A global scavenging and circulation ocean model of thorium-230 and protactinium-231 with improved particle dynamics (NEMO–ProThorP 0.1)

Marco van Hulten1,2, Jean-Claude Dutay1, and Matthieu Roy-Barman1

1Laboratoire des Sciences du Climat et de l’Environnement, IPSL, CEA–Orme des Merisiers, 91191 Gif-sur-Yvette, France
2Geophysical Institute, University of Bergen, Bergen, Norway

Correspondence to: M. M. P. van Hulten <Marco.Hulten@uib.no>

Pre- and postprints may be found at arXiv:1708.04157.

Abstract. In this paper, we set forth a 3-D ocean model of the radioactive trace isotopes \(^{230}\text{Th}\) and \(^{231}\text{Pa}\). The interest arises from the fact that these isotopes are extensively used for investigating particle transport in the ocean and reconstructing past ocean circulation. The tracers are reversibly scavenged by biogenic and lithogenic particles.

Our simulations of \(^{230}\text{Th}\) and \(^{231}\text{Pa}\) are based on the NEMO–PISCES ocean biogeochemistry general circulation model, which includes biogenic particles, namely small and big particulate organic carbon, calcium carbonate and biogenic silica. Small and big lithogenic particles from dust deposition are included in our model as well. Their distributions generally compare well with the small and big lithogenic particle concentrations from recent observations from the GEOTRACES programme, except for boundary nepheloid layers for which, as up to today, there are no non-trivial, prognostic models available on a global scale. Our simulations reproduce \(^{230}\text{Th}\) and \(^{231}\text{Pa}\) dissolved concentrations: they compare well with recent GEOTRACES observations in many parts of the ocean. Particulate \(^{230}\text{Th}\) and \(^{231}\text{Pa}\) concentrations are significantly improved compared to previous studies, but they are still too low because of missing particles from nepheloid layers. Our simulation reproduces the main characteristics of the \(^{231}\text{Pa}/^{230}\text{Th}\) ratio observed in the sediments, and supports a moderate affinity of \(^{231}\text{Pa}\) to biogenic silica as suggested by recent observations, relative to \(^{230}\text{Th}\).

Future model development may further improve understanding, especially when this will include a more complete representation of all particles, including different size classes, manganese hydroxides and nepheloid layers. This can be done based on our model, as its source code is readily available.

1 Introduction

Oceanic circulation and the carbon cycle play a major role in the regulation of the past and present climate. Heat and carbon dioxide in the atmosphere tend to equilibrate with the ocean surface, and are transported down into the deep ocean through the Meridional Overturning Circulation (MOC). Biogeochemical cycling also generates organic carbon that transfers into the deep ocean through particle sinking. Because of this, the strength of the MOC and particle removal participate actively in the regulation of the climate on the Earth.

Trace elements are also affected by these mechanisms, and represent useful tools to provide constraints on these processes. The GEOTRACES programme has generated a unique, large data set that can now be used to better understand biogeochemical oceanic processes. Modelling quantifies and provides more information on the processes that control the oceanic distribution
of these new observations. In present day climate, it is difficult to measure the MOC strength, and for past climate there are no measurements available at all. Isotopes and trace elements from sediment cores are used as proxies to infer past ocean circulation. Several examples include carbon isotopes (Broecker et al., 1988), the cadmium/calcium ratio (Rosenthal et al., 1997), the ratio between protactinium-231 and thorium-230 ($^{231}$Pa/$^{230}$Th) (Böhm et al., 2015), and the neodymium isotope ratio $^{143}$Nd/$^{144}$Nd (Piotrowski et al., 2005). These proxies are affected by dynamical and biogeochemical processes. Including these proxies in a climate model is a way to better understand the climatic signal they register.

We will focus on $^{230}$Th and $^{231}$Pa, because these isotopes are well documented by the international GEOTRACES programme, and they are particularly suitable to study the transfer of particulate matter since the isotopes’ source in the ocean is perfectly known: radioactive decay of uranium isotopes. Others have modelled $^{143}$Nd and $^{144}$Nd (Arsouze et al., 2008, 2009; Ayache et al., 2016), $^{13}$C (Tagliabue et al., 2009) and $^{14}$C (Mouchet, 2013). The ratio between $^{230}$Th and $^{231}$Pa is used as a proxy for past ocean conditions, but this signal is potentially affected by both circulation and biogeochemical changes. Therefore, a correct understanding of the scavenging and the underlying particle dynamics is essential in order to better simulate these tracers (Dutay et al., 2015).

Protactinium-231 and thorium-230 are produced in the ocean by the $\alpha$-decay of uranium-235 and uranium-234, respectively. Because the activity of uranium is approximately uniform in the ocean, $^{231}$Pa and $^{230}$Th are produced at a relatively constant rate ($\beta_{Pa} = 2.33 \times 10^{-3}$ dpm m$^{-3}$ a$^{-1}$) and $\beta_{Th} = 2.52 \times 10^{-2}$ dpm m$^{-3}$ a$^{-1}$, dpm = disintegrations per minute) (Henderson and Anderson, 2003). They are both scavenged rapidly by the many particles that reside in the ocean and settle towards the seafloor. $^{231}$Pa is less sensitive to particle scavenging than $^{230}$Th, which is reflected in the longer residence time of $^{231}$Pa (80–200 yr) compared to that of $^{230}$Th (20–40 yr) (Yu et al., 1996). $^{231}$Pa and $^{230}$Th are radioactive, decaying to radium isotopes and having a half-life of 32.76 kyr and 75.40 kyr, respectively. Each combination of particle–radionuclide adsorption has a different reactivity. Other factors may affect the adsorption of radionuclides onto particles. For example, smaller particles have larger surface area to volume ratios, which results in an increase in the number of these radionuclides adsorbed per particle. Additionally, while the adsorption rate is expected to increase with particle concentration, the adsorption rate may be partly limited by the coagulation of non-filtered particles (or colloids) to filtered particles (Honeyman et al., 1988; Honeyman and Santschi, 1988). The vertical distributions of natural radionuclides, such as $^{230}$Th and $^{231}$Pa, are hence sensitive to the distribution and mixture of particles. As a consequence of the different particle reactivities of $^{230}$Th and $^{231}$Pa, the dissolved concentration ratio $^{231}$Pa/$^{230}$Th deviates from the production activity ratio of 0.093 (Anderson et al., 1983; Anderson, 2003; Rutgers van der Loeff et al., 2016).

As both particle dynamics and circulation of the ocean affect $^{230}$Th and $^{231}$Pa, numerical biogeochemical general circulation models are used to study the relative contribution of these mechanisms. The isotopes have been simulated in models of intermediate complexity, for instance by Henderson et al. (1999) (LSG-OGCM), Marchal et al. (2000) (EMIC 2.5D), Heinze et al. (2006) (HAMOCC) and Luo et al. (2010). More complex ocean general circulation models models have also been used to simulate these tracers Dutay et al. (2009) (NEMO–PISCES), Siddall et al. (2007); Rempfer et al. (2017) (Bern3D) and Gu and Liu (2017) (CESM). Dutay et al. (2009) demonstrated that the particle concentration simulated by the PISCES model in the deep ocean was a factor of 2 in the mesopelagic zone to 50 in the deepest ocean too low. This lead to overestimated radionuclide concentrations in the deep ocean. Therefore, it is crucial to improve the representation of the particles (Dutay et al., 2009). Rempfer et al. (2017) showed that taking into account additional sinks at the seafloor and at the ocean margins yields an improved agreement with observations, especially for the dissolved phases of $^{230}$Th and $^{231}$Pa. Particulate ratios improved to a lesser extent; the authors have not presented evaluation of their simulated particulate concentrations. Gu and Liu (2017) had similar goals as this study.
In this study, we try to improve on previous studies that simulate the distribution of $^{230}$Th and $^{231}$Pa. Our approach is to improve the mechanistic description of the particle and radionuclide cycling, as well as on the side of system design and reusability of the model. We evaluate how well the model fits with observations, but tuning is not one of our main goals. Just like Dutay et al. (2009), we use the NEMO–OPA (Nucleus for European Modelling of the Ocean – Océan PAralélsé) ocean general circulation model (Madec and the NEMO team, 2016) and the PISCES biogeochemical model (Aumont et al., 2015).

Aumont et al. (2017) showed that dissolution rates of Particulate Organic Carbon (POC) in PISCES were overestimated, and they improved on this by introducing a spectrum of different labilities. This improved the simulation of both small and big POC significantly, so we use this same model for our simulations. There are several improvements since Dutay et al. (2009), namely the new model

- includes lithogenic particles from dust deposition;
- improved the biogeochemistry, affecting the biogenic particle distributions (Aumont et al., 2015, 2017);
- includes three different phases per nuclide (dissolved, and adsorbed onto big (and small) particles), whereas Dutay et al. (2009) include only a single compartment (total concentration) for each nuclide from which they calculated the respective phases based on chemical equilibrium;
- is more precise/explicit on the mathematical formalism;
- is written in Fortran 95 instead of Fortran 77, making the extension of its use to other modern Fortran models easier;
- is part of a modern model framework, NEMO–TOP, facilitating its use with other models in this framework.

The main objective of this paper is to improve on the simulation of $^{230}$Th and $^{231}$Pa (the dissolved and two particulate size classes of particles for both nuclides), based on an improved modelling of small and big particles.

New observations are available from the GEOTRACES programme. Especially the North Atlantic GA03 transects will be used for model validation; because on this transect not only dissolved $^{230}$Th and $^{231}$Pa have been measured (Hayes et al., 2015b), but also their adsorbed forms (Hayes et al., 2015b) and biogenic and lithogenic particle concentrations in two size classes (Lam et al., 2015).

## 2 Model description

In order to simulate the biogenic particle dynamics and its interaction with the $^{230}$Th and $^{231}$Pa trace isotopes, we use the biogeochemical circulation model NEMO–PISCES (Madec, 2008; Aumont et al., 2015). This model has been employed for many other studies concerning trace metals, as well as large-scale ocean biogeochemistry (e.g. Gehlen et al., 2007; Arsouze et al., 2009; Dutay et al., 2009; Tagliabue et al., 2010; Van Hulten et al., 2013, 2014, 2017b). We force PISCES by a climatological year of circulation fields (including turbulent diffusion) that was obtained from the dynamical component of NEMO. Table 1 gives an overview of this and other components of the model and their relevant properties.

All model fields are defined on the ORCA2 discrete coordinate system, an irregular grid covering the whole world ocean with a nominal resolution of $2^\circ \times 2^\circ$, with an increased resolution in the meridional direction near the equator and Antarctica, and in both horizontal directions in the Mediterranean, Red, Black and Caspian Seas. On the Northern Hemisphere, it has two coordinate singularities, one in Canada and the other in Russia, such that both singularities fall outside the computational domain. The vertical resolution of the ORCA2 grid is 10 m in the upper 100 m, increasing downwards to 500 m, such that there are 30 layers in total and the ocean has a maximum depth of 5000 m (Madec and Imbard, 1996; Murray, 1996). The timestep
circulation (OPA) prescribed forcing (off-line physics) (e.g. used by Arsouze et al., 2009) 6.0 h

biogenic particles prognostically integrated by PISCES (Aumont et al., 2015) 1.5 h

– POC two size classes settling with \( w_s = 2 \text{ m d}^{-1} \) and \( w_b = 50 \text{ m d}^{-1} \); variable reactivity (Aumont et al., 2017) 6.0 h

– CaCO\(_3\) one size class settling with \( w_b = 50 \text{ m d}^{-1} \); higher order dissolution (e.g. Subhas et al., 2015) 1.5 h

– bSiO\(_2\) one size class settling with \( w_b = 50 \text{ m d}^{-1} \); no changes 6.0 h

lithogenic particles based on forcing of dust deposition; two size classes settling with \( w_s = 2 \text{ m d}^{-1} \) and \( w_b = 50 \text{ m d}^{-1} \) 1.5 h

radionuclide model six prognostic tracers (dissolved, small and big adsorbed; \(^{231}\text{Pa}\) and \(^{230}\text{Th}\)) 6.0 h

Table 1. Model components and properties essential for the radionuclide model. OPA stands for Océan PAralalisé.

of the model is 6 h for the dynamics and the radionuclides, and 1.5 h for the biogeochemistry (PISCES) and the lithogenic particles. When necessary, sub-timestepping is done for all sinking components in the model.

2.1 Circulation

The circulation was obtained by forcing NEMO in the ORCA2 configuration with climatological air-sea boundary conditions, consisting of heat, fresh water and momentum fluxes that were derived from bulk formulae. They are functions of wind, sea surface temperature, air temperature, air humidity and evaporation minus precipitation. For the tropics, daily wind stress was used, which was based on European Remote Sensing (ERS) satellite data, and for the polar regions, NCEP/NCAR re-analysis data (Kalnay et al., 1996; Kistler et al., 2001). Surface salinity was restored with a timescale of 60 days towards the seasonal Polar Science Center Hydrographic Climatology (PHC) dataset to avoid model drift (Timmermann et al., 2005). The last year of this 200-year simulation is used as our one-year climatology with a resolution of five days of the dynamics.

2.2 Particle dynamics

This version of PISCES includes two size classes of POC, both with differential remineralisation rates (Aumont et al., 2017), one size class of biogenic silica (bSiO\(_2\)) and one class of calcium carbonate (CaCO\(_3\)) (Fig. 1). In the model, particles sink down with two velocities: \( w_s = 2 \text{ m d}^{-1} \) and \( w_b = 50 \text{ m d}^{-1} \). Aumont et al. (2015) marks the diameter boundary at 100 \( \mu \text{m} \), but as we need to compare with observations, the size classes will be taken to correspond with “small” particles (\( \phi \leq 51 \mu \text{m} \)) and “big” particles (\( \phi > 51 \mu \text{m} \)).

The dissolution equation for calcium carbonate is given by

\[
\frac{d[\text{CaCO}_3]}{dt} = -R[\text{CaCO}_3],
\]

where the rate variable (constant in \( t \)) for calcite dissolution is

\[
R = k \cdot (1 - \Omega)^n,
\]

where \( k \) and \( n \) are two somewhat restricted, though tunable, parameters that signify a dissolution rate constant and a reaction rate order, respectively. The calcite saturation state is given by

\[
\Omega = \frac{[\text{Ca}^{2+}] [\text{CO}_3^{2-}]}{K_{sp}^\prime},
\]

where the rate variable (constant in \( t \)) for calcite dissolution is

\[
R = k \cdot (1 - \Omega)^n,
\]

where \( k \) and \( n \) are two somewhat restricted, though tunable, parameters that signify a dissolution rate constant and a reaction rate order, respectively. The calcite saturation state is given by

\[
\Omega = \frac{[\text{Ca}^{2+}] [\text{CO}_3^{2-}]}{K_{sp}^\prime},
\]
Figure 1. Conceptual model of particle dynamics, on which the numerical model is based. Nanophytoplankton and diatoms (in green) take up nutrients and $\text{CO}_2$, which are released again from respiration and remineralisation of $\text{bSiO}_2$, POC, dissolved organic matter and lithogenic particles. The nutrients, $\text{CO}_2$ and dissolved organic matter are not represented in the figure, because only particles impact $^{231}\text{Pa}$ and $^{230}\text{Th}$. Zooplankton are denoted by the black box. All sinking particles are denoted by blue boxes. Effectively, this figure comprises the internal cycling of PISCES, minus details that are not of interest here, plus the lithogenic dust model. Small and big particulate Organic Matter are denoted by sPOM and bPOM, both subject to the differential lability scheme (Aumont et al., 2017), and $\text{bSiO}_2$ stands for biogenic silica. Similarly, sLith and bLith stand for small and big lithogenic particles. Sinking is denoted by the red arrows; triple arrows means fast, normal arrows slow.

where $K'_{sp}$ is the product of the saturation concentrations of calcium and carbonate. This can be approximated by

$$\Omega \approx \frac{[\text{CO}_2^{-3}]}{[\text{CO}_2^{-3}]}_{\text{sat}},$$

because relative variations in $[\text{Ca}^{2+}]$ are small. For $\text{CaCO}_3$ we changed the standard first-order dissolution kinetics parameterisation to a fourth-order dissolution, based on evidence of Keir (1980) and subsequent studies. For our simulation we used a calcite dissolution rate constant of $k = 2.5 \text{ mo}^{-1}$ and a dissolution order of $n = 3.9$ (Subhas et al., 2015).

In addition to biogenic particles, we introduced lithogenic dust particles in the model. The yearly average dust flux is derived from Hauglustaine et al. (2004) and is presented in Fig. 2. It is used by the model as the input of lithogenic ocean particles as well as for nutrient supply in PISCES. This dust deposition field has been tested in biogeochemical studies with this configuration of NEMO (e.g. Van Hulten et al., 2013).

Small and big lithogenic particles are added to the upper layer of the ocean according to:

$$\frac{\partial P_{\text{Litho}}}{\partial t} \Bigg|_{\text{surface}} = f \frac{\Phi_{\text{dust}}}{\Delta z_1},$$

where $P_{\text{Litho}}$ is the small (big) lithogenic particle concentration, $f$ is the fraction of the dust that gets partitioned into the small (big) lithogenic particles in the ocean, $\Delta z_1 = 10 \text{ m}$ is the thickness of the upper model layer, and $\Phi_{\text{dust}}$ is the dust flux.

Our model has two size classes for lithogenic particles, so this equation is applied for two different concentrations $P_{\text{Litho}}$ and respective fractions $f$. We set the small lithogenic dust flux fraction to 20 % and the big one to 80 %. Once partitioned in the ocean, the lithogenic particles sink down, changing their concentrations throughout the ocean according to

$$\frac{dP_{\text{Litho}}}{dt} = -w \cdot \frac{\partial P_{\text{Litho}}}{\partial z} + \left( A \nabla_h^2 + B \frac{\partial^2}{\partial z^2} \right) P_{\text{Litho}},$$

where $w$ is the settling velocity, set to the constant $2 \text{ md}^{-1}$ for the small lithogenic particles and to $50 \text{ md}^{-1}$ for the big particles. The depth, $z$, is positive upwards, $\nabla_h$ is the horizontal divergence, and $A$ and $B$ are respectively the horizontal and
vertical eddy diffusivity coefficients. The material derivative includes a term for eddy-induced velocity (Gent and McWilliams, 1990; Gent et al., 1995). Equation (6) is identical to the settling of small and big POC (Aumont et al., 2015). Of course, there are also biological and chemical sources and sinks for POC. However, for lithogenic particles there are no such sources or sinks because the only source in our model is dust deposition and we assume the lithogenic particles are refractory. The lithogenic particles are removed from the model domain when arriving at the seafloor, which means that they are buried in the sediment.

2.3 Radionuclides

Thorium-230 and protactinium-231 are produced throughout the ocean from the decay of $^{234}\text{U}$ and $^{235}\text{U}$, respectively. Because of long residence times of over 200 kyr, these uranium isotopes are approximately homogeneously distributed throughout the ocean, and do not change much over time (Ku et al., 1977). The residence time of $^{234}\text{U}$ is $3.2-5.6 \times 10^5$ a, which is much longer than the full mixing time of the world ocean of about $10^3$ a (Dunk et al., 2002). The $^{234}\text{U}$ concentration can vary about 10%, depending mostly on the salinity (Owens et al., 2011), but that is smaller than uncertainties arising from other assumptions in our model. Therefore, we assume that the production rates of $^{230}\text{Th}$ and $^{231}\text{Pa}$ are constant, both in space and time.

The $^{230}\text{Th}$ and $^{231}\text{Pa}$ radionuclides are reversibly scavenged by biogenic and lithogenic particles (Fig. 3). We will assume, as in previous studies (e.g. Siddall et al., 2005; Dutay et al., 2009), that the adsorption and desorption reaction rates are sufficiently fast compared to radionuclide production, decay, advection, mixing, change in particle distribution and settling of the adsorbed
Figure 3. The conceptual reversible scavenging model for the radionuclides. The radioisotopes, $^{230}$Th and $^{231}$Pa, are depicted in orange when in the dissolved phase. Just like with the other PISCES tracers, the dissolved and particulate radionuclides are transported by circulation and eddy diffusion.

phases (see discussion in section 6). Because of that, we equilibrate between the dissolved and adsorbed phases instantly at each time step. This means, only considering ad- and desorption processes at this point, that we must solve this set of equations for every nuclide $i$:

$$0 = \frac{\partial}{\partial t}(A_{i,D} + A_{i,S} + A_{i,B}),$$  
(7a)

$$A_{i,S} = A_{i,D} \sum_{j \in S} K_{ij} P_j,$$  
(7b)

$$A_{i,B} = A_{i,D} \sum_{j \in B} K_{ij} P_j,$$  
(7c)

where $A_{i,D}$ stands for the activity of nuclide $i \in \{^{230}\text{Th}, ^{231}\text{Pa}\}$, and where $P_j$ stands for the concentration of particle $j \in \{\text{sPOC}, \text{bPOC}, \text{CaCO}_3, \text{bSiO}_2, \text{sLitho}, \text{bLitho}\}$ (in gram per gram of seawater, so strictly this is a mass fraction). $D$ is the set of non-sinking phases (here only dissolved), $S$ of small particles that sink with $2 \text{ m d}^{-1}$ and $B$ of big particles that sink with $50 \text{ m d}^{-1}$ (in the same way as Eq. (6) for lithogenic particles). For any particle size class $J \in \{S, B\}$ and any radionuclide $i$, we define $A_{i,J} = \sum_{j \in J} A_{ij}$. Finally, $K_{ij}$ is the equilibrium partition coefficient of nuclide $i$ for particle $j$. As with small and big POC, adsorbed $^{230}$Th and $^{231}$Pa should aggregate and disaggregate. However, any transference of radionuclides between two particle types or size classes, in addition to the instant equilibration, would not have any effect as there would quickly be a new equilibrium of the radionuclides between the particles and the dissolved phase at the next instant reequilibration (which happens each timestep). Therefore there is no equation for the radionuclides addressing aggregation.

Since we cannot solve this analytically, this will be done numerically by first assigning a new value to the dissolved nuclide activity:\footnote{Concentration of radionuclides (amount per unit of volume) is proportional to its (radio)activity (disintegrations per unit of time). These terms are used interchangeably throughout this paper. Moreover, they are considered identical: the activity or concentration $[^{230}\text{Th}]_D \equiv A_{230\text{Th}}$ is expressed in mBq m$^{-3}$, and thus we report activity ratios of $^{231}\text{Pa} / ^{230}\text{Th}$.}

$$A_{i,D} := \frac{A_{i,D} + A_{i,S} + A_{i,B}}{1 + \sum_{j} K_{ij} P_j},$$  
(8)

When summation bounds are not specified, the union of all phases, $D \cup S \cup B$, is assumed.
Then, we calculate the activity of $i$ that is adsorbed onto small and big particles by applying Eqs (7b) and (7c). With this approach, the small and big adsorbed concentrations equilibrate instantly. Assuming that the change in adsorption strength is much smaller than the relative change in tracer activity, $\forall_{i,j} \partial_t \sum_{j \in J} K_{ij} P_j \ll \partial_t A_{i,D}/A_{i,D}$, the total activity of every $i$ is conserved, i.e. Eq. (7a) holds. Then,

**Proof.** Let the total adsorption strength for any isotope $i$ be $Q_i = \sum_j K_{ij} P_j$ and the total amount of the same isotope $T_i = A_{i,D} + A_{i,S} + A_{i,B}$, and let primes denote the updated concentrations. Assume that the adsorption strength for every isotope $i$ is constant ($Q'_i \equiv Q_i$).

$$T'_i = \frac{T_i}{1 + Q'_i} + A'_{i,D} Q'_i$$

$$= \frac{T_i}{1 + Q_i} + \frac{T_i}{1 + Q_i} Q_i$$

$$= \frac{T_i}{1 + Q_i} (1 + Q_i) = T_i$$

$$\Rightarrow \partial_t T'_i = \partial_t T_i = 0. \quad \square$$

The $^{230}\text{Th}$ and $^{231}\text{Pa}$ that are adsorbed onto the particles follow the same law as the small and big (lithogenic) particles (Eq. 6). Of course, by definition, the adsorbed radioisotope and the particle settle with the same speed, and thus we have implemented it.

The decay terms of $^{230}\text{Th}$ and $^{231}\text{Pa}$ are much smaller than the other sources and sinks, but they are included in the model:

\[
\frac{dA_{i,D}}{dt} = -\beta_i A_{i,D} + (A\nabla^2 + B\frac{\partial^2}{\partial z^2})A_{i,D}, \quad (9a)
\]

\[
\frac{dA_{i,S}}{dt} = -\lambda_i A_{i,S} - w_s \frac{\partial A_{i,S}}{\partial z} + (A\nabla^2 + B\frac{\partial^2}{\partial z^2})A_{i,S}, \quad (9b)
\]

\[
\frac{dA_{i,B}}{dt} = -\lambda_i A_{i,B} - w_b \frac{\partial A_{i,B}}{\partial z} + (A\nabla^2 + B\frac{\partial^2}{\partial z^2})A_{i,B}, \quad (9c)
\]

where $\beta_i$ and $\lambda_i$ are respectively the production rate and radioactive decay of isotope $i$.

3 Simulations

For the numerical simulations, we forced the just described model, an adjusted version of PISCES with lithogenic particles and radiotracers, with the off-line circulation fields. The model was spun up for 500 yr, after which it was in an approximate steady state (decadal drift of ~0.002 % for total $^{230}\text{Th}$ and ~0.058 % for total $^{231}\text{Pa}$). Protactinium-231 has a larger drift than thorium-230, because $^{230}\text{Th}$ is everywhere in the ocean more quickly removed because of its high particle reactivity. The lithogenic particles are in a steady state, and the PISCES variables are in an approximate steady state (e.g. phosphate shows a drift of ~0.005 % per decade).

The partition coefficients $K_{ij}$, with $i \in \{\text{Th, Pa}\}$, depend on the type of particle $j$ and are given in Table 2. These coefficients have large uncertainties still, but their values can be constrained by reported values from different experimental studies (e.g. Chase et al., 2002; Geibert and Usbeck, 2004; Hayes et al., 2015b). Therefore, we had quite some freedom in prescribing values. The adsorption onto calcium carbonate is a factor two decreased from Chase et al. (2002). This brings the $K$ value of Pa closer to that in Hayes et al. (2015b) based on field measurements, namely 0.9±0.4 M$g^{-1}$ (10$^6$ gram of seawater per gram of particles), but since we maintained the ratio of $K$ values, the partition coefficient of Th is much smaller than found by Hayes et al. (2015b). It is consistent with the laboratory results of Geibert and Usbeck (2004), but they cleaned the biogenic silica aggressively, bought carbonate that should be organic-free and clay (smectite) was purchased as a commercial standard and not
Table 2. Partition coefficients for the different modelled particles in $10^6$ gram of seawater per gram of particles. Between braces is the value for the sensitivity simulation discussed in Section 6.1.

<table>
<thead>
<tr>
<th>Particle</th>
<th>$K_{Pa}$ (Mg g$^{-1}$)</th>
<th>$K_{Th}$ (Mg g$^{-1}$)</th>
<th>Settling speed</th>
</tr>
</thead>
<tbody>
<tr>
<td>small POC</td>
<td>2.0</td>
<td>5.0</td>
<td>2 m d$^{-1}$</td>
</tr>
<tr>
<td>big POC</td>
<td>0.4</td>
<td>1.0</td>
<td>50 m d$^{-1}$</td>
</tr>
<tr>
<td>biogenic silica</td>
<td>0.5 (0.4)</td>
<td>0.5 (1.0)</td>
<td>50 m d$^{-1}$</td>
</tr>
<tr>
<td>CaCO$_3$</td>
<td>0.12</td>
<td>5.0</td>
<td>50 m d$^{-1}$</td>
</tr>
<tr>
<td>small lithogen.</td>
<td>10.0</td>
<td>50.0</td>
<td>2 m d$^{-1}$</td>
</tr>
<tr>
<td>big lithogen.</td>
<td>1.0</td>
<td>5.0</td>
<td>50 m d$^{-1}$</td>
</tr>
</tbody>
</table>

cleaned (Geibert and Usbeck, 2004, as well as pers. comm. January 2018). In the real ocean, solid minerals are not clean but have organic matter around them, giving rise to increased scavenging (Chuang et al., 2014, for diatoms). Therefore, our $K$'s for at least biogenic silica and calcium carbonate may be lower than what is typically considered realistic. The actual reason for the relatively low $K$ values is that we only have fast sinking biogenic silica and calcium carbonate particles in the model that represent also smaller particles that sink slower. Thus using higher $K$ values would result in too much export of Pa and Th. For small lithogenic particles, $K$ is set about a factor five larger than literature (Geibert and Usbeck, 2004; Hayes et al., 2015b), whereas big lithogenic particles have a smaller value than reported in the literature. The supplementary document contains a more exhaustive table of information, including an estimated literature range (Table S3). The consequences of chosen values of the partition coefficients is discussed further in Section 6.

4 Observations

In this study, we will focus on the GEOTRACES GA03 transect in the North Atlantic Ocean. Recently, a large number of measurements on both radionuclides and their carrier particles have been collected on this transect. This unique combination makes it especially useful to evaluate a radionuclide scavenging model. We will also compare our global ocean model with several observational datasets throughout the ocean (Table 3). Observations obtained from the GEOTRACES programme are denoted with the respective GEOTRACES transect number (Mawji et al., 2015).

For the carrier particles most of our data come from Lam et al. (2015), which is a recent GEOTRACES dataset at the GA03 transect in the North Atlantic Ocean. An older compilation of particles is taken from Lam et al. (2011). We use some older data as well (Table 3). Particle concentrations were determined by filtering seawater in situ.

Concentrations of both dissolved and particulate phases of $^{230}$Th and $^{231}$Pa were taken from Hayes et al. (2015a) (GA03) and Hayes et al. (2014) (Pacific Ocean). Other data are listed in Table 3.

To evaluate the sediment $^{231}$Pa/$^{230}$Th flux of the model, we will compare with compilations of the Holocene (i.e. top core particulate concentrations) (Table 3).
<table>
<thead>
<tr>
<th>Transect</th>
<th>Year</th>
<th>Expedition</th>
<th>Ocean basin</th>
<th>Tracers used</th>
<th>Citation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carrier particles POC, CaCO$_3$, bSiO$_2$ and lithogenic</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>–</td>
<td>1982–97</td>
<td>WCR, Line P, SOFeX, K2, JGOFS</td>
<td>Pacific and Atlantic</td>
<td>s/bPOC, bSiO$_2$, CaCO$_3$</td>
<td>Lam et al. (2011)</td>
</tr>
<tr>
<td>GA03</td>
<td>2011</td>
<td>US GT10 and GT11</td>
<td>North Atlantic</td>
<td>POC, bSiO$_2$, CaCO$_3$; s and b</td>
<td>Lam et al. (2015)</td>
</tr>
</tbody>
</table>

Radionuclides $^{230}$Th and $^{231}$Pa

| – | 1979 | R/V Knorr cruise 73/leg 16 | Central-east Pacific | $^{230}$Th$_{D,S,B}$ | Bacon and Anderson (1982) |
| – | 1976–98 (multiple) | global | $^{230}$Th$_{D,S,B}$ | Henderson et al. (1999) |
| – | 1983–02 (multiple) | global | $^{230}$Th$_{D,S,B}$ | Marchal et al. (2007) |
| GIPY5_w | 2008 | ANT XXIV/3 | Southern Oc. / Drake | $^{230}$Th$_{D,S,B}$ | Venchiarutti et al. (2011) |
| GIPY5_e | 2008 | ANT XXIV/3 | Southern Oc. / 0° E | $^{230}$Th$_{D,S,B}$ | Venchiarutti et al. (2011) |
| – | 2009 | SO202-INOPLEX, ALOHA, SAFe | North Pacific | $^{230}$Th$_D$, $^{231}$Pa$_D$ | Hayes et al. (2013) |
| GA02 | 2011 | JC 057 | Southwest Atlantic | $^{230}$Th$_{D,S,B}$, $^{231}$Pa$_{D,S,B}$ | Deng et al. (2014) |
| GA03 | 2010 | US GT10 and GT11 | North Atlantic | $^{230}$Th$_{D,S,B}$, $^{231}$Pa$_{D,S,B}$ | Hayes et al. (2015b) |

Sediment top core $^{231}$Pa/$^{230}$Th

| – | 1966–97 (multiple) | global | total particulate | Holocene compilation$^a$
| – | 2009 | R/V M. Dufresne, MD173/RETRO3 | global | total particulate |
| | | | | Burckel et al. (2015, 2016) |

Table 3. Observations used for comparison with the model simulations.

$^a$ http://climotope.earth.ox.ac.uk/data_compilations

5 Results

5.1 Circulation

As mentioned before, our model is part of a global general circulation model, but instead of solving the Navier-Stokes equations, our tracers are advected by the circulation fields of a previous simulation of the dynamical ocean model. Since the overturning circulation is of importance for the redistribution of the tracers, we here present basic results.

Figure S1 of the supplementary document presents the Overturning Stream Function (OSF) of the Atlantic Ocean. The OSF is defined as the zonally (through the basin) and vertically (from the surface downwards) integrated meridional component of the current velocity. We use this as a measure for the Atlantic Meridional Overturning Circulation (AMOC). The upper overturning cell transports 14 Sv ($1$ Sv = $10^6$ m$^3$s$^{-1}$) on average. Observations suggest higher values of about $19 \pm 5$ Sv (Cunningham et al., 2007; Rayner et al., 2011; Sinha et al., 2018). The lower cell has an overturning strength of about 6 Sv, which is stronger than the about 2 Sv from estimates (e.g. Talley et al., 2003). This overestimation is mostly due to the fact that the AMOC is shallow. The AMOC reaches about 2500 m depth, whereas observational studies show the deep water sinks down to about 4000 m. At around 30° N the AMOC has weakened notably, which is consistent with some studies (e.g. Johnson, 2008), but the Antarctic Bottom Water (AABW) does not go as far north as other studies suggest (e.g. 45° N in Van Aken, 2011).
Figure 4. Particle concentrations from the PISCES model at the surface ocean. Observations are represented as coloured discs (Brun-Cottan et al., 1991; Druffel et al., 1992; Lam et al., 2011, 2015). The unit of every modelled and measured particle concentration is mgm$^{-3}$.

The Antarctic Circumpolar Current is also an important feature for large-scale ocean circulation. The through-flow at Drake Passage is a good measure for that. In our model the flux through Drake Passage is 200 Sv, which slightly overestimates recently reported values (e.g. 173 ± 11 Sv in Donohue et al., 2016).

5.2 Particles

Figure 4 shows the surface concentrations of total POC, big calcium carbonate, big biogenic silica and total lithogenic particles. Observations are plotted as coloured discs on top of the modelled concentrations. The modelled biogenic particles include living matter. For the model, we assume POC includes all phytoplankton and microzooplankton (not mesozooplankton since it may swim away), calcium carbonate contains the assumed fraction of CaCO$_3$ in the phytoplankton, and biogenic silica includes living diatoms. The modelled concentrations and patterns of total POC compare well with the observations (Fig. 4a).

For instance, coastal and equatorial Pacific POC concentrations are both in the model and the observations elevated compared to other regions, albeit that the spatial extent of the oligotrophic regions appears to be too small in the model. We compare our modelled CaCO$_3$ (big, fast-sinking, calcium carbonate particles), with the big calcium carbonate particles from observations. As the model tries to represent CaCO$_3$ with only one size class, neither comparing with only big particles nor comparing with total CaCO$_3$ is completely fair. Incidentally, we have data of big CaCO$_3$ for both the Atlantic and Pacific Ocean, whereas only for the Atlantic Ocean we have small particle data. Even though the meridional patterns of big CaCO$_3$ particles are reproduced, its concentrations are generally overestimated, especially in the Gulf of Alaska (Fig. 4b). Contrarily, total observed [CaCO$_3$], which is only provided along section GA03 where small particulate CaCO$_3$ measurements are available, is higher than the prediction of our modelled (only big) CaCO$_3$ particle concentration. The model produces a reasonable spatial distribution of biogenic silica: there are more elevated values in the high latitudes, but concentrations are underestimated at the surface at low latitudes (Fig. 4c).
Figure 5. Particle fields at the GA03 North Atlantic GEOTRACES transect; observations (Lam et al., 2015) as coloured discs.
The recent large dataset obtained from the full-ocean depth GEOTRACES GA03 transect (Lam et al., 2015) provides an opportunity to analyse the performance of PISCES in more detail. PISCES generally produces the right order of magnitude for all four biogenic particles (small and big POC, calcium carbonate and biogenic silica), but there still remain some shortcomings in their distributions (Fig. 5a–d).

- The total POC concentration in Fig. 5a is up to a factor of 4 underestimated in the deep oligotrophic ocean. In the upper 200 m of the ocean the model overestimates the observations, though at some points at the surface the POC concentration is underestimated (also Fig. 4a). In both the observations and the model the fraction of big POC varies from zero to 0.6 (Fig. 5b), but the spatial distributions are very different. More detailed results and discussion on the simulation of POC are to be found in Aumont et al. (2017).

- The model underestimates the CaCO$_3$ concentrations from 70$^\circ$ W to 25$^\circ$ W by a factor of 2 to 10, but east of that up to Africa the prediction lies close to or overestimates the observations. In the Canary Basin and up to Portugal (meridional transect at the right), the model reproduces the right order of magnitude, but it does not reproduce the correct profiles everywhere (Fig. 5c).

- Biogenic silica concentrations are generally reproduced but the model overestimates the higher concentrations observed along the western margin (Fig. 5d).

Finally, the modelled total lithogenic particle concentration at the surface shows, as expected, a close resemblance with dust deposition patterns (Fig. 2), and mostly compares well with observations (Fig. 4d). Only near the coasts of the USA and of Portugal the model strongly underestimates lithogenic particle concentrations. Concerning the deep ocean, our model captures quite nicely the general distribution at the GA03 transect (Figs. 5e and 5f). However, the concentrations near the western boundary are strongly underestimated, especially those of big lithogenic particles. Our model reproduces the observed fraction of big lithogenic particles of ~0.1 to ~0.3 in most of the deep ocean, but it underestimates the much larger fraction of big particles observed in the upper 200 m of the ocean (0.1–0.2 in the model versus 0.3–0.9 in the observations).

5.3 Thorium-230 and protactinium-231

$[^{230}\text{Th}]_D$ stands for the concentration of $^{230}\text{Th}$ that is in the dissolved phases. Similarly, $[^{230}\text{Th}]_S$ is the concentration of $^{230}\text{Th}$ that is adsorbed onto the small particles S, $[^{230}\text{Th}]_B$ the concentration adsorbed onto the big particles B; and similarly for $^{231}\text{Pa}$. The modelled dissolved distributions of $^{230}\text{Th}$ and $^{231}\text{Pa}$ are underestimated at the surface (Figs 6 and 7). Below the surface, $[^{230}\text{Th}]_D$ is much better captured by the model (also Fig. 8a for the GA03 transect). However, observations show lower values near the bottom in the western part of the GA03 section and at 45$^\circ$ W, associated with more intense scavenging related to respectively nepheloid layers and manganese oxides from hydrothermal vents, which are not produced in the simulation (Figs 8a and 8b).

In the intermediate and deep waters of all the oceans, modelled $[^{231}\text{Pa}]_D$ is generally of the correct order of magnitude but is strongly overestimated below 2500 m depth (Fig. 8b), especially in the Pacific Ocean (Fig. 7c,d).

The concentrations of the adsorbed phases of $^{230}\text{Th}$ at GA03 are presented in Figs 8c and 8e. In the deep ocean, modelled $[^{230}\text{Th}]_S$ and $[^{230}\text{Th}]_B$ have lower values than $[^{230}\text{Th}]_D$, which is consistent with observations. Furthermore, compared with Dutay et al. (2009), we have notably improved $[^{230}\text{Th}]_S$ and $[^{230}\text{Th}]_B$. Other global modelling studies have not reported adsorbed concentrations of $[^{230}\text{Th}]_D$ and $[^{231}\text{Pa}]_D$. However, the model still underestimates the observed $[^{230}\text{Th}]_S$ and $[^{230}\text{Th}]_B$.

Contrarily, small $^{231}\text{Pa}$ particles are overestimated in our model below 1500 m at the GA03 transect (Fig. 8d). Big $^{231}\text{Pa}$ particles are simulated more realistically (Fig. 8f).
Figure 6. The dissolved thorium-230 activity at four depth levels (mBq m$^{-3}$), observations as discs at the same colour scale.

Figure 7. The dissolved protactinium-231 activity at four depth levels (mBq m$^{-3}$), observations as coloured discs.
Figure 8. Radionuclide concentrations at the GA03 North Atlantic GEOTRACES transect. (a) and (b) display dissolved concentrations, (c) and (d) show the amounts on small particles, and (e) and (f) those on big particles. Everything is in (mBq m$^{-3}$). Observations (Hayes et al., 2015a) are shown as coloured discs.
Figure 9. Radionuclide concentrations in mBq m$^{-3}$ at stations in the North Pacific (around ALOHA station, 158° W, 23° N) and North Atlantic Oceans (around the BATS station, 64° W, 29° N). The left two panels (a,b) display $[^{230}\text{Th}]_D$, and the right two (c,d) $[^{231}\text{Pa}]_D$. The line is the model, and the speckles are the observations.

Table 4. Relative global budget of $^{231}\text{Pa}$ and $^{230}\text{Th}$ in the different particulate phases (“global stock”) in percentages. Globally averaged fluxes in the different phases (“global particle flx”), and the same but for the North Atlantic Ocean (44–24° W, 25–56° N) and the Weddell Sea (44–24° W, 76–63° S), all in percentages associated with each particle type.

<table>
<thead>
<tr>
<th></th>
<th>POC</th>
<th>bSiO$_2$</th>
<th>CaCO$_3$</th>
<th>Litho.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{231}\text{Pa}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>global stock</td>
<td>35.5</td>
<td>10.5</td>
<td>3.1</td>
<td>50.8</td>
</tr>
<tr>
<td>global particle flx</td>
<td>16.5</td>
<td>53.5</td>
<td>15.8</td>
<td>14.2</td>
</tr>
<tr>
<td>North Atlantic flx</td>
<td>16.5</td>
<td>25.7</td>
<td>15.6</td>
<td>42.1</td>
</tr>
<tr>
<td>Southern Ocean flx</td>
<td>5.6</td>
<td>93.7</td>
<td>0.6</td>
<td>0.1</td>
</tr>
<tr>
<td>$^{230}\text{Th}$</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>global stock</td>
<td>21.3</td>
<td>3.2</td>
<td>24.3</td>
<td>51.2</td>
</tr>
<tr>
<td>global particle flx</td>
<td>5.9</td>
<td>9.9</td>
<td>75.8</td>
<td>8.7</td>
</tr>
<tr>
<td>North Atlantic flx</td>
<td>4.4</td>
<td>2.8</td>
<td>69.9</td>
<td>22.9</td>
</tr>
<tr>
<td>Southern Ocean flx</td>
<td>9.7</td>
<td>71.1</td>
<td>18.9</td>
<td>0.3</td>
</tr>
</tbody>
</table>

To show clearly the change of $[^{230}\text{Th}]_D$ and $[^{231}\text{Pa}]_D$ with respect to depth, profiles are plotted in Fig. 9. $[^{230}\text{Th}]_D$ is linearly increasing downwards, which matches with the observations, but below 3000 m near Bermuda, $[^{230}\text{Th}]_D$ increases where it should decrease according to the observations. The shape of $[^{231}\text{Pa}]_D$ matches that of the observations for the upper 2 km, below which our model overestimates the observations up to a factor four at the bottom of the ocean.

Globally in the model, only 0.3% of the $^{231}\text{Pa}$ sits in the particulate pool, and for $^{230}\text{Th}$ this is 1.3%. The rest is in the dissolved phase. Observational data show that more than 10% of $^{230}\text{Th}$ sits in the particulate pool, typically adsorbed onto small calcium carbonate particles. The underestimation by our model can be explained by the fact that we only have big, fast-sinking CaCO$_3$ particles in the model. Since the big particles are removed quickly, these cannot act as a realistic CaCO$_3$-associated $^{230}\text{Th}$ pool without depleting $^{230}\text{Th}$, and thus we underestimate the particulate radionuclide concentrations.

Table 4 gives two types of information on the adsorbed phases. One is the amount fraction of radionuclide adsorbed onto each particle (“global stock”). The other is the fraction of the flux carried by each type of particle (the other rows) for the global
ocean and two regions of the ocean. No distinction is made between big and small particles (they are summed). The stock and the flux are not necessarily the same, because the big particles have a different settling velocity from the small particles. For example, only for POC and lithogenic particles we have slowly sinking particles on which much of the radionuclides are adsorbed, whereas the big affinity of Pa to bSiO$_2$ mostly results in a strong export (and similarly for Th on CaCO$_3$).

Only a small amount of $^{230}$Th is adsorbed onto biogenic silica (3 %), though the amount is larger for $^{231}$Pa (11 %). However, the global settling flux of $^{231}$Pa is primarily (54 %) determined by bSiO$_2$, particularly due to the high bSiO$_2$ fluxes in the Southern Ocean. Most of the modelled particulate $^{231}$Pa and $^{230}$Th is on the lithogenic particles, but lithogenic particles account for only 14 % of the $^{231}$Pa flux and 9 % of the $^{230}$Th flux. If lithogenic particles from nepheloid layers were included, this fraction would be higher. The flux contribution is also different from what is in the pools when we look at CaCO$_3$: only 24 % of the $^{230}$Th is on calcium carbonate, but CaCO$_3$ is for 76 % responsible for the $^{230}$Th export. These discrepancies between the contribution of each particle type to the flux and to the stock of radionuclides arise from the different settling velocities for each type of particle.

The relative contributions of the different particulate phases also vary for different regions of the ocean. Most notably, biogenic silica is for 94 % responsible for $^{231}$Pa export in the Southern Ocean.

Compared to Dutay et al. (2009), the improvement of the $^{230}$Th profile shape is improved, but only to a small extent due to the large improvement in the POC representation (Aumont et al., 2017), because the POC accounts for only 6 % of the vertical transport of $^{230}$Th (Table 4). The improvement is mostly due to the addition of lithogenic dust particles and the adjusted CaCO$_3$ dissolution. Lithogenic particles and CaCO$_3$ hardly dissolve compared to POC and hence the downward particle flux remains constant, which is in agreement with 1-D models which show linear profiles of $^{230}$Th$_D$ (e.g. Roy-Barman, 2009).

### 5.4 Sedimentation flux ratio of $^{231}$Pa/$^{230}$Th

The sedimentation flux of the total adsorbed $^{231}$Pa/$^{230}$Th ratio captures the general patterns of the upper sediment core $^{231}$Pa/$^{230}$Th concentration ratio (Fig. 10). Consistent with observations, the model produces more elevated $^{231}$Pa/$^{230}$Th ratio values in the Southern Ocean, the northern part of the Indian Ocean, the Pacific Ocean, and along the coastal upwelling regions. However, at some places, like much of the Southern Ocean, our model tends to overestimate the ratio derived from the sediment core observations.

### 6 Discussion

We succeed to generate the global patterns of the dissolved nuclide concentrations. However, we underestimate radioactivities in the surface waters (Figs 7a and 6a). This shortcoming may be due to the instant equilibration between the dissolved and the adsorbed phases (Henderson et al., 1999). After decay of U into $^{231}$Pa and $^{230}$Th, the tracers instantly adsorb onto the particles in the surface ocean and are exported from the mixed layer. The equilibrium scavenging approach is commonly used in Pa/Th modelling (Siddall et al., 2005; Dutay et al., 2009; Gu and Liu, 2017). It allows the model to use partition coefficients that can be directly constrained by observations (although consensus values for these coefficients are still not available). A non-equilibrium approach to scavenging could be considered, but it would necessitate the use of adsorption and desorption coefficients ($k_+ , k_-$) that are currently very poorly constrained by observations. Observations shows equilibrium partition coefficient $K$ values varying (decreasing) with particle flux (Roy-Barman et al., 1996; Chase et al., 2002), and we apply these in our simulation (i.e. lower $K$ values for large, fast sinking particles). This parameterisation produces effects that are similar to those of a non-equilibrium system for fast sinking particles.
The reversible scavenging model uses partition coefficients $K_{ij}$ for the different isotopes $i$ and particles $j$. Many studies provide constraints on these coefficients but estimations vary strongly between different studies. Small particles are the most important scavengers and largely control the shape of the vertical profile of the tracers (Dutay et al., 2009). This also shows from sedimentary isotope records (Kretschmer et al., 2011). This is explained by the specific surface of small particles, which is larger than that of big particles. Therefore higher adsorption values are set for small particles compared to the bigger particles of the same type (namely, 5 times higher for POC, and 10 times higher for lithogenic particles). Compared to Dutay et al. (2009), we succeed to simulate the tracer concentrations using reasonable $K$ values. This is due to improvement in (especially small) particle concentrations, which were generated with the lability parametrisation of POC (Aumont et al., 2017), the change of the CaCO$_3$ dissolution parameterisation, and the addition of lithogenic dust in our ocean model. This shows that at least two particle size classes are needed to simulate dissolved and particulate thorium and protactinium. Our model does not include small particles for all types (there are neither small CaCO$_3$ nor small bSiO$_2$ particles), even though we expect that better results can be reached upon adding those particles akin to small POC and small lithogenic particles.

On the GA02 transect, the correlation coefficient $r$ of the data–model comparison of [${}^{230}$Th]$_D$ is 0.80, which is close to what was reported by Rempfer et al. (2017) in their simulations without bottom-boundary scavenging. On the GA03 section, $r = 0.78$. The correlation between model and observation are presented as scatter plots (supplementary document, Fig. S2).

There are a couple of interesting features to note on the comparisons. Firstly, the hydrothermal plume over the ridge results in ${}^{230}$Th-poor seawater that is not reproduced by the model (red triangle in Fig. S2, GA03). Secondly, in the western boundary currents, very low dissolved ${}^{230}$Th concentrations are observed due to strong nepheloids and/or possibly strong deep ventilation from the north. Neither of these processes are represented in the model. The lack of nepheloids has an especially large impact.
on the GA02 transect, which has a relatively large number of measured profiles near the western boundary. Finally, between 32 and 20° W, the model tends to underestimate $^{230}$Th. The value of the correlation index is not that important, because the goal of this study is not to give a perfect model–data comparison.

The provided dust flux does not distinguish between different dust particle sizes or types. Furthermore, dust deposition is uncertain; therefore we chose a dust flux that was available to the ORCA2 configuration of NEMO, and its biogeochemistry has been tested with that dust flux. However, given the significant impact of dust particles to thorium and protactinium concentrations, it would be useful to look into the effect of different dust deposition fields, and of using different dust particles size classes. A good model of $^{230}$Th (and other isotopes of thorium) could even constrain the sporadic and uncertain dust deposition, but all this falls outside the scope of the present study.

Our model adds 80% of the dust deposition into the fast-sinking lithogenic particle compartment (corresponding to $\varnothing > 51 \mu m$), and only 20% goes into the slowly-sinking compartment (corresponding to $\varnothing \leq 51 \mu m$). This is necessary to reproduce the distributions of lithogenic particles. However, airborne dust particles typically have a diameter of smaller than $20 \mu m$ (Knippertz and Stuut, 2014) and thus fall clearly within the small size class of less than $50 \mu m$. Recently, there have been observations of aerosols larger than $20 \mu m$ (Van Does et al., 2016), but they do not reach far enough into the atmosphere above the open ocean to explain the high concentration of big lithogenic ocean particles. The explanation for the apparently required high fraction of big lithogenic particles is that smaller aerosols aggregate in the upper layers of the ocean. Moreover, though more hypothetically, there may be strong aggregation with biogenic particles just below the surface, below which the aggregates partly disaggregate again to result in the $\sim 0.2$ big lithogenic fraction in the deep ocean (Fig. 5f).

The underestimation of lithogenic particle concentrations at the western boundary is expected. The reason is that we only have dust deposition as a source of lithogenic particles, whereas nepheloid layers are not included. Nepheloid layers are at least locally an important source of lithogenic (and biogenic) particles (Lam et al., 2015). With the transport of $^{230}$Th and $^{231}$Pa through the western boundary current, a significant portion may be scavenged. Moreover, the periodic transport through the North Atlantic Gyre would result in lower $[^{230}$Th$]_D$ and $[^{231}$Pa$]_D$ throughout a large part of the North Atlantic Ocean, possibly improving the concentrations in the deep ocean. Therefore it will be useful to include nepheloid layers in the future. We have not done this so far, because we do not know how to model nepheloid layers. Except for trivial models, like the one of Rempfer et al. (2017) who forced an additional constant scavenging rate in the bottom box of the ocean model, no large-scale, prognostic nepheloid models have been developed.

We overestimate the radionuclide activity in the deep ocean, which is partly because we underestimate particle concentrations. Especially thorium adsorbs well onto lithogenic particles, which are underestimated in the West Atlantic Ocean (in the subsurface, west of about 43° W, Fig. 5e). Below 2 km depth, also POC is underestimated (Fig. 5a), even though the lability parameterisation improved the distribution by over an order of magnitude compared with previous versions of PISCES (Aumont et al., 2017). Small POC and the small lithogenic particles are the only small particles. Their underestimation in the deep ocean results in an overestimation of the radionuclides in the deep ocean. In our simulation, $[^{230}$Th$]_D$ is not that much overestimated (outside the Arctic Ocean). However, $[^{231}$Pa$]_D$ is strongly overestimated in the deep Pacific and Atlantic Oceans.

Clearly the model does not remove $^{231}$Pa efficiently enough from the deep ocean (Figs 7c,d, 8b and Fig. 12–upper panel). Two likely reasons may be that the waters are not well ventilated in the model (older than in reality), or that there is not enough scavenging. The Atlantic OSF (Fig. S1) shows that the upper overturning cell is too shallow compared to observational studies, so there is too little ventilation. This means that $^{231}$Pa can build up in the deep water due to sluggish ventilation of the physical model (Dutay et al., 2002; Biastoch et al., 2008). Moreover, the AABW has weakened in the deep North Atlantic Ocean near the high-[$^{231}$Pa$]_D$ region (Fig. 12–upper panel), which may also contribute to the high dissolved $^{231}$Pa concentrations. The volume transport of the lower cell is about 6 Sv near 20° N and still 2 Sv near 40° N, which is in the order of magnitude of
what is reported by literature. Moreover, the relationship between sediment $^{231}$Pa/$^{230}$Th at any given site and the overturning circulation is very complex. In general, any increased opportunity for protactinium to scavenge would increase the sedimentary $^{231}$Pa/$^{230}$Th ratio. Specifically, a slower overturning would mean more Pa-scavenging and a higher ratio “just downstream of the sites of deep water formation” (Luo et al., 2010). Similarly, relatively stronger scavenging of Pa means such a higher sedimentary $^{231}$Pa/$^{230}$Th, which we can see in the Southern Ocean and some coastal areas where the concentration of $b$SiO$_2$ is high. For these reasons, it is not obvious whether the weak overturning is large enough to explain the discrepancy between the modelled and the observed $[^{231}\text{Pa}]_D$.

In reality, there are many regions in the North Atlantic Ocean where there is sediment resuspension and where there are nepheloid layers (Gardner and Sullivan, 1981; Lam et al., 2015; Gardner et al., 2017). This is consistent with the fact that our model underestimates lithogenic particle concentrations in the West Atlantic Ocean (Fig. 5e). The additional lithogenic particles would scavenge more $^{231}$Pa, resulting in lower $[^{231}\text{Pa}]_D$. Even though the enforced scavenging occurs near the floor and the western boundary of the ocean, a strong flux of water passes through the latter region, and is transported through the North Atlantic Gyre and through the rest of the Atlantic, diluting high tracer concentrations. The small POC and lithogenic particles are now underestimated in much of the deep ocean. They would contribute to lower radio tracer concentrations as well.

Rempfer et al. (2017) confirmed that an additional bottom sink affects $^{231}$Pa and $^{230}$Th significantly. They used a homogeneous extra scavenger in their model grid’s bottom grid cell. Therefore, it would be worth testing if a realistic distribution of nepheloids would result in the right amount of scavenging.

Other particles may include resuspended (nepheloidal) biogenic particles but also manganese and iron hydroxides that are not included in our model, and a smaller class of calcium carbonate and biogenic silica particles in addition to the big-particle classes that are already in the model. Manganese oxides are available especially near hydrothermal vents, but also throughout the Pacific Ocean in low concentrations but much higher than in the Atlantic Ocean. Indeed, it has been argued that hydrothermal inputs may provide additional removal of $^{231}$Pa and $^{230}$Th (Lopez et al., 2015; Rutgers van der Loeff et al., 2016; German et al., 2016), and recently this is confirmed based on an analysis of the $\sim$10° S zonal GP16 transect in the Pacific Ocean (Pavia et al., 2017).

Finally, the particle concentration effect (Honeyman et al., 1988) should be taken into account in future models, particularly when regions of high particle concentration (e.g., ocean margins and nepheloid layers) are included.

### 6.1 Effect of scavenging by $b$SiO$_2$ on the $^{231}$Pa/$^{230}$Th sedimentation flux ratio

Previously, it was suggested that Pa has a stronger affinity for bSiO$_2$ than Th has, i.e. $F_{\text{Pa/Th,}b\text{SiO}_2} > 1$ (Henderson et al., 1999; Chase et al., 2002; Dutay et al., 2009). This “standard view” has weakened over time, so it is often accepted that $F_{\text{Pa/Th,}b\text{SiO}_2} \gtrsim 1$ (Venchiarutti et al., 2011; Rutgers van der Loeff et al., 2016; Rempfer et al., 2017). We argue here that it is Th which has the stronger affinity to bSiO$_2$ ($F_{\text{Pa/Th,}b\text{SiO}_2} < 1$), similarly (though not quite) like other particles.

Our standard simulation (with $F_{\text{Pa/Th,}b\text{SiO}_2} = 1$) yields a too high sedimentation $^{231}$Pa/$^{230}$Th ratio compared to top-core sediment observations below diatom-rich areas such as the Southern Ocean. In that region, bSiO$_2$ largely controls the particle scavenging of the two tracers, especially that of $^{231}$Pa (Table 4). In order to estimate how strongly the model depends on the value of the bSiO$_2$ partition coefficient we performed a sensitivity experiment where we set $K_{\text{Pa,}b\text{SiO}_2} = 0.4$ Mgg$^{-1}$ and $K_{\text{Th,}b\text{SiO}_2} = 1.0$ Mgg$^{-1}$ such that now $F_{\text{Pa/Th,}b\text{SiO}_2} = 0.4$ (Table 2).

As a result of this reduction, $^{231}$Pa/$^{230}$Th flux ratio is not that much overestimated anymore in diatom-rich regions (Fig. 11). This result suggests that protactinium has a weaker affinity to biogenic silica than thorium has, though the fractionation is closer to 1 than that of other particle types (Table 2). This result is consistent with Geibert and Usbeck (2004) whose laboratory study
Figure 11. Sedimented $^{231}\text{Pa}/^{230}\text{Th}$ ratio when we set $K_{\text{Pa},\text{biSiO}_2}/K_{\text{Th},\text{biSiO}_2} = 0.4$. Top core measurements are presented as discs.

shows no definitive affinity of either Th or Pa to biogenic silica. Their average $K$ values actually suggest that thorium has a higher affinity to biogenic silica.

We included lithogenic particles in the model from deposited dust. Since lithogenic particles have a strong relative affinity with $^{230}\text{Th}$ ($K_{\text{Pa},\text{Lith}}/K_{\text{Th},\text{Lith}} = 0.2$) and since they are mostly prevalent in the (northern) Atlantic Ocean, much of the $^{230}\text{Th}$ is scavenged in the Atlantic Ocean. Calcium carbonate $K_{\text{Pa}}/K_{\text{Th}}$ is even smaller (0.024) and is present throughout much of the Atlantic but not in the Southern Ocean. This leaves protactinium to be scavenged by biogenic silica in the Southern Ocean when it arrives there through the AMOC. Therefore, even with the smaller-than-conventional $K$ ratio of 0.4 for biogenic silica, the familiar pattern of higher values of $^{231}\text{Pa}/^{230}\text{Th}$ in the Southern Ocean compared to most of the rest of the ocean is still reproduced.

7 Conclusion

The purpose of this study is two-fold. Firstly, we set out a model of $^{231}\text{Pa}$ and $^{230}\text{Th}$, complete with all the necessary particle improvements and additions. This includes an improved underlying particle dynamics from NEMO–PISCES as well as the addition of lithogenic particles. We have succeeded in this, and the model has been presented and implemented such that it can be used for future studies, including for the modelling and validation of ocean circulation in the past.

Secondly, this model helps us to study the interplay between particle and water transport that control the $^{231}\text{Pa}$ and $^{230}\text{Th}$ profiles. We have shown that by improving on the particles, we improved the radionuclide distributions and fluxes, and we have shown to what extent the different particle phases drive the scavenging of $^{231}\text{Pa}$ and $^{230}\text{Th}$. 
Figure 12. Dissolved protactinium-231 (upper panel), and thorium-230 (lower panel) at the Drake Passage (GIPY5) and West Atlantic (GA02) transects (mBq m$^{-3}$); observations as discs. The Atlantic OSF, in Sv, is superimposed as a contour.
Dissolved $^{230}$Th and $^{231}$Pa concentrations are realistic in the intermediate-depth ocean (big improvement compared to Dutay et al. (2009)) but not in the upper part of the ocean. A finite equilibration time between the different radionuclide phases may help. The model can be extended to include this in future versions. It would double the number of adsorption/desorption parameters whose values should be determined through a careful literature and model sensitivity study.

In the deep ocean, the overestimation of $^{230}$Th and $^{231}$Pa in several regions is likely to be caused, at least partly, by missing nepheloid particles, but also manganese oxides (from hydrothermal vents) may improve the distributions. Of course, reported adsorption/desorption parameters vary a lot between different studies, meaning that different, yet still plausible, combination of partition coefficients could better describe the available data. Additionally, the circulation may be too weak, notfreshening AABW fast enough, and hence $[^{230}$Th$]_D$ and $[^{231}$Pa$]_D$ become too high near the ocean floor.

8 Code availability

The mathematical variable names correspond to the Fortran variable as described in Table S1 of the supplementary document. We encourage the reader to use our model, NEMO–ProThorP, to build extended and improved models. We have implemented two particle size classes of adsorbed nuclides, which is the minimum that is needed to produce good results. Instead of introducing a new tracer for every particle type, we only distinguish between “adsorbed onto small particles” and “adsorbed onto big particles”, meaning that one is restricted, in this set-up, to include only particles that sink with the two respective settling speeds for scavenging. Whereas this is somewhat restricting, it is computationally efficient, and it restricts the number of degrees of freedom (which is usually a good thing in complex models). NEMO–ProThorP can also be used to set up a non-instant equilibration model (with a $k_+$ and $k_-$) that may yield better concentrations in the upper ocean.

The underlying model, NEMO 3.6 (svn revision 5283), can be downloaded from http://www.nemo-ocean.eu/ (Madec and the NEMO team, 2016) after creating a login. NEMO includes the biogeochemical PISCES model (Aumont et al., 2015). For reproducibility purposes, version 0.1.0 of the radionuclide and lithogenic particles model code can be obtained at https://dx.doi.org/10.5281/zenodo.1009065 (Van Hulten et al., 2017a). However, we plan to make this code available as part of the NEMO model.

The NEMO model is available under the CeCILL free software licence, modelled after the GNU GPL. The lithogenic particles and $^{230}$Th/$^{231}$Pa-specific code is licensed under the same terms, or, at your option, under the GNU General Public License version 3 or higher. The authors do appreciate if, besides the legal adherence to copyleft and attribution, they are informed about the use of the code.

Finally, the most important raw model output files are available at PANGAEA (van Hulten et al., 2018). The Julia scripts used for the statistics are included in the supplementary document. This may be useful to reproduce the results or further inspect the model output.

9 Author contributions

The model and the simulations were designed by MvH, JCD and MRB. MvH implemented the code and performed the simulations. The manuscript was prepared by MvH with close collaboration and major contributions from MRB and JCD.

The authors declare that they have no conflict of interest.

Acknowledgements. We would like to thank Marion Gehlen and Olivier Aumont for the discussions on the calcite parameterisation in PISCES, among other things. The first author is grateful to Jörg Lippold for both the discussion and encouragement that also helped this work.
This study was supported by a Swedish Research Council grant (349-2012-6287) in the framework of the French–Swedish cooperation in the common research training programme in the climate, environment and energy agreement between VR and LSCE, for the project “Particle transport derived from isotope tracers and its impact on ocean biogeochemistry: a GEOTRACES project in the Arctic Ocean”. This study was partly supported by the project “Overturning circulation and its implications for the global carbon cycle in coupled models” (ORGANIC, The Research Council of Norway, grant no. 239965).

The authors wish to acknowledge the use of Ferret, a product of NOAA’s Pacific Marine Environmental Laboratory. Most of the plots in this paper were created by the Ferret visualisation library ComPlot (Van Hulten, 2017). Finally, the language Julia was used for some of the statistics.
References

Aken, H.M. van: GEOTRACES, the hydrography of the Western Atlantic Ocean, 2011.


