, Zstandard compression is more than 10 times faster while offering a similar compression ratio. On this dataset, Digit Rounding provides the highest compression ratio with compression/decompression speeds similar to the one obtained with Bit Grooming. The lowest errors are obtained with Bit Grooming but with a compression ratio slightly lower than Digit Rounding. The compression ratio obtained with Sz is even lower.

Next we focused on the *pixel_area* variable of the representative SWOT L2 pixel cloud product. This variable is a list of 1,300,111 values in double precision. The data volume is 9.92MB (uncompressed). A precision of 11 significant digits is required for this variable (*nsd* = 11). Sz is configured in the relative error bounded mode with *pw_relBoundRatio* = 5e-9 only because it cannot achieve higher precision. Bit Grooming and Digit Rounding are configured with *nsd* = 11. The results are provided in Table 11. Compared to the SWOT baseline compression, Zstandard compression is more than 7 times faster while offering a similar compression ratio. Sz provides the highest compression ratio but does not allow achieving the required precision of 11 digits. Moreover, in this configuration Sz compression is very slow. As for the *height* variable, Digit Rounding provides the highest compression ratio with compression/decompression speeds similar to the one obtained with Bit Grooming. The lowest errors are obtained with Bit Grooming but with a compression ratio lower than Digit Rounding.

Table 12 provides the results of the compression of the full simulated SWOT L2_HR_PIXC pixel cloud product. The maximum absolute error and the mean absolute error are not provided because this dataset contains several variables compressed with different parameters. Compared to the SWOT baseline compression, Zstandard increases the compression speed by over 5 times, while offering a similar compression ratio. Sz compression was not applied because it does not allow achieving the high precision required on some variables. Bit Grooming and Digit Rounding was configured on a per-variable basis to keep the precision required by the scientists on each variable. Compared to the baseline, Bit Grooming and Digit Rounding increase the compression respectively by 20% and 30% with similar compression speeds and faster decompression.

The results for the compression of the representative SWOT L2 pixel cloud product are provided in Table 13. Compared to the baseline, Zstandard compression is nearly 4 times faster while offering a similar compression ratio. Bit Grooming increases the compression ratio by 29% with higher compression speed. And Digit Rounding increases the compression ratio by 34% with slightly lower compression speed than Bit Grooming. Bit Grooming and Digit Rounding provides the fastest

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decompression. Our recommendation for the compression of SWOT datasets is thus to use the Digit Rounding algorithm to achieve high compression, at the price of a lower compression speed than the lossless solutions, considering that for SWOT the driver is product size, and taking into account the ratio between compression time and processing time.

7 Conclusions

5 This study evaluated lossless and lossy compression algorithms both on synthetic datasets and on realistic simulated datasets of future science satellites. The compression methods were applied using NetCDF-4 and HDF5 tools. It has been shown that the impact of the compression level options of Zstandard or Deflate on the compression ratio achieved is not significant compared to the impact of the Shuffle or Bitshuffle preprocessing. However, high compression levels can significantly reduce the compression speed. Deflate and Zstandard with low compression levels are both reasonable options to consider
10 for the compression of scientific datasets, but must always follow a Shuffle or Bitshuffle preprocessing step. It has been shown that Zstandard can speed-up the compression of CFOSAT and SWOT datasets compared to the baseline solution based on Deflate.

The lossy compression of scientific datasets can be achieved in two different error-bounded modes: absolute and relative error-bounded. Four algorithms have been studied: Sz, Decimal Rounding, Bit Grooming and Digit Rounding. One useful
15 feature of the last three is that the accuracy of the compressed data can easily be interpreted: rather than defining an absolute or a relative error bound, they define the number of significant decimal digits or the number of significant digits. In absolute error-bounded mode, Sz provide higher compression ratios than Decimal Rounding on most datasets. However for the compression of real scientific datasets, its usability is reduced by the fact that only one error bound can be set for all the variables composing the dataset. It cannot be easily configured to achieve the precision required variable per variable. This is
20 why we rather recommend the Decimal Rounding algorithm to achieve fast and effective compression of the CFOSAT dataset. In relative error-bounded mode, the Digit Rounding algorithm introduced in this work provides higher compression ratios than the Bit Grooming algorithm from which it derives, but with lower compression speed. Sz can provide even higher compression ratios but fails achieving the high precision required for some variables. This is why we rather recommend the Digit Rounding algorithm to achieve relative error bounded compression of SWOT datasets with a compression ratio 30%
25 higher than the baseline solution for SWOT compression.

8 Code and data availability

The Digit Rounding software source code is available from CNES GitHub at https://github.com/CNES/Digit_Rounding. The datasets are available upon request to Xavier Delaunay (xavier.delaunay@thalesgroup.com) or to Flavien Gouillon (Flavien.Gouillon@cnes.fr). The Supplement details the datasets and provides the command lines used for running the
30 compression tools.

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Table 1: Representation of the value of π in IEEE-754 single-precision binary representation (first row) and results preserving 4 significant digits with the Bit Grooming algorithm (second row) or preserving 12 mantissa bits (third row). This table builds on Table 1 in (Zender, 2016a).

Sign	Exponent	Mantissa	Decimal	Notes
0	10000000	10010010000111111011011	3.14159265	Exact value of π
0	10000000	10010010000111100000000	3.14154053	Result of Bit Grooming with $nsd = 4$, 15 mantissa bits preserved
0	10000000	10010010000100000000000	3.14111328	Result preserving only 12 mantissa bits, allows the 4 significant digits of π to be preserved.

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Table 2: Representation of the value of π in IEEE-754 single-precision binary representation (first row) and results preserving a varying number of significant digits (*nsd*) with the Digit Rounding algorithm. This table can be compared to Table 2 in (Zender, 2016a) providing the Bit Grooming results for π.

Sign	Exponent	Mantissa	Decimal	Notes
0	10000000	10010010000111111011011	3.14159265	Exact value of π
0	10000000	10010010000111111011011	3.14159265	$nsd = 8$
0	10000000	10010010000111111011010	3.14159250	$nsd = 7$
0	10000000	10010010000111111010000	3. 14159012	$nsd = 6$
0	10000000	10010010000111110000000	3. 14157104	$nsd = 5$
0	10000000	10010010000100000000000	3.14111328	$nsd = 4$
0	10000000	10010010100000000000000	3. 14453125	$nsd = 3$
0	10000000	10010100000000000000000	3. 15625000	$nsd = 2$
0	10000000	11000000000000000000000	3. 50000000	$nsd = 1$
0	10000000	00000000000000000000000	4.00000000	$nsd = 0$

10 **Table 3: Maximum absolute errors and mean absolute errors of the Digit Rounding algorithm preserving a varying number of significant digits (*nsd*) on an artificial dataset composed of 1,000,000 values evenly spaced over the interval [1.0, 2.0].**

nsd	Maximum absolute error	Mean absolute error	Mean error
1	0.4999999999	0.1732423125	-0.0796879687
2	0.0312500000	0.0127722254	-0.0003056211
3	0.0039062500	0.0016125222	-0.0000074545
4	0.0004882812	0.0001983929	-0.0000001013
5	0.0000305176	0.0000125886	-0.0000000017
6	0.0000038147	0.0000015736	-0.0000000002
7	0.0000004768	0.0000001937	0.0000000000

Table 4: Comparison between the compression ratio obtained with the Digit Rounding algorithm and the compression ratio obtained with the Bit Grooming algorithm reported in (Zender, 2016a) on a MERRA dataset. Shuffle and Deflate with level 1 lossless compression is applied. The reference for the CR computation is Deflate (level 5) compressed data size of 244.3MB.

NSD	Bit Grooming		Digit Rounding	
	Size (MB)	CR (%)	Size (MB)	CR (%)
~7	223.1	91.3	226.1	92.6
6	225.1	92.1	225.8	92.4
5	221.4	90.6	222.0	90.9
4	201.4	82.4	**191.1**	**78.2**
3	185.3	75.9	**165.1**	**67.6**
2	150.0	61.4	**111.1**	**45.5**
1	100.8	41.3	**64.9**	**26.6**

Table 5: Compression results of the absolute error-bounded compression algorithms Sz and Decimal Rounding on datasets *s1* and *s3D*.

Dataset	Compression method	CR	CS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$	SNR (dB)
s1	Sz (*absErrBound* = 0.5, Gzip_BEST_SPEED)	5.39	133	0.5	0.2499	30.84
s1	Decimal Rounding (*dsd* = .0, *dflt_lvl*=1)	7.50	100	0.5	0.2501	30.83
s3D	Sz (*absErrBound* = 0.5, Gzip_BEST_SPEED)	12.97	29	0.5	0.2500	45.97
s3D	Decimal Rounding (*dsd* = .0, *dflt_lvl*=1)	5.56	80	0.5	0.2500	45.97

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Table 6: Compression results of the relative error-bounded compression algorithms Sz, Bit Grooming, and Digit Rounding on dataset *s1*.

Compression method	CR	CS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$	SNR (dB)
Sz (*pw_relBoundRatio* = 0.00424, Gzip_BEST_SPEED)	5.08	100	0.484	0.199	32.78
Bit Grooming (*nsd* = 3, *dflt_lvl*=1)	3.09	57	0.0312	0.0156	54.93
Bit Grooming (*nsd* = 2, *dflt_lvl*=1)	4.38	57	0.250	0.125	36.54
Digit Rounding (*nsd* = 3, *dflt_lvl*=1)	4.02	40	0.5	0.195	34.51

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Table 7: Compression results of Sz, Bit Grooming, and Digit Rounding in relative error-bounded compression mode on dataset s3D.

Compression method	CR	CS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$	SNR (dB)
Sz (*pw_relBoundRatio* = 0.00345, Gzip_BEST_SPEED)	4.32	26	0.487	0.0737	54.56
Bit Grooming (*nsd* = 3, *dflt_lvl*=1)	2.35	46	0.0625	0.0079	73.96
Bit Grooming (*nsd* = 2, *dflt_lvl*=1)	3.04	51	0.5	0.0629	55.89
Digit Rounding (*nsd* = 3, *dflt_lvl*=1)	2.60	18	0.5	0.0239	58.87

5 **Table 8: Compression results for the *ground_range_5* variable in the CFOSAT L1A product.**

Compression method	CR	CS (MB/s)	DS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$
CFOSAT Clipping + Shuffle + Deflate (3)	2.34	38 (*)	123	1.00e-3	5.00e-4
CFOSAT Clipping + Zstd (2)	2.20	108 (*)	84	1.00e-3	5.00e-4
Sz (*absErrBound* = 1e-3, Gzip_BEST_SPEED)	26.53	60	42	1.00e-3	4.99e-4
Decimal Rounding (*dsd* = .3) + Shuffle + Deflate (1)	5.85	74	187	4.88e-4	2.36e-4
Bit Grooming (*nsd* = 8) + Shuffle + Deflate (1)	4.78	67	190	2.44e-4	1.22e-4
Digit Rounding (*nsd* = 8) + Shuffle + Deflate (1)	5.83	37	38	4.88e-4	2.44e-4

(*) The time taken for the CFOSAT Clipping method is not taken into account in the compression speed computation.

Table 9: Compression results for the CFOSAT L1A product.

Compression method	CR	CS (MB/s)	DS (MB/s)
CFOSAT Clipping + Shuffle + Deflate (3)	5.21	51 (*)	68
CFOSAT Clipping + Shuffle + Zstd (2)	5.38	72 (*)	78
Sz (*absErrBound*, Gzip_BEST_SPEED)	15.45	88	89
Decimal Rounding + Shuffle + Deflate (1)	9.53	101	268
Bit Grooming (*nsd* = 8) + Shuffle + Deflate (1)	4.16	75	262
Digit Rounding (*nsd* = 8) + Shuffle + Deflate (1)	4.32	37	85

(*) The time taken for the CFOSAT Clipping method is not taken into account in the compression speed computation.

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Table 10: Compression results for the *height* variable in the simplified simulated SWOT L2_HR_PIXC pixel cloud product.

Compression method	CR	CS (MB/s)	DS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$
Shuffle + Deflate (4)	1.12	24	212	0	0
Shuffle + Zstd (2)	1.12	271	181	0	0
Sz (*pw_relBoundRatio* = 5e-6, Gzip_BEST_SPEED)	2.06	35	155	3.16e-5	1.19e-7
Bit Grooming (*nsd* = 6) + Shuffle + Deflate (1)	2.34	33	217	7.58e-6	2.53e-7
Digit Rounding (*nsd* = 6) + Shuffle + Deflate (1)	2.38	35	217	3.05e-5	7.95e-7

**Table 11: Compression results for the *pixel_area* variable in the representative SWOT L2 pixel cloud product.**

Compression method	CR	CS (MB/s)	DS (MB/s)	e_{abs}^{max}	$\overline{e_{abs}}$
Shuffle + Deflate (4)	1.50	32	248	0	0
Shuffle + Zstd (2)	1.50	237	165	0	0
Sz (*pw_relBoundRatio* = 5e-9, Gzip_BEST_SPEED)	3.24	0.3	165	2.51e-6	4.56e-7
Bit Grooming (*nsd* = 11) + Shuffle + Deflate (1)	2.11	43	245	1.86e-9	3.16e-10
Digit Rounding (*nsd* = 11) + Shuffle + Deflate (1)	2.40	40	240	3.73e-9	1.86e-9

5 **Table 12: Compression results for the simplified simulated SWOT L2_HR_PIXC pixel cloud product.**

Compression method	CR	CS (MB/s)	DS (MB/s)
Shuffle + Deflate (4)	14.37	107	92
Shuffle + Zstd (2)	14.36	589	97
Bit Grooming + Shuffle + Deflate (1)	17.44	141	336
Digit Rounding + Shuffle + Deflate (1)	18.92	100	393

Table 13: Compression results for the representative SWOT L2 pixel cloud product.

Compression method	CR	CS (MB/s)	DS (MB/s)
Shuffle + Deflate (4)	1.99	35	258
Shuffle + Zstd (2)	1.99	139	90
Bit Grooming + Shuffle + Deflate (1)	2.55	52	276
Digit Rounding + Shuffle + Deflate (1)	2.65	42	228

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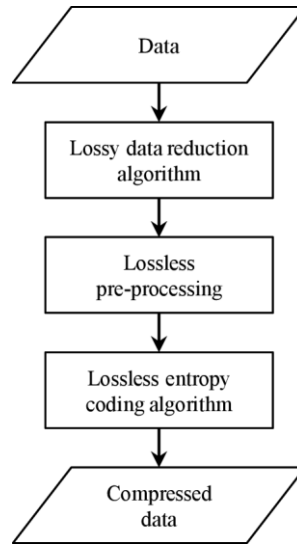
Figure 1: Compression chain showing the data reduction, preprocessing and lossless coding steps.

Input:

$\{s_i\}_{i=0}^n$ input sequence of samples

Output:

$\{\tilde{s}_i\}_{i=0}^n$ output sequence of quantized samples

Parameter:

nsd number of significant digits preserved in each sample

Algorithm:

For each input sample s_i in $\{s_i\}_{i=0}^n$:

1. Get binary exponent e_i and mantissa m_i of value s_i according to Eq. (7)
2. Tabulate value v for $\log_{10}(m_i)$
3. Compute the approximated number of digits before the decimal separator in sample value s_i following Eq. (8)
4. Compute quantization factor power p_i following Eq. (6)
5. Compute quantization factor q_i as in Eq. (5)
6. Compute quantized value $\tilde{s}_i$ as in Eq. (1)

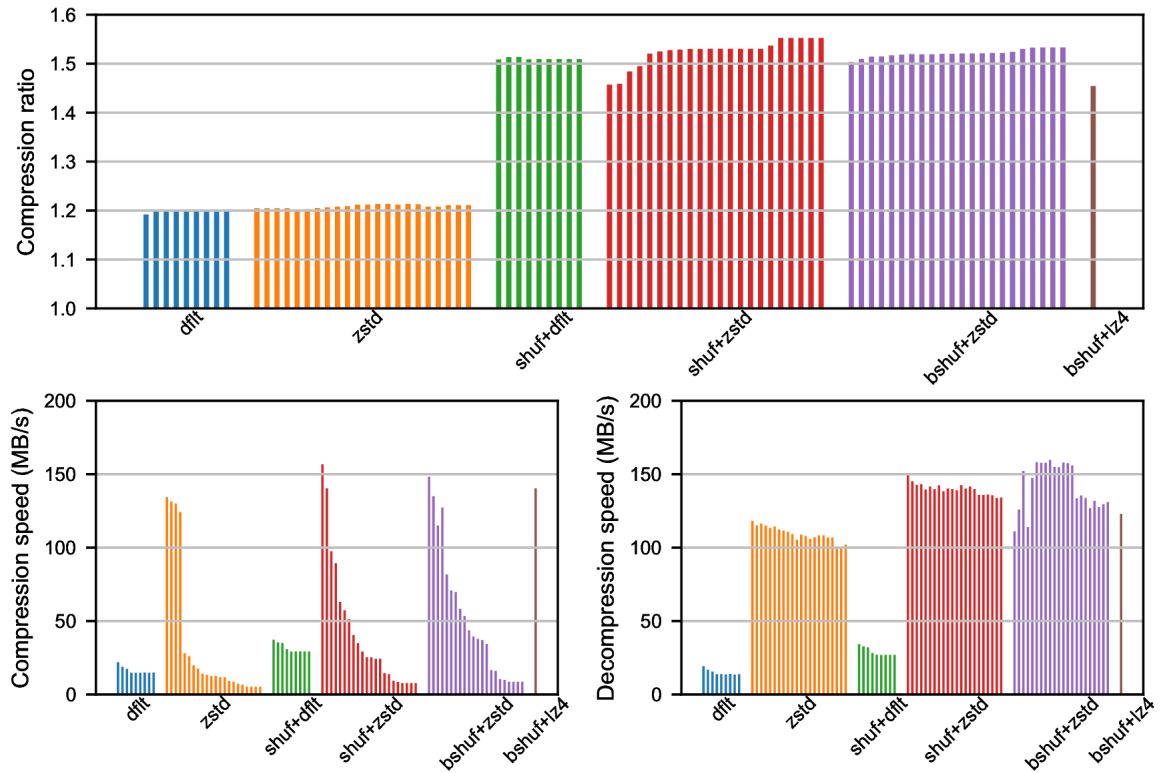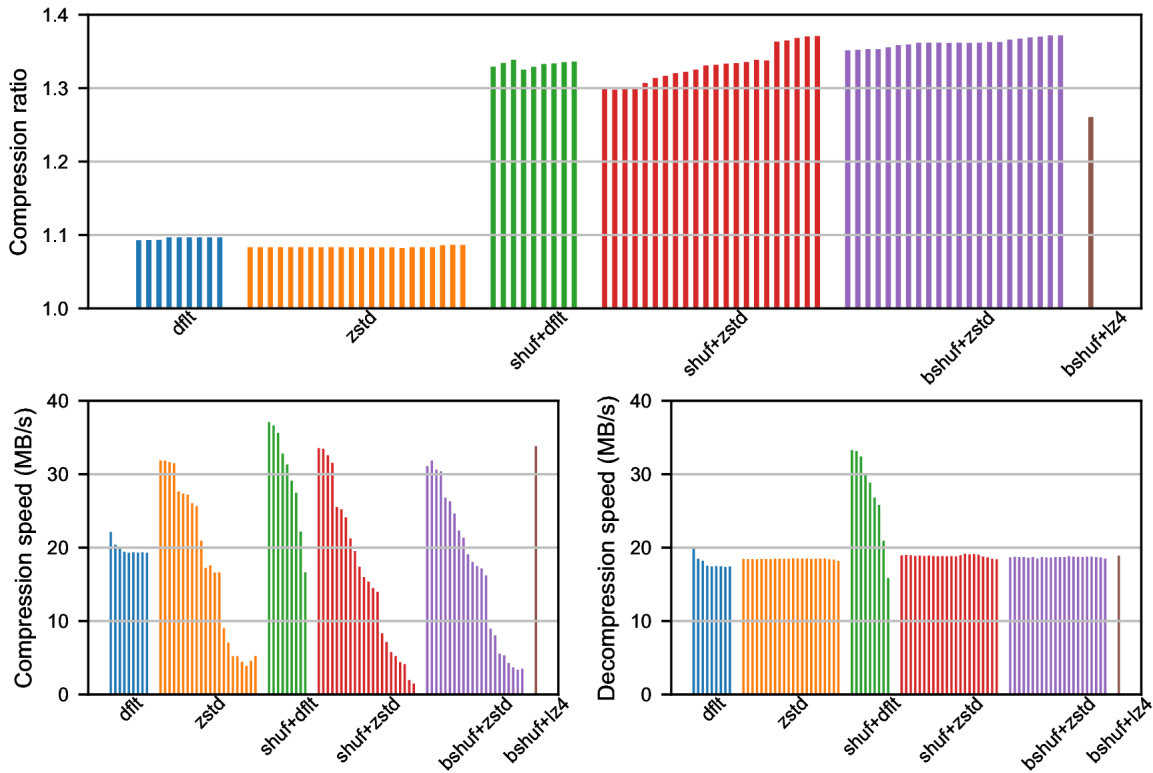
5   **Figure 2: The Digit Rounding algorithm.**

Figure 3: Results obtained for the lossless compression of the *s1* dataset with Deflate (dflt), Zstandard (zstd), Shuffle and Deflate (shuf+dflt), Shuffle and Zstandard (shuf+zstd), Bitshuffle and Zstandard (bshuf+zstd), Bitshuffle and LZ4 (bshuf+lz4). Compression ratios (top), compression speeds (bottom left), and decompression speeds (bottom right). Vertical bars represent the results for different compression levels: from 1 to 9 for Deflate, from 1 to 22 for Zstandard, only one level for LZ4**.**

Figure 4: Results obtained for the lossless compression of the *s3D* dataset with Deflate (dflt), Zstandard (zstd), Shuffle and Deflate (shuf+dflt), Shuffle and Zstandard (shuf+zstd), Bitshuffle and Zstandard (bshuf+zstd), Bitshuffle and LZ4 (bshuf+lz4). Compression ratios (top), compression speeds (bottom left), and decompression speeds (bottom right).

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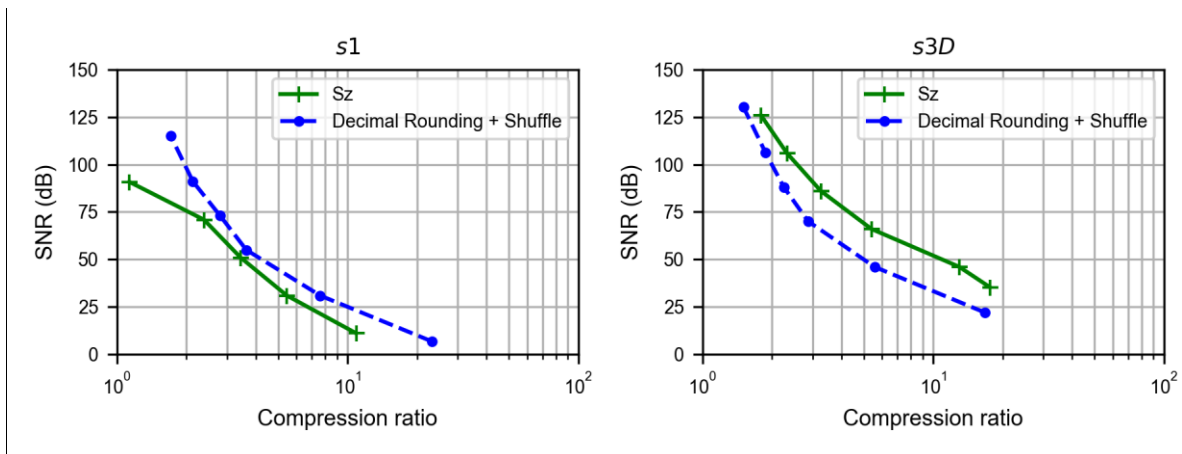
Figure 5: Comparison of the compression results (SNR vs. compression ratio) of the Sz and Decimal Rounding algorithms in absolute error-bounded compression mode, on the *s1* dataset (left) and *s3D* dataset (right).
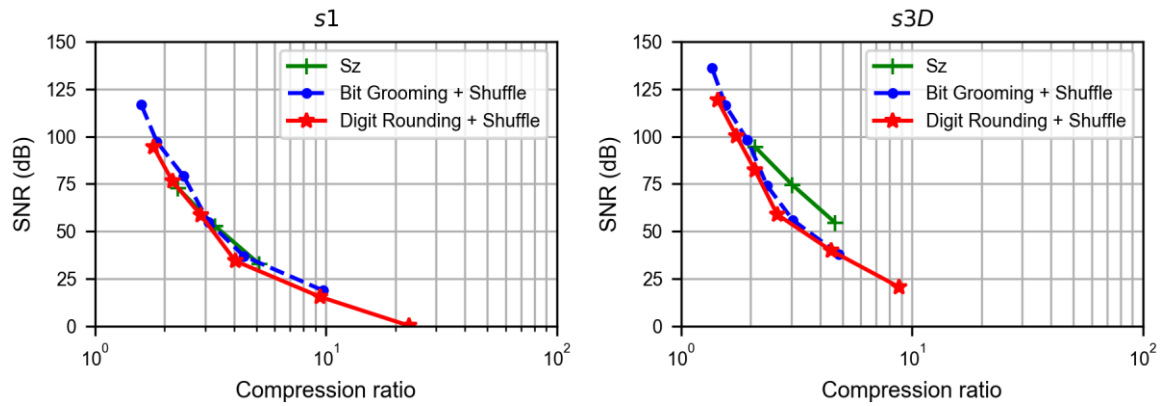
Figure 6: Comparison of the compression results (SNR vs. compression ratio) of the Sz, Bit Grooming and Digit Rounding algorithms in relative error-bounded compression mode, on the *s1* dataset (left) and *s3D* dataset (right).
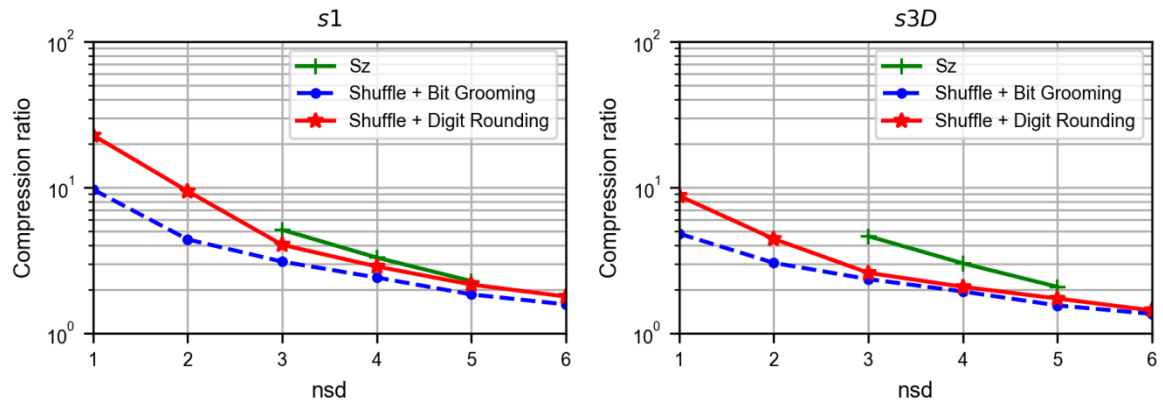

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Figure 7: Compression ratio as a function of the user-specified number of significant digits (*nsd*) for the Sz, Bit Grooming and Digit Rounding algorithms, on the *s1* dataset (left) and *s3D* dataset (right).