



The Gravitational Process Path (GPP) model (v1.0) – a GIS-based simulation framework for gravitational processes

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Abstract. The Gravitational Process Path (GPP) model can be used to simulate the process path and run-out area of gravitational processes based on a digital terrain model (DTM). The tool combines several sub-models (process path, run-out length and material deposition) to simulate the movement of a mass point from an initiation site to the deposition area. For each sub-model several modeling approaches are provided, which makes the tool configurable for different processes like rockfall, debris flows or snow avalanches. The tool can be applied to large-coverage studies like natural hazard susceptibility mapping on a regional scale but also contains components for scenario based modeling of single events. Both the modeling approaches and precursor implementations of the tool have proven their practicability in numerous studies, including also geomorphological research questions like the delineation of sediment cascades or the study of process connectivity. This is the first completely rewritten open source implementation, extended and improved in many ways. The tool has been committed to the main repository of the System for Automated Geoscientific Analyses (SAGA) and thus will be available with every SAGA release.

1 Introduction

This paper introduces the Gravitational Process Path (GPP) model version 1.0, an attempt to provide a GIS-based modeling framework for the simulation of process path and run-out area of gravitational processes. It combines several modeling approaches in a single tool and simulates the movement of a mass point over a raster DTM (digital terrain model) from an initiation site to the deposition area. It concatenates several sub-models (process path, run-out, deposition), each with several modeling approaches, and is configurable for different processes like rockfall, debris flows or avalanches. Working on raster data sets, some of the modeling approaches had to be extended to work in 2.5D.

The GPP model includes stochastic (random walk, Markov chain, Monte Carlo simulation), physically based and empirical modeling approaches and provides the option of terrain modification by material deposition during operation. Although some of the approaches are rather simplistic, realistic results can be achieved with the great advantage of requiring only a few input parameters. This makes it possible to use the tool in large-coverage studies on a regional scale, but it also includes some components for scenario modeling of single events. Typical applications are natural hazard susceptibility mapping (e.g., Zimmermann et al., 1997; Heinimann et al., 1998; Wichmann and Becht, 2004; Wichmann and Becht, 2005; Mergili et al., 2015; Proske and Bauer, 2016) and geomorphological process studies, e.g. on sediment cascades or process connectivity (e.g.,



Wichmann, 2006; Wichmann et al., 2009; Haas et al., 2012a; Heckmann et al., 2012; Heckmann and Schwanghart, 2013; Heckmann et al., 2016).

The individual modeling approaches and model components have proven their applicability to different geomorphological processes and research questions in several studies. The single flow direction path finding approach of O'Callaghan and Mark (1984), also known as the D8 flow direction approach (Jenson and Domingue, 1988), has been used in various hydrological applications including the derivation of watershed basins and catchment area. Gamma (1996, 2000) introduced the dfwalk model for debris flow modeling, including a random walk approach for process path delineation of gravitational processes. The random-walk approach has been used by various authors for rockfall modeling (e.g., Wichmann and Becht, 2006; Haas et al., 2012b; Proske and Bauer, 2016), debris flow modeling (e.g., Zimmermann et al., 1997; Heinimann et al., 1998; Wichmann and Becht, 2004; Wichmann, 2006; Mergili et al., 2015) and avalanche modeling (e.g., Heckmann, 2006; Schmidtner, 2012).

Run-out distance calculation approaches based on the energy line principle (e.g., Heim, 1932; Hungr and Evans, 1988) have been used for various processes including rockfall (e.g., Heinimann et al., 1998; Dorren, 2003), debris flows (e.g., Zimmermann et al., 1997) and avalanches (e.g., Körner, 1980). The 1-parameter friction model of Scheidegger (1975) has been used for rockfall run-out calculations in several studies (e.g., van Dijke and van Westen, 1990; Meißl, 1998; Dorren and Seijmonsbergen, 2003; Wichmann and Becht, 2005; Wichmann, 2006; Haas et al., 2012b). The avalanche model of Voellmy (1955) and its derivatives, the VSG model (Salm et al., 1990) and the PCM model (Perla et al., 1980), have been applied for avalanche run-out modeling by e.g., Körner (1976), Hegg (1996) and Heckmann (2006). The PCM model has also been applied to model debris flows (Rickenmann, 1990; Zimmermann et al., 1997; Heinimann et al., 1998; Gamma, 2000; Wichmann, 2006; Mergili et al., 2012; Mergili et al., 2015) and large rock slides (e.g., Körner, 1976).

The GPP model is the first open source implementation based on our previous work, but it is completely reworked and enhanced in various aspects. It is implemented as a tool for the System for Automated Geoscientific Analyses (SAGA, Conrad et al., 2015) and is released as free open-source software (licensed under the GPL). The source code has been committed to the main repository of SAGA hosted at sourceforge.net (<https://sourceforge.net/projects/saga-gis/>), and binaries are available with every SAGA release.

2 General model structure

The GPP model works on a raster DTM. Initiation sites, usually derived by some kind of disposition modeling or (field) mapping, are organized in so called release areas, made up of one or more start cells. Generally, there are several model realizations computed from each start cell by calculating a user-defined number of model iterations (Monte Carlo simulation). Only the overlay of all iterations leads to the final model result, i.e. the complete process area, as every iteration will show a different result because of the stochastic components in the model. Additionally, the terrain might be modified by the deposition of material in each model iteration: there is a model component which handles natural or artificial sinks, and also some components to deposit material on process stop or along the process path. This allows the model to overcome sinks or to simulate the plugging of a channel.



Fig. 1 shows a basic setup, usually used for gravitational process path modeling on a regional scale. As this setup does not include the filling of sinks, a hydrologically sound DTM must be used. In each model iteration, a particle is initialized using information from its start cell. In a first step, one of the process path models is used to update the particle's path. In case there is no valid process path cell, and the path has reached the border of the DTM or a NoData cell, the particle does not move on and the next particle is initialized. If the next cell in the process path could be determined, one of the run-out models is used to update the speed of the particle, or, in case of an approach based on the energy line principle, the respective angle criterion is checked. In case the particle has stopped, the next particle is initialized. Otherwise, the next cell of the process path is determined.

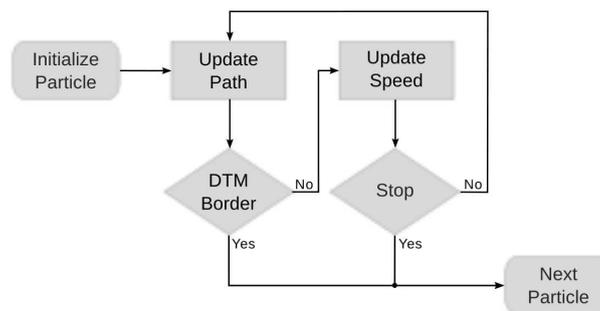


Figure 1. Flowchart of a basic GPP model configuration for modeling on a regional scale.

A model configuration including the filling of sinks is depicted in Fig. 2. This setup requires additional information on the material available per start cell. In case the process path has ended up in a sink, the amount of material available for the particle is checked. This amount of material is then used to fill up the process path upslope while preserving a downward slope, allowing the next particle to overcome the sink. In case the material available in an iteration is not enough or the sink is larger, several model iterations might be necessary to completely fill up the sink. After the attempt to fill the sink, the next particle is initialized.

Fig. 3 shows a fully featured setup of the GPP model, which is usually used for scenario modeling of a single (or some few) events. In this setup, material may be deposited when a particle stops, depending on the chosen deposition model and whether there is (still) material available for the particle. Then the next particle is initialized. In case the particle did not stop, it depends again on the chosen deposition model and the available material whether material is deposited along the process path or not. Then the next cell of the process path is determined. The deposition of material on stop or based on slope and velocity along the process path alters the terrain between successive model iterations.

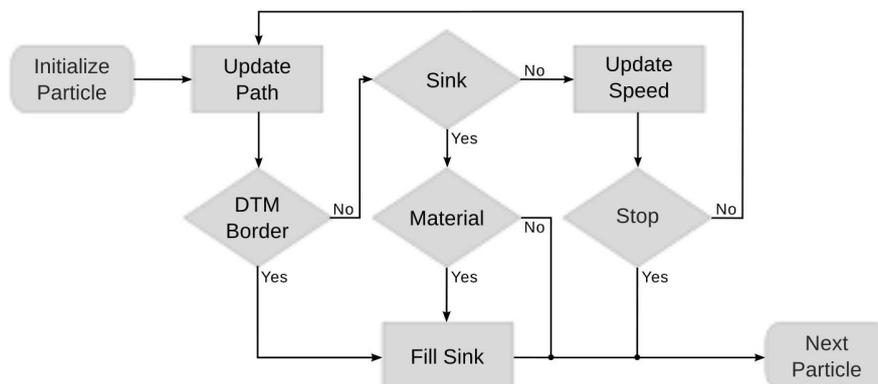


Figure 2. Flowchart of a GPP model configuration making use of the sink filling approach.

The sequence in which particles (start cells) are initialized depends on the chosen processing order. Three different ordering schemes are implemented:

10 (a) Release areas in sequence: the release areas are processed one by one; in each model iteration, all start cells of a release area are processed in ascending order of their elevation. This configuration computes all model iterations for the start cells of release area one, next for the start cells of release area two and so on.

(b) Release areas in sequence per iteration: the release areas are processed one by one in each model iteration; the start cells are processed in ascending order of their elevation. This configuration computes a single model iteration with the start cells
 15 of release area one, next with all start cells of release area two and so on; then the next model iteration is run over all release areas.

(c) Release areas in parallel per iteration: in each model iteration the start cells of all release areas are processed in ascending order of their elevation. With this configuration, all start cells are processed in each model iteration sorted by elevation, irrespective of their membership to a certain release area.

Depending on the overall configuration, the GPP model requires just a few or more parameters. These are either global parameters, used throughout the simulation, or (optionally) spatially distributed parameters provided as raster data sets. An example for the latter are spatially distributed friction values depending on factors like surface characteristics or water content.

3 Model components

5 Within the following sections, the currently implemented model approaches of each model component are described in detail. The user can choose which model should be used in each component and combine these selections to simulate various processes. Typical model configurations are presented in Sect. 4.

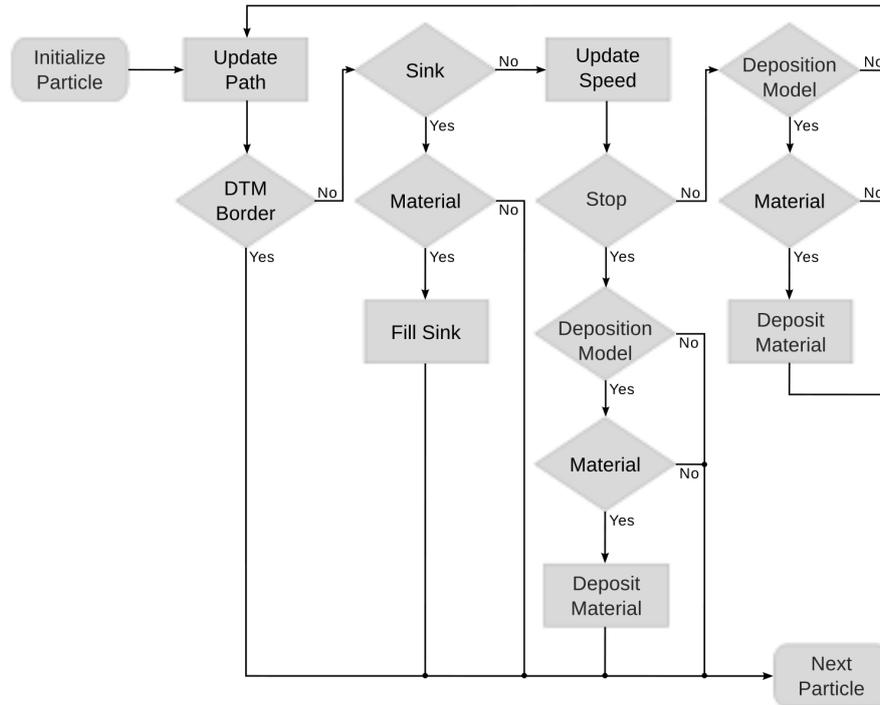


Figure 3. Flowchart of a fully featured GPP model configuration for scenario modeling.

3.1 Process path modeling approaches

The modeling of process pathways on a raster DTM has been a research topic since many years. The fact that each raster cell has only eight immediate neighbor cells results in problems to reconstruct the correct flow direction over longer distances. Basically there are two different kinds of methods, single and multiple flow direction algorithms, for which a lot of modeling approaches have been proposed. A simple (single flow direction) solution has been proposed by O’Callaghan and Mark (1984) which selects that neighbor cell as next flow path cell to which the steepest downward slope is observed. Multiple flow direction approaches (e.g., Freeman, 1991) usually distribute the accumulated water or material among all neighbor cells to which a downward slope is recognized. But most of these approaches have been developed for hydrological applications and are only of limited use in order to model gravitational processes: the amount of water is usually distributed in more or less the same proportions to the neighbors, irrespective of the local slope conditions. Therefore Gamma (1996, 2000) introduced the *mfd* approach (multiple flow directions for debris flows) which is sensitive to the local slope conditions.



3.1.1 Maximum slope

This approach, as proposed by O’Callaghan and Mark (1984), is implemented mainly for convenience in order to provide a
 10 simple means to detect the process path along the gradient of gravity. A particle follows the steepest descent of the slope:

$$n = \max\{(z - z_i)/d_i\} \quad (1)$$

where n is the neighbor of steepest descent, z is the elevation of the currently processed cell, z_i is the elevation of neighbor cell i , and d_i is the horizontal distance to neighbor cell i .

The model result is thus deterministic, with the exception of its behavior (as implemented in the GPP model) when two or
 15 more neighbor cells show the same steepest descent or when a flat area is reached. In the first case, one of the neighbors cells is chosen by random. On flat areas a set of potential neighbor cells is determined which is made up of all neighbors with the same elevation as the current cell which have not been traversed yet in the current model iteration. From this set, a process path cell is chosen by random. Together with the possibility that the terrain could be modified by sink filling or material deposition between two model iterations, this introduces a probabilistic component.

20 The *Maximum Slope* model approach has no special parameters besides those controlling the mode of operation of the GPP model main loop, like the number of model operations or the processing order. The pseudo-random number generator can be initialized either with the current time or a fixed seed value. The latter will always produce the same succession of values for a given seed value and will thus give the same results for consecutive tool runs.

3.1.2 Random walk

25 With this approach, the process path is modeled by a variant of the dfwalk model of Gamma (2000). The model can be adjusted to different geomorphological processes by three calibration parameters. For the currently processed grid cell, a set \mathbf{N} of potential flow path cells is determined from all immediate neighbor cells in a 3 by 3 window which have a lower elevation than the central cell. There are two parameters available – a slope threshold and a parameter controlling divergent flow – to further reduce this set. Possible flow path cells are determined by the *mfdf* criterion (Gamma, 2000; Wichmann and Becht, 2005):

$$\mathbf{N} = \left\{ n_i \mid \left\{ \begin{array}{ll} \gamma_i \geq (\gamma_{max})^a & \text{if } 0 < \gamma_{max} \leq 1 \\ \gamma_i = \gamma_{max} & \text{if } \gamma_{max} > 1 \end{array} \right. , \quad i \in \{1, 2, \dots, 8\}, \quad a \geq 1 \right\} \quad (2)$$

5 and

$$\gamma_i = \frac{\tan \beta_i}{\tan \beta_{thres}}, \quad \beta_i \geq 0, \quad i \in \{1, 2, \dots, 8\} \quad (3)$$

where γ_{max} is the $\max\{\gamma_i\}$, β_i is the slope to neighbor cell i , β_{thres} is a slope threshold and a is an exponent to control the amount of divergent flow. The slope threshold makes it possible to adjust the model to different relief: in steep sections of the



process path, where the terrain slope is near the threshold, only steep neighbors are allowed in addition to the steepest descent.

- 10 In flat sections, almost all lower neighbor cells are potential flow path cells and the tendency for divergent flow is increased. This is an important property which is missing the modeling approaches developed for hydrological processes. The degree of divergent flow can be controlled by parameter a .

From the final set \mathbf{N} , a cell is picked by random. The probability for each cell p_i is given by

$$p_i = \begin{cases} \frac{\tan \beta_i \cdot p}{\sum_j \tan \beta_j} & \text{if } i' \in \mathbf{N} \\ \frac{\tan \beta_i}{\sum_j \tan \beta_j} & \text{if } i' \notin \mathbf{N} \end{cases} \quad i, j \in \mathbf{N}, \quad p \geq 1 \quad (4)$$

- 15 where i' denotes the previous flow direction and p is a persistence factor (which is also contained in the computation of the sum if $i' \in \mathbf{N}$). A tendency towards the steepest descent is always achieved as the transition probabilities are weighted by slope. In case the previous flow direction i' is contained in the set \mathbf{N} , the persistence factor is used to give this direction a higher weight and thus a higher probability to get selected. This property (Markov Chain) can be used to reduce abrupt changes in flow direction. Finally the transition probabilities are scaled to accumulated values between 0 and 1, and the pseudo-random
 20 generator is used to select one flow path cell from the set.

In the GPP model, the approach is extended to also handle flat areas. This is done like described for the *Maximum Slope* approach with the same restriction that a potential successor cell must not have been traversed yet in the current model iteration in order to prevent endless loops.

- Besides the parameters controlling the Monte Carlo simulation like the number of iterations, the *Random Walk* approach
 25 has three parameters to calibrate the model in order to mimic the behavior of different geomorphological processes. The *mfd* criterion (Eq. (2)) controls below which terrain slope divergent flow is allowed. Multiple neighbors are only allowed in case the steepest local slope is lower than the slope threshold. This is accompanied by the exponent for divergent flow: below the slope threshold, the parameter controls the degree of divergence. Finally, the persistence factor can be used to achieve a greater fixation in the direction of movement (accounting for inertia) as may be the case for debris flows or wet snow avalanches.
 30 Rockfall may be modeled with (almost) no persistence and a higher degree of divergence.

- The result of several model iterations is a raster data set with encoded transition frequencies, i.e. how many times a grid cell has been traversed. Figure 4 shows the effect of different parameter settings for the three calibration parameters slope threshold, exponent for divergent flow and persistence factor. Here, the run-out length was calculated with the *Geometric Gradient* approach using an angle of 26.5° . The number of model iterations is set to 1000 in the examples (a) to (j). In Fig. 4 (a) to (e) the slope threshold (40°) and the persistence factor (1.0) are fixed, while the exponent for divergent flow is increased in several steps (1.0, 1.1, 1.2, 1.5, and 2.0). It is obvious that the extent of the process area increases significantly because of
 5 the higher degree of lateral spreading.

In Fig. 4 (f) to (j) the exponent for divergent flow (1.5) and the persistence factor (1.0) are fixed, while the slope threshold is increased gradually (15° , 20° , 30° , 40° , and 60°). It can be seen that the point at which lateral spreading is allowed is moving up the torrential fan, resulting in an increase of the total process area.

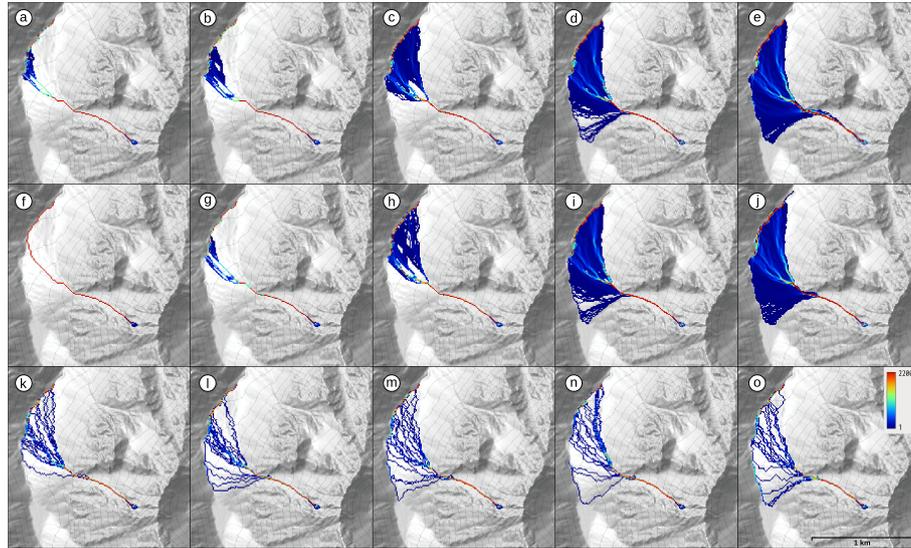


Figure 4. Effect of different random walk parameter settings; (a) to (e): different exponents for divergent flow (1.0, 1.1, 1.2, 1.5, and 2.0); (f) to (j): different slope thresholds (15°, 20°, 30°, 40°, and 60°); (k) to (o): different persistence factors (1.0, 1.5, 2.0, 2.5, and 3.0). For details see text.

Figure 4 (k) to (o) shows the results of a stepwise increase of the persistence factor (1.0, 1.5, 2.0, 2.5, and 3.0) while the slope threshold (40°) and the exponent of divergent flow (2.0) are fixed. Here, only a single iteration was calculated from each start cell in order to visualize single trajectories. It is obvious that with higher persistence factors the number of changes in direction along a trajectory is decreasing.

3.2 Run-out modeling approaches

In order to determine the run-out length of a particle, the GPP model implements various approaches. These range from rather simple but convenient approaches (regarding e.g., the comparison with field observations) based on the energy line principle to 1- and 2-parameter friction models.

5 3.2.1 Energy line approaches

The run-out length of a process is often described by the vertical and horizontal distances covered by a particle from its start to the stopping position:

$$\tan \alpha = dv/dh \tag{5}$$



where α is the angle to the horizontal and dv and dh are the vertical and horizontal offset, respectively. Both offsets can be
10 defined differently, see below. This describes a straight energy line from the start to the stopping position (Heim, 1932). With
a straight energy line, the velocity can be calculated by (Körner, 1980):

$$v_i = \sqrt{2 \cdot g \cdot h_v} \quad (6)$$

where v_i is the velocity [ms^{-1}] on the currently processed grid cell, g is the acceleration due to gravity [ms^{-2}] and h_v is
the height difference [m] between the energy line and the current grid cell i . Although the angle α is not constant, it can be
15 observed that it has a characteristic value range for gravitational movements of a specific type. The calibration of the angle α ,
which can be measured quite easily, is usually done by field observations and mapping. All approaches based on the energy
line principle provide the possibility to output raster data sets with encoded stopping positions and the maximum velocity
encountered in each cell of the process path.

3.2.2 Geometric gradient

20 The geometric gradient (Heim, 1932) defines the vertical offset as the vertical distance between the release area and the end
of the deposit. The horizontal offset is defined as the horizontal distance between these two points. This modeling approach
thus requires just the friction angle α as input. The GPP model supports both a global friction angle or a raster data set with
friction angles for each start cell. Once the angle between the start cell of the particle and the current position of the particle
drops below the friction angle α , the end of the deposit is reached.

25 3.2.3 Fahrboeschung

The Fahrboeschung principle (Heim, 1932) defines the vertical offset like the geometric gradient. But the horizontal offset is
not defined as the horizontal distance between start and end point but as the length of the horizontal projection of the actual
process path. Again, the friction angle can be provided either as a global value or by a raster data set with friction angles for
each start cell.

30 3.2.4 Shadow angle

Both the geometric gradient and the Fahrboeschung principle do not take into account that with rockfalls most of the initial
energy is dissipated once a rock impacts on the talus slope for the first time (Broilli, 1974; Dorren, 2003). Thus Hungr and
Evans (1988) proposed the shadow angle, which defines the vertical offset as the vertical distance between the first impact
location on the talus slope and the end of the deposit. The horizontal offset is defined as horizontal distance between the first
5 impact location and the end of the deposit. From this it follows that the shadow angle is always smaller than the geometric
gradient.

The shadow angle can again be provided either as a global value or by a raster data set with shadow angles for each start cell.
In order to determine the location of the first impact of a particle on the talus slope, the GPP model implements two different



approaches: (i) the user provides a raster data set with impact areas. Once a particle reaches a cell encoded as impact area,
10 the location of this cell is used to measure the shadow angle; (ii) a threshold describing the slope angle above which free fall
is assumed is provided. As soon as the angle between the start cell and the current position of the particle drops below the
threshold, the location of this cell is used to measure the shadow angle.

3.2.5 1-parameter friction model

The 1-parameter friction model has been developed to simulate rockfall and is based upon concepts introduced by Scheidegger
15 (1975), which have been extended by various authors (van Dijke and van Westen, 1990; Meißl, 1998; Dorren and Seijmonsber-
gen, 2003). The GPP model implements several of these approaches, more details can be found in Wichmann and Becht (2005)
and Wichmann (2006). The 1-parameter friction model calculates the velocity on the currently processed grid cell according
to the velocity on the previous cell of the process path, the slope and a friction parameter. Once the velocity becomes zero, the
end of the deposit is reached. Once a block is detached from the rock face, it is falling in free air:

$$20 \quad v_i = \sqrt{2 \cdot g \cdot h_f} \quad (7)$$

where v_i is the velocity [ms^{-1}] on the currently processed grid cell, g is the acceleration due to gravity [ms^{-2}] and h_f is
the height difference [m] between the start cell and the current grid cell i . The impact on the talus slope occurs, similar to the
shadow angle model, if (a) a particle reaches a cell encoded as impact area or (b) the angle between the start cell and the current
position of the particle drops below the free fall threshold. The decrease of velocity on the talus slope due to energy loss on the
25 first impact can be calculated in two different ways:

(i) energy reduction (Scheidegger, 1975):

$$v_i = \sqrt{2 \cdot g \cdot h_f \cdot K} \quad (8)$$

where K is the amount of unspent energy ($K \leq 1$, i.e. for an energy reduction of 75 % K is 0.25).

(ii) preserved component of velocity (Kirkby and Statham, 1975):

$$v_i = \sqrt{2 \cdot g \cdot h_f \cdot \sin \beta_i} \quad (9)$$

5 where β_i denotes the local slope gradient [$^\circ$]. Here, the component of the fall velocity parallel to the talus slope surface is
conserved.

Approach (i) requires the user to specify the amount of energy reduction in percent. With approach (ii) usually larger run-out
distances are modeled. The strong dependence of approach (ii) on the slope of the impact cell complicates the model calibration
(Wichmann, 2006). Approach (i) is used as the default in the GPP model. After the impact, two different modes of motion can
10 be modeled (Scheidegger, 1975):



(i) sliding:

$$v_i = \sqrt{v_{(i-1)}^2 + 2 \cdot g \cdot (h - \mu_s \cdot D)} \quad (10)$$

where $v_{(i-1)}$ is the velocity [ms^{-1}] on the previous grid cell of the process path, h is the height difference [m] between adjacent grid cells, D is the horizontal difference [m] between adjacent grid cells and μ_s is the sliding friction coefficient [-].

15 (ii) rolling:

$$v_i = \sqrt{v_{(i-1)}^2 + 10/7 \cdot g \cdot (h - \mu_r \cdot D)} \quad (11)$$

where μ_r is the rolling friction coefficient [-].

Once the velocity on a grid cell becomes zero, the end of the deposit is reached. The model calibration usually requires only two parameters: the amount of energy loss on impact [%] and the sliding/rolling friction coefficient [-]. The latter can be provided either as global value or spatially distributed by providing a raster data set with friction values. Impact on the talus slope can either be modeled by providing an input raster data set with impact areas or by using a slope threshold (see Sect. 3.2.4). Besides the possibility to output a raster data set with encoded stopping positions, a raster data set with the maximum velocity encountered in each cell of the process path can be output.

3.2.6 PCM model

25 The PCM model (Perla et al., 1980) is a 2-parameter friction model originally developed to calculate the run-out distance of avalanches. It is based on the model of Voellmy (1955). The model has also been applied to debris flows by various authors (Rickenmann, 1990; Zimmermann et al., 1997; Gamma, 2000; Wichmann, 2006). It is a center of mass model and it is assumed that the motion is mainly governed by a sliding friction coefficient μ and a mass-to-drag ratio M/D . In steeper parts of the process path, the velocity is mainly influenced by M/D , whereas the velocity in the run-out area is dominated by μ . The velocity on the currently processed grid cell depends on the velocity of the previous cell, the slope, the slope length and the

5 two friction coefficients:

$$v_i = \sqrt{\alpha_i \cdot (M/D)_i \cdot (1 - \exp^{\beta_i}) + (v_{(i-1)})^2 \cdot \exp^{\beta_i}} \quad (12)$$

and

$$\alpha_i = g (\sin \theta_i - \mu_i \cos \theta_i) \quad (13)$$

$$\beta_i = \frac{-2L_i}{(M/D)_i}$$

where v_i is the velocity [ms^{-1}] on the currently processed grid cell, g is the acceleration due to gravity [ms^{-2}], θ is the local slope [°], L is the slope length between adjacent grid cells [m], μ is the sliding friction coefficient [-], and M/D is the mass-



to-drag ratio [m]. Perla et al. (1980) assume the following velocity correction for $v_{(i-1)}$ before v_i is calculated in case of a concave transition in slope direction:

$$v_{(i-1)}^* = \begin{cases} v_{(i-1)} \cos(\theta_{(i-1)} - \theta_i) & \text{if } \theta_{(i-1)} \geq \theta_i \\ v_{(i-1)} & \text{if } \theta_{(i-1)} < \theta_i \end{cases} \quad (14)$$

The correction is based on the conservation of linear momentum and has a higher magnitude in case of abrupt transitions.

15 The accurate stopping position on a grid cell may be calculated by:

$$s = \frac{(M/D)_i}{2} \ln \left(1 - \frac{(v_{(i-1)})^2}{\alpha_i (M/D)_i} \right) \quad (15)$$

where s is the length [m] of the process path segment on the grid cell. In the GGP model, s is not calculated and the process stops as soon as the square root in Eq. 12 becomes undefined. Thus the raster cell size determines the precision of the stopping position, which is a reasonable compromise for a grid based model.

20 Gamma (2000) proposed to incorporate the velocity correction (Eq. 14) directly into the velocity calculation (Eq. 12):

$$v_i = \sqrt{\alpha_i \cdot (M/D)_i \cdot (1 - \exp^{\beta_i}) + (v_{(i-1)})^2 \cdot \exp^{\beta_i} \cdot \cos(\Delta\theta_i)} \quad (16)$$

and

$$\Delta\theta_i = \begin{cases} \theta_{(i-1)} - \theta_i & \text{if } \theta_{(i-1)} > \theta_i \\ 0 & \text{if } \theta_{(i-1)} \leq \theta_i \end{cases} \quad (17)$$

Equation (16) is also implemented in the GPP model. The model has to be calibrated by the friction parameters μ and M/D .

25 In order to overcome the problem of mathematical redundancy – various combinations of the two parameters can result in the same run-out distance – the parameter M/D is usually taken to be constant along the process path. It is only calibrated once in order to obtain realistic maximum velocity ranges for a given process. Both friction parameters can be provided either as a global value or spatially distributed by a raster data set. In the GPP model implementation it is also required to provide an initial velocity [ms^{-1}] in order to avoid that the process already stops on the first grid cell along the process path. As with the 1-parameter friction model, it is possible to output raster data sets with encoded stopping positions and maximum velocities.

5 3.3 Deposition modeling approaches

The GPP model implements various deposition modeling approaches. In order to use these approaches, an input raster data set with material heights per start cell is required. This total material height is then averaged by the number of iterations to calculate the material height available for a particle in each iteration. Material that has not been spent in an iteration is made



available for the remaining iterations. Deposited material immediately alters the terrain and the next iteration is computed on
10 the modified DTM.

The most important deposition approach is the filling of sinks, which allows the GPP model to overcome small depressions or even larger obstacles like retention basins. Others simply deposit material once a particle stops or allow deposition along the process path based on slope and/or velocity thresholds. The latter can be used to model scenarios like channel plugging.

3.3.1 Sink filling

15 The sink filling approach is immediately activated once a raster data set with material heights per start cell is provided as input. As soon as a sink is detected, the particle stops and material is deposited. The deposition is done preserving a downward slope if procurable, avoiding to create new sinks and making it possible to overcome the obstacle in subsequent model iterations.

The sink filling approach is based on Gamma (2000) with slight modifications: (i) the overflow cell and the depth of the sink are determined; (ii) if the depth of the sink can not be filled with the material available for the current model iteration,
20 all material available is deposited and the computation stops; (iii) the sink is filled up to the height which is preserving a user specified minimum slope to the overflow cell; (iv) in order to avoid the creation of another sink, material is deposited on the process path above the sink; therefore it is tested if the material left over is enough to fill up the process path above the sink while preserving the minimum slope; in case the available material is not enough to preserve this slope, the angle is continuously decreased until a minimal downward slope can be preserved. In case material is left over, it is made available for
25 the subsequent iterations. Gamma (2000) did not use a user specified minimum slope to preserve, but determined the average slope along the process path above the sink for the last 50 meters. For us this turned out to be too dependent on the local slope conditions, often resulting in large angles and thus using too much material which is then missing to fill the sink upwards.

3.3.2 On stop

This approach simply deposits material on the grid cell of the modeled stopping position. The amount of material deposited
30 on this cell is controlled by the *Initial Deposition on Stop* parameter, which describes the percentage of the available material which is deposited at the stopping position. The rest of the material is used to fill up the process path above the stopping position. The angle used to do this while preserving a downward slope is determined in a way that all material left over in this iteration is used.

The approach makes it possible to adjust the deposition behavior to different geomorphological processes: simulating a rock fall event, the *Initial Deposition on Stop* parameter can be set to 100 %, simulating the deposition of single rocks. With debris
5 flows or snow avalanches, it can be set lower in order to archive a more lobe like deposition pattern. Nevertheless, the approach is not intended to realistically simulate the deposition pattern. But it can be used for scenario modeling, forcing the process path into different directions in subsequent model iterations.



3.3.3 Slope / velocity based

The *On Stop* deposition approach can be extended by slope and/or velocity based components, which can be used to force the deposition of material along the process path. Such components have been proposed by Gamma (2000) and are used in a modified way in the GPP model. Again, this approach is most useful for scenario modeling in order to simulate debris jamming or channel plugging. It is also useful if a high resolution DTM with great detail is used. The deposition starts once the slope or the velocity drops below a specific threshold. At a slope or velocity of zero, the *Maximum Deposition along Path* parameter controls how many percent of the material available in this model iteration is deposited. At the slope/velocity threshold the percentage of material deposition is zero which results in a linear relation.

The slope and velocity based approaches can be used separately or in combination. In the latter case, a deposition height is calculated with both approaches and the lower deposition height is applied. This reduces artifacts resulting from the usage of a single threshold. For example, on flat areas, no material is deposited as long as the velocity is still high.

The slope/velocity based approaches have a further parameter, the *Minimum Path Length*, which describes the distance along the process path that must be exceeded before deposition sets in. This is required to simulate the behavior of a volume (and not single particles) and to prevent the deposition of material shortly after the process has initiated or even within the release area itself. It is also useful to have more control on the position along the process path where deposition should set in, especially in case of cascades with alternating steeper and gently dipping slope profile sections.

3.4 Model input and output

This section provides a brief summary on the GPP model parameters, input, and output data sets. Table A1 shows the process path model parameters, grouped by model. The run-out parameters are shown in Table A2 and the deposition parameters in Table A3. Some of the parameters are global parameters, others can be provided as raster data sets in order to use spatially distributed parameter values. The input and output data sets are summarized in Table A4.

4 Model configurations and application examples

Use cases of the GPP model on a regional scale are natural hazard susceptibility mapping and the derivation of geomorphological process areas and sediment cascades. It is possible to simulate different scenarios based upon e.g., process magnitude, the existence of protection forest or protection measures. The inclusion of the deposition model component is usually only done on a more local scale. The modeling approaches available for each model component make it possible to simulate different gravitational processes depending on the overall model configuration. Within the following sections typical model configurations and parameter settings are described for rockfall, debris flow and avalanche modeling. Run-out calculations using one of the approaches based on the energy line principle have been used for all three process types, but as they are straight forward to use they are not discussed in detail. A separate section provides further information on scenario modeling. It must be noted that the parameter ranges provided for each process have to be considered as approximate values only and are thought to provide



an initial guess. For example, Wichmann et al. (2008) have shown that for debris flow modeling the random walk and friction model parameters decrease with lower DTM resolutions.

10 4.1 Rockfall

A typical model configuration for rockfall modeling on a regional scale, e.g., to create susceptibility maps, combines the modeling approaches shown in Table 1. Usually the *Random Walk* approach is used to determine the process path, using rather permissive parameter settings regarding lateral spreading. The slope threshold is set rather high, usually in conformance with the threshold for free fall, in order to permit changes in direction already with the first impact on the talus slope. The exponent of divergence is comparatively high, too, in contrast to a rather small persistence factor which mimics the fact that rocks often change direction on impact.

Table 1. Model configuration for rockfall modeling on a regional scale and approximate parameter ranges (compiled from Wichmann, 2006; Wichmann and Becht, 2006; Proske and Bauer, 2016).

Model component	Model approach	Parameter	Value range
Process path	Random walk	slope threshold	55–65°
		exponent of divergence	1.5–2.0
		persistence factor	1.0–1.6
Run-out	1-parameter friction model	threshold free fall	55–65°
		energy reduction	70–75 %
		mu	0.35–2.5, spatially distributed
		mode of motion	sliding

The threshold of free fall used in the *1-parameter friction model* depends on the DTM resolution, but should conform with the slope threshold of the *Random Walk* model. The energy reduction on impact is usually about 75 % as investigated by Broilli (1974). When the model is applied on a regional scale, the friction coefficient μ should be provided spatially distributed as raster data set. Table 2 shows sliding friction coefficients for different materials and land cover. Spatially distributed friction coefficients are also very useful for scenario modeling, e.g., in order to determine the consequences of protection forest removal or reforestation.

The model configuration thus requires the following raster data sets as input: a DTM, a raster with encoded release areas, and a raster with spatially distributed friction coefficients. Model outputs, describing the derived process area, are raster data sets with encoded transition frequencies, encountered maximum velocities and stopping positions.



Table 2. Coefficients of friction for different materials and land cover (compiled from van Dijke and van Westen, 1990; Dorren and Seijmonsbergen, 2003; Wichmann, 2006).

Material / land cover	Friction coefficients (μ)
Tills	0.35–0.5
Residual soils	0.4–0.5
Fluvial materials	0.4–0.5
Bare rock	0.4–0.9
Scree materials:	
- marl	0.35–0.45
- flysch	0.6–0.7
- sandstone	0.7–0.8
- dolomite	0.7–0.8
- limestone	0.8–0.9
Rockfall materials	0.9–1.0
Meadow	0.5–0.6
Alpine shrubs	0.6–0.9
Bushes	0.6–0.7
Open forest	1.0–2.0
Dense forest	> 2.0

5 4.2 Debris flows

A typical model configuration for debris flow modeling on a regional scale is shown in Table 3. Again, the *Random Walk* approach is used for path finding. The slope threshold is usually set to angles slightly above the slope of the torrential fan. The exponent of divergence depends on the size of the simulated events. The larger the event, the higher the exponent. Its value also depends on the grain size and water content, with lower values for flowslides and higher values for coarse-grained debris flows. The persistence factor is higher compared to rockfall as persistence is given in the case of debris flows.

Run-out distances are calculated on basis of the PCM model. The M/D drag ratio is usually calibrated once to match the highest observed velocities of a specific type of debris flow. The friction parameter μ is once again provided spatially distributed as a raster data set. Based on the observation that the sliding friction coefficient tends towards lower values with increasing catchment area, attributed to a changing rheology with higher discharges along the process path, Gamma (2000) derived the following estimating functions from debris flows in Switzerland:

$$\text{minimum run-out: } \mu = 0.25 \cdot a^{-0.21} \quad \text{likely run-out: } \mu = 0.19 \cdot a^{-0.24} \quad \text{maximum run-out: } \mu = 0.13 \cdot a^{-0.25}$$

with a = catchment area in km^2 . Such data sets can be easily computed from a raster with encoded catchment area (i.e. flow accumulation). Gamma (2000) and Wichmann and Becht (2005) additionally apply minimum (0.045) and maximum (0.3)



5 thresholds in order to exclude extreme values. The model configuration thus requires a DTM, a raster with encoded release areas, and a raster with spatially distributed friction coefficients as input. Model outputs, describing the derived process area, are again raster data sets with encoded transition frequencies, encountered maximum velocities and stopping positions.

Table 3. Model configuration for debris flow modeling on a regional scale and approximate parameter ranges (compiled from Zimmermann et al., 1997; Gamma, 2000; Wichmann and Becht, 2005; Wichmann, 2006).

Model component	Model approach	Parameter	Value range
Process path	Random walk	slope threshold	20–40°
		exponent of divergence	1.3–3.0
		persistence factor	1.5–2.0
Run-out	PCM model	mu	0.04–0.8, spatially distributed
		M/D ratio	20–150

4.3 Avalanches

10 The model configuration for avalanche modeling on a regional scale resembles that for debris flow modeling, but the parameter variability is higher because of the different properties of powder and wet snow avalanches (see Table 4). All *Random Walk* parameters usually require higher values in order to be able to reproduce the extent of the process area. The friction parameter μ is lower for larger events, and the lower the snow density is, with powder avalanches showing the lowest values. The M/D ratio is usually higher with larger (and powder) avalanches, resulting in higher maximum velocities. Both friction parameters can be provided spatially distributed. For example, Heckmann (2006) used spatially distributed M/D values based on vegetation cover as substitute for surface roughness.

Table 4. Model configuration for avalanche modeling on a regional scale and approximate parameter ranges (compiled from Perla et al., 1980; Salm et al., 1990; Hegg, 1996; Heckmann, 2006; Schmidtner, 2012).

Model component	Model approach	Parameter	Value range
Process path	Random walk	slope threshold	45–60°
		exponent of divergence	1.3–5.0
		persistence factor	1.5–3.0
Run-out	PCM model	mu	0.1–0.5, spatially distributed
		M/D ratio	20–1000, spatially distributed



4.4 Scenario modeling

5 Scenario modeling usually addresses topics like process magnitude, the impact of protection forest or protection measures. Different process magnitudes are usually modeled by using a different number of model iterations and/or friction coefficients. For example, different friction coefficients can be used to assess the relevance of protection forest by simulating events with and without forest cover and to compare how the run-out distances increase (e.g., Wichmann, 2006; Proske and Bauer, 2016). Different friction coefficients have also been used to simulate different block sizes in rockfall modeling (e.g., Haas et al.,
10 2012b). The influence of protection measures can be analyzed by manipulating the DTM to include barriers or retention basins and to observe the impact on the extent of the processes area. Here, deposition modeling is usually involved for sink filling. Deposition of material and sink filling are also required with high resolution DTMs in order to fill up small depressions, to overcome obstacles, or to simulate the break out of incised channels.

In order to demonstrate the approach for sink filling, a 10 m DTM has been modified to include a sink along the process
15 path. For the sake of simplicity, the process path is modeled using the *Maximum Slope* approach with 1000 iterations and no friction and deposition models. Figure 5 (a) shows that the process stops at the end of the sink in case no material is provided. If 50 m³ of material are provided, the process overcomes the sink and stops not until the next sink is reached. This sink can not be overcome because there is not enough material left over.

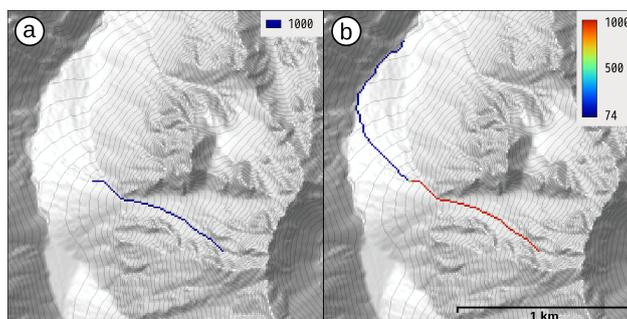


Figure 5. Sink filling; (a) the process stops in a sink; (b) the process overcomes the sink and stops in the next sink because no material is left over.

Figure 6 illustrates the sink filling approach in detail. In case only a single iteration is calculated (Fig. 6 (a)), all material provided is available in that iteration. The sink can thus be filled at once, preserving the slope specified with the minimum slope parameter (here 2.5°). Figure 6 (b) shows the successive filling of the sink when ten model iterations are calculated and
5 thus only 50/10 m³ of material are available per iteration.

Figure 7 shows the result of modeling two different magnitudes of debris flow events from five release areas on a 10 m, hydrologically sound DTM. The process path is modeled with the *Random Walk* approach (slope threshold = 40°, exponent of divergence = 2, persistence factor = 1.5, model iterations = 1000) and the run-out distance is calculated with the PCM model. Because debris flow velocities are usually lower than 12–15 ms⁻¹, M/D is set to 40 m. The two events are modeled using a

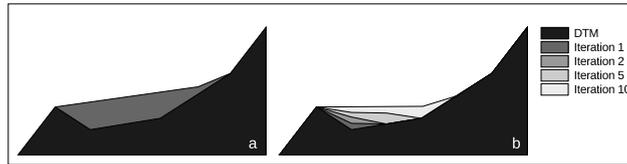


Figure 6. Longitudinal profile illustrating the sink filling approach; (a) single model iteration, (b) ten model iterations.

10 friction parameter μ of 0.25 for the medium event and a μ of 0.13 for the large event. In both cases the initial velocity is set to 1 ms^{-1} .

The maximum velocities reached along the steeper parts of the process path are almost the same (16 ms^{-1} for the large event, 15 ms^{-1} for the medium event), but the run-out distances significantly increase with the lower friction value μ used for the large event. The stopping positions are well distributed over the torrential fan because of the different process path lengths and slope profiles of the respective random walks. The number of stops per grid cell resembles the pattern of the transition frequencies.

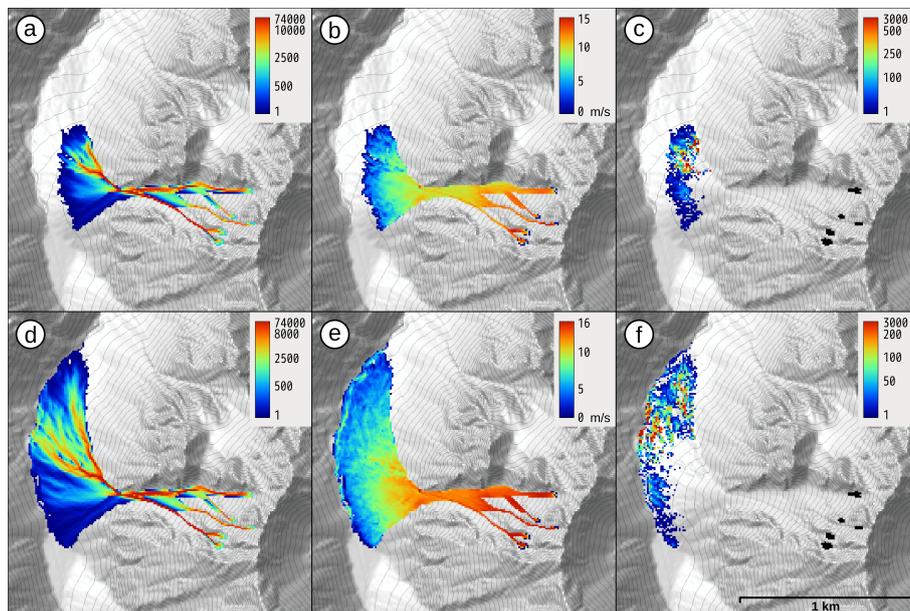


Figure 7. Medium (top) and large (bottom) debris flow events; (a) and (d) transition frequencies, (b) and (e) maximum velocities, and (c) and (f) stopping positions. For details see text.

Figures 8 (b) and (c) show the modeling results of the large event from four release areas on a hydrologically sound 2.5 m DTM (same random walk and friction model settings as in the 10 m case above). At this DTM resolution the debris flow channels are sharply incised and the process path is forced to follow the channels in case no material deposition along the process path is simulated. Figures 8 (d) to (f) show the result using 3750 m^3 of material in total (equally distributed over the release areas) and the deposition model approach $\min(\text{slope}; \text{velocity})$ & *on stop* with the following parameter settings: initial

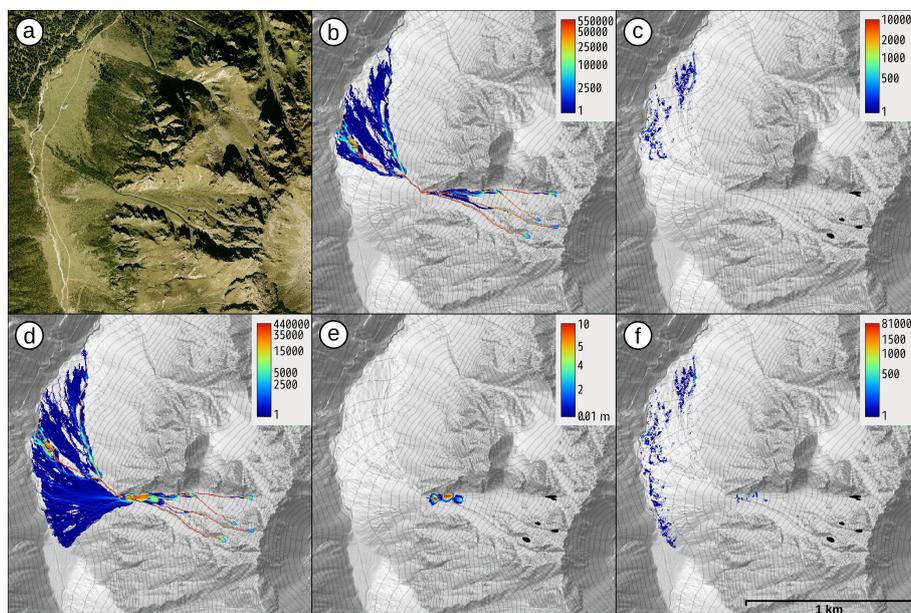


Figure 8. Deposition modeling scenario on a high resolution 2.5 m DTM; (a) orthophoto, (b) transition frequencies (no deposition), (c) stopping positions (no deposition), (d) transition frequencies (deposition), (e) material deposition heights, (f) stopping positions (deposition). For details see text.

deposition on stop = 20 %, slope threshold = 35°, velocity threshold = 12 ms⁻¹; maximum deposition along path = 20 % and minimum path length = 650 m. This parameter setting constrains the material deposition to the head of the torrential fan, successively filling up the incised channel and permitting the process to break out of the channel. In consequence, the process area covers the complete fan. Comparing the stopping positions (Fig. 8 (f)) with the material deposition heights (Fig. 8 (e)) it can be seen that although the deposition approach tries to deposit material while preserving a downward slope, new sinks are introduced in some cases because the available material per model iteration is not always enough to meet this requirement. Such sinks are then filled up in subsequent model iterations (see also Fig. 6 (b)).

5 Discussion and Conclusion

The GPP model integrates several well known model approaches which have proven in practice into a single GIS-based simulation framework. The framework is highly modular and provides the possibility to combine different modeling approaches and thus to model different kinds of gravitational processes. Although some model components are based on rather simple concepts it is their complex interaction which permits to delineate the extend of gravitational process areas. Reasonable, spatially distributed results can be obtained with a minimum of input data and model parameters, recommending the framework especially for susceptibility mapping on regional scales. Nevertheless, recent additions to the model approaches like sink filling and deposition modeling make it also interesting for scenario modeling on various scales. Like with every other simulation



model it must be pointed out that it is a prerequisite to understand the functionality of the model components in detail before their application and the interpretation of the model results.

Besides its pure scientific application, the GPP model also qualifies as kind of sandbox game because of its characteristics.

10 Dynamic processes are reproduced by stochastic components and Monte Carlo simulation. Basically only a DTM and a map of release areas is required to get started. This allows its straightforward application in education. Additional information like spatially distributed friction coefficients derived from land cover maps are easily added for scenario modeling making e.g., the impact of protection forest decline immediately obvious.

The GPP model is implemented in the FOSS SAGA (Conrad et al., 2015) and is thus completely integrated into a GIS environment which facilitates the preparation of input data and the analysis of the results. This avoids cumbersome data editing and data format conversions. Furthermore, the integration of the model's source code into the official SAGA source code repository will assure source code maintenance and easy application since the GPP model will be included in every SAGA binary release.

5 The GPP model is an attempt to bundle the development efforts put into several geomorphological process models within the last years into a single free and open source application. We feel that making them available in a new and free implementation, even extended by new components, is important for geomorphological and natural hazards related research. The modular structure of the framework and in particular of the source code facilitates the addition of further model approaches. Thus we are looking forward to contributions extending the framework.

6 Code availability

The SAGA source code repository, including the GPP model, is hosted at <https://sourceforge.net/projects/saga-gis/> using a git repository. Read only access is possible without login. Alternatively, the source code and binaries can be downloaded directly
10 from the files section at <https://sourceforge.net/projects/saga-gis/>.

Appendix A



Table A1. The process path parameters of the GPP model.

Model	Parameters	Description
Maximum slope	Iterations	Number of model iterations from each start cell [-]
	Processing order	Processing order of start cells; choice
	Seed value	Pseudo-random number generator initialization
Random walk	Iterations	Number of model iterations from each start cell [-]
	Processing order	Processing order of start cells; choice
	Seed value	Pseudo-random number generator initialization
	Slope threshold	Threshold below which lateral spreading is modeled [°]
	Exponent	Exponent controlling the amount of lateral spreading [-]
	Persistence factor	Factor used as weight for the current flow direction [-]



Table A2. The run-out parameters of the GPP model.

Model	Parameters	Description
Geometric gradient	Friction angle	Angle between the release area and the end of the deposit (straight-line distance) [°]; either spatially distributed or global
Fahrboeschung principle	Friction angle	Angle between the release area and the end of the deposit (process path length) [°]; either spatially distributed or global
Shadow angle	Friction angle	Angle between first impact location on the talus slope and the end of the deposit (straight-line distance) [°]; either spatially distributed or global
	Threshold angle free fall	Minimum angle between start cell and current cell to model free fall [°]; alternatively a raster data set with slope impact areas can be provided
	Slope impact areas raster	Mapped slope impact areas as raster data set, optional
1-parameter friction model	Threshold angle free fall	Minimum angle between start cell and current cell to model free fall [°]; alternatively a raster data set with slope impact areas can be provided
	Slope impact areas raster	Mapped slope impact areas as raster data set, optional
	Method impact Reduction	Approaches to calculate the velocity reduction on slope impact; choice Amount of energy reduction on slope impact [%]
	Mu	Friction parameter μ [-]; alternatively a raster data set with friction values can be provided
	Mu raster	Spatially distributed friction values [-] as raster data set, optional
	Mode of motion	The mode of motion, either sliding or rolling
PCM model	Mu	Friction parameter μ [-]; alternatively a raster data set with friction values can be provided
	Mu raster	Spatially distributed friction values [-] as raster data set, optional
	Mass to drag ratio	Mass to drag ratio M/D [m]; alternatively a raster data set with M/D values can be provided
	Mass to drag ratio raster	Spatially distributed M/D values [m] as raster data set, optional
	Initial velocity	The initial velocity of a particle [ms^{-1}]



Table A3. The deposition parameters of the GPP model.

Model	Parameters	Description
Sink Filling	Minimum slope	Minimum slope to preserve on sink filling [°]
On stop	Initial deposition on stop ¹	Percentage of available material initially deposited on stopping cell [%]
Slope & on stop	Slope threshold ²	Slope angle below which the deposition of material sets in [°]
	Maximum deposition along process path ¹	Percentage of material which is deposited at most [%]
	Minimum path length ¹	Path length which has to be reached before material deposition is enabled [m]
Velocity & on stop	Parameters denoted by ¹	
	Velocity threshold	Velocity below which the deposition of material sets in [ms ⁻¹]
min(slope;velocity) & on stop	Parameters denoted by ^{1,2}	

¹also used by the models below; ²also used by the *min(slope;velocity) & on stop* model



Table A4. The input and output data sets of the GPP model.

Data set	Description
Digital terrain model	In case no <i>Material</i> data set for sink filling is provided, this must be a hydrologically sound DTM [m]; input data set
Release Areas	Release areas encoded by unique integer IDs, all other cells NoData [-]; input data set
Material	Height of material available in each start cell [m]; used for sink filling and material deposition; optional input data set
Friction Angle	Spatially distributed friction angles [°]. Optionally used with the <i>Geometric Gradient</i> , <i>Fahrboeschung</i> or <i>Shadow Angle</i> friction model; optional input data set
Slope Impact Areas	Slope impact grid, impact areas encoded with valid values, all other NoData. Optionally used with the <i>Shadow Angle</i> or the <i>I-parameter friction model</i> ; optional input data set
Friction Parameter Mu	Spatially distributed friction parameter μ [-], optionally used with the <i>I-parameter friction model</i> or the <i>PCM Model</i> ; optional input data set
Mass to Drag Ratio	Spatially distributed M/D ratio [m], optionally used with the <i>PCM Model</i> ; optional input data set
Process Area	Delineated process area with encoded transition frequencies [count]; output data set
Deposition	Height of material deposited in each cell [m]; optional output data set in case a grid with material amounts is provided as input
Maximum Velocity	Maximum velocity observed in each cell [ms^{-1}]; optional output data set of the run-out models
Stopping Positions	Stopping positions, showing cells in which the run-out length has been reached [count]; optional output data set

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