Supplemental material to "The SUPECA kinetics for scaling redox reactions in networks of mixed substrates and consumers and an example application to aerobic soil respiration"

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Below we provide auxiliary information for the numerical benchmark of the SUPECA kinetics.

The equations for fixed-point iteration are

$$\begin{bmatrix} S_1 \end{bmatrix}_{new} = \begin{bmatrix} S_1 \end{bmatrix}_T \left( 1 + \frac{\begin{bmatrix} M \end{bmatrix}_{old}}{K_{MS1}} + \frac{k_{BS1} \begin{bmatrix} B \end{bmatrix}_{old}}{k_{BS2} \begin{bmatrix} S_2 \end{bmatrix}_{old}} + \frac{k_{BS2}}{k_2^+} \begin{bmatrix} B \end{bmatrix}_{old} \frac{\begin{bmatrix} S_2 \end{bmatrix}_{old}}{\begin{bmatrix} S_1 \end{bmatrix}_{old}} + \frac{k_{BS1}}{k_2^+} \begin{bmatrix} B \end{bmatrix}_{old} \right)^{-1}$$
(S-1)

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$$\begin{bmatrix} S_2 \end{bmatrix}_{new} = \begin{bmatrix} S_2 \end{bmatrix}_T \left( 1 + \frac{k_{BS2} \begin{bmatrix} B \end{bmatrix}_{old}}{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}} + \frac{k_{BS2}}{k_2^+} \begin{bmatrix} B \end{bmatrix}_{old} + \frac{k_{BS1}}{k_2^+} \begin{bmatrix} B \end{bmatrix}_{old} \frac{\begin{bmatrix} S_1 \end{bmatrix}_{old}}{\begin{bmatrix} S_2 \end{bmatrix}_{old}} \right)^{-1}$$
(S-2)

$$\begin{bmatrix} B \end{bmatrix}_{new} = \begin{bmatrix} B \end{bmatrix}_{T} \left( 1 + \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_{BS2} \begin{bmatrix} S_2 \end{bmatrix}_{old}} + \frac{k_{BS2} \begin{bmatrix} S_2 \end{bmatrix}_{old}}{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}} + \frac{k_{BS2} \begin{bmatrix} S_2 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_2 \end{bmatrix}_{old} + \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old} = \frac{k_{BS1} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{k_2^+} \begin{bmatrix} S_1 \end{bmatrix}_{old}}{$$

$$\begin{bmatrix} M \end{bmatrix}_{new} = \begin{bmatrix} M \end{bmatrix}_T \left( 1 + \frac{\begin{bmatrix} S_1 \end{bmatrix}_{old}}{K_{MS1}} \right)^{-1}$$
(S-4)

The iteration starts with initial condition  $[S_1]_{old} = [S_1]_T$ ,  $[S_2]_{old} = [S_2]_T$ ,  $[B]_{old} = [B]_T$ , and  $[M]_{old} = [M]_T$ . The iteration stops when the relative change between two consecutive iterations is smaller than 10<sup>-4</sup>.

## Supplementary figure

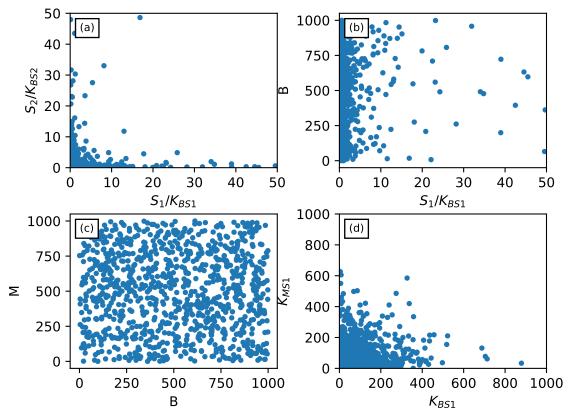


Figure S1. Scatter plots of the parameters used in the numerical benchmark of the SUPECA kinetics (which is Figure 4 in the main text).