



1 **Global Sensitivity Analysis of Parameter Uncertainty in Landscape Evolution Models**

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10

11 **Abstract**

12

13 Landscape Evolution Models have a long history of use as exploratory models, providing greater
14 understanding of the role large scale processes have on the long-term development of the Earth's
15 surface. As computational power has advanced so has the development and sophistication of these
16 models. This has seen them applied at increasingly smaller scale and shorter-term simulations at
17 greater detail. However, this has not gone hand-in-hand with more rigorous verifications that are
18 commonplace in the applications of other types of environmental models- for example Sensitivity
19 Analyses.

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21 This can be attributed to a paucity of data and methods available in order to calibrate, validate and
22 verify the models, and also to the extra complexity Landscape Evolution Models represent - without
23 these it is not possible to produce a reliable Objective Function against which model performance can
24 be judged. To overcome this deficiency, we present a set of Model Functions - each representing an
25 aspect of model behaviour - and use these to assess the relative sensitivity of a Landscape Evolution
26 Model (CAESAR-Lisflood) to a large set of parameters via a global Sensitivity Analysis using the Morris



27 Method. This novel combination of behavioural Model Functions and the Morris Method provides
28 insight into which parameters are the greatest source of uncertainty in the model, and which have the
29 greatest influence over different model behaviours. The method was repeated over two different
30 catchments, showing that across both catchments and across most model behaviours the choice of
31 Sediment Transport formula was the dominate source of uncertainty in the CAESAR-Lisflood model,
32 although there were some differences between the two catchments. Crucially, different parameters
33 influenced the model behaviours in different ways, with Model Functions related to internal
34 geomorphic changes responding in different ways to those related to sediment yields from the
35 catchment outlet.

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37 This method of behavioural sensitivity analysis provides a useful method of assessing the performance
38 of Landscape Evolution Models in the absence of data and methods for an Objective Function
39 approach.

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41 **1. Introduction**

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43 Landscape Evolution Models (LEMs) investigate how the Earth's surface evolves over timescales
44 ranging from hundreds to millions of years (Coulthard and Van De Wiel, 2012; Martin and Church,
45 2004; Pazzaglia, 2003; Tucker and Hancock, 2010; Van De Wiel et al., 2011). They represent the earth's
46 surface with a regular or irregular mesh and simulate how the surface evolves over time as a function
47 of tectonic processes, and erosion and deposition from fluvial, glacial, aeolian and hillslope processes.
48 LEMs have proved to be very useful scientific tools to understand how Earth surface processes interact
49 to shape the landscape.

50 More recently, LEMs have improved considerably in their ability to simulate the physical environment,
51 and this has developed in parallel with improvements in computational efficiency and power. This
52 allows LEMs to go beyond highly simplified models of landform development but to also incorporate



53 increasingly complex processes such as pedogenesis (Vanwalleghem et al., 2013; Welivitiya et al.,
54 2016) and periglacial processes (Andersen et al., 2015; Egholm et al., 2015). Other processes are now
55 being handled in more detail such as hydrodynamic flow models and aeolian processes (Adams et al.,
56 2017; Coulthard et al., 2013; Liu and Coulthard, 2017). These developments led to Coulthard et al.
57 (2013) describing them as ‘second generation’ LEMs that extend previously explanatory and
58 explorative models to be used for prediction of future changes in landscapes, such as for the mining
59 industry (e.g. Hancock et al., 2017; Saynor et al., 2012).

60 However, more detailed physical representations of the processes that shape the Earth’s surface
61 involve a larger number of parameters that are typically not legitimated by theories but must be
62 determined from empirical data or are incompletely known (Oreskes et al., 1994; Petersen, 2012). If
63 LEMs are to be operationally used for prediction or as decision-making tools in the future, their
64 outputs must be evaluated against the uncertainty in input parameters – a task that is increasingly
65 difficult for a large number of parameters. Sensitivity analysis (SA) investigates how variations in the
66 output of a numerical model can be attributed to its input factors (Pianosi et al., 2016), but has rarely
67 been conducted for LEMs. The aim of this study is thus to conduct a SA of the widely used and highly
68 parameterized LEM CAESAR-Lisflood (Coulthard et al., 2013) - in particular, we wish to be able to
69 detect the parameters that have the greatest influence on the model. As model sensitivity may be
70 influenced by different landscapes, we run the SA in two individual and distinct catchments.

71

72 ***1.1 Sensitivity Analysis and Landscape Evolution Models***

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74 The application of SA in environmental modelling has a history spanning four decades (Norton, 2008)
75 and forms an important component of using models for decision-making, including model
76 development, calibration and uncertainty analysis (Yang, 2011). SA addresses five key questions
77 (Cariboni et al., 2007; Neumann, 2012; Song et al., 2012, 2015):



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1. Which parameters have the greatest influence on the model?

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2. If additional data could be used to reduce the uncertainty in a parameter, which would most reduce the model output variance?

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3. Are there parameters with such low influence that their values could be fixed without impact on the model outputs?

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4. If parameter values emerge as incorrect, how will they influence model outputs?

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5. Which parameters influence model outputs in different regions (parameter space)?

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Clearly, based on the above, an appraisal of model sensitivity is important to fully understand and apply model results. In a review of applications of SA in environmental models, Yang (2011) identified two common approaches to SA – local and global. Local SA are limited, considering only the impacts of factors on model outputs locally, whilst global SA typically utilise Monte-Carlo methods to assess the sensitivity of impacts across the whole parameter space (Yang, 2011). For complex models with non-linear behaviours, the use of Local SA can be highly biased as they neglect the non-linear interactions between parameters (Oakley and O’Hagan, 2004; Pappenberger et al., 2006; Yang, 2011). Global SA are more computationally expensive, but as the methods are more reliable, they are attractive to modellers (Yang, 2011).

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However, for LEMs there are surprisingly few examples of SA being carried out. This can be explained by three inter-related issues: (i) LEMs typically have a large number of model parameters; (ii) long model run times can make multiple simulations for SA impractical; and (iii) model behaviour can be highly non-linear (e.g. Coulthard and Van De Wiel, 2007; Larsen et al., 2014; Van De Wiel and Coulthard, 2010), leading to potentially complex SA interpretations. Large numbers of model parameters and long run times, in particular, make Monte-Carlo methods extremely time consuming – and therefore often unviable.

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105 There are several past studies investigating how LEMs respond to process changes and model
106 parameters, including changes in climate variability and precipitation resolution (Armitage et al., 2017;
107 Coulthard and Skinner, 2016a; Ijjasz-Vasquez et al., 1992; Tucker and Bras, 2000), channel widths
108 (Attal et al., 2008), vegetation (Collins, 2004; Istanbuluoglu and Bras, 2005), and variations in initial
109 conditions (Hancock, 2006; Hancock et al., 2016; Ijjasz-Vasquez et al., 1992; Willgoose et al., 2013).
110 Yet few studies explicitly perform SA and most of the applications described above are exploring LEM
111 sensitivity to processes, or changes in environmental conditions, and are more correctly referred to
112 as exploratory tests (Larsen et al., 2014). On the other hand, investigations to ascertain the model's
113 response to potential uncertainties (e.g from model parameterisation) can be deemed as true SA (eg,
114 Armitage et al., 2017; Coulthard and Skinner, 2016a; Hancock et al., 2016).

115

116 The study by Ziliani et al. (2013) is another example of a LEM SA, seeking to spatially calibrate a reach-
117 scale application of the CAESAR LEM to field observations. They performed a two-stage SA, utilising
118 the Morris Method (MM) (as adapted by Campolongo et al., 2007) as a pre-screening before a more
119 complex local SA was applied. The study investigated the model's sensitivity to 12 user-defined
120 parameters, using MM to exclude those showing the least influence on performance measures from
121 the subsequent SA and calibration. Whilst Ziliani et al. (2013) demonstrated the feasibility of applying
122 MM as a global SA to a reach-scale LEM, it was applied as a pre-screening stage to identify parameters
123 to focus model calibration on, and not to observe model behaviour.

124

125 ***1.2 Metrics for Landscape Evolution Model Assessment***

126

127 An issue with the testing of LEMs is finding the field data and statistical tools that can actively
128 discriminate between what is a good model and a bad model, and for parameterisation (Hancock and
129 Willgoose, 2001; Hancock et al., 2016; Tucker and Hancock, 2010). As the models are designed to



130 assess both short (annual to decadal) to long-term (geological time scale), the data and assessment
131 methods require both a multi-dimensional approach. The application of SA to environmental models
132 often assesses the impacts of factors based on variations in values of an objective function, which is
133 often an error score between observed and simulated values – for example, a common approach in
134 hydrology would to use the Nash-Sutcliffe score (Nash and Sutcliffe, 1970) as an objective function,
135 and catchment discharges as a value. The objective function approach was used by Ziliani et al. (2013),
136 matching the outputs of a reach simulation in CAESAR to observed patterns of wet/dry pixels,
137 erosion/deposition, and vegetation. However, the objective function approach is generally not
138 practical for LEMs due to a paucity of observed data to use as a value, so often the results from LEMs
139 are assessed qualitatively, relying on visual interpretation of the final simulated landforms or cross-
140 section profiles (eg. Hancock et al., 2010; 2015; Hancock and Coulthard, 2012; Coulthard and Skinner,
141 2016a).

142

143 The use of catchment outlet statistics, such as sediment yield time series, allow for comparison
144 between simulations to indicate a catchment's response to perturbations (e.g. Coulthard et al., 2012;
145 Coulthard and Skinner, 2016b; Hancock and Coulthard, 2012). However, although this provides some
146 information about the catchment response as it gives an incomplete picture. Coulthard and Skinner
147 (2016b) showed that simulations calibrated to provide equivalent sediment yields, to compensate for
148 loss of spatial and temporal resolution in rainfall inputs, produced different landscape shapes.
149 Statistics based on measurements from the catchment outlet cannot account for factors such as
150 geomorphic equifinality, self-organised criticality, and autogenics, which act as a non-linear filter on
151 the response (Coulthard and Van De Wiel, 2007, 2013; Hancock et al., 2016; Jerolmack and Paola,
152 2010; Van De Wiel and Coulthard, 2010).

153

154 Hancock and Willgoose (2001) reviewed statistical attempts to define catchment geomorphology,
155 including width function, cumulative area distribution, area-slope relationship, and hypsometric



156 curve, and used these as an objective function between physical experiments and numerical
157 experiments using SIBERIA. However, although statistically similar, there were visually clear
158 differences between the physical models and the simulations. Other methods employed include
159 changes to mean elevations (Hancock et al., 2010, 2011), and Optimal Channel Network (Ibbitt et al.,
160 1999). However, although visual difference may be observed between simulations, variations within
161 these measurements have proved to be small for timescales of 1000 years and less (Hancock et al.,
162 2010, 2011), so are limited in their scalability. There is, therefore, a clear need for more objective
163 statistical methods for critically evaluating and comparing landscapes that can also be used for
164 evaluating the accuracy/reliability (or otherwise) of LEMs. Field data at the catchment scale that
165 includes erosion and deposition data, vegetation type and change as well as sediment transfer at
166 critical points along the stream network is required. Such all-encompassing catchment scale data is
167 currently not available.

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169 ***1.3 A Global SA for a catchment LEM***

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171 This study demonstrates the first application of a Global SA to a catchment LEM (CAESAR-Lisflood),
172 using MM to assess the model's sensitivity to user-defined parameters – in total 15 parameters are
173 selected based on known importance to the model or because the model's response to the parameter
174 is presently poorly understood. Although not all the parameters chosen are universal between LEMs,
175 many LEMs have equivalents. A set of 15 model functions has been developed which reflects core
176 behavioural responses of the model, and these will indicate whether the same parameters influence
177 all behaviours, or whether the different behaviours respond to different parameters. The method is
178 applied to two contrasting catchments (scale, environment and climate) to assess how transferable
179 an individual SA is to different conditions.

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181



182 **2. Methods**

183

184 The test applies the MM method to perform a global SA on the CAESAR-Lisflood model for two
185 contrasting catchments – the Upper Swale, UK (medium sized, temperate, perennial), and Tin Camp
186 Creek, Australia (small sized, tropical, ephemeral). For each catchment, 15 user-defined parameters
187 are assessed against a set of 15 model functions. Finally, the changes in elevations across the
188 catchments are assessed.

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190 **2.1 CAESAR-Lisflood**

191

192 The LEM used is the CAESAR-Lisflood model (Coulthard et al., 2013). CAESAR-Lisflood is a second
193 generation LEM, capable of simulations with greater physical realism than first generation models but
194 also with increased complexity – the model features a large number of fixed, physically-based, or user-
195 defined parameters. This additional complexity may result in an increased non-linearity and sensitivity
196 to model parameters.

197

198 A full description of the CAESAR-Lisflood model can be found in Coulthard et al. (2013), and its core
199 functionality is only summarised here. The model utilises an initial DEM built from a regular grid of
200 cells, and in the catchment mode (as used in this model set up) is driven by a rainfall timeseries
201 (Coulthard and Skinner, 2016b). At each timestep the rainfall input is converted to surface runoff using
202 a version of TOPMODEL (Beven and Kirkby, 1979), and distributed across the catchment and routed
203 using the Lisflood-FP component (Bates et al., 2010). The Lisflood-FP component generates flow
204 depths and velocities, which are used by the CAESAR component to simulate fluvial erosion, transport
205 and deposition, across 9 grain sizes, using an active layer system, and altering the elevation values of
206 the grid (Van De Wiel et al., 2007).

207



208 CAESAR-Lisflood is freely available and since 1996 there have been 62 published studies using the
209 model over a wide range of temporal and spatial scales (Skinner and Coulthard, 2017). These previous
210 studies provide useful background into model parameter interactions helping to inform the choice of
211 the user-defined parameters used for the SA as described in Section 2.4. Some studies have also
212 investigated the model's sensitivities to external factors - for example, Coulthard and Skinner (2016)
213 investigated the sensitivity of the CAESAR-Lisflood model to the spatial and temporal resolution of
214 precipitation. Other studies have investigated the influence of processes which could be described as
215 both SA and an exploratory test with, for example, Coulthard and Van De Wiel (2017) examining how
216 the use of a spatially variable 'm' parameter, representing the land use of an area, could influence the
217 outputs of the model.

218

219 **2.2 Morris Method**

220

221 Hydrological models faced similar issues to LEMs in the past, in regards to model complexity and
222 resulting processing times when applying SA. To overcome them, hydrologists have used the method
223 of Morris (1991). The MM can be regarded as a global SA, although it actually performs multiple local
224 SA sampled from across the full parameter space – this produces a series of local evaluations, the
225 mean of which is an approximation of the global variance (Saltelli et al., 2000; van Griensven et al.,
226 2006; Norton, 2009). The main strength of the MM is its computational efficiency. Herman et al. (2013)
227 showed that the MM could estimate similar variance in model outputs to the Sobol' Variance-based
228 global SA method (Sobol', 2001), yet required 300 times less evaluations, and significant less data
229 storage for an application to a distributed catchment hydrological model. The robustness of this
230 approach has been further shown by numerous workers (e.g. Brockmann and Morgenroth, 2007;
231 Pappenberger et al., 2008; Yang, 2011). However, the MM cannot provide a full quantitative
232 assessment of parameter sensitivity and is dependent upon the user-defined bounds to the parameter
233 space. It can successfully rank parameters between the least and most influential to model outputs,



234 but cannot determine parameters' exact relative influence (Brockmann and Morgenroth, 2007). This
 235 combination of advantage and limitation has seen it used extensively as a pre-screening stage,
 236 isolating the most influential parameters for further SA with quantitative, yet more computationally
 237 expensive, methods (e.g. Ratto et al., 2007; Song et al., 2015; Yang, 2011; Ziliani et al., 2013).

238

239 This paper uses the MM described in Ziliani et al. (2013), i.e. the original MM of Morris (1991), as
 240 extended by Campolongo et al. (2007). The Design of Experiment (DOE) used the R Statistical
 241 Environment and the "sensitivity" software package (Pujol, 2009). A full description of the method can
 242 be found in these papers, but a summary is provided here.

243

244 MM operates as a series of local SA starting with a stochastically selected set of initial parameters
 245 drawn from the global parameter space. For each parameter, a defined boundary of available values
 246 is set and divided into a series of equal incremental steps - each parameter is subsequently altered
 247 one-at-a-time (OAT) by a number of incremental steps, until each parameter has been altered once.
 248 The change in the model output measures, or model factors, is observed between each test – these
 249 are the Elementary Effects (EE). This process is repeated a number of times and the mean and standard
 250 deviations of the EE for each parameter is calculated – the Main Effect (ME). The higher the mean ME
 251 for a parameter shows greater influence of that parameter on the factor, and a higher standard
 252 deviation indicates greater non-linear relationships with other parameters. The calculation of an EE
 253 can be summarised as in Equation 1 –

254

$$255 \quad d_{ij} = \left| \frac{y(x_1, x_2, \dots, x_{i-1}, x_i + \Delta_i, x_{i+1}, \dots, x_k) - y(x_1, x_2, \dots, x_{i-1}, x_i, x_{i+1}, \dots, x_k)}{\Delta_i} \right|$$

256

257 where, d_{ij} is the j th EE of the i th model output measure (eg, $i=1$ refers to Sediment Transport Formula,
 258 see Table 1), k is the number of parameters investigated (here 15), $y(x_1, x_2, \dots, x_k)$ is the value of the



259 model output measure, r is the number of repetitions (here $r = 100$), and Δ_i is the change in
260 incremental steps parameter i was altered by.

261

262 **2.3 Study Basins**

263

264 **2.3.1. Upper Swale, UK**

265

266 The Swale catchment, UK, is a medium sized basin (181 km²) with 500 m of elevation drop (Figure 1).

267 It has been used extensively in previous CAESAR/CAESAR-Lisflood applications (Coulthard et al., 2012;

268 Coulthard and Macklin, 2001; Coulthard and Skinner, 2016a; Coulthard and Van De Wiel, 2013). For

269 this SA, it represents a medium basin in a temperate climate. All simulations on the Swale are based

270 on a 50 m resolution DEM and 30 years in duration. Precipitation inputs are 10 years of NIMROD

271 composite RADAR rainfall estimates (Met Office, 2003) (1 h – 5 km resolution) repeated.

272

273 **2.3.2. Tin Camp Creek, Australia**

274

275 The Tin Camp Creek catchment is a small sub-catchment (0.5 km²) of the full Tin Camp Creek system

276 (Hancock et al., 2010; Hancock, 2006) (Figure 1). The basin has a 45 m of elevation drop and is in the

277 tropical region of the Northern Territory, Australia. Contrasting to the Swale, Tin Camp Creek is much

278 smaller and the region has pronounced wet and dry seasons, with short intense rainstorms a feature

279 of wet season precipitation. The DEM is at 10 m grid cell resolution, and like the Swale simulations are

280 30 years in length. The rainfall input is taken from observations from a single raingauge at Jabiru

281 Airport, providing a 1 h – lumped resolution timeseries for 23 years, which was looped to create the

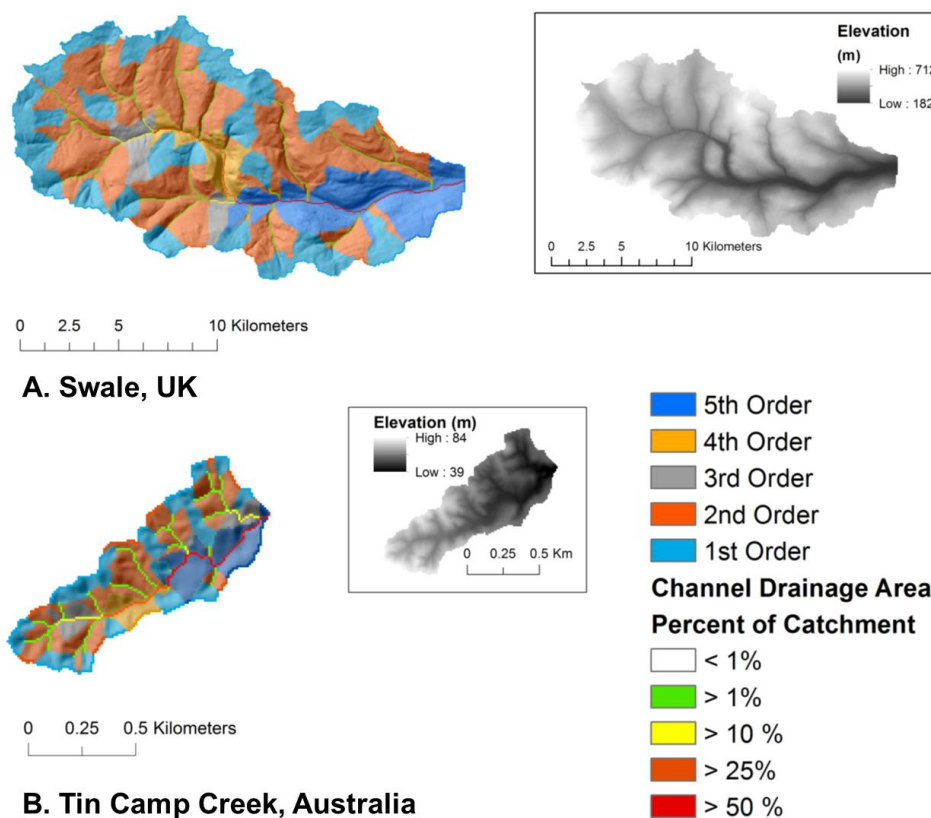
282 30 year record required.

283



284 For both basins the changes in the mean elevation across different areas of the catchment will be
 285 assessed as a representation of changes in the geomorphology. Each basin was sub-divided into
 286 regions corresponding to the watersheds of five stream orders based on the proportion of the
 287 catchment drained – 1st = < 1 %; 2nd = > 1 %; 3rd = > 10 %; 4th = > 25 %; 5th = > 50 % (see Figure 1).

288



289
 290 **Figure 1 – Elevation map for the Upper Swale catchment, UK (top), and Tin Camp Creek catchment, Australia**
 291 **(bottom). Each catchment is sub-divided into watersheds of five stream orders based on the proportion of the**
 292 **catchment drained.**

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 295



296 **2.4 User-Defined Parameters**

297

298 **Table 1 – User-defined parameters used and the min-max values for the two study catchments.**

Code	Parameter	Steps	Upper Swale	Tin Camp Creek
(1) SED	Sediment Transport Formula	2	1 Wilcock & Crowe / 2 Einstein	1 Wilcock & Crowe / 2 Einstein
(2) MEL	Max Erode Limit (m)	5	0.01; 0.015; 0.02; 0.025; 0.03	0.001; 0.0015; 0.002; 0.0025; 0.003
(3) CLR	In Channel Lateral Erosion Rate	5	10; 15; 20; 25; 30	10; 15; 20; 25; 30
(4) LAT	Lateral Erosion Rate	5	2.5e ⁻⁶ ; 3.75e ⁻⁶ ; 5e ⁻⁶ ; 6.25e ⁻⁶ ; 7.5e ⁻⁶	1.5e ⁻⁶ ; 2.25e ⁻⁶ ; 3e ⁻⁶ ; 3.75e ⁻⁶ ; 4.5e ⁻⁶
(5) VEG	Vegetation Critical Shear Stress (Pa)	5	10; 15; 20; 25; 30	2; 3.25; 4.5; 5.75; 7
(6) MAT	Grass Maturity Rate (yr)	5	0.5; 0.75; 1; 1.25; 1.5	0.5; 0.875; 1.25; 1.625; 2
(7) SCR	Soil Creep Rate (m/yr)	5	0.00125; 0.001875; 0.0025; 0.003125; 0.00375	0.00125; 0.001875; 0.0025; 0.003125; 0.00375
(8) SFT	Slope Failure Threshold (°)	5	40; 42.5; 45; 47.5; 50	40; 42.5; 45; 47.5; 50
(9) IOD	In/Out Difference (m ³ .s ⁻¹)	5	2.5; 3.75; 5; 6.25; 7.5	0.1; 0.175; 0.25; 0.325; 0.4
(10) MinQ	Min Q Value (m)	5	0.25; 0.375; 0.5; 0.625; 0.75	0.025; 0.0375; 0.05; 0.0625; 0.075
(11) MaxQ	Max Q Value (m)	5	2.5; 3.75; 5; 6.25; 7.5	2.5; 3.75; 5; 6.25; 7.5
(12) SEC	Slope for Edge Cells	5	0.0025; 0.00375; 0.005; 0.00625; 0.0075	0.0025; 0.00375; 0.005; 0.00625; 0.0075
(13) EVR	Evaporation Rate (m/d)	5	0.00067; 0.001005; 0.00134; 0.001675; 0.00201	0.0025; 0.004375; 0.00625; 0.008125; 0.01
(14) MNR	Manning's n Roughness	5	0.03; 0.035; 0.04; 0.045; 0.05	0.03; 0.0325; 0.035; 0.0375; 0.04
(15) GSS	Grain Size Set	5	Set 1; Set 2; Set 3; Set 4; Set 5	Set 1; Set 2; Set 3; Set 4; Set 5

299

300 The MM varies the value of each parameter tested once per repeat, and here we use 100 repeats.

301 Therefore, careful consideration was required in the selection of parameters as each parameter tested

302 added 100 model runs to the test – there are 49 user-defined parameters in the version of CAESAR-

303 Lisflood model used (v1.8), and even excluding parameters associated with dune and soil

304 development, there are still 35 user-defined parameters. To test each would require 3600 model runs

305 for each catchment, yet the inclusion of some parameters is likely to add little value. Therefore, in



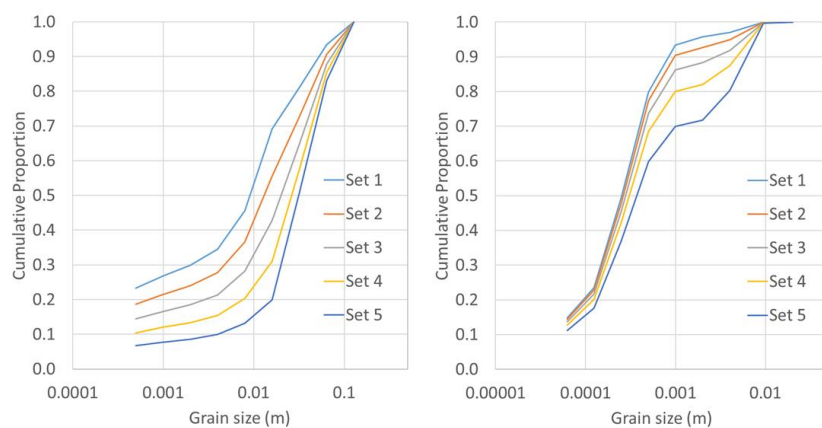
306 total, 15 user-defined parameters were tested (Table 1) and the selection was based on prior
307 knowledge of the importance of these parameters, or due to a lack of previous knowledge of the
308 influence of the parameters on the model – full justification of the selection of parameters can be
309 found in Supplement S1 of the Supplementary Material.

310

311 The Morris Method is a qualitative method and the results are subjective on the range of values and
312 number of iterative steps set by the user. Therefore, it is necessary to set each parameter's range to
313 be broadly equal to the others. Whilst it is difficult to define what this means it is also difficult to
314 estimate without prior knowledge - something this study is attempting to address. Here, as a general
315 rule, we have used a default value taken from past calibrations and varied this by +/- 25 % and +/- 50
316 %. There are some instances where this was not appropriate, and instead a minimum and maximum
317 bound was set instead, and 5 iterative steps of equal distance determined (for example, the Manning's
318 n Roughness for Tin Camp Creek).

319

320 The Sediment Transport Laws employed for SED were Einstein (Einstein, 1951) and Wilcock & Crowe
321 (Wilcock and Crowe, 2003). This was applied as a binary two-step, switching from one Law to the
322 other.



323

324 **Figure 2 – Sediment grain size distribution sets for the Upper Swale (left) and Tin Camp Creek (right),**
325 **showing the cumulative proportions.**

326

327 Grain size distribution has been shown to influence erosion patterns and erosion rate (Hancock and
328 Coulthard, 2012)). It is more difficult to define iterative steps for the sediment grain size sets which
329 include 9 different grain sizes and proportions in each. Instead, these were skewed by altering the
330 proportions of the five smallest grain sizes +/- 25 % and 50 %, and the opposite to the four largest
331 grain sizes, before adjusting the final proportions to equal one based on the relative values. This
332 produces two sets biased for smaller grain sizes (Sets 1 and 2), and two sets biased for larger grain
333 sizes (Sets 4 and 5), as well as the default grain size set (Set 3). The grain size distributions can be seen
334 in Figure 2.

335

336 **2.5 Model Functions**

337

338 The common method of assessing a model's sensitivity to parameters values via SA is to observe the
339 variations to objective function measures, yet as discussed in Section 1.3 the use of objective functions



340 is often not feasible or appropriate when simulating using LEMs. Also in Section 1.3, previous attempts
 341 to quantify changes to the geomorphology of catchments were discussed, showing that no statistical
 342 methods, whether based on catchment outlet or some feature of the landscape within the catchment,
 343 fully captured or reflected the geomorphic change. The methods reviewed in Hancock and Willgoose
 344 (2001) have also been shown to be of little value for simulations of 1000 years and less.

345

346 **Table 2 – Model Functions and the associated core behaviours.**

Model Function	Core Behaviour
Total Sediment Yield (m ³)	Catchment Sediment Yield
Mean Daily Sediment Yield (m ³)	
Peak Daily Sediment Yield (m ³)	
Time to Peak Sediment Yield (s)	
Days when Sediment Yield > Baseline (d)	
Total Net Erosion (m ³)	Internal Geomorphology
Total Net Deposition (m ³)	
Area with > 0.02 m Erosion (m ²)	
Area with > 0.02 m Deposition (m ²)	
Total Discharge (m ³)	Catchment Discharge
Mean Daily Discharge (m ³)	
Peak Daily Discharge (m ³)	
Time to Peak Discharge (s)	
Days when Discharge > Baseline (d)	
Total Model Iterations (calculations)	Model Efficiency

347

348 The method we have used is to abandon the objective function approach and instead assess the model
 349 against a series of Model Functions designed to reflect some of the core behaviours displayed in the
 350 model. It should be noted that this is a philosophical difference to traditional applications of SA – here
 351 we are not testing the model against its skill in simulating the physical environment, but rather how
 352 the model responds behaviourally to the uncertainty in the user-defined parameters detailed in
 353 Section 2.4 – in this sense it also differs from methods of assessing parameter uncertainty, such as the
 354 Generalised Likelihood Uncertainty Estimation (GLUE) of Beven and Binley (1992), yet is an important
 355 step towards the adoption of such techniques with LEMs. The 15 model functions (Table 2) are simple,
 356 scalable and transferable between different catchment types, and can be applied to simulations of



357 different timeframes. The model functions are based on outputs which are not unique to CAESAR-
358 Lisflood, so can be applied to other LEM and geomorphic models.

359

360 The ME of each parameter versus each model function was normalised based on the proportion of
361 the ME for highest ranking parameter for that model function – therefore the highest ranked
362 parameter for each model function always scored 1. The scores for each parameter were aggregated
363 for across all model functions based on the mean of the scores. The model functions were sub-divided
364 into core behaviour groups (Table 2), and the scores aggregated again for each core behaviour.

365 LEMs are subject to transient model behaviour (an internal model adjustment), as the model reacts
366 to effects of the initial DEM surface and the global grain size distribution. During the initial period of
367 model simulation this results in accelerated sediment processes as the model removes uneven
368 surfaces and noise, and easily mobilises smaller grain sizes in the channel. This is commonly accounted
369 for by allowing the model to run for a ‘spin-up’ period before the simulation begins. It is possible that
370 small differences in the model could be exaggerated during this period, therefore the first 10 years of
371 each simulation has been discounted for the calculation of the model functions.

372

373 **3. Results**

374

375 **3.1 All Model Functions**

376

377 Figure 3 shows the spread of parameter influence for both catchments, where the higher the mean of
378 the aggregated MEs indicates greater sensitivity in the model to that parameter, and the higher
379 standard deviation shows greater non-linearity to other parameters. Table 3 shows the parameters
380 ranked for both catchments, based on the aggregated mean ME values. The most influential
381 parameter is SED (see Table 1 for full description of parameter abbreviations), ranked top for both and
382 also being most influential by a reasonable margin, having an aggregated mean of at least 0.2 higher



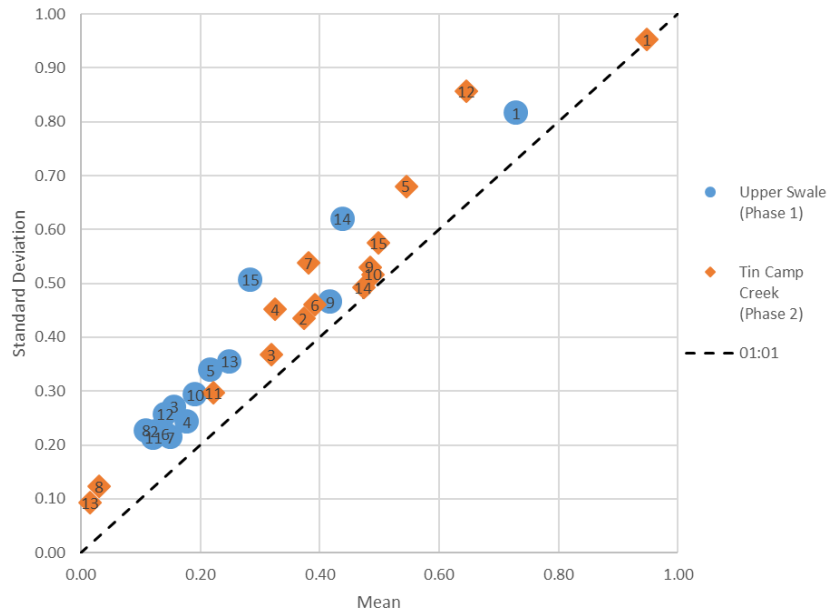
383 than the 2nd ranked parameter. Other parameters, such as VEG, IOD, MNR, MinQ and GSS, rank highly
 384 or mid-range. There is a visually close correlation between the most influential parameters and those
 385 which display the most non-linearity.

386

387 **Table 3 – Parameters ranked by means for each catchment from the aggregated scores for all Elementary**
 388 **Effects.**

Rank (by mean: 1 = most influential)	Upper Swale	Tin Camp Creek
1	SED	SED
2	MNR	SEC
3	IOD	VEG
4	GSS	GSS
5	EVR	MinQ
6	VEG	IOD
7	MinQ	MNR
8	LAT	MAT
9	CLR	SCR
10	SCR	MEL
11	SEC	LAT
12	MAT	CLR
13	MEL	MaxQ
14	MaxQ	SFT
15	SFT	EVR

389



390

391 **Figure 3 – Aggregated scores for all Elementary Effects where: 1 = SED; 2 = MEL; 3 = CLR; 4 = LAT; 5 = VEG; 6 =**
 392 **MAT; 7 = SCR; 8 = SFT; 9 = IOD; 10 = MinQ; 11 = MaxQ; 12 = SEC; 13 = EVR; 14 = MNR; and 15 = GSS.**

393

394 **3.2 Catchment Sediment Yield Vs Internal Geomorphology**

395

396 The core behaviours of Catchment Sediment Yield and Internal Geomorphology show a different
 397 response to the changes in parameter values, as can be seen in Figure 4, and also the rankings in Table
 398 4. For both catchments, SED is ranked as most influential for Catchment Sediment Yields. For influence
 399 on the Internal Geomorphology, SEC ranks higher in the Tin Camp Creek catchment. The Upper Swale
 400 catchment displays a similar response with both behaviours, with SED and MNR most influential and
 401 by similar amounts, although GSS has less influence on Internal Geomorphology. The change in
 402 response for Tin Camp Creek is more varied – SED is less influential on Internal Geomorphology, and
 403 SEC is the most influential with a higher aggregated mean. GSS is slightly less influential, and MNR
 404 slightly more, and VEG is more influential on the Internal Geomorphology than it is on Catchment



405 Sediment Yield. For both model functions, there again is a strong visually correlation between those
406 parameters showing the most influence and those showing the most non-linear behaviour.

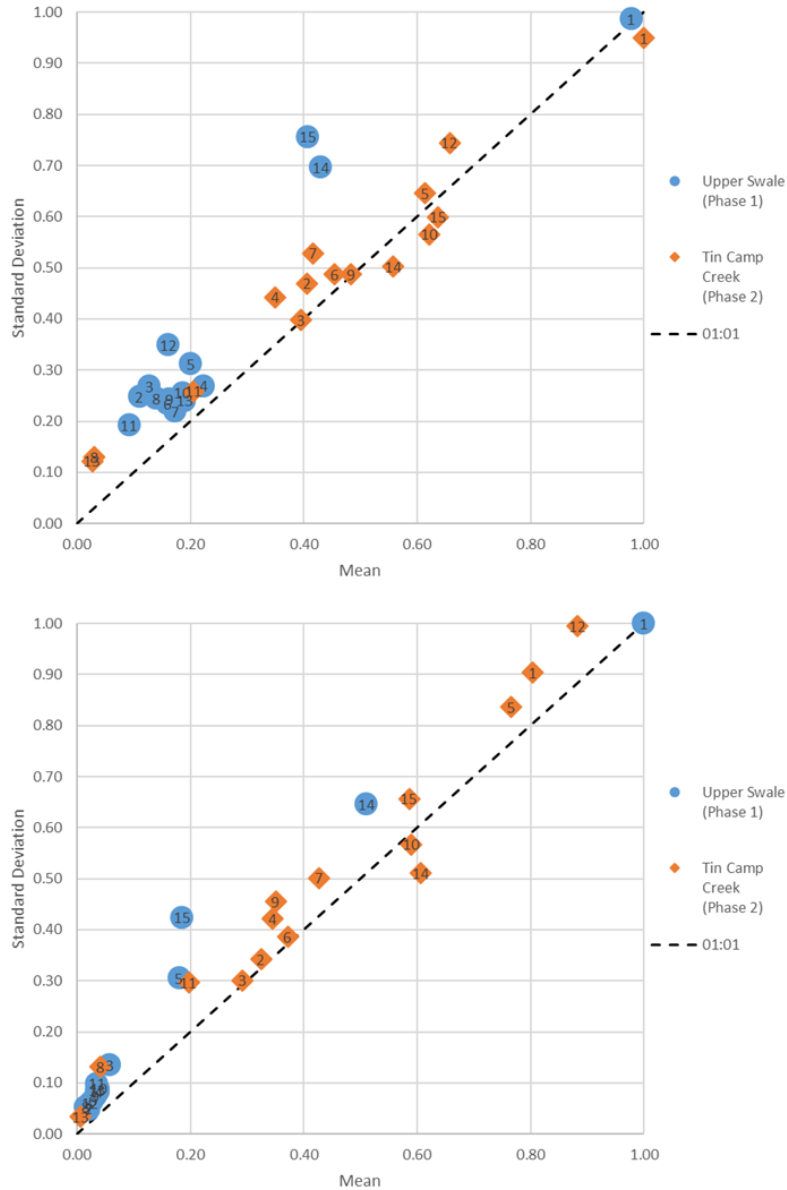
407

408 **Table 4 – Parameters ranked by means for each catchment from the aggregated scores for Catchment**

409 **Sediment Yields (SY) and Internal Geomorphology Elementary Effects (IG).**

Rank (by mean: 1 = most influential)	Upper Swale		Tin Camp Creek	
	SY	IG	SY	IG
1	SED	SED	SED	SEC
2	MNR	MNR	SEC	SED
3	GSS	GSS	GSS	VEG
4	LAT	VEG	MinQ	MNR
5	VEG	CLR	VEG	MinQ
6	EVR	LAT	MNR	GSS
7	MinQ	MinQ	IOD	SCR
8	SCR	MaxQ	MAT	MAT
9	IOD	EVR	SCR	IOD
10	SEC	IOD	MEL	LAT
11	MAT	MAT	CLR	MEL
12	SFT	SEC	LAT	CLR
13	CLR	SCR	MaxQ	MaxQ
14	MEL	MEL	SFT	SFT
15	MaxQ	SFT	EVR	EVR

410



411

412 **Figure 4 – Aggregated scores for Sediment Yield Elementary Effects (top) and Internal Geomorphology**

413 **(bottom) where: 1 = SED; 2 = MEL; 3 = CLR; 4 = LAT; 5 = VEG; 6 = MAT; 7 = SCR; 8 = SFT; 9 = IOD; 10 = MinQ; 11**

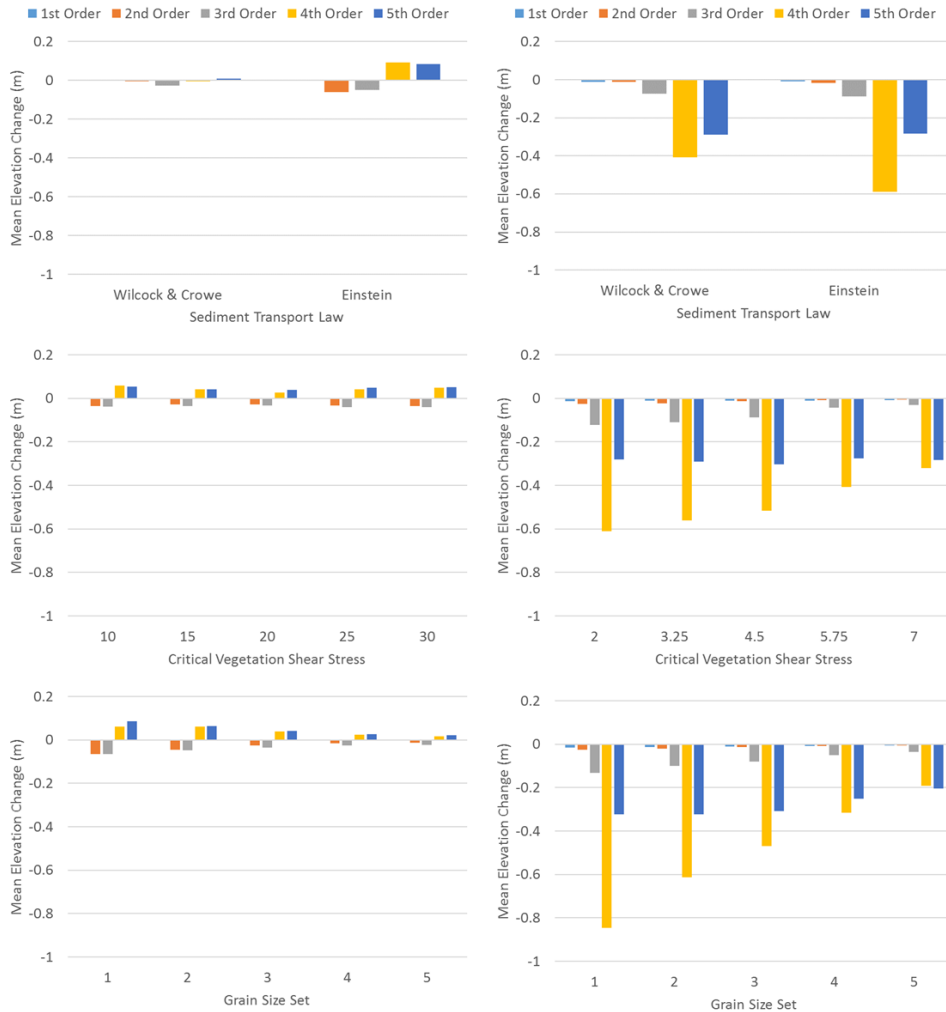
414 **= MaxQ; 12 = SEC; 13 = EVR; 14 = MNR; and 15 = GSS.**

415



416 **3.3 Changes in the Mean Elevations**

417



418

419 **Figure 5 – Changes in the mean elevations for Upper Swale (left), and Tin Camp Creek (right) for the tests split**

420 **by SED (top), VEG (middle), and GSS (bottom). The catchment is sub-divided into watersheds of five stream**

421 **orders, based on proportion of catchment drained.**

422



423 The test results were binned by the parameter values used, and the mean changes in the mean
424 elevations across the 5 stream orders calculated – Figure 5 shows the changes in each catchment for
425 parameters SED, VEG and GSS. In general, the patterns of changes remain similar despite changing
426 parameter values, yet rates of change do vary – for example, for GSS, the mean reduction in elevations
427 decreases across the catchments using grain size sets biased towards larger grain sizes. In both
428 catchments, the largest variations are observed in the 4th and 5th stream orders.

429

430 **4. Discussion**

431 The SA has been applied here to a single LEM, CAESAR-Lisflood, and the implications for that model
432 have been discussed above. Yet the results also reveal some important insights concerning metrics,
433 transferability, sediment transport laws, and full uncertainty analysis, which are relevant to all LEMS.

434

435 *1. Metrics*

436

437 Interestingly, the findings show that different metrics provide us with different indications of model
438 sensitivity. This has important implications for how to measure LEM performance – and more widely
439 how to quantify and assess geomorphic change within a basin. For example, Figure 4 and Table 4 show
440 that the model has different responses when assessed using sediment yield model functions
441 (calculated from the catchment outlet) to when using the internal geomorphology model functions
442 (based on spatial measures from within the catchment). Whilst at-a-point sediment yields are
443 straightforward to extract from simulation data and easily related to field measurements (e.g. gauges),
444 similar or identical yields may conceal very different behaviours within the basin. This is important for
445 users to realise that when calibrating LEMs, changes in sediment yields from a catchment outlet only
446 provide partial information of what is changing internally. We therefore argue that metrics
447 incorporating *spatial* changes in the basin (as well as bulk figures) are vital for assessing LEM
448 performance. (i.e. a nested set of flumes within a catchment to quantify discharge and sediment



449 output) This is especially important as the shape of the landscape – where material has been eroded
450 and deposited – is effectively the basins geomorphic memory and will directly influence subsequent
451 model performance. For other basin scale models (e.g. hydrological models) this aspect is possibly not
452 so important given the limited memory of basin antecedence.

453

454 *2. Transferability*

455

456 For environmental models, a single selection of calibrated parameter values is not transferable
457 between catchments as the conditions are different. The same is true for SAs and here we have clear
458 different behaviours between the two catchments tested – some of this can be attributed to the
459 different conditions in each catchment and associated data, but also to the choice of parameter values
460 used in the SA (ie, the minimum and maximum bounds set). The bounds of the parameter values are
461 chosen to be appropriate to the catchment they are applied to. Hence, SA are not transferable
462 between catchments, and should be performed as a preliminary phase for any new investigation.
463 Another consideration is that a single calibrated parameter set is also likely to be non-stationary,
464 especially when factors such as climate and land-use are also non-stationary, and similarly this may
465 impact on model behaviour over time.

466

467 *3. Sediment Transport Formulae*

468

469 Our SA shows that the choice of sediment transport formula (SED) had a very strong impact on the
470 model functions, and as sediment transport formulae are also integrated into other LEMs and
471 geomorphic models they will affect their outcomes too. This is, however, to be expected as previous
472 studies have shown that erosion thresholds in sediment transport for LEMs have a significant impact
473 on a model's sensitivity to climate forcings (Tucker, 2004). Looking at sediment transport formulae
474 themselves, Gomez and Church (1989) tested 11 different sediment transport formulae to the same



475 data sets and showed widespread variation in predictions – in some cases over orders of magnitude.
476 The variation in the model performance can be explained by the derivation of the sediment transport
477 formulae themselves, that are often empirically based on limited laboratory and field data, sometimes
478 representing temporal averages over equilibrium conditions (Gomez and Church, 1989). The formulae
479 do not, and were likely never intended to, represent the full variation of flow conditions Therefore,
480 when applied to different situations, they can be wrong (Coulthard et al., 2007a). This, however,
481 presents researchers using LEMs with a considerable problem, as it is highly likely that the sediment
482 transport formula to be used was not designed or calibrated for that particular application. The
483 SIBERIA model (Hancock et al., 2010; 2016; 2017; Willgoose et al., 2003) overcomes this issue by
484 having a version of the Einstein (1950) sediment transport law that is calibrated or tuned to field data
485 on erosion rates. However, even when calibrated, LEMs (and their sediment transport formulae) face
486 another hurdle with the non-stationarity of basin sediment yields. For example, a calibrated LEM will
487 be adjusted to perform for a set of observed sediment outputs or erosion and deposition patterns. If,
488 due to climate change for example, rainfall and channel flows significantly increase then the initial
489 calibration may no longer be valid (Coulthard et al., 2007b). The issue of non-stationarity has been a
490 considerable focus of the hydrological community in recent years. However, despite all the above
491 limitations, LEMs – when applied correctly – have generally been found to compare well with available
492 field data. Nonetheless, the issue of the scaling of parameters for different catchments and even more
493 importantly DEM grid size is an issue that remains to be addressed.

494

495 *4. Full Uncertainty Analysis*

496

497 It is important to note that the MM does not provide an absolute value of sensitivity, but ranks each
498 factor based on its relative influence on the model. This means it can be used to assess the main
499 sources of uncertainty on a particular model set up. The next step would be to establish how the
500 uncertainty caused by model parameters (e.g. the choice of sediment transport formula) compares to



501 other identified sources of uncertainty, such as rainfall input uncertainty, DEM observation and
502 resolution uncertainty, and length of spin-up period. For example, it may be that the choice of
503 sediment transport formula may only be a minor source of uncertainty compared to the DEM
504 resolution, or equally, it might be the most significant source of uncertainty in LEMs.
505 Importantly, whilst the simulation of long-term development of landscapes may be somewhat
506 resilient to uncertainty (Hancock et al., 2016), any attempt to reproduce, predict or forecast physical
507 changes, especially if there is a decision-making element, should have the same appreciation of
508 uncertainty and rigorous testing that has been applied to models such as Lisflood-FP. For example, the
509 Lisflood-FP has been rigorously tested and benchmarked for decision-making purposes (Hunter et al.,
510 2005; Neelz & Pender, 2013), and the use of SA to assess model response and uncertainty is standard
511 practise (Di Baldassarre et al., 2009; Fewtrell et al., 2008, 2011; Hall et al., 2005; Horritt and Bates,
512 2001, 2002; Hunter et al., 2008; Neal et al., 2011; Sampson et al., 2012), often as a stage of calibration
513 using the GLUE method (Aronica et al., 2002; Bates et al., 2004; Horritt et al., 2006; Hunter et al., 2005;
514 Pappenberger et al., 2007; Wong et al., 2015). Uncertainty in model predictions can be accounted for
515 by utilising probabilistic measures and uncertainty cascades (for example, Pappenberger et al., 2005;
516 Stephens et al., 2012). This is not considered unique to CAESAR-Lisflood, and any application of an
517 LEM or other geomorphic model for operational, decision-making or forecasting applications should
518 make full consideration of all associated uncertainties.

519

520 *5. Limitations*

521

522 There are limitations to the methodology presented here. The MM should not be considered a
523 quantitative assessment of sensitivity – it is designed to be an efficient pre-screening method to isolate
524 key parameters for further assessment or for calibration, and ranks parameter values based only on
525 their relative influence of the model. It is also subjective in the sense that the user defines the
526 parameter space explored by setting minimum and maximum values. The range of these values and



527 the number of iterative steps between them will have an influence on the relative influence shown –
528 here, the fact that SED was binary, with no intermediate steps, whereas most other parameters had
529 five equal and iterative steps, will have affected its overall relative influence. Reducing the number of
530 iterative steps would likely increase the EEs calculated, and increasing would reduce them, and shift
531 the other parameters' relative influence against that for SED. This is acknowledged here, but the range
532 of parameter values and the steps used were appropriate to represent the possible uncertainties in
533 the model (i.e., they were based on proportional deviations from previous calibrated parameter sets).
534 An obvious limitation to this exercise is computational resource. This test incorporated 1600 individual
535 model runs to test the behavioural response of the model to 15 parameters, in just two catchments,
536 and this partly influenced the choice to limit the simulation periods to 30 years. We used a batch mode
537 functionality of CAESAR-Lisflood to run simulations of each repeat (16 model runs each) consecutively,
538 and distributed batches across different machines – this is feasible for the model set ups described.
539 However, for long-term simulations for catchments the size of the Upper Swale, individual model runs
540 can take several weeks and running several runs consecutively becomes prohibitive. One solution
541 would be to distribute the jobs on High Performance Computing (HPC) facilities, where the time for a
542 single model run would not significantly decrease, but several hundred, even thousands, of individual
543 model runs can be performed coincidentally.

544

545 The methodology has only been applied to the CAESAR-Lisflood model, and although some of the
546 findings will have implications to other LEMs, most will be unique to CAESAR-Lisflood and the model
547 set ups presented. The methodology should serve as a tool for users to determine the behaviour of
548 each model set up prior to calibration and simulation. For CAESAR-Lisflood itself, future SA should
549 analyse more catchments of different sizes and environmental conditions. The two model set ups
550 used here should be analysed again but using a long-term timeframe to understand how the model
551 behaviour might evolve over longer simulations.

552



553 **5. Conclusions**

554

555 The feasibility of performing global SA to a highly parameterised catchment LEM has been
556 demonstrated through the application of the MM to the CAESAR-Lisflood model. The test was
557 repeated over two different catchments suggesting some model behaviours are universal, and others
558 vary depending on the catchment characteristics providing crucial information to inform future model
559 developments. This analysis confirms that the sediment transport formulae are a significant source of
560 uncertainty in LEMs, and in the CAESAR-Lisflood model the use of one formula over another can result
561 in an order of magnitude differences in sediment yields when all other factors are kept constant.

562

563 In addition to the above, the results reveal the parameters in CAESAR-Lisflood which exert the greatest
564 influence, and whilst we can only apply this to the CAESAR-Lisflood model itself, it is likely that LEMs
565 with comparable parameters will display similar behaviours. Some of the most influential parameters,
566 like MNR, GSS and VEG are physically-based, so any uncertainty can be reduced by gathering data
567 from the field – in these tests each of these parameters utilised global values initially, so more detailed
568 field measurements could be utilised to provide spatially distributed values and further reduce
569 uncertainty. The parameters which are most likely to be an issue for operators are those which have
570 a medium influence and are set based on data characteristics for numerical efficiency – these include
571 IOD, MinQ and MaxQ. For example, the typical and recommended value for MinQ is 1/100 of the DEM
572 resolution and here, by varying the value yet keeping resolution the same, some variation was
573 observed in the results – it is not yet determined whether any difference in model results at different
574 resolutions are due to changes in values of MinQ and MaxQ, or the grid resolutions, or a combination
575 of the two, and this will be a focus for future work.

576



577 The application of a global SA should become a vital step in any investigation using LEMs. This paper
578 has demonstrated that the use of the MM is efficient for this purpose and yielded some useful insights
579 into model behaviour that can be fed back into the model set up, and future model development.

580

581 **Model and Data Availability**

582

583 The data produced by this study is made available on request from the corresponding author. The
584 CAESAR-Lisflood model used in this study is freely available under a GNU licence from

585 <http://www.coulthard.org.uk>

586

587 **Competing Interests**

588 The authors declare that they have no conflict of interest.

589

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591

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599 study is freely available under a GNU licence from <http://www.coulthard.org.uk>

600



601 **References**

- 602 Adams, J. M., Gasparini, N. M., Hobbey, D. E. J., Tucker, G. E., Hutton, E. W. H., Nudurupati, S. S. and
603 Istanbulluoglu, E.: The Landlab v1.0 OverlandFlow component: a Python tool for computing shallow-
604 water flow across watersheds, *Geosci. Model Dev*, 10, 1645–1663, doi:10.5194/gmd-10-1645-2017,
605 2017.
- 606 Andersen, J. L., Egholm, D. L., Knudsen, M. F., Jansen, J. D. and Nielsen, S. B.: The periglacial engine
607 of mountain erosion - Part 1: Rates of frost cracking and frost creep, *Earth Surf. Dyn.*, 3(4), 447–462,
608 doi:10.5194/esurf-3-447-2015, 2015.
- 609 Armitage, J. J., Whittaker, A. C., Zakari, M. and Campforts, B.: Numerical modelling landscape and
610 sediment flux response to precipitation rate change, *Earth Surf. Dyn. Discuss.*, (May), 1–31,
611 doi:10.5194/esurf-2017-34, 2017.
- 612 Aronica, G., Bates, P. D. and Horritt, M. S.: Assessing the uncertainty in distributed model predictions
613 using observed binary pattern information within GLUE, *Hydrol. Process.*, 16(10), 2001–2016,
614 doi:10.1002/hyp.398, 2002.
- 615 Attal, M., Tucker, G. E., Whittaker, A. C., Cowie, P. A. and Roberts, G. P.: Modelling fluvial incision
616 and transient landscape evolution: Influence of dynamic Channel adjustment, *J. Geophys. Res. Earth
617 Surf.*, 113(3), 1–16, doi:10.1029/2007JF000893, 2008.
- 618 Di Baldassarre, G., Schumann, G. and Bates, P. D.: A technique for the calibration of hydraulic models
619 using uncertain satellite observations of flood extent, *J. Hydrol.*, 367(3), 276–282,
620 doi:10.1016/j.jhydrol.2009.01.020, 2009.
- 621 Bates, P. D., Horritt, M. S., Aronica, G. and Beven, K.: Bayesian updating of flood inundation
622 likelihoods conditioned on flood extent data, *Hydrol. Process.*, 18(17), 3347–3370,
623 doi:10.1002/hyp.1499, 2004.
- 624 Bates, P. D., Horritt, M. S. and Fewtrell, T. J.: A simple inertial formulation of the shallow water
625 equations for efficient two-dimensional flood inundation modelling, *J. Hydrol.*, 387(1–2), 33–45,
626 doi:10.1016/j.jhydrol.2010.03.027, 2010.
- 627 Beven, K. and Binley, A.: The future of distributed models: model calibration and uncertainty
628 prediction, *Hydrol. Process.*, 6, 279–298 [online] Available from:
629 <http://onlinelibrary.wiley.com/doi/10.1002/hyp.3360060305/full> (Accessed 8 May 2014), 1992.
- 630 Beven, K. and Kirkby, M.: A physically based, variable contributing area model of basin hydrology/Un
631 modèle à base physique de zone d'appel variable de l'hydrologie du bassin versant, *Hydrol. Sci. J.*,
632 24(1), 37–41 [online] Available from:
633 <http://www.tandfonline.com/doi/abs/10.1080/02626667909491834> (Accessed 8 May 2014), 1979.
- 634 Brockmann, D. and Morgenroth, E.: Comparing global sensitivity analysis for a biofilm model for two-
635 step nitrification using the qualitative screening method of Morris or the quantitative variance-based
636 Fourier Amplitude Sensitivity Test (FAST), *Water Sci. Technol.*, 56(8), 85–93,
637 doi:10.2166/wst.2007.600, 2007.
- 638 Campolongo, F., Cariboni, J. and Saltelli, A.: An effective screening design for sensitivity analysis of
639 large models, *Environ. Model. Softw.*, 22(10), 1509–1518, doi:10.1016/j.envsoft.2006.10.004, 2007.
- 640 Cariboni, J., Gatelli, D., Liska, R. and Saltelli, A.: The role of sensitivity analysis in ecological modelling,
641 *Ecol. Modell.*, 203(1–2), 167–182, doi:10.1016/j.ecolmodel.2005.10.045, 2007.
- 642 Collins, D. B. G.: Modeling the effects of vegetation-erosion coupling on landscape evolution, *J.
643 Geophys. Res.*, 109(F3), 1–11, doi:10.1029/2003JF000028, 2004.



- 644 Coulthard, T., Hicks, D. and Wiel, M. Van De: Cellular modelling of river catchments and reaches:
645 Advantages, limitations and prospects, *Geomorphology*, 90(3–4), 192–207,
646 doi:10.1016/j.geomorph.2006.10.030, 2007a.
- 647 Coulthard, T., Neal, J., Bates, P., Ramirez, J., de Almeida, G. and Hancock, G.: Integrating the
648 LISFLOOD-FP 2D hydrodynamic model with the CAESAR model: implications for modelling landscape
649 evolution, *Earth Surf. ...*, 38(15), 1897–1906, doi:10.1002/esp.3478, 2013.
- 650 Coulthard, T. J. and Macklin, M. G.: How sensitive are river systems to climate and land-use changes?
651 A model-based evaluation, *J. Quat. Sci.*, 16(4), 347–351, doi:10.1002/jqs.604, 2001.
- 652 Coulthard, T. J. and Skinner, C. J.: The sensitivity of landscape evolution models to spatial and
653 temporal rainfall resolution, *Earth Surf. Dyn.*, 4(3), 757–771, doi:10.5194/esurf-4-757-2016, 2016a.
- 654 Coulthard, T. J. and Skinner, C. J.: The sensitivity of landscape evolution models to spatial and
655 temporal rainfall resolution, *Earth Surf. Dyn. Discuss.*, 1–28, doi:10.5194/esurf-2016-2, 2016b.
- 656 Coulthard, T. J. and Van De Wiel, M. J.: Quantifying fluvial non linearity and finding self organized
657 criticality? Insights from simulations of river basin evolution, *Geomorphology*, 91(3–4), 216–235,
658 doi:10.1016/j.geomorph.2007.04.011, 2007.
- 659 Coulthard, T. J. and Van De Wiel, M. J.: Modelling river history and evolution, *Philos. Trans. R. Soc. A*
660 *Math. Phys. Eng. Sci.*, 370(1966), 2123–2142, doi:10.1098/rsta.2011.0597, 2012.
- 661 Coulthard, T. J. and Van De Wiel, M. J.: Climate, tectonics or morphology: What signals can we see in
662 drainage basin sediment yields?, *Earth Surf. Dyn.*, 1(1), 13–27, doi:10.5194/esurf-1-13-2013, 2013.
- 663 Coulthard, T. J. and Van De Wiel, M. J.: Modelling long term basin scale sediment connectivity,
664 driven by spatial land use changes, *Geomorphology*, 277, 265–281,
665 doi:10.1016/j.geomorph.2016.05.027, 2017.
- 666 Coulthard, T. J., Lewin, J. and Macklin, M. G.: 12 Non-stationarity of basin scale sediment delivery in
667 response to climate change, *Dev. Earth Surf. Process.*, 11(7), 315–331, doi:10.1016/S0928-
668 2025(07)11131-7, 2007b.
- 669 Coulthard, T. J., Ramirez, J., Fowler, H. J. and Glenis, V.: Using the UKCP09 probabilistic scenarios to
670 model the amplified impact of climate change on drainage basin sediment yield, *Hydrol. Earth Syst.*
671 *Sci.*, 16(11), 4401–4416, doi:10.5194/hess-16-4401-2012, 2012.
- 672 Egholm, D. L., Andersen, J. L., Knudsen, M. F., Jansen, J. D. and Nielsen, S. B.: The periglacial engine
673 of mountain erosion - Part 2: Modelling large-scale landscape evolution, *Earth Surf. Dyn.*, 3(4), 463–
674 482, doi:10.5194/esurf-3-463-2015, 2015.
- 675 Einstein, H. A.: Bed-load function for sediment transportation in open channel flows, *Illionois State*
676 *Water Surv. Bull.* 41, 43–49, 1951.
- 677 Fewtrell, T. J., Bates, P. D., Horritt, M. and Hunter, N. M.: Evaluating the effect of scale in flood
678 inundation modelling in urban environments, *Hydrol. Process.*, 22(26), 5107–5118,
679 doi:10.1002/hyp.7148, 2008.
- 680 Fewtrell, T. J., Duncan, A., Sampson, C. C., Neal, J. C. and Bates, P. D.: Benchmarking urban flood
681 models of varying complexity and scale using high resolution terrestrial LiDAR data, *Phys. Chem.*
682 *Earth, Parts A/B/C*, 36(7), 281–291, doi:10.1016/j.pce.2010.12.011, 2011.
- 683 Gomez, B. and Church, M.: An Assessment of Bedload Sediment transport Formulae for Gravel Bed
684 Rivers, *Water Resour. Res.*, 25(6), 1161–1186, 1989.
- 685 van Griensven, A., Meixner, T., Grunwald, S., Bishop, T., Diluzio, M. and Srinivasan, R.: A global



- 686 sensitivity analysis tool for the parameters of multi-variable catchment models, *J. Hydrol.*, 324(1–4),
687 10–23, doi:10.1016/j.jhydrol.2005.09.008, 2006.
- 688 Hall, J. W., Tarantola, S., Bates, P. D. and Horritt, M. S.: Distributed Sensitivity Analysis of Flood
689 Inundation Model Calibration, *J. Hydraul. Eng.*, 131(2), 117–126, doi:10.1061/(ASCE)0733-
690 9429(2005)131:2(117), 2005.
- 691 Hancock, G. and Willgoose, G.: Use of a landscape simulator in the validation of the SIBERIA
692 catchment evolution model: Declining equilibrium landforms, *Water Resour. Res.*, 37(7), 1981–1992,
693 doi:10.1029/2001WR900002, 2001.
- 694 Hancock, G. R.: The impact of different gridding methods on catchment geomorphology and soil
695 erosion over long timescales using a landscape evolution model, *Earth Surf. Process. Landforms*,
696 31(8), 1035–1050, doi:10.1002/esp.1306, 2006.
- 697 Hancock, G. R. and Coulthard, T. J.: Channel movement and erosion response to rainfall variability in
698 southeast Australia, *Hydrol. Process.*, 26(5), 663–673, doi:10.1002/hyp.8166, 2012.
- 699 Hancock, G. R., Lowry, J. B. C., Coulthard, T. J., Evans, K. G. and Moliere, D. R.: A catchment scale
700 evaluation of the SIBERIA and CAESAR landscape evolution models, *Earth Surf. Process. Landforms*,
701 35(8), 863–875, doi:10.1002/esp.1863, 2010.
- 702 Hancock, G. R., Coulthard, T. J., Martinez, C. and Kalma, J. D.: An evaluation of landscape evolution
703 models to simulate decadal and centennial scale soil erosion in grassland catchments, *J. Hydrol.*,
704 398(3–4), 171–183, doi:10.1016/j.jhydrol.2010.12.002, 2011.
- 705 Hancock, G. R., Coulthard, T. J. and Lowry, J. B. C.: Predicting uncertainty in sediment transport and
706 landscape evolution - the influence of initial surface conditions, *Comput. Geosci.*, 90, 117–130,
707 doi:10.1016/j.cageo.2015.08.014, 2016.
- 708 Hancock, G. R., Verdon-Kidd, D. and Lowry, J. B. C.: Sediment output from a post-mining
709 catchment ??? Centennial impacts using stochastically generated rainfall, *J. Hydrol.*, 544, 180–194,
710 doi:10.1016/j.jhydrol.2016.11.027, 2017.
- 711 Herman, J. D., Kollat, J. B., Reed, P. M. and Wagener, T.: Technical Note: Method of Morris
712 effectively reduces the computational demands of global sensitivity analysis for distributed
713 watershed models, *Hydrol. Earth Syst. Sci.*, 17(7), 2893–2903, doi:10.5194/hess-17-2893-2013, 2013.
- 714 Horritt, M., Bates, P. and Mattinson, M.: Effects of mesh resolution and topographic representation
715 in 2D finite volume models of shallow water fluvial flow, *J. Hydrol.*, 329(1–2), 306–314,
716 doi:10.1016/j.jhydrol.2006.02.016, 2006.
- 717 Horritt, M. S. and Bates, P. D.: Effects of spatial resolution on a raster based model of flood flow, *J.*
718 *Hydrol.*, 253(1–4), 239–249, doi:10.1016/S0022-1694(01)00490-5, 2001.
- 719 Horritt, M. S. and Bates, P. D.: Evaluation of 1D and 2D numerical models for predicting river flood
720 inundation, *J. Hydrol.*, 268(1), 87–99, doi:10.1016/S0022-1694(02)00121-X, 2002.
- 721 Hunter, N. M., Horritt, M. S., Bates, P. D., Wilson, M. D. and Werner, M. G. F.: An adaptive time step
722 solution for raster-based storage cell modelling of floodplain inundation, *Adv. Water Resour.*, 28(9),
723 975–991, doi:10.1016/j.advwatres.2005.03.007, 2005.
- 724 Hunter, N. M., Bates, P. D., Neelz, S., Pender, G., Villanueva, I., Wright, N. G., Liang, D., Falconer, R.
725 A., Lin, B., Waller, S., Crossley, A. J. and Mason, D. C.: Benchmarking 2D hydraulic models for urban
726 flooding, *Proc. Inst. Civ. Eng. - Water Manag.*, 161(1), 13–30, doi:10.1680/wama.2008.161.1.13,
727 2008.
- 728 Ibbitt, R. P., Willgoose, G. R. and Duncan, M. J.: Channel network simulation models compared with



- 729 data from the Ashley River, New Zealand, *Water Resour. Res.*, 35(12), 3875–3890,
730 doi:10.1029/1999WR900245, 1999.
- 731 Ijjasz-Vasquez, E. J., Bras, R. L. and Moglen, G. E.: Sensitivity of a basin evolution model to the nature
732 of runoff production and to initial conditions, *Water Resour. Res.*, 28(10), 2733–2741,
733 doi:10.1029/92WR01561, 1992.
- 734 Istanbuluoglu, E. and Bras, R. L.: Vegetation-modulated landscape evolution: Effects of vegetation
735 on landscape processes, drainage density, and topography, *J. Geophys. Res. Earth Surf.*, 110(2), 1–
736 19, doi:10.1029/2004JF000249, 2005.
- 737 Jerolmack, D. J. and Paola, C.: Shredding of environmental signals by sediment transport, *Geophys.*
738 *Res. Lett.*, 37(19), 1–5, doi:10.1029/2010GL044638, 2010.
- 739 Larsen, L., Thomas, C., Eppinga, M. and Coulthard, T.: Exploratory modeling: Extracting causality
740 from complexity, *Eos (Washington, DC)*, 95(32), 285–286, doi:10.1002/2014EO320001, 2014.
- 741 Liu, B. and Coulthard, T. J.: Modelling the interaction of aeolian and fluvial processes with a
742 combined cellular model of sand dunes and river systems, *Comput. Geosci.*, 106, 1–9,
743 doi:10.1016/j.cageo.2017.05.003, 2017.
- 744 Martin, Y. and Church, M.: Numerical modelling of landscape evolution: geomorphological
745 perspectives, *Prog. Phys. Geogr.*, 28(3), 317–339, doi:10.1191/0309133304pp412ra, 2004.
- 746 Met Office: 5km UK Composite Rainfall Data from the Met Office NIMROD System, NCAS Br. Atmos.
747 Data Centre, available at : <http://catalogue.ceda.ac.uk/uuid/82adec1f896af6169112d09cc1174499>
748 (last access: 20 September 2016), 2003.
- 749 Morris, M. D.: Factorial Sampling Plans for Preliminary Computational Experiments, *Technometrics*,
750 33(2), 161–174, doi:10.2307/1269043, 1991.
- 751 Nash, J. and Sutcliffe, J.: River flow forecasting through conceptual models part I—A discussion of
752 principles, *J. Hydrol.*, 10, 282–290 [online] Available from:
753 <http://www.sciencedirect.com/science/article/pii/0022169470902556> (Accessed 8 May 2014), 1970.
- 754 Neal, J., Schumann, G., Fewtrell, T., Budimir, M., Bates, P. and Mason, D.: Evaluating a new
755 LISFLOOD-FP formulation with data from the summer 2007 floods in Tewkesbury, UK, *J. Flood Risk*
756 *Manag.*, 4(2), 88–95, doi:10.1111/j.1753-318X.2011.01093.x, 2011.
- 757 Neelz, S. & Pender, G.: Benchmarking the latest generation of 2D hydraulic modelling packages.
758 [online] Available from: [http://evidence.environment-](http://evidence.environment-agency.gov.uk/FCERM/Libraries/FCERM_Project_Documents/SC120002_Benchmarking_2D_hydraulic_models_Report.sflb.ashx)
759 [agency.gov.uk/FCERM/Libraries/FCERM_Project_Documents/SC120002_Benchmarking_2D_hydrauli](http://evidence.environment-agency.gov.uk/FCERM/Libraries/FCERM_Project_Documents/SC120002_Benchmarking_2D_hydraulic_models_Report.sflb.ashx)
760 [c_models_Report.sflb.ashx](http://evidence.environment-agency.gov.uk/FCERM/Libraries/FCERM_Project_Documents/SC120002_Benchmarking_2D_hydraulic_models_Report.sflb.ashx), 2013.
- 761 Neumann, M. B.: Comparison of sensitivity analysis methods for pollutant degradation modelling: A
762 case study from drinking water treatment, *Sci. Total Environ.*, 433(October), 530–537,
763 doi:10.1016/j.scitotenv.2012.06.026, 2012.
- 764 Norton, J. P.: Algebraic sensitivity analysis of environmental models, *Environ. Model. Softw.*, 23,
765 963–972, doi:10.1016/j.envsoft.2007.11.007, 2008.
- 766 Norton, J. P.: Selection of Morris trajectories for initial sensitivity analysis, *IFAC.*, 2009.
- 767 Oakley, J. E. and O’Hagan, A.: Probabilistic Sensitivity Analysis of Complex Models : A Bayesian
768 Approach Author (s): Jeremy E . Oakley and Anthony O'Hagan Published by : Wiley for the Royal
769 Statistical Society Stable URL : <http://www.jstor.org/stable/3647504> Probabilistic sensitiv , 66(3),
770 751–769, 2004.



- 771 Oreskes, N., Shrader-Frechette, K. and Belitz, K.: Verification, Validation, and Confirmation of
 772 Numerical Models in the Earth Sciences, *Science* (80-.), 263, 641–646, doi:10.2307/2883078, 1994.
- 773 Pappenberger, F., Beven, K. J., Hunter, N. M., Bates, P. D., Gouweleeuw, B. T., Thielen, J. and Roo, A.
 774 P. J. De: Cascading model uncertainty from medium range weather forecasts (10 days) through a
 775 rainfall-runoff model to flood inundation predictions within the European Flood Forecasting System
 776 (EFFS), *Hydrol. Earth Syst. Sci. Discuss.*, 9(4), 381–393, doi:10.5194/hess-9-381-2005, 2005.
- 777 Pappenberger, F., Harvey, H., Beven, K., Hall, J. and Meadowcroft, I.: Decision tree for choosing an
 778 uncertainty analysis methodology : a wiki experiment, *Hydrol. Process.*, 20, 3793–3798,
 779 doi:10.1002/hyp, 2006.
- 780 Pappenberger, F., Frodsham, K., Beven, K., Romanowicz, R. and Matgen, P.: Fuzzy set approach to
 781 calibrating distributed flood inundation models using remote sensing observations, *Hydrol. Earth*
 782 *Syst. Sci. Discuss.*, 11(2), 739–752 [online] Available from: [https://hal.archives-ouvertes.fr/hal-](https://hal.archives-ouvertes.fr/hal-00305049/)
 783 [00305049/](https://hal.archives-ouvertes.fr/hal-00305049/) (Accessed 24 May 2017), 2007.
- 784 Pappenberger, F., Beven, K. J., Ratto, M. and Matgen, P.: Multi-method global sensitivity analysis of
 785 flood inundation models, *Adv. Water Resour.*, 31(1), 1–14, doi:10.1016/j.advwatres.2007.04.009,
 786 2008.
- 787 Pazzaglia, F. J.: *Landscape evolution models*, pp. 247–274., 2003.
- 788 Petersen, A. C. (Arthur C.: *Simulating nature : a philosophical study of computer-simulation*
 789 *uncertainties and their role in climate science and policy advice*, CRC Press. [online] Available from:
 790 <https://books.google.co.uk/books?hl=en&lr=&id=I4GhNkiPv3EC&oi=fnd&pg=PP1&dq=Simulating+N>
 791 [ature:+A+Philosophical+Study+of+Computer-](https://books.google.co.uk/books?hl=en&lr=&id=I4GhNkiPv3EC&oi=fnd&pg=PP1&dq=Simulating+N)
 792 [Simulation+Uncertainties+and+Their+Role+in+Climate+Science+and+Policy+Advice&ots=EKmUbPTt](https://books.google.co.uk/books?hl=en&lr=&id=I4GhNkiPv3EC&oi=fnd&pg=PP1&dq=Simulating+N)
 793 [VZ&sig=BisleTDNw3E0_EpozyLbxjJHUdg#v=onepage&q=Simulating+Nature%3A+A+Philosophical+Study](https://books.google.co.uk/books?hl=en&lr=&id=I4GhNkiPv3EC&oi=fnd&pg=PP1&dq=Simulating+N)
 794 [of+Computer-Simulation+Uncertainties+and+Their+Role+in+Climate+Science+and+Policy+Advice&f=false](https://books.google.co.uk/books?hl=en&lr=&id=I4GhNkiPv3EC&oi=fnd&pg=PP1&dq=Simulating+N)
 795 (Accessed 18 August 2017), 2012.
- 796 Pianosi, F., Beven, K., Freer, J., Hall, J. W., Rougier, J., Stephenson, D. B. and Wagener, T.: Sensitivity
 797 analysis of environmental models: A systematic review with practical workflow, *Environ. Model.*
 798 *Softw.*, 79, 214–232, doi:10.1016/j.envsoft.2016.02.008, 2016.
- 799 Pujol, G.: R Package “sensitivity”. Version 1.4-0, 2009.
- 800 Ratto, M., Pagano, A. and Young, P.: State Dependent Parameter metamodelling and sensitivity
 801 analysis, *Comput. Phys. Commun.*, 177(11), 863–876, doi:10.1016/j.cpc.2007.07.011, 2007.
- 802 Saltelli, A., Chan, K. and Scott, E. M.: *Sensitivity Analysis*, John Wiley, New York, 2000.
- 803 Sampson, C. C., Fewtrell, T. J., Duncan, A., Shaad, K., Horritt, M. S. and Bates, P. D.: Use of terrestrial
 804 laser scanning data to drive decimetric resolution urban inundation models, *Adv. Water Resour.*, 41,
 805 1–17, doi:10.1016/j.advwatres.2012.02.010, 2012.
- 806 Saynor, M. J., Lowry, J., Erskine, W. D., Coulthard, T. and Hancock, G.: Assessing Erosion and Run-Off
 807 Performance of a Trial Rehabilitated, *Proc. Life Mine Conf. July 2012, (July)*, 10–12, 2012.
- 808 Skinner, C. and Coulthard, T.: Caesar-Lisflood Existing Applications Parameter Listings - May 2017, ,
 809 doi:10.5281/ZENODO.800558, 2017.
- 810 Sobol', I.: Global Sensitivity Indices for Nonlinear Mathematical Models:Review, *Math. Comput.*
 811 *Simul.*, 55, 271–280, doi:10.1016/S0378-4754(00)00270-6, 2001.
- 812 Song, X., Zhan, C., Xia, J. and Kong, F.: An efficient global sensitivity analysis approach for distributed
 813 hydrological model, *J. Geogr. Sci.*, 22(2), 209–222, doi:10.1007/s11442-012-0922-5, 2012.



- 814 Song, X., Zhang, J., Zhan, C., Xuan, Y., Ye, M. and Xu, C.: Global sensitivity analysis in hydrological
815 modeling: Review of concepts, methods, theoretical framework, and applications, *J. Hydrol.*,
816 523(225), 739–757, doi:10.1016/j.jhydrol.2015.02.013, 2015.
- 817 Stephens, E. M., Bates, P. D., Freer, J. E. and Mason, D. C.: The impact of uncertainty in satellite data
818 on the assessment of flood inundation models, *J. Hydrol.*, 414–415, 162–173,
819 doi:10.1016/j.jhydrol.2011.10.040, 2012.
- 820 Tucker, G. E.: Drainage basin sensitivity to tectonic and climatic forcing: implications of a stochastic
821 model for the role of entrainment and erosion thresholds, *Earth Surf. Process. Landforms*, 29(2),
822 185–205, doi:10.1002/esp.1020, 2004.
- 823 Tucker, G. E. and Bras, R. L.: A stochastic approach to modelling the role of rainfall variability in
824 drainage basin evolution, *Water Resour. Res.*, 36(7), 1953, doi:10.1029/2000WR900065, 2000.
- 825 Tucker, G. E. and Hancock, G. R.: Modelling landscape evolution, *Earth Surf. Process. Landforms*,
826 35(1), 28–50, doi:10.1002/esp.1952, 2010.
- 827 Vanwalleghem, T., Stockmann, U., Minasny, B. and McBratney, A. B.: A quantitative model for
828 integrating landscape evolution and soil formation, *J. Geophys. Res. Earth Surf.*, 118(2), 331–347,
829 doi:10.1029/2011JF002296, 2013.
- 830 Welivitiya, W. D. D. P., Willgoose, G. R., Hancock, G. R. and Cohen, S.: Exploring the sensitivity on a
831 soil area-slope-grading relationship to changes in process parameters using a pedogenesis model,
832 *Earth Surf. Dyn.*, 4(3), 607–625, doi:10.5194/esurf-4-607-2016, 2016.
- 833 Van De Wiel, M. J. and Coulthard, T. J.: Self-organized criticality in river basins: Challenging
834 sedimentary records of environmental change, *Geology*, 38(1), 87–90, doi:10.1130/G30490.1, 2010.
- 835 Van De Wiel, M. J., Coulthard, T. J., Macklin, M. G. and Lewin, J.: Embedding reach-scale fluvial
836 dynamics within the CAESAR cellular automaton landscape evolution model, *Geomorphology*, 90(3–
837 4), 283–301, doi:10.1016/j.geomorph.2006.10.024, 2007.
- 838 Van De Wiel, M. J., Coulthard, T. J., Macklin, M. G. and Lewin, J.: Modelling the response of river
839 systems to environmental change: Progress, problems and prospects for palaeo-environmental
840 reconstructions, *Earth-Science Rev.*, 104(1–3), 167–185, doi:10.1016/j.earscirev.2010.10.004, 2011.
- 841 Wilcock, P. R. and Crowe, J. C.: Surface-based Transport Model for Mixed-Size Sediment, *J. Hydraul.*
842 *Eng.*, 129(2), 120–128, doi:10.1061/(ASCE)0733-9429(2003)129:2(120), 2003.
- 843 Willgoose, G. R., Hancock, G. R. and Kuczera, G.: A Framework for the Quantitative Testing of
844 Landform Evolution Models, pp. 195–216, American Geophysical Union., 2013.
- 845 Wong, J. S., Freer, J. E., Bates, P. D., Sear, D. A. and Stephens, E. M.: Sensitivity of a hydraulic model
846 to channel erosion uncertainty during extreme flooding, *Hydrol. Process.*, 29(2), 261–279,
847 doi:10.1002/hyp.10148, 2015.
- 848 Yang, J.: Convergence and uncertainty analyses in Monte-Carlo based sensitivity analysis, *Environ.*
849 *Model. Softw.*, 26(4), 444–457, doi:10.1016/j.envsoft.2010.10.007, 2011.
- 850 Ziliani, L., Surian, N., Coulthard, T. J. and Tarantola, S.: Reduced-complexity modeling of braided
851 rivers: Assessing model performance by sensitivity analysis, calibration, and validation, *J. Geophys.*
852 *Res. Earth Surf.*, 118(4), 2243–2262, doi:10.1002/jgrf.20154, 2013.
- 853