

25th June 2018

Dear GMD Editor & Reviewers,

Re. Revision #2 of gmd-2017-257: A General Lake Model (GLM)

We thank you again for the opportunity for our paper to be considered for publication in GMD, and are very grateful for the additional comments received on the first revision of the paper. We have found the comments very insightful and they have guided us to significantly improve this version of the manuscript.

The revised paper includes the suggested corrections to the equations figures and text, and updated detail in some of the figures and sub-sections as suggested by the reviewers. The detailed replies are provided below.

Based on this revision, we are now confident to release the code-base associated with this paper and results presented herein. The code is therefore stamped on GitHub as v3.0. A DOI for the code has been added to the paper, and a separate DOI for the example files presented herein has also been generated.

We thank you again for the significant time and effort that have gone into the discussion and look forward to your decision.

Kind Regards

A handwritten signature in blue ink, appearing to read 'MH', is located below the 'Kind Regards' text.

Matthew Hipsey, on behalf of all co-authors.

Anonymous Referee #1

Overview

This paper describes a one-dimensional hydrodynamic lake model GLM, which has already been used for a number of applications in the scientific literature. The paper is generally well written and structured. It gives a comprehensive overview of the model structure and equations, and shortly describes available tools for pre- and post-processing and for linking the model to other models.

I have rejected the previous version of this manuscript because there were far too many errors already in the first few equations. This has certainly been improved in the current version. However, I feel there are still too many errors and inconsistencies. These are problematic for two reasons. First, given the large number of errors reported in the first and this second review, I have to assume that there are still quite a few remaining errors that were not spotted by any of the reviewers. This reduces the trust both in the model description and in the model itself, as the reader never knows whether the equations are only wrongly written or also wrongly implemented. Second, the inconsistencies in the notation make it sometimes hard for the model user to understand the details. I am aware that writing a flawless model description is a very tedious work, but this can't be avoided

REPLY: We very much appreciate the substantial time invested by the reviewer in combing through the details of this paper, and apologise we have rushed previous submissions without an adequate level of checking. The review process has not only led to improved manuscript but in going through the review the model code has advanced in several areas. In particular, the consistency of the notation has matured over the course of the reviews, and we feel the current revision has now stabilised in terms of notation and has improved clarity. We would be happy to acknowledge the reviewer specifically in the paper given the significant improvements they have made, should they wish to forego anonymity.

General comments to model description

The total lake water balance is missing in the model description. It is shortly mentioned in the caption of Figure 2, but it should be described in detail in a separate section.

REPLY: Agreed, we have updated Section 2.2 to include this.

Section 2.3.3: I don't understand why three different parameterizations for saturation vapor pressure are included, which should give the same results within 1-2% at most, but only one parameterization for the latent heat flux (eq. 22), where different parameterizations can yield very different evaporation rates (see, e.g., Rosenberry et al., 2007, doi:10.1016/j.jhydrol.2007.03.018).

REPLY: We understand clearly the point. The reason is due to the organic nature of the model development where different users and developers have sought to use specific algorithms for particular applications. It is our hope that over time we can enrich the options for other algorithms (such as evaporation, as suggested) to ensure the model's wide applicability to diverse lake types.

Section 2.6.1: It is somewhat confusing that first a total energy balance is introduced as being relevant for mixing, but subsequently only parts of that energy balance are used in each step. I think it would be clearer for the reader to first describe the individual energy components, and then the different steps in the mixing calculation, and remove the total energy balance, which is not explicitly used in the model.

REPLY: We considered this suggestion and would prefer to provide the overall energy requirement and amount available. We note that most aspects of the model are also similar, for example the water balance or surface heat balance, in that they have a sequential solution within the model. In our response to Rev 2 we aimed to improve the description in this section and feel the overall summary of the energy terms in

this form helps the reader see the overall picture before the specific steps are explained.

Section 2.6.2: It is not clear to which part of the water column this mixing regime applies (the wording includes "below the epilimnion", "below the thermocline" and "in the hypolimnion". I assume it applies to all layers that are not within the surface mixed layer, according to Eq. (53), but this should also be made clear in the text.

REPLY: It is right that the mixing algorithm is applied to all layers that are not in the surface mixed layer. We modified the text throughout this section to improve clarity and consistency.

Section 2.8. The wave properties are calculated based on the average lake depth, but the wave velocity in the i th layer is then calculated from the local depth of this layer. I don't really know, but wouldn't it be more consistent to estimate also the wave properties from the local depth of the layer? It seems to me you could potentially underestimate local wave heights and thus resuspension in shallow waters with the given approach.

REPLY: The horizontally averaged nature of the model and this parameterisation means that we are only able to compute a single set of wave characteristics across the entire lake surface (ie. wave length and wave height are assumed constant) - and for this computation the depth to the lake bottom is required, for which we assume an average lake depth to get the mean wave conditions. Once computed, we then translate the orbital velocity based on these wave characteristics down the water column to get as a function of depth from the water surface, and this is where the layer specific depths are used. This is now clarified in the opening text of the section.

Code availability: I was not able to clearly identify the source code for GLM version 2.4. or 3.0 (probably not yet available?) or previously published versions on the GitHub repository. Also, the information on the GLM website (<http://aed.see.uwa.edu.au/research/models/GLM/Pages/documentation.html>) is not updated and does not link to the GitHub repository. All release versions, also past versions to allow reproducing previous calculations, should be published on GitHub and linked from the GLM website.

REPLY: It appears you accessed an archived version of the GLM web page dating back some time. The main download page that has version 2.4 and 3.0 bundles is here, including links to source code in GitHub:

http://aed.see.uwa.edu.au/research/models/GLM/latest_release.html

Comments to Figures

Figure 2: Fonts are rather small. The water balance should be described in the text rather than in the figure caption. I also think the notation used here is not entirely consistent with the model description.

REPLY: Figure updated, improved fonts and updated caption. New opening to Section 2.2 now provides overview of lake scale water balance.

Figure 3: increase fonts, albedo_mode is not introduced in the text.

REPLY: albedo_mode is removed from the caption text to be consistent with other sections (input configuration file details will be reported under the user instructions on the model website rather than in this paper). Fonts will be updated at proofing

Figure 4: what is the grey area in Fig 4a? The area where $f_{BEN} < 0.2$? if so, the color scale should be adapted accordingly. Also, the grey area is at least 80% of AS, but in Fig 4c, the fraction is always $>30\%$. Is this for the same lake?

REPLY: Figure updated.

Figure 5: How is it possible that the net heat balance is always positive for Ellen Brook Nature Reserve? This should lead to a massive heating of the lake throughout the year. Also net LW radiation is not shown in this figure. Is it missing from the budget? Please check. In the legend, ϕ_{LW} should be replaced by $\phi_{LW} \text{ Net}$

REPLY: Apologies, there was a problem with that plot for that version of the model that has been rectified.

Figure 6: use larger font for conditions, these are hardly readable even zoomed to > 100%. Shouldn't SF be multiplied with Δt in the top boxes (and RF in box 4 from the top)? Are the equations in boxes 6 and 7 from the top correct? RF has a unit, so it should not be in the exponent. And typical values of RF (unit m/s) are on the order of 10^{-6} , so $\exp(-RF)$ is virtually nothing. In the third box from the bottom, the first equation must be wrong (check units). It is not clear what happens in the lowermost case (transition from snow to white ice?).

REPLY: Thanks for highlighting the problems with the figure; the figure has been re-drafted. The readability is improved plus we now distinguish more clearly between the rainfall and snowfall components that land on the water vs on the ice/snow, and have corrected the other issues following review of the corresponding code.

Figure 9: What drives vertical transport in case a) where vertical diffusivity in the hypolimnion should be zero? And what causes the local minima in the vertical profiles in cases a) and c)? If a tracer is released in the bottom cell and moves upward by diffusion, its concentration should always be monotonically decreasing upward. If other processes (such as river intrusions) are responsible for these minima, why don't they exist in case b)?

REPLY: To clarify, the passive tracer diffusing out of the sediment is not just entering into the bottom layer, but also into all layers simultaneously. For the bottom layer the area of the sediment in contact with the water layer is 100%, but for the remaining layers the area of sediment in contact with the water depends on the layer height range relative to the hypsographic shape. For layers near the surface the sediment area relative to layer area is very small, so the input is less noticeable. It may be the case that layers in the hypolimnion (or elsewhere) have a different layer area to sediment area ratio, and this leads to a relatively different areal loading rate. As it is a 1D model, the input is instantly homogenised across the layer leading to the vertical variation in concentration noticeable in the layers of the hypolimnion (Figure 9a). For the case of constant diffusivity, the diffusion rate is high and it becomes smoothed and monotonic (Figure 9b), but for the depth dependent diffusivity model the diffusion rate is less with distance from the thermocline and so the smoothing is more modest (Figure 9c). Figure caption updated to avoid confusion.

Figure 10: α_{inf} is not very clearly drawn, also what exactly is δz_{inf} ? In general, it would be useful if the discretisation in Eqs. (60) ff could be more clearly linked to the Figure, using exactly the same notation (Δz_j and δx_{inf} in the figure, but Δz_{jinf} and Δx_{inf} in the equations).

REPLY: Figure updated, including consistent symbol notation, and improved depiction of the vertical excursion length scale.

Figure 12c: why is there bottom water withdrawal around day 20?

REPLY: Thanks for pointing this out. In the test case with the activated bottom outlet, the bottom withdrawal was only opened during flooding conditions. We have added this information to the Figure caption

Figure 14: increase fonts, the subscripts are impossible to read at 100% size. HS, L and T are not used in the figure or text, remove from caption. Is the lower limit of the height axes at 1 m rather than 0 m on purpose?

REPLY: Figure updated.

Figure 15: This is a useful overview of the code structure. However, I think two things are nowhere explained in the text: what is the difference between `do_model` and `do_model_nonavg`? And what is `do_bubbler`?

REPLY: Figure updated, and in addition the (now three) entry points to the model are explained.

Figure 16: Fonts are very small at 100% size.

REPLY: Updated

Figure 17: "exposed sediment" is impossible to read at 100% size. Figure 17b can be removed.

REPLY: Updated, without the (b) panel, and updated detail.

Figure 18: As I understand, the grey shaded areas show the 80% uncertainty range of model projections based on the posterior uncertainty of the model parameters. However, it seems strange to me that this projection can deviate so much from the observed hypolimnion temperatures. These observations have a very small uncertainty (maybe 0.1 °C?), and such large deviations should lead to very low values for the likelihood in the Bayesian analysis.

REPLY: The figure does have three shades, and it is the winter band (80th) that is deviating notably in the hypolimnion, as you have noted. The optimisation for this simulation used surface and bottom and thermocline depth to optimise the objective function. In this case the model has some sensitive parameters related to mixing that lead to full mixing vs stratification. This parameter combinations were less likely, but did contribute to a wide tail in the posterior probability. It is possible the algorithm could have been conditioned better, and this was intended to highlight the potential for this approach with GLM.

Detailed comments to equations

Eq. (1): replace $Ab-1 + 0.5(Ab-Ab-1)$ with $0.5(Ab + Ab-1)$.

REPLY: Updated

Eqs. (2) and (3) are now correct, but might be easier to read if V_b was defined as the level below H_{mi} rather than V_b-1 .

REPLY: Yes indeed! Updated.

Eq. (4): According to Eq. (8), ϕE is positive if water is evaporated, thus E is negative (line 26) and should be added rather than subtracted in Eq (4), or maybe better, the minus sign should be removed in line 26?

REPLY: Agreed, updated

Explain in a few words the intention of Eqs. (5) and (6), where, depending on meteorological conditions, precipitation will either be added to the water volume, or to the snow cover, referring to section 2.4. Also, I think the notation is inconsistent between here and section 2.4. Here, SF , and RF are the fractions of rain and snow that are added to the fluid water volume. In section 2.4, they are used also for rain and snow that are added to the snow cover.

REPLY: Thank you for this suggestion, and noting the slightly different intention of these variables between section 2.2 and 2.4. We have updated accordingly (including updating Figure 6).

Eq. (8). In order to optimize the calculation speed, consider replacing the calculated density of the surface layer by an average water density. This is an option for all equations where a calculated density is used as a

multiplying (or dividing) factor. Density variations in lakes are in almost all cases $< 1\%$, which is negligible compared to other uncertainties in model parameters. These are generally only relevant if density differences are calculated.

REPLY: Thank you for this suggestion, we will review the code with this in mind. For now, we compute the density for all layers anyway for mixing, and utilise that for this equation.

Eq. (9): Why is fsw not included in the third option? I think it would make sense to have the option available to scale SW radiation also in this case.

REPLY: Agreed - we added this to the code and updated Eq.

Eq. (10) replace C with Cx

REPLY: Updated

Eq. (11) I did not see the base for this equation in Luo et al (2010).

REPLY: The equation came from our own data; Luo was cited as an alternative source for a similar function. Wording slightly modified.

Eq. (12a) $\sin(x - \pi/2)$ and $\sin(x + \pi/2)$ could be simplified to $-\cos(x)$ and $\cos(x)$, respectively.

REPLY: we left as is

Eq. (12c) I think RHx should be multiplied rather than divided by 100.

REPLY: We have settled on RH as %, therefore, this division by 100 is removed.

I have the impression that Eqs (20c) and (20d) should be valid for different units of ea as they are written here. Please check.

REPLY: To the best of our knowledge they are in hPa, consistent with our units for ea.

Eq. (23) Something must be wrong with all three equations. They all yield results that are far away from the correct saturation vapor pressure. Saturation vapor pressure is 6.1 hPa for 0 °C. But for TS = 0 °C, Eq. (23a) results in $\exp(0.7858) = 2.2$, Eq. (23b) in $\exp(0) = 1$ and Eq. (23c) in $10^0 = 1$. Also the exponent in c is far too high for any temperature other than 0°C.

REPLY: Apologies for this poor checking. The Tabata (1973) is the main one being used within the code and this was implemented properly, but the equation as written in the paper with a spurious Ts; we have now removed the other two options (which weren't being used) and updated accordingly.

Eq. (25c) The nominator should be 2, rather than LD in front of the square root according to Markfort et al. (also because otherwise the units are not correct). Furthermore, $\cos^{-1}(x)$ is ambiguous. It is sometimes used for arccos(x), and sometimes for $1/\cos(x)$.

REPLY: Updated

Eq. (32) Shouldn't it be ϕSW_0 also in the second line of the equation?

REPLY: Yes, updated.

Eq. (39): Should it be ρSML instead of π_i in the last term? If not, the term in parentheses could be simplified to sum of $\Delta z_i \pi_i (h_i - h_{sml})$

REPLY: Simplified as suggested

Eq. (41) g needs to be added to the two equations for reduced gravity.

REPLY: Updated

Eq. (42) I think it should be Δt rather than t in the upper equation?

REPLY: Checked and updated

Eq. (49): I think this equation should have a minus sign. N_2 is usually defined to be positive if the stratification is stable, i.e. if the density of the upper layer is smaller than the density of the lower layer. Here it is the opposite.

REPLY: Updated - thank you for spotting this. Our function was correct in the code, and took in ρ_1 (upper) and ρ_2 (lower), and then computed $\rho_2 - \rho_1$, which was reported backwards in the paper.

Eq. (52): I don't understand the last term of this equation. $h_s - |h_{in}|$ seems to me to be almost the same as $z_{in}|$ (depending on how exactly the latter is defined) so the term in parentheses should be almost zero?

REPLY: This term is the depth over which the inflow plunges in one day (rather than the amount from the beginning of its transit, which you may be expecting?)

Eq. (53): the meaning of σ is unclear. The unit of N_2 is s^{-2} , that of its variance would be s^{-4} , but this obviously can't be what is meant here.

REPLY: Apologies for the confusion here again, this was checked during the revision for unit consistency but somehow the notation update didn't occur. The intention for σ was the length scale of the water column corresponding to the N_2 distribution variance. The variance of the buoyancy distribution is computed by first finding the 1st moment of the N_2 distribution (ie. centre of buoyancy in metres above the bottom). This symbol should have been changed to dz_σ^2 . In this case the units are m^2 .

Eq. (54): should be $fdif$ in the exponents.

REPLY: Updated

Eqs (56) ff. Maybe I looked at the wrong place, but I was not able to find all the corresponding equations in Fischer et al. (1979) and Antenucci et al. (2005). Since Fischer et al. is rather voluminous, it might be useful to mention the respective equation number from the original publication. I did not see Eqs. (56) and (57) anywhere in Fischer, and the corresponding Eq. (2) looks rather different in Antenucci. Eq. (58) corresponds to eq (4) in Antenucci, but $\tan \alpha$ is replaced by $\tan \phi_{inf}$, and the \tan is in the denominator here and in the numerator in Antenucci (not sure whether that is on purpose there, though).

REPLY: Thank you again for your keen eye here. We have cleaned up this section with careful cross checking that the angles are reported right, and a review of the original references on which these were based. Since the Fischer book is harder to access we make a general reference to it, and now rely on the Imberger and Patterson eq (which uses a slightly different form), the Antenucci paper, and we now also cite a nice analysis using a similar approach by Ayala et al 2014.

Eq. (61) and following line: I don't completely this. The second equation in line 9 can be simplified, using eq. 61, to $z_{infj} = z_{infj-1} + \delta z_{infj-1}$. But according to the first equation in line 9 after reducing the index j by 1, also $z_{infj-1} + \delta z_{infj-1} = h_s - h_{ij-2}$. So that means $z_{infj} = h_s - h_{ij-2}$?

REPLY: This section has been reviewed and updated to be more clear, and these sub-scripts updated to prevent confusion here.

Eq. (62) For a given Δz_{inf} , and a given discharge, the flow velocity should be smaller if the channel is wider, i.e. if the angle α_{inf} is larger. But this equation implies the opposite. Please check.

REPLY: Thank you for noticing this mistake; The velocity is Q divided by channel area, which is computed based on the water depth (Δz). In the code it is $Q * \cos(\alpha_{inf}) / (\Delta z \sin(\alpha_{inf}))$, which we mistakenly wrote in Eq 62 with $\tan(\alpha_{inf})$ as a numerator.

Eq. (71): the equation calculating the seepage as a function of lake head is somewhat inconsistent as it applies the entire lake head to the entire area, and all water is removed from the bottom layer, i.e. it in fact treats the lake as a rectangular box.

REPLY: Yes, this is the case. Mostly this option is used in shallow systems, but in a future iteration we plan to take this suggestion and partition the seepage from the overlying layers based on their respective extent of exposure to sediment area.

Details in the text

p5/l15: ΔH_{mi} is 0.1 m here and 0.01 m in Table 1

REPLY: Updated in Table 1

p6/l4: Section 2.6 only describes layer merging by mixing from above, i.e. in the surface mixed layer. Can layer merging also occur in deeper waters, and if yes, under what conditions?

REPLY: Layer merging and splitting below the thermocline occurs if they contract or expand due to inflow/outflow processes affecting these layers, beyond the prescribed thickness limits. The sentence below this in this paragraph is now:

"Layer volumes change due to depth-specific changes in mixing, inflows and outflows, and thickness limits, Δz_{min} and Δz_{max} , are enforced to adequately resolve the vertical density gradient, generally with fine resolution occurring in the metalimnion and thicker cells where gradients are weak."

p8/l16: remove "either"?

REPLY: Updated

p 9/10: ζ is not atmospheric diffusive radiation, but "a constant related to atmospheric diffuse radiation" according to Table 1. It remains unclear, what this means.

REPLY: Updated; This is as reported in the supporting reference.

p11/l8: ϕ_{SWS} is defined here as the fraction heating up the surface layer but in Table 1 as the radiation flux crossing the water surface (should be ϕ_{SW0} in the table?).

REPLY: These two symbols are different (the former is the amount remained in the SML, whereas the latter is the total incoming amount. The table is updated to have both.

p11/l23: A_{Ben}/A_s is a fraction, not a percentage.

REPLY: Updated

p11/l15: unit for vapor pressure needs to be given here or in Table 1.

REPLY: This was in Table 1, listed as hPa

p15/l20ff: I am not sure I understand the procedure for calculating ice melting here. I understand that first

ϕ_{SW0} is calculated from eq. 31, then T_0 is calculated such that $\phi_0 = \phi_{net}$ (how is this done?), , and if T_0 is then equal or larger than the melting temperature T_m , melting is determined from eq 30. Is that correct? Consider revising the text in this section to clarify.

REPLY: This subsection has been re-written to more clearly explain the heat conduction approach and associated boundary conditions that control ice layer changes.

p18/l5: replace possible with available?

REPLY: 18 doesnt seem relevant to this comment, so I am assuming this refers to P19 Line 5. Updated as suggested.

p19/l9: the notation z_{msl} is inconsistent, as all other layer thicknesses are named Δz .

REPLY: The notation is that Δz is referring to a layer thickness whereas z is referring to depth from the surface. In this case they are essentially equivalent, but since the SML may have more than one layer, we prefer to keep the dz_{msl}/dt notation here. The text is however updated however to refer to depth rather than thickness.

p20/l2: difference to what?

REPLY: The sentence is updated: "*... the potential energy that would be released by mixed layer deepening is computed as the difference in the moments of layer masses in the epilimnion (surface mixed layer) about the lake bottom, relative to the well-mixed condition.*"

p21/l16-18: this is not clear.

REPLY: P21 is a figure so I am assuming this refers to P20 Line 16-18, where the shear velocity is computed. This text is updated.

p23/l6: if α_{TKE} is interpreted as diffusivity, why then $K_z = CHYP$ and not $K_z = \alpha_{TKE}$?

REPLY: Thanks for noticing the discrepancy - when we revised the paper we replaced α_{TKE} with CHYP, but missed this reference in the text.

p23/l10: "contains 85% of N_2 " sounds strange, as N_2 is not a property that can be reasonably summed up across layers. Table 1 defines the same variable as the "fraction that contains 85% of the N_2 variance". This is even less clear. Is it calculated by summing up all N_2 values and then taking the volume for which the sum is 85% of the sum for the entire lake? If so, this is virtually the same as the volume that contains 85% of the density difference between the top and the bottom of the lake.

REPLY: Thanks for pointing out that this remains confusing, we have updated to make this more clear. To clarify, N_2 varies following an approximate normal distribution with height, and the centre of the distribution is the height where the centre of buoyancy is located, computed as the 1st moment of the vertical N_2 distribution. The vertical length scale which captures one standard deviation of this distribution is then computed (see also comment above; dz_{σ^2}). The volume being referred to here, \bar{V}_{N_2} is the volume of the lake above the height where this standard deviation is positioned. For convenience, this is called the 85% volume since a symmetric normal distribution is assumed and the volume does not account for the volume below the 1st standard deviation (~15% of N_2 variance).

p23/l15: which density difference?

REPLY: This is referring to the rate of working doen by the inflow as it plunges. Updated to say "*... the difference in density between the inflow water and layer into which it inserts*".

p25/l9: delete "the tangent of"

REPLY: Updated

p26/l9: really daily time step? The time scale for river intrusions is usually rather minutes to hours than days. So does this ever take more than one step?

REPLY: For many applications of modest to large sized lakes this can take many days; for small lakes and reservoirs though it can complete the insertion in just one step.

p26/l14: should be Δz_{in} instead of z_{in} in the equation.

REPLY: I think it is correct as is, the equation is computing the vertical change in elevation of the parcel from the previous time; the term in the brackets ($h-z$) is the height of the top of the inflow after the days travel where as $h-\Delta z$ is the thickness of water above the inflow.

p27/l12: should refer to Eq. (52)?

REPLY: Updated

p31/l5: verb is missing.

REPLY: description updated.

p31/l8: If no weir is present I assume Q_{Ovfl} is the same as Eq. (73), but with $Q_{weir} = 0$?

REPLY: Yes, description updated.

p31/l9: Is Δh_s the result of eq. (4)?

REPLY: Yes, description updated.

p35/l5: iti -> it

REPLY: Updated

p37/l2: I can't remember having read anything about solar shading in the model description.

REPLY: Updated - shading now mentioned when introducing f_{sw} , and cross referenced to this point also.

p37/l16: In Figure 16, glmttools is called GLMr.

REPLY: Figure updated

References: I did not check the list, but noticed that Spigel and Imberger (1980) is missing

REPLY: Updated to include this reference. Reference list also checked for formatting throughout.

Comments to Table 1

This table is very useful, but it needs to be thoroughly checked and corrected. I checked only a small part of the variables, the following list of inconsistencies and missing variables is therefore certainly incomplete:

I think the following variables used in the paper are missing in Table 1 (incomplete list):

Cwn, H0, NSW, Ksoil ea, θ_s , θ_a , δz_{soil}

- The variables α_b and β_b should go to Lake domain.
- Use per mil rather than ppt for parts per thousand, as the latter is generally used for parts per trillion.
- Check definition of θ_S
- Use Kelvin without degree sign.
- AC is AWS in Eq. 25b?
- most of the h's should be height above datum rather than height above bottom.
- fw is calculated in Eq. (83), not Eq. (78).

REPLY: The variables e_a , θ_S , θ_a , δz_{soil} were already present, but we have added H_0 , NSW , K_{soil} so thank you for identifying these. The other changes have been updated, except the lower case h's are all above the lake bottom by definition (lower case h is all from the lake bottom, and upper case H is from the datum).

Furthermore, the variables are mostly ordered alphabetically, but not completely, and the assignment of variables to the different classes of variables can be ambiguous. It is therefore often rather difficult to find a variable in the Table.

REPLY: The table has been refined to include all variables under sequential headings:

Indices

Time variables

Lake domain (volumes, areas, heights and depths)

Other simulation variables and general parameters (listed alphabetically)

Finally, it is unclear which parameter values are hard-coded and which can be modified by the user. Some parameters are defined as configurable, but for some others, which can also be defined by the user according to the text, just one value is given

REPLY: In the case where the numbers in the "value" column are for hard-coded parameters the otherwise they are the default suggestions. We have now referred to in the comments column the section of the configuration file where the parameters can be set. A new footnote is added to clarify the entries in this column.

Anonymous Referee #2

Overview

I appreciate the work that has been done on this revision. The layer splitting and merging scheme is now much better described and makes sense (end of p. 4 to middle of p. 6). The big Table 1, even though it might feel excessive, makes sure that everything has its proper definition and units. I still have some comments, mostly minor, and will recommend publication contingent on minor revision, even though I feel like I still haven't sufficiently combed the equations for inconsistencies.

REPLY: Many thanks for the time you have spent on the revised manuscript and we are grateful for the suggestions for corrections and improvements. Specific responses are provided below.

Some things that I still consider somewhat major:

1. P. 5, 1st paragraph: This starts to explain the split/merge scheme, and refers to Fig. 1, which doesn't show layers at all. You might want to add a separate figure that schematically shows a split and a merge. Fig. 1 can also benefit from having sensible heat flux included. So you'll want to reference the current Fig. 1 for the processes that lead to splitting and merging, and another figure (or panel) for the split/merge scheme itself.

REPLY: We note that Figure 1 does depict layers, albeit relatively faint. You are right they do not depict the merging/splitting scheme. We have adopted the suggestion for a new figure in the mixing section (now Figure 8) that depicts the mixing changes on the layer structure. It is somewhat idealised but can help readers interpret the content in the section.

2. The paragraph on p. 8, lines 9-13 is a rather good example of a brief description of the general concept that the following sub-sub-sections will fill in. Other sections should have more like this.

REPLY: Thanks for noting this and the suggestion. Sub-Sections that previously include a brief general concept description include 2.8, 2.7 and 2.3; we have therefore made modifications to the openings of sub-sections 2.2, 2.4, 2.5 and 2.6, plus we revisited 2.8.

3. Eqs. 37 and 38 are some that I decided to take a fairly close look at. In eq. 37, it seems to have the correct units, but the only thing in the equation that is suggestive of a wave number is the K-H billow length, which only has a single value, and other terms don't even have that. The "per wave number" part of the definition suggests that you might be able to do an integral across wave numbers to get a value per mass, but I'm not seeing how this works. In eq. 38, the units don't work out right. The part inside the brackets seems to have the right units (meters squared per second squared), but then is multiplied by a length.

REPLY: Many thanks for identifying this. We introduced some confusion in the units table definitions for these two terms. Both terms are based on an approximation of TKE made available per mass (m^2/s^2), that is then integrated over the depth of the layer being raised. As you correctly identified, this was accounting for the depth integration in the case of E_{TKE} , and not for E_{PE} . Whilst the units matched the definition per wavenumber, that was not our intent as this is a bulk estimate across the spectrum, and the unit description is corrected.

4. Table 1 should have an explanation in the header that says that a hyphen in the units column means no units. This made me ask myself what a hyphen in the value column means, and I don't think it is all that consistent. Some are distinctly independent variables (t and z). Some indicate the space-time location of a feature of the system (such as $t_{sub b}$ and H). To what extent might these be characterized as calculated? $[t]$ seems to be more of a device used in coding the algorithm. $E_{sub TKE}$ and $E_{sub PE}$ seem more clearly to be calculated. $U_{sub 10}$ seems to be time-series input (observed). $e_{sub *}$ is altogether undefined in the table. $E_{sub PE}$ seems like it should be defined as potential energy within the stratified water column *per mass*, but see the previous comment about eq. 38.

REPLY: Table 1 has been updated, including fixes to the above mistakes, and consistency with the value descriptions (and associated footnote).

5. Fig. 10: The inset should have a better 3-D effect. Consult an expert to add color and sheen so that it is unambiguous which direction each surface points. I don't understand why $\alpha_{sub inf}$ is called a "half angle". It's the angle between the two sloping sides of the idealized river channel, right?

REPLY: The figure has been updated for this revision; whilst we didnt get the 3D effect it is hopefully less ambiguous now what the angles are referring to.

Minor comments:

1. P. 3, lines 12-14: I hesitate to call FLake a 1-D model. Maybe more like 0.5-D, because of its predefined shapes of temperature profile curves.

REPLY: Yes, this is a bulk model; the citation to Kirillin et al., (2011) is removed (but remains referred to elsewhere so is left in the list).

2. P. 3, line 26: It would be more convincing that GLEON is a large group if you explicitly state a number of participants.

REPLY: Thank you for the suggestion; it now reads:

"... availability to a broad community (e.g., GLEON has >500 members from around 50 countries)."

3. P. 6, line 3: This sentence seems very confusing. When you say energy, to you mean heat energy, TKE, or something else? Density instability promotes mixing, so it doesn't make sense to overcome instability to trigger mixing. And "accounting for" can be taken as either a cause or an effect; I'd rather see it expressed more explicitly as an effect of mixing.

REPLY: Thank you for observing this inaccurate wording. The sentence is redrafted as :

"When density instabilities occur between adjacent layers, or when sufficient turbulent kinetic energy becomes available to overcome stable density gradients, then layers merge, thereby accounting for the process of mixing."

4. Hyphen police: See my previous comments. P. 6, line 19: "Well mixed" is an adverb + adjective, so should not have a hyphen. Captions to Figs. 2 and 5: "Time series" should have no hyphen. P. 14, line 2: "Length scale" without a hyphen.

REPLY: Updated; we should have them all now, and will also consider as the paper goes through to type-setting.

5. P. 6, line 27: The word "latent" should be before "heat flux".

REPLY: Updated

6. Eqs. 5 and 6: It seems that you are defining the water level as the level of liquid water if no ice were displacing it, while ice thickness is simply ice volume/area. In other words, when freezing occurs, water is withdrawn from the top layer of liquid water and transferred to the ice layer. This needs to be very explicit in order to understand these equations.

REPLY: Section 2.2 introduction has been modified to include the volume balance, and this is now made explicit.

7. P 8, line 10: "Uppermost" should be one word.

REPLY: Updated

8. P. 8, line 13: I don't think you've defined "RHS". Some might know this, but perhaps not all.

REPLY: Updated

9. P. 10, eq. 13: Is zenith-angle dependence already built into the definition of incoming light? Otherwise direct sunlight should have this formula with z divided by the cosine of the zenith angle, and diffuse light should use some effective average zenith angle.

REPLY: Depending on the solar radiation option (Eq 10 in the new revision), users can either input measured incoming solar data or predict it based on the bird model. The albedo for all options (Eq 13) accounts for the zenith angle, if the albedo options 2 or 3 are adopted.

10. P. 10, line 11: "Adsorption" refers to material being incorporated; for radiation, it should be "absorption".

REPLY: Updated

11. P. 12, line 9: Add "water vapour" before "mixing ratio".

REPLY: Updated

12. The journal's spelling standard apparently is British English, and this manuscript mostly follows that, but I noticed at least one occurrence of "vapor" on p. 16, line 2.

REPLY: Updated

13. P. 12, eq. 23b: Is there a citation for August-Roche-Magnus?

REPLY: Note this Eq has been updated, and this options removed.

14. P. 13, line 4: I'm not sure whether "within the internal boundary layer" implies that you need to define an internal boundary-layer height and measure at multiple heights within that range, or whether it only needs to be measured near the surface.

REPLY: To improve clarity we have reworded this sentence:

"To ensure data provided is from within the internal boundary layer over the lake surface, this option requires the provision of wind speed, air temperature and relative humidity data from near the lake surface (e.g., 2-10 m, depending on lake size), supplied at approximately hourly resolution."

15. P. 15, last line: "Penetrative" misspelled.

REPLY: Updated

16. P. 20, line 12: The formula at the beginning of this line should be multiplied by g .

REPLY: Updated

17. P. 23, line 11: There should be a semi-colon before "however".

REPLY: Updated

18. P. 25, line 9: ϕ should be the angle of slope. I think this is better than just saying "slope" which is often expressed as a ratio, and I think "tangent" here is unintentional.

REPLY: Updated

19. The citation and the reference give different dates for Makler-Pick et al.

REPLY: Updated

20. Mueller et al. (2016) is out of alphabetical order.

REPLY: Updated

21. Snortheim et al. is missing a date.

REPLY: Updated

22. Tennessee Valley Authority (TVA) needs to be alphabetized according to the way that it is stated in the citations. It is not alphabetized correctly for either "TVA" or "Tennessee Valley Authority". I suggest leaving the citations as they are and alphabetizing it as "TVA (Tennessee Valley Authority)".

REPLY: Updated as suggested

A General Lake Model (GLM 3.0) for linking with high-frequency sensor data from the Global Lake Ecological Observatory Network (GLEON)

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Matthew R Hipsey^{1,*}, Louise C Bruce¹, Casper Boon¹, Brendan Busch¹, Cayelan C. Carey², David P Hamilton³, Paul C. Hanson⁴, Jordan S. Read⁵, Eduardo de Sousa¹, Michael Weber⁶, Luke A. Winslow⁷

¹ UWA School of Agriculture & Environment, The University of Western Australia, Crawley WA, 6009, Australia

10 ² Department of Biological Sciences, Virginia Tech, Blacksburg VA, USA

³ Australian Rivers Institute, Griffith University, Nathan QLD, 4111, Australia

⁴ Center for Limnology, University of Wisconsin - Madison, Madison WI, USA

⁵ Center for Integrated Data Analytics, U.S. Geological Survey, Middleton WI, USA

⁶ Department of Lake Research, Helmholtz Centre for Environmental Research - UFZ, Magdeburg, Germany

15 ⁷ Department of Biological Sciences, Rensselaer Polytechnic Institute, Troy NY, USA

* Correspondence to: Matthew R. Hipsey (matt.hipsey@uwa.edu.au)

Keywords: lake, stratification, mixing, water balance, climate change, water quality, observatory network,

Word count: 13,000 words (text); 24,000 words (text+references+figures&tables+appendices)

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Abstract. The General Lake Model (GLM) is a one-dimensional open-source code designed to simulate the hydrodynamics of lakes, reservoirs and wetlands. GLM was developed to support the science needs of the Global Lake Ecological Observatory Network (GLEON), a network of researchers attempting to use lake sensors to understand lake functioning and address questions about how lakes around the world respond to climate and land-use change. The scale and diversity of lake types, locations and sizes, as well as the expanding observational datasets, created the need for a robust community model of lake dynamics with sufficient flexibility to accommodate a range of scientific and management questions relevant to the GLEON community. This paper summarises the scientific basis and numerical implementation of the model algorithms, including details of sub-models that simulate surface heat exchange and ice-cover dynamics, vertical mixing and inflow/outflow dynamics. We demonstrate the suitability of the model for different lake types, that vary substantially in their morphology, hydrology and climatic conditions. GLM supports a dynamic coupling with biogeochemical and ecological modelling libraries for integrated simulations of water quality and ecosystem health, and options for integration with other environmental models are outlined. Finally, we discuss utilities for the analysis of model outputs and uncertainty assessments, model operation within a distributed cloud-computing environment, and as a tool to support learning of network participants.

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1 Introduction

Lakes and other standing waters support extensive ecosystem services such as water supply, flood mitigation, hydropower, aesthetic and cultural benefits, as well as fisheries and biodiversity (Mueller et al., 2016). Lakes are often considered to be “sentinels of change”, providing a window into the sustainability of activities in their associated river basins (Williamson et al., 2009). They are also particularly susceptible to impacts from invasive species and land use development, which often lead to water quality deterioration and loss of ecosystem integrity. Recent estimates have demonstrated their significance in the earth system, contributing to heterogeneity in land surface properties and feedbacks to regional and global climate through energy, water and biogeochemical transfers (Martynov et al., 2012; Cole et al., 2007). For example, Tranvik et al. (2009) suggest carbon burial in lakes and reservoirs is substantial on a global scale, on the order of 0.6 Pg yr^{-1} , or four times the oceanic burial rate.

Given the diversity of lakes among continents, region-specific pressures and local management approaches, the Global Lake Ecological Observatory Network (GLEON: gleon.org) was initiated in 2004 as a grass-roots science community with a vision to observe, understand and predict freshwater systems at a global scale (Hanson et al., 2016). In doing so, GLEON has been a successful example of collaborative research within the hydrological and ecological science disciplines. GLEON aims to bring together environmental sensor networks, numerical models, and information technology to explore ecosystem dynamics across a vast range of scales - from individual lakes or reservoirs (Hamilton et al., 2015) to regional (Read et al., 2014; Klug et al., 2012), and global extents (Rigosi et al., 2015; O’Reilly et al., 2015). Ultimately, it is the aim of the network to facilitate discovery and synthesis, and to provide an improved scientific basis for sustainable freshwater resource management.

Environmental modelling forms a critical component of observing systems, as a way to make sense of the “data deluge” (Porter et al., 2012), allowing users to build virtual domains to support knowledge discovery at the system scale (Ticehurst et al., 2007; Hipsey et al., 2015). In lake ecosystems, the tight coupling between physical processes and water quality and ecological dynamics has long been recognised. Models have capitalized on a comprehensive understanding of physical processes (e.g., Imberger and Patterson, 1990; Imboden and Wüest, 1995) to use hydrodynamic models as an underpinning basis for coupling to ecological models. Such models have contributed to our understanding of lake dynamics, including ~~aspects such as~~ [applications associated with](#) climate change (Winslow et al., 2017), eutrophication dynamics (Matzinger et al., 2007), harmful algal bloom dynamics (Chung et al., 2014), and fisheries (Makler-Pick et al., ~~2009~~[2011](#)).

In recent decades a range of 1, 2, and 3-dimensional hydrodynamic models has emerged for lake simulation. Depending on the dimensionality, the horizontal resolution of these models may vary from metres to tens of kilometres with vertical resolutions from sub-metre to several metres. As in all modelling disciplines, identifying the most parsimonious model structure and degree of complexity and resolution is challenging, and users in the lake modelling community often tend to rely on heuristic rules or practical reasons for model choice (Mooij et al., 2010). High-resolution models are suited to studying events that occur at the time scale of flow dynamics, but are not always desirable for ecological studies over longer

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time scales due to their computational demands and level of over-parameterisation. On the other hand, simple models may be more agile for a particular application, and more suited to parameter identification and scenario testing workflows. However, it has been the case within GLEON that simple models are often less applicable across a wide variety of domains, making them less generalizable, which is a key requirement of synthesis studies. Despite the fact that there is a relatively large diversity of models and approaches for aquatic ecosystem simulation (Janssen et al., 2015), it is generally agreed that to improve scientific collaboration within the limnological modelling community, there is an increasing need for flexible, open-source community models (Trolle et al., 2012). Whilst acknowledging that there is no single model suitable for all applications, a range of open-source community models and tools can enhance scientific capabilities, and foster scientific collaboration and combined efforts (Read et al., 2016). There are ~~several~~ examples of such initiatives being successful in the oceanography, hydrology and climate modelling communities.

With this in mind, the General Lake Model (GLM), a one-dimensional (1D) hydrodynamic model for enclosed aquatic ecosystems, was developed. The lake modelling community has often relied on 1D models, which originated to capture lake water balance and thermal stratification dynamics (e.g., Imberger and Patterson, 1981; Saloranta and Andersen, 2007; Perroud et al., 2009; Kirillin et al., 2011; Stepanenko et al., 2013). The use of 1D structure is justified across a diverse range of lake sizes given the dominant role of seasonal changes in vertical stratification on lake dynamics, including oxygen, nutrient and metal cycling and plankton dynamics (Hamilton and Schladow, 1997; Gal et al., 2009). Despite advances in computing power and more readily available 3D hydrodynamic drivers, 1D models continue to remain attractive as they are easily linked with biogeochemical and ecological modelling libraries for complex ecosystem simulations. This allows 1D models to be used to capture the long-term trajectory and resilience of lakes and reservoirs to climate change, hydrologic change and land use change. For example, such models have been used to model long-term changes to oxygen, nutrient cycles, and the changing risk of algal blooms (e.g., Peeters et al., 2007; Hu et al., 2016; Snortheim et al., 2017). Furthermore, the low computational requirements of this approach relative to 3D models is more suited to parameter identification and uncertainty analysis, making it an attractive balance between process complexity and computational intensity.

GLM emerged as a new open-source code in 2012, with the design goal of balancing the complexity of dimensional representation, applicability to a wide range of standing waters, and availability to a broad community (e.g., GLEON [has >500 members from around 50 countries](#)). The scope and capability of the model has developed rapidly with application to numerous lakes and lake-types within the GLEON network and beyond (e.g., Read et al., 2014; Bueche et al., 2017; Snortheim et al., 2017; Weber et al., 2017; Menció et al., 2017; Bruce et al., 2018). It is unique in that its suitability now ranges from ephemeral wetlands and ponds to deep lakes, from natural systems to heavily managed man-made reservoirs, and across climatic regions. Given that individual applications ~~of the model~~ rarely engage the full array of features or describe the full details of the model structure, the aim of this paper is to present a complete description of GLM, including the scientific background (Section 2), and model code organization (Section 3). The approach to coupling with biogeochemical models is also discussed (Section 4) since a main objective of the model development is to intimately link with biogeochemical models to support exploration of stratification and vertical mixing on the dynamics of biogeochemical cycles and lake ecology. Finally, an overview of the use of the model within the context of GLEON specific requirements

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for model analysis, integration and education (Section 5-6) is described. In order to better define the typical level of model performance across these diverse lake types, a companion paper by Bruce et al. (2018) has undertaken a systematic assessment of the model's error structure against 31 lakes.

2 Model Overview

5 2.1 Background and layer structure

The 1D approach adopted by GLM resolves a vertical series of layers that capture the variation in water column properties. Users may configure any number of inflows and outflows, and more advanced options exist for simulating aspects of the water and heat balance (Figure 1). Depending on the context of the simulation, either daily or hourly meteorological time series data for surface forcing is required, and daily time series of volumetric inflow and outflow rates can also be supplied.

10 The model is suitable for operation in a wide range of climate conditions and is able to simulate ice formation, as well as accommodating a range of atmospheric forcing conditions.

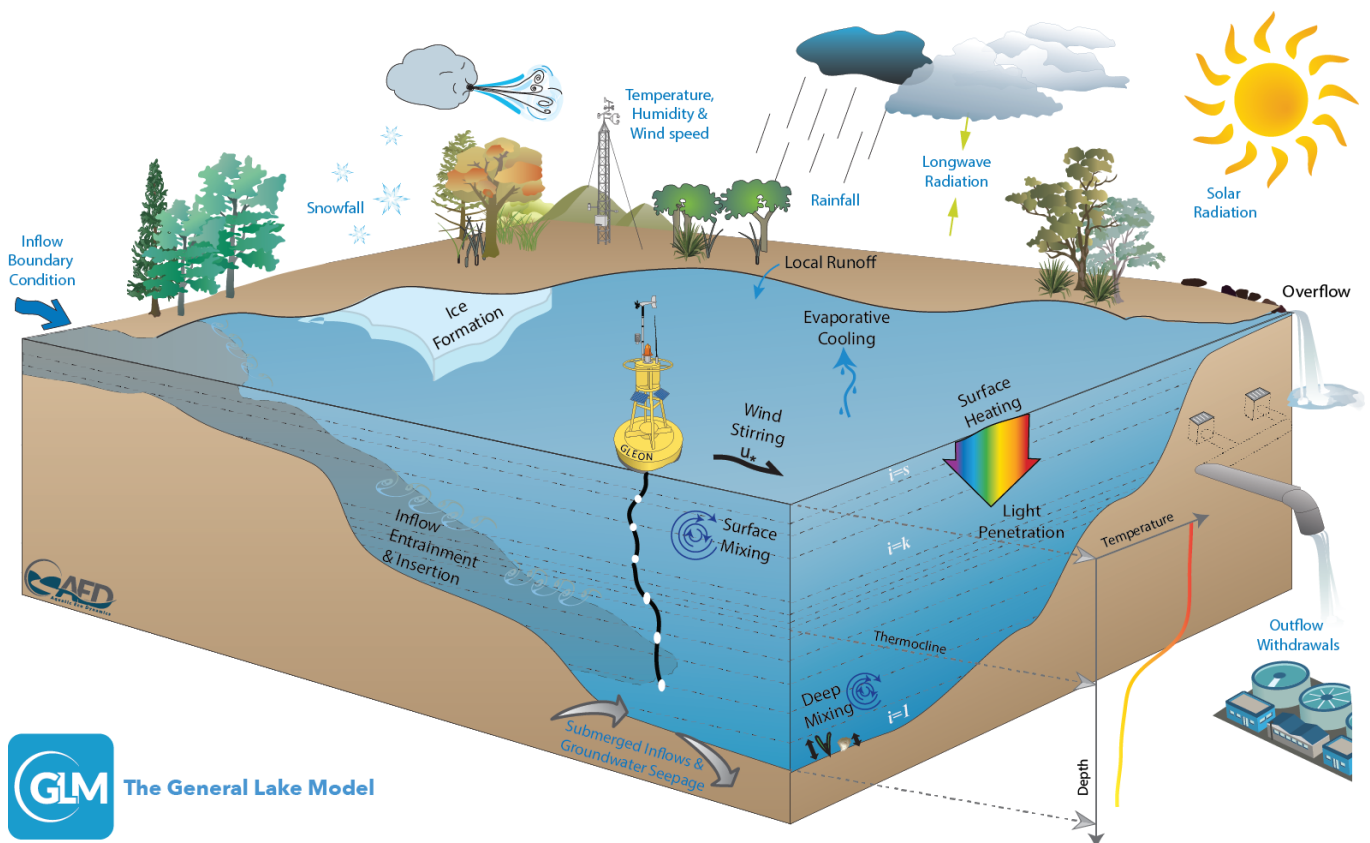


Figure 1: Schematic of a GLM simulation domain, input information (blue text) and key simulated processes (black text).

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Although GLM is a new model code written in the C programming language, the core layer structure and mixing algorithms are founded on principles and experience from model platforms including the Dynamic Reservoir Simulation Model (DYRESM; Imberger and Patterson, 1981; Hamilton and Schladow, 1997) and the Dynamic Lake Model (DLM; Chung et



al., 2008). Other variations have been introduced to extend this underlying approach through applications to a variety of lake and reservoir environments (e.g., Hocking & Patterson, 1991; McCord & Schladow, 1998; Gal et al., 2003; Yeates and Imberger, 2003). The layer structure is numbered from the lake bottom to the surface, and adopts the flexible Lagrangian layer scheme first introduced by Imberger et al. (1978) and Imberger and Patterson (1981). The approach defines each layer, i , as a ‘control volume’ (Figure 1) that can change thickness by contracting and expanding in response to inflows, outflows, mixing with adjacent layers, and surface mass fluxes, as depicted schematically in Figure 1. As the model simulation progresses, density changes due to surface heating, vertical mixing, and inflows and outflows lead to dynamic changes in the layer structure, associated with layers amalgamating, expanding, contracting or splitting. Notation used throughout the model description is provided in Table 1.

As layers change, their volumes change based on the site-specific hypsographic curve, whereby the overall lake volume, V_{max} , is defined as $\int_{H_0}^{H_{max}} A[H] dH$, with the elevation (H), and area (A) relationship provided as a series of points based on bathymetric data. This computation requires the user to provide a number, N_{BSN} , of heights with corresponding areas. The cumulative volume at any lake elevation is first estimated as:

$$V_b = V_{b-1} + [A_{b-1} + 0.5(A_b + A_{b-1})](H_b - H_{b-1}) \quad (1)$$

where $2 \leq b \leq N_{BSN}$. Using this raw hypsographic data, a refined height-area-volume relationship is then internally computed using finer height increments (e.g., $\Delta H_{mi} \sim 0.1$ m), giving N_{MORPH} levels that are used for subsequent calculations. The area and volume at the height of each increment, H_{mi} , are interpolated from the supplied information as:

$$V_{mi} = V_{b-1} \left(\frac{H_{mi}}{H_{b-1}} \right)^{\alpha_{b-1}} \quad \text{and} \quad A_{mi} = A_{b-1} \left(\frac{H_{mi}}{H_{b-1}} \right)^{\beta_{b-1}} \quad (2)$$

where V_{mi} and A_{mi} are the volume and area at each of the elevations of the interpolated depth vector, and V_{b-1} and A_{b-1} refer to the nearest b level below H_{mi} such that $H_{b-1} < H_{mi}$. The interpolation coefficients are computed as:

$$\alpha_b = \left[\frac{\log_{10} \left(\frac{V_{b+1}}{V_b} \right)}{\log_{10} \left(\frac{H_{b+1}}{H_b} \right)} \right] \quad \text{and} \quad \beta_b = \left[\frac{\log_{10} \left(\frac{A_{b+1}}{A_b} \right)}{\log_{10} \left(\frac{H_{b+1}}{H_b} \right)} \right]. \quad (3)$$

Within this lake domain, the model solves the water balance by including several user configurable water fluxes that change the layer structure. Initially, the layers are assumed to be of equal thickness, and the initial number of layers, $N_{LEV}(t = 0)$ is computed based on the initial water depth. Water fluxes include surface mass fluxes (evaporation, rainfall and snowfall), inflows (surface inflows, submerged inflows and local runoff from the surrounding exposed lake bed area) and outflows (withdrawals, overflow and seepage). Surface mass fluxes operate on a sub-daily time step, Δt , by impacting the surface layer thickness (described in Section 2.2), whereby the dynamics of inflows and outflows modify the overall lake water balance and layer structure on a daily time step, Δt_d , by adding, merging or removing layers (described in Section 2.7). Depending on whether a surface (areal) mass flux or volumetric mass flux is being applied, the layer volumes are updated by interpolating changes in layer heights, whereby $V_i = f[h_i]$, and i is the layer number, or layer heights are updated by interpolating changes in layer volumes, whereby $h_i = f[V_i]$.



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Each layer also contains heat, salt (S) and other constituents (C) which are generically referred to as scalars. These are subject to mass conservation as layers change thickness or are merged or split. The specific number of other constituents depends on the configuration of the associated water quality model, but typically includes attributes such as oxygen, nutrients and phytoplankton. Layer density is computed from the local salinity and temperature according to TEOS-10, whereby $\rho_i = \rho[T_i, S_i]$. [When density instabilities occur between adjacent layers, or when sufficient turbulent kinetic energy becomes available to overcome stable density gradients, then layers merge, thereby accounting for the process of mixing](#) ~~When sufficient energy becomes available to overcome density instabilities between adjacent layers, the layers merge, thereby accounting for the process of mixing~~ (Section 2.6). For deeper systems, a stable vertical density gradient ~~will form~~ [seasonally](#) –in response to periods of high solar radiation creating warm, buoyant water overlying cooler, denser water, separated by a metalimnion region which includes the thermocline. Layer [volumes thickness change due to depth-specific changes in mixing, inflows and outflows, and thickness](#) limits, Δz_{min} and Δz_{max} , are enforced to adequately resolve the vertical density gradient, generally with fine resolution occurring in the metalimnion and thicker cells where ~~mixing is active~~ [gradients are weak](#). The number of layers, $N_{LEV}[\{t\}]$, is adjusted throughout the simulation to maintain homogenous properties within a layer. It has been reported that numerical diffusion at the thermocline can be restricted using this layer structure and mixing algorithm (depending on the minimum and maximum layer thickness limits set by the user), making it particularly suited to long-term investigations, and ideally requiring limited site-specific calibration (Patterson et al., 1984; Hamilton and Schladow, 1997; Bruce et al., 2018).

Because this approach assumes layer properties are laterally averaged, the model is suitable for investigations where resolving the horizontal variability is not a requirement of the study. This is often the case for ecologists and biogeochemists studying central basins of natural lakes (e.g., Gal et al., 2009), managers simulating drinking water reservoirs (e.g., Weber et al., 2017), or mining pit lakes (e.g., Salmon et al., 2017), or for analyses exploring the coupling between lakes and regional climate (e.g., Stepanenko et al., 2013). Further, whilst the model is able to resolve vertical stratification, the approach is also able to be used to simulate shallow lakes, wetlands, wastewater ponds and other small waterbodies that experience well-mixed conditions. In this case, the layer resolution, with upper and lower layer bounds specified by the user, will automatically be reduced, and the mass of water and constituents, and energy will continue to be conserved. The remainder of this section outlines the model components and provides example outputs for five water bodies that experience a diverse hydrology. [\(Figure 2\)](#).

2.2 ~~Surface~~ **Water balance**

[The general nature of the model to accommodate a wide diversity of lake types has necessitated flexibility in configuration of water inputs and outputs \(schematically depicted in Figure 1\). The net water flux over the entire lake is summarised as:](#)

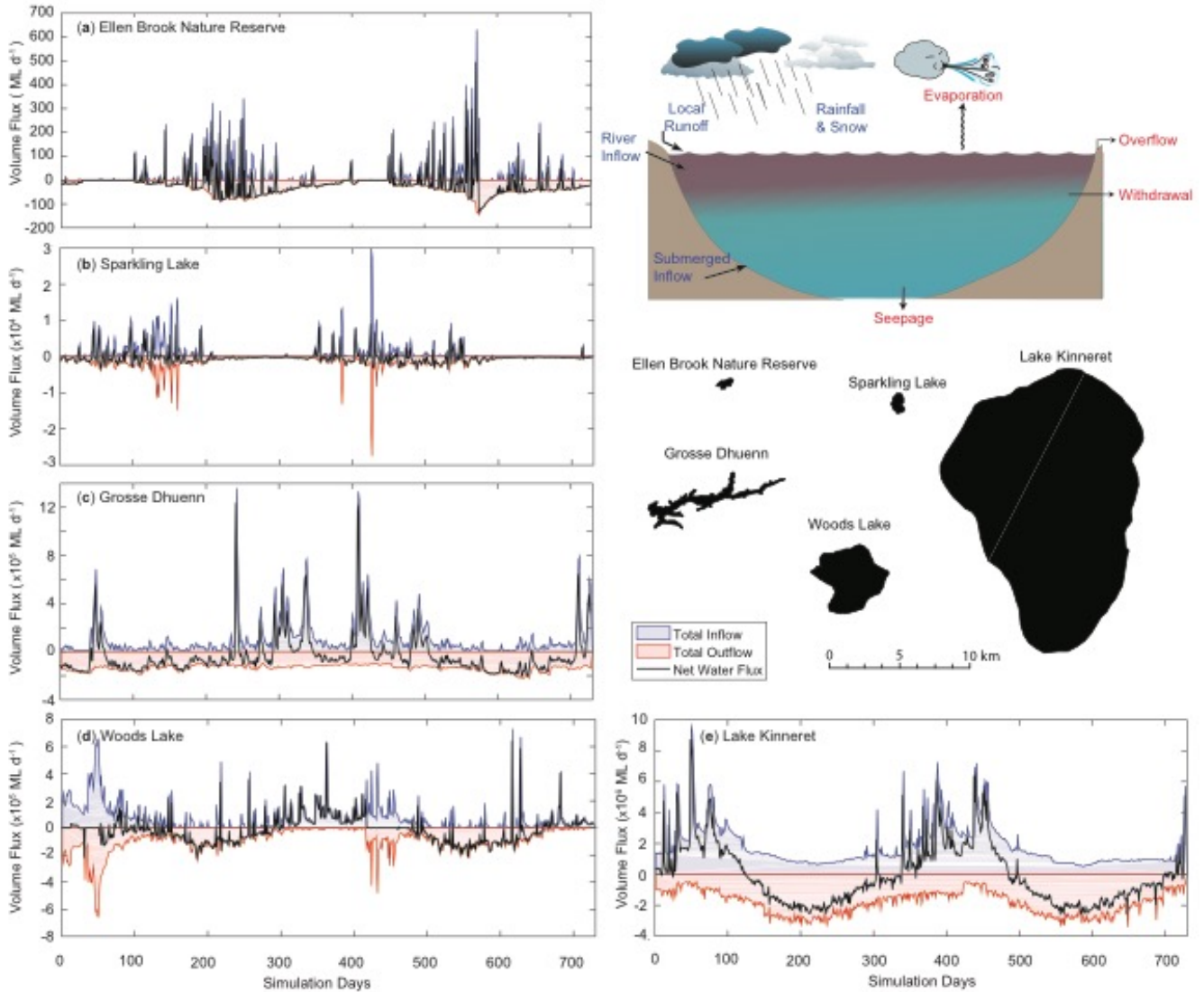
$$\frac{dV}{dt} = A_s \frac{dh_s}{dt} + \sum_I^{N_{INF}} Q_{inf_{oI}} - \sum_O^{N_{OUTF}} Q_{out_{fO}} - Q_{seepage} - Q_{ovfl} \quad (4)$$

where V is the overall lake volume, t is time, the changes due to fluxes at the water surface, $h_{s,z}$ are expanded upon below, and the remaining inflow and outflow terms are described in detail in Section 7. For practical reasons the equation is numerical solved in two stages with different times steps for the surface flux change and all other fluxes. Furthermore, in any given application, not all the inputs and outputs are relevant and users may customise the water balance components accordingly; examples demonstrating lake hydrology from wetlands to reservoirs to deep lakes are presented in Figure 2. Note that Eq. 4 accounts for the liquid water balance, and in cold climates the model will also track the amount of water allocated into an overlying ice layer (Section 2.4), which interacts with the surface water balance as indicated next.

- 10 The mass balance of the surface layer is computed at each model time step (Δt ; usually hourly), by modifying the surface layer height, $h_{s,z}$ according to:

$$\frac{dh_s}{dt} = R_F + S_F + \frac{Q_R}{A_s} - E - \frac{d\Delta z_{ice}}{dt} \quad (5)$$

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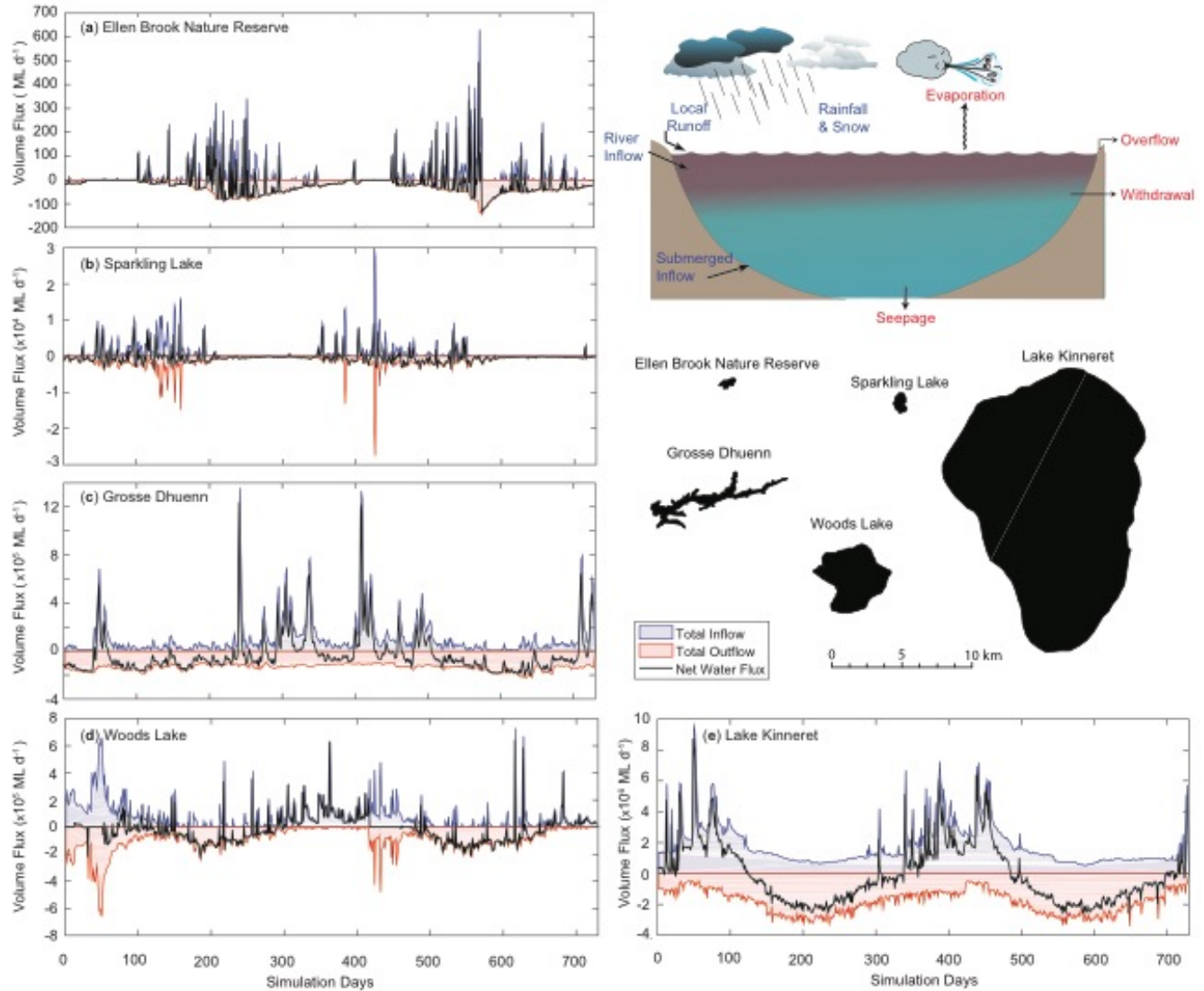


Figure 2: A two-year times series of the simulated daily water balance for five example lakes, a-e, that range in size and hydrology. The water balance components summarised are depicted schematically in the inset, and partitioned into inputs and outputs. The daily net water flux is computed from Eq. 4. For more information about each lake, the simulation configuration and input data, refer to the Data availability section.

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$$\frac{dh_s}{dt} = R_F + S_F + \frac{Q_R}{A_s} - E - \frac{d\Delta z_{ice}}{dt} \quad (5)$$

where h_s is the top height of the surface layer (m), t is the time (s), E is the evaporation mass flux computed from the latent heat flux ϕ_E , described below ($E = -\phi_E / \lambda_v \rho_s$; m s^{-1}), R_F is rainfall and S_F is snowfall (m s^{-1}). Depending on the meteorological conditions, precipitation will either be added to the water volume, or to the surface of the ice cover (see section 2.4), and R_F and S_F therefore both affect the influence the water surface height depending on the presence of ice cover according to:

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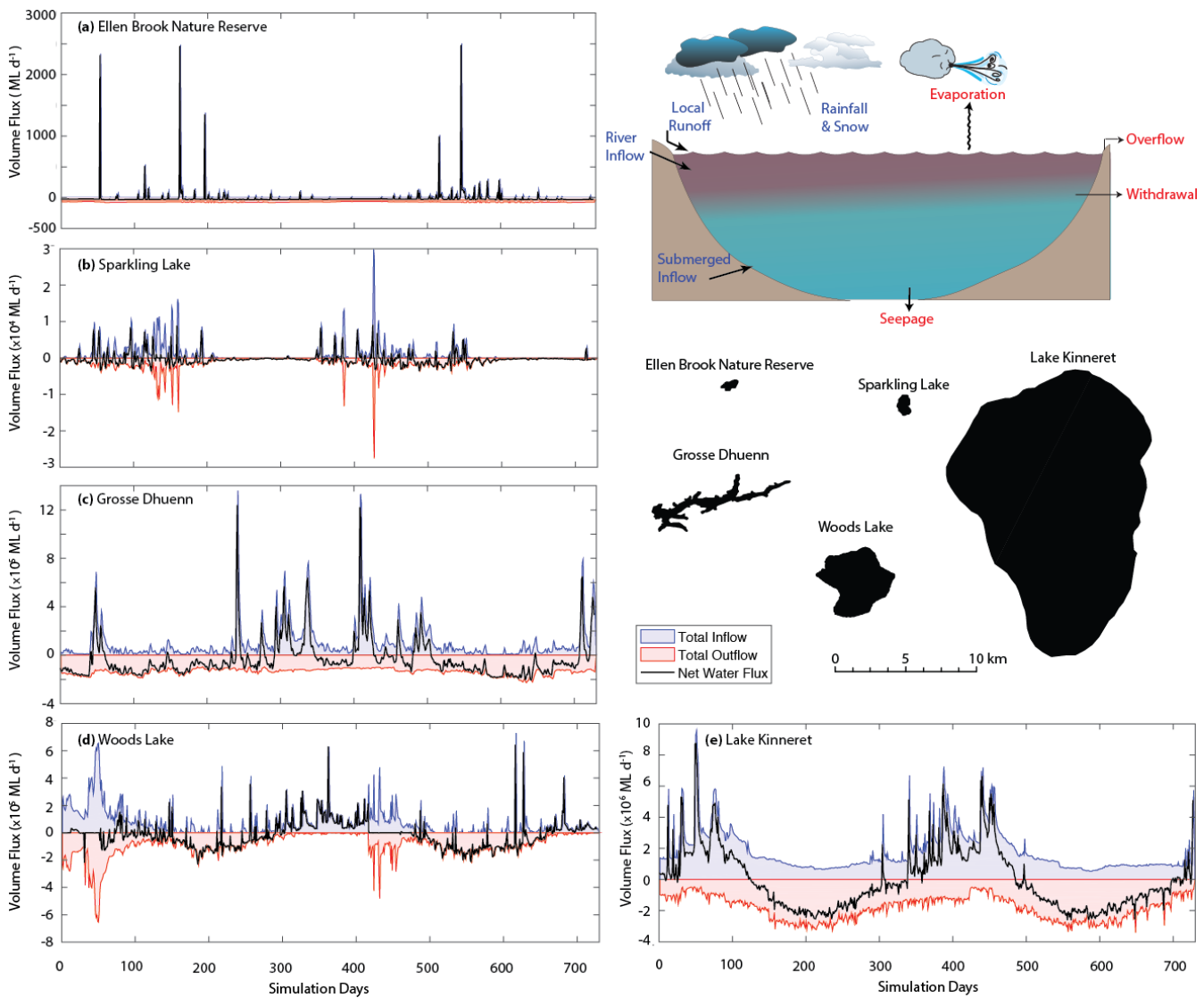
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$$R_F = \begin{cases} f_R R_{\bar{x}} / c_{\text{seeday}}, & \text{if } \Delta z_{\text{tee}} = 0 \\ f_R R_{\bar{x}} / c_{\text{seeday}}, & \text{if } \Delta z_{\text{tee}} > 0 \text{ and } T_a > 0 \\ 0, & \text{if } \Delta z_{\text{tee}} > 0 \text{ and } T_a \leq 0 \end{cases} \quad (5)$$

and

$$S_F = \begin{cases} f_S f_{\text{SWE}} S_{\bar{x}} / c_{\text{seeday}}, & \text{if } \Delta z_{\text{tee}} = 0 \\ 0, & \text{if } \Delta z_{\text{tee}} > 0 \end{cases} \quad (6)$$

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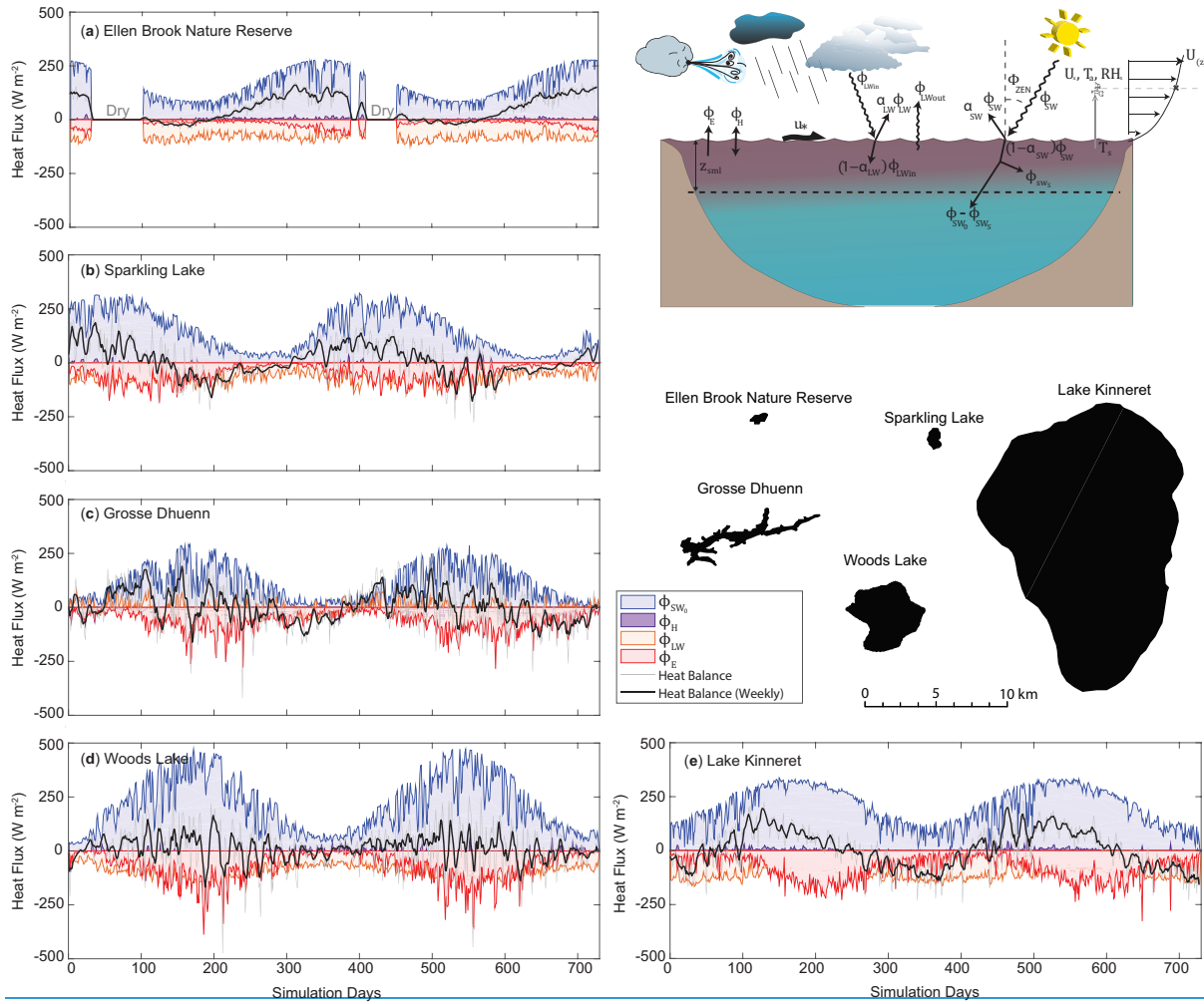


Figure 2: A two-year times-series of the simulated daily water balance for five example lakes, a–e, that range in size and hydrology. The water balance components summarised are depicted schematically in the inset, and partitioned into inputs and outputs. The net water flux in a time step is: $dV/dt = \Delta h_s A_s + \sum_i^{N_{INFL}} Q_{inf_{vi}} - \sum_o^{N_{OUTF}} Q_{out_{fo}} - Q_{ovfl} - Q_{seepage}$. For more information about each lake, the simulation configuration and input data, refer to the Data availability section.

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$$R_F = \begin{cases} f_R R_x / c_{secd\text{ay}}, & \text{if } \Delta z_{ice} = 0 \\ f_R R_x / c_{secd\text{ay}}, & \text{if } \Delta z_{ice} > 0 \text{ and } T_a > 0 \\ 0, & \text{if } \Delta z_{ice} > 0 \text{ and } T_a \leq 0 \end{cases} \quad (6)$$

and

$$S_F = \begin{cases} f_S f_{SWE} S_x / c_{secd\text{ay}}, & \text{if } \Delta z_{ice} = 0 \\ 0, & \text{if } \Delta z_{ice} > 0 \end{cases} \quad (7)$$

Here f_R and f_S are user definable scaling factors that may be applied to adjust the input data values, R_x and S_x respectively. The surface height of the water column is also impacted by ice formation or melting of the ice layer sitting on the lake surface, according to $d\Delta z_{ice}/dt$, as described in Section 2.4.

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Q_R is an optional term to account for runoff to the lake from the exposed riparian banks, which may be important in reservoirs with a large drawdown range, or wetlands where periodic drying of the lake may occur. The runoff volume generated is averaged across the area that the active lake surface area (A_S) is not occupying, and the amount is calculated using a simple model based on exceedance of a rainfall intensity threshold, R_L (m day^{-1}), and runoff coefficient:

$$Q_R = \max[0, f_{ro}(R_F - R_L/c_{secday})](A_{max} - A_S) \quad (78)$$

where f_{ro} is the runoff coefficient, defined as the fraction of rainfall that is converted to runoff at the lake's edge, and A_{max} is the maximum possible area of inundation of the lake (the area provided by the user as the N_{BSN} value).

Note that mixing dynamics (i.e., the merging or splitting of layers to enforce the layer thickness limits), will impact the thickness of the surface mixed layer, z_{sml} , but not change the overall lake height. However, in addition to the terms in Eq. 54, h_s is modified due to volume changes associated with river inflows, withdrawals, seepage or overflows, which are described in subsequent sections.

2.3 Surface energy balance

A balance of shortwave and longwave radiation fluxes, and sensible and evaporative heat fluxes (all W m^{-2}) determines the net cooling and heating across the surface. The general heat budget equation for the upper-most layer is described as:

$$c_w \rho_s z_s \frac{dT_s}{dt} = \phi_{SW_S} - \phi_E + \phi_H + \phi_{LW_{in}} - \phi_{LW_{out}} \quad (89)$$

where c_w is the specific heat capacity of water, T_s is the surface temperature, and z_s and ρ_s are the depth and density of the surface layer ($i = N_{LEV}$), respectively. The [right-hand side \(RHS\)](#) heat flux terms are [numerically](#) computed at each time step, and include several options for customizing the individual surface heat flux components, which are expanded upon below.

2.3.1 Solar heating and light penetration

Solar radiation is the key driver of the lake thermodynamics and may be input based on daily or hourly measurements from a nearby pyranometer. If data is not available then users may choose to ~~either~~ have GLM compute surface irradiance from a theoretical approximation based on the Bird Clear Sky insolation model (BCSM) (Bird, 1984), modified for cloud cover and latitude. ~~Therefore, the~~ options for input are summarised as:

$$\phi_{SW_0} = \begin{cases} (1 - \alpha_{SW}) f_{SW} \phi_{SW_x} f[d, t - [t]], & \text{Option 1: daily insolation data provided} \\ (1 - \alpha_{SW}) f_{SW} \phi_{SW_x}, & \text{Option 2: sub-daily input data provided} \\ (1 - \alpha_{SW}) f_{SW} \hat{\phi}_{SW}, & \text{Option 3: data is computed from the BCSM} \end{cases} \quad (9a10a-c)$$

where ϕ_{SW_0} is the solar radiation flux entering the surface layer, ϕ_{SW_x} is the incoming shortwave radiation flux supplied by the user, f_{SW} is a scaling factor that may be applied and adjusted as part of the calibration process ([for example to capture the effects of shading](#)), and α_{SW} is the albedo for shortwave radiation. If daily data is supplied (Option 1), the model

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continues to run at a sub-daily time step, but applies the algorithm outlined in Hamilton and Schladow (1997) to distribute the daily solar energy flux over a diurnal cycle, based on the day of the year, d , and time of day, $t - [t]$. For Option 3 the BCSM is used (Bird, 1984; Luo et al., 2010):

$$\hat{\phi}_{SW} = \frac{\hat{\phi}_{DB} + \hat{\phi}_{AS}}{1 - (\alpha_{SW} \alpha_{SKY})} f[C_x] \quad (1011)$$

where the total irradiance, $\hat{\phi}_{SW}$, is computed from direct beam $\hat{\phi}_{DB}$, and atmospheric scattering $\hat{\phi}_{AS}$ components (refer to Appendix A for a detailed outline of the BCSM equations and parameters). In GLM, the clear sky value is then reduced according to the cloud cover data provided by the user, C_x , according to:

$$f[C_x] = 0.66182 C_x^2 - 1.5236 C_x + 0.98475 \quad (124)$$

which is based on a polynomial regression of cloud data from Perth Airport, Australia, compared against nearby sensor data ($R^2 = 0.952$; see also [a similar relationship by](#) Luo et al., 2010).

10 The albedo, α_{SW} , is the reflected fraction of the incoming radiation and depends on surface conditions including the presence of ice, waves and the angle of incident radiation. For open water conditions, users may configure:

Option 1 : Daily approximation, Hamilton and Schladow (1997)

$$\alpha_{SW} = \begin{cases} 0.08 - 0.02 \sin\left[\frac{2\pi}{365}d - \frac{\pi}{2}\right] & \text{:northern hemisphere} \\ 0.08 & \text{:equator} \\ 0.08 - 0.02 \sin\left[\frac{2\pi}{365}d + \frac{\pi}{2}\right] & \text{:southern hemisphere} \end{cases} \quad (132a)$$

Option 2 : Briegleb et al. (1986)

$$\alpha_{SW} = \frac{1}{100} \left(\frac{2.6}{\cos[\Phi_{zen}]^{1.7} + 0.065} + 15(\cos[\Phi_{zen}] - 0.1)(\cos[\Phi_{zen}] - 0.5)(\cos[\Phi_{zen}] - 1) \right) \quad (132b)$$

Option 3 : Yajima and Yamamoto (2015)

$$\alpha_{SW} = \max \left[0.02, 0.001 \frac{RH_x}{100} [1 - \cos(\Phi_{zen})]^{0.33} - 0.001 U_{10} [1 - \cos(\Phi_{zen})]^{-0.57} - 0.001 \zeta [1 - \cos(\Phi_{zen})]^{0.829} \right] \quad (132c)$$

where Φ_{zen} is the solar zenith angle (radians) as outlined in Appendix A, RH_x is the relative humidity, ζ is [the percentage of the](#) atmospheric diffuse radiation, d is the day of year, and U_x is wind speed. The second (oceanic) and third (lacustrine) options are included to allow for diel and seasonal variation of albedo from approximately 0.01 to 0.4 depending on the sun-angle (Figure 3). Albedo is calculated separately during ice cover conditions using a customised algorithm, outlined below in Section 2.4.

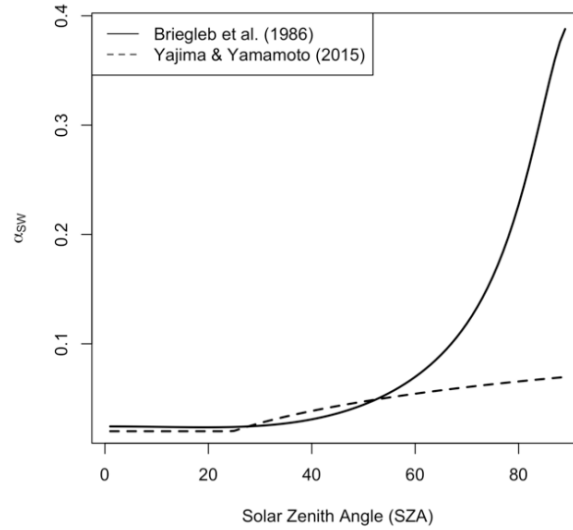


Figure 3: Variation of albedo (α_{SW}) with solar zenith angle (SZA = $\Phi_{zen}180/\pi$, degrees) for [options albedo_mode 2](#) and [3](#) (Eq. 132). For option 3, settings of RH = 80 % and U = 6 m s⁻¹ were assumed.

- 5 The depth of penetration of shortwave radiation into the lake is wavelength specific, and depends on the water clarity via the light extinction coefficient, K_w (m⁻¹). Two approaches are supported in GLM. The first option assumes the Photosynthetically Active Radiation (PAR) fraction of the incoming light is the most penetrative, and follows the Beer-Lambert Law:

$$\phi_{PAR}[z] = f_{PAR} \phi_{SW_0} \exp[-K_w z] \quad (143)$$

where z is the depth of any layer from the surface. K_w may be set by the user as constant or linked to the water quality model (e.g., FABM or AED2, see Section 4) in which case the extinction coefficient will change as a function of depth and time according to the concentration of dissolved and particulate constituents. For this option Beer's Law is only applied for the photosynthetically active fraction, f_{PAR} , which is set as 45% of the incident light. The amount of radiation heating the surface layer, ϕ_{SW_S} , is therefore the photosynthetically active fraction that is attenuated across z_{smt} , plus the entire $(1 - f_{PAR})$ fraction, $\phi_{SW_S} = \phi_{SW_0} - \phi_{PAR}[z_{smt}]$, which [implicitly assumes accounts for the](#) near infra-red and ultraviolet bandwidths of the incident shortwave radiation ~~$\phi_{SW_S} = \phi_{SW_0} - \phi_{PAR}[z_{smt}]$~~ [and implicitly assumes these](#) have significantly higher attenuation coefficients (Kirk, 1994). The second option adopts a more complete light absorption algorithm that integrates the attenuated light intensity across the bandwidth spectrum:

$$c_w \rho_s \Delta z_i \frac{dT_i}{dt} = \sum_{lk=1}^{N_{SW}} \phi_{SW_{i,lk}}[z_i] - \sum_{lk=1}^{N_{SW}} \phi_{SW_{i-1,lk}}[z_{i-1}] \quad (145)$$

where lk is the bandwidth index $\phi_{SW_{i,lk}}[z_i]$ is the radiation flux at the top of the i th layer. For this option, the model by Cengel and Ozisk (1984) is adopted to compute $\phi_{SW_{i,lk}}[z_i]$, which more comprehensively resolves the light climate including

incident and diffuse radiation components, the angle of incident light and transmission across the light surface (based on the Fresnel equations), and reflection off the bottom. These processes are wavelength specific and the user must specify the number of simulated bandwidths, N_{SW} , and their respective absorption coefficients, K_{WI} .

- 5 The light reaching the benthos may be used in some applications as an indicator of benthic productivity, and a proxy for the type of benthic habitat that might emerge. In addition to the light profiles, GLM also predicts the benthic area of the lake where light intensity exceeds a user defined fraction of the surface irradiance, $f_{BEN_{crit}}$ (Figure 4):

$$A_{BEN} = A_s - A[h_{BEN}] \quad (165)$$

where $h_{BEN} = h_s - z_{BEN}$, and z_{BEN} is calculated from Beer's law:

$$z_{BEN} = -\frac{\ln[f_{BEN_{crit}}]}{K_w} \quad (176)$$

and the daily average benthic area above the threshold is then reported as a percentage ($100 \times A_{BEN}/A_s$).

10

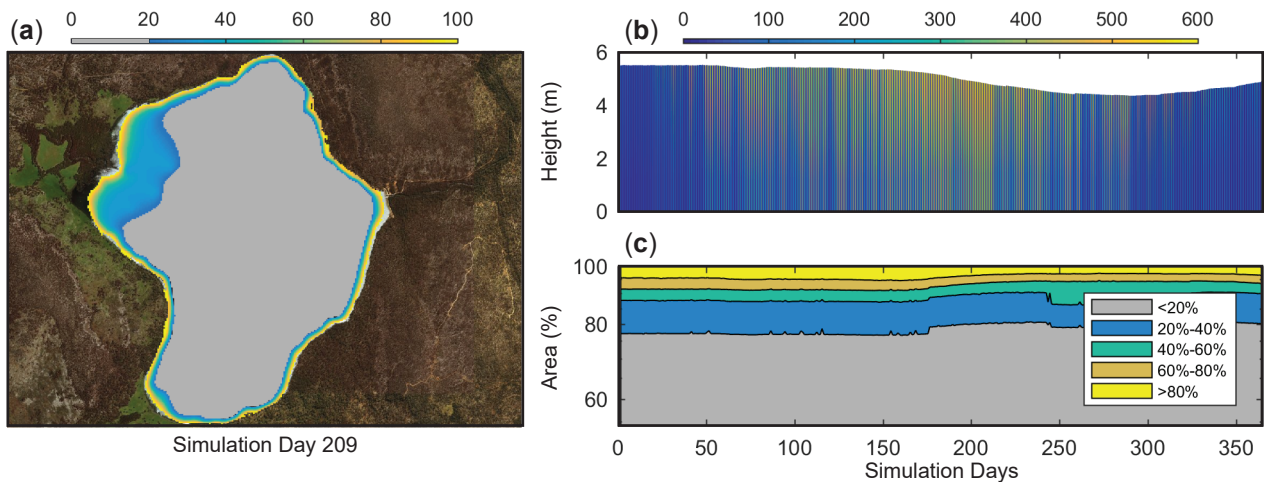


Figure 4: Example light data outputs from a GLM application to Woods Lake, Australia, showing a) the ratio of benthic to surface light, $\phi_{PAR_{BEN}}/\phi_{SW_0}$ (%), overlain on the lake map based on the bathymetry, with the area where $f_{BEN_{crit}} < 0.2$ depicted in grey, b) a time series of the depth variation in light ($W m^{-2}$), and c) a time series of A_{BEN}/A_s (as %) for various $f_{BEN_{crit}}$ values (as %).

15

2.3.2 Longwave radiation

Longwave radiation can be provided as a net flux, an incoming flux or, if there is no radiation data from which longwave radiation can be computed, then it may be calculated by the model internally based on the cloud cover fraction and air temperature. Net longwave radiation is described as:

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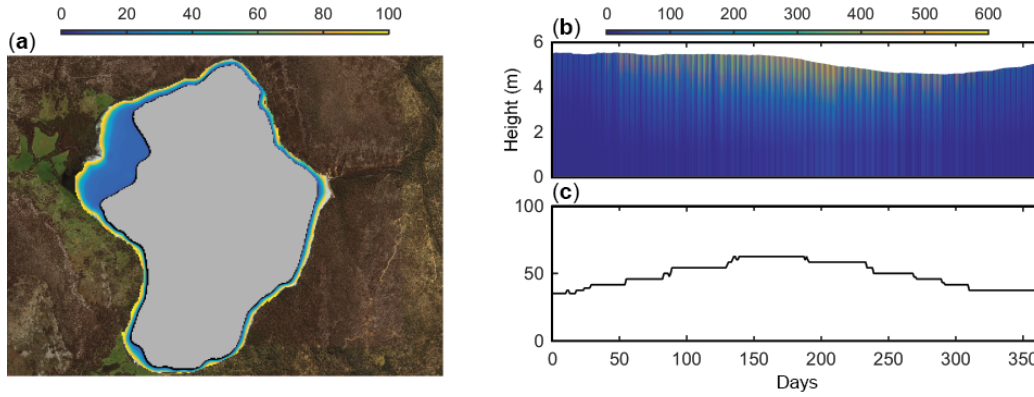


Figure 4: Example light data outputs from a GLM application to Woods Lake, Australia, showing a) the ratio of benthic to surface light, $\phi_{PAR_{BEN}}/\phi_{SW_v}$ (%), overlain on the lake map based on the bathymetry, b) a time series of the depth variation in light ($W m^{-2}$), and c) a time series of A_{BEN}/A_s (as %) for $f_{BEN_{EFF}} = 0.2$.

5

$$\phi_{LW_{net}} = \phi_{LW_{in}} - \phi_{LW_{out}} \quad (187)$$

where

$$\phi_{LW_{out}} = \varepsilon_w \sigma (\theta_s)^4 \quad (198)$$

and σ is the Stefan-Boltzman constant and ε_w the emissivity of the water surface, assumed to be 0.985. If the net or incoming longwave flux is not provided, the model will compute the incoming flux from:

10

$$\phi_{LW_{in}} = (1 - \alpha_{LW}) \varepsilon_a^* \sigma (\theta_a)^4 \quad (209)$$

where α_{LW} is the longwave albedo (0.03). The emissivity of the atmosphere can be computed considering emissivity of cloud-free conditions (ε_a), based on air temperature (T_a) and vapour pressure, and extended to account for reflection from clouds, such that $\varepsilon_a^* = f[T_a, C_x, e_a, C_x]$ (see Henderson-Sellers, 1986; Flerchinger, 2009). Options available in GLM include:

15

$$\varepsilon_a^* = \begin{cases} (1 + 0.275 C_x)(1 - 0.261 \exp[-0.000777 T_a^2]), & \text{Option 1: Idso and Jackson (1969)} \\ (1 + 0.17 C_x^2) (9.365 \times 10^{-6} (\theta_a)^2), & \text{Option 2: Swinbank (1963)} \\ (1 + 0.275 C_x) 0.642 (e_a/\theta_a)^{1/7}, & \text{Option 3: Brutsaert (1975)} \\ (1 - C_x^{2.796}) 1.24 (e_a/\theta_a)^{1/7} + 0.955 C_x^{2.796}, & \text{Option 4: Yajima and Yamamoto (2015)} \end{cases} \quad (210a-d)$$

where, C_x is the cloud cover fraction (0-1), e_a the air vapour pressure calculated from relative humidity, and options 1-4 are chosen via the cloud mode variable. Note that cloud cover is typically reported in octals (0-8) with each value depicting a fraction of 8, thus a value of 1 would correspond to a fraction of 0.125. Some data may also include cloud type and their respective heights. If this is the case, good results have been reported by averaging the octal values for all cloud types to get an average cloud cover.

20

If longwave radiation data does not exist and cloud data is also not available, but solar irradiance is measured, then GLM rad_mode setting 3 will instruct the model to compare the measured and theoretical clear-sky solar irradiance (estimated by the BCSM; Eq. 110) to approximate the cloud cover fraction by assuming that $\phi_{SW_x}/\hat{\phi}_{SW} = f[C_x]$. Note that if neither shortwave or longwave radiation is provided, then the model will use the BCSM to compute incoming solar irradiance, and cloud cover will be assumed to be 0 (noting that this is likely to be an overestimate of downwelling shortwave radiation).

2.3.3 Sensible and latent heat transfer

The model accounts for the surface fluxes of sensible heat and latent heat using commonly adopted bulk aerodynamic formulae. For sensible heat:

$$\phi_H = -\rho_a c_a C_H U_{10} (T_s - T_a) \quad (22\pm)$$

where c_a is the specific heat capacity of air, C_H is the bulk aerodynamic coefficient for sensible heat transfer, T_a the air temperature and T_s the temperature of the water surface layer. The air density (kg m^{-3}) is computed from $\rho_a = 0.348 (1 + r)/(1 + 1.61r) p/T_a$, where p is air pressure (hPa) and r is the [water vapour](#) mixing ratio, which is used to compute the gas constant.

For latent heat:

$$\phi_E = -\rho_a C_E \lambda_v U_{10} \frac{\omega}{p} (e_s[T_s] - e_a[T_a]) \quad (23\pm)$$

where C_E is the bulk aerodynamic coefficient for latent heat transfer, e_a the air vapour pressure, e_s the saturation vapour pressure (hPa) at the surface layer temperature ($^{\circ}\text{C}$), ω the ratio of molecular mass of water to molecular mass of dry air ($= 0.622$) and λ_v the latent heat of vaporisation. The vapour pressure ~~can be~~ calculated by the ~~linear following~~ formula [from Tabata \(1973\)](#):

$$e_s[T_s] \quad (24)$$

$$= 10^{(9.28603523 \frac{2322.37885}{T_s + 273.15})} \begin{cases} \exp \left[2.3026 \left(7.5 \frac{T_s}{T_s + 237.3} \right) + 0.7858 \right], & \text{Option 1: TVA (1972) - Magnus-Teter} & \text{3a)} \\ \exp \left[6.1094 \left(\frac{17.625 T_s}{T_s + 243.04} \right) \right], & \text{Option 2: August-Roche-Magnus} & \text{(23)} \\ 10^{(9.28603523 \frac{2322.37885}{T_s + 273.15})}, & \text{Option 3: Tabata (1973) - Linear} & \text{b)} \end{cases}$$

(23)

e)

and

$$e_a[T_a] = (f_{RH} RH_x / 100) f_{RH} RH_x e_s[T_a] \quad (25)$$



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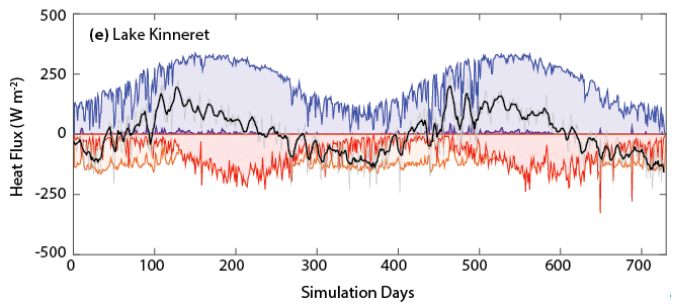
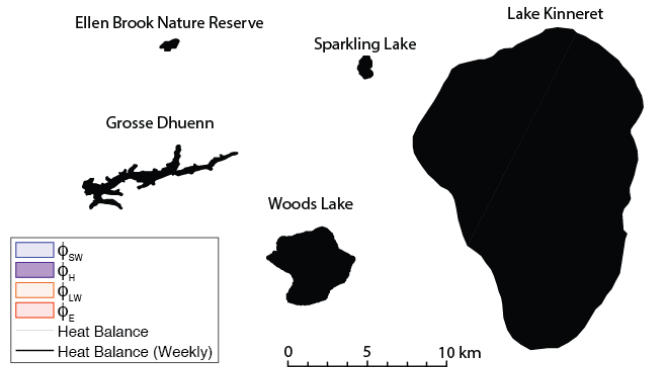
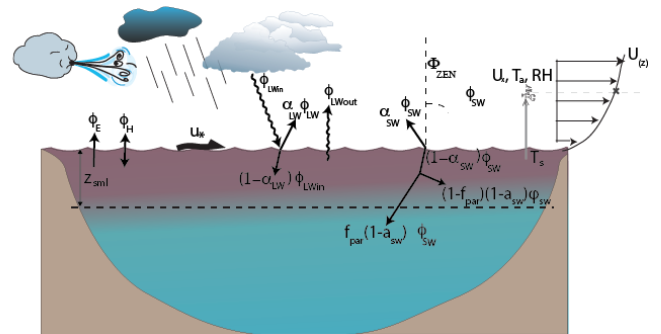
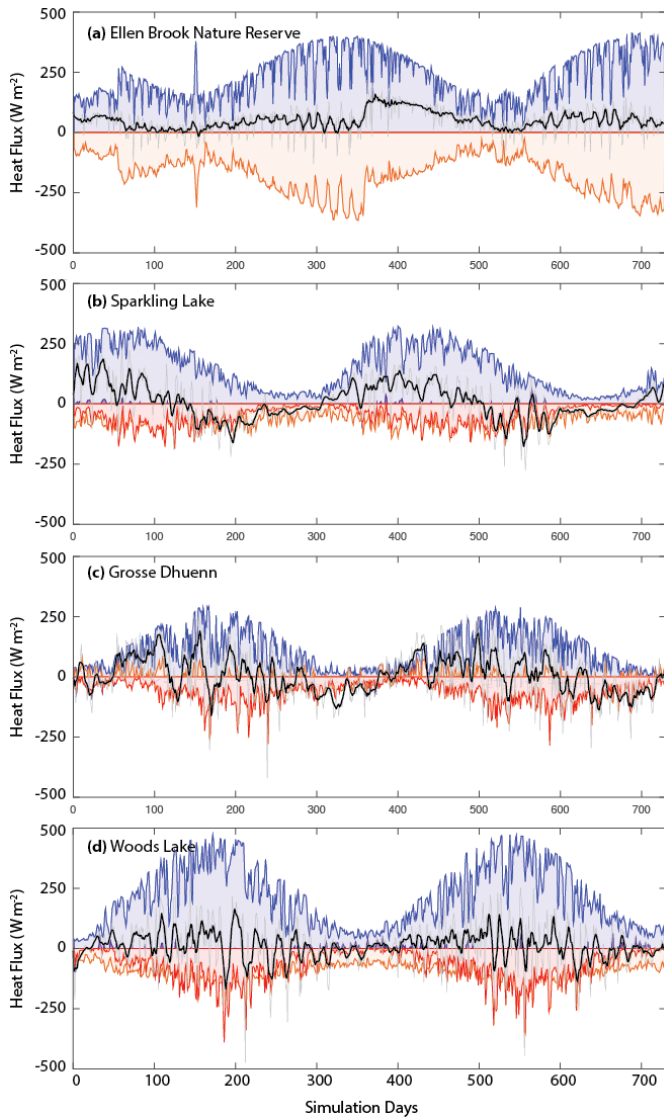
4)

The net heat fluxes for the example lakes are shown in Figure 5.

Correction for non-neutral atmospheric stability: For long-time (e.g., seasonal) integrations, the bulk-transfer coefficients for momentum, C_D , sensible heat, C_H , and latent heat, C_E , can be assumed approximately constant because of the negative feedback between surface forcing and the temperature response of the water body (e.g., Strub and Powell, 1987). At finer timescales (hours to weeks), the thermal inertia of the water body is too great and so the transfer coefficients ~~must~~ should be specified as a function of the degree of atmospheric stratification experienced in the internal boundary layer that develops over the water (Woolway et al., 2017). Monin and Obukhov (1954) parameterised the stratification in the air column using the now well-known stability parameter, z/L , which is used to define corrections to the bulk aerodynamic coefficients C_H and C_E , using the numerical scheme presented in Appendix B. The corrections may be optionally applied within a simulation, and if enabled, the transfer coefficients used above are automatically updated. To ensure data provided is from within the internal boundary layer over the lake surface, ~~this option requires the measurement-provision~~ of wind speed, air temperature and relative humidity data from near the lake surface (e.g., 2-10 m, depending on lake size) ~~within the internal boundary layer over the lake surface~~, supplied at ~~an~~ approximately hourly resolution.

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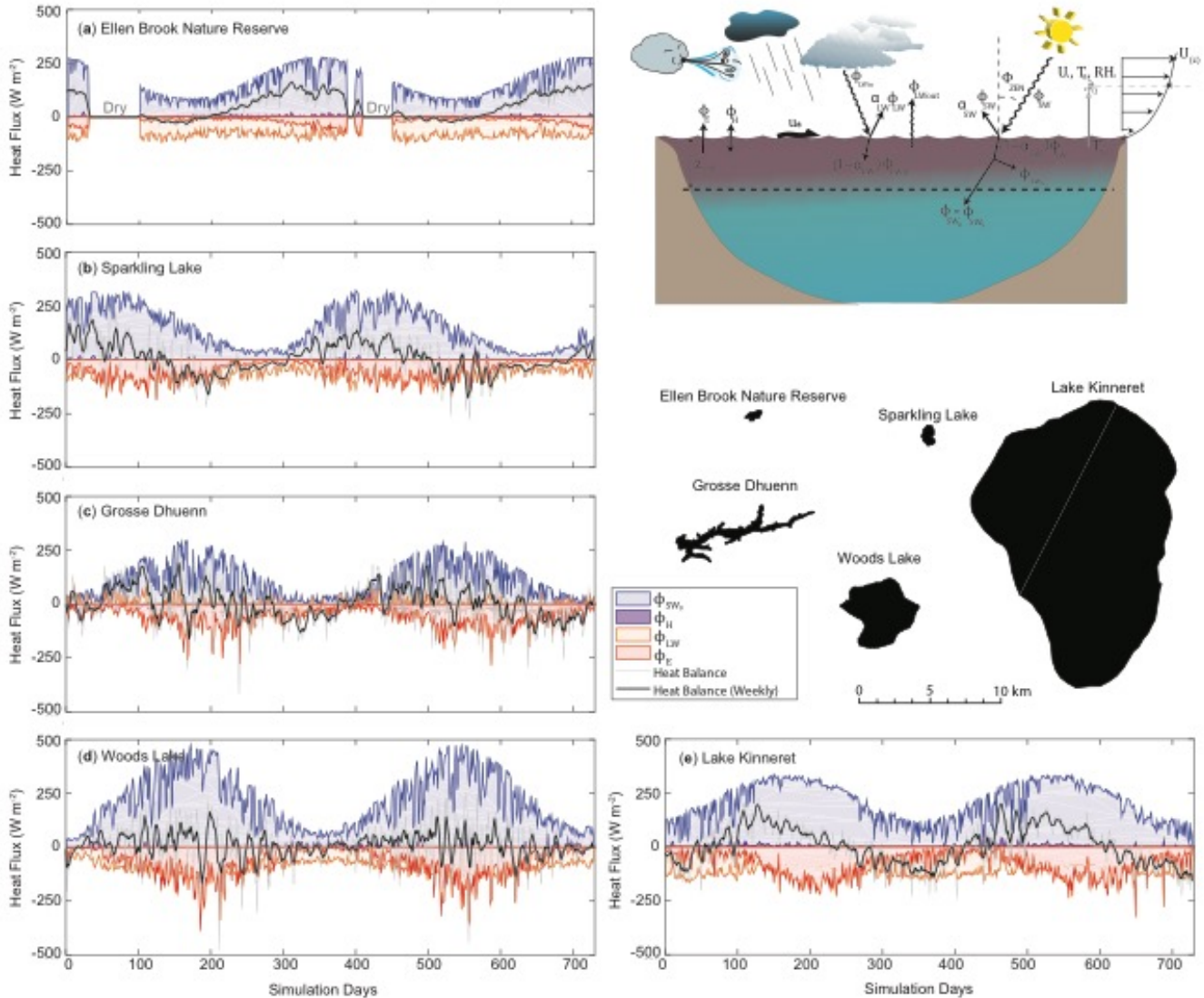


Figure 5: A two year times series of the simulated daily heat fluxes for the five example lakes, a-e, that were depicted in Figure 2. The heat balance components summarised are depicted schematically in the inset, as described in Section 2.3 and the "Heat Balance" line refers to the LHS of Eq. 8.

5

Wind sheltering: Wind sheltering may be important depending on the lake size and shoreline complexity, and is parameterised according to several methods based on the context of the simulation and data available. For example, Hipsey and Sivapalan (2003) presented a simple adjustment to the bulk transfer equation to account for the effect of wind sheltering in small reservoirs using a shelter index to account for the length scale associated with the vertical obstacle relative to the horizontal length scale associated with the water body itself. Markfort et al. (2010) estimate the effect of a similar sheltering length-scale on the overall lake area. Therefore, within GLM, users may specify the degree of sheltering or fetch limitation using either constant or direction-specific options for computing an "effective" area:

10

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$$A_E = \begin{cases} A_S, & \text{Option 0: no sheltering (default)} \\ A_S \tanh\left(\frac{A_S}{A_{WS}}\right), & \text{Option 1: Yeates \& Imberger (2003)} \\ \frac{L_D^2}{2} \cos^{-1} \arccos\left(\frac{x_{WS}\Phi}{L_D}\right) - \frac{x_{WS}\Phi}{L_D^2} \sqrt{L_D^2 - (x_{WS}\Phi)^2}, & \text{Option 2: Markfort et al. (2010)} \\ f_{WS}[\Phi_{wind}] A_S, & \text{Option 3: user – defined shelter index} \end{cases} \quad (265a-d)$$

where A_{WS} is a user defined critical lake area for wind sheltering to dominate, x_{WS} is a user defined sheltering distance, and L_D the lake diameter ($L_D = 0.5(L_{crest} + W_{crest})$). For option 1, the sheltering factor is held constant for the simulation

5

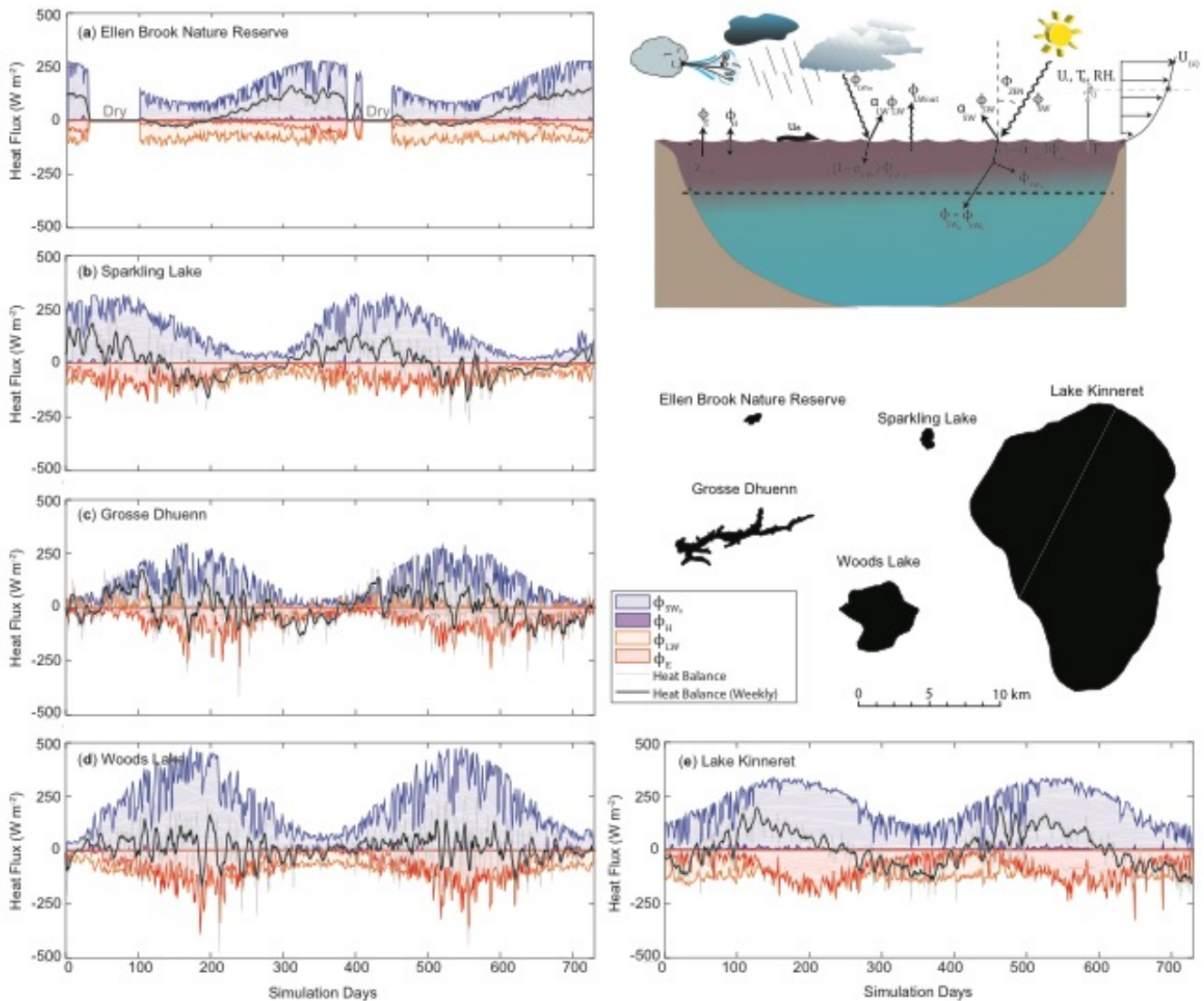


Figure 5: A two-year times series of the simulated daily heat fluxes for the five example lakes, a-e, that were depicted in Figure 2. The heat balance components summarised are depicted schematically in the inset, as described in Section 2.3 and the "Heat Balance" line refers to the LHS of Eq. 9.



based on the size of the lake, whereas the latter two options require users to additionally input wind direction data, and a direction function, $f_{WS}[\Phi_{wind}]$, to allow for a variable sheltering effect over time. In the case of option 2, this function scales the sheltering distance, x_{WS} , as a function of wind direction, $x_{WS}^{\Phi} = x_{WS} (1 - \min(f_{WS}[\Phi_{wind}], 1))$, whereas in the case of option 3 the function reads in an effective area scaling fraction directly based on a pre-calculated shelter index.

5

The ratio of the effective area to the total area of the lake, A_E/A_S , is then used to scale the wind speed data input by the user, U_x , as a means of capturing the average wind speed over the entire lake surface, such that $U_{10} = f_U U_x A_E/A_S$, where f_U is a wind speed adjustment factor that can be used to assist calibration, or to correct the raw wind speed data to the reference height of 10 m.

10

Still-air limit: The above formulations only apply when sufficient wind exists to create a defined boundary layer over the surface of the water. As the wind tends to zero (the ‘still-air limit’), Eqs. 224-232 become less appropriate as they do not account for free convection directly from the water surface. This is a relatively important phenomenon for small lakes, cooling ponds and wetlands since they tend to have small fetches that limit the energy input from wind. These water bodies may also have large areas sheltered from the wind and will develop surface temperatures warmer than the atmosphere for considerable periods. Therefore, users can optionally augment Eqs. 224-232 with calculations for low wind speed conditions by calculating the evaporative and sensible heat flux values for both the given U_{10} and for an assumed $U_{10} = 0$. The chosen value for the surface energy balance (as applied in Eq. 89) is found by taking the maximum value of the two calculations:

15

$$\phi_x^* = \begin{cases} \max[\phi_x, \phi_{x_0}] & , \quad \text{Option 1: no – sheltering area} \\ \max[\phi_x, \phi_{x_0}] A_E/A_S + \phi_{x_0} (A_S - A_E)/A_S & , \quad \text{Option 2: still – air sheltered area} \end{cases} \quad (276)$$

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where ϕ_{x_0} is the zero-wind flux for either the evaporative or sensible heat flux (and ϕ_x is calculated from Eqs. 242-232). The two zero-wind speed heat flux equations are from TVA (1972), but modified to return energy flux in SI units (W m^{-2}):

$$\phi_{E_0} = \rho_s \lambda_v \alpha_e (\vartheta_s - \vartheta_a) \quad (287a-b)$$

$$\phi_{H_0} = \alpha_h (T_s - T_a)$$

$$\alpha_e = 0.137 f_0 \frac{K_{air}}{c_a \rho_s} \left(g \frac{|\rho_a - \rho_o|}{\rho_a \nu_a D_a} \right)^{1/3} \quad (298a-b)$$

$$\alpha_h = 0.137 f_0 K_{air} \left(g \frac{|\rho_a - \rho_o|}{\rho_a \nu_a D_a} \right)^{1/3}$$

25

where $\vartheta = \kappa e/p$, with the appropriate vapour pressure values, e , for both surface and ambient atmospheric values. Here, K_{air} is the molecular heat conductivity of air ($\text{J m}^{-1} \text{s}^{-1} \text{C}^{-1}$), ν_a is the kinematic viscosity of the air ($\text{m}^2 \text{s}^{-1}$), ρ_o is the density of the saturated air at the water surface temperature, ρ_s is the density of the surface water, f_0 is a dimensionless roughness



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correction coefficient for the lake surface and D_a is the molecular heat diffusivity of air ($\text{m}^2 \text{s}^{-1}$). Note that the impact of low wind speeds on the drag coefficient is captured by the modified Charnock relation (Eq. A24-A25), which includes an additional term for the smooth flow transition (see also Figure A1).

5 2.4 Snow and ice dynamics

Depending on the prevailing environmental conditions the extent of ice and snow cover can significantly impact the lake water balance and mixing regime. The algorithms for GLM ice and snow dynamics are based on previous ice modelling studies that adopt a three-layer scheme for resolving blue ice (or black ice), white ice (or snow ice) and snow (Patterson and Hamblin, 1988; Gu and Stefan, 1993; Rogers et al., 1995; Vavrus et al., 1996; Launiainen and Cheng, 1998; Magee et al., 2016). Blue ice is formed through direct freezing of lake water into ice whereas white ice is generated in response to flooding, when the mass of snow that can be supported by the buoyancy of the ice cover is exceeded (Rogers et al., 1995). The upper snow layer is subject to compaction and melting based on surface meteorological conditions and the ice layers are affected by the lake water at the lower boundary. The algorithms for GLM ice and snow dynamics are based on previous ice modelling studies (Patterson and Hamblin, 1988; Gu and Stefan, 1993; Rogers et al., 1995; Vavrus et al., 1996; Launiainen and Cheng, 1998; Magee et al., 2016). To solve the heat transfer equation, the ice model uses a quasi-steady assumption that the time scale for heat conduction through the ice is short relative to the time scale of changes in meteorological forcing (Patterson and Hamblin, 1988; Rogers et al., 1995).

Blue ice initially forms when the water goes below 0°C . Once fresh snow deposits on the surface it is subject to densification, which depends on the air temperature and amount of rainfall (Figure 6); the density of fresh snowfall is determined as the ratio of measured snowfall height to water-equivalent height, with any values exceeding the assigned maximum or minimum snow density (defaults: $\rho_{s,max} = 300 \text{ kg m}^{-3}$, $\rho_{s,min} = 50 \text{ kg m}^{-3}$) truncated to the appropriate limit. The snow compaction model equation is based on the exponential decay formula of McKay (1968), with selection of snow compaction parameters based on air temperature (Rogers et al., 1995) as well as on and depending on whether rainfall or snowfall is being added. The approach of snow compaction used by Rogers et al. (1995) is to set the residual snow density to its maximum value when there is fresh snowfall. This method is found to produce increases in snow density that are too rapid when there is only light snowfall. As a result, GLM uses a gradual approach where the new snowfall and the existing snow is used to form a layer with a combined mass and average density. When the weight of snow exceeds the buoyancy of the blue ice layer:

$$\Delta z_{snow} \rho_{snow} > \{ \Delta z_{blue} (\rho_w - \rho_{blue}) + \Delta z_{white} (\rho_w - \rho_{white}) \} \quad (30)$$

then the ice will crack, and surface water will seep into the snow layer leading to formation of white ice; this is limited to the snow amount matching the buoyancy of the ice layer, and the lake height is reduced accordingly.

To capture the changing thickness of the ice and snow layers due to melting or freezing, the model employs a quasi-steady assumption to solve the heat transfer equation through the layers by assuming that the time scale for heat conduction is short relative to the time scale of changes in meteorological forcing (Patterson and Hamblin, 1988; Rogers et al., 1995). By assigning appropriate boundary conditions at the ice-atmosphere and the ice-water interfaces, the model computes the upward conductive heat flux through the ice and snow cover to the atmosphere, termed ϕ_0 .

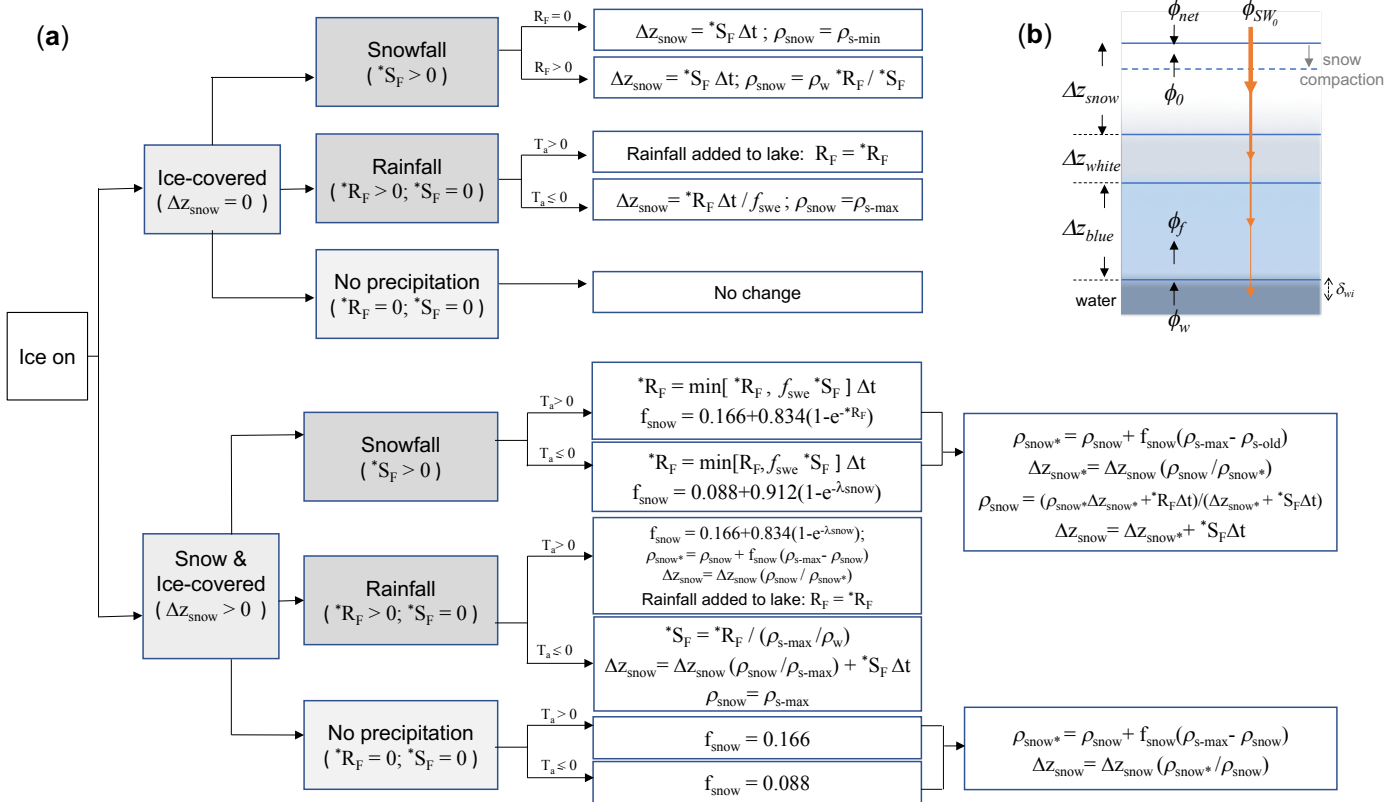


Figure 6: a) Decision tree describing updates to the snow cover each time step according to the amount of incident rainfall ($*R_F$) and snowfall ($*S_F$), air temperature (T_a) and snow compaction rules. b) schematic of ice and snow layers and heat fluxes. Refer to text and Table 1 for definitions of other variables. Here $*R_F = f_R R_x / c_{\text{seconday}}$ and $*S_F = f_S S_x / c_{\text{seconday}}$ if ice cover is present, otherwise they are set to 0 and the model reverts to Eq. 6-7.

The steady-state conduction equations are used with a three-layer ice model that includes blue ice (or black ice), white ice (or snow ice) and snow (see Eq. 1 and Fig. 5 of Rogers et al., 1995), and forced at the surface based on shortwave radiation which is partitioned into two components, a visible (f_{vis}) and an infra red ($1 - f_{\text{vis}}$) spectral band. Blue ice is formed through direct freezing of lake water into ice whereas white ice is generated in response to flooding, when the mass of snow that can be supported by the buoyancy of the ice cover is exceeded (Rogers et al., 1995). By assigning appropriate boundary conditions to the interfaces and solving the quasi-steady state equation for heat transfer numerically, the model computes the upward conductive heat flux through the ice and snow cover to the atmosphere, termed ϕ_0 . The estimation of ϕ_0 applies an empirical equation to estimate snow conductivity, K_{snow} , from its density (Ashton, 1986; Figure 6).

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The estimation of ϕ_0 applies an empirical equation to estimate snow conductivity, K_{snow} , from its density (Ashton, 1986; Figure 6). At the upper solid surface (which could be ice or snow), a heat flux balance is employed to provide the condition for surface melting:

$$\begin{aligned} \phi_0[T_0] + \phi_{net}[T_0] &= 0 & T_0 < T_m \\ \phi_{net}[T_0] &= -\rho_{ice,snow} \lambda_f \frac{d\Delta z_{ice,snow}}{dt} & T_0 = T_m \end{aligned} \quad (2931)$$

$$(32\theta)$$

where λ_f is the latent heat of fusion, $\Delta z_{ice,snow}$ is the height of either the upper snow or ice layer, $\rho_{ice,snow}$ is the density of either the relevant snow or ice layer, determined from the surface medium properties, T_0 is the temperature at the solid surface, T_m is the melt-water temperature (0 °C) and $\phi_{net}[T_0]$ is the net incoming heat flux for non-penetrative penetrative radiation at the solid surface:

$$\phi_{net}[T_0] = \phi_{LWin} - \phi_{LWout}[T_0] + \phi_H[T_0] + \phi_E[T_0] + \phi_R[T_0] \quad (33\pm)$$

where the heat fluxes between the solid boundary and the atmosphere are calculated as outlined previously, but with modification for the determination of vapour pressure over ice or snow ($e_{s_{ice}}[T_0] = e_s[T_0](1 + 9.72 \times 10^{-3} T_0 + 4.2 \times 10^{-5} T_0^2)$; Jeong, 2009), and the addition of the rainfall heat flux, ϕ_R , ($\phi_R = {}^*R_F \rho_w \lambda_f$ to capture the freezing effect if $T_0 < T_m$, or simply as ${}^*R_F c_w \rho_w (T_a - T_0)$ if $T_0 = T_m$; Rogers et al., 1995). To determine the flow of heat through the layers, Rogers et al. (1995) derived:

$$\begin{aligned} \Lambda(\phi_0 - \phi_{SW_0}) &= T_m - T_0 & (34) \\ &- \left\{ f_{VIS} \phi_{SW_0} \left(\frac{(1 - e^{-K_{s1}\Delta z_{snow}})}{K_{snow} K_{s1}} + e^{-K_{s1}\Delta z_{snow}} \frac{(1 - e^{-K_{w1}\Delta z_{white}})}{-K_{w1}\Delta z_{white}} \right. \right. \\ &+ \left. \left. e^{-K_{s1}\Delta z_{snow} - K_{w1}\Delta z_{white}} \frac{(1 - e^{-K_{b1}\Delta z_{blue}})}{-K_{b1}\Delta z_{blue}} \right) \right\} \\ &- \left\{ (1 - f_{VIS}) \phi_{SW_0} \left(\frac{(1 - e^{-K_{s2}\Delta z_{snow}})}{K_{snow} K_{s2}} + e^{-K_{s2}\Delta z_{snow}} \frac{(1 - e^{-K_{w2}\Delta z_{white}})}{-K_{w2}\Delta z_{white}} \right. \right. \\ &+ \left. \left. e^{-K_{s2}\Delta z_{snow} - K_{w2}\Delta z_{white}} \frac{(1 - e^{-K_{b2}\Delta z_{blue}})}{-K_{b2}\Delta z_{blue}} \right) \right\} \\ &+ \phi_{si} \Delta z_{snow} \Lambda - \frac{\phi_{si} \Delta z_{snow}^2}{2K_{snow}} \end{aligned}$$

where $\Lambda = \left(\frac{\Delta z_{snow}}{K_{snow}} + \frac{\Delta z_{white}}{K_{white}} + \frac{\Delta z_{blue}}{K_{blue}} \right)$, ϕ_{SW_0} is the shortwave radiation penetrating the ice/snow surface, K refers to the light attenuation coefficient of the ice and snow components designated with subscripts s , w and b for snow, white ice and blue ice respectively, and the Δz terms refers to the thickness of snow, white ice and blue ice. This is rearranged and solved for T_0 and ϕ_0 by using a bilinear iteration until surface heat fluxes are balanced (i.e., $\phi_0[T_0] = -\phi_{net}[T_0]$) and T_0 is stable (\pm

0.001 °C). In the presence of ice (or snow) cover, a surface temperature $T_0 > T_m$ indicates that energy is available for melting. The amount of energy for melting is calculated by setting $T_0 = T_m$ to determine the reduced thickness of snow or ice (as shown in Eq. 32). The estimation of ϕ_0 applies an empirical equation to estimate snow conductivity, K_{snow} , from its density (Ashton, 1986):

$$K_{snow} = 0.021 + 0.0042 \rho_{snow} + (2.2 \times 10^{-9} \rho_{snow}^3) \quad (35)$$

5

The heat flux in the ice near the ice-water interface is:

$$\begin{aligned} \phi_f = \phi_0 - f_{VIS} \phi_{SW_0} (1 - \exp[-K_{s1} \Delta z_{snow} - K_{w1} \Delta z_{white} - K_{b1} \Delta z_{blue}]) \\ - (1 - f_{VIS}) \phi_{SW_0} (1 - \exp[-K_{s2} \Delta z_{snow} - K_{w2} \Delta z_{white} - K_{b2} \Delta z_{blue}]) \\ - \phi_{si} \Delta z_{snow} \end{aligned} \quad (36)$$

where ϕ_{si} is a volumetric heat flux for the formation of white ice, which is given in Eq. 14 of Rogers et al. (1995) and ice and snow light attenuation coefficients in GLM are also fixed to the same values as those given by Rogers et al. (1995).

10 Shortwave albedo for the ice or snow surface (required for Eq. 10) is a function of surface medium (see Table 1 of Vavrus et al., 1996) with values varying from 0.08 to 0.6 for ice and from 0.08 to 0.7 for snow, depending on the surface temperature and their layer thickness.

Accretion or ablation of blue ice occurs at the ice-water boundary based on the conductive heat flux from water into the ice,

15 ϕ_{w_2} as given by the finite difference approximation: where ϕ_{SW_0} is the shortwave radiation penetrating the ice/snow surface, K refers to the light attenuation coefficient of the ice and snow components designated with subscripts s , w and b for snow, white ice and blue ice respectively, and Δz refers to the thickness of snow, white ice and blue ice. ϕ_{white}^* is a volumetric heat flux for the formation of snow ice, which is given in Eq. 14 of Rogers et al. (1995). Ice and snow light attenuation coefficients in GLM are fixed to the same values as those given by Rogers et al. (1995). Shortwave albedo for the ice or
 20 snow surface is a function of surface medium (snow or ice), surface temperature and ice or snow thickness (see Table 1 of Vavrus et al., 1996). Values of albedo derived from these functions vary from 0.08 to 0.6 for ice and from 0.08 to 0.7 for snow, depending on the surface temperature and their layer thickness.

$$\phi_w = -K_{water} \frac{\Delta T}{\delta_{wi}}, \quad (37)$$

25 where K_{water} is the molecular conductivity of water (assuming the water is stagnant under the ice), and ΔT is the temperature difference between the surface water of the lake and the bottom of the blue ice layer, $T_m - T_s$. This occurs across an assigned length scale, δ_{wi} , for which a value of 0.1–0.5 m is usual, based on the reasoning given in Rogers et al. (1995) and the typical vertical water layer resolution of a model simulation (0.125–1.5 m). Note that a wide variation in

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techniques and values are used to determine the basal heat flux immediately beneath the ice pack (e.g., Harvey, 1990) which suggests that this may need careful consideration during calibration.

5 The imbalance between ϕ_f moving through the blue ice layer and the heat flux from the water into the ice, ϕ_w , gives the rate of change of ice thickness at the interface with water:

$$\frac{d\Delta z_{blue}}{dt} = \frac{\phi_f - \phi_w}{\rho_{blue} \lambda_f} \quad (383)$$

~~where ρ_{blue} is the density of blue ice and ϕ_w is given by a finite difference approximation of the conductive heat flux from water to ice:~~

$$\phi_w = -K_{water} \frac{\Delta T}{\delta_{wi}}, \quad (34)$$

10 ~~where K_{water} is molecular conductivity of water (assuming the water is stagnant), and ΔT is the temperature difference between the surface water of the lake and the bottom of the blue ice layer, $T_m - T_s$. This occurs across an assigned length-scale δ_{wi} , for which a value of 0.1–0.5 m is usual, based on the reasoning given in Rogers *et al.* (1995) and the typical vertical water layer resolution of a model simulation (0.125–1.5 m). Note that a wide variation in techniques and values is used to determine the basal heat flux immediately beneath the ice pack (e.g., Harvey, 1990) which suggests that this may need careful consideration during calibration.~~

15

~~Figure 6 summarizes the algorithm to update ice cover, snow cover and water depth. The ice cover equations are applied when water temperature first drops below 0 °C. The ice thickness is set to its minimum value of 0.05 m, which is suggested by Patterson and Hamblin (1988) and Vavrus *et al.* (1996). The need for a minimum ice thickness relates primarily to horizontal variability of ice cover during the formation and closure periods. The ice cover equations are discontinued and open water conditions are restored in the model when the thermodynamic balance first produces ice thickness < 0.05 m. Example outputs are shown in Figure 7; and see also Yao *et al.* (2014) for a previous application.~~

20

2.5 Sediment heating

25 The water column thermal budget may also be affected by heating or cooling from the soil/sediment below. For each layer, the rate of temperature change depends on the temperature gradient and the relative area of the layer volume in contact with bottom sediment:

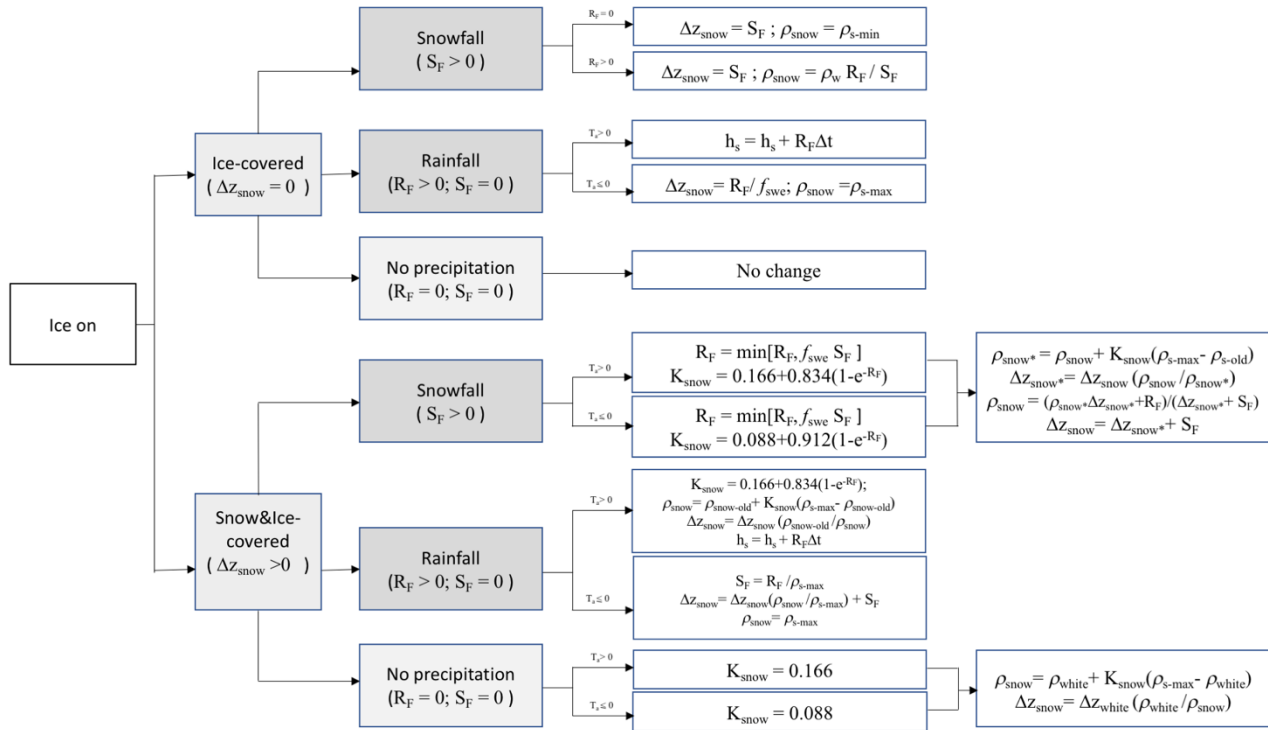


Figure 6: Decision tree to update snow cover and water depth according to snow compaction, rainfall (R_F) and snowfall (S_F) each time step. Refer to text and Table 1 for definitions of other variables.

- 5 After the change in ice thickness due to heat exchange is calculated, the effects of snowfall, rainfall, and compaction of snow are calculated through appropriate choice of one of several options, depending on the air temperature and whether ice or snow is the upper solid boundary (Figure 6). Density of fresh snowfall is determined as the ratio of measured snowfall height to water equivalent height, with any values exceeding the assigned maximum or minimum snow density (defaults: $\rho_{s\text{-max}} = 300 \text{ kg m}^{-3}$; $\rho_{s\text{-min}} = 50 \text{ kg m}^{-3}$) truncated to the appropriate limit. The snow compaction model is based on the exponential decay formula of McKay (1968), with selection of snow compaction parameters based on air temperature (Rogers et al., 1995) as well as on rainfall or snowfall. The approach of snow compaction used by Rogers et al. (1995) is to set the residual snow density to its maximum value when there is fresh snowfall. This method is found to produce increases in snow density that are too rapid when there is only light snowfall. As a result, GLM uses a gradual approach where the new snowfall and the existing snow is used to form a layer with a combined mass and average density. Example outputs are shown in Figure 7, and see also Yao et al. (2014) for a previous application.
- 10
- 15

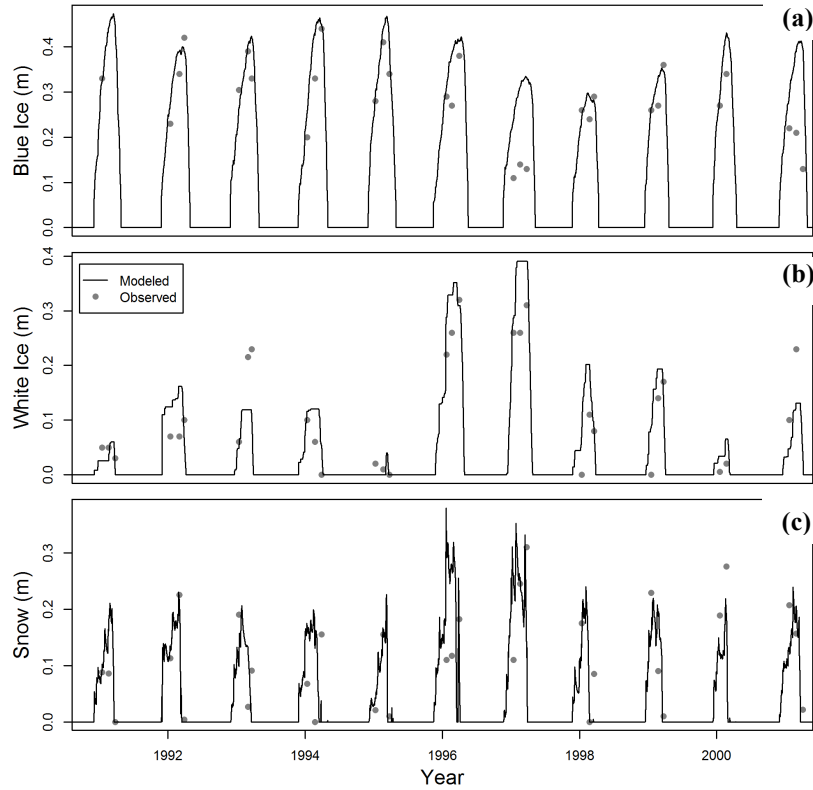


Figure 7: Example of modelled and observed thickness of (a) blue ice, Δz_{blue} , (b) white ice, Δz_{white} , and (c) snow, Δz_{snow} , for Sparkling Lake, Wisconsin. Points are the average observed thicknesses.

5

$$c_w \rho_i \Delta V_i \frac{dT_i}{dt} = K_{soil} \frac{(T_{z_i} - T_i)}{\delta z_{soil}} (A_i - A_{i-1}) \quad (395)$$

where K_{soil} is the soil/sediment thermal conductivity and δz_{soil} is the length scale associated with the heat flux. The temperature of the bottom sediment varies seasonally, and also depending on its depth below the water surface, such that:

$$T_{z_i} = T_{z_{mean}} + \delta T_z \cos \left[\frac{2\pi}{365} (d - d_{T_z}) \right] \quad (4036)$$

10 where z is the soil/sediment zone that the i^{th} layer overlays (see Section 4 for details), T_{z_i} , is the temperature of this zone, $T_{z_{mean}}$ is the annual mean sediment zone temperature, δT_z is the seasonal amplitude of the soil temperature variation, and d_{T_z} is the day of the year when the soil temperature peaks. By defining different sediment zones, the model can therefore allow for a different mean and amplitude of littoral waters compared to deeper waters. A dynamic sediment temperature diffusion model is also under development, which will be [available-suitable](#) when empirical data for the above parameters in
 15 Eq. [36-40](#) is not [possibleavailable](#).

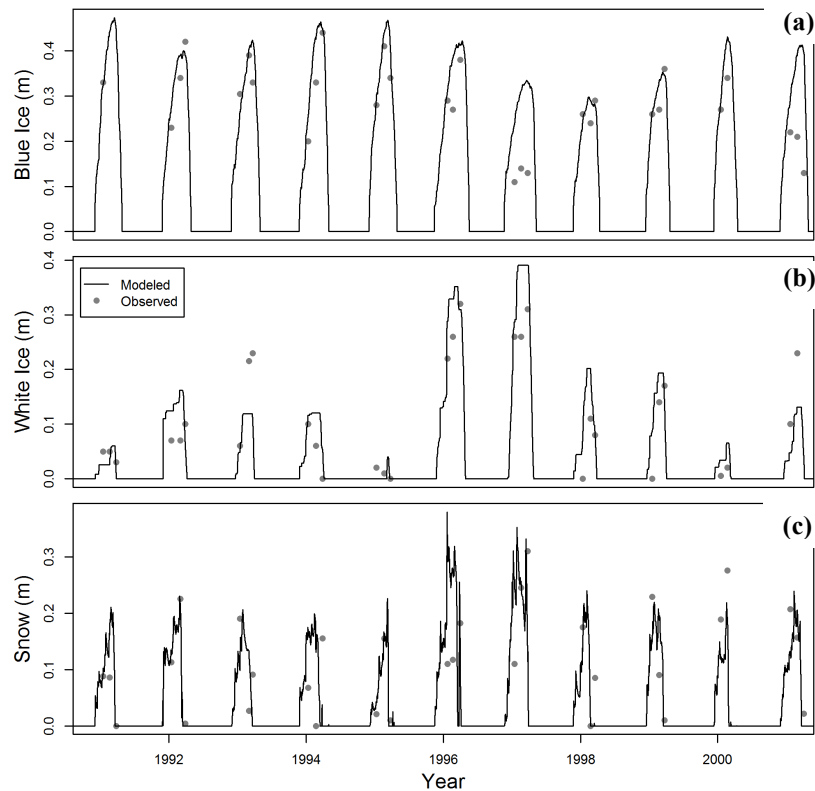


Figure 7: Example of modelled and observed thickness of (a) blue ice, Δz_{blue} , (b) white ice, Δz_{white} , and (c) snow, Δz_{snow} , for Sparkling Lake, Wisconsin. Points are the average observed thicknesses.

5 2.6 Stratification and vertical mixing

Mixing processes in lakes are varied and depend upon the degree of meteorological and hydrological forcing, the lake morphometry, and nature of thermal stratification experienced by the lake at the time of forcing. Numerous models adopt an eddy-diffusivity approach whereby mixing is captured using the advection-dispersion equation (e.g., Riley and Stefan, 1988). GLM adopts an energy balance approach as used in DYRESM whereby the mixing dynamics are based on estimating the amount of turbulent energy available, which are separately computed for the surface mixed layer (surface mixing), and for mixing below the thermocline (deep mixing).

2.6.1 Surface mixed layer

To compute mixing of layers, GLM works on the premise that the balance between the available energy, E_{TKE} , and the energy required for mixing to occur, E_{PE} , provides for the surface mixed layer (sml) deepening rate dz_{sml}/dt , where z_{sml} is the thickness-depth from the surface to the bottom of the surface mixed layer. For an overview of the dynamics, readers are referred to early works on bulk mixed layer depth models by Kraus and Turner (1967) and Kim (1976), which were subsequently extended by Imberger and Patterson (1981) and Spigel et al. (1986) as a basis for hydrodynamic model design.

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Using this approach, the available kinetic energy is calculated due to contributions from wind stirring, convective overturn, shear production between layers, and Kelvin-Helmholtz (K-H) billowing. ~~They may be combined and summarised~~ Overall, ~~the turbulent energy generated for mixing~~ is (Hamilton and Schladow, 1997):

$$E_{TKE} = \underbrace{\frac{0.5C_K(w_*^3) \Delta t}{\text{convective overturn}}}_{\text{convective overturn}} + \underbrace{\frac{0.5C_K(C_W u_*^3) \Delta t}{\text{wind stirring}}}_{\text{wind stirring}} + \underbrace{0.5 C_S \left[u_b^2 + \frac{u_b^2 d \delta_{KH}}{6 dz_{sml}} + \frac{u_b \delta_{KH}}{3} \frac{du_b}{dz_{sml}} \right]}_{\substack{\text{shear production} \\ \text{K-H production}}} \Delta z_{k-1} \quad (4137)$$

where δ_{KH} is the K-H billow length scale (described below), u_b is the shear velocity at the interface of the mixed layer, and C_K , C_W , and C_S are mixing efficiency constants. For mixing to occur, the energy must be sufficient to lift up water in the layer below the bottom of the mixed layer, denoted here as the layer $k - 1$, with thickness Δz_{k-1} , and accelerate it to the mixed layer velocity, u_* . This must also accounts for energy consumption associated with K-H billowing. In total, the energy required to entrain a layer into the mixed layer ~~production and is~~ expressed as: E_{PE} :

$$E_{PE} = \left[\underbrace{\frac{0.5C_T(w_*^3 + C_W u_*^3)^{2/3}}{\text{acceleration}}}_{\text{acceleration}} + \underbrace{\frac{\Delta \rho}{\rho_o} g z_{sml}}_{\text{lifting}} + \underbrace{\frac{g \delta_{KH}^2 d(\Delta \rho)}{24 \rho_o dz_{sml}} + \frac{g \delta_{KH} \Delta \rho d \delta_{KH}}{12 \rho_o dz_{sml}}}_{\text{K-H consumption}} \right] \Delta z_{k-1} \quad (4238)$$

To numerically resolve Eq. ~~37-41~~ and ~~38-42~~ the model sequentially computes the different components of the above expressions with respect to the layer structure, checking the available energy relative to the required amount (depicted schematically in Figure 8). GLM follows the sequence of the algorithm presented in detail in Imberger and Patterson (1981), whereby layers are combined due to convection and wind stirring first, and then the resultant mixed layer properties are used when subsequently computing the extent of shear mixing and the effect of K-H instabilities. Plots indicating the role of mixing in shaping the thermal structure of the example lakes are shown in Figure ~~98~~.

To compute the mixing energy available due to convection, in the first step, the value for w_* is calculated, which is the turbulent velocity scale associated with convection brought about by cooling at the air-water interface. The model adopts the algorithm used in Imberger and Patterson (1981), whereby the potential energy that would be released by mixed layer deepening is computed as the difference in the ~~from the first~~ moments of the layer masses in the epilimnion (surface mixed layer) about the lake bottom, relative to the well-mixed condition; ~~which~~ This is numerically computed by summing from the bottom-most layer of the epilimnion, k , up to N_{LEV} :

$$w_*^3 = \frac{g}{\rho_{sml} \Delta t} \sum_{i=k}^{N_{LEV}} [(\rho_i \Delta z_i) (\tilde{h}_i - \widetilde{h_{sml}})] \left(\sum_{i=k}^{N_{LEV}} [\rho_i \Delta z_i \tilde{h}_i] - \widetilde{h_{sml}} \sum_{i=k}^{N_{LEV}} [\rho_i \Delta z_i] \right) \quad (4339)$$

where ρ_{sml} is the mean density of the mixed layer including the combined layer, ρ_k is the density of the k^{th} layer, Δz_i is the height difference between two consecutive layers within the loop ($\Delta z_i = h_i - h_{i-1}$), \tilde{h}_i is the mean height of layers to be mixed ($\tilde{h}_i = 0.5[h_i + h_{i-1}]$), and $\widetilde{h_{sml}}$ is the epilimnion mid height, calculated as: $\widetilde{h_{sml}} = 0.5(h_s + h_{k-1})$.

The velocity scale u_* of the surface layer is associated with wind stress and calculated according to the wind strength:

$$u_*^2 = \frac{\rho_a}{\rho_{sml}} C_D U_{10}^2 \quad (440)$$

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where C_D is the drag coefficient for momentum. The model first checks to see if the energy available from Eqs. 3943 and 4044 can overcome the energy required to mix the $k - 1$ layer into the surface mixed layer (Figure 8e); i.e., mixing of $k - 1$ occurs if:

$$C_K(w_*^3 + C_W u_*^3) \Delta t \geq (g'_k z_{sml} + C_T(w_*^3 + C_W u_*^3)^{2/3}) \Delta z_{k-1} \quad (454)$$

where $g'_k = g \frac{\Delta \rho}{\rho_0}$ is the reduced gravity between the mixed layer and the $k - 1$ layer, calculated as $g (\rho_{sml} - \rho_{k-1}) / (0.5(\rho_{sml} + \rho_{k-1}))$. If the mixing condition is met the layers are combined, the energy required to combine the layer is removed from the available energy, k is adjusted, and the loop continues to the next layer. Where the mixing energy is substantial and the mixing reaches the bottom layer, then the mixing routine ends. If the condition in Eq. 4445 is not met, then ~~the any residual~~ energy is stored for the next time step, and the mixing algorithm continues as outlined below.

10

Once stirring is completed, mixing ~~due that is generated due~~ to velocity shear is ~~applied accounted for~~. Parameterising the shear velocity, ~~denoted u_b~~ , in a one-dimensional model ~~is can be problematic, difficult, but however~~ the approximation used in Imberger and Patterson (1981) is applied, ~~whereby~~:

$$u_b = \begin{cases} \frac{u_*^2 \Delta t}{z_{sml}} + u_{b_{old}}, & t \leq t_b + \delta t_{shear} \\ 0, & t > t_b + \delta t_{shear} \end{cases} \quad (4246)$$

15

~~where $u_{b_{old}}$ is from the previous time step, and zeroed between shear (wind) events. Therefore, this such that there is model will yield~~ a simple linear increase in the shear velocity over time for a constant wind stress. ~~This, is~~ considered relative to δt_{shear} , which is the cut-off time, ~~beyond this time which~~ it is assumed no further shear-induced mixing occurs for that event. ~~The velocity $u_{b_{old}}$ is from the previous time step, and zeroed between shear events.~~ This cut-off time assumes use of only the energy produced by shear at the interface during a period equivalent to half the basin-scale seiche duration, δt_{iw} , which can be modified to account for damping (Spigel, 1978):

20

$$\delta t_{shear} = \begin{cases} 1.59 \delta t_{iw} & \frac{\delta t_{damp}}{\delta t_{iw}} \geq 10 \\ \left(1 + 0.59 \left[1 - \cosh \left(\frac{\delta t_{damp}}{\delta t_{iw}} - 1 \right) \right] \right) \delta t_{iw} & \frac{\delta t_{damp}}{\delta t_{iw}} < 10 \end{cases} \quad (4347)$$

where δt_{damp} is the time scale of damping. The wave period is approximated based on the stratification as $\delta t_{iw} = L_{META} / 2c$, where L_{META} is the length of the basin at the thermocline, calculated from $\sqrt{A_{k-1}(4/\pi)(L_{crest}/W_{crest})}$, and c is the internal wave speed:

$$c = \sqrt{|g'_{EH}| \frac{\delta_{epi} \delta_{hyp}}{(\delta_{epi} + \delta_{hyp})}} \quad (484)$$

25 where δ_{epi} and δ_{hyp} are characteristic vertical length scales associated with the epilimnion and hypolimnion:



$$\delta_{epi} = \frac{\Delta V_{epi}}{0.5(A_s + A_{k-1})} ; \delta_{hyp} = \frac{V_{k-1}}{0.5A_{k-1}} \quad (495)$$

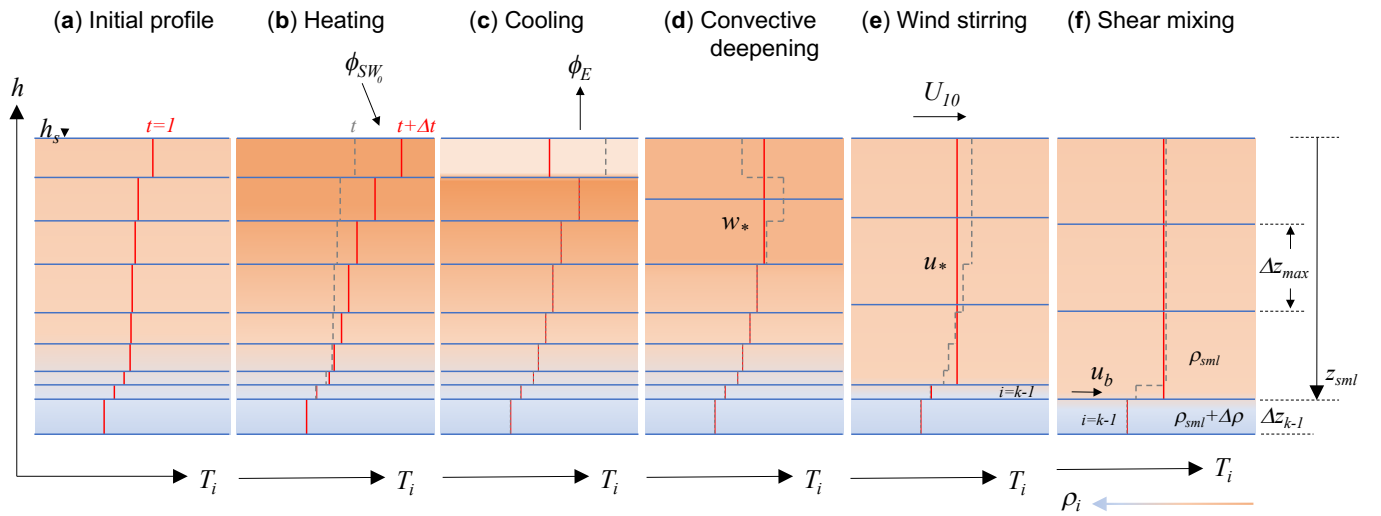


Figure 8: Schematic depiction of layer changes during stratification and mixing. Consecutive panels show changes from a) the initial layer and thermal profile, to b) heating due to solar radiation, to c) evaporative cooling, which creates d) convective mixing, which is followed by e) a wind event causing stirring, and f) shear mixing across the thermocline.

The time for damping of internal waves in a two-layer system can be parameterised by estimating the length scale of the oscillating boundary layer, through which the wave energy dissipates, and the period of the internal standing wave (see Spiegel and Imberger, 1980):

$$\delta t_{damp} = \frac{\sqrt{v_w}}{c_{damp} \delta_{ss}} \frac{2(\delta_{epi} + \delta_{hyp})}{u_*^2} \sqrt{\frac{c}{2 L_{META}}} \frac{\delta_{hyp}}{\delta_{epi}} (\delta_{epi} + \delta_{hyp}) \quad (4650)$$

Once the velocity is computed from Eq. 462, the energy for mixing from velocity shear is compared to that required for lifting and accelerating the next layer down, and layers are combined if there is sufficient energy, i.e. when:

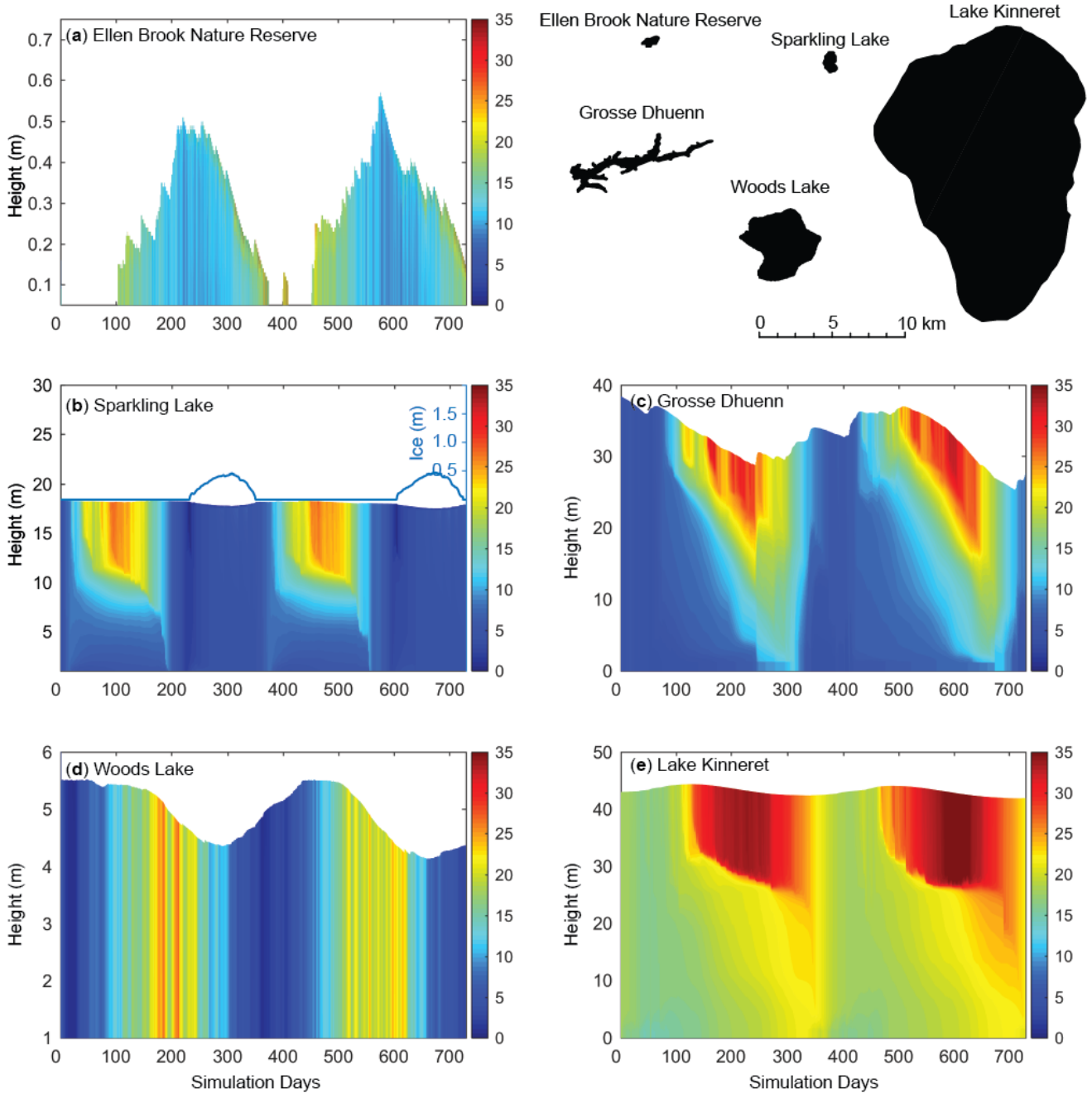
$$0.5 C_S \left[\frac{u_b^2 (z_{sml} + \Delta \delta_{KH})}{6} + \frac{u_b \delta_{KH} \Delta u_b}{3} \right] + \left[g'_k \delta_{KH} \left(\frac{\delta_{KH} \Delta z_{k-1}}{24 z_{sml}} - \frac{\Delta \delta_{KH}}{12} \right) \right] \geq (g'_k z_{sml} + C_T (w_*^3 + C_W u_*^3)^{2/3}) \Delta z_{k-1} \quad (5147)$$

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where the billow length scale is $\delta_{KH} = C_{KH} u_b^2 / g'_{EH}$ and $\Delta\delta_{KH} = 2 C_{KH} u_b \Delta u_b / g'_{EH}$; in this case the reduced gravity is computed from the difference between the epilimnion and hypolimnion, and C_{KH} is a measure of the billow mixing efficiency.

- 5 Once shear mixing is done, the model checks the resultant density interface to see if it is unstable to shear, such that K-H billows would be expected to form, i.e., if the metalimnion thickness is less than the K-H length scale, δ_{KH} . If K-H mixing is required, layers are further split and a linear density profile is set over the metalimnion.

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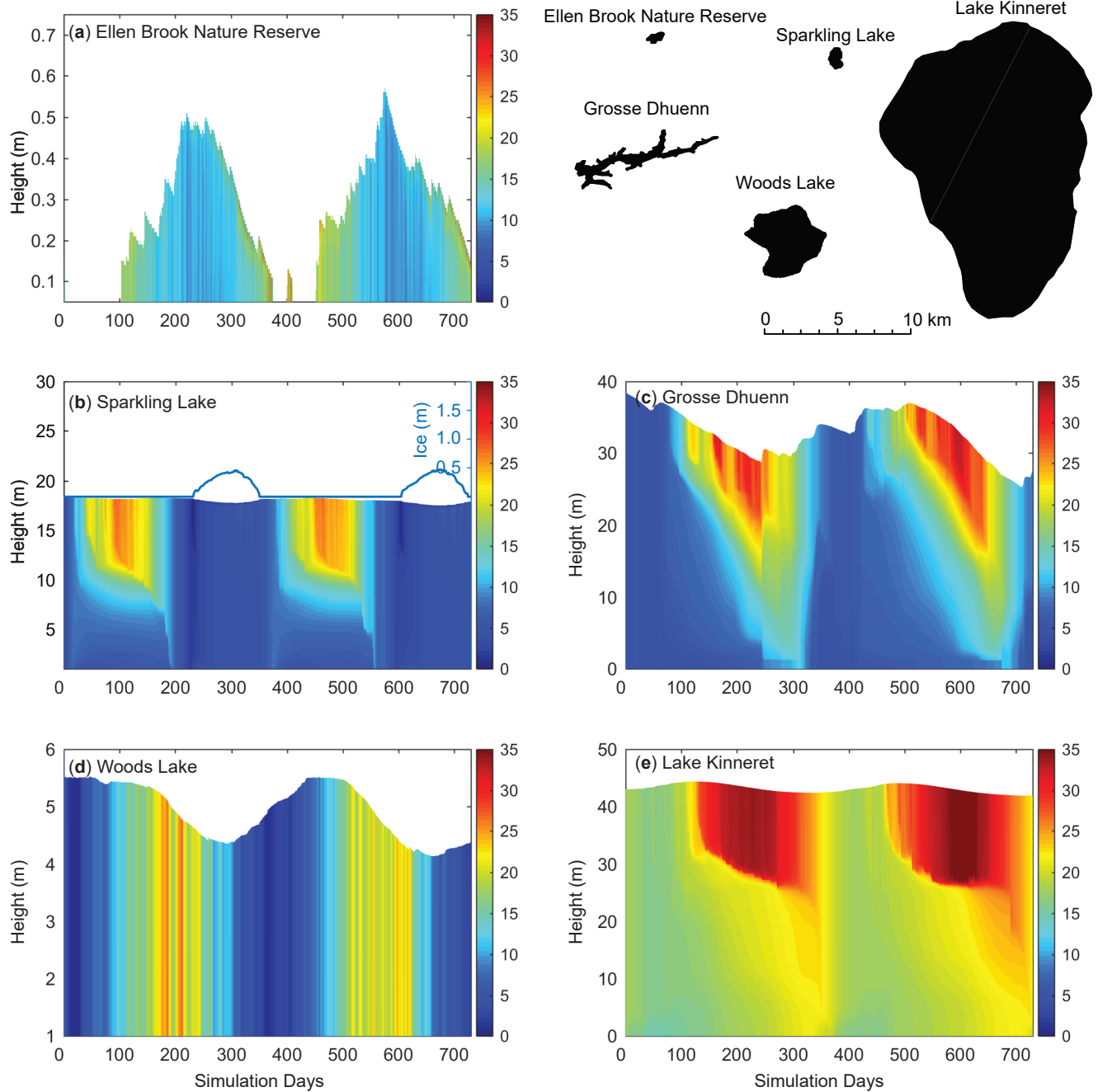


Figure 89: A two-year time-series of the simulated temperature profiles for five example lakes, a-e, that range in size and hydrology. For more information about each lake and the simulation configuration refer to the Data availability section (refer also to Fig. 2 and 5). Sparkling Lake (d) also indicates the simulated depth of ice on the RHS scale.

2.6.2 Deep mixing

Mixing below the ~~epilimnion-thermocline~~ in lakes, in the deeper ~~stratified regions~~~~hypolimnion-of the water column~~, is modelled using a characteristic vertical diffusivity, $D_z = D_\epsilon + D_m$, where D_m is a constant molecular diffusivity for scalars and D_ϵ is the turbulent diffusivity. Three hypolimnetic mixing options are possible in GLM including: (1) no diffusivity, $D_z = 0$, (2) a constant vertical diffusivity D_z over the water depth below the ~~thermocline-surface mixed layer~~ or (3) a derivation by Weinstock (1981) used in DYRESM, which is described as being suitable for regions displaying weak or strong stratification, whereby diffusivity increases with dissipation and decreases with heightened stratification.

For the constant vertical diffusivity option, the coefficient $C_{HYP} \alpha_{TKE}$ is interpreted as the vertical diffusivity ($\text{m}^2 \text{s}^{-1}$), i.e., $D_z = C_{HYP}$, and applied uniformly below the surface mixed layer. For the Weinstock (1981) model, the diffusivity is computed varies depending on the strength of stratification and the rate of turbulent dissipation, according to:

$$D_z = \frac{C_{HYP} \epsilon_{TKE}}{N^2 + 0.6 k_{TKE}^2 u_*^2} \quad (48/52)$$

where C_{HYP} in this case is the mixing efficiency of hypolimnetic TKE (~ 0.8 in Weinstock, 1981) and u_* is defined as above. N^2 is the Brunt-Väisälä (buoyancy) frequency defined for a given layer as:

$$N^2_i = \frac{g \Delta \rho}{\rho \Delta z} \approx \frac{g(\rho_{i+2} - \rho_{i-2})}{\rho_{ref}(h_{i+2} - h_{i-2})} \quad (49)$$

where ρ_{ref} is the average of the layer densities. This is computed from layer 3 upwards, averaging over the span of 5 layers, until the vertical density gradient exceeds a set tolerance. k_{TKE} is the turbulence wavenumber:

$$k_{TKE}^2 = \frac{\epsilon_{wn} A_s}{\tilde{V}_{N^2} \Delta z_{smt}} \quad (50)$$

The stratification strength is computed using the Brunt-Väisälä (buoyancy) frequency, N^2 , defined for a given layer as:

$$N^2_i = \frac{g \Delta \rho}{\rho \Delta z} \approx \frac{g(\rho_{i-2} - \rho_{i+2})}{\rho_{ref}(h_{i+2} - h_{i-2})} \quad (53)$$

where ρ_{ref} is the average of the layer densities. This is computed from layer 3 upwards, averaging over the span of 5 layers, until the vertical density gradient exceeds a set tolerance. N^2 varies following an approximate normal distribution with height, centred at the height where the centre of buoyancy is located, computed each time-step from the 1st moment of the vertical N^2 distribution. Additionally, we estimate the vertical length scale associated with one standard deviation about the centre of the N^2 distribution, denoted δz_{σ} .

where \tilde{V}_{N^2} is a fractional volume of the lake that contains 85% of N^2 . The diffusivity increases in line with the turbulent dissipation rate. This can be complex to estimate in stratified lakes, however, GLM adopts a simple approach as

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described in Fischer et al. (1979) where a “net dissipation” is approximated by assuming dissipation is in equilibrium with energy inputs from external [drivers/forcing](#):

$$\varepsilon_{TKE} \approx \overline{\varepsilon_{TKE}} = \varepsilon_{WIND} + \varepsilon_{INFLOW} \quad (5154)$$

5 which is expanded and calculated per unit mass as:

$$\overline{\varepsilon_{TKE}} = \underbrace{\frac{1}{\tilde{V}_{N^2} \bar{\rho}} m C_D \rho_a U_{10}^3 A_s}_{\text{rate of working by wind}} + \underbrace{\frac{1}{(\tilde{V}_{N^2} - \Delta V_S) \bar{\rho}} \sum_I^{N_{INF}} g (\rho_{ins_I} - \rho_{i_{ins_I}}) Q_{inf_{ins_I}} ((h_s - z_{inf_{ins_I}}) - h_{i_{ins_I}-1})}_{\text{rate of work done by inflows}} \quad (5255)$$

where $\bar{\rho} = 0.5(\rho_1 + \rho_{N_{LEV}})$ is the mean density of the water column. The work done by inflows is computed based on the flow rate, [the and considers the](#) depth the inflow plunges to, and the [density difference/difference in density between the inflow water and layer into which it inserts](#), summed over all configured inflows. [These sources are normalised over the mass of water contained above the area of mixing. This is estimated using \$\tilde{V}_{N^2}\$, which is the fractional volume of the lake that is contained above the height that corresponds to being one standard deviation below the centre of buoyancy, and is therefore the volume of the lake over which 85% of the \$N^2\$ variance is captured. The turbulence wavenumber, \$k_{TKE}\$, is then estimated from:](#)

$$k_{TKE}^2 = \frac{c_{wn} A_s}{\tilde{V}_{N^2} \Delta z_{sml}} \quad (56)$$

where c_{wn} is a coefficient.

Since the dissipation is assumed to concentrate close to the level of strongest stratification, the “mean” diffusivity [from suggested by](#) Eq. [5248](#) is modified to decay exponentially within the layers as they increase their distance from the thermocline:

$$D_{z_i} = \begin{cases} 0 & -h_i \geq (h_s - z_{sml}) \\ \frac{C_{HYP} \overline{\varepsilon_{TKE}}}{N^2_i + 0.6 k_{TKE}^2 u_*^2} D_{\bar{z}} \exp \left[-\frac{(h_s - z_{sml} - h_i)^2}{\delta z_{\sigma}^2} - \frac{(h_s - z_{sml} - h_i)^2}{\sigma} \right] & h_i < (h_s - z_{sml}) \end{cases} \quad (573)$$

where δz_{σ} is [the variance of the \$N^2\$ distribution below the bottom of the mixed layer, \$h_s - z_{sml}\$, and used to this](#) scales the depth over which the mixing is assumed to decay [below the bottom of the mixed layer, \$h_s - z_{sml}\$.](#)

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Once the diffusivity is approximated (~~for~~ either [using a constant value model](#) or [Eq. 57](#)), the diffusion of any scalar, C (including [temperature](#), [salinity](#) and [any water quality attributes](#)), between two layers is numerically accounted for by the following mass transfer expressions:

$$C_{i+1} = \bar{C} + e^{-f_{dif}} \frac{\Delta z_i \Delta C}{(\Delta z_{i+1} + \Delta z_i)} \quad (58a,b)$$

$$C_i = \bar{C} - e^{-f_{dif}} \frac{\Delta z_{i+1} \Delta C}{(\Delta z_{i+1} + \Delta z_i)}$$

- 5 where \bar{C} is the weighted mean concentration of C for the two layers, and ΔC is the concentration difference between them. The smoothing function, f_{dif} , is related to the diffusivity according to:

$$f_{dif} = \frac{D_{z_{i+1}} + D_{z_i}}{(\Delta z_{i+1} + \Delta z_i)^2} \Delta t \quad (59)$$

- and the above diffusion algorithm is run once up the water column and once down the water column as a simple explicit
 10 method for capturing diffusion of mass to both the upper and lower layers. An example of the effect of hypolimnetic mixing on a hypothetical scalar concentration released ~~into~~ [from the sediment to the water column layers and accumulating in the](#) hypolimnion is shown in Figure [109](#).

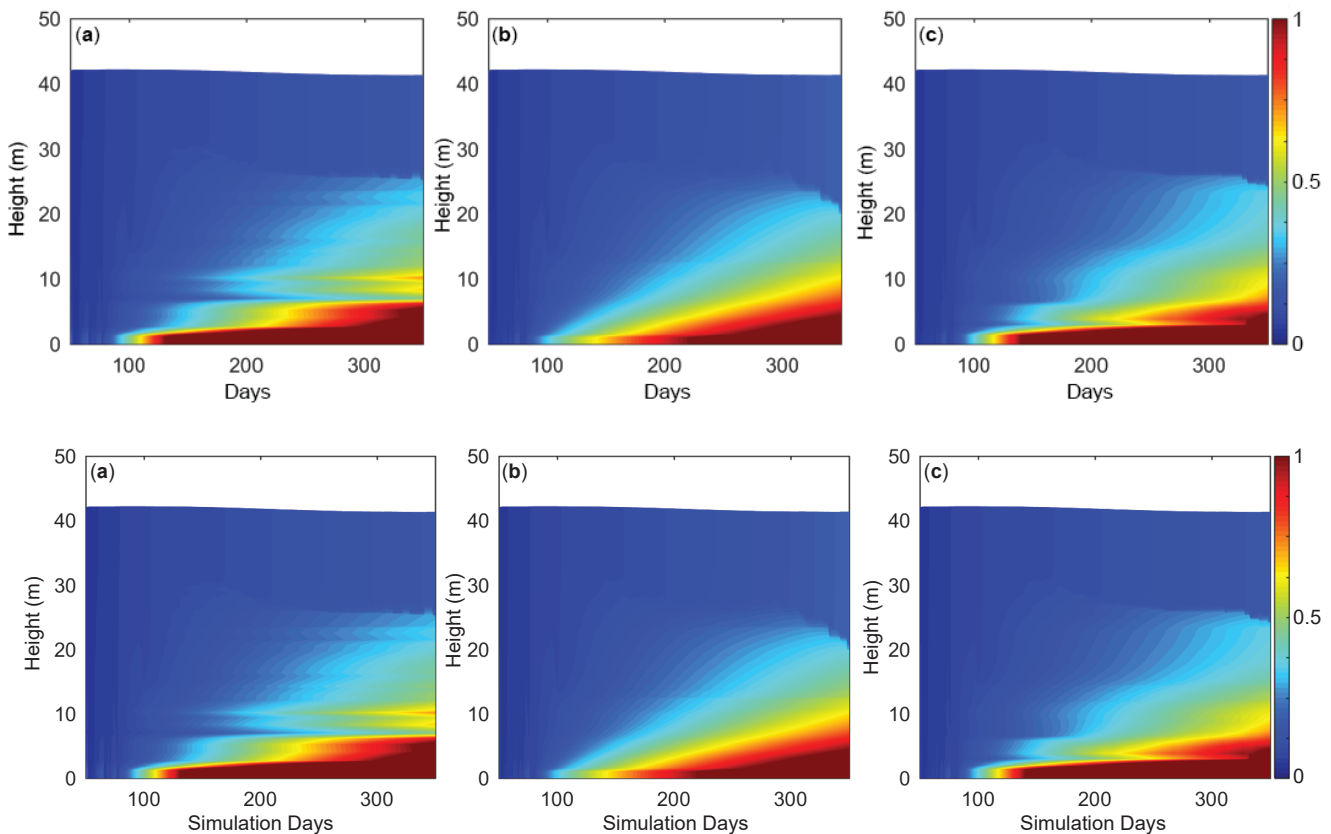




Figure 910: Example simulations for Lake Kinneret showing the hypolimnetic concentration of a passive tracer (normalised units) released from the sediment into the bottom-water layers at a constant rate for the case: a) without deep mixing, b) with a constant vertical diffusivity, $D_z = 2 \times 10^{-6} \text{ m}^2 \text{ s}^{-1}$, and c) with the depth-dependent calculated vertical diffusivity formulation (Eq. 4857). The thermal structure for this case is in Figure 8c.

5

2.7 Inflows and outflows

Aside from the surface fluxes of water described above, the water balance of a lake is controlled by the specifics of the inflows and outflows. Inflows can be specified as local runoff from the surrounding (dry) lake domain (Q_R described separately above, Eq. 87), rivers entering at the surface of the lake that will be buoyant or plunge depending on their momentum and density (Section 2.7.1), or submerged inflows (including groundwater) that enter at depth (Section 2.7.2). Four options for outflows are included in GLM. These include withdrawals from a specified depth (Section 2.7.3), adaptive offtake (Section 2.7.4), vertical groundwater seepage (Section 2.7.5), and river outflow/overflow from the surface of the lake (Section 2.7.6). Any number of lake inflows and outflows can be specified and, except for the local runoff term, all are applied at a daily time step. Depending on the specific settings of each, these water fluxes can impact the volume of the individual layers, ΔV_i , as well as the overall lake volume (Eq. 4).

10

15

2.7.1 River inflows

As water from an inflowing river connects with a lake or reservoir environment, it will form a positively or negatively buoyant intrusion depending on the density of the incoming river water in the context of the water column stratification. As the inflow progresses towards insertion, it will entrain water at a rate depending on the turbulence created by the inflowing water mass (Fischer et al., 1979). For each configured inflow the characteristic rate of entrainment coefficient of the intrusion, E_{inf} , is computed based on the bottom drag being experienced by the inflowing water, C_{Dinf} , and the water stability using the approximation given in Imberger and Patterson (1981) as written in Ayala et al. (2014) Fischer et al. (1979):

20

$$E_{inf} = 1.6 \frac{C_{Dinf}^{3/2}}{Ri_{inf}} \quad (6056)$$

where the inflow where C_{Dinf} is the user-specified drag coefficient for the inflow. The inflow Richardson number, Ri_{inf} , characterises the stability of the water in the context of the inflow channel geometry. Imberger and Patterson (1981) (Fischer et al., 1979), computed derived a simple estimate based on the drag coefficient by assuming the velocity (and Froude number) is typically small and considering the channel geometry, which is adapted in GLM as:

25

$$Ri_{inf} = \frac{C_{Dinf} \left(1 + 0.21 \sqrt{C_{Dinf}} \sin \alpha_{inf} \right)}{\sin \alpha_{inf} \tan \phi_{inf}} \quad (6157)$$

where α_{inf} is the stream half angle assuming an approximate triangular cross-section, and ϕ_{inf} is the tangent angle of the slope of the inflow thalweg relative to horizontal, at the point in the region where it meets the water body (Figure 110).

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Therefore, using Eq. 60 and 61, a simple approximation of stream geometry and bottom roughness can be used to parameterise the characteristic rate of entrainment as it enters the waterbody.

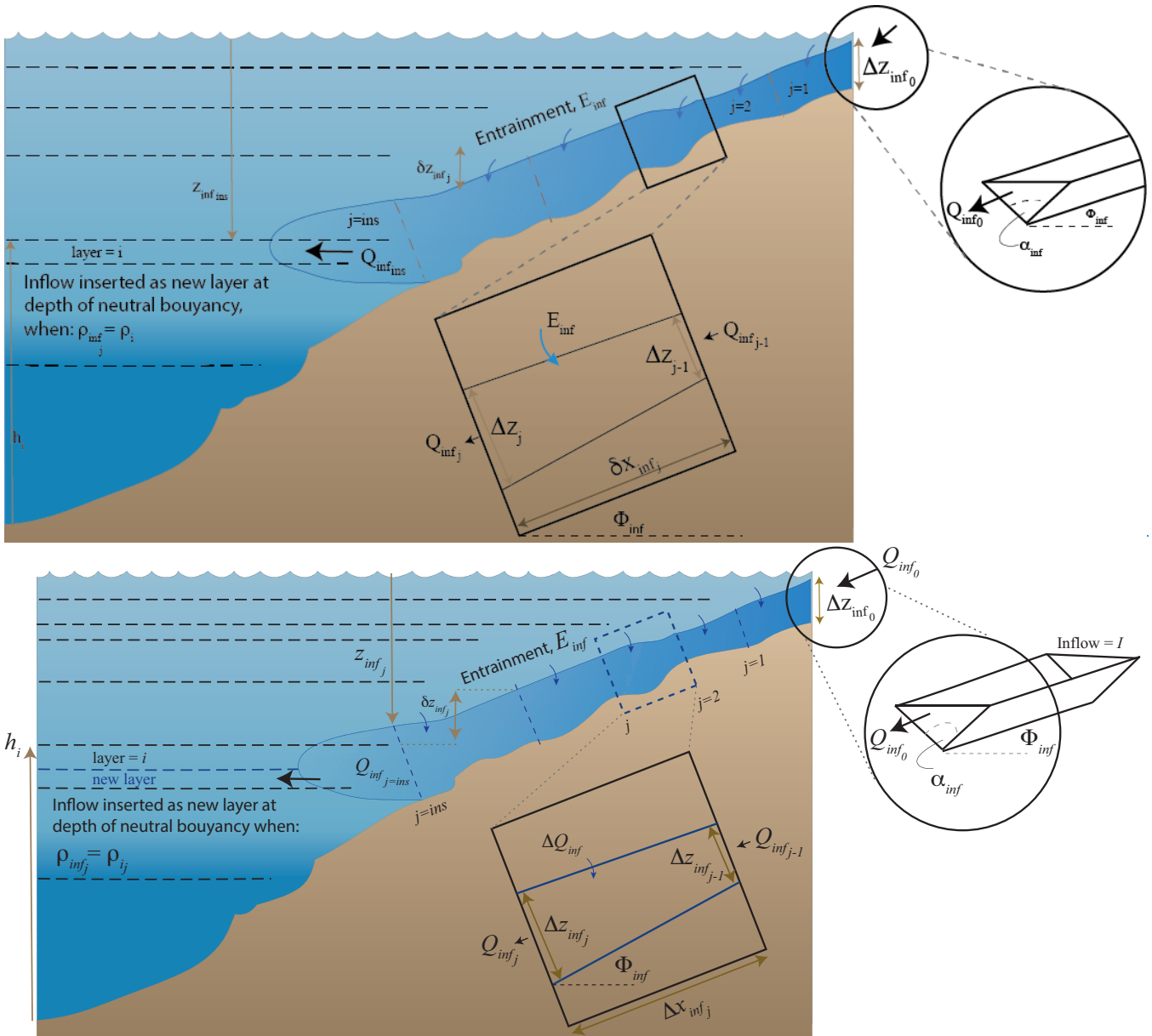


Figure 1011: Schematic showing inflow insertion depth, entrainment, E_{inf} , slope, Φ_{inf} and half-bottom slope angle, α_{inf_2} of an inflowing river, I , entering with a prescribed at a flow rate of Q_{inf_0} , and estimated starting starting thickness of Δz_{inf_0} .

- 10 On entry, the inflow algorithm captures two phases: first, the inflowing water crosses the layers of the lake until it reaches a level of neutral buoyancy, and second, it then undergoes insertion. In the first part of the algorithm, the daily inflow parcel is

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tracked down the lake-bed and its mixing with layers is updated until it is deemed ready for insertion. The initial estimate of the intrusion thickness, Δz_{inf_0} , is computed ~~from as in~~ Antenucci et al. (2005) and Ayala et al. (2014):

$$\Delta z_{inf_0} = \left(2 \frac{Ri_{inf}}{g'_{inf}} \left(\frac{Q_{inf_0}}{\tan \alpha_{inf}} \right)^2 \right)^{1/5} \quad (5862)$$

where $Q_{inf_0} = f_{inf} Q_{inf_x} / c_{secday}$ is the inflow discharge entering the domain, based on the data provided as a boundary condition, Q_{inf_x} , and g' is the reduced gravity of the inflow as it enters:

$$g'_{inf} = g \frac{(\rho_{inf} - \rho_s)}{\rho_s} \quad (6359)$$

where ρ_{inf} is the density of the inflow, computed from the supplied inflow properties of temperature and salinity (T_{inf_x}, S_{inf_x}), and ρ_s is the density of the surface layer. If the inflowing water is deemed to be positively buoyant ($\rho_{inf} < \rho_s$), or the model only has one layer ($N_{LEV} = 1$), then the inflow water over the daily time step is added to the surface layer volume

10 ($\Delta V_{N_{LEV}} = Q_{inf_0} \Delta t_d$), and h_s is updated accordingly. Otherwise, this inflow volume is treated as a parcel which travels down through the lake layers, and its properties are subsequently incremented over each ~~daily~~ time step, j , (currently daily) until it inserts. The thickness of an inflow parcel increases over each increment due to entrainment, assuming:

$$\Delta z_{inf_j} = 1.2 E_{inf} \Delta x_{inf_j} + \Delta z_{inf_{j-1}} \quad (6064)$$

where Δz_{inf_j} is the inflow thickness and Δx_{inf_j} is the distance travelled by the inflowing water parcel ~~in the over the~~ j^{th} time step. The distance travelled is estimated based on the change in the vertical elevation-height of the inflow, $\delta z_{inf} \delta z$, and the slope-angle of the inflow river, ϕ_{inf} , as given by:

$$\Delta x_{inf_j} = \frac{\delta z_{inf_{j-1}}}{\sin \Phi_{inf}} \quad (651)$$

~~Where, the vertical excursion for the step is approximated as the difference between its starting height and the bottom of the nearest layer that it sits above, $h_{i_{j-1}}$, such that $\delta z_{inf_j} = (h_s - z_{inf_{j-1}}) - h_{i_{j-1}} (h_s - z_{inf_j}) - h_{i_{j-1}}$, where $z_{inf_{j-1}}$ is the depth of the inflow from the surface at the start of the time step, and and the depth of the inflow from the surface is this is subsequently updated from~~ $z_{inf_j} = z_{inf_{j-1}} + \Delta x_{inf_j} \sin \Phi_{inf}$. The average velocity of the inflow parcel ~~for that increment is~~

20 ~~calculated is updated based on the incoming flow rate~~ from:

$$u_{inf_j} = \frac{Q_{inf_{j-1}} \tan \alpha_{inf}}{(\Delta z_{inf_j})^2 \tan \alpha_{inf}} \quad (662)$$

where the numerator links the relationship between inflow height and channel width in order to define the cross-sectional area of the flow. This velocity is used to estimate the time scale of transport of the parcel ($\delta t_d = \Delta x_{inf_j} / u_{inf_j}$). Following conservation of mass, the flow is estimated to increase according to Fischer et al. (1979) (see also Antenucci et al., 2005):


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$$\Delta Q_{inf_j} = Q_{inf_{j-1}} \left[\left(\frac{\Delta z_{inf_j}}{\Delta z_{inf_{j-1}}} \right)^{5/3} - 1 \right] \quad (673)$$

whereby ΔQ_{inf_j} is removed from the volume of the corresponding layer, i_j , and added to the previous time-step inflow $Q_{inf_{j-1}}$ to capture the entrainment effect on the inflow for the next increment. The properties associated with ΔQ_{inf_j} are assumed to match those of the i_j layer, and mixed into the inflow parcel, to update temperature, salinity and density, ρ_{inf_j} .

5 The inflow travel algorithm (Eqs. ~~62-63~~67) increments through j until the density of the inflow reaches its depth of neutral buoyancy: $\rho_{inf_j} \leq \rho_{i_j}$. Once this condition is met, the second part of the algorithm creates a new layer of thickness dependent on the inflow volume at that time (including the successive additions from entrainment; Eq. ~~67~~69).

10 ~~Note that~~Since a new inflow parcel is created each day, and the user may configure multiple inflows, N_{INF} , ~~creating~~a complex set of parcels being tracked via Eqs. ~~5660-6367~~, and a queue of new layers to be inserted, is created. Following creation of a new layer for ~~the an~~ inflow parcel, N_{LEV} is incremented and all layer heights above the new layer are updated. The new inflow layer is then subject to the thickness limits criteria within the layer limit checking routine and may amalgamate with adjacent layers or be ~~for combining or splitting layers~~ divided into thinner layers.

15

Aside from importing mass into the lake, river inflows also contribute turbulent kinetic energy ~~to that may dissipate in~~ the hypolimnion, as discussed in Sect 2.6.2 (e.g., see Eq. ~~4955~~), and they contribute to the scalar transport in the water column by adding mass contained within the inflow parcels, and contributing to mixing of properties via entrainment as described above (Figure ~~12~~4a); see also Fenocchi et al. (2017).

20

2.7.2 Submerged inflows

Submerged inflows are inserted at the user-specified depth h_{inf_a} with zero entrainment by utilising the second part of the algorithm described in Section 2.7.1. Once ~~t~~he submerged inflow volume is added as a new layer which it may then be mixed with adjacent layers (above or below) depending on the density difference and layer thickness criteria (Figure ~~12~~4b).

25 This option can be used across one or more inflow elevations to account for groundwater input to a lake, or for capturing a piped inflow, for example.

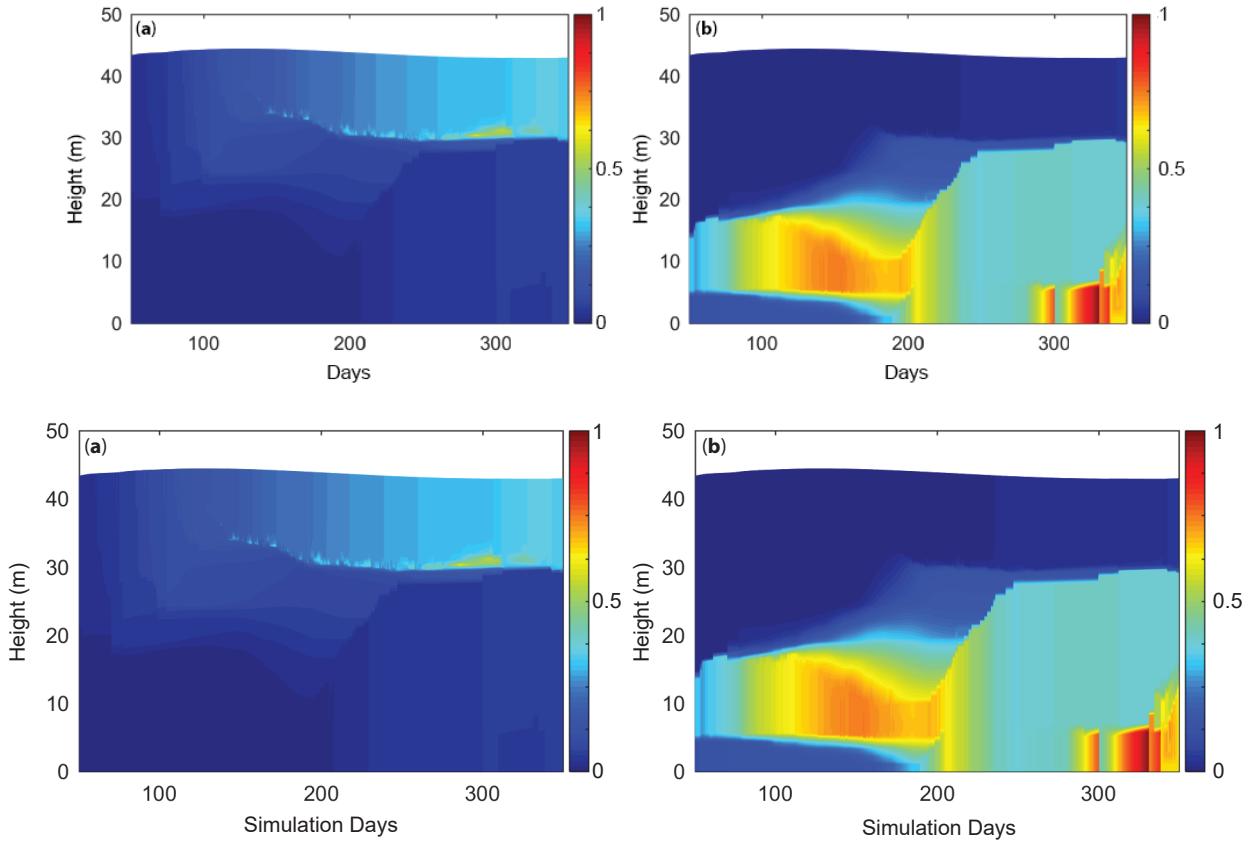


Figure 412: Example simulations demonstrating inflow insertion example for the case where a) the inflow was set as a surface river inflow and subject to the insertion algorithm (Eqs. 6056-6367) prior to insertion, and b) the inflow was set as a submerged inflow at a specified height ($h_{inf} = 5$ m). Once entering the water column, the tracer, C , is subject to mixing during inflow entrainment in case (a), and by surface and/or deep mixing once inserted, for both cases (a) and (b). The colour scale represents an arbitrary inflow concentration which entered with a value of 1.

2.7.3 Withdrawals

10 Outflows from a specific depth can include outlets from a dam wall offtake or other piped withdrawal, or removal of water that may be lost due to groundwater recharge ~~or seepage to an outflow~~. For a stratified water column, the water will be removed from the layer corresponding to the specified withdrawal height, h_{outf} , as well as layers above or below, depending on the strength of discharge and stability of the water column. Accordingly, the model assumes an algorithm where the thickness of the withdrawal layer is dependent on the internal Froude (Fr) and Grashof (Gr) numbers, and the parameter, R
 15 (see Fischer et al., 1979; Imberger and Patterson, 1981):

$$Fr = \frac{f_{outf} Q_{outfx} / c_{secd}ay}{N_{outf} W_{outf} L_{outf}^2} \quad (684)$$

$$Gr = \frac{N_{outf}^2 A_{outf}^2}{D_{outf}^2} \quad (695)$$



$$R = FrGr^{1/3} \quad (7066)$$

where W_{outf} , L_{outf} and A_{outf} are the width, length and area of the lake at the outlet elevation, and D_{outf}^2 is the vertical diffusivity averaged over the layers corresponding to the withdrawal thickness, δ_{outf} (described below). To calculate the width and length of the lake at the height of the outflow, it is assumed, firstly, that the lake shape can be approximated as an ellipse, and secondly, that the ratio of length to width at the height of the outflow is the same as that at the lake crest. The length of the lake at the outflow height, L_{outf} and the lake width, W_{outf} are given by:

$$L_{outf} = \sqrt{A_{outf} \frac{4 L_{crest}}{\pi W_{crest}}} \quad (6771)$$

$$W_{outf} = L_{outf} \frac{W_{crest}}{L_{crest}} \quad (6872)$$

where A_{outf} is the area of the lake at the outflow height, L_{crest} is the length and W_{crest} the width of the lake at the crest height.

The thickness of the withdrawal layer is calculated depending on the value of R (Fischer et al., 1978, 1979), such that:

$$\delta_{outf} = \begin{cases} 2L_{outf} Gr^{-1/6} & R \leq 1 \\ 2L_{outf} Fr^{1/2} & R > 1 \end{cases} \quad (7369)$$

If stratification is apparent near h_{outf} , either above or below this elevation, then the thickness computed in Eq. 69-73 may not be symmetric about the offtake level (Imberger and Patterson, 1981); therefore the algorithm separately computes the thickness of the withdrawal layer above and below, denoted $\delta_{outf_{top}}$ and $\delta_{outf_{bot}}$, respectively. The Brunt-Väisälä frequency is averaged over the relevant thickness, N_{outf}^2 , and calculated as:

$$N_{outf}^2 = \frac{g}{\delta_{outf}} \frac{\rho_{outf} - \rho_i}{\rho_{outf}} \quad (740)$$

where ρ_{outf} is the density of the layer corresponding to the height of the withdrawal, i_{outf} , and ρ_i is the density of the water column at the edge of the withdrawal layer, as determined below. The proportion-flow of water withdrawn-taken from each layer influenced by the withdrawal, Q_{outf_i} , either above or below the layer of the outlet elevation, requires identification of the upper and lower-most layer indices influenced by the outflow, denoted i_{top} and i_{bot} . Once the layer range is defined, Q_{outf_i} is computed for the layers between i_{outf} and i_{top} , and i_{outf} and i_{bot} , by partitioning the total outflow using a function to calculate the proportion of water withdrawn from any layer that fits the region of water drawn in a given time ($Q_{outf_i} = f[f_{outf} Q_{outf_x} / c_{secday}, h_i, h_{i-1}, h_{outf}, \delta_{outf_{bot}}, \delta_{outf_{top}}]$; see Imberger and Patterson, 1981, Eq. 65). Given that users configure any height for a withdrawal outlet and flow rates of variable strength, the upper ($h_{outf} + \delta_{outf_{top}}$) and lower ($h_{outf} - \delta_{outf_{bot}}$) elevation limits computed by the algorithm are limited to the lake surface layer or bottom layer. Once computed, the volumes are removed from the identified layer set, and their height and volumes updated accordingly. Q_{outf_i} is constrained within the model to ensure no more than 90% of a layer can be removed in a single time step. Depending on the fractional contribution from each of the layers the water is withdrawn from, the water taken will have the associated



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weighted average of the relevant scalar concentrations (T_{outf} , S_{outf} , C_{outf} ~~heat, salinity and water quality~~) which are reported in the outlet file for the particular withdrawal. This routine is repeated for each withdrawal considered, denoted O , and the model optionally produces a summary file of ~~all~~ the combined outflow water and its properties.

2.7.4 Adaptive offtake dynamics

- 5 For reservoir applications, a special outflow option has been implemented that extends the dynamics in Section 2.7.3 to simulate an adaptive offtake or selective withdrawal. This approach is used for accommodating flexible reservoir withdrawal regimes and their effects on the thermal structure within a reservoir. For this option, a target temperature is specified by the user and GLM identifies the corresponding withdrawal height within a predefined (facility) range to meet this target temperature during the runtime of the simulation, i.e., the withdrawal height adaptively follows the thermal stratification in
- 10 the reservoir. The target temperature can be defined as a constant temperature (e.g., 14°C) or a time series (via a *.csv file), such as a measured water temperature from an upstream river that could be used to plan environmental releases from the reservoir to the downstream river. The selected height of the adaptive offtake is printed out in a *.txt file for assisting reservoir operation. In addition to the basic adaptive offtake function, GLM can also simulate withdrawal mixing, i.e., water
- 15 discharges at both locations need to be predefined by the user (via the standard outflow *.csv files) and GLM chooses the adaptive withdrawal from a height, where the water temperature is such that the resulting mixing temperature meets the target temperature. This withdrawal mixing is a common strategy in reservoir operation where deep water withdrawal and temperature control are required simultaneously to prevent deleterious downstream impacts.
- 20 An example of the adaptive offtake function with and without withdrawal mixing, assuming a constant water temperature of 14°C for the outflow water, shows that GLM is able to deliver a constant outflow temperature of 14°C during the stratified period (Figure 132). In winter, when the water column is cooler than 14°C , the model withdraws surface water. The adaptive offtake functionality can be used in a stand-alone mode or also linked to the dissolved oxygen concentration (when operated with the coupled water quality model AED2, see Section 4). In the latter case, the effect of the withdrawal regime
- 25 on the oxygen dynamics in the hypolimnion can be simulated (see Weber et al., 2017). In this setting, the simulated hypolimnetic dissolved oxygen concentration at a specified height is checked against a user-defined critical threshold. If the hypolimnetic oxygen falls below the critical threshold, the height of the adaptive offtake will be automatically switched to a defined height (usually deep outlets in order to remove the oxygen-depleted water) to withdraw water from this layer, until the oxygen concentrations have recovered.

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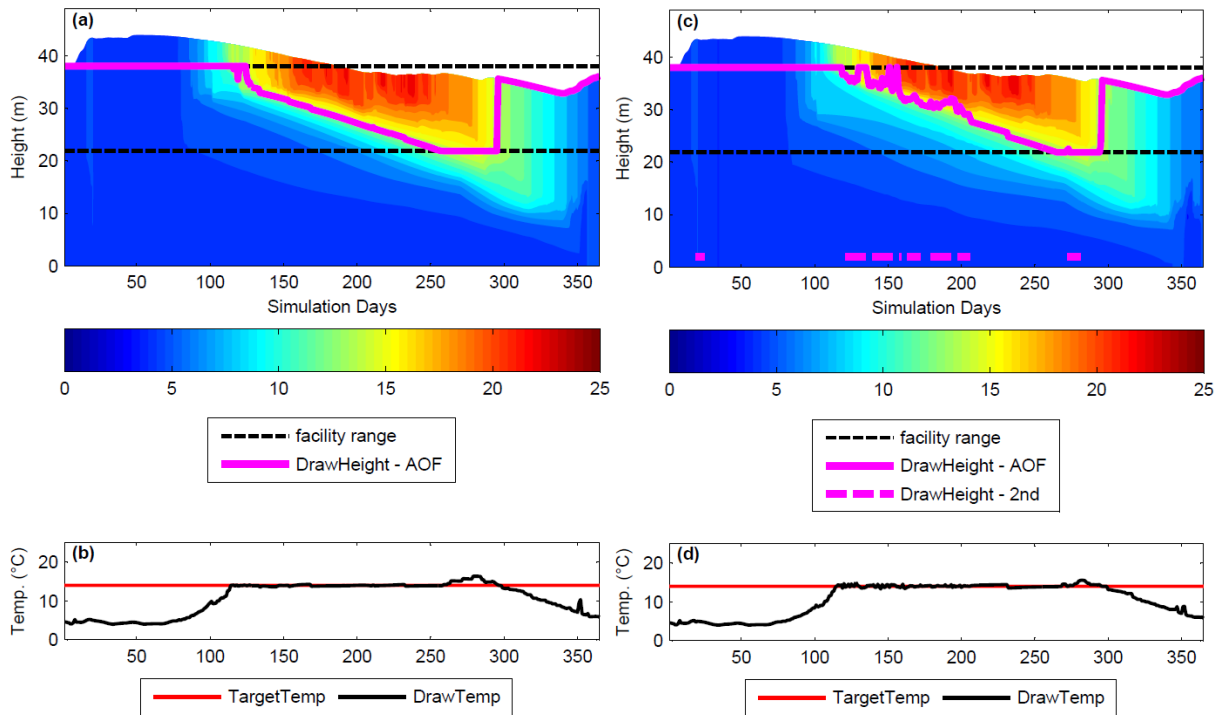


Figure 1213: Adaptive offtake reservoir simulation; water temperatures of the adaptive offtake model assuming a constant target temperature of 14 °C (a,b) without and (c,d) with mixing with the bottom outlet withdrawal. The black dashed line (a,c) represents the height range of the variable withdrawal facility (AOF) and the magenta lines the adaptive offtake and second withdrawal height (here: bottom outlet). In the scenario with the activated second withdrawal (c), the bottom outlet was only periodically opened during flooding conditions. Panels (b) and (d) indicate where the actual withdrawal temp (DrawTemp, T_{outf}) was able to meet the target (TargetTemp).

10 2.7.5 Seepage

Seepage of water from the lake can also be configured within the model, for example, as might be required in a wetland simulation or for small reservoirs perched above the water table that experience leakage to the soil below. The seepage rate, $Q_{seepage}$, can be assumed constant or dependent on the overlying lake head:

$$Q_{seepage} = \begin{cases} -GA_s/c_{secd\text{ay}}, & \text{Option 1: constant rate} \\ -\left(\frac{K_{seep}}{\Delta z_{soil}}\right) \frac{A_s h_s}{c_{secd\text{ay}}} \left(\frac{K_{seep}}{\Delta z_{soil}}\right) \frac{A_s h_s}{(c_{secd\text{ay}})}, & \text{Option 2: Darcy flux based on water height} \end{cases} \quad (75+)$$

where G is the seepage rate (m day^{-1}), and K_{seep} is the soil hydraulic conductivity (m day^{-1}) and Δz_{soil} is an assumed soil thickness over which the seepage is assumed to occur. The water leaving the lake is treated as a "vertical withdrawal" whereby the water exits via the bottom-most layer(s), and the amount $\Delta V_G = Q_{seepage} \Delta t_d$, is generally all taken from the bottom-most layer ($i = 1$), however, it is constrained within the model to ensure no more than 90% of the layer can be reduced in any one time step; where $\Delta V_G > 0.9V_{i=1}$ then the routine sequentially loops up through the above layers until



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enough lake volume has been identified to cover the seepage demand. Once the individual layer volumes are incremented due to the seepage flux, ΔV_{G_i} , the heights of all layers ($h_1: h_s$) are re-computed based on the hypsographic curve using $h_i = f[V_i]$. Where seepage reduces the lake below 0.05 m, the lake becomes dry and will continue to have zero volume until new inputs from rain or inflows (e.g., Figure 98a).

5 2.7.6 Overflows

Once the lake volume exceeds the maximum volume, the excess water is assumed to leave the domain as an overflow. The flow rate, Q_{ovfl} , is computed based on the interim volume, V_S^* , prior to the end of the daily time-step, where $V_S^* = V_S^t + \Delta h_s A_s + \Delta t \left(\sum_I^{N_{INF}} Q_{info_I} - \sum_O^{N_{OUT}} Q_{outfo_O} - Q_{seepage} \right)$, and Δh_s is the cumulative change in the daily water level over the day. Users can optionally also specify a crest elevation which ~~sits~~ lies below the elevation of maximum lake volume, and support a rating curve linking the height of water above the crest level with the overflow volume:

$$Q_{weir} = \begin{cases} 0, & V_S^* \leq V_{crest} \\ \frac{2}{3} C_{D_{weir}} \sqrt{2g} b (h_s^* - h_{crest})^{3/2}, & V_S^* > V_{crest} \end{cases} \quad (762)$$

where h_s^* is the interim update to the water surface height prior to the overflow computation, $C_{D_{weir}}$ is a coefficient related to the drag of the weir, b is the width of the crest and h_{crest} is the height of the crest level. The overflow rate is then computed as the sum of the flow over the weir crest and the volume of water exceeding the volume of the domain:

$$Q_{ovfl} = \begin{cases} Q_{weir}, & V_S^* \leq V_{max} \\ Q_{weir} + (V_S^* - V_{max})/\Delta t_d, & V_S^* > V_{max} \end{cases} \quad (773)$$

15 If no crest is configured below the maximum lake height, then Eq. 77 assumes $Q_{weir} = 0$.

2.8 Wave height and bottom stress

Resuspension of sediment from the bed of lakes depends on the stresses created by water movement across the lake bottom. Wind induced resuspension ~~of sediment from the bed of shallow lakes in particular~~ is sporadic and occurs as the waves at the water surface create oscillatory currents that propagate down to the lake-bed and exceed a critical threshold. The wave climate that exists on a lake can be complex and depend on the fetch over which the wind has blown, the time period over which the wind has blown, and complicating factors such as wind-sheltering and variations in bottom topography. The horizontally averaged nature of GLM means that only a single set of wave characteristics across the entire lake surface can be computed for a given time-step and these are assumed to be at steady-state. Note that GLM does not predict resuspension and sediment concentration directly, but computes the bottom shear stress for later use by coupled sediment and water quality modules. Since each layer has a component that is considered to overlay sediment (Section 4), the stress experienced at the sediment-water interface is able to approximated as a function of depth in relation to the surface wave climate. ~~Nonetheless, even without this explicit formulation, t~~ The model can therefore identify the depth-range and areal extent and where there is potential for bed-sediment resuspension to occur, i.e., by computing the area of the lake over which the bed shear stress exceeds some critical value required for resuspension to occur.

30

To compute the stress at the lake bottom the model estimates the surface wave conditions using a simple, fetch-based, steady state wave model (Laenen and LeTourneau, 1996; Ji 2008). The average wave geometry (wave period, significant wave height and wave length), is predicted based on the wind speed and fetch over which the waves develop (Figure 143), whereby the fetch is approximated from the lake area:

$$F = 2\sqrt{A_s/\pi} \quad (784)$$

5

and the wave period, δt_{wave} , is calculated from fetch as based on:

$$\delta t_{wave} = 7.54 \left(\frac{U_{10}}{g} \right) \tanh[\xi] \left(\frac{gF}{U_{10}^2} \right)^{0.333} \tanh \left[\frac{0.0379 \left(\frac{gF}{U_{10}^2} \right)^{0.333}}{\tanh[\xi]} \right] \left(\frac{0.0379 \left[\frac{gF}{U_{10}^2} \right]^{0.333}}{\tanh(\xi)} \right) \quad (795)$$

where:

$$\xi = 0.833 \left(\frac{gz_{avg}}{U_{10}^2} \right) \left[\frac{gz_{avg}}{U_{10}^2} \right]^{0.375} \quad (8076)$$

and z_{avg} is the average lake depth. The typical wave length is then estimated from:

$$\delta x_{wave} = \frac{g(\delta t_{wave})^2}{2\pi} \left[\frac{g(\delta t_{wave})^2}{2\pi} \right] \tanh \left[\frac{2\pi z_{avg}}{g(\delta t_{wave})^2} \right] \left(\frac{2\pi z_{avg}}{\left[\frac{g(\delta t_{wave})^2}{2\pi} \right]} \right) \quad (7781)$$

and the significant wave height from:

$$\delta z_{wave} = 0.283 \left(\frac{U_{10}^2}{g} \right) \tanh[\zeta] \left(\frac{gF}{U_{10}^2} \right)^{0.5} \tanh \left[\frac{0.00565 \left(\frac{gF}{U_{10}^2} \right)^{0.5}}{\tanh[\zeta]} \right] \left(\frac{0.00565 \left[\frac{gF}{U_{10}^2} \right]^{0.5}}{\tanh(\zeta)} \right) \quad (7882)$$

10 where

$$\zeta = 0.53 \left(\frac{gz_{avg}}{U_{10}^2} \right) \left[\frac{gz_{avg}}{U_{10}^2} \right]^{0.75} \quad (7983)$$

Based on these properties the orbital wave velocity at the surface can be translated at down the depth of the water column, such that (in the i^{th} layer) it is calculated as:

$$U_{orb_i} = \frac{\pi \delta z_{wave}}{\delta t_{wave} \sinh \left[\frac{2\pi z_{i-1}}{\delta x_{wave}} \right]} \quad (840)$$

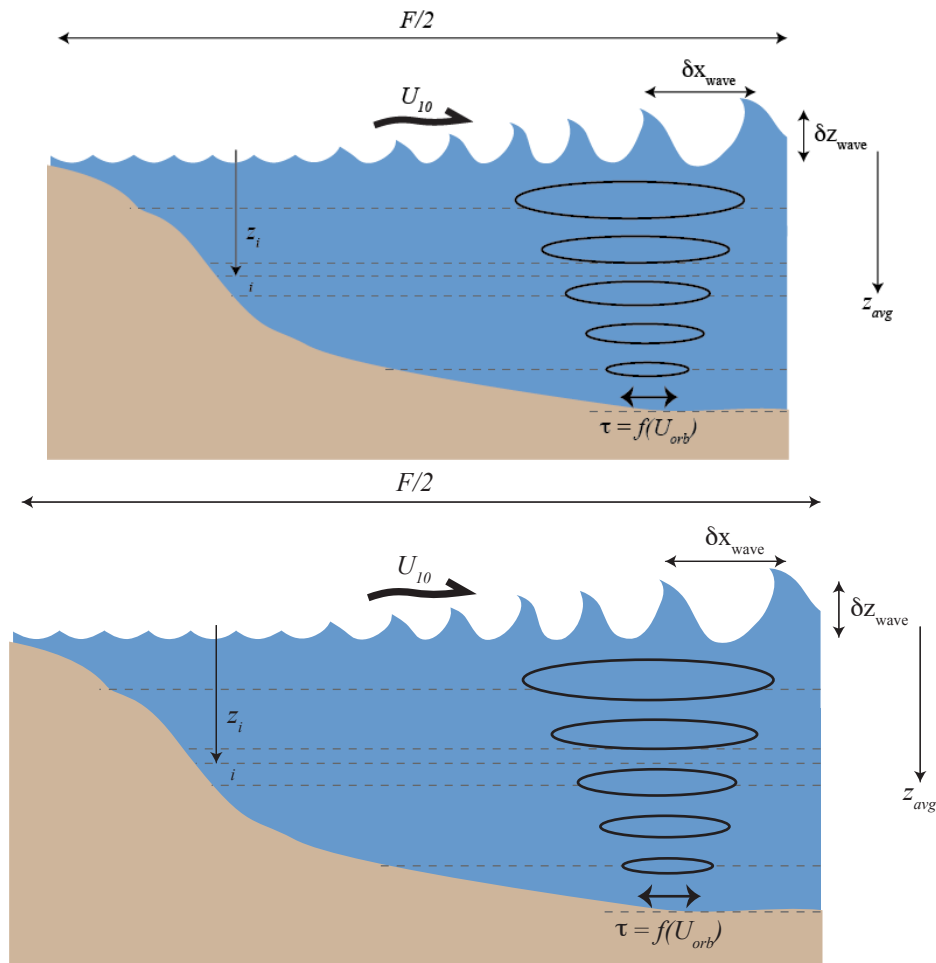


Figure 1314: Schematic of the wave estimation approach depicting the lake fetch, surface wind speed, wave height, wavelength and bottom stress created by the orbital velocity.

5

For each layer, the total shear stress experienced at the lake bed portion of that layer (equivalent in area to $A_i - A_{i-1}$) is calculated from:

$$\tau_i = \frac{1}{2} \rho_i (f_w U_{orb_i}^2 + f_c U_{m_i}^2) [f_w U_{orb_i}^2 + f_e U_{m_i}^2] \quad (851)$$

10 where U_m is the mean layer velocity, which for simplicity is assumed based on the velocity estimate made during the mixing calculations (Eq. 440) in the surface mixed layer, such that:

$$U_{m_i} = \begin{cases} u_*, & i \geq k \\ 0, & i < k \end{cases} \quad (862)$$



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The friction factors depend upon the characteristic particle diameter of the lake bottom sediments, δ_{ss} and the fluid velocity.

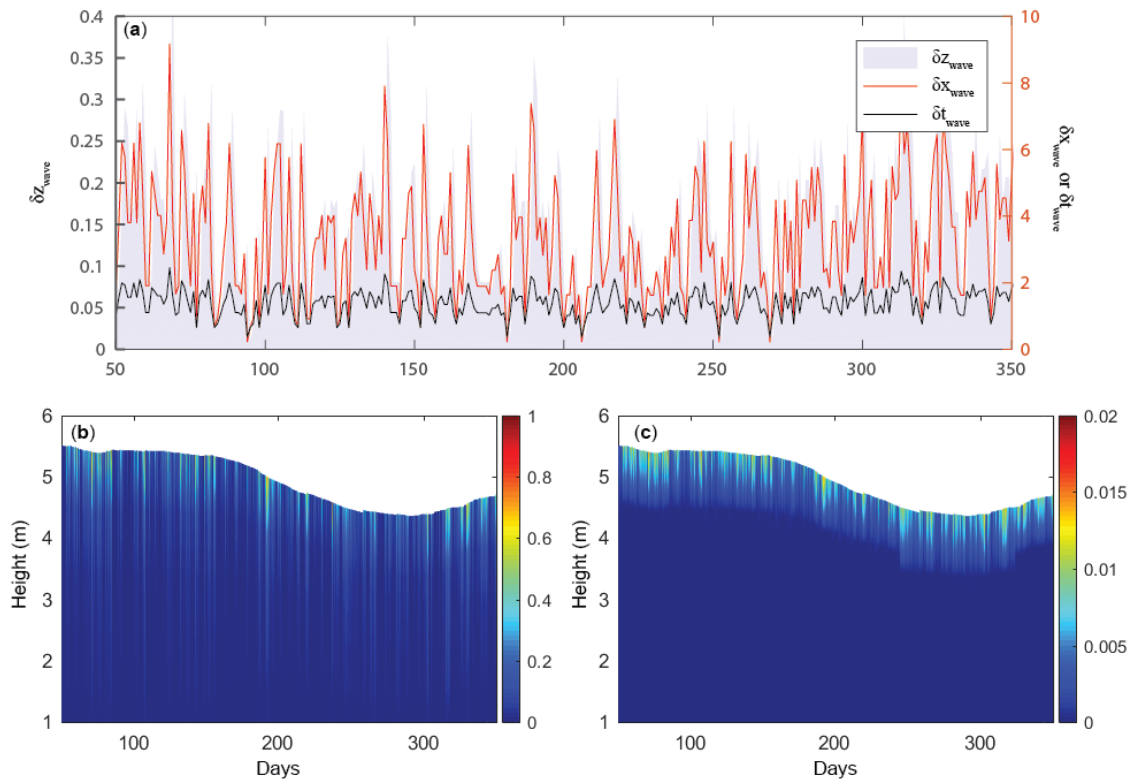
For the current induced stress, we compute $f_c = 0.24/\log \left[12z_{avg}/2.5\delta_{ssz_i} \right] \left(\frac{12z_{avg}/2.5\delta_{ssz_i}}{12z_{avg}/2.5\delta_{ssz_i}} \right)$, and for waves (Kleinans and Grasmeyer, 2006):

$$f_w = \exp \left[-5.977 + 5.213 \left(\frac{U_{orb_i} \delta t_{wave}}{5\pi \delta_{ssz_i}} \right)^{-0.194} \right] \quad (873)$$

where δ_{ssz_i} is specific for each layer i , depending on which sediment zone it overlays (see Section 4). The current and wave

5 induced stresses at the lake bottom manifest differently within the lake, as demonstrated in Figure 154 for a shallow lake.

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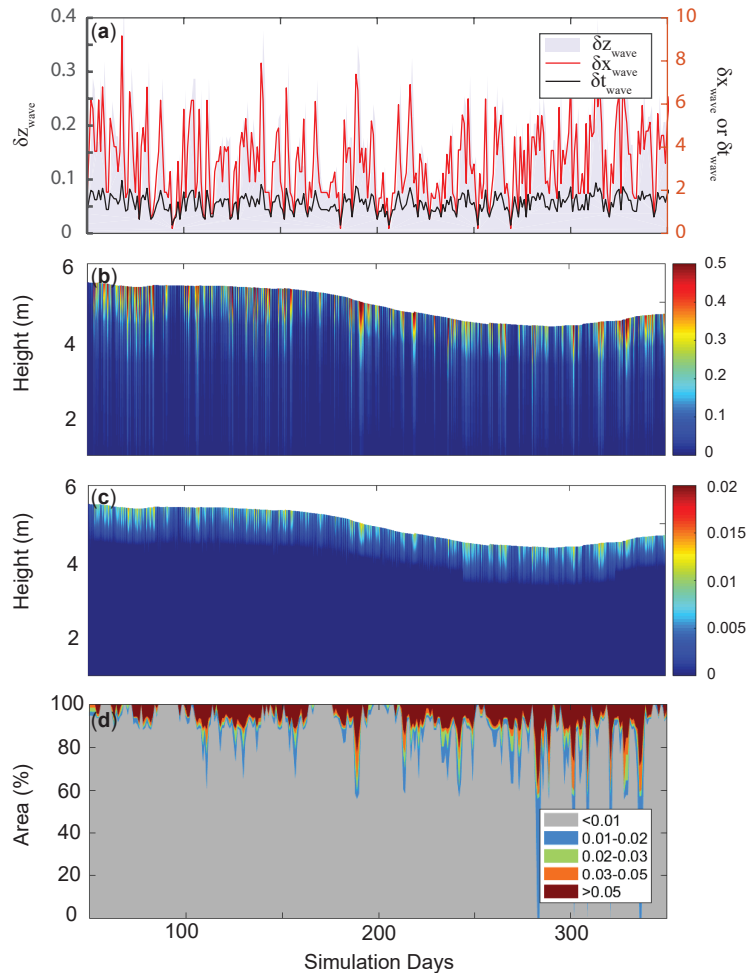


Figure 1415: Simulation from Woods Lake, Australia, showing a) time series of surface wave properties ($H_s = \delta z_{wave}$, $L = \delta x_{wave}$ and $T = \delta t_{wave}$), b) orbital velocity, U_{orb} (m s^{-1}), and c) comparison with the layer mean velocities, U_m (m s^{-1}), and d) lake-bed area fraction within each of five depicted shear stress categories (based on τ_i , N m^{-2}).

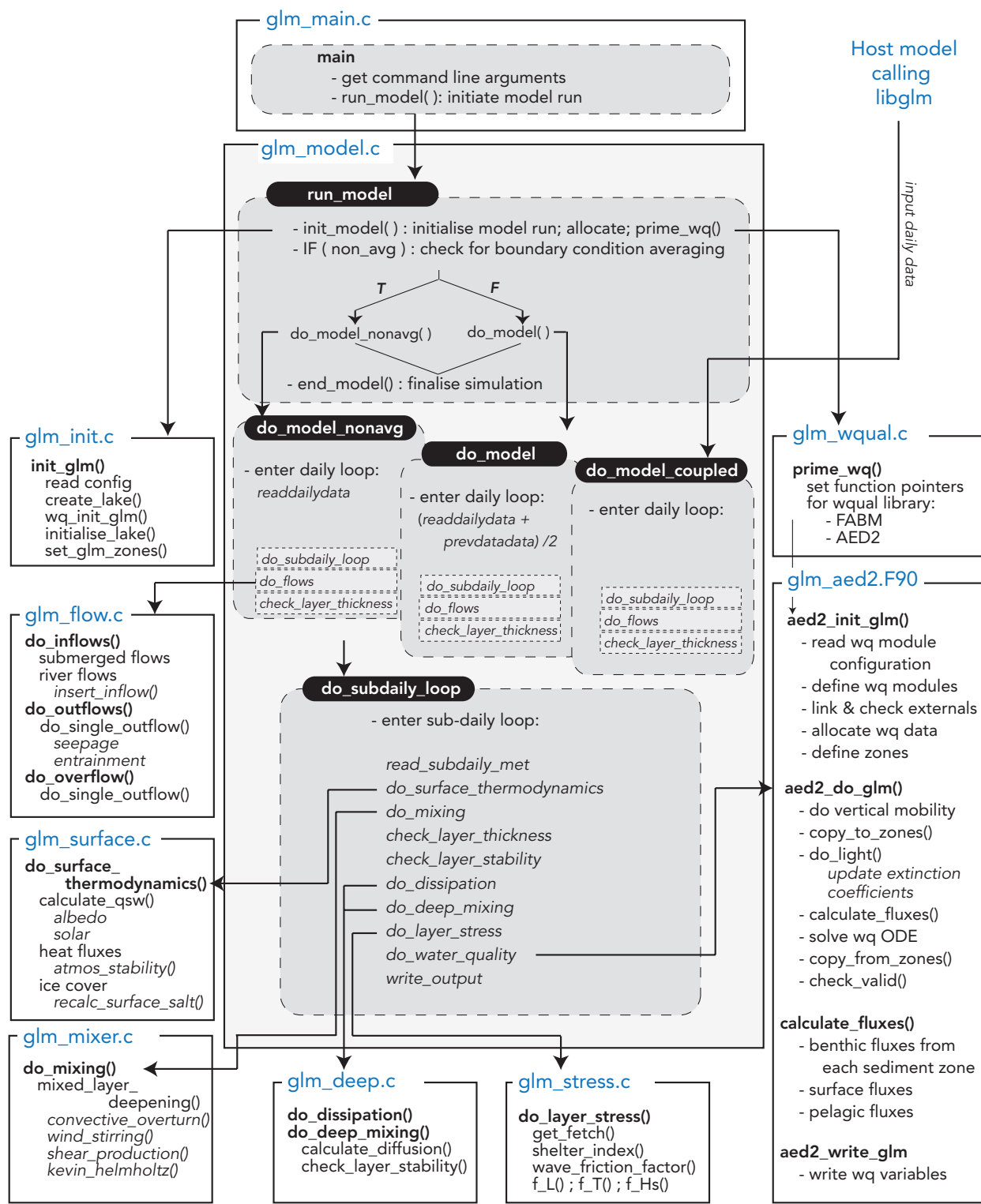
5

3 Code organization and model operation

Aside from the core water balance and mixing functionality, the model features numerous options and extensions in order to make it a fast and easy-to-use package suitable for a wide range of contemporary applications. Accommodating these requirements has led to the modular code structure outlined in Figure 165. The model is written in C, with a Fortran-based interface module to link with Fortran-based water quality modelling libraries described in Section 4. The model compiles with gcc, and gfortran, and commercial compilers, with support for Windows, OS X and Linux.

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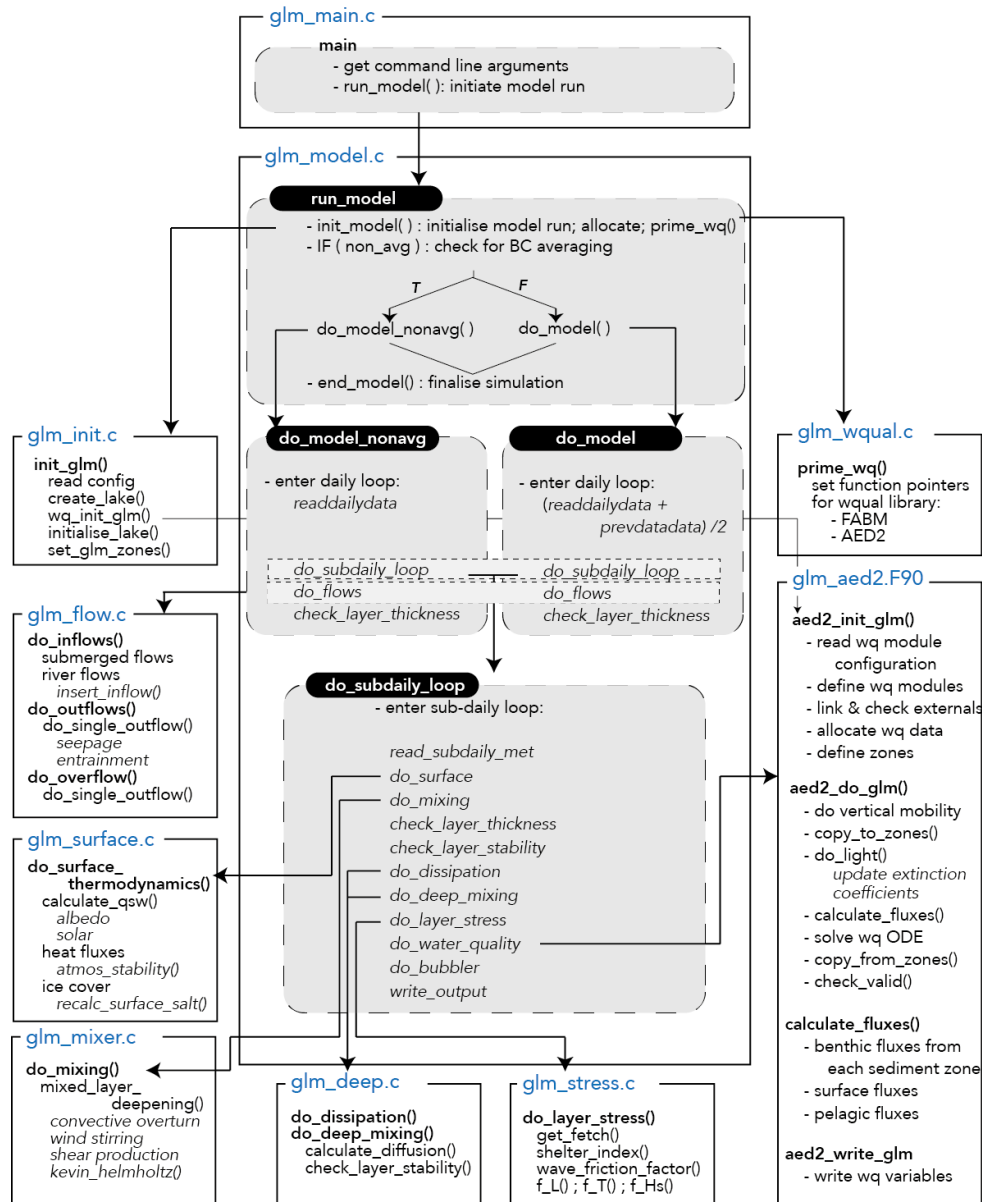


Figure 1516: Overview of GLM code structure and logic-program flow. Each module is depicted as a box with the main routines and functions summarised. Three entry points to the main model routines are possible depending on the desired treatment of the inflow and outflow boundary condition data: do model uses the flow boundary condition data over the present and previous day in order to get the midday value, do model nonavg uses that from the present day only, and do model coupled passes in the present day flows from the host.

The model may also be compiled as a library, termed libGLM, that can be called as a plugin into other models (e.g., see Section 5.4). Whilst the model is not object-oriented, users may easily customise specific modules described in Section 2 by adding or extending options for alternate schemes or functions.

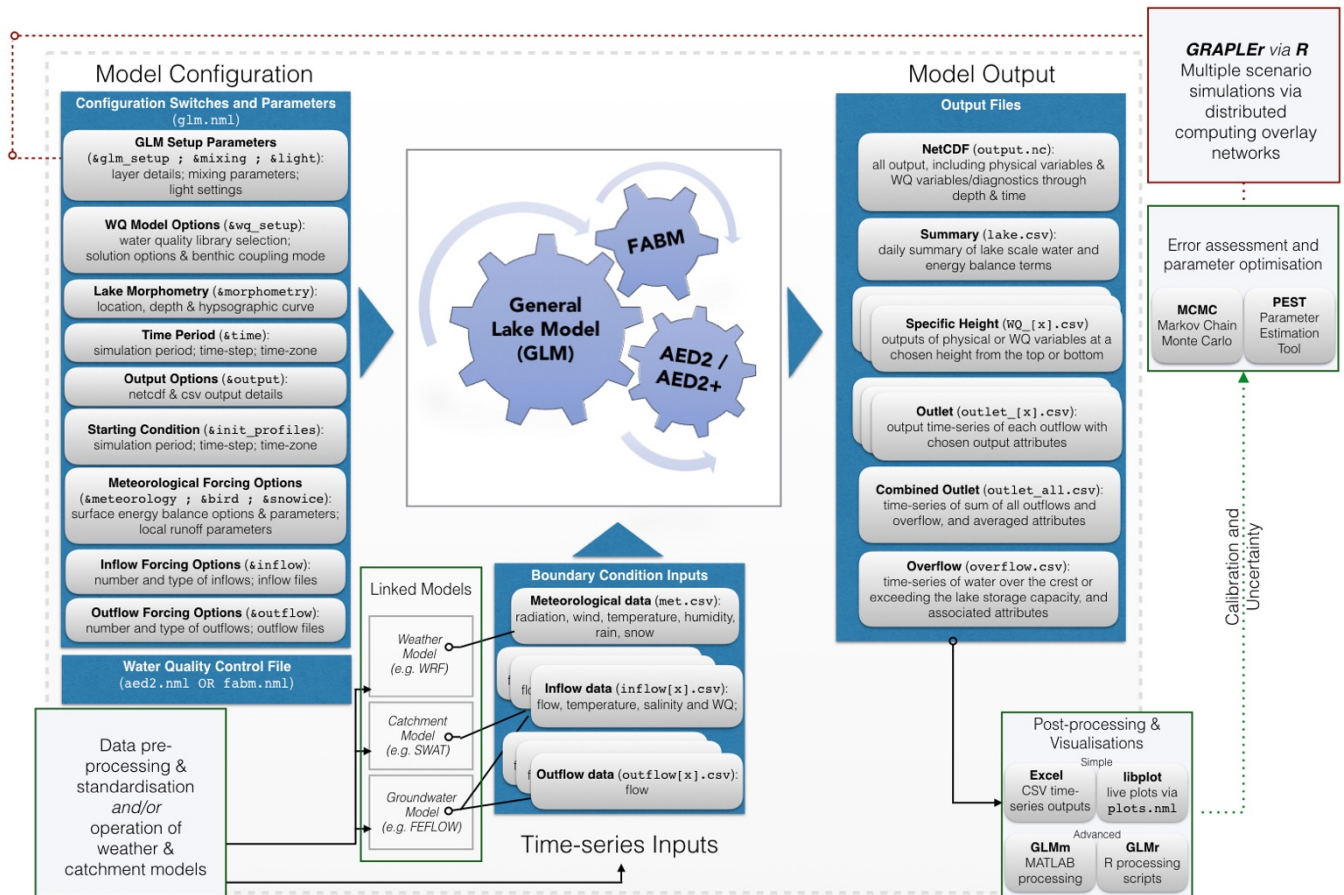
To facilitate the use of the model in teaching environments and for users with limited technical support, it may be operated without any third-party software, as the input files consist of “namelist” (nm1) text files for configuration and csv

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files for meteorological and flow time series data (Figure 176). The outputs from predictions are stored into a structured netCDF file, which can be visualised in real-time through the simple inbuilt plotting library (libplot) or may be opened for post-processing in MATLAB, R, or any other tool supporting the open netCDF format (see Section 5.1). Parameters and configuration details are input through the main `glm.nml` text file (Figure 176) and default parameters and their associated descriptions are outlined in Table 1.



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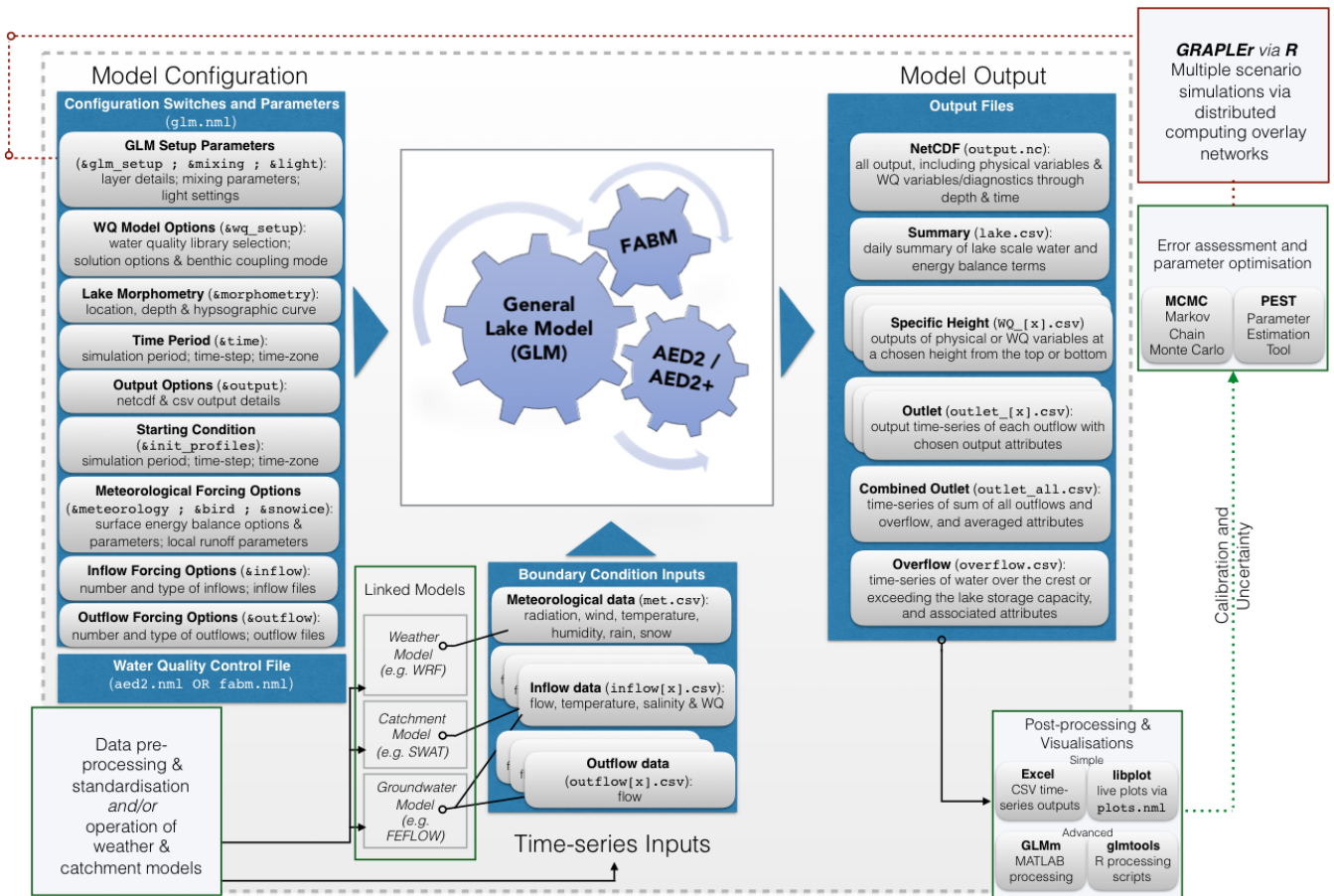


Figure 4617: Flow diagram showing the input information required for operation of the model, the outputs, and analysis pathways.

5 4 Dynamic coupling with biogeochemical and ecological model libraries

Beyond modelling the vertical temperature distribution, the water, ice and heat balance, as well as the transport and mixing in a lake, the model has been designed to couple with biogeochemical and ecological model libraries. Currently the model is distributed pre-linked with the AED2 simulation library (Hipsey et al., 2013) and the Framework for Aquatic Biogeochemical Models (FABM; Bruggeman and Bolding, 2014). Through connection with these libraries, GLM [creates a set \$C\$ of](#) ~~can simulate the seasonal changes in vertical profiles of~~ [scalar variables, where by \$C \in \mathbb{C}\$, which resolve the vertical profiles and mass balance of](#) turbidity, oxygen, nutrients, phytoplankton, zooplankton, pathogens and other water quality variables of interest. Documentation of these models is beyond the scope of the present paper, however, two features [associated with the coupling](#) are highlighted here as ~~being~~ relevant to managing physical-ecological interactions.

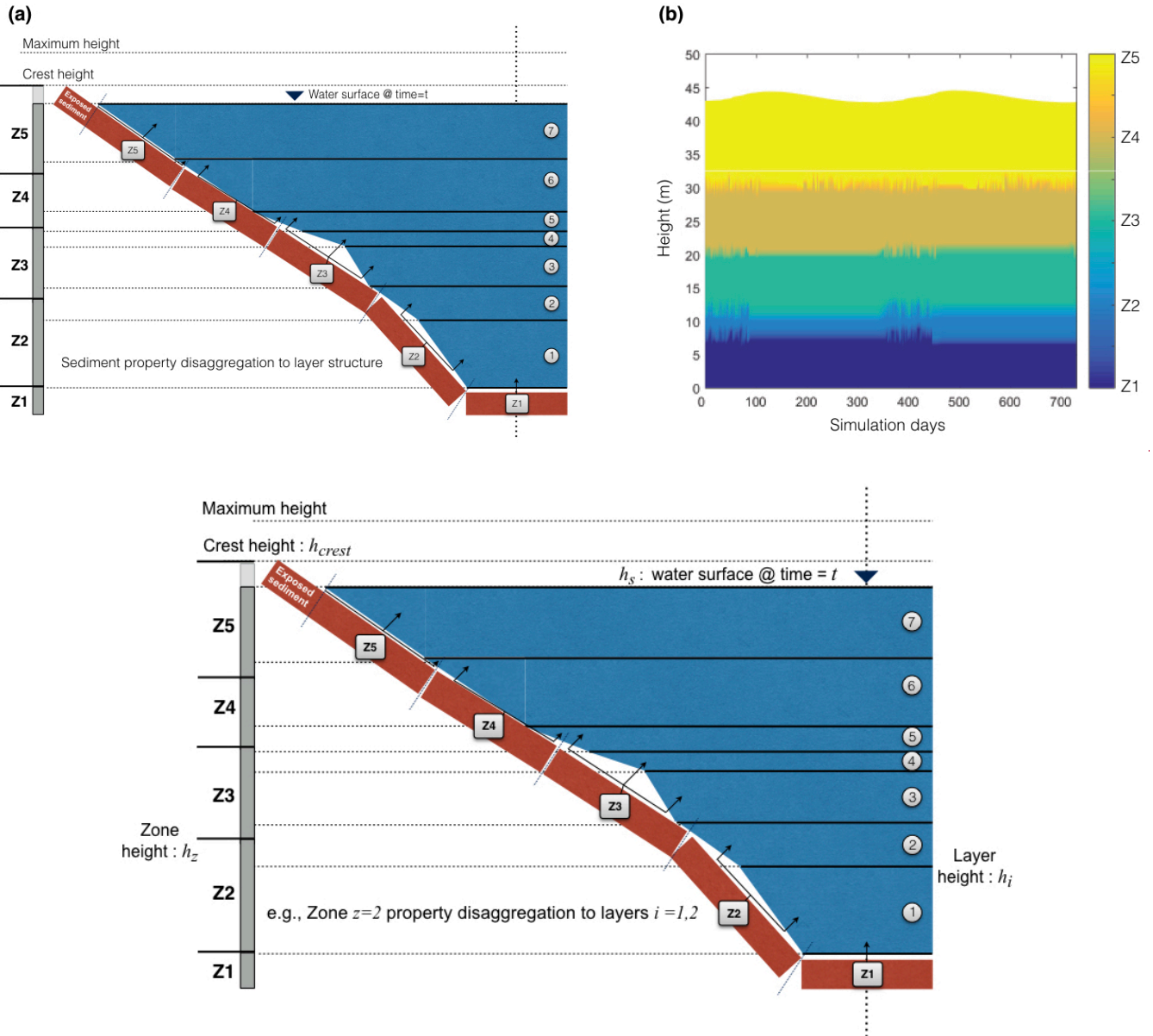
15 Firstly, the model is designed to allow a user defined number of sediment zones that span the depth of the lake. Using this approach, the current setup allows for depth-dependent sediment properties, both for physical properties such as roughness



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5 or sediment heat flux (as outlined in previous sections), and also biogeochemical properties such as sediment nutrient fluxes and benthic ecological interactions. Since the GLM layer structure is flexible over time (i.e., layer ~~depths~~ heights are not fixed), any interactions between the water and sediment/benthos must be managed at each time step. The model ~~therefore~~ supports disaggregation and/or aggregation of layer properties, for mapping individual water layers to one or more sediment zones (Figure 1~~87~~). The weightings provided by each layer to the sediment are based on the relative depth overlap of a layer with the depth range of the sediment zone, with the heights of zone boundaries denoted h_z . This approach makes the model suitable for long-term assessments of wetland, lake and reservoir biogeochemical budgets, as is required ~~including~~ for C, N and other attribute balances ~~as required~~ (Stepanenko et al., 2016).

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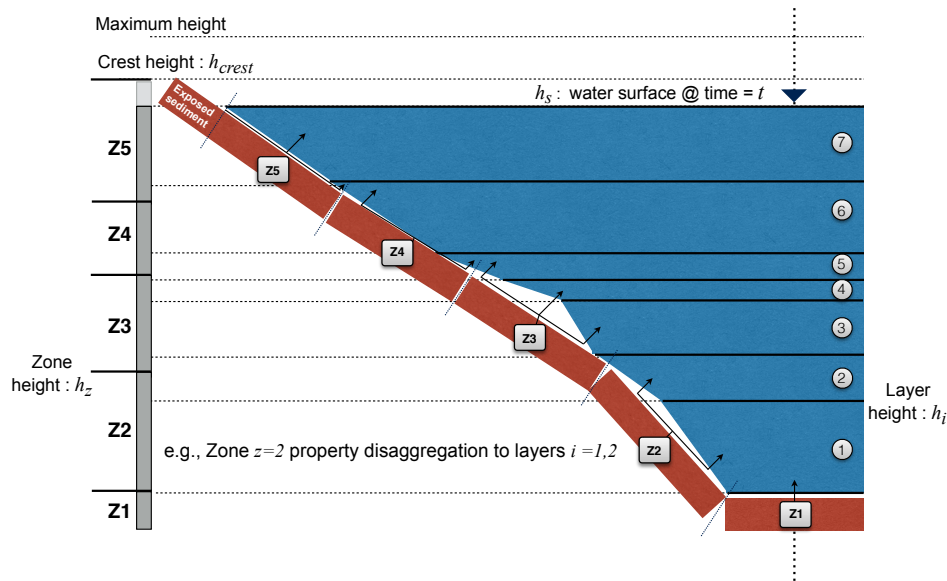


Figure 1718: a) Schematic of a lake model layer structure (indicated by layers $i=1-7$), in conjunction with five sediment “zones” (Z1-Z5) activated when `benthic_mode = 2`. The dynamically varying layer structure is re-mapped to the fixed sediment zone locations at each time step in order for the sediment zone to receive the average overlying water properties, and for the water to receive the appropriate information from benthic/sediment variables. b) example of GLM output showing the sediment zone each water layer is mapped to.

Secondly, the water quality modules feed-back to GLM properties related to the water and/or heat balance. Feedback options are included for external libraries to provide water density additions, and to modify bottom friction, f_w , the light attenuation coefficient, K_w , solar shading f_{SWR} , and rainfall interception, f_R .

5 Workflow tools for integrating GLM with sensor data and supporting models

The GLM model has been designed to support integration of large volumes of data coming from instrumented lakes, including many GLEON sites. These data consist of high-frequency and discrete time series observations of hydrologic fluxes, meteorology, temperature, and water quality (e.g., Hamilton et al., 2015). To facilitate research that requires running the model using these data sources, we have created GLM interfaces in the R and MATLAB analysis environments. These tools support user-friendly access to the model and include routines that streamline the process of calibrating models or running various scenarios. In addition, for assessment of lake dynamics in response to catchment or climatic forcing, it is desirable to be able to connect GLM with other model platforms associated with surface and groundwater simulation, and weather prediction (Read et al., 2016).

20 5.1 R and MATLAB libraries for model setup and post-processing

The R and MATLAB scientific languages are commonly used in aquatic research, often as part of automated modelling and analysis workflows. GLM has a client library for both, and these tools are shared freely online. The R package is called “`glmtools`” (<https://github.com/USGS-R/glmtools>) and the MATLAB library is called “GLMm”



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(<https://github.com/AquaticEcoDynamics/GLMm>). Both tools have utilities for model output pre- and post-processing. The pre-processing components can be used to format and modify data inputs and configuration files, and define options for how GLM executes. Post-processing tools include visualizations of simulation results (as shown in the results figures above), comparisons to field observations, and various evaluations of model performance.

5 5.2 Utilities for assessing model performance, parameter identification and uncertainty analysis

In order to compare the performance of the model for various types of lakes, numerous metrics of model performance are relevant. These include simple measures like surface or bottom temperature, or ice thickness. It is also possible to assess the model's performance in capturing higher-order metrics relevant to lake dynamics, including Schmidt Stability, thermocline depth, ice on/off dates (see also Bruce et al., 2018, for a detailed assessment of the model's accuracy across a wide diversity of lakes across the globe). With particular interest in the model's ability to interface with high frequency sensor data for calculation of key lake stability metrics (Read et al., 2011), continuous wavelet transform comparisons are also possible (Kara et al., 2012), allowing assessment of the time scales over which the model is able to capture the observed variability within the data.

As part of the modelling process, it is common to adjust parameters to get the best fit with available field data and, as such, the use of a Bayesian Hierarchical Framework in the aquatic ecosystem modelling community has become increasingly useful (e.g., Zhang and Arhonditsis, 2009; Romarheim et al., 2015). Many parameters described throughout Section 2 are attempts at physically based descriptions where there is relatively little variation (Bruce et al., 2018), thereby reducing the number of parameters that remain uncertain. For others, however, their variation reflects imperfect formulation of some processes that are not completely described numerically. Therefore, within MATLAB, support scripts for GLM to work with the Markov Chain Monte Carlo (MCMC) code outlined in Haario et al. (2006) can be used to provide improved parameter estimates and uncertainty assessment (Figure 19; see also Huang et al., 2017~~8~~). Example setups for use of GLM within the PEST (Parameter Estimation Tool) have also been developed, giving users access to a wide range of assessment methodologies. The PEST framework allows for calibration of complex models using highly-parameterised regularisation with pilot-points (Doherty, 2015). Sensitivity matrices derived from the calibration process can also be utilised in linear and non-linear uncertainty analysis.

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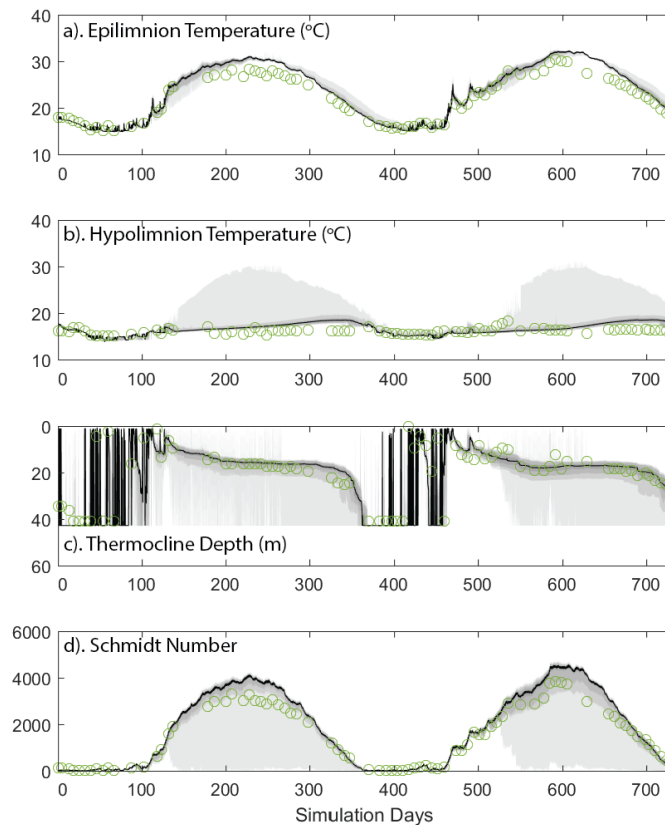


Figure 1819: Depiction of parameter uncertainty for a GLM simulation of Lake Kinneret, Israel, following calibration against observations (green circles) via MCMC for a) epilimnion temperature, b) hypolimnion temperature, c) thermocline depth, and d) Schmidt number. The black line indicates the 50th-percentile likelihood of the prediction, and the grey bands depict the 40th, 60th and 80th percentile.

5.3 Operation in the cloud: GRAPLER

Questions relevant to land use and climate change are driving scientists to develop numerous scenarios for how lake ecosystems might respond to changing exogenous drivers. An important approach to addressing these questions is to simulate lake or reservoir physical-biological interactions in response to changing hydrology, nutrient loads or meteorology, and then infer consequences from the emergent properties of the simulation, such as changes in water clarity, extent of anoxia, mixing regime, or habitability to fishes (Hipsey et al., 2015). Often, it takes years or even decades for lakes to respond fully to changes in exogenous drivers, requiring simulations to recreate lake behavior over extended periods. While most desktop computers can run a decade-long, low-resolution simulation in less than one minute, high-resolution



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simulations of the same extent may require minutes to hours of processor time. When questions demand hundreds, thousands or even millions of simulations, the desktop approach is no longer suitable.

Through access to distributed computing resources, modellers can run thousands of GLM simulations in the time it takes to run a few simulations on a desktop computer. Collaborations between computer scientists in the Pacific Rim Applications and Grid Middleware Assembly (PRAGMA) and GLEON have led to the development of GRAPLEr (GLEON Research and PRAGMA Lake Expedition in R), software, written in R, that enables modellers to distribute batches of GLM simulations to pools of computers (Subratie et al., 2017). Modellers use GRAPLEr in two ways: by submitting a single simulation to the GRAPLEr Web service, along with instructions for running that simulation under different climate scenarios, or by configuring many simulations on the user's desktop computer, and then submitting them as a batch to the Web service. The first approach provides a high degree of automation that is well suited to training and instruction, and the second approach has the full flexibility often needed for research projects. In all approaches, GRAPLEr converts the submitted job to a script that is used by the scheduling program HTCondor (Thain et al., 2005) to distribute and manage jobs among the computer pool and ensure that all simulations run and return results. An iPOP overlay network (Ganguly et al., 2006) allows the compute services to include resources from multiple institutions, as well as cloud computing services.

GRAPLEr's Web service front-end shields the modeller from the compute environment, greatly reducing the need for modellers to understand distributed computing; they therefore only need to install the R package, know the URL of the GRAPLEr Web service, and decide how the simulations should be setup.

20

5.4 Integration with catchment and climate models

GLM simulations may be coupled with catchment models, such as the Soil Water Assessment Tool (SWAT) or similar catchment models, simply by converting the catchment model output into the inflow file format via conversion scripts (e.g., Bucak et al., 2018). Similarly, scripts exist for coupling GLM with the Weather Research Forecasting (WRF) model, or similar climate models, for specification of the meteorological input file from weather prediction simulations (e.g., Hansen et al., 2018).

The above coupling approaches require the models to be run in sequence. For the simulation of lake-wetland-groundwater systems, however, two-way coupling is required to account for the flow of water into and out of the lake throughout the simulation. For these applications, the interaction ~~can be~~ has been simulated using GLM coupled with the 3D groundwater flow model, FEFLOW (<https://www.mikepoweredbydhi.com/products/feflow>). For this case, the GLM code is compiled as a Dynamic Link Library (DLL), termed libGLM, and loaded into FEFLOW as a plug-in module. The coupling between GLM and FEFLOW is implemented using a one-step lag between the respective solutions of the groundwater and lake models. This approach, in most simulations, does not introduce a significant error, however, error can be assessed and reduced using smaller time step lengths. The GLM module was designed to accommodate situations of variable lake geometry, by using a dry-lake/wet-lake approach, ~~whereby-~~ In this approach, dry-lake areas are defined as those above the current lake level and

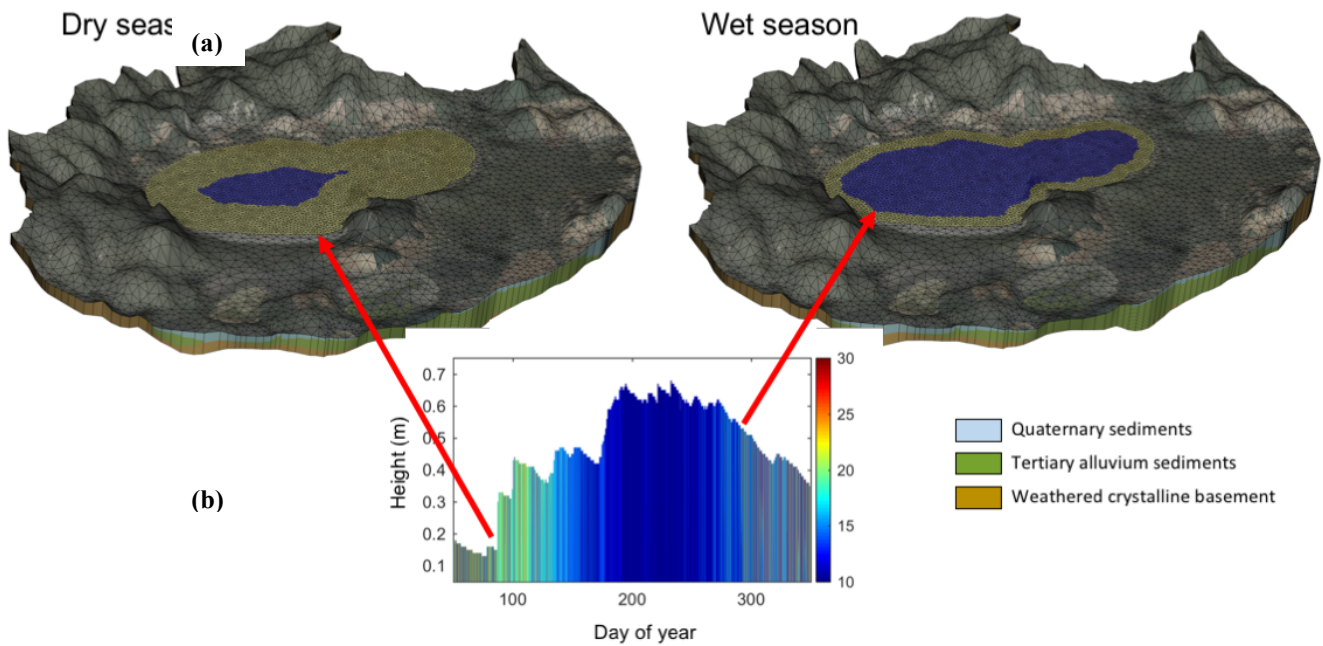
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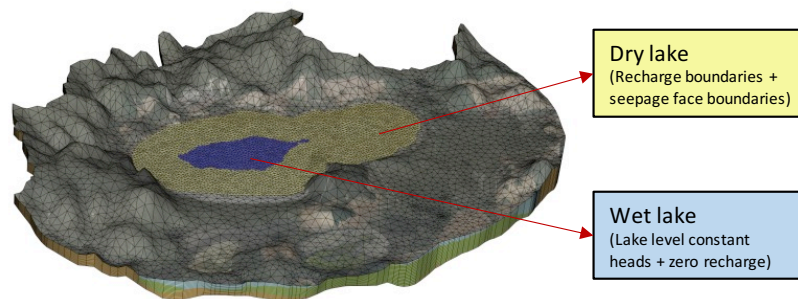
wet-lake areas as below the current lake level. Different boundary types in FEFLOW are assigned to dry-lake and wet-lake areas (Figure [2019](#)). The calibration of such coupled models is often complex, given the large number of parameters and sensitivities when different sources of information are utilised (for example flow and water level measurements). The FEFLOW-GLM coupling structure allows for a relatively straightforward integration with PEST, based on existing

5 FEFLOW workflows.

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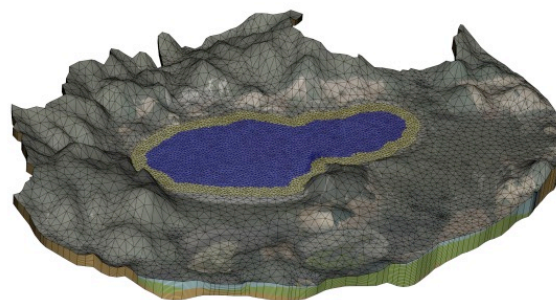


Dry season
 (lake level at 171.4 mAHD)



38500 [m]

Wet season
 (lake level at 171.8 mAHD)



38500 [m]

- Quaternary sediments
- Tertiary alluvium sediments
- Weathered crystalline basement



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Figure 1920: Example of ~~water level lake boundary~~ changes during ~~wet and dry~~ seasonal cycles from Lake Muir, Australia. GLM water level is ~~periodically~~ communicated to ~~the 3D~~ FEFLOW ~~groundwater model via a plugin calling libGLM, to each time step~~ and used as a constant head boundary condition for all wet cells ~~within the FEFLOW mesh~~.

5 6 GLM as a tool for teaching environmental science and ecology

Environmental modelling is integral for understanding complex ecosystem responses to anthropogenic and natural drivers, and also provides a valuable tool for engaging students learning environmental science (Carey and Gougis, 2017). Previous pedagogical studies have demonstrated that engaging students in modelling provides cognitive benefits, enabling them to build new scientific knowledge and conceptual understanding (Stewart et al., 2005; Schwarz et al., 2009). For example, modelling forces students to analyze patterns in data, create evidence-based hypotheses for those patterns and make their hypotheses explicit, and develop predictions of future conditions (Stewart et al., 2005). As a result, the U.S. National Research Council has recently integrated modelling into the *Next Generation Science Standards*, which provide recommendations for primary and secondary school science pedagogy in the United States (NRC, 2013). However, it remains rare for undergraduate and graduate science courses to include the computer-based modelling that environmental scientists need to manage natural ecosystems.

A teaching module for the use of GLM within undergraduate and graduate classrooms has been developed to explore lake responses to climate change (Carey and Gougis, 2017). The GLM module, called the “Climate Change Effects on Lake Temperatures”, teaches students how to set up a simulation for a model lake within R. After they are able to successfully run their lake simulations, they force the simulation with climate scenarios of their own design to examine how lakes may change in the future. To improve computational efficiency, students also learn how to submit, retrieve, and analyze hundreds of model simulations through distributed computing overlay networks embedded via the GRAPLEr interface (Section 5.3). Hence, students participating in the module learn computing and quantitative skills in addition to improving their understanding of how climate change affects lake ecosystems.

Initial experiences teaching GLM as well as pre- and post-assessments indicate that participation in the module improves students’ understanding of lake responses to climate change (Carey and Gougis, 2017). By modifying GLM boundary condition data and exploring model output, students are able to better understand the processes that control lake responses to altered climate, and improve their predictions of future lake change. Moreover, the module exposes students to computing and modelling tools not commonly experienced in most university classrooms, building competence with manipulating data files, scripting, creating figures and other visualizations, and statistical and time series analysis; all skills that are transferrable for many other applications.



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7 Conclusions

As part of GLEON activities, the emergence of complex questions about how different lake types across the world are responding to climate change and land-use change has created the need for a robust, accessible community code suitable for a diverse range of lake types and simulation contexts. Here, GLM is presented as a tool that meets many of the needs of network participants ~~for their individual lake simulation requirements with suitability to a wide array of lake types and sizes, whilst also in addition to being suitable for meeting the need for a application in a distributed way simulation~~ across tens to thousands of lakes ~~as is required~~ for regional and global scale assessments (e.g., Kirillin et al., 2011). Recent examples ~~have included~~ an application of the model for assessing how the diversity of ~~>~~2000 lakes in ~~the a~~ lake-rich landscape in Wisconsin respond to climate, including projected warming (Read et al., 2014; Winslow et al., 2017). Given its computationally efficient nature, it is envisioned that GLM can be made available as a library for use within in land-surface models (e.g., the Community Land Model, CLM), allowing improved representation of lake dynamics in regional hydrological or climate assessments. With further advances in the degree of resolution and scope of earth system models, we further envisage GLM as an option suitable to be embedded within these models to better allow the simulation of lake stratification, air-water interaction of momentum and heat, and also biogeochemically relevant variables associated with contemporary questions about greenhouse gases emissions such as CO₂, CH₄, and N₂O.

Since the model is one-dimensional, it assumes no horizontal variability in the simulated water layers and users must therefore ensure their application of the model is suited to this simplifying assumption. For stratified systems, the parameterization of mixing due to internal wave and inflow intrusion dynamics is relatively simple, making the model ideally suited to longer-term investigations ranging from weeks to decades (depending on the domain size), and for coupling with biogeochemical models to explore the role that stratification and vertical mixing play on lake ecosystem dynamics. However, the model can also be used for shallow lakes, ponds and wetland environments where the water column is relatively well mixed. In cases where the assumption of one-dimensionality is not met for a particular lake application, a two or three dimensional model may be preferred.

This paper has focused on description of the hydrodynamic model, but we highlight that the model is a platform for coupling with advanced biogeochemical and ecological simulation libraries for water quality prediction and integrated ecosystem assessments. As with most coupled hydrodynamic-ecological modelling platforms, GLM handles the boundary conditions and transport of variables simulated within these libraries, including the effects of inflows, vertical mixing, and evapo-concentration. Whilst the interface to these libraries is straightforward, the Lagrangian approach adopted within GLM for simulation of the water column necessitates the adoption of sediment zones on a static grid that is independent from the water column numerical grid.

More advanced workflows for operation of the model within distributed computing environments and with data assimilation algorithms is an important application when used within GLEON capabilities related to high frequency data and its interpretation. The 1D nature of the model makes the run-times modest and therefore the model suitable for application



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within more intensive parameter identification and uncertainty assessment procedures. This is particularly relevant as the needs for network participants to expand model configurations to further include biogeochemical and ecological state variables. It is envisioned that continued application of the model will allow us to improve parameter estimates and ranges, and this will ultimately support other users of the model in identifying parameter values, and assigning parameter prior distributions. Since many of the users the model is intended for may not have access to the necessary cyberinfrastructure, the use of GLM with the open-source GRAPLER software in the R environment provides access to otherwise unavailable distributed computing resources. This has the potential to allow non-expert modellers within the science community to apply good modelling practices by automating boundary condition and parameter sensitivity assessments, with technical aspects of simulation management abstracted from the user.

10

Finally, the role of models in informing and educating members of the network and the next generation of hydrologic and ecosystem modellers has been identified as a critical element of synthesis activities and supporting cross-disciplinary collaboration (Weathers et al., 2017). Initial use of GLM within the classroom has found that teaching modules integrating GLM into classes improves students' understanding of lake ecosystems.

15 **Code availability**

The GLM code is provided as open-source under the GNU GPL3 license, and version controlled via the GitHub repository: <https://github.com/AquaticEcoDynamics/GLM>. ~~*[Code DOI to be inserted here on final acceptance]*~~; DOI: [10.5281/zenodo.1297331](https://doi.org/10.5281/zenodo.1297331)

Data availability

20 The five example lakes used to demonstrate the model operation are described along with model input files (and associated hydrologic and meteorological forcing data) within the GitHub repository:

https://github.com/AquaticEcoDynamics/GLM_Examples ~~*[Examples DOI to be inserted here on final acceptance]*~~ <https://github.com/AquaticEcoDynamics/GLM/tree/master/Examples/2.4.0>; DOI: [10.5281/zenodo.1297415](https://doi.org/10.5281/zenodo.1297415)

~~*[Examples DOI to be inserted here on final acceptance]*~~

25 **Acknowledgments**

The primary code of GLM has been developed by MH, LB, CB, BB and DH at The University of Western Australia in collaboration with researchers participating in GLEON, with support provided by a National Science Foundation (NSF) (USA) Research Coordination Network Award. Whilst GLM is a new code, it is based on the large body of historical research and publications produced by the Centre for Water Research at the University of Western Australia, which we

30 acknowledge for the inspiration, development and testing of several of the model algorithms that have been adopted.

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Table 1. Summary of GLM parameters – notation with values for constants, recommended – suggested (default) values for parameters, and supporting and information and references, where relevant.

Symbol	Description	Units	Value	Comments	Reference
σ	Stefan-Boltzmann constant	$W\ m^{-2}\ K^{-4}$	5.67×10^{-8}	Not adjustable in glm.nml	
g	acceleration due to gravity	$m\ s^{-2}$	9.81		
c_a	specific heat capacity of air	$J\ kg^{-1}\ ^\circ C^{-1}$	1005		
c_l	specific heat capacity of air	$J\ kg^{-1}\ ^\circ C^{-1}$	2050		
c_w	specific heat capacity of liquid water	$J\ kg^{-1}\ ^\circ C^{-1}$	4185.5		
λ_e	Latent heat of evaporation	$J\ kg^{-1}$	2.453×10^6		
λ_f	Latent heat of fusion	$J\ kg^{-1}$	3.340×10^5		
ω	ratio of molecular weight of water to molecular weight of air	-	0.622		
c_{second}	number of seconds per day	$s\ day^{-1}$	86400		
<u>Indices/Indices</u>					
N_{BSN}	user provided number of basin height points		configurable	set in &morphometry	
N_{MORPH}	internally computed number of vertical height increments for the hypsographic curve		computed	$H_{b=N_{BSN}} \Delta H_{mi} + 10$	
N_{LEV}	number of layers, which varies over time		variable		
N_{INF}	number of inflows configured		configurable	set in &inflows	
N_{OUT}	number of outlets configured		configurable	set in &outflows	
N_{SW}	number of shortwave radiation bands configured		configurable	set in &light	
N_{SZ}	number of sediment zones configured		configurable	set in &sediment	
b	hypsographic data point index		index		
mi	internal hypsographic curve increment		index		
i	index of computational layer		index		
i_j	index of the lake layer at an equivalent depth to inflow parcel j		index		
i_{bot}	index of lower most layer impacted by a given withdrawal/outflow		index		
i_{top}	index of the upper-most layer impacted by a given withdrawal/outflow		index		
i_{outf}	index of the lake layer aligning with a withdrawal/outflow extraction point		index		
s	layer index of the layer at the surface of the lake		index		
k	layer index of the layer at the bottom of the surface mixed layer (sml; epilimnion)		index		
j	index of inflow parcel transport, prior to insertion		index		
z	index of sediment zone		index		
l	index of light bandwidth fraction		index		



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Symbol	Description	Units	Value	Comments	Reference
I	inflow index		index		
O	outflow index		index		
Time					
t	time	s	-		
t_b	time when a shear event begins	s	-		
$\lfloor t \rfloor$	floor of time	s	-	used to compute the time within a day, to to to	
Δt	time step used by the model	s	3600	numerical time increment the model uses	
TZ	Time Zone indicated by number of hours from GMT	hr	configurable	set in &time	
$N_{\Delta t}$	number of time-steps to simulate day-of-the year	-	configurable variable	set in &time	
$c_{second} N_{\Delta t}$	number of seconds per day number of time-steps to simulate	s day ⁻¹	86400 configurable		
d	day of the year	-	variable		
δt_d	time-scale of inflow parcel transport	s	computed		
δt_{wave}	period of surface waves	s	computed	Eq. 7079	
δt_{iw}	period for internal waves	s	computed	$\delta t_{iw} = L_{META}/2c$	Spigel and Imberger (1980)
δt_{shear}	cut-off time for internal wave induced velocity shear	s	computed	Eq. 4047	
δt_{damp}	time-scale of internal wave damping	s	computed	Eq. 4350	Spigel and Imberger (1980)
N_{OUT}	number of outlets configured	-	configurable	set in -&outflows	
N_{INF}	number of inflows configured	-	configurable	set in -&inflows	
N_{LEV}	number of layers, which varies over time	-	variable		
N_{BSN}	user provided number of basin height points	-	configurable	set in -&morphometry	
N_{MORPH}	internally computed number of vertical height increments for the hypsographic curve	-	computed	$H_b = \frac{\Delta H_{mi}}{N_{BSN}} + 10$	
Lake setting (volumes, areas and lengths)					
V_{max}	maximum volume of the lake	m ³	computed	once exceeded, excess water is passed to overflow	
V_{crest}	volume of the lake at the crest height	m ³	computed	volume corresponds to height, h_{crest}	
V_b	lake volume at the hypsographic data point b	m ³	configurable	Eq. 1	
V_{mi}	interpolated volume at internal morphometry table increment mi	m ³	computed	Eq. 2	
V_i	volume of the lake at the top of the i th layer	m ³	variable	$\sum_{j=1}^i \Delta V_j$	
V_s	volume of the lake at the top of the surface layer ($i = N_{LEV}$)	m ³	variable	$V[h_{i=N_{LEV}}]$	
V_s^*	interim calculation of the volume of the lake at the top of the surface layer	m ³	variable	used to estimate lake volume prior to overflow calculation	
ΔV_i	volume of the ith layer	m ³	variable	$V[h_i] - V[h_{i-1}]$	
\tilde{V}_{N^2}	a fractional volume of the lake that contains 85% of N^2 variance	m ³	variable	computed as the volume of the lake above the height which is one standard deviation (δz_σ) below the height at the centre of buoyancy	



Symbol	Description	Units	Value	Comments	Reference
ΔV_i	volume of the i^{th} layer	m^3	variable	$V[h_i] - V[h_{i-1}]$	
ΔV_{epi}	volume of the epilimnion	m^3	variable	$\Delta V_{epi} = V_s - V_{k-1}$	
ΔV_{k-1}	volume of the layer below the surface mixed layer/epilimnion	m^3	variable	$V[h_{i=k-1}]$	
A_{max}	maximum possible area of the lake	m^2	configurable	$A_{max} = A_{b=N_{BSN}}$	
A_b	lake area above datum at the hypographic data point b	m^2	configurable	set in <code>&morphometry</code>	
A_{mi}	lake area at internal morphometry table increment mi	m^2	computed		
A_i	lake area of the i^{th} layer	m^2	variable		
$A[H]$	lake area at a given height / elevation	m^2	configurable	area-height relationship	
A_s	area of the lake surface	m^2	variable		
A_{BEN}	lake bottom (benthic) area exceeding the critical light threshold $\phi_{BEN_{crit}}$	m^2	variable		
A_E	effective area of the lake surface exposed to wind stress	m^2	computed		
A_{EWS}	critical area below which wind sheltering may occur	m^2	10^7	set in <code>&fetch</code>	Xenopoulos and Schindler (2001)
A_{outf}	area of the lake at the height of the relevant outflow	m^2	computed		
A_{k-1}	lake area at the top of the metalimnion	m^2	variable		
H	variable referring to height above datum	m above datum		$H = H_0 + h$	
H_{max}	maximum height of the lake, at the lake crest above which water will overflow	m above datum	configurable	set in <code>&morphometry</code> set in <code>&morphometry</code>	
H_{crest}	height at the lake crest	m above datum	configurable		
H_0	bottom height of the lake	m above datum	configurable		
H_b	height above datum at the hypographic data point b	m above datum	configurable		
H_{mi}	height above datum at internal morphometry table increment mi	m above datum	computed		
ΔH_{mi}	height increment used for the model's internal hypographic curve interpolation function	m	0.01		
h	height above a datum	m above lake bottom			
h_i	height above a datum at the top of layer i	m above lake bottom	variable		
h_s	height of the upper-top surface of the top-uppermost (surface) layer above the datum	m above lake bottom	variable	Eq. 54	
h_s^*	interim surface height computed prior to overflow calculation	m above lake bottom	computed		
h_B	height of the upper-top surface of the bottom-most layer above the datum	m above lake bottom	variable	Eq. 68	
h_{BEN}	height at which the $\phi_{BEN_{crit}}$ is reached	m above lake bottom	variable		
h_z	height of the uppermost limit of the sediment zone z	m above lake bottom	configurable	set in <code>&sediment if benthic_mode=2</code>	
\tilde{h}_i	height of the middle of the i^{th} layer	m above lake bottom	variable		
\tilde{h}_{sml}	height of the middle of the epilimnion	m above lake bottom	variable		



Symbol	Description	Units	Value	Comments	Reference
h_{outf}	height of a configured outflow	m above lake bottom	configurable	set in <code>&outflow</code>	
h_{inf}	height of a submerged inflow	m above lake bottom	configurable	set in <code>&inflow</code>	
h_{insI}	height of the bottom of the layer where an inflow parcel associated with the I^{th} inflow inserted	m above lake bottom	variable		
h_{insI-1}	height of the bottom of the layer where an inflow parcel associated with the I^{th} inflow inserted height of a submerged inflow	m above lake bottom m above lake bottom	variable configurable	set in <code>&inflow</code>	
h_{crest}	height of the lake crest where water begins to overflow	m above lake bottom	computed	$h_{crest} = H_{crest} - H_0$	
z	depth from the lake surface, or height above the lake surface	m from water surface			
z_{avg}	average depth of the lake	m	variable		
z_{BEN}	depth to the lake where critical light threshold is exceeded	m from water surface	variable	Eq. 175	
z_{sml}	depth to the thermocline from the surface	m from water surface	variable	also, vertical thickness of the surface mixed layer (sml).	
z/L	Monin-Obukhov stability parameter	-	computed	Eq. A26	
z_o	water surface roughness length	m	computed	Eq. A24	
z_θ	water surface heat roughness length	m	computed		
z_e	water surface moisture roughness length	m	computed		
$z_{inf_{insI}}$	depth that an inflow parcel associated with inflow I inserts	m from water surface	variable	depth from the surface where an inflow reaches its level of neutral buoyancy	
Δz_i	thickness of the i^{th} layer	m	variable		
Δz_{k-1}	thickness of the layer below the epilimnion	m	variable		
Δz_{min}	minimum layer thickness	m	0.5	Should be estimated relative to lake depth; set in <code>&glm_setup</code>	Bruce et al. (2018)
Δz_{max}	maximum layer thickness	m	1.5		Bueche et al. (2017)
Δz_{ice}	combined thickness of the white ice and blue ice	m	computed	$\Delta z_{white} + \Delta z_{blue}$	
$\Delta z_{ice,snow}$	thickness of top layer of ice cover, depending on ice or snow presence	m	computed	Eq. 3229	
Δz_{snow}	thickness of snow	m	variable	Eq. 3229; Figure 6	
Δz_{white}	thickness of white ice	m	variable	Eq. 3229	
Δz_{blue}	thickness of blue ice	m	variable	Eq. 382	
Δz_{info}	thickness of an inflow parcel before transport into the lake	m	computed	Eq. 6255	
Δz_{inf_j}	thickness of inflow parcel j	m	variable	Eq. 6457	
δz_σ	vertical length scale of one standard deviation about the centre of the N^2 distribution	m	computed		
δz_{inf_j}	vertical transport length of inflow parcel j	m	variable	$\delta z_{inf_j} = (h_s - z_{inf_j}) - h_{i_j-1}$	
δz_{wave}	significant wave height of surface waves	m	computed	Eq. 7382	



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Symbol	Description	Units	Value	Comments	Reference
δz_{soil}	thickness of soil layer	m	0.5	relevant layer thickness for computing sediment heat diffusion or water seepage	
Other notation (sorted alphabetically)					
a	Charnock constant	-	0.012	relates roughness length to wind speed	
AM	air mass factor	-	computed	Eq. A7	
AM_p	air mass factor at pressure p	-	computed	Eq. A7	
AOD_{500}	aerosol optical depth at 500 nm	-	0.033 – 0.10		
AOD_{380}	aerosol optical depth at 380 nm	-	0.038 – 0.15		
α	Charnock constant	-	0.012		
b	width of the weir crest	m	configurable	used if $H_{crest} < H_{max}$; set in &outflow	
c	internal wave speed	$m s^{-1}$	computed	Eq. 48†	
c_a	specific heat capacity of air	$J kg^{-1} °C^{-1}$	1005		
c_i	specific heat capacity of air	$J kg^{-1} °C^{-1}$	2050		
c_w	specific heat capacity of liquid water	$J kg^{-1} °C^{-1}$	4185.5		
c_{damp}	coefficient related to damping rate of internal waves	-	104.1		Spigel (1978)
c_{wn}	coefficient related to wavenumber calculation	-	12.4		
C	set of scalars being simulated	various	variable	variable number of scalars managed by GLM which are subject to mixing and mass conservation	
C_i	concentration of relevant scalar, including salinity or water quality variable, in the i^{th} layer	various	variable	Eq. 5†	
\bar{C}	mean concentration of two or more layers	various	computed variable		
ΔC	difference in concentration of two layers	various	computed variable		
C_{inf}	concentration of relevant scalar in the outflowing water	various	time-series input		
C_{outf}	concentration of relevant scalar in the outflowing water	various	variable		
C_{KH}	Mixing efficiency - Kelvin-Helmholtz turbulent billows	-	0.3	set in &mixing "a good rule of thumb..."	Sherman et al. (1978)
C_{HYP}	mixing efficiency of hypolimnetic turbulence	-	0.5	applied differently based on deep_mixing model (see text), set in &mixing ; general diffusivities in Jellison and Melack (1993)	Weinstock (1981); general diffusivities in Jellison and Melack (1993)
C_T	m Mixing efficiency - unsteady turbulence (acceleration)	-	0.51	best fit of experiments reviewed set in &mixing from Wu (1973) selected from a range given in Spigel et al. (1986)	Sherman et al. (1978) Spigel et al. (1986) Yeates & Imberger (2003) Wu (1973)
C_S	m Mixing efficiency - shear production	-	0.3		
C_W	m Mixing efficiency - wind stirring	-	0.23		
C_K	m Mixing efficiency - convective overturn	-	0.2		
$C_{D_{inf}}$	stream-bed drag of an inflowing rivers	-	0.016	set based on inflow bed roughness in &inflow	
$C_{D_{weir}}$	drag associated with weir crest	-	0.62	set in &outflow	



Symbol	Description	Units	Value	Comments	Reference
C_D	bulk aerodynamic coefficient for momentum	-	0.0013	see also Appendix B; Eq. A23	
C_E	bulk aerodynamic coefficient for latent heat transfer	-	0.0013	from Hicks' (1972) collation of ocean and lake data; many studies since use similar values; internally calculated if atmospheric stability correction is on.	Fischer et al. (1979) Bruce et al. (2018) Bueche et al. (2017)
C_H	bulk aerodynamic coefficient for sensible heat transfer	-	0.0013		
C_{XN}	generic notation for neutral value of bulk transfer coefficient	-	selected	X = H or E	
C_{DN-10}	value of bulk transfer coefficient for momentum under neutral atmospheric conditions, referenced to 10m height.	-	computed	see also Appendix B	
C_{HEN}	value of bulk transfer coefficient for heat/moisture under neutral atmospheric conditions, referenced to 10m height.	-	0.0013		
C_x	cloud cover fraction	-	time-series input		
d_{Tz}	day of the year when the soil temperature peaks, for the z^{th} zone	-	1-365		
D_z	effective vertical diffusivity of scalars in water	$\text{m}^2 \text{s}^{-1}$	computed		
D_ε	diffusivity of scalars in water due to turbulent mixing	$\text{m}^2 \text{s}^{-1}$	computed		
D_m	molecular diffusivity for scalars in water	$\text{m}^2 \text{s}^{-1}$	1.25×10^{-9}		
D_a	molecular heat diffusivity of air	$\text{m}^2 \text{s}^{-1}$	2.14×10^{-5}	reported as $0.077 \text{ m}^2 \text{ hr}^{-1}$	TVA (1972)
D_{outf}	average vertical diffusivity of scalars in layers spanning the withdrawal thickness	$\text{m}^2 \text{s}^{-1}$	computed	values from Eq. 57 averaged over the relevant layers	Imberger and Patterson (1981)
e_s	saturation vapour pressure	hPa	computed	Eq. 242	Tabata (1973) various
e_a	atmospheric vapour pressure	hPa	computed	Eq. 253	
e_*	humidity scale	hPa	computed		
E_{TKE}	turbulent kinetic energy per unit mass available for mixing, per mass per wavenumber integrated over layer depth	$\text{m}^3 \text{s}^{-2}$	computed -	Eq. 4134	Imberger and Patterson (1981)
E_{PE}	potential energy within the stratified water column integrated over layer depth	$\text{m}^3 \text{m}^3 \text{s}^{-2}$	computed -	Eq. 4235	Hamilton and Schladow (1997)
E	evaporation mass flux	m s^{-1}	variable	$E = -\phi_E / \lambda_v \rho_s$	
E_{inf}	inflow entrainment	-	computed	Eq. 6053	
EQT	equation of time	-	computed	Eq. A4	
F	fetch	m	computed	approximated from the square root of the lake area, Eq. 7869	
F_T	internal Froude number of the lake subject to a water withdrawal	-	computed	Eq. 684	
f_R, f_S	rainfall, snowfall scaling factor	-	1	used to adjust/calibrate model to meteorological data	
f_{SW}	solar radiation scaling factor	-	1		
f_U	wind-speed scaling factor	-	1		
f_{AT}	air temperature scaling factor	-	1		
f_{RH}	relative humidity scaling factor	-	1		
f_{inf}	inflow rate scaling factor	-	1	used to adjust flow boundary condition data	
f_{outf}	outflow rate scaling factor	-	1		



Symbol	Description	Units	Value	Comments	Reference
f_{SWE}	snow water equivalent fraction	m rain/m snow	0.1		
f_{snow}	snow compaction constant	-	computed	Figure 6	
f_{WS}	wind-sheltering scaling factor	-	1	function used to scale the wind-sheltering length scale or lake surface area, based on the direction of the wind	
f_{ro}	runoff coefficient	m runoff/m rain	0.2	depends on land slope and soil type	
f_{PAR}	fraction of global incoming radiation flux which is photosynthetically active	-	0.45		Jellison and Melack (1993)
f_{VIS}	visible bandwidth fraction	-	0.3		Rogers et al. (1995)
$f_{BEN_{crit}}$	fraction of surface irradiance at the benthos, which is considered critical for productivity	-	0.2	set in <code>&glm_setup_light</code>	
f_w	friction factor used for current stress calculation	-	computed	Eq. 8778	Kleinmans and Grasmeyer (2006)
f_c	friction factor used for wave stress calculation	-	computed		
f_0	roughness correction coefficient for the lake surface	-	0.5		TVA (1972)
f_{dif}	smoothing factor used for diffusion	-	computed	Eq. 592	
g	acceleration due to gravity	$m\ s^{-2}$	9.81		
g'_k	reduced gravity between the mixed layer and the $k - 1$ layer	$m\ s^{-2}$	computed		
g'_{EH}	reduced gravity between the epilimnion and the hypolimnion	$m\ s^{-2}$	computed		
g'_{inf}	reduced gravity between the inflowing water and adjacent lake water	$m\ s^{-2}$	computed		
G	seepage rate	$m\ day^{-1}$	0		
Gr	Grashof number related to an outflow extraction	-	computed	Eq. 692	Imberger and Patterson (1981)
k_{TKE}	turbulence wavenumber	m^{-1}	computed	Eq. 546	
K_w	light extinction coefficient	m^{-1}	0.5	set in <code>&glm_setup_light</code> , or updated via the linked water quality model; can be estimated from Secchi depth data	
K_{wl}	light extinction coefficient of the l^{th} bandwidth fraction	m^{-1}	configurable	set in <code>&light</code> , and used if <code>light_model = 2</code>	Cengel and Ozisk (1984)
K_{w1}	Waveband 1, snow ice light extinction	m^{-1}	48.0		
K_{w2}	Waveband 2, snow ice light extinction	m^{-1}	20.0		
K_{b1}	Waveband 1, blue ice light extinction	m^{-1}	1.5		
K_{b2}	Waveband 2, blue ice light extinction	m^{-1}	20.0		Rogers et al., (1995),
K_{s1}	Waveband 1, snow light extinction	m^{-1}	6		Patterson and Hamblin (1988)
K_{s2}	Waveband 2, snow light extinction	m^{-1}	20		Ashton (1986)
K_{snow}	molecular heat conductivity of snow	$J\ m^{-1}\ s^{-1}\ ^\circ C^{-1}$	computed	dependent on snow density according to Eq. 35 Fig-6	Yao et al., (2014)
$K_{ice_{white}}$	molecular heat conductivity of white ice	$J\ m^{-1}\ s^{-1}\ ^\circ C^{-1}$	2.3		
$K_{ice_{blue}}$	molecular heat conductivity of blue ice	$J\ m^{-1}\ s^{-1}\ ^\circ C^{-1}$	2.0		
K_{water}	molecular heat conductivity of water	$J\ m^{-1}\ s^{-1}\ ^\circ C^{-1}$	0.57		



Symbol	Description	Units	Value	Comments	Reference
K_{air}	molecular heat conductivity of air	$J m^{-1} s^{-1} °C^{-1}$	2.8×10^{-3}	reported as $0.1 kJ m^{-1} hr^{-1} K^{-1}$	TVA (1972)
K_{soil}	heat conductivity of soil/sediment	$J m^{-1} s^{-1} °C^{-1}$	1.2	varies from 0.25 for organic soil to 2.9 for inorganic particles	
K_{seep}	hydraulic conductivity of soil below the lake	m day⁻¹	configurable	set in &outflows	
Lat	Latitude	degrees, + for N	configurable	set in &morphometry	
$Long$	Longitude	degrees + for E	configurable		
L_D	equivalent circular diameter of the lake	m	computed		
L_{META}	length of the lake at the depth of the thermocline region (metalimnion)	m	computed		
L_{outf}	length of the lake at the height of the relevant outflow	m	computed		
L_{crest}	length of the lake at the upper most height of the domain	m	configurable		
m	constant used to compute the rate at which work from the wind is converted	-	4.6×10^{-7}		
N^2	the buoyancy frequency, a measure of water column stratification	s^{-2}	computed	Eq. 53	
N_{outf}^2	the buoyancy frequency, a measure of water column stratification, about the layers impacted by the water outflow	s^{-2}	computed	Eq. 74	
Oz	ozone concentration	atm-cm	0.279 - 0.324		Luo et al. (2010)
p	air pressure	hPa	1013	assumed constant	
Q_{inf_x}	rate of a single water inflow provided by the user as input to the model	$m^3 day^{-1}$	time-series input	based on the non_avg flag in &glm_setup, the supplied value at the current time step or the average of the current and past time step is used, depending on whether the daily data is referenced from midday or midnight	
Q_{outf_x}	rate of a single water outflow provided by the user as input to the model	m³ day⁻¹	time-series input		
Q_{inf_0}	rate of a single water inflow prior to the inflow entering the lake	$m^3 s^{-1}$	computed	$Q_{inf_0} = f_{inf} Q_{inf_x} / c_{secday}$	
Q_{inf_j}	flow rate of inflow water parcel during transit, at the j^{th} increment	$m^3 s^{-1}$	variable	Eq. 670 used to increment between j steps	
ΔQ_{inf_j}	rate of entrained water for an inflow at the j^{th} increment	m³ s⁻¹	computed		
$Q_{inf_{ins_l}}$	flow rate of inflowing water at the point of insertion, for inflow- l	$m^3 s^{-1}$	variable	Figure 11	
Q_{outf_x}	rate of water outflow provided by the user as input to the model	$m^3 day^{-1}$	time-series input		
Q_{outf}	rate of a single water outflow exiting the lake	m³ s⁻¹	computed	$Q_{outf} = f_{outf} Q_{outf} / c_{secday}$	
Q_{outf_i}	flow rate of water being extracted from the i^{th} layer	$m^3 s^{-1}$	computed	$Q_{outf} = \sum_i^{N_{LEV}} Q_{outf_i}$	
Q_{ovfl}	rate of over flowing water leaving the lake	$m^3 s^{-1}$	computed	Eq. 773	
Q_{weir}	flow rate of water discharging over the crest, before flooding	$m^3 s^{-1}$	computed	Eq. 762	
$Q_{seepage}$	flow rate of water discharging from the lake bottom via seepage	m³ s⁻¹	computed	Eq. 75	
Q_R	boundary run-off into the lake surface layer	$m^3 s^{-1}$	computed	Eq. 8	
R	dimensionless parameter describing a water withdrawal flow regime	-	computed	Eq. 70	
R_x	rainfall rate supplied in the input file	m day⁻¹	time-series input	user supplied rainfall rate	
R_L	rainfall intensity threshold before run-in occurs	$m day^{-1}$	0.04	depends on land slope and soil type	



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Symbol	Description	Units	Value	Comments	Reference
R_{snow}	critical rainfall rate incident on snow that controls densification	m day^{-1}	configurable	set in &snowice	
RH_x	relative humidity	-	time-series input	user-supplied relative humidity between 0 and 1	
R_F	rainfall rate entering the water column	m s^{-1}	computed	Eq. 65	
$*R_F$	rainfall rate incident on the ice/snow layer	m s^{-1}	computed	$*R_F = f_R R_x / c_{secday}$	
R_x	rainfall rate supplied in the input file	m day^{-1}	time-series input	user-supplied rainfall rate	
r	water vapour mixing ratio	-	computed	ratio of water mass to total air mass	
Ri_{inf}	Richardson number of the inflow water	-	computed	Eq. 6154	
Ri_B	bulk Richardson number of the atmosphere over the lake	-	computed	Eq. A34	
S_x	snowfall rate supplied in the input file	m day^{-1}	time-series input	user supplied snowfall rate	
S_F	snowfall rate entering the water column	m s^{-1}	computed	Eq. 76	
$*S_F$	snowfall rate incident on the ice/snow layer	m s^{-1}	computed	$*S_F = f_S S_x / c_{secday}$	
S_i	salinity of the i^{th} layer	‰ppt	variable		
S_{inf_x}	salinity of water entering in an inflow	g m^{-3}	time-series input		
S_{out_f}	salinity of outflowing water	g m^{-3}	variable		
SZA	solar zenith angle	degrees	variable	$SZA = \Phi_{zen} 180/\pi$	
T_s	temperature of the surface layer	$^{\circ}\text{C}$	variable	Eq. 98	
T_x	air temperature supplied by the user	$^{\circ}\text{C}$	time-series input	user supplied air temperature	
T_a	air temperature	$^{\circ}\text{C}$	computed	$T_a = f_{AT} T_x$	
T_d	dew point temperature	$^{\circ}\text{C}$	computed		
T_i	temperature of the i^{th} layer	$^{\circ}\text{C}$	variable		
T_m	melt-water temperature	$^{\circ}\text{C}$	0		
T_0	temperature at the solid (ice/snow) surface	$^{\circ}\text{C}$	variable		
T_{inf_x}	temperature of water entering in an inflow	$^{\circ}\text{C}$	time-series input		
T_{out_f}	salinity of outflowing water	$^{\circ}\text{C}$	variable		
T_{z_i}	temperature of the sediment zone z which underlies layer i	$^{\circ}\text{C}$	computed	Eq. 40	
$T_{z_{mean}}$	annual mean temperature of the z^{th} sediment zone	$^{\circ}\text{C}$	configurable	set in &sediment; corresponds to the sediment temperature at a depth of δz_{soil}	
δT_z	seasonal amplitude of the soil temperature variation	$^{\circ}\text{C}$	configurable	set in &sediment	
T_{aa}	aerosol absorptance of incoming light in the atmosphere	-	computed	Eq. A17	
T_{mix}	scattering due to mixed gases	-	computed	Eq. A11	
T_{ozone}	ozone scattering of incident light in the atmosphere	-	computed	Eq. A10	
$T_{rayleigh}$	Rayleigh scattering of incident light in the atmosphere	-	computed	Eq. A9	
T_{watvap}	scattering of incident light in the atmosphere due to water vapour	-	computed	Eq. A14	



Symbol	Description	Units	Value	Comments	Reference
θ_v	virtual temperature of the atmospheric boundary layer above the lake	$^{\circ}\text{K}$	computed		
θ_a	temperature of the atmospheric boundary layer above the lake	$^{\circ}\text{K}$	computed	$\theta_a = f_{ax} T_* + 273.15$	
θ_s	temperature of the atmosphere at the lake surface	$^{\circ}\text{K}$	variable	$\theta_s = T_s + 273.15$	
θ_z					
U_{10}	wind speed above the lake referenced to 10m height	m s^{-1}	computed	wind speed corrected to reference height	
U_x	wind speed above the lake surface provided by the user	m s^{-1}	time-series input	user supplied snowfall rate	
U_{orb_i}	orbital wave velocity experienced at the bottom of the i^{th} layer	m s^{-1}	variable	Eq. 8475	
U_{m_i}	mean layer velocity of the i^{th} layer	m s^{-1}	variable	Eq. 8677	
u_{inf_j}	average velocity of an inflow parcel being tracked, prior to insertion	m s^{-1}	variable	Eq. 6659	
u_*	friction velocity	$\text{m}^3 \text{s}^{-3}$	computed	Eq. 4437	
u_b	velocity shear at the base of the thermocline	m s^{-1}	variable	Eq. 4639	
u_{bold}	velocity shear at the thermocline at the previous time-step	m s^{-1}	variable	reset between shear events	
W	total precipitable water vapour	atm-cm	1.1 - 2.2		Luo et al. (2010)
Wm	atmospheric water mass factor, computed for calculating water scattering	-	computed	Eq. A12	
W_{crest}	width of the lake at the upper most point	m	configurable	set in & morphology	
W_{outf}	width of the lake at the height of an outflow	m	computed	Eq. 7265	
w_*^3	turbulent velocity scale within the surfaced mixed layer, due to convective cooling	m s^{-1}	computed	Eq. 4336	Imberger and Patterson (1981)
x_{ws}	default sheltering distance defined as the distance from the shoreline at which wind stress is no longer affected by sheltering	m	configurable	set in & fetch; approximated as $50 \times x$ the vertical height of the sheltering obstacle/landform	Markfort et al. (2010)
x_{ws}^{ϕ}	sheltering distance adjusted for changes in wind direction	m	computed	$x_{ws}^{\phi} = x_{ws} (1 - \min(f_{ws}[\Phi_{wind}], 1))$	
δx_{wave}	wave length of surface waves	m	computed	Eq. 8172	
Δx_{inf_j}	lateral distance travelled by an inflow parcel per j increment, prior to insertion	m	computed	Eq. 6558	
α_{inf}	half-angle describing the width of an inflow river channel	degrees	configurable	user supplied in & inflow based on width and depth of the relevant river	
α_h	coefficient for sensible heat flux into still air	$\text{J m}^{-2} \text{s}^{-1} \text{ } ^{\circ}\text{C}^{-1}$	computed	Eq. 297b	TVA (1972)
α_e	coefficient for evaporative flux into still air	m s^{-1}	computed	Eq. 297a	TVA (1972)
α_{LW}	longwave albedo	-	0.03		
α_{SW}	albedo of shortwave radiation at the water surface	-	computed	Eq. 13 for water; uses empirical algorithm for ice cover	
α_{SKY}	scattered radiation within the sky	-	computed	$\alpha_{SKY} = 0.0685 + (1 - 0.84) (1 - T_{as})$	Bird (1984)
α_b	interpolation coefficient for volume	-	computed	Eq. 3	
β_b	interpolation coefficient for area	-	computed	Eq. 3	
δ_{wi}	length-scale associated with conduction of heat at the ice-water interface	m	0.039		Rogers et al. (1995)

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Symbol	Description	Units	Value	Comments	Reference
δ_{KH}	length-scale associated with formation of Kelvin-Helmholtz billows at the interface of two-layer stratification	m	computed		Imberger and Patterson (1981)
δ_{epi}	length-scale associated with the epilimnion	m	computed	Eq. 49	
δ_{hyp}	length-scale associated with the hypolimnion	m	computed	Eq. 49	
δ_{outf}	length-scale associated with the vertical thickness of the zone of influence of a withdrawal	m	computed	Eq. 7366	Imberger and Patterson (1981)
$\delta_{outf_{top}}$	thickness of withdrawal layer above the withdrawal height	m	computed		
$\delta_{outf_{bot}}$	thickness of withdrawal layer below the withdrawal height	m	computed		
δ_{ss}	particle diameter of bottom sediment	m	80×10^{-6}		
ϵ_{TKE}	TKE dissipation flux per unit mass	$m^2 s^{-3}$	-	Eq. 5448	
$\overline{\epsilon_{TKE}}$	steady-state/equilibrium TKE dissipation flux per unit mass	$m^2 s^{-3}$	computed	Eq. 5549	
ϵ_{WIND}	TKE dissipation flux created by power introduced by the wind	$m^2 s^{-3}$	computed	Eq. 5549	
ϵ_{INFLOW}	TKE dissipation flux caused by inflow plunging creating seiching	$m^2 s^{-3}$	computed	Eq. 5549	
ϵ_w	emissivity of the water surface	-	0.985		
ϵ_a	emissivity of the atmosphere under cloud-free conditions	-	computed	$\epsilon_a^*[T_a, e_a, 0]$	
ϵ_a^*	emissivity of the atmosphere including cloud reflection	-	computed	Eq. 21 ; options 1-4 are chosen via the cloud_mode variable in <code>meteo</code> <code>49</code>	Henderson-Sellers (1986)
ϕ_{SW_x}	shortwave radiation flux provided in the input file	$W m^{-2}$	time-series input	user supplied solar radiation data	-
$\phi_{SW_{so}}$	shortwave radiation flux crossing the water surface	$W m^{-2}$	computed	Eq. 109	-
ϕ_{SW_s}	shortwave radiation flux heating the surface mixed layer	$W m^{-2}$	computed		-
$\hat{\phi}_{SW}$	total incident shortwave radiation flux computed from the BCSM assuming clear-sky conditions	$W m^{-2}$	computed	Eq. 10-11 and Appendix A	Bird (1984)
$\hat{\phi}_{DB}$	direct beam radiation on a horizontal surface at ground level on a clear day	$W m^{-2}$	computed	Eq. A19	
$\hat{\phi}_{AS}$	radiation from atmospheric scattering hitting ground level on a clear day	$W m^{-2}$	computed	Eq. A20	
$\hat{\phi}_{ETR}$	extra-terrestrial radiation hitting the top of the atmosphere	$W m^{-2}$	computed	Eq. A1	
ϕ_{PAR}	downwelling PA-photosynthetically active radiation intensity within the water column	$W m^{-2}$	computed	Eq. 143	Kirk (1994)
$\phi_{PAR_{BEN}}$	light incident on the bottom of a layer, corresponding to the benthic area	$W m^{-2}$	variable		
$\phi_{LW_{in}}$	longwave radiation incident heat flux at the water surface	$W m^{-2}$	variable	Eq. 20+8	
$\phi_{LW_{out}}$	longwave radiation outgoing heat flux from the water surface	$W m^{-2}$	variable	Eq. 197	
$\phi_{LW_{net}}$	net longwave radiation flux across the lake surface	$W m^{-2}$	computed	Eq. 186	
ϕ_H	sensible heat flux across the water surface	$W m^{-2}$	computed	Eq. 220	
ϕ_E	latent heat flux	$W m^{-2}$	computed	Eq. 23+	
ϕ_{E_0}	latent heat flux under zero-wind conditions	$W m^{-2}$	computed	Eq. 286a	



Symbol	Description	Units	Value	Comments	Reference
ϕ_{H_0}	sensible heat flux under zero-wind conditions	W m ⁻²	computed	Eq. 286b	
ϕ_x	generic identifier for either of ϕ_E or ϕ_H	W m ⁻²	computed		
ϕ_{x_0}	generic identifier for either of ϕ_{E_0} or ϕ_{H_0}	W m ⁻²	computed		
ϕ_x^*	maximum value of either ϕ_{x_0} or ϕ_x	W m ⁻²	selected	Eq. 274	
ϕ_0	upward conductive heat flux through the ice and snow cover to the atmosphere	W m ⁻²	computed	Eq. 34	
ϕ_{net}	net incoming heat flux at the ice-atmosphere interface	W m ⁻²	computed	Eq. 3329	Rogers et al. (1995)
ϕ_R	heat flux due to rainfall	W m ⁻²	computed		Rogers et al. (1995)
ϕ_f	heat flux in the blue ice near the ice-water interface	W m ⁻²	computed	Eq. 364	
ϕ_w	heat flux from the water to the blue ice	W m ⁻²	computed	Eq. 373	
$\phi_{si} \phi_{white}^*$	heat flux per unit volume due to formation of white ice by flooding	W m ⁻²	computed		Rogers et al. (1995)
Φ_{zen}	solar zenith angle	radians	variable	Eq. A6	
Φ_{day}	day angle	radians	computed	Eq. A2	
Φ_{dec}	solar declination angle	radians	computed	Eq. A3	
Φ_{hr}	hour angle	radians	computed	Eq. A5	
Φ_{wind}	wind direction	degrees	time-series input	optionally provided as a boundary condition based on <code>fetch_mode</code> , set in <code>&fetch</code>	
Φ_{inf}	angle of the lake bed slope in the region where the inflow enters into the lake	degrees	configurable	user provided in <code>&inflow</code>	
$\rho_{\bar{a}}$	air density	kg m ⁻³	computed	computed as a function of air temperature, humidity and pressure in <code>atm_density</code>	
κ	von Karman's constant	-	0.41		
λ_v	latent heat of evaporation	J kg ⁻¹	2.453×10 ⁶		
λ_f	Latent heat of fusion	J kg ⁻¹	3.340×10 ⁵		
λ_{snow}	coefficient controlling the rate of densification of snow following rainfall	-	computed	$\lambda_{snow} = *R_F c_{seday} / R_{snow}$	adapted from Rogers et al. (1995)
Λ	dimensionless variable associated with light penetration through ice required for heat conduction calculation	-	computed		
θ_v	virtual temperature of the atmospheric boundary layer above the lake	K	computed		
θ_a	temperature of the atmospheric boundary layer above the lake	K	computed	$\theta_a = f_{AT} T_x + 273.15$	
θ_s	temperature of the atmosphere at the lake surface	K	variable	$\theta_s = T_s + 273.15$	
θ_*	temperature scale	K	computed		
ρ_a	air density	kg m ⁻³	computed	computed as a function of air temperature, humidity and pressure in <code>atm_density</code>	TVA (1972)
ρ_o	density of saturated air at the water surface temperature	kg m ⁻³	computed		
ρ_i	density of the i^{th} layer	kg m ⁻³	variable	compute for each layer based on temperature and salinity, using TEOS-10 or UNESCO (1981);	TEOS-10: teos-10.org UNESCO (1981)



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Symbol	Description	Units	Value	Comments	Reference
				set density_model in &glm_setup	
ρ_s	density of the surface water layer ($i=N_{LEF}$)	kg m ⁻³	variable		
ρ_w	reference water density	kg m ⁻³	1000		
ρ_{sml}	mean density of the mixed layer	kg m ⁻³	variable		
ρ_{ref}	average of layer densities over which reduced gravity is being computed	kg m ⁻³	computed		
$\rho_{ice,snow}$	density of the snow or ice	kg m ⁻³	selected		
ρ_{white}	density of snow ice	kg m ⁻³	890		
ρ_{blue}	density of blue ice	kg m ⁻³	917		
ρ_{snow}	density of snow	kg m ⁻³	variable		
$\rho_{s,min}$	assigned minimum snow density	kg m ⁻³	50	set in &snowice	
$\rho_{s,max}$	assigned maximum snow density	kg m ⁻³	300	set in &snowice	
ρ_{snow*}	intermediate snow density estimate	kg m ⁻³	computed	see Figure 6	
ρ_{outf}	density of the lake layer corresponding to the height of withdrawal, i_{outf}	kg m ⁻³	computed		
ρ_{ij}	density of the lake layer, i , which is at an equivalent depth to inflow parcel j	kg m ⁻³	computed		
ρ_{inf}	density of inflowing water as it enters the lake	kg m ⁻³	computed		
ρ_{ins_j}	density of inflowing water parcel at the j th increment during its transit	kg m ⁻³	computed		
ρ_{ins_l}	density of the inflow parcel associated with inflow l when it inserted	kg m ⁻³	computed		
ρ_{ins_l}	density of the lake layer, l , where the inflow l inserted	kg m ⁻³	computed		
σ	Stefan-Boltzmann constant	W m⁻² K⁻⁴	5.67×10⁻⁸		
τ_i	total shear stress experienced at the lake bed portion of layer i	N m ⁻²	computed	Eq. 8576	
ϑ_s	dimensionless moisture content of air at water's surface	-	computed	$\vartheta_s = \kappa e_s/p$	TVA (1972)
ϑ_a	dimensionless moisture content of the air above the lake	-	computed	$\vartheta_a = \kappa e_a/p$	
ν_a	kinematic viscosity of air	m ² s ⁻¹	1.52×10 ⁻⁵	reported as 0.0548 m ² hr ⁻¹	
ν_w	kinematic viscosity of water	m ² s ⁻¹	1.14×10 ⁻⁶		
ω	ratio of molecular weight of water to molecular weight of air	-	0.622		
ψ_M	similarity function for momentum in the air above the lake	-	computed	Eq. A30	
ψ_E	similarity function for moisture in the air above the lake	-	computed	Eq. A30	
ψ_H	similarity function for heat in the air above the lake	-	computed	Eq. A30	
ξ	dimensionless parameter used for wave period calculation	-	computed	Eq. 8071	
ζ	dimensionless parameter used for wave period calculation	-	computed	Eq. 8374	
ς	constant related to percentage of atmospheric diffuse radiation	%	6		Yajima and Yamamoto (2015)

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[* Either a numeric value for fixed constants or descriptors of the source of the value are provided. Descriptors include index, computed, configurable \(default\), variable, selected or time-series input, with supporting information in the comment column.](#)

5

Appendix A: Bird solar radiation model

The Bird Clear Sky Model (BCSM) was developed by (Bird, 1984) to predict clear-sky direct beam, hemispherical diffuse, and total hemispherical broadband solar radiation on a horizontal surface. Average solar radiation is computed at the model time-step (e.g., hourly) based on ten user specified input parameters (Table A1).

Table A1: Parameters required for the BCSM model.

Variable	Description	Example values (e.g., Liu et al., 2016)
Lat	Latitude (degrees, + for N)	-31.77
Long	Longitude (degrees + for E)	116.03
TZ	Time Zone indicated by number of hours from GMT	+7.5
AP	Atmospheric Pressure (millibars)	1013
O ₃	Ozone Cone. (atm-cm)	0.279–0.324
W	Total Precipitable Water Vapour (atm-cm)	1.1–2.2
AOD ₅₀₀	Aerosol Optical Depth at 500 nm	0.033–0.1
AOD ₃₈₀	Aerosol Optical Depth at 380 nm	0.038–0.15
α _{sur}	Surface albedo	0.2

The solar constant in the model is taken as 1367 W m⁻², which is corrected due to the elliptical nature of the Earth's orbit and consequent change in distance to the sun. This calculation gives us the Extra-Terrestrial Radiation ($\hat{\Phi}_{ETR}$), at the top of the atmosphere:

$$\hat{\Phi}_{ETR} = 1367 \left(1.00011 + 0.034221 \cos(\Phi_{day}) + 0.00128 \sin(\Phi_{day}) + 0.000719 \cos(2\Phi_{day}) \right) \quad A1$$

where the day angle, Φ_{day} , is computed using, d , the day number:

$$\Phi_{day} = 2\pi \left(\frac{d-1}{365} \right) \quad A2$$

The solar declination, Φ_{dec} (radians), is computed from:

$$\Phi_{dec} = \left[\begin{array}{l} 0.006918 - 0.399912 \cos(\Phi_{day}) + 0.070257 \sin(\Phi_{day}) - 0.006758 \cos(2(\Phi_{day})) \\ + 0.000907 \sin(2\Phi_{day}) - 0.002697 \cos(3(\Phi_{day})) + 0.00148 \sin(3(\Phi_{day})) \end{array} \right] \quad A3$$

We then solve the equation of time:

$$EQT = \left[\begin{array}{l} 0.0000075 + 0.001868 \cos(\Phi_{day}) - 0.032077 \sin(\Phi_{day}) \\ -0.014615 \cos(2(\Phi_{day})) - 0.040849 \sin(2(\Phi_{day})) \end{array} \right] \times 229.18 \quad A4$$

in order to compute the hour angle, Φ_{hr} , calculated with noon zero and morning positive as:

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$$\Phi_{hr} = 15(hr - 12.5) + Long - 15 TZ + \left(\frac{EQT}{4}\right) \quad A5$$

where TZ is the time-zone shift from GMT. The zenith angle, Φ_{zen} (radians), is calculated from:

$$\cos(\Phi_{zen}) = \cos(\Phi_{dec})\cos(\Phi_{hr})\cos(Lat) + \sin(\Phi_{dec})\sin(Lat) \quad A6$$

When Φ_{zen} is less than 90° , the air mass factor is calculated as:

$$AM = \left[\cos(\Phi_{zen}) + \frac{0.15}{(93.885 - \Phi_{zen})^{1.25}} \right]^{-1} \quad A7$$

which is corrected for atmospheric pressure, p (hPa),

$$AM_p = \frac{AM p}{101.3} \quad A8$$

5 AM_p is then used to calculate the Rayleigh Scattering as:

$$T_{rayleigh} = e^{[-0.0903 AM_p^{0.84} + (1 + AM_p - AM_p^{1.01})]} \quad A9$$

The effect of ozone scattering is calculated by computing ozone mass, which for positive air mass is:

$$T_{ozone} = \left[1 - \left(0.1611 (Oz AM) (1 + 139.48 (Oz AM))^{-0.3035} \right) - \frac{0.002715 (Oz AM)}{1 + 0.044 (Oz AM) + 0.0003 (Oz AM)^2} \right] \quad A10$$

The scattering due to mixed gases for positive air mass is calculated as:

$$T_{mix} = e^{[-0.0127 AM_p^{0.26}]} \quad A11$$

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Then the water scattering is calculated by getting the water mass:

$$Wm = W AM_p \quad A12$$

where W is the precipitable water vapour. This can be approximated from dew point temperature, e.g.:

$$\ln W = a T_d + b \quad A13$$

where a and b are regression coefficients which have been taken as 0.09, 0.07, 0.07 and 0.08 for values of a , while b is 1.88, 2.11, 2.12 and 2.01 in spring, summer, autumn and winter (Luo et al., 2010).

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Then the water scattering effect is calculated as:

$$T_{watvapwater} = \left[1 - \frac{(2.4959 Wm)}{1 + (79.034 Wm)^{0.6828} + 6.385 Wm} \right] \quad A14$$

The scattering due to aerosols requires the Aerosol Optical Depth at 380 nm and 500 nm:

$$TauA = 0.2758 AOD_{380} + 0.35 AOD_{500} \quad A15$$

and the scattering due to aerosols is then calculated as:

$$T_{aerosol} = e^{(-TauA)^{0.873} (1 + TauA - TauA^{0.7088}) AM^{0.9108}} \quad A16$$

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We also define:

$$T_{aa} = 1 - [0.1 (1 - AM + AM^{1.06}) (1 - T_{aerosol})] \quad A17$$

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and:

$$\frac{0.5(1 - T_{rayleigh}) + 0.84(1 - T_{aerol})}{1 - AM + AM^{1.02}} \quad \text{A18}$$

where the 0.84 value used is actually the proportion of scattered radiation reflected in the same direction as incoming radiation.

5

The direct beam radiation on a horizontal surface at ground level on a clear day is given by,

$$\hat{\phi}_{DB} = 0.9662 \hat{\phi}_{ETR} T_{rayleigh} T_{ozone} T_{mix} T_{watvap} T_{aerosol} \cos(\Phi_{zen}) \quad \text{A19}$$

$$\hat{\phi}_{AS} = 0.79 \hat{\phi}_{ETR} T_{ozone} T_{mix} T_{watvap} T_{aa} \cos(\Phi_{zen}) \quad \text{A20}$$

The total irradiance hitting the surface is therefore (W m^{-2}):

$$\hat{\phi}_{SW} = \frac{\hat{\phi}_{DB} + \hat{\phi}_{AS}}{1 - (\alpha_{SW} \alpha_{SKY})} \quad \text{A21}$$

The albedo is computed for the sky as:

$$\alpha_{SKY} = 0.068 + (1 - 0.84) \left(1 - \frac{T_{aerosol}}{T_{aa}}\right) \quad \text{A22}$$

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Appendix B: Non-neutral bulk transfer coefficients

The iterative procedure used in this analysis to update correct the bulk-transfer coefficients based on atmospheric conditions is conceptually similar to the methodology discussed in detail in Launiainen and Vihma (1990). The first estimate for the neutral drag coefficient, C_{DN} , is specified as a function of wind speed as it is commonly observed to increase with U_{10} . This is modelled by first estimating the value referenced to 10m height above the water from:

$$C_{DN-10} = \begin{cases} 0.001 & U_{10} \leq 5 \\ 0.001 (1 + 0.07[U_{10} - 5]) & U_{10} > 5 \end{cases} \quad \text{Option 1 : Francey and Garratt (1978), Hicks (1972)} \quad \text{A23}$$

$$C_{DN-10} = 1.92 \times 10^{-7} U_{10}^3 + 0.00096 \quad \text{Option 2 : Babanin and Makin (2008)}$$

and then computing the Charnock formula with the smooth flow transition (e.g., Vickers et al., 2013):

$$z_o = \frac{a u_*^2}{g} + 0.11 \frac{v_a}{u_*} \quad \text{A24}$$

where a is the Charnock constant, u_* is the approximated friction velocity ($\sqrt{C_{DN-10} U_{10}^2}$) using Eq. A23. The drag is re-computed using:

$$C_{DN-10} = \left[\frac{\kappa}{\ln\left(\frac{10}{z_o}\right)} \right]^2 \quad \text{A25}$$

where κ is the von Karman constant (Figure A1). Note the neutral humidity/temperature coefficient, C_{HWN-10} , is held constant at the user defined C_H value and is assumed not to vary with wind speed.

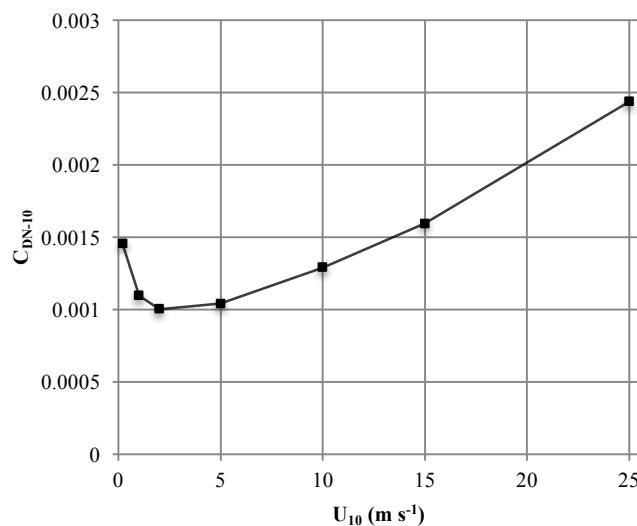


Figure A1: Scaling of the 10-m neutral drag coefficient with wind speed, U_{10} (Eqns A23-25)

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Under non-neutral conditions in the atmospheric boundary layer, the transfer coefficients vary due to stratification in the air column, as was parameterised by Monin and Obukhov (1954) using the now well-known stability parameter, z/L , where L is the Obukhov length defined as:

$$L = \frac{-\rho_a u_*^3 \theta_v}{\kappa g \left(\frac{\phi_H}{c_a} + 0.61 \frac{\theta_a \phi_E}{\lambda_v} \right)} \quad \text{A26}$$

where $\theta_v = \theta_a(1 + 0.61e_a)$ is the virtual air temperature and ϕ_H and ϕ_E are the bulk fluxes. Paulson (1970) presented a solution for the vertical profiles of wind speed, temperature and moisture in the developing boundary layer as a function of the Monin-Obukhov stability parameter; the so-called flux-profile relationships:

$$\begin{aligned} U_z &= \frac{u_*}{\kappa} \left[\ln \left(\frac{z}{z_o} \right) - \psi_M \left(\frac{z}{L} \right) \right] & \text{A27a-c} \\ \theta_a - \theta_s &= \frac{\theta_*}{\kappa} \left[\ln \left(\frac{z}{z_\theta} \right) - \psi_H \left(\frac{z}{L} \right) \right] \\ e_a - e_s &= \frac{e_*}{\kappa} \left[\ln \left(\frac{z}{z_e} \right) - \psi_E \left(\frac{z}{L} \right) \right] \end{aligned}$$

where ψ_M , ψ_H and ψ_E are the similarity functions for momentum, heat and moisture respectively, and z_o , z_θ and z_e are their respective roughness lengths. For unstable conditions ($L < 0$), the stability functions are defined as (Paulson 1970; Businger et al., 1971; Dyer, 1974):

$$\psi_M = 2 \ln \left(\frac{1+x}{2} \right) + \ln \left(\frac{1+x^2}{2} \right) - 2 \tan^{-1} x + \frac{\pi}{2} \quad \text{A28a}$$

$$\psi_E = \psi_H = 2 \ln \left(\frac{1+x^2}{2} \right) \quad \text{A28b}$$

where

$$x = \left[1 - 16 \left(\frac{z}{L} \right)^{1/4} \right] \quad \text{A29}$$

During stable stratification ($L > 0$) they take the form:

$$\psi_M = \psi_E = \psi_H = \begin{cases} -5 \left(\frac{z}{L} \right) & 0 < \frac{z}{L} < 0.5 \\ 0.5 \left(\frac{z}{L} \right)^{-2} - 4.25 \left(\frac{z}{L} \right)^{-1} - 7 \left(\frac{z}{L} \right) - 0.852 & 0.5 < \frac{z}{L} < 10 \\ \ln \left(\frac{z}{L} \right) - 0.76 \left(\frac{z}{L} \right) - 12.093 & \frac{z}{L} > 10 \end{cases} \quad \text{A30}$$

Substituting Eqns. 20-21 into (A27) and ignoring the similarity functions leaves us with neutral transfer coefficients as a function of the roughness lengths:

$$C_{XN} = \kappa^2 \left[\ln \left(\frac{z}{z_o} \right) \right]^{-1} \left[\ln \left(\frac{z}{z_X} \right) \right]^{-1} \quad \text{A31}$$

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where the N sub-script denotes the neutral value and X signifies either D , H or E for the transfer coefficient and o , θ or e for the roughness length scale. Inclusion of the stability functions into the substitution and some manipulation (Imberger and Patterson, 1990; Launianen and Vihma, 1990) yields the transfer coefficients relative to these neutral values:

$$\frac{C_X}{C_{XN}} = \left[1 + \frac{C_{XN}}{\kappa^2} \left(\psi_M \psi_X - \frac{\kappa \psi_X}{\sqrt{C_{DN}}} - \frac{\kappa \psi_M \sqrt{C_{DN}}}{C_{XN}} \right) \right] \quad \text{A32}$$

5

Hicks (1975) and Launianen and Vihma (1990) suggested an iterative procedure to solve for the stability corrected transfer coefficient using (A32) based on some initial estimate of the neutral values (as input by the user). The surface flux is subsequently estimated according to Eqns. 20-21 and used to provide an initial estimate for L (Eq. A26). The partially corrected transfer coefficient is then recalculated and so the cycle goes. Strub and Powell (1987) and Launianen (1995),
 10 presented an alternative based on estimation of the bulk Richardson number, Ri_B , defined as:

$$Ri_B = \frac{gz}{\theta_v} \left(\frac{\Delta\theta + 0.61 \theta_v \Delta e}{U_z^2} \right) \quad \text{A33}$$

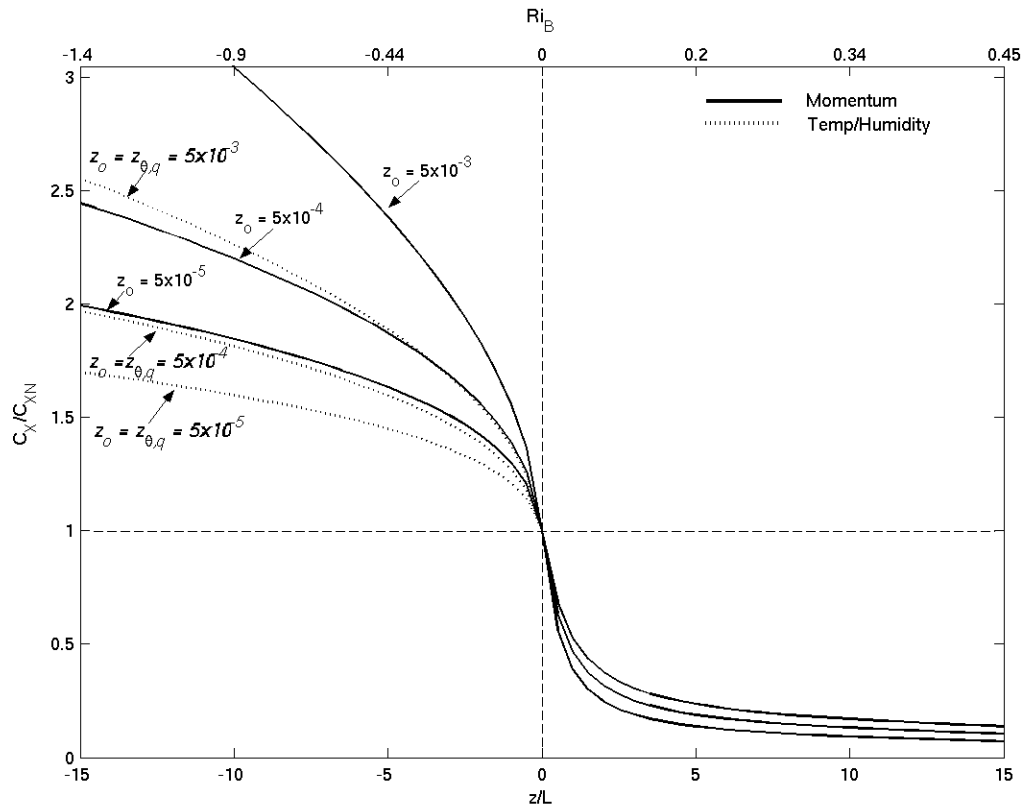
and related as a function of the stability parameter, z/L , according to:

$$Ri_B = \frac{z}{L} \left(\frac{\kappa \sqrt{C_{DN}} / C_{HEN} - \psi_{H,E}}{[\kappa / \sqrt{C_{DN}} - \psi_M]^2} \right) \quad \text{A34}$$

where it is specified that $C_{HN} = C_{EN} = C_{HEN}$. Figure A2 illustrates the relationship between the degree of atmospheric stratification (as described by both the bulk Richardson number and the Monin-Obukhov stability parameter) and the transfer coefficients scaled by their neutral value.



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5 **Figure A2: Relationship between atmospheric stability (bottom axis – z/L , top axis – Ri_B) and the bulk-transfer coefficients relative to their neutral value (C_X/C_{XN} where X represents D , H or E) for several roughness values (computed from Eq. A32). The solid line indicates the momentum coefficient variation (C_D/C_{DN}) and the broken line indicates humidity and temperature coefficient (C_{HE}/C_{HEN}) variation.**