

# Coarse-grained component concurrency in Earth System modeling: parallelizing atmospheric radiative transfer in the GFDL AM3 model using the Flexible Modeling System coupling framework

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**Abstract.** Climate models represent a large variety of processes on a variety of time and space scales, a canonical example of multi-physics multi-scale modeling. Current hardware trends, such as Graphical Processing Units (GPUs) and Many-Integrated Core chips (MICs), are based on, at best, marginal increases in clock speed, coupled with vast increases in concurrency, particularly at the fine grain. Multi-physics codes face particular challenges in achieving fine-grained concurrency, as different physics and dynamics components have different computational profiles, and universal solutions are hard to come by.

We propose here one approach for multi-physics codes. These codes are typically structured as *components* interacting via software frameworks. The component structure of a typical Earth system model consists of a hierarchical and recursive tree of components, each representing a different climate process or dynamical system. This recursive structure generally encompasses a modest level of concurrency at the highest level (e.g atmosphere and ocean on different processor sets) with serial organization underneath.

We propose to extend concurrency much further by running more and more lower- and higher-level components in parallel with each other. Each component can further be parallelized on the fine grain, potentially offering a major increase in scalability of Earth system models.

We present here first results from this approach, called Coarse-grained Component Concurrency, or CCC. Within the Geophysical Fluid Dynamics Laboratory (GFDL) Flexible Modeling System (FMS), the atmospheric radiative transfer component has been configured to run in parallel with a composite component consisting of every other atmospheric component, including the atmospheric dynamics and all other atmospheric physics components. We will explore the algorithmic challenges involved in such an approach, and present results from such simulations. Plans to achieve even greater levels of coarse-grained concurrency by extending this approach within other components such as the ocean, will be discussed.

## 1 Introduction

Climate and weather modeling have historically been among the most computationally demanding domains using high-performance computing. Its history parallels that of modern computing itself, starting with experiments on the ENIAC (Platzman, 1979) and continuing through several changes in supercomputing architecture, including the vector and parallel eras.

- 5 The transition from vector to parallel computing was “disruptive”, to use a currently popular term. The computing industry itself was transitioning from being primarily responsive to military and scientific needs, to being dominated by a mass market demanding cheap and ubiquitous access to computing. This gradually led to demise of specialized computational machines and the high end of the market also being dominated by clusters built out of mass-market commodity parts (Ridge et al., 1997; Sterling, 2002).
- 10 The community weathered the challenge well, without significant loss of pace of scientific advance. More narrowly stated, Earth System Models (ESMs) continued to demonstrate continual increases in both resolution and complexity across the vector/parallel transition. For example, the typical resolution of climate models used for the Intergovernmental Panel on Climate Change (IPCC) assessments and their complexity (the number of feedbacks and phenomena simulated), exhibits a steady increase from the 1990 First Assessment Report (known as FAR) to the Fourth Assessment Report (AR4) (Solomon, 2007, see
- 15 e.g the iconic *Figure 1.2*<sup>1</sup> and *Figure 1.4*<sup>2</sup> from the Summary for Policymakers).

- A second disruption is upon us in the current era. Current computing technologies are based on increased concurrency of arithmetic and logic, while the speed of computation and memory access itself has stalled. This is driven by many technological constraints, not least of which is the energy budget of computing (Cumming et al., 2014; Charles et al., 2015; Kogge et al., 2008). These massive increases in concurrency pose challenges for high-performance computing (HPC) applications: an
- 20 era where existing applications would run faster with little or no effort, simply by upgrading to newer hardware, has ended. Substantial recoding and re-architecture of applications is needed. This poses particular challenges to applications such as climate modeling, where we must simulate many interacting subsystems. The state of play of climate computing in the face of these challenges, is surveyed in Balaji (2015) and references therein: for the current generation of technology, the gains to be had seem modest, and the effort of recoding immense. Whether we will continue to demonstrate continued increases in
- 25 resolution and complexity through this transition remains to be seen.

ESMs<sup>3</sup> are canonical multi-physics codes, with many interacting components, each often built by independent teams of specialists. The coupling of these components, while respecting algorithmic constraints on conservation and numerical accuracy, is a scientific and technological challenge unto itself. Within each component of an ESM, code is parallelized using multiple techniques, including distributed and shared memory parallelism, as well as vector constructs.

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<sup>1</sup>[https://www.ipcc.ch/publications\\_and\\_data/ar4/wg1/en/figure-1-2.html](https://www.ipcc.ch/publications_and_data/ar4/wg1/en/figure-1-2.html)

<sup>2</sup>[https://www.ipcc.ch/publications\\_and\\_data/ar4/wg1/en/figure-1-4.html](https://www.ipcc.ch/publications_and_data/ar4/wg1/en/figure-1-4.html)

<sup>3</sup>Note that we are using the term “ESM” generically to denote any level in the hierarchy of complexity of weather and climate models: ranging from single-component models, e.g an atmospheric general circulation model, to models that include coupling with the ocean and land, biospheres, an interactive carbon cycle, and so on. See Figure 2.

Multi-physics codes are particularly challenged by the coming trends in HPC architecture. These codes typically involve many physical-chemical-biological variables (complexity) and associated process representations in code. Computational load is evenly distributed across many components, each embodying different physics: there are no performance “hotspots”. This also means that fresh operators and operands – embodied in physics subroutines and associated variables – are constantly being transferred to and from memory with each context switch, and locality and reuse are hard to achieve. This is particularly unsuited to the novel architectures currently on the horizon. These include graphical processing units (GPUs) which can concurrently process  $\mathcal{O}(100)$  data streams following the same instructions sequence, and the Many-Integrated Core (MIC) architecture, which allows many ( $\mathcal{O}(100)$ ) execution threads to access the same memory. These hardware trends have made the cost of data movement prohibitive relative to computing itself, thus strongly favoring codes where both instructions and data have a high rate of reuse and computational intensity (ratio of floating-point operations to memory operations). Algorithms that exhibit *fine-grained concurrency*, where multiple computationally intensive and concurrent data streams follow the same instruction sequence, are best adapted to the emerging architectures of this decade.

The next computational landmark at this juncture is the “exascale”,  $\mathcal{O}(10^{18})$  operations per second. Given the earlier discussion on the stalling of Moore’s Law, the rate of atomic arithmetic operations is still  $\mathcal{O}(10^9)$  per second, thus requiring us to achieve  $\mathcal{O}(10^9)$  concurrency. While continuing to extend physical and dynamical algorithms toward the fine-grained concurrency of the coming era, we believe multi-physics codes must also attempt to share the available concurrency across many physical components, in order to best exploit these new systems. Of the many factors of 10 increase in performance needed to get to the exascale, we believe at least one can come from component organization. We propose here a major architectural change in the construction of coupled models, such as ESMs. We demonstrate here a possible approach to extending the current rather modest amount of concurrency among ESM components (typically 2-4 top-level realms such as atmosphere, ocean, and land) to a more massive increase in *coarse-grained component concurrency* (CCC).

In this study, we examine the radiation component (which computes radiative transfer in the atmosphere in response to dynamically evolving concentrations of radiatively active chemical species) of the GFDL Flexible Modeling System (FMS). This is a relatively expensive component of the atmospheric physics, and is usually run at a much coarser timestep than the rest of the atmosphere (temporal subsampling), purely for expediency rather than any physical justification. Other approaches to reducing the computational burden of radiative transfer include subsampling in the spectral domain (Pincus and Stevens, 2009; Bozzo et al., 2014) or in the spatial as well as the temporal domain (Morcrette, 2000; Morcrette et al., 2008). Some of these methods have been shown to be effective over short timescales (e.g numerical weather prediction and medium-range forecasting) but contribute to model bias over climate timescales. Adaptive methods that tune the subsampling by examining the degree of spatial and temporal correlation in model fields have also been proposed (Manners et al., 2009).

We focus here on temporal subsampling. This purely expedient choice of timestep has been shown by Pauluis and Emanuel (2004) to be a potential source of instability and bias in radiating atmospheres. Xu and Randall (1995) have also shown that this problem gets considerably worse as the resolution of models increases. A useful way to think about this is that using different timesteps for the radiation component vis-à-vis the rest of the physics creates a discrepancy between the cloud field and the “cloud shadow field” seen by the radiation component, which can lead to numerical issues. Our method permits us to reduce

the timestep to match the rest of the atmosphere, *with the same time to solution*, at a modest computational cost in terms of allocated processors. This method does not rule out subsampling along other dimensions (spatial or spectral), which may be superimposed as well in future developments. The effects of subsampling are not fully understood yet, and further study is needed to understand how results converge as various forms of subsampling are eliminated. That said, subsampling is clearly  
5 a matter of expediency and reducing computational expense: there is no case at all to be made that it is in any way numerically or physically superior to the alternative.

The structure of the paper is as follows. In Section 2 we briefly review current approaches to parallelism in ESMs, particularly in the coupling framework. In Section 3 we describe our approach to coarse-grained concurrency, how it is achieved without increasing data movement. In Section 4 we show results from standard AMIP (the Atmospheric Model Intercomparison Project:  
10 Gates, 1992) simulations using the CCC approach. The associated computational results show decreased time to solution for concurrent versus serial approaches in otherwise identical physical formulations, and the ability to run with a much smaller radiation timestep without increasing the time to solution. Finally, in Section 5 we discuss plans and prospects for extending this approach further within FMS, and its potential application on novel architectures.

## 2 Concurrency in Earth System Models

15 Weather and climate modeling have always been in the innovative vanguard of computing, dating all the way back to the origins of modern computing in John von Neumann’s pioneering studies (Dahan-Dalmedico, 2001). The ability to apply instruction sequences to multiple data streams – concurrency – has long been a cornerstone of performance engineering. The pioneering vector processors of Seymour Cray’s era in the late 1970s allowed a data stream to flow through a hardware innovation known as *vector registers*, which allowed the same instruction sequences to apply to each succeeding element in the data stream, known  
20 as SIMD (single-instruction multiple-data). Over time, vectors grew to support extremely complex programming sequences, evolving into single-program, multiple-data, or SPMD.

In the 1980s, machines such as the Cray X-MP (the MP stood for multi-processor) were introduced. Here for the first time *parallelism* appears at a very high-level, allowing the concurrent execution of multiple tasks, which were themselves SPMD vector programs. This was the first introduction of coarse-grained concurrency. This led to the development of the  
25 MPMD framework: multiple-program, multiple-data. Soon after, distributed computing, consisting of networked clusters of commodity computers, known as symmetric multi-processors (SMPs), began to dominate HPC, owing to the sheer advantage of the volume of the mass market.

To take advantage of distributed computing, new techniques of concurrency began to be developed, such as domain decomposition. Here the globally discretized representation of physical space in a model component is divided into domains  
30 and assigned to different processors. Data dependencies between domains are resolved through underlying communication protocols, of which the Message-Passing Interface MPI (Gropp et al., 1998) has become the *de facto* standard. The details of message-passing are often buried inside software frameworks (of which the GFDL Flexible Modeling System, described in Balaji (2012) is an early example), and this convenience led to the rapid adoption of distributed computing across a wide va-

riety of applications. Within the distributed domains, further fine-grained concurrency is achieved between processors sharing physical memory, with execution threads accessing the same memory locations, using protocols such as OpenMP (Chandra et al., 2001).

Climate computing has achieved widespread success in the distributed computing era. Most ESMs in the world today are MPMD applications using a hybrid MPI-OpenMP programming model. At the highest end, ESMs (or at least, individual components within them, see e.g Dennis et al., 2012, S.-J. Lin and C. Kerr, private communication) have been run on  $\mathcal{O}(10^5)$  distributed processors and  $\mathcal{O}(10)$  shared-memory execution threads, which places them among the most successful HPC applications in the world today (Balaji, 2015). Even higher counts are reported on some leadership machines, but these are more demonstrations than production runs for science (e.g Xue et al., 2014).

## 2.1 Coupling algorithms in Earth System Models

There are diverse component architectures across Earth System Models (Alexander and Easterbrook, 2015), but they nonetheless share common features for the purposes of discussion of the coupling algorithms. Consider the simplest case, that of two components, called  $A$  and  $O$  (symbolizing atmosphere and ocean). Each has a dependency on the other at the boundary. When the components execute serially, the call sequence can be schematically represented as:

$$A^{t+1} = A^t + f(A^t, O^t) \quad (1)$$

$$O^{t+1} = O^t + g(A^{t+1}, O^t) \quad (2)$$

where  $f()$  and  $g()$  nominally represent the feedbacks from the other component, and the superscript represents a discrete timestep. Note that in the second step,  $O$  is able to access the updated state at  $A^{t+1}$ . This is thus formally equivalent to Euler forward-backward time integration, or Matsuno timestepping, as described in standard textbooks on numerical methods (e.g Durrant, 1999).

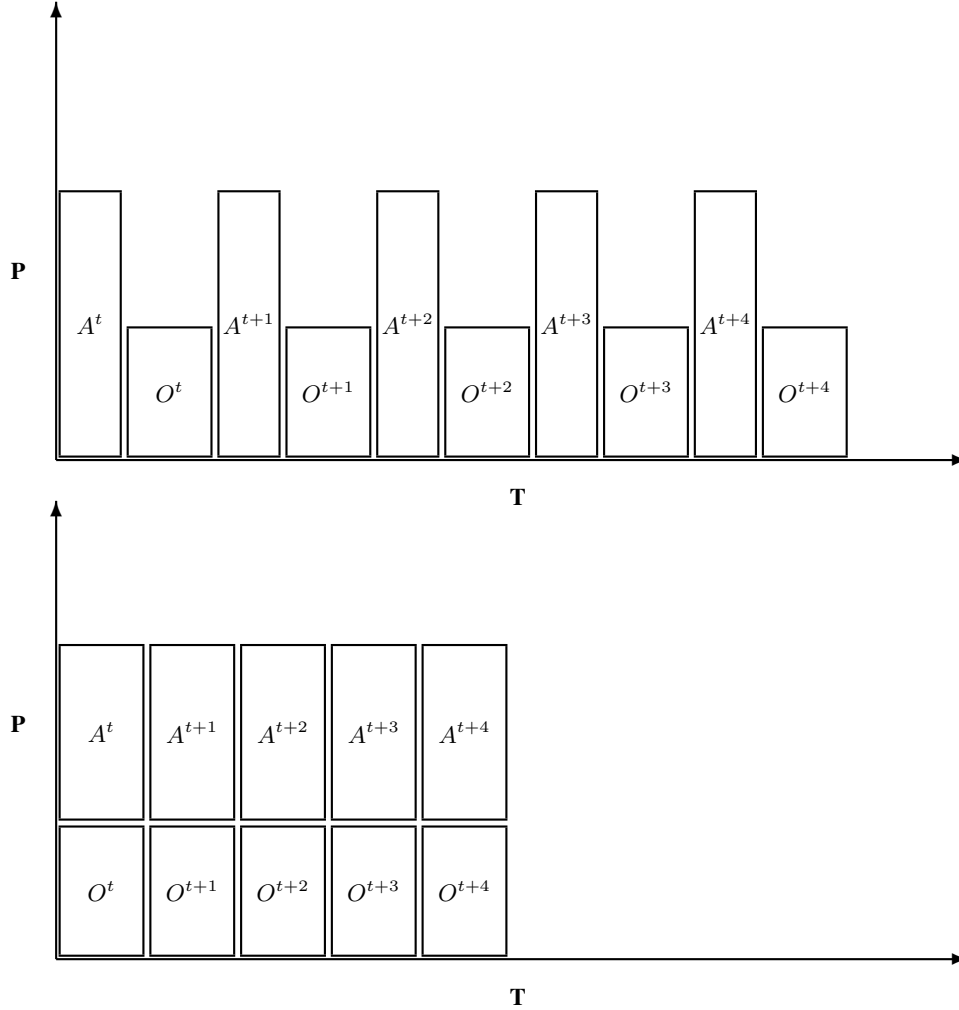
In a parallel computing framework, now assume the components are executing concurrently. (Figure 1 shows the comparison of serial and concurrent methods in parallel execution.) In this case,  $O$  only has access to the *lagged* state  $A^t$ .

$$A^{t+1} = A^t + f(A^t, O^t) \quad (3)$$

$$O^{t+1} = O^t + g(A^t, O^t) \quad (4)$$

Thus, the results will not be identical to the serial case. Furthermore, while we cannot undertake a formal stability analysis without knowing the forms of  $f$  and  $g$ , this coupling algorithm is akin to the Euler forward method, which unlike Matsuno's method is formally *unconditionally unstable*. Nevertheless, this parallel coupling sequence is widely, perhaps universally, used in today's atmosphere-ocean general circulation models (AOGCMs). This is because for the particular application used here,

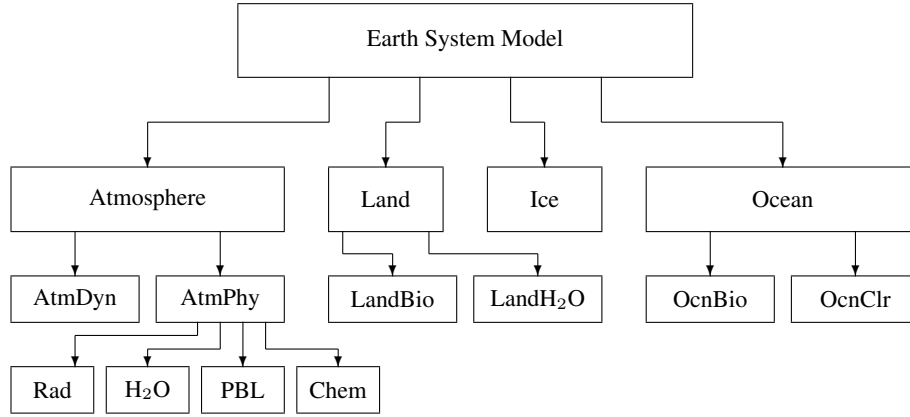
that of modeling weather and climate, we find that the system as a whole has many physical sources of stability.<sup>4</sup> Radiative processes are themselves a source of damping of thermal instability, and we also note that within each component there are internal processes and feedbacks which are often computed using implicit methods, and other methods aimed at reducing instability. This is nonetheless a reason for caution, and in Section 5 we will revisit this issue in the context of future work.



**Figure 1.** Serial and concurrent coupling sequences, with time on the X-axis and processors on the Y-axis. In the serial case, both components may not scale to the same processor count, leaving some processors idle. Note that in the concurrent coupling sequence below,  $O^{t+1}$  only has access to the lagged state  $A^t$ .

<sup>4</sup> We are familiar with things that work in theory, but not in practice... this is something that works in practice but not in theory! This is a good example of the opportunistic nature of performance engineering.

This discussion has introduced the notions underlying serial and concurrent coupling in the context of two components  $A$  and  $O$ . An actual ESM has many other components, such as land and sea ice. Components themselves are hierarchically organized. An atmosphere model can be organized into a “dynamics” (solutions of fluid flow at the resolved scale) and “physics” components (subgrid scale flow, and other thermodynamic and physical-chemical processes, including those associated with clouds and subgridscale convection, and the planetary boundary layer). Similarly the land component can be divided into a hydrology and a biosphere component, and the ocean into dynamics, radiative transfer, biogeochemistry, and marine ecosystems. A notional architecture of an ESM is shown in Figure 2. Different ESMs around the world embody these differently in code; this figure is not intended to define the software structure of all ESMs, which tend to be quite diverse (Alexander and Easterbrook, 2015).



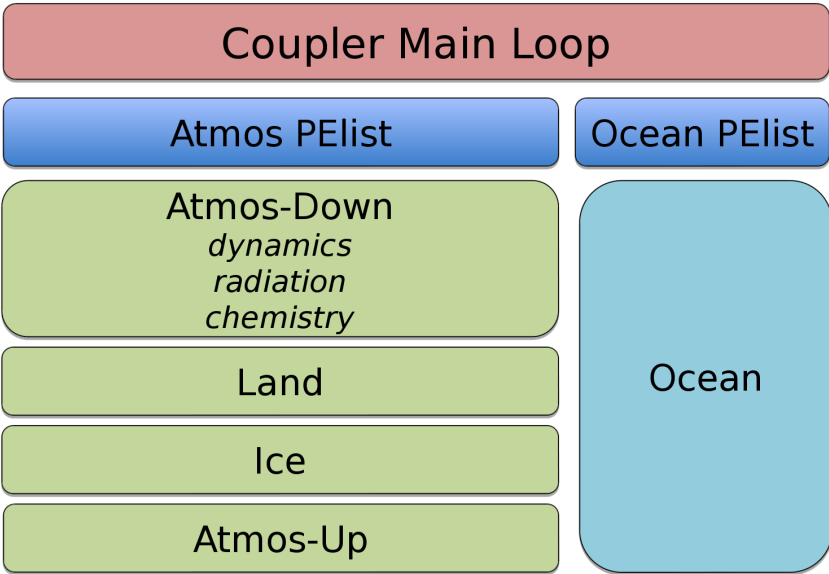
**Figure 2.** Notional architecture of an Earth System Model, with components embodying different aspects of the climate system, hierarchically organized. Models on a hierarchy of complexity ranging from single-component (e.g atmosphere-only) models to full-scale coupled models with an interactive biosphere, are often constructed out of a palette of components within a single modeling system.

- 10 How the notional architecture of Figure 2 gets translated into a parallel coupled ESM code is quite problem-specific. As the science evolves and computing power grows, the boundary of what is resolved and unresolved changes. Also, models grow in sophistication in terms of the number of processes and feedbacks that are included.

For the purposes of this study, we describe the actual code architecture of the GFDL Flexible Modeling System (FMS). The atmosphere and ocean components are set up to run in parallel in distributed memory, communicating on the slow coupling timestep  $\Delta t_{\text{cpld}}$ , on the order of  $\Delta t_{\text{cpld}} = 3600$  sec for its flagship application, decadal-centennial climate change. Within the slow coupling loop, the atmosphere communicates on a fast coupling timestep  $\Delta t_{\text{atm}}$  with a typical value of 1200 sec, set by the constraints of atmospheric numerical and physical stability.

As the land and ocean surfaces have small heat capacity, reacting essentially instantaneously to changes in atmospheric weather, stability requires an implicit coupling cycle. The implicit coupling algorithm requires an down-up sweep through the

atmosphere and planetary (land and ocean) surface systems, for reasons detailed in Balaji et al. (2006). The parallel coupling architecture of FMS is shown in Figure 3.



**Figure 3.** FMS parallel coupling architecture in processor-time space, with processors across, and time increasing downward. Components have different horizontal and vertical extents to indicate the degree of parallelism and time of execution, though these extents are notional and not to be interpreted as drawn to scale. Within a single executable for the entire coupled system, the atmosphere and ocean components run concurrently in distributed memory (MPI, indicated in deep blue). Within the atmosphere stack, components execute serially, including tight coupling to the land and ice-ocean surface. The down-up sequence of implicit coupling is explained in Balaji et al. (2006). These components internally shared-memory (OpenMP) coupling, indicated in light green. The ocean component at the present time is MPI-only, indicated in light blue.

The “Atmos-Up” step is quite lightweight, including adjustments to the atmospheric state imposed by moist physics, and completing the up-sweep of a tridiagonal solver for implicit coupling of temperature and other tracers, as described in Balaji et al. (2006). The bulk of the atmospheric physics computational load resides in the “Atmos-Down” step.

The atmospheric radiation component is a particularly expensive component of atmospheric physics, which is why it was chosen as the target for increasing coupling concurrency in FMS. This component is described below.

### 2.2 The radiation component in FMS

The radiation component in FMS is one of the most expensive components within the atmospheric physics. It consists of short-wave and longwave radiation components. The shortwave component is based on Freidenreich and Ramaswamy (1999), where “line-by-line” (LBL) radiative transfer calculations have been grouped into pseudo-monochromatic bands, and shown in bench-



mark calculations to provide a similar response to the benchmark LBL results. The calculations have a strong dependency on the evolving (through advection, cloud processes, and chemistry) state of radiatively active species in the atmosphere, including atmospheric water vapor, CO<sub>2</sub>, O<sub>3</sub>, aerosols, and condensed water fields, in addition to the basic physical state variables. The longwave radiation components (Schwarzkopf and Ramaswamy, 1999) similarly use approximations for computational efficiency, and also interact strongly with atmospheric liquid- and gas-phase chemical species, including water vapor and clouds. The species shared between atmospheric physics, chemistry, and radiation are referred to as *tracers*, a term applied to 3D model fields (in atmosphere or ocean) that are advected by the evolving dynamics, and participating in physics and chemistry processes at individual gridpoints.

Despite the simplifying approximations, the radiation component remains prohibitively expensive. As a result, this component is stepped forward at a slower rate than the rest of the atmospheric physics, with  $\Delta t_{\text{rad}} = 10800$  sec, or  $9 * \Delta t_{\text{atm}}$ , as a typical value. The planetary surface albedo, whose time evolution is a function of solar zenith angle only, alone is stepped forward on the atmospheric timestep  $\Delta t_{\text{atm}}$ . This means that at intermediate (non-radiation) atmospheric timesteps, the radiation is responding to a lagged state of atmospheric tracers, which may be as much as  $\Delta t_{\text{rad}} - \Delta t_{\text{atm}}$  ( $\sim 3$  h) behind.

This timestep discrepancy is vexing, but most climate models around the world make a similar compromise, with a radiation timestep longer than the physics timestep. If the promise of massive increases in concurrency on future architectures is kept, a concurrent radiation component may offer a way forward. Simultaneously, we may be able to decrease the discrepancy between  $\Delta t_{\text{rad}}$  and  $\Delta t_{\text{atm}}$ , and bring us toward more physical consistency between the radiative and physico-chemical atmospheric states (Pauluis and Emanuel, 2004; Xu and Randall, 1995).

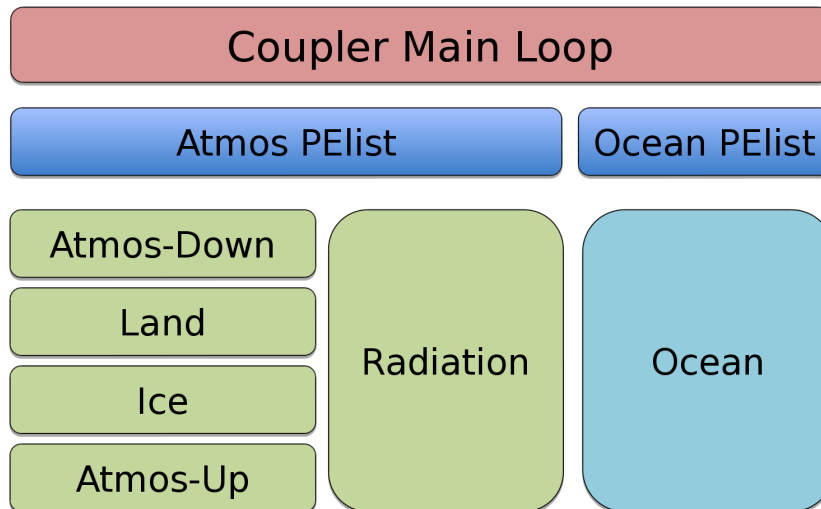
### 3 Coarse-grained component concurrency

Before we begin describing a method for casting the radiation code in FMS as a concurrent component, we need to describe the current methodology shown in Figure 3. Concurrency between atmosphere and ocean component on the slow coupling timestep is achieved using distributed computing techniques, with the components running on separate processor sets or *PElists*. In FMS terminology, a PE or *processing element* is a unit of hardware supporting a single execution thread, sometimes called a *core*. A PElist is synonymous with a “communicator” in MPI terminology, and lists the PEs assigned in distributed memory processing. Each PE in a PElist can spawn multiple shared-memory execution threads. These threads are assigned to other PEs to avoid contention. Coupling fields are transferred between atmosphere and ocean using the exchange grid (Balaji et al., 2006) and message passing. Within the atmosphere component, shared-memory parallelism using OpenMP is already implemented. For the dynamics phase, the OpenMP acts on individual loops, some of which may contain calls to subroutines or comprised of large programmatic constructs. These include regions where concurrency is on slabs (horizontally tightly-coupled) and others organized in columns (vertically tightly coupled).

Unlike the dynamics, the physics is organized entirely columnwise, and individual columns – the  $k$  index in an  $(i, j, k)$  discretization – have no cross-dependency in  $(i, j)$  and can execute on concurrent fine-grained threads. The arrays here can be organized into groups of vertical columns, or *blocks*, that can be scheduled onto the same OpenMP threads at a high (coarse)

level – meaning a single thread will persistently see the block (thus assuring thread data affinity) through the complete Atmos-Down phase (*sans* dynamics), and again through the Atmos-Up phase.

- We now come to the reorganization of components for CCC in the current study. Understanding that the radiation is but one phase of the physics, which is already utilizing blocks and OpenMP threads, it makes sense to extend the concept and have the radiation run concurrently in a separate group of OpenMP threads. In the concurrent radiation architecture, shown in Figure 4, the decision was made to utilize *nested* OpenMP, instead of a flat threadpool. Each MPI-rank assigned to the atmosphere PELIST starts up an OpenMP region with two threads, one to act as the master for the radiation and the other to drive the non-radiation components. These “master” threads are able to utilize the nested OpenMP constructs, to start up a number of atmosphere threads ( $A$ ) and radiation threads ( $R$ ) where the total numbers of threads  $T = A + R$ . For a given value of  $T$ ,  $A$  and  $R$  can be dynamically adjusted during the course of a run to achieve optimal load-balance. Because the radiation and atmosphere concurrency occur at a high level, the memory space is unique to each component and furthermore, the memory space is unique to each block. This separation of memory spaces ensures there are no performance deficiencies due to cache coherency effects (false sharing or cache invalidations). A single data synchronisation point (copy) at the end of each radiation time step ensures that the atmospheric and radiation components remain completely independent.
- In the limit, we could create blocks containing a single column, so that  $A$  and  $R$  both equal the number of columns in the domain, and  $T = 2A$ . But the overheads associated with moving in and out of threaded regions of code must be amortized by having enough work per OpenMP thread instance. Current processors rely on having a moderate number of data elements to achieve best performance by hiding the various latencies for each instruction, including time spent waiting for operands to be loaded to memory registers. Empirically, on current technology, we have found optimal results using blocks of  $\mathcal{O}(32)$  columns.



**Figure 4.** Concurrent radiation architecture. See Figure 3 for comparison, and explanation of legends.

## 4 Results

### 4.1 Results from AMIP runs

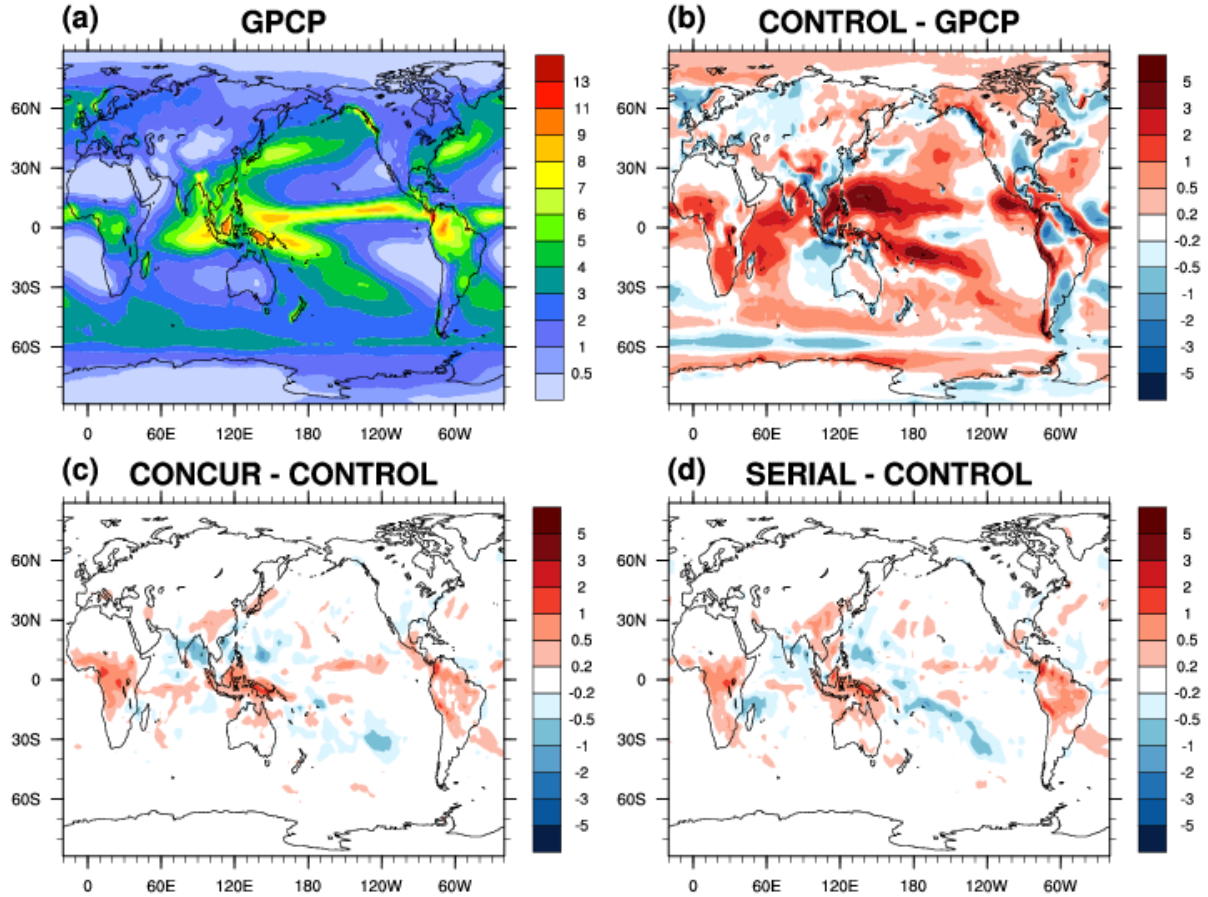
The model utilized here is based on AM3, the atmosphere-land component of the GFDL Climate Model Version 3 (CM3) model (Donner et al., 2011), a model with a relatively well-resolved stratosphere, with a horizontal resolution of approximately 100 km and 48 vertical levels. Here the original AM3 has been modified to include an experimental cumulus convection scheme, and a reduced chemistry representation including gas and aqueous-phase sulfate chemistry from prescribed emissions (Zhao et al., 2016). This model is forced using observed sea surface temperatures (SSTs) as a lower boundary condition over a 20-year period 1981-2000. The three experiments described here are:

1. the control run (CONTROL) using serial radiation with a radiative time step  $\Delta t_{\text{rad}}$  of 3 hours ( $\Delta t_{\text{rad}} = 9\Delta t_{\text{atm}}$  where  $\Delta t_{\text{atm}} = 1200$  s is the time scale on which the atmospheric state is updated;
2. serial radiation (SERIAL) using  $\Delta t_{\text{rad}} = \Delta t_{\text{atm}} = 1200$  s; and
3. concurrent radiation (CONCUR) also using  $\Delta t_{\text{rad}} = \Delta t_{\text{atm}} = 1200$  s. The difference between the SERIAL and CONCUR experiments shows the impact of concurrent coupling (the radiation sees the lagged atmospheric state), while the CONTROL and SERIAL experiments only differ in the radiative time step. We could of course attempt CONCUR while maintaining  $\Delta t_{\text{rad}}/\Delta t_{\text{atm}} = 9$ , but because of the lagged timestep, this is not recommended: the atmospheric and radiative states would be effectively 21600 s, or 6 h, out of synchrony.

All versions of the model utilize what we refer to as a solar interpolator. At the beginning of a radiative time step, the distribution of radiatively-active atmospheric constituents, such as water vapor and clouds, are input into computations of both shortwave and longwave radiative fluxes. When  $\Delta t_{\text{rad}}$  is longer than  $\Delta t_{\text{atm}}$  all solar fluxes are rescaled every  $\Delta t_{\text{atm}}$  by normalizing by the incident solar radiation using the zenith angle appropriate for that atmospheric time step. Any sensitivity to the  $\Delta t_{\text{rad}}$  radiation time step is due to the fact that the radiatively-active constituents are held fixed for the duration of that time step and not due to neglected changes in the incoming solar flux (Morcrette, 2000).

We show here the effects of changing the radiation timestep on precipitation and top-of-atmosphere radiative fluxes in the AMIP simulation. Figure 5 shows the annual mean precipitation bias for the three experiments with respect to the Global Precipitation Climatology Project (GPCP) v2.2 (Adler et al., 2003) climatology. Panel (b) shows the difference between CONTROL and observational precipitation climatology, while (c) and (d) show the model-model differences between the CONTROL run and the SERIAL and CONCUR climatologies. The difference in the pattern of annual mean precipitation due to the change in time step (Figure 5, Panels c and d) is negligible compared to the difference between the model and observations. Panels (c) and (d) are similar to first approximation, indicating that the difference in precipitation pattern due

to the choice of serial versus concurrent integration is smaller than the difference due to the radiation time step and even less significant as compared to the difference between model and observations.



**Figure 5.** Comparison of model climatologies against GPCP precipitation. (a) shows the GPCP climatology, and (b) the model climatological biases for the CONTROL run. Panels (c) and (d) show model-model difference versus CONTROL for CONCUR and SERIAL runs respectively, plotted on the same color scale as (b).

The more significant difference in the simulation due to the change in radiation time step is in the energy balance at the top of the atmosphere between absorbed shortwave and outgoing longwave radiation. The simulated annual mean pattern of this net energy flux is displayed in Figure 6 in analogous format to Figure 5. The energy flux data is CERES EBAF edition 2.8 satellite data (Loeb et al., 2009). Neither the radiation time step nor the choice of serial versus concurrent integration modifies the geographical pattern of model bias significantly, but they do alter the simulation with a fairly spatially uniform

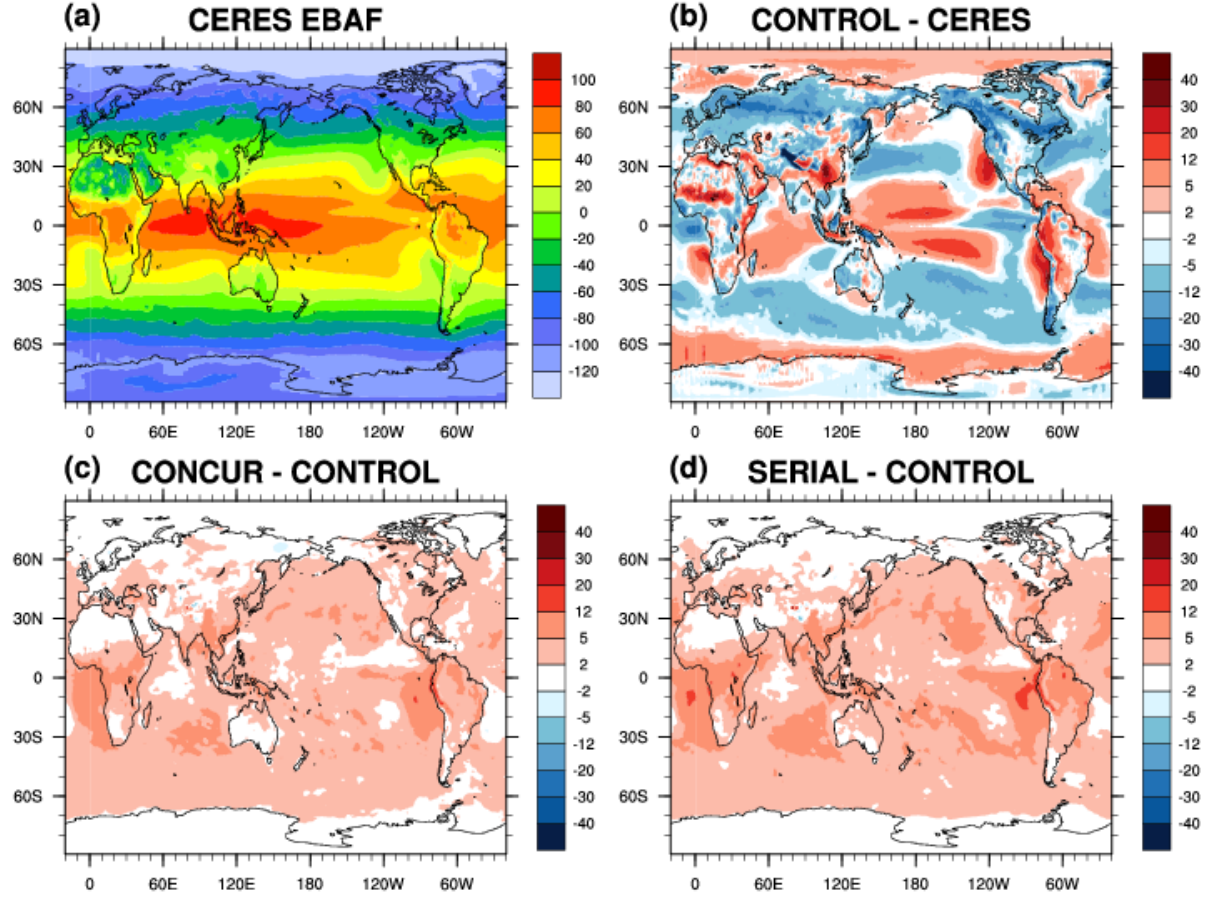
offset. Again the details of all the experiments are similar but a closer examination of the global mean biases show the SERIAL and CONCUR cases (Figure 6, Panels c and d) differ from the CONTROL by about +3.1 to +3.6 W/m<sup>2</sup>. This magnitude of flux difference would have a significant effect on a coupled atmosphere-ocean model. (Compare the change in flux due to a doubling of CO<sub>2</sub> concentrations, holding radiatively active atmospheric constituents fixed, of about 3.5 W/m<sup>2</sup>). Nearly all of this difference is in the absorbed shortwave, most of which occurs over the oceans and tropical land areas. The source of this difference is primarily clouds and to a lesser extent water vapor, as determined by examining the clear-sky energy balance, a model diagnostic. The diurnal cycle of clouds and solar radiation appear to be the key factors in determining the sign and size of these responses. The diurnal peak in clouds over the oceans typically occurs close to sunrise, so there is a downward trend in cloudiness on average at the peak in incoming solar radiation. Therefore the CONTROL case sees more cloudiness over the longer radiative time step, therefore leading to more reflection by clouds and less absorption of shortwave radiation at the surface and in the atmosphere.

To be a viable climate model, the global mean top of atmosphere energy balance has to be small, less than 1 W/m<sup>2</sup>, to avoid unrealistic climate drift. This global energy balance is tuned in all models, as our ability to simulate the Earth’s cloud field from first principles is inadequate to generate a radiation field with the required fidelity. Parameters in the model that control the cloud simulation and that are not strongly constrained by observations are used in this tuning process (see e.g Hourdin et al., 2016, for a description of the tuning process). The model simulations displayed here have not been “retuned” so as to isolate the effects of the radiation time step and coupling strategy. In our experience a retuning of 3-4 W/m<sup>2</sup> is viable, but large enough that the resulting changes in other aspects of the model simulation can be non-negligible, emphasizing the importance of algorithms that make the reduction in the radiative time step less onerous computationally. However, the difference between serial and concurrent coupling of 0.5 W/m<sup>2</sup> is well within the range in which retuning has marginal impact on other aspects of the simulation, encouraging examination of the performance of the concurrent option.

## 4.2 Scaling and performance results

Comparisons of the computational performance of the 3 configurations (CONTROL, SERIAL and CONCUR) were performed on the NOAA supercomputer Gaea. Recall that CONTROL is intrinsically computationally less expensive as the  $\Delta t_{\text{rad}} = 9 * \Delta t_{\text{atm}}$  setting implies that the radiation code is executed very seldom. As the results of Section 4.1 suggest that we should shorten  $\Delta t_{\text{rad}}$  if we can, the aim is now to recover the overall model throughput (measured in simulated years per day, or SYPD) of CONTROL using the CONCUR configuration with the shorter timestep  $\Delta t_{\text{rad}} = \Delta t_{\text{atm}}$ , but at a higher processor count. The other measure in our comparison is that of the integrated processor-time computational resource request, measured in compute-hours per simulated year (CHSY). These are key measures of computational cost (time to solution, and resource consumption) used at modeling centers around the world (Balaji et al., 2016).

Initial studies were performed on a machine configuration that used AMD Interlagos processors on Cray’s Gemini high-speed interconnect. For any given PE count, we attempt different partitions between processors and threads (MPI and OpenMP) to arrive at the optimal processor/thread layout for that PE count. As Table 1 shows, CONTROL achieved 9.25 SYPD on 1728 PEs. The SERIAL configuration shows the relative cost of radiation to the rest of the model, as shortening  $\Delta t_{\text{rad}}$  from 10800 s



**Figure 6.** Comparison of model climatologies against CERES EBAF v2.8 climatological top-of-atmosphere radiation budget shown in (a). Panel (b) shows model climatological biases for the CONTROL run. Panels (c) and (d) show model-model difference versus CONTROL for CONCUR and SERIAL runs respectively, plotted on the same color scale as (b).

to 1200 s, without changing the processor count, substantially raises the total cost of radiation computations within the code, bringing time to solution down to 5.28 SYPD. Running CONCUR on the same processor count increases this time to 5.9 SYPD. Increasing the processor count to 2592 brings us back to 9.1 SYPD. Thus, one can achieve the goal of setting  $\Delta t_{\text{rad}} = \Delta t_{\text{atm}}$  without loss in time to solution (SYPD), at a cost of 1.52X (the CHSY ratio of the two configurations) in resources. Thus decreasing the radiation timestep 9-fold has raised the computational cost by about 50%, indicating that the original cost of radiation in units of CHSY was about 5%. Models where this fraction is higher will derive an even more substantial benefit from the CCC approach. We believe that as computing architectures express more and more concurrency while clock speeds

stall (see Section 5 below), this will be a key enabling technology for maintaining time to solution while increasing parallelism. While these results are for an atmosphere-only model, they can be readily extended to other components in a more complex model. As noted below in Section 5, we are planning to extend the CCC approach to other components including atmospheric chemistry and ocean biogeochemistry.

Configuration	$\Delta t_{\text{rad}}/\Delta t_{\text{atm}}$	MPI*OMP	NPES	SYPD	CHSY
CONTROL	9	864*2	1728	9.25	4483
SERIAL	1	864*2	1728	5.28	7854
CONCUR	1	432*4	1728	5.90	7029
CONCUR	1	648*4	2592	9.10	6836

**Table 1.** Performance results from the various configurations discussed. MPI\*OMP shows the assignment of MPI processes and OpenMP threads. In the CONCUR cases 2 threads each are assigned to atmosphere and radiation components. NPES is the total PE count (MPI\*OMP). SYPD measures throughput in simulated years per day, and CHSY is the computation cost in processor-hours per simulated year (NPES\*24/SYPD).

## 5 Summary and Conclusions

We are at a critical juncture in the evolution of high-performance computing, another “disruptive” moment. The era of decreasing time to solution at a fixed problem size, with little no effort, is coming to an end. This is due to the ending of the conventional meaning of Moore’s Law (Chien and Karamcheti, 2013), and a future where hardware arithmetic and logic speeds stall, and further increases in computing capacity are in the form of increased concurrency. This comes in the form of heterogeneous computing architectures, where co-processors or accelerators such as Graphical Processing Units (GPUs) provide SIMD concurrency; the other prevalent approach is in the Many-Integrated Core (MIC) architectures, with a vastly increased thread space, an order of magnitude higher than the  $\mathcal{O}(10)$  thread parallelism achieved with today’s hybrid MPI-OpenMP codes.

It is very likely that radical reimagining of ESM codes will be necessary for the coming novel architectures (Balaji, 2015). That survey of the current “state of play” in climate computing notes that multi-physics codes, which are fundamentally MPMD in nature, are particularly unsuited to these novel architectures. While individual components show some speedup, whole MPMD programs show only modest increases in performance (see e.g Govett et al., 2014; Iacono et al., 2014; Fuhrer et al., 2014; Ford et al., 2014). Other approaches, such as the use of “inexact” computing (Korkmaz et al., 2006; Düben et al., 2014), are still in very early stages.

We have demonstrated a promising new approach for novel and heterogeneous architectures for MPMD codes such as Earth System models. It takes advantage of the component architecture of ESMs. While concurrency has been achieved at the very highest level of ESM architecture shown in Figure 2, the components are themselves MPMD within a hierarchical component architecture.

In the light of our discussion we propose a precise definition of a component as a unit of concurrency. For the purposes of the coarse-grained concurrency (CCC) approach, a *component* may be defined as *one of many units in a multi-physics model, that is itself SIMD for the most part*. While the word has been loosely used earlier, this study has provided guidance on how we should think about components, and thus, this definition will be followed for the rest of the discussion in this section.

5 Fine-grained parallelism approaches, such as those surveyed in Mittal and Vetter (2015), may be applied within a component as so defined, but are likely to fail above that level. A substantial increase in overall scalability of an ESM may be achieved if several components are run concurrently. We are currently exploring CCC in several other computationally burdensome model components, including atmospheric chemistry and ocean biogeochemistry. It is clear however that this is not an universal solution: given the constraint that concurrent components can only “see” each others’ time-lagged state, some components are  
10 too tightly coupled to be amenable to the CCC approach.

Furthermore, we have demonstrated a method where multiple components that share a large number of model fields can be run concurrently *in shared memory*. This avoids the necessity of message passing between components that need to synchronize on fine timescales.

We believe the CCC approach will afford very tangible benefits on heterogeneous architectures such as GPUs, and architectures with a wide ( $\mathcal{O}(100-1000)$ ) thread space, such as MICs. In particular:  
15

- Threading within a SIMD component has not been shown to scale beyond a rather modest thread count. By running multiple components within a single thread space, the thread count can be considerably increased.
- Even with additional work in improving the SIMD performance of components, it is clear that some components are better suited to SIMD architectures than others. In a heterogeneous system, with different hardware units, this method  
20 may permit different components to be scheduled on the hardware unit to which they are best suited. For example, we could imagine some embarrassingly parallel components executing on a GPU while another, less suited to that architecture, executes on its host CPU (central processing unit).

There remain caveats to this approach. As shown in the discussion of Equation 3 above, the coupling of concurrent components might be formally unstable. We are exploring more advanced time-coupling algorithms, including 3-time-level schemes  
25 such as Adams-Bashforth (see Durran, 1999). Such algorithms have been successfully used within the atmospheric dynamical core of FMS, for two-way nesting. In this approach, the coarse- and fine-mesh components execute concurrently rather than serially as in conventional nesting approaches (Harris and Lin, 2013). We are also exploring a combination of the 3-time-level schemes with time-staggering of components, which no longer suffers from formal instability.

.We conclude that coarse-grained concurrency remains a very promising road to the future of Earth System modeling on  
30 novel, massively-concurrent HPC architectures.



## 6 Source code and data availability

Source code and data, including model output and performance data, associated with this study are freely available upon request.

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