A generic pixel-to-point comparison for simulated large-scale ecosystem properties and ground-based observations: an example from the Amazon region

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Abstract. Comparing model output and observed data is an important step for assessing model performance and quality of simulation results. However, such comparisons are often hampered by differences in spatial scales between local point observations and large-scale simulations of grid-cells or pixels. In this study, we propose a generic approach for a pixel-to-point comparison that accounts for the uncertainty resulting from landscape variability and measurement errors in ecosystem variables, and provide statistical measures. The basic concept of our approach is to determine the statistical properties of small-scale (within-pixel) variability and observational errors, and to use this information to correct for their effect when large-scale area averages (pixel) are compared to small-scale point estimates. We demonstrate our approach by comparing simulated values of aboveground biomass, woody productivity (woody net primary productivity, NPP) and residence time of woody biomass from four dynamic global vegetation models (DGVMs) with measured inventory data from permanent plots in the Amazon rainforest, a region with the typical problem of low data availability, a scale mismatch and high model uncertainty. We find that the DGVMs under- and overestimate aboveground biomass by 25% and up to 60%, respectively.

Our comparison metrics provide a quantitative measure for model-data agreement and show moderate to good agreement with the region-wide spatial biomass pattern detected by plot observations. However, all four DGVMs overestimate woody productivity and underestimate residence time of woody biomass even when accounting for the large uncertainty range of the observational data. This is because DGVMs do not represent the relation between productivity and residence time of

5   woody biomass correctly. Thus, the DGVMs may simulate the correct large-scale patterns of biomass but for the wrong reasons. We conclude that more information about the underlying processes driving biomass distribution are necessary to improve DGVMs. Our approach provides robust statistical measures for any pixel-to-point comparison, which is applicable for evaluation of models and remote sensing products.

1 Introduction

10   The rate of environmental change in tropical South America and in particular in the Amazon region has been unprecedented in the last decades (e.g. Lewis *et al.* 2011; Davidson *et al.* 2012). Estimates of the amount of carbon stored in tropical rainforest biomass differ strongly (Avitabile et al., 2016;Baccini et al., 2012;Saatchi et al., 2011;Mitchard et al., 2014). In addition, estimated carbon release to the atmosphere from land-use change is uncertain (e.g. Houghton et al., 2012;Baccini et al., 2017;Song et al., 2015;Harris et al., 2012). Nonetheless, a successful implementation of protection incentives, e.g. for

15   reducing emissions from deforestation and degradation (REDD+), requires both accurate estimates of existing regional carbon stocks as well as improved projections of future scenarios (e.g. Langner et al., 2014).

Dynamic global vegetation models (DGVMs) are important tools to estimate impacts of climate and land-use change on the carbon cycle (e.g. Cramer *et al.* 2004; Sitch *et al.* 2008). To correctly capture carbon dynamics in tropical forests, DGVMs need to improve the simulation approach of drought-related mortality and other types of tree mortality that control stand

20   density (Pillet *et al.* 2018), and they need to incorporate how nutrient availability limits woody productivity (Quesada *et al.* 2012; Johnson *et al.* 2016). At the same time, model evaluation based on available data is necessary for which the primary source are ground-based observations of AGB obtained from forest census data (Lopez-Gonzalez et al. 2011; Brienen et al. 2014; Lopez-Gonzalez et al. 2014; Mitchard et al. 2014; Brienen et al. 2015; Johnson et al. 2016). When conducting data-model comparisons at the plot scale, the spatial resolution of both get into focus. The size of forest plots is typically in the

25   order of 1 ha or less, whereas average DGVM grid-cell resolution is determined by the available gridded climate data set, which is usually about several thousand square kilometers (>100,000 ha). Plot observations are affected by observational errors, uneven spatial distribution (Saatchi et al. 2015) and variability due to natural gap dynamics (Chambers *et al.* 2013), and thus are likely to exhibit substantial deviation from average large-scale properties. The problem of comparing point data with model results obtained at grid-cell (pixel) size occurs in many applications of remote sensing and ecological modelling.

30   So far, we lack a reliable and objective method to compare simulation results from DGVMs at grid-cell scale (pixel) and plot (point) observations. Several studies, that evaluated patterns of interpolated maps from plot data and model simulations, concluded that the observed and simulated spatial patterns do not match (e.g. Johnson *et al.* 2016). Here, we complement

these findings by providing quantitative statistical measures for such comparisons and present an approach for performing pixel-to-point comparisons while accounting for different statistical properties of point and pixel values and its uncertainties. The basic concept of the approach is to determine statistical properties from small-scale variability and observational errors in ecosystem variables, in order to account for these effects when comparing large-scale area averages (pixels) and small-

5   scale plot estimates (points).

We apply our approach by comparing point estimates of ecosystem properties obtained from forest inventories (Mitchard *et al.* 2014; Brienen *et al.* 2015) to corresponding simulated pixel values from four state-of-the-art DGVMs. Similar to Johnson et al. (2016), we focus on three ecosystem properties that are well defined and represented in both, DGVMs and forest inventories: (i) aboveground biomass (AGB, in Mg C ha^{-1}); (ii) aboveground woody productivity (WP, in Mg C ha^{-1} yr^{-1});

10   and (iii) residence time of woody biomass (τ in years).

We evaluate the accuracy of the spatial pattern of these three ecosystem properties and provide statistical measures for the quality of model simulations in comparison to observations, thereby accounting for small-scale landscape variability and associated measurement errors. We demonstrate the strength of our approach by highlighting its applicability for model evaluation and model benchmarking.

15   In particular, we address three research questions:

1)   How well do models represent variations in aboveground biomass across the Amazon region? We expand the pure (visual) qualitative comparison by deriving three statistical metrics for a quantitative comparison.

2)   How can we evaluate differences between observed and simulated spatial biomass patterns (based on the presented metrics), in particular when considering different allometric equations? We discuss the effects of inadequate data

20   and associated model uncertainty.

3)   What can we learn from the spatial heterogeneity and underlying drivers of spatial biomass patterns? We analyze simulated and observed patterns of WP and τ.

2 Methods

Landscape variability depends on the extent and resolution of the study area (Turner et al., 2001). Point measurements within

25   a pixel of larger spatial scale, for example, may reveal small-scale spatial variabilities within the pixel. We derive a "within-pixel variability" that so far has not been accounted for in earlier approaches. We present three steps to calculate three metrics that provide a measure on the best achievable correlation between point and pixel values (see Fig. 1).

2.1 A generic method for point-to-pixel comparisons

2.1.1 Calculate the "global variability" across the region of interest

Assume, we have a dataset X with a number N of point observations x_i at location i (e.g. plot observations from inventory data). In the first step, we calculate the mean $\bar{x}$ and variance σ_x^2 across all plots in a region (e.g. across the Amazon region).

5   The variance σ_x^2 denotes the global variability (i.e. the variability across the whole Amazon region) at point scale (Fig. 1a).

2.1.2 Calculate within-pixel variability

In the second step, we identify within-pixel variability from point measurements. With coarser pixel resolution, the spatial variability (here: global variability) is reduced. In order to compare pixel values against point values, global variability at point scale needs to be reduced by the within-pixel variability (variability component ε_i; Fig. 1b).

10   The variability component ε_i is assumed to be normally distributed with zero mean and variance σ_ε^2:

$$\varepsilon_i \sim \mathcal{N}(0, \sigma_\varepsilon^2) \tag{1}$$

Based on the variability component ε_i, we estimate the within-pixel variance σ_ε^2 from the point observations by analysing their covariance, which is equivalent to the nugget effect (i.e. the sum of variance caused by small-scale variability and observation error) in a semivariogram (see SI Methods). Due to the limited amount of inventory data, we assume here, that

15   σ_ε^2 is stationary across the region of interest (for details on that assumption see discussion and SI Results).

The global variance at point scale σ_x^2 now differs from the corrected global variance at pixel scale, $\sigma_{x,corr}^2$, as variances add quadratically, assuming that the (small scale) variability component ε_i has errors uncorrelated to the global distribution of x :

$$\sigma_{x,corr}^2 = \sigma_x^2 - \sigma_\varepsilon^2 \tag{2}$$

2.1.3 Metrics for the comparison of two datasets with different spatial resolutions

20   In a third step, we compare the point data x_i with simulated data y_i at pixel scale. Similar to the above procedure, we calculate the mean $\bar{y}$ and variance σ_y^2 for the simulated pixels that contain point observations (hereby we assign each point observation the pixel value in which the point is located). We then compare the simulation results by applying three metrics:

    1) Mean bias (MB): the ratio of means $\bar{y}/\bar{x}$ across the whole region as a measure of the mean bias in the patterns which is not affected by small scale variability;

25   2) Pattern amplitude (PA): the ratio of standard deviations $\sigma_y/\sigma_{x,corr}$ using the corrected global variability (i.e. removed within-pixel variability) and serves as a measure of differences in pattern amplitude or in the variability of the simulated and observed data;

    3) Similarity of pattern (SP): We use r_{corr} as a measure of the similarity of the 'shape' of spatial patterns, i.e. the spatial correlation of simulated and observed data (see SI). Accordingly, we can calculate the maximum achievable

correlation coefficient r_{max}, which is derived from correlating the observational data set at point scale to the same observational data set at pixel scale (see Fig. 1a, b and SI).

The limited number of point observations and their non-random spatial distribution in the Amazon region affects the accuracy of the comparison. We therefore estimate confidence intervals for the comparison metrics MB, PA and SP, respectively, by applying a bootstrapping technique (10,000 repetitions). Because the estimation of σ_ε^2 is based on the analysis of the spatial correlation structure of the data, a block-bootstrapping is performed (Politis and Romano, 1994). For each permutation, the domain of observations is randomly divided into 100 tiles (random orientation and offset, ca. pixel size) from which a random recombination is drawn with replacement. This technique assures that the spatial correlation structure of the data remains intact.

2.2 Application of the pixel-to-point comparison to simulated and observed data from the Amazon region

2.2.1 Observed data at point scale: Description of site-level data

We use forest census-based datasets of AGB (Lopez-Gonzalez et al., 2011;Lopez-Gonzalez et al., 2014;Mitchard et al., 2014), WP and woody loss (WL; Brienen et al., 2014), and convert it from dry biomass to carbon mass (see SI Methods). For the calculation of AGB, we use different allometric equations that account e.g. for regional differences in wood density or tree height (Table S1).

2.2.2 Simulated data at pixel scale: Description of DGVM simulations

We use outputs from four state-of-the-art DGVMs, namely the Lund-Potsdam-Jena DGVM for managed Land (LPJmL, Bondeau et al., 2007;Gerten et al., 2004;Sitch et al., 2003), the Joint U.K. Land Environment Simulator (JULES), v. 2.1. (Best et al., 2011;Clark et al., 2011), the INtegrated model of LAND surface processes (INLAND) model (a development of the IBIS model, Kucharik et al., 2000) and the Organising Carbon and Hydrology In Dynamic EcosystEms (ORCHIDEE) model (Krinner et al., 2005). A short description of each of the applied models is provided in the Supplementary Information (SI Methods). The models were applied to the Amazon region covering the area of 88°W to 34°W and 13°N to 25°S at a spatial resolution of 1°x 1° lat/lon. Model runs were performed based on the standardized Moore Foundation Andes-Amazon Initiative (AAI) modelling protocol (Zhang et al., 2015). The same set of models and output variables was analysed in Johnson et al. (2016).

2.2.3 Comparing inventory and simulation results

In our application, data set X corresponds to the inventory measurements at point scale (Fig. 1a). For this dataset, we have to derive the within-pixel variability (Fig. 1b). Data set Y corresponds to the simulated pixel values (Fig. 1c). Hence, the pixel scale is defined by the resolution of the model simulation (1°x1°, approximately 12,200 km², Fig. 1c). We calculate the three metrics (sect. 1.3) from the observed and simulated ecosystem variables AGB, WP and τ.

3 Results

3.1 Comparison of aboveground biomass (AGB)

The visual comparison indicates that the spatial pattern of AGB from the plots (Fig. 2a and Fig. S1) differs from the spatial patterns of AGB simulated by either DGVM (Fig. 2c-f). In addition, the DGVM patterns are vastly different among each
5 other.

Mean $\bar{x}$ and global variability σ_x of AGB for all plot observations across the Amazon region (Fig. 3a) range from 134-153 and 36-50 MgC ha^{-1}, respectively (Tab. S2), depending on the allometric equation applied. Within-pixel variability σ_ε, as calculated from Eq. S1, ranges between 28 and 36 MgC ha^{-1}. The corrected variability of observed AGB at pixel-scale ($\sigma_{x,corr}$) is thus substantially lower than the global variability and ranges between 22-39 MgC ha^{-1} (Fig. 4a, Tab. S2). Based
10 on these estimates we calculate the maximum achievable coefficients r_{max} for a comparison between pixel averages and point estimates of 0.61 to 0.78 for different allometric models (Fig. 5).

The models simulate a continuous cover of biomass across the Amazon region at a spatial resolution of 1°x1° pixel size. For our comparison, we only use the simulated pixel values of AGB at each plot location. Thus, the estimated statistical properties are not representative for the entire Amazon region but only for a relatively small subset of pixels (i.e. 98 pixels as
15 in Fig. 2a/b). For simulated AGB from the four DGVMs, we estimate a mean $\bar{y}$ of 114 MgC ha^{-1} for INLAND, 151 MgC ha^{-1} for JULES, 217 MgC ha^{-1} for ORCHIDEE and 170 MgC ha^{-1} for LPJmL (Fig. 3a, Tab. S3). Depending on the allometric equation applied to calculate observed biomass (Tab. S1), INLAND underestimates mean AGB by 15-25%. LPJmL and ORCHIDEE overestimate AGB by 11-26 and 42-62%, respectively. JULES deviates only by 1% from AGB derived from the 2-parameter allometric equations (kdr2p, kd2p), but overestimates AGB derived from all 3-parameter allometric
20 equations by 12% (Tab. S3).

Mean global variability of simulated AGB, σ_y, ranges between 13 MgC ha^{-1} for JULES and 62 MgC ha^{-1} for ORCHIDEE (Fig. 4a and Tab. S3). Without correcting for small-scale variability σ_ε in the point-to-pixel comparison, we would conclude that the pattern amplitude simulated by ORCHIDEE and LPJmL agree quite well with observed patterns (Fig. 4b). However, when accounting for the lower corrected variability ($\sigma_{x,corr}$), because the error of observation-based estimates at pixel-level
25 is smaller, it becomes easier to falsify models with uncertain data. We find that LPJmL and ORCHIDEE both overestimate the observed spatial amplitude by 43% and 62%, respectively (Fig. 4c and see Tab. S3 for other allometric models). For INLAND and JULES, on the other hand, we find a corresponding underestimation of pattern amplitude by 14 and 65%, respectively. We also note that confidence intervals for $\sigma_y/\sigma_{x,corr}$ are large in particular for ORCHIDEE and LPJmL (Fig. 4c).

30 Correlation coefficients indicating the similarity of simulated and observed patterns of AGB range from 0.25 - 0.53 (corrected) across all models (Tab. S3). The highest similarity of pattern (i.e. best correlation values r_{corr}) is found for ORCHIDEE, lowest similarity of pattern for LPJmL. Across the three models INLAND, JULES and LPJmL, generally,

higher similarity of pattern is found for the allometric models that include regional height models and mean or species specific wood density (Kdhr, Kdh; Fig. 5).

3.2 Comparison of woody productivity (WP)

Mean $\bar{x}$ and variability at pixel-scale $\sigma_{x,corr}$ of observed WP are 2.57 and 0.38 Mg C ha^{-1} yr^{-1}, respectively. There seems to
5 be a weak spatial pattern in the plot estimates at pixel level (Fig. 6a), which is not reflected by the models (Fig. 6c-f). The DGVMs display a distinct pattern of WP across the region that strongly differs among the four models (Fig. 6c-f).

Mean WP simulated by the DGVMs ($\bar{y}$) is between 4-5 Mg C ha^{-1} yr^{-1} for LPJmL and JULES, and 8-9 Mg C ha^{-1} yr^{-1} for INLAND and ORCHIDEE, respectively (Tab. S4). All DGVMs strongly overestimate mean WP (Tab. 1A). In addition, most models overestimate the pattern amplitude, and the simulated variability ranges between 0.72 and 1.6 Mg C ha^{-1} yr^{-1}
10 (Tab. S4). Pattern similarity of observed and simulated data is low ranging from 0.03 to 0.50 (Tab.1A), even with a relatively low maximum achievable correlation of 0.65 (Tab. 1A).

3.3 Comparison of residence time of woody biomass (τ)

Mean $\bar{x}$ and variability at pixel-scale $\sigma_{x,corr}$ of observed τ are 74 and 28 years, respectively. Again the visual comparison shows that the simulations do not match the observations (Fig. 7a vs. Fig. 7c-f). The simulated mean $\bar{y}$ of τ ranges between
15 15 (INLAND) to 35 (LPJmL) years with a variability of 3 (INLAND) to 8 (LPJmL) years. This is displayed in our comparison metrics: Mean bias results in very low values (i.e. strong underestimation of 53 to 80%; Tab. 1B) and pattern amplitude is strongly underestimated by 65 to 87% (Tab. 1B). The similarity of pattern is very low for all models (Tab. 1B).

4 Discussion

We here present a novel approach for a pixel-to-point comparison. We account for the reduced observed variability when
20 going from point to pixel scale by evaluating three indicators, i.e. the mean bias, the pattern amplitude and the similarity of spatial pattern (section 1.3). We use an example from the Amazon region by comparing model output from four DGVMs and forest inventory data. In the following, we discuss our findings of substantial discrepancies between simulated and observed patterns of AGB, WP and τ across the Amazon region.

4.1 How well do model simulations represent observed biomass patterns across the Amazon?

25 Interpolated biomass maps from plot observations (e.g. Johnson et al., 2016;Malhi et al., 2006) should be treated with caution since plot observations may not be representative at the landscape-scale (Chave et al., 2004). As a result, a direct and meaningful comparison of observed and simulated maps is currently not feasible but reliable biomass estimates are necessary for implementation of protection incentives and future projections of biomass development. Our results demonstrate that most models are in good agreement and deviate from mean observational biomass by less than 20% (i.e. low mean bias c.f.

Fig. 3) and their variability at landscape-scale deviates by about 40% (i.e. pattern amplitude, c.f. Fig. 4). Such relatively good agreement was also found in simulation runs from Delbart et al. (2010) and Johnson et al. (2016). Our results even yield relatively high similarity in observed and simulated spatial patterns of AGB at pixel scale (except LPJmL; c.f. Fig. 5), given the fact that the maximum achievable correlation in the data itself is only 0.6-0.8 (Fig. 5). However, while our

5 approach shows that some models could provide robust estimates for standing biomass stocks across the Amazon region (c.f. Fig. 2) it highlights that currently DGVMs do not represent productivity and related turnover correctly (i.e. the relation between productivity and residence time of woody biomass). As a result, the models might simulate the correct patterns for the wrong reasons as far as it can be derived from observational data. Ground observations suggest that forest structure, forest dynamics and species composition vary across the Amazon region, such that variations in geology and soil

10 fertility/mechanical properties coincide with region-wide variations in aboveground biomass, growth and stem mortality rates (Johnson et al., 2016;Quesada et al., 2012). In addition, disturbances with different sizes and frequency may be an important additional driver for such variations (Espírito-Santo et al., 2014;Rödig et al., 2017). It is necessary to consider such processes in DGVMs.

4.2 How to evaluate differences between observed and simulated patterns of biomass (based on the presented

15 **metrics), in particular when considering different allometric models?**

As discussed by several authors (e.g. Baker et al., 2004;Chave et al., 2006;Chave et al., 2014;Réjou-Méchain et al., 2017), the methodology used to convert plot measurements to actual biomass may lead to differential biomass estimates depending on the respective assumptions of the allometric equations employed (i.e. using species-level or mean wood density, and regional or continental height models, see SI Tab. S1). As a result, we here find a more or less pronounced pattern of

20 biomass variability across the Amazon region based on respective assumption used (c.f. Fig. 2). While mean global variability of biomass is highest for the allometric equations including species-level wood density (c.f. Figure S1, Table S2), highest within-pixel variability is found for biomass values estimated from two-parameter allometric equations (Tab. S2) excluding tree height (c.f. Table S1). This result is also reflected by the lower maximum achievable correlation coefficient (r_{max}), describing how observational data at point scale correlates with observational data at pixel scale, which is particularly

25 low for the two-parameter allometric equations (Fig. 5). Albeit the fact that three out of four DGVMs achieve a relatively good agreement between simulated and observed patterns at the pixel scale we find substantial uncertainty in the observational data due to spatial heterogeneity of local vegetation characteristics such as the structural and functional tree species composition that affects biomass estimates across the Amazon (see also Rödig et al. 2017). The uncertainty resulting from conversion of raw inventory measurements into biomass from measured allometries is generally neglected in model-

30 data comparisons. However, it strongly affects our pixel-to-point comparison metrics, thereby remaining an important bottleneck for good model-data biomass comparisons (see also Réjou-Méchain et al., 2017). A solution could be to compare modelled allometry with observational data.

4.3 What can we learn from including spatial heterogeneity and underlying drivers of biomass?

The four DGVMs applied in this study generally capture the observed pattern of AGB but strongly overestimate observed WP and underestimate τ, and, from a pixel perspective, do not show strong variability across the Amazon region, thereby not capturing observed gradients (c.f. Fig. 6 and Tab. 1). WP and τ are driving AGB and are calculated by different schemes in

5 the four DGVMs, e.g., regarding carbon allocation and drivers for mortality. Recent studies highlight that variation in stem mortality rates determines spatial variation in AGB and therefore conclude that mortality should be modeled on the basis of individual stems, due to the fact that stem-size distributions and stand density are important for predicting variation in aboveground biomass (Johnson et al., 2016;Rödig et al., 2017;Pillet et al., 2018). However, the mechanisms leading to stem mortality need to be implemented in models based on experimental data that are only recently becoming available (Meir et

10 al., 2015;Rowland et al., 2015). Overall, the DGVMs are able to reproduce the observed spatial pattern of AGB across the Amazon region, whereas for WP the model performance is less good and reproduction of the spatial pattern in mortality is generally very poor (Fig. 2, 6, 7). This suggests that models need to account for processes such as WP and mortality more mechanistically by including factors associated with resource limitation and disturbances regimes (see also Johnson et al. 2016). Recent efforts aiming at improving simulated Amazon forest biomass and productivity by including spatial variation

15 in biophysical parameters (such as τ and Vcmax) have found that using single values for key parameters limits simulation accuracy (Castanho et al., 2013). Thus, we conclude that a more mechanistic representation of the processes driving the spatial variability of carbon stocks and fluxes, forest structure and tree demographic dynamics is necessary to improve simulation accuracy (Rödig et al., 2018).

5 Future applications of the methodological approach and outlook

20 In general, we assume that the basic concept of our method is applicable to any comparison between two datasets that are characterized by differences in spatial scale. If the process that causes small-scale variability can be approximated as white noise, corrected statistics can be computed. Notwithstanding future developments of next generation DGVMs, the most relevant step of the presented approach is to account for the within-pixel variability σ_ε from the point data to allow for a comparison of observational and simulated data. Due to relatively sparse plot data availability, we assume here that σ_ε is

25 stationary across the Amazon region. To evaluate this assumption further, we have calculated a regional within-pixel variability σ_ε (Fig. S2) and find that it is in the range of the Amazon-wide σ_ε of 28 to 36 Mg C ha^{-1} (depending on the allometric equation used, see Tab. S2). Field studies show that forest dynamics vary locally, mostly due to variations in natural disturbance regimes, mortality and edaphic properties (e.g. Baker et al., 2004;Chambers et al., 2013;Chave et al., 2006;Malhi et al., 2006;John et al., 2007), which in turn strongly influences our calculated within-pixel variability and thus,

30 the metrics of the pixel-to-point comparison. Recent regional studies, that combine observational plot data and remote-sensing products from applications such as LIDAR (regions of Peru: Marvin et al. (2014), French Guyana: Fayad et al. (2016), Congo: Xu et al. (2017)), have already proven to detect spatial variability at high spatial resolution, which could be

used to calculate a pixel-wise within-pixel variability. Upcoming remote sensing missions as the Global Ecosystem Dynamics Investigation Lidar (GEDI), the ESA BIOMASS mission, the NASA-ISRO Synthetic Aperture Radar (NISAR) mission, or the proposed Tandem-L mission (Moreira et al., 2015) will have the potential to provide non-stationary values of within-pixel variability for all regions of the Amazon. Thus, it is desirable to include regionally or locally specific estimates

5 of σ_ε^2 in our analyses, which could be derived e.g. from above mentioned remote sensing data or from individual tree-based high-resolution simulations (e.g. Rödig et al., 2017). In any case, we conclude that upcoming model-data comparison studies should at least account for stationary within-pixel variability when comparing simulated spatial data to data from discrete observational networks.

6 Code and data availability

10 All models are described in more detail in the supplementary material. Model code is partly available from the respective modelling groups. Model output from the AMAZALERT project can be made available upon request. The permanent archive of the observational data from Mitchard et al. (2014) can be accessed at http://dx.doi.org/10.5521/FORESTPLOTS.NET/2014_1, see also Lopez-Gonzales et al. (2014). The inventory data from Brienen et al. (2015) are available at http://dx.doi.org/10.5521/ForestPlots.net/2014_4, see also Brienen et al. (2014).

7 Author contribution

15 AR and JH conceived the ideas and designed methodology, and contributed equally to the paper; AR, JH, ER, PP and CZ analysed the data; FL, KT, MG, CR, BC, GS performed simulation runs; all authors contributed to writing the paper.

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Figures
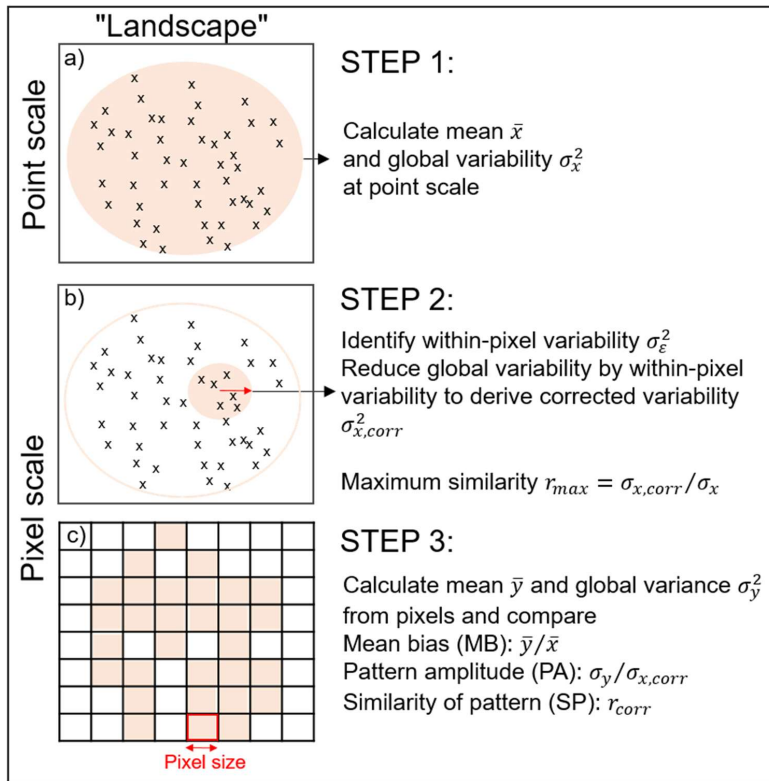
Figure 1: Schematic overview of the three steps in the pixel-to-point comparison. Note that we refer to "landscape" as the region of interest for which point and pixel data are available. A block bootstrapping with 10000 repetitions is performed to derive confidence intervals of the comparison metrics. The detailed set of equations to calculate maximum similarity, PA and SP can be found in the SI.
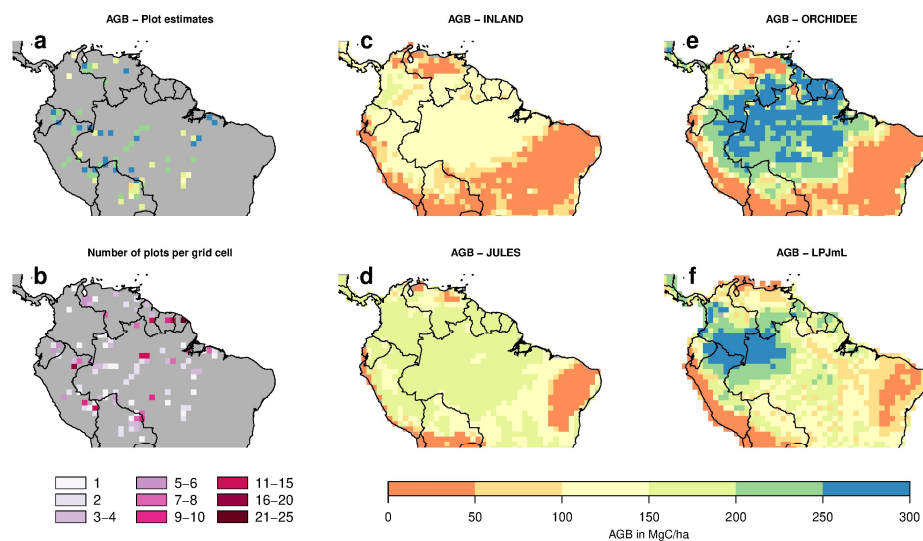
Figure 2. Estimates of aboveground biomass (AGB) from forest plots in 1° x 1° pixels. (a) Mean AGB per pixel derived from inventory data based on one allometric equation (Kdhr, see SI for explanation and other allometric equations). (b) Number of plots per pixel and (c-f) simulated AGB from four DGVMs.
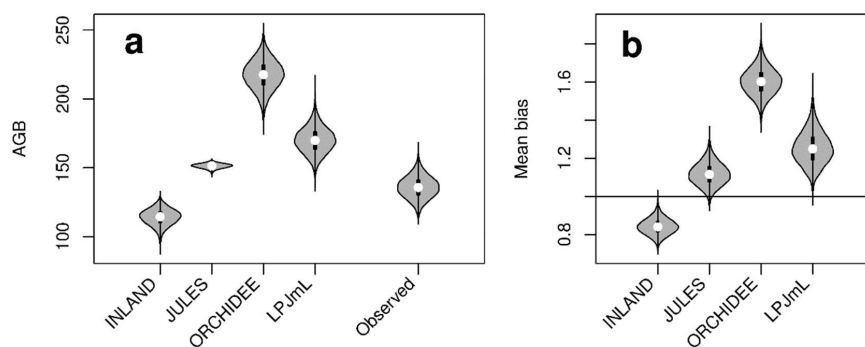
Figure 3. Distribution of aboveground biomass (AGB in MgC/ha) from the four DGVMs and from the observational plots (see also Table S2 and S3). The figure shows (a) the mean value (white dot) and distribution from bootstrapping of absolute AGB values from the four simulations and observed (grey violins). b) Mean bias as the ratio of mean simulated and mean observed AGB ($\overline{y}/\overline{x}$).
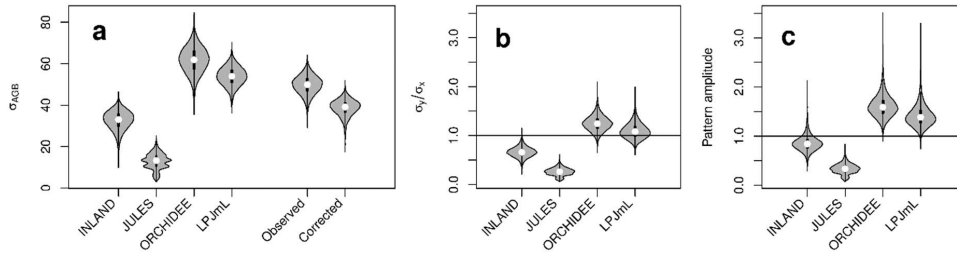
Figure 4: (a) Standard deviations of AGB (in MgC/ha) for the four models and observational data based on one allometric equation (see also Table S2, S3). For the observational data, the global variability at point scale ("observed") and the corrected variability at pixel scale ("corrected") is given; (b) ratio of standard deviations without correcting for within-pixel variability, (c)
5 **corrected metrics of pattern amplitude ($\sigma_y/\sigma_{x,corr}$).**
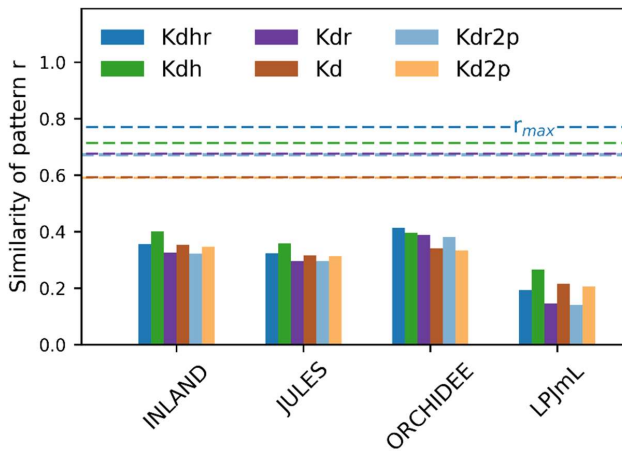
Figure 5: The similarity of the observed vs. simulated spatial pattern of AGB at pixel scale (as indicated by *r* given in bars). The similarity is calculated for different versions of observed AGB derived from six allometric models (indicated by the colors, see Tab.
10 **S1). The dashed line shows the maximum achievable correlation coefficients r_{max} from the observational data and for the different allometric models.**
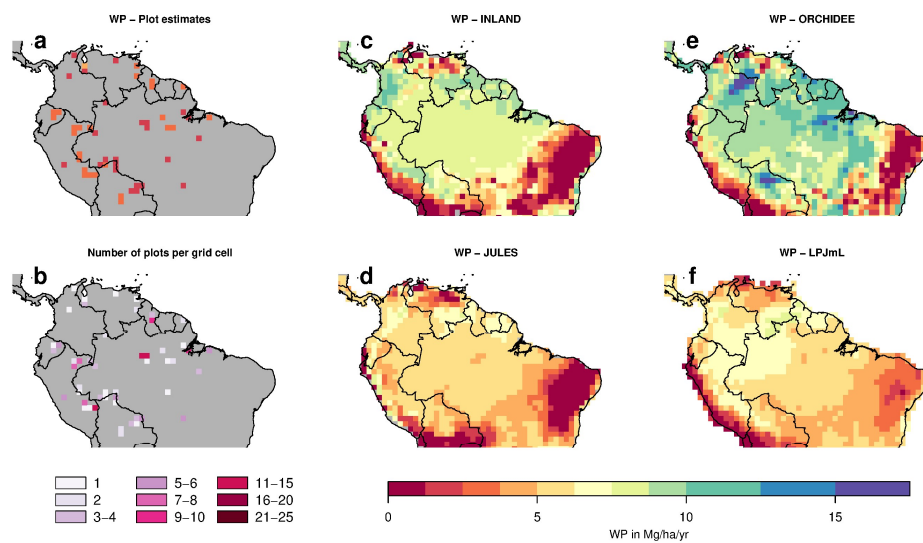
Figure 6. Estimates of aboveground woody productivity (WP) from forest plots in 1° x 1° pixels. (a) Mean WP from inventory plots. (b) Number of plots per pixel and (c-f) simulated WP from four DGVMs.
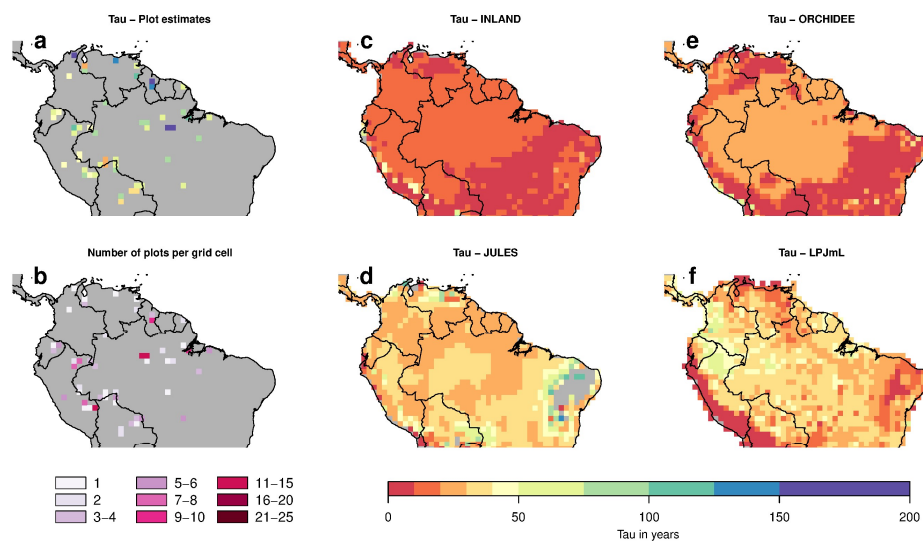
Figure 7. Estimates of woody biomass residence time (τ) from forest plots in 1° x 1° pixels. (b) Mean residence time from inventory plots. (b) Number of plots per pixel and (c-f) simulated τ from four DGVMs.

Tables

Table 1. Results of the point-to-pixel comparison for (A) woody productivity (WP) and (B) residence time of woody biomass (τ). In brackets, the 5% and 95% confidence intervals are given. Blue boxes indicate when models overestimate observed values, red boxes indicate underestimation.

A) Woody productivity (WP)	Mean $\bar{x}$ (Mg/ha/yr)	Corrected global variability $\sigma_{x,corr}$ (Mg/ha/yr)	Max. achievable correlation r_{max}
Observed	2.57	0.38	0.67
	Mean bias ($\bar{y}/\bar{x}$)	Pattern amplitude ($\sigma_y/\sigma_{x,corr}$)	Similarity of pattern (r_{corr})
INLAND	3.11 (2.91 – 3.31)	2.91 (1.75 – 4.83)	0.36 (0.11 – 0.35)
JULES	2.01 (1.88 – 2.14)	1.91 (1.08 – 3.25)	0.38 (0.07 – 0.37)
ORCHIDEE	3.55 (3.21 – 3.96)	4.26 (2.64 – 6.96)	0.03 (-0.25 – 0.01)
LPJmL	1.74 (1.63 – 1.83)	1.99 (1.36 – 3.16)	0.50 (0.27 – 0.50)
B) Residence time (τ)	$\bar{x}$ (years)	$\sigma_{x,corr}$ (years)	r_{max}
Observed	73.84	28.04	0.64
	Mean bias ($\bar{y}/\bar{x}$)	Pattern amplitude ($\sigma_y/\sigma_{x,corr}$)	Similarity of pattern (r_{corr})
INLAND	0.20 (0.17 – 0.24)	0.13 (0.06 – 0.25)	0.01 (-0.30 – 0.02)
JULES	0.42 (0.35 – 0.51)	0.24 (0.07 – 0.46)	-0.23 (-0.68 – -0.22)
ORCHIDEE	0.35 (0.29 – 0.42)	0.24 (0.12 – 0.45)	0.08 (-0.22 – 0.08)
LPJmL	0.47 (0.38 – 0.59)	0.35 (0.19 – 0.61)	-0.18 (-0.46 – -0.18)